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Skyrme-EDF for charge-changing excitation modes

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Outline

Self-consistent Skyrme-pnQRPA approach

✓ GT strengths in neutron-rich deformed Zr isotopes deformation T=0 pairing

pn-pair transfer strengths in N=Z nuclei in fp-shell collectivity of the pn-pairing vibration

Skyrme energy-density functional (EDF) approach Energy functional: $\mathcal{E} = \int d\mathbf{r} \mathcal{H}(\mathbf{r})$ Energy density: $\mathcal{H} = \mathcal{H}_{kin} + \mathcal{H}_{Skyrme} + \mathcal{H}_{em}$ Skyrme energy density: $\mathcal{H}_{Skyrme} = \sum \left[\sum \left(\mathcal{H}_{tt_3}^{even} + \mathcal{H}_{tt_3}^{odd} \right) \right]$ $\mathcal{H}_{tt_3}^{\text{even}} = C_t^{\rho} \rho_{tt_3}^2 + C_t^{\Delta\rho} \rho_{tt_3} \Delta\rho_{tt_3} + C_t^{\tau} \rho_{tt_3} \tau_{tt_3} + C_t^{\nabla J} \rho_{tt_3} \nabla \cdot \mathbf{J}_{tt_3} + C_t^{J} \overleftrightarrow{J}_{tt_3}^2$ $\mathcal{H}_{tt_3}^{\text{odd}} = C_t^s \, \mathbf{s}_{tt_3}^2 + C_t^{\Delta s} \, \mathbf{s}_{tt_3} \cdot \Delta \mathbf{s}_{tt_3} + C_t^T \, \mathbf{s}_{tt_3} \cdot \mathbf{T}_{tt_3} + C_t^{\nabla s} \, (\nabla \cdot \mathbf{s}_{tt_3})^2 + C_t^j \, \mathbf{j}_{tt_3}^2 + C_t^{\nabla j} \, \mathbf{s}_{tt_3} \cdot \nabla \times \mathbf{j}_{tt_3}$ T-odd densities vanish in g.s of e-e nuclei T-odd Skyrme energy density is not well constrained, but plays a role in studying compact star EoS of polarized neutron matter: T-odd components $\frac{\mathcal{H}}{\rho_0} = 2^{4/3} \left(\frac{3\pi^2}{2}\right)^{2/3} \left[\frac{\hbar^2}{2m} + \left(C_0^{\tau} + C_1^{\tau} + C_0^{\tau} + C_1^{T}\right)\rho_0\right]\rho_0^{2/3} + \left(C_0^{\rho} + C_1^{\rho} + C_0^{s} + C_1^{s}\right)\rho_0$

isovector components

T-odd energy density seen in nuclear responses Collective motion is generated by the residual interaction $v_{\rm res}(\boldsymbol{r}_1, \boldsymbol{r}_2) \equiv \frac{\delta^2 \mathcal{E}}{\delta \rho(\boldsymbol{r}_1) \delta \rho(\boldsymbol{r}_2)}$: self-consistency spin density spin excitation modes Nuclear response to the IV external field: $\int d\boldsymbol{r} r^L Y_L \hat{\boldsymbol{s}}_{1t}$ IV spin density: $\hat{s}_{1t} = \psi^{\dagger}(\boldsymbol{r}\sigma\tau)\langle\sigma|\boldsymbol{\sigma}|\sigma'\rangle\langle\tau|\boldsymbol{\tau}_{t}|\tau'\rangle\psi(\boldsymbol{r}\sigma'\tau')$ Gamow-Teller, Spin dipole,...

Self-consistent Skyrme-EDF approach for spin-isospin excitations in superfluid systems

North Carolina + Oak Ridge group



Role of T = 0 pairing in Gamow–Teller states in N = Z nuclei

C.L. Bai^a, H. Sagawa^{b,c,*}, M. Sasano^c, T. Uesaka^c, K. Hagino^d, H.Q. Zhang^e, X.Z. Zhang^e, F.R. Xu^f

Intermezzo -constrained by ab-initio calculations-



KY, PTEP2013,113D02 Self-consistent pnQRPA for spin-isospin excitations in deformed nuclei

starting point: Skyrme EDF $\mathcal{E}[\rho(\mathbf{r}), \tilde{\rho}(\mathbf{r})]$

variation w.r.t densities

The

Collecti

resic

The coordinate-space Hartree-Fock-Bogoliubov eq. for ground states

J. Dobaczewski et al., NPA422(1984)103

$$\begin{pmatrix} h^{q}(\boldsymbol{r},\sigma) - \lambda^{q} & \tilde{h}^{q}(\boldsymbol{r},\sigma) \\ \tilde{h}^{q}(\boldsymbol{r},\sigma) & -(h^{q}(\boldsymbol{r},\sigma) - \lambda^{q}) \end{pmatrix} \begin{pmatrix} \varphi_{1,\alpha}^{q}(\boldsymbol{r},\sigma) \\ \varphi_{2,\alpha}^{q}(\boldsymbol{r},\sigma) \end{pmatrix} = E_{\alpha} \begin{pmatrix} \varphi_{1,\alpha}^{q}(\boldsymbol{r},\sigma) \\ \varphi_{2,\alpha}^{q}(\boldsymbol{r},\sigma) \end{pmatrix}$$

"s.p." hamiltonian and pair potential: $h^{q} = \frac{\delta \mathcal{E}}{\delta \rho^{q}}, \quad \tilde{h}^{q} = \frac{\delta \mathcal{E}}{\delta \tilde{\rho}^{q}}$
 $q = \nu, \pi$
 $q = \nu, \pi$
The proton-neutron quasiparticle RPA eq. for excited states $[\hat{H}, \hat{O}_{\lambda}^{\dagger}] |\Psi_{\lambda}\rangle = \omega_{\lambda} \hat{O}_{\lambda}^{\dagger} |\Psi_{\lambda}\rangle$
Collective excitation = coherent superposition of 2qp excitations:
 $\hat{O}_{\lambda}^{\dagger} = \sum_{\alpha\beta} X_{\alpha\beta}^{\lambda} \hat{a}_{\alpha,\nu}^{\dagger} \hat{a}_{\beta,\pi}^{\dagger} - Y_{\alpha\beta}^{\lambda} \hat{a}_{\beta,\pi} \hat{a}_{\alpha,\nu}$
residual interactions derived self-consistently :
 $v_{\text{res}}(r_{1}, r_{2}) = \frac{\delta^{2} \mathcal{E}}{\delta \rho_{1t_{3}}(r_{1}) \delta \rho_{1t_{3}}(r_{2})} \tau_{1} \cdot \tau_{2} + \frac{\delta^{2} \mathcal{E}}{\delta s_{1t_{3}}(r_{1}) \delta s_{1t_{3}}(r_{2})} \sigma_{1} \cdot \sigma_{2} \tau_{1} \cdot \tau_{2}$

Canonical basis and quasiparticle basis

J. Engel et al., PRC60 (1999) 014302

$$A_{pn,p'n'} = E_{p,p'} \delta_{n,n'} + E_{n,n'} \delta_{p,p'} + \widetilde{V}_{pn,p'n'} (u_p v_n u_{p'} v_{n'} + v_p u_n v_{p'} u_{n'}) + V_{pn,p'n'} (u_p u_n u_{p'} u_{n'} + v_p v_n v_{p'} v_{n'})$$
(16)

$$B_{pn,p'n'} = \widetilde{V}_{pn,p'n'} (v_p u_n u_{p'} v_{n'} + u_p v_n v_{p'} u_{n'}) - V_{pn,p'n'} (u_p u_n v_{p'} v_{n'} + v_p v_n u_{p'} u_{n'}).$$
(17)

calculation cost ~ BCS-QRPA

introduction of cutoff occupation probability

KY, PTEP (2013)113D02

(7)

(8)

calculation cost ~ 4*BCS-QRPA

introduction of cutoff simply by the 2qp energy

pp(hh) and ph excitations are treated on the same footing
$$\begin{split} A_{\alpha\beta\alpha'\beta'} &= (E_{\alpha} + E_{\beta})\delta_{\alpha\alpha'}\delta_{\beta\beta'} \\ &+ \int d1d2d1'd2'\{\varphi_{1,\alpha}^{\nu}(r_{1}\bar{\sigma_{1}})\varphi_{1,\beta}^{\pi}(r_{2}\bar{\sigma_{2}})\bar{v}_{pp}(12;1'2')\varphi_{1,\alpha'}^{\nu*}(r_{1}'\bar{\sigma_{1}}')\varphi_{1,\beta'}^{\pi*}(r_{2}'\bar{\sigma_{2}}') \\ &+ \varphi_{2,\alpha}^{\nu}(r_{1}\sigma_{1})\varphi_{2,\beta}^{\pi}(r_{2}\sigma_{2})\bar{v}_{pp}(12;1'2')\varphi_{2,\alpha'}^{\nu*}(r_{1}'\sigma_{1}')\varphi_{2,\beta'}^{\pi*}(r_{2}'\sigma_{2}') \\ &+ \varphi_{1,\alpha}^{\nu}(r_{1}\bar{\sigma_{1}})\varphi_{2,\beta'}^{\pi*}(r_{2}\sigma_{2})\bar{v}_{ph}(12;1'2')\varphi_{2,\alpha}^{\pi}(r_{1}'\sigma_{1}')\varphi_{1,\beta'}^{\pi*}(r_{2}'\bar{\sigma_{2}'}) \\ &+ \varphi_{1,\beta}^{\pi}(r_{1}\bar{\sigma_{1}})\varphi_{2,\alpha'}^{\nu*}(r_{2}\sigma_{2})\bar{v}_{ph}(12;1'2')\varphi_{2,\alpha}^{\nu}(r_{1}'\sigma_{1}')\varphi_{1,\beta'}^{\pi*}(r_{2}'\bar{\sigma_{2}'}) \\ &+ \varphi_{1,\beta}^{\pi}(r_{1}\bar{\sigma_{1}})\varphi_{2,\alpha'}^{\pi}(r_{2}\bar{\sigma_{2}})\bar{v}_{ph}(12;1'2')\varphi_{2,\alpha}^{\nu}(r_{1}'\sigma_{1}')\varphi_{2,\bar{\alpha}'}^{\pi*}(r_{1}'\sigma_{1}')\varphi_{2,\bar{\beta}'}^{\pi}(r_{2}'\bar{\sigma_{2}'}) \\ &- \varphi_{2,\alpha}^{\nu}(r_{1}\sigma_{1})\varphi_{2,\beta}^{\pi}(r_{2}\sigma_{2})\bar{v}_{ph}(12;1'2')\varphi_{1,\bar{\alpha}'}^{\nu}(r_{1}'\bar{\sigma_{1}'})\varphi_{1,\bar{\beta}'}^{\pi}(r_{2}'\bar{\sigma_{2}'}) \\ &- \varphi_{1,\alpha}^{\nu}(r_{1}\bar{\sigma_{1}})\varphi_{1,\bar{\beta}'}^{\pi}(r_{2}\bar{\sigma_{2}})\bar{v}_{ph}(12;1'2')\varphi_{2,\alpha}^{\nu}(r_{1}'\sigma_{1}')\varphi_{2,\bar{\beta}'}^{\pi}(r_{2}'\bar{\sigma_{2}'}) \\ &- \varphi_{1,\beta}^{\pi}(r_{1}\bar{\sigma_{1}})\varphi_{1,\bar{\alpha}'}^{\nu}(r_{2}\bar{\sigma_{2}})\bar{v}_{ph}(12;1'2')\varphi_{2,\alpha}^{\nu}(r_{1}'\sigma_{1}')\varphi_{2,\bar{\beta}'}^{\pi}(r_{2}'\bar{\sigma_{2}'}) \\ &- \varphi_{1,\beta}^{\pi}(r_{1}\bar{\sigma_{1}})\varphi_{1,\bar{\alpha}'}^{\nu}(r_{2}\bar{\sigma_{2}})\bar{v}_{ph}(12;1'2')\varphi_{2,\alpha}^{\nu}(r_{1}'\bar{\sigma_{1}'})\varphi_{2,\bar{\beta}'}^{\mu}(r_{2}'\bar{\sigma_{2}'}) \\ &- \varphi_{1,\beta}^{\pi}(r_{1}\bar{\sigma_{1}})\varphi_{1,\bar{\alpha}'}^{\nu}(r_{2}\bar{\sigma_{2}})\bar{v}_{ph}(12;1'2')\varphi_{2,\alpha}^{\nu}(r_{1}'\bar{\sigma_{1}'})\varphi_{2,\bar{\beta}'}^{\mu}(r_{2}'\bar{\sigma_{2}'}) \\ &- \varphi_{1,\beta}^{\pi}(r_{1}\bar{\sigma_{1}})\varphi_{1,\beta}^{\mu}(r_{2}\bar{\sigma_{2}})\bar{v}_{ph$$

QRPA for heavy axially-deformed nuclei with HPC

HFB cal. (64 CPUs) Box size: 14.7 fm × 14.4 fm Cut-off: $\Omega \leq \frac{31}{2}, E_{\alpha} \leq 60$ MeV

HFB Hamiltonian: block diagonal in Ω^{π} distributed to cores

QRPA cal. (512 CPUs) Cut-off: $E_{\alpha} + E_{\beta} \leq 60 \text{ MeV}$ Matrix elements of A and B:

2D-numerical integration independent of each 2qp configuration

For each K^π # of 2qp excitation: ~50,000

matrix elements: 590 core hours diagonalization: 330 core hours with the help of ScaLapack

GT strengths and beta-decay properties of neutron-rich Zr isotopes

β -decay half-lives in neutron-rich Zr isotopes

S. Nishimura et al., PRL106(2011)052502



β -decay half-lives in neutron-rich Zr isotopes

S. Nishimura et al., PRL106(2011)052502



Deformed Zr isotopes on the r-process path



T. Sumikama et al., PRL106(2011)202501

GT giant resonance



$d\boldsymbol{r}\hat{\psi}^{\dagger}(\boldsymbol{r}\sigma\tau)\langle\sigma|\boldsymbol{\sigma}_{K}|\sigma'\rangle\langle\tau|\boldsymbol{\tau}_{t_{3}}|\tau'\rangle\hat{\psi}(\boldsymbol{r}\sigma'\tau')$



\checkmark sudden onset of deformation at N=60

SLy4: A. Blazkiewicz et al., PRC71(2005)054321

 \checkmark fragmentation of strength distribution due to deformation

separable pnRPA: P. Urkedal et al., PRC64(2001)054304

 \checkmark SkM* and SLy4 give almost the same ($\Delta E{<}1$ MeV) excitation energies of GTGR

g₀'=0.94 (SkM*), 0.90 (SLy4)



excitation energy w.r.t. the g.s of daughter

I MeV smearing width

GTGR: the need of self-consistency



 \checkmark a repulsive character of the residual interaction raises the peak energy

 \checkmark low-lying strengths are absorbed to the highenergy peak

strong collectivity of the GTGR

✓ the collectivity generated by the Landau-Migdal approximation is weak

$$v_{\rm ph}(\boldsymbol{r}_1 \, \boldsymbol{r}_2) = N_0^{-1} \left[f_0' \tau_1 \cdot \tau_2 + g_0' \sigma_1 \cdot \sigma_2 \tau_1 \cdot \tau_2 \right] \delta(\boldsymbol{r}_1 - \boldsymbol{r}_2)$$

LM parameter: M. Bender et al., PRC65(2002)054322

self-consistency is required for a quantitative description of the GTGR

IV giant dipole resonance: Anti-analog GDR $\hat{F}_{1K}^{t_3} = \sum_{\sigma} \sum_{\tau,\tau'} \int d\mathbf{r} r Y_{1K} \hat{\psi}^{\dagger}(\mathbf{r} \sigma \tau) \langle \tau | \mathbf{\tau}_{t_3} | \tau' \rangle \hat{\psi}(\mathbf{r} \sigma \tau')$



SLy4 + mixed-type pairing

✓ deformation splitting (Ksplitting) is clearly seen as in GDR

AGDR and neutron skin thickness

linear relationship between the neutron-skin thickness and the AGDR energy



A. Krasznahorkay, N. Paar, D. Vretenar, M.N.Harakeh, Phys. Scr. T154(2013)4018

J.Yasuda, T.Wakasa et al., PTEP2013, 063D02

T=0 (S=I) pairing

 \checkmark affects the GT response

if we have (a) T=I pairing condensate(s)

due to the coupling between the p-h and p-p excitations



we may see the effect in the low-lying states that are generated by 2qp excitations around the Fermi levels

 \checkmark does not affect the gs properties in N>Z nuclei



a form of the interaction or an np-pairing EDF is seldom known

Take the simplest one;

$$v_{\rm pp}^{T=0}(\boldsymbol{r}, \boldsymbol{r}') = \frac{1+P_{\sigma}}{2} \frac{1-P_{\tau}}{2} V_0 \delta(\boldsymbol{r}-\boldsymbol{r}')$$

the pairing strength determined to reproduce the β -decay half-life of ¹⁰⁰Zr (7.1 s)

Low-lying GT states

SLy4+Mixed-type pairing 0.1 MeV smearing width



Low-lying GT states



selection rule for GT-

 $|\langle \pi[Nn_3\Lambda]\Omega = \Lambda + 1/2|t_-\sigma_{+1}|\nu[Nn_3\Lambda]\Omega = \Lambda - 1/2\rangle| = \sqrt{2}$

106 Zr

constructed dominantly by $\pi[413]7/2 \otimes \nu[413]5/2$ particle-like particle-like

 $\sqrt{T}=0$ pairing effective

neutrons added

108, 110Zr

 $\begin{array}{ll} \pi[413]7/2 \otimes \nu[413]5/2 \\ \text{particle-like} & \text{hole-like} \end{array}$

√T=0 pairing ineffective

Beta-decay half-lives



✓ Fermi's golden rule

N. B. Gove, M. J. Martin, At. Data Nucl. Data Tables 10(1971)205

✓ Fermi and Gamow-Teller strengths included

✓ SkM* produces longer half-lives primarily due to a large Q-value

approximate Q-value

$$Q_{\beta^{-}} = \Delta M_{n-H} + B(A, Z+1) - B(A, Z)$$
$$\simeq \Delta M_{n-H} + \lambda_{\nu} - \lambda_{\pi} - E_{0}$$
$$E_{0} = \min[E_{\nu} + E_{\pi}]$$

cf. J. Engel et al., PRC60(1999)014302

Beta-decay half-lives with T=0 pairing



✓ Strength of T=0 pairing determined at N=60

SLy4

✓ reproduces well the observed isotopic dependence with T=0 pairing
 ✓ Effect of the T=0 pairing is small beyond N=68

SkM*

 \checkmark gives a strong deformed gap at N=64

$\sqrt{pn-pair}$ transfer strengths in N=Z nuclei in fp-shell

Proton-neutron pair excitations

$$\hat{P}_{T=0,S=1,S_z=0}^{\dagger} = \frac{1}{2} \sum_{\sigma,\sigma'} \sum_{\tau} \int d\boldsymbol{r} \hat{\psi}^{\dagger}(\boldsymbol{r}\sigma\tau) \langle \sigma | \boldsymbol{\sigma}_0 | \sigma' \rangle \hat{\psi}^{\dagger}(\boldsymbol{r}\tilde{\sigma}'\tilde{\tau})$$

IS spin triplet

IV

$$\hat{P}_{T=0,S=1,S_{z}=\pm1}^{\dagger} = \frac{1}{2} \sum_{\sigma,\sigma'} \sum_{\tau} \int d\boldsymbol{r} \hat{\psi}^{\dagger}(\boldsymbol{r}\sigma\tau) \langle \sigma | \boldsymbol{\sigma}_{\pm1} | \sigma' \rangle \hat{\psi}^{\dagger}(\boldsymbol{r}\tilde{\sigma}'\tilde{\tau})$$

$$\begin{array}{ll} & \hat{P}_{T=1,T_z=0,S=0}^{\dagger} \\ \text{spin singlet} & = \frac{1}{2} \sum_{\sigma} \sum_{\tau,\tau'} \int d\boldsymbol{r} \hat{\psi}^{\dagger}(\boldsymbol{r}\sigma\tau) \langle \tau | \boldsymbol{\tau}_0 | \tau' \rangle \hat{\psi}^{\dagger}(\boldsymbol{r}\tilde{\sigma}\tilde{\tau}') \\ \end{array}$$

Interactions employed for pn-pairing vibration in fp-shell nuclei



 44 Ti $\Delta n = 1.82 \text{ MeV}$ $\Delta p = 1.87 \text{ MeV}$

pnQRPA eq:

p-h channel: SGII

p-p channel:

$$v_{\rm pp}^{T=0}(\boldsymbol{r}\sigma\tau, \boldsymbol{r}'\sigma'\tau') = f \times V_0 \frac{1+P_\sigma}{2} \frac{1-P_\tau}{2} \left[1-\frac{\rho(\boldsymbol{r})}{\rho_0}\right] \delta(\boldsymbol{r}-\boldsymbol{r}')$$
$$v_{\rm pp}^{T=1}(\boldsymbol{r}\sigma\tau, \boldsymbol{r}'\sigma'\tau') = V_0 \frac{1-P_\sigma}{2} \frac{1+P_\tau}{2} \left[1-\frac{\rho(\boldsymbol{r})}{\rho_0}\right] \delta(\boldsymbol{r}-\boldsymbol{r}')$$

cf. C. Bai et al., PLB719(2013)116



f=1.3			
42 Sc		$J^{\pi} = 1^+$	$J^{\pi} = 0^+$
configuration	$E_{\alpha} + E_{\beta}$	$M^{S=1,S_z=0}_{\alpha\beta}$	$M^{S=0}_{\alpha\beta}$
$\pi 1 f_{7/2} \otimes \nu 1 f_{7/2}$	7.5	1.70	2.85
$\pi 1 f_{7/2} \otimes \nu 1 f_{5/2}$	15.2	0.62	
$\pi 1 f_{5/2} \otimes \nu 1 f_{7/2}$	14.7	0.51	
$\pi 2p_{3/2} \otimes \nu 2p_{3/2}$	16.1	0.17	0.22
$\pi 1d_{3/2}\otimes u 1d_{3/2}$	4.2	0.25	0.48
$\pi 2s_{1/2} \otimes \nu 2s_{1/2}$	6.6	0.25	
$\pi 1d_{3/2}\otimes u 1d_{5/2}$	10.1	0.32	
$\pi 1d_{5/2}\otimes u 1d_{3/2}$	10.2	0.32	
$\pi 1d_{5/2} \otimes \nu 1d_{5/2}$	16.1	0.16	0.31

Transition matrix element

$$\langle \lambda | \hat{P}_{T,S}^{\dagger} | 0 \rangle = \sum_{\alpha \beta} M_{\alpha \beta}^{T,S}$$



f=1.3			
⁵⁸ Cu		$J^{\pi} = 1^+$	$J^{\pi} = 0^+$
configuration	$E_{\alpha} + E_{\beta}$	$M^{S=1,S_z=0}_{\alpha\beta}$	$M^{S=0}_{\alpha\beta}$
$\pi 2p_{3/2} \otimes \nu 2p_{3/2}$	4.5	1.28	1.90
$\pi 2p_{1/2}\otimes u 2p_{3/2}$	6.4	0.39	
$\pi 2p_{3/2} \otimes \nu 2p_{1/2}$	6.5	0.37	
$\pi 2p_{1/2}\otimes u 2p_{1/2}$	7.9		0.26
$\pi 1 f_{5/2} \otimes \nu 1 f_{5/2}$	9.7	0.15	0.55
$\pi 1 f_{7/2} \otimes \nu 1 f_{7/2}$	5.1	0.17	0.50

Collective pn-pairing vibration mode precursory to the T=0 pairing condensation

$\Delta E = \omega_{1+} - \omega_{0+}$



approaching the critical point to the T=0 pairing condensation $f_c=1.53$

Enhancement of the transfer strengths



d-tranfer: ⁴⁰Ca(³He,p)⁴²Sc

$$\frac{\sigma(1^+)_{\rm exp}}{\sigma(1^+)_{\rm unp}} = 23.9$$

F. Pühlhofer, NPA116 (1968) 516

RCNP



Y. Fujita et al., PRL112 (2014) 112502
T. Adachi, Y. Fujita et al., NPA788 (2007) 70c



Summary

Fully-selfconsistent deformed pnQRPA is developed in a Skyrme EDF framework

Microscopic and quantitative description of spin-isospin excitations in nuclei with arbitrary mass number whichever they are spherical or deformed, located around the stability line or close to the drip line

provide a microscopic input to the astrophysical simulation

Deformation effects on spin-isospin responses

Tiny deformation splitting in Gamow-Teller excitation

Fragmentation of GTGR

Clear deformation splitting in Anti-analog GDR as seen in IVGDR

Effects of T=0 pairing

Low-lying GT states are sensitive to the location of the Fermi levels, and the beta-decay half-lives are shortened

Proton-neutron pair-transfer strengths

Strong collectivity due to the T=0 pairing suggests emergence of a soft mode toward the T=0 pairing condensation

Restoration of the isospin symmetry breaking (ISB)

SkM* w/o pairing

Even w/o the Coulomb int., the ISB occurs in N>Z nuclei in a MFA $[H_{MF}, T_{-}] \neq 0$ C. A. Engelbrecht and R. H. Lemmer, PRL24(1970)607

IAS appears as a NG mode in the pnRPA

Ex. ⁹⁰Zr (N-Z=10) w/o Coulomb

10

 $\rho_{\max} \times z_{\max} = 14.7 \text{ fm} \times 14.4 \text{ fm}$ $\Delta \rho = \Delta z = 0.6 \text{ fm}$ $E_{2qp} \le 60 \text{ MeV}$



Restoration of the isospin symmetry breaking (ISB)

Ex. ⁹⁰Zr (N-Z=10) w/o Coulomb



protons are paired

Restoration of the isospin symmetry breaking (ISB) Ex. ⁹⁰Zr (N-Z=10) w/o Coulomb inclusion of the T=1 (S=0) pairing interaction in the pnQRPA

$$v_{\rm pp}^{T=1}(\boldsymbol{r}, \boldsymbol{r}') = \frac{1 - P_{\sigma}}{2} \frac{1 + P_{\tau}}{2} V_0 \left[1 - \frac{1}{2} \frac{\rho_{00}(\boldsymbol{r})}{\rho_0} \right] \delta(\boldsymbol{r} - \boldsymbol{r}')$$

