

Astrophysical Implications of the Symmetry Energy

Ken'ichiro Nakazato

(Tokyo University of Science)



"Science with S π RIT TPC" workshop @ RIKEN, Jun. 5, 2015

Topics

Supernova explosion

Sumiyoshi-san's talk



Hot (proto-)neutron star



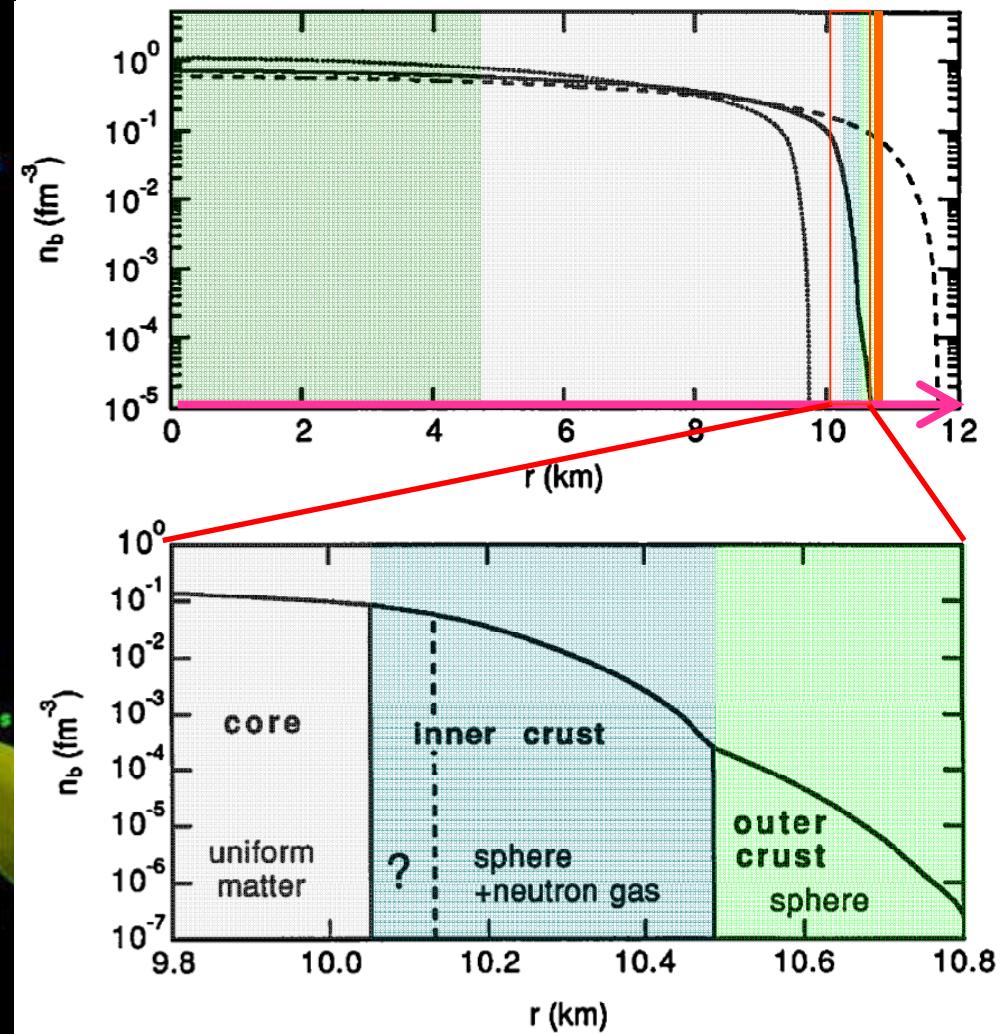
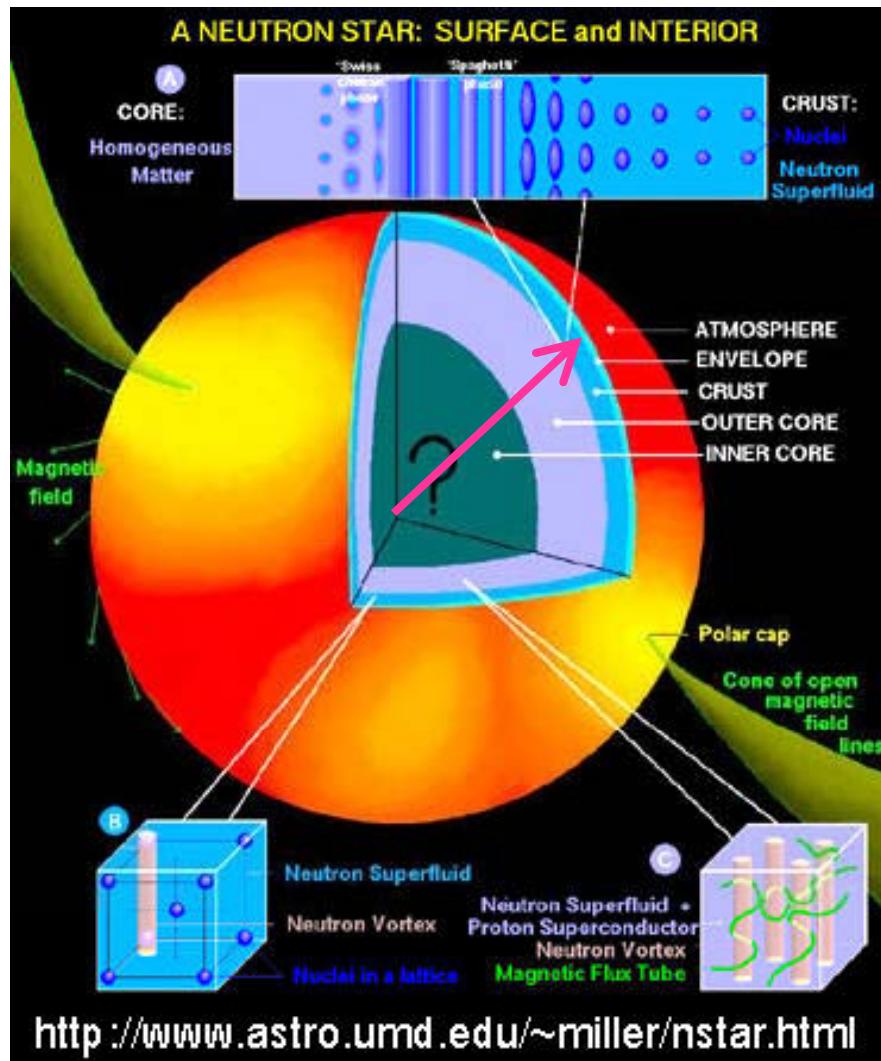
Neutron star

my topics



Interior of neutron stars

- Core (“packed” nuclear matter) + Crust(skin)



Neutron stars and EOS

- Structure of neutron stars (spherical case)
 - TOV equation (balance of gravity and pressure)

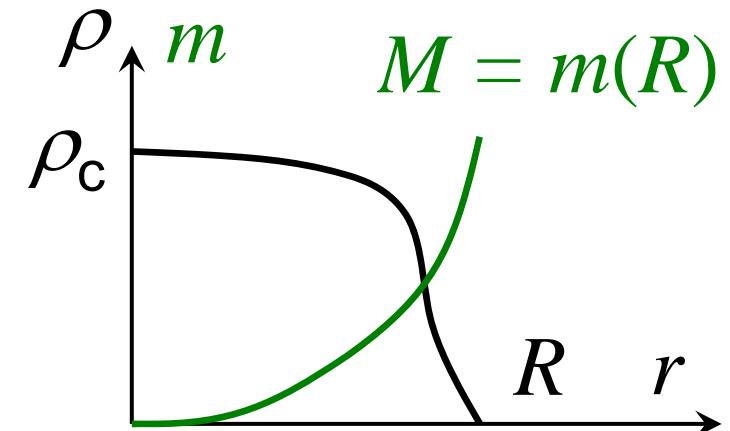
$$\frac{dP(r)}{dr} = -\frac{G \left\{ m(r) + 4\pi r^3 P(r)/c^2 \right\} \varepsilon(r) + P(r)}{r^2 \left\{ 1 - 2Gm(r)/rc^2 \right\} c^2}$$

- Equation of state (EOS)

$$P = P(\rho)$$

- Boundary conditions

$$\begin{cases} m(r) = 0 @ r = 0 \\ \text{central density } \rho_c \end{cases}$$



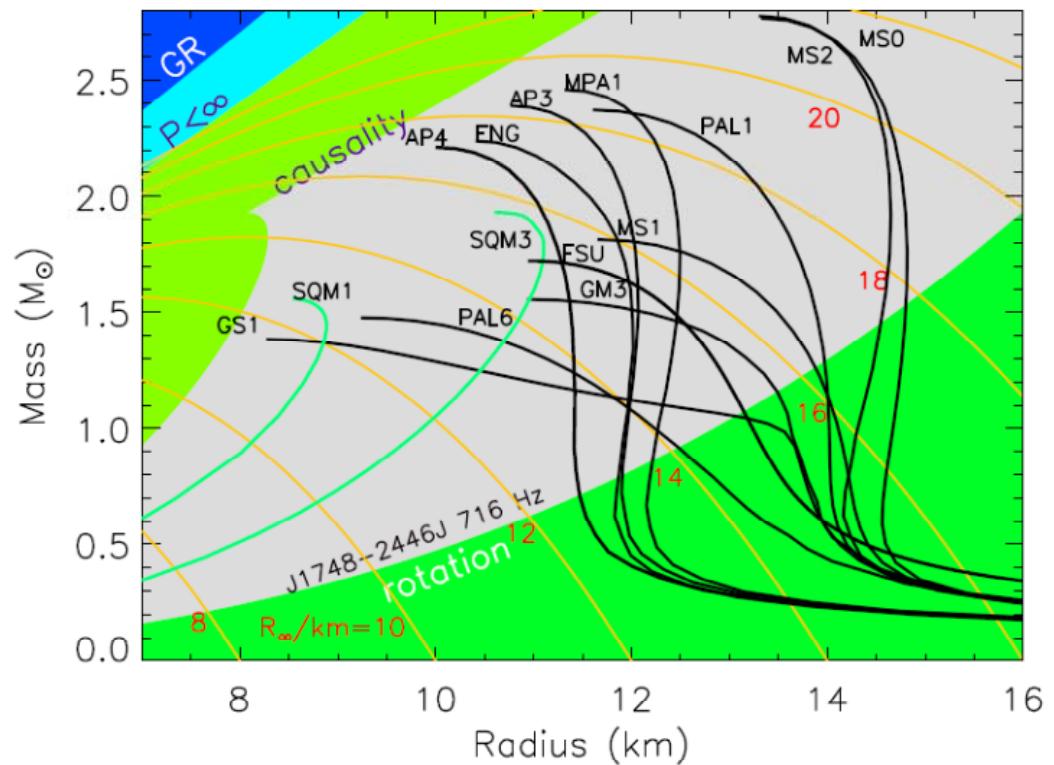
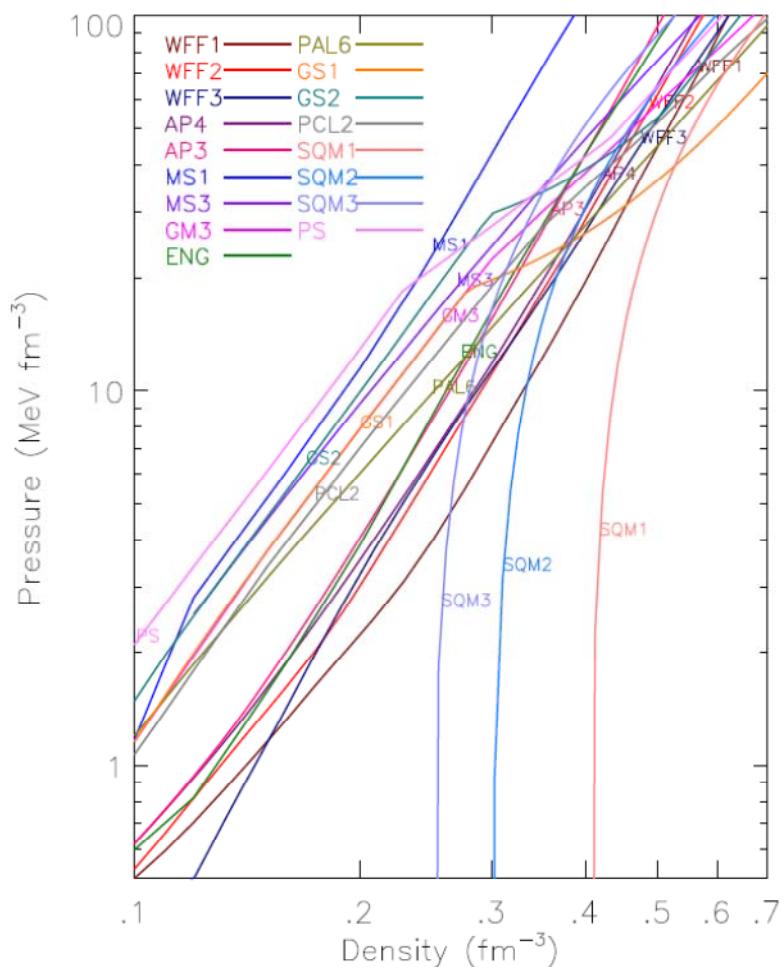
$$\begin{cases} \rho(R) = 0 \text{ at surface} \\ \text{radius } R, \text{ mass } M = m(R) \end{cases}$$

EOS determines M - R relation

equation of state

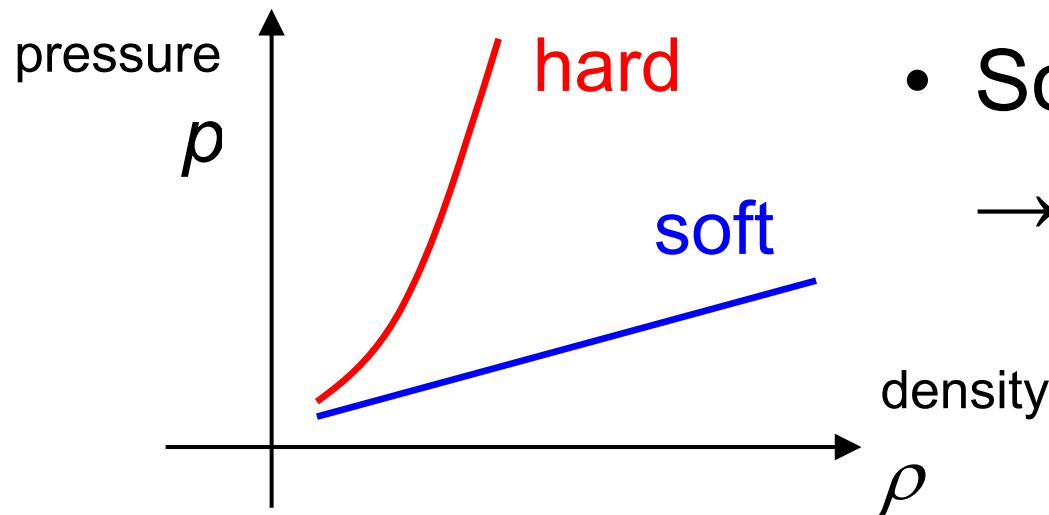


mass-radius relation
(M - R)



(Lattimer 2012)

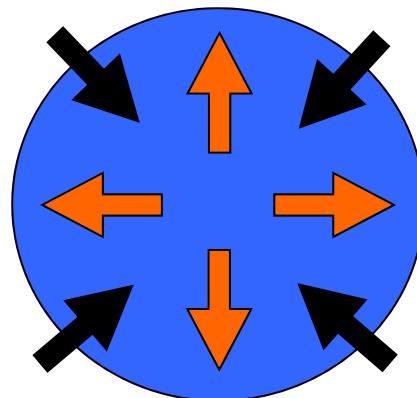
EOS and NS maximum mass



- Soft = compressible
→ easy to raise density

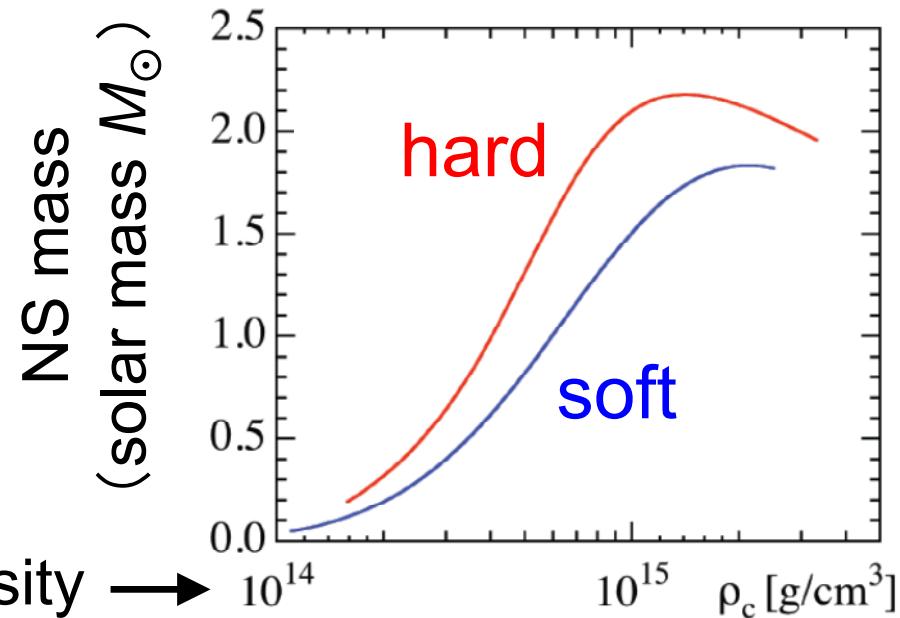


- Hard EOS have high NS maximum mass



gravity
nuclear force
(repulsion)

central density →

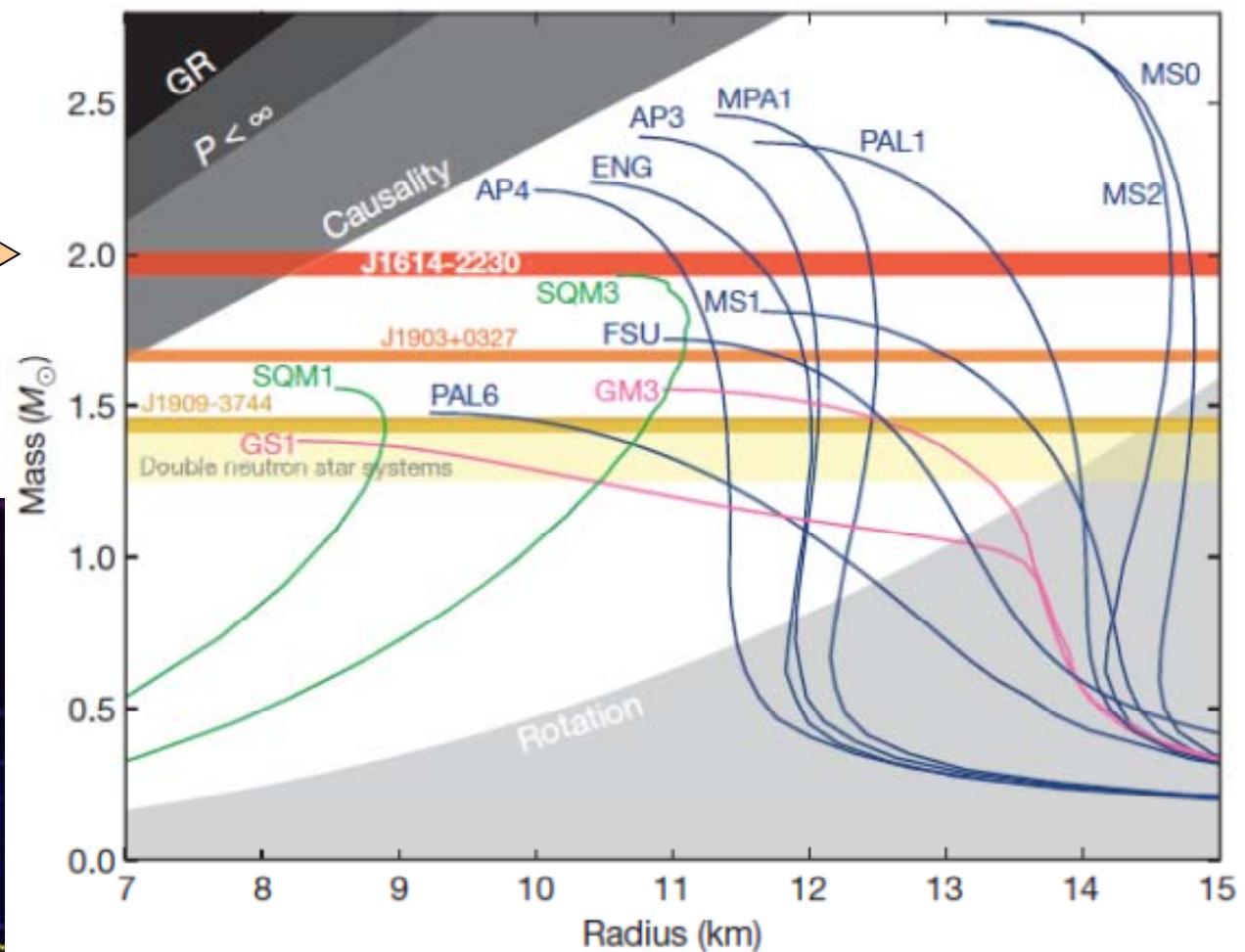
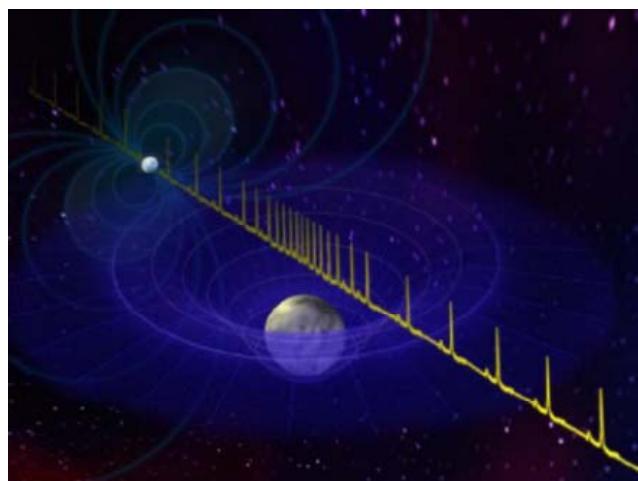


Discovery of $2M_{\odot}$ neutron star

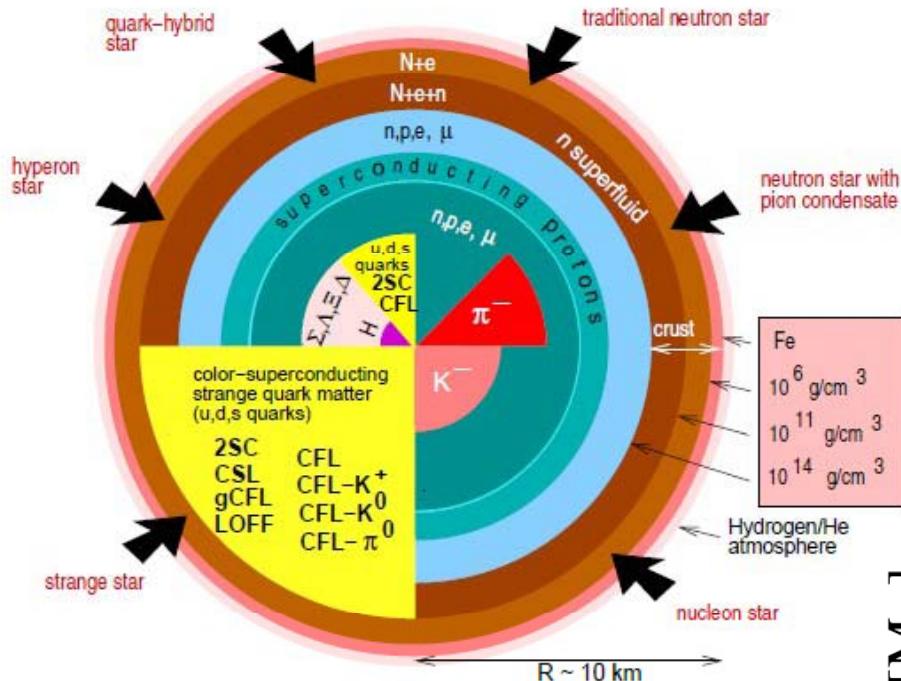
- Pulsar J1614-2230 puts a tight constraint on EOS!

Demorest et al., Nature 467 (2010) 1081

Shapiro delay



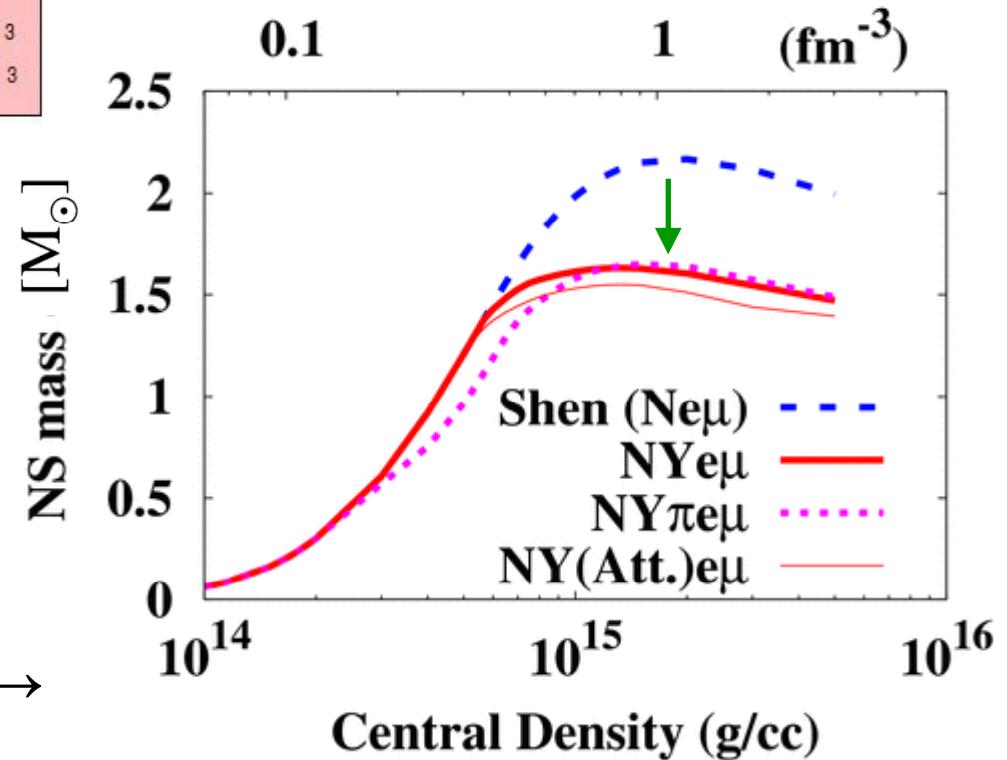
Most of NS mass is core



effects of hyperon and/or pion inclusion

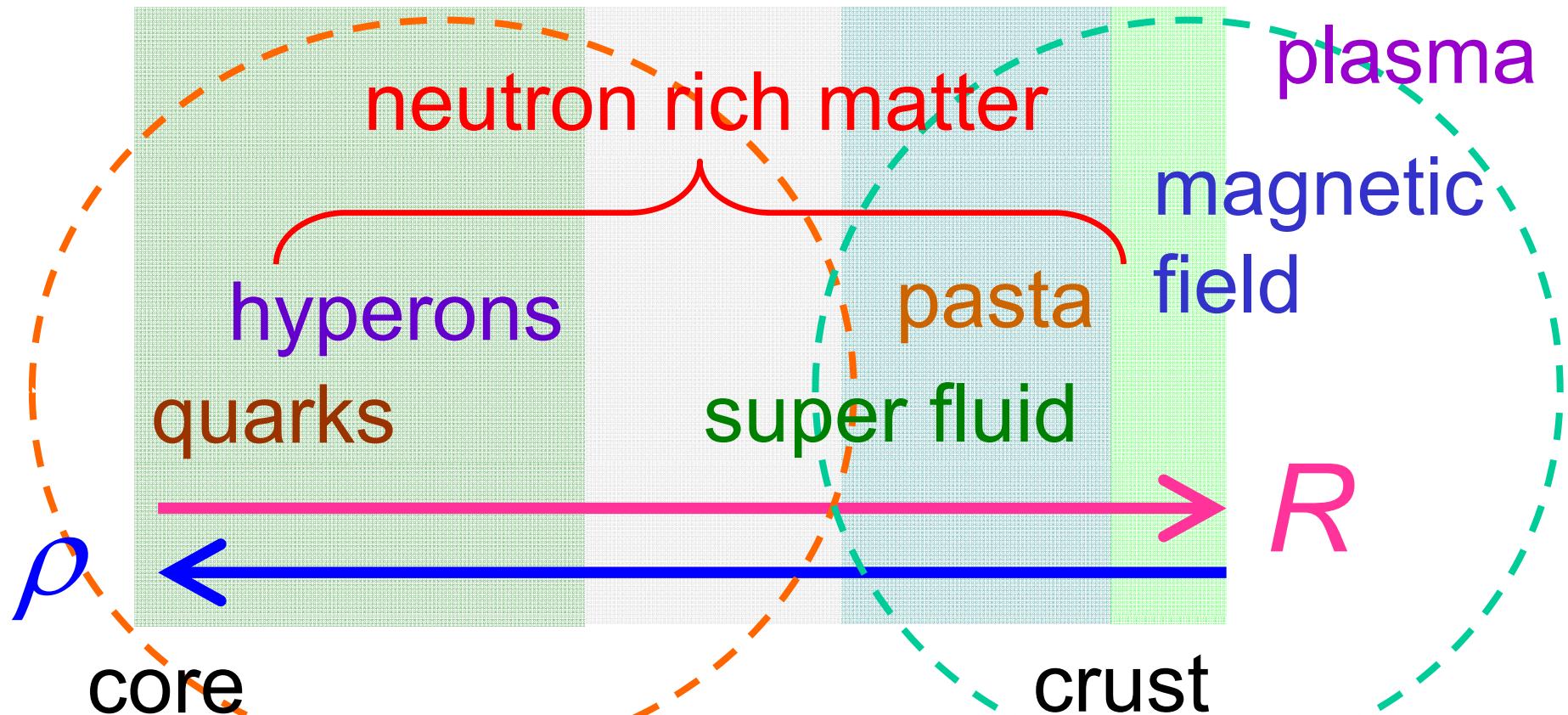
Ishizuka et al. (2008) →

- Not only new degrees of freedom, but also supra-nuclear density EOS are important!



Physics in neutron stars

Symmetry Energy!!

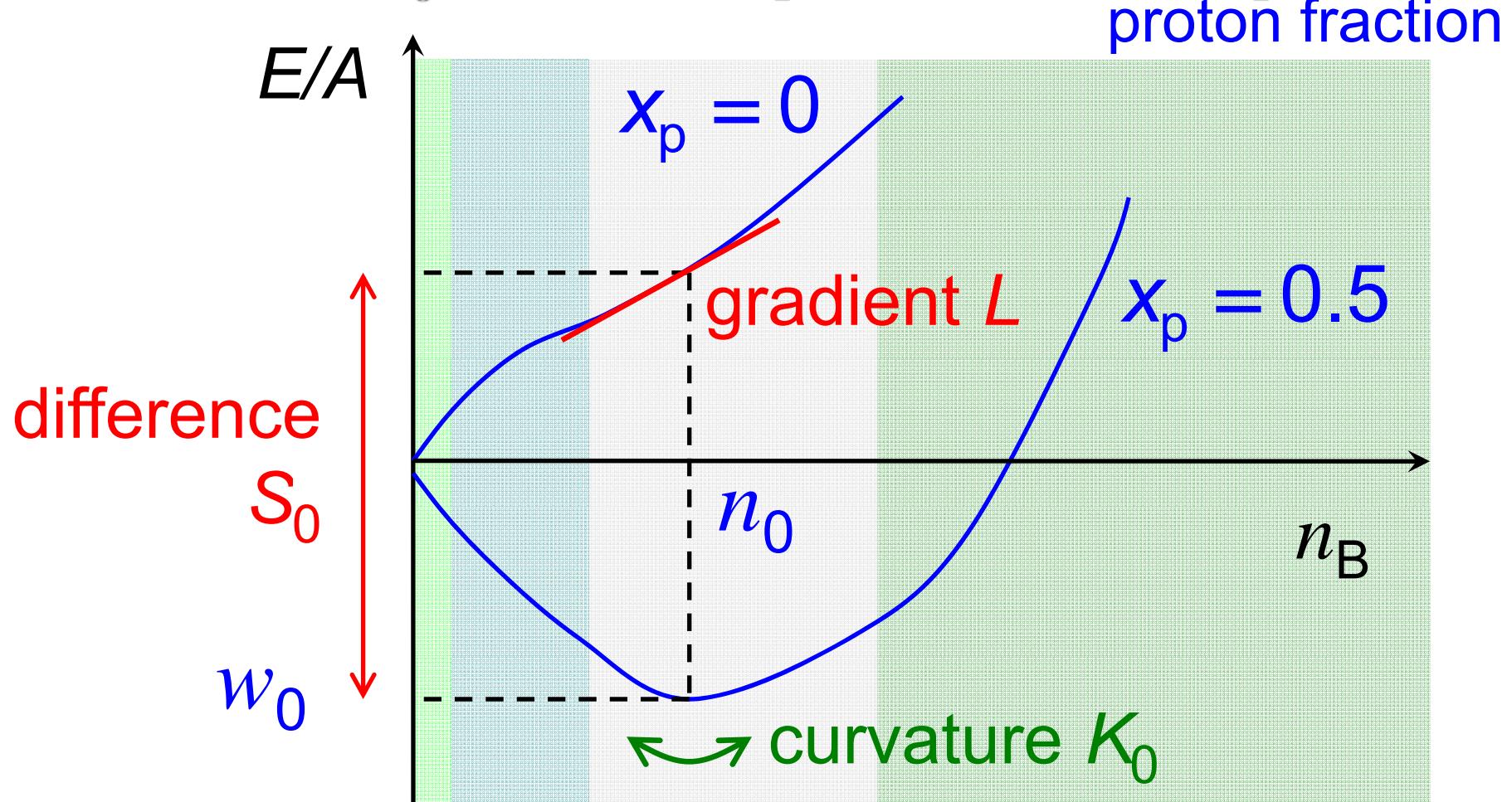


determine M and R important for emission

EOS and saturation parameters

- Saturation parameters characterize EOS.

$$w = w_0 + \frac{K_0}{18n_0^2}(n - n_0)^2 + \left[S_0 + \frac{L}{3n_0}(n - n_0) \right] (1 - 2\underline{x}_p)^2$$



Values of saturation parameters

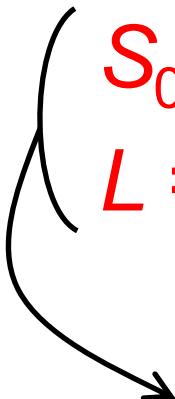
$$n_0 = 0.15 - 0.16 \text{ fm}^{-3}$$

$$w_0 \sim -16 \text{ MeV}$$

$$K_0 = 230 - 250 \text{ MeV} \text{ (Piekarewicz 2010)}$$

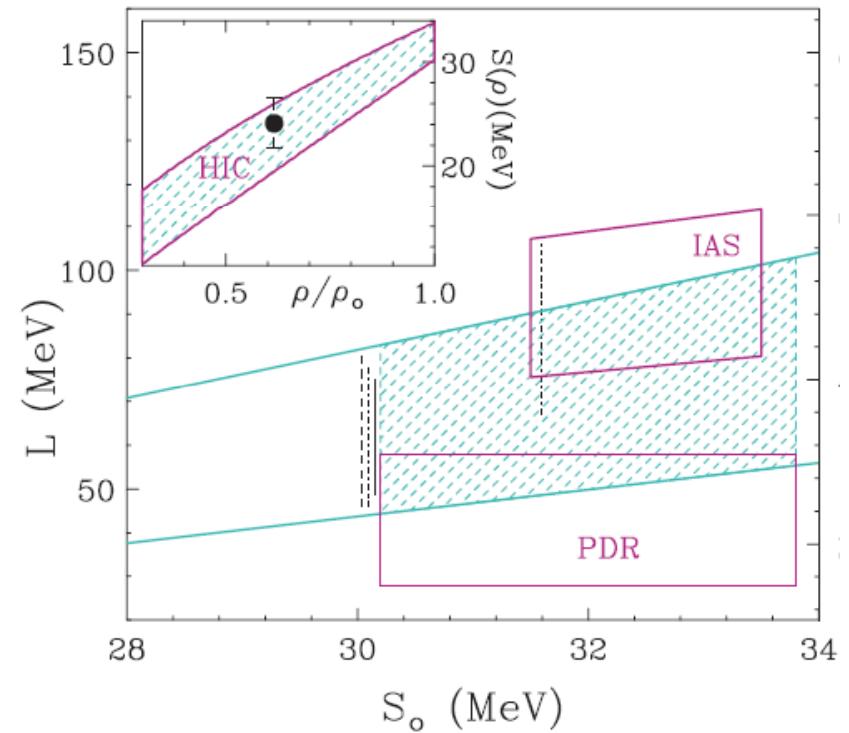
$$S_0 = 30 - 34 \text{ MeV} \text{ (Tsang et al. 2009)}$$

$$L = 20 - 100 \text{ MeV} ? ? ?$$



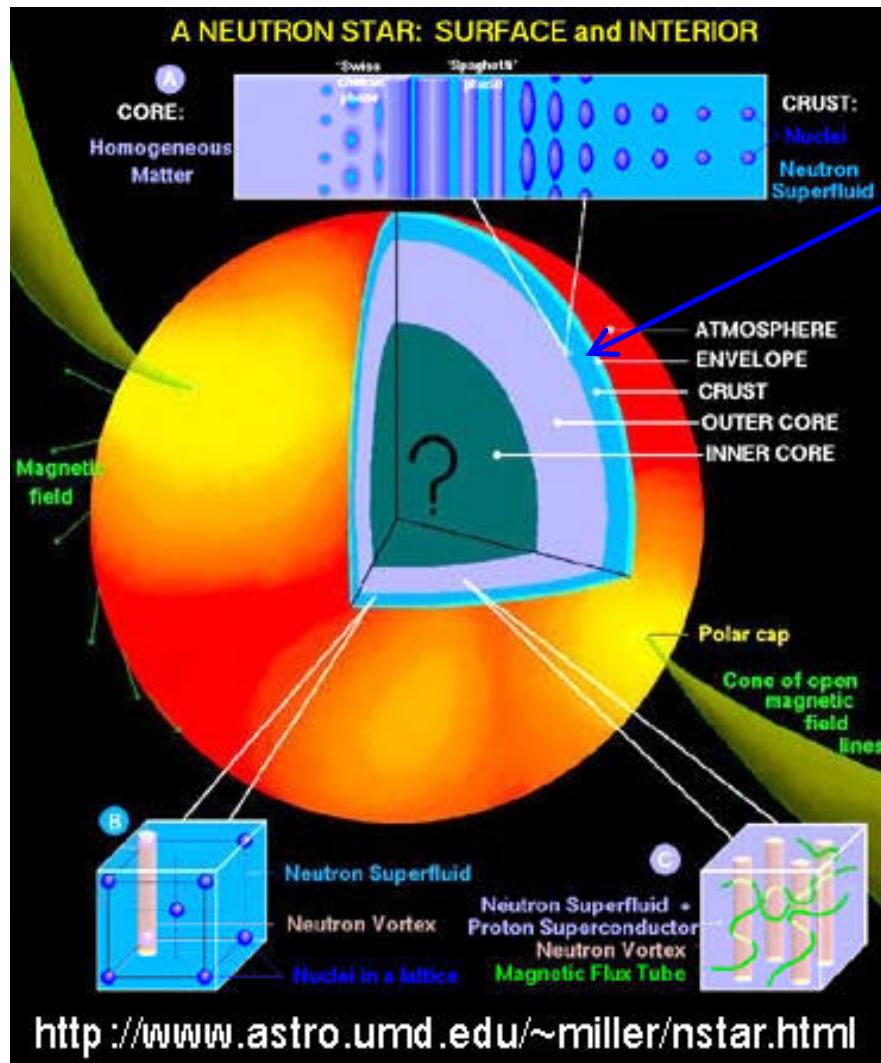
related to
symmetry energy!!

→ Are important for
neutron stars?

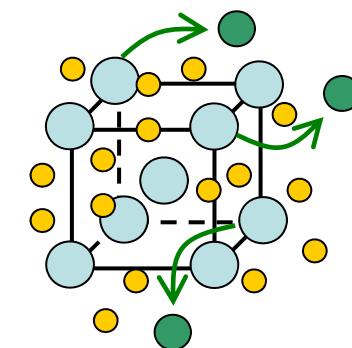


Neutron star crust

- Crystalline structure of nuclei



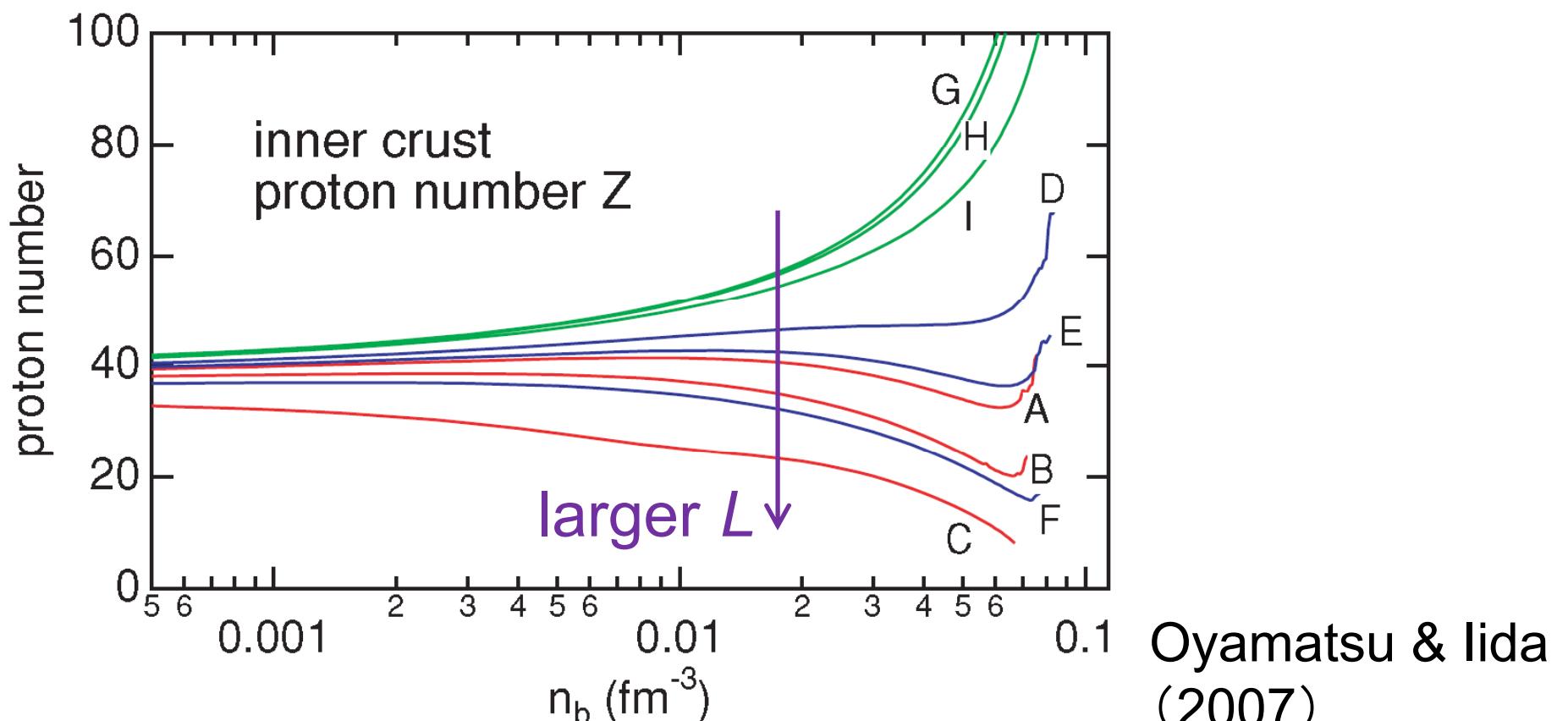
crust



- nuclei
- electrons
- dripped neutrons

Crust nuclei and L parameter

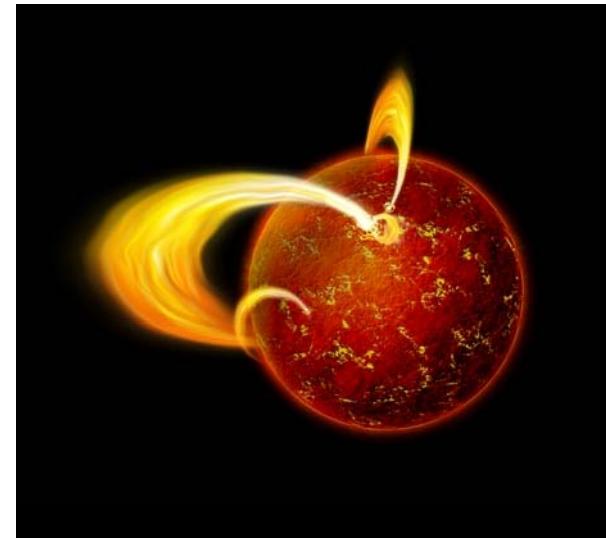
- Proton number of crust nuclei depends on L .



Proton number is small, if L is large.

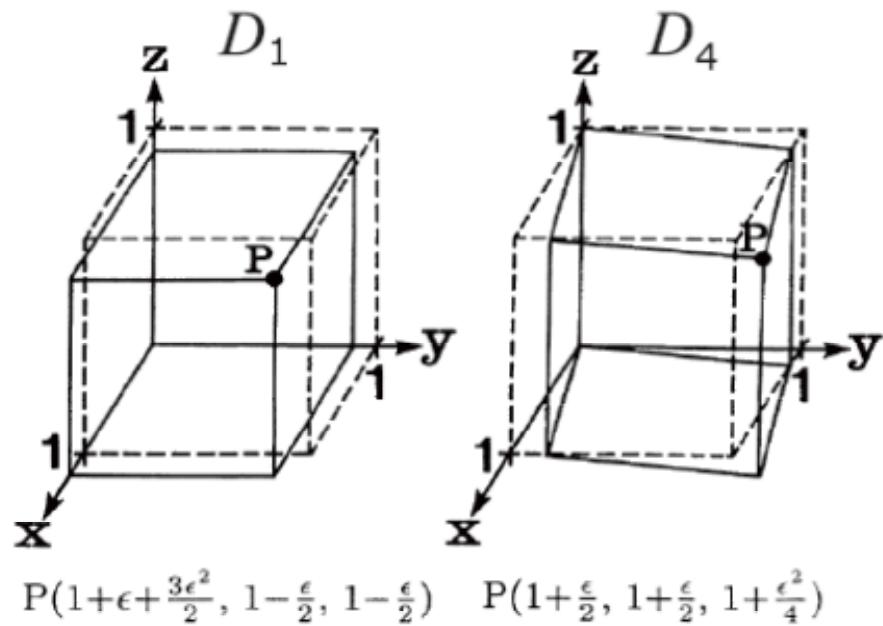
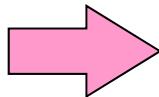
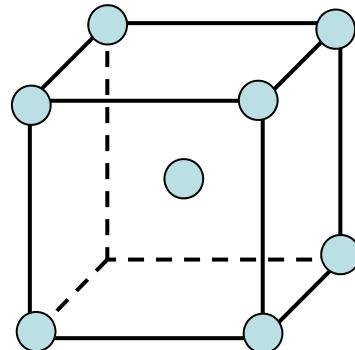
Giant flare and QPO of SGR

- Soft gamma-ray repeater (SGR)
 - Neutron stars with high magnetic field ($>10^{14}$ G)
- 3 giant flares are detected from SGRs.
 - SGR 0526–66 (1979)
 - SGR 1900+14 (1998)
 - SGR 1806–20 (2004)
- Quasi periodic oscillation (QPO) is discovered in a decaying tail of giant flare.
(SGR 1806–20)



Origin of QPOs

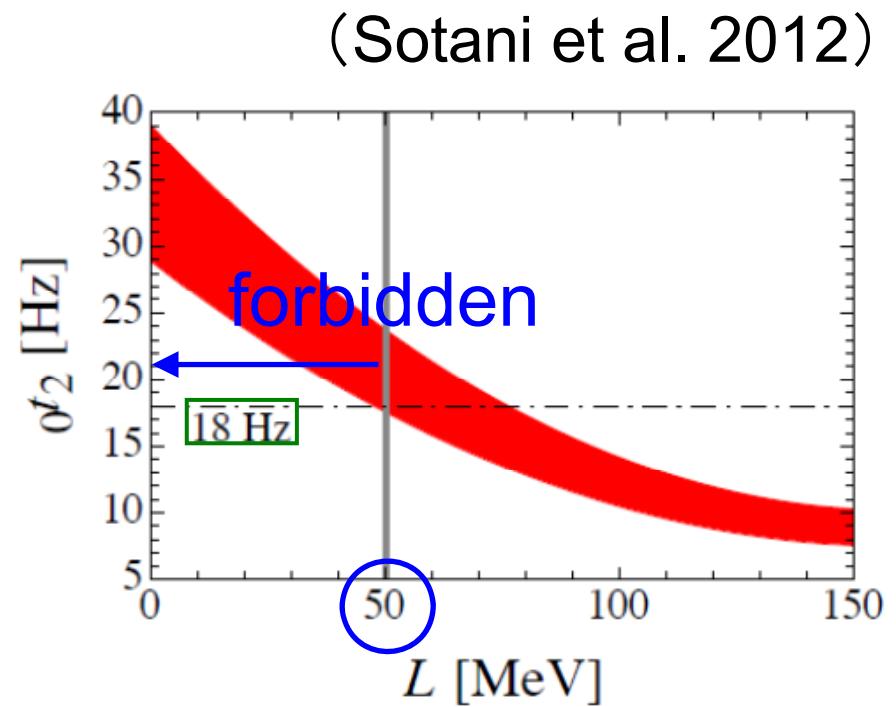
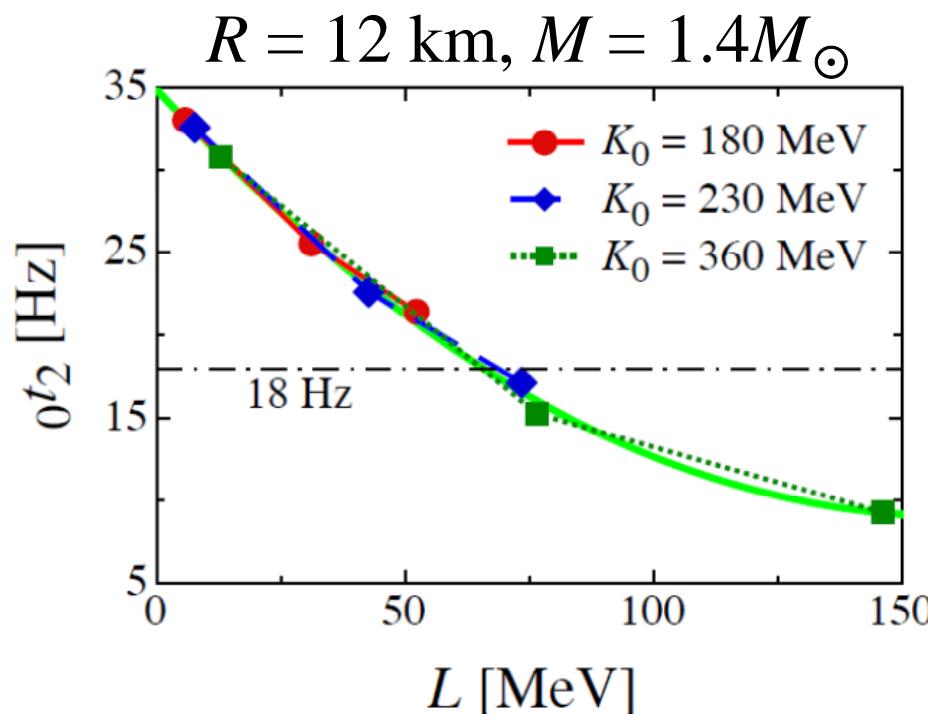
- Crustal shear mode
 - Note: other hypotheses also exist
- The oscillation frequency of Coulomb lattice depends on proton number
→ **depends on L !!**



(Ogata and Ichimaru 1990)

Constraint on L parameter

- General relativistic perturbative calculation to find eigenfrequencies for various L .
- To reproduce 18 Hz (lowest frequency) QPO, $L > 50$ MeV.

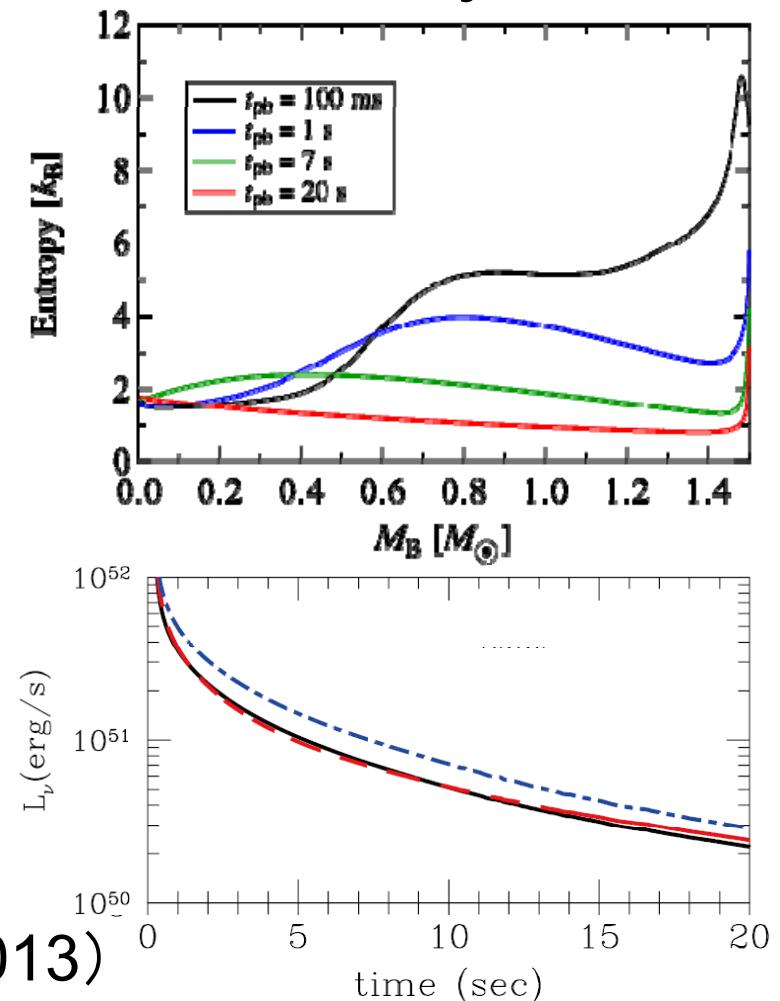


Hot (proto-)neutron stars

- Nascent hot neutron star (proto-neutron star : PNS) just after supernova is cooled by neutrino emission.
- Neutrino-nucleus scattering cross section depends on the mass number

$$\sigma \propto A^2$$

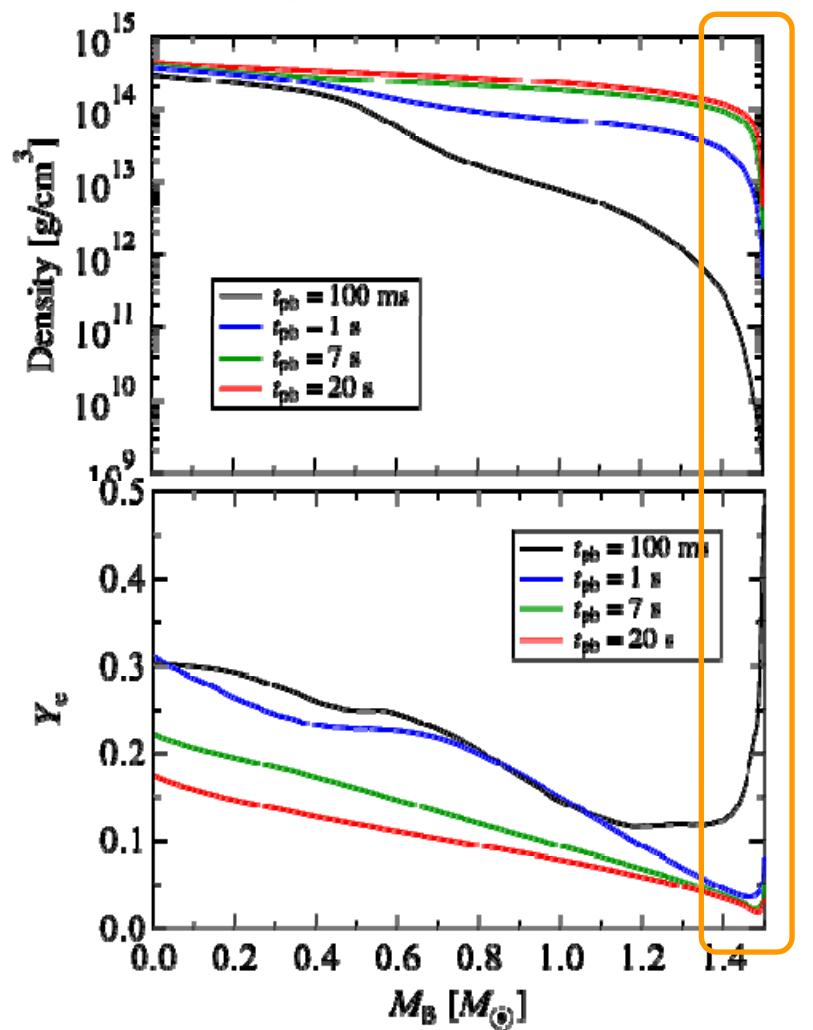
→ depends on L !?



(Nakazato et al. 2013)

Nuclei in proto-neutron stars

- Inhomogeneous phase will appear during the proto-neutron star (PNS) cooling.



→ Nucleation

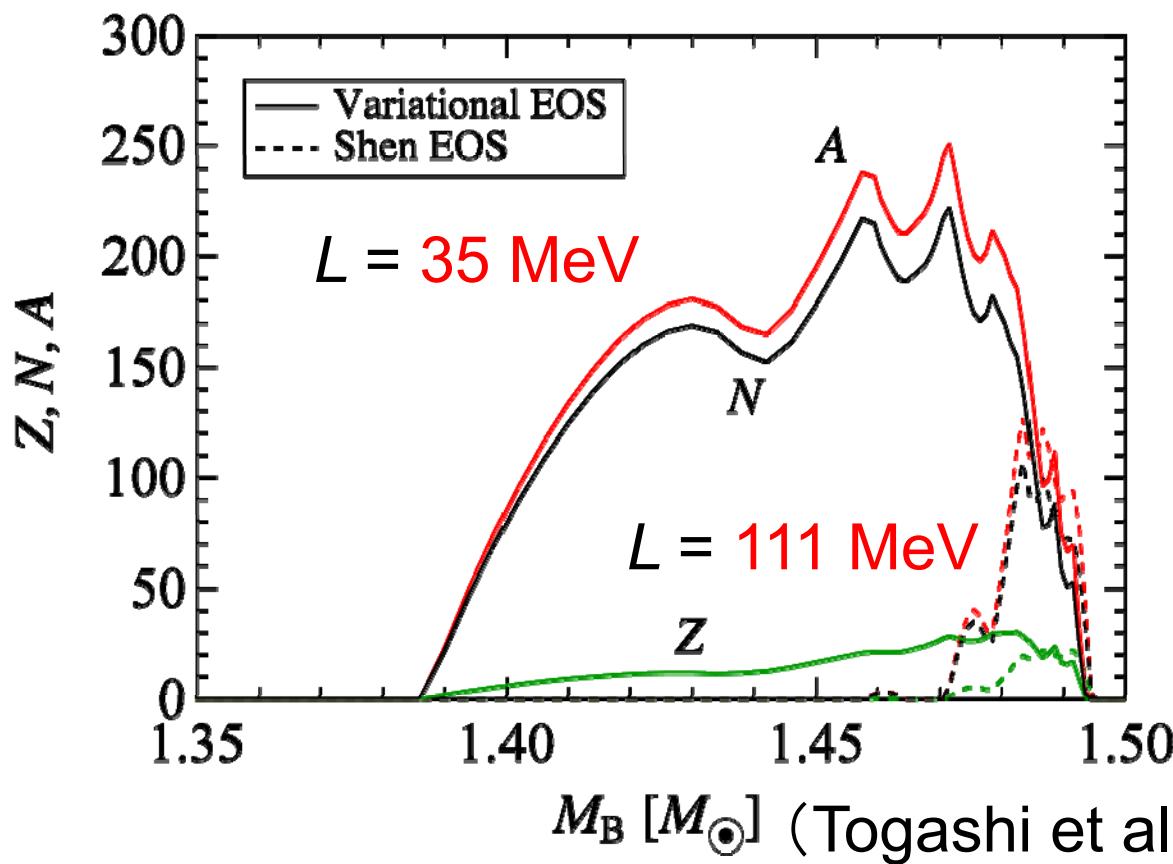
near the surface,
low density and
neutron rich



transition to
inhomogeneous
phase (proto-crust)

Size of nuclei in PNS

- Comparing two EOS's with different L .
 - variational method (Togashi et al. in prep.), $L = 35 \text{ MeV}$
 - relativistic mean field (Shen et al. 1998), $L = 111 \text{ MeV}$



Inhomogeneous phase is wide & mass number is large for small L .

↓
crucial for ν
(future work!)

Summary

- Symmetry energy is important for astrophysics.
- Supra-nuclear density EOS is crucial for $M-R$ relation of neutron stars, as well as exotic components (hyperons, quarks etc.).
- Symmetry energy is characterized by S_0 and L .
- L determines nuclear size in inhomogeneous phase of neutron stars and proto-neutron stars.
 - $L > 50$ MeV according to crust oscillation
 - cooling by neutrinos will be affected by L