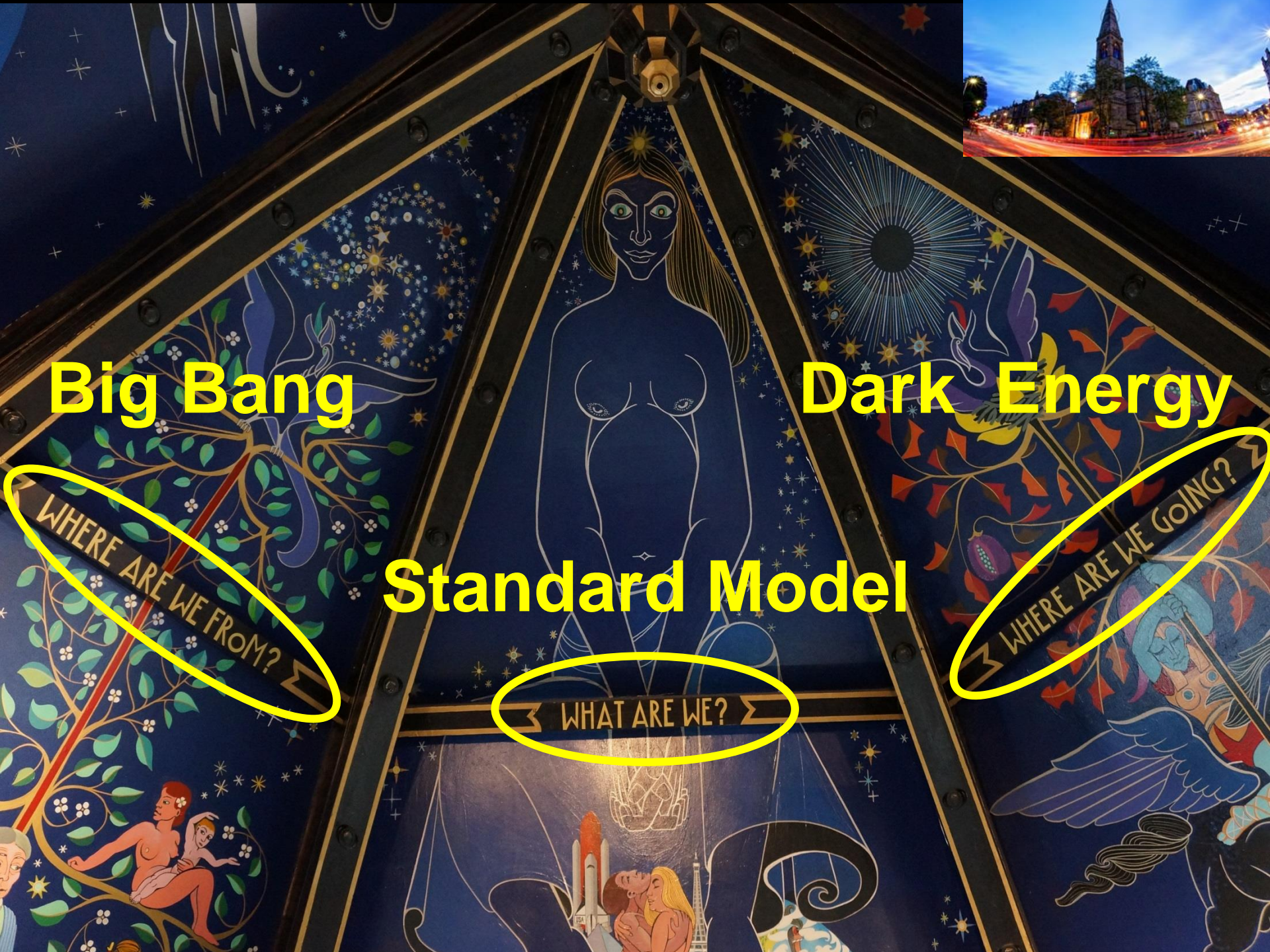


QCD Theory Overview

T. Hatsuda (Nishina Center & iTHES, RIKEN)





Big Bang

Dark Energy

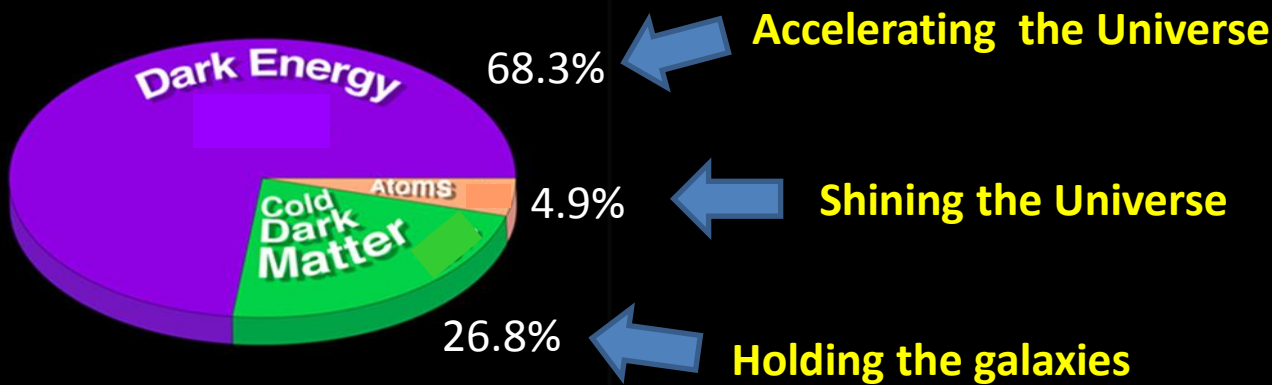
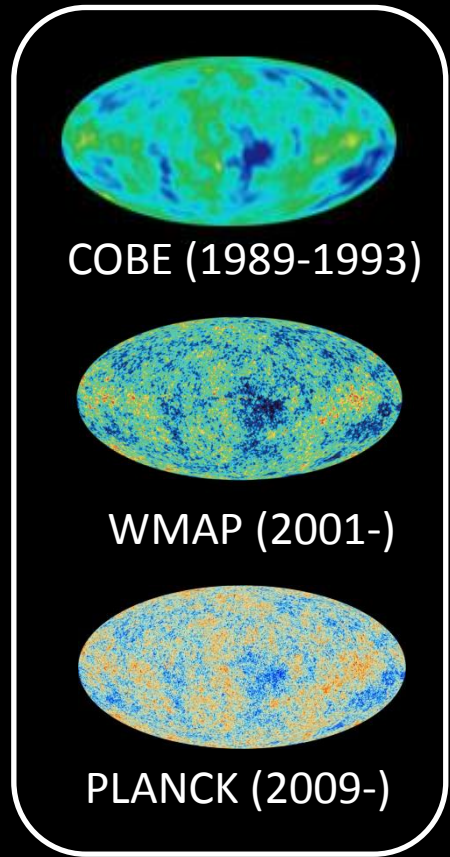
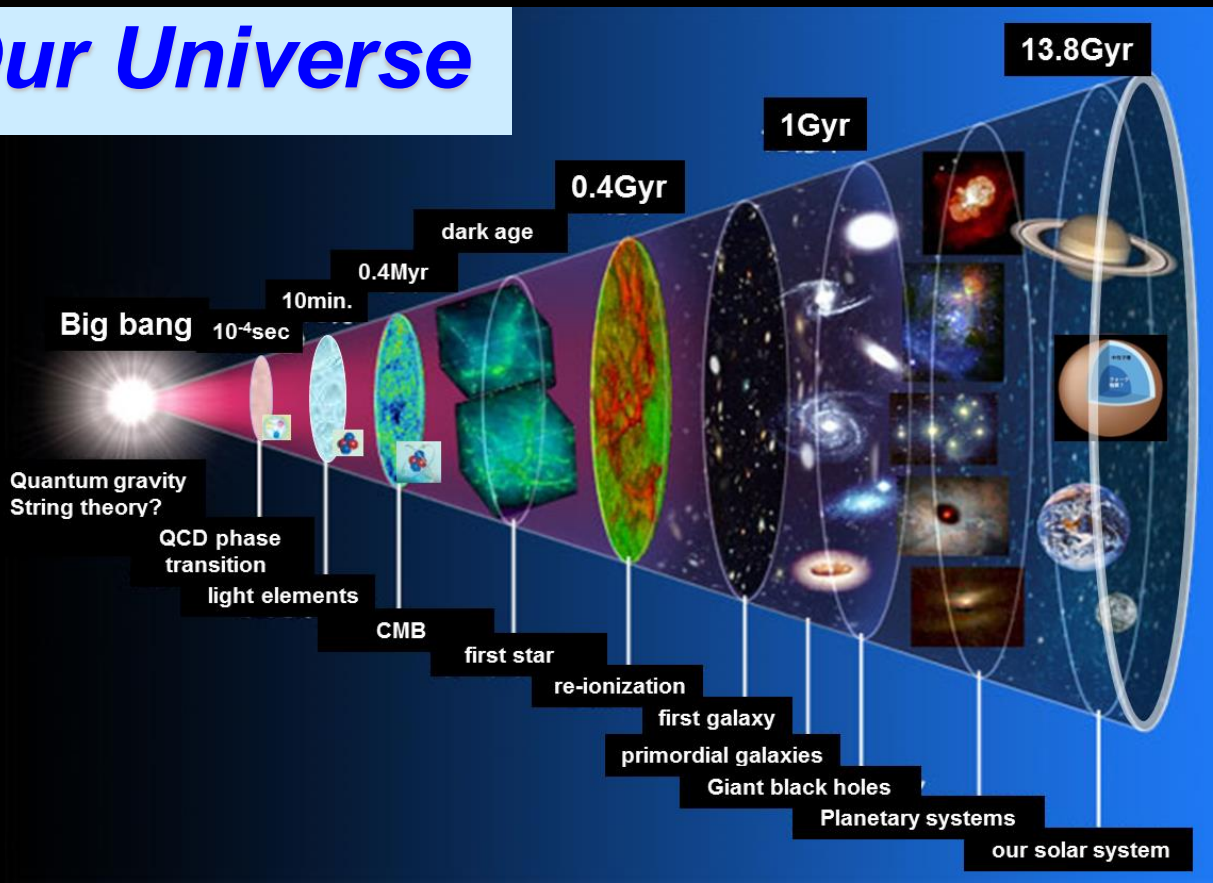
Standard Model

WHERE ARE WE FROM?

WHAT ARE WE?

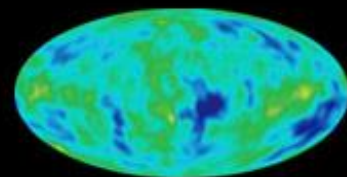
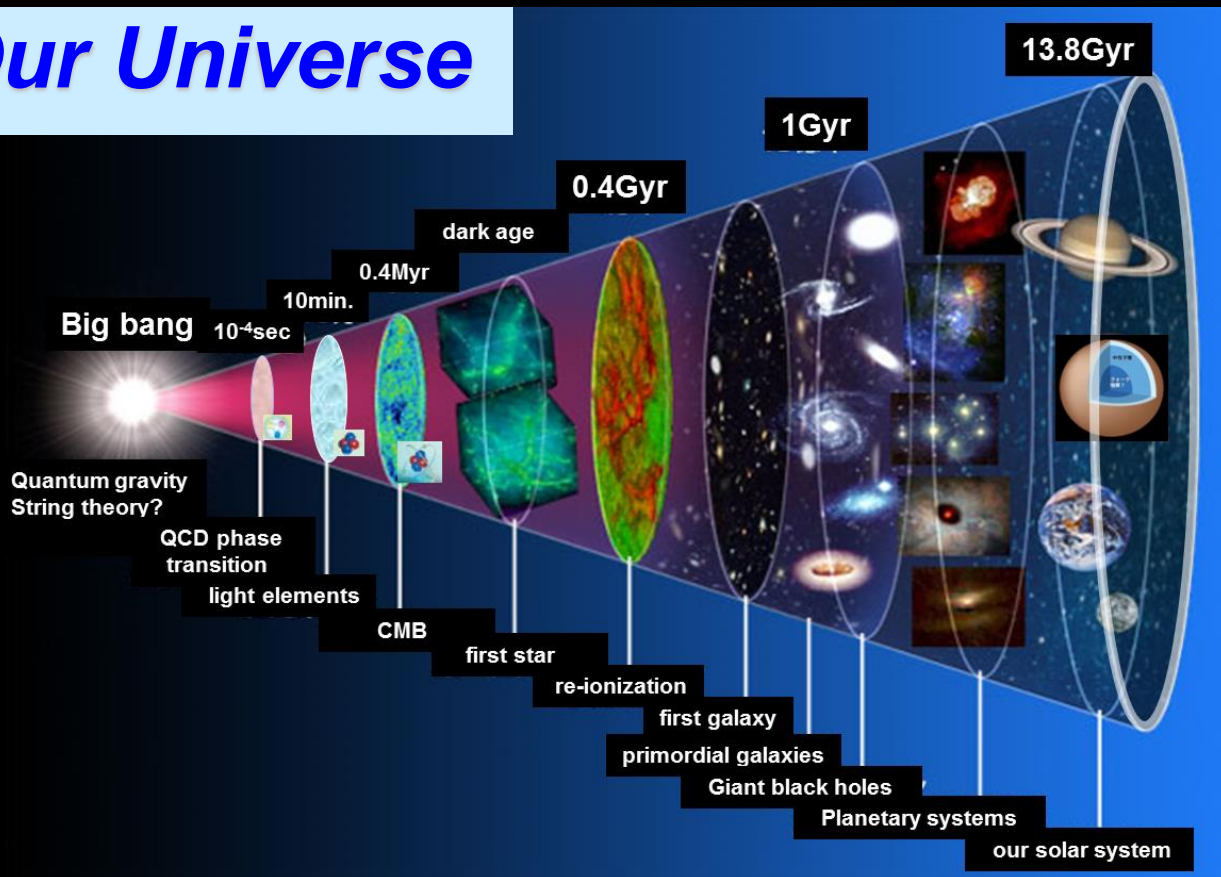
WHERE ARE WE GOING?

Our Universe

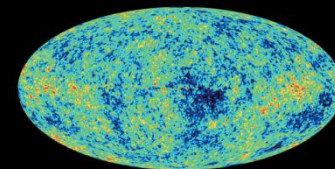


Planck (March 21, 2013)

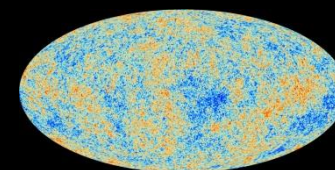
Our Universe



COBE (1989-1993)

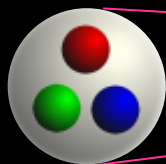


WMAP (2001-)



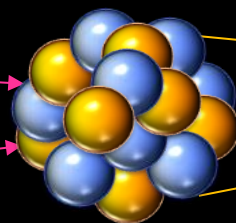
PLANCK (2009-)

nucleon



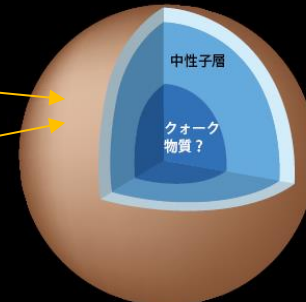
$r \sim 1$ [fm]

nucleus



$r \sim 10$ [fm]

Neutron star



$r \sim 10$ [km]

Quantum Chromo Dynamics (QCD)

1966 color SU(3) gauge theory for strong interaction (Nambu)

1973 Asymptotic freedom (Gross & Wilczek, Politzer)

1974 Quark confinement (Wilson)



Y. Nambu

QCD = SU(3) gauge theory for color charges (**B**, **R**, **G**)

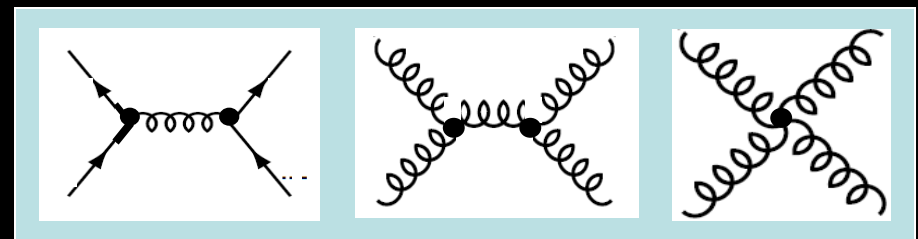
$$\mathcal{L} = -\frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu} + \bar{q}\gamma^\mu (i\partial_\mu - gt^a A_\mu^a)q - m\bar{q}q$$

$$G_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf_{abc}A_\mu^b A_\nu^c$$

$$[t^a, t^b] = if_{abc}t^c$$

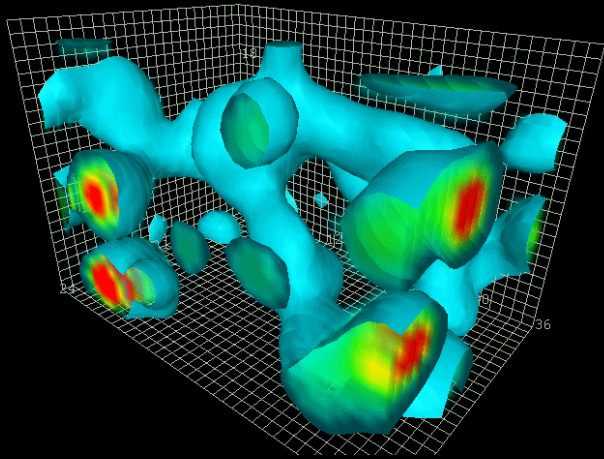


- Intrinsic parameters: m, g
- External parameters: Q, T, ρ_B etc



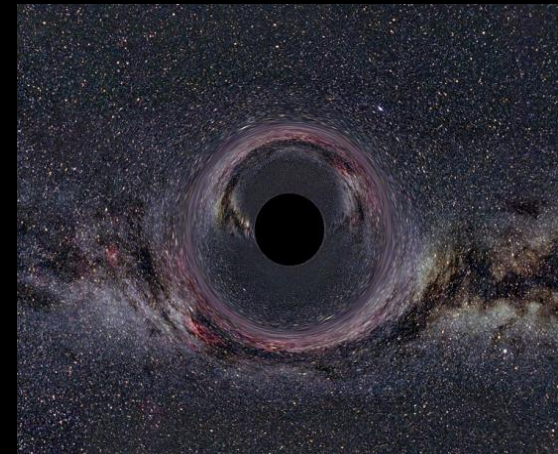
Challenges in QCD

QCD: Non-linear
Strong coupling
Quantum



Holography

GR: Non-linear
Weak coupling
Classical



1. **Mathematical challenge**

2. Tool to search physics beyond SM

3. Nucleon structure (spin, glue, ...)

4. Multi-quarks

5. New states of matter (QGP, QM)

↔ **one of the seven millennium problems**

↔ B-factory, LHC, ILC

↔ Jlab, RHIC

↔ B-factory, Spring-8, Jlab, GSI, J-PARC

↔ RHIC, LHC, N_{\star} , Q_{\star}

Yang-Mills and Mass gap : One of seven Millennium Problems
by Clay Mathematics Institute (May 24, 2000)

Official description (A. Jaffe and E. Witten)

QCD must have....

- (1) It must have a “mass gap,” that is, there must be some strictly positive constant Δ such that every excitation of the vacuum has energy at least Δ .
- (2) It must have “quark confinement,” that is, even though the theory is described in terms of elementary fields, such as the quarks, that transform non-trivially under $SU(3)$, the physical particle states – such as the proton, neutron, and pion – are $SU(3)$ -invariant.
- (3) It must have “chiral symmetry breaking,” which means that the vacuum is potentially invariant (in the limit that the quark bare masses vanish) only under a certain subgroup of the full symmetry group that acts on the quark fields.

The first point is necessary to explain why the nuclear force is strong but short-ranged; the second is needed to explain why we never see individual quarks; and the third is needed to account for the “current algebra” theory of soft pions that was developed in the 1960’s.

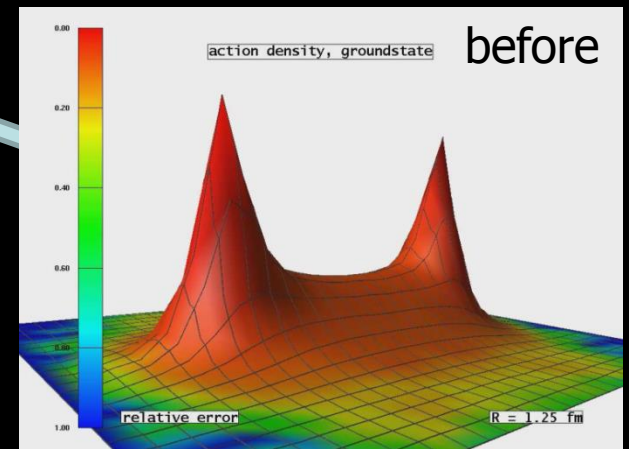
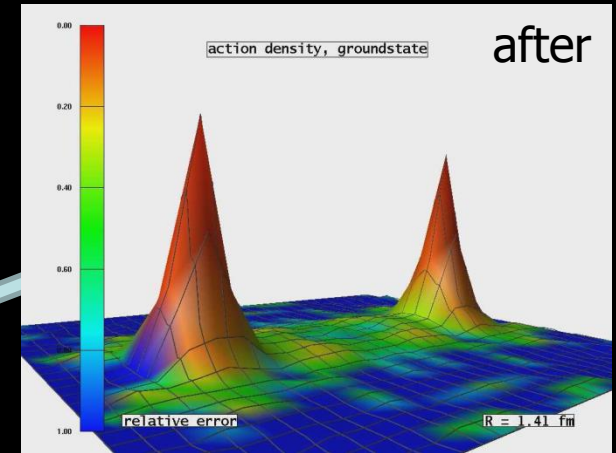
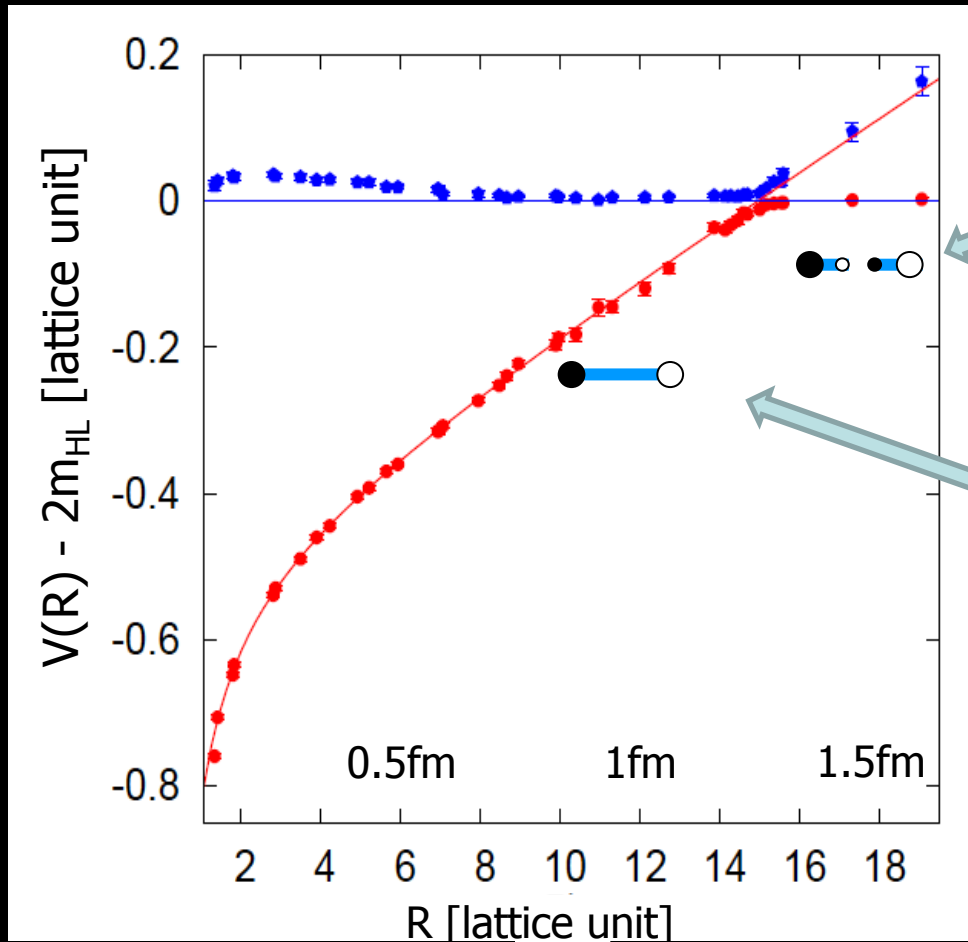
Now we can state the Millennium Problem:

Yang-Mills Existence And Mass Gap: *Prove that for any compact simple gauge group G , quantum Yang-Mills theory on \mathbb{R}^4 exists and has a mass gap $\Delta > 0$.*

P2: Confinement from lattice QCD

Heavy Q-Qbar potential

$$V(R) = \left(c - \frac{a}{R} + \sigma R \right) \theta(R_0 - R)$$



Yang-Mills and Mass gap : One of seven Millennium Problems
by Clay Mathematics Institute (May 24, 2000)

Official description (A. Jaffe and E. Witten)

QCD must have....

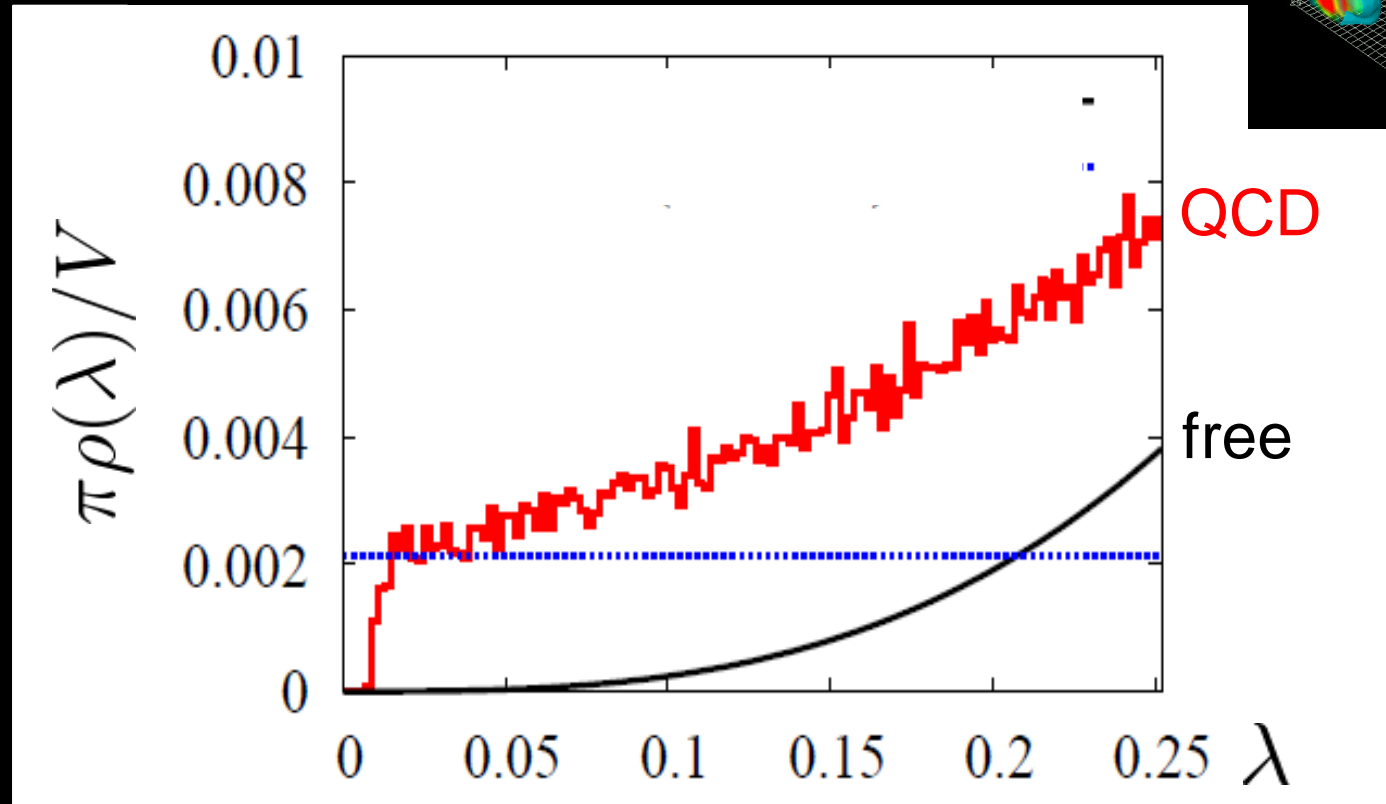
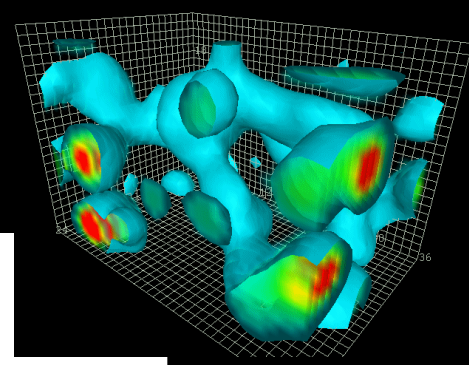
- (1) It must have a “mass gap,” that is, there must be some strictly positive constant Δ such that every excitation of the vacuum has energy at least Δ .
- (2) It must have “quark confinement,” that is, even though the theory is described in terms of elementary fields, such as the quarks, that transform non-trivially under $SU(3)$, the physical particle states – such as the proton, neutron, and pion – are $SU(3)$ -invariant.
- (3) It must have “chiral symmetry breaking,” which means that the vacuum is potentially invariant (in the limit that the quark bare masses vanish) only under a certain subgroup of the full symmetry group that acts on the quark fields.

The first point is necessary to explain why the nuclear force is strong but short-ranged; the second is needed to explain why we never see individual quarks; and the third is needed to account for the “current algebra” theory of soft pions that was developed in the 1960’s.

Now we can state the Millennium Problem:

Yang-Mills Existence And Mass Gap: *Prove that for any compact simple gauge group G , quantum Yang-Mills theory on \mathbb{R}^4 exists and has a mass gap $\Delta > 0$.*

P3: Chiral condensate from lattice QCD



$$\langle \bar{q}q \rangle = -(251 \pm 7 \pm 11 \text{ MeV})^3 \quad \text{at } 2 \text{ GeV}$$

Dynamical overlap fermion, 2-flavor
S. Hashimoto (JLQCD Coll.) arXiv:0811.1257 [hep-lat]

Yang-Mills and Mass gap : One of seven Millennium Problems
by Clay Mathematics Institute (May 24, 2000)

Official description (A. Jaffe and E. Witten)

OCD must have....

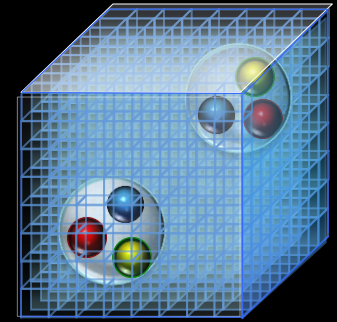
- (1) It must have a “mass gap,” that is, there must be some strictly positive constant Δ such that every excitation of the vacuum has energy at least Δ .
- (2) It must have “quark confinement.” that is, even though the theory is described in terms of elementary fields, such as the quarks, that transform non-trivially under $SU(3)$, the physical particle states – such as the proton, neutron, and pion – are $SU(3)$ -invariant.
- (3) It must have “chiral symmetry breaking.” which means that the vacuum is potentially invariant (in the limit that the quark bare masses vanish) only under a certain subgroup of the full symmetry group that acts on the quark fields.

The first point is necessary to explain why the nuclear force is strong but short-ranged; the second is needed to explain why we never see individual quarks; and the third is needed to account for the “current algebra” theory of soft pions that was developed in the 1960's.

Now we can state the Millennium Problem:

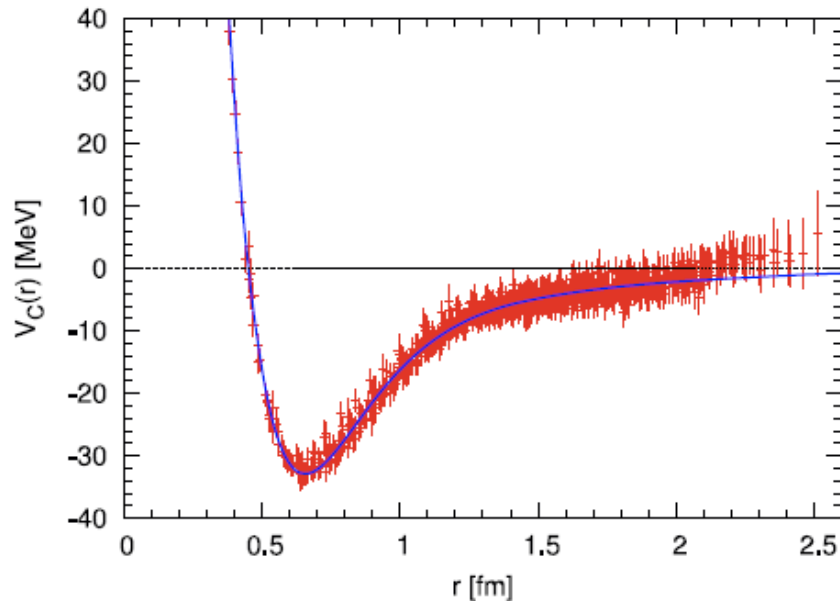
Yang-Mills Existence And Mass Gap: *Prove that for any compact simple gauge group G , quantum Yang-Mills theory on \mathbb{R}^4 exists and has a mass gap $\Delta > 0$.*

P1: Nuclear Force from lattice QCD

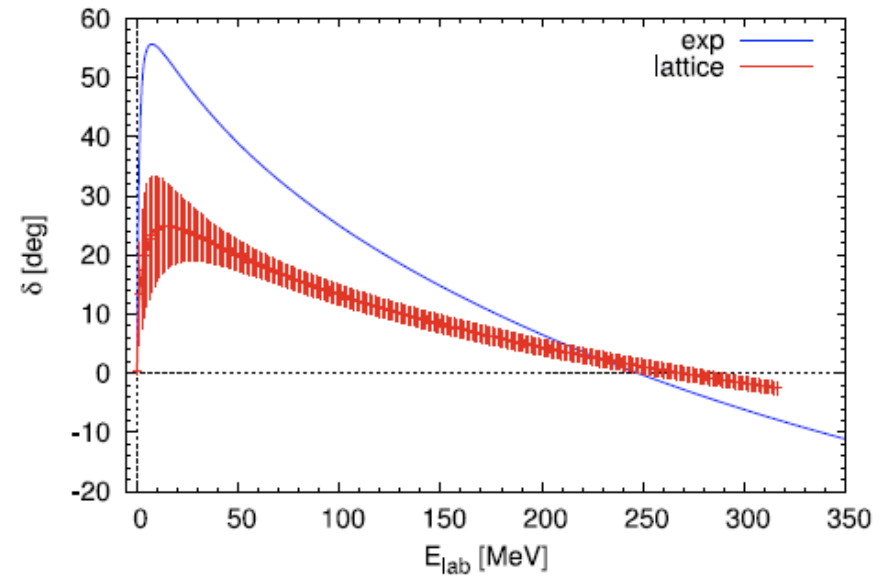


Ishii, Aoki & Hatsuda, Phys. Rev. Lett. 92 (2007) 022001
Ishii et al., [HAL QCD Coll.], Phys. Lett. 712 (2012) 437

1S_0 NN potential (Lattice QCD)



1S_0 NN phase shift (Lattice QCD)



$M_\pi \sim 3 M_\pi(\text{phys.}) \rightarrow M_\pi = M_\pi(\text{phys.}), \text{ NN, NNN}$
by K-Computer

Precision QCD

$$\mathcal{L} = -\frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu} + \bar{q}\gamma^\mu(i\partial_\mu - gt^a A_\mu^a)q - m\bar{q}q$$

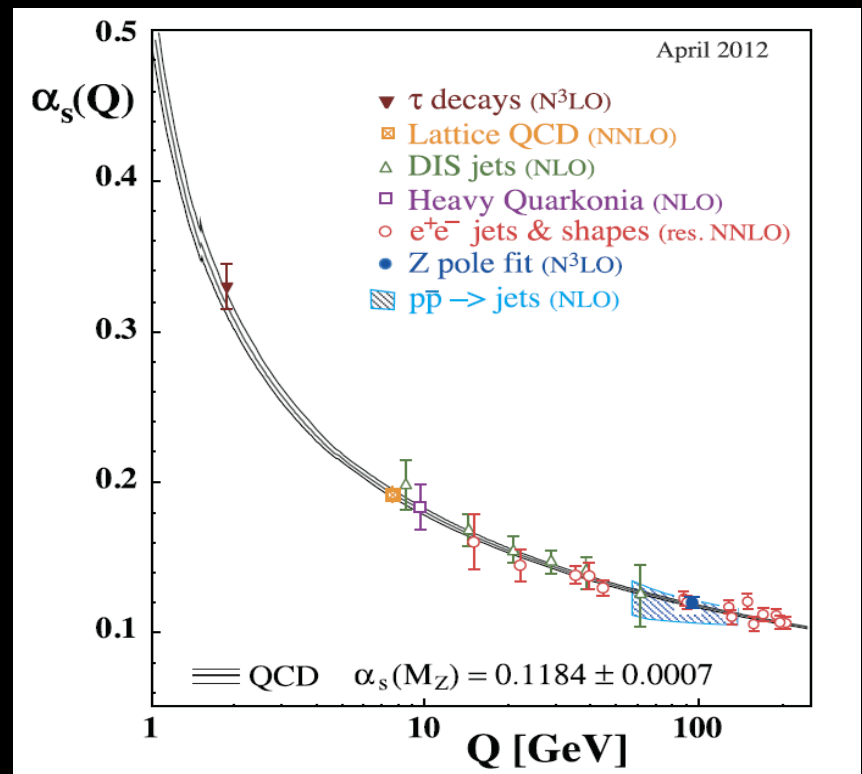
$$G_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf_{abc}A_\mu^b A_\nu^c$$

Running masses: $m_q(Q)$

quark masses (from lattice QCD)	[MeV] (MS-bar @ 2GeV)
m_u	2.16(9)(7)
m_d	4.68(14)(7)
m_s	93.8(2.4)

FLAG Collaboration update(July 26, 2013)
<http://itpwiki.unibe.ch/flag/>

Running coupling: $\alpha_s(Q)=g^2/4\pi$



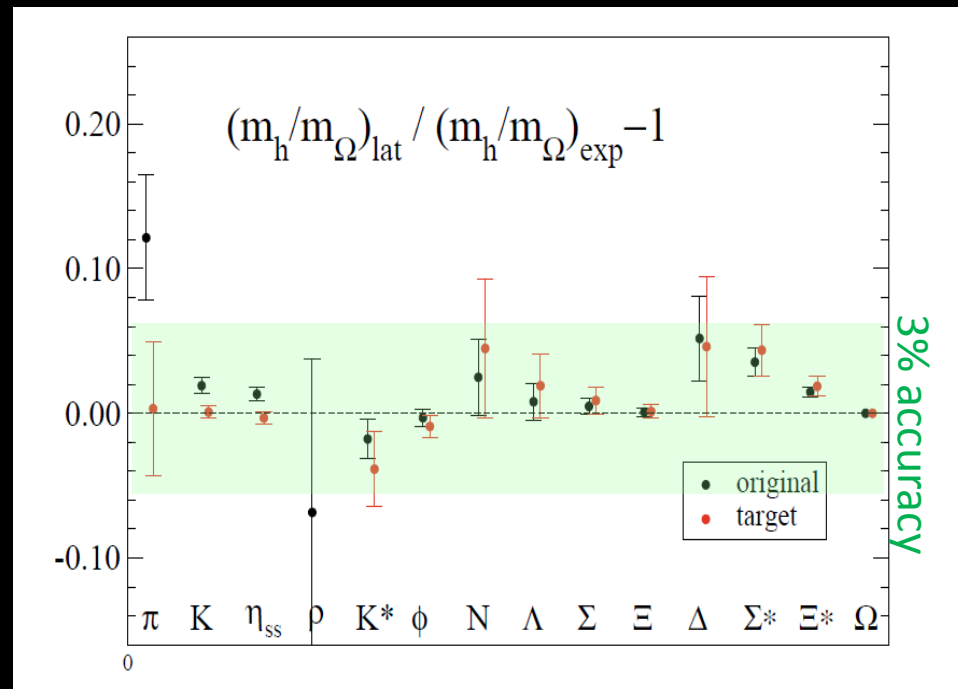
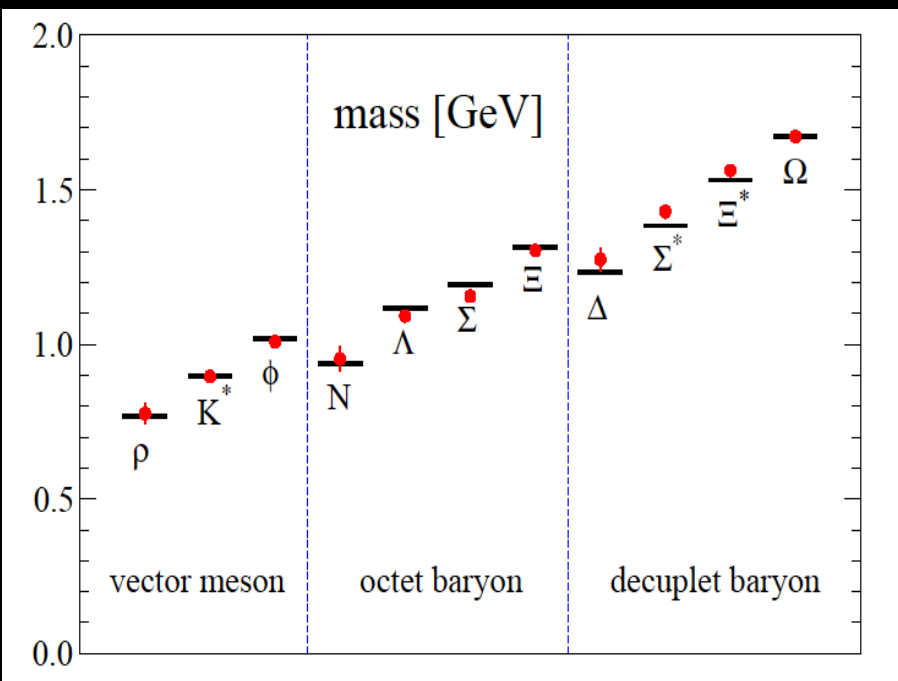
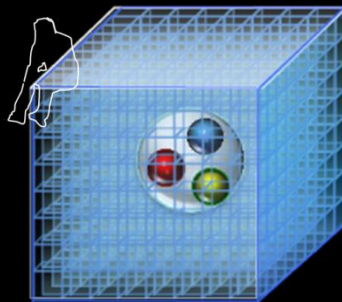
PDG (2012) <http://pdg.lbl.gov/>

Hadron masses @ 2009

$$m_{\pi} > 156 \text{ MeV}$$

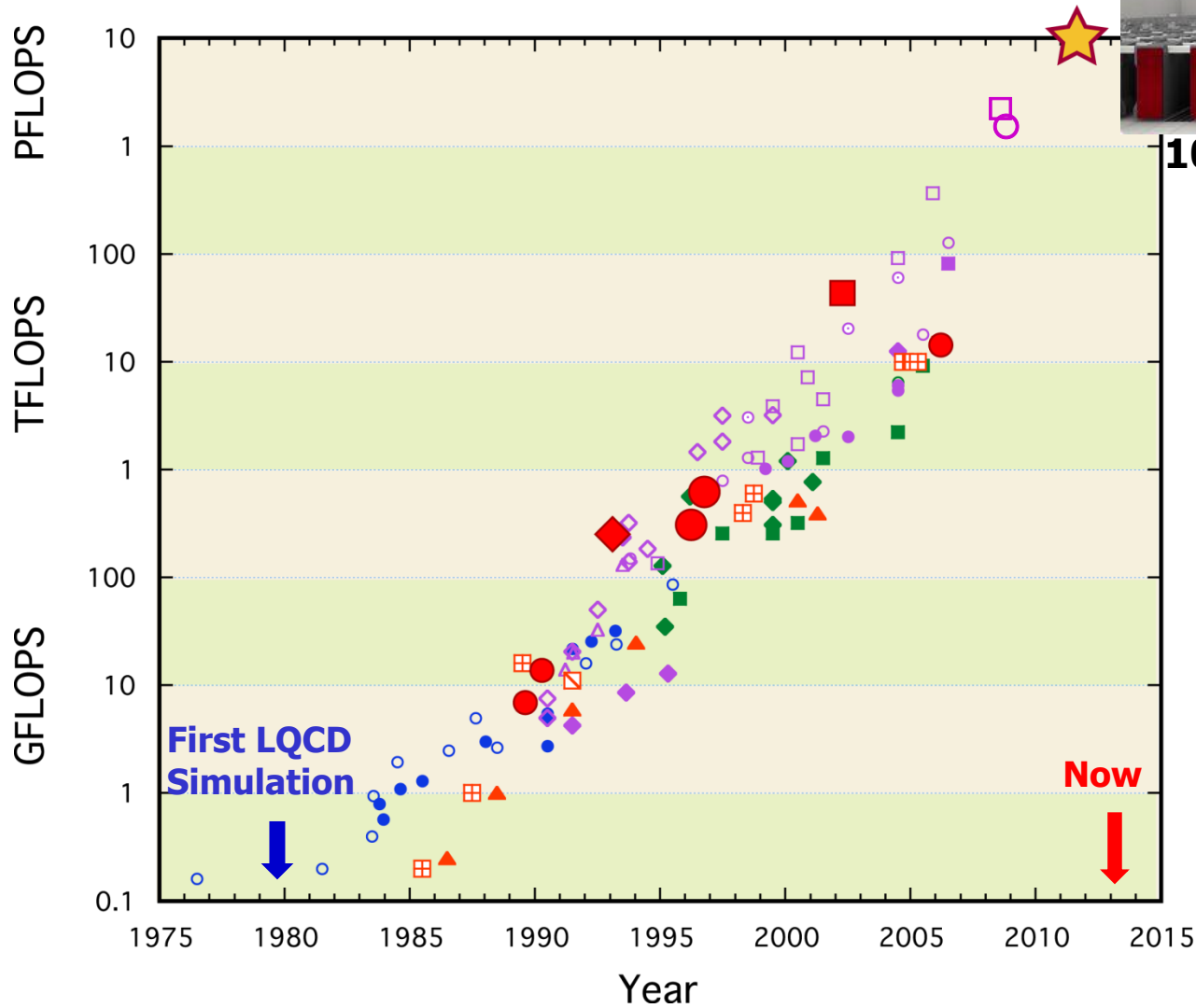
Hadron masses @ 2010

$$m_{\pi} = 135 \text{ MeV}$$



Toward large-scale Physical-point simulations

<http://www.aics.riken.jp/en/>

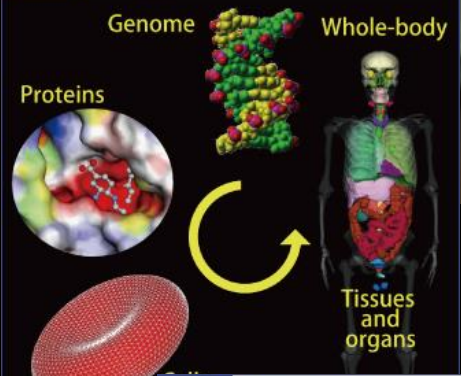


**10PFlops K computer
(RIKEN)**

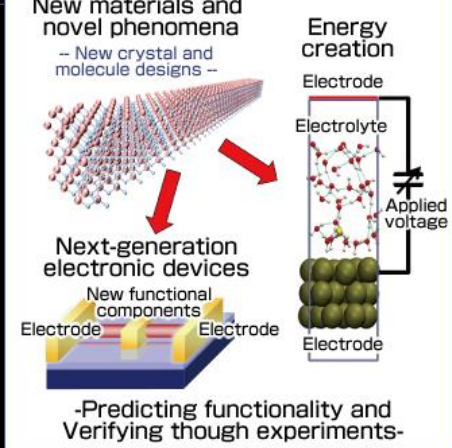


K computer (AICS)

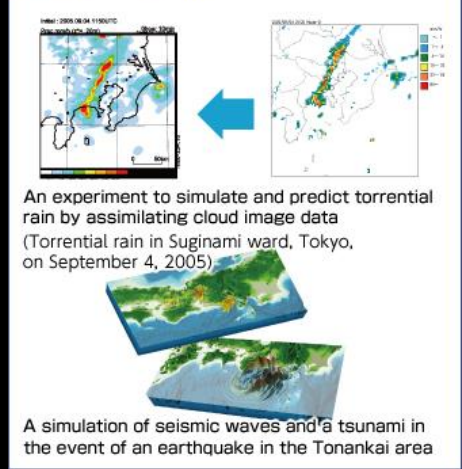
1 Life science / Drug manufacture



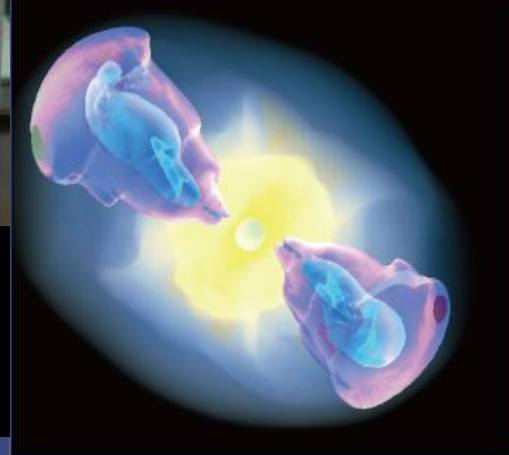
2 New Materials and Energy Creation



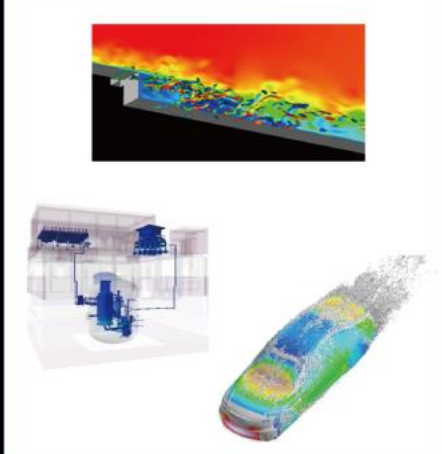
3 Global change prediction for disaster prevention/reduction



5 The origin of matter and the universe



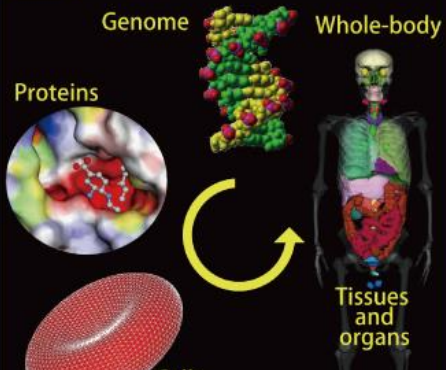
4 MONOZUKURI (Industrial Innovation)





K computer (AICS)

1 Life science /
Drug manufacture



5 The origin of matter
and the universe



The origin of matter
and the universe

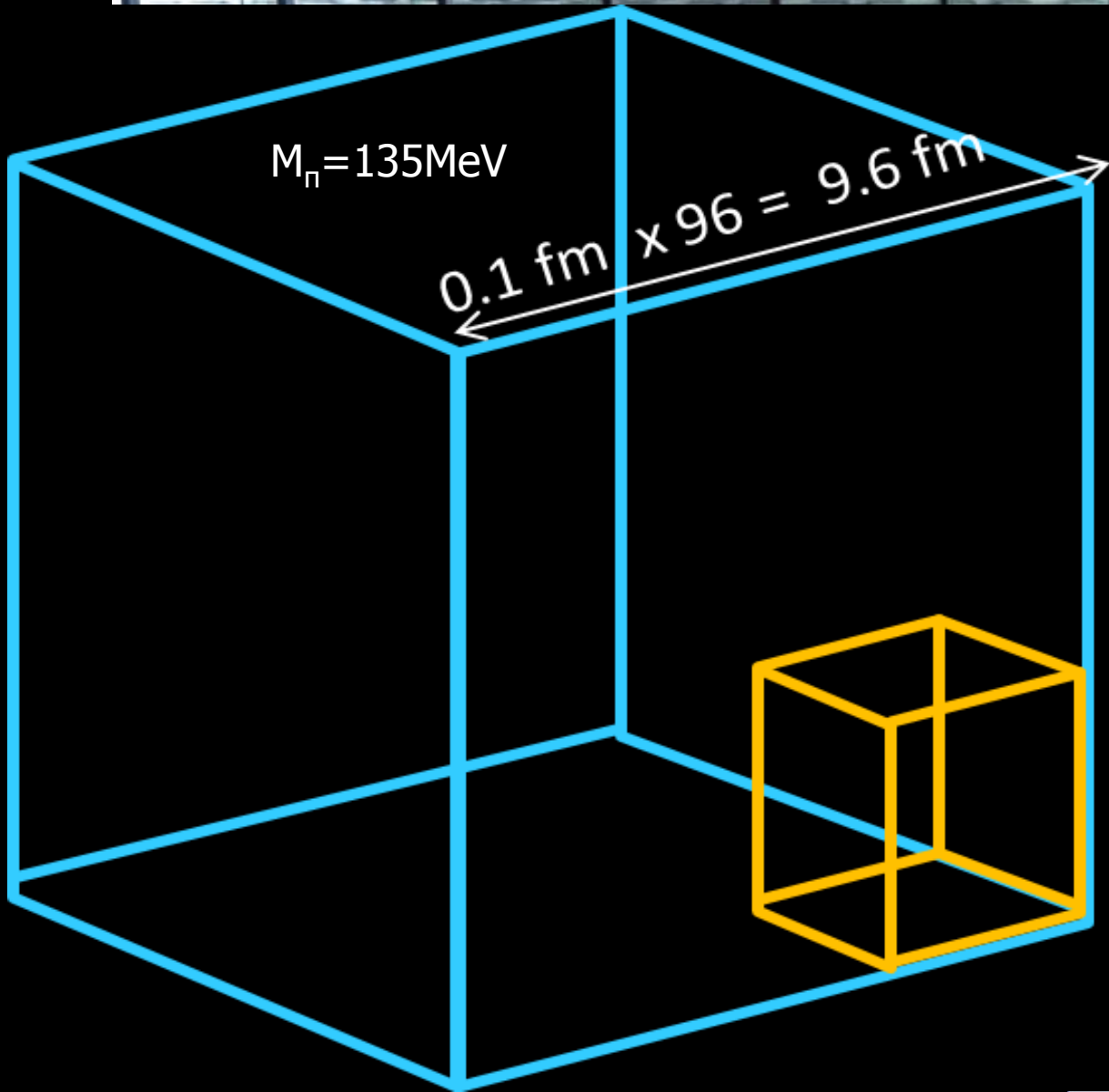
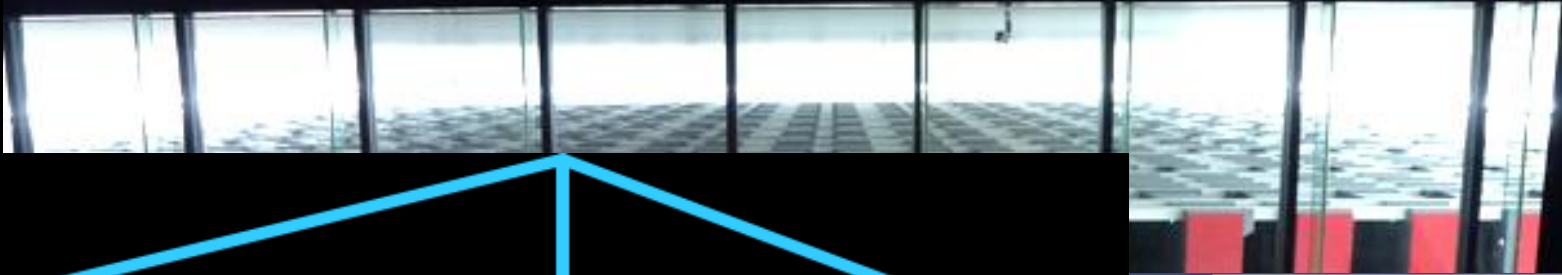
Lattice QCD

Nucleus

Supernova Explosion

Early Star Formation

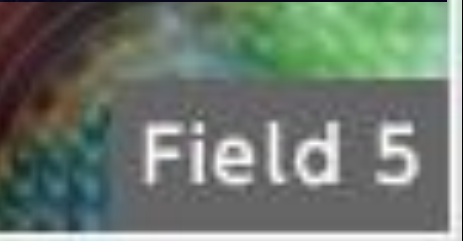
Field 5



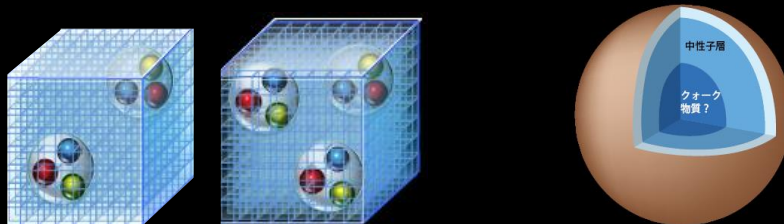
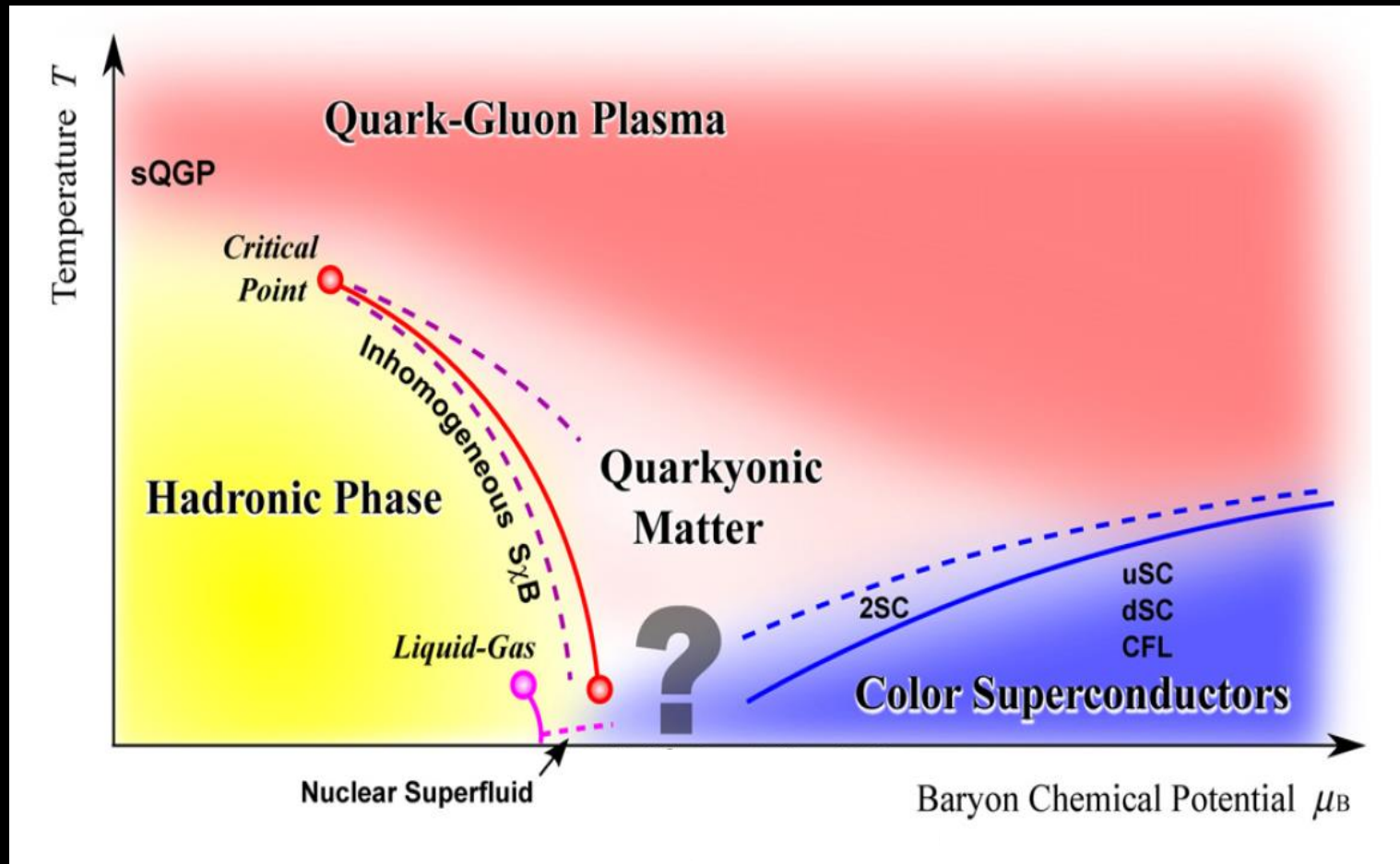
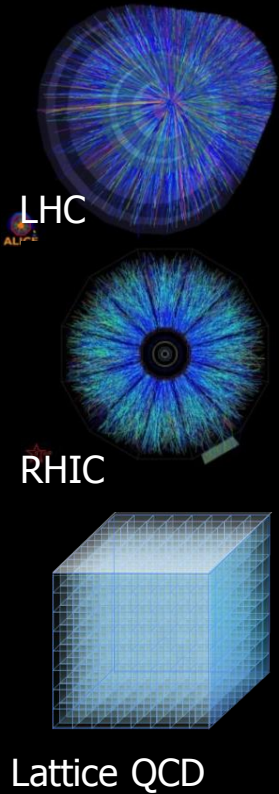
5 The origin of matter and the universe



- Lattice QCD
- Nucleus
- Supernova Explosion
- Early Star Formation

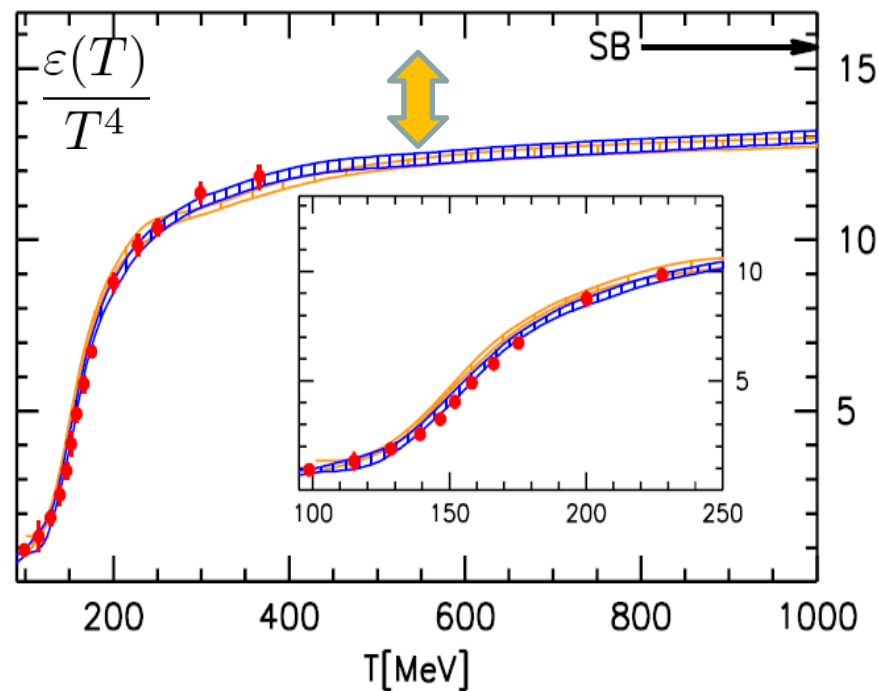
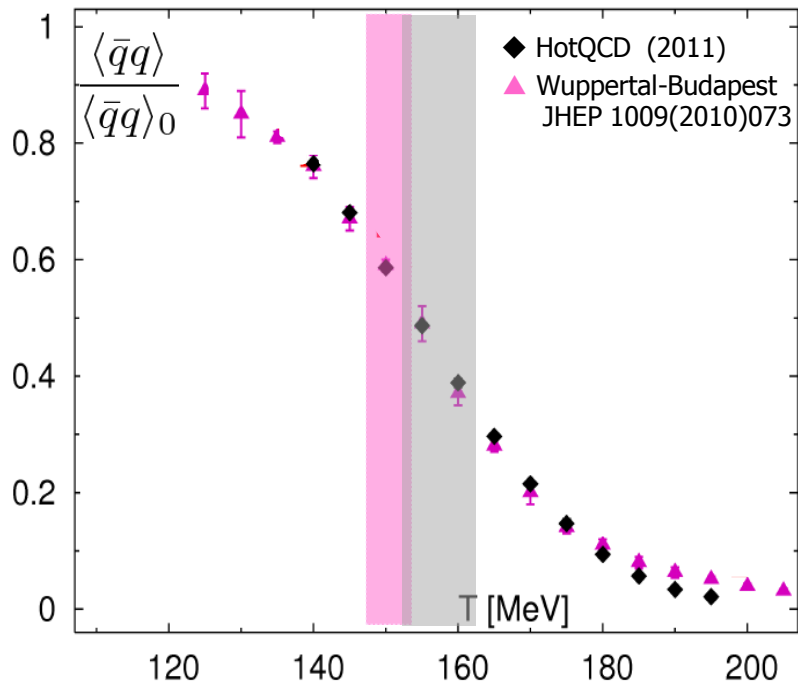
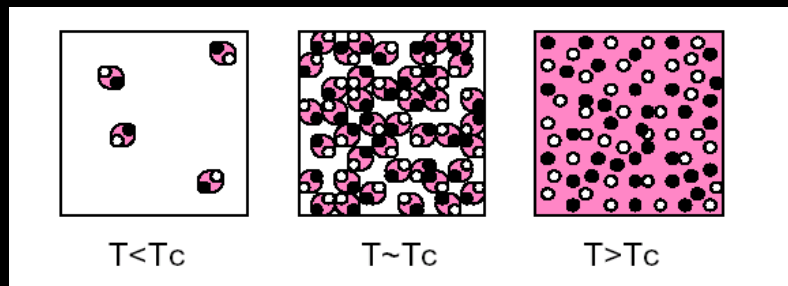


QCD Phase Diagram



K. Fukushima and T. Hatsuda,
 "The Phase Diagram of Dense QCD"
 Rep. Prog. Phys. 74 (2011) 014001

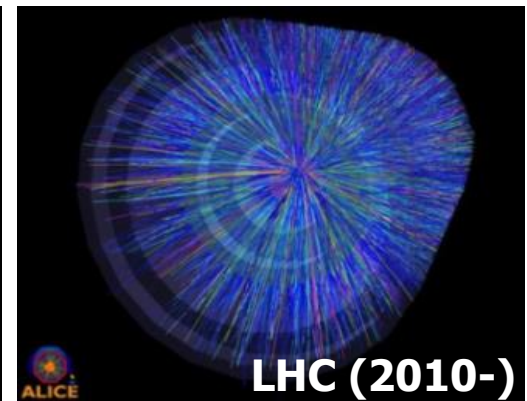
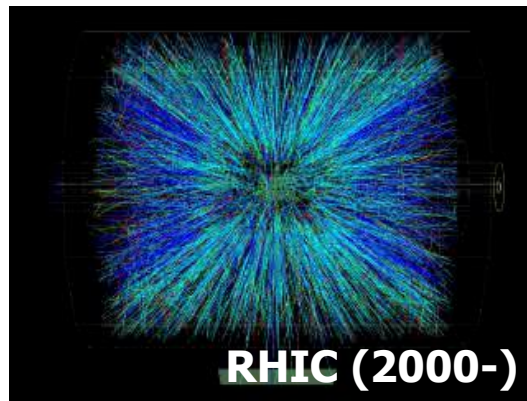
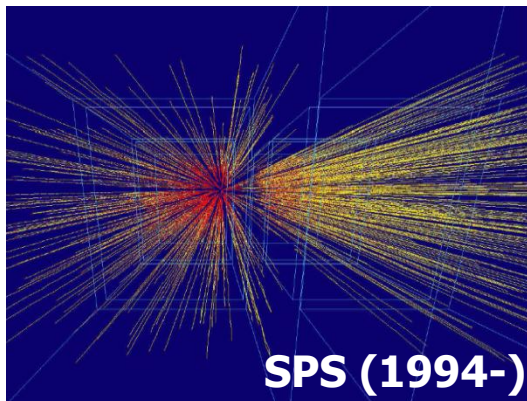
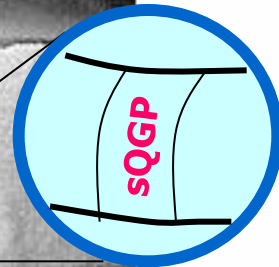
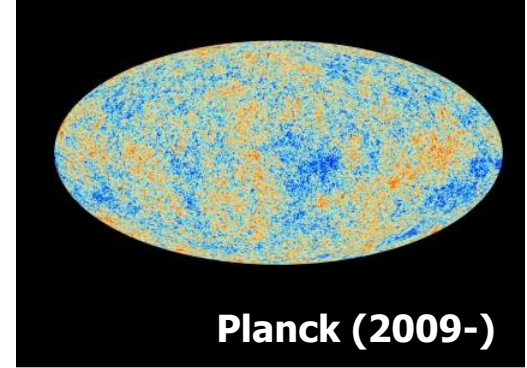
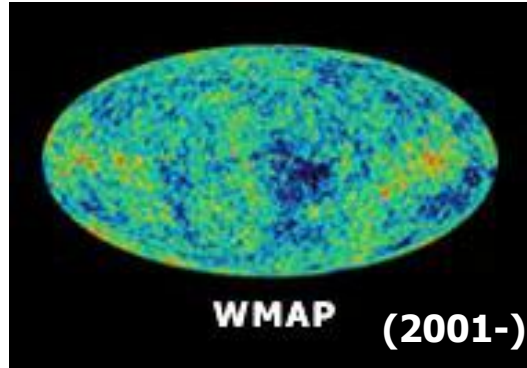
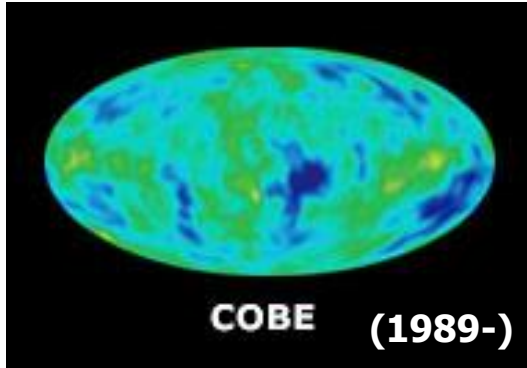
Hadron-Quark Crossover in hot QCD



Wuppertal-Budapest Coll. JHEP 1011 (2010) 77

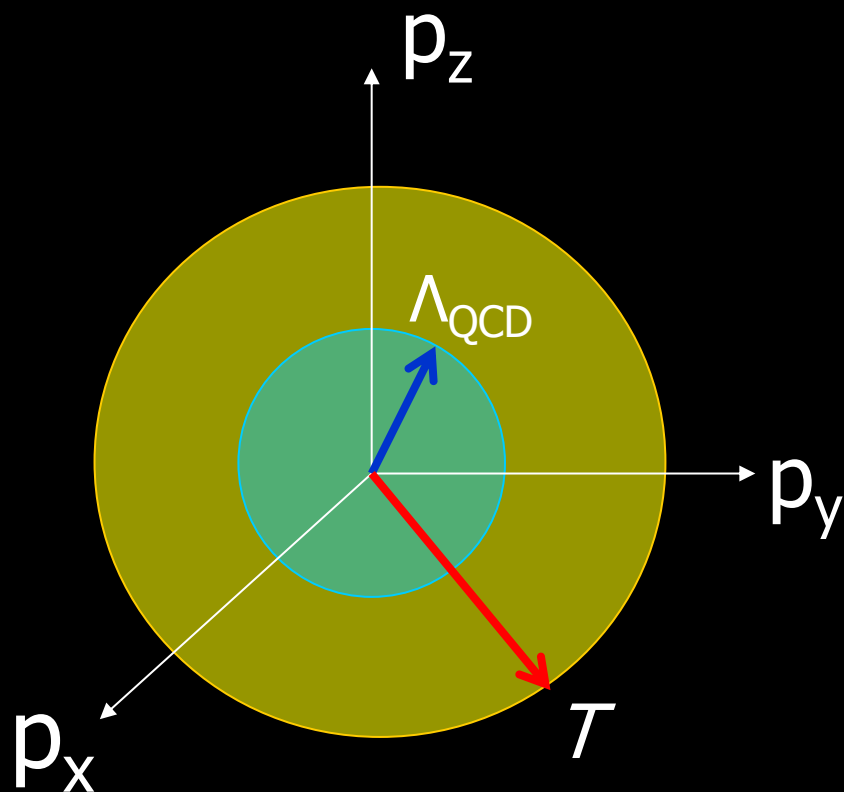
$T_{pc} = 150-160 \text{ MeV}$

Big Bang

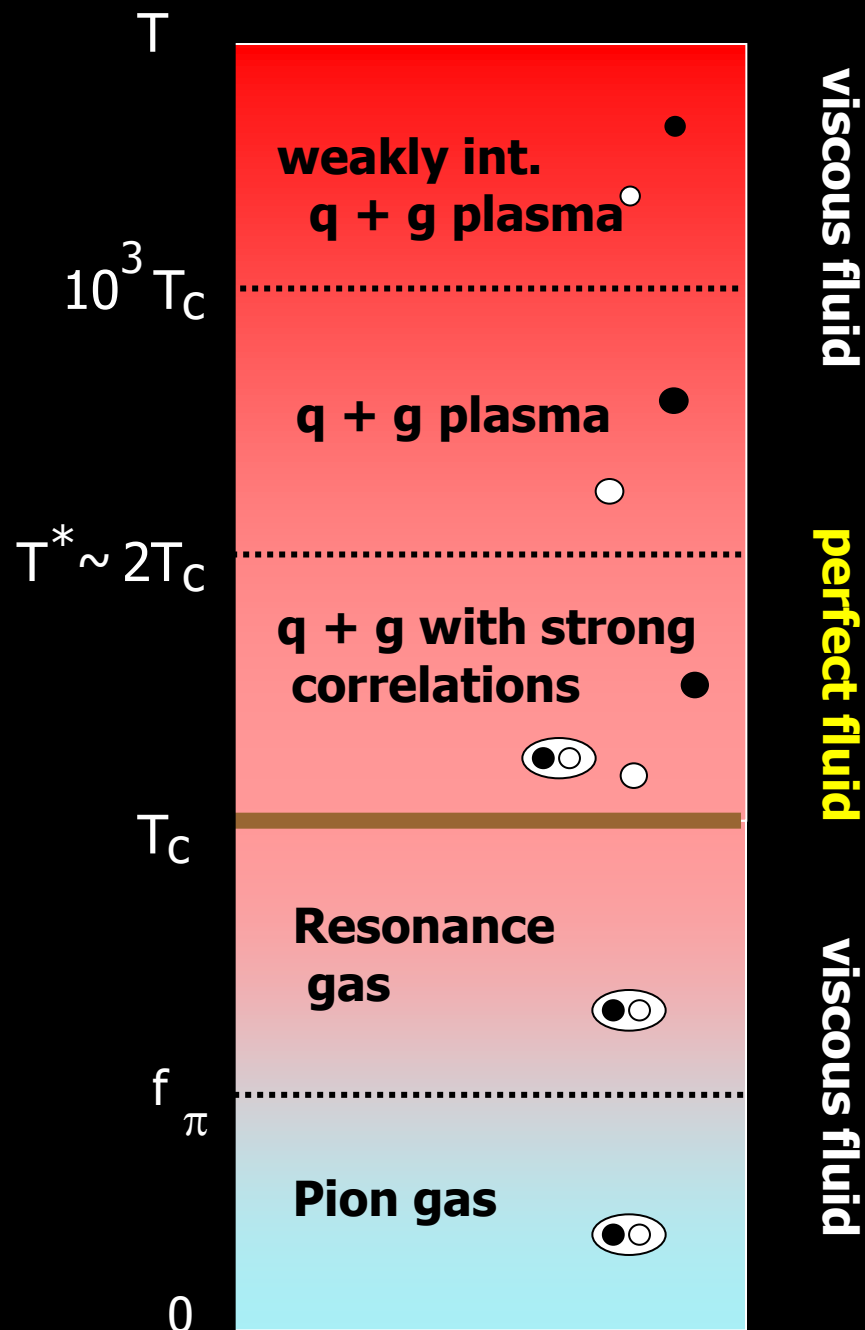


Little Bang

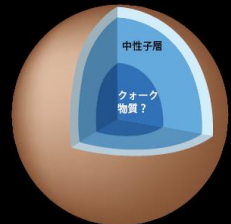
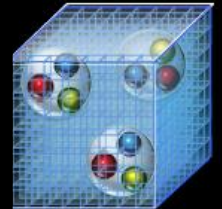
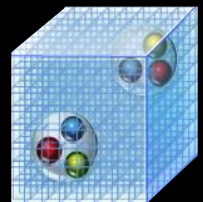
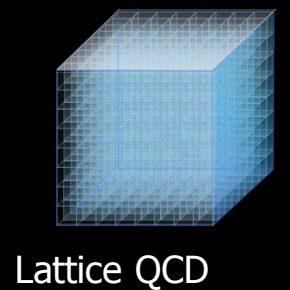
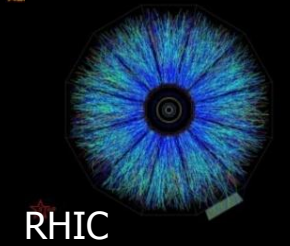
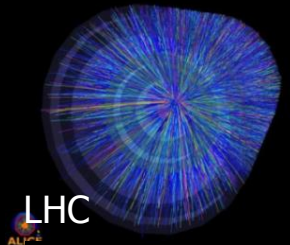
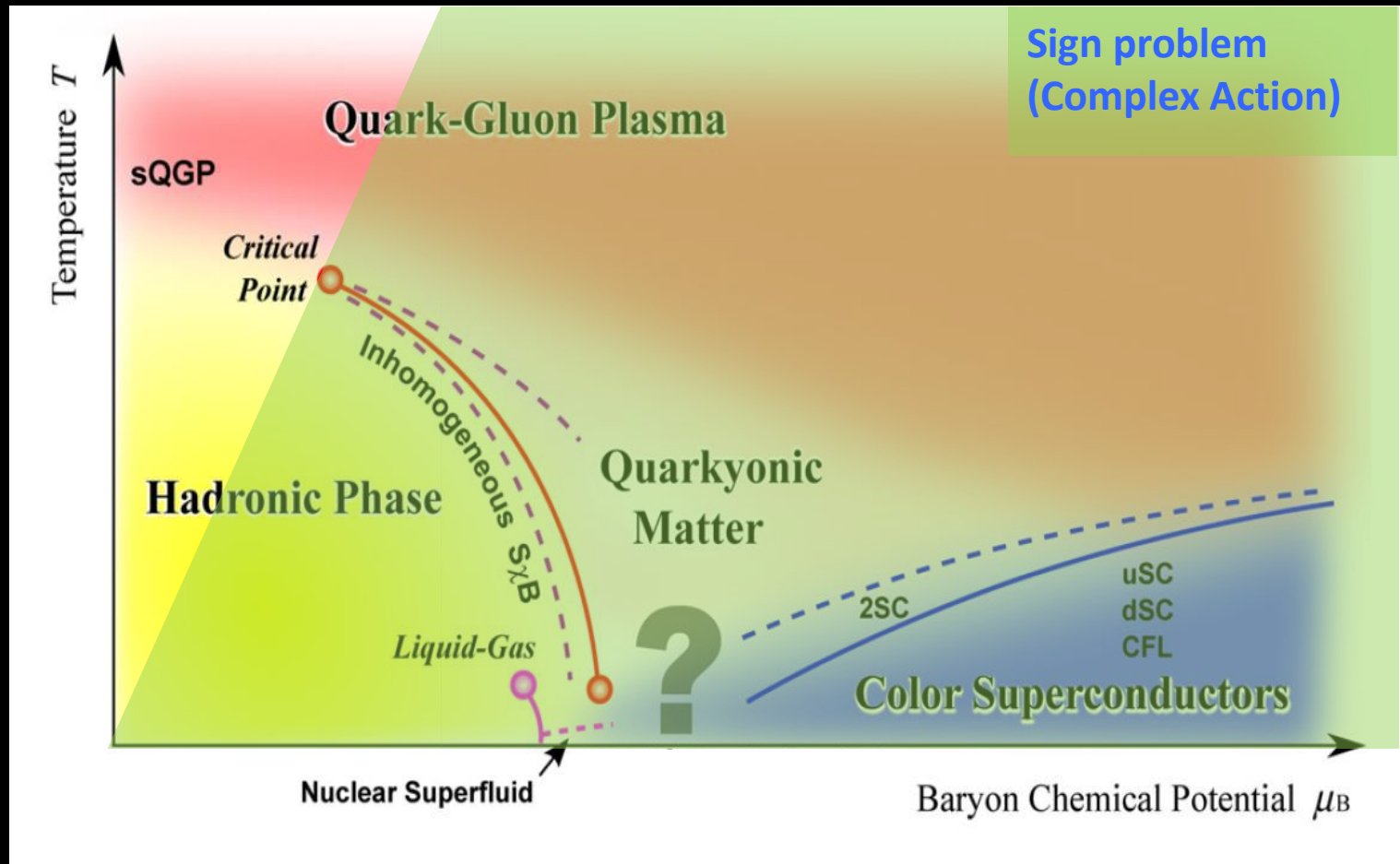
Strongly correlated QGP



Hatsuda & Kunihiro, PRL 51 (1985)
 DeTar, PRD 32 (1985)
 Nakamura & Sakai, PRL 94 (2005)



QCD Phase Diagram



K. Fukushima and T. Hatsuda,
 "The Phase Diagram of Dense QCD"
 Rep. Prog. Phys. 74 (2011) 014001

N_{\star} observations

Current:

$$M = (1.97 \pm 0.04) M_{\odot} \quad (\text{Nature 2010})$$

$$M = (2.01 \pm 0.04) M_{\odot} \quad (\text{Science 2013})$$

\Leftrightarrow cold EOS

X-ray bursts \Leftrightarrow cold EOS

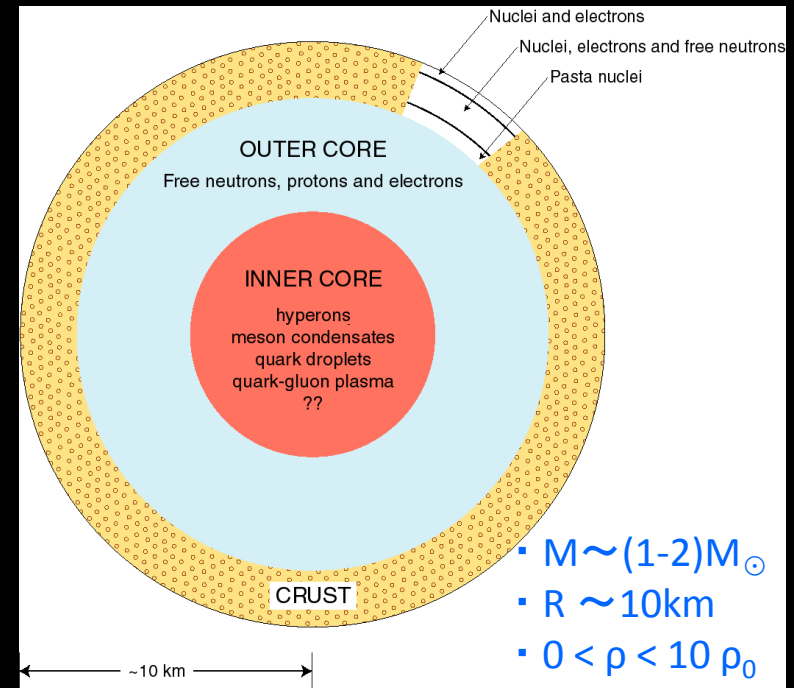
Cooling of CAS-A \Leftrightarrow 3P_2 superfluid?

Magnetars \Leftrightarrow ferromagnetic core?

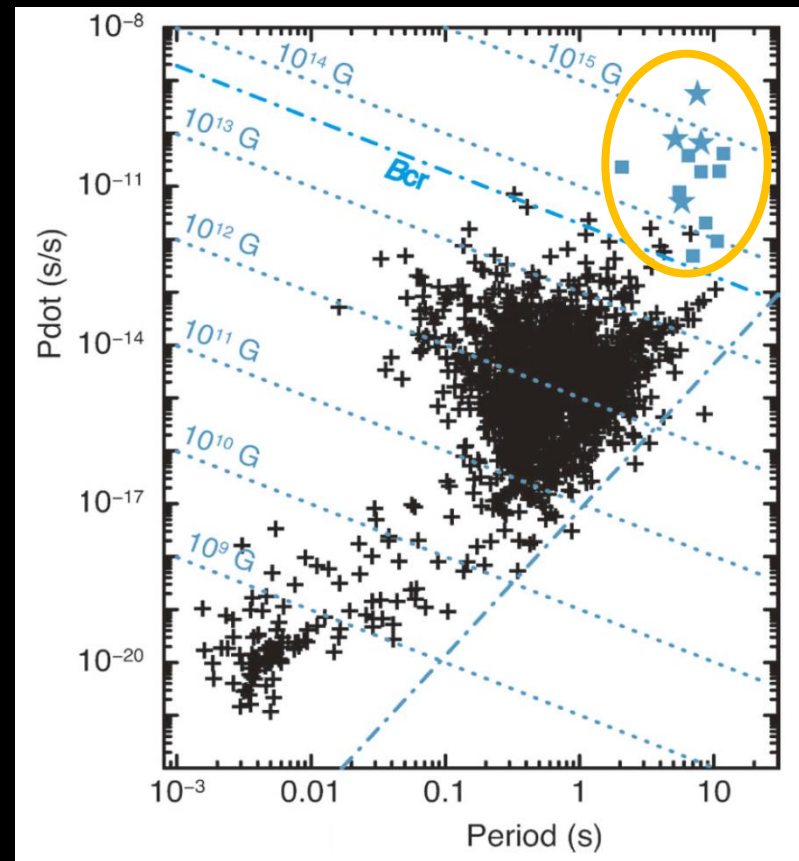
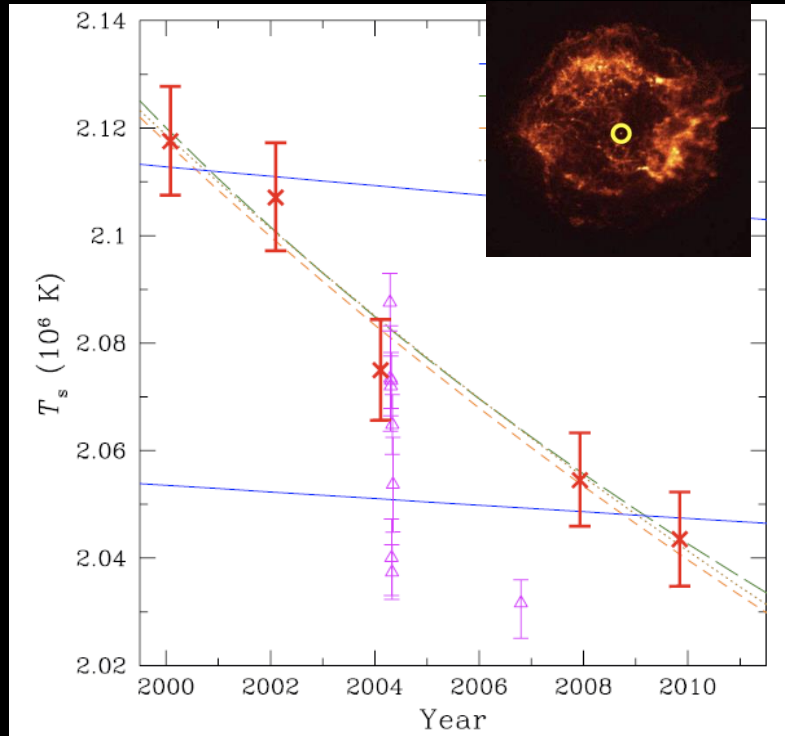
Future:

GW from N_{\star} merger \Leftrightarrow hot EOS

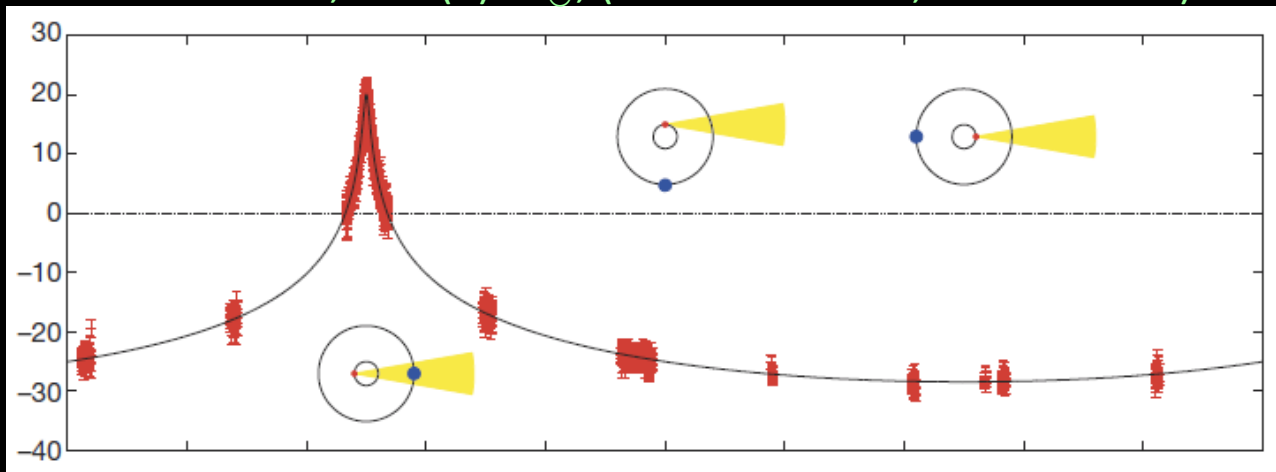
Seismology \Leftrightarrow crust structure



Cassiopeia A Cooling, 4% decrease in 9 years
(Heinke & Ho, ApJ 2010)



PSR J1614-2230 , 1.97(4) M_{\odot} , (Demorest et al., Nature 2010)

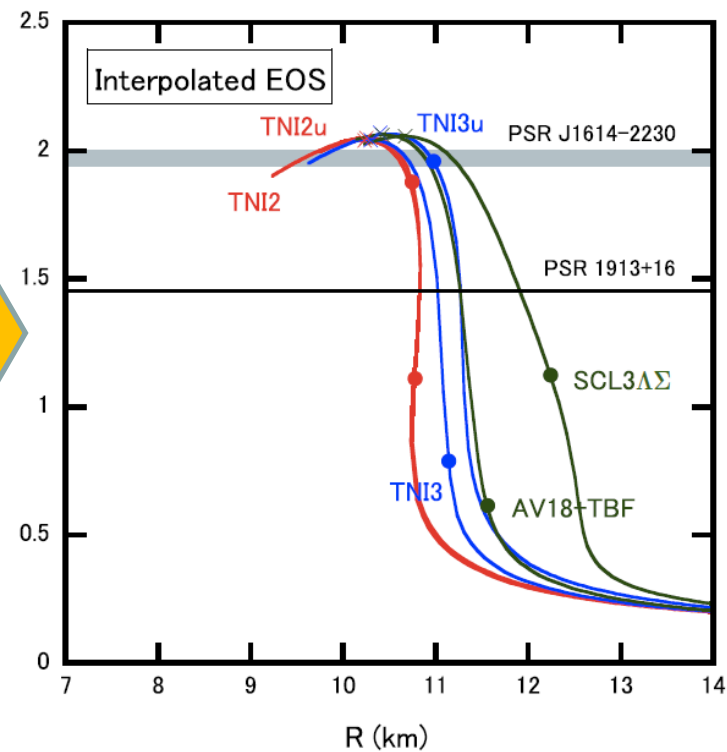
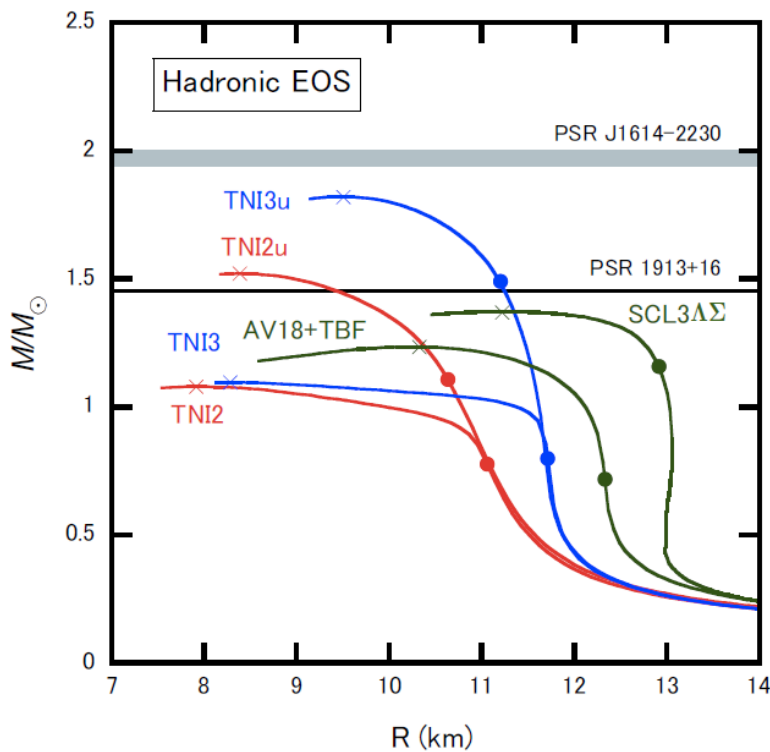
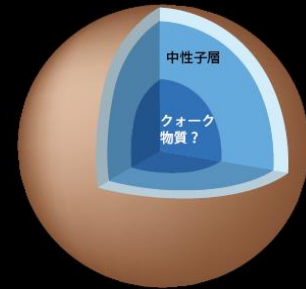
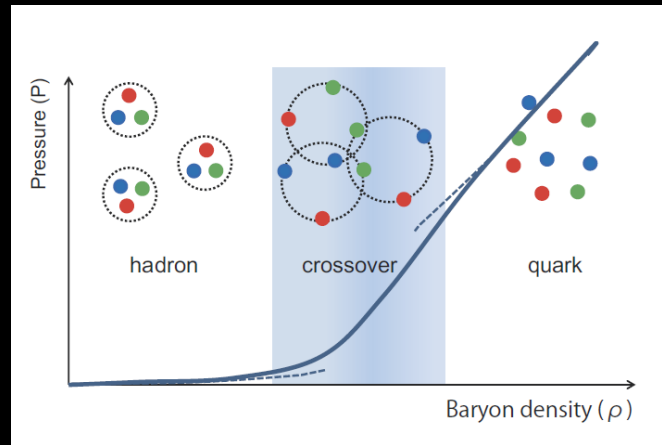


Magnetars
(from Enoto, 2012)
 $B_s = 3.2 \times 10^{19} \nu (P \dot{P})$ [G]

T, B, M

Hadron-Quark crossover in dense QCD

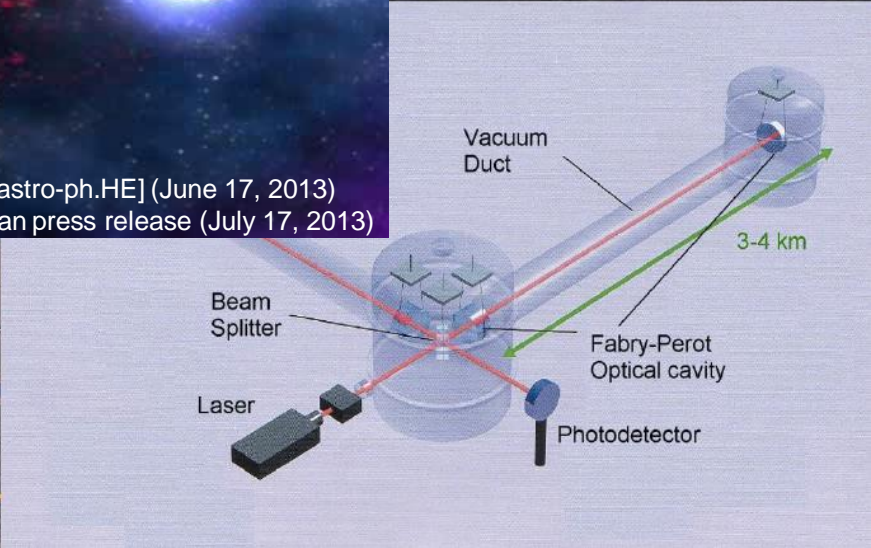
Hatsuda, Tachibana, Yamamoto & Baym,
Phys. Rev. Lett. 97, 122001 (2006)



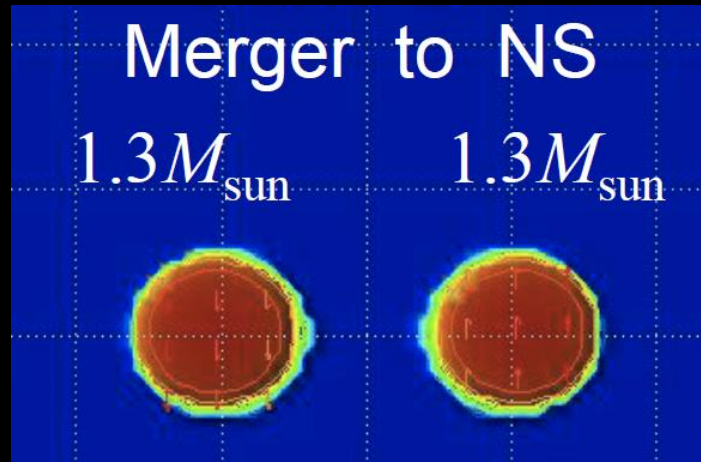
Gravitational wave from N_{\star} merger



Berger et al., arXiv:1306.3960[astro-ph.HE] (June 17, 2013)
Animation in Harvard-Smithsonian press release (July 17, 2013)

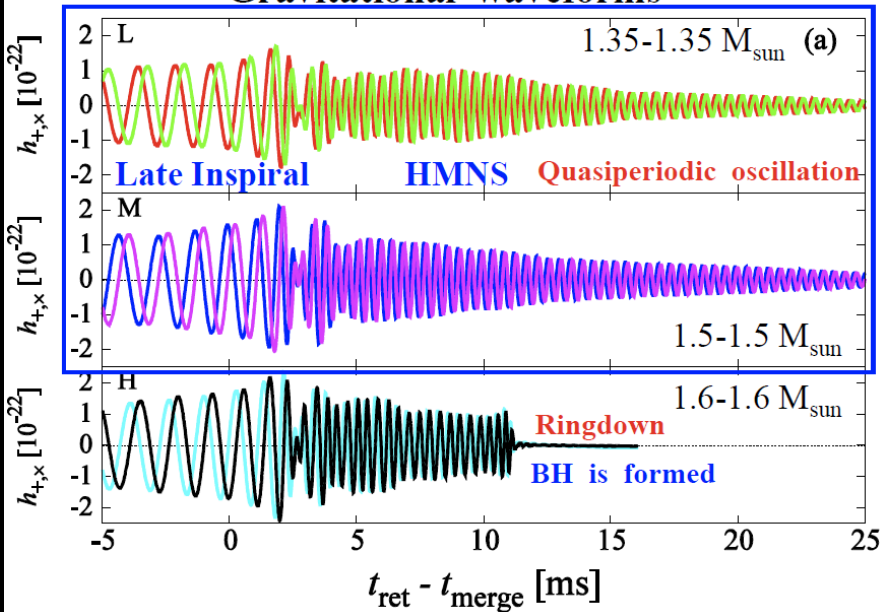


EOS from Gravitational Wave Detection

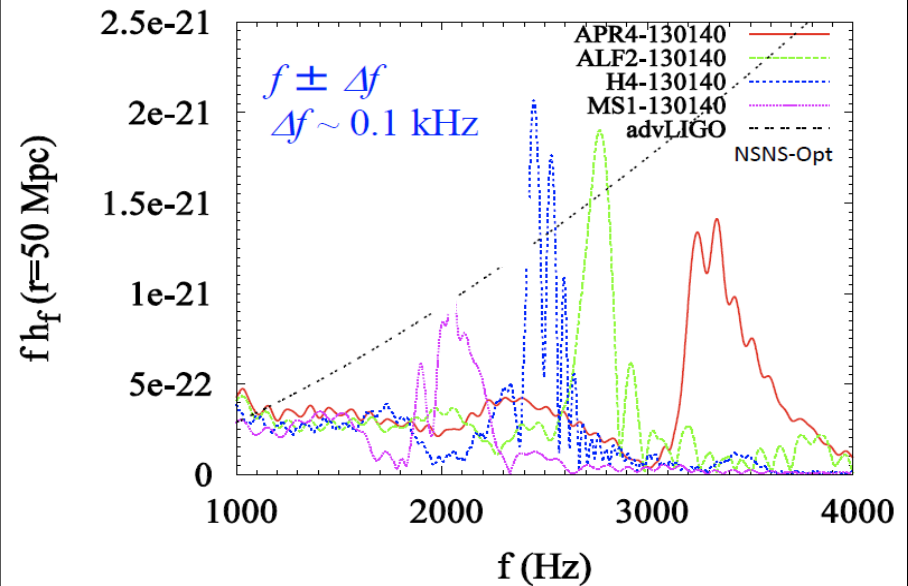


Sekiguchi, Kiuchi, Kyutoku & Shiata, PRL (2011)

Gravitational waveforms



Fourier spectrum



Did we understand QCD better than before after all ?

1. Impressive progress for past 40 years

- Theory : pQCD, lattice QCD, holography
- Expt. : e-p, p-p, p-A, A-A expt., astro. obs.

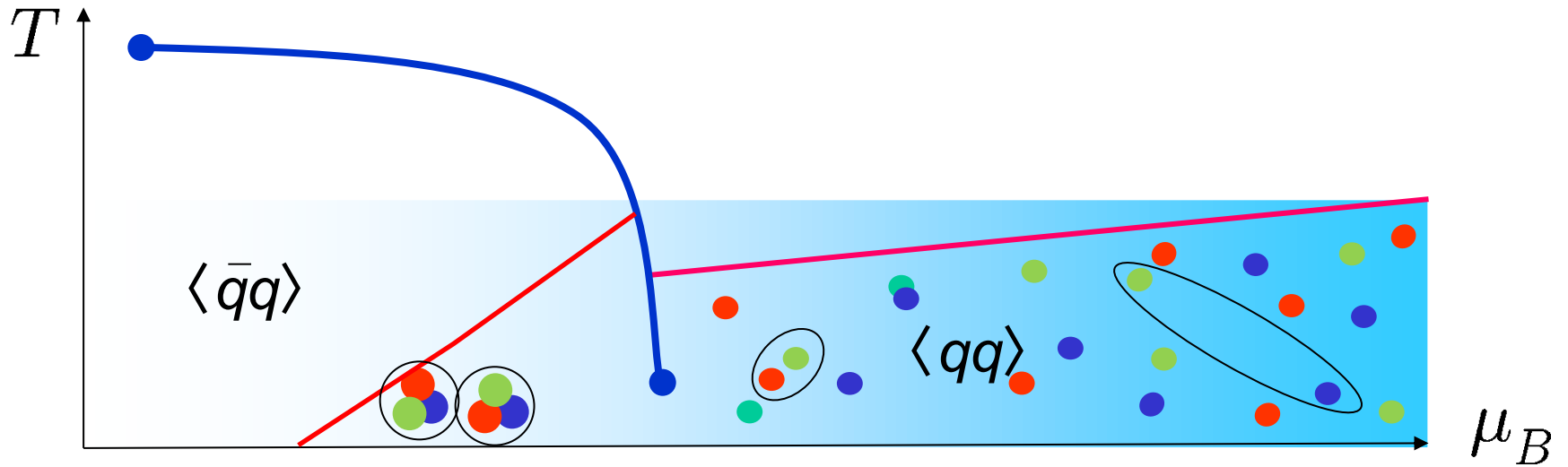
2. Understanding of QCD ~ understanding of glue

- Asymptotic freedom : chromo para-magnetism (Nielsen, Hughes, 1981)
- Confinement : no simple understanding yet
- sQGP, sQM, CGC: IR - UV crossover ($Q = T, \mu, x$)

3. Probe the role of glue through “Diquark” ?

- Possible agent to bridge IR - UV crossover in dense matter ?

Hadron-Quark Phase Transition and the role of "Diquarks"



Nuclear superfluid



Fermion+Diquark



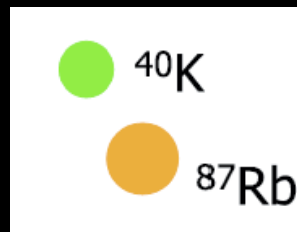
Diquark superfluid



Induced superfluid



Fermi-Bose mixture

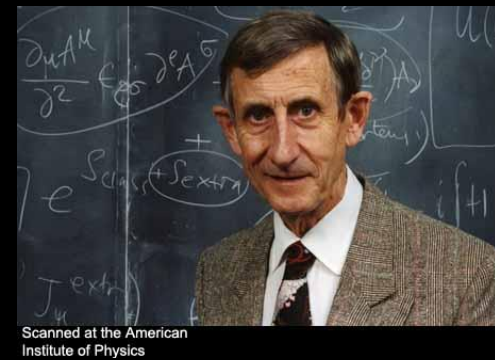


$$a_{\text{NN}}^{\text{Born}} = -\frac{m_{\text{N}}}{2m_{\text{R}}} a_{\text{bf}}$$

Maeda, Baym & Hatsuda, Phys. Rev. Lett. 103 ('09)

Summary

"The Scientist as Rebel"
by Freeman J. Dyson



It often happens that the understanding of **the mathematical nature of an equation** is impossible without a detailed understanding of its solutions. **The black hole** is a case in point.

Yellow → GR

Yellow → QCD

Pink → BH

Pink → Proton, QGP

The progress of science requires the growth of understanding in both directions, downward from the whole to the parts and upward from the parts to the whole.