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The hyperon puzzle in Neutron Stars

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Neutron Stars: bulk properties

Mass	$M \sim 1.5 M_{\odot}$
Radius	R ~ 10 km
Centr. Density	$ ho_{c} = (4 - 8) ho_{0}$
Compactness	$R/R_g \sim 2-4$
Baryon number	A ~ 10^{57}
Binding energy	B ~ 10 ⁵³ erg
B/A ~ 100 M	$IeV \qquad B/(Mc^2) \sim 10\%$

Stellar structure: General Relativity

Giant "atomic nucleus" or "hypernucleus" bound by gravity

 $R_{g \odot} = 2.95 \text{ km}$

 $M_{\odot} = 1.989 \times 10^{33} \,\mathrm{g}$ $R_{\odot} = 6.96 \times 10^{5} \,\mathrm{km}$

 $\rho_0 = 2.8 \times 10^{14} \,\text{g/cm}^3$ (nuclear saturation density)

 $R_g \equiv 2GM/c^2$ (Schwarzschild radius)



Atomic Nuclei: bulk properties



Relativistic equations for stellar structure

Tolman – Oppenheimer – Volkov equations (TOV)

Μ

$$\frac{dP}{dr} = -G \quad \frac{m(r)\rho(r)}{r^2} \quad \left(1 + \frac{P(r)}{c^2\rho(r)}\right) \left(1 + 4\pi \frac{r^3P(r)}{m(r) c^2}\right) \left[1 - \frac{2Gm(r)}{c^2 r}\right]^{-1}$$

$$\frac{dm}{dr} = 4\pi r^2 \rho(r)$$

$$\frac{d\Phi}{dr} = -\frac{1}{\rho(r)c^2} \frac{dP}{dr} \left(1 + \frac{P(r)}{\rho(r)c^2}\right)^{-1}$$
Due needs the equation of state (EOS) of dense matter, $P = P(\rho)$, up to very high densities
Black Holes
Neutron Stars
$$M_{max}(EOS) \geq \text{ all measured neutron star masses}$$

Two "heavy" Neutron Stars



P. Demorest et al., Nature 467 (2010) 1081

PSR J0348+0432 $M_{NS} = 2.01 \pm 0.04 M_{\odot}$

NS – WD binary system

 $M_{WD} = 0.172 \pm 0.003 M_{\odot}$ (companion mass)

 $P_b = 2.46 \text{ hr}$ (orbital period) P = 39.12 ms (PSR spin period)

 $i = 40.2^{\circ} \pm 0.6^{\circ}$ (inclination angle)

Antoniadis et al., Science 340 (2013) 448

Measured Neutron Star Masses



Neutron star physics in a nutshell

1) Gravity compresses matter at very high density

2) Pauli priciple

Stellar constituents are different species of identical fermions (n, p,...,e⁻, μ⁻) → antisymmetric wave function for particle exchange → Pauli principle
Chemical potentials μ_n, μ_p,...μ_e rapidly increasing functions of density
3) Weak interactions change the isospin and strangeness content of dense matter to minimize energy

Cold catalyzed matter (Harrison, Wakano, Wheeler, 1958) The ground state (minimum energy per baryon) of a system of **hadrons** and **leptons** with respect to their mutual **strong** and **weak interactions** at a given total baryon density n and temperature T = 0.

Nucleon Stars [(n, p, e⁻, μ^-)-matter] having $M_{max}(EOS) \ge 2 M_{\odot} \longrightarrow \rho_c (M_{max}) > \rho_{Y-thr}$



D. Logoteta, I. Bombaci (2014)

Hyperons appear in the stellar core above a threshold density $\rho_{Y-thr} \approx (2-3) \rho_0$

$$\mu_{p} = \mu_{n} - \mu_{e} = \mu_{\Sigma^{+}}$$
$$\mu_{n} = \mu_{\Sigma^{0}} = \mu_{\Xi^{0}} = \mu_{\Lambda}$$
$$\mu_{n} + \mu_{e} = \mu_{\Sigma^{-}} = \mu_{\Xi^{-}}$$
$$\mu_{\mu} = \mu_{e}$$
$$n_{n} + n_{\Sigma^{+}} = n_{e} + n_{\mu} + n_{\Sigma^{-}} + n_{e}$$

Equation of State of Hyperonic Matter



I. Bombaci

D. Logoteta, I. Bombaci (2014)

The hyperon puzzle in Neutron Stars

Many hyperonic matter EOS models (mostly microscopic models) predict the presence of hyperons in the NS core, but they give

 $M_{max} < 2 M_{\odot}$

not compatible with measured NS masses

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Many hyperonic matter EOS models (mostly microscopic models) predict the presence of hyperons in the NS core, but they give

 $M_{max} < 2 M_{\odot}$

not compatible with measured NS masses

A baffling problem which likely originates from our incomplete knowledge (model dependence) of the baryonic interactions.



To be solved for any given value of the total baryon number density $n_{\rm B}$

Microscopic approach to nuclear matter EOS

input

Two-body nuclear interactions: V_{NN}

"realistic" interactions: e.g. Argonne, Bonn, Nijmegen interactions. Parameters fitted to NN scattering data with χ^2 /datum ~1

Three-body nuclear interactions: \mathbf{V}_{NNN}

semi-phenomenological. Parameters fitted to

- binding energy of A = 3, 4 nuclei or
- empirical saturation point of symmetric nuclear matter: $n_0 = 0.16 \text{ fm}^{-3}$, E/A = -16 MeV

	AV18	AV18/UIX	Exp.
B(3H)	7.624	8.479	8.482
B(3He)	6.925	7.750	7.718
B(4He)	24.21	28.46	28.30

Nuclear Matter at $n = 0.16 \text{ fm}^{-3}$ $E^{\text{pot}}(2BF)/A \sim -40 \text{ MeV}$ $E^{\text{pot}}(3BF)/A \sim -1 \text{ MeV}$

Values in MeV

A. Kievsky, S. Rosati, M.Viviani, L.E. Marcucci, L. Girlanda, Jour. Phys.G 35 (2008) 063101 A. Kievsky, M.Viviani, L. Girlanda, L.E. Marcucci, Phys. Rev. C 81 (2010) 044003 Z.H. Li, U. Lombardo, H.-J. Schulze, W. Zuo, Phys. Rev. C 77 (2008) 034316

Microscopic EOS for nuclear matter: Brueckner-Bethe-Goldstone theory

$$G_{\tau\tau'}(\omega) = V + V \sum_{k_a k_b} \frac{|k_a k_b\rangle Q_{\tau\tau'} \langle k_a k_b|}{\omega - e_{\tau}(k_a) - e_{\tau'}(k_b)} G_{\tau\tau'}(\omega)$$

$$e_{\tau}(k) = \frac{\hbar^2 k^2}{2m} + U_{\tau}(k)$$

$$U_{\tau}(k) = \sum_{\tau'} \sum_{k'} \langle kk' | G_{\tau\tau'}(e_{\tau}(k) + e_{\tau'}(k')) | kk' \rangle_{A}$$

$$\widetilde{E}(n_{n},n_{p}) \equiv \frac{E}{A} = \frac{1}{A} \left\{ \sum_{\tau} \sum_{k} \frac{\hbar^{2} k^{2}}{2M} + \frac{1}{2} \sum_{\tau} \sum_{k} U_{\tau}(k) \right\} \qquad n_{p} = \frac{1}{2} (1-\beta)n$$



 ρ_{Y-thr} depends on NNN interaction

Message taken from Nucleon Stars

(i.e. Neutron Stars with a pure nuclear matter core)

NN interactions are essential to have "large" stellar mass

For a free neutron gas $M_{max} = 0.71 \text{ M}_{\odot}$ (Oppenheimer and Volkoff, 1939)

NNN interactions are essential

(i) to reproduce the correct **empirical saturation point of nuclear matter**

(ii) to reproduce measured neutron star masses, i.e. to have $M_{max} > 2 M_{\odot}$

Few-body (A \leq 4) nuclear systems properties and/or the saturation properties of nuclear matter can not constrain the NNN interactions at high density

models of Nucleon Stars (i.e. Neutron Stars with a pure nuclear matter core) are able to explain measured Neutron Star masses as those of **PSR J1614-2230 and PSR J0348+0432** $M_{NS} \approx 2 M_{\odot}$

> but the presence of hyperons in the star seems unavoidable: *hyperon puzzle problem*

Microscopic approach to hyperonic matter EOS

input

2BF: nucleon-nucleon (NN), nucleon-hyperon (NY), hyperon-hyperon (YY) e.g. Nijmegen, Julich models

3BF: NNN, NNY, NYY, YYY

Hyperonic sector: experimental data

1. YN scattering data ≈ 50 (NN data ≈ 4300)

2. Hypernuclei : $\approx 40_{\Lambda}X$, $\approx 5_{\Lambda\Lambda}X$ (nuclei ≈ 3300)





Microscopic EOS for hyperonic matter: extended Brueckner theory

$$G(\omega)_{B_{1}B_{2}B_{3}B_{4}} = V_{B_{1}B_{2}B_{3}B_{4}} + \sum_{B_{5}B_{6}} V_{B_{1}B_{2}B_{5}B_{6}} \frac{Q_{B_{5}B_{6}}}{\omega - e_{B_{5}} - e_{B_{6}}} G(\omega)_{B_{5}B_{6}B_{3}B_{4}}$$

$$e_{B_{i}}(k) = M_{B_{i}}c^{2} + \frac{\hbar^{2}k^{2}}{2M_{B_{i}}} + U_{B_{i}}(k)$$

$$U_{B_{i}}(k) = \sum_{B_{j}} \sum_{k' \leq k_{FB_{j}}} \langle \vec{k}\vec{k'} | G_{B_{i}B_{j}B_{i}B_{j}}(\omega) = e_{B_{i}} + e_{B_{j}}) | \vec{k}\vec{k'} \rangle$$

V is the baryon -baryon interaction for the baryon octet (n, p, Λ , Σ^{-} , Σ^{0} , Σ^{+} , Ξ^{-} , Ξ^{0})

Energy per baryon in the BHF approximation

$$E/N_{B} = 2\sum_{B_{i}} \int_{0}^{k_{F}[B_{i}]} \frac{d^{3}k}{(2\pi)^{3}} \left\{ M_{B_{i}}c^{2} + \frac{\hbar^{2}k^{2}}{2M_{B_{i}}} + \frac{1}{2}U_{B_{i}}^{N}(k) + \frac{1}{2}U_{B_{i}}^{Y}(k) \right\}$$

Baldo, Burgio, Schulze, Phys.Rev. C61 (2000) 055801; Vidaña, Polls, Ramos, Engvik, Hjorth-Jensen, Phys.Rev. C62 (2000) 035801; Vidaña, Bombaci, Polls, Ramos, Astron. Astrophys. 399, (2003) 687.

Equation of State of Hyperonic Matter



BHF Av18 + TNF + ESC08b no hyperonic TBF

D. Logoteta, I. Bombaci (2014)

TNF: Z H., Li, U. Lombardo, H.-J. Schulze, W. Zuo, Phys. Rev. C 77 (2008)

Stellar mass



The stellar mass-radius relation

NN(Av18) + NNN + NY(ESC08 or NSC89) no hyperonic TBF



Z. H. Li, H.-J. Schulze, Phys. Rev. C 78 (2008) 028801

H.-J. Schulze, T. Rijken, Phys. Rev. C 84 (2011) 035801

Hyperons in Neutron Stars: implications for the stellar structure

The presence of hyperons reduces the maximum mass of neutron stars:

$\Delta M_{max} \approx (0.5 - 1.2) M_{\odot}$

Therefore, to neglect hyperons always leads to an overstimate of the maximum mass of neutron stars



Hyperonic TBF as a possible solution of the hyperon puzzle in neutron stars

YNN three-body forces in hypernuclei

A. Gal, Phys. Rev. Lett. 18 (1967) 568
R. K. Bhaduri, B.A. Losieau, Y. Nogami, Ann. Phys. 44 (1967) 55
B.A. Losieau, Nucl. Phys. B 9 (1969) 169
A.R. Bodmer, Q.N. Usmani, J. Carlson, Phys. Rev. C29 (1984) 684

"Universal" three-body forces between nucleons and hyperons

S. Nishizaki, Y. Yamamoto, T. Takatsuka, Prog. Theor. Phys. 105 (2001) 607

- S. Nishizaki, Y. Yamamoto, T. Takatsuka, Prog. Theor. Phys 108 (2002) 703
- T. Takatsuka, Prog. Theor. Phys. Suppl. 156 (2004) 84
- Y. Yamamoto, T. Furumoto, N. Yasutake, Th. Rijken, Phys. Rev. C 90, (2014) 045805

Yamamoto's talk and Takatsuka's talk in this section

Estimation of the effect of hyperonic TBF on the maximum mass of neutron stars

I.Vidaña, D. Logoteta, C. Providencia, A. Polls, I. Bombaci, EPL 94 (2011) 11002

BHF calculations: NN (Av18) + NY (NSC89)
 TBF: phenomenological density dependent contact terms

$$\varepsilon_{3} = a_{NN} n_{N}^{2} + b_{NN} n_{N}^{\gamma_{NN}+1}$$

$$+ a_{N\Lambda} n_{N} n_{\Lambda} + b_{N\Lambda} n_{N} n_{\Lambda} \frac{n_{N}^{\gamma_{N\Lambda}} + n_{\Lambda}^{\gamma_{N\Lambda}}}{n_{N} + n_{\Lambda}}$$

$$+ a_{N\Sigma} n_{N} n_{\Sigma} + b_{N\Sigma} n_{N} n_{\Sigma} \frac{n_{N}^{\gamma_{N\Sigma}} + n_{\Sigma}^{\gamma_{N\Sigma}}}{n_{N} + n_{\Sigma}}$$

Energy density form inspired by S. Balberg, A. Gal, Nucl Phys. A 625, (1997) 435

we assume:

$$a_{N\Lambda} = a_{N\Sigma} \qquad b_{N\Lambda} = b_{N\Sigma} \qquad \gamma_{N\Lambda} = \gamma_{N\Sigma}$$
$$\frac{a_{NY}}{a_{NN}} = \frac{b_{NY}}{b_{NN}} \equiv x$$

empirical saturation point of symmetric NM

Binding energy of Λ in NM

$$B_{\Lambda} = -28 \text{ MeV} = U_{\Lambda} (k=0) + a_{NY} n_0 + b_{NY} n_0^{\gamma_{NY}} \Longrightarrow \gamma_{NY}$$

effect of hyperonic TBF on the maximum mass of neutron stars



γ_{NN}	x	γ_{YN}	Maximum Mass
	0	-	1.27(2.22)
	1/3	1.49	1.33
2	2/3	1.69	1.38
	1	1.77	1.41
	0	-	1.29(2.46)
	1/3	1.84	1.38
2.5	2/3	2.08	1.44
	1	2.19	1.48
	0	-	1.34(2.72)
	1/3	2.23	1.45
3	2/3	2.49	1.50
	1	2.62	1.54
	0		1.38(2.97)
3.5	1/3	2.63	1.51
	2/3	2.91	1.56
	1	3.05	1.60

I.Vidaña, D. Logoteta, C. Providencia, A. Polls, I. Bombaci, EPL 94 (2011) 11002

Miscroscopic hyperonic TBF

Two-meson exchange NNY potential

D. Logoteta, I. Vidaña, C. Providencia, Nucl. Phys. A 914 (2013) 433

Microscopic EOS for hyperonic matter: AFDM

Gandolfi's talk this morning,

Lonardoni's talk in this section



Microscopic EOS for hyperonic matter: AFDM

Gandolfi's talk this morning,

Lonardoni's talk in this section



Relativistic Mean Field models for the hyperonic matter EOS

- **Strong vector-meson mediated repulsive interaction**
- o increase of $g_{\rho Y}$ coupling (" $\sigma \omega \rho$ " model)
- \circ inclusion of vector mesons with hidden strangeness (ϕ meson)
- **density dependent coupling constants**

Miyatsu's talk in this section

H. Huber, M.K. Weigel, F. Weber, Z. Naturforsch. 54A (1999) 77
F. Hoffman, C.M. Kleil, H. Lenske, Phys. Rev. C 64 ((2001) 034314
V. Dexheimer, S. Schramm, Astrophys. J. 683 (2008) 943
I. Bombaci, P.K. Pandha, C. Providencia, I. Vidana, Phys. Rev. D 77 (2008) 083002
A. Taurines, C.Vasconcellos, M. Malheiro, M. Chiapparini, Mod. Phys. Lett. A 15 (2000) 1789
T. Miyatsu, T. Katayama, K. Saito, Phys. Lett. B 709 (2012) 242
S. Weissenborn, D. Chatterjee, J. Schaffner-Bielich, Phys. Rev. C 85 (2012) 065802
E.N.E. van Dalen, G. Colucci, A. Sedrakian, Phys. Lett. B 734 (2014) 383

Glendenning – Moszkowski EOS



M_{max} increases and the stellar hyperon content decreases

increasing $g_{\rho Y}$ and $g_{\omega Y}$



S. Weissenborn, D. Chatterjee, J. Schaffner-Bielich, Phys. Rev. C 85 (2012) 065802

Neutron Stars in the QCD phase diagram

Lattice QCD at $\mu_{b}=0$ and finite T

► The transition to Quark Gluon Plasma is a crossover Aoki et ,al., Nature, 443 (2006) 675

 Deconfinement transition temperature T_c

HotQCD Collaboration T_c= 154 ± 9 MeV Bazarov et al., Phys.Rev. D85 (2012) 054503

Wuppertal-Budapest Collab. T_c = 147 ± 5 MeV Borsanyi et al., J.H.E.P. 09 (2010) 073



Neutron Stars: high μ_{b} and low T

Lattice QCD calculations are presently not possible Quark deconfinement transition expected of the first order Z. Fodor, S.D. Katz, Prog. Theor Suppl. 153 (2004) 86

"A link between lattice QCD and measured neutron star masses" I. Bombaci, D. Logoteta, Mont. Not. Royal Astron. Soc. 433 (2013) L79



I. Bombaci, A. Drago, INFN Notizie, n. 13, 15 (2003)

"Neutron Stars"

Nucleon Stars

Hyperon Stars

Hadronic Stars

Strange Stars

Hybrid Stars

Quark Stars

1st order phase transitions are triggered by the **nucleation** of a **critical size drop** of the **new (stable) phase** in a **metastable mother phase**



Virtual drops of the stable phase are created by small localized fluctuations in the state variables of the metastable phase

Gibbs' criterion for phase equilibrium

$$\begin{split} \mu_{H} &= \mu_{Q} \equiv \mu_{0} \\ T_{H} &= T_{Q} \equiv T \\ P(\mu_{H}) &= P(\mu_{Q}) \equiv P(\mu_{0}) \equiv P_{0} \end{split}$$

$$\mu_{H} = \frac{\varepsilon_{H} + P_{H} - s_{H}T}{n_{b,H}}$$
$$\mu_{Q} = \frac{\varepsilon_{Q} + P_{Q} - s_{Q}T}{n_{b,Q}}$$

1st order phase transitions are triggered by the **nucleation** of a **critical size drop** of the **new (stable) phase** in a **metastable mother phase**



Virtual drops of the stable phase are created by small localized fluctuations in the state variables of the metastable phase

Astrophysical consequences of the nucleation process of quark matter (QM) in the core of massive pure hadronic compact stars ("<u>Hadronic Stars</u>", HS).

Berezhiani, Bombaci, Drago, Frontera, Lavagno, Astrophys. Jour. 586 (2003) 1250 I. Bombaci, I. Parenti, I. Vidaña, Astrophys. Jour. 614 (2004) 314 I. Bombaci, G. Lugones, I. Vidaña, Astron. & Astrophys. 462 (2007) 1017

Metastability of Hadronic Stars



Μ

Hadronic Stars above a threshold value of their gravitational mass are <u>metastable</u> to the conversion to Quark Stars (QS) (hybrid stars or strange stars)

Berezhiani, Bombaci, Drago, Frontera, Lavagno, Astrophys. Jour. 586 (2003) 1250 I. Bombaci, I. Parenti, I. Vidaña, Astrophys. Jour. 614 (2004) 314 I. Bombaci, G. Lugones, I. Vidaña, Astron. & Astrophys. 462 (2007) 1017

Metastability of Hadronic Stars



Quantum nucleation theory

I.M. Lifshitz and Y. Kagan, 1972; K. Iida and K. Sato, 1998



The critical mass of metastable Hadronic Stars

Def.:
$$M_{cr} \equiv M_{HS}(\tau = 1 \text{ yr})$$

• HS with $M_{thr} < M_{HS} < M_{cr}$ are metastable with $\tau = 1 \text{ yr} \div \infty$

HS with $M_{HS} > M_{cr}$ are very unlikely to be observed

The critical mass M_{cr} plays the role of an effective maximum mass for the hadronic branch of compact stars



Bombaci, Parenti, Vidaña, Astrophys. Jour. 614 (2004) 314



I. Bombaci, D. Logoteta (2014)

SQM EOS: Alford et al. Astrophys. J. 629 (2005); Fraga et al., Phys. Rev. D 63 (2001)



I. Bombaci, D. Logoteta (2014)

SQM EOS: Alford et al. Astrophys. J. 629 (2005); Fraga et al., Phys. Rev. D 63 (2001)

Total energy released in the stellar conversion



Assuming that the stellar baryonic mass is conserved during the stellar conversion, the total energy released in the process is :

 $E_{conv} = M_{cr} - M_{QS}(M^{b}_{cr})$ ~ 10⁵³ erg

I. Bombaci, & B. Datta, Astrophys. J. Lett. 530 (2000) L69

Supernova-GRB connection: Hadronic Star → Quark Star conversion model



Berezhiani, Bombaci, Drago, Frontera, Lavagno, Astrophys. Jour. 586 (2003) 1250

Summary

"Hyperon puzzle" in Neutron star physics $M_{max} < 2 M_{\odot}$

quest for extra pressure at high densities

(i)

strong short-range repulsion in NY, YY interactions

repulsive NNY, NYY, YYY 3-baryon interactions

strong vector-meson mediated repulsive interaction (RMF)

 (ii) or, the transition to Strange Quark Matter produce a stiffening of the EOS due e.g. to perturbative quark interactions
 NS → Quark Stars (hybrid or strange stars)





