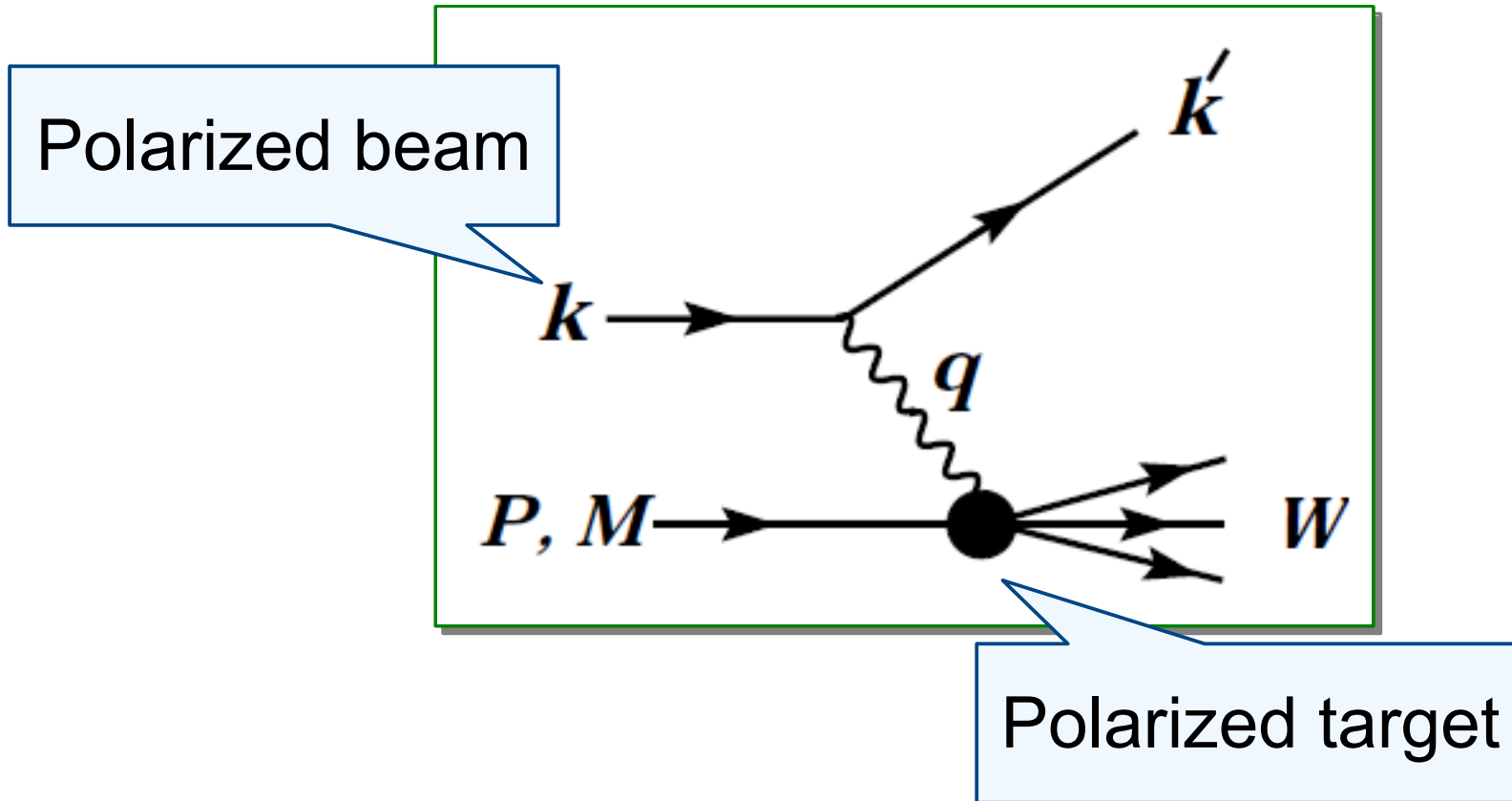




2. Spin structure of the proton in DIS





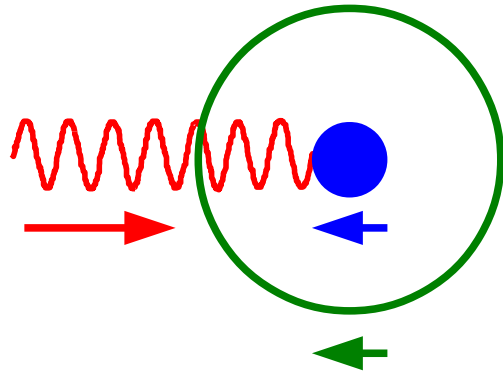
2. Spin structure of the proton in DIS

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- Polarized Deep Inelastic Scattering
- Spin structure of the proton
- Semi-inclusive DIS
 - Flavor tagging
- Spin-Flavor structure of the proton

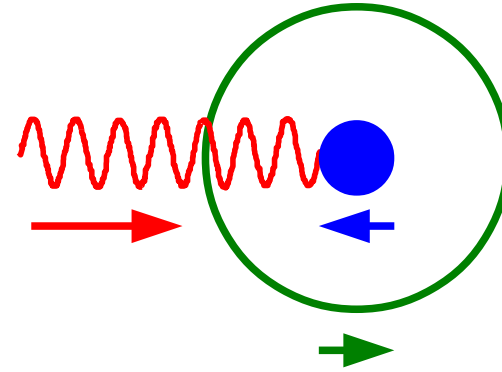
Polarized lepton beam

- ➡ Polarized γ^*
- ➡ Select quark spin



Parallel $q^+(x)$

Polarized nucleon target



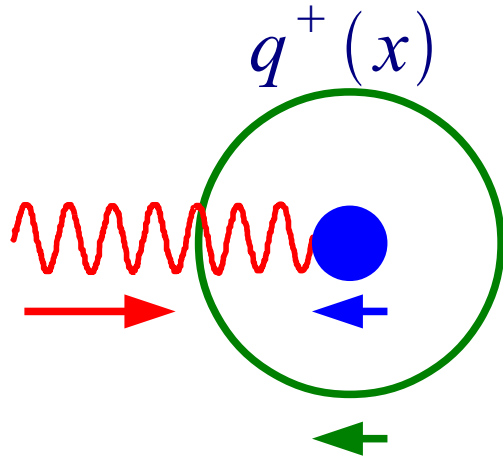
Anti-parallel $q^-(x)$

Unpol. PDF

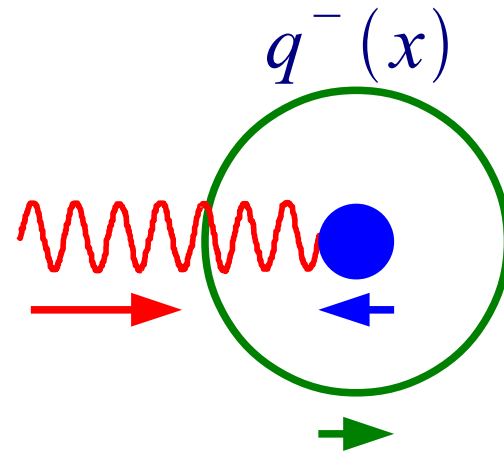
Unpol. Str. Func.

$$q(x) = q^+(x) + q^-(x)$$

$$F_1(x) = \frac{1}{2} \sum_q e_q^2 q(x)$$



Structure function



PDF

Unpol. $F_1(x) = \frac{1}{2} \sum_q e_q^2 q(x)$

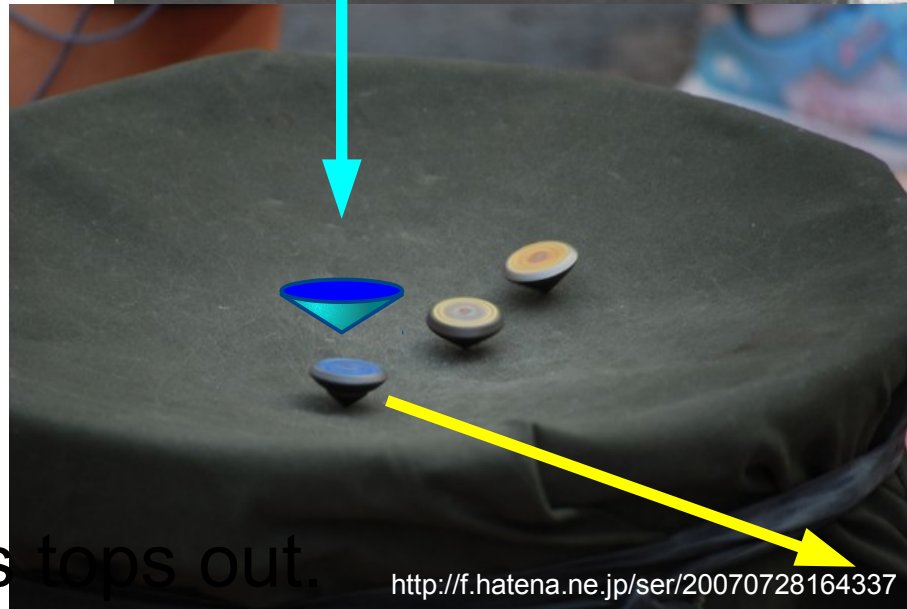
$$q(x) = q^+(x) + q^-(x)$$

Pol. $g_1(x) = \frac{1}{2} \sum_q e_q^2 \Delta q(x)$

$$\Delta q(x) = q^+(x) - q^-(x)$$



In Japan,
we have a game with tops,
called “be-goma”.



Try to kick the enemy's tops out.

To probe the elements,
let's hit with this top!



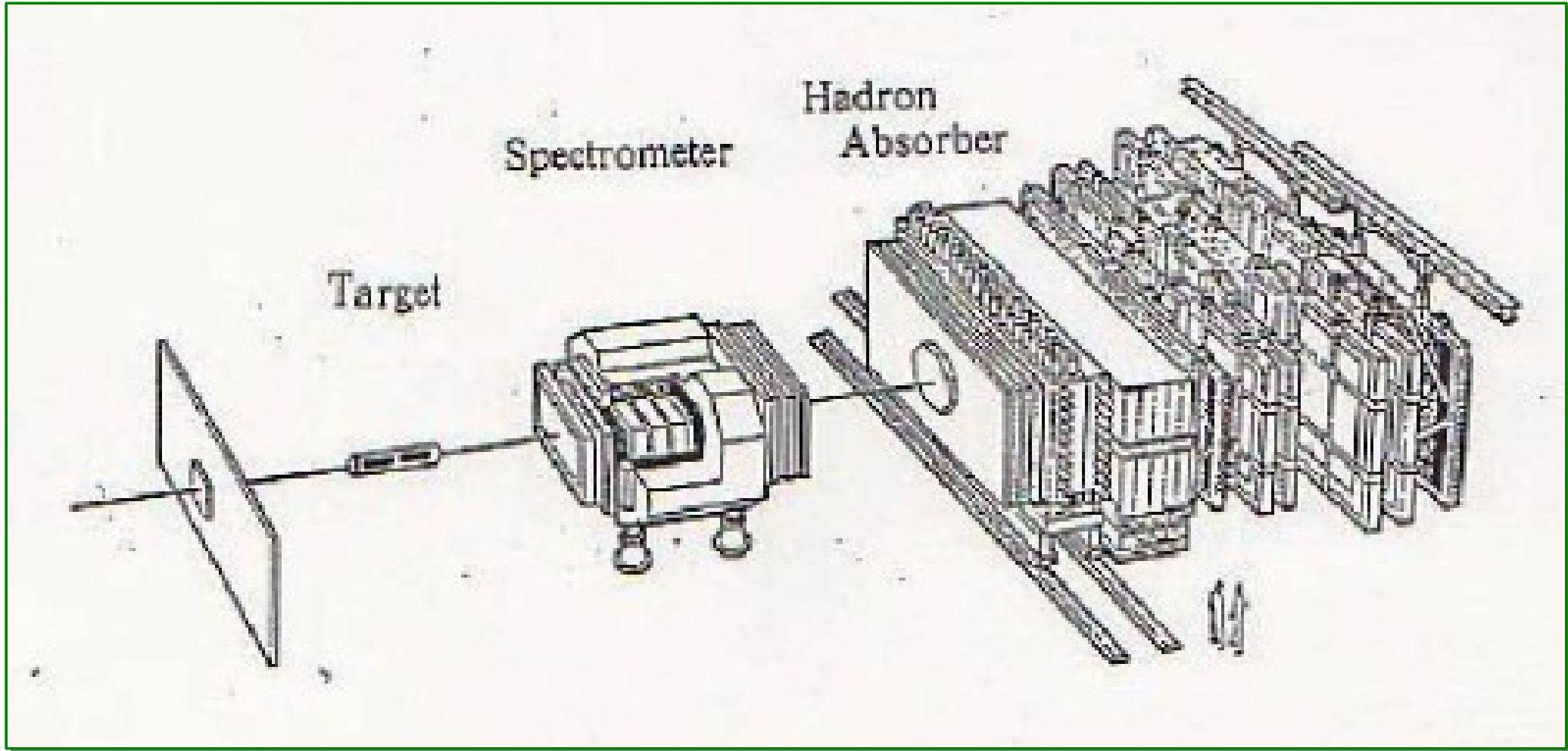
Now it becomes possible



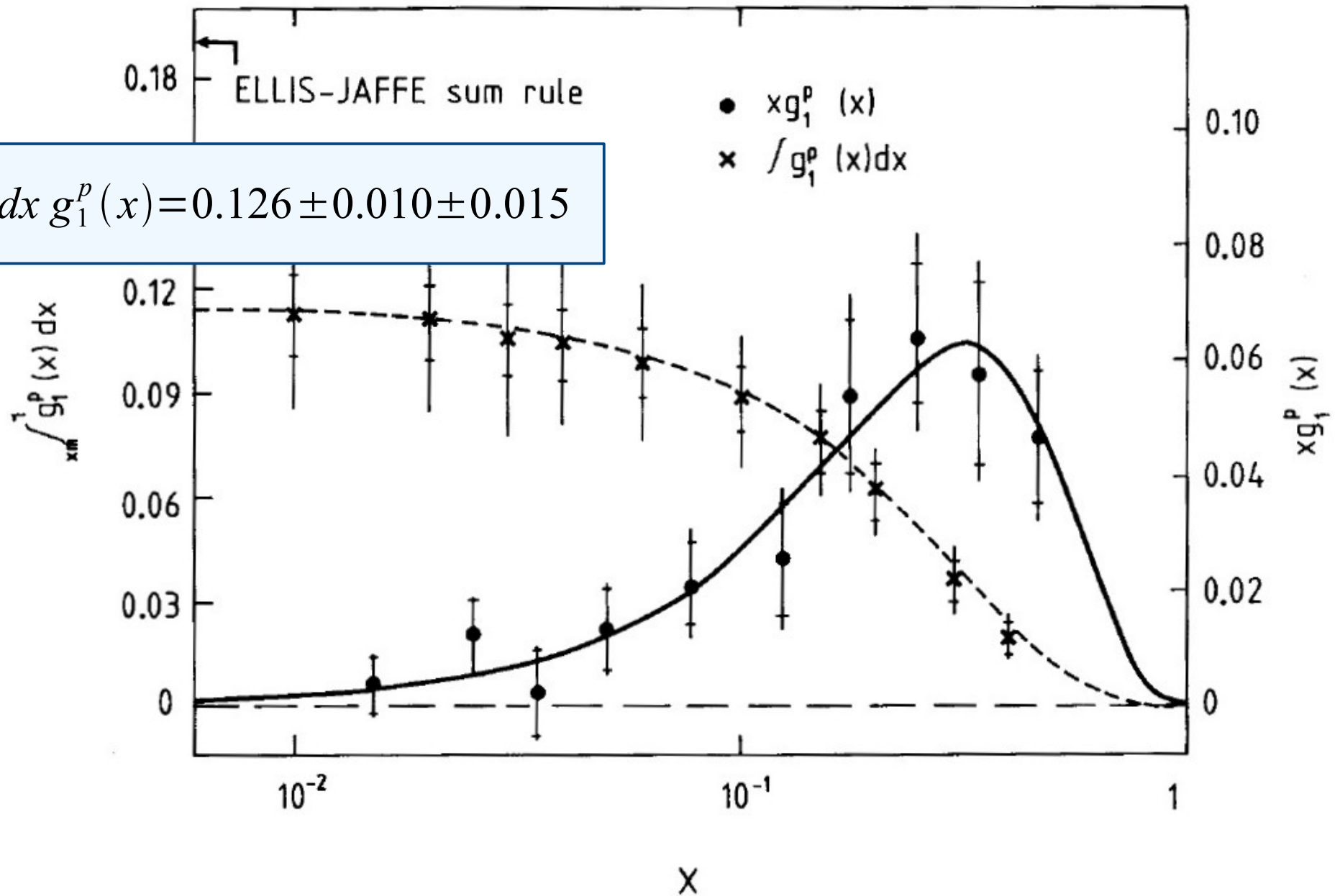


CERN-EMC experiment

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$$\int_0^1 dx g_1^p(x) = 0.126 \pm 0.010 \pm 0.015$$





Spin problem

⊗ q + q-bar

Nucl. Phys. B328 (1989) 1, Phys. Lett. B206 (1988) 364

$$\int_0^1 dx g_1^p(x) = \frac{1}{2} \left(\frac{4}{9} \Delta u + \frac{1}{9} \Delta d + \frac{1}{9} \Delta s \right)$$

$$= \frac{1}{9} a_0 + \frac{1}{12} a_3 + \frac{1}{36} a_8$$

$$\Delta \Sigma = \Delta u + \Delta d + \Delta s = a_0$$

$$\Delta u - \Delta d = a_3 = 1.26$$

$$\Delta u + \Delta d - 2 \Delta s = a_8 = 0.58$$

From weak decay:

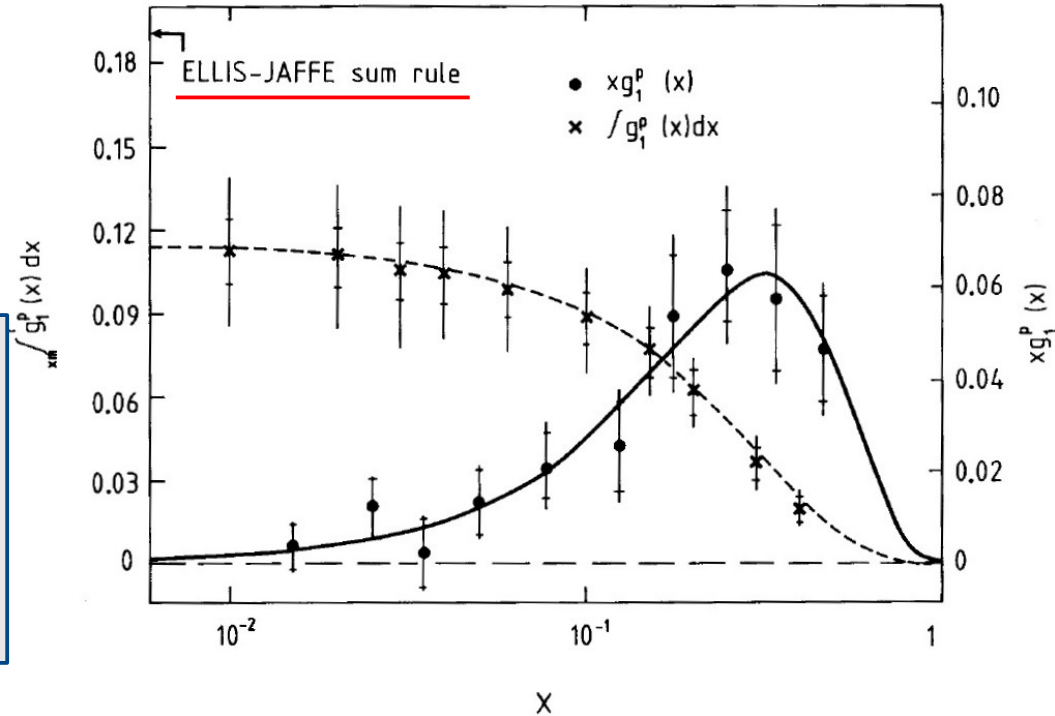
$$= 1.26$$

$$= 0.58$$

If $\Delta s = 0$, $a_0 = a_8 = 0.58$

$$\int_0^1 dx g_1^p(x) = 0.186$$

Ellis-Jaffe Sum Rule



$$\int_0^1 dx g_1^p(x) = 0.126 \pm 0.010 \pm 0.015$$

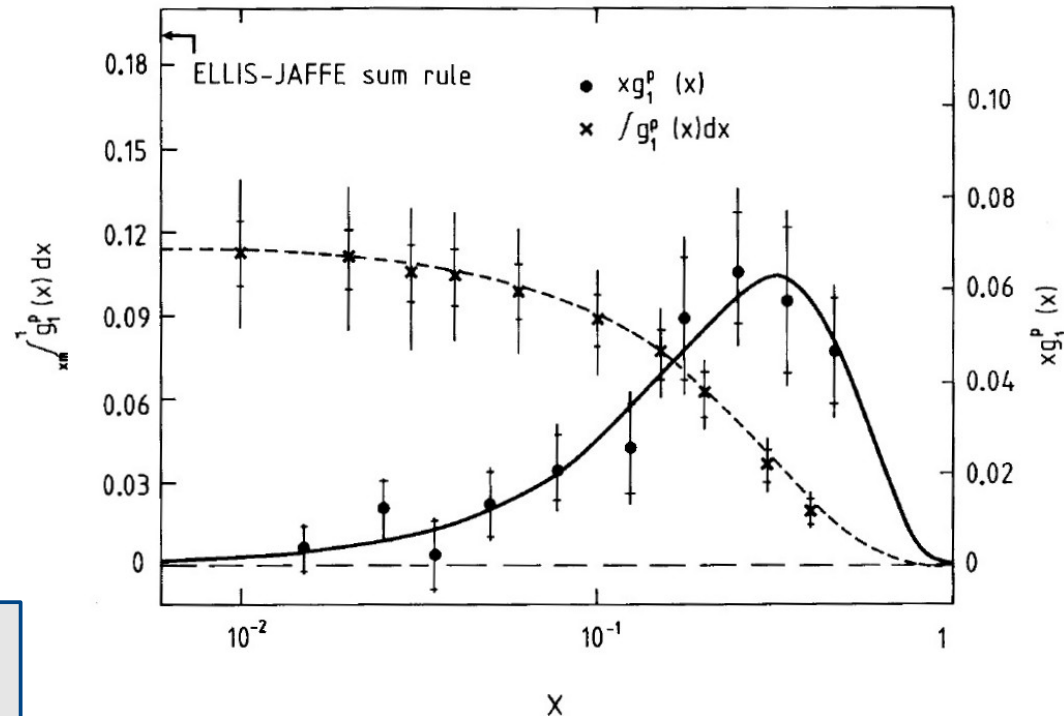
$$\int_0^1 dx g_1^p(x) = 0.126 \pm 0.010 \pm 0.015$$

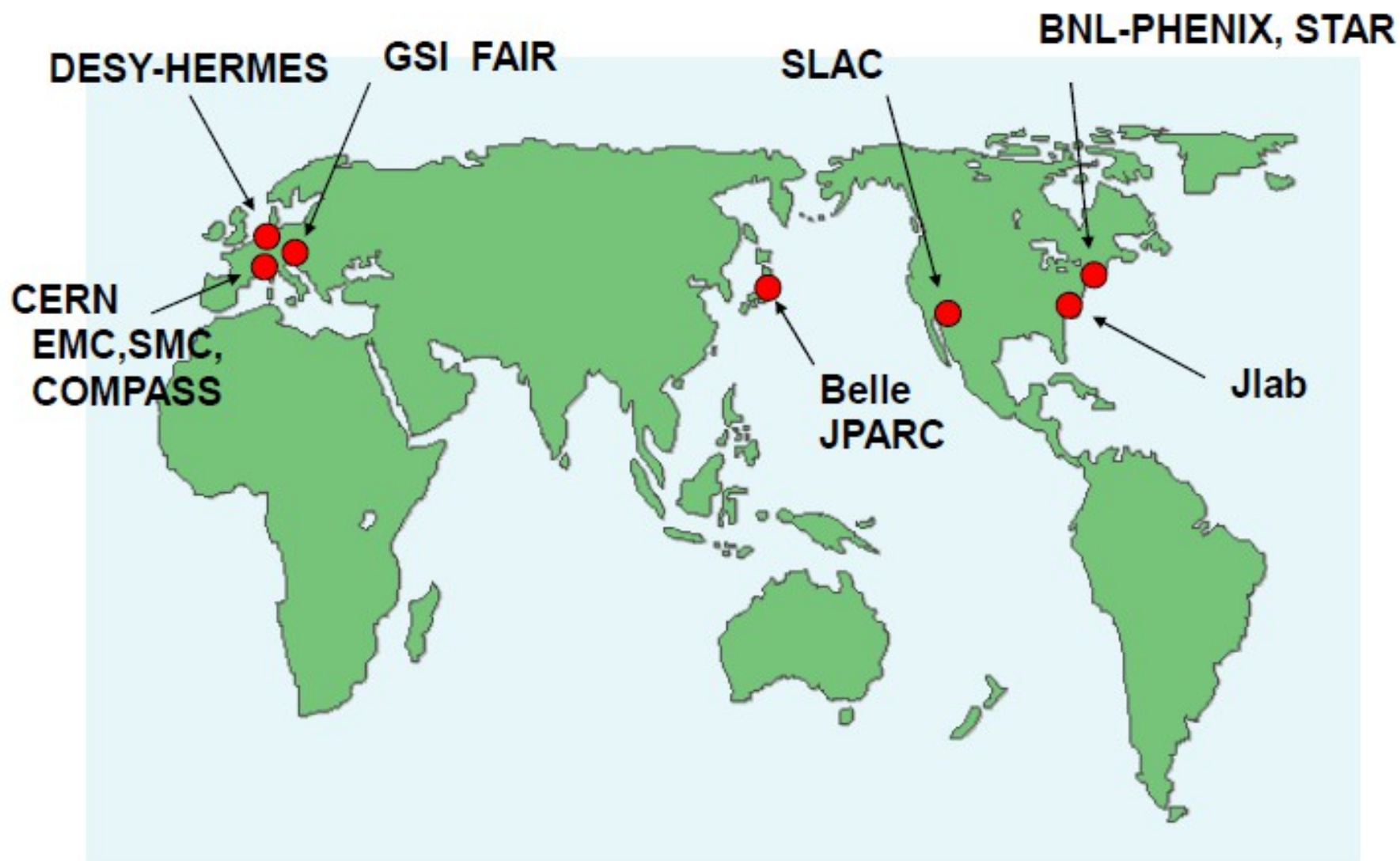
$$= \frac{1}{9} \Delta \Sigma + \frac{1}{12} a_3 + \frac{1}{36} a_8$$



From weak decay:
 $a_3 = 1.26$
 $a_8 = 0.58$

$$\Delta \Sigma = 0.120 \pm 0.094 \pm 0.138$$



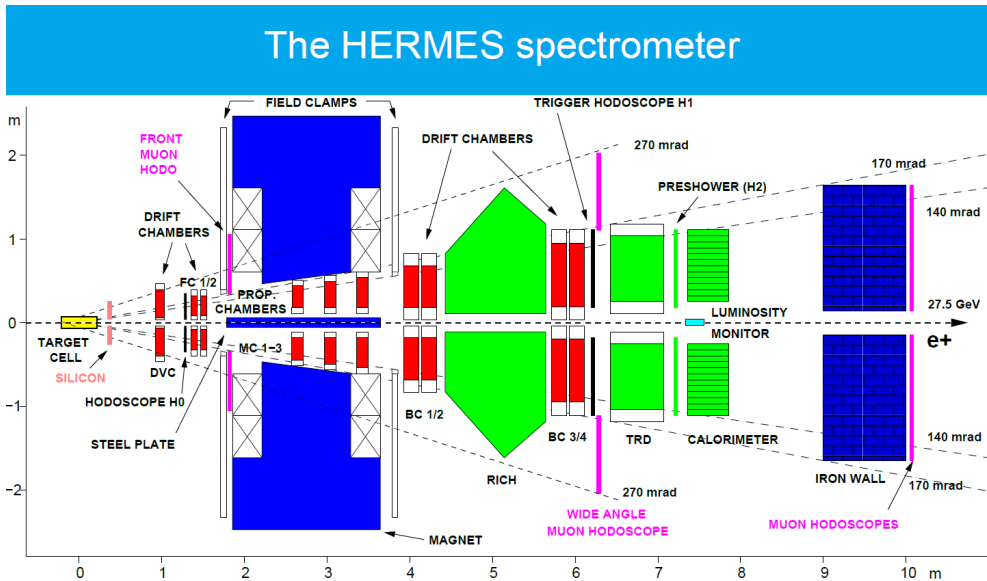


**500 ~ 1000 experimental physicists now,
Strong activities of theoretical physicists**



Polarized DIS experiment

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Internal gas targets:

- Longitudinally polarized H, D
- Transversely polarized H
- Unpolarized $H, D, {}^4He, N, Ne, Kr, Xe$

Forward magnetic spectrometer

- Momentum resolution 1-2%
- Particle identification: $RICH, TRD, H2, calorimeter$

S. Yaschenko, Overview of recent HERMES results

4

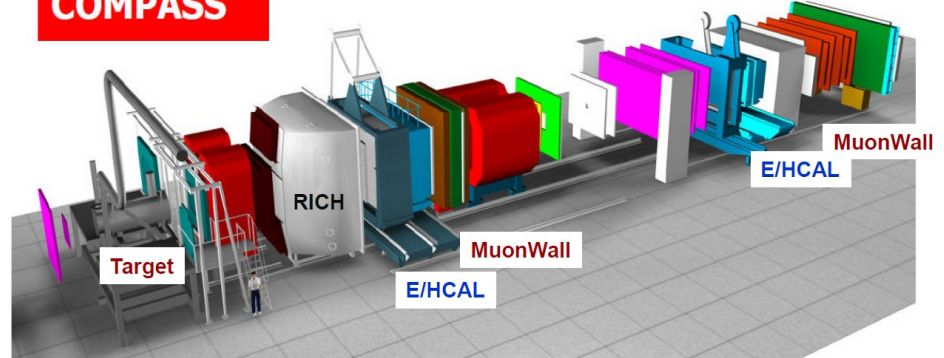


COMPASS spin

- high energy beam
- large angular acceptance
- broad kinematical range

two stages spectrometer
 Large Angle Spectrometer (SM1)
 Small Angle Spectrometer (SM2)

COMPASS



variety of tracking detectors to cope with different particle flux from $\theta = 0$ to $\theta \approx 200$ mrad

- SciFi
- Silicon
- Micromegas
- MWPC
- GEMs
- Straws
- SDC
- W45

Beam	26.7 GeV	pol. electron/positron
Target	1996-1997	Long. H
	1998-2000	Long. D
	2002-2005	Trans. H
	2006-2007	unpol. H

Beam	160 GeV	pol. muon
Target	2002 - 2006	Long. + Trans. 6LiD
	2007	Long. + Trans. NH_3
	2010	Trans. NH_3
	2011	Long. NH_3

+ JLab experiments

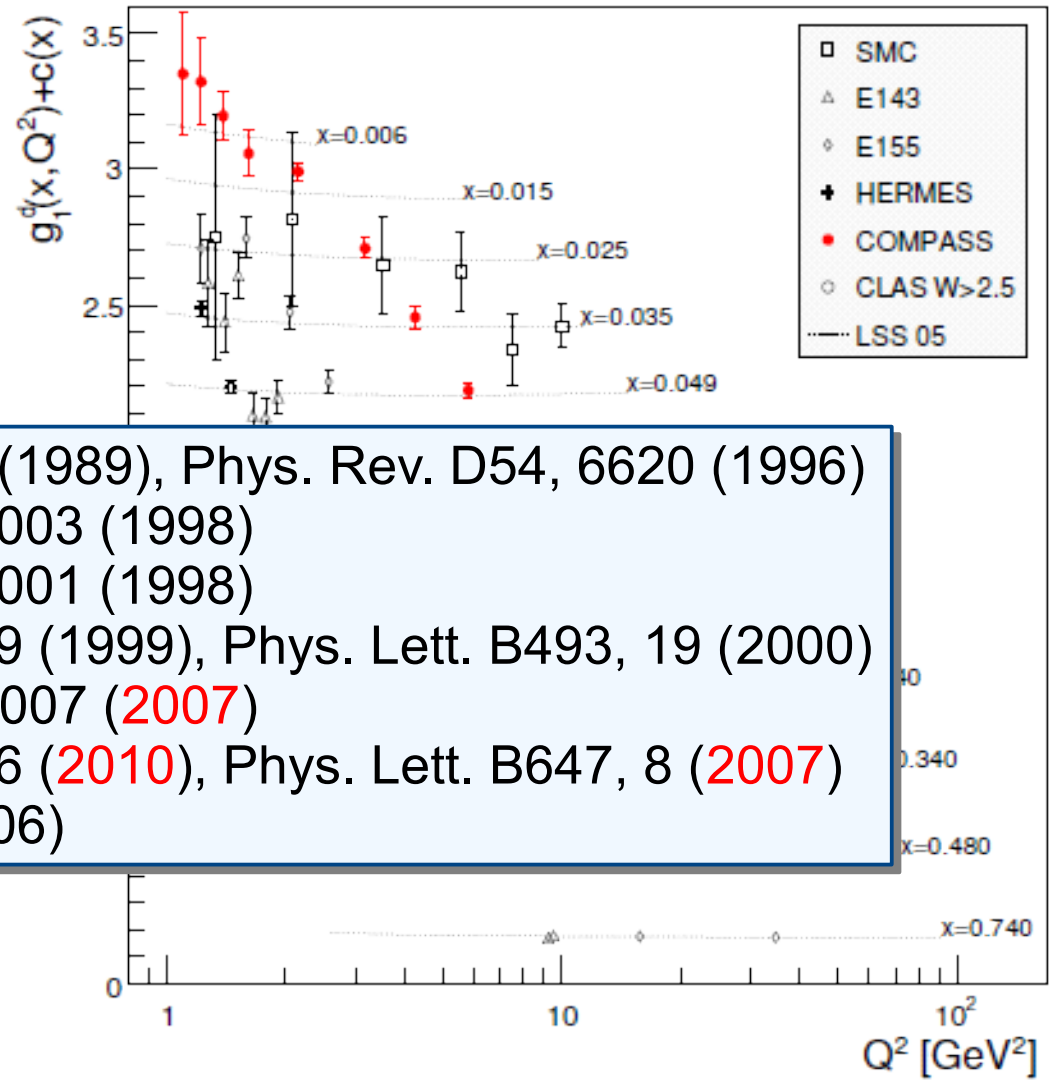
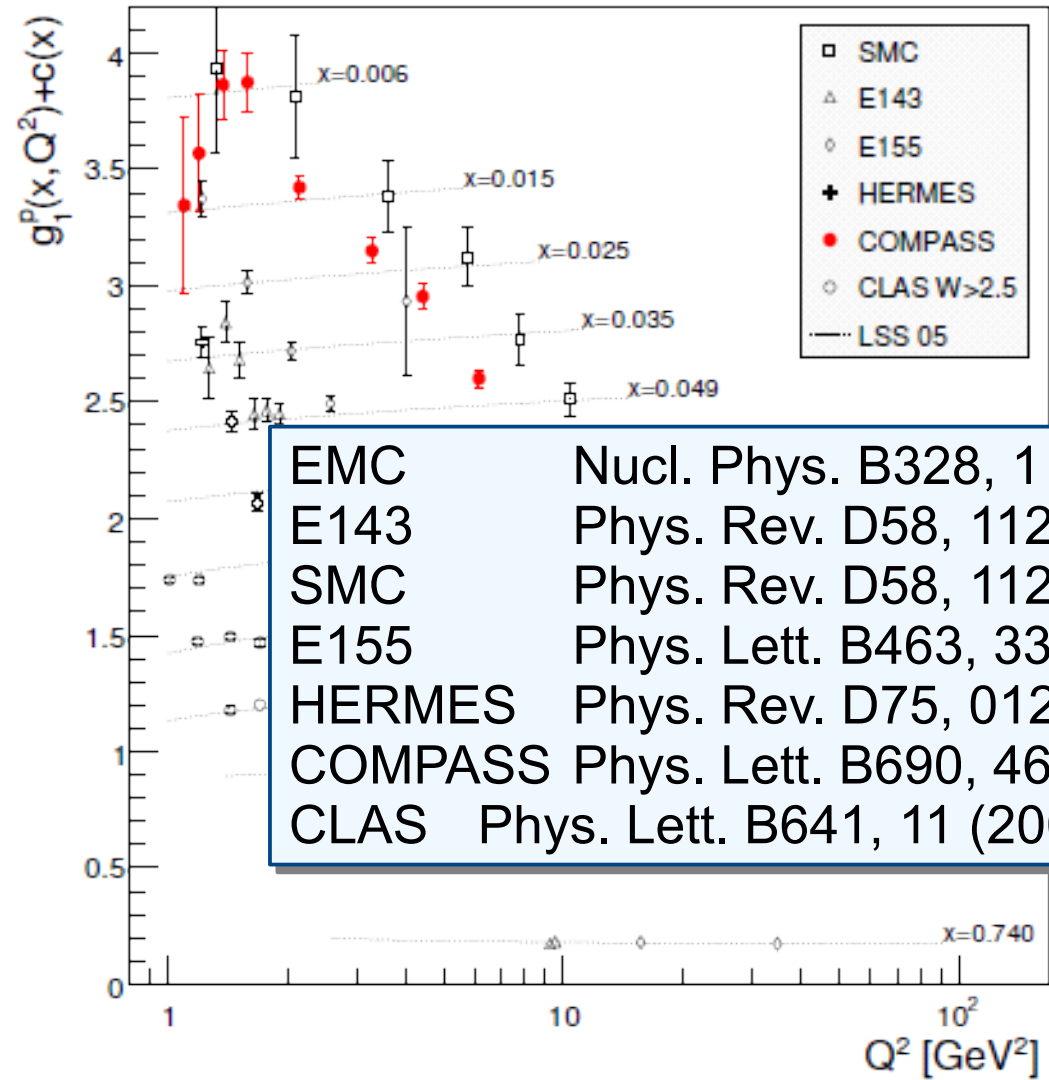


Polarized structure function

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Proton

Deuteron



EMC	Nucl. Phys. B328, 1 (1989), Phys. Rev. D54, 6620 (1996)
E143	Phys. Rev. D58, 112003 (1998)
SMC	Phys. Rev. D58, 112001 (1998)
E155	Phys. Lett. B463, 339 (1999), Phys. Lett. B493, 19 (2000)
HERMES	Phys. Rev. D75, 012007 (2007)
COMPASS	Phys. Lett. B690, 466 (2010), Phys. Lett. B647, 8 (2007)
CLAS	Phys. Lett. B641, 11 (2006)



Polarized structure function

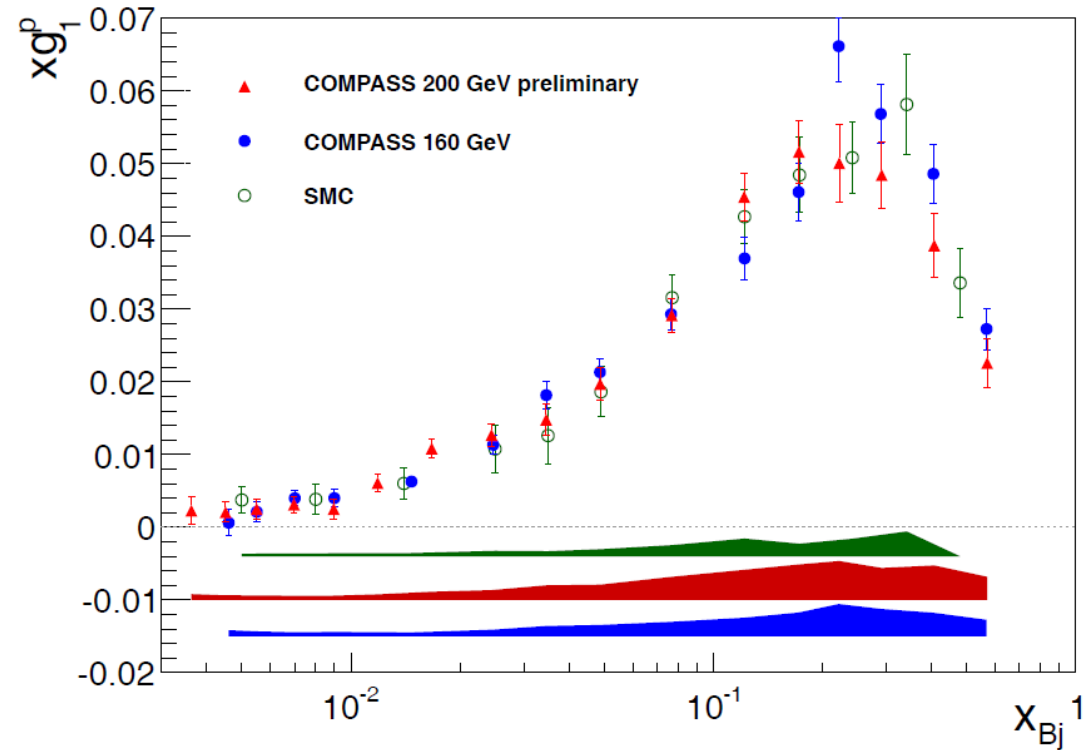
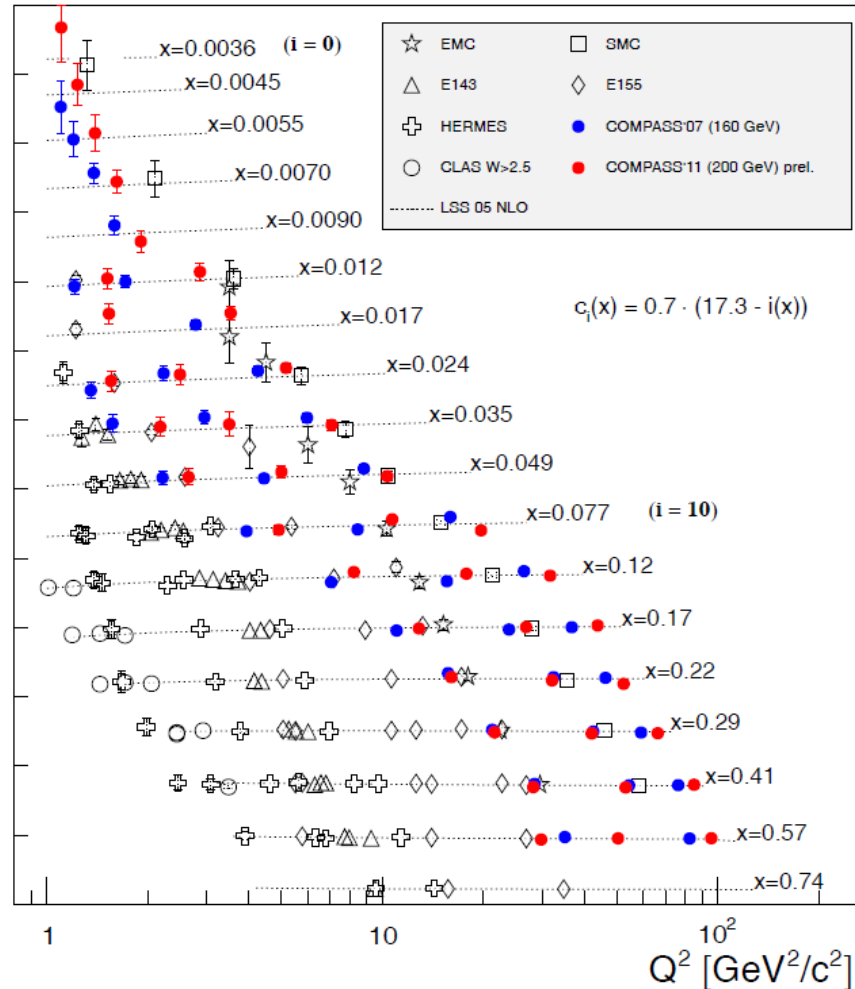
V. Andrieux, DIS2013



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Years	Target	Beam Energy
2002-2006	${}^6\text{LiD}$	160 GeV
2007	NH_3	160 GeV
2011	NH_3	200 GeV

$g_1^p(x, Q^2) + c_1(x)$





Strange quark: Δs

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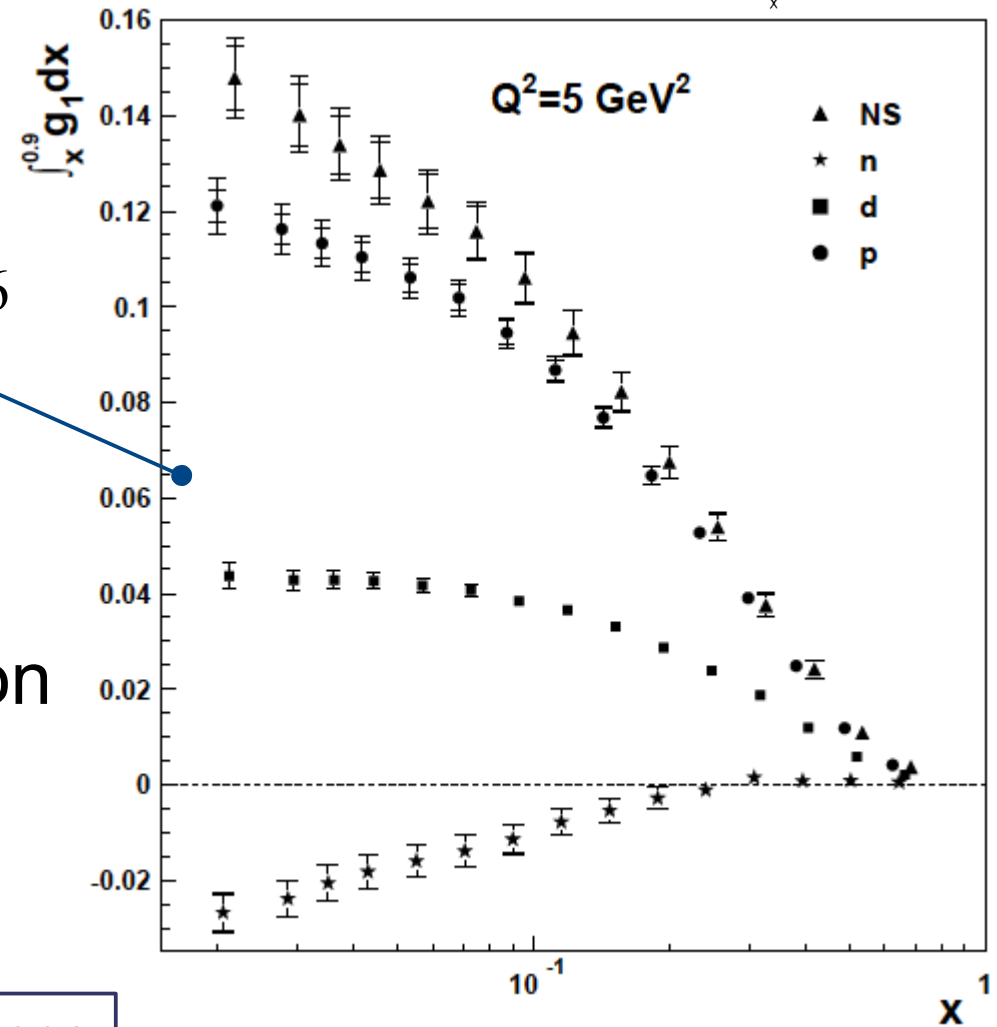
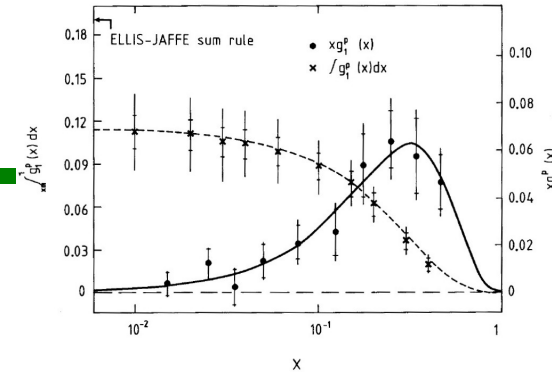
Phys. Rev. D 75 (2007) 012007

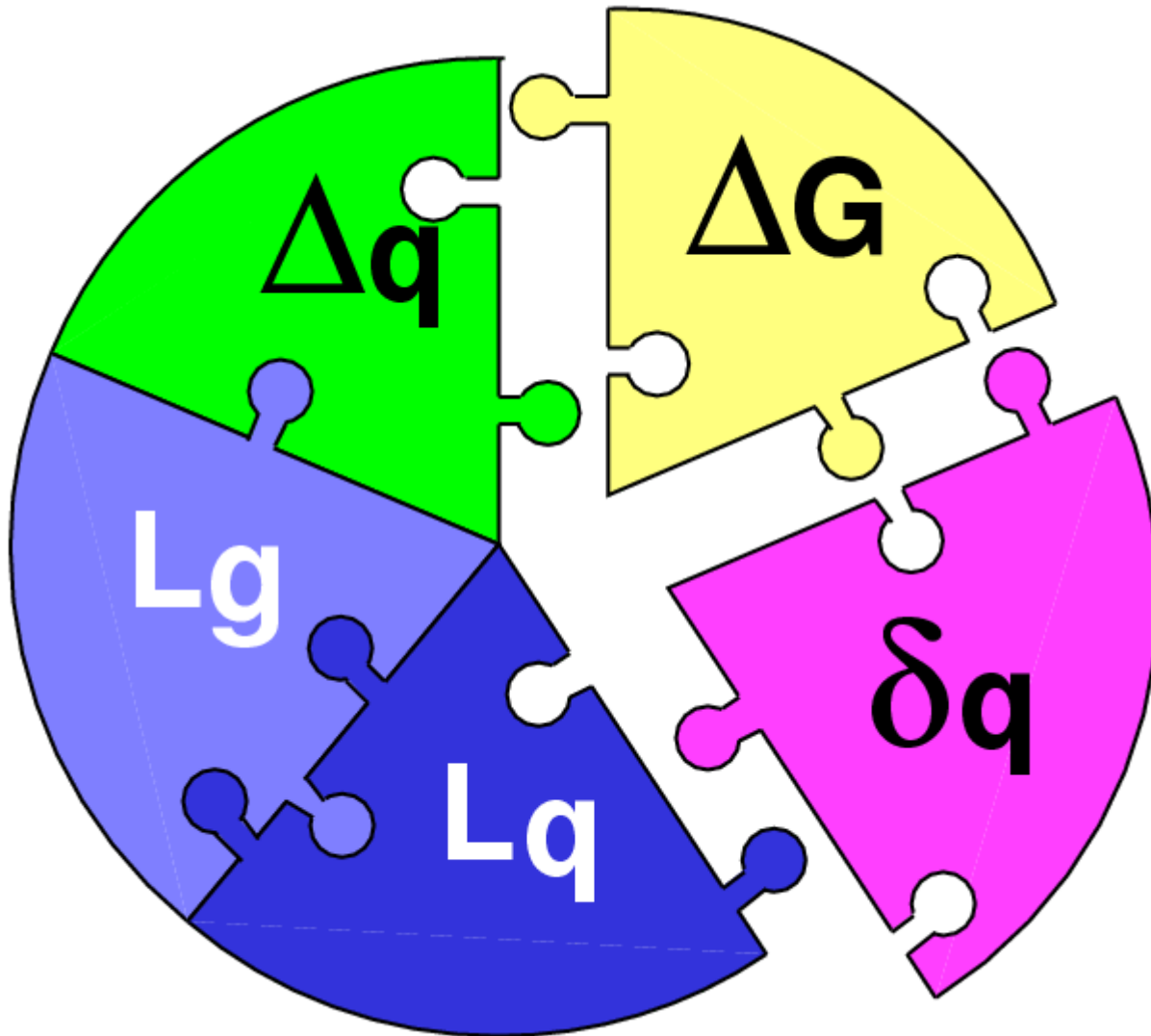
$$\int_{0.021}^{0.9} g_1^d(x, 5 \text{ GeV}^2) dx = 0.0436 \pm 0.0012 \pm 0.018 \pm 0.0008 \pm 0.0026$$

Assumption:

- High x contribution = 0
- Saturation in the lower x region
- **SU(3) flavor symmetry:**

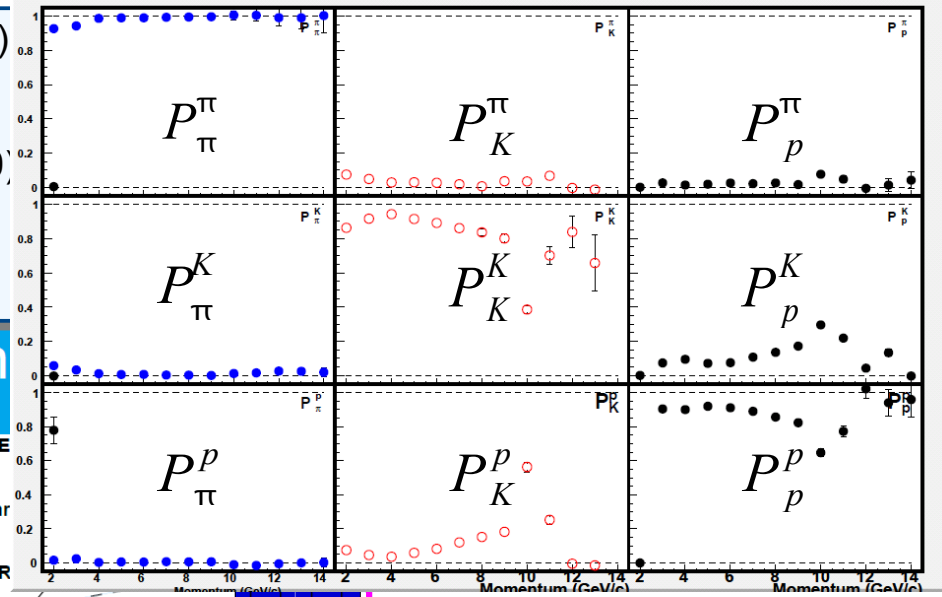
$$\Delta s(5 \text{ GeV}^2) = -0.085 \pm 0.013 \pm 0.008 \pm 0.009$$



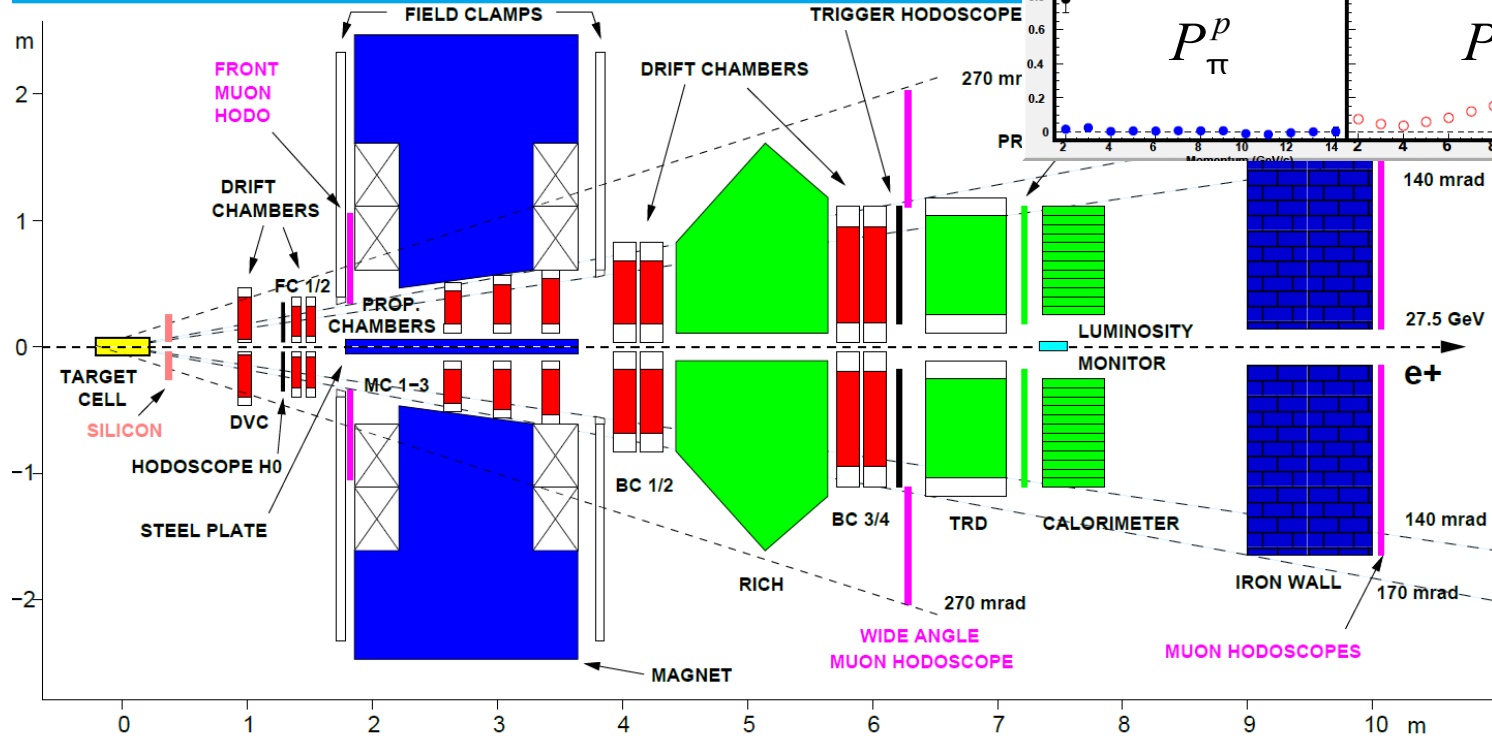


DIS 2nd generation, Semi-Inclusive measurement

- EMC Nucl. Phys. B328, 1 (1989), Phys. Rev. D54, 6620 (1996)
- E143 Phys. Rev. D58, 112003 (1998)
- SMC Phys. Rev. D58, 112001 (1998)
- E155 Phys. Lett. B463, 339 (1999), Phys. Lett. B493, 19 (2000)
- HERMES Phys. Rev. D75, 012007 (2007)
- COMPASS Phys. Lett. B690, 466 (2010), Phys. Lett. B647, 8 (2007)
- CLAS Phys. Lett. B641, 11 (2006)



The HERMES spectrom



Internal gas targets:

- Longitudinally polarized H, D
- Transversely polarized H
- Unpolarized $H, D, {}^4\text{He}, N, Ne, Kr, Xe$

Forward magnetic spectrometer

- Momentum resolution $1-2\%$
- Particle identification:
 $RICH, TRD, H_2, calorimeter$

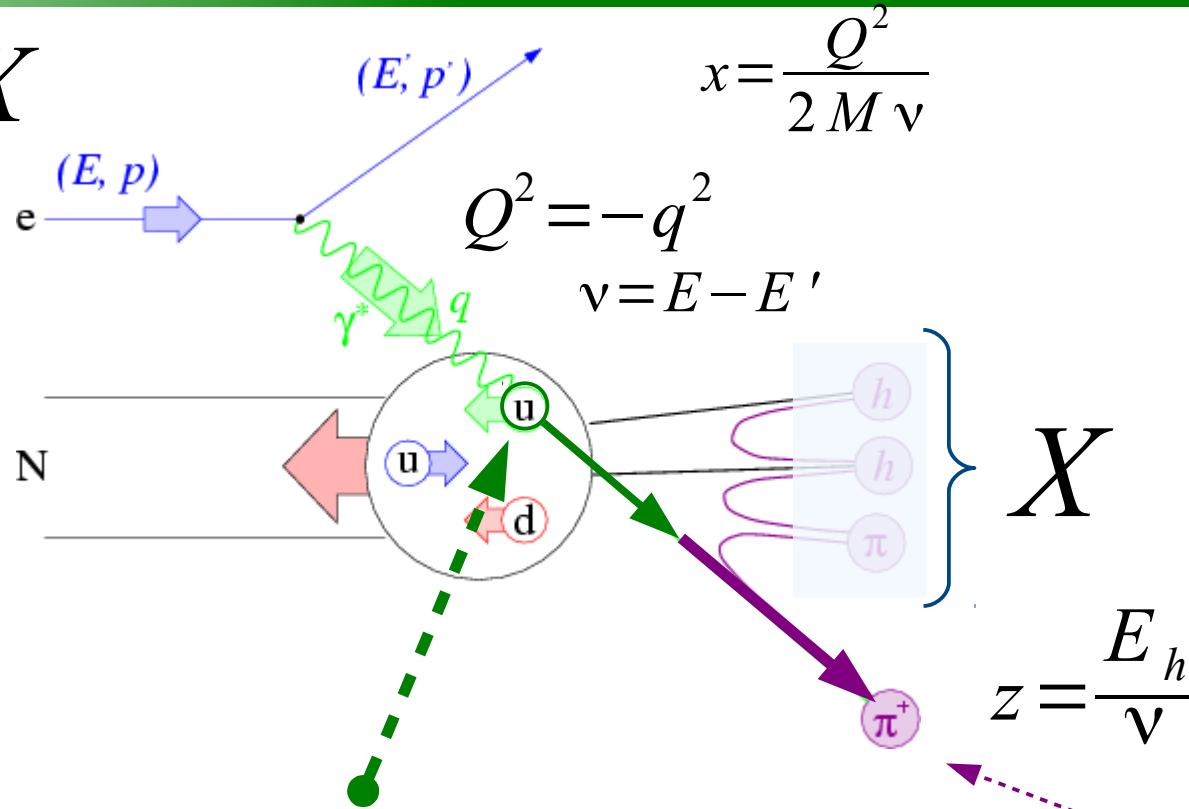


Semi-inclusive measurement of DIS

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$$e N \rightarrow e' h X$$

$$x = \frac{Q^2}{2 M \nu}$$



$$\sigma^{e N \rightarrow e' h X} = \sum_q f^{N \rightarrow q} \otimes \hat{\sigma}^{e q \rightarrow e' q} \otimes D^{q \rightarrow h}$$

Parton **D**istribution **F**unction

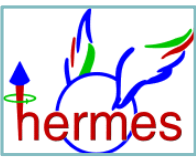
$$f(x, Q^2)$$

Fragmentation **F**unction

$$D(z, Q^2)$$



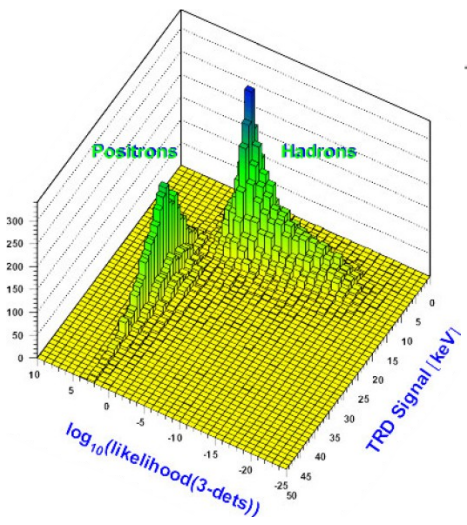
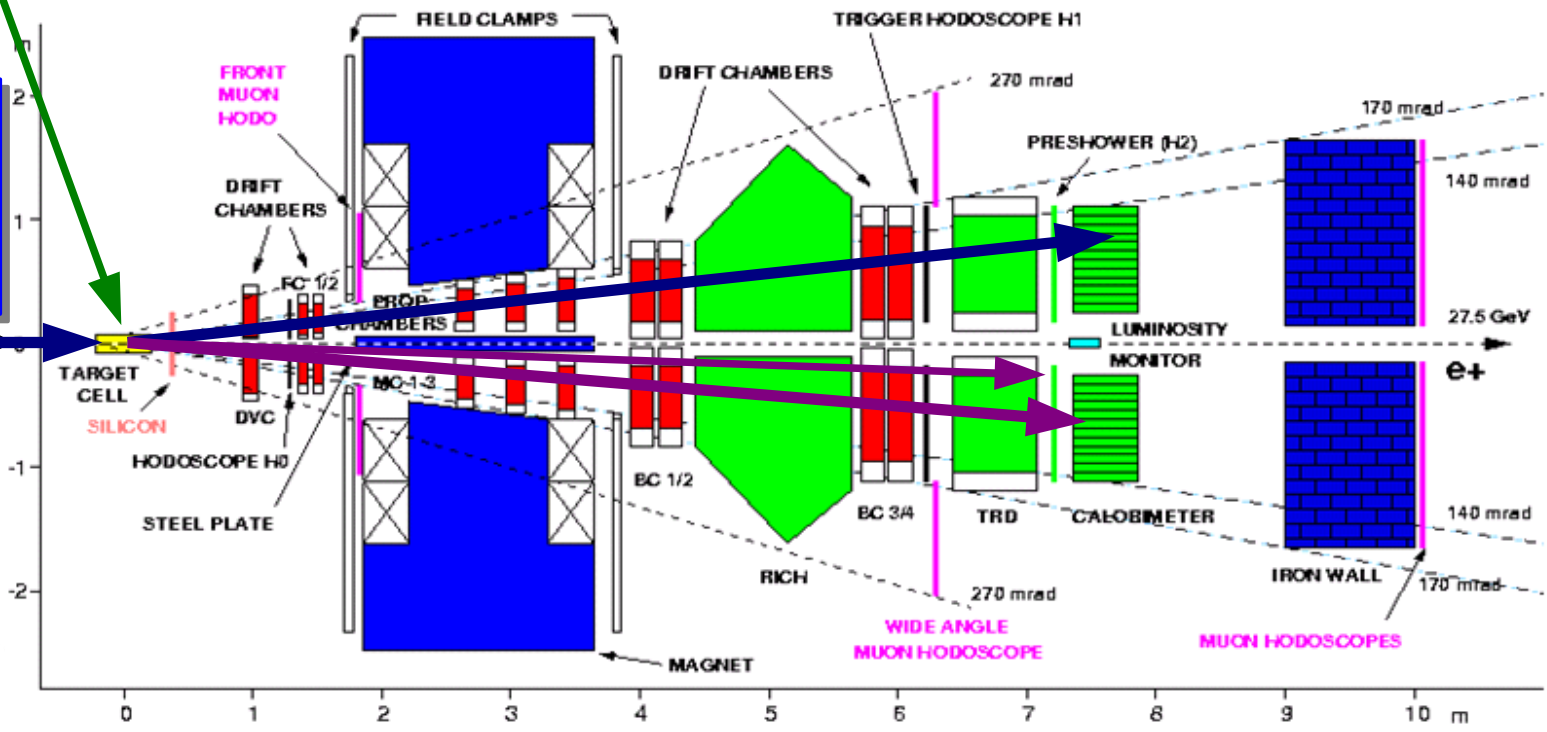
Example: HERMES experiment



Targets: Unpolarized H, D, nuclei
Longitudinally polarized H, D ($P \sim 85\%$)
Transversely polarized H ($P \sim 75\%$)

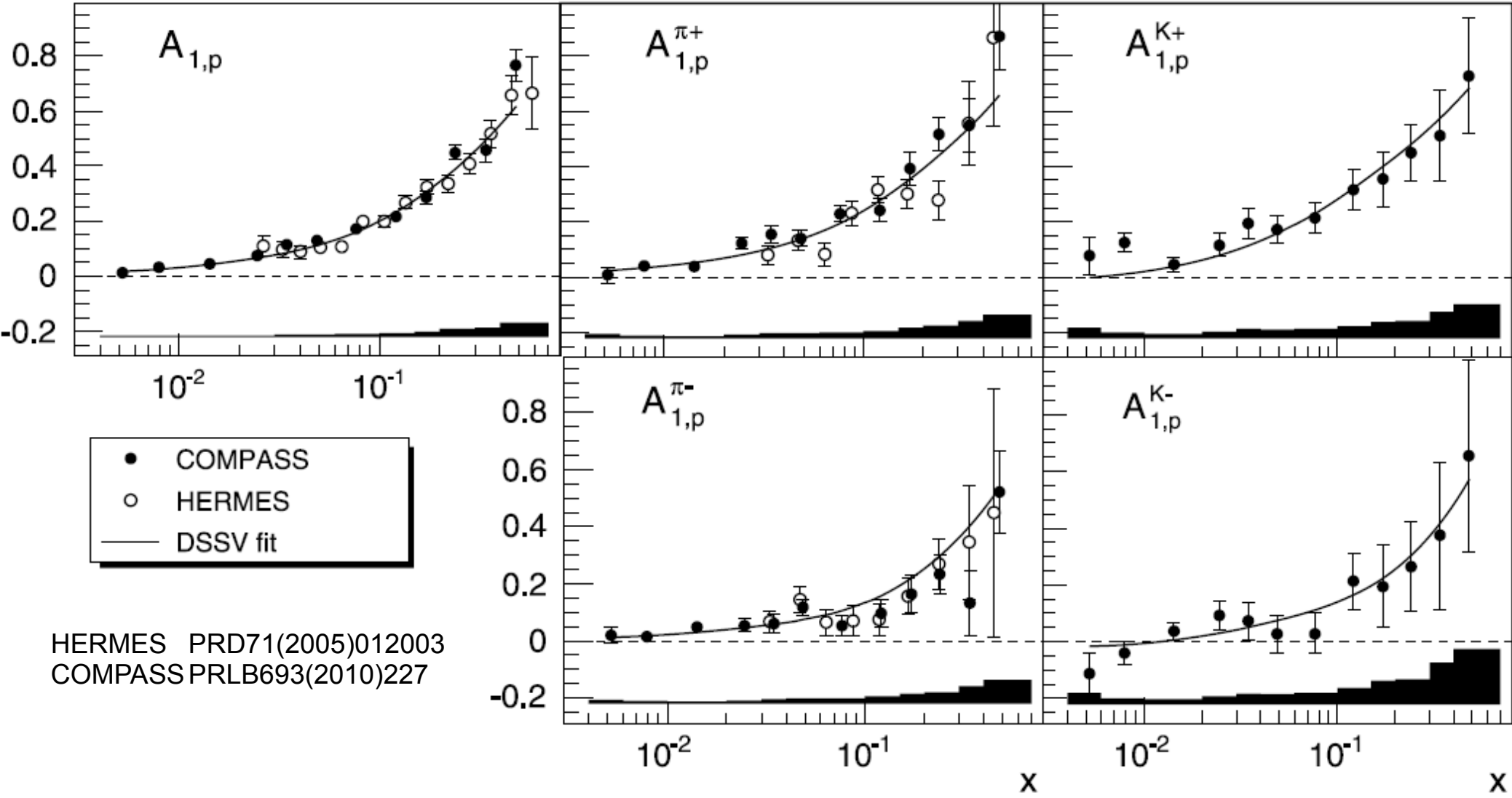
$$e + N \rightarrow e' + h + X$$

HERA: 27.6 GeV
polarized
 electron/positron



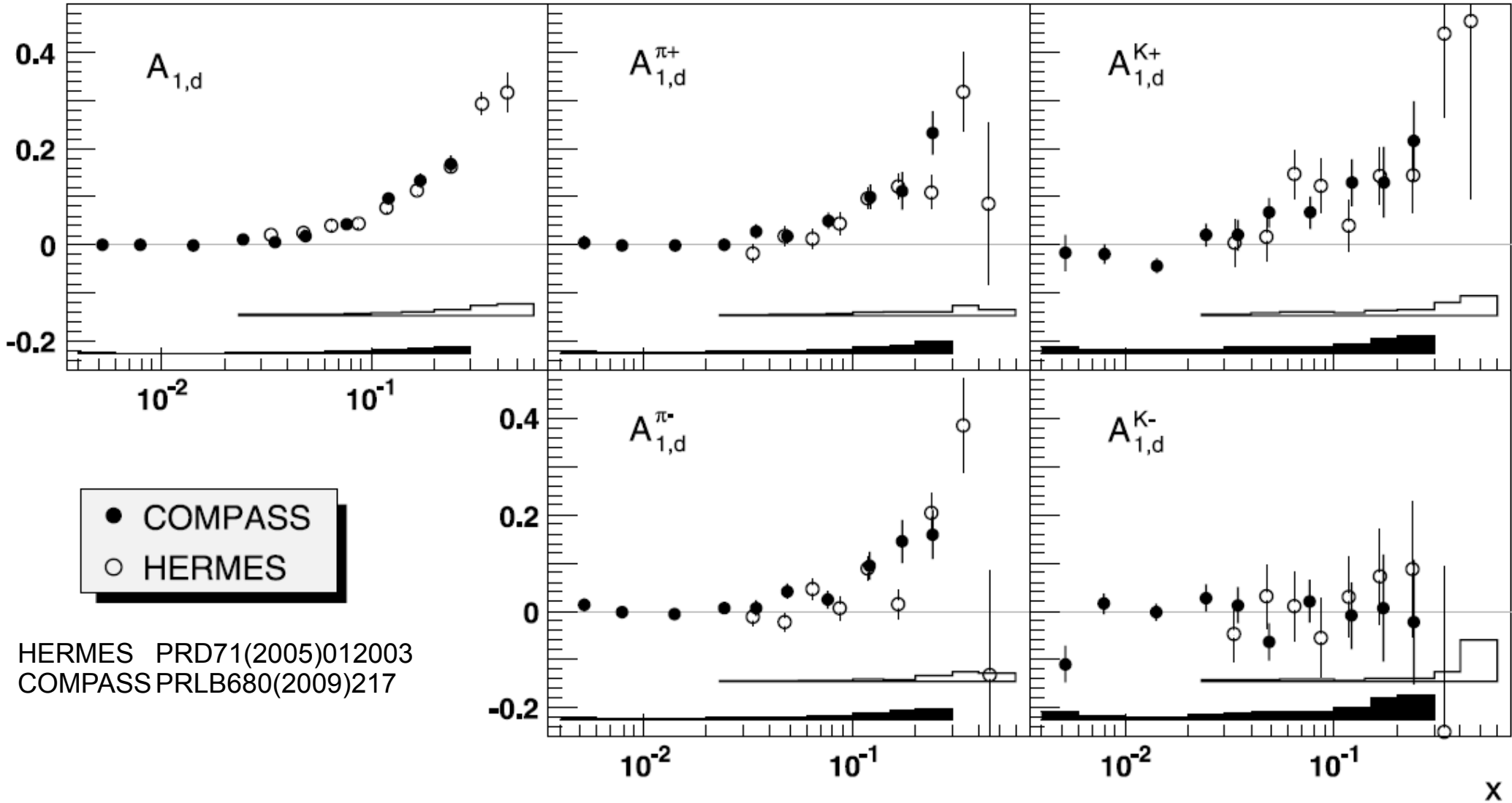
Reconstruction: $\Delta p/p < 2\%$, $\Delta\theta < 0.6$ mrad
 Lepton selection efficiency: $> 99\%$
 with hadron contamination $< 1\%$
 Hadron ID with RICH: π, K, p in $2 < p < 15$ GeV/c

Double spin asymmetry in SIDIS: proton target



HERMES PRD71(2005)012003
COMPASS PRLB693(2010)227

Double spin asymmetry in SIDIS: proton target





Quark helicity distributions

PRD71(2005)012003

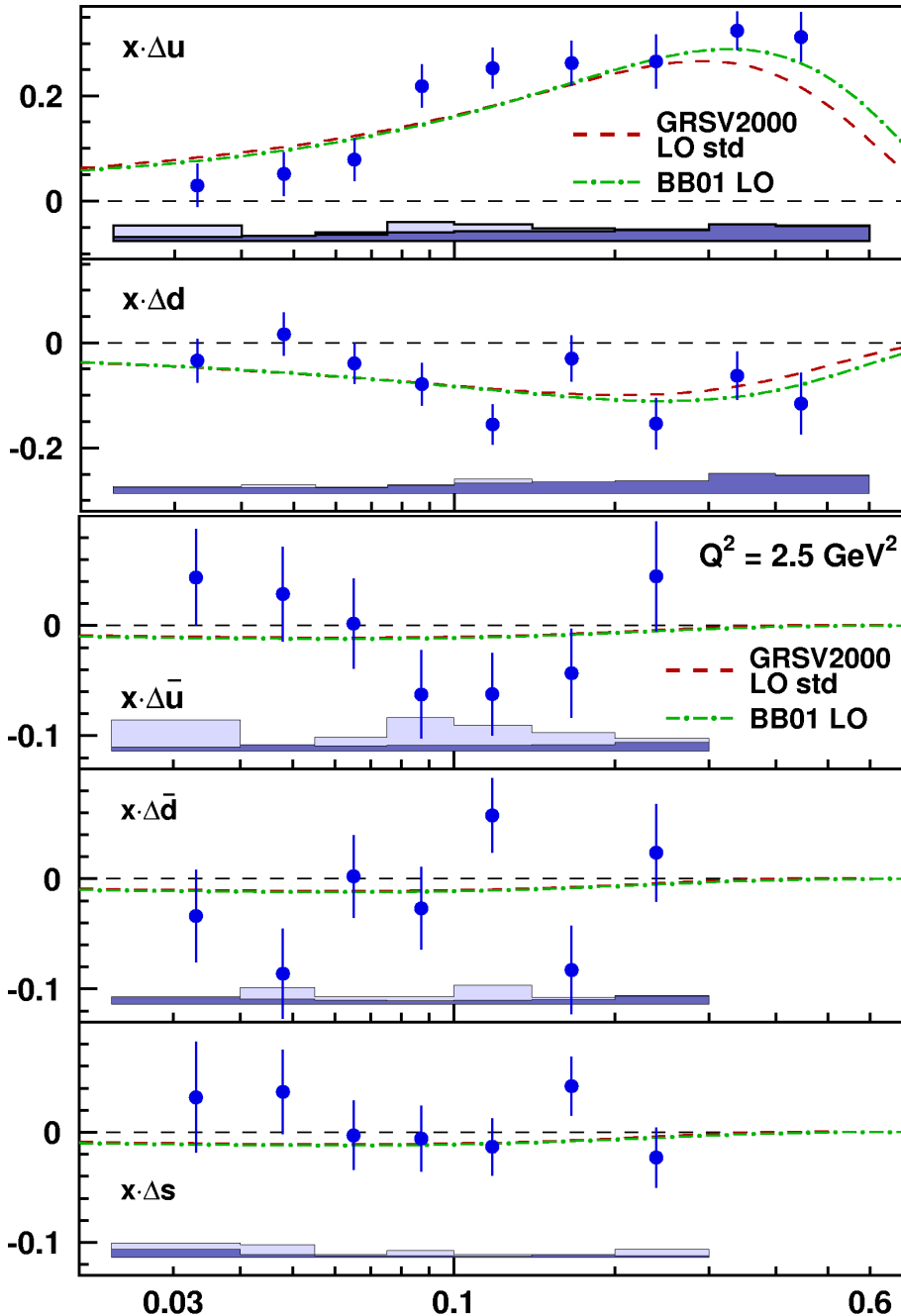
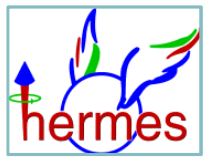


TABLE VIII. First and second moments of various helicity distributions in the measured range at a scale of $Q_0^2 = 2.5 \text{ GeV}^2$.

$0.023 < x < 0.6$	Moments in measured range
Δu	$0.601 \pm 0.039 \pm 0.049$
$\Delta \bar{u}$	$-0.002 \pm 0.036 \pm 0.023$
Δd	$-0.226 \pm 0.039 \pm 0.050$
$\Delta \bar{d}$	$-0.054 \pm 0.033 \pm 0.011$
Δs	$0.028 \pm 0.033 \pm 0.009$

Inclusive measurements [PRD75\(2007\)012007](#)
 $\Delta s + \Delta \bar{s} = -0.085 \pm 0.013 \pm 0.008 \pm 0.009$
 $\Delta \Sigma = 0.330 \pm 0.025 \pm 0.011 \pm 0.028$

$\Delta \Sigma$	$0.347 \pm 0.024 \pm 0.066$
Δq_3	$0.880 \pm 0.045 \pm 0.107$
Δq_8	$0.262 \pm 0.078 \pm 0.045$

From charged kaon asymmetry [PLB666\(2008\)446](#)

$\Delta s + \Delta \bar{s} = 0.037 \pm 0.019 \pm 0.027$

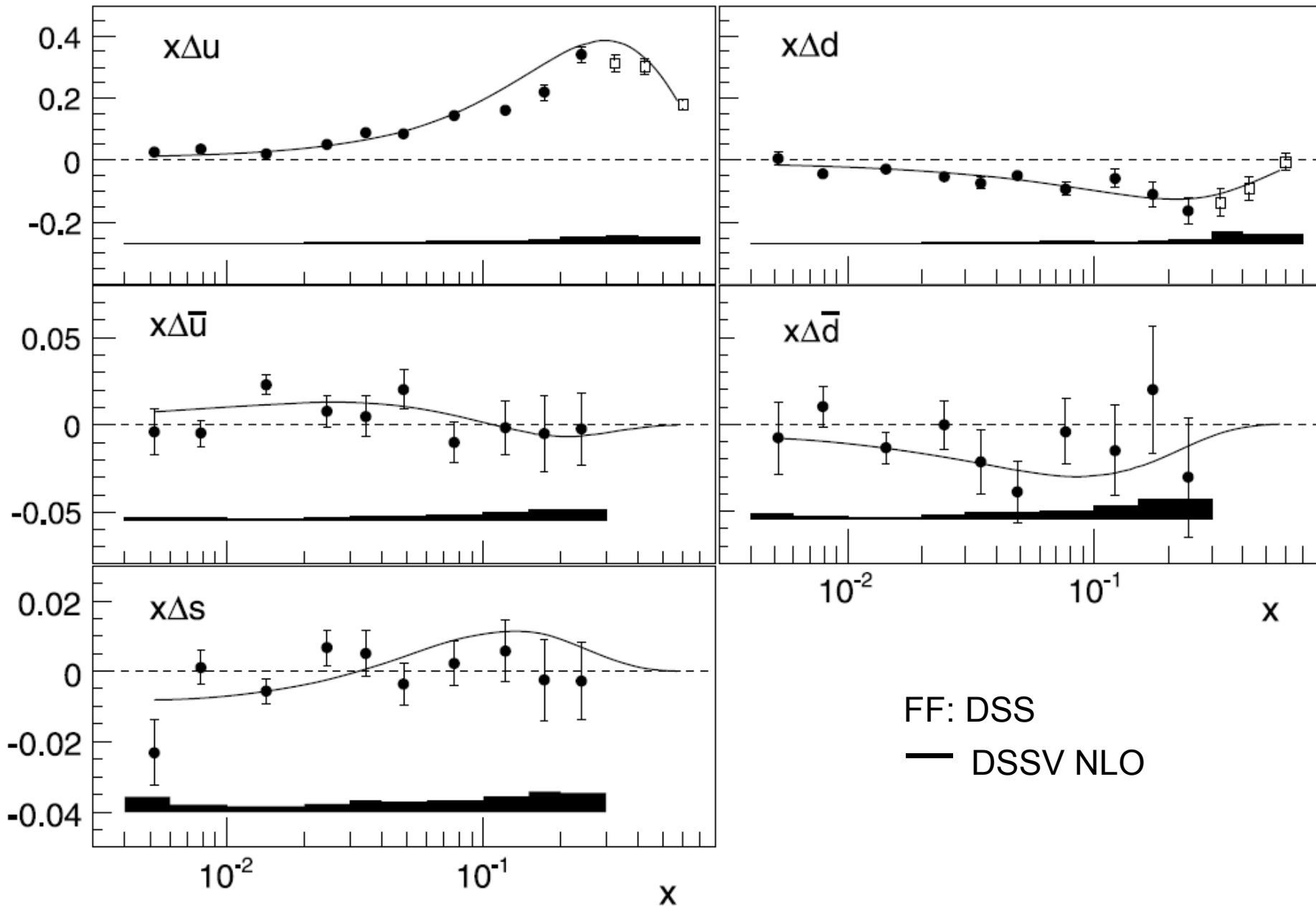


Quark helicity distributions

COMPASS PRLB693(2010)227

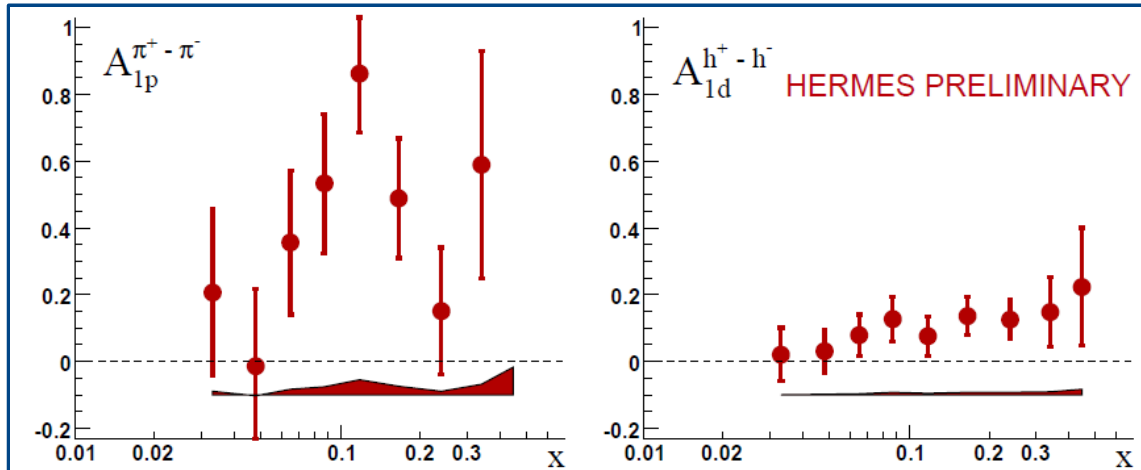


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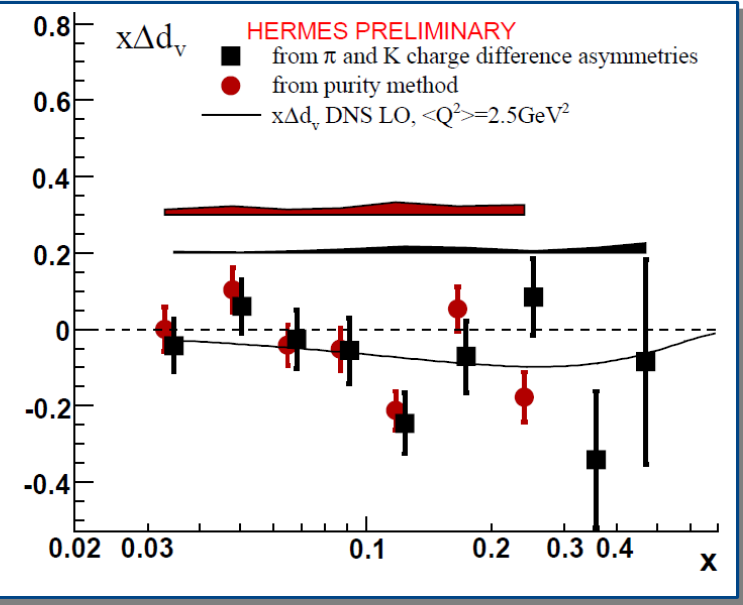
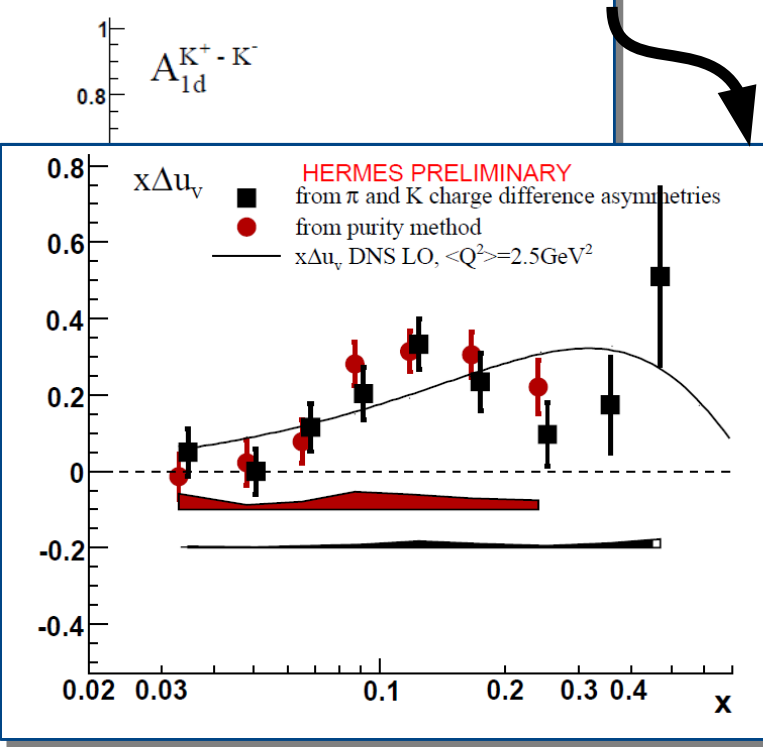
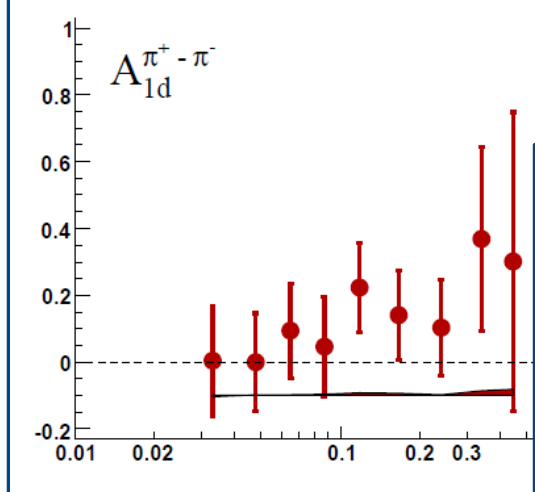


Difference asym. & valence quark



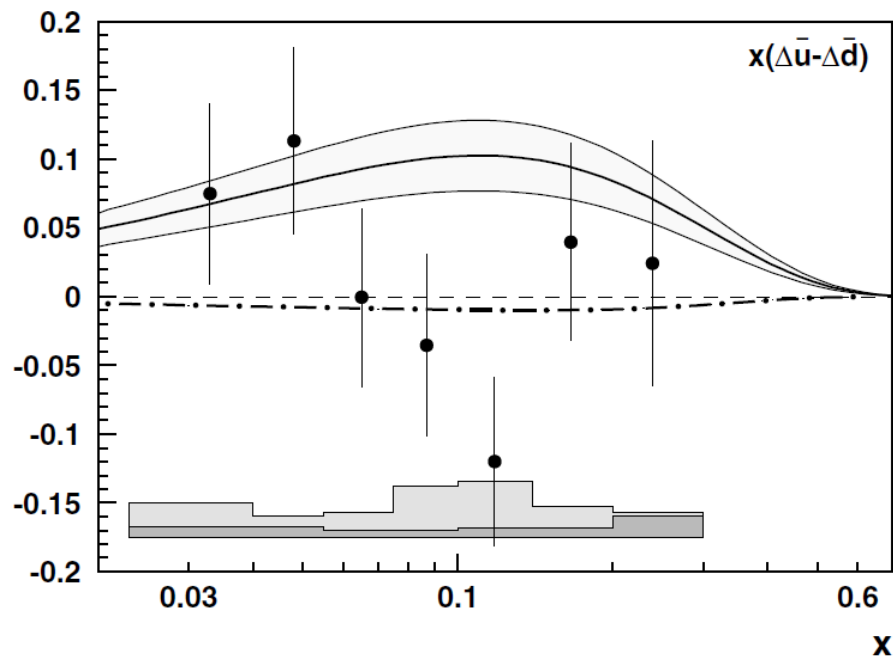
$$A_{1p}^{\pi^+ - \pi^-} = \frac{\Delta 4u_v - \Delta d_v}{4u_v - d_v}$$

$$A_{1d}^{\pi^+ - \pi^-} = \frac{\Delta u_v - \Delta d_v}{u_v - d_v}$$

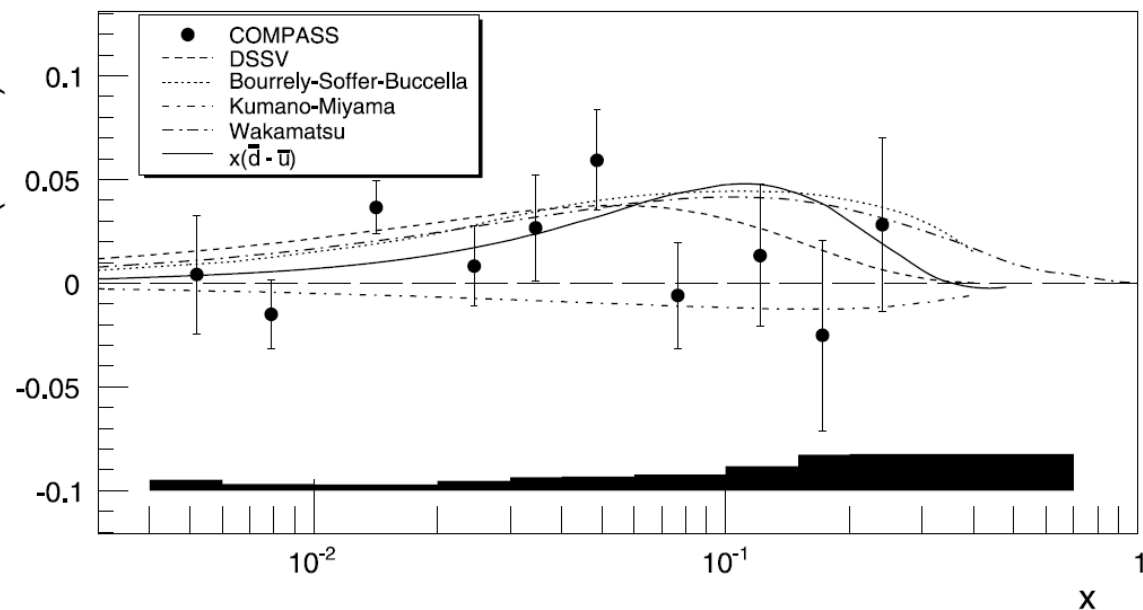


$$x (\Delta \bar{u} - \Delta \bar{d})$$

HERMES PRD71(2005)012003



COMPASS PRLB693(2010)227



COMPASS $\int_{0.004}^{0.3} (\Delta \bar{u} - \Delta \bar{d}) dx = 0.06 \pm 0.04 \pm 0.02 @ Q^2 = 3 (\text{GeV}/c)^2$

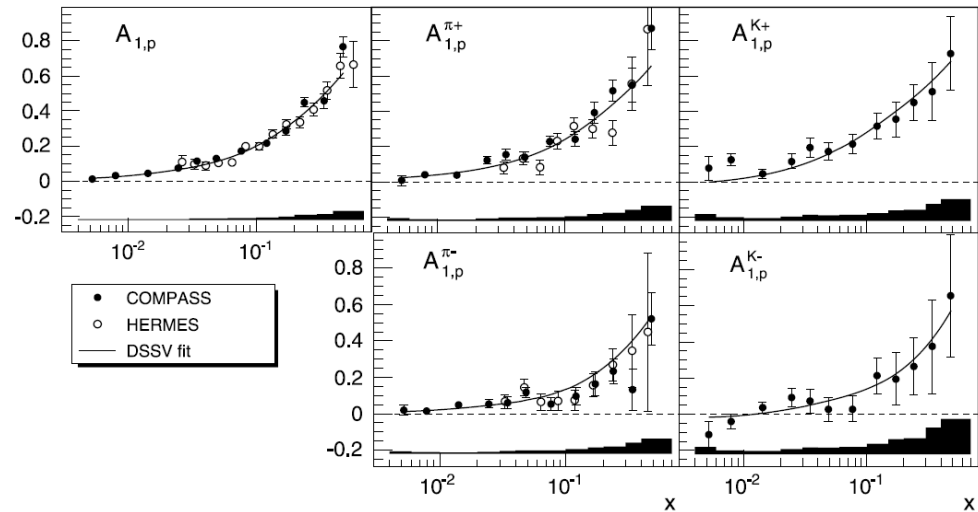
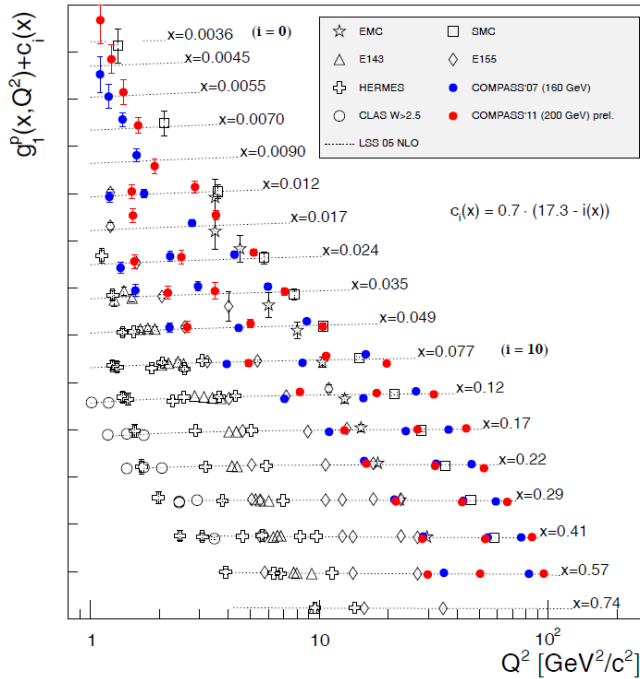
HERMES $\int_{0.023}^{0.6} (\Delta \bar{u} - \Delta \bar{d}) dx = 0.048 \pm 0.057 \pm 0.028 @ Q^2 = 2.5 (\text{GeV}/c)^2$

unp. E866 $\int_0^1 (\bar{u} - \bar{d}) dx = -0.118 \pm 0.012 @ Q^2 = 54 (\text{GeV}/c)^2$



$\Delta q, \Delta G$ from the global analysis

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Fragmentation Function
 $D(z, Q^2)$ i.e., DSS

+ QCD Evolution
 (pQCD parts)

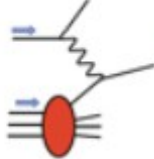
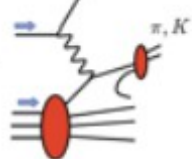
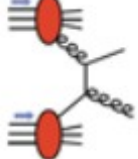


$\Delta q(x), \Delta G(x)$

Target difference
 Hadron difference

From scaling violation

overview of recent helicity PDF fits @ NLO

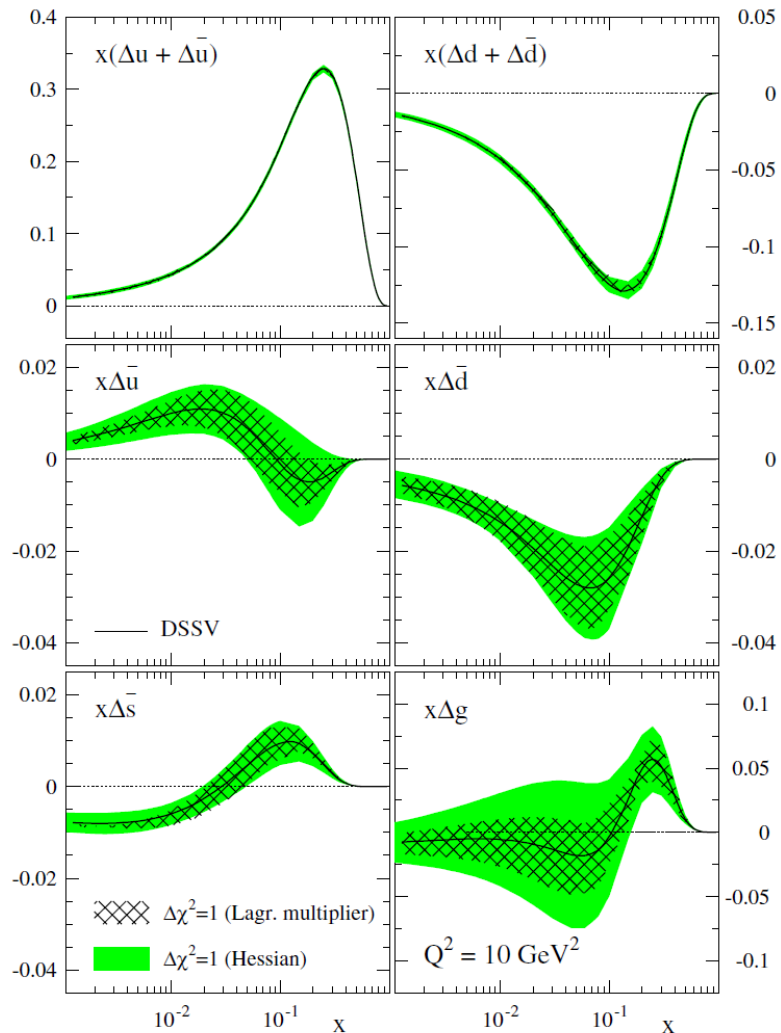
				uncertainties	last update
NNPDF Ball, Forte, Guffanti, Nocera, Rodolfi, Rojo				100 replicas stat. approach	1303.7236 Nocera (Tue)
DSSV de Florian, Sassot, MS, Vogelsang				L.M. $\Delta\chi^2 = 8$ (1) (Hessian $\Delta\chi^2 = 1$)	0904.3821 [DSSV+/++: 1112.0904 1304.0079]
LSS Leader, Sidorov, Stamenov				Hessian $\Delta\chi^2 = 1$	1010.0574
BB Blumlein, Bottcher				Hessian $\Delta\chi^2 = 1$	1010.3113
⋮	⋮	⋮	⋮		⋮
GRSV Gluck, Reya, MS, Vogelsang					1 st NLO analysis 9508347



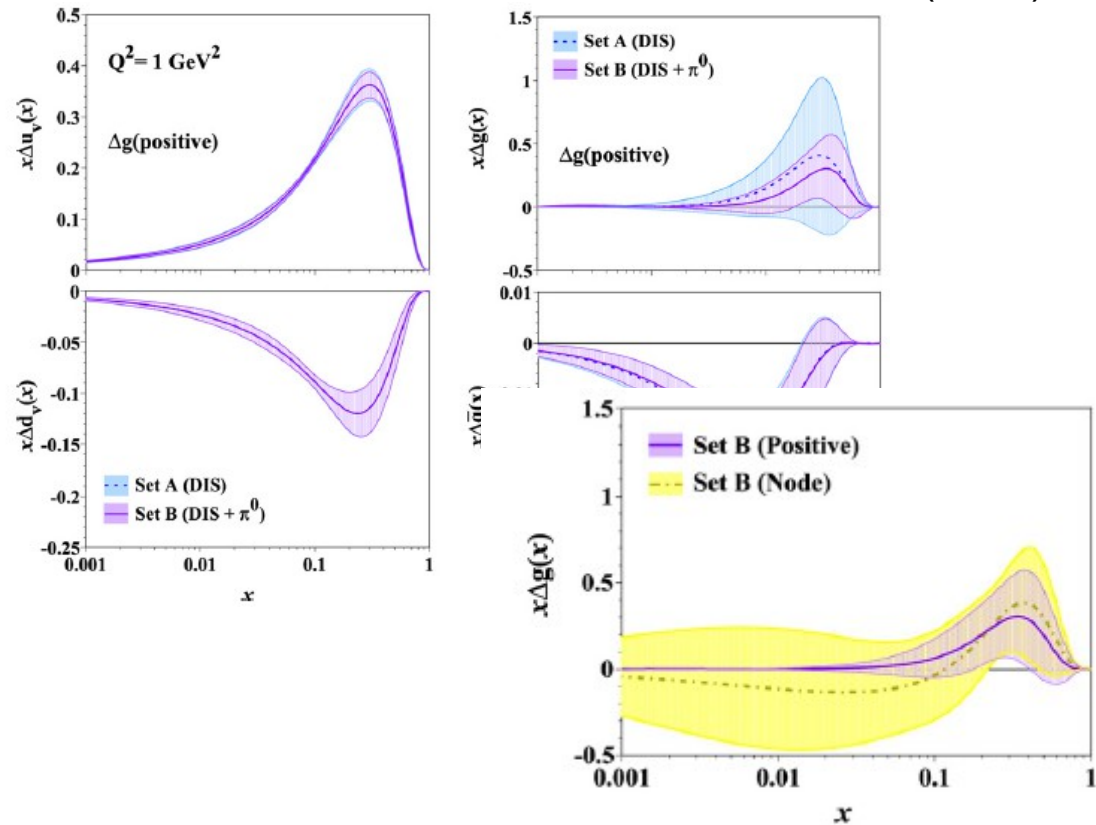
$\Delta q, \Delta G$ from the global analysis

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DSSV, PRD80(2009)034030



AAC, NPB813(2009)106



Lagrange multiplier $\Delta\chi^2 = 1$

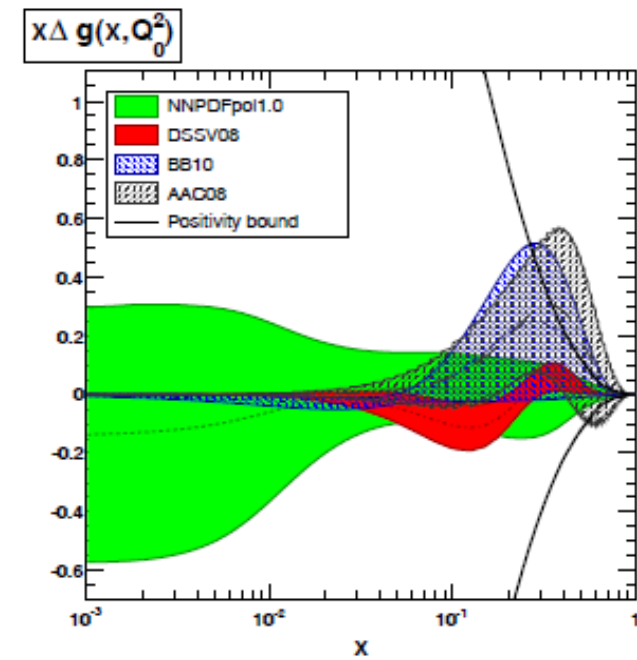
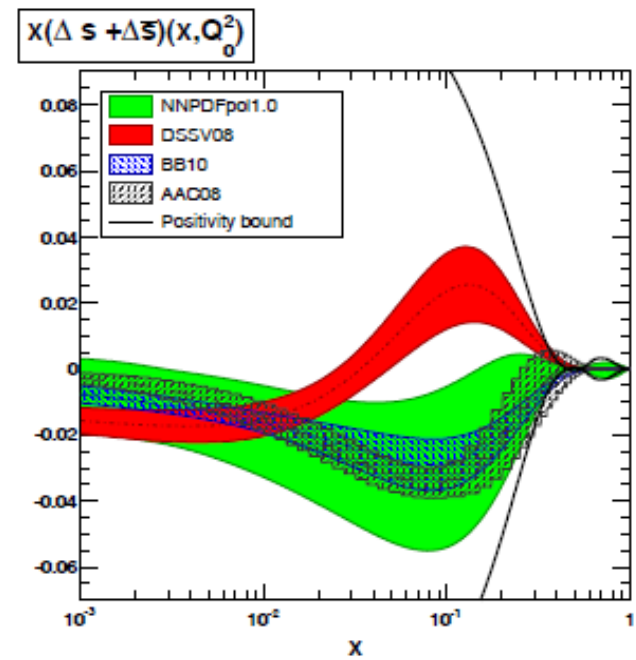
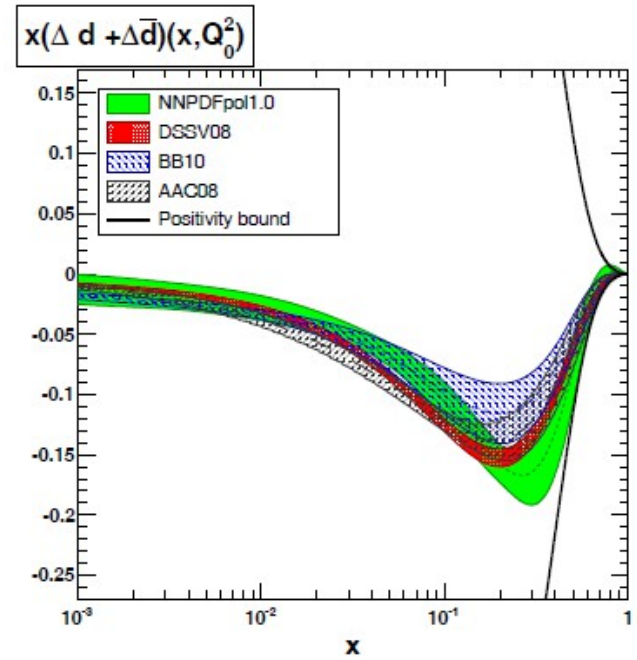
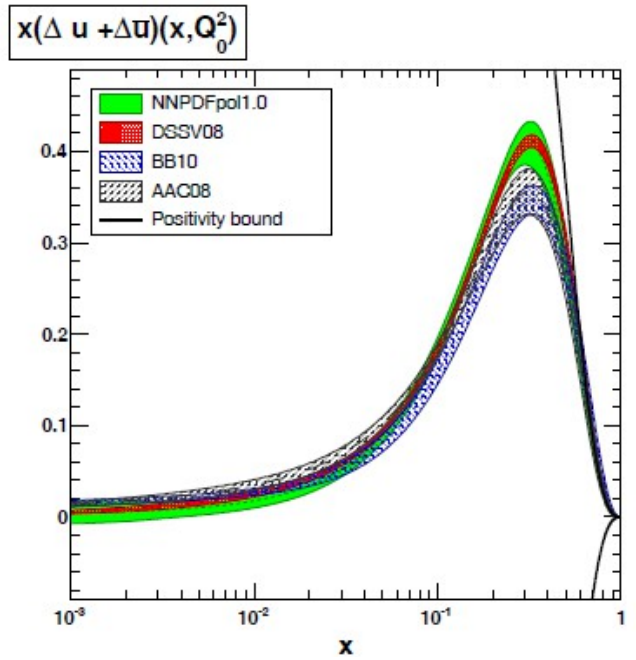
$\Delta u + \Delta \bar{u}$	$0.793^{+0.011}_{-0.012}$
$\Delta d + \Delta \bar{d}$	$-0.416^{+0.011}_{-0.009}$
$\Delta \bar{u}$	$0.028^{+0.021}_{-0.020}$
$\Delta \bar{d}$	$-0.089^{+0.029}_{-0.029}$
$\Delta \bar{s}$	$-0.006^{+0.010}_{-0.012}$
$\Delta \Sigma$	$0.366^{+0.015}_{-0.018}$
Δg	$0.013^{+0.106}_{-0.120}$
Δg^{RHIC}	$0.005^{+0.051}_{-0.058}$



$\Delta q, \Delta G$ from the global analysis

E. R. Nocera, DIS2013

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DSSV08
[\[arXiv:0904.3821\]](#)
 DIS+SIDIS+pp (π^0 /jet)

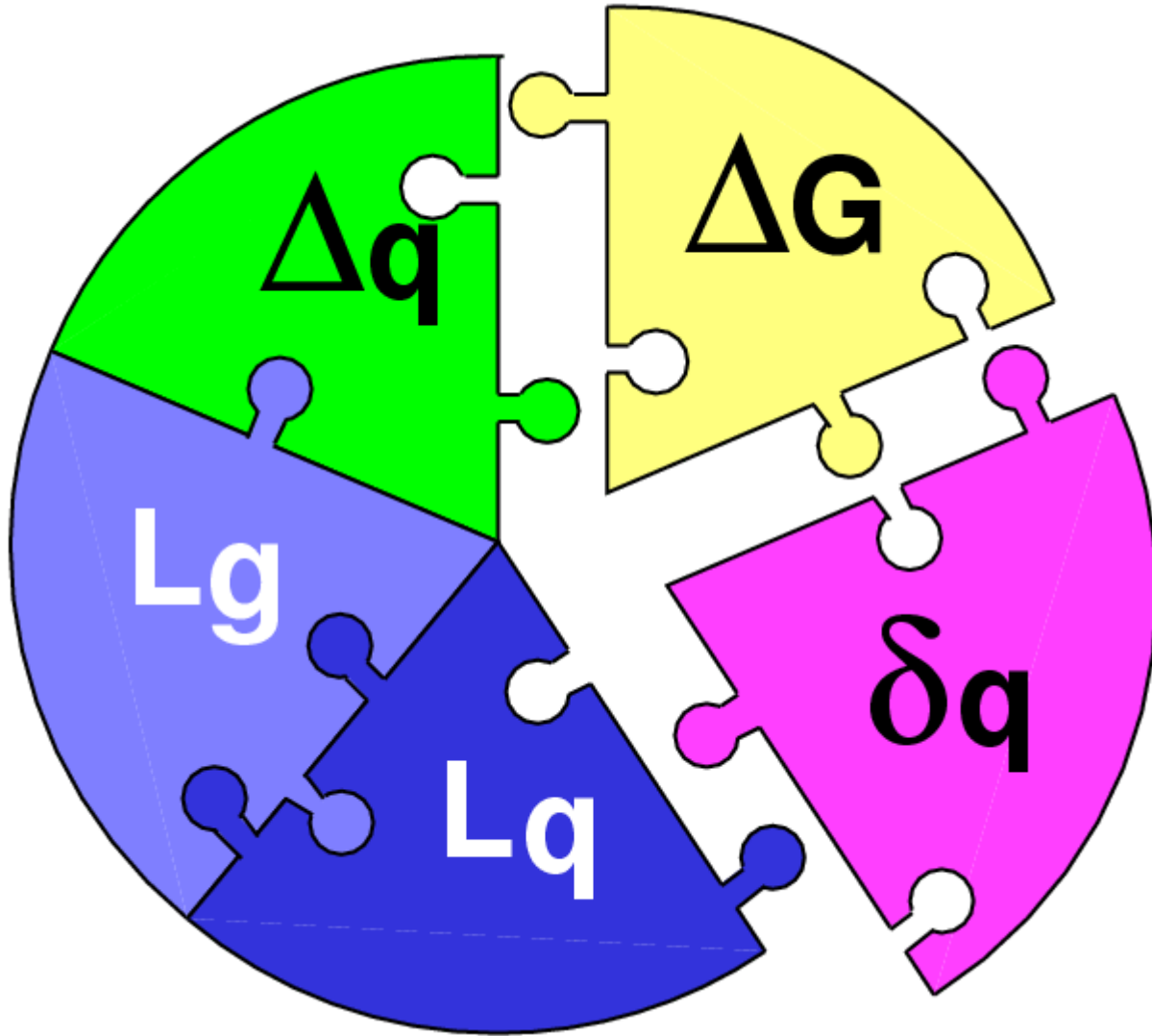
BB10
[\[arXiv:1005.3113\]](#)
 DIS only

AAC08
[\[arXiv:0808.0413\]](#)
 DIS+pp (π^0)

DSSV08
[\[arXiv:0904.3821\]](#)
 DIS+SIDIS+pp (π^0 /jet)

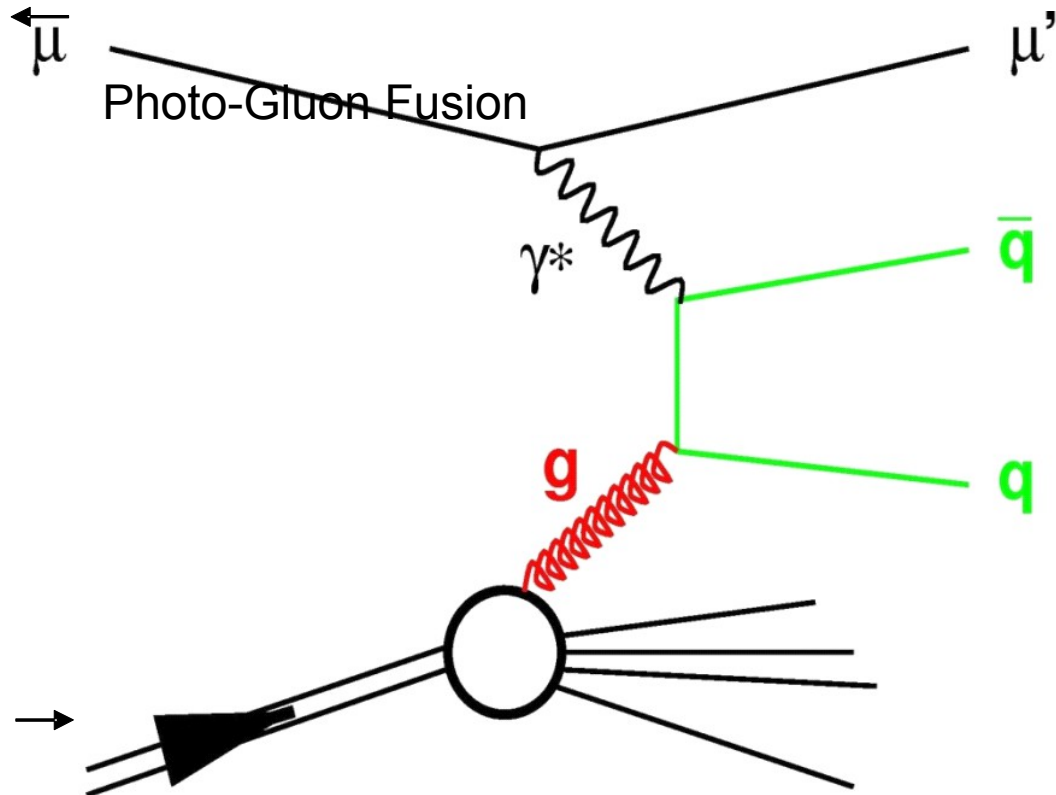
BB10
[\[arXiv:1005.3113\]](#)
 DIS only

AAC08
[\[arXiv:0808.0413\]](#)
 DIS+pp (π^0)



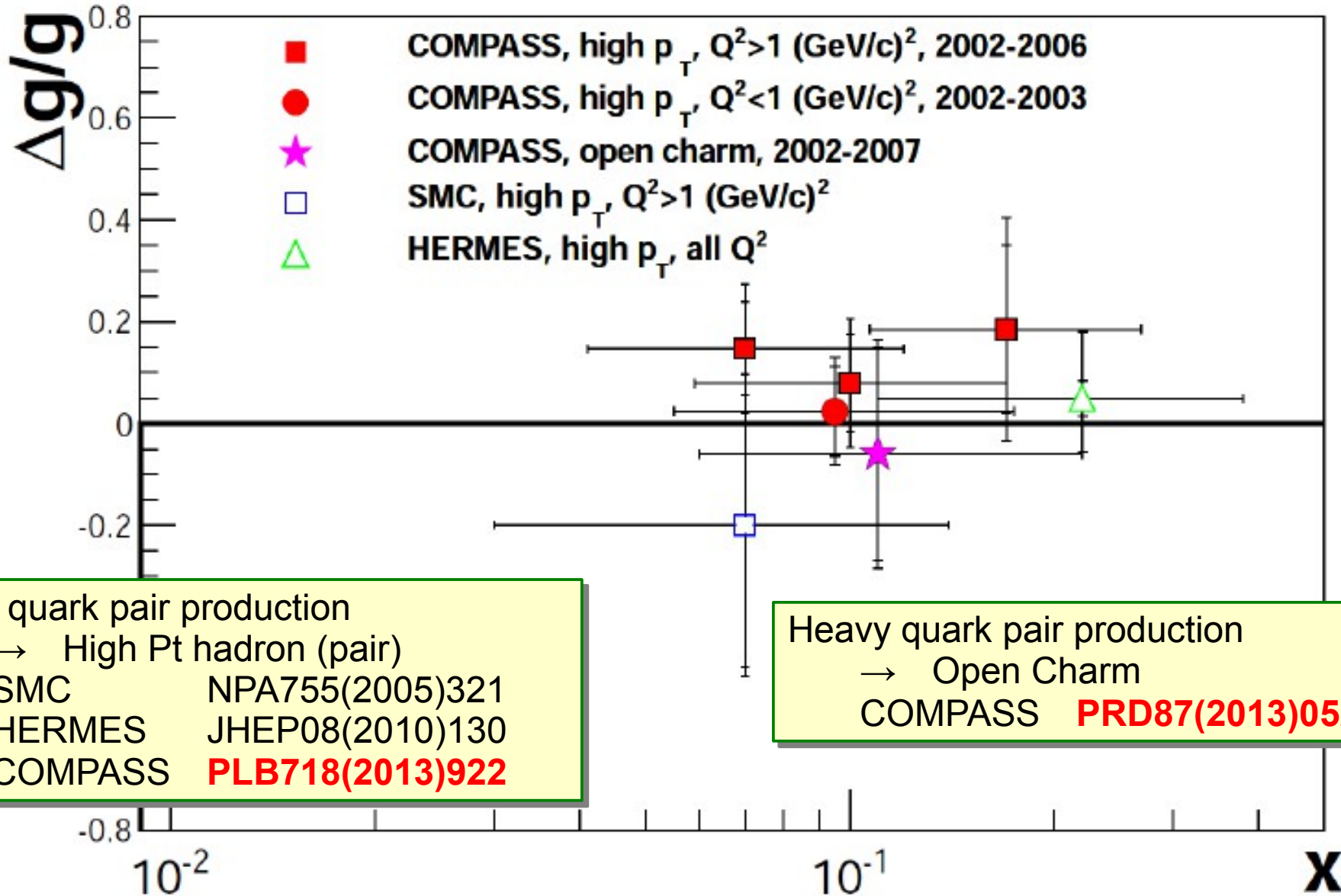


Direct determination on ΔG in SIDIS



Light quark pair production
→ High Pt hadron (pair)
SMC NPA755(2005)321
HERMES JHEP08(2010)130
COMPASS **PLB718(2013)922**

Heavy quark pair production
→ Open Charm
COMPASS **PRD87(2013)052018**



Light quark pair production
 → High Pt hadron (pair)
 SMC NPA755(2005)321
 HERMES JHEP08(2010)130
 COMPASS **PLB718(2013)922**

Heavy quark pair production
 → Open Charm
 COMPASS **PRD87(2013)052018**

