

Exotic baryons as a hadronic molecule in the heavy quark region

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**Yasuhiro Yamaguchi and Elena Santopinto ,
arXiv:1606.08330 [hep-ph].**

MENU2016 – The 14th International Conference
on Meson-Nucleon Physics and the Structure of the Nucleon

25-30 July 2016, Kyoto, Japan

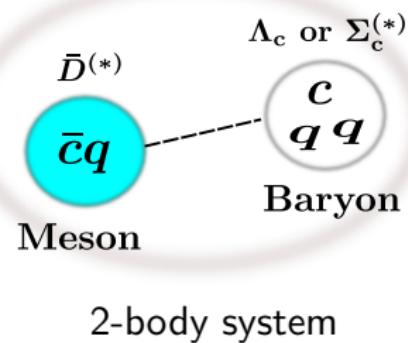
Hidden-charm pentaquarks as **a molecules**

① Introduction

- Exotic hadron in the heavy quark region
- Observed Pentaquarks
- Heavy Quark Spin Symmetry and Coupled channels

② Meson-Baryon molecules:

$$\bar{D}^{(*)}\Lambda_c^{(*)} - \bar{D}^{(*)}\Sigma_c^{(*)}$$



③ Summary

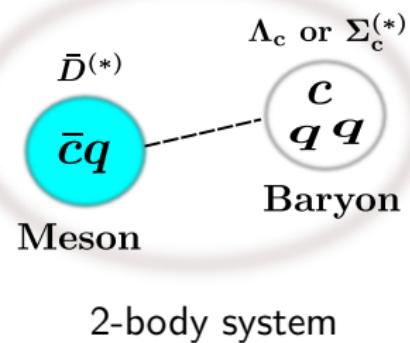
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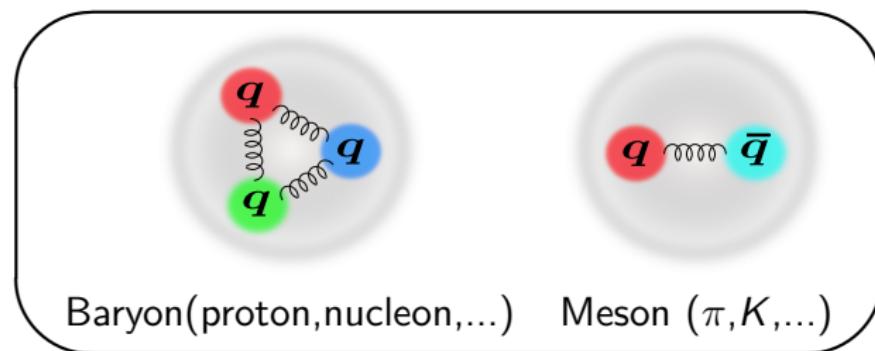
$$\bar{D}^{(*)}\Lambda_c^{(*)} - \bar{D}^{(*)}\Sigma_c^{(*)}$$



③ Summary

Hadrons in the heavy quark region

- Hadron: Composite particle of **Quarks** and **Gluons**
- Constituent quark model (Baryon(qqq) and Meson $q\bar{q}$) has been successfully applied to the hadron spectra!



▷ Quark-quark potential

S. Godfrey and N. Isgur, PRD32(1985)189

$$V(r) = -\frac{a}{r} + br + \dots$$

Exotic hadrons in the heavy quark region

Introduction

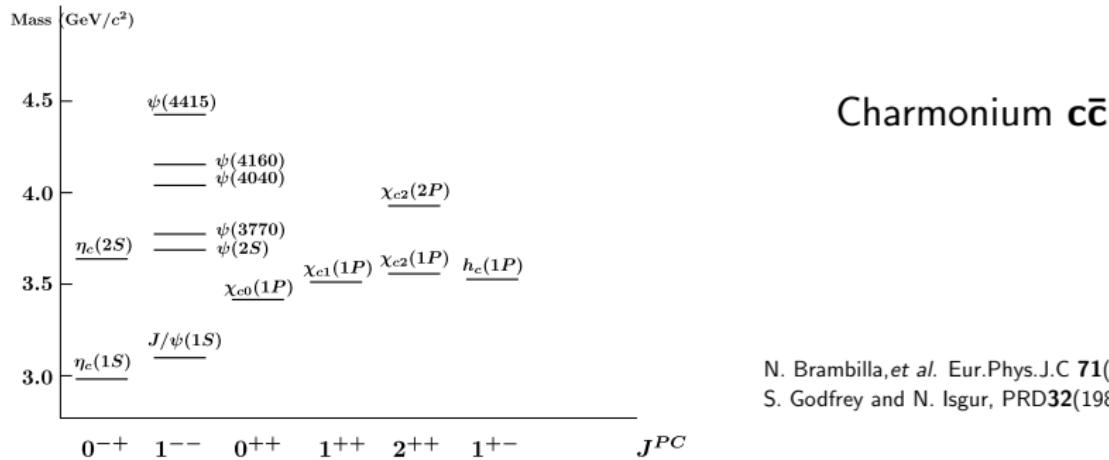
- ▷ Observation of **the Exotic Hadron in the heavy quark (c, b) sectors!**

Exotic hadrons in the heavy quark region

Introduction

- ▷ Observation of **the Exotic Hadron in the heavy quark (c, b) sectors!**

e.g. Spectra of Charmonia



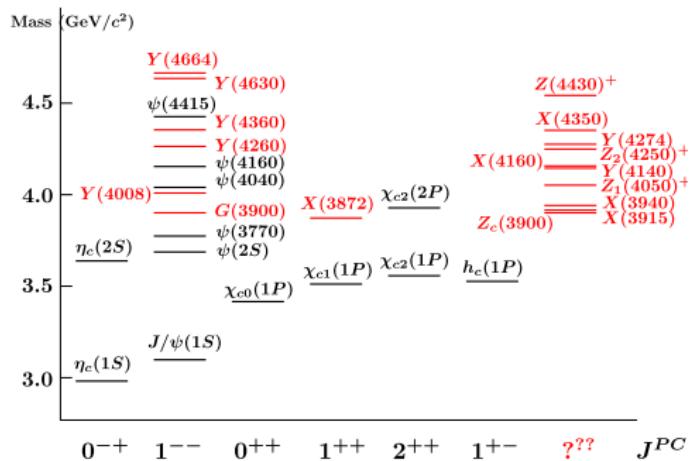
N. Brambilla, et al. Eur.Phys.J.C **71**(2011)1534
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Exotic hadrons in the heavy quark region

Introduction

- ▷ Observation of **the Exotic Hadron in the heavy quark (c, b) sectors!**

e.g. Spectra of Charmonia



Charmonium $c\bar{c}$
and
Exotic hadrons ($\neq c\bar{c}$)
X, Y, Z

N. Brambilla, et al. Eur.Phys.J.C 71(2011)1534
S. Godfrey and N. Isgur, PRD32(1985)189

- ▷ What is **the structure of exotic hadrons** ?
- ▷ Why are many exotic hadrons found in **the heavy quark region**?

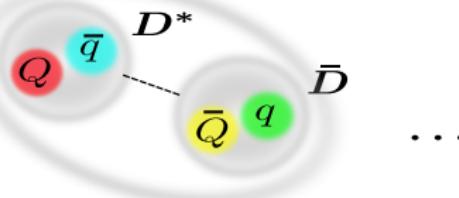
Exotic structure: Hadronic molecules

Introduction

Exotic hadrons \Rightarrow Multiquark states?



Tetraquark
(Compact)



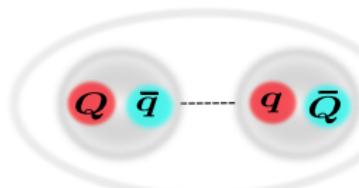
Hadronic molecule

Exotic structure: Hadronic molecules

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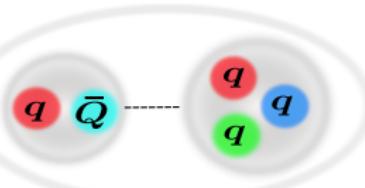
Hadronic molecules

Meson-Meson ($X, Y, Z?$)



$X(3872), Z_b$

Meson-Baryon



$\Lambda_c^*, \text{Pentaquark}???$

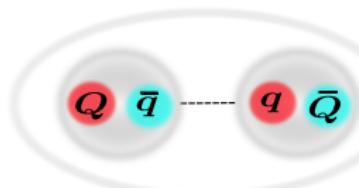
- Loosely bound states (resonances) of hadrons
→ Appearing **near the thresholds** (M-M, M-B,...)
⇒ Analogous to **Atomic Nuclei**
- Molecules are formed by **the Hadron-Hadron interaction** dynamically.

Exotic structure: Hadronic molecules

Introduction

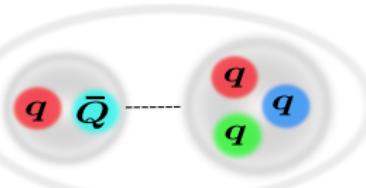
Hadronic molecules

Meson-Meson ($X, Y, Z?$)



$X(3872), Z_b$

Meson-Baryon



$\Lambda_c^*, \text{Pentaquark}???$

► Theoretical researches

- $X(3872)$ as $D\bar{D}^*$,

M. T. AlFiky, *et al.*, PLB**640**(2006)238, M. B. Voloshin, Prog. Part. Nucl. Phys. **61**(2008)455

- Z_b as $B\bar{B}^*$, J. R. Zhang, *et al.*, PLB**704**(2011)312, S. Ohkoda, *et al.*, PRD**86**(2012)014004

- $\Lambda(1405)$ as $\bar{K}N$, T. Hyodo and D. Jido, Prog. Part. Nucl. Phys. **67** (2012) 55

- Λ_c^* as DN , T. Mizutani, A. Ramos, PRC**74**(2006)065201, C. Garcia-Recio, *et al.*, PRD**79**(2009)054004

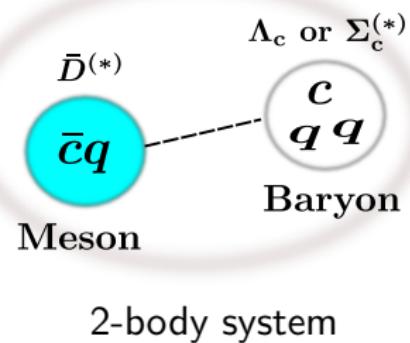
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③ Summary

Observation of two hidden-charm pentaquarks !!

Introduction

PRL 115, 072001 (2015)

PHYSICAL REVIEW LETTERS

WCK CHUNG
14 AUGUST 2015



Observation of $J/\psi p$ Resonances Consistent with Pentaquark States in $\Lambda_b^0 \rightarrow J/\psi K^- p$ Decays

R. Aaij *et al.*^{*}

(LHCb Collaboration)

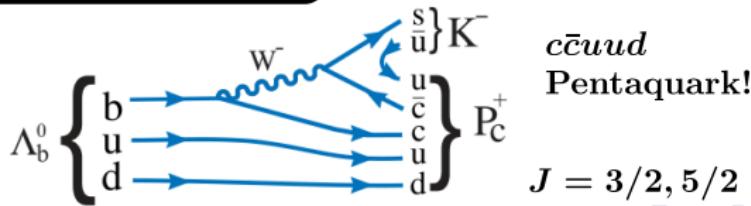
(Received 13 July 2015; published 12 August 2015)

Observations of exotic structures in the $J/\psi p$ channel, which we refer to as charmonium-pentaquark states, in $\Lambda_b^0 \rightarrow J/\psi K^- p$ decays are presented. The data sample corresponds to an integrated luminosity of 3 fb^{-1} acquired with the LHCb detector from 7 and 8 TeV pp collisions. An amplitude analysis of the three-body final state reproduces the two-body mass and angular distributions. To obtain a satisfactory fit of the structures seen in the $J/\psi p$ mass spectrum, it is necessary to include two Breit-Wigner amplitudes that each describe a resonance state. The significance of each of these resonances is more than 9 standard deviations. One has a mass $\mathbf{1} 4380 \pm 8 \pm 29 \text{ MeV}$ and a width of $205 \pm 18 \pm 86 \text{ MeV}$, while the second is narrower, with a mass $\mathbf{2} 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$ and a width of $39 \pm 5 \pm 19 \text{ MeV}$. The preferred J^P assignments are of opposite parity, with one state having spin $3/2$ and the other $5/2$.

DOI: [10.1103/PhysRevLett.115.072001](https://doi.org/10.1103/PhysRevLett.115.072001)

PACS numbers: 14.40.Pq, 13.25.Gv

$\Lambda_b^0 \rightarrow K^- P_c^+$ decay



Observation of two hidden-charm pentaquarks !!

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PRL 115, 072001 (2015)

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WILLY LINDNER
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1. $M = 4380 \pm 8 \pm 29 \text{ MeV}$, $\Gamma = 205 \pm 18 \pm 86 \text{ MeV}$ (Broad)
 2. $M = 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$, $\Gamma = 39 \pm 5 \pm 19 \text{ MeV}$ (Narrow)
- J^P Assignment: $3/2^-, 5/2^+$; $3/2^+, 5/2^-$; $5/2^+, 3/2^-$

What is the structure of the pentaquarks?

Introduction

Theoretical discussions

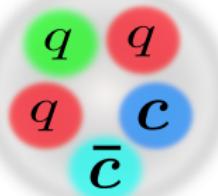
- Compact pentaquark?

- ▷ Quark model

W.L.Wang *et al.*, PRC**84**(2011)015203

G. Yang and J. Ping, (2015), arXiv:1511.09053

...



Pentaquark
(Compact)

- Hadronic molecule?

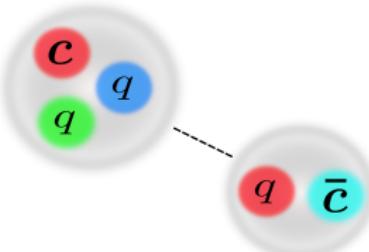
- ▷ SU(4) flavor symmetry

J.-J.Wu *et al.*, PRL**105**(2010)232001

C.W.Xiao *et al.*, PRD**88**(2013)056012

T. Uchino,*et al.*, Eur.Phys.J.A**52**(2016)43

...

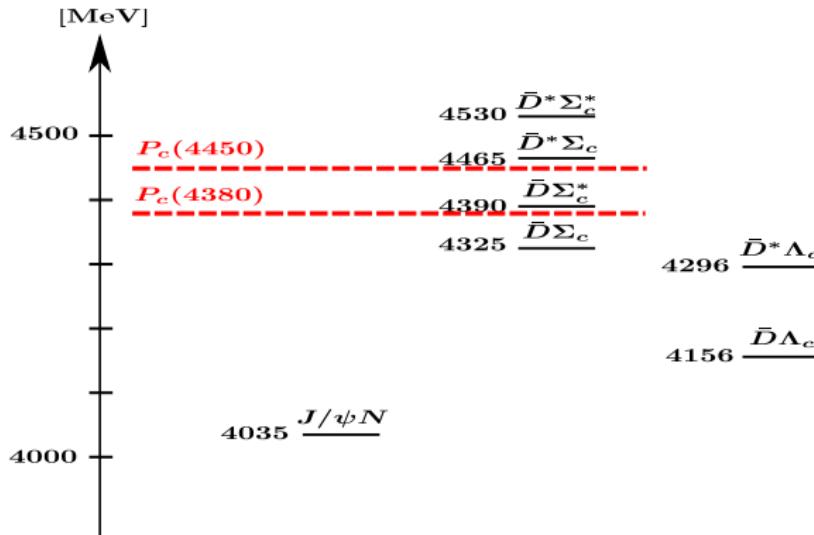


Hadronic molecule

Important issue of the heavy pentaquarks

Introduction

- Pentaquarks are close to **the meson-baryon thresholds**
⇒ **Hadronic molecules** appears near the thresholds!



- Heavy Quark Spin Symmetry**

⇒ SU(4) symmetry is broken in the charm quark sector.

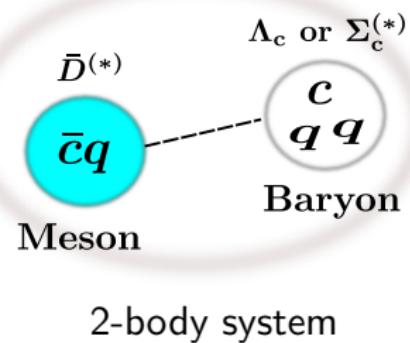
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- **Heavy Quark Spin Symmetry and Coupled channels**

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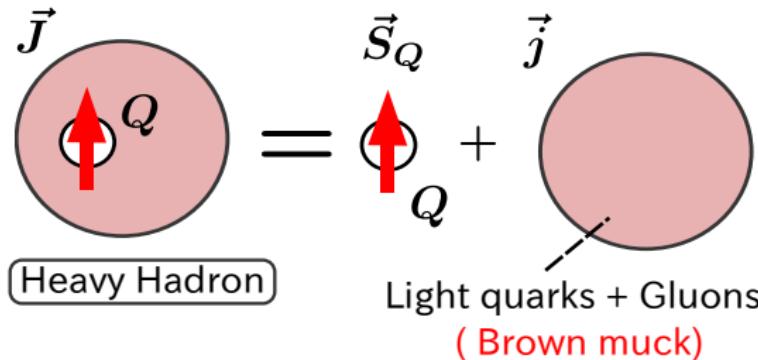
Heavy Quark Spin Symmetry and Mass degeneracy

Introduction

Heavy Quark Spin Symmetry (HQS)

N.Isgur,M.B.Wise,PLB232(1989)113

- **Suppression of Spin-spin force** in $m_Q \rightarrow \infty$.
- ⇒ Decomposition of **Heavy quark spin** and **Light components**
 $\vec{J} = \vec{L} + \vec{S} = \vec{S}_Q + \vec{j}$



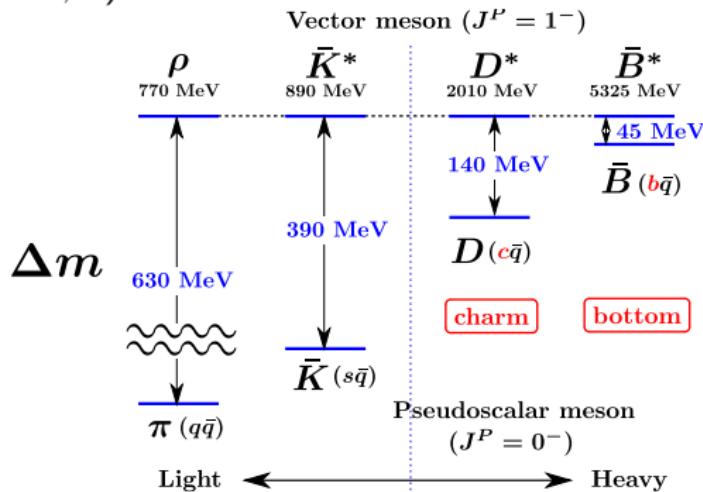
⇒ **Mass degeneracy** of hadrons with the different J

- Mass degeneracy of $\{D, D^*\}(Q\bar{q})$, $\{\eta_c, J/\psi\}(Q\bar{Q})$, $\{\Sigma_c, \Sigma_c^*\}(Qqq)$ (baryons)...

Mass degeneracy of heavy hadrons

Introduction

- Mass difference between vector and pseudoscalar mesons.
 $(Q\bar{q}, q = u, d)$

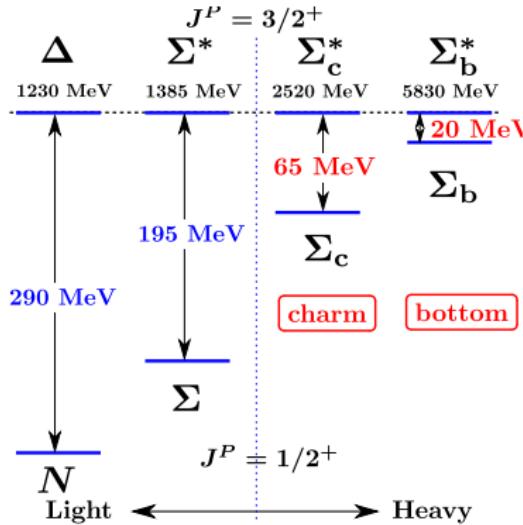


- ▷ Δm decreases when the quark mass increases.
- ▷ Mass degeneracy of heavy hadrons appears!

Mass degeneracy of heavy hadrons

Introduction

- Mass difference between $1/2^+$ and $3/2^+$ baryons. (Qqq , $q = u, d$)



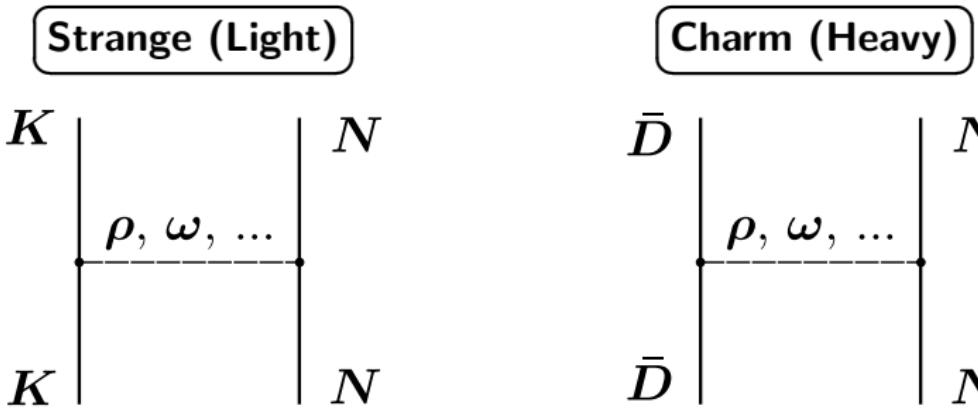
- Δm decreases when the quark mass increases.
- Mass degeneracy of heavy hadrons appears!

⇒ Small mass splitting leads to **Channel couplings!**

Small mass splitting and Interactions (KN and $\bar{D}N$)

Introduction

- Interaction between K (light meson) and N
⇒ Short range force (ρ, ω exchanges...) dominates.

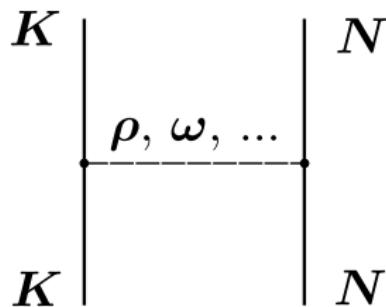


Small mass splitting and Interactions (KN and $\bar{D}N$)

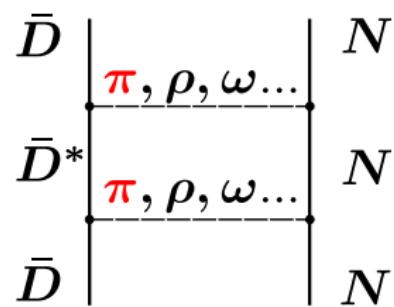
Introduction

- Interaction between K (light meson) and N
 \Rightarrow Short range force (ρ, ω exchanges...) dominates.

Strange (Light) (KK π ×)



Charm (Heavy)



- In the heavy (c, b) sector, the Heavy Quark Spin Symmetry induces **the $\bar{D} - \bar{D}^*$ mixing**.
 $m_{K^*} - m_K \sim 400 \text{ MeV} \Leftrightarrow m_{D^*} - m_D \sim 140 \text{ MeV}$
- Appearance of the **the one π exchange potential**.

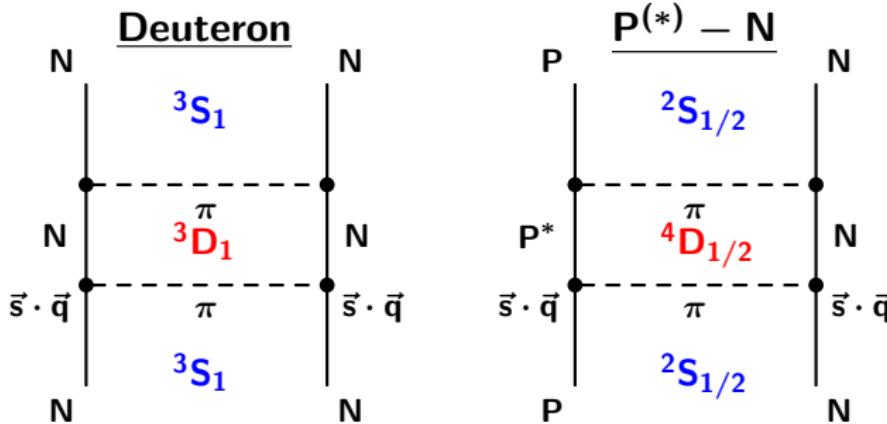
T.D.Cohen, P.M.Hohler, R.F.Lebed PRD72(2005)074010, S.Yasui, K.Sudoh, PRD80(2009)034008,

Y.Yamaguchi, S.Ohkoda, S.Yasui, A.Hosaka PRD84(2011)014032,...

π exchange potential (OPEP) and Coupled channel

Introduction

- OPEP is important to bind atomic nuclei.
- Tensor force of the OPEP generates a strong attraction.



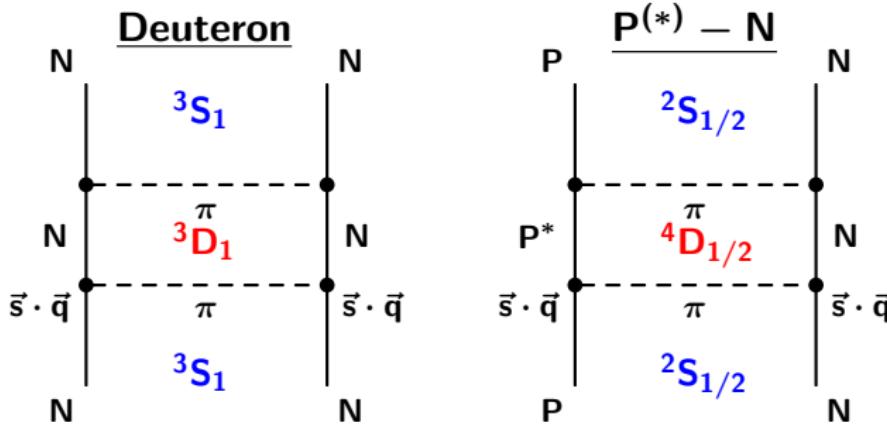
$$\text{Tensor force} \Rightarrow {}^3S_1 - {}^3D_1$$

$$PN({}^2S_{1/2}) - P^*N({}^4D_{1/2})$$

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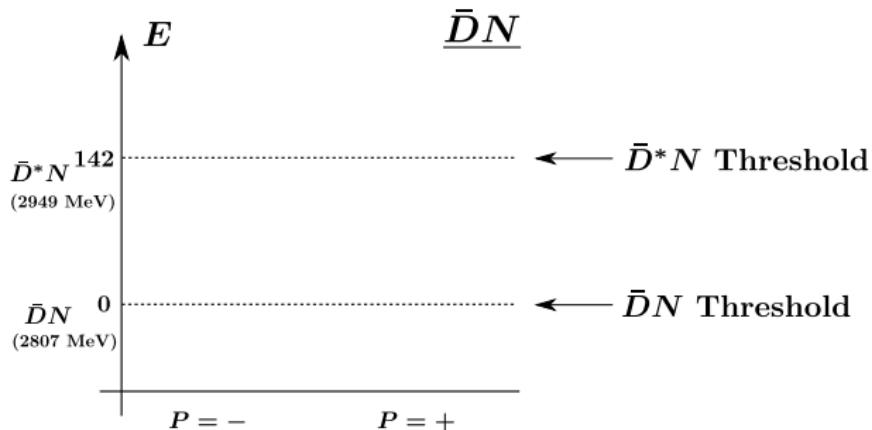
$$\text{Tensor force} \Rightarrow ^3S_1 - ^3D_1$$

$$PN(^2S_{1/2}) - P^*N(^4D_{1/2})$$

- HQS: mixing of $D - D^*$
- Tensor force: mixing of $S - D$ ($P - F$)

Energy spectra of \bar{D} meson-Nucleon ($\bar{D}N$) states

Introduction



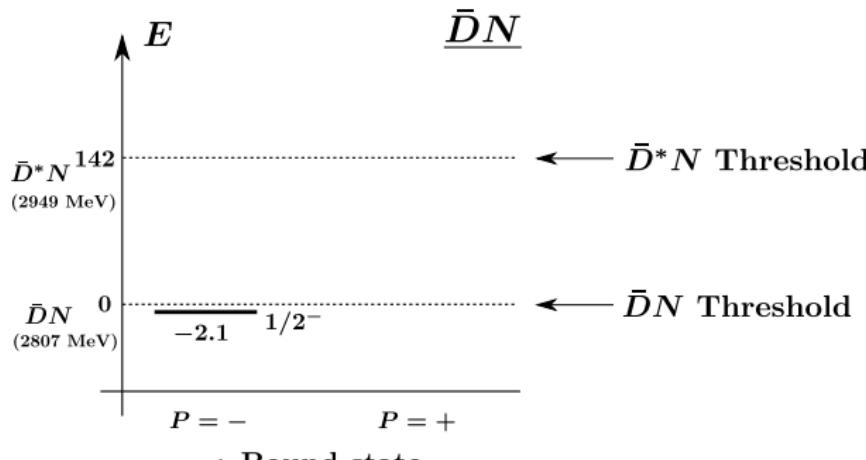
Unit: MeV

Y.Y., S.Ohkoda, S.Yasui and A.Hosaka, PRD84 014032 (2011) and PRD85 054003 (2012)

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- One bound state

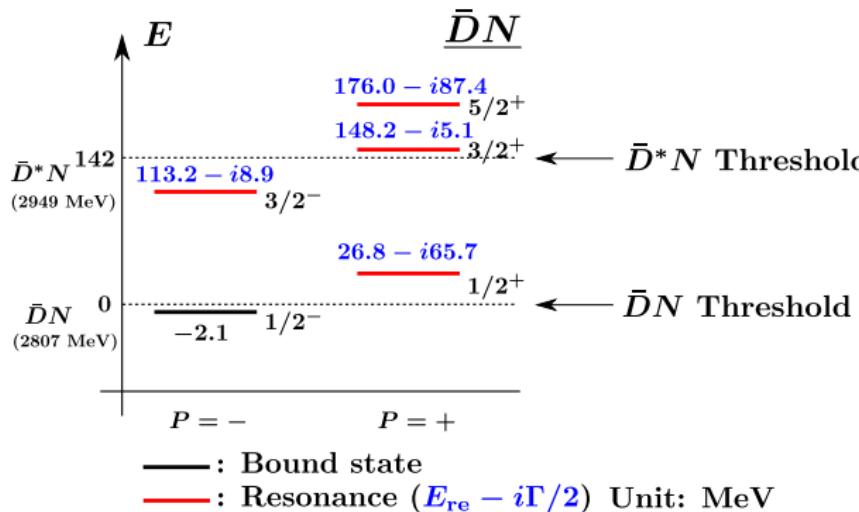


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Energy spectra of \bar{D} meson-Nucleon ($\bar{D}N$) states

Introduction

- One bound state, and resonances in charm

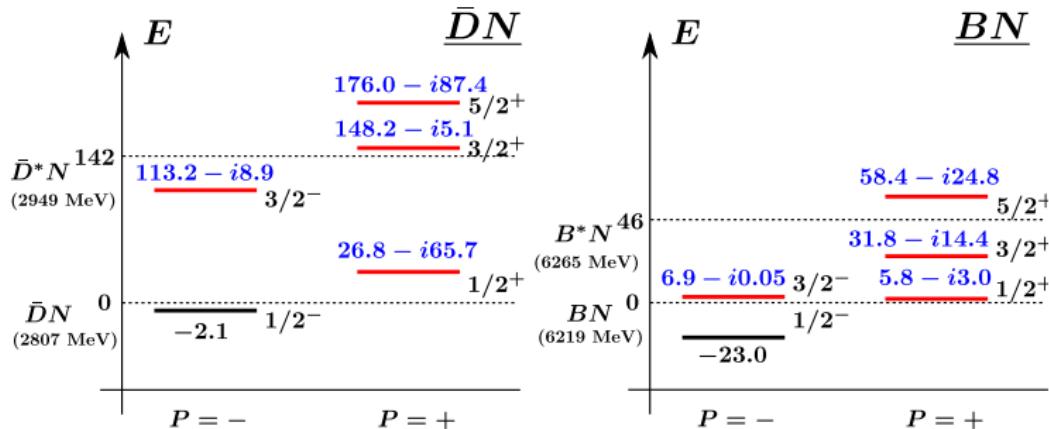


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Energy spectra of \bar{D} meson-Nucleon ($\bar{D}N$) states

Introduction

- One bound state, and resonances in charm and bottom sectors!



— : Bound state

— : Resonance ($E_{re} - i\Gamma/2$) Unit: MeV

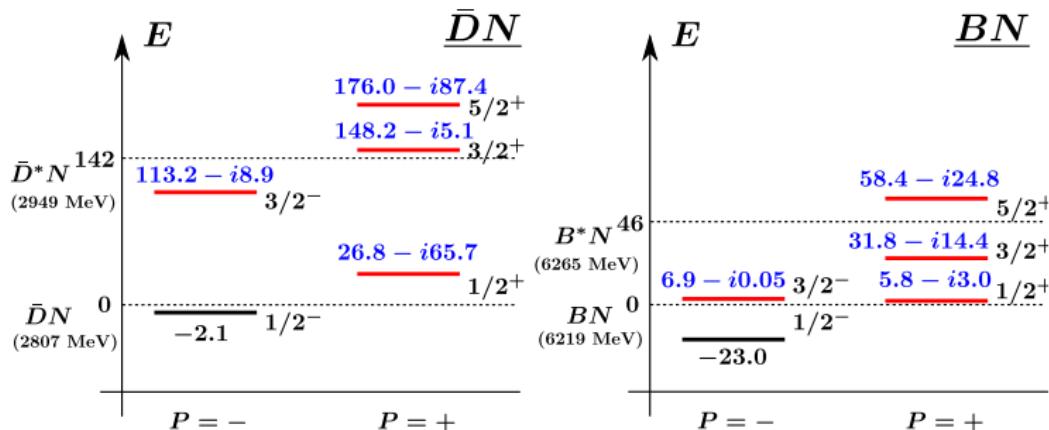
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- Many states near the thresholds. \Leftrightarrow No KN bound state

Energy spectra of \bar{D} meson-Nucleon ($\bar{D}N$) states

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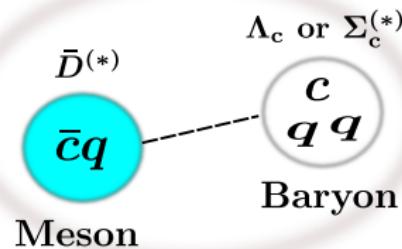
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- Many states near the thresholds. \Leftrightarrow **No KN bound state**
- The tensor force from the $\bar{D} - \bar{D}^*$ mixing** is important to produce a strong attraction!

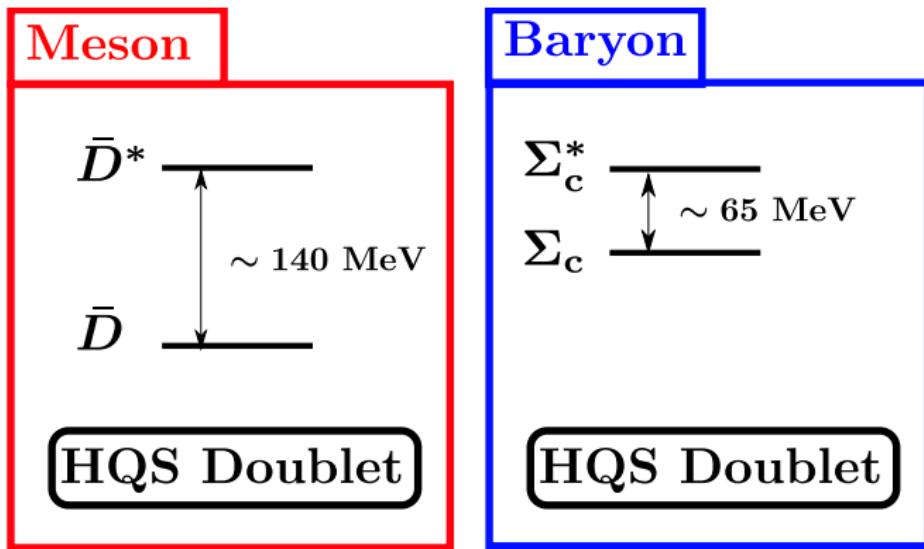
Channel coupling of Hidden-charm meson-baryon state



Coupled channels of the hidden-charm pentaquark

Introduction

- $\bar{D} - \bar{D}^*$ and $\Sigma_c - \Sigma_c^*$ mixings

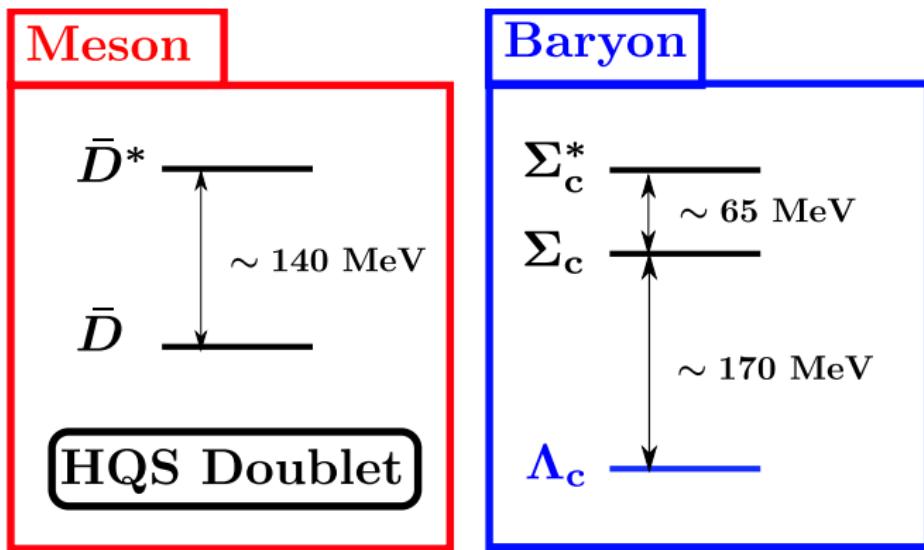


- Mass degeneracy of $\bar{D}\Sigma_c$, $\bar{D}\Sigma_c^*$, $\bar{D}^*\Sigma_c$ and $\bar{D}^*\Sigma_c^*$

Coupled channels of the hidden-charm pentaquark

Introduction

- $\bar{D} - \bar{D}^*$ and $\Sigma_c - \Sigma_c^*$ mixings



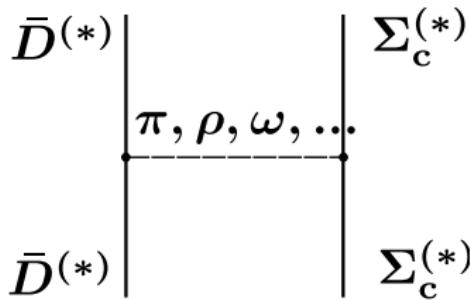
- Mass degeneracy of $\bar{D}\Sigma_c$, $\bar{D}\Sigma_c^*$, $\bar{D}^*\Sigma_c$ and $\bar{D}^*\Sigma_c^*$
- Λ_c (cqq): $\bar{D}^{(*)}\Lambda_c$ channel?

Coupled channels of the hidden-charm pentaquark

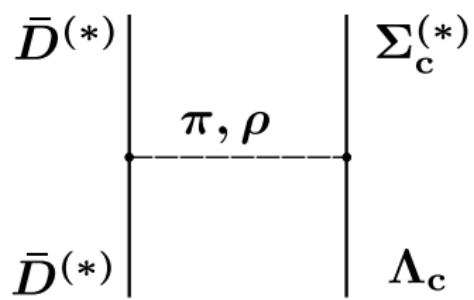
Introduction

- $\bar{D}^{(*)}\Lambda_c - \bar{D}^{(*)}\Sigma_c^{(*)}$ mixing (analogous to $\Lambda N - \Sigma N$)
 $m_{\Sigma_c} - m_{\Lambda_c} \sim 170$ MeV

$\bar{D}^{(*)}\Sigma_c^{(*)}$ coupling



$\bar{D}^{(*)}\Lambda_c^{(*)} - \bar{D}^{(*)}\Sigma_c^{(*)}$ coupling



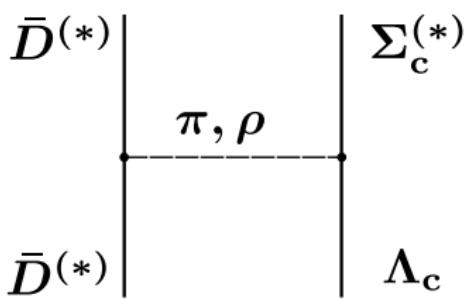
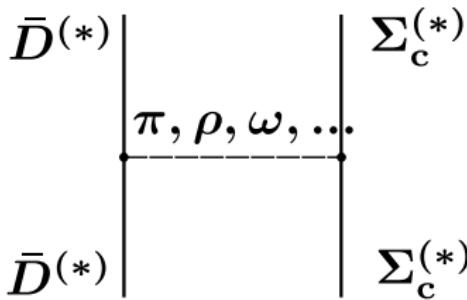
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$\bar{D}^{(*)}\Lambda_c^{(*)} - \bar{D}^{(*)}\Sigma_c^{(*)}$ coupling



⇒ $\bar{D}\Lambda_c, \bar{D}^*\Lambda_c, \bar{D}\Sigma_c, \bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$ (**6 thresholds!**)

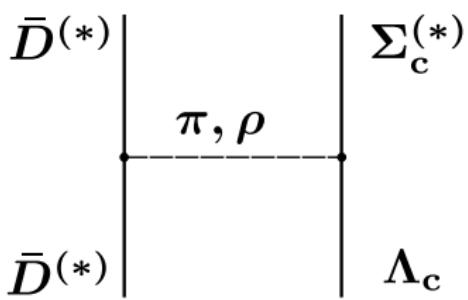
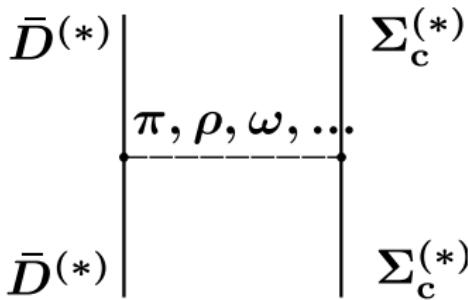
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$\bar{D}^{(*)}\Sigma_c^{(*)}$ coupling

$\bar{D}^{(*)}\Lambda_c^{(*)} - \bar{D}^{(*)}\Sigma_c^{(*)}$ coupling



⇒ $\bar{D}\Lambda_c, \bar{D}^*\Lambda_c, \bar{D}\Sigma_c, \bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$ (**6 thresholds!**)

- Coupling to a state with $\ell \neq 0$ (D -wave,...)
⇒ **Tensor force producing a strong attraction!**

Coupled-Channels

- Allowed channels (^{2S+1}L) for $J^P = 3/2^\pm, 5/2^\pm$

| J^P | Channels |
|---------|----------|
| $3/2^-$ | |
| $3/2^+$ | |
| $5/2^-$ | |
| $5/2^+$ | |

- $J^P = 3/2^\pm$:
- $J^P = 5/2^\pm$:

Coupled-Channels

- Allowed channels (${}^{2S+1}L$) for $J^P = 3/2^\pm, 5/2^\pm$

| J^P | Channels |
|---------|---|
| $3/2^-$ | $\bar{D}\Lambda_c({}^2D)$, $\bar{D}^*\Lambda_c({}^4S, {}^2D, {}^4D)$, $\bar{D}\Sigma_c({}^2D)$, $\bar{D}\Sigma_c^*({}^4S, {}^4D)$, $\bar{D}^*\Sigma_c({}^4S, {}^2D, {}^4D)$, $\bar{D}^*\Sigma_c^*({}^4S, {}^2D, {}^4D, {}^6D, {}^6G)$ |
| $3/2^+$ | |
| $5/2^-$ | |
| $5/2^+$ | |

- $J^P = 3/2^\pm$: **15 channels!**
- $J^P = 5/2^\pm$:

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| $3/2^+$ | $\bar{D}\Lambda_c(^2P)$, $\bar{D}^*\Lambda_c(^2P, ^4P, ^4F)$, $\bar{D}\Sigma_c(^2P)$, $\bar{D}\Sigma_c^*(^4P, ^4F)$, $\bar{D}^*\Sigma_c(^2P, ^4P, ^4F)$, $\bar{D}^*\Sigma_c^*(^2P, ^4P, ^6P, ^4F, ^6F)$ |
| $5/2^-$ | |
| $5/2^+$ | |

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| $5/2^-$ | $\bar{D}\Lambda_c(^2D)$, $\bar{D}^*\Lambda_c(^2D, ^4D, ^4G)$, $\bar{D}\Sigma_c(^2D)$, $\bar{D}\Sigma_c^*(^4D, ^4G)$, $\bar{D}^*\Sigma_c(^2D, ^4D, ^4G)$, $\bar{D}^*\Sigma_c^*(^6S, ^2D, ^4D, ^6D, ^4G, ^6G)$ |
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- $J^P = 3/2^\pm$: **15 channels!**
- $J^P = 5/2^\pm$: **16 channels!**

Coupled-Channels

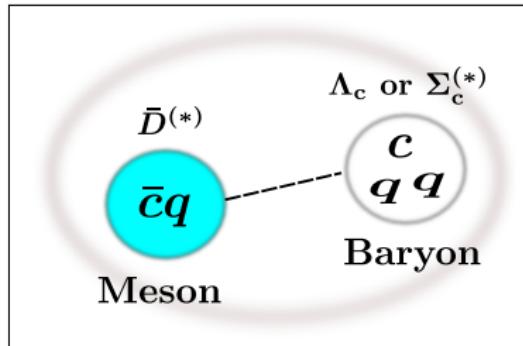
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| $5/2^+$ | $\bar{D}\Lambda_c(^2F)$, $\bar{D}^*\Lambda_c(^4P, ^2F, ^4F)$, $\bar{D}\Sigma_c(^2F)$, $\bar{D}\Sigma_c^*(^4P, ^4F)$, $\bar{D}^*\Sigma_c(^4P, ^2F, ^4F)$, $\bar{D}^*\Sigma_c^*(^4P, ^6P, ^2F, ^4F, ^6F, ^6H)$ |

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- $J^P = 5/2^\pm$: **16 channels!**

Main Subject: Pentaquarks

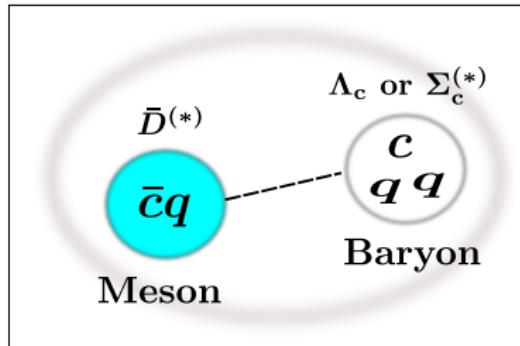
- Hadronic molecules formed by **hidden-charm meson-baryon**.



- Bound and resonant states of $\bar{D}^{(*)}\Lambda_c - \bar{D}^{(*)}\Sigma_c^{(*)}$
- △ Coupling to $\bar{D}^{(*)}\Lambda_c$ and $\bar{D}^{(*)}\Sigma_c^{(*)}$
- △ Coupling to the state with $\ell \neq 0$
- △ Negative and Positive parity states ($P = \pm$)

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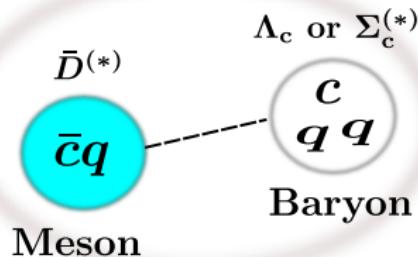
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The full-coupled channel analysis of $\bar{D}^{(*)}\Lambda_c - \bar{D}^{(*)}\Sigma_c^{(*)}$
has never performed so far !

Results of $\bar{D}^{(*)}B$ states (2-body)



$$\bar{D}^{(*)}\Lambda_c - \bar{D}^{(*)}\Sigma_c^{(*)}$$

Exotic states ($c\bar{c}qqq$)

Bound state and Resonance

- We solve the coupled-channel Schrödinger equations with $J^P = 3/2^\pm, 5/2^\pm$ and isospin $I = 1/2$.
- Interaction: $\pi\rho\omega\sigma$ exchange potentials

$\bar{D}^{(*)}B$ Interaction: Meson exchange potential

- Effective Lagrangian with heavy quark symmetry

R.Casalbuoni *et al.*, Phys.Rept.**281** (1997)145, T.M.Yan *et al.*, PRD**46**(1992)1148,
Y.-R.Liu and M.Oka, PRD**85**(2012)014015

Meson: $\mathcal{L}_{\pi HH} = g_\pi \text{Tr} [H_b \gamma_\mu \gamma_5 A_{ba}^\mu \bar{H}_a]$

Baryon:

$$\mathcal{L}_{\pi BB} = \frac{3}{2} g_1 i v_\kappa \varepsilon^{\mu\nu\lambda\kappa} \text{tr} [\bar{S}_\mu A_\nu S_\lambda] + g_4 \text{tr} [\bar{S}^\mu A_\mu \Lambda_c]$$

Heavy meson and baryon fields

$$H_a = \frac{1+\not{v}}{2} [\mathbf{P}_a^\ast \mu \gamma^\mu - \mathbf{P}_a \gamma^5] \quad (1^- \text{ and } 0^-)$$

$$S_\mu = \Sigma_\mu^\ast + \frac{\delta}{\sqrt{3}} (\gamma_\mu + v_\mu) \gamma_5 \Sigma \quad (3/2^+ \text{ and } 1/2^+)$$

- $\bar{D} - \bar{D}^*$ and $\Sigma_c - \Sigma_c^*$ mixings

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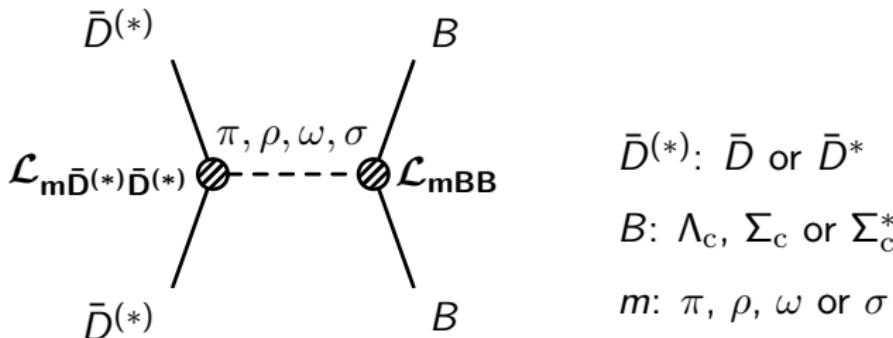


Fig: Meson exchange diagram

$$V_{\bar{D}^{(*)}B - \bar{D}^{(*)}B}^{\pi} = G \left[\vec{\mathcal{O}}_1 \cdot \vec{\mathcal{O}}_2 C(r) + S_{\mathcal{O}_1 \mathcal{O}_2} T(r) \right]$$

$C(r)$: Central force, $T(r)$: Tensor force

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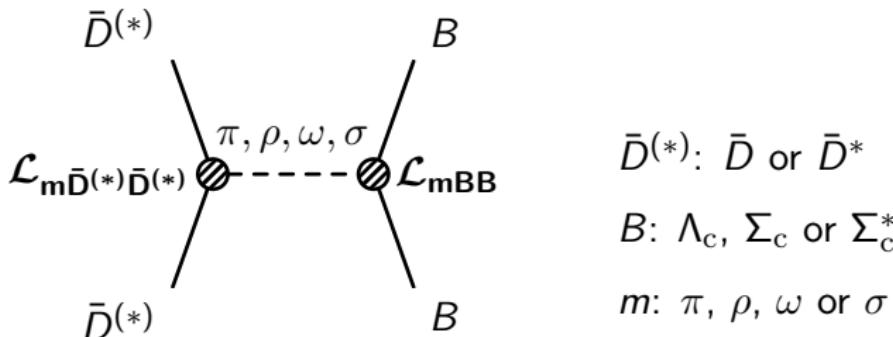


Fig: Meson exchange diagram

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$C(r)$: Central force, $T(r)$: Tensor force

- Form factor with common cutoff $\Lambda \leftarrow$ Free parameter

$$F(\Lambda, \vec{q}) = \frac{\Lambda^2 - m_\alpha^2}{\Lambda^2 + |\vec{q}|^2} \quad (\text{fixed by the observed mass of } P_c)$$

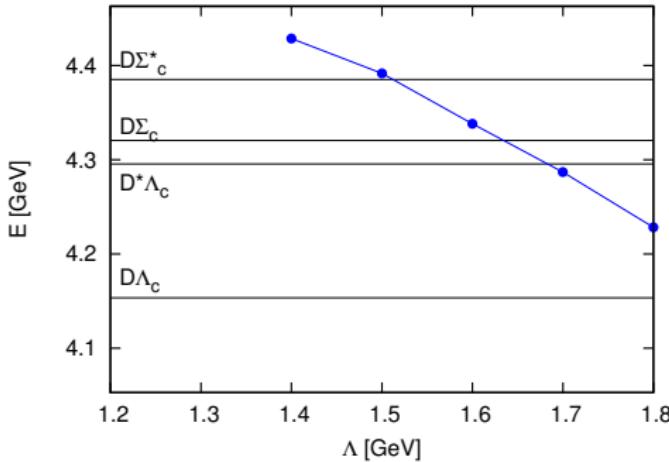
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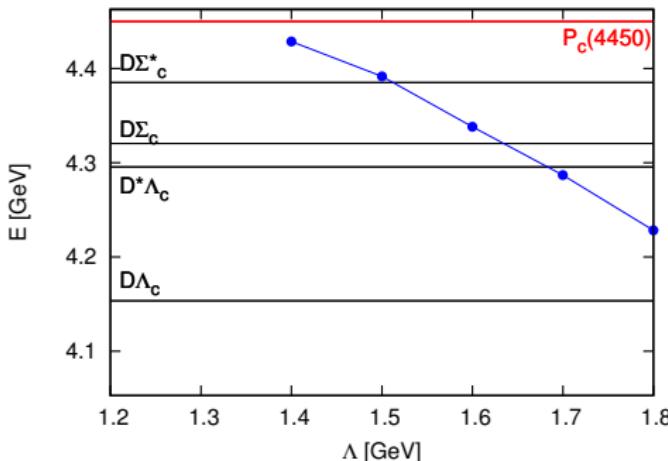
→ In our results, only **the $J^P = 5/2^-$ state** appears above the $\bar{D}\Sigma_c^*$ threshold!



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$P_c^+(4450)$:

$$M = 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$$

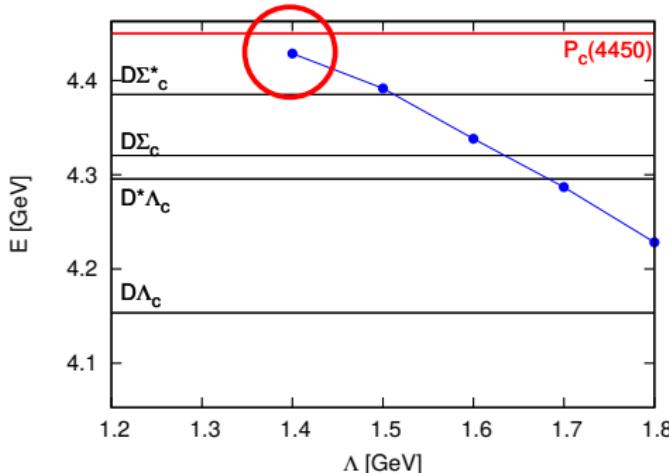
$J^P = 5/2^-$ state:

$$M = 4428.6 \text{ MeV} \text{ in } \Lambda = 1400 \text{ MeV}$$

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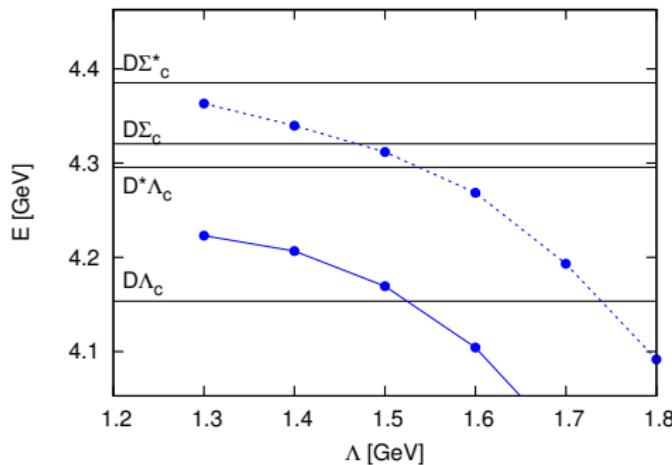
Cutoff $\Lambda = 1400$ MeV, J^P of $P_c^+(4450) = 5/2^-$

What is J^P of $P_c^+(4380)$?

- ▷ $P_c^+(4450)$: $J^P = 5/2^- \Rightarrow J^P$ of $P_c^+(4380)$ is **3/2⁺!**

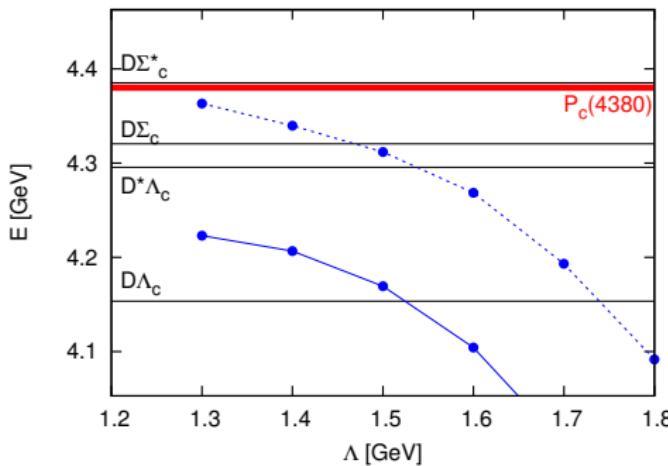
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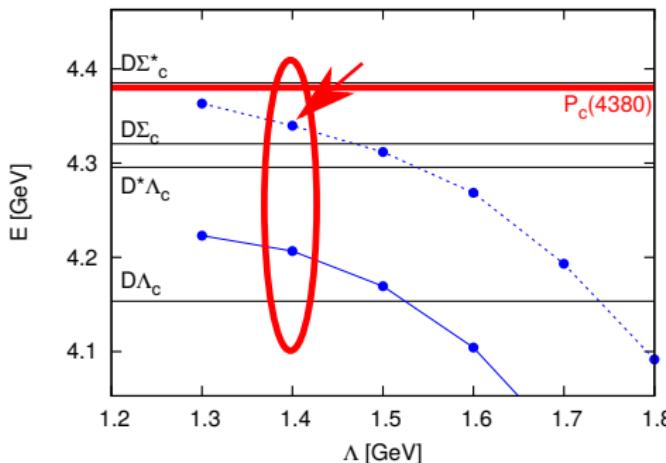


$P_c^+(4380)$: $M = 4380 \pm 8 \pm 29$ MeV

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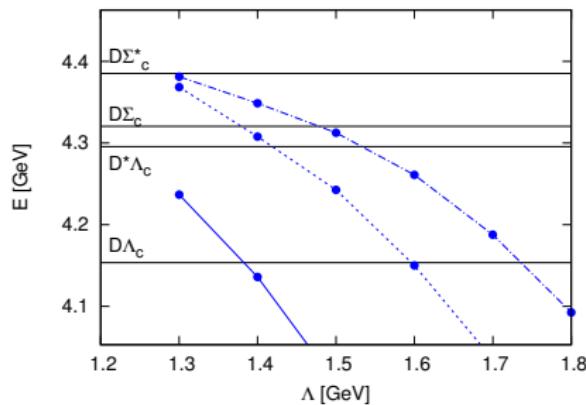
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$P_c^+(4380)$: **$J^P = 3/2^+$** $P_c^+(4450)$: **$J^P = 5/2^-$**

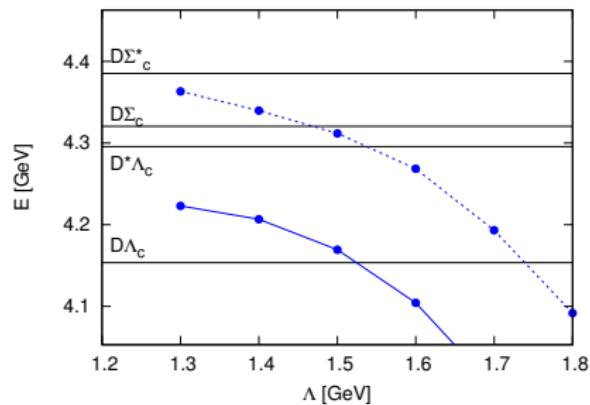
Cutoff $\Lambda = 1400$ MeV

Other predicted states

(i) $J^P = 3/2^-$



(ii) $J^P = 3/2^+$



- In $\Lambda = 1400$ MeV,

$J^P = 3/2^-$: 4136.0 MeV, 4307.9 MeV and 4348.7 MeV

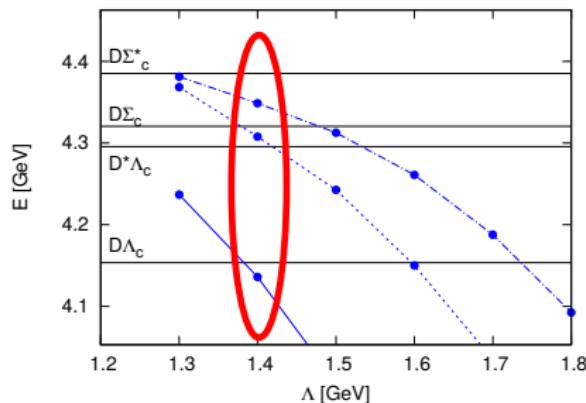
$J^P = 3/2^+$: 4206.7 MeV

New states are predicted!

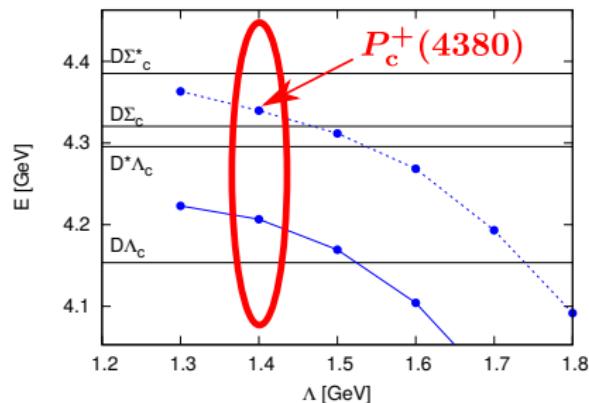
(can be decayed to $J/\psi p$, $\bar{D}^{(*)}\Lambda_c, \dots$)

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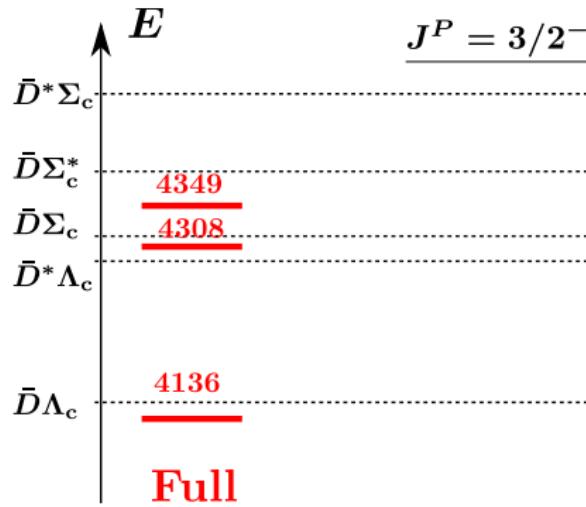
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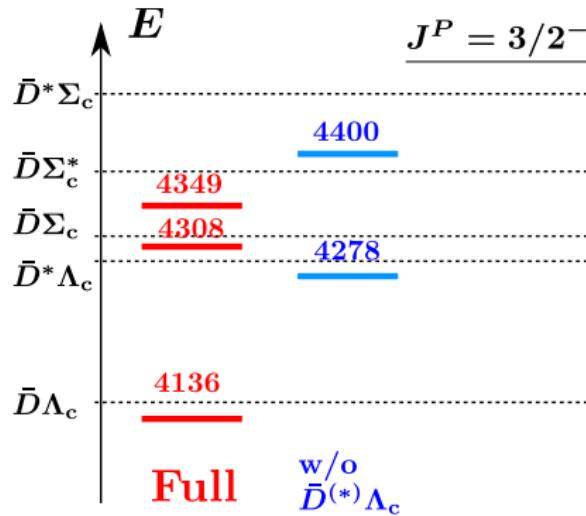
Channel-coupling effects

- Obtained mass with **Full channel coupling**, without $\bar{D}^{(*)}\Lambda_c$ and **without $\ell > 0$ ($\ell > 1$)**



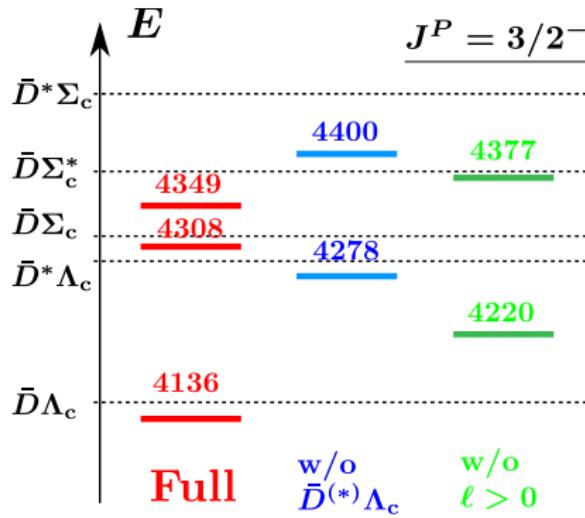
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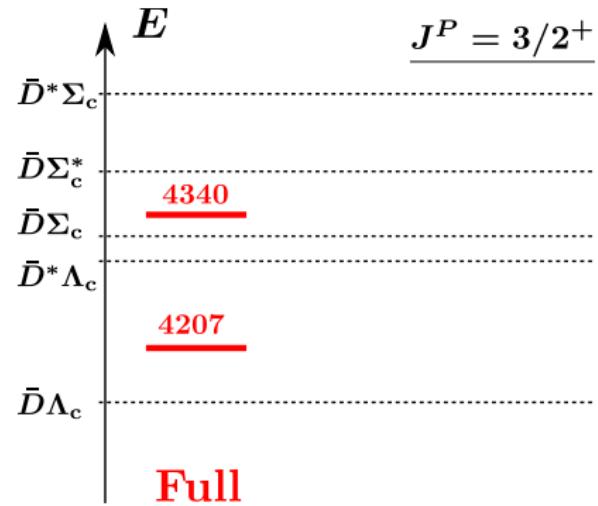
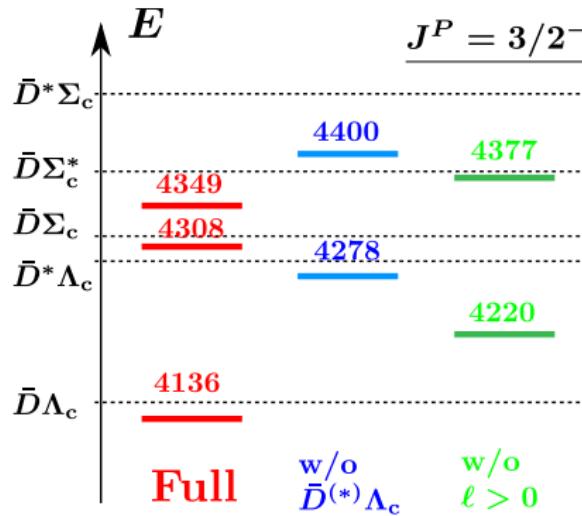
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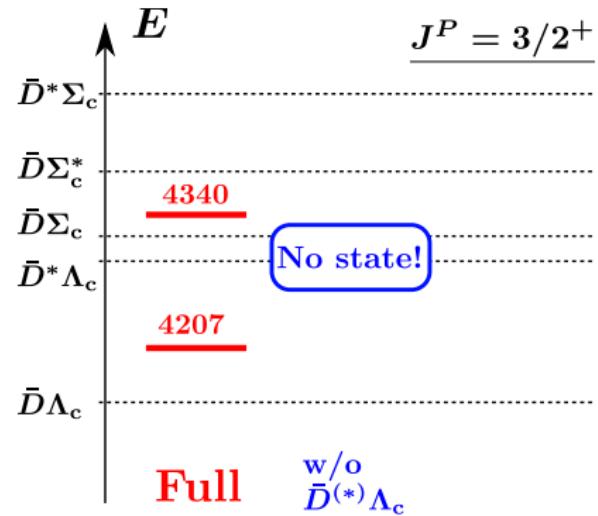
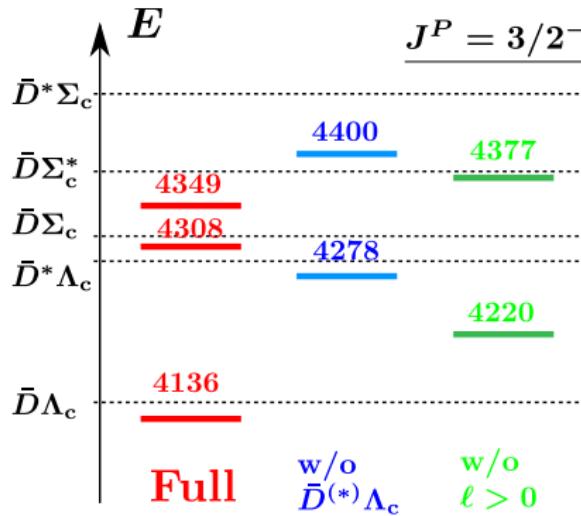
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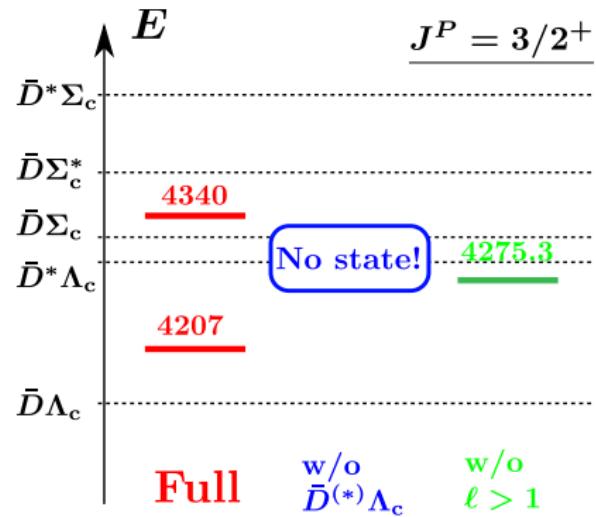
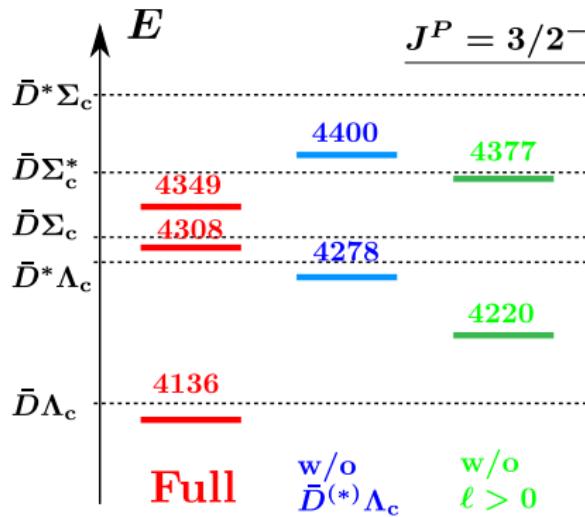
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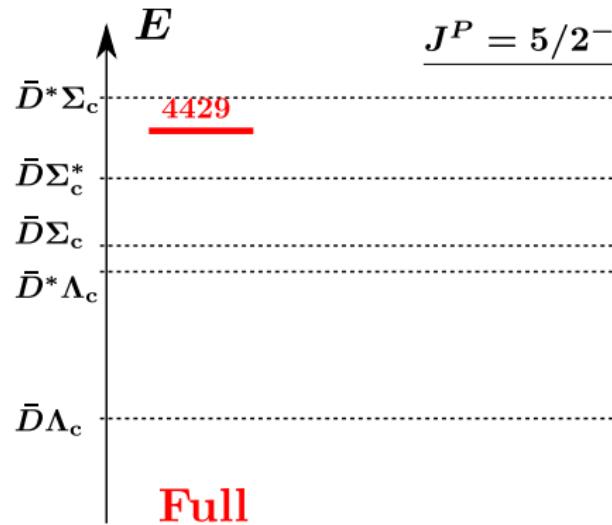
- Obtained mass with **Full channel coupling**, without $\bar{D}^{(*)}\Lambda_c$ and **without $\ell > 0$ ($\ell > 1$)**



- $\bar{D}^{(*)}\Lambda_c$ and $\ell > 0$ ($\ell > 1$) components are not negligible.

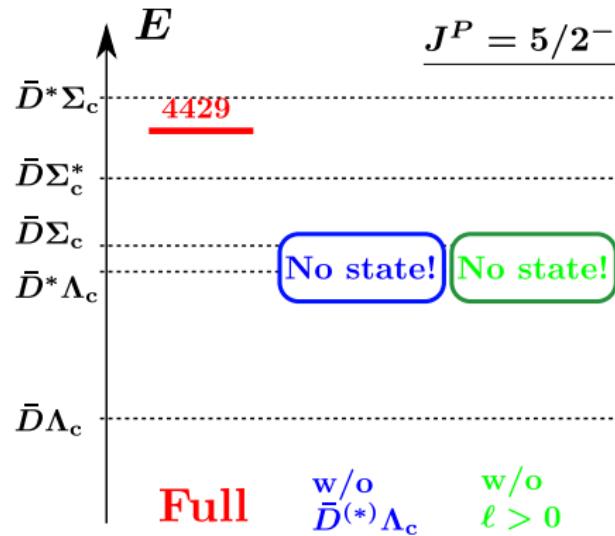
Channel-coupling effects

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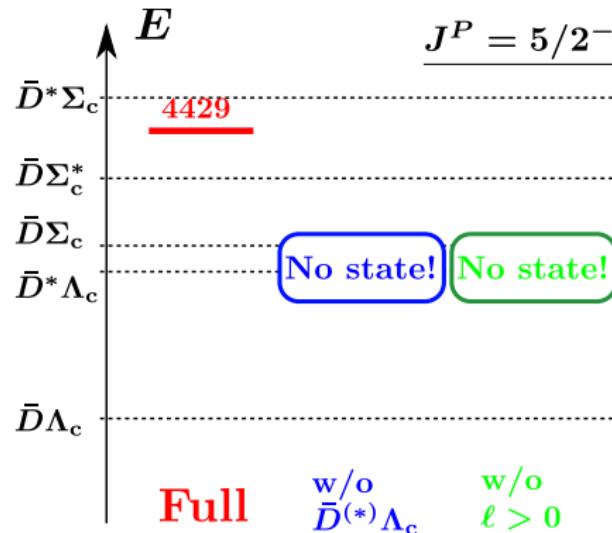
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Channel-coupling effects

- Obtained mass with **Full channel coupling**, **without $\bar{D}^{(*)}\Lambda_c$** and **without $\ell > 0$**



- $\bar{D}^{(*)}\Lambda_c$ and $\ell > 0$** components are important!

Summary

Subject: Hidden-charm pentaquarks as a meson-baryon molecule



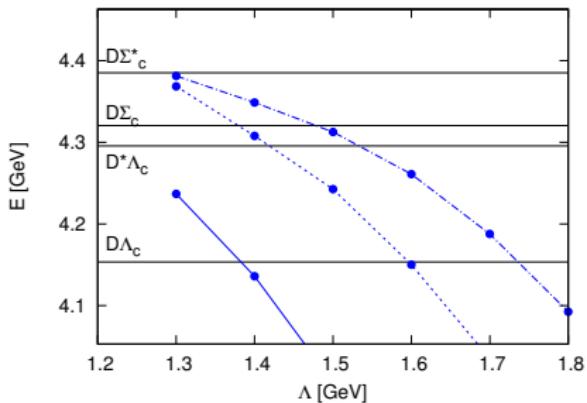
- Coupled-channel analysis is performed, taking into account...
 - ▷ Meson-baryon components $\bar{D}^{(*)}\Lambda_c - \bar{D}^{(*)}\Sigma_c^{(*)}$
 - ▷ Couplings to states with $\ell > 0$ ($S - D - G, P - F - H$)
⇒ **Tensor force**
 - ▷ Negative and positive parity states with $J^P = 3/2^\pm, 5/2^\pm$
- The meson exchange potential respecting to **the heavy quark spin symmetry** is employed.
- The J^P assignment of $P_c^+(4380)$ and $P_c^+(4450)$ is **$3/2^+$** and **$5/2^-$** , respectively.
- New states are predicted in $J^P = 3/2^\pm$.

Outlook

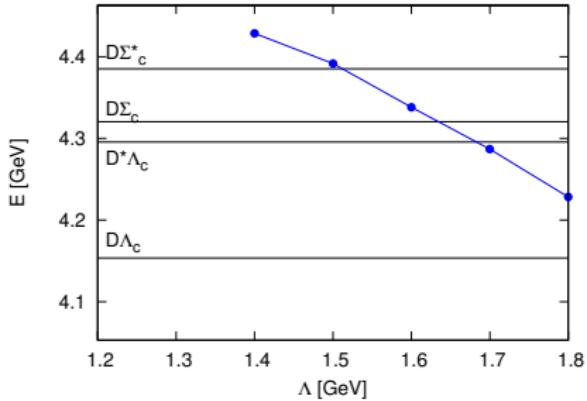
- Coupling to $J/\psi p$, cutoff Λ , $1/m_Q$ correction,...

Back up

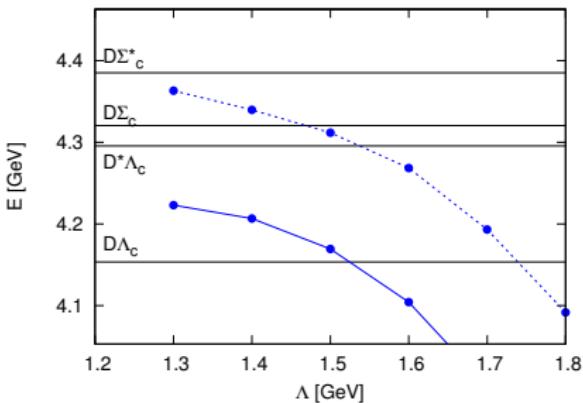
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(iii) $J^P = 5/2^-$



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(iv) $J^P = 5/2^+$

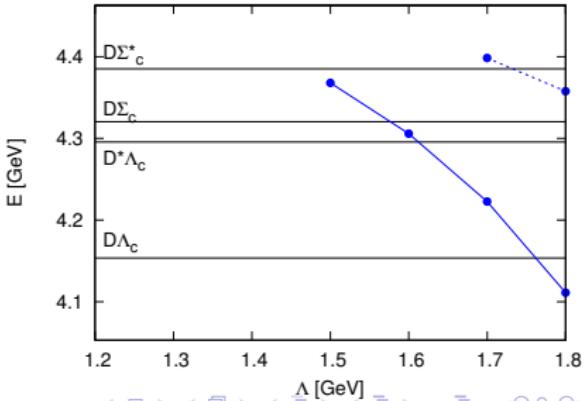


Table : Obtained masses in $\Lambda = 1400$ MeV.

| J^P | $E = E_{\text{re}} - i\Gamma/2$ [MeV] |
|---------|---|
| $3/2^-$ | 4136.0, 4307.9 – $i18.8$, 4348.7 – $i21.1$ |
| $3/2^+$ | 4206.7 – $i41.2$, 4339.7 – $i26.8$ |
| $5/2^-$ | 4428.6 – $i89.1$ |

Table : Obtained masses with full channel coupling (Full), without $\bar{D}^{(*)}\Lambda_c$ (w/o $\bar{D}^{(*)}\Lambda_c$) and without large orbital angular momentum ℓ (w/o $\ell > 0$ or w/o $\ell > 1$) in $\Lambda = 1400$ MeV.

| J^P | Channels | Mass [MeV] |
|---------|------------------------------|------------------------|
| $3/2^-$ | Full | 4136.0, 4307.9, 4348.7 |
| | w/o $\bar{D}^{(*)}\Lambda_c$ | 4278.4, 4400.4 |
| | w/o $\ell > 0$ | 4220.4, 4376.6 |
| $3/2^+$ | Full | 4206.7, 4339.7 |
| | w/o $\bar{D}^{(*)}\Lambda_c$ | — |
| | w/o $\ell > 1$ | 4275.3 |
| $5/2^-$ | Full | 4428.6 |
| | w/o $\bar{D}^{(*)}\Lambda_c$ | — |
| | w/o $\ell > 0$ | — |

Table : Comparison of the lowest mass of hidden-charm meson-baryon molecules with $I(J^P) = 1/2(3/2^-)$ by this work with the early works. The obtained masses are shown in the second column in the unit of MeV. The value of this work is in $\Lambda = 1400$ MeV. The third column gives the channels which are considered in those works.

| Ref. | Mass [MeV] | Channels |
|-----------------------------|------------|---|
| This work | 4136.0 | $\bar{D}\Lambda_c, \bar{D}^*\Lambda_c, \bar{D}\Sigma_c, \bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$ |
| PRL 105 (2010)232001 | 4415 | $\bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$ with only <i>S</i> -wave |
| PRC 84 (2010)015202 | 4454 | $\bar{D}^*\Sigma_c, \bar{D}^*\Sigma_c^*$ with only <i>S</i> -wave |
| PRD 88 (2013)056012 | 4334.5 | $J/\psi N, \bar{D}^*\Lambda_c, \bar{D}^*\Sigma_c, \bar{D}\Sigma_c^*, \bar{D}^*\Sigma_c^*$ with only <i>S</i> -wave |