Microphysics for GR-Hydro merger simulations

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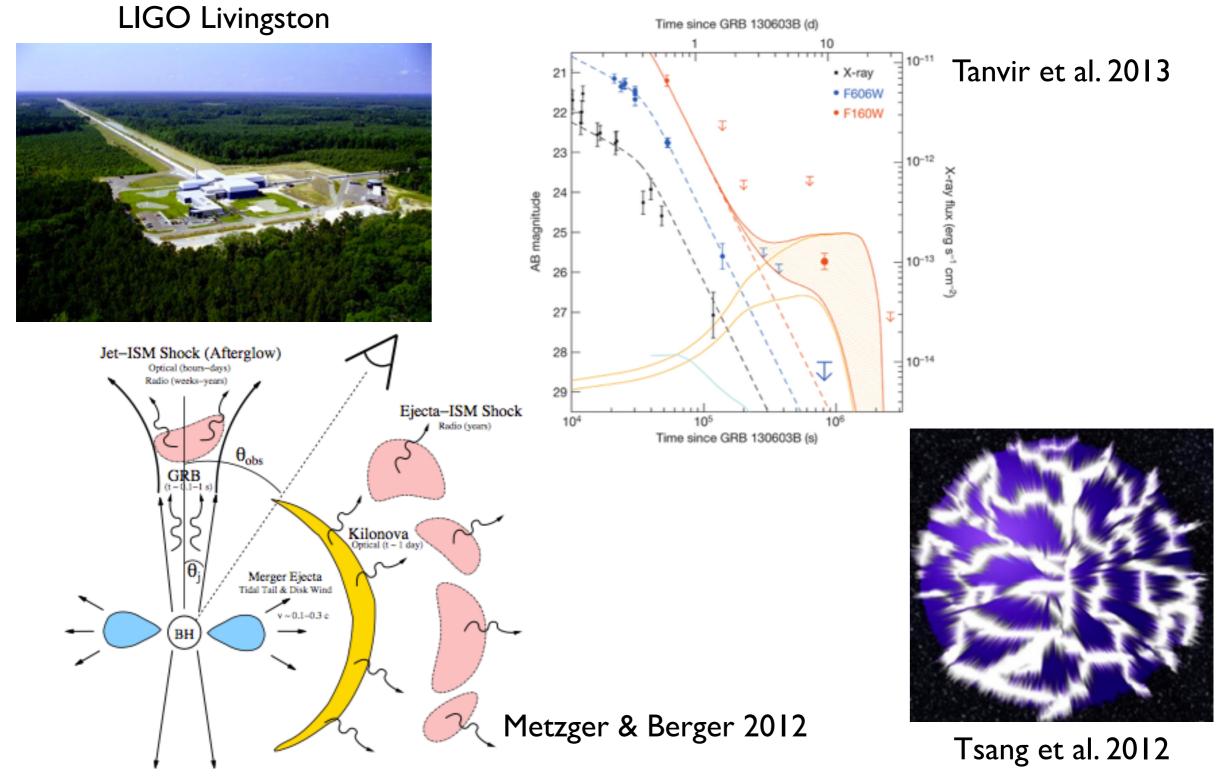
Hawaii 2014

Collaborators

- Brett Deaton (WSU)
- Matt Duez (WSU)
- Evan O'Connor (UNC)
- Christian Ott (Caltech)
- Luke Roberts (Caltech)

- Lawrence Kidder (Cornell)
- Curran Muhlberger (Cornell)
- Harald Pfeiffer (CITA)
- Bela Szilagyi (Caltech)
- Mark Scheel (Caltech)

Observing Mergers

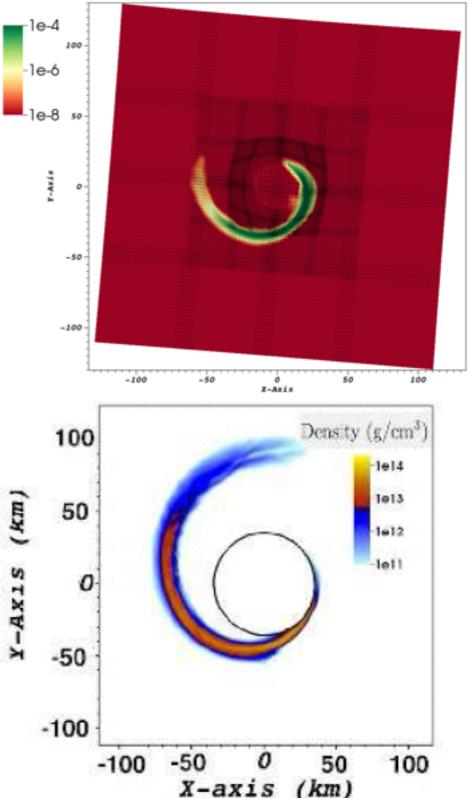


Important Physics

- General Relativity + Hydrodynamics
- Magnetic Fields
- Neutrino Radiation
- Equation of state of dense matter $P(\rho,T,Y_e)$
- Nuclear reactions in disk / outflows

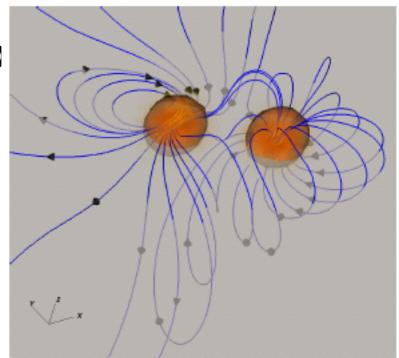
Challenges: GR-Hydro

- Formulation of Einstein's equations
 - BSSN, Generalized Harmonics
- Shock capturing schemes in GR
- Highly relativistic flows
- Scales to resolve (density, distances)
- ~10⁵ CPU-hrs



Challenges: B-fields

- Ideal MHD: resolve growth of instabilities (e.g. MRI grows on short length scales)
 - ~10⁷ CPU-hrs
- Magnetically dominated regime in lo density regions
 - Atmosphere treatment
- Reconnection, current sheets



Ponce et al 2014

Challenges: Neutrinos

• 6+1-D problem (t, x, p) => High CPU-cost

$$p^{\alpha} \left[\frac{\partial f_{\nu}}{\partial x^{\alpha}} - \Gamma^{\beta}_{\ \alpha\gamma} \ p^{\gamma} \frac{\partial f_{\nu}}{\partial p^{\beta}} \right] = \left[\frac{df_{\nu}}{d\tau} \right]_{\text{coll}}$$

- Stiff equations: absorption in optically thick regions, redshift terms
- Simplified formalisms exist, but only order-ofmagnitude accurate (or with known artifacts)
- See simulations later in this talk...

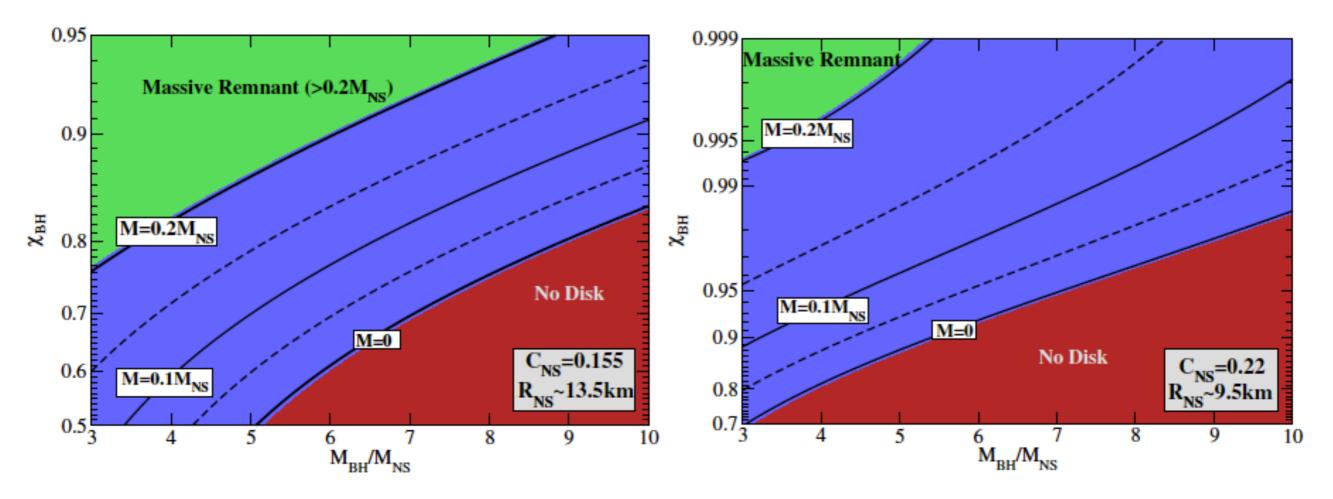
Results



Results

BH-NS "Disruption Line"

Foucart 2012



Approximate disruption condition from NR simulations:

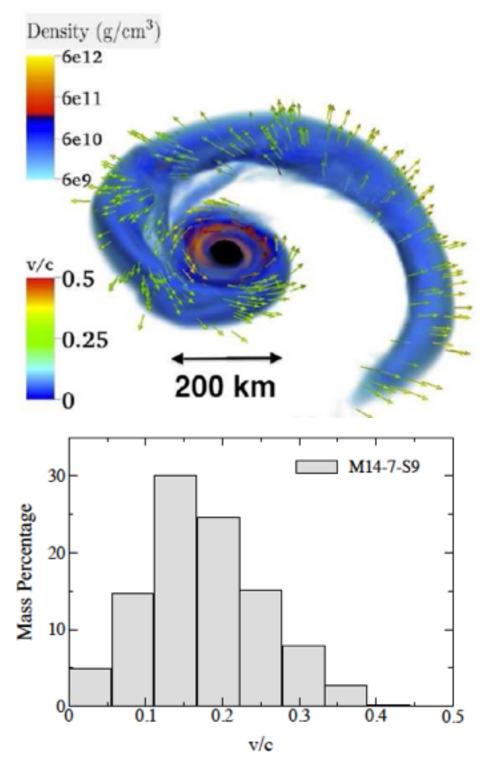
$$C_{\rm NS} \lesssim \left(2 + 2.14q^{2/3} \frac{R_{\rm ISCO}}{6M_{\rm BH}}\right)^{-1}$$

BhNs Mergers: Outflows

Foucart et al. 2013/4; Kyutoku et al. 2013; Lovelace et al. 2013, Deaton et al. 2013; Hotokezaka et al. 2014

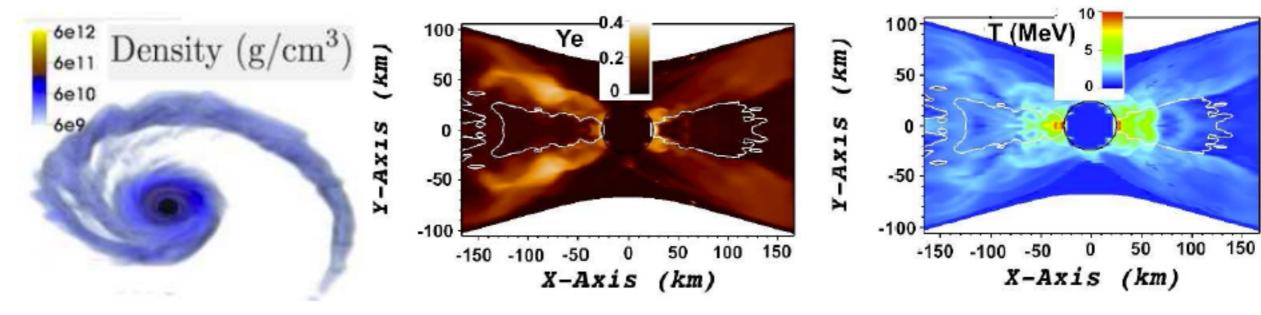
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- NS disruption:
 - More ejecta than NS-NS
 - Anisotropic => kicks
 - Low T, neutron rich
 - Strong r-process
- Disk outflows (e.g. Fernandez & Metzger 2014)
 - Probably subdominant



Accretion Disks

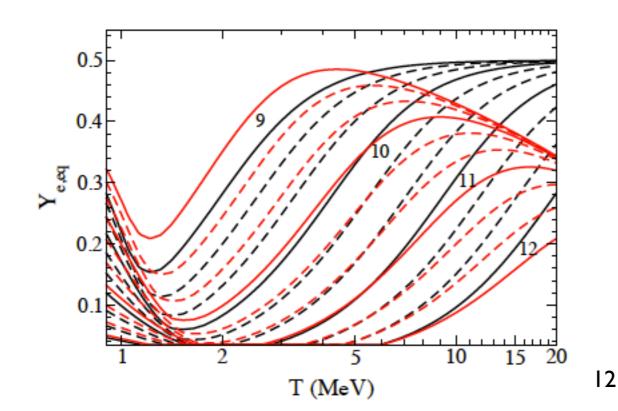
Foucart et al 2014

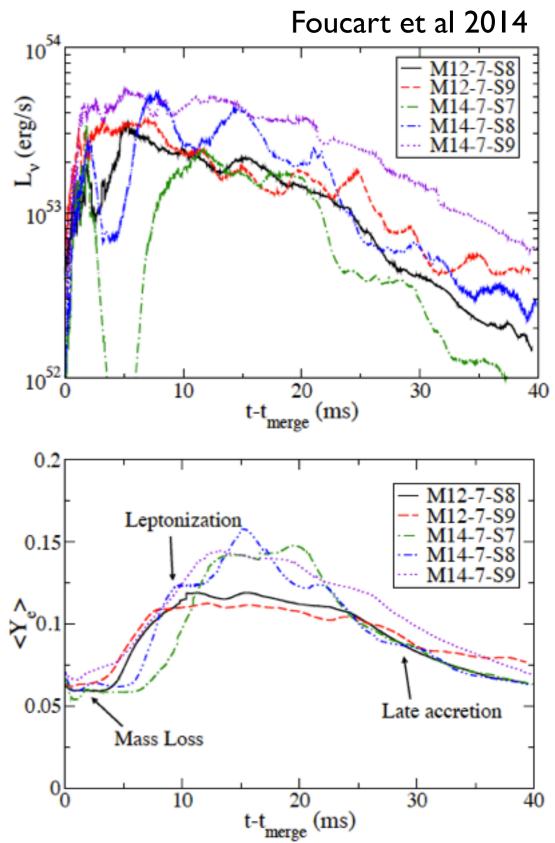


- Massive dynamical ejecta
- Disk with T~5-10 MeV
- Core neutron rich, Ye<0.1
 - •But Ye~0.2-0.4 in low-density regions

Neutrino Emission

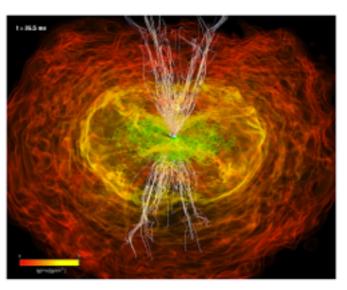
- No impact before merger
- Main source of cooling
- Energy deposition
- Sets Ye in disk / outflow



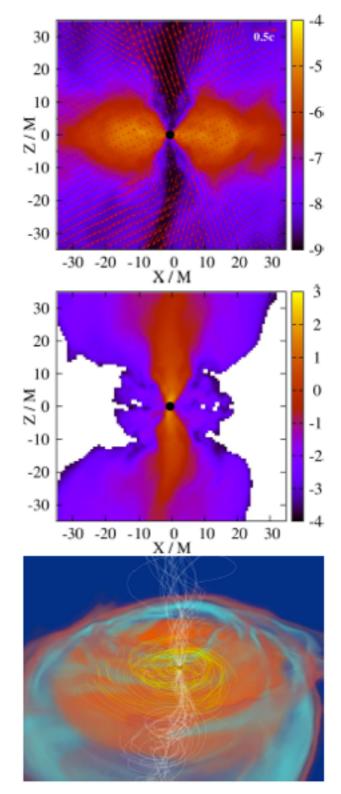


Magnetic fields - Jets?

- Dynamically not important before merger
 - EM precursors?
- Critical post-merger (MRI, jets, winds)
- Hard to resolve numerically



Rezzolla et al. 2011

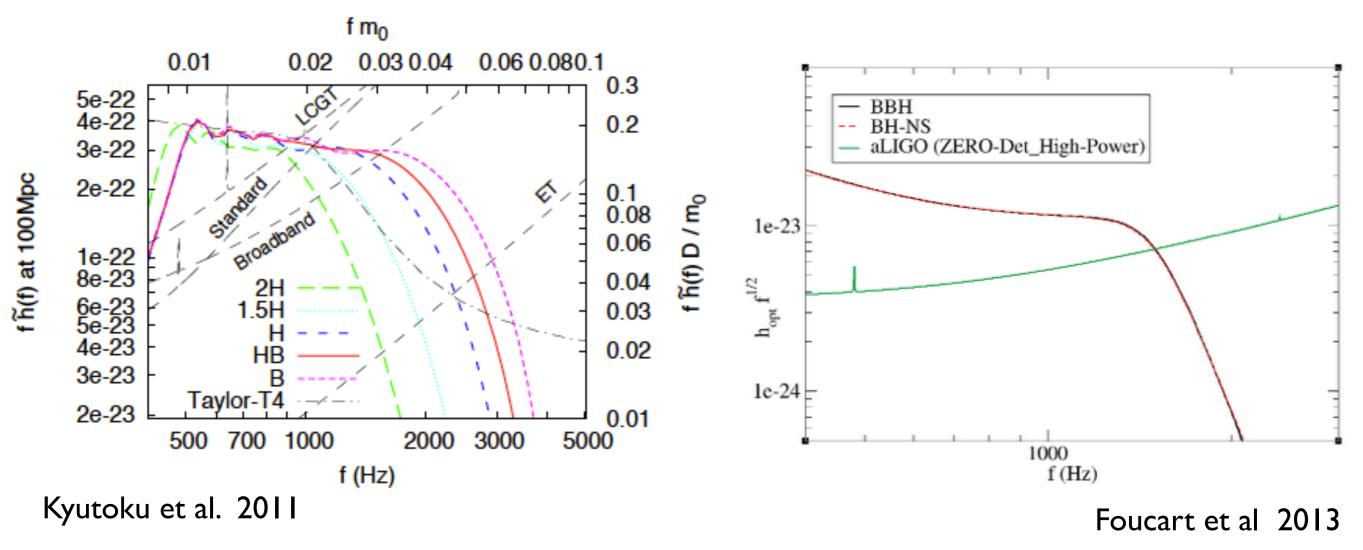


Etienne et al 2012

Gravitational Waves

GW signal - low mass

GW signal - high mass



Finite size effects matter for low mass systems / high spins
Weak effects for "typical" NS-BH system

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Neutrino Treatment

- Leakage (Deaton et al. 2013, Foucart et al. 2014)
 - Cooling only, possibly ad-hoc heating
- Moment Scheme (from Shibata et al. 2011)
 - Closure, Crossing beams, Stiff equations
- Radiation Transport
 - Very expensive...

Moment Formalism

 $T^{\mu\nu} = E n^{\mu} n^{\nu} + F^{\mu} n^{\nu} + F^{\nu} n^{\mu} + P^{\mu\nu}$

$$\begin{aligned} \partial_t \tilde{E} &+ \partial_j (\alpha \tilde{F}^j - \beta^j \tilde{E}) \\ &= \alpha (\tilde{P}^{ij} K_{ij} - \tilde{F}^j \partial_j \ln \alpha - \tilde{S}^\alpha n_\alpha) \\ \partial_t \tilde{F}_i &+ \partial_j (\alpha \tilde{P}_i^j - \beta^j \tilde{F}_i) \\ &= (-\tilde{E} \partial_i \alpha + \tilde{F}_k \partial_i \beta^k + \frac{\alpha}{2} \tilde{P}^{jk} \partial_i \gamma_{jk} + \alpha \tilde{S}^\alpha \gamma_{i\alpha} \end{aligned}$$

$$\tilde{S}^{\alpha} = \sqrt{\gamma} \left(\eta u^{\alpha} - \kappa_a J u^{\alpha} - (\kappa_a + \kappa_s) H^{\alpha} \right)$$

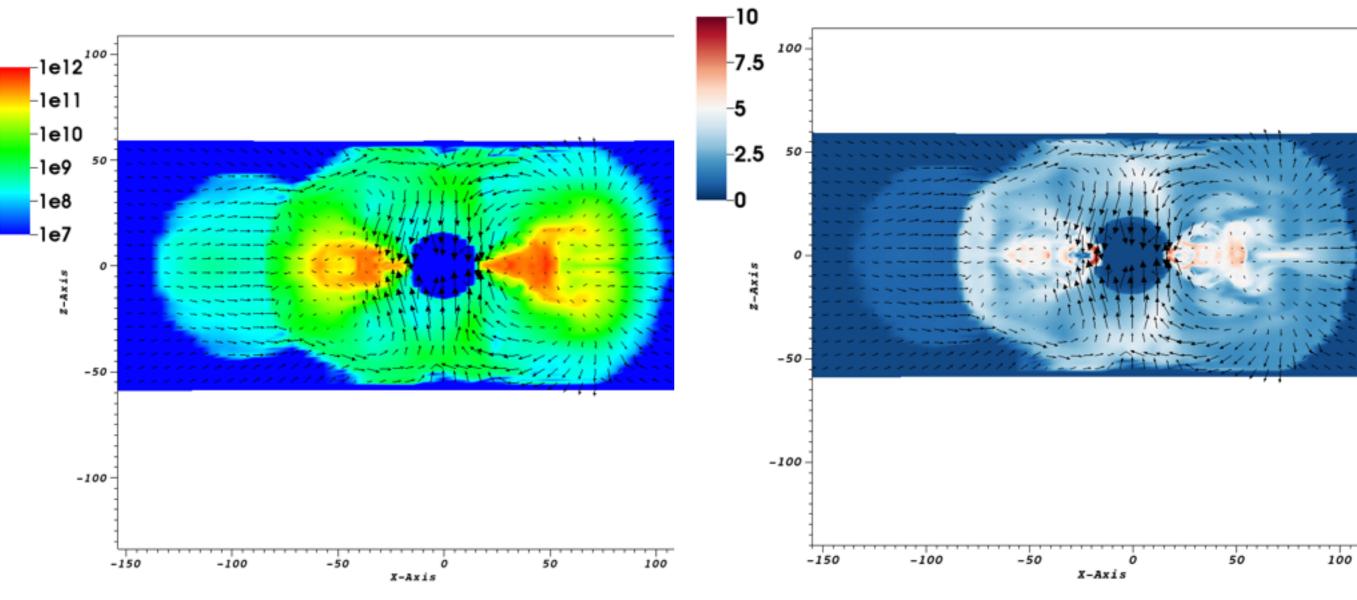
$$P^{ij} = \frac{3\chi(\zeta) - 1}{2} P^{ij}_{\text{thin}} + \frac{3(1 - \chi(\zeta))}{2} P^{ij}_{\text{thick}}$$

- Issues:
 - Closure!
 - Grey approx.
 - Stiff terms

MI Results

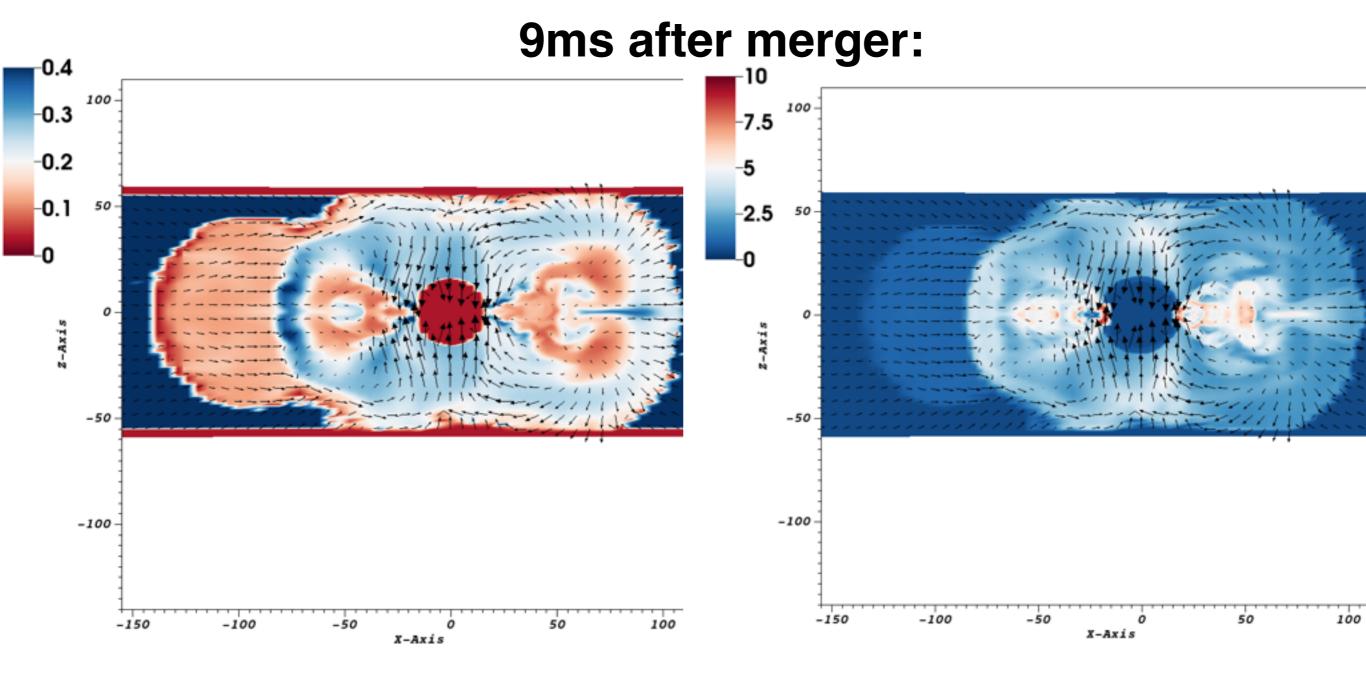
• Global properties similar to leakage results



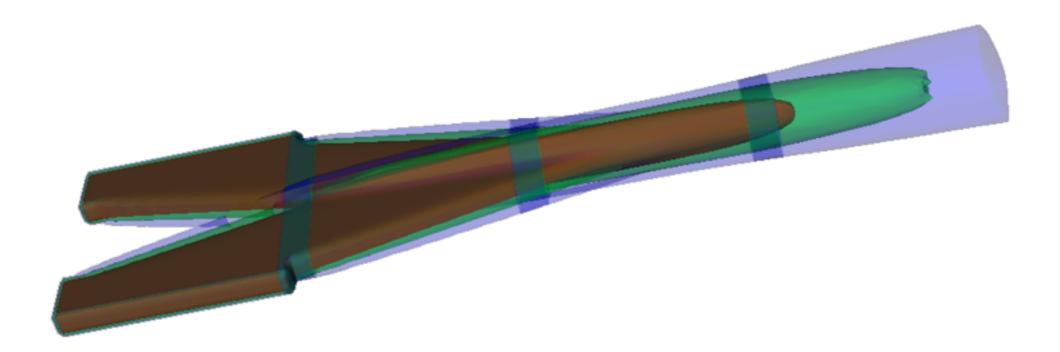


MI Results

• Global properties similar to leakage results



MI Problems



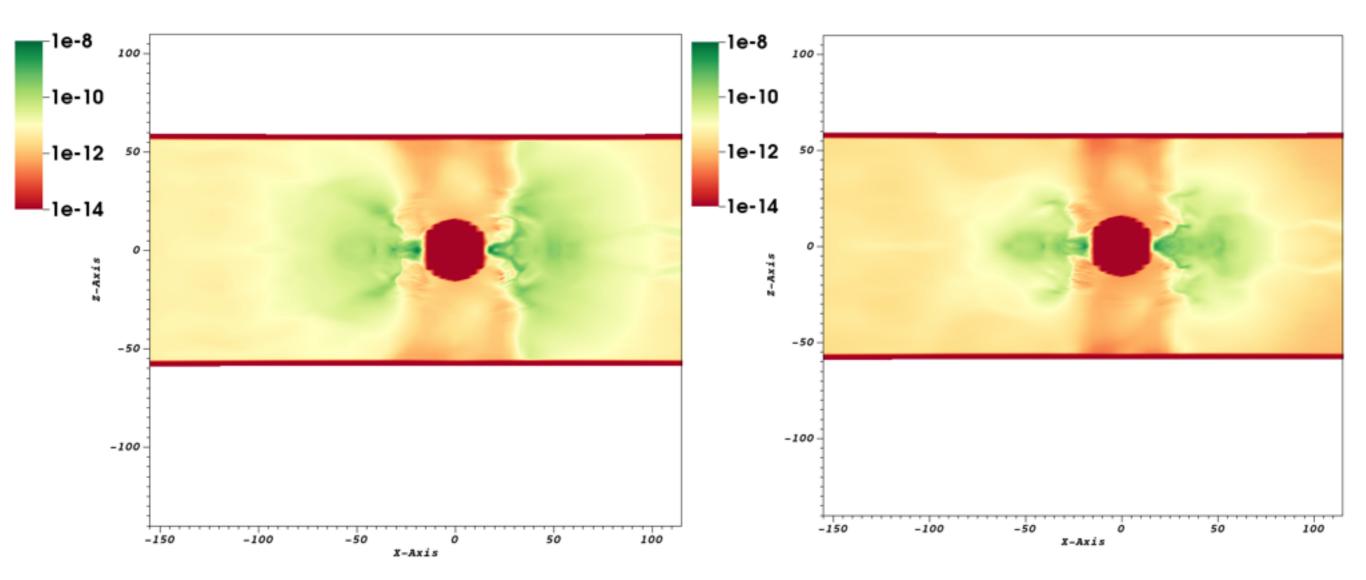
Can't handle crossing beams!

MI Results

9ms after merger:

Antineutrinos

Neutrinos



Conclusions

- Can predict disruption / global properties
- GW not as promising as BNS
 - Work still necessary on modeling
- Improved microphysics
 - Can we get a jet?
 - Neutrino energy deposition?
 - Wind & Composition?