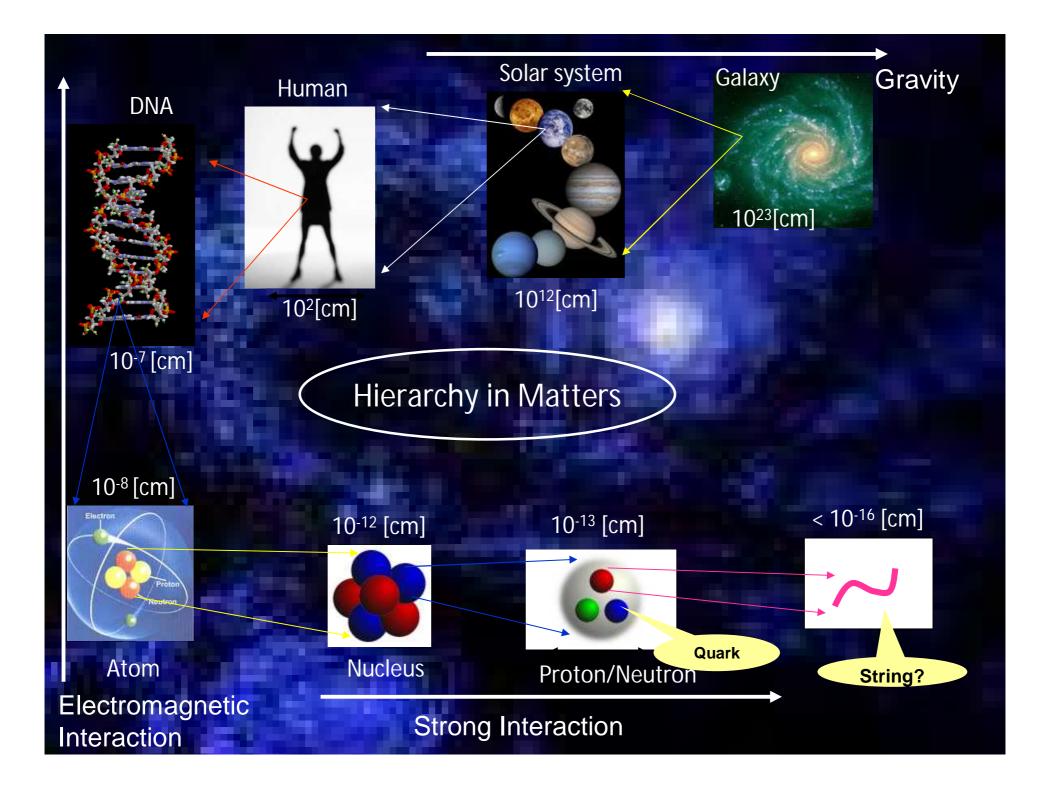
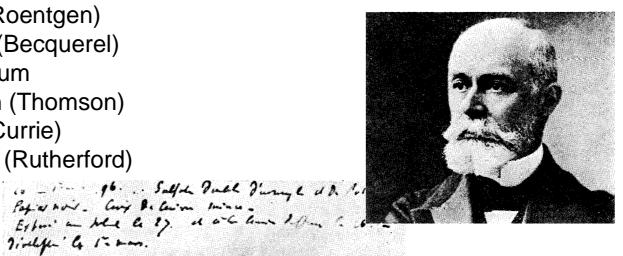
# **Nuclear Theory**





# Discovery of radioactivity (End of 19<sup>th</sup> century)

1895 Discovery of X-ray (Roentgen)
1896 Natural radioactivity (Becquerel) alpha-ray from Uranium
1897 Discovery of electron (Thomson)
1898 Polonium, Radium (Currie)
1900 alpha, beta, gamma (Rutherford)



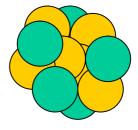
1911 Discovery of nucleus (Rutherford) 1932 Discovery of neutron (Chadwick)

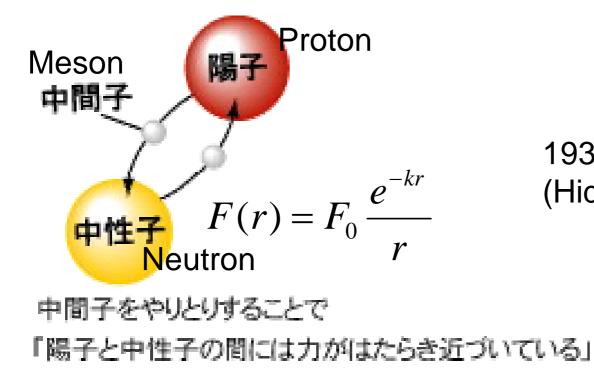
Rutherford) Chadwick) des Sciences de Paris [122, 501 (1896)] に載った. (CEA)

> 図3.3 三種類の放射線  $\alpha$ ,  $\beta$ ,  $\gamma$ . この三つは,進行方向に垂直な磁場の中で, それぞれが描く軌跡によって区別される.  $\alpha$ 線(ヘリウム核)は正の電荷をも

#### Nuclear interaction: Force to bind nucleus

Protons and neutrons bound together to form a nucleus.





1934: Meson theory (Hideki Yukawa)



Quarks and gluons are described by the QCD.

### How small is the nucleus?

Estimate the Compton wave length of pion

$$\lambda_{\pi} = \frac{\hbar}{m_{\pi}c} \sim 1.4 \text{ fm}$$

This is a typical magnitude of range of nuclear force

$$F(r) \sim F_0 \frac{\exp(-r/\lambda_\pi)}{r}$$

and the typical size of nucleus.

# How strong is the nuclear force?

There is a deuteron (p+n) that is a bound state of a proton and a neutron. The range of the force is roughly the pion Compton wave length.

(1) Estimate order of magnitude using the uncertainty principle

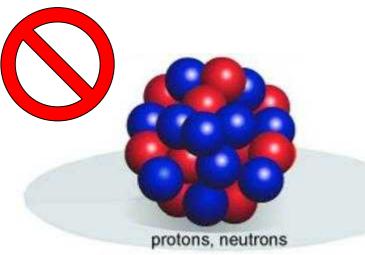
$$\Delta x \cdot \Delta p \sim \hbar$$
$$Mc^2 \sim 1 \,\text{GeV} = 1000 \,\text{MeV}$$

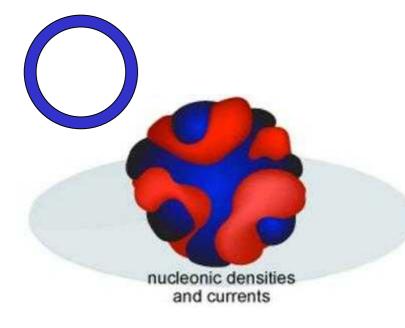
At least, order of 10 MeV

(2) Estimate order of nuclear time scale

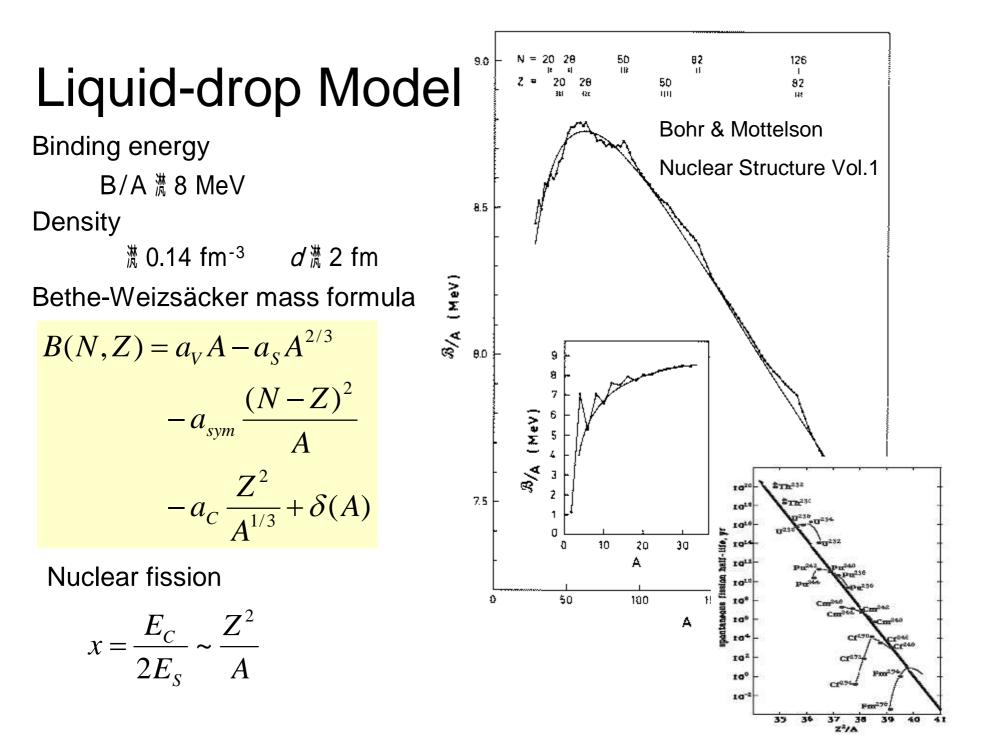
Order of  $10^{-22}$  s

### Image of nucleus









#### Nucleus as a quantum liquid

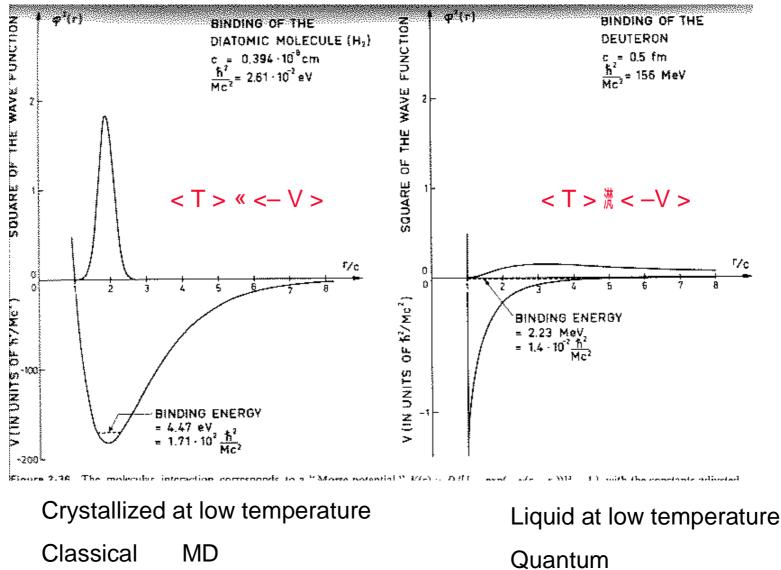
- Classical vs Quantum
  - Strength of interaction vs Zero-point kinetic energy

$$V_0$$
 vs  $\hbar^2/2Mc^2$ 

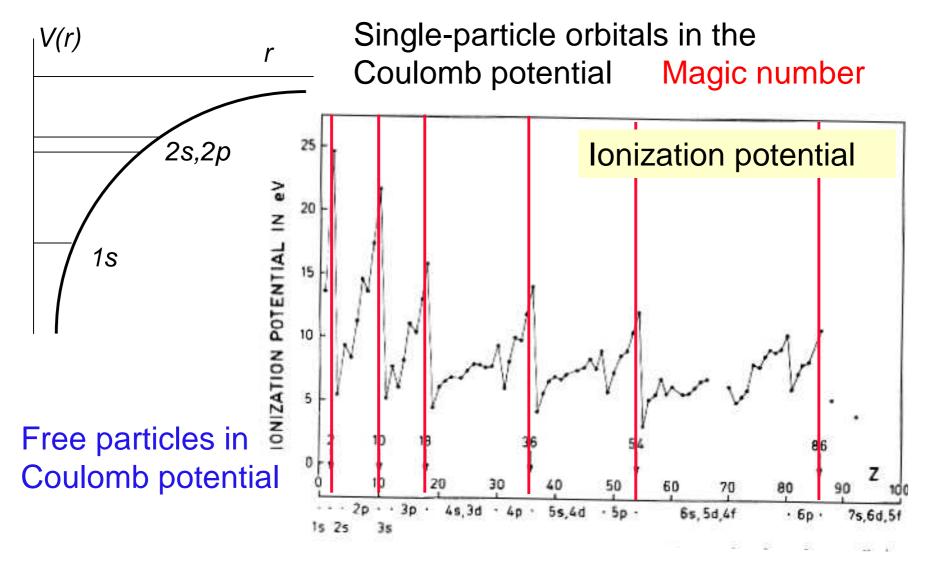
c: Length scale of the interaction  $V_0$ : Energy scale of the interaction

### Nuclear force vs molecular force

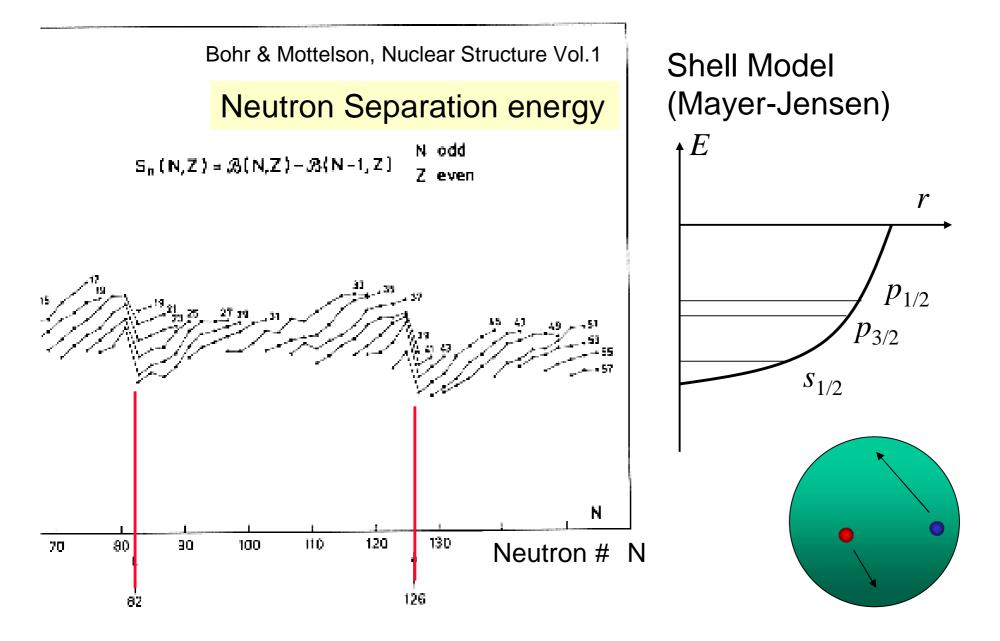
Bohr, Mottelson, Nucl. Str. Vol.1



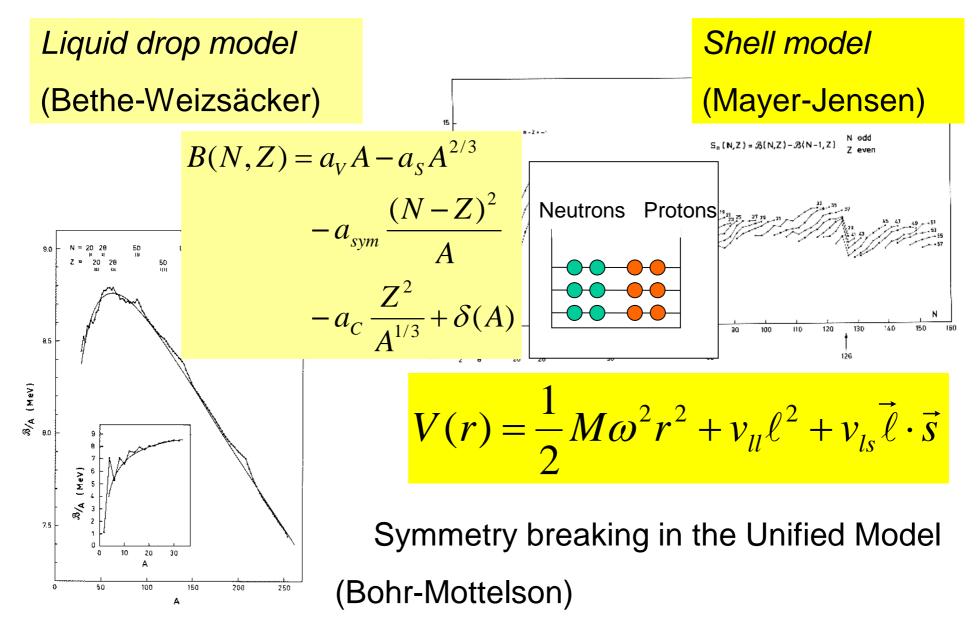
# Electronic single-particle motion in atoms



#### Nucleonic single-particle motion in nucleus



# Nucleus is liquid or gas?



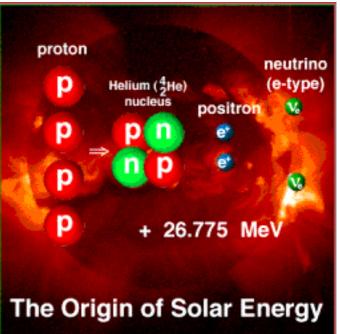
# Different reaction rate

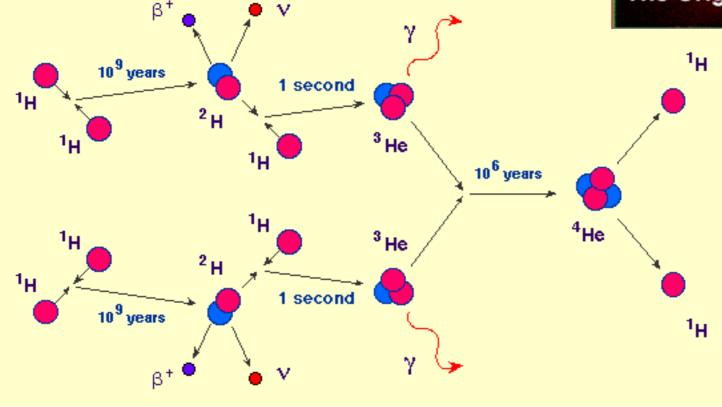
- Transfer reaction (Strong interaction)
  - $-^{15}N(p, )^{12}C$
  - ~ 0.5 b (E=2 MeV)
- Capture reaction (Electromagnetic interaction)
  - $-{}^{3}\text{He}($ ,  $)^{7}\text{Be}$
  - $\sim 10^{-6} \text{ b} (\text{E}=2 \text{ MeV})$
- Weak process (Weak interaction)
  - $-p(p,e^+)d$
  - $\sim 10^{-20} \text{ b} (\text{E}=2 \text{ MeV})$



# pp chain (I)

•  $p(p,e^+)d$  reaction determines the lifetime of the sun

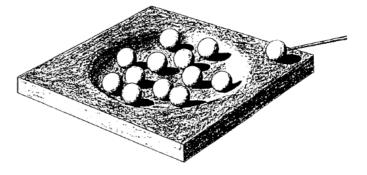


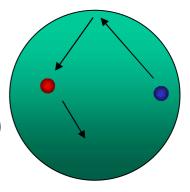


#### Nucleus with Different Time Scales

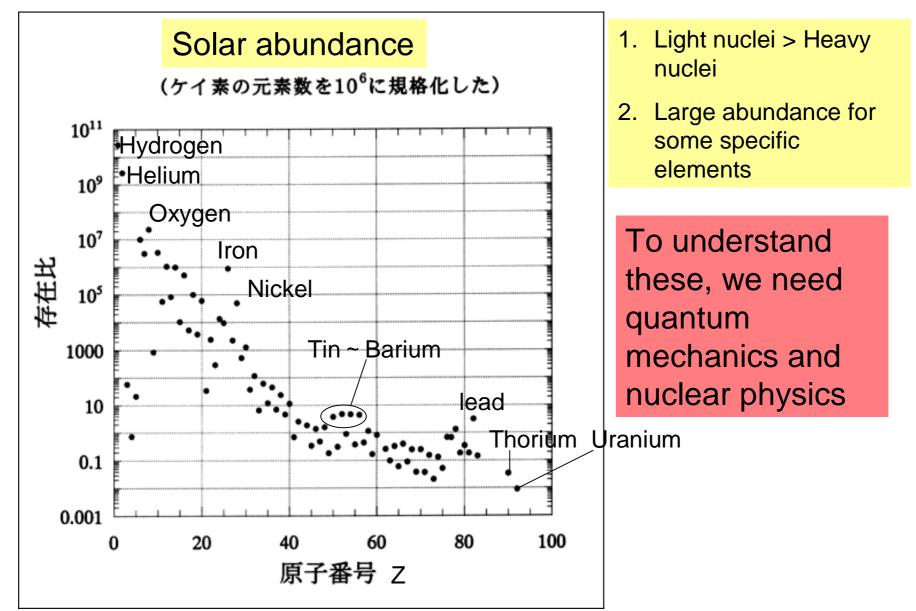
- Time period of nucleonic Fermi motion
  - $_{\rm F} \sim R/v_{\rm F} \sim 10^{-22} \, {\rm sec}$
- Collision time
  - <sub>c</sub> >> <sub>F</sub> (Nucleon near Fermi energy)
  - $_{c}$   $\overline{=}$   $_{F}$  (Thermal neutron)
  - If the residence time is much larger than <sub>c</sub>, "chaotic state" (compound nucleus).

Nucleus shows different faces (aspects) in different time scales.

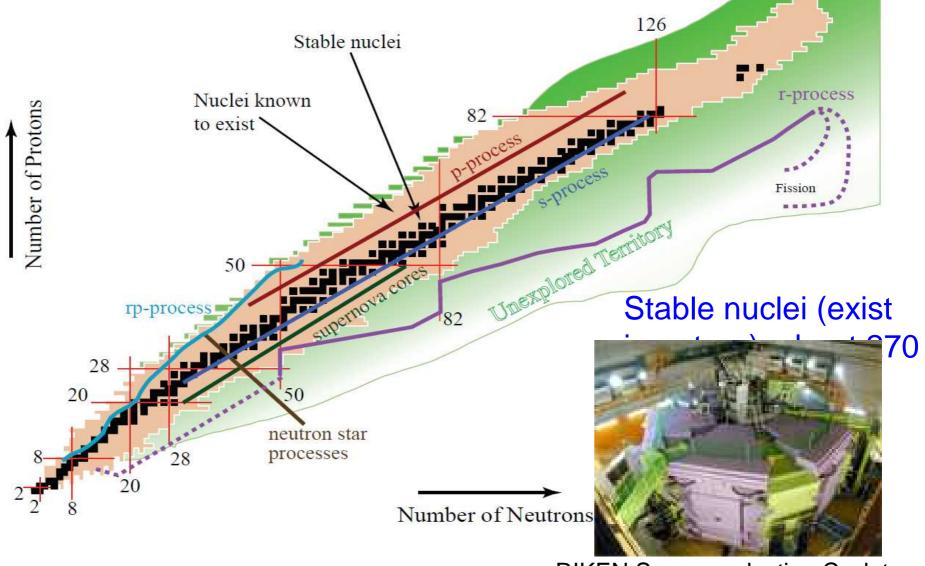




# Where we came from?

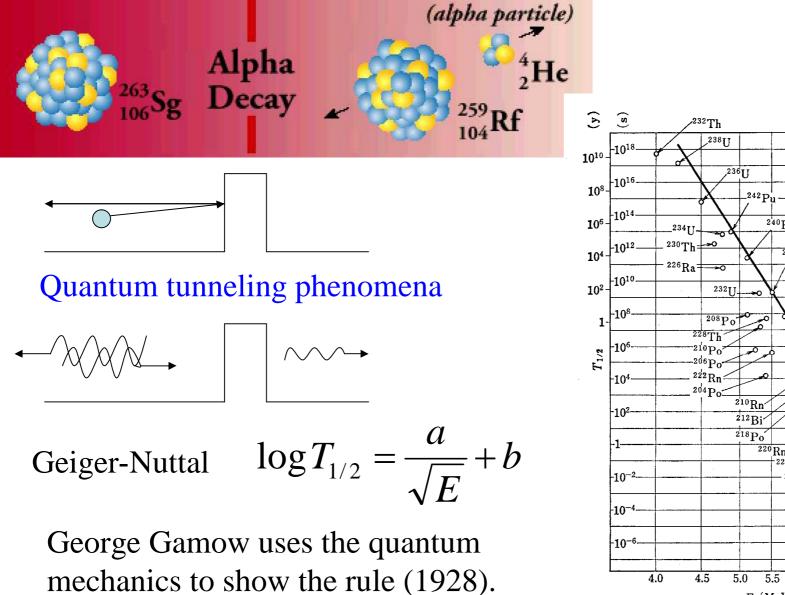


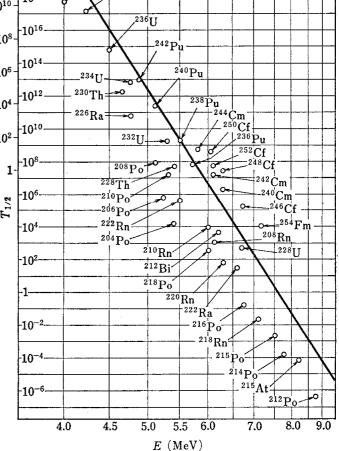
#### **Nuclear Chart and Element Synthesis**



**RIKEN Superconducting Cyclotron** 

# Tunnel effect (alpha decay)





#### **Nuclear Power**

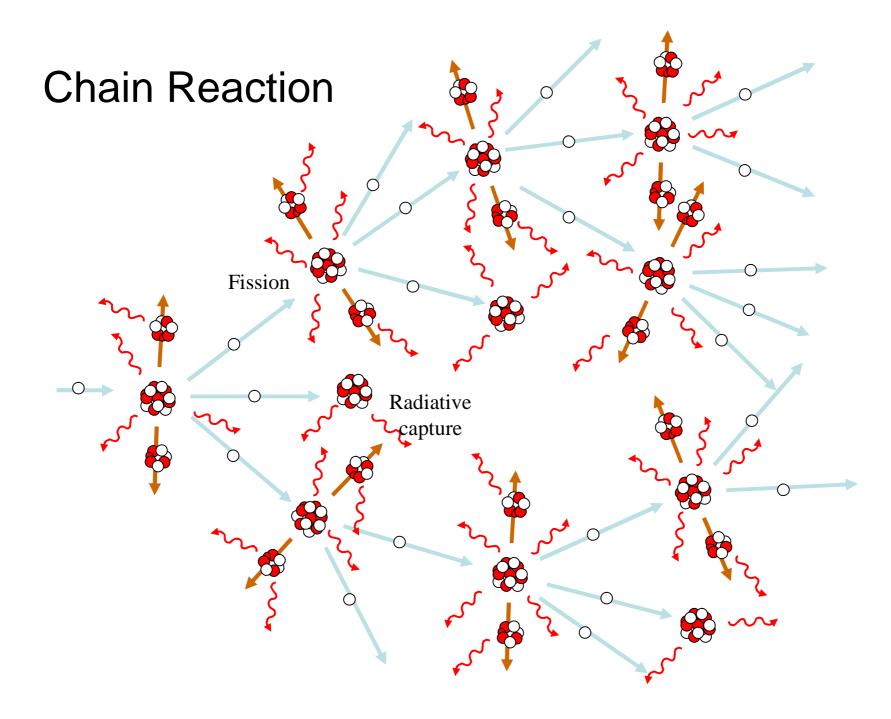


If Uranium absorbs a slow neutron, the fission occurs and neutrons are emitted. These neutrons are decelerated and collide with other Uranium.

#### (Chain Reaction)

The neutron absorption cross section of 235U enhances at low energy (~several thousands barns).

The chain reaction stops if the speed of neutrons are too fast.



# **Neutron Cross Section**

The radius of stable nucleus is approximately given by

$$R = r_0 A^{1/3}$$
,  $r_0 = 1.2$  fm,  $A = N + Z$ 

Assume a simple square-well potential model of radius R, obtain cross section in the classical mechanics?

$$\sigma = \pi R^2 \approx 1.7 \text{ b}$$

In the quantum mechanics, the cross section depends on energy.

At low-energy limit,

$$\sigma = \pi a^2$$
, *a*:scattering length

