

Emerging lattice approach to K-Unitarity Triangle

Lehner + Lunghi + AS
in prep

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Lattice 2015; 07/17/15

Kobe-Japan

Outline

 $\frac{b \quad m^w \quad d}{\text{Expect Large CPV}}$

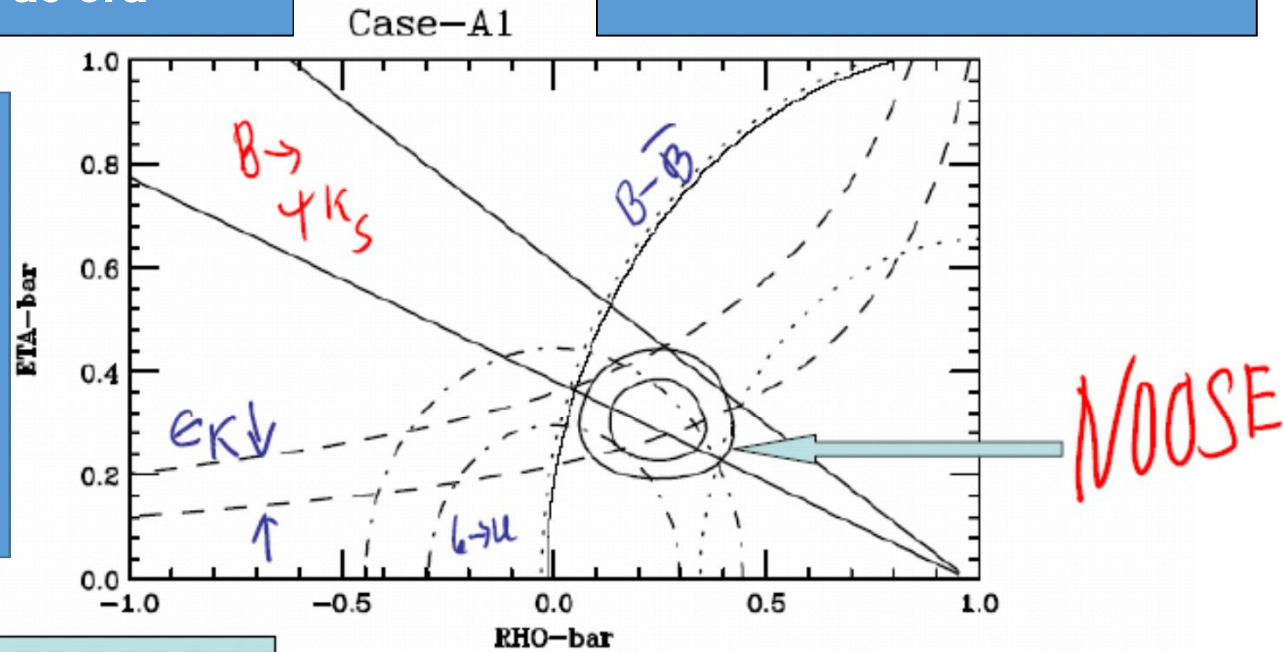
- Reminiscences: Lattice & *the* UT = "SUT" for Standard UT
- Recent developments on the lattice in tackling long-standing non-perturbative challenges in K-decays
- In concert with expts path towards a K-UT
- Its potential relevance: a particularly picturesque illustration
- Implications

In the "beginning" "Dawn" of
the asymmetric B-Fac era

Atwood & AS, hep-ph/0103197

B-CP Feb'01 Ise, Japan

1st Hint of
confirmation of CKM
CP description



Most bands due
To theory errors

New physics will be a perturbation, important
to use clean theory and lots of statistics.

Lunghi+AS, arXiv.0707.0212

($\sin 2\beta = 0.78 \pm 0.04$)

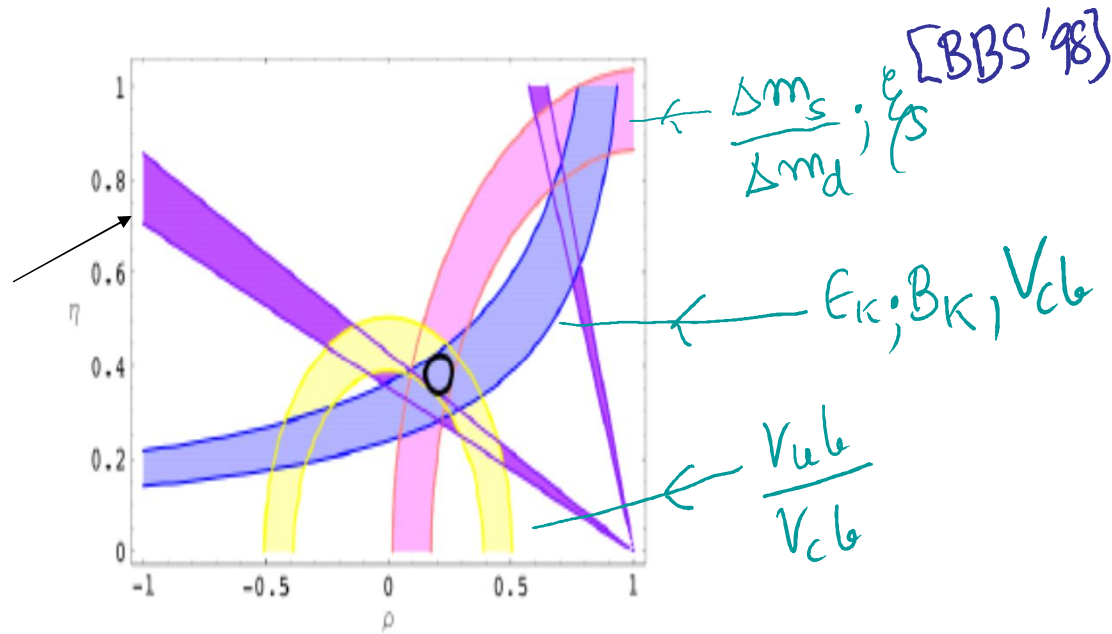


Figure 1: Unitarity triangle fit in the SM. The constraints from $|V_{ub}/V_{cb}|$, ϵ_K , $\Delta M_{B_s}/\Delta M_{B_d}$ are included in the fit; the region allowed by $a_{\psi K}$ is superimposed.

C ALSO
UTFITS '07

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Poster Designed by T. Iijima, Y. Iwasaki,
S. Kataoka, N. Katayama, K. Miyabayashi

小林益川理論が正解だった！ Bファクトリーが放った決定打

Courtesy: Tom Browder

Critical Role of the B factories in the verification of the KM hypothesis was recognized and cited by the Nobel Foundation

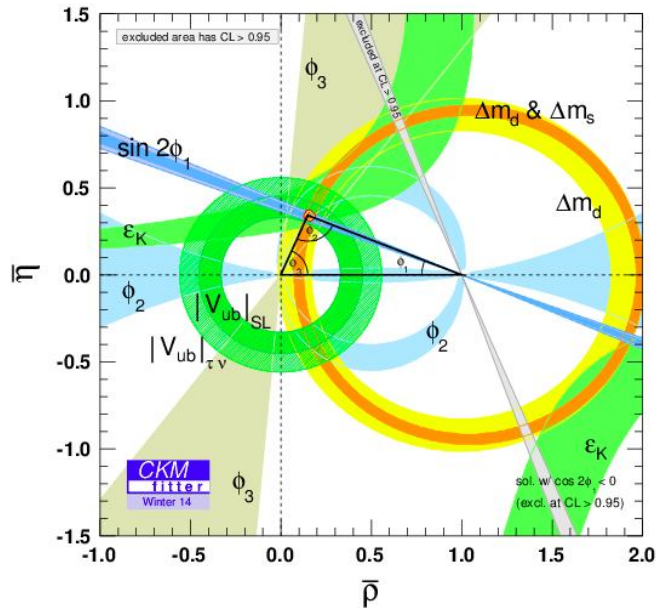
A single irreducible phase in the weak interaction matrix accounts for most of the CPV observed in kaons and B's.



CP violating effects in the B sector are O(1) rather than O(10⁻³) as in the kaon system.

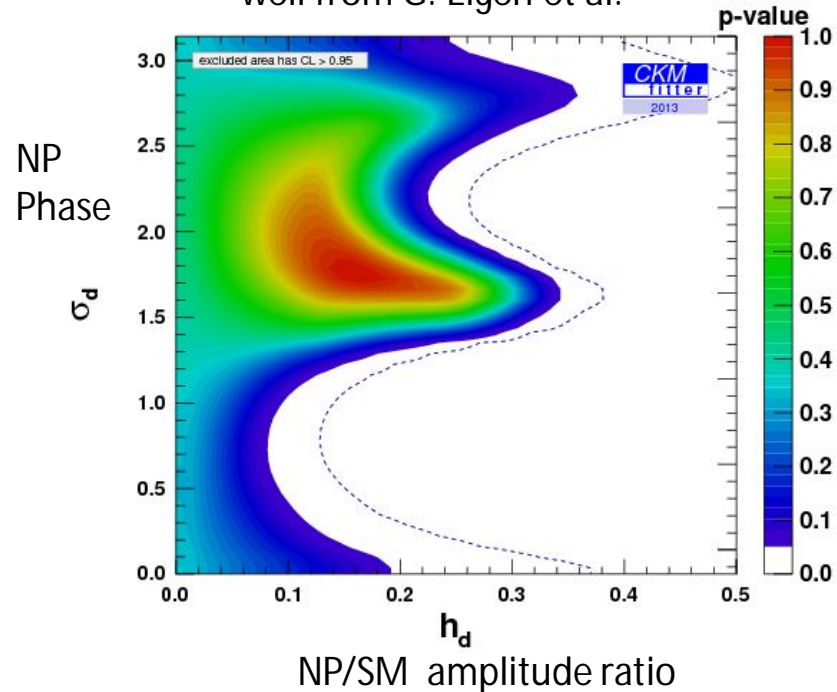
Results from Global Fits to Data (CKMFitter Group)

Great progress on φ_3 or γ (first from B factories and now in the last two years from LHCb (several new results at ICHEP2014)). These measure the phase of V_{ub}



Looks good
(except for an issue with $|V_{ub}|$)

ICHEP2014: Similar results from UTFIT (D. Derkach) as well from G. Eigen et al.



But a 10-20% NP amplitude in B_d mixing is perfectly compatible with all current data.

A lesson from history (I)

"A special search at Dubna was carried out by E. Okonov and his group. They did not find a single $K_L \rightarrow \pi^+ \pi^-$ event among 600 decays into charged particles [12] (Anikira et al., JETP 1962). At that stage the search was terminated by the administration of the Lab. The group was unlucky."

-Lev Okun, "The Vacuum as Seen from Moscow"

1964: $BF = 2 \times 10^{-3}$

A failure of imagination? Lack of patience?

CHRISTENSEN,
CANNON, FITCH
& TURLAY
BNL 1964

=> Precision! Precision! Precision!
Need of the day.

Analogously can lattice sharpen tests now via K's?

- In B's, in conjunction with experiments, Lattice WME helped in attaining a milestone in our understanding of CP
- Since m_K is ~ 10 times lighter, the non-perturbative effects are much more difficult and quantitatively a lot bigger, can the lattice meet this long-standing challenge and render K-tests become precise?

A dream for some

Blucher, Winstein and
Yamanaka '09

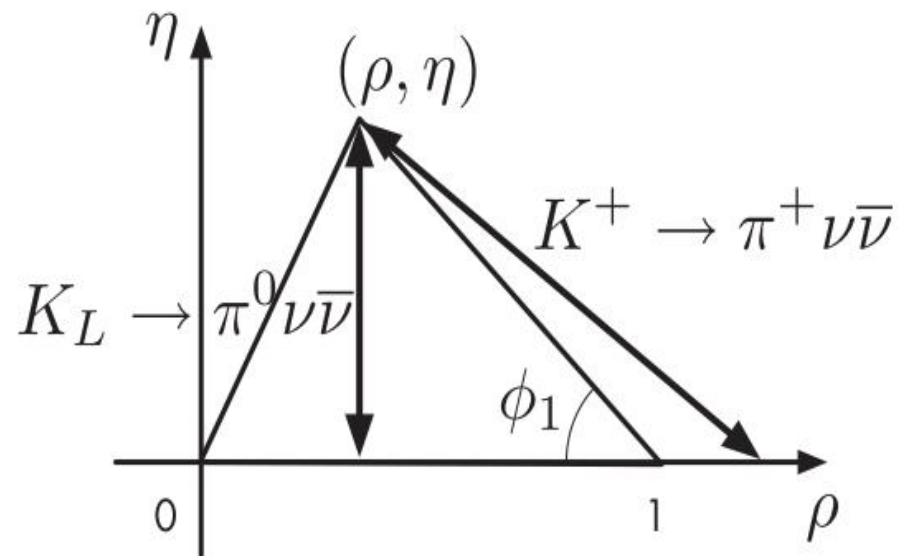


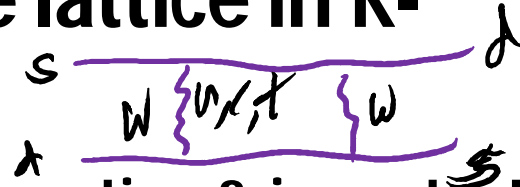
Fig. 14. Unitarity triangle.

A Faster way in the officing?

Promising developments on the lattice in K-decays.....RBC-UKQCD (1 of 4 pages)

- ε'/ε C. Kelly talk
- Personal perspective: a quest for $\sim 1/3$ of a century! O(8 grads)
- Started with CWB (Wilson); for this physics Chiral symm on the lattice is a pre-requisite [off-shoot B-physics] => on to DWF (with Tom B)=> RBC [with BNT became flagship project] use ChPT + quenched => huge quench[GP] pathologies=full QCD is mandatory for this physics not just χS ; full QCD + ChPT=> large chiral corrections => RBC-UKQCD[esp CP] direct K=> 2π a la Lellouch- Luscher @ threshold=> @physical kinematics.....

Promising developments on the lattice in K-decays.....RBC-UKQCD



- Long-distance (non-local) effects; most interesting & important in Δm_K because of extreme sensitivity to chiral structure of Heff see Beall, Bander + AS, PRL '82 $\delta O(40\%)$ Brod & Gorban

See N.Christ talk here & many more.....Look forward to Δm_K from lattice as a useful observable for constraining NP.

- ϵ_K LD $\delta O(7\%)$N.Christ talk here & many more
- $K^+ \Rightarrow \pi \nu \nu$ $\delta O(\text{few}\%)$Xu Feng talk
- $K \Rightarrow \pi e e$A. Lawson talk here; [A.Portelli]; C. Sachrajda @LAT'14
- \Rightarrow Pathways to K-UT

Bonus: forward to m. di, Si dai'10

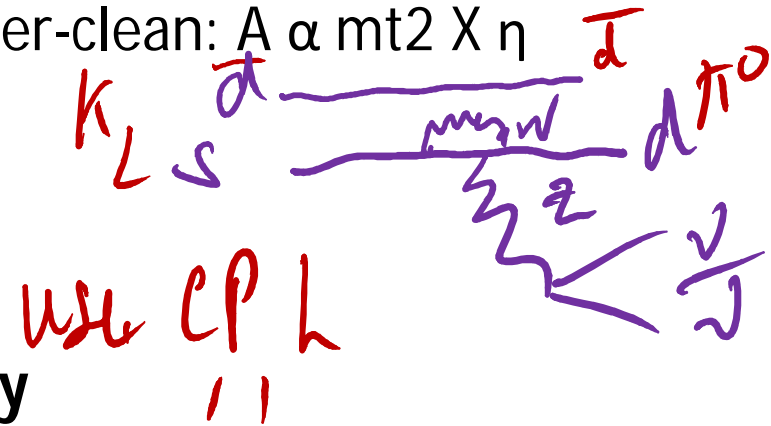
More on K-decays=>rare K's

Taku Yamamoto @CKM2014

- $K_L \Rightarrow \pi^0 \nu \nu$... "Gold-plated", i.e Theory super-clean: $A \propto m_t^2 X \eta$

LITTENBERG PRD '89

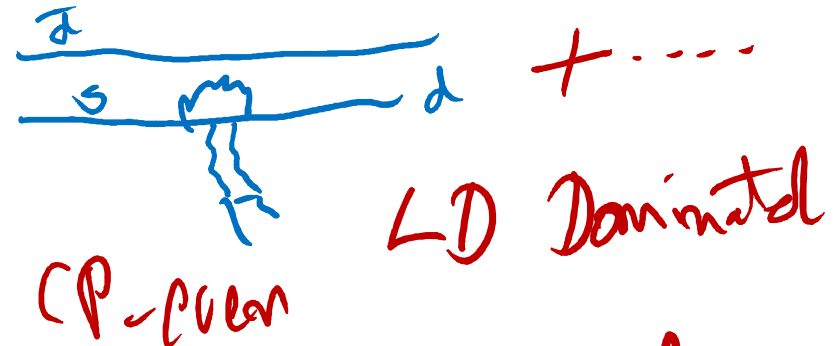
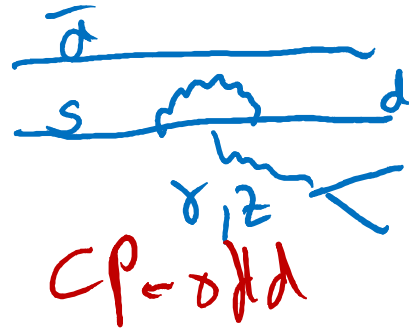
Nothing \rightarrow Nothing



- Observe: The above expt is exceedingly challenging (esp for precision) and expensive.
- Assertion: Once the (exptal) community realizes we mean business by reducing errors on $\text{Im } A_0$ to around $\sim 20\%$ they will get the message loud and clear: It is much more cost effective to invest in better lattice calculation(s) of eps'

$K_L \Rightarrow \pi^0 e e$

- Much more readily (seems) can do essentially the same physics as $K_L \Rightarrow \pi \nu \nu$
- Very rich; e.g can study energy asymm....
- Long-standing challenge for theory: Reliably quantify CP-conserving contamination



- Challenge for expt: huge background from $e e \gamma \gamma$
- $\text{Br}[K_L \Rightarrow \pi^0 e e]_{\text{dir-CP}} \sim 6 \times 10^{-12}$; $\text{CPC} \sim 2 \times 10^{-12}$
- $\text{Br}[K_L \Rightarrow \gamma \gamma e e] \sim 5.95 \times 10^{-7}$!! PDG Imposes severe demands on energy resolution

H. Greenlee
PRD '90

→ AJB '93

Why bother: Flavor alignment

- In the SM as you switch on weak interactions, gauge eigenstates no longer stay aligned with the mass eigenstates; CKM-matrix in fact monitors this misalignment
- As you go to BSMs, naturalness arguments strongly suggest a similar misalignment => new mixing matrix and likely $O(1)$ new CP-odd phase(s)
- While examples of this abound in specific models most telling perhaps is to consider the case of a geometric theory of flavor, based on warped extra-dim a la RS as its just about the most compelling

RANDALL+SUNDRUM '99

Points along 5th dim
 correspond to
 diff. eff.
 4d scale!

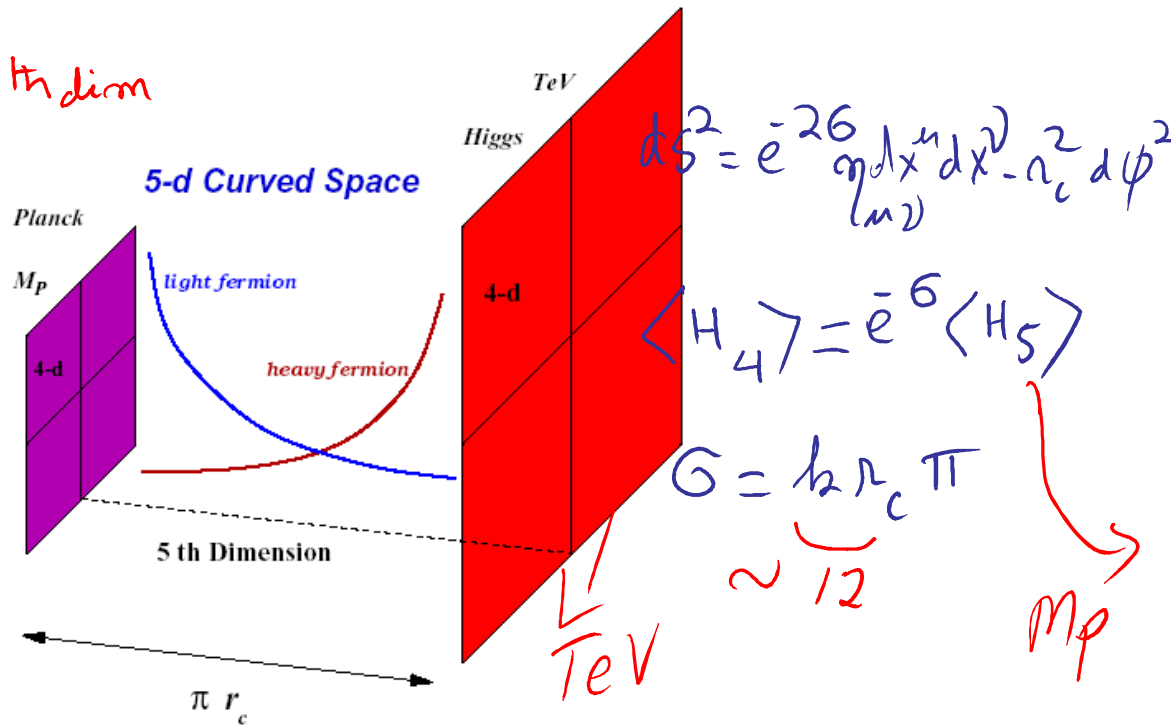


Figure 1: Warped geometry with flavor from fermion localization. The Higgs field resides on the TeV-brane. The size of the extra dimension is $\pi r_c \sim M_P^{-1}$.

Simultaneous resolution to hierarchy and flavor puzzles
 See Grosman + Neubert; Gherghetta + Pomarol; Davoudaisi, Hewett+ Rizzo

Fermion "geography" (localization) naturally explains:

- Why they are light (or heavy)
- Flavor structure examined in detail in (Agashe, Perez, AS'04) :
- FCNC for light quarks are severely suppressed automatically
- RS-GIM MECHANISM flavor changing transitions though at the *tree level* (resulting from rotation from interaction to mass basis) are suppressed roughly to the same level as the loop in SM => CKM mixings (& mass) hierarchy.
- O(1) CP ubiquitous;nedm, in fact ALL DIR-CP [$\epsilon'/\epsilon, \gamma, \Delta ACP(B \rightarrow K\pi), \Delta(\sin 2\beta); S[B \rightarrow K^* \rho\gamma]; \Delta ACP(D)..$] are an exceedingly important path to **BM**-phase and new physics
- Most flavor violations are driven by the top
-

Gedalia, Tsikoni + Perez '09

$$E_K, \Delta m_K : 10^3 \text{ TeV} \Rightarrow R_{SF} \sim 10 \text{ TeV}!$$

EXTENSIVE STUDIES by Blanke et al , '09; and by Cassagrande et al '08; &.....

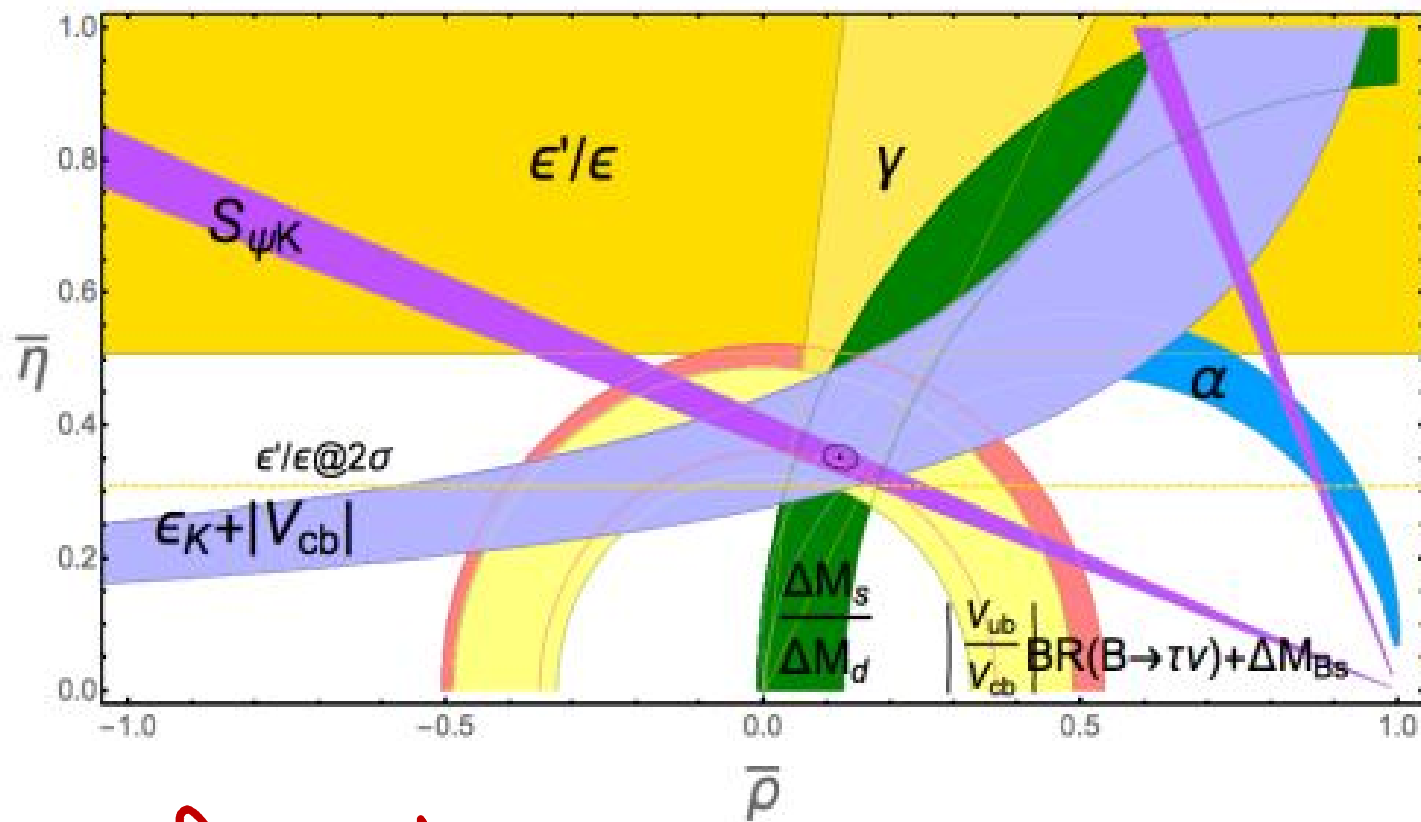
Localization parameters of the 3-families of quarks

$$\begin{array}{lll} c_{Q_1} = -0.579, & c_{Q_2} = -0.517, & c_{Q_3} = -0.473 \\ c_{u_1} = -0.742, & c_{u_2} = -0.558, & c_{u_3} = +0.339 \\ c_{d_1} = -0.711, & c_{d_2} = -0.666, & c_{d_3} = -0.553 \end{array}$$

Table from
M. Neubert
@Moriond09

⇒ masses of the 6 quarks in RS!
⇒ However, (i) RS does not predict masses.

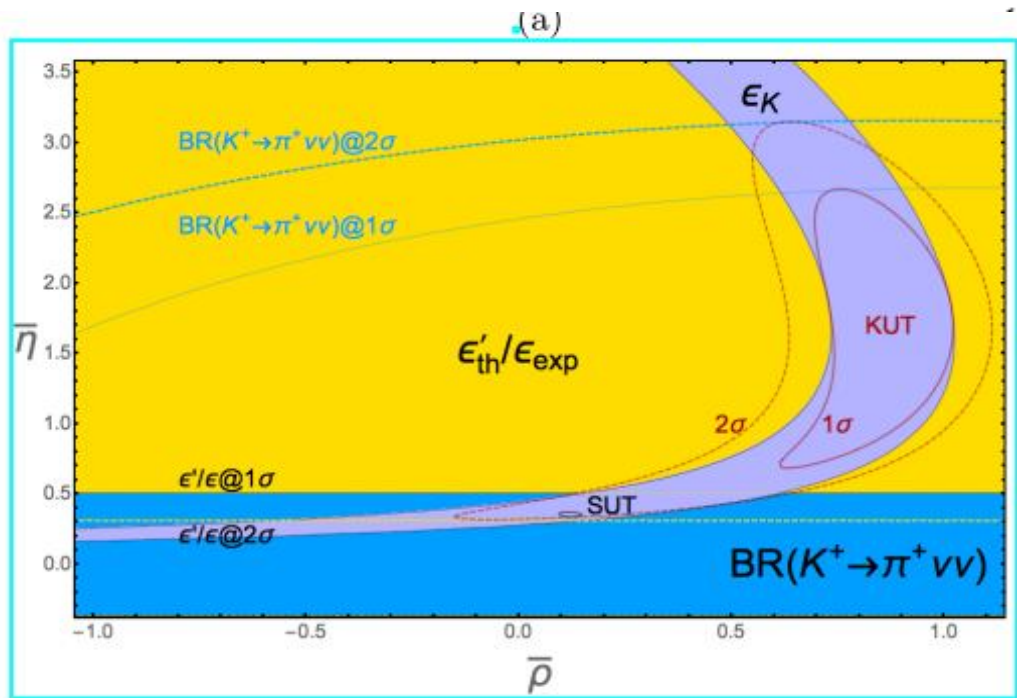
Lattice ϵ'/ϵ & SUT



LLS in prep

Sketch of an emerging K-UT

$$\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \begin{cases} (8.64 \pm 0.60) \times 10^{-11} & \text{SM} \\ (17.3^{+11.5}_{-10.5}) \times 10^{-11} & \text{E949 BNL} \end{cases}$$



$$\text{Re}\left(\frac{\epsilon'}{\epsilon}\right)_K = \begin{cases} (16.7 \pm 1.6) \times 10^{-4} & \text{PDG 2015} \\ (1.36 \pm 5.21_{\text{stat}} \pm 4.49_{\text{syst}}) \times 10^{-4} & \text{ABC+UKQCD '15} \end{cases}$$

LHS '15

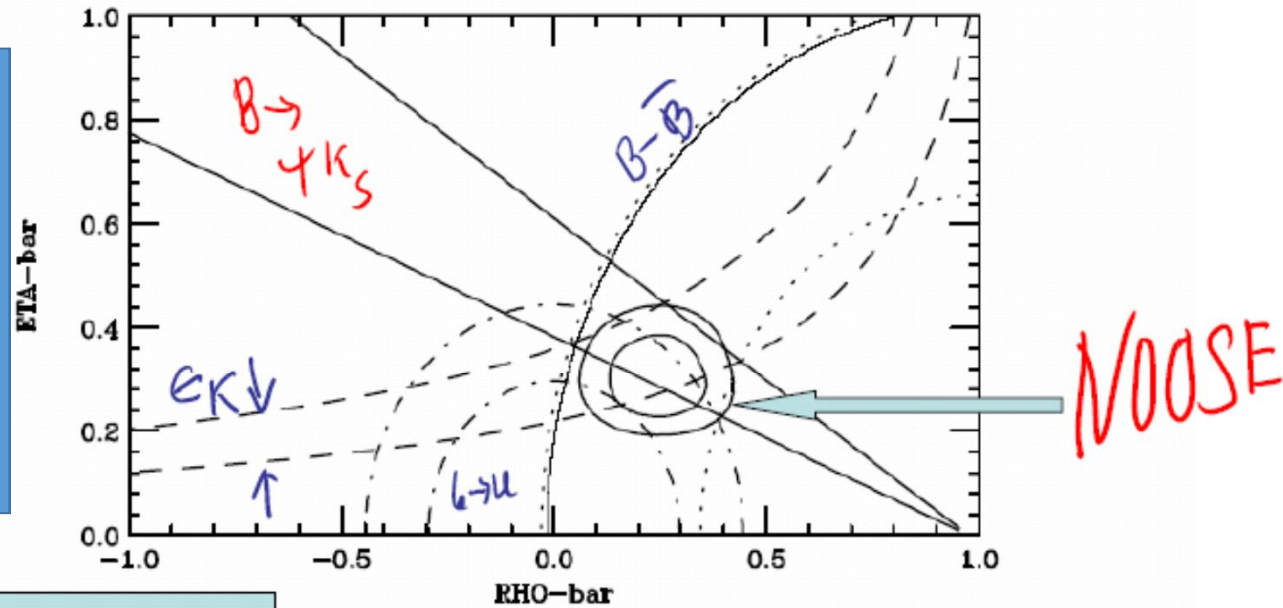
In the "beginning"

Atwood & AS, hep-ph/0103197

B-CP Feb'01 Ise, Japan

1st Hint of confirmation of CKM CP description

Case-A1



Most bands due
To theory errors

New physics will be a perturbation, important
to use clean theory and lots of statistics.

Legendary American
Philosopher

Yogi Berra	
	
Catcher / Manager / Outfielder	
Born: May 12, 1925 St. Louis, Missouri	
Batted: Left	Threw: Right
MLB debut	
September 22, 1946 for the New York Yankees	
Last MLB appearance	
May 9, 1965 for the New York Mets	
<i>Career statistics</i>	

The Future

- Yogi Berra: “Its difficult to make predictions, especially about the future”

Stolen from
Sheldon Stone



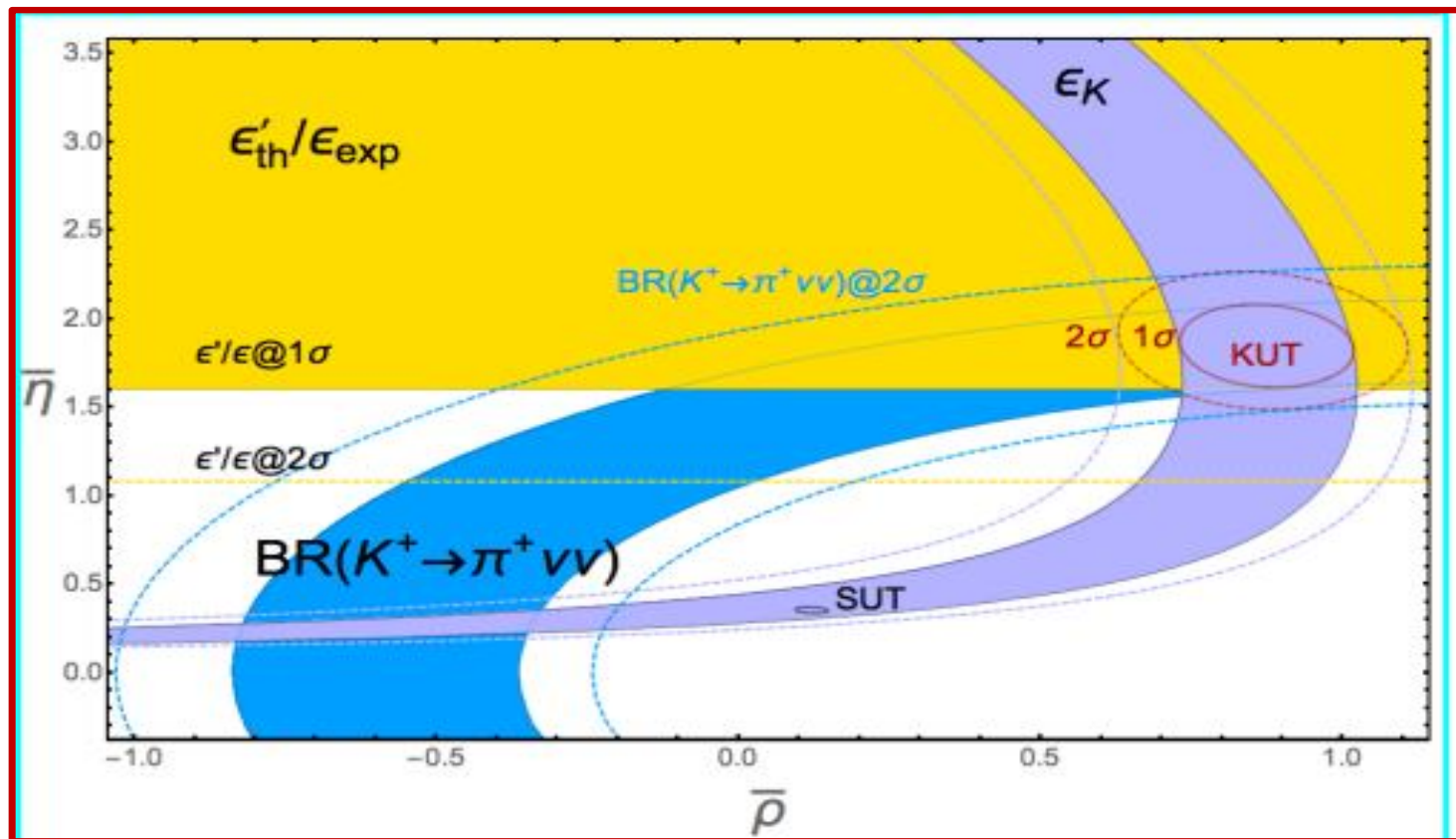
■ New York Yankees (1964, 1984-1985)
■ New York Mets (1972-1975)
Career highlights and awards
■ 15× All-Star selection (1948, 1949, 1950, 1951, 1952, 1953, 1954, 1955, 1956, 1957, 1958, 1959, 1960, 1961, 1962)
■ 13× World Series champion (1947, 1949, 1950, 1951, 1952, 1953, 1956, 1958, 1961, 1962, 1969, 1977, 1978)
■ 3× AL MVP (1951, 1954, 1955)
■ New York Yankees #8 retired
■ Major League Baseball All-Century Team
Member of the National
☆☆☆ Baseball Hall of Fame ☆☆☆
Induction 1972
Note 85.61% (second ballot)

BNL, 3/22/11; A. Sor...

Proof of the pudding: underlying method is systematically improvable

- BK in full QCD with DWF '07 error $O(7\%)$
 - ~2012 many discretizations , WA error $O(1-2\%)$
 - KI3, A2, fB's , BB's.....
 - mq's....
- 0 doubt that A0, A2 for eps' will not go that way for quite sometime to come.....to ~10% total
- After that EM& isospin effects need to be ascertained quantitatively.

POSSIBLE KUT CIRCA 2020

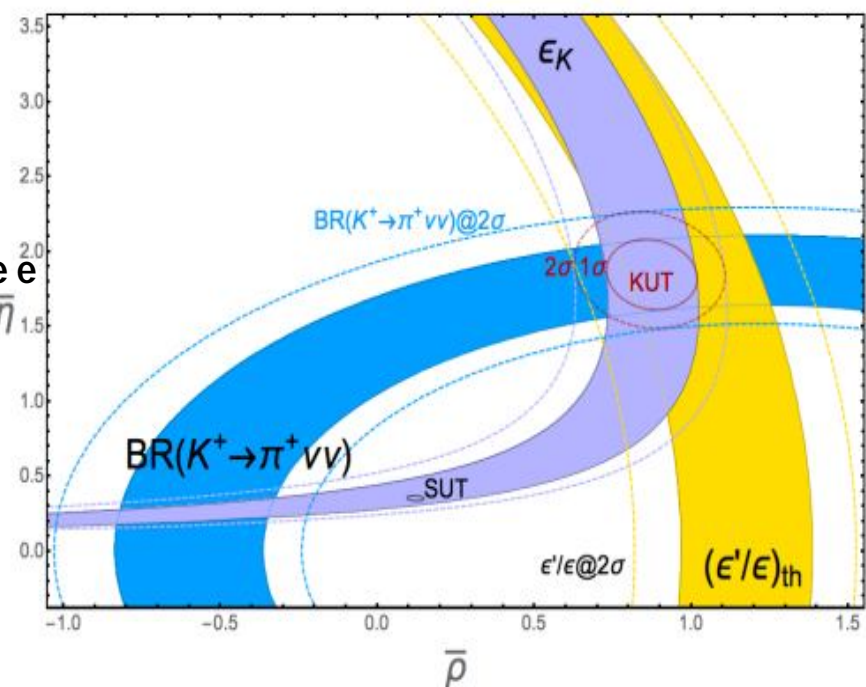
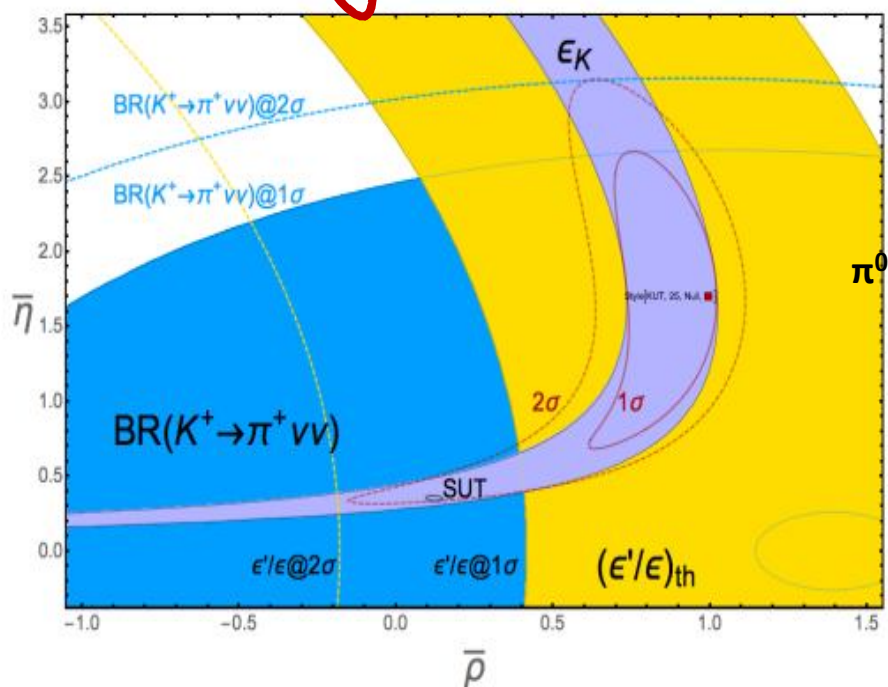


NO
unique
S, η !

A new observable on the horizon

CP conserving observable

$\epsilon'_{th}/\epsilon_K$



See behavior, Lunghi, A.G. in paper

Summary & Outlook

- In the past ~2 decades, in conjunction with experiments, lattice calculation of weak matrix elements, played a significant role in establishing that the SM-CKM paradigm of CP violation works to about an accuracy of ~ 15%.
- In the past few years, significant progress on the lattice has been made in tackling long-standing problems of ε'/ε , LD non-local contributions to Δm_K , ε_K , $K \rightarrow \pi + \nu\nu$, $K \rightarrow \pi e e$
- In conjunction with existing expt info and with further improvements therein, a unitarity triangle based primarily on K-decays will become available.
- Advantage?: When searching for small effects, diff. perspectives may be useful. [Moreover, have reservations of global fits; e.g B & α have issues]
- This [combined] strategy should lead to more stringent tests of the SM and for clues to new phenomena