Pion Production in Heavy-Ion Collisions

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Interest: π as Probe of High- ρ Symmetry Energy B-A Li PRL88(02)192701: $S(\rho > \rho_0) \Rightarrow n/p_{\rho > \rho_0} \Rightarrow \pi^-/\pi^+$



Simulations of Heavy-Ion Collisions

Separation of time and distance scales:

- Short scales reduced to negligible extent with outcomes of events treated probabilistically
- Long scales treated explicitly and deterministically
- Cut-off scales: $t \sim 1 \text{ fm}/c$, $r \lesssim 1 \text{ fm}$
- Primarily binary collision processes

Equation of state: if there is an optical potential affecting a particle, that particle impacts the interaction parts of thermodynamic functions.

Low-*E* pion production: $N + N \leftrightarrow N + \Delta$, $\Delta \longleftrightarrow N + \pi$



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Δ in π –*N* Interactions

π –*p* scattering cross sections



$$\sigma = \frac{4\pi}{p^2} \frac{2J+1}{2s+1} \frac{\Gamma^2/4}{(E-m_\Delta c^2)^2 + \Gamma^2/4}$$

 $J=3/2,\,m_{\Delta}=1232\,\text{MeV}/c^2,\,\Gamma(p)\propto p^3$



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π Production

Inelastic NN Interactions

Decomposition of inelastic *NN* cross section Weil *et al* EPJA48(12)111





Charged- π Yields, Theory & Expt

Production and Absorption: Detailed Balance

Time reversal symmetry: same magnitude of mtx element for forward & backward process,

$$|\mathcal{M}_{NN\to N\Delta}| = |\mathcal{M}_{N\Delta\to NN}|.$$

$$\frac{\mathrm{d}N_{\Delta}}{\mathrm{d}t} \propto \int \mathrm{d}\boldsymbol{p} \, \delta(\boldsymbol{p}_{N} + \boldsymbol{p}_{\Delta} - \boldsymbol{p}_{N} - \boldsymbol{p}_{N}) \\ \times \, \delta(\epsilon_{N} + \epsilon_{\Delta} - \epsilon_{N} - \epsilon_{N}) \\ \times \, |\mathcal{M}_{NN \to N\Delta}|^{2} \left(f_{N} f_{N} - f_{N} f_{\Delta}\right)$$

in equilibrium: $f = e^{(\mu - \epsilon)/T}$

$$\sigma \mathbf{v} \propto \int \mathrm{d} \boldsymbol{p} \, \delta(\boldsymbol{E} - \boldsymbol{E}) \, |\mathcal{M}|^2$$

Detailed-balance relation: $\sigma_{NN \to N\Delta} \Leftrightarrow \sigma_{N\Delta \to NN}$ Relation nontrivial for Δ due to mass spread.

Balance violated: no thermal distribution, no law of mass action





Charged- π Yields, Theory & Expt

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$$egin{aligned} rac{\mathrm{d}m{N}_\Delta}{\mathrm{d}t} &\propto \int \mathrm{d}m{p}\,\delta(m{p}_N+m{p}_\Delta-m{p}_N-m{p}_N)\ & imes\,\delta(\epsilon_N+\epsilon_\Delta-\epsilon_N-\epsilon_N)\ & imes\,|\mathcal{M}_{NN o N\Delta}|^2\left(f_N\,f_N-f_N\,f_\Delta
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Charged-*π* Yields, Theory & Expt

Conclusions

Δ Decay Time

Ambiguity in deciding on time of π production



PD&Pratt PRC53(96)249

Different perspectives yield different Δ lifetimes

 $\Delta \tau$ consistent with thermal equilibrium most often used, but it yields unphysically long-lived Δ close to threshold.

 \Rightarrow Need to transition to direct 3-ptcle production?



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π vs Baryon Optical Potentials

$$\Delta \longleftrightarrow N + \pi$$
 $U_{\Delta} \stackrel{?}{=} U_N + U_{\pi}$

'Conservation' of potential consistent with the quark perspective. Also also greatly facilitates calculations of process kinematics as thresholds in kinetic energy stay put.

Ferini *et al* NPA762(05)147: $U_{\pi} = 0 \& U_{\Delta} = U_N$ employed in most models, including IBUU.

However, a strong isospin-dependent potential is needed to explain the existence of pionic atoms!

pBUU: *U* dependent on conserved quantities, density of baryon number and isospin - π end up with potentials that depend on isospin & symmetry energy



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Symmetry-Energy Derived π Potential





Technical Differences between Calculations





Pions Probe System at High- ρ !



 π test the maximal densities reached and collective motion then



Pions as Probe of High- ρ Symmetry Energy B-A Li PRL88(02)192701: $S(\rho > \rho_0) \Rightarrow n/\rho_{\rho > \rho_0} \Rightarrow \pi^-/\pi^+$



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Dedicated Experimental Efforts

SAMURAI-TPC Collaboration (8 countries and 43 researchers): comparisons of near-threshold π^- and π^+ and also *n-p* spectra and flows at RIKEN, Japan. NSCL/MSU, Texas A&M U Western Michigan U, U of Notre Dame GSI, Daresbury Lab, INFN/LNS U of Budapest, SUBATECH, GANIL China IAE, Brazil, RIKEN, Rikkyo U Tohoku U, Kyoto U

AT-TPC Collaboration (US & France)





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Interpretation of FOPI Data

Reisdorf et al NPA781(07)459



Transport IBUU04 Xiao et al PRL102(09)062502

Symmetry energy dropping with ρ , at $\rho > \rho_0$!?



Net π Yields and $U(\rho, \rho)$ in pBUU Reisdorf *et al* NPA781(07)459



Jun Hong & PD PRC90(14)024605, π^- and π^+

?Imperfect Mom Dependence?? [No sensitivity to π/Δ rates] affects maximal densities reached



π Yields Reproduced with Softened U(p)



 π Production

Inferior Description of Midrapidity Flow Anisotropy



solid: new U(p), dashed: old U(p)

Jun Hong & PD PRC90(14)024605

 $R_N \leftrightarrow$ elliptic flow

too weak with new U(p



FOPI π^-/π^+ Reproduced by pBUU

... irrespectively of U(p), right panel



Left panel: discrepancies in the literature - correlation vs anticorrelation of $S(\rho > \rho_0)$ with π^-/π^+ .



π Production

FOPI π^-/π^+ Reproduced by pBUU ... irrespectively of $S_{int}(\rho) = S_0 (\rho/\rho_0)^{\gamma}$:





 π Production

Original Idea Still Correct for High- $E \pi$'s



$$S_{
m int}(
ho) = S_0 \, (
ho/
ho_0)^\gamma$$

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n/p Ratio in pBUU at $\rho > \rho_0$

changes with the supranormal symmetry energy:



$$S_{\text{int}}(
ho) = S_0 \left(
ho /
ho_0
ight)^2$$



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Why Differences for Net π Ratios?

In pBUU isospin-driven π^{\pm} optical potential



 π/Δ rate sensitivities claimed in Larionov&Mosel NPA728(03)135; Prassa *et al* NPA789(07)311 and Song&Ko PRC91(15)014901. Virtually none there in pBUU



Energy Conservation?

Cozma arXiv:1409.3110 claims that relative π yields are highly sensitive to the manner in which energy conservation is imposed on individual collisions in case of mo-dependent mean fields.

Problem: Detailed balance relations not considered.

$$\sigma \mathbf{v} \propto \int \mathrm{d} \boldsymbol{p} \, \delta(\boldsymbol{E} - \boldsymbol{E}) \, |\mathcal{M}|^2$$

 $\sigma_{NN\to N\Delta} \Leftrightarrow \sigma_{N\Delta\to NN}$

Relative yields for different energy conservations:



- Pions probe high-ρ matter, net density, n/p-ratio, collective flow there! ... U(p)
- Uncertainties in the near-threshold π production: Δ lifetime, $\pi \& \Delta$ optical potentials, in-medium rates.
- pBUU reproduces FOPI π^-/π^+ , irrespectively of details in *U* and *S*.
- High-energy π^+/π^- ratio more robust than ratio of net yields. Sensitivity to the dependence of effective masses on isospin?
- Azimuthal dependence of π^+/π^- ratio?

Acknowledgement: US Natl Science Foundation



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