

# Search for $ppK^-$ in exclusive $pp \rightarrow pK^+\Lambda$ reaction using Partial Wave Analysis

Robert Münzer  
for the FOPI and HADES Collaboration

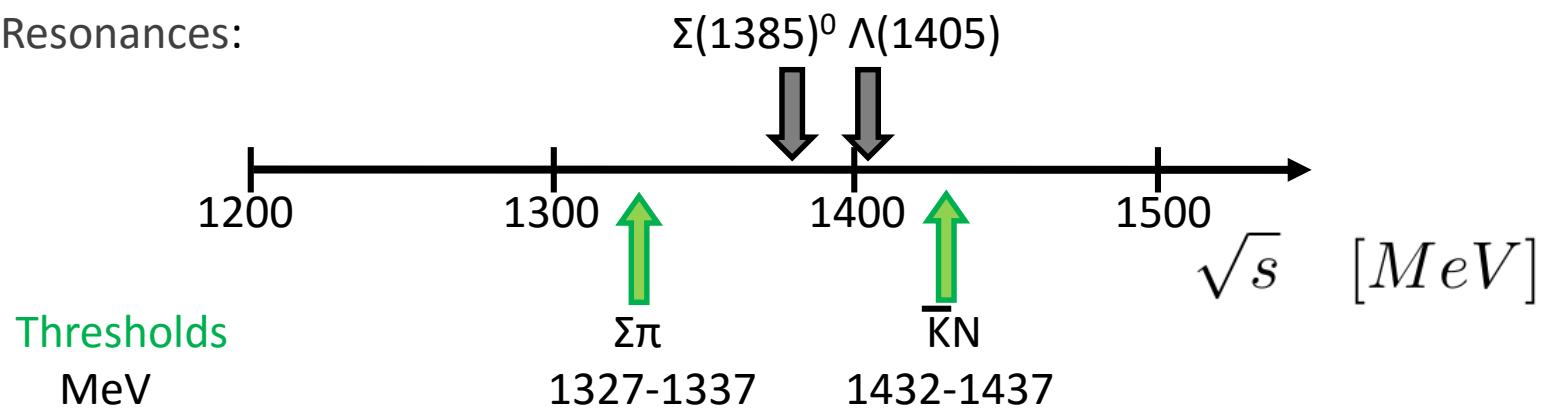
Excellence Cluster Universe, Technical University of Munich

# Outline

- Introduction: Kaonic Cluster in theory and experiment
- Results for exclusive measurement in  $p + p$  from HADES + FOPI
  - Partial Wave Analysis approach
- Combined Data Analysis Data samples
  - Parallel Analysis different exclusive data samples.
- Summary
- Outlook

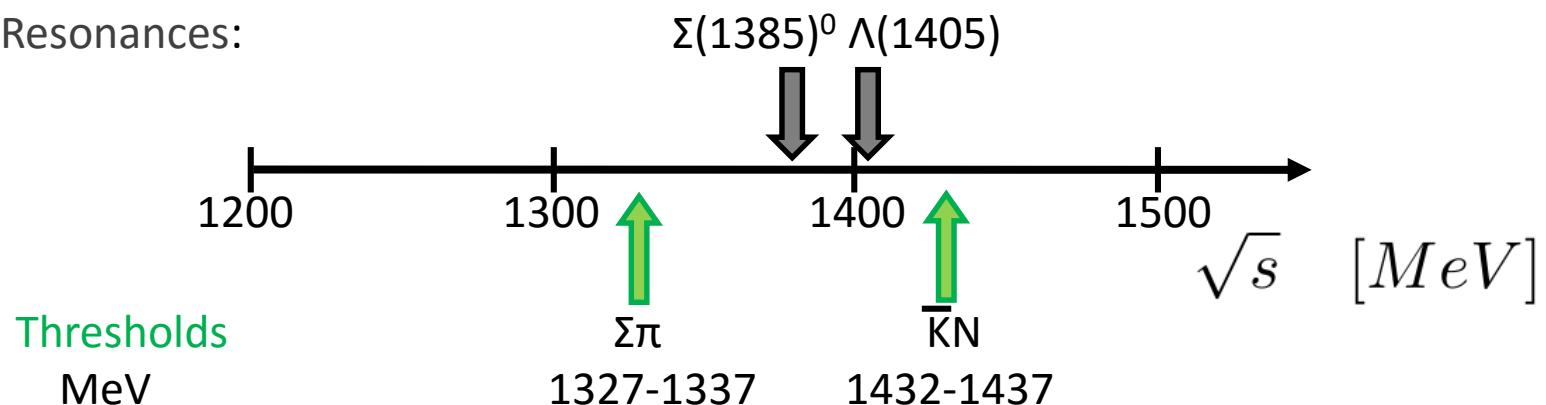
# Resonance near $\bar{K}N$ Threshold

Resonances:

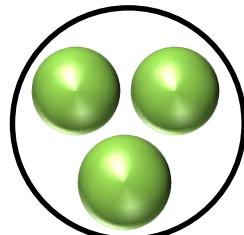


# Resonance near $\bar{K}N$ Threshold

Resonances:

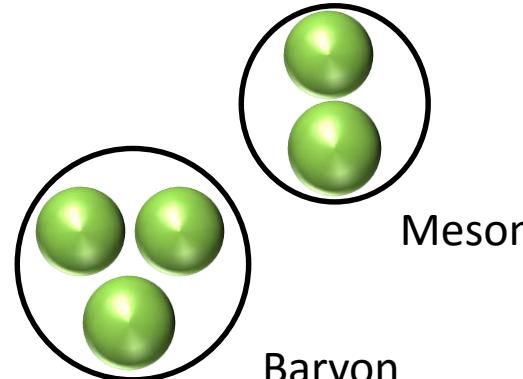


$\Sigma(1385)$



3 quark

$\Lambda(1405)$



Baryon

Meson

# Kaonic Cluster



## Theoretical Predictions

Chiral, energy dependent

	var. [DHW09, DHW08]	Fad. [BO12b, BO12a]	var. [BGL12]	Fad. [IKS10]	Fad. [RS14]
$BE$	17–23	26–35	16	9–16	32
$\Gamma_m$	40–70	50	41	34–46	49
$\Gamma_{nm}$	4–12	30			

Non-chiral, static calculations

	var. [YA02, AY02]	Fad. [SGM07, SGMR07]	Fad. [IS07, IS09]	var. [WG09]	var. [FIK <sup>+</sup> 11]
$BE$	48	50–70	60–95	40–80	40
$\Gamma_m$	61	90–110	45–80	40–85	64–86
$\Gamma_{nm}$	12			~20	~21

**Binding Energy (BE):**

10-100 MeV

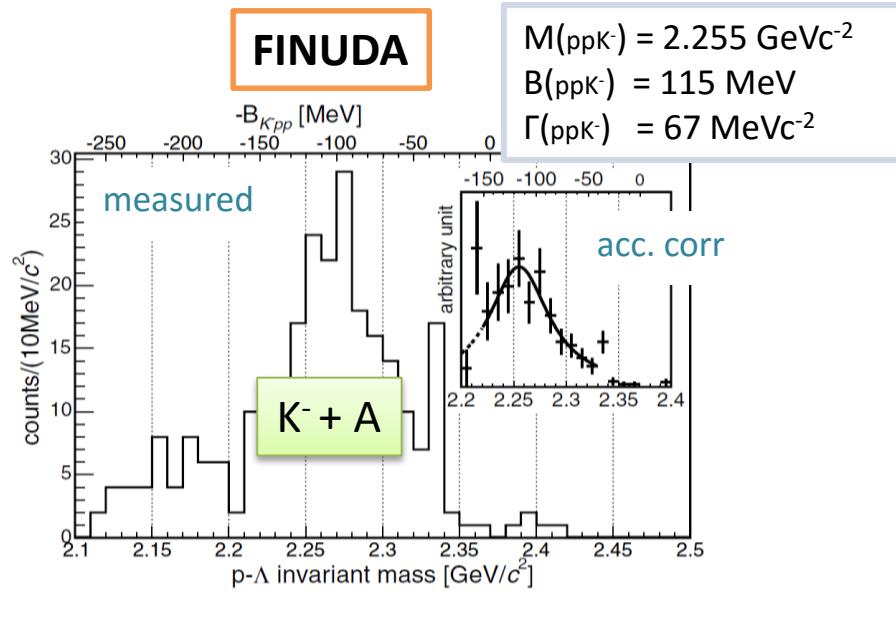
**Mesonic Decay ( $\Gamma_m$ )**

30-110 MeV

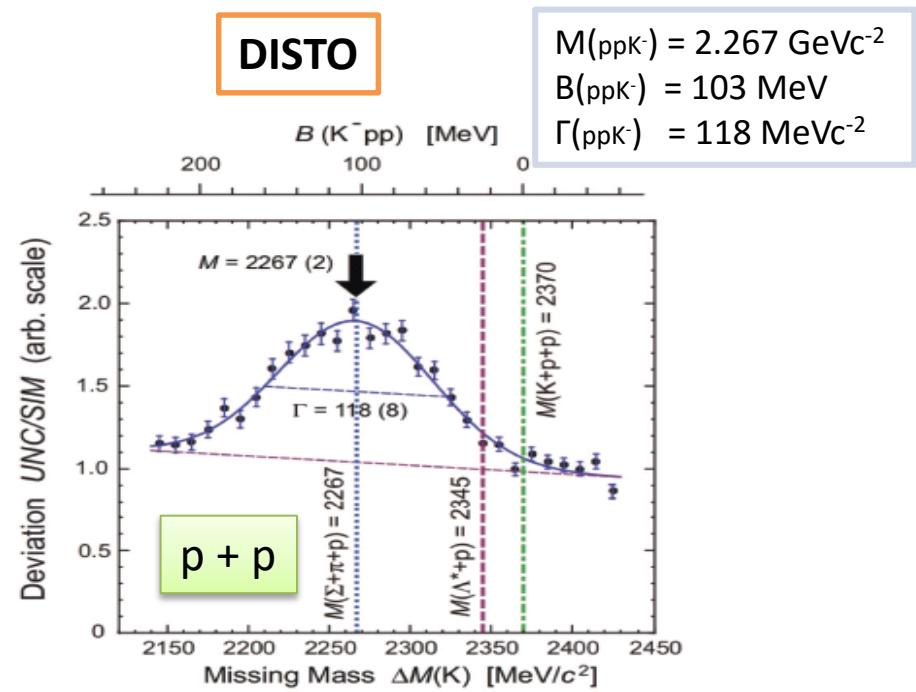
**Non-Mesonic Decay ( $\Gamma_{nm}$ )**

4-30 MeV

# Experimental Results on ppK<sup>-</sup>



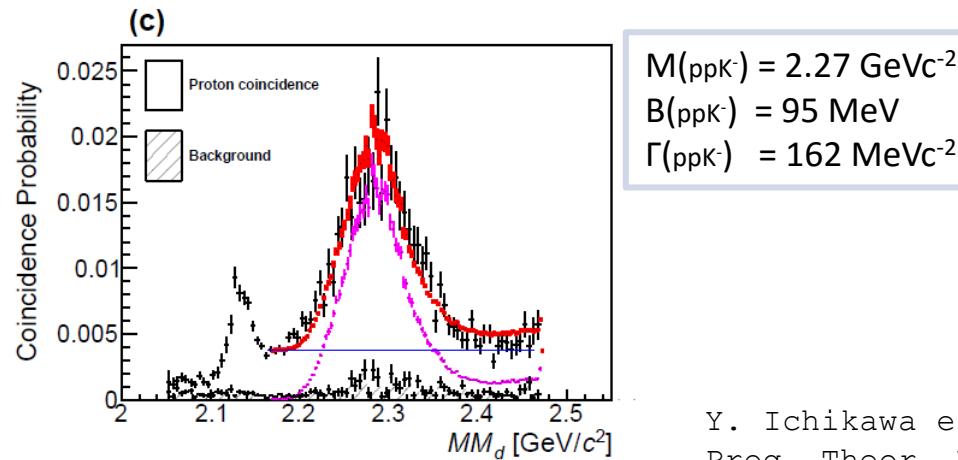
M. Agnello et al.  
 Phys.Rev.Lett.**94** (2005)



T. Yamazaki et al.  
 Phys.Rev.Lett.**104**, (2010)

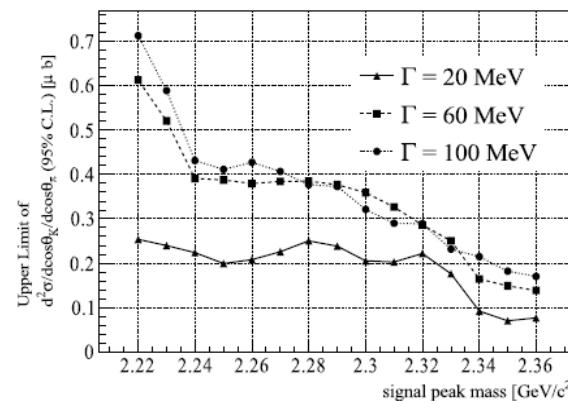
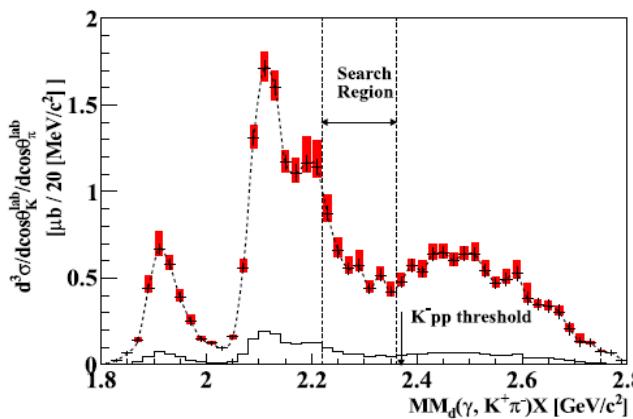
# Experimental Results on ppK<sup>-</sup>

E-27 JParc



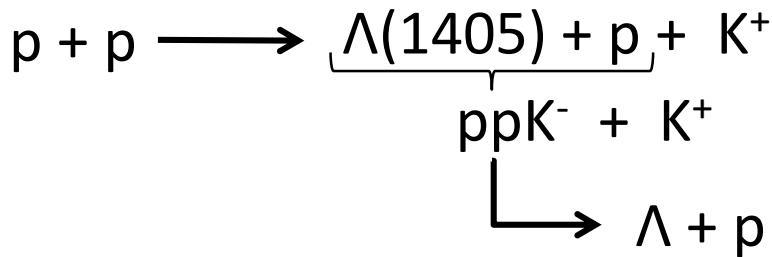
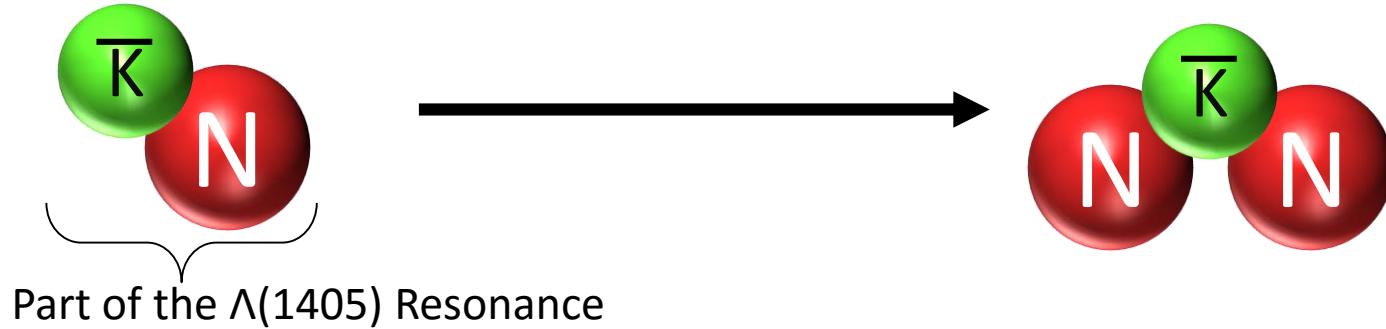
Y. Ichikawa et al.  
 Prog. Theor. Exp. Phys. 2013

LEPS/ SPRING8

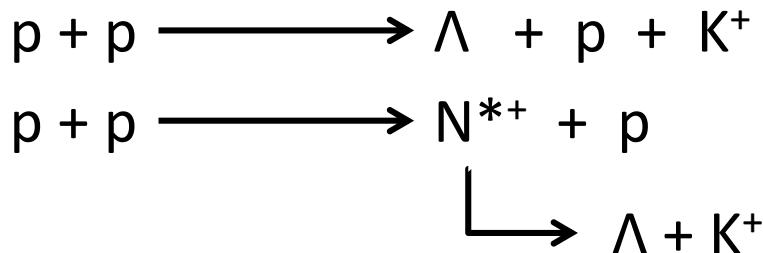


A.O. Tokayasu et al.  
 Phys.Lett. B728, (2014)

# Kaonic Cluster



**Physical Background:**



**$N^{*+}$  - Resonances**

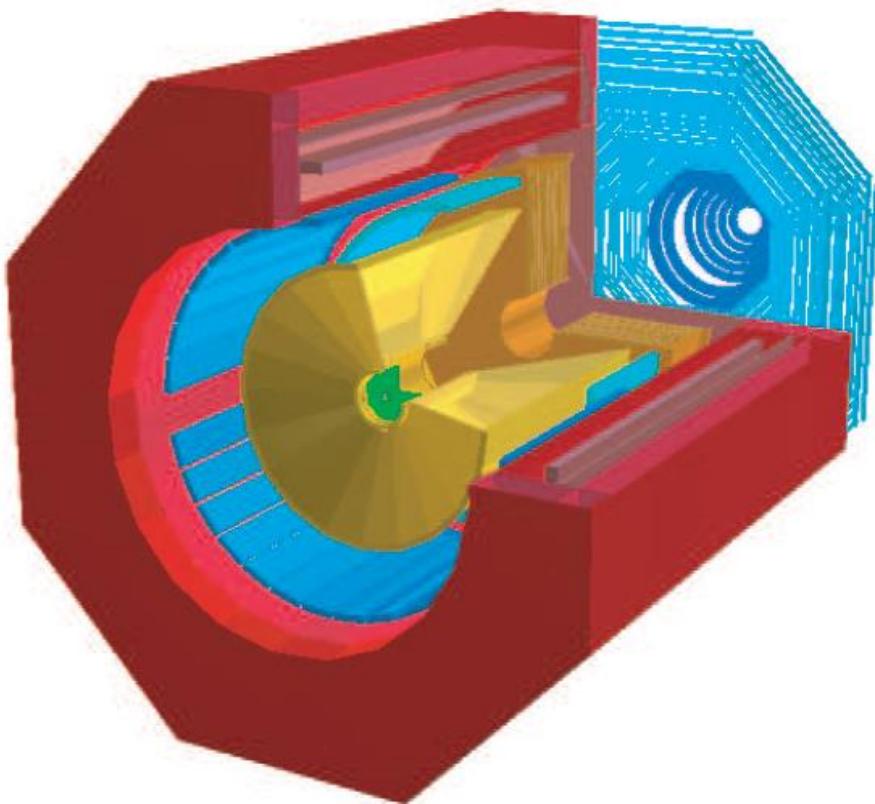
	Mass [ $\text{GeV}/c^2$ ]	Width [ $\text{GeV}/c^2$ ]	$\Gamma_{\Lambda K}/\Gamma_{All}$ %
$N(1650)S_{11}$	1.655	0.150	3-11
$N(1710)P_{11}$	1.710	0.200	5-25
$N(1720)D_{13}$	1.720	0.250	1-15
$N(1875)D_{13}$	1.875	0.220	$4 \pm 2$
$N(1880)P_{11}$	1.870	0.235	$2 \pm 1$
$N(1895)S_{11}$	1.895	0.090	$18 \pm 5$
$N(1900)P_{13}$	1.900	0.250	0-10

J. Beringer  
Phys. Rev. D86 (2012)

# Experimental Data

# The FOPI Experiment

SIS18 GSI Darmstadt



Beam Energy: 3.1 GeV

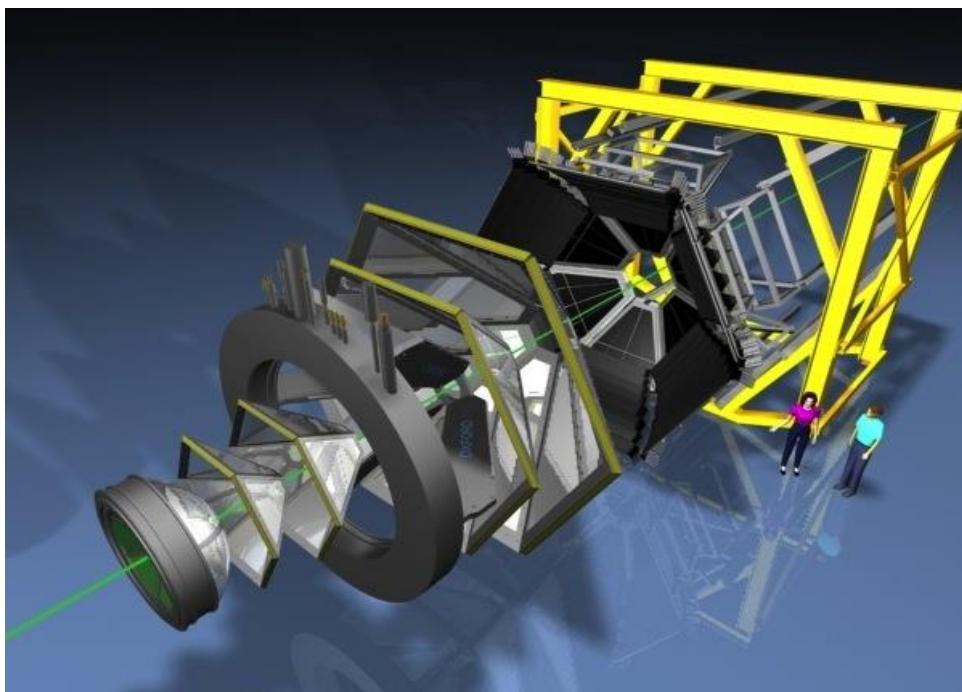
- Fixed-target Setup
- Full azimuthal coverage,  $5^\circ - 110^\circ$  in polar angle
- Momentum resolution  $\approx 7\% - 15\%$
- Particle identification via  $dE/dx$  & ToF

Trigger Detector – SiAViO:

$\Lambda$  – Enhancement:  $14.1 \pm 7.9(stat)_{-0.6}^{+4.3}$

# The HADES experiment

High Acceptance Di-electron Spectrometer  
GSI, Darmstadt



Beam Energy: 3.5 GeV

- Fixed-target Setup
- Full azimuthal coverage,  $15^\circ - 185^\circ$  in polar angle
- Momentum resolution  $\approx 1\% - 5\%$
- Particle identification via  $dE/dx$  & ToF

HADES Coll. (G. Agakishiev et al.),  
Eur. Phys. J. **A41** (2009)

# Total Data Set

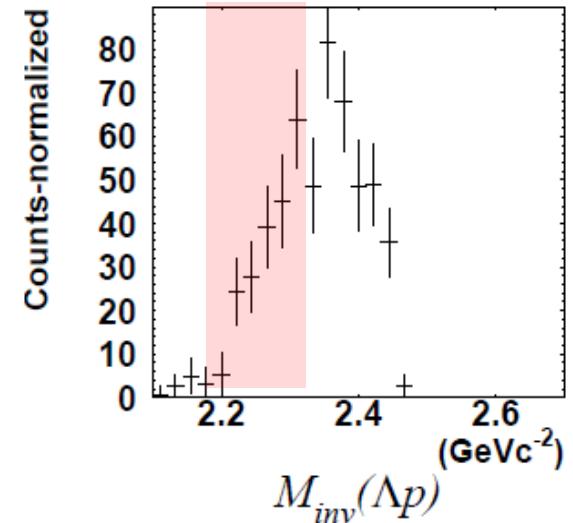
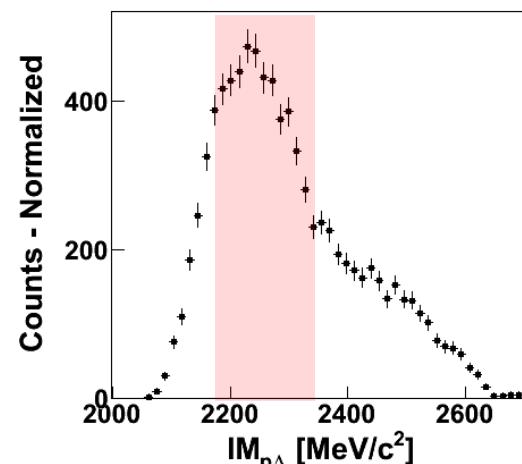
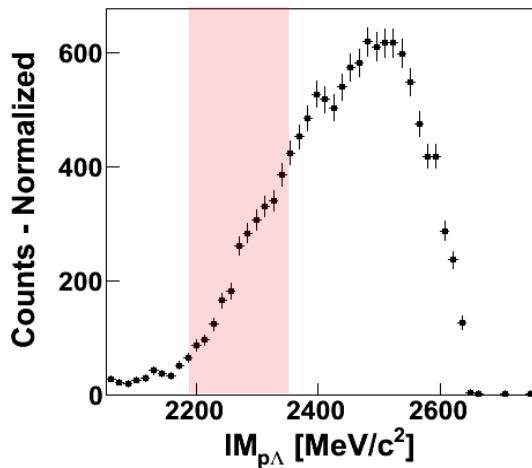
Hades Data  $E_{beam}=3.5$  GeV

Had. Wall Data  $E_{beam}=3.5$  GeV

FOPI Data  $E_{beam}=3.1$  GeV

Total Number of exclusive Events: 21000

Total Number of exclusive Events: 903



No Peak Visible  
No Signal?

R. Münzer, Hyperfine Interaction, in print

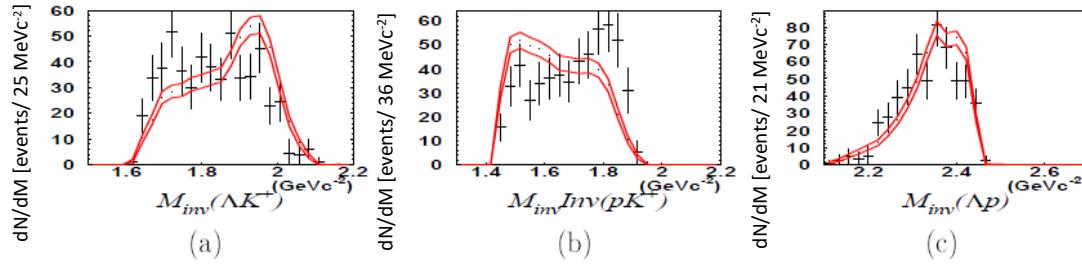
G. Agakishiev, Phys. Lett. B742 (2015) 242–248

# Model Comparison

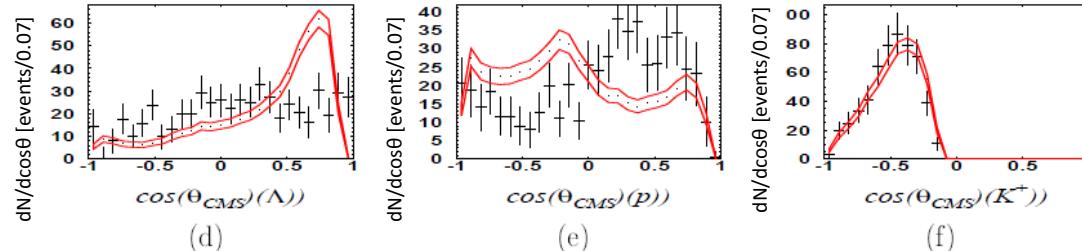
Phase Space Simulation  
Partial Wave Analysis

# Phase Space Simulation

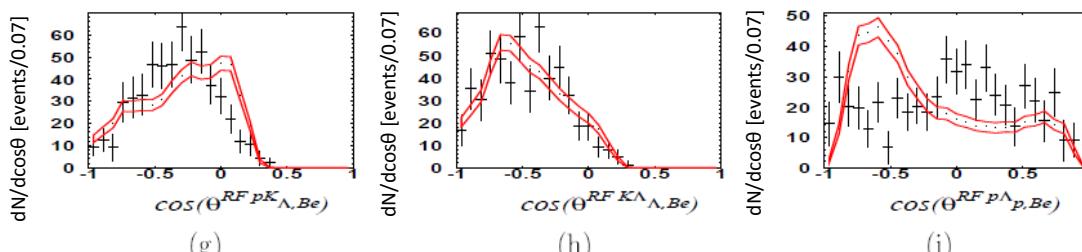
Masses



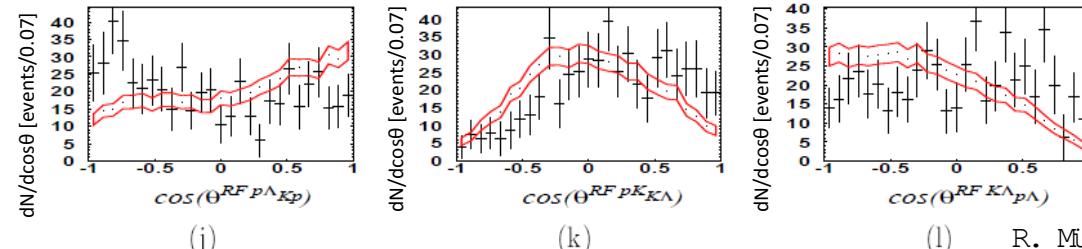
CMS Angle



G.-J.-Angle

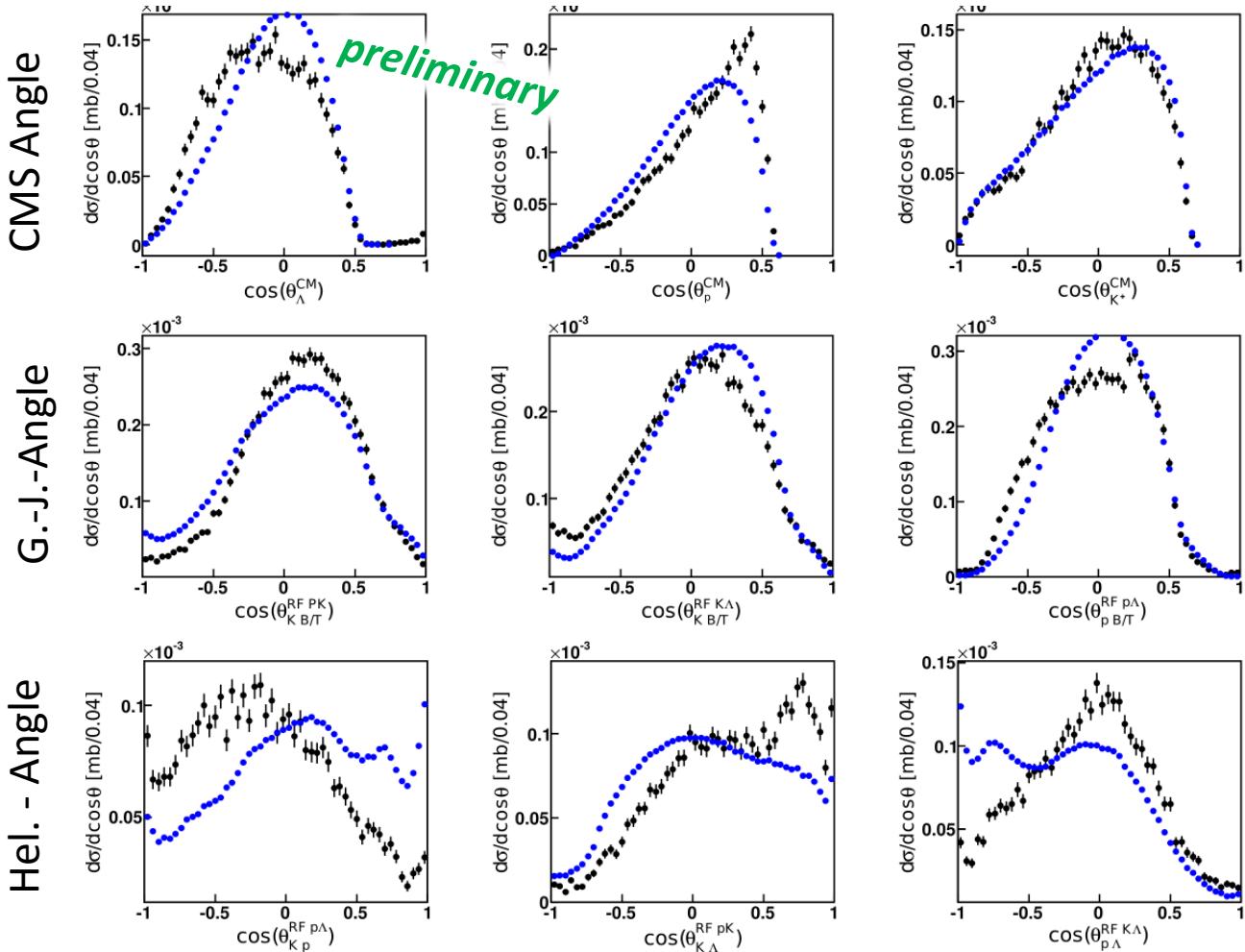


Hel. - Angle



+ Experimental Data  
— pp → p K<sup>+</sup> Λ Phase Space

# Phase Space Model



**Inside HADES acceptance**

- Experimental Data
- $pp \rightarrow p + K^+ + \Lambda$  Phase Space

G. Agakishiev, Phys. Lett. B742 (2015) 242–248

# Partial Wave Analysis

## Bonn-Gatchina PWA Framework

A. Sarantsev et.al., Eur.Phys J A 25 2005

### Cross-section Decomposition

$$d\sigma = \frac{(2\pi)^4 |A|^2}{4|k|\sqrt{s}} d\phi(P, q_1, q_2, q_3), \quad P = k_1 + k_2$$

$A$  : reaction amplitude  $A \propto A_{tr}^\alpha(s)$  (Transition amplitude of wave  $\alpha$ )

$k$  : 3-momentum of the initial particle in the CM

$s - P^2$  :  $(k_1 + k_2)^2$

$d\phi(P, q_1, q_2, q_3)$ : invariant three-particle phase space

### Parameterization of the Transition

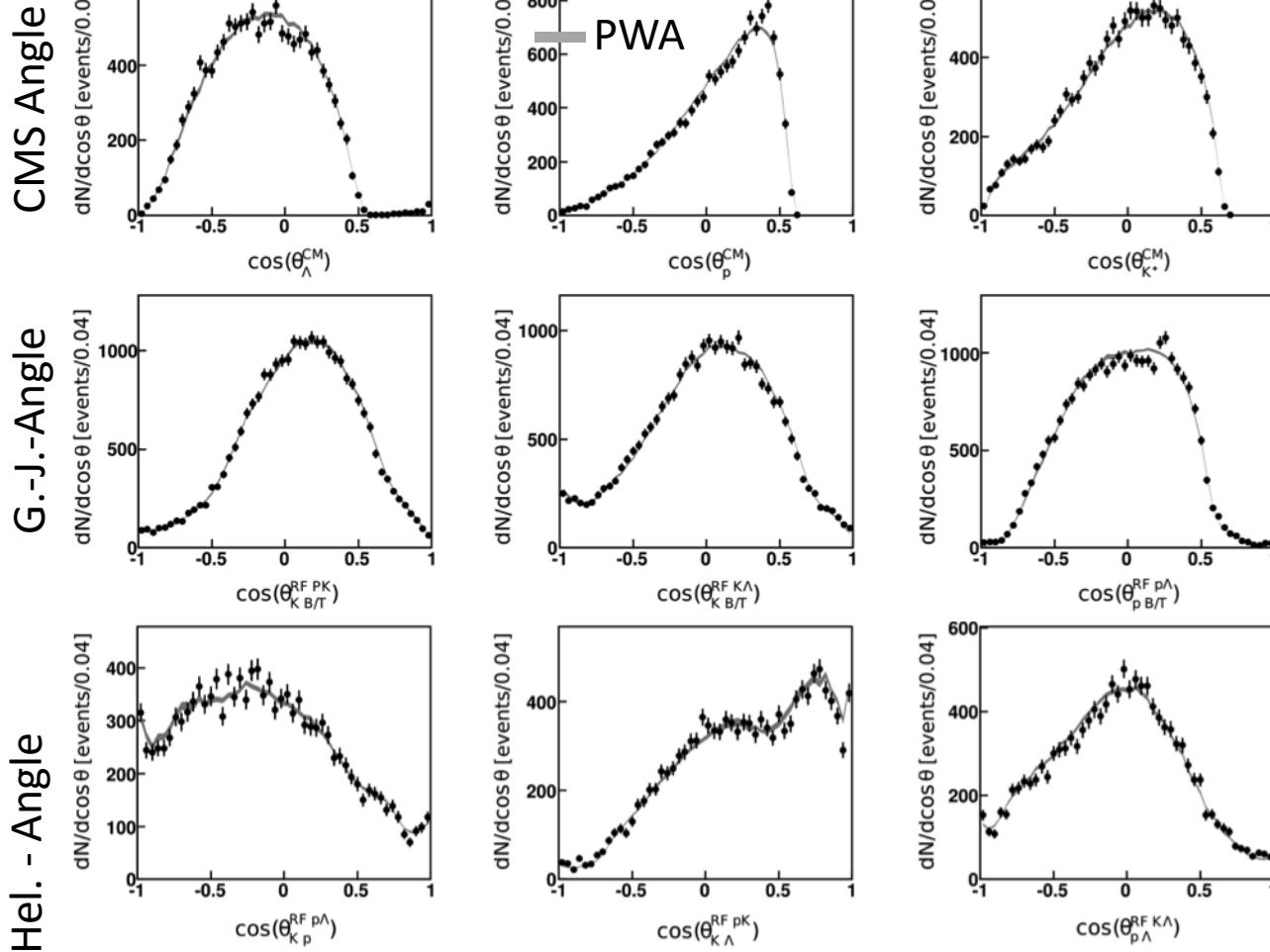
$$A_{tr}^\alpha(s) = (a_1^\alpha + a_3^\alpha \sqrt{s}) e^{ia_2^\alpha}$$

$a_1^\alpha$  Constant amplitude

$a_2^\alpha$  Phase

$a_3^\alpha$  Energy dependent amp.

# Four Best PWA Solutions

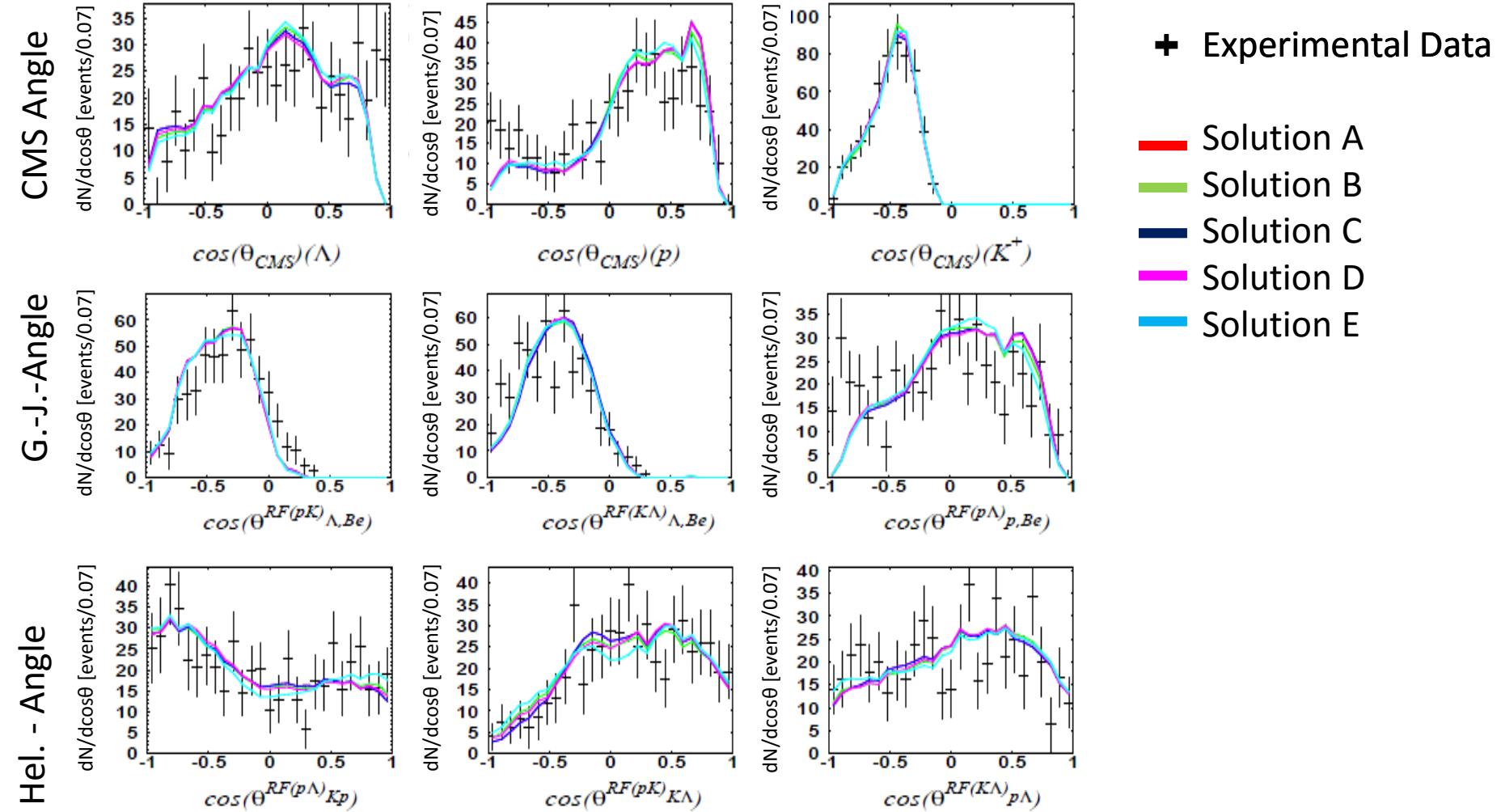


Inside HADES acceptance

Measured Data  
PWA solutions

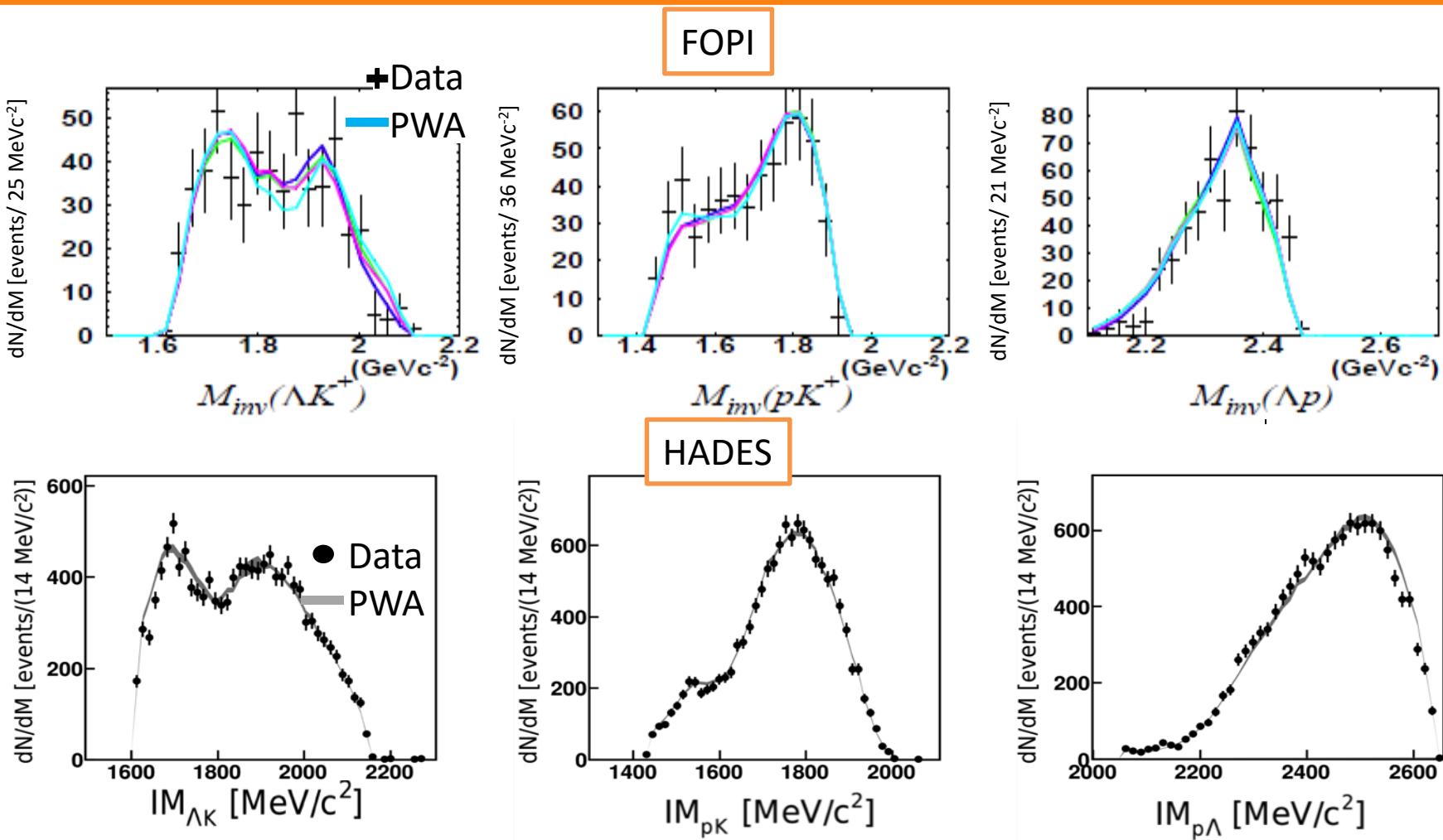
G. Agakishiev, Phys. Lett. B742 (2015) 242–248

# PWA Results



R. Münzer, Hyp. Int., 233, 1-3, 159-166 (2015)

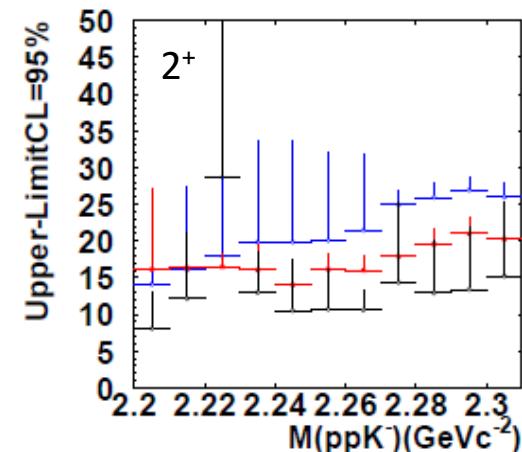
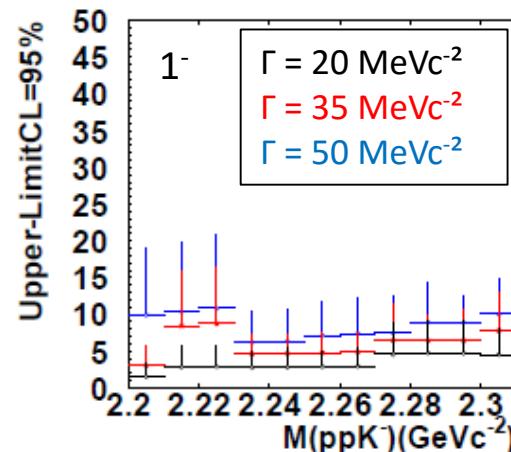
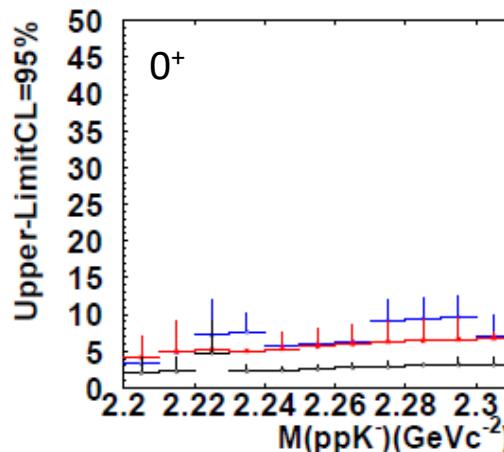
# Four Best PWA Solutions



R. Münzer, Hyp. Int., 233, 1-3, 159–166 (2015) / G. Agakishiev, Phys. Lett. B742 (2015) 242–248

# Upper Limit of ppK<sup>-</sup> Contribution

# ppK<sup>-</sup> Upper Limit Determination



p + p → p + K<sup>+</sup> + Λ  
Total Cross Section

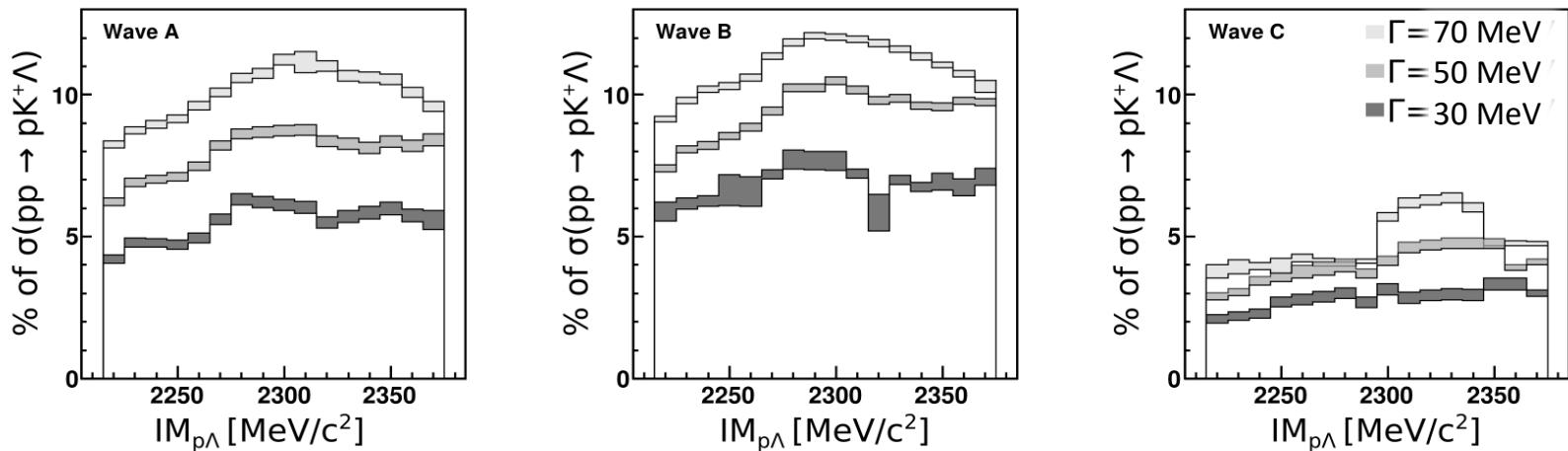
$$\sigma_{pK^+\Lambda} = 41.0 \pm 12.8 \mu\text{b}$$

Interpolated from literature

Upper Limit Cross Section

Γ (MeVc <sup>-2</sup> )	Cross Section (μb)
20	$7.6 \pm 1.2^{-3.5} - 22.4 \pm 3.6^{-10.7}$
35	$6.3 \pm 1.7^{-0.6} - 9.5 \pm 2.6^{-0.9}$
50	$10.2 \pm 1.8^{-4.5} - 11.6 \pm 3.4^{-0.6}$
60	$11.2 \pm 1.9^{-5.0} - 33.8 \pm 5.2^{-16.9}$
80	$11.4 \pm 2.7^{-3.8} - 35.9 \pm 5.7^{-17.4}$

# Upper Limit



Measured total cross-section:  $\sigma_{pK^+\Lambda} = 38.12 \pm 0.43^{+3.55}_{-2.83} \pm 2.67(p+p\text{-error}) - 2.9(\text{background}) \mu\text{b}$

Upper limit of ppK<sup>-</sup> Cross Section:

$\Gamma (\text{MeVc}^{-2})$	Cross Section ( $\mu\text{b}$ )
0 <sup>+</sup>	1.9 – 3.9
1 <sup>-</sup>	2.1 – 4.2
2 <sup>+</sup>	0.7 – 2.1

Production Cross Section  $\Lambda(1405)$

$$9.2 \pm 0.9 \pm 0.7^{+3.3}_{-1.0} \mu\text{b}$$

HADES coll. (G. Agakishiev et al.)  
Phys. Rev. C 87, 025201 (2013)

G. Agakishiev, Phys. Lett. B 742 (2015) 242–248

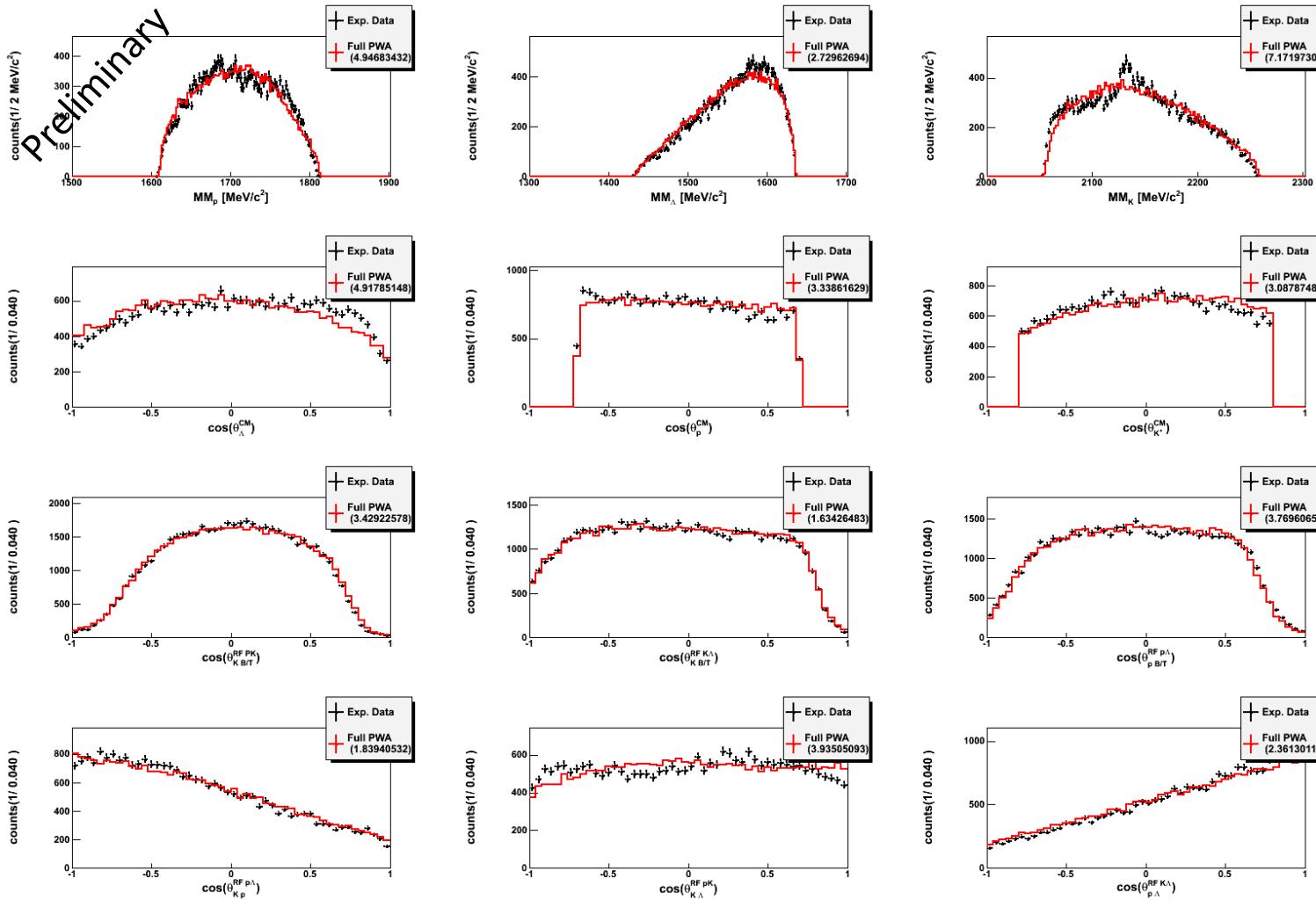
# Combined Analysis

# Outlook

- Improvement of background description
- Combined Analysis

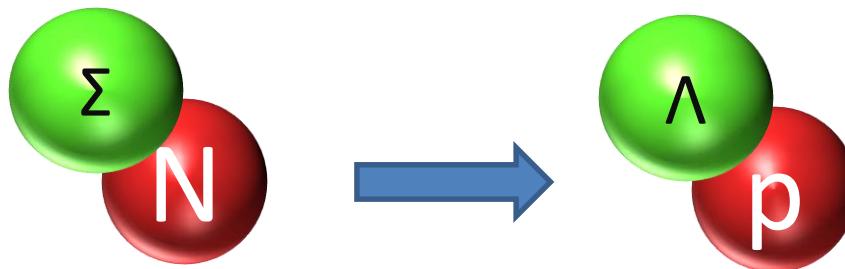
Experiment	$E_B$ [GeV]	pK <sup>+</sup> Λ Statistics	$\varepsilon_{ppK^-}$ [MeV]	Status
COSY-TOF	1.96	~160k	-104	In Preparation
DISTO	2.15	120 k	-114	Available
COSY-TOF	2.16	3.6 k	-104	Available
COSY-TOF	2.16	40 k	-104	Available
COSY-TOF	2.16	~90k	-104	In Preparation
COSY-TOF	2.25	36 k	-83	Available
COSY-TOF	2.40	1.6 k	-24	Available
DISTO	2.5	304 k	26	Available
DISTO	2.85	424 k	116	Available
FOPI	3.1	0.9 k	196	Single PWA
HADES	3.5	21 k	315	Single PWA

# PWA Results – COSY-TOF@2.16 GeV



# The $\Sigma N$ Cusp Effect

Coupled Channel:



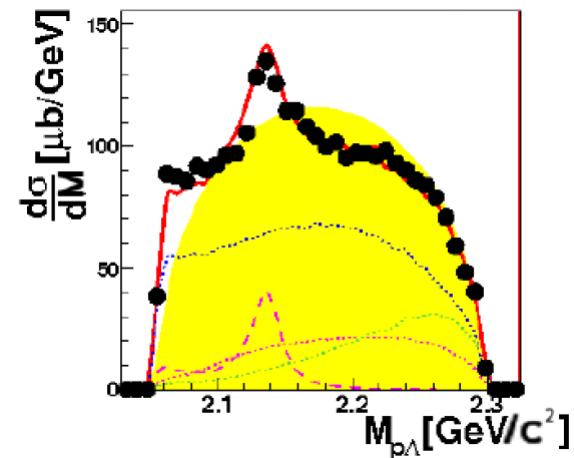
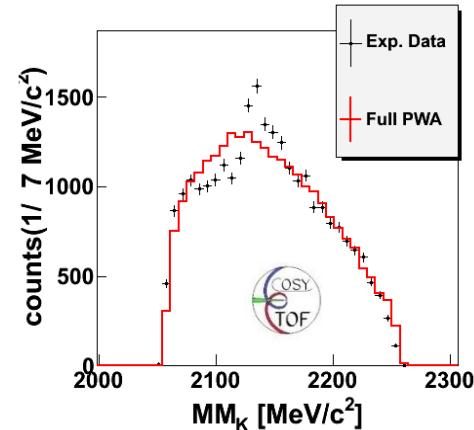
At Threshold :  $2130 \text{ MeV}c^{-2}$

Quantum Number of Cusp:  $0^+ / 1^+$  ( $L=0,2$ )

Spectral Function:

Breit Wigner

Flatté



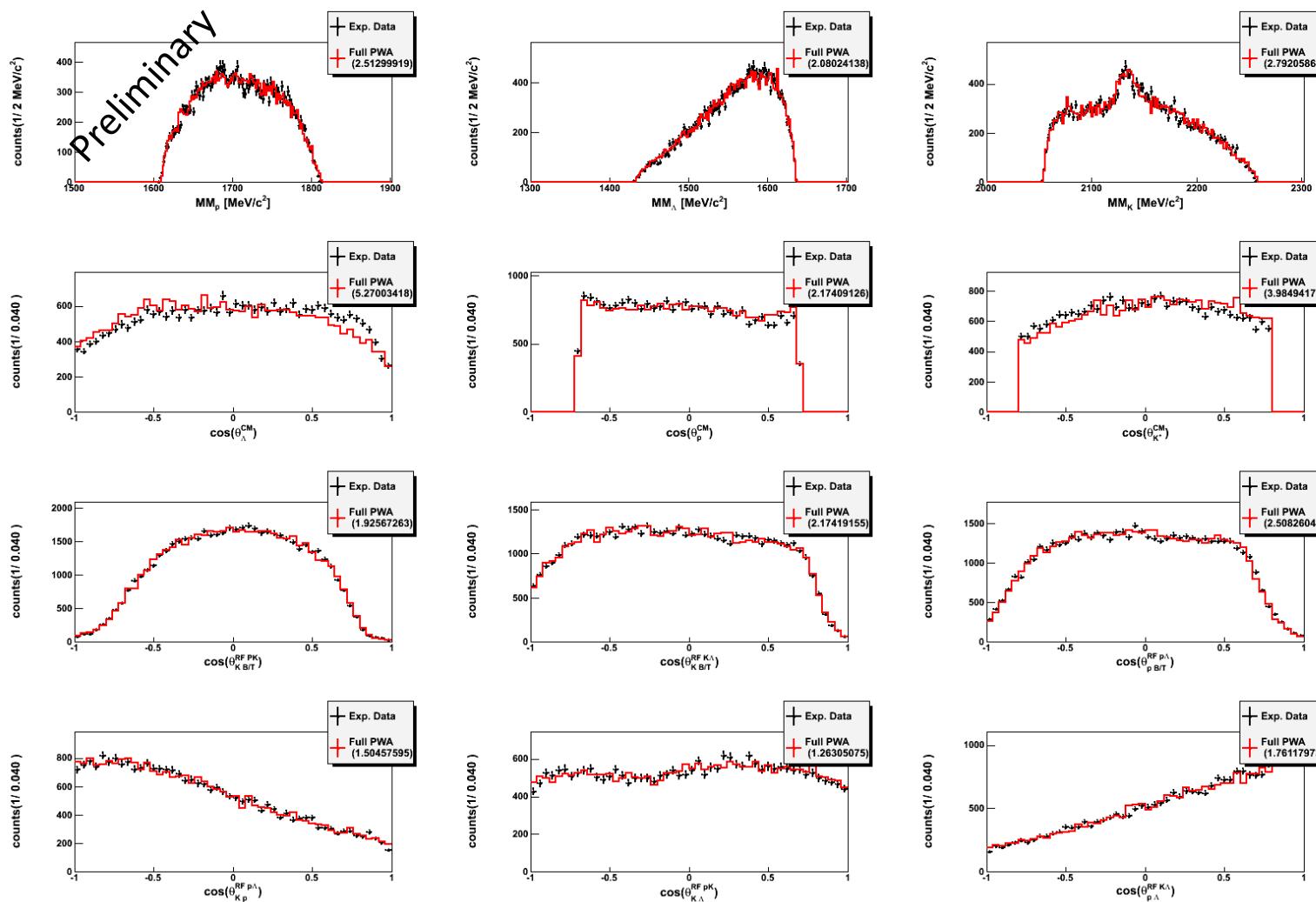
S.Abd El-Samad, Eur.Phys.J A49(2013)

# Cusp Spectral Function

Relativistic Breit-Wigner Distribution:

$$\frac{d\sigma}{dm} \approx \frac{1}{(M^2 - s - i\Gamma M)}$$

# PWA Results with Cusp – COSY-TOF@2.16 GeV

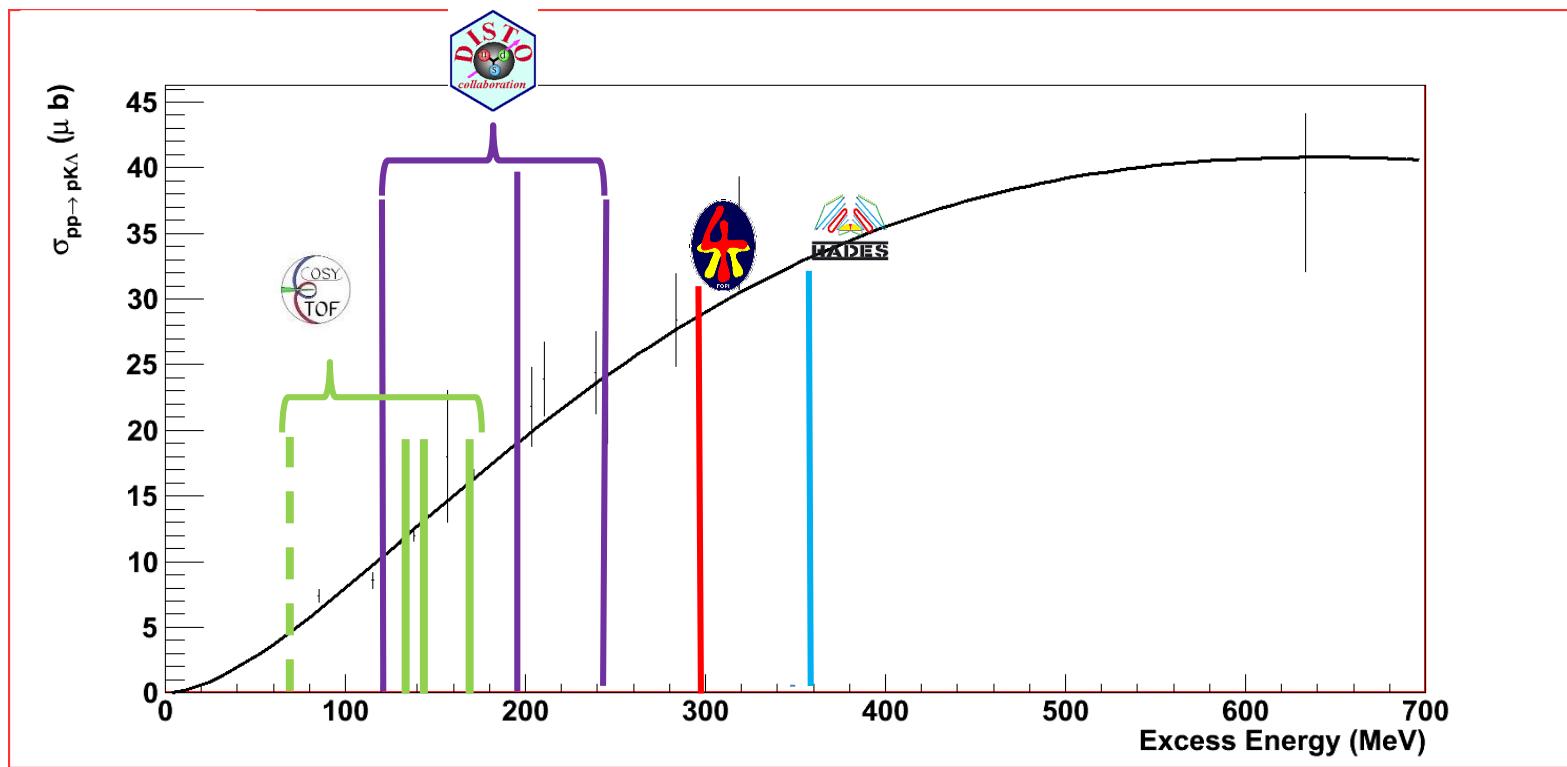


# Data Sets

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DISTO	2.15	120 k	-114	Combined PWA
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COSY-TOF	2.16	40 k	-104	Combined PWA
COSY-TOF	2.16	~90k	-104	In Preparation
COSY-TOF	2.25	36 k	-83	Combined PWA
COSY-TOF	2.40	1.6 k	-24	Combined PWA
DISTO	2.5	304 k	26	Combined PWA
DISTO	2.85	424 k	116	Combined PWA
FOPI	3.1	0.9 k	196	Combined PWA
HADES	3.5	21 k	315	Combined PWA

# Total Cross Section

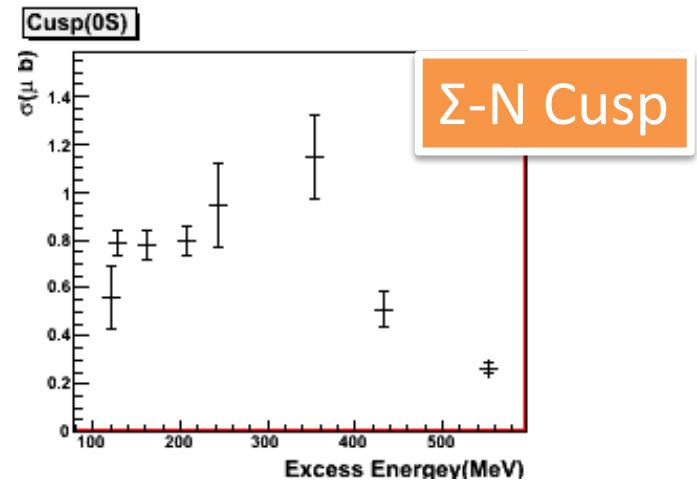
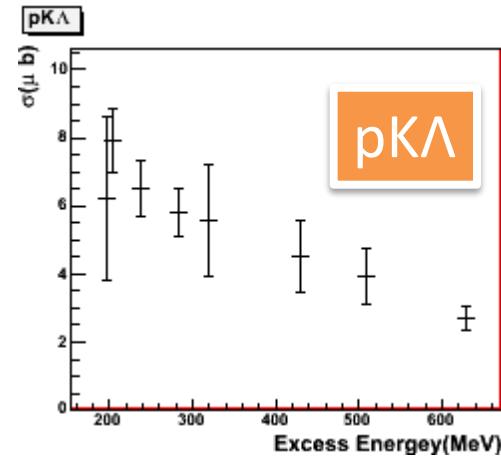
Relative Contribution scaled by total cross section



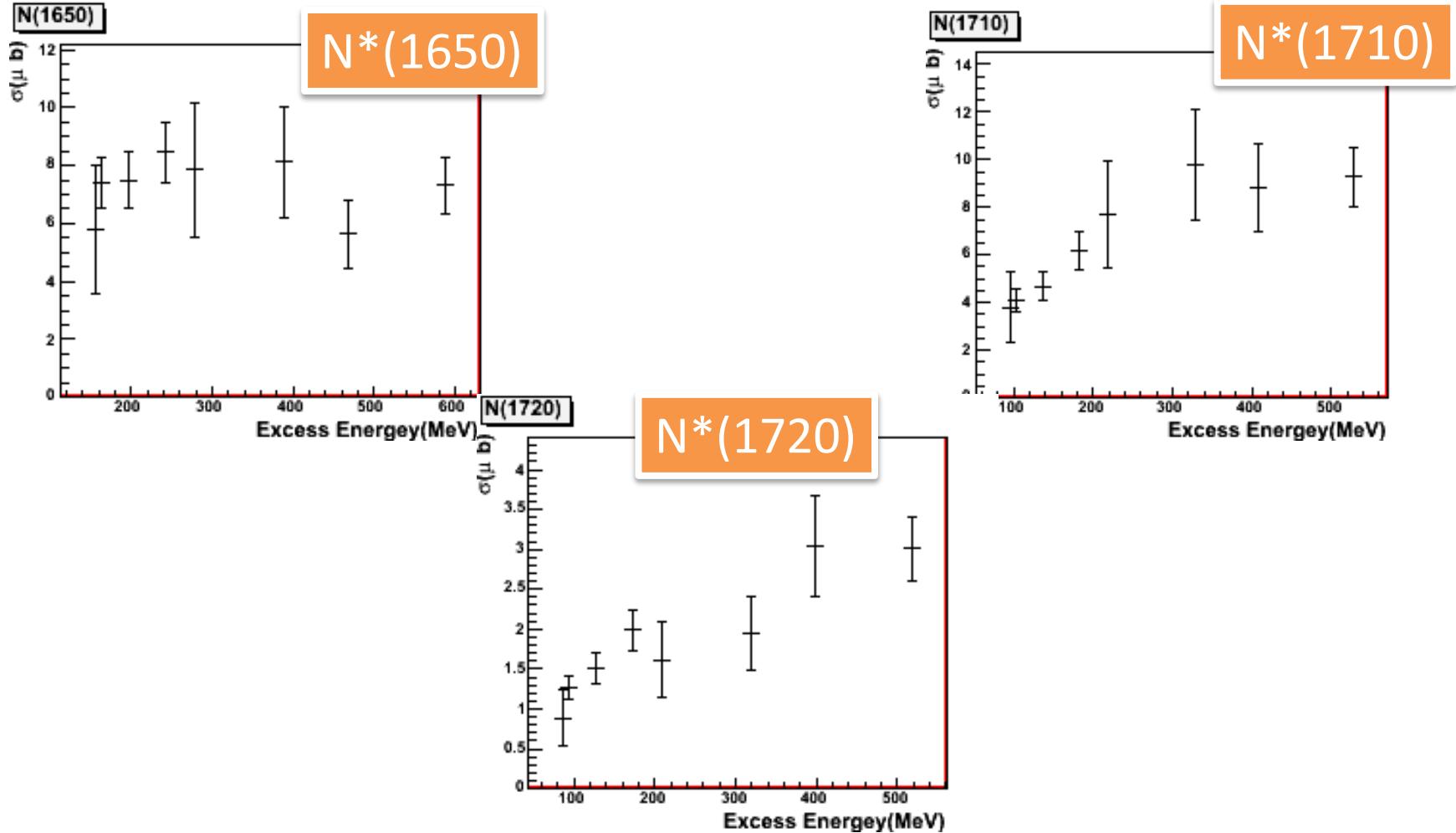
# Cross Section

$$\sigma(p + p) \rightarrow \text{Channel} \rightarrow p + K^+ + \Lambda$$

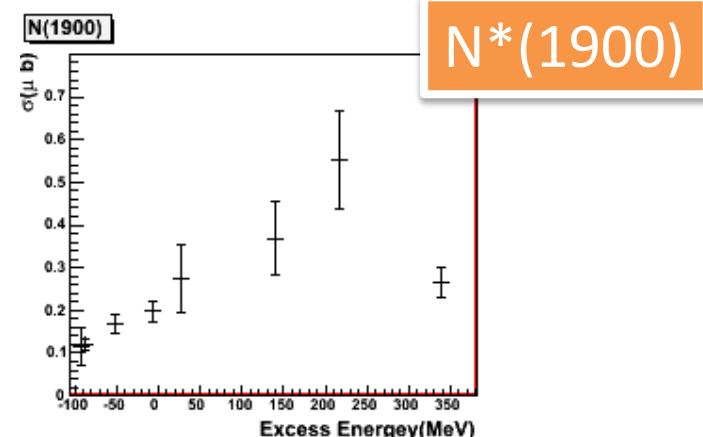
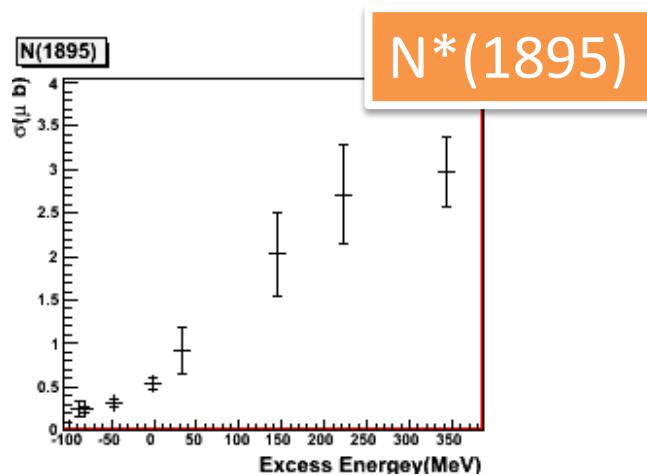
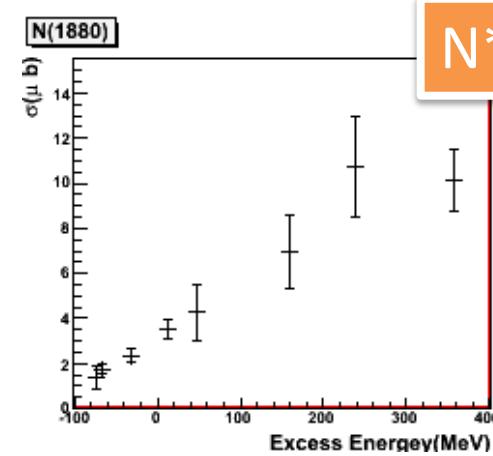
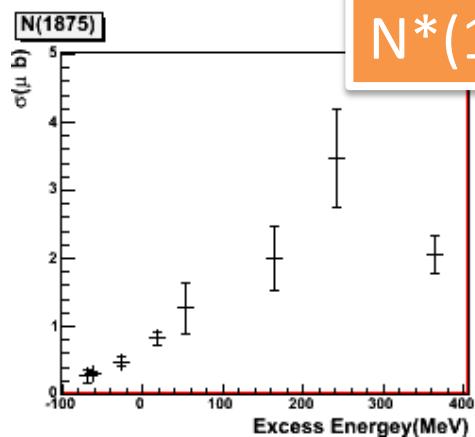
Convoluted Cross Section  
Production + Branching Ratio



# Cross Section



# Cross Section



# Cusp Spectral Function

Relativistic Breit-Wigner Distribution:

$$\frac{d\sigma}{dm} \approx \frac{1}{(M^2 - s - i\Gamma M)}$$

Flatte Distribution:

$$\frac{d\sigma}{dm} \approx \frac{\sqrt{\Gamma_{\Lambda p}}}{(M^2 - s - i(\Gamma_{\Lambda p} + \Gamma_{\Sigma N})M)}$$

$$\Gamma_{\Lambda p} = g_{p\Lambda} q_{p\Lambda} \quad \Gamma_{\Sigma p} = g_{p\Sigma} q_{p\Sigma}$$

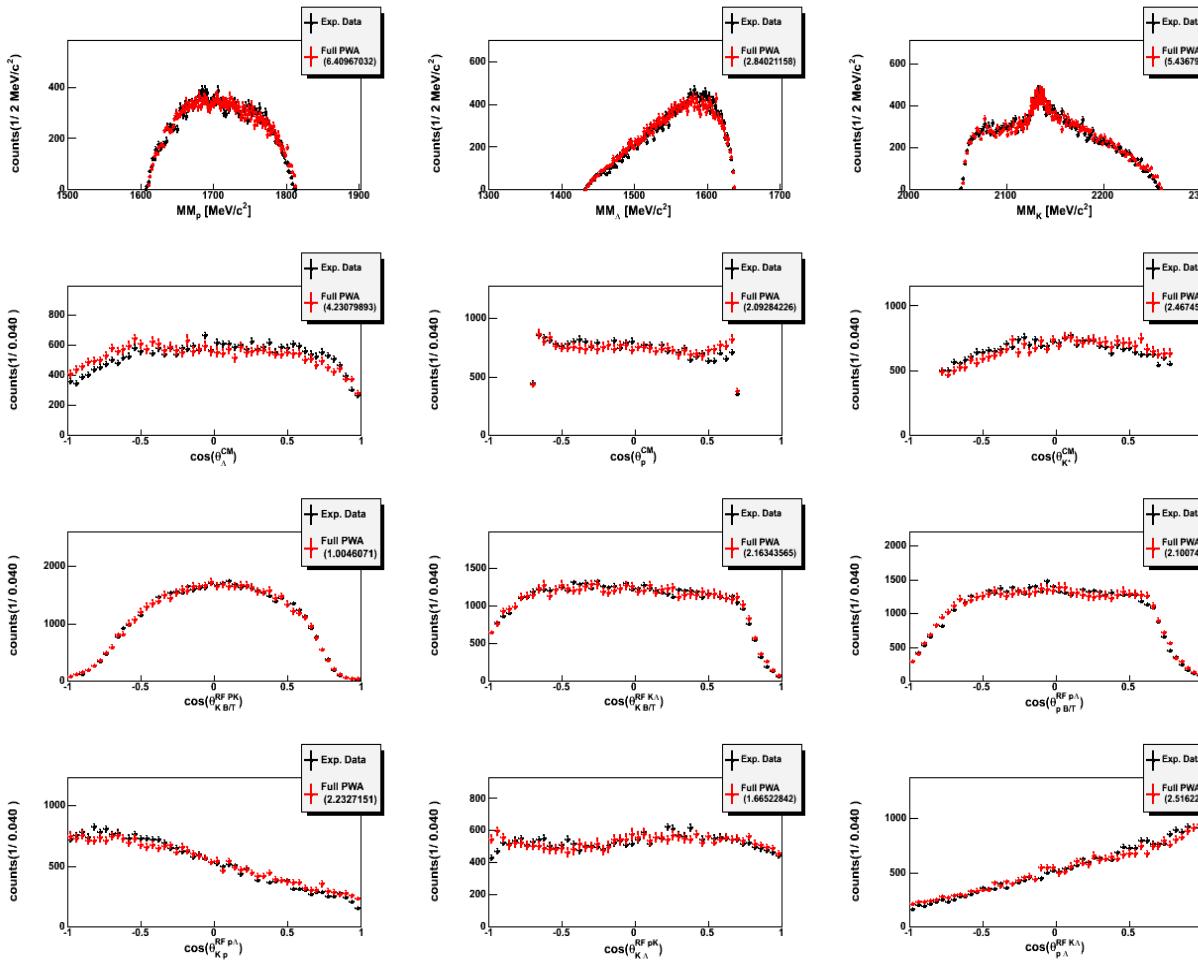
$q_{p\Lambda}, q_{p\Sigma}$ : Relative Momentum

$g_{p\Lambda}, g_{p\Sigma}$ : Couplong Constants

$g_{p\Lambda} \ll g_{p\Sigma}$ : Asymetric Structure

$g_{p\Lambda} \gg g_{p\Sigma}$ : Symetric Structure

# COSY-TOF@2.16GeV



Error bars for cusp are a bit high.

Black dots: Exp data  
Red dots with error bars: PWA results

Resulting value:  
 $g_{p\Lambda}: (0.143)^2$   
 $g_{p\Sigma}: (0.001)^2$

# Summary

- Kaonic Bound State
  - Kaon Nucleon Bound States -> Predicted by Theory but not conclusive Properties
  - Experimental Results show different behavior
  - No Signal Visible in p + p Reaction data measured at FOPI and HADES
  - Production Mechanism has to be described by Partial Wave Analysis including Interference
  - Extraction of Upper Limit:    0.7 - 4.1  $\mu\text{b}$  (HADES)   7.1 - 35.7  $\mu\text{b}$  (FOPI)
- Combined Analysis
  - Set of 9 different data sample can be fitted in parallel with BG-PWA analysis
  - Extraction of excitation function → Strong contribution of  $N^*$
  - Contribution of  $\text{ppK}^-$  very small → No further channel required
  - $\Sigma\text{-N}$  can be reproduced by BG-PWA: symmetric shape -> Coupling  $p\text{-}\Lambda > \Sigma\text{-N}$

# Thank You



**HADES Collaboration**



**FOPI Collaboration**



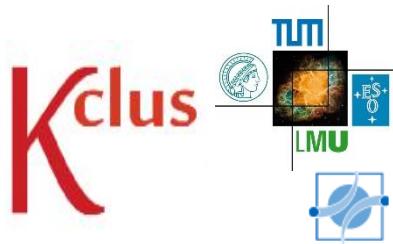
**DISTO Collaboration**  
M. Maggiora



**COSY-TOF Collaboration**  
J. Ritman, E. Roderburg  
F. Hauenstein, D. Gronzka



**Bonn Gatchina Group**  
A. Sarantsev



**K-Cluster – Excellence Cluster Universe – TU Munich**  
L. Fabbietti, E. Epple, P. Klose, S. Lu, J. Siebenson, D. Soliman