

Zc(3900) from coupled-channel HAL QCD approach on the lattice

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HAL QCD (Hadrons to Atomic nuclei from Lattice QCD)

Sinya Aoki, Shinya Gongyo, Takumi Iritani, Takaya Miyamoto (YITP, Kyoto Univ.)

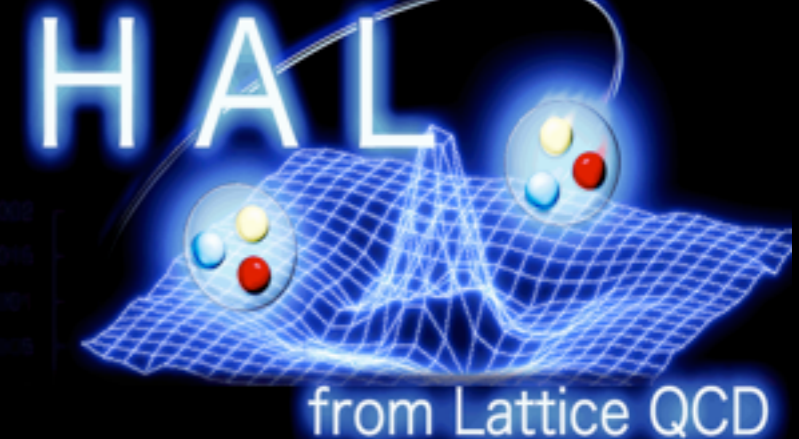
Takumi Doi, Tetsuo Hatsuda, Yoichi Ikeda (RIKEN)

Takashi Inoue (Nihon Univ.)

Noriyoshi Ishii, Keiko Murano (RCNP, Osaka Univ.)

Hidekatsu Nemura, Kenji Sasaki (Univ. Tsukuba)

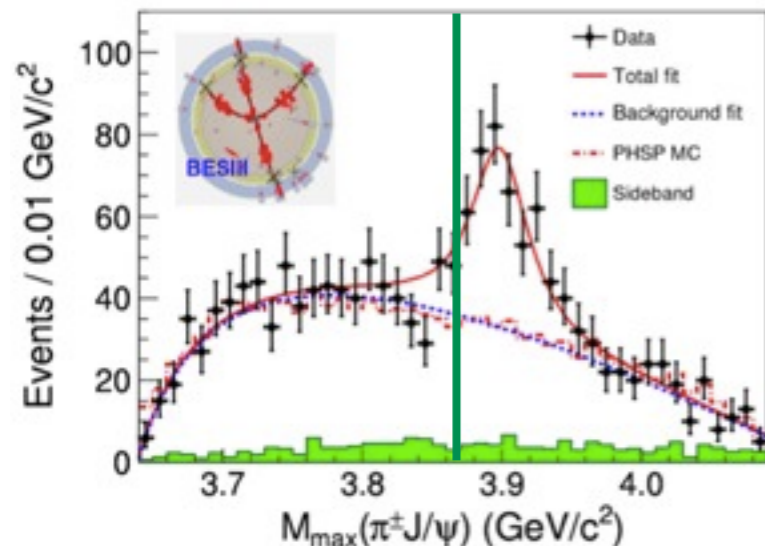
Hadrons to Atomic nuclei



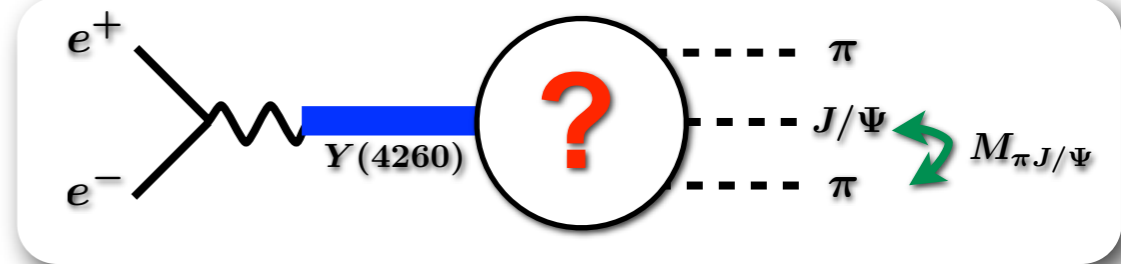
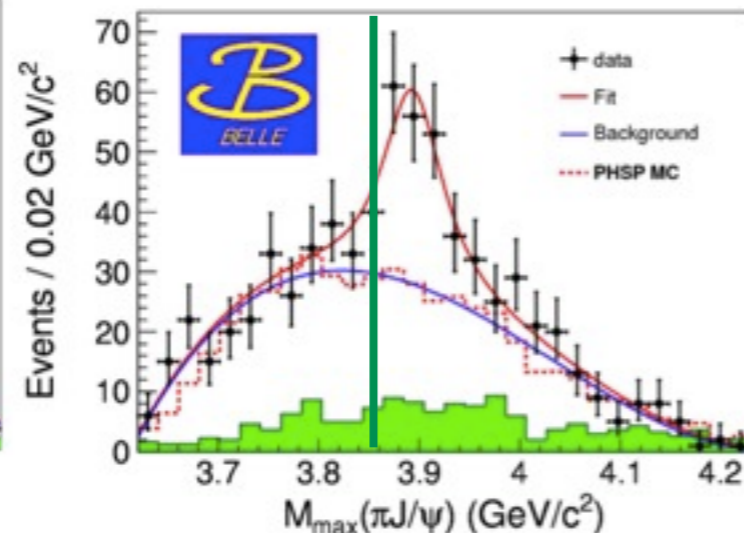
The 33rd International Symposium on Lattice Field Theory(Lattice2015)
@Kobe International Conference Center, Jul. 14--18, 2015.

What is $Z_c(3900)$?

BESIII Coll., PRL110 (2013).



Belle Coll., PRL110 (2013).



- observed in $\pi^{\pm}J/\psi$ invariant mass spectra
- require 4 quarks ($cc^{\text{bar}}ud^{\text{bar}}$)
- $J^P = 1^+$ seems most probable

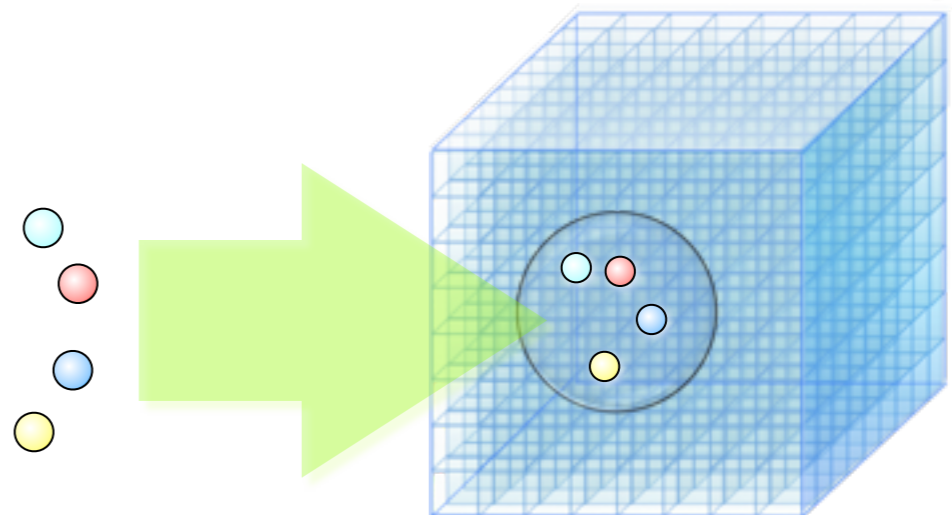
BESIII Coll., PRL112 (2014).

★ structure of $Z_c(3900)$ from models

- Tetraquark? Maiani et al. (2013).
- $D^{\text{bar}}D^*$ molecule? Nieves et al. (2011)
+ many others
- Charmonium-hadronium? Voloshin (2008).
- cusp? Chen et al. (2013), Swanson (2015).

➔ **poor information on interactions**

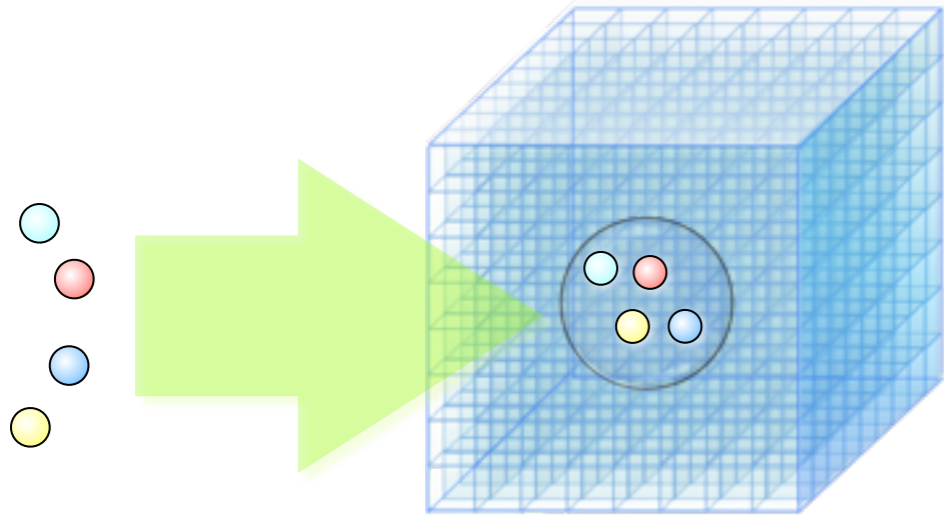
★ LQCD simulations for $Z_c(3900)$



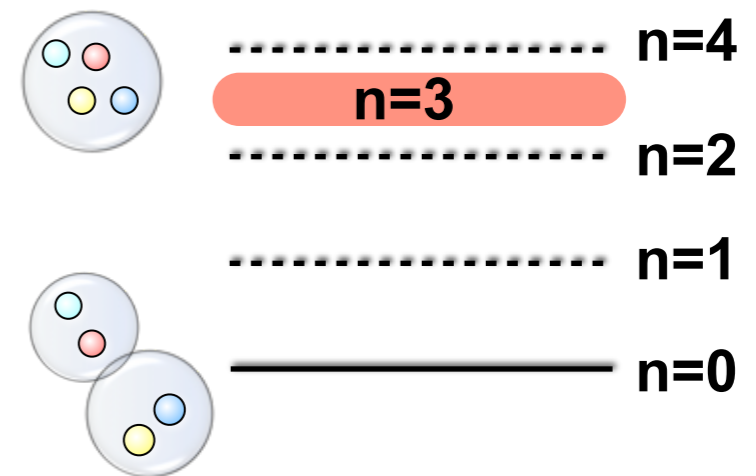
How to study $Z_c(3900)$ on the lattice?

◆ Conventional approach: LQCD spectrum

➔ identify all relevant $W_n(L)$ ($n=0,1,2,3,\dots$)



$$\langle 0 | \phi_1(\vec{x} + \vec{r}, \tau) \phi_2(\vec{x}, \tau) | \text{hadrons} \rangle = \sum_n \psi_n(\vec{r}) e^{-W_n \tau}$$



✓ No positive evidence for $Z_c(3900)$

[S. Prelovsek et al., PLB 727, 172 \(2013\).](#)

[S.-H. Lee et al., PoS Lattice2014 \(2014\).](#)

[S. Prelovsek et al., PRD91, 014504 \(2015\).](#)

★ Why is the peak observed in expt.?

- Broad resonance? Kinematical effect?
- Key is S-matrix elements w/ coupled-channel

➔ Lüscher's finite size formula in coupled-channel system

in practice, assumption about interaction kernels or K-matrices necessary

How to study $Z_c(3900)$ on the lattice?

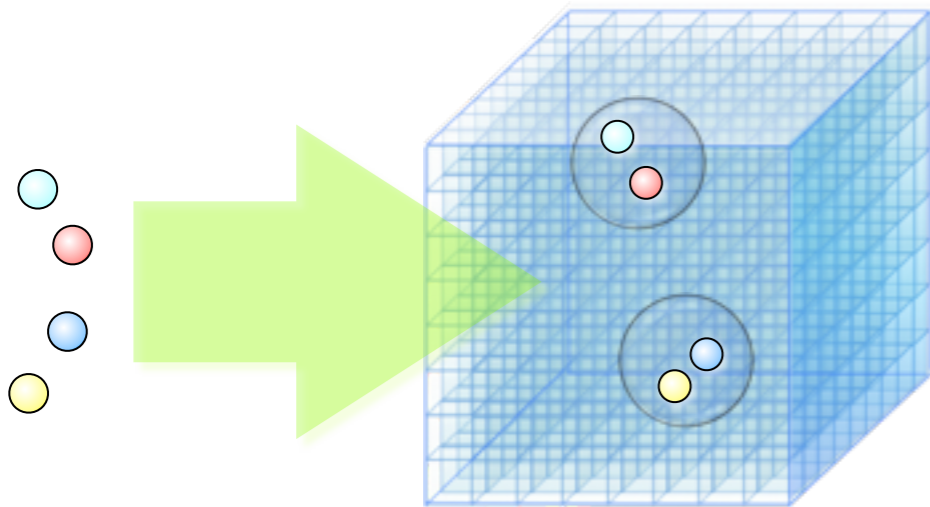
◆ HAL QCD approach: energy-independent interaction kernel

➔ measure not only temporal but also spatial correlation

[Ishii, Aoki, Hatsuda, PRL99, 02201 \(2007\).](#)

[Aoki, Hatsuda, Ishii, PTP123, 89 \(2010\).](#)

[Ishii et al.\(HAL QCD\), PLB712, 437\(2012\).](#)



$$\langle 0 | \phi_1(\vec{x} + \vec{r}, \tau) \phi_2(\vec{x}, \tau) | \text{hadrons} \rangle = \sum_n \psi_n(\vec{r}) e^{-W_n \tau}$$

★ **NBS wave functions: $\psi_n(r)$**

$$\left(\nabla^2 + \vec{k}_n^2 \right) \psi_n(\vec{r}) = 2\mu \int d\vec{r}' U(\vec{r}, \vec{r}') \psi_n(\vec{r}')$$

✓ **$U(r,r')$ contains all 2PI contributions**

➔ **Extension to coupled-channel system is straightforward**

- measure wave functions in each channel
- extract potential matrix faithful to S-matrix
- calculate observables (mass spectrum, pole position,)

[Aoki et al. \[HAL QCD Coll.\], Proc. Jpn. Acad., Ser. B, 87 \(2011\); PTEP 2012, 01A105 \(2012\).](#)

Contents

- **Introduction : $Z_c(3900)$ & HAL QCD method**
- **LQCD setup**
- **Coupled-channel potential matrix for $Z_c(3900)$ in $I(J^P)=1(1^+)$**
- **2-body invariant mass spectra & pole of $Z_c(3900)$**
- **Production reactions of $Z_c(3900)$**
- **Summary**

Lattice QCD setup

$N_f=2+1$ full QCD configurations generated by PACS-CS Coll.

[PACS-CS Coll., S. Aoki et al., PRD79, 034503, \(2009\).](#)

- Iwasaki gauge & $O(a)$ -improved Wilson quark actions
- $a=0.0907(13)$ fm $\rightarrow L\sim 2.9$ fm ($32^3 \times 64$)

Light meson mass [conf.1, conf.2, conf.3] (MeV)

$M_\pi=701(1), 572(1), 411(1)$ [PDG:135 (π^0)]

$M_\rho=1097(4), 1000(5), 896(8)$ [PDG:770 (ρ^0)]

Tsukuba-type Relativistic Heavy Quark (RHQ) action for charm quark

[S. Aoki et al., PTP109, 383 \(2003\).](#)

➔ remove leading cutoff errors $O(m_c a)$, $O(\Lambda_{\text{QCD}} a)$, ...

- We are left with $O((a\Lambda_{\text{QCD}})^2)$ error (\sim a few %)
- We employ RHQ parameters tuned by Namekawa et al.

[Y. Namekawa et al., PRD84, 074505 \(2011\).](#)

Charmed meson mass [conf.1, conf.2, conf.3] (MeV)

$M_{\eta_c}=3024(1), 3005(1), 2988(1)$ [PDG:2981]

$M_{J/\psi}=3143(1), 3118(1), 3097(1)$ [PDG:3097]

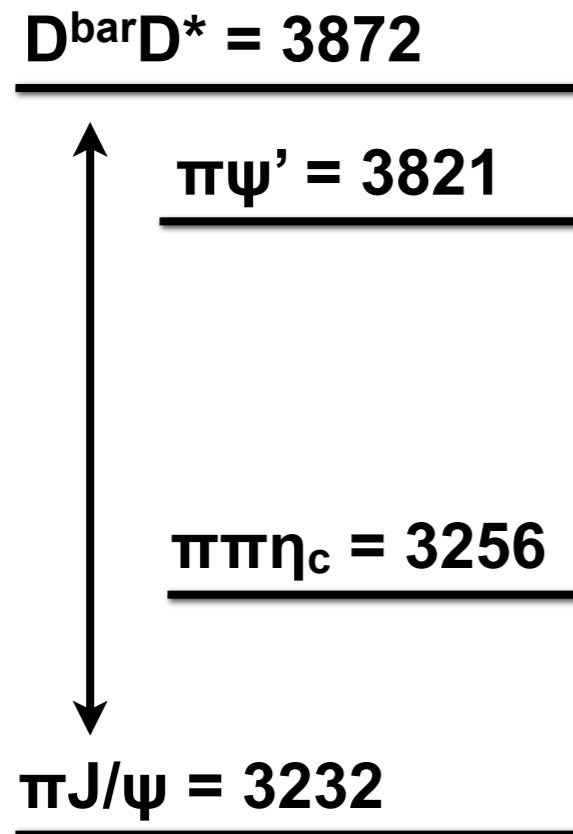
$M_D=2000(1), 1947(1), 1903(1)$ [PDG:1865 (D^0)]

$M_{D^*}=2159(2), 2101(2), 2056(3)$ [PDG:2007 (D^{*0})]

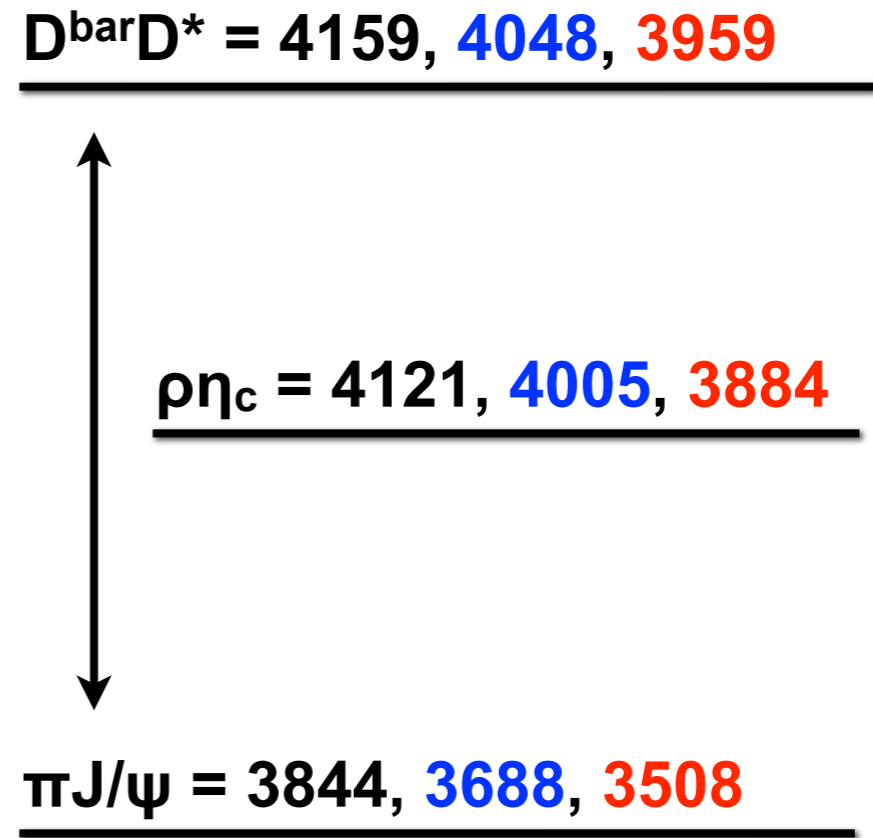
Lattice QCD setup : thresholds

✦ Thresholds in $I^G J^P = 1^+ 1^+$ channel

Physical thresholds



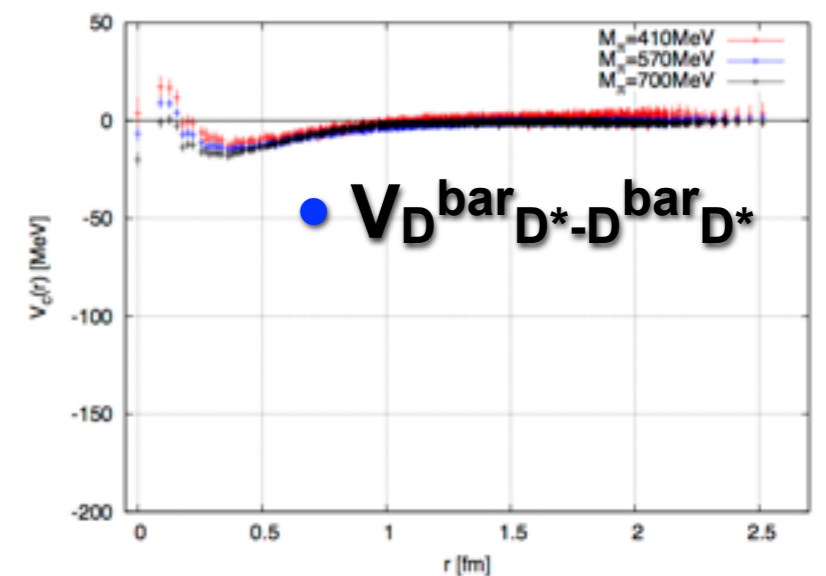
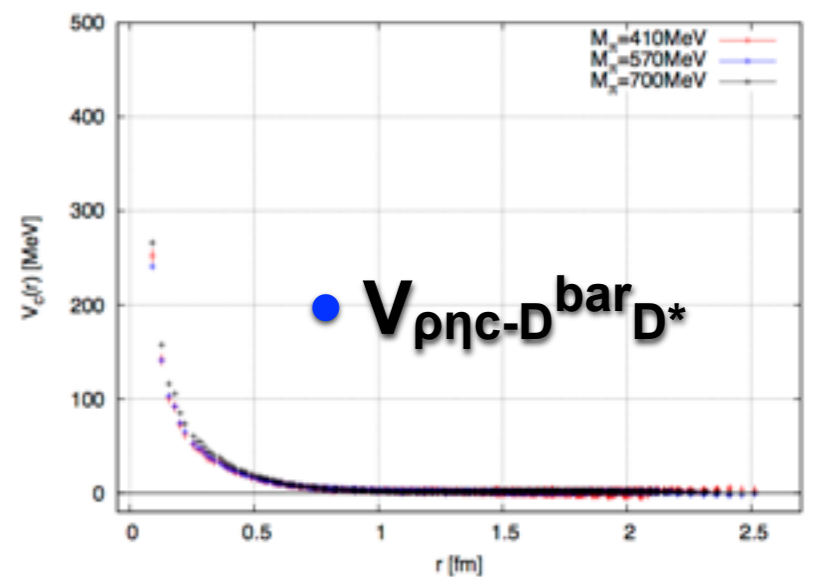
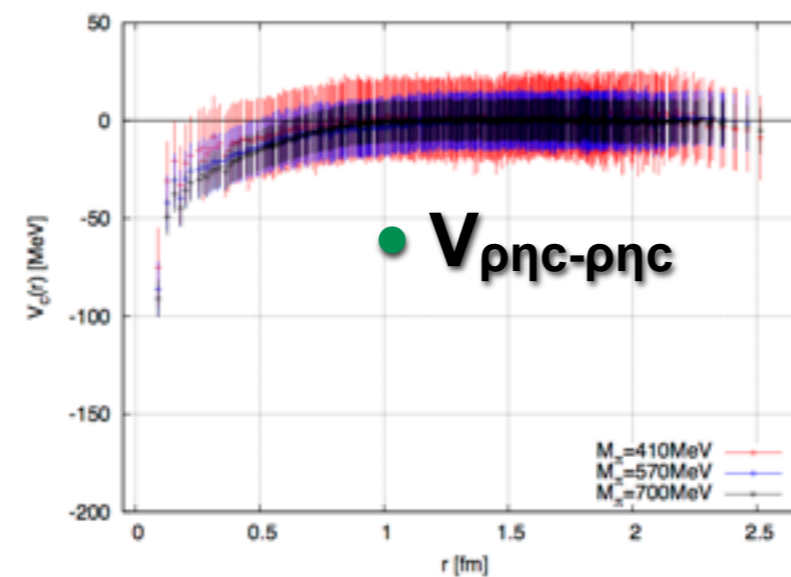
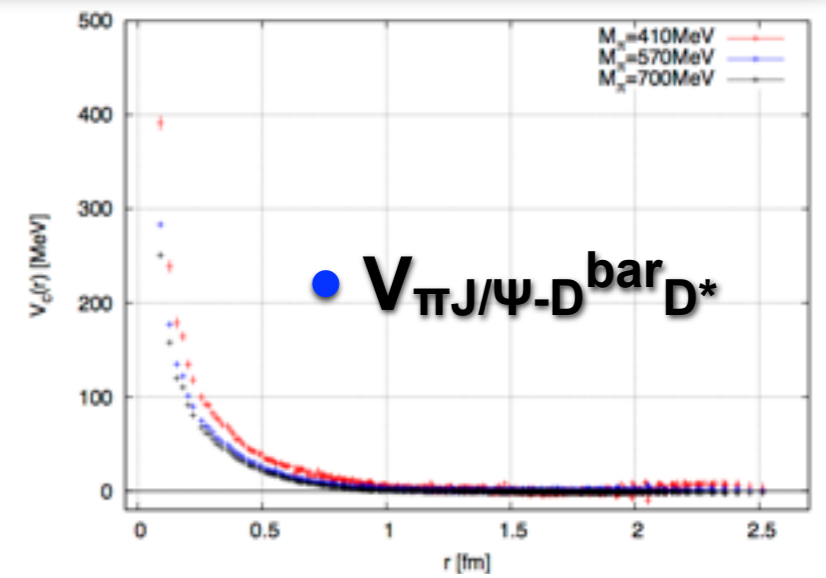
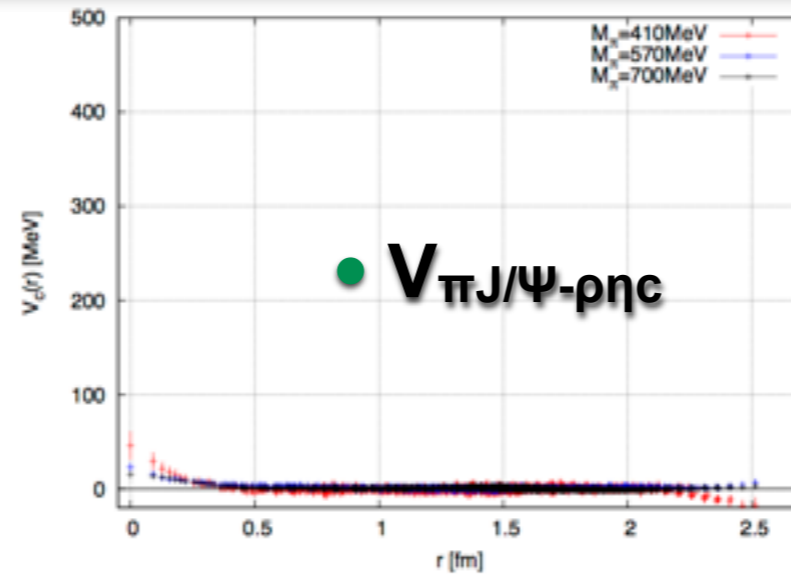
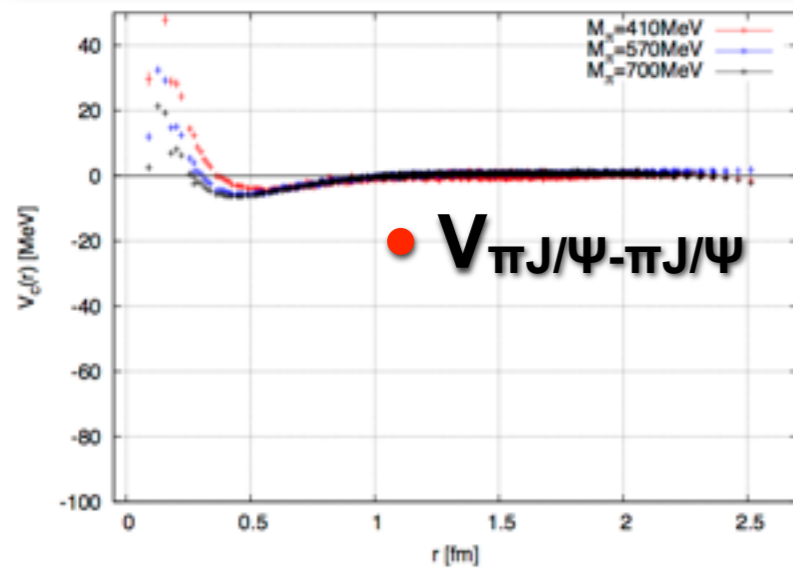
LQCD simulation



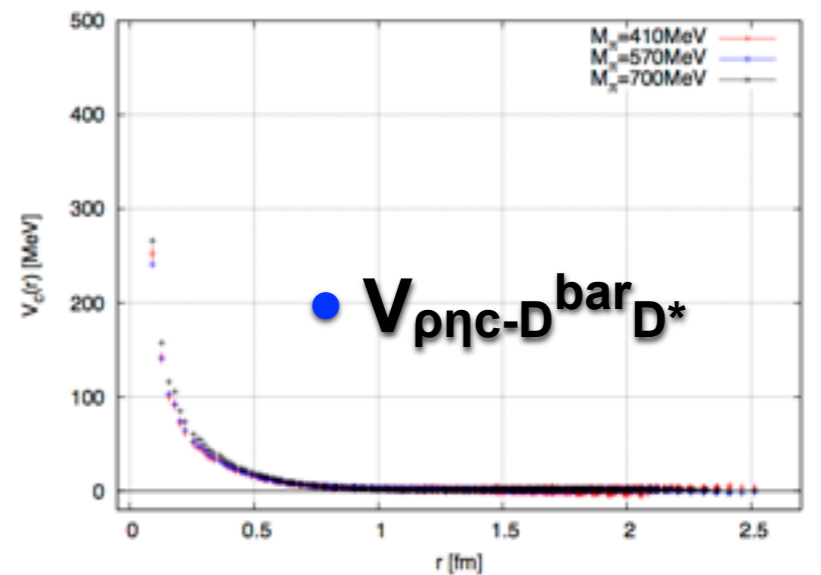
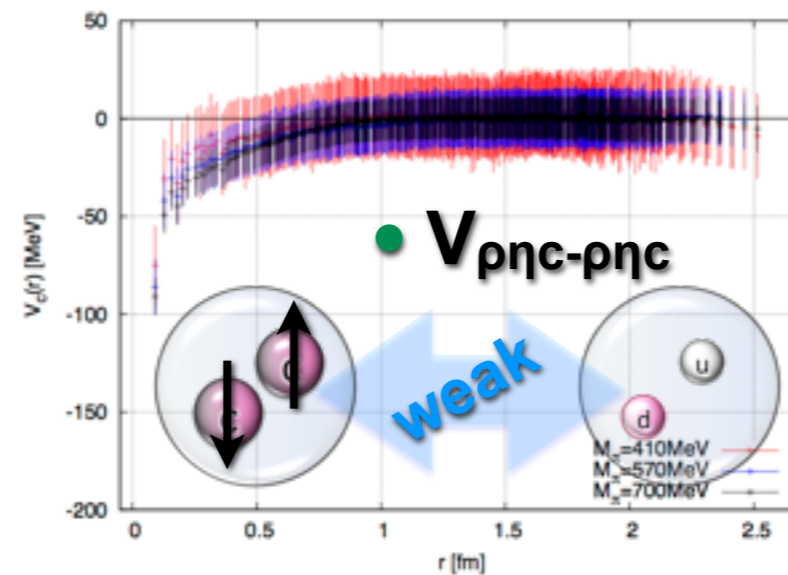
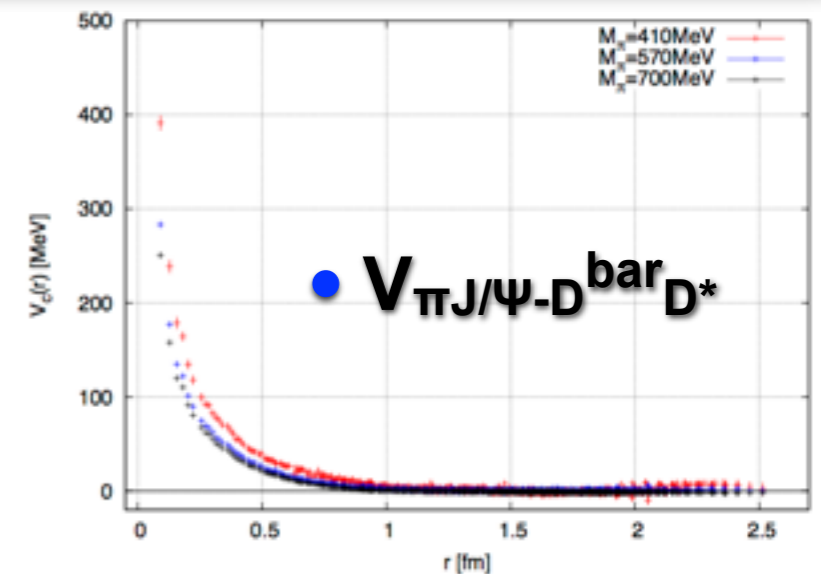
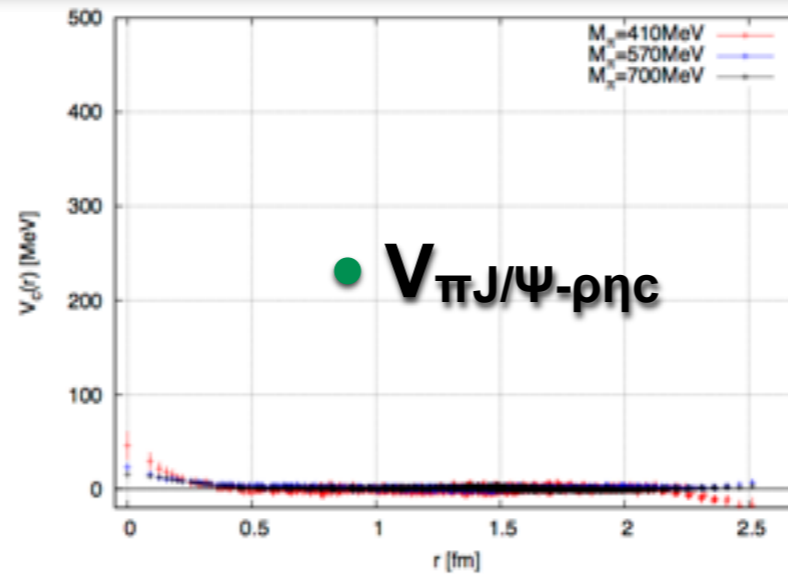
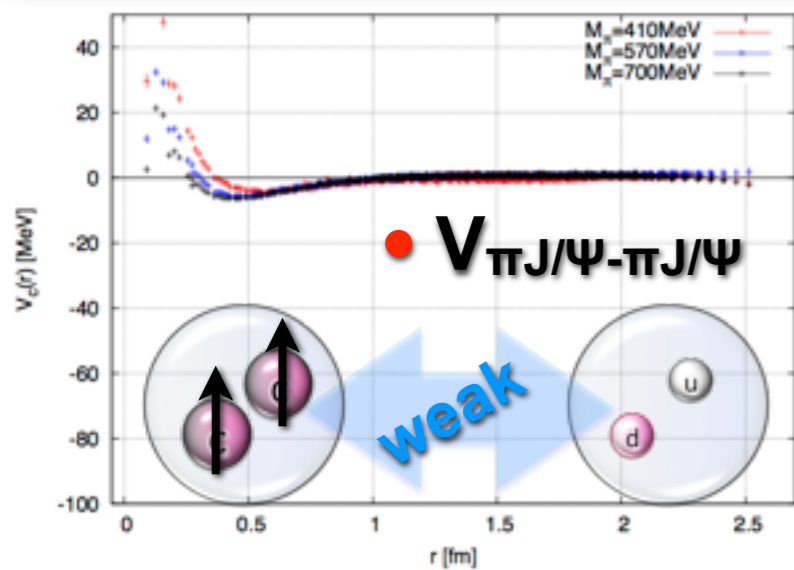
- $M_{\pi\psi'} > M_{D^{\text{bar}}D^*}$ due to heavy pion mass
- $\rho \rightarrow \pi\pi$ decay not allowed w/ $L \sim 3\text{fm}$

✦ **S-wave $\pi J/\psi - \rho\eta_c - D^{\text{bar}}D^*$ coupled-channel analysis**

Potential matrix ($\pi J/\psi$ - $\rho\eta_c$ - $D^{\text{bar}}D^*$)

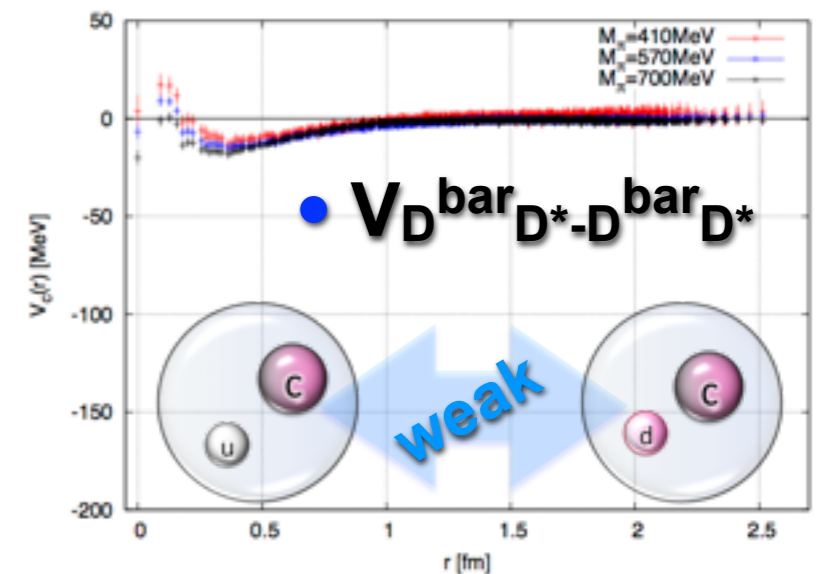


Potential matrix ($\pi J/\psi$ - $\rho\eta_c$ - $D^{\text{bar}}D^*$)

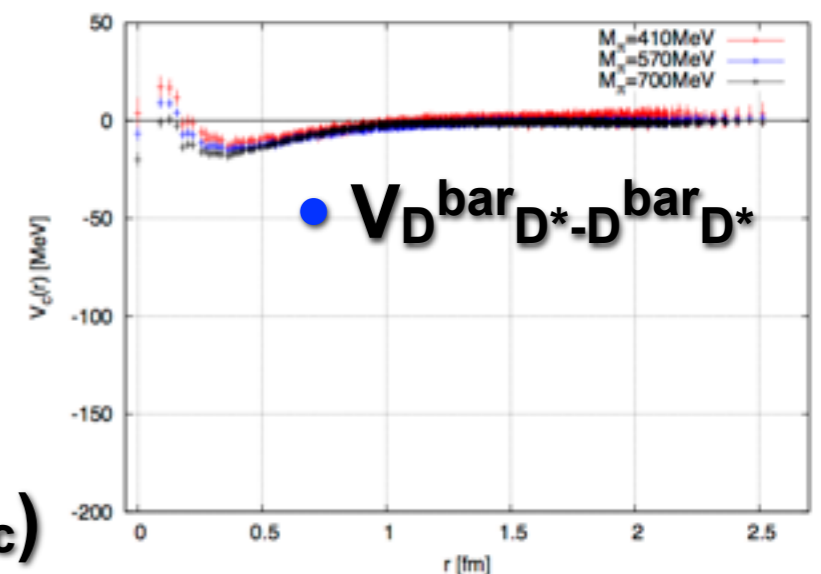
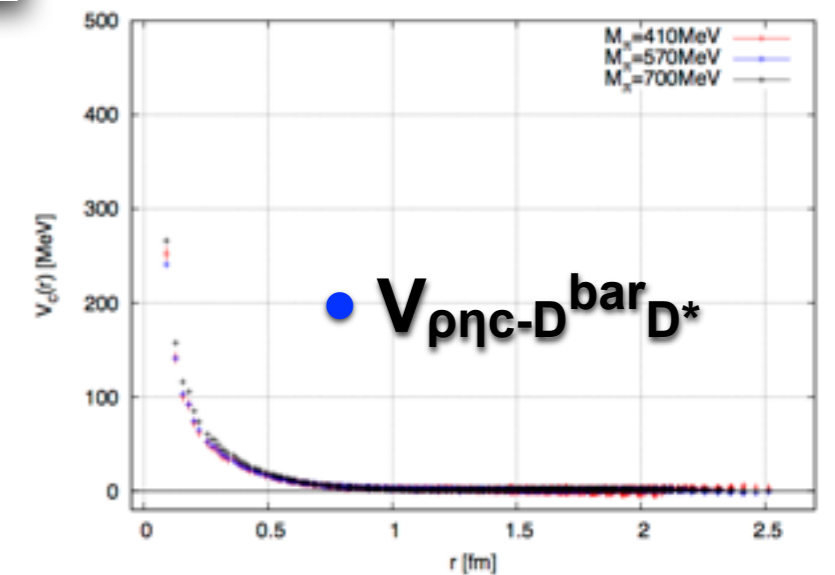
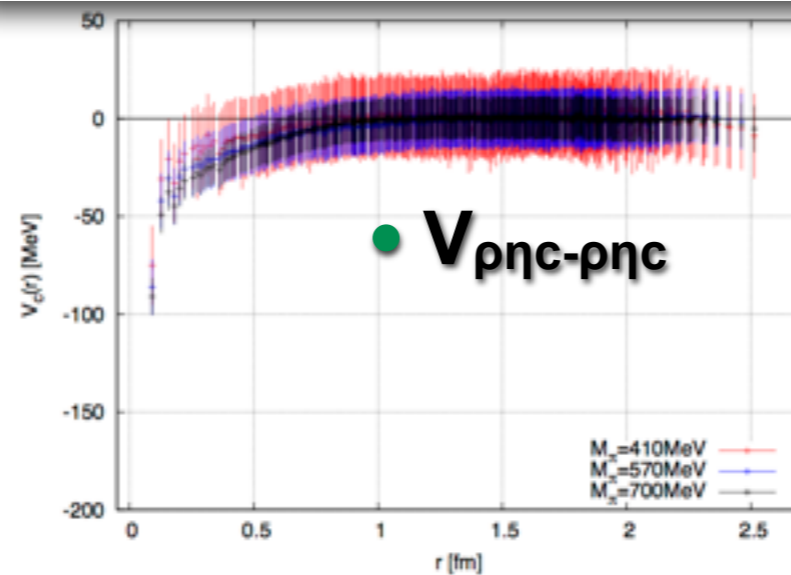
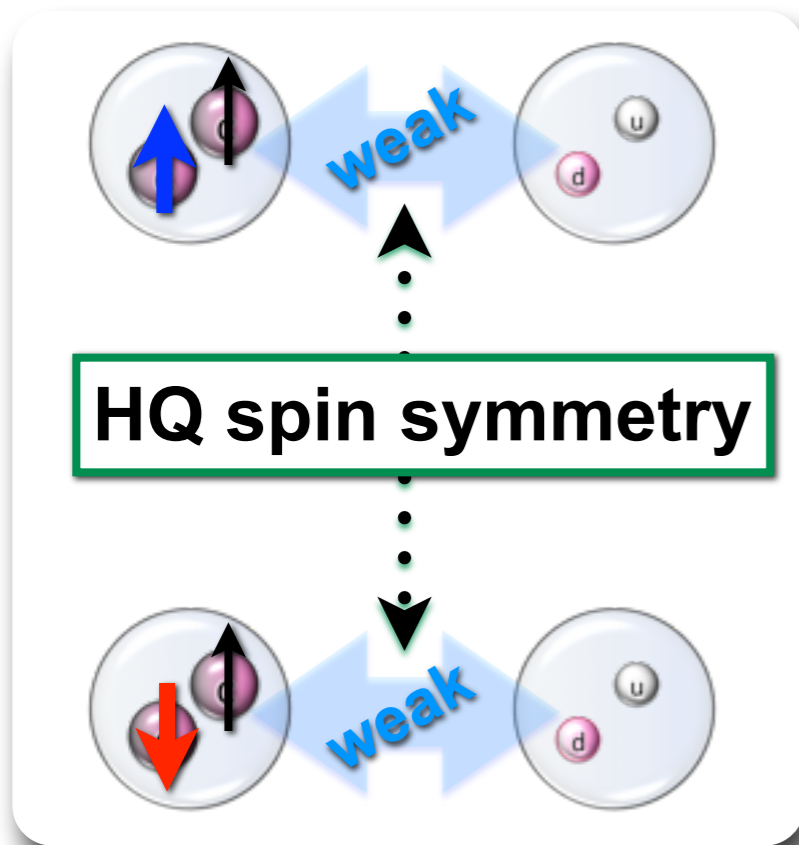
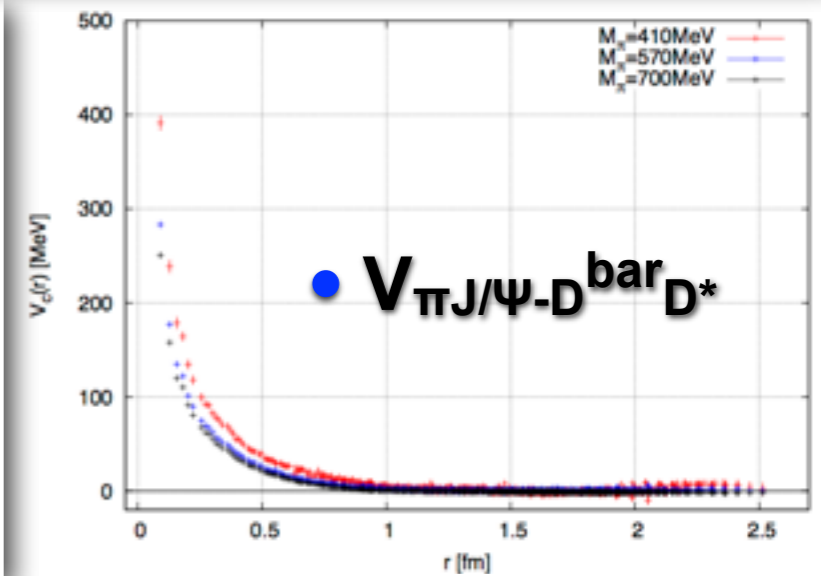
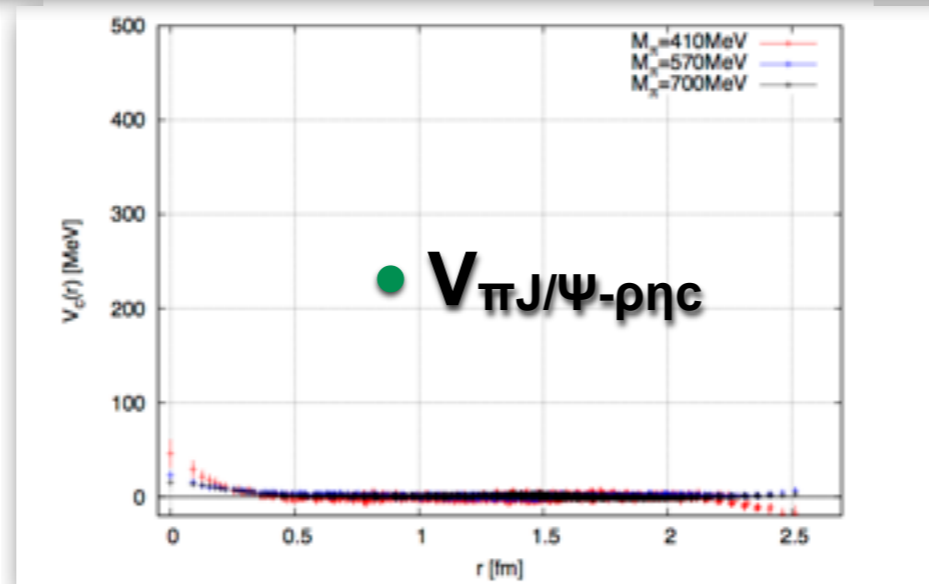
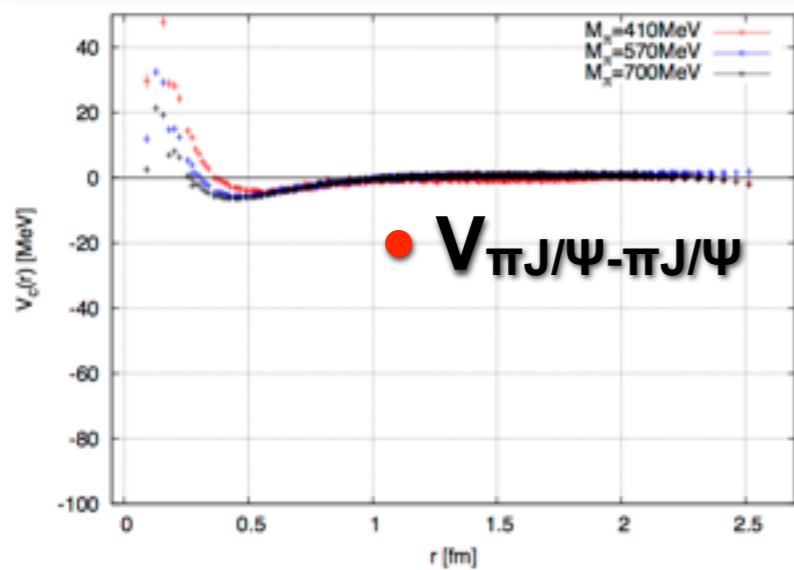


- All diagonal potentials are weak

➔ no bound $D^{\text{bar}}D^*$



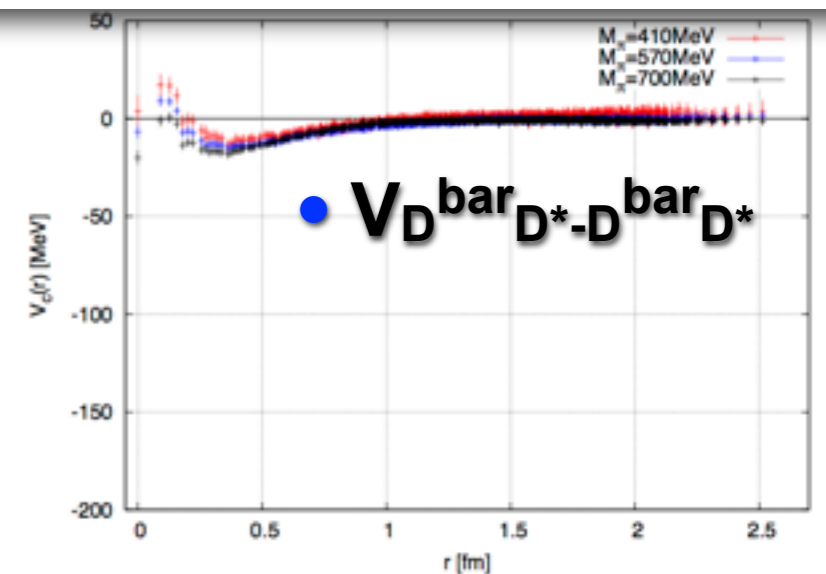
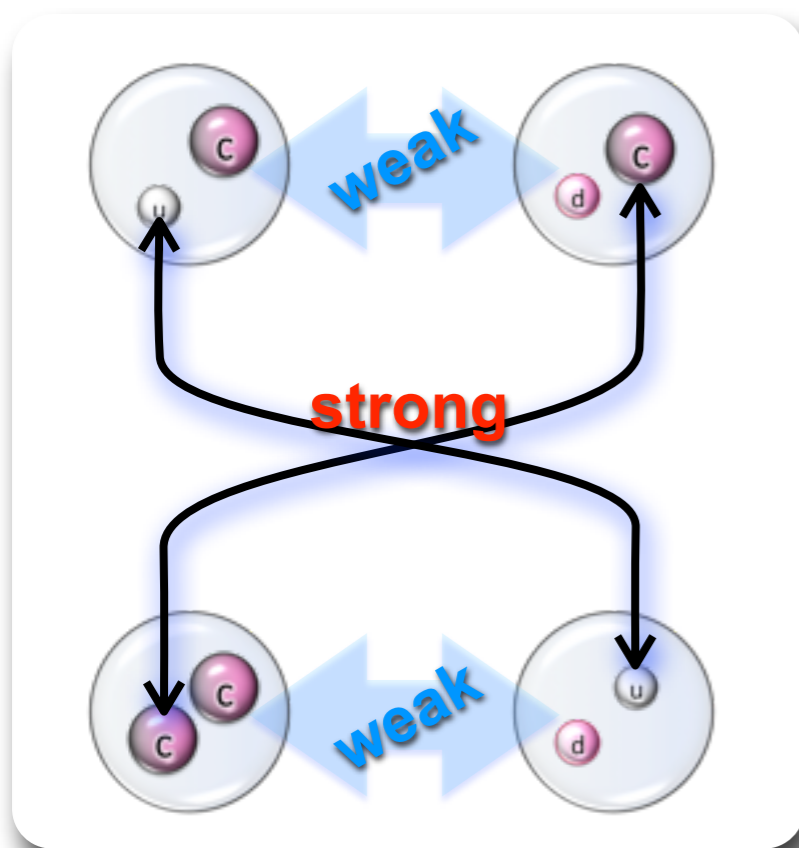
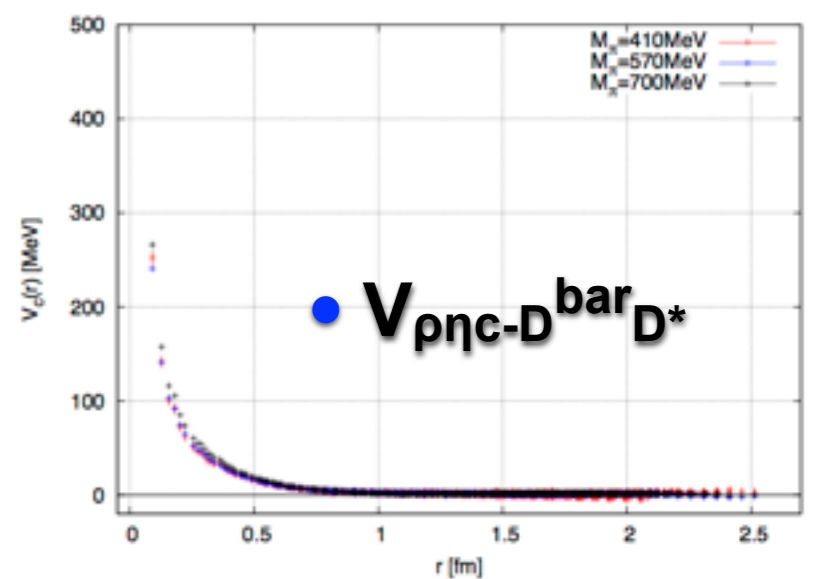
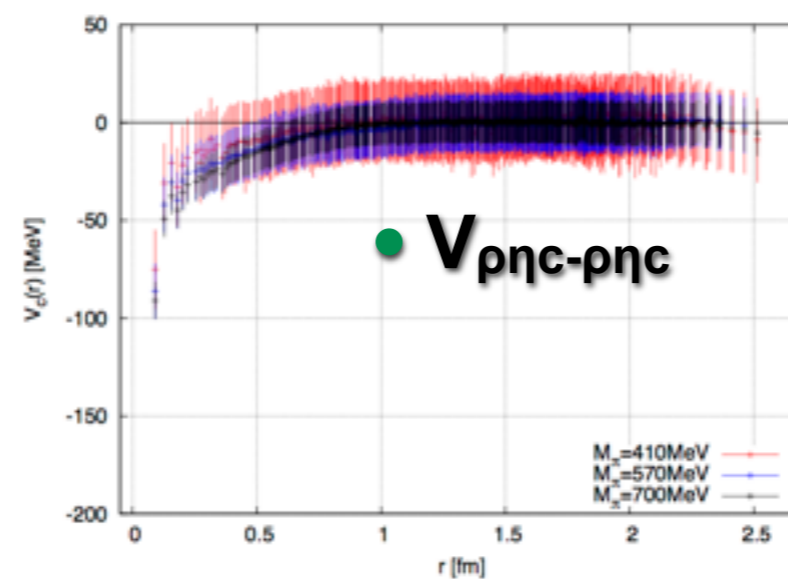
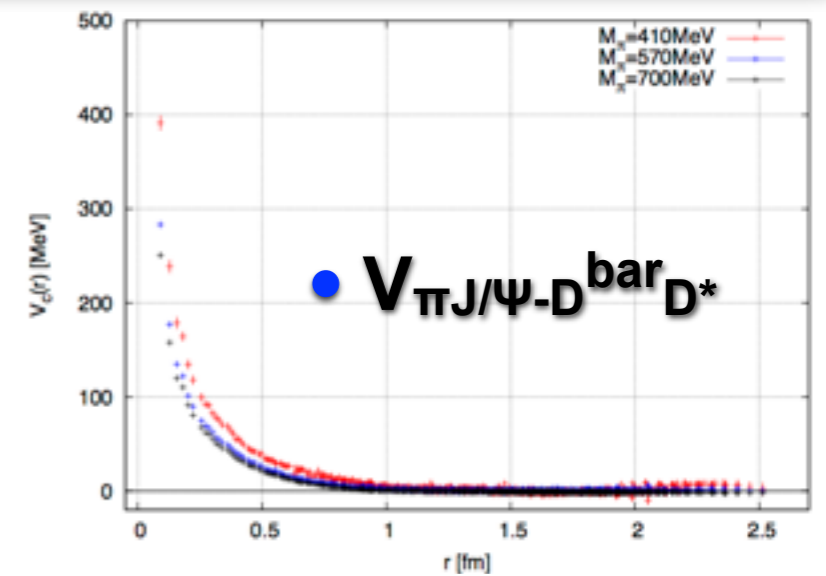
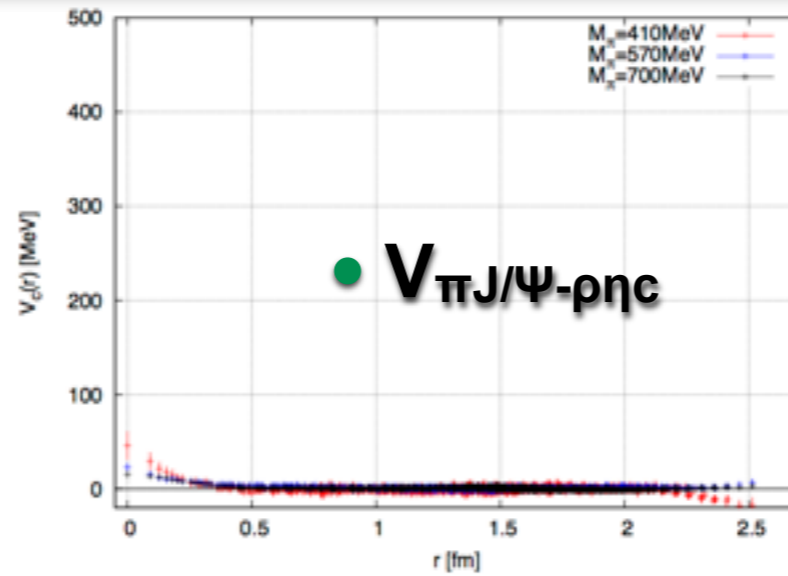
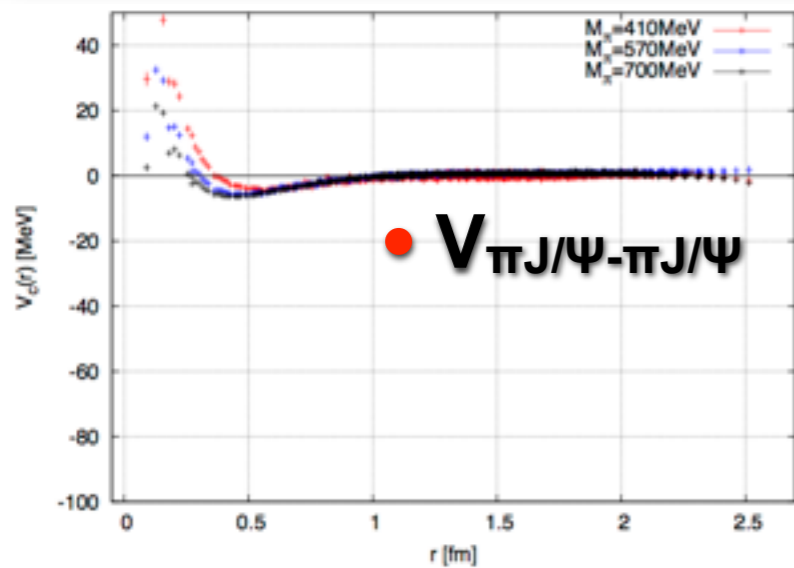
Potential matrix ($\pi J/\psi$ - $\rho\eta_c$ - $D^{\text{bar}}D^*$)



• Weak $\pi J/\psi$ - $\rho\eta_c$ potential

➡ charm quark spin-flip is suppressed by $O(1/m_c)$

Potential matrix ($\pi J/\psi$ - $\rho \eta_c$ - $D^{\text{bar}} D^*$)

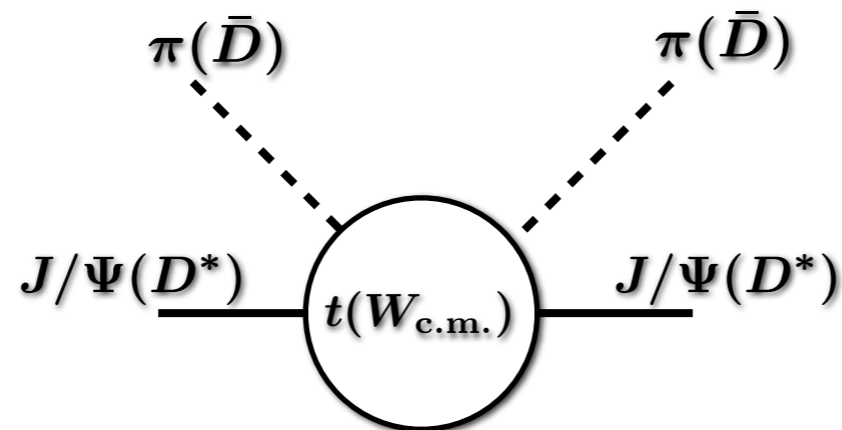


- Strong off-diagonal $D^{\text{bar}} D^*$ potentials

✓ strong charm-quark-exchange interactions

Two-body observables : structure of $Z_c(3900)$ in $I^G(J^P)=1^+(1^+)$

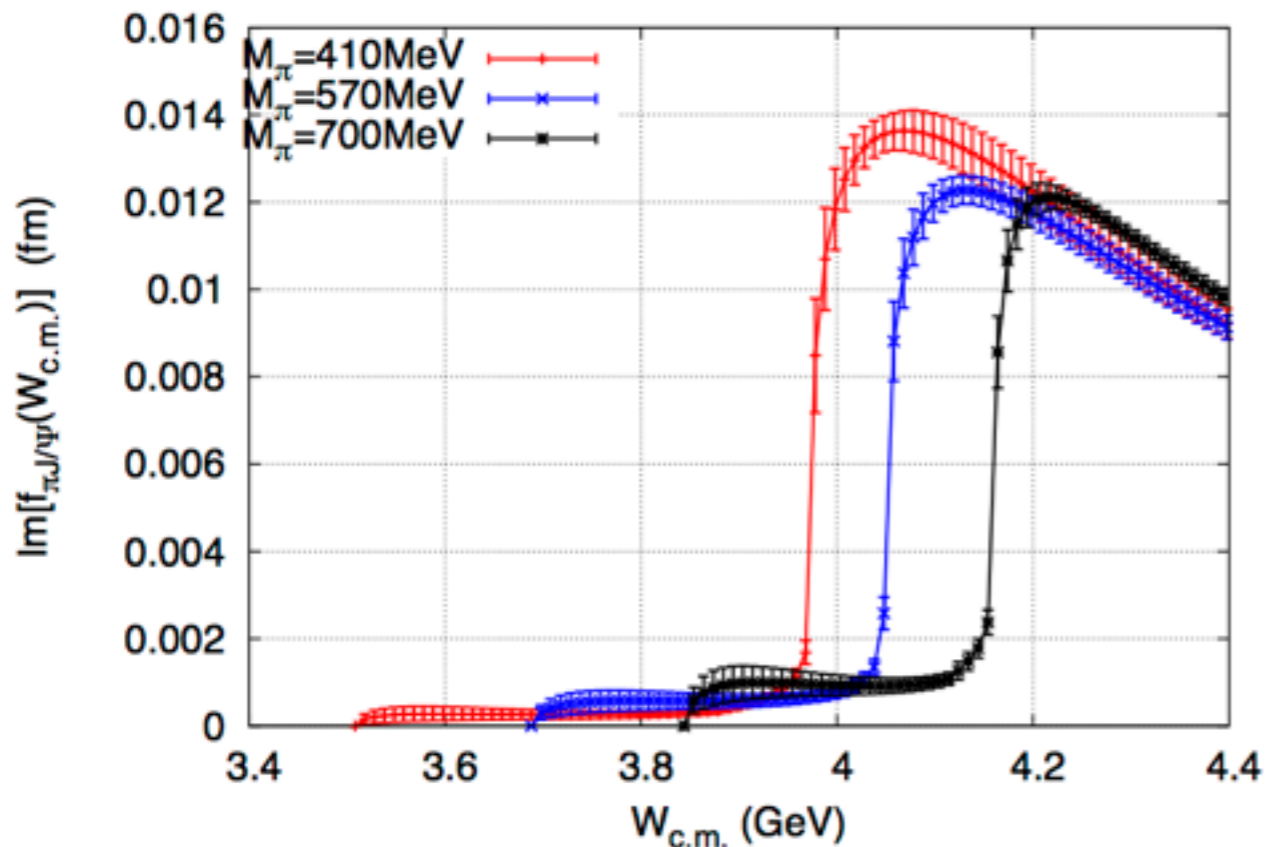
- Invariant mass distributions of $\pi J/\psi$ & $D^{\text{bar}}D^*$ s-wave scattering
- ➔ ideal experimental setting for production reactions of $Z_c(3900)$



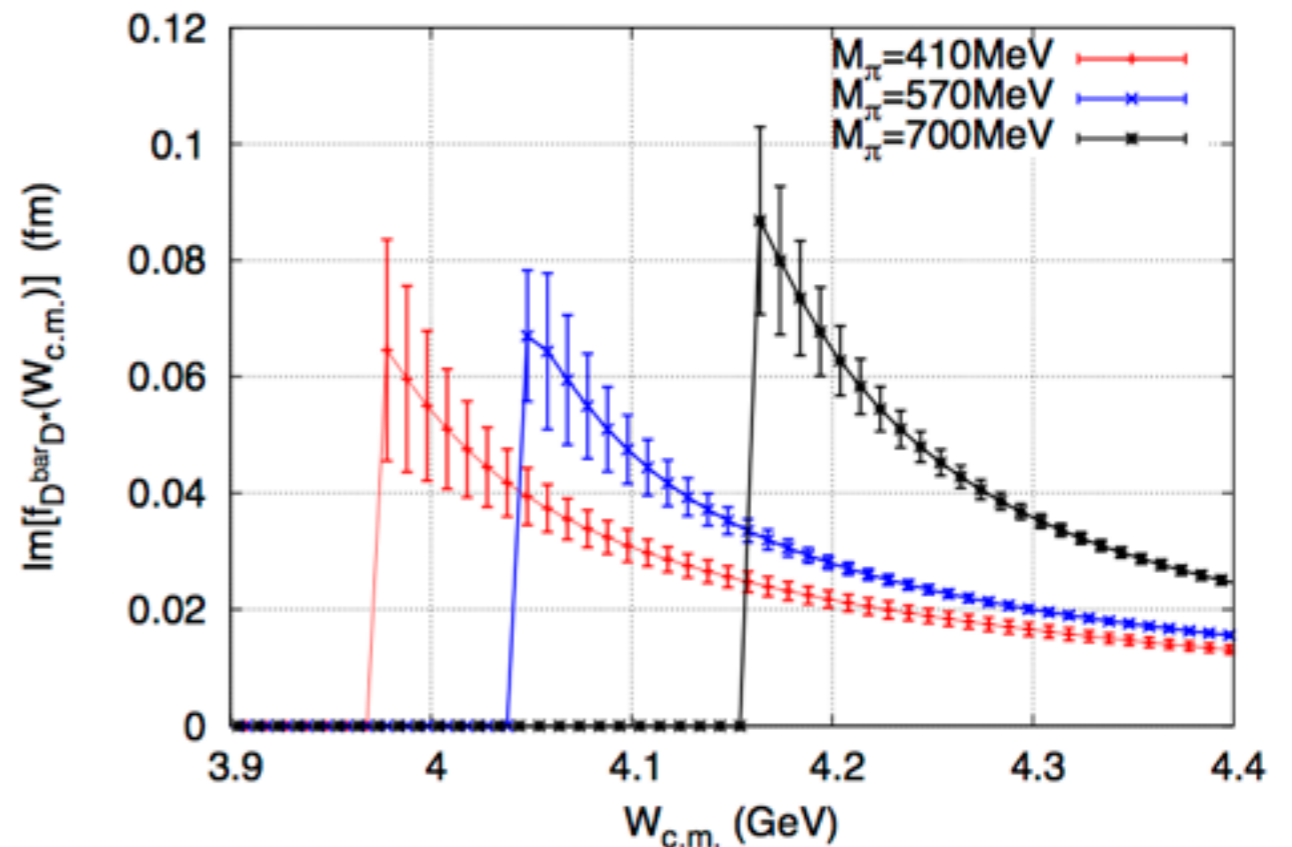
- Pole positions of $Z_c(3900)$ to determine structure of $Z_c(3900)$

2-body scattering & inv. mass spectra

- $\pi J/\psi$ invariant mass



- $D^{\text{bar}}D^*$ invariant mass



✓ enhancement near $D^{\text{bar}}D^*$ threshold due to large $\pi J/\psi$ - $D^{\text{bar}}D^*$ coupling

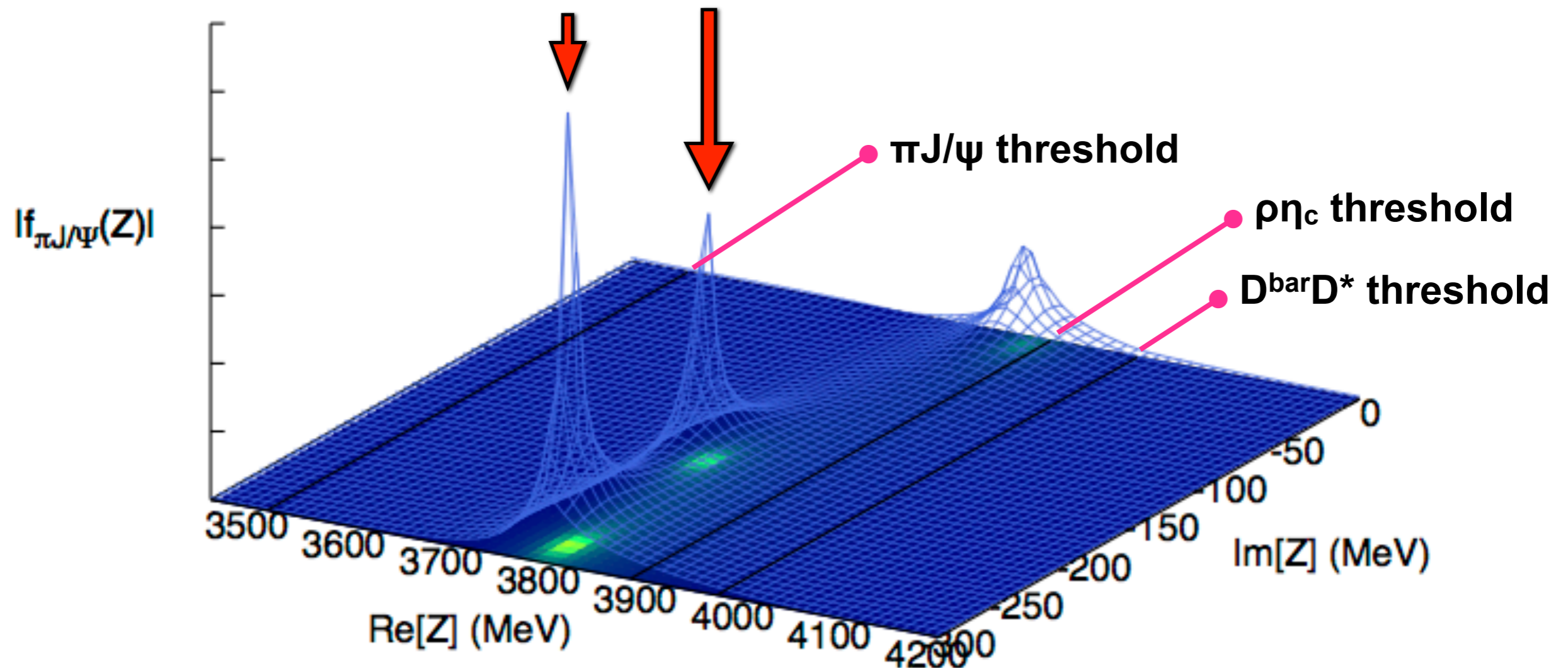
- peak in $\pi J/\psi$ invariant mass
- enhancement (**cusp?**) in $D^{\text{bar}}D^*$ invariant mass

(No m_q dependence on qualitative behaviors of line shapes)

Pole search ($\pi J/\psi$:2nd, $\rho\eta_c$:2nd, $D^{\text{bar}}D^*$:2nd)

✿ input : LQCD potential matrix @ $m_\pi=410\text{MeV}$

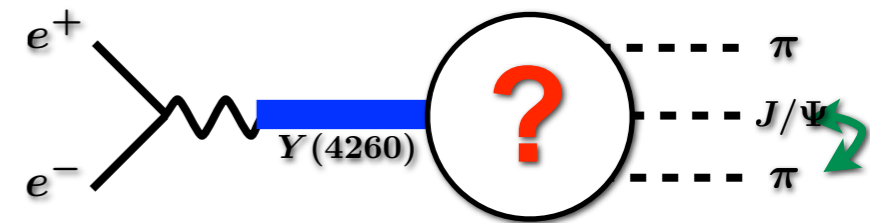
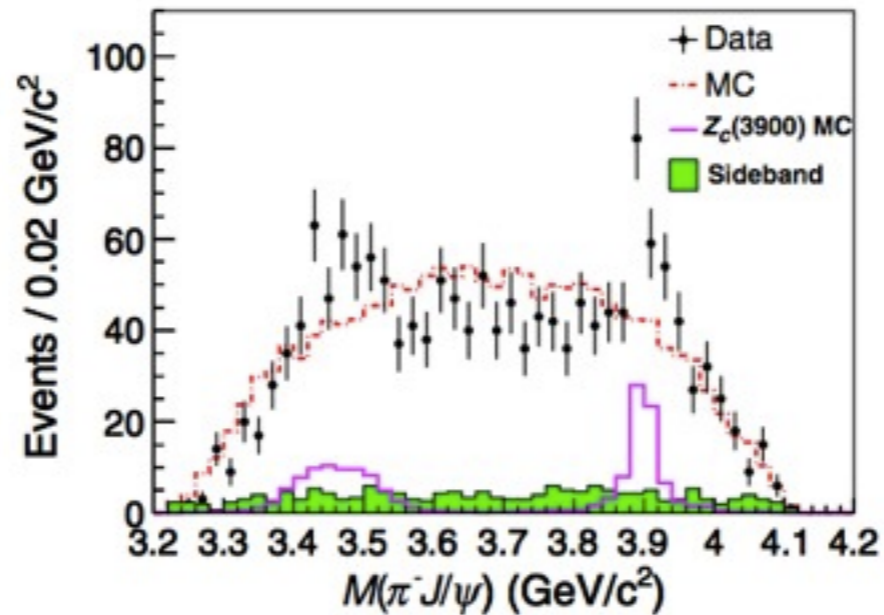
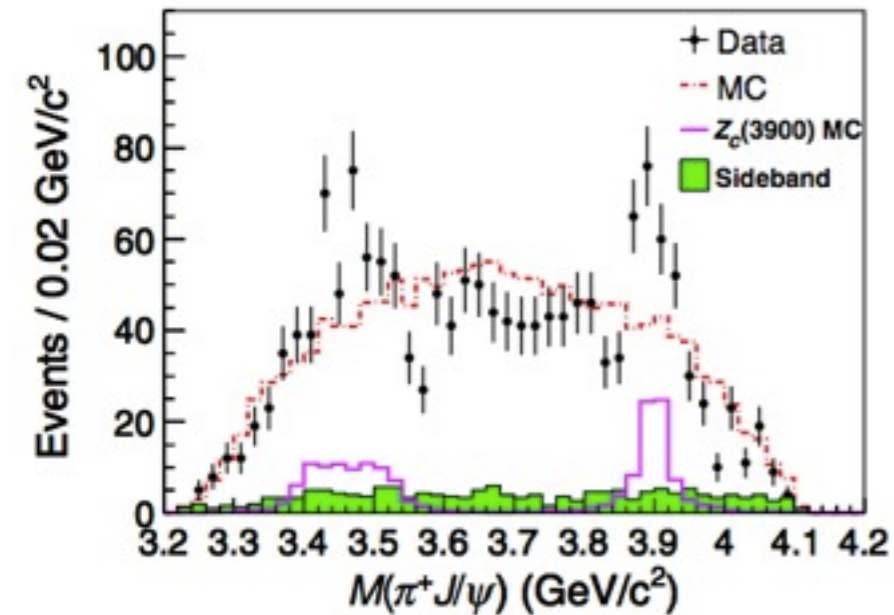
Poles of S-matrix



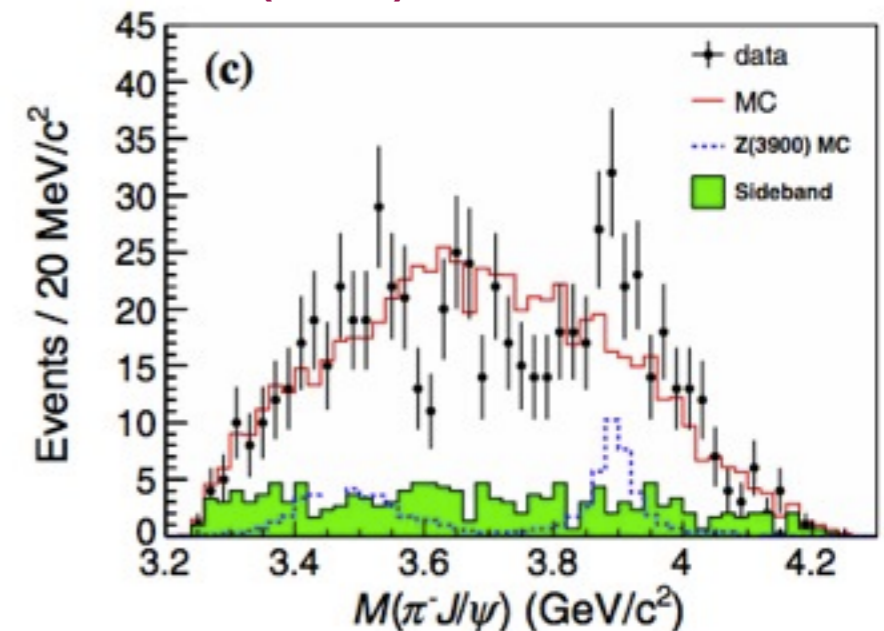
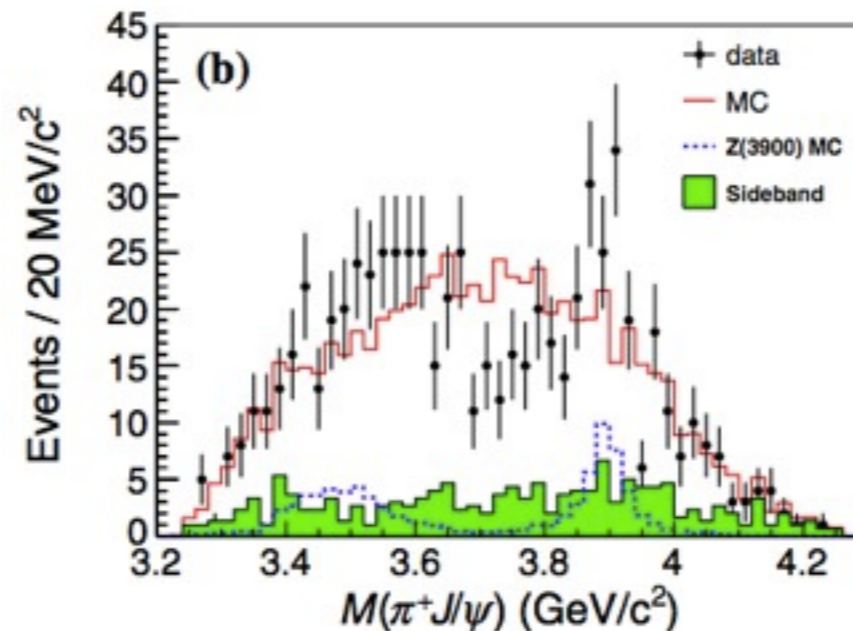
- ✓ “**Virtual (shadow)**” poles on the most adjacent complex energy plane for $Z_c(3900)$ energy region are found
- ✓ These poles contribute to threshold enhancement of amplitude

Y(4260) three-body decay : comparison with expt. data

BESIII Coll., PRL110, 252001, (2013).

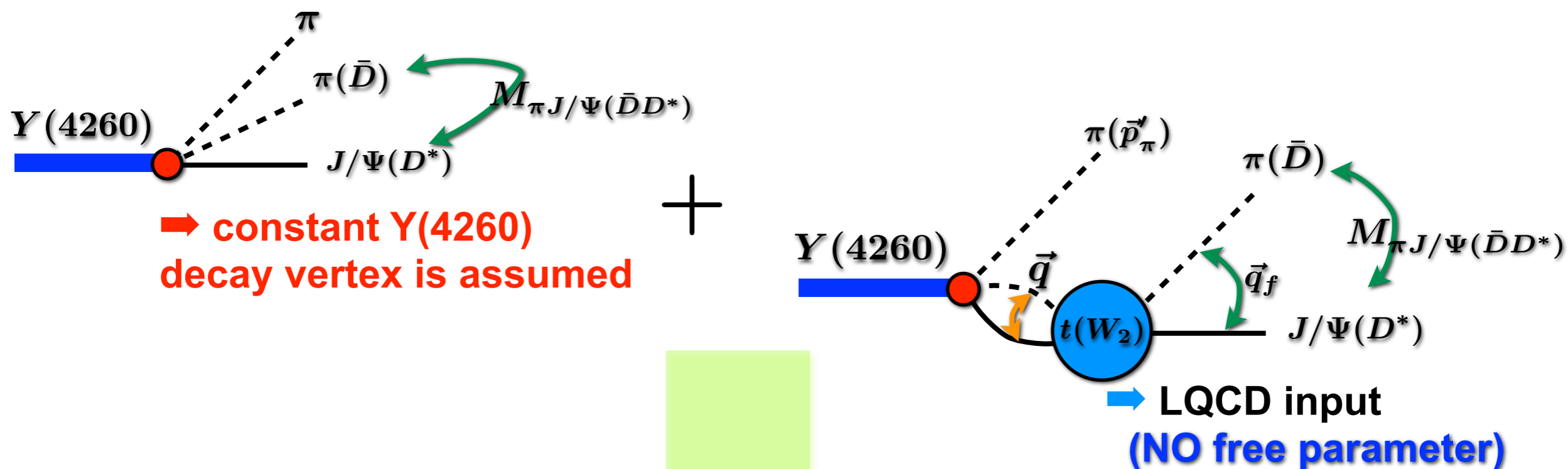


Belle Coll., PRL110, 252002, (2013).



Three-body decay of $Y(4260)$

$$d\Gamma \propto (2\pi)^4 \delta^4(P - p'_\pi - p_{\pi(\bar{D})} - p_{J/\Psi(D^*)}) d^3 p'_\pi d^3 p_{\pi(\bar{D})} d^3 p_{J/\Psi(D^*)} \sum_f |T_{if}|^2$$



✓ Leading order of Faddeev equations

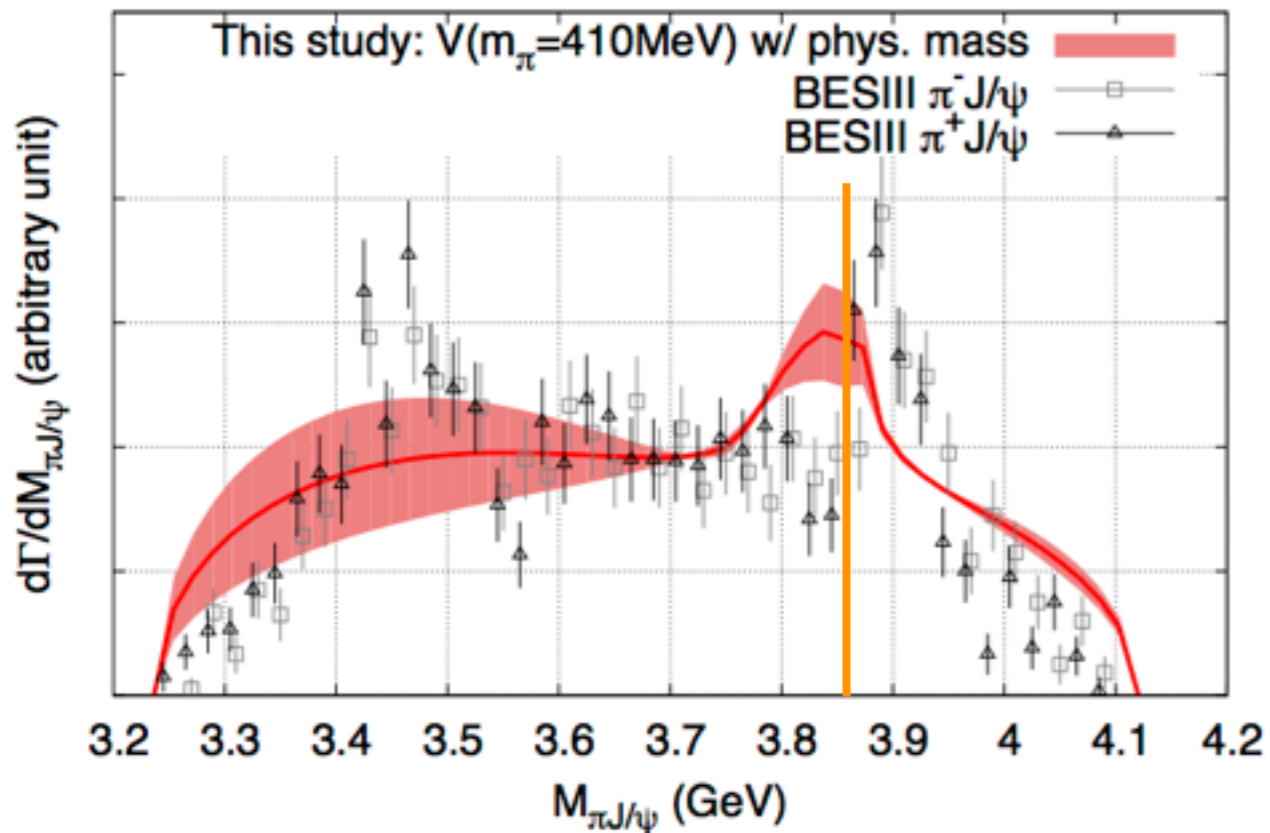
$$T_{if}(\vec{p}'_\pi, \vec{q}_f; W_3) = \sum_{n=\pi J/\Psi, \bar{D}D^*} C_n \left[\delta_{nf} + \int d^3 q \frac{1}{W_3 - E_\pi(\vec{p}'_\pi) - E_n(\vec{q}, \vec{p}'_\pi) + i\epsilon} t(\vec{q}, \vec{q}_f) \right]$$

physical hadron masses employed & S-wave calculation

✓ comparison with expt. data

✓ property of $Y(4260)$ decay

Invariant mass spectra ($\pi J/\psi$ & $D^{\text{bar}} D^*$)



parameters: $C_{D^{\text{bar}} D^*}/C_{\pi J/\psi} = R e^{i\theta}$
 $\rightarrow R=0.95(18), \theta=-58(44)$ deg.

★ $Z_c(3900)$ production ratio

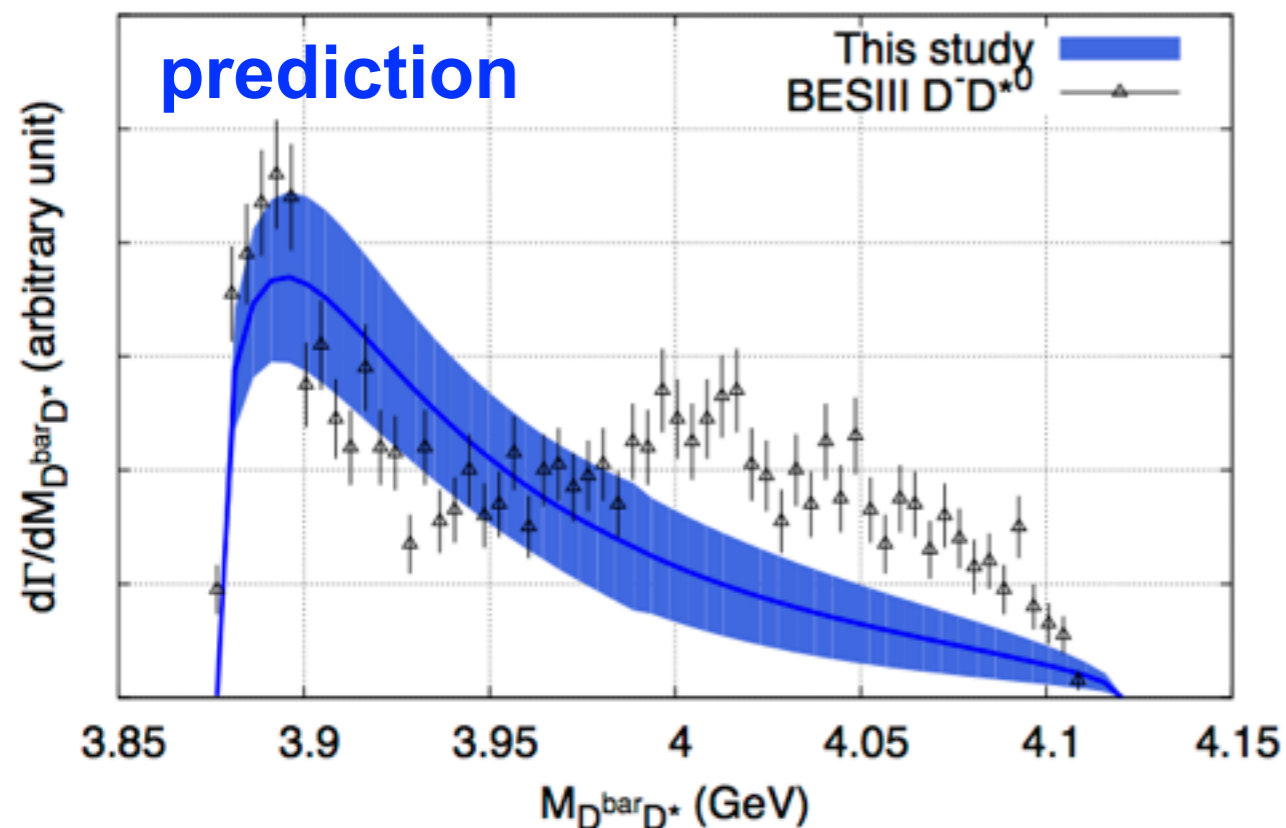
- LQCD prediction

$$27 \pm 7\%$$

- Expt.

$$21.5 \pm 3.3\% \text{ (BESIII)}$$

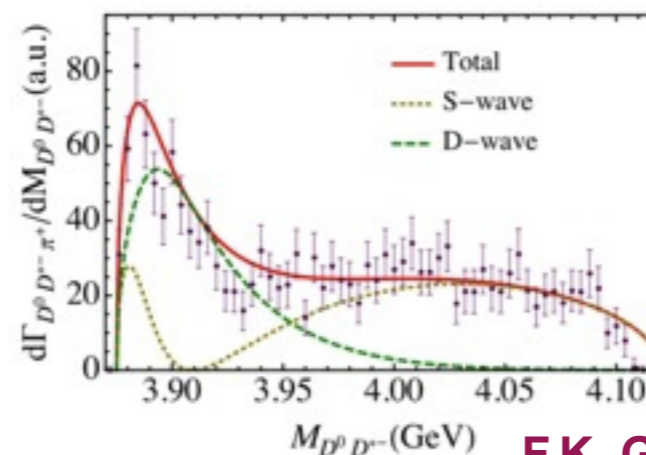
$$29.0 \pm 8.9\% \text{ (Belle)}$$



- Qualitatively good line shape

- Deviation from EXPT. data at high energies

\rightarrow higher partial wave??



Summary

❖ Applications of coupled-channel HAL QCD method

• Zc(3900) in $I^G(J^P)=1^+(1^+)$ channel on the lattice @ $m_\pi=410-700\text{MeV}$

➔ Large channel coupling between $\pi J/\Psi$ and $D^{\text{bar}}D^*$ is a key

➔ Heavy quark spin symmetry is seen in c.c. potentials

➔ Similar line shape of inv. mass to expt. is observed

▶ Zc(3900) is neither simple $D^{\text{bar}}D^*$ molecule nor $J/\Psi + \pi$ -cloud

▶ shadow poles on complex energy plane are found (w/ relatively large width)

❖ Physical point simulation is the next step

❖ Future plans

▶ other systems : Zc(4025), X(3872)

▶ extension to bottom systems