

# Meson - Spectroscopy with with COMPASS at CERN

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TU München





# Brief Overview

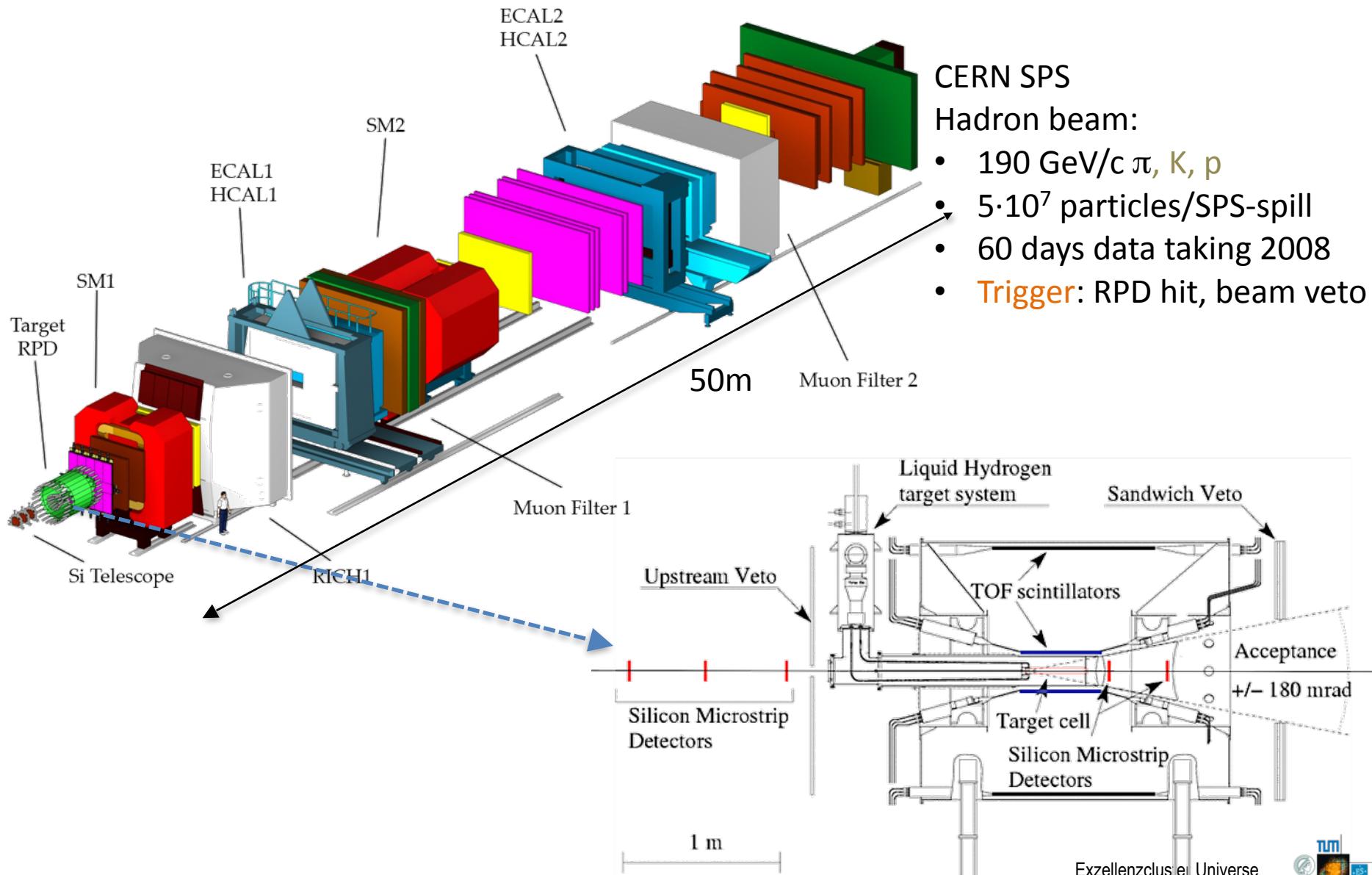


COMPASS performs physics with  $p$ ,  $K$ ,  $\pi$  beams

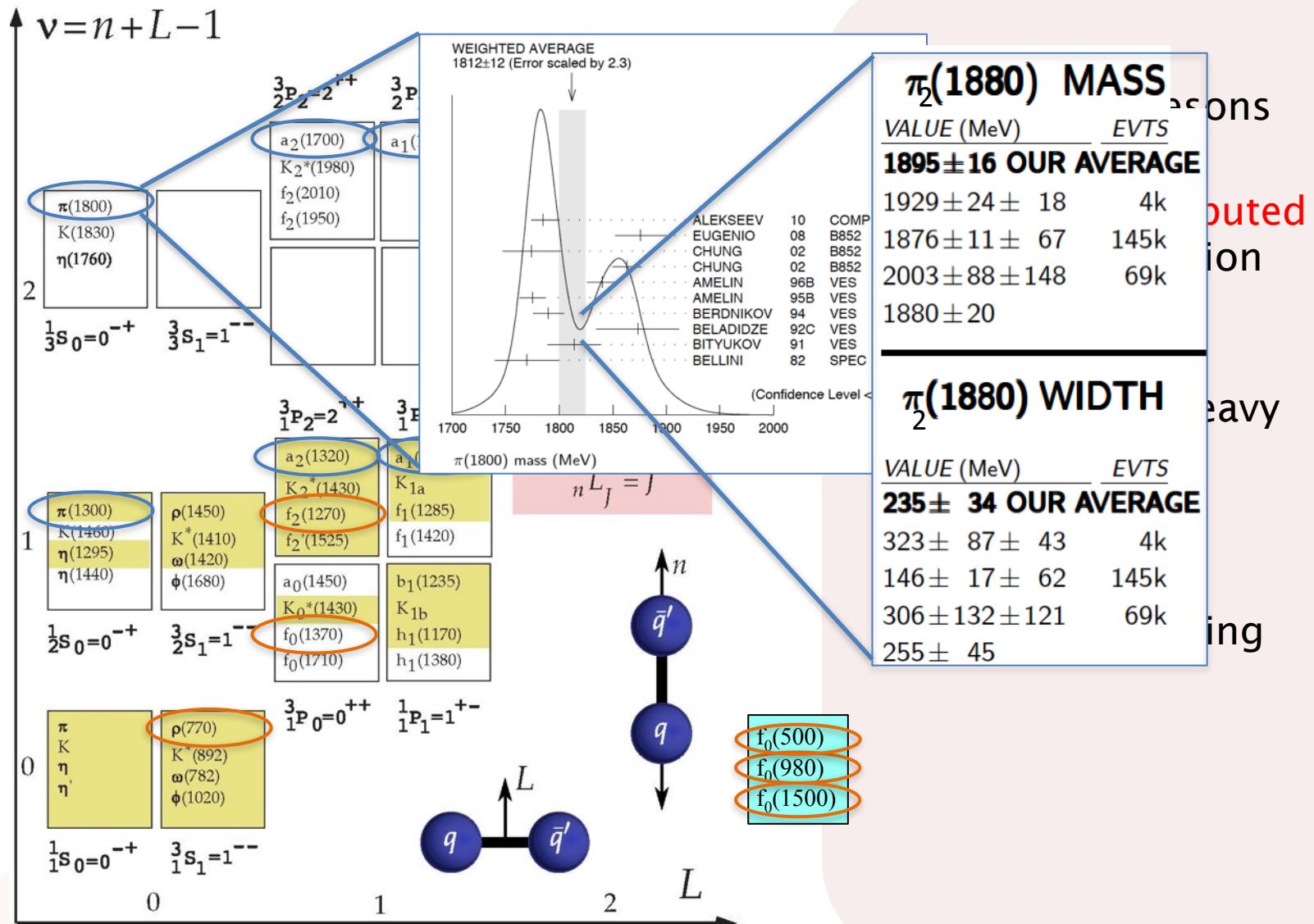
Examples will be given on

- Diffraction with  $\pi$  into  $3\pi$  (this talk)
- Spectroscopy in strong interaction
  - Introduction
  - Identification method (PWA)
  - results for  $a_J$  and  $\pi_J$  states
- New insights into production/decay dynamics
- Conclusions

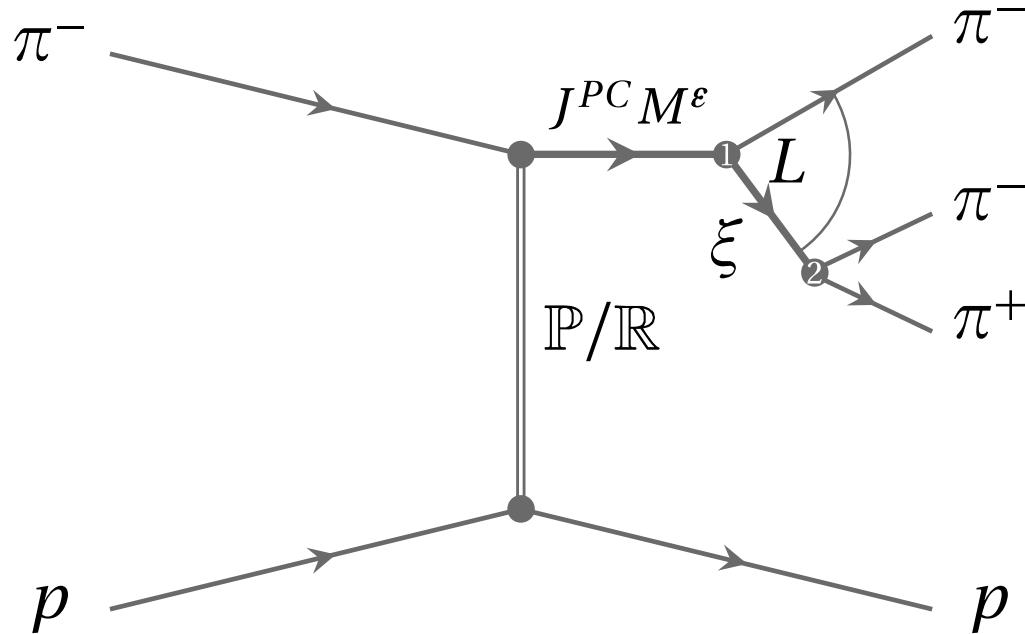
# The COMPASS Experiment



# Constituent Quarks and Mesons



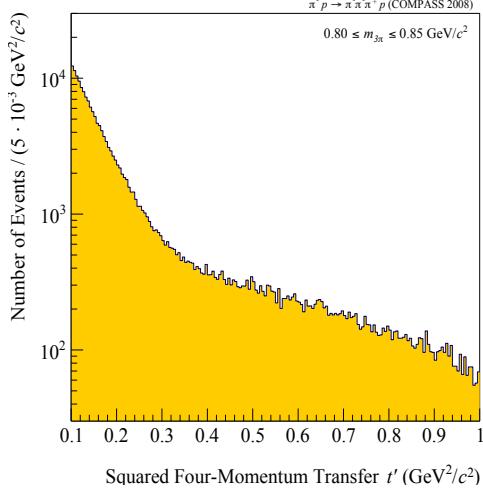
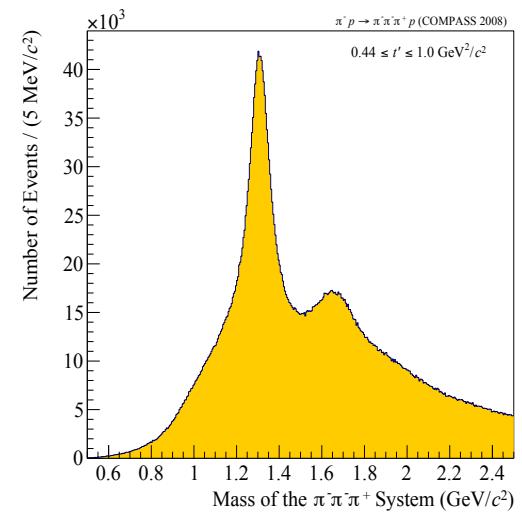
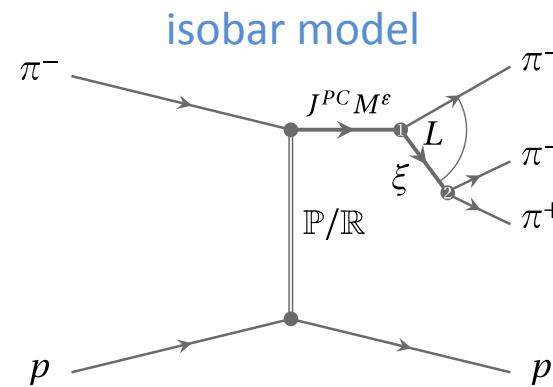
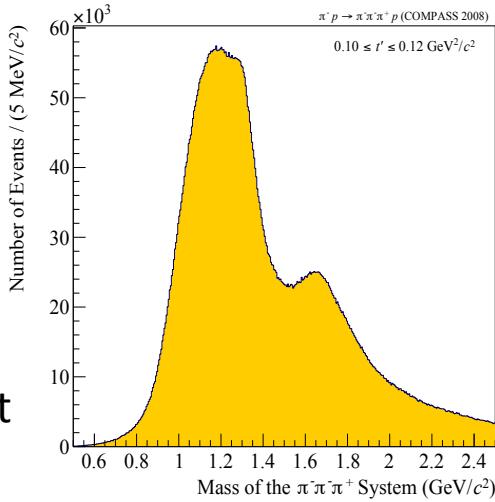
# Kinematics



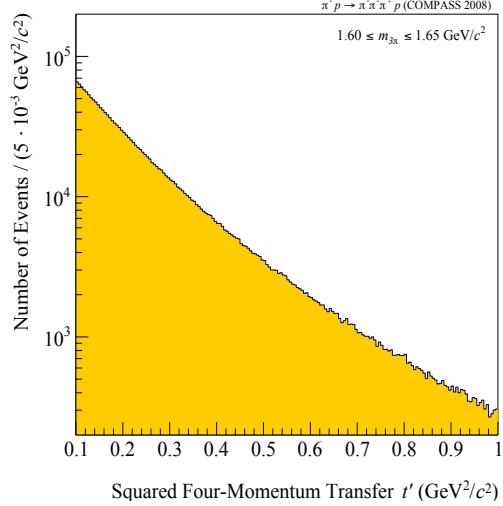
Example: production of  $3\pi$



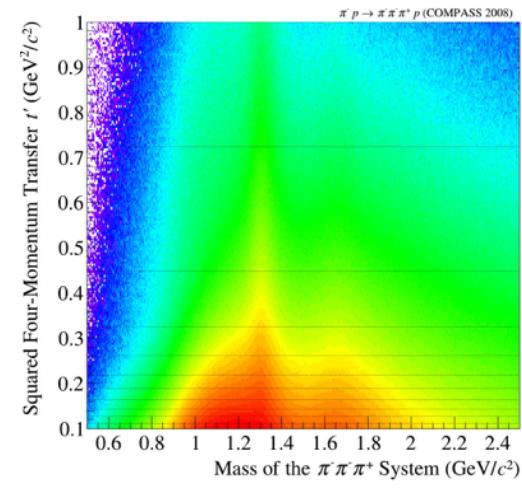
# Kinematics and Isobars



$0.8 < m_{3\pi} < 0.85$



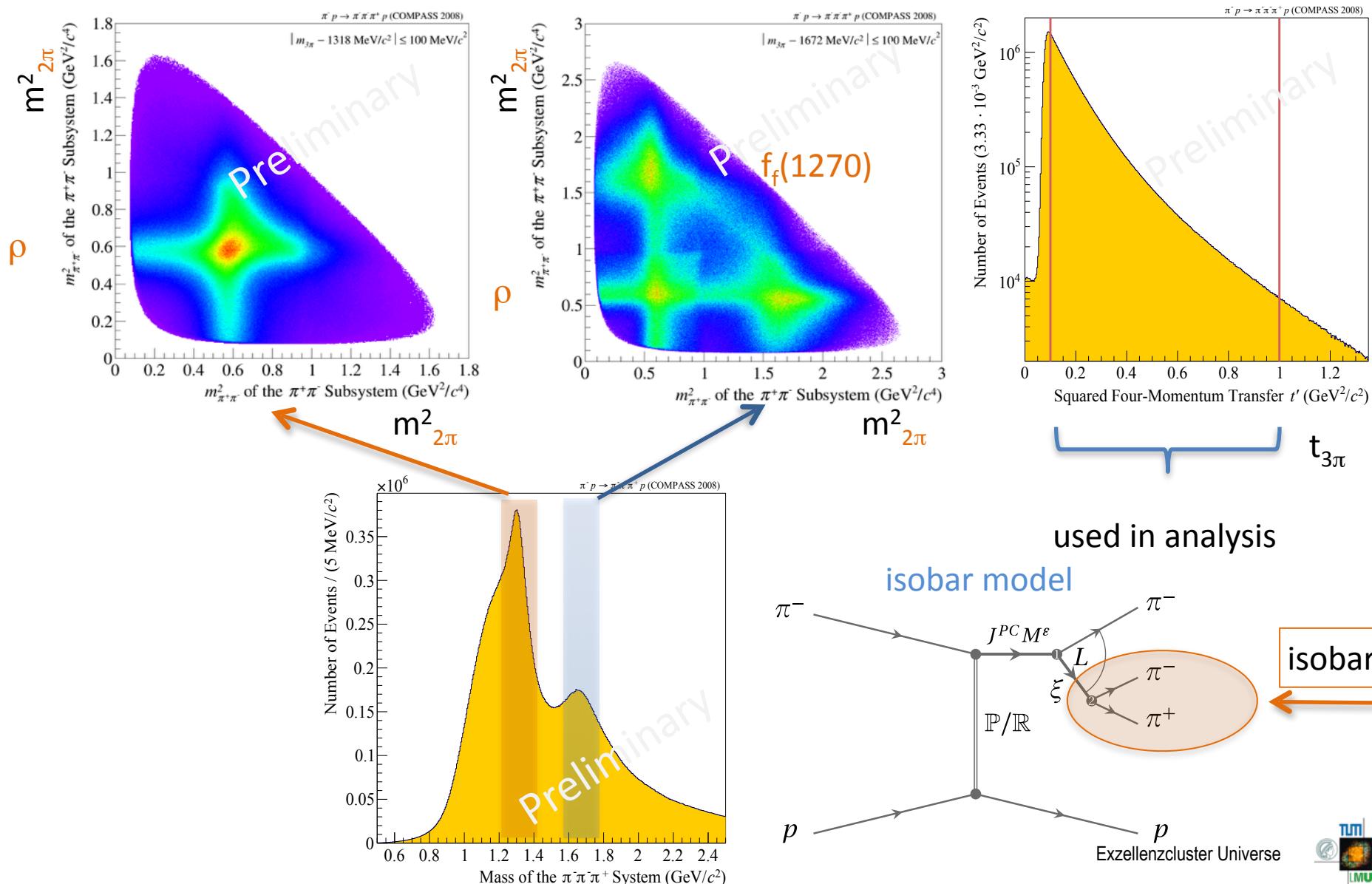
$1.6 < m_{3\pi} < 1.65$



grid of  $t$  used  
 $\Delta m: 20$  MeV/c<sup>2</sup>

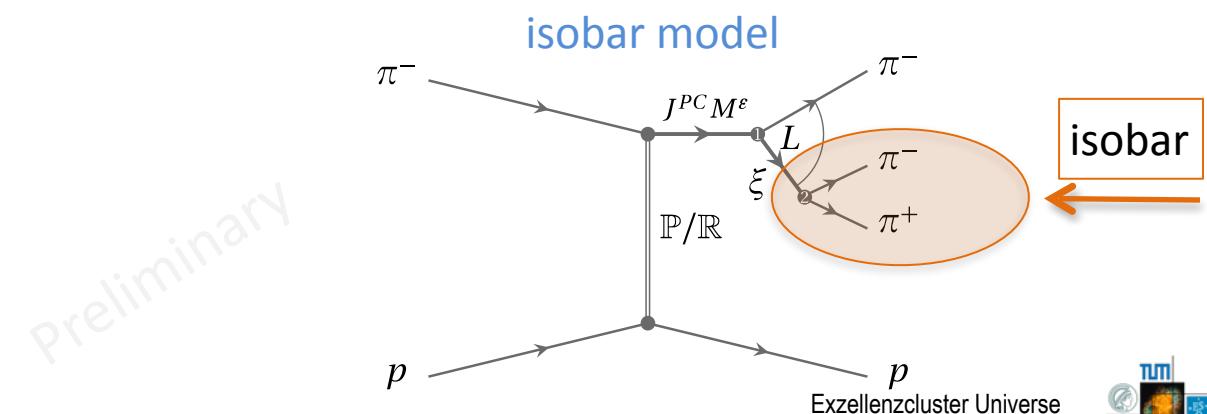
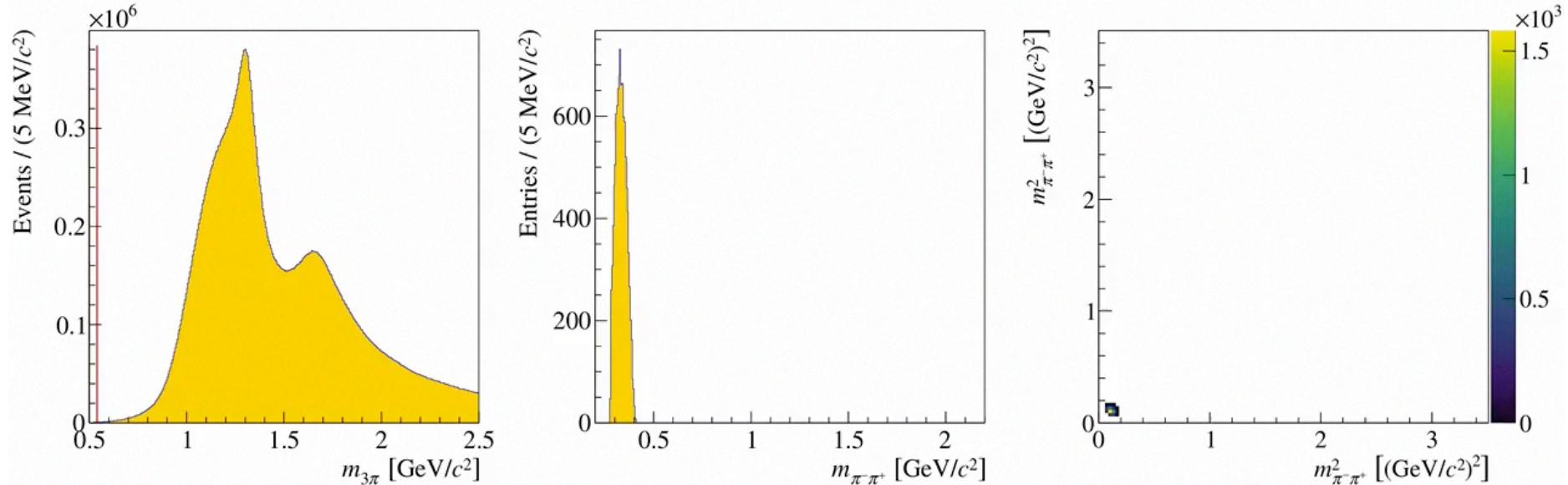
# First Impressions

## Motivation for Isobar Model



# First Impressions

## Motivation for Isobar Model



# Partial wave analysis

inspired by M. Pennington



What is PWA ?

Describe population in 5-dimensional phase space in  $\pi\pi\pi$  by model

- step 1
- Define a set of quantum numbers  $J^{PC}$
  - Define a set of possible decay channels for each  $J^{PC}$   
 $(X^- \rightarrow \text{isobar} + \pi; \text{isobar} \rightarrow \pi\pi)$  : **wave** (88 waves used)
    - each such “**wave**” has a pre-determined population in phase space
    - each wave may have alignment of  $J$  described by quantum number  $M$
  - For each bin of  $20 \text{ MeV}/c^2$  mass of  $\pi\pi\pi$  and bin of  $t$ : determine which **coherent** combination of waves fits distribution best
  - Obtain spin-density matrix

## What is PWA ?

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    - ( $X^- \rightarrow \text{isobar} + \pi; \text{isobar} \rightarrow \pi\pi$ ) : **wave** (88 waves used)
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  - For each bin of  $20 \text{ MeV}/c^2$  mass of  $\pi\pi\pi$  and bin of  $t$ : determine which **coherent** combination of waves fits distribution best
  - Obtain **spin-density matrix**
- 
- Describe spin density matrix (submatrix) by model containing resonances and non-resonant contributions connecting all mass bins
  - Determine **resonance parameters**

step 1

step 2

# Amplitude Analysis

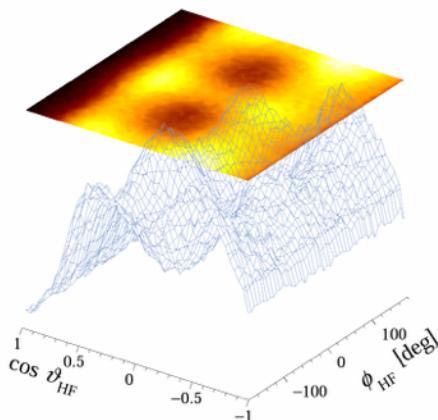
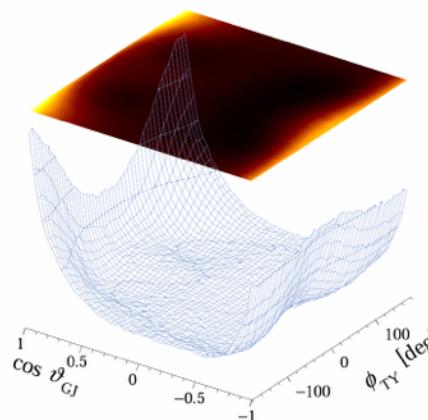
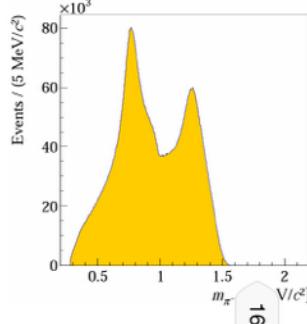
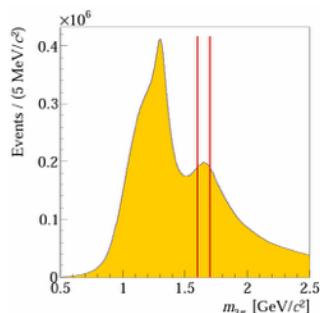
Use helicity amplitudes :

5-dimensional phase space:

mass of  $3\pi$

2 angles in  $3\pi$  rest frame

2 angles in isobar rest frame



# Amplitude Analysis

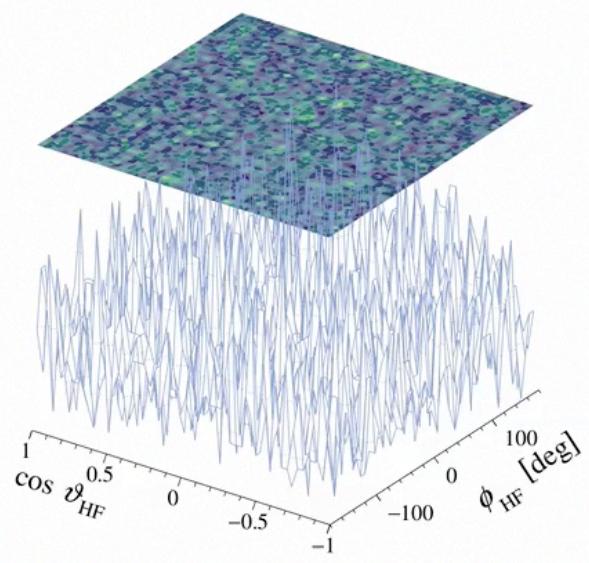
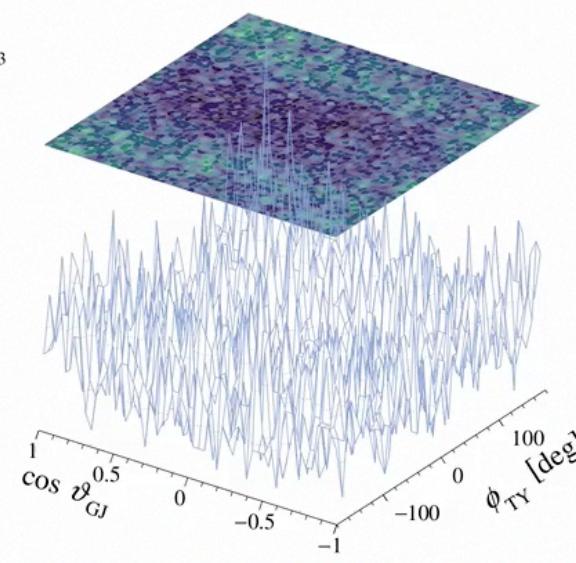
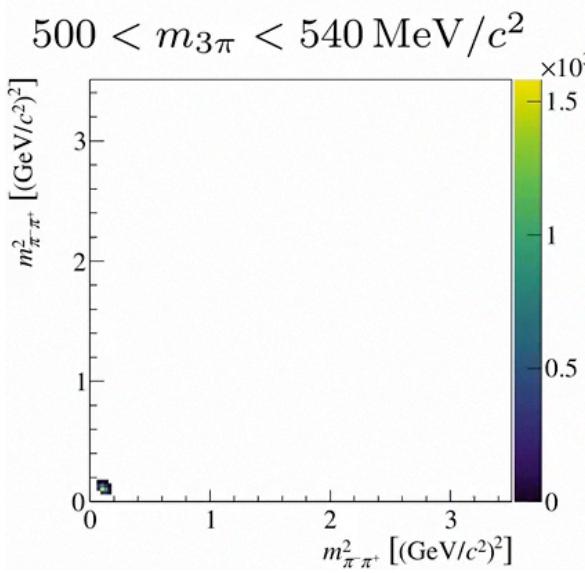
Use helicity amplitudes :

5-dimensional phase space:

Dalitz plot

2 angles in  $3\pi$  rest frame

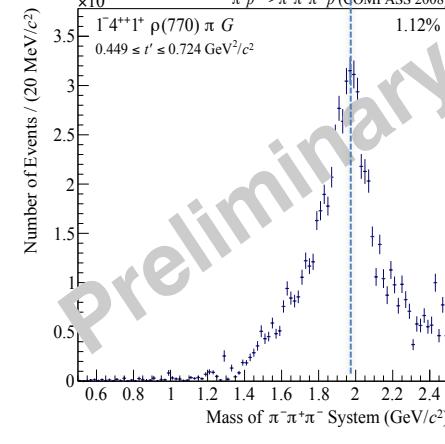
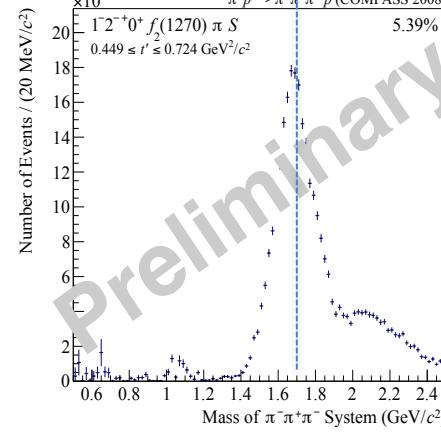
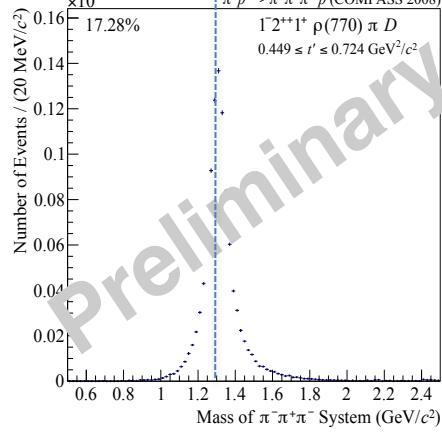
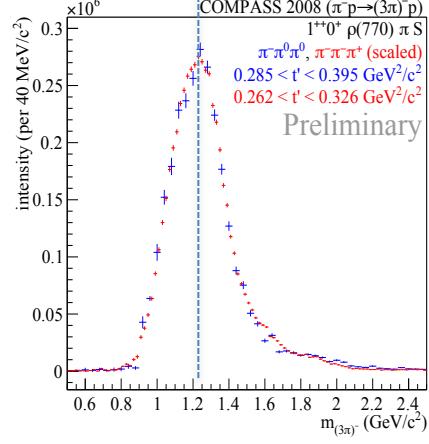
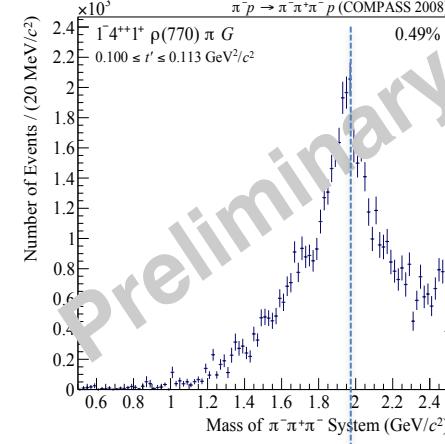
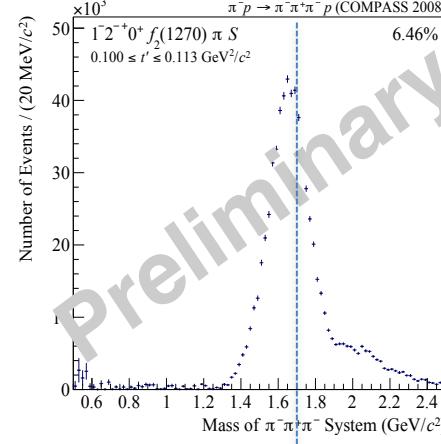
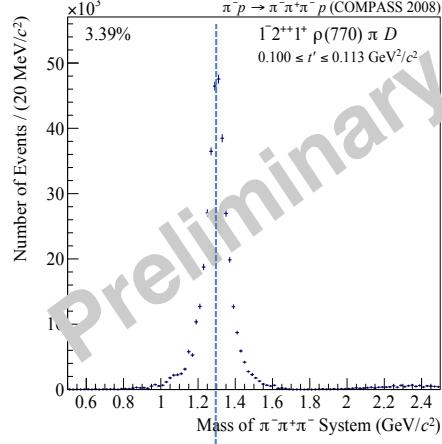
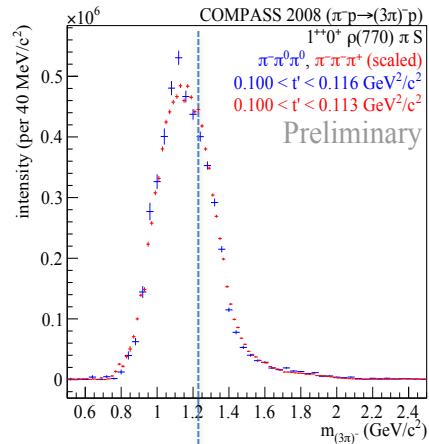
2 angles in isobar rest frame



# Spectral shape of waves t dependence



low t



$1^{++}0^+ \rho \pi S$

$2^{++}1^+ \rho \pi D$

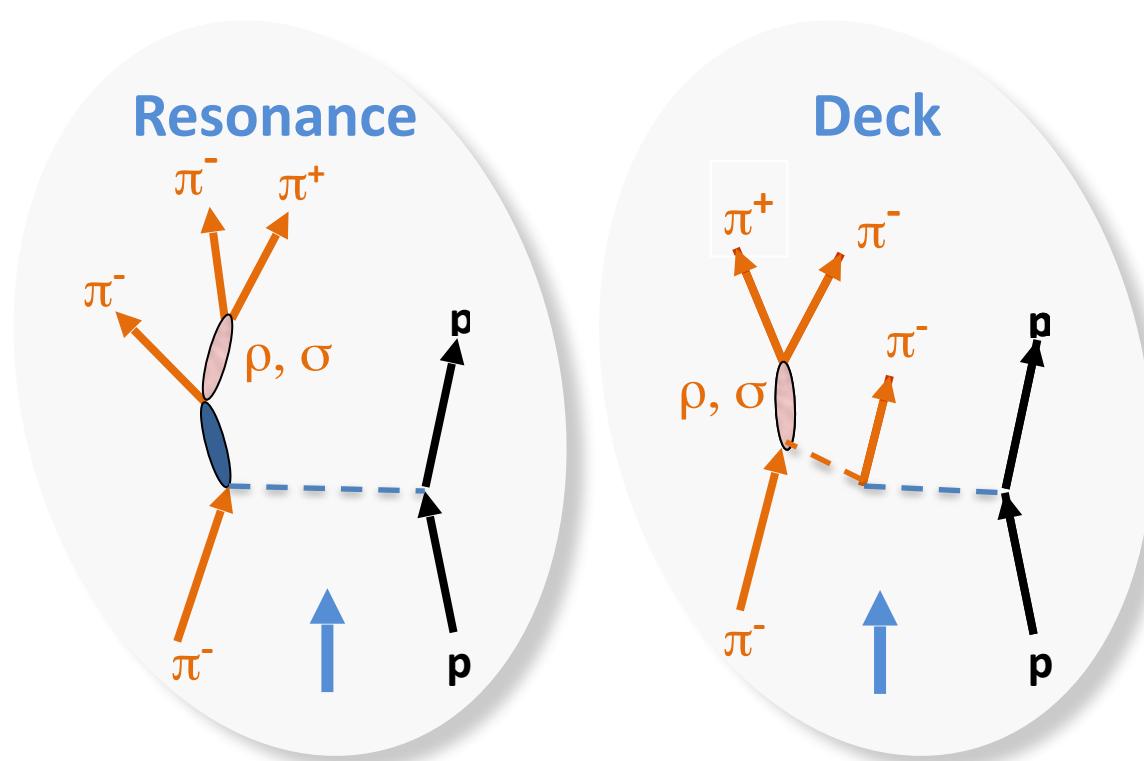
$2^{-0^+} f_2 \pi S$

$4^{++}1^+ \rho \pi G$

# Model for Spin Density Matrix

Describe the results obtained independently in different mass bins by a model

- select physics contributions
- fit to **spin density matrix** (not only to simple mass spectra)
- use 14 waves (out of all 88 waves)
  - 722 **free parameters**
  - 76505 **data points**

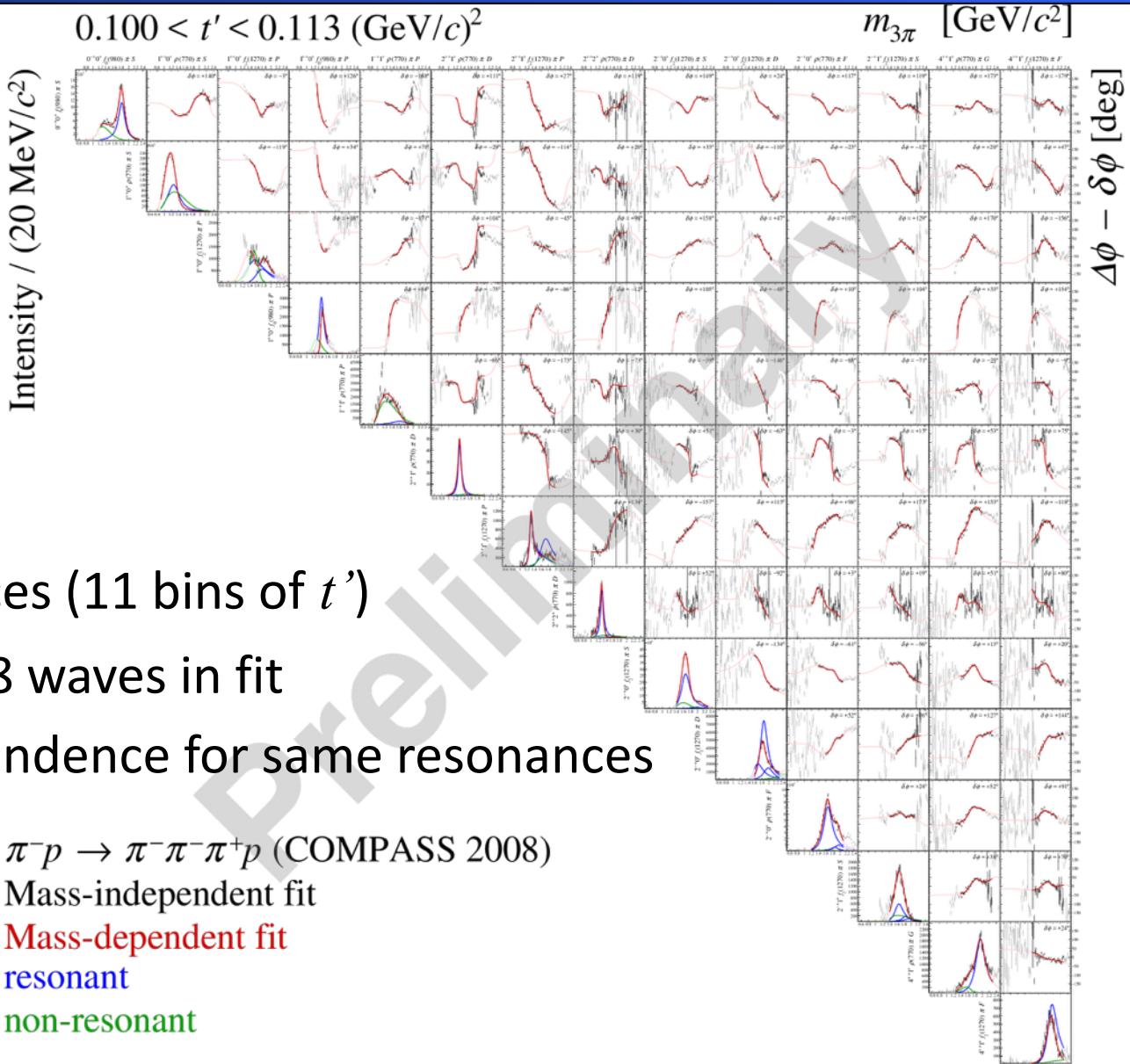


Two types of contributions

# Find the Resonances



Reference  
wave



- 11 matrices (11 bins of  $t'$ )
- use 14/88 waves in fit
- fix t-dependence for same resonances

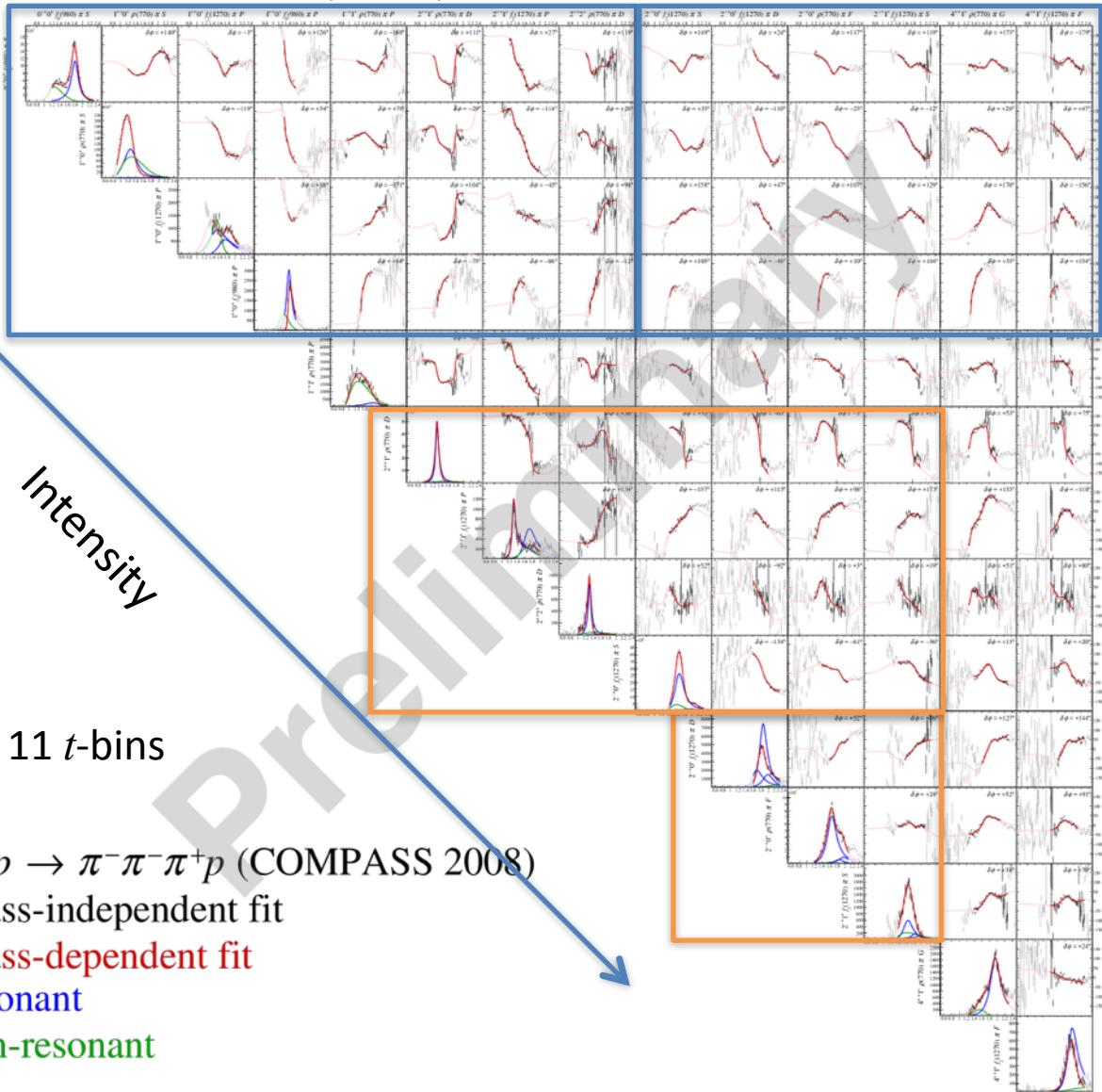
$\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$  (COMPASS 2008)  
 Mass-independent fit  
 Mass-dependent fit  
 resonant  
 non-resonant

# Find the Resonances

$0.100 < t' < 0.113 \text{ (GeV}/c^2)$

$m_{3\pi} \text{ [GeV}/c^2]$

$[\delta\phi] \phi\varrho - \phi V$



simultaneous fit in 11  $t$ -bins

$\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$  (COMPASS 2008)

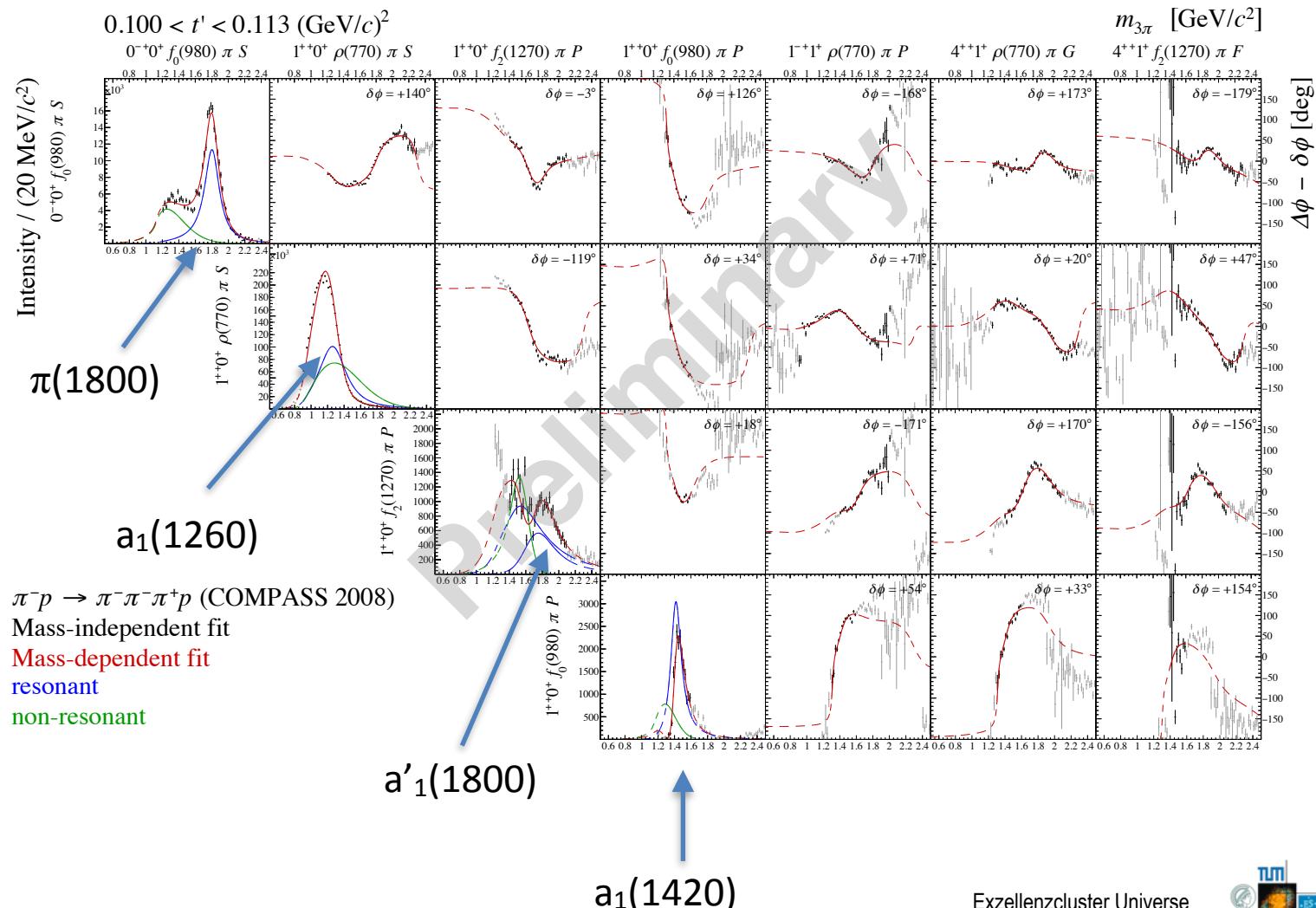
Mass-independent fit

Mass-dependent fit  
resonant

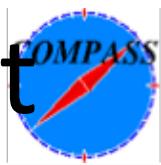
non-resonant

# Find the Resonances

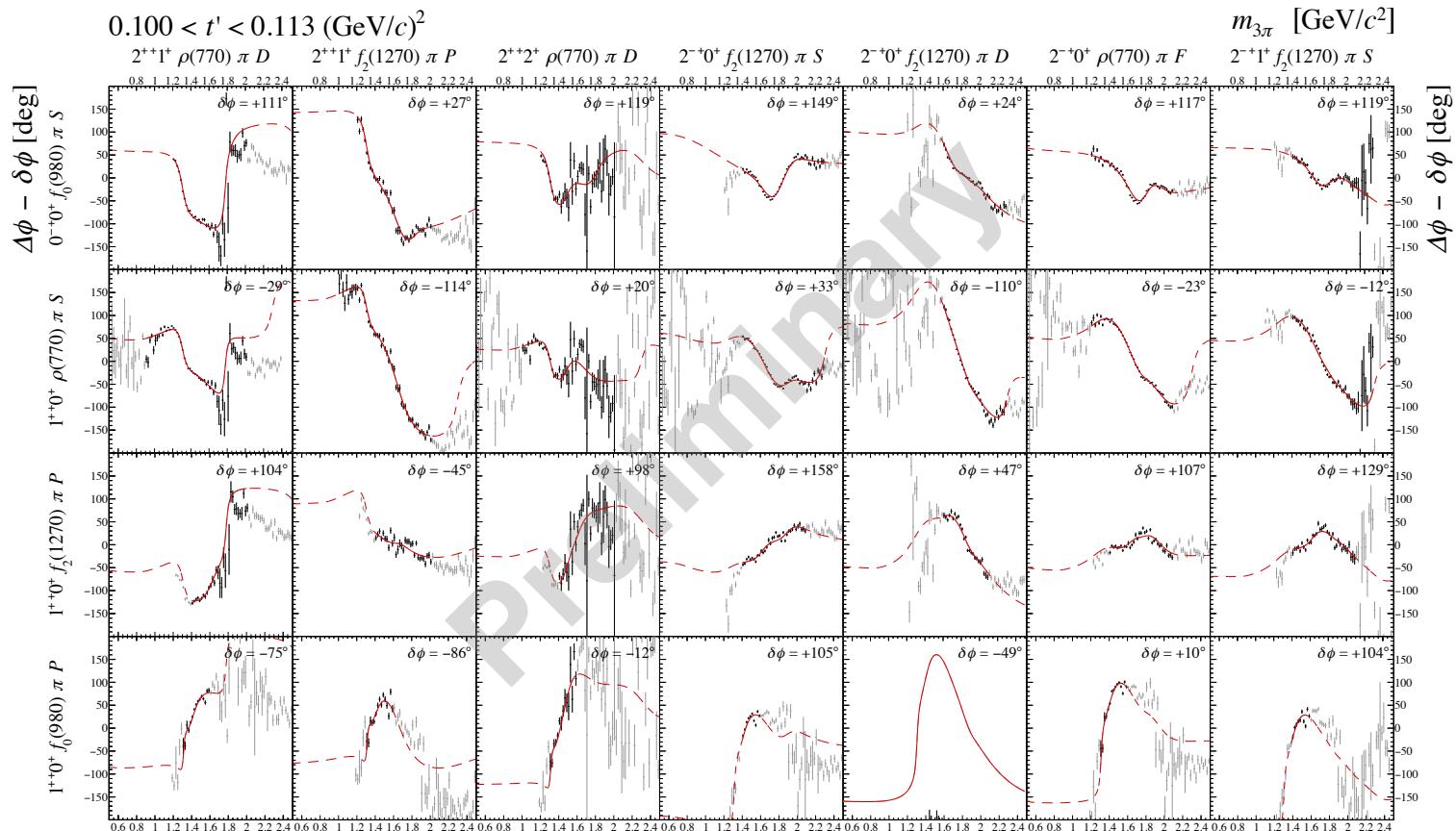
- Axialvector mesons:  $1^{++}$



# Phases are important ingredient



- Phases axialvector mesons:  $1^{++}$

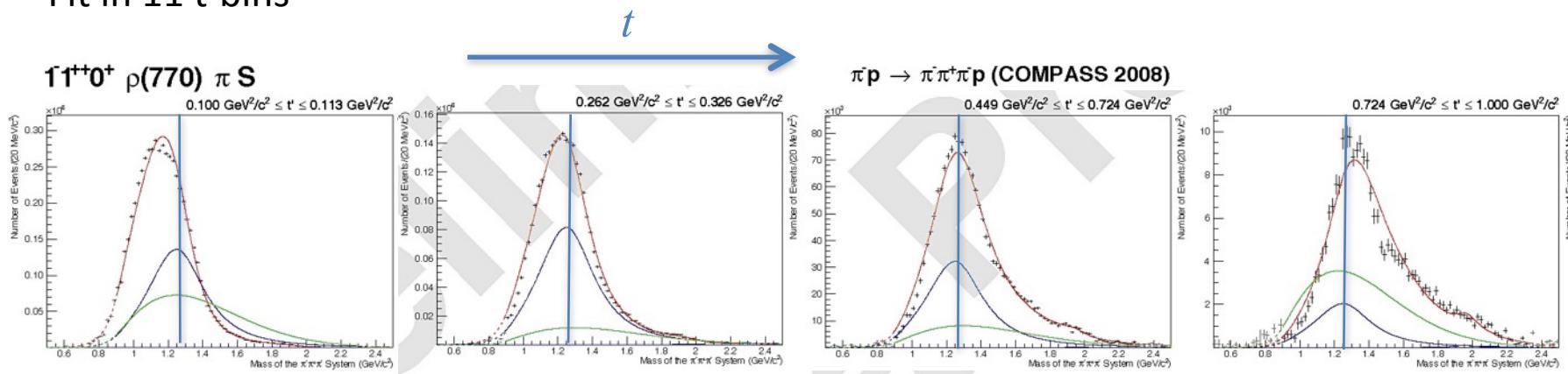


# Mass dependent fits

$$1^{++} 0^+ \rho \pi S$$

$$J^{PC} M^\varepsilon [isobar] \pi L$$

Fit in 11 t-bins

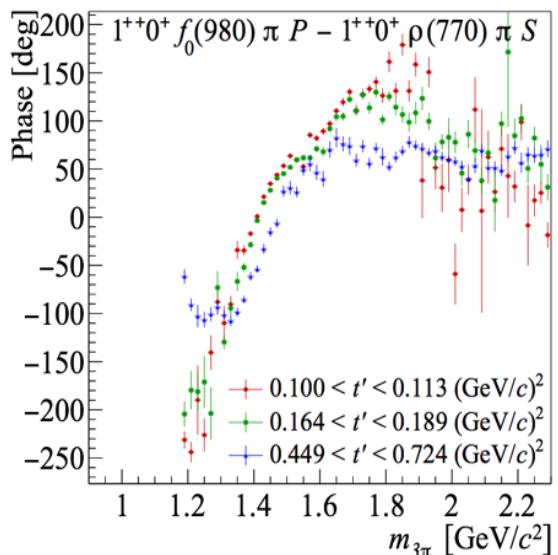
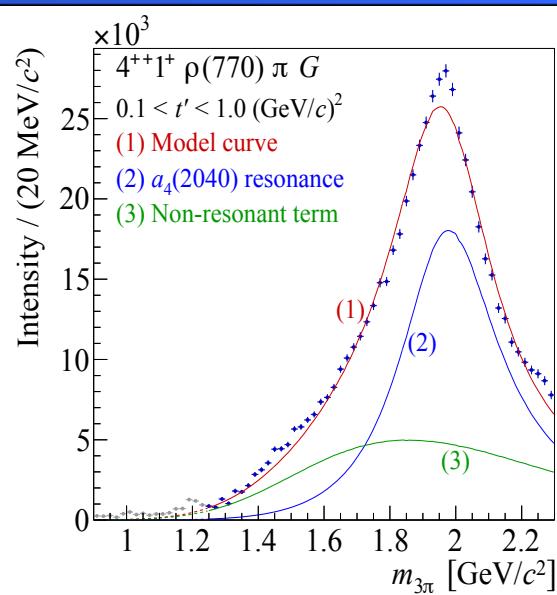
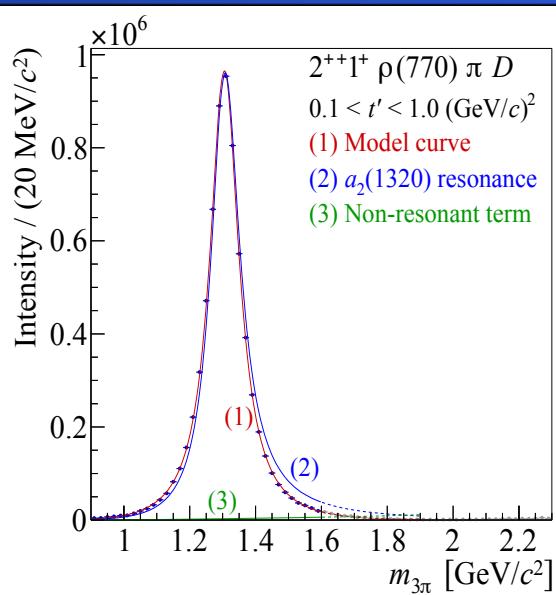
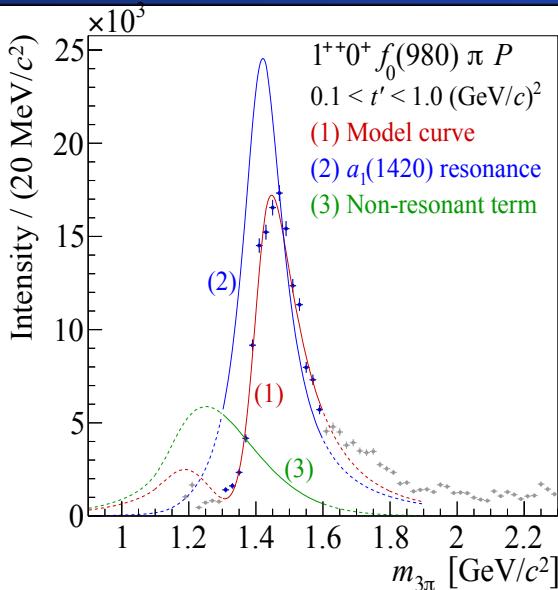


Strongly t-dependent  
spectral shape around  $a_1(1260)$

—  
Interference of non-resonant  
with  $a_1(1260)$

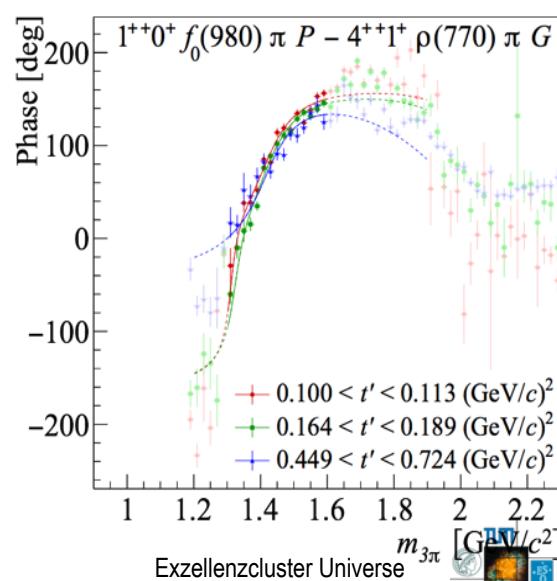


# New Observation: $a_1(1420)$



Observation:

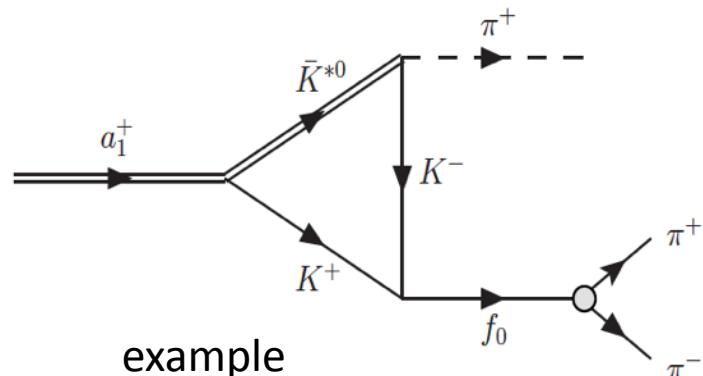
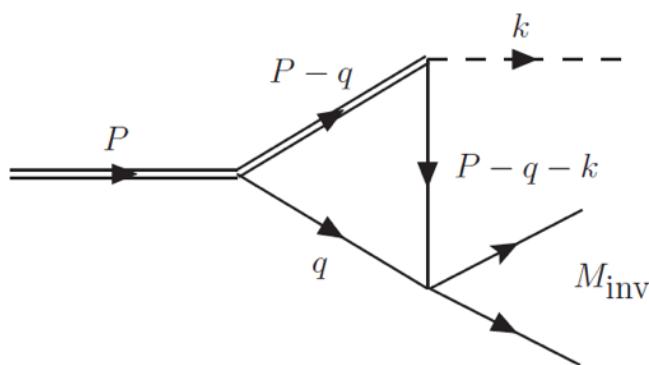
- Decay only :  $[f_0(980)] \pi P$
- Mass :  $1413 \pm 15 \pm 13 \text{ MeV}/c^2$
- Width:  $157 \pm 8 \pm 23 \text{ MeV}/c^2$



Various explanations proposed for interpretation:

- Dynamics

- Interference of  $a_1(1260)$  with Deck amplitude ( $\Delta\phi = 180^\circ$  shifted by 100 MeV) (Berger et al.)
- triangular anomaly coupling  $a_1(1260) \rightarrow KK^* \rightarrow KK\pi$  and  $KK \leftrightarrow f_0(980)$  ( $\Delta\phi = 90^\circ$ ) (Mikhasenko et al.)
- triangular anomaly :  $a_1(1260) \rightarrow f_0(980)\pi$  decay shows up 200 MeV above  $M(a_1(1260))$  (Aceti et al.)
- Requires same t dependence for  $a_1(1260)$  and  $a_1(1420)$



# Kinematics: Dependence on $t$

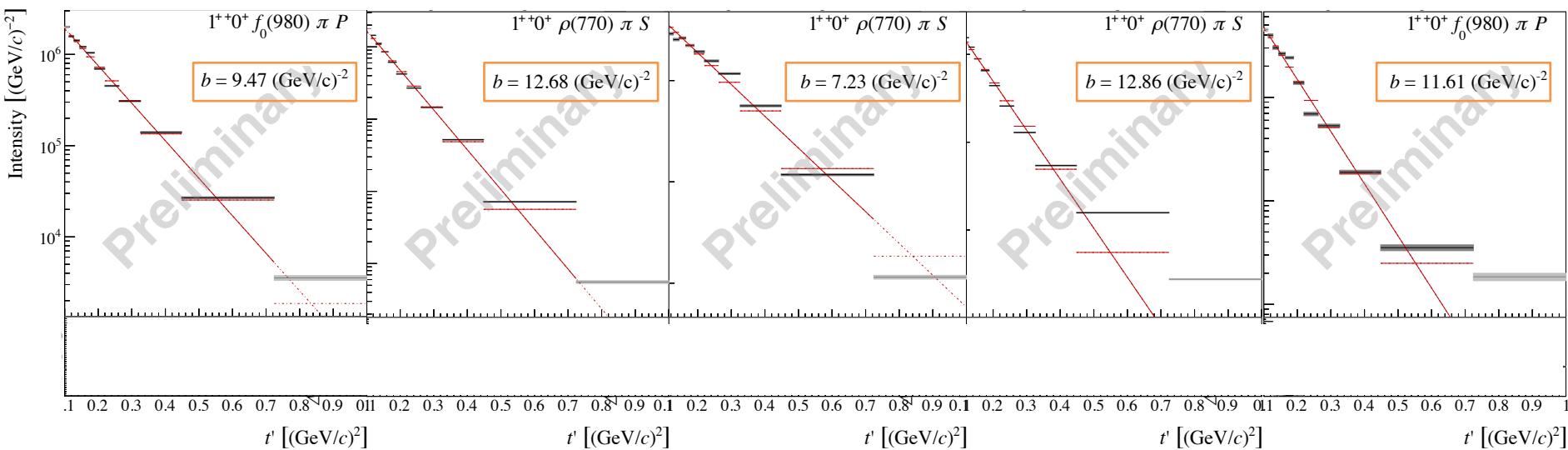


$a_1$  (1420)

$a_1$  (1260)

$a_1$  (1640)

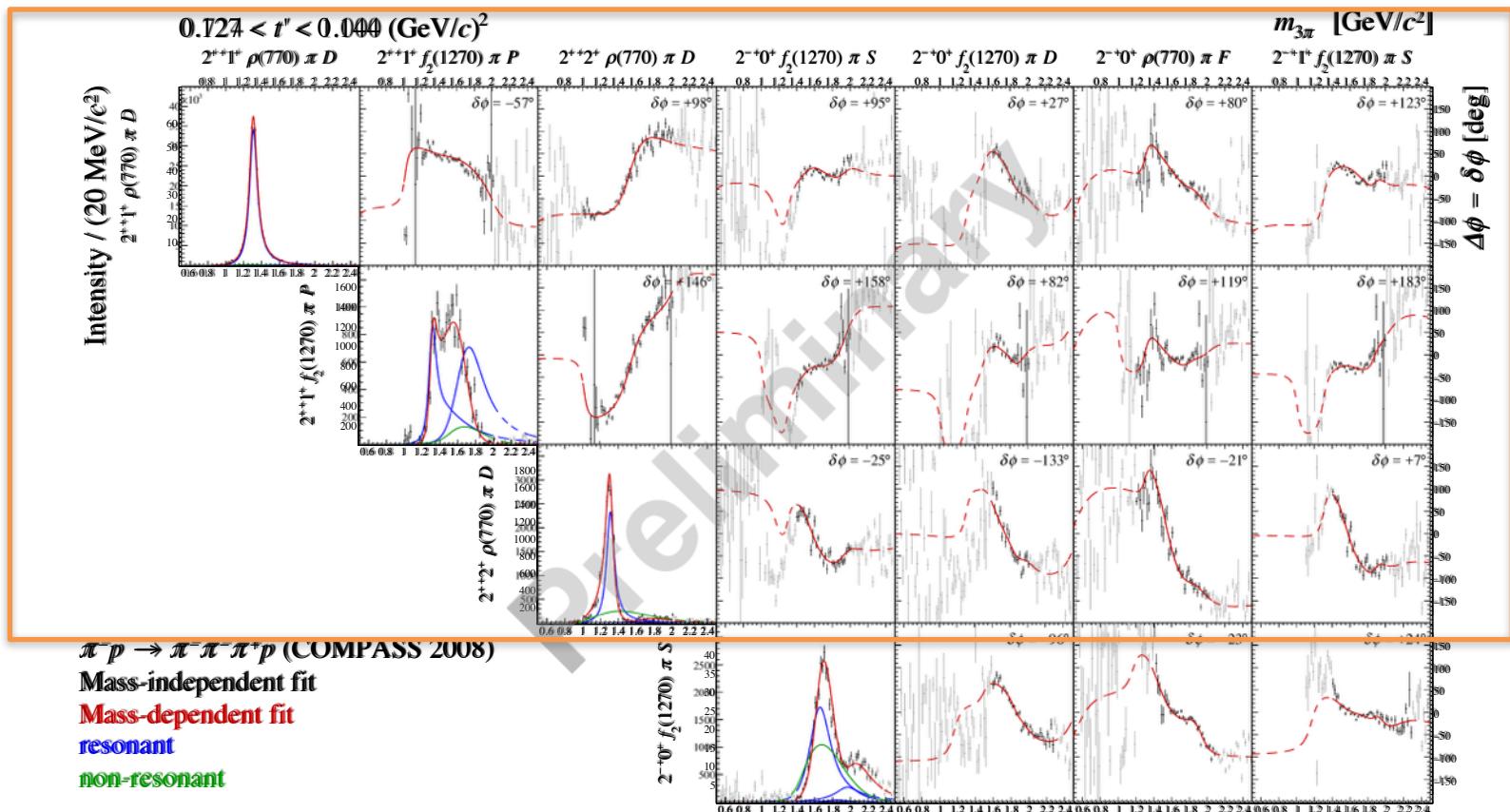
non-resonant



- $a_1$  (1260) has **larger slope** for  $t$  distribution than  $a_1$  (1420)
- $a_1$  (1260) slope **consistent to non-resonant** contributions
- ....but : **separation**  $a_1$  (1260) and non-resonant contribution difficult

# Find the Resonances

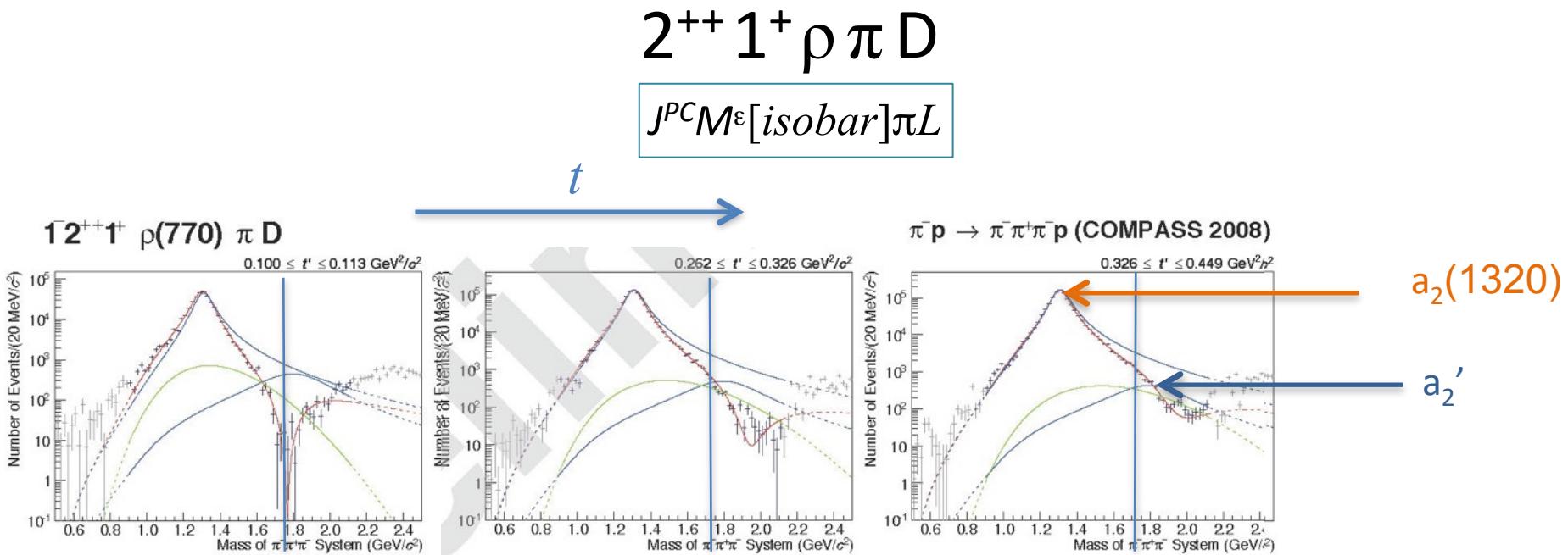
- Axialvector mesons:  $2^{++}$



low  $t$

high  $t$

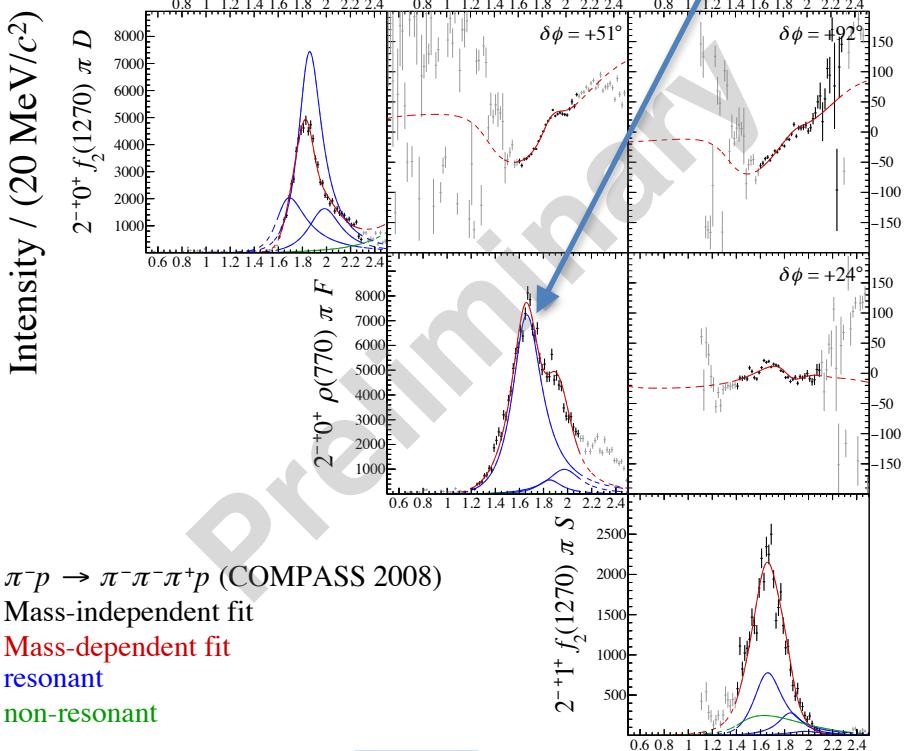
# Mass dependent fits $a_2(1320)$



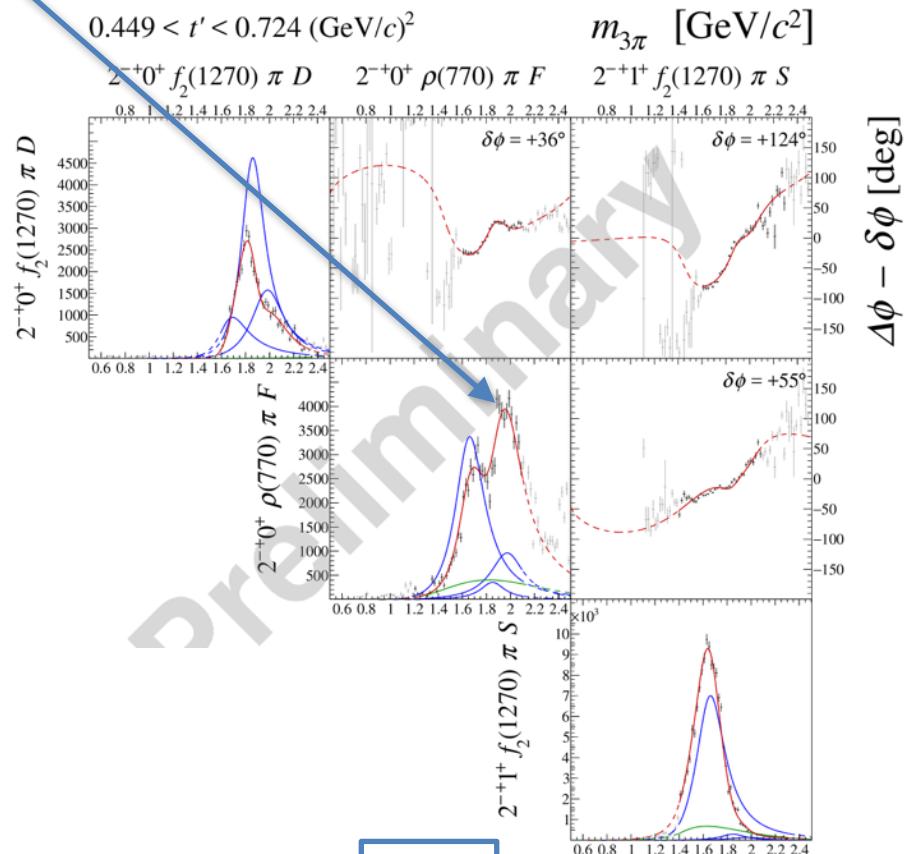
Strongly  $t$ -dependent  
interference effects  
 $high\text{-mass } a_2'$

# Find the Resonances

- Pseudoscalar mesons:  $2^{-+}$



low  $t$

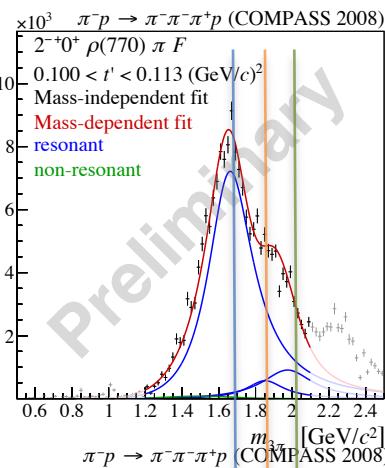


high  $t$

# The Case of $\pi_2$

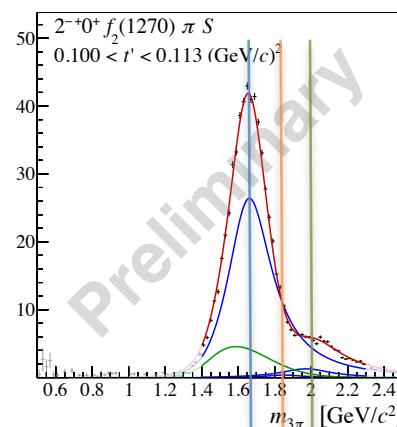
$\pi_2(1670)$

$m = 0$



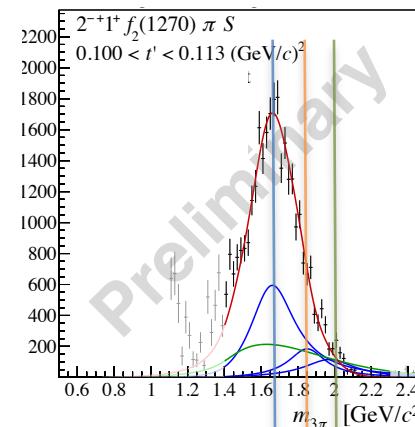
$\pi_2(1880)$

$m = 0$

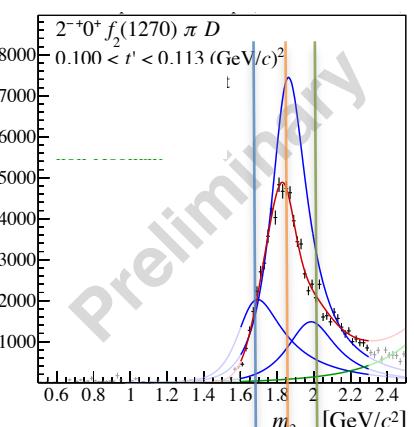


$\pi_2(2005)$

$m = 1$



$m = 0$



low  $t$

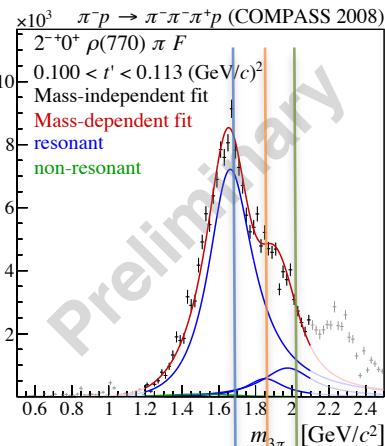
high  $t$

- very different production/decay characteristics

# The Case of $\pi_2$

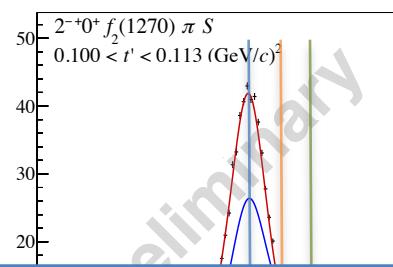
$\pi_2(1670)$

$m = 0$



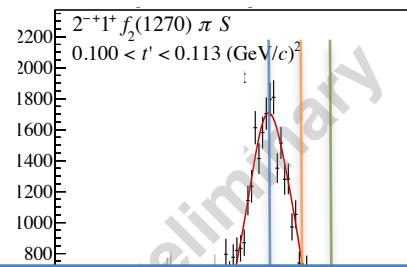
$\pi_2(1880)$

$m = 0$



$\pi_2(2005)$

$m = 0$

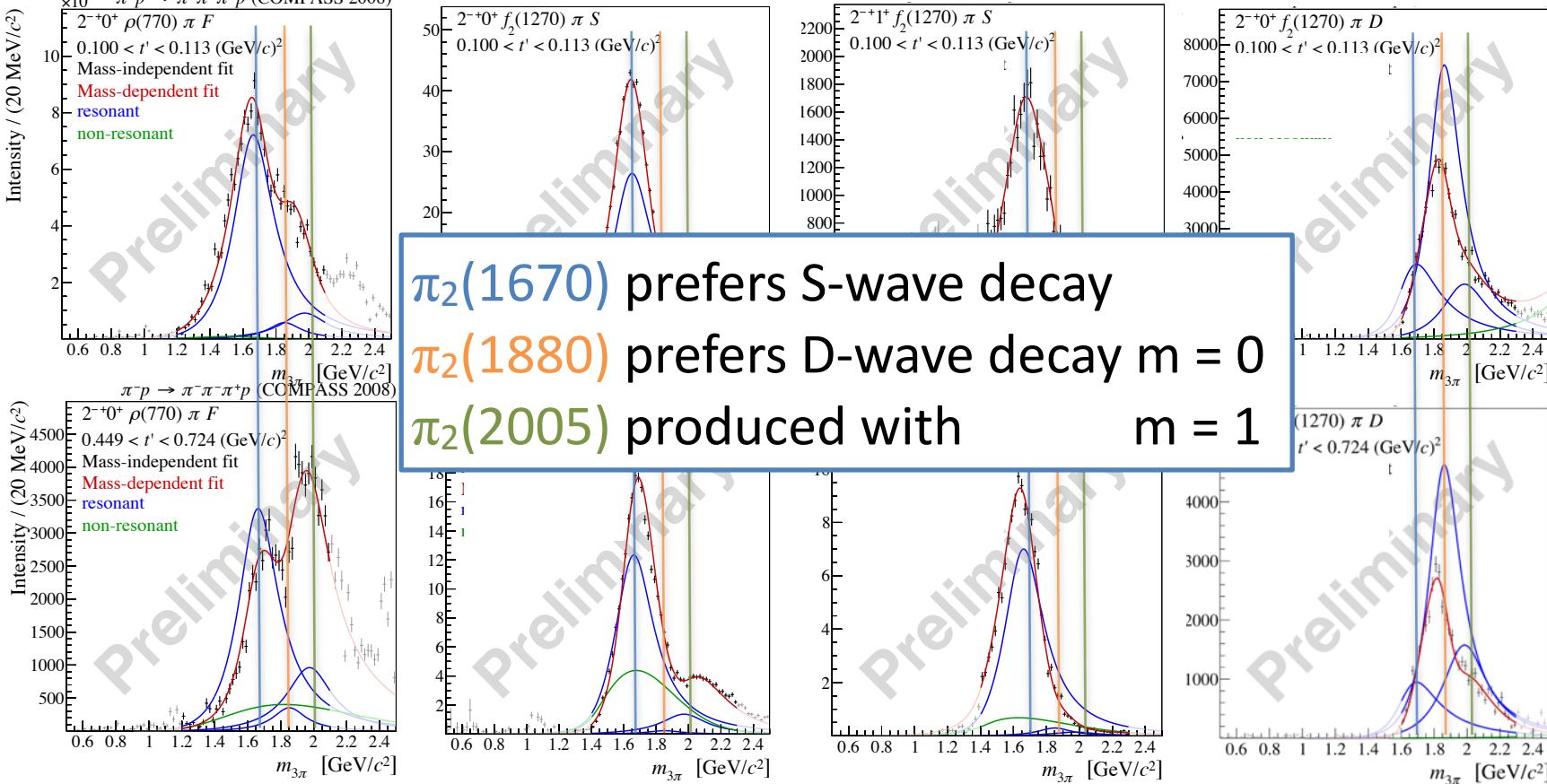


$\pi_2(1670)$  prefers S-wave decay

$\pi_2(1880)$  prefers D-wave decay  $m = 0$

$\pi_2(2005)$  produced with  $m = 1$

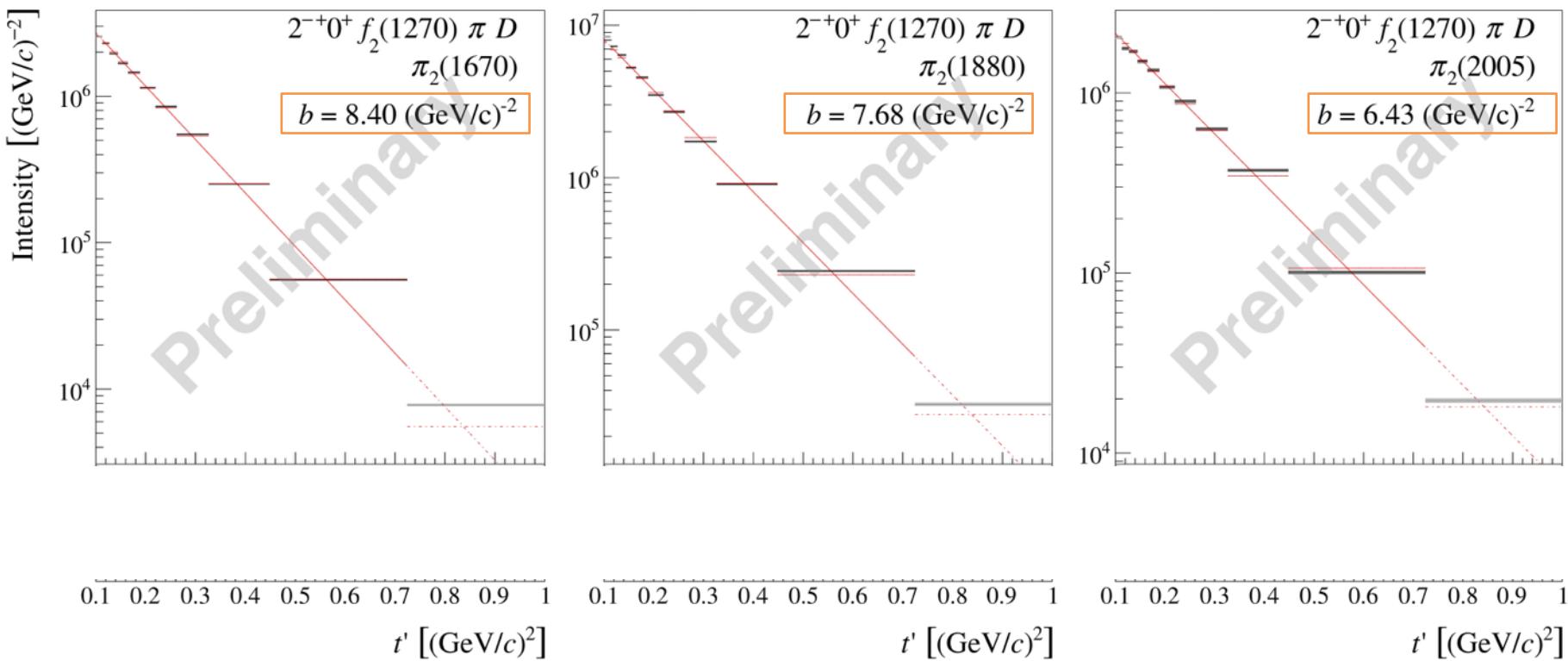
low  $t'$



high  $t'$

- very different production/decay characteristics

# Kinematics: Dependence on t



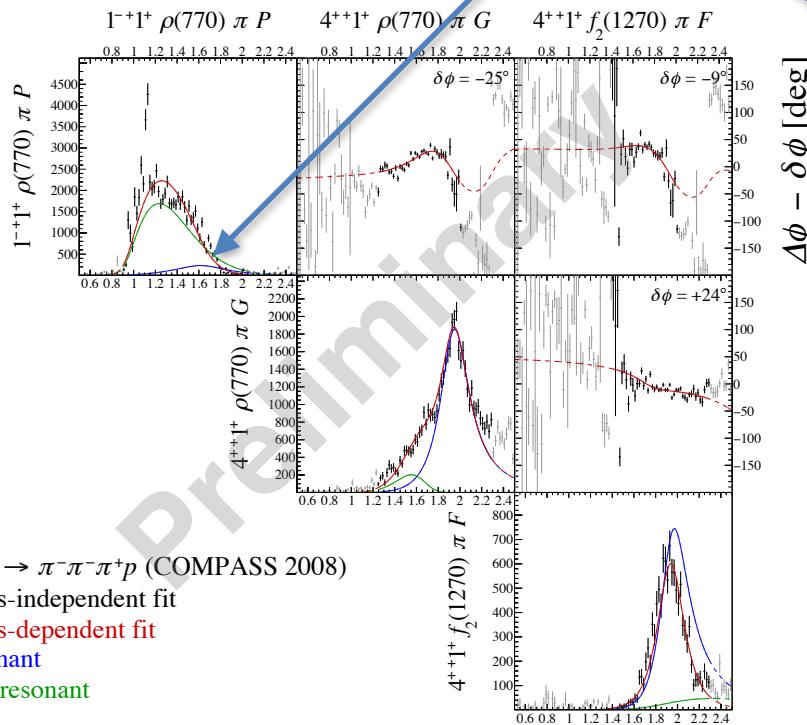
Background:  $b = (13.5 \text{ GeV/c})^{-2}$

# Find the Resonances

- Exotic mesons:  $1^+$

Intensity / (20 MeV/c<sup>2</sup>)

$$0.100 < t' < 0.113 (\text{GeV}/c)^2$$



$\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$  (COMPASS 2008)

Mass-independent fit

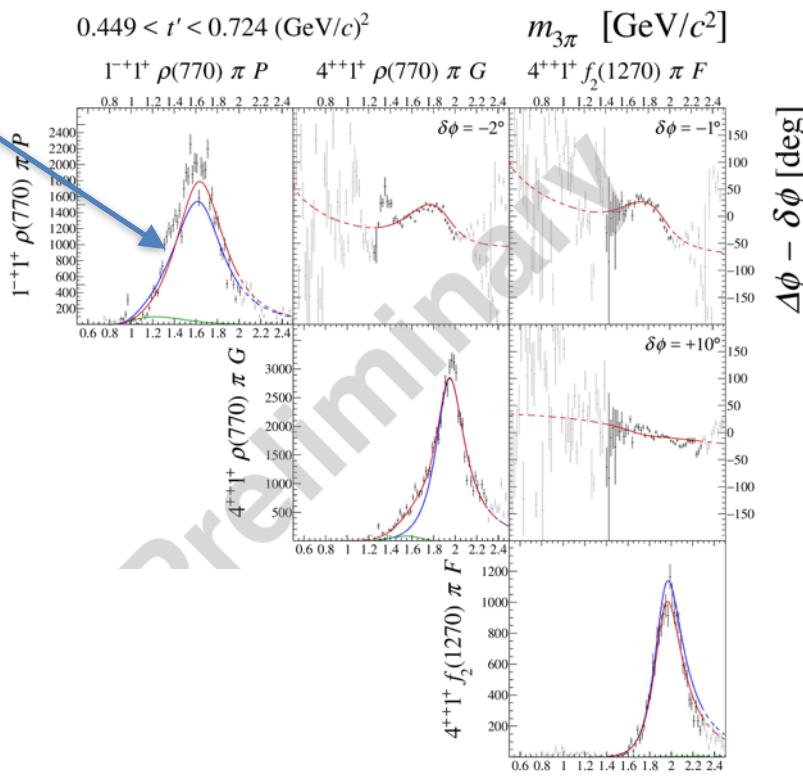
Mass-dependent fit

resonant

non-resonant

low  $t'$

$$0.449 < t' < 0.724 (\text{GeV}/c)^2$$



high  $t'$

# Find the Resonances

- Exotic mesons:  $1^+$

Intensity / (20 MeV/c<sup>2</sup>)

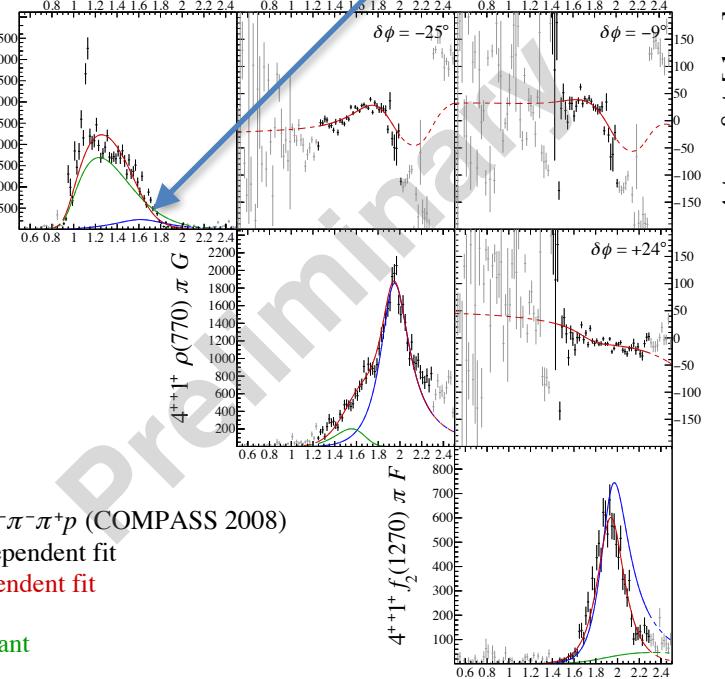
$$0.100 < t' < 0.113 \text{ (GeV/c)}^2$$

$1^{-+1^+} \rho(770) \pi P$

$4^{++1^+} \rho(770) \pi G$

$$m_{3\pi} \text{ [GeV/c}^2]$$

$4^{++1^+} f_2(1270) \pi F$



$\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$  (COMPASS 2008)

Mass-independent fit

Mass-dependent fit

resonant

non-resonant

low  $t'$

$$0.724 < t' < 1.000 \text{ (GeV/c)}^2$$

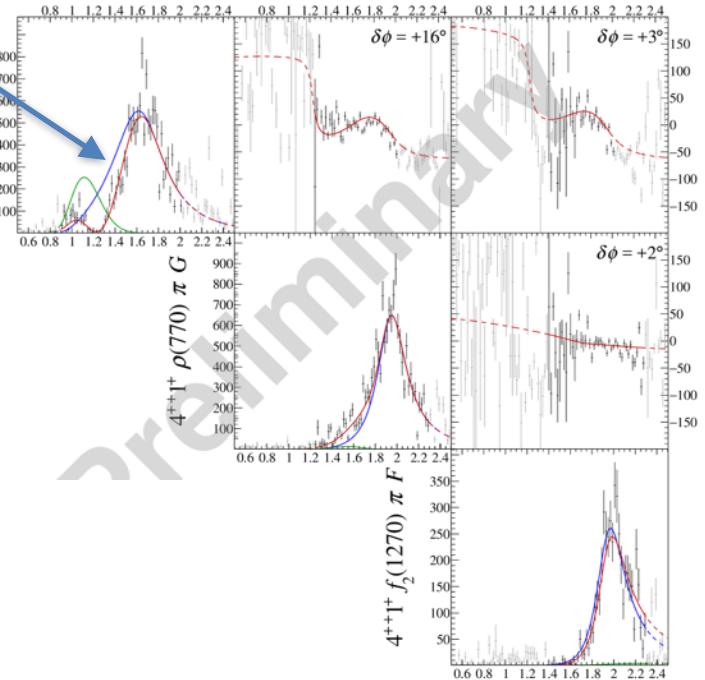
$1^{-+1^+} \rho(770) \pi P$

$4^{++1^+} \rho(770) \pi G$

$$m_{3\pi} \text{ [GeV/c}^2]$$

$4^{++1^+} f_2(1270) \pi F$

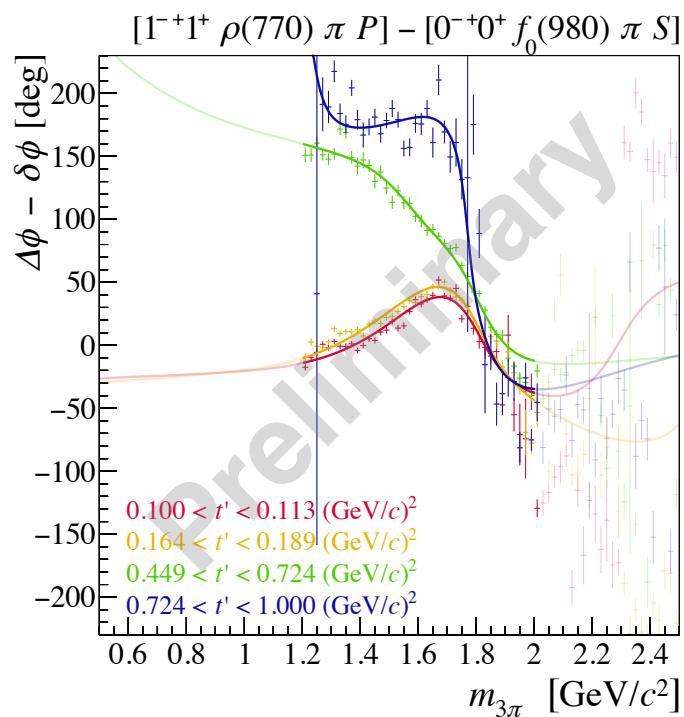
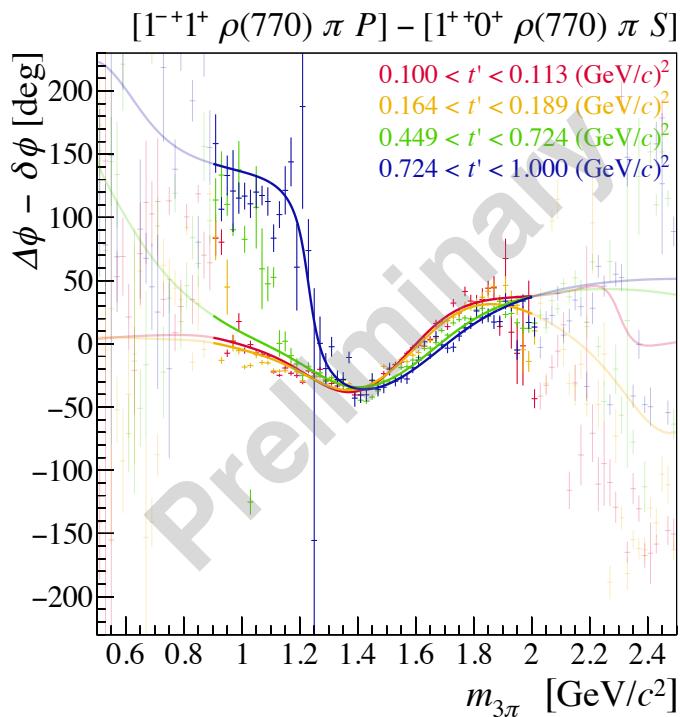
$$\Delta\phi - \delta\phi \text{ [deg]}$$



high  $t'$

# Find the Resonances - Phases

- Exotic mesons:  $1^{+}$



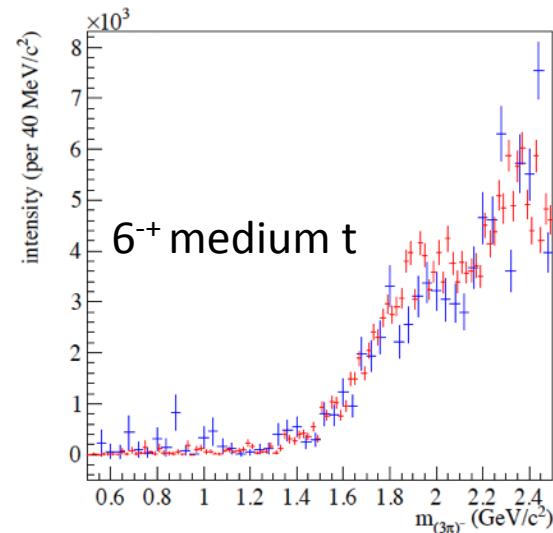
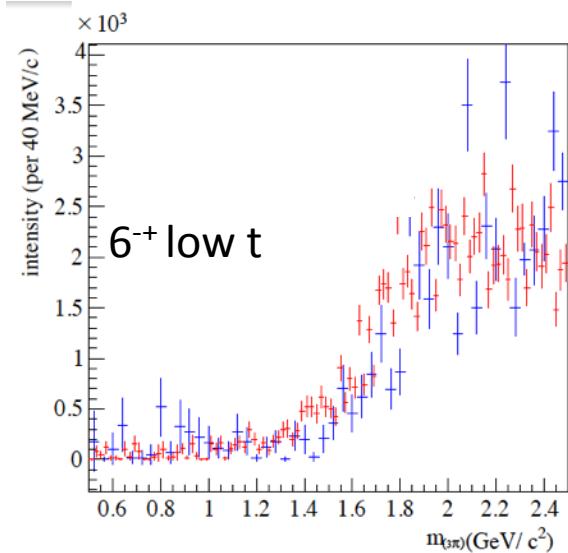


# 6<sup>+</sup>Deck Simulations - Data

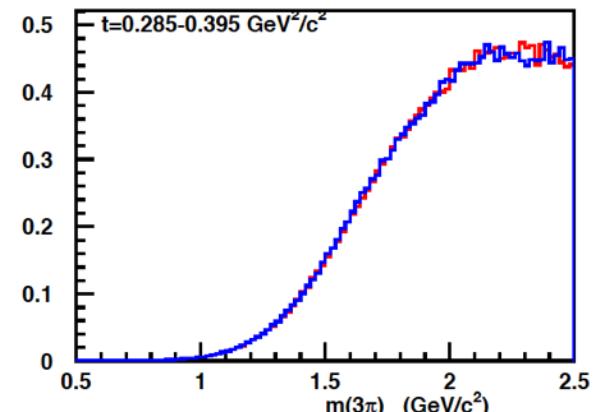
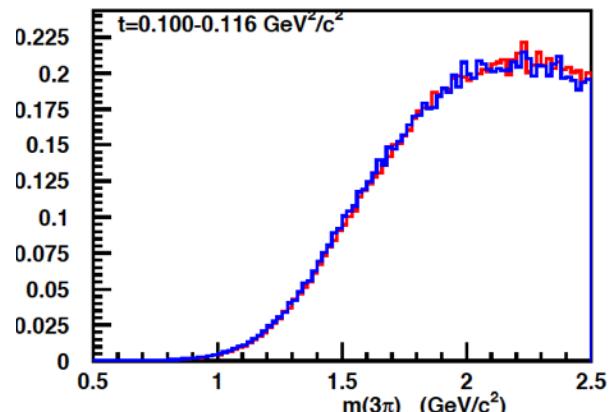


- wave w/o resonance
- compare final states

Data



Deck MC

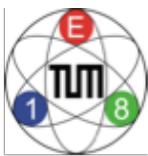




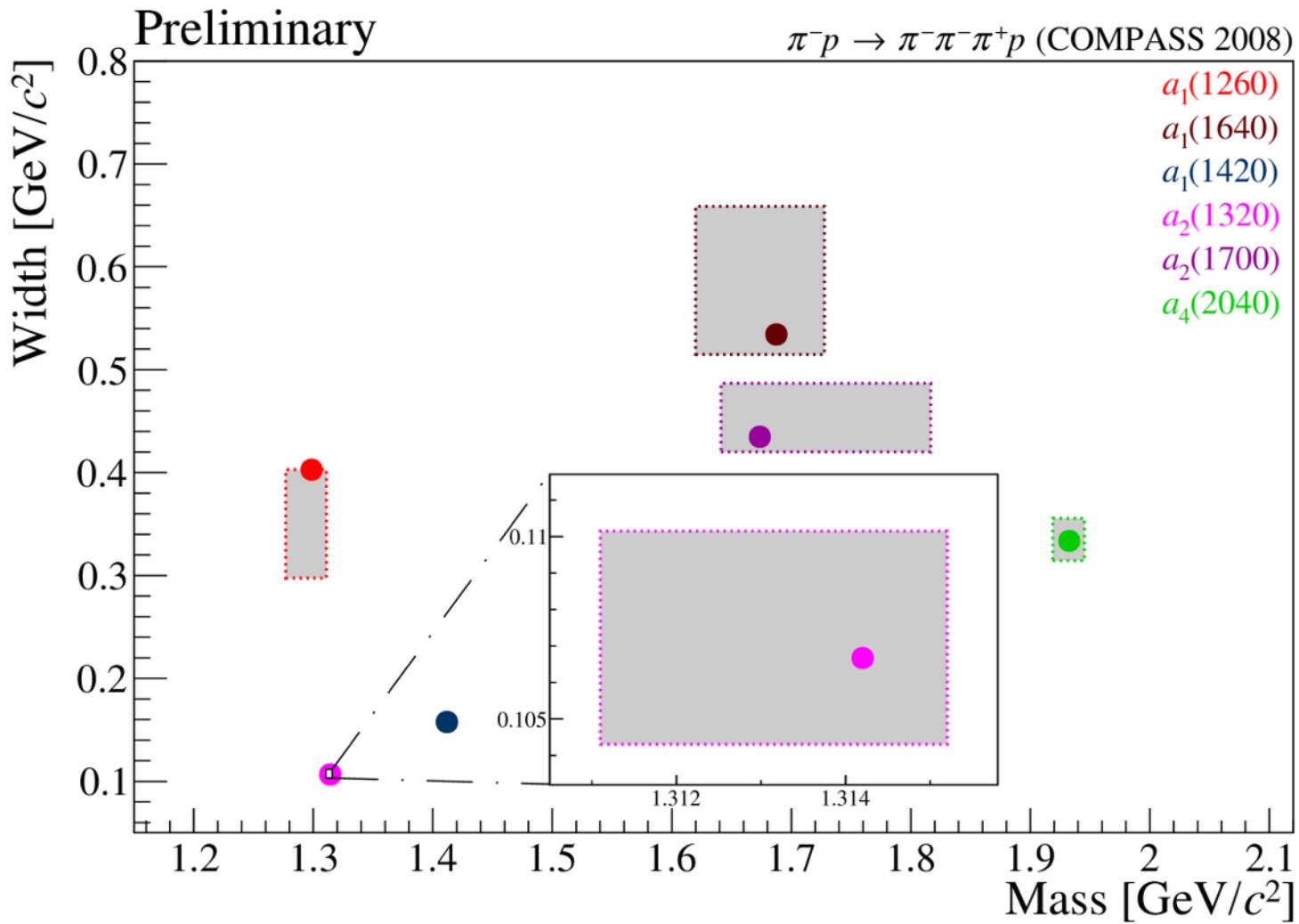
# Systematic Studies



- Largest set of systematic studies done ever
  - Omitting waves
  - Modification of resonance models
  - Variation of NR parametrization (analytical function vs. Deck MC)
  - Modified  $\chi^2$  use of correlation in spin-density matrix
  - alternating fit order of 700 parameters
- Biggest influence on
  - $a_1(1260)$ ,  $a_2(1700)$ ,  $\pi_1(1600)$
  - strong correlation  $a_1(1260) - \pi_1(1600)$  resonance parameters found

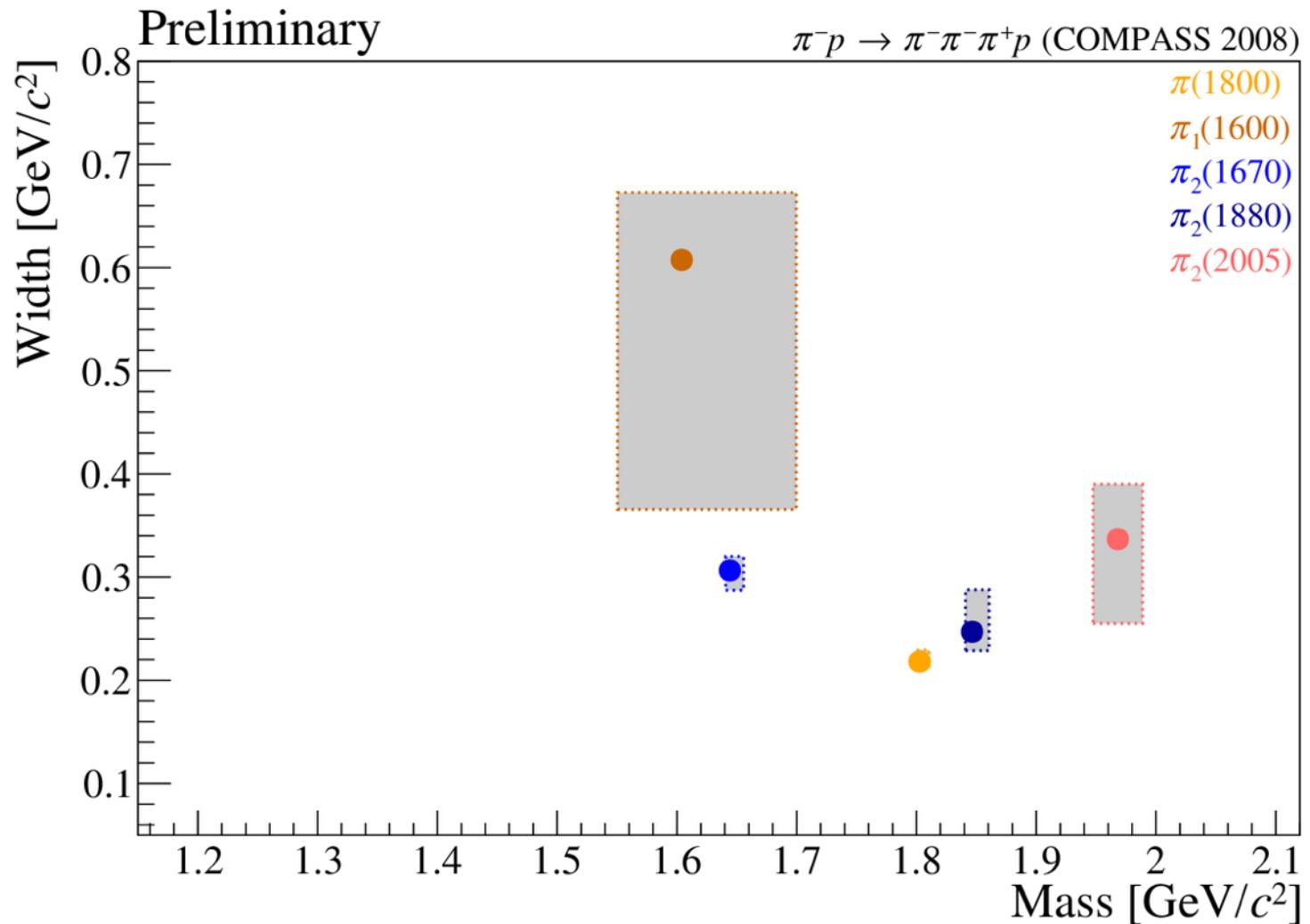


# Axialvector Mesons

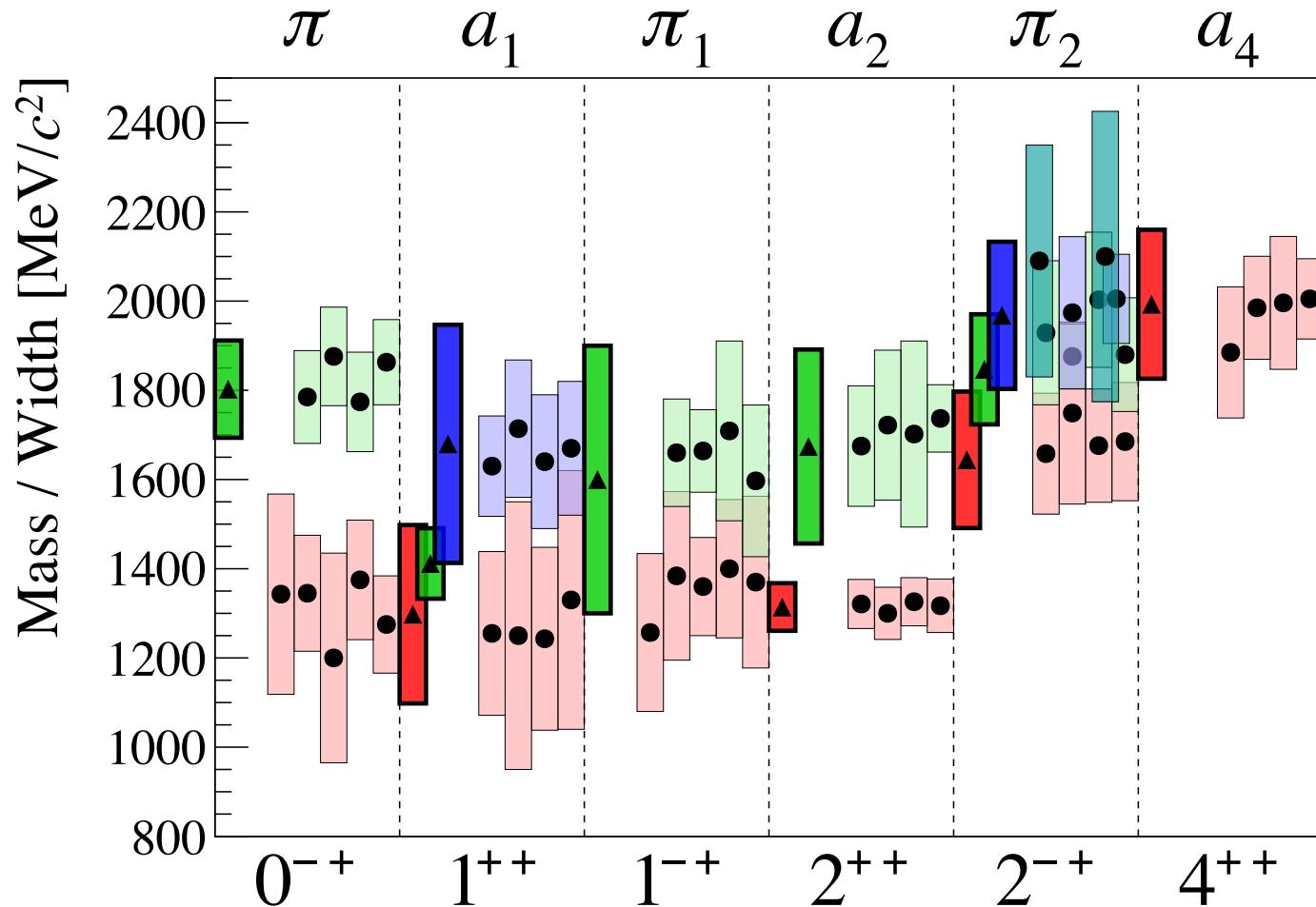




# Pseudoscalar Mesons

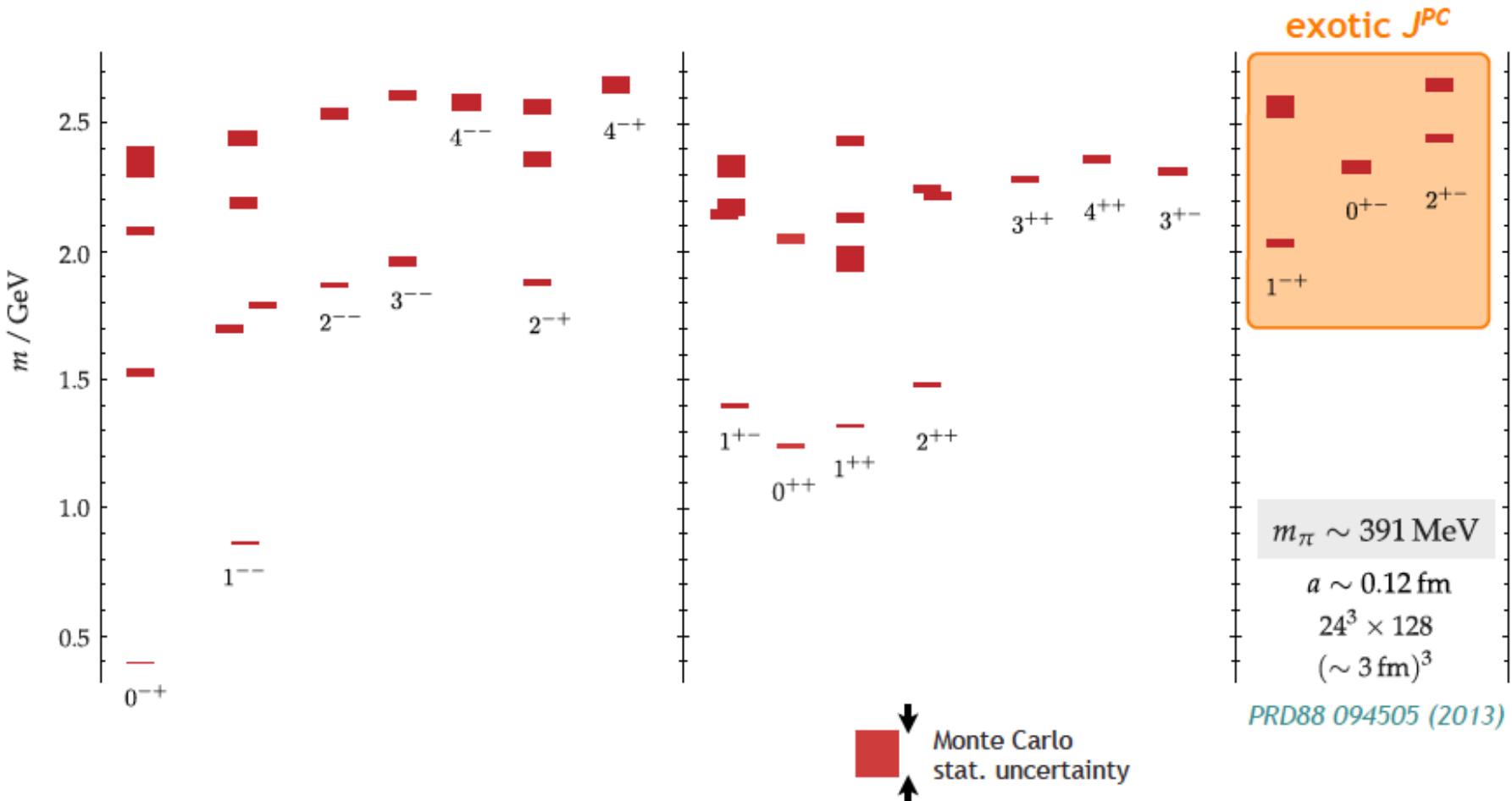


# Summary - Resonances



- COMPASS provides consistent analysis and realistic uncertainties

# Mesons on the Lattice

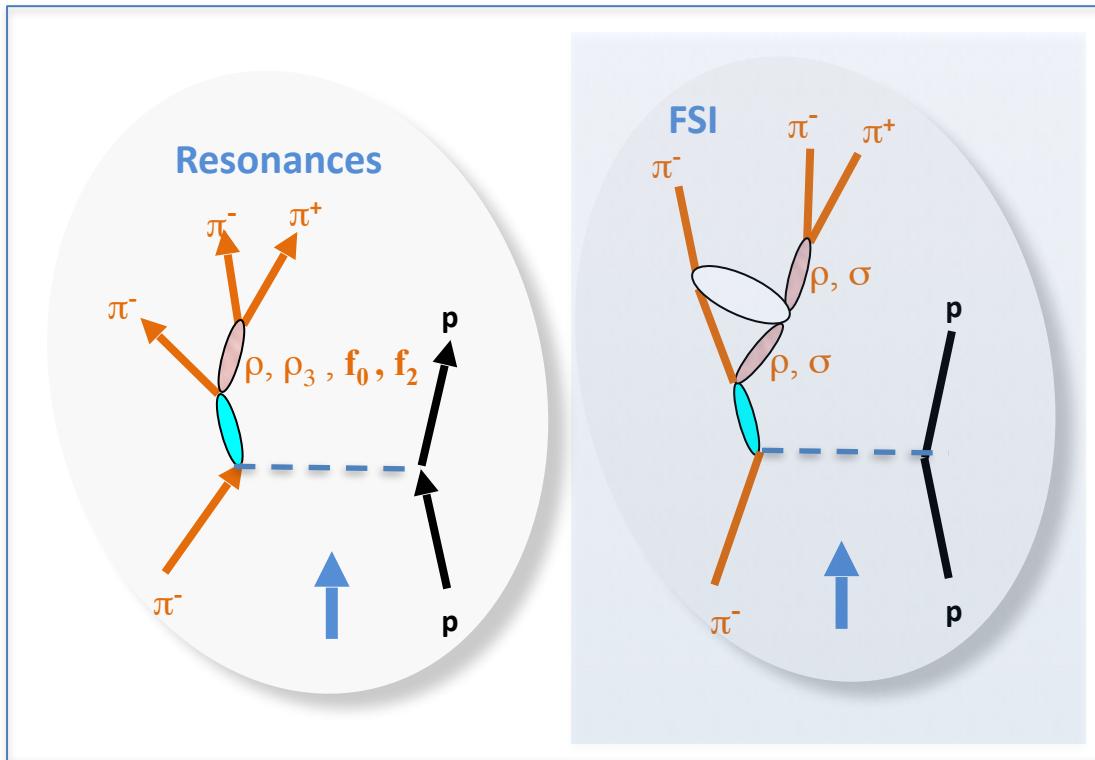


# What about the building blocks

- We have solved a puzzle – but were the building blocks correct ?



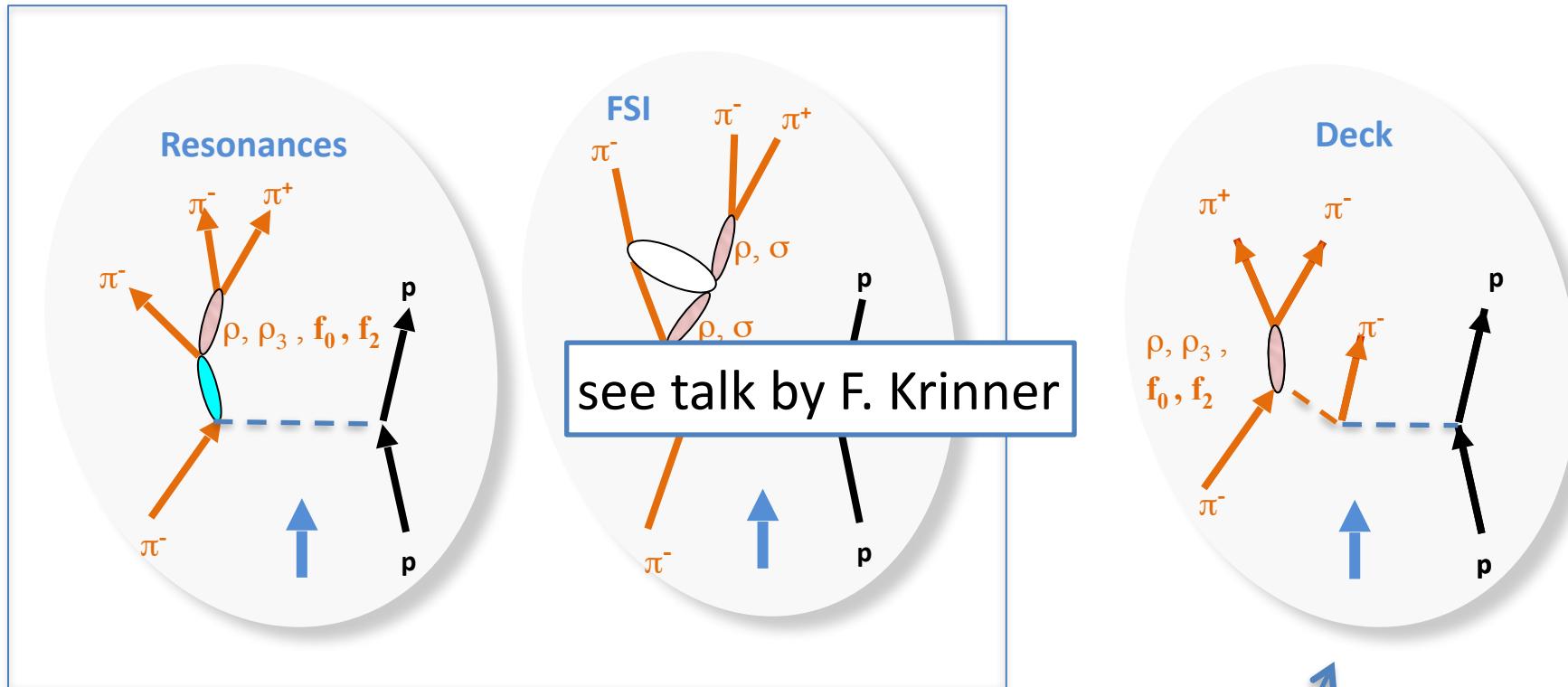
# New Paths to Meson Decays



- Select  $J^{PC}$  via PWA
- For each  $J^{PC}$  and mass-bin in  $3\pi$  :
  - determine composition and shapes of  $2\pi$  isobars
  - complex couplings
  - non-resonant contributions (via  $t$ -dependence)



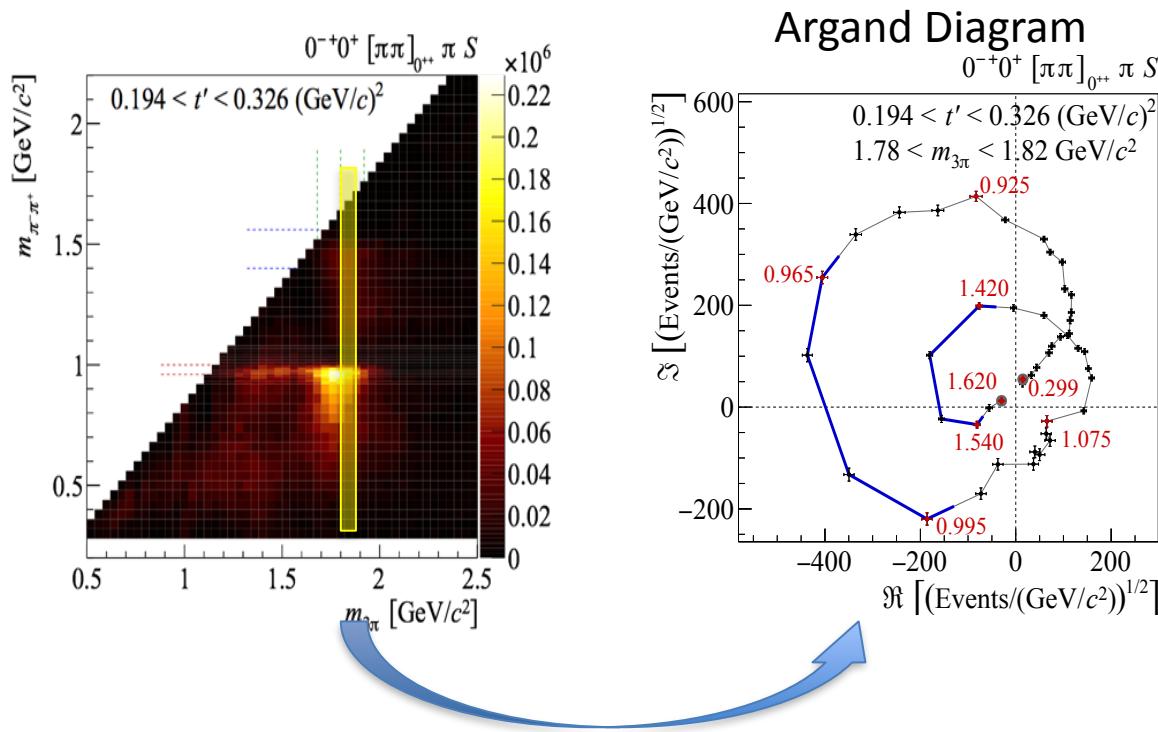
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## Study decay of $\pi(1800)$ into $3\pi$

Here:  $2\pi$  S-wave intermediate state

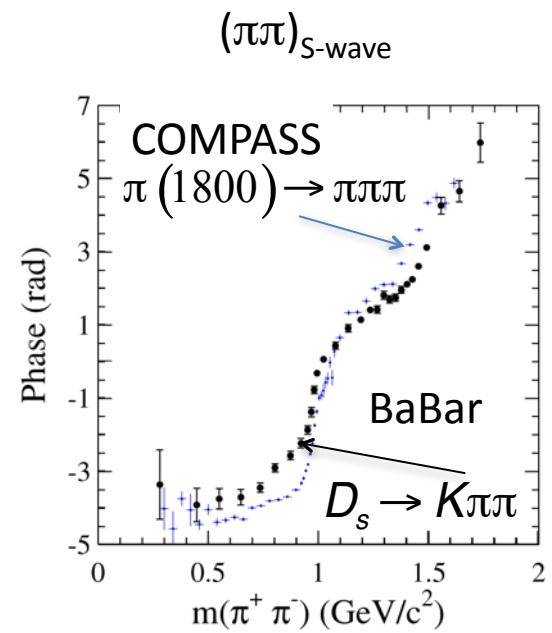
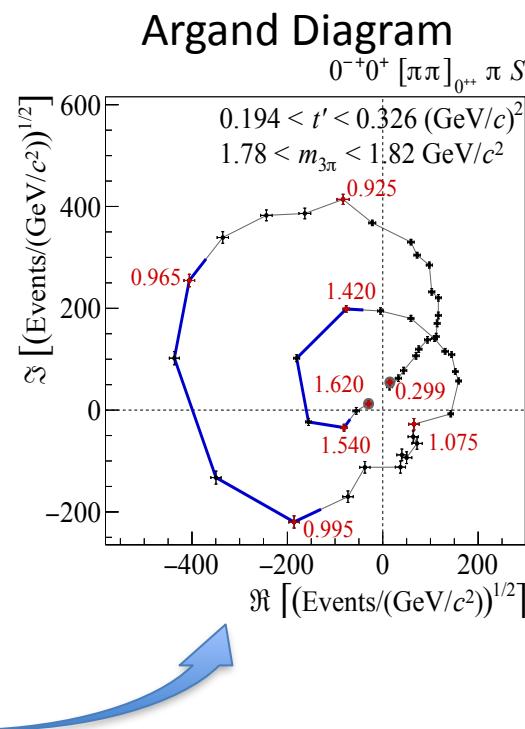
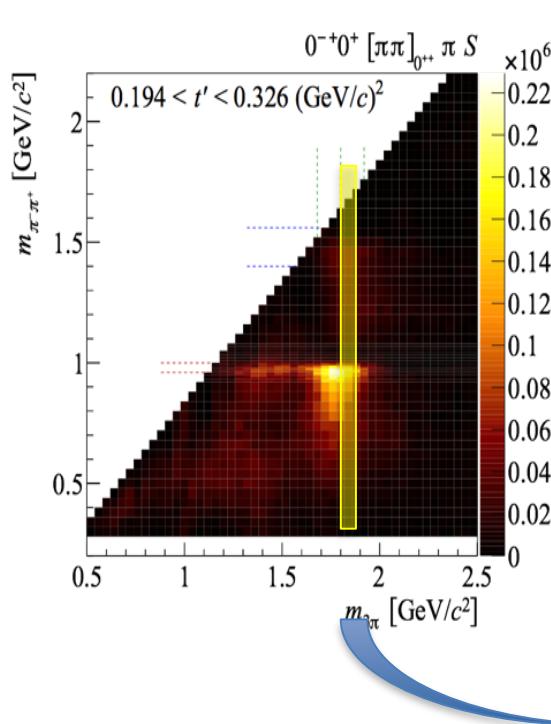


Perform **de-isobaring** of analysis extract  $2\pi$  from data  
 „model independent“ (HQ decay language)

# Studying the Structure of Decays

Study decay of  $\pi(1800)$  into  $3\pi$

Here:  $2\pi$  S-wave intermediate state



$(\pi\pi)_{S\text{-wave}}$  Similar for weak and strong decays !!  
Subtle differences will tell us more

# Ongoing Projects

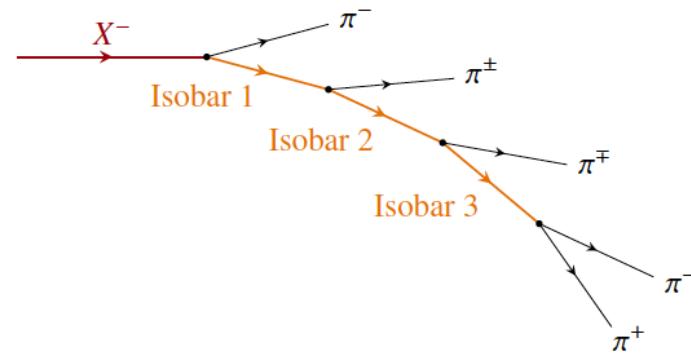
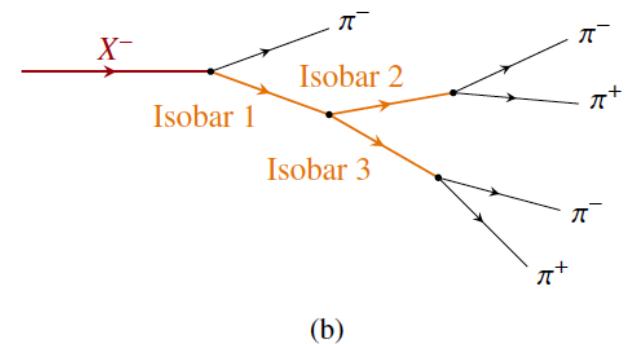
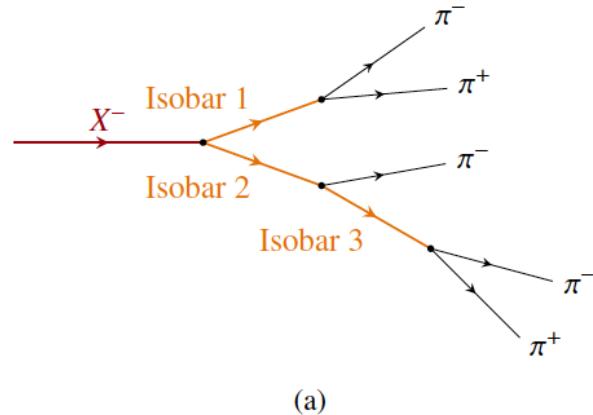
Ongoing **theory support** allows to address challenging tasks

- Fit to  $\pi\pi$  S-wave using known scattering amplitudes
  - Known up to  $1.2 \text{ GeV}/c^2$
  - Combine with knowledge about higher mass scalars
- Include more  $3\pi$   $J^{PC}$  in freed- isobar analysis
- Includes more  $2\pi$   $J^{PC}$  in freed- isobar analysis
- Fit to spin-density matrix without BW
  - Use K-matrix parametrisation with analytical function and poles
  - Extract **pole parameters**
- Joint fit of  $\pi^-\pi^+\pi^-$  and  $\pi^-\pi^0\pi^0$  data

# 5 $\pi$ Final State

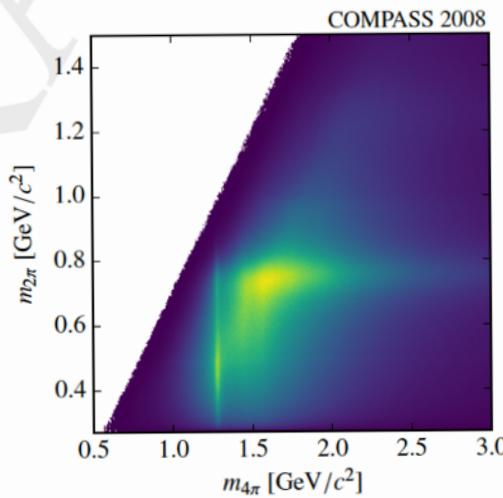
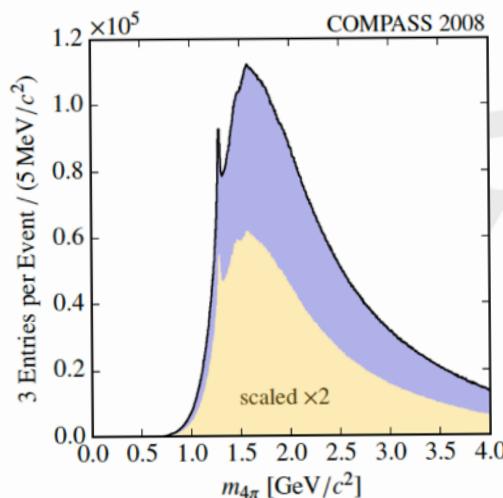
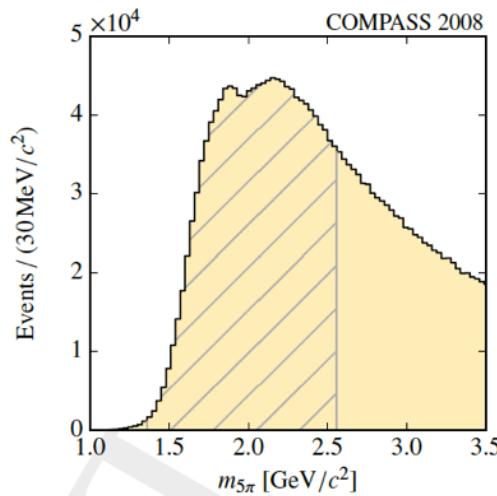
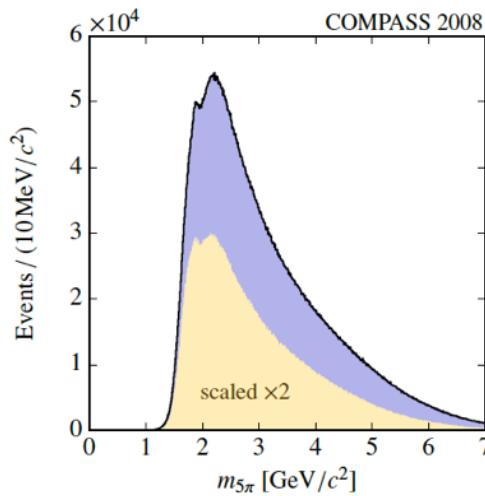


- Isobar model for 5 $\pi$
- about 1500 possible amplitudes ( $L < 3$ )

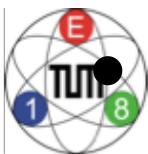


# 5 $\pi$ Final State

- Access high mass resonances - investigate heavy isobars



- select low  $t$  ( $0.1 < t < 0.15$ )  
little non-exclusive bkgd.
- consider only small values  $L < 3$



# 5π Final State



## Status

- Develop method to select most significant amplitudes
- Problems
  - Selection must be smooth across all mass bins
  - High sensitivity to isobar parametrization
  - Phase information much reduced
  - Many similarities to  $\eta\pi\pi\pi$

# Conclusion

Using new “2D” fit method to perform PWA in  $m_{3\pi}$  and  $t$ :

- Find new iso-vector state  $a_1(1420)$ 
  - $M_{a_1(1420)} = 1412\text{-}1422 \text{ MeV}/c^2$  ,  $\Gamma_{a_1(1420)} = 130\text{-}150 \text{ MeV}/c^2$
  - (exclusive) decay into  $f_0(980)\pi$  in relative P-wave
  - Nature of  $a_1(1420)$  ?
- Determine resonance parameters from largest ever fit to spin density matrix
  - Coherent determination of  $a_J$  and  $\pi_J$  states
  - Largely consistent parameters with previous experiments
  - Reveal systematic uncertainties
  - existences of  $\pi_1(1600)$  required



# Conclusion

- Developed **new method** to establish shape of isobar-spectrum
  - **first application:**  $[\pi\pi]_S^*$ :
    - Strongly depends on  $m_{3\pi}$  and on  $J^{PC}$  of mother wave
    - Reveals information on **scalar isobars** (measure phases in decays)
    - Extend to full isobar-free analysis (ongoing)
      - Iterative (bootstrapping) approach does not work !
      - Artifacts !! can be removed by proper treatment (work in progress)
      - Applications to heavy meson decays
  - Kaon beam data analysis started

Open Path to Dalitz-plot analysis using PWA  
from PWA identified states

Needs high statistics !!

Exzellenzcluster Universe