

Lattice simulations of technicolour theories  
with adjoint fermions and supersymmetric Yang-Mills theory  
– the conformal window for adjoint fermions –

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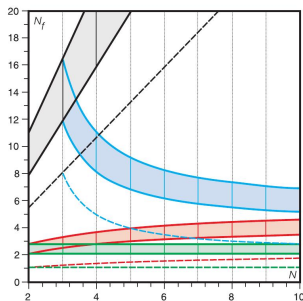
- 1 Adjoint QCD and supersymmetric Yang-Mills theory
- 2 Lattice supersymmetric Yang-Mills theory
- 3 Lattice minimal walking technicolour
- 4 Lattice one flavour adjoint QCD
- 5 Conclusions

In collaboration with I. Montvay, G. Münster, U. D. Özugurel,  
S. Piemonte, D. Sandbrink, P. Giudice, A. Athenodorou, E. Bennett,  
B. Lucini

## Conformal window for adjoint QCD

Technicolour candidates  
(more “natural” EW sector):

- requirement: close to conformal (walking) behaviour, large  $\gamma_m$ , light scalar
- so far: not clear if these requirements can be fulfilled
- perturbative arguments: conformal window starts above  $N_f = 2$  adj. QCD



[Dietrich, Sannino,  
hep-ph/0611341]

## Adjoint QCD

adjoint  $N_f$  flavour QCD:

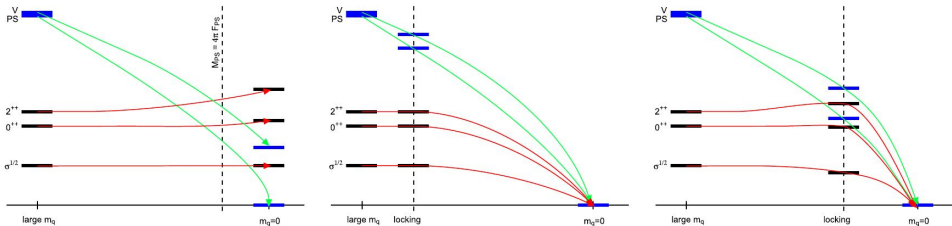
$$\mathcal{L} = \text{Tr} \left[ -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \sum_i^{N_f} \bar{\psi}_i (\not{D} + m) \psi_i \right]$$

$$D_\mu \psi = \partial_\mu \psi + ig[A_\mu, \psi]$$

- $\psi$  Dirac-Fermion in the adjoint representation
  - adjoint representation allows Majorana condition  $\psi = C\bar{\psi}^T$   
 $\Rightarrow$  half integer values of  $N_f$ :  $2N_f$  Majorana flavours
- Symmetry breaking by condensate:

$$\text{SU}(2N_f) \rightarrow \text{SO}(2N_f)$$

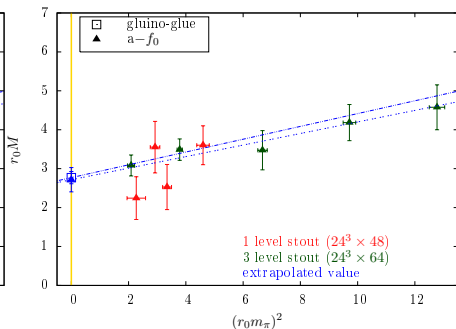
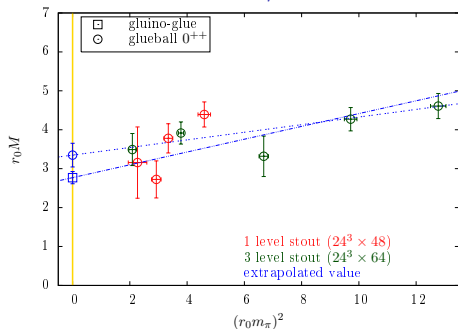
# Mass spectrum of near conformal theory



[Lucini, arXiv:1503.00371]

- QCD like: light pNGb from chiral symmetry breaking at  $m \rightarrow 0$
- (near) conformal:  $m$  only scale setting parameter, no mass scale at  $m \rightarrow 0$
- $M \sim m^{1/(1+\gamma_m)}$

## $N_f = 1/2$ : Lattice simulations of SYM



Safe lower point:

theory not conformal, multiplet formation  $0^-$ ,  $0^+$ , spin-1/2  
 $m_{0^{++}} > m_{a-\pi}$ ; finite mass in chiral limit:  $m_{a-\pi} \rightarrow 0$

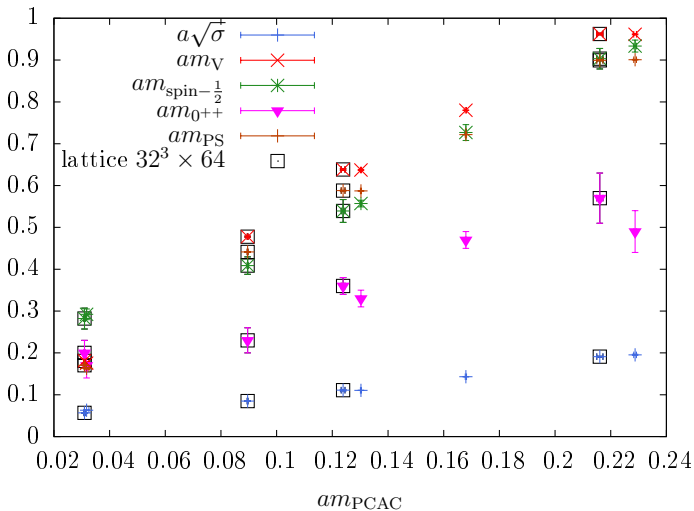
→ More on Saturday: Talk by Pietro Giudice and Stefano Piemonte

## $N_f = 2$ : Lattice simulations of MWT

### Simulation details:

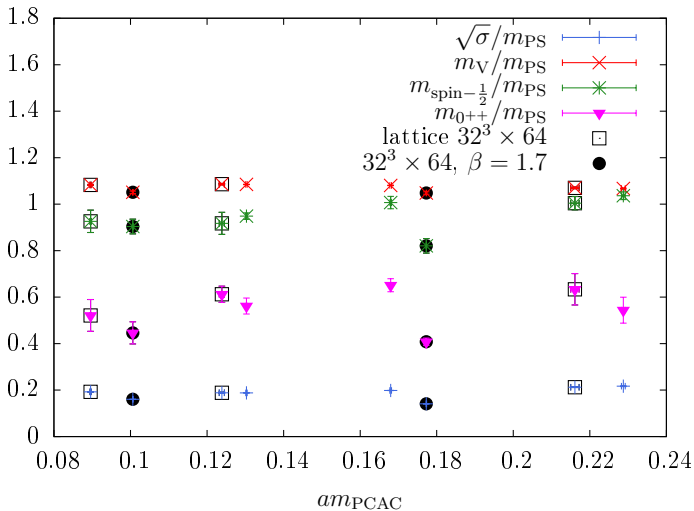
- DESY-Münster (preliminary)
- two lattice spacings ( $\beta = 1.5, 1.7$ )
- three volumes ( $24^3, 32^3, (48^3)$ )
- $\sim 5$  different residual quark masses
- tree level improved gauge action, stout smeared unimproved Wilson fermions

# Mass spectrum of MWT





## Mass spectrum of MWT at different $\beta$



## Observations for MWT

Safe upper point:

theory seems conformal, light scalar

$m_{0^{++}} < m_{PS}$ ; conformal scaling

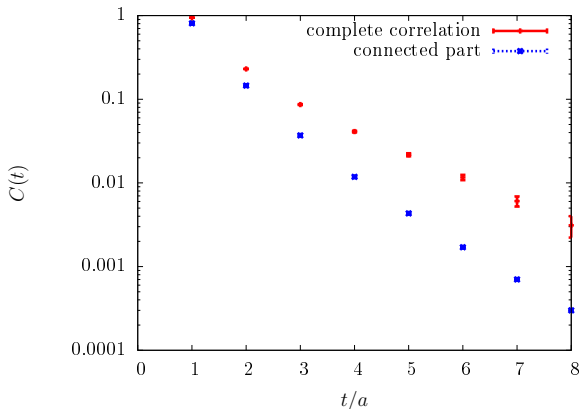
- spectrum consistent with  $\gamma_m \sim 0.38 \Rightarrow$  might be too small

## New result for $N_f = 2$ : Spin-1/2 state

$$\sum_{\mu,\nu} \sigma_{\mu\nu} \text{tr} [F^{\mu\nu} \lambda]$$

- specific state for adjoint QCD
- fractionally charged particles (?)
- Spin-1/2 first state above scalar glueball, below  $m_{PS}$

## New result for $N_f = 2$ : Mesonic scalar state



triplet:  
 0.747(17)  
 singlet:  
 0.540(53)  
 glueball:  
 0.33(2)  
 $m_{PS}$ : 0.5873(3)

- dominant disconnected contributions
- below  $m_{PS}$  but still much larger than the glueball  $0^{++}$
- gluonic dominance of the scalar ground state

## Lattice simulations of $N_f = 1$ adjoint QCD

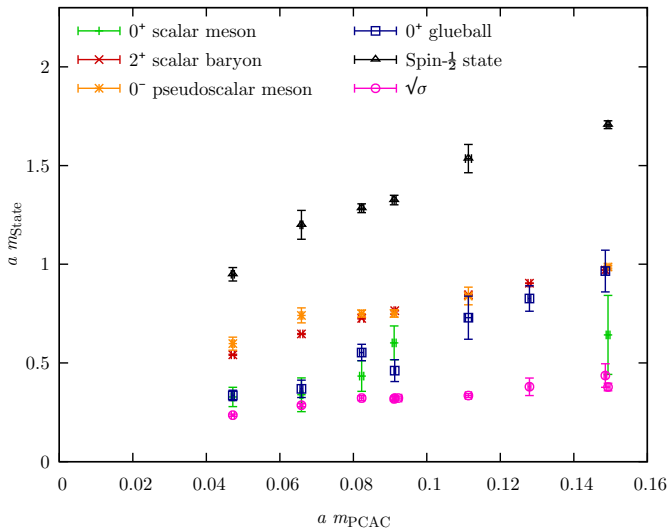
### Simulation details:

- investigated finite volume effects (less severe than for MWT)
- unimproved Wilson action
- several states analysed (baryons, mesons, glueballs, ...)
- presented in: [PoS LATTICE2013 (2014) 066], [Athenodorou, Bennett, GB, Lucini, arXiv:1412.5994]
- new update: second lattice spacing ( $\beta = 2.05$ ,  $\beta = 2.2$ )

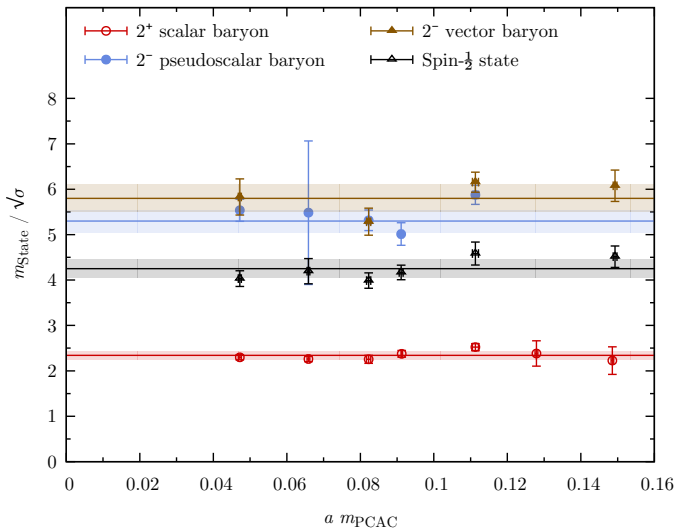
## The states of $N_f = 1$ adjoint QCD

- $SU(2)$ : baryons (diquarks) from two spinors
- $SU(2) \rightarrow SO(2) \simeq U(1)_B$ :  
states are labelled by  $U(1)^P$
- $\bar{\psi}\psi$ :  $0^+$ , scalar meson (“scalar singlet”)
- $\psi^T C\psi$ :  $2^-$ , pseudoscalar baryon (“scalar triplet”)
- $\psi^T C\gamma_5\psi$ :  $2^+$ , scalar baryon (“pseudoscalar triplet”) = pNGb

# Results for $N_f = 1$ adjoint QCD

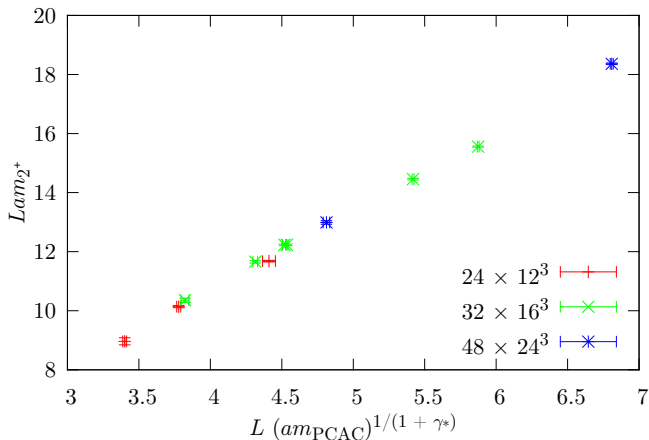


# Results for $N_f = 1$ adjoint QCD



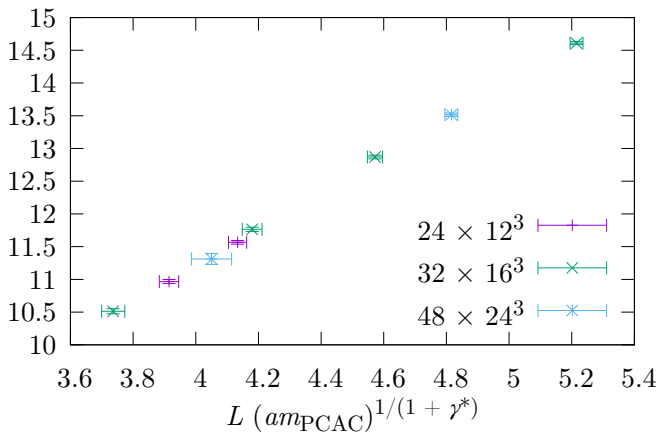


## Results for $N_f = 1$ adjoint QCD



$\gamma_m^* = 0.9$ , from mode number:  $\gamma_m^* = 0.92(1)$

# Results for $N_f = 1$ adjoint QCD $\beta = 2.2$



$$\gamma_m^* = 0.7$$

## Results for $N_f = 1$ adjoint QCD

- light scalar ✓
- (near) conformal ✓
- $\gamma_m^* \sim 0.9$  ✓
- smaller lattice spacing:  $\gamma_m^* \sim 0.7$  (preliminary)

Further investigations needed:

- combination with additional fermions needed for ew symmetry breaking (UMWT)
- relation to  $\mathcal{N} = 2$  supersymmetric YM theory

## Conclusions

- lattice simulations show SUSY multiplet structure in SYM
- lattice simulations resolve large difference of non-conformal SYM and conformal MWT
- $N_f = 1$  adjoint QCD on the (near) conformal side and includes light scalar and large  $\gamma_m$
- SYM below lower end of theories that show light scalar and (near) conformal behaviour
- “exotic” state in adjoint QCD:  $m_{\text{spin-1/2}} < m_{PS}$  for  $N_f = 2$  ;  
 $m_{\text{spin-1/2}} > m_{\text{scalar baryon}}$  for  $N_f = 1$
- light mesonic scalar state for  $N_f = 1$  and 2;  
 $N_f = 2$ : glueball better signal for low scalar state