



Photoproduction of η and η' mesons on proton

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on behalf of the A2 Collaboration at MAMI

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Outline

- **η MAID-2003**
- **Review of experimental data**
- **Regge phenomenology for background**
- **η MAID-2016 for η and η' photoproduction**
- **Summary**

η MAID-2003

η MAID is an isobar model for η -photo and electroproduction on nucleons, for more details see: [W.-T. Chiang, S.N. Yang, L. Tiator, D. Drechsel, NP A700 \(2002\) 429.](#)

Model ingredients:

- Born terms (very small contribution),
- ρ - and ω -meson exchanges in the t-channel, which are described by ρ - and ω poles.
- nucleon resonances parameterized with Breit-Wigner shapes.

Model variable parameters:

- Born terms: coupling η to nucleon $g_{\eta NN}^2$;
- vector mesons: hadronic vector g_v and tensor g_t couplings, dipole form factor Λ_v ;
- resonances: mass M_R , total width Γ_R at the resonance peak , branching ratio $\beta_{\eta N}$;
photoexcitation helicity amplitudes $A_{1/2}, A_{3/2}$;
- total and partial widths have an energy dependence with an damping factor assumed to be the same for all resonances;
- relative sign between $N^* \rightarrow \eta N$ and $N^* \rightarrow \pi N$ couplings, $\zeta_{\eta N} = \pm 1$.

Data set:

- total and differential cross sections of MAMI and GRAAL;
- photon asymmetry of GRAAL ($E_\gamma < 1.1$ GeV);
- electroproduction cross sections of Jlab.

Reggeized model for η and η' photoproduction,

[W.-T. Chiang, S.N. Yang, L. Tiator, M. Vanderhaeghen, D. Drechsel, PRC 68 \(2003\) 045202.](#)

Main difference: vector meson exchanges are described in terms of Regge trajectories.

It should be important for high energies, $W > 2.5$ GeV.

Data sets



- $d\sigma/d\Omega$, A2MAMI: $E_\gamma=0.71-1.57$ GeV [Prakhov, preliminary]
- $d\sigma/d\Omega$, CBELSA/TAPS-09: $E_\gamma=0.87-2.55$ GeV [PRC 80 (2009) 055202]
- $d\sigma/d\Omega$, CLAS-09: $E_\gamma=1.46-3.7$ GeV [PRC 80 (2009) 045213]
- T, F A2MAMI-14: $E_\gamma=0.71-1.4$ GeV [PRL 113 (2013) 102001]
- Σ , GRAAL-07: $E_\gamma=0.71-1.5$ GeV [EPJA 33 (2007) 169]
- E, CLAS-15: $E_\gamma=0.71-2.15$ GeV [PLB 755 (2016) 64]

- $d\sigma/dt$, DESY-70 $E_\gamma=4, 6$ GeV [PLB 33 (1970) 236]
- $d\sigma/dt$, WLS-71 $E_\gamma=4, 8$ GeV [PLB 37 (1971) 326]
- $d\sigma/dt$, Σ , Daresbury-76 $E_\gamma=2.5, 3$ GeV [PLB 61 (1976) 479]
- $d\sigma/dt$, CEA-68 $E_\gamma=4$ GeV [PRL 21 (1968) 1205]
- T, Daresbury-80 $E_\gamma=4$ GeV [NP B185 (1981) 269]

Data sets



- $d\sigma/d\Omega$, A2MAMI: $E_\gamma=1.45-1.57$ GeV [Prakhov, preliminary]
- $d\sigma/d\Omega$, CBELSA/TAPS-09: $E_\gamma=1.53-2.48$ GeV [PRC 80 (2009) 055202]
- $d\sigma/d\Omega$, CLAS-09: $E_\gamma=1.51-3.43$ GeV [PRC 80 (2009) 045213]
- Σ , GRAAL-15: $E_\gamma=1.46-1.48$ GeV [EPJA 51 (2015) 77]

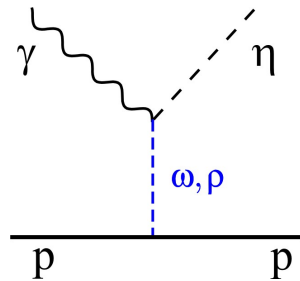


- $d\sigma/d\Omega$, A2MAMI-14: $E_\gamma=0.72-1.40$ GeV [RRC 90 (2014) 015205]
- $d\sigma/d\Omega$, CBELSA/TAPS-11: $E_\gamma=0.74-2.06$ GeV [EPJA 47 (2011) 89]
- Σ , GRAAL-08: $E_\gamma=0.74-1.44$ GeV [PRC 78 (2008) 015203]

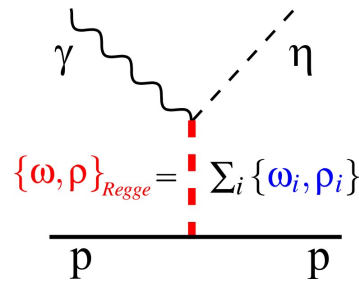


- $d\sigma/d\Omega$, CBELSA/TAPS-11: $E_\gamma=1.53-2.45$ GeV [EPJA 47 (2011) 11]

Regge phenomenology

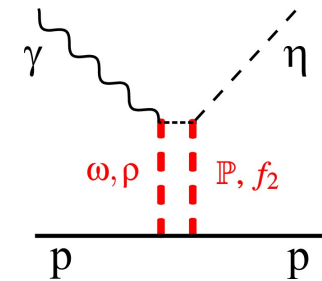


vector meson
single poles



vector meson
Regge trajectories

+



vector meson
Regge cuts

Regge phenomenology

The pole-like Feynman propagators are replaced by Regge propagators for each vector meson in the t-channel:

$\rho (1^-)$ exchange:

$$\frac{1}{t - m_\rho^2} \implies \mathcal{P}_{\text{Regge}}^\rho = \left(\frac{s}{s_0} \right)^{\alpha_\rho(t)-1} \frac{\pi\alpha'_\rho}{\sin(\pi\alpha_\rho(t))} \frac{\mathcal{S} + e^{-i\pi\alpha_\rho(t)}}{2} \frac{1}{\Gamma(\alpha_\rho(t))}, \quad (1)$$

$\omega (1^-)$ exchange:

$$\frac{1}{t - m_\omega^2} \implies \mathcal{P}_{\text{Regge}}^\omega = \left(\frac{s}{s_0} \right)^{\alpha_\omega(t)-1} \frac{\pi\alpha'_\omega}{\sin(\pi\alpha_\omega(t))} \frac{\mathcal{S} + e^{-i\pi\alpha_\omega(t)}}{2} \frac{1}{\Gamma(\alpha_\omega(t))}. \quad (2)$$

The parameter s_0 is a mass scale taken as $s_0 = 1 \text{ GeV}^2$.

\mathcal{S} is the signature of the trajectory. For bosons $\mathcal{S} = (-1)^J$, so for the vector mesons $\mathcal{S} = -1$.

The gamma function $\Gamma(\alpha(t))$ suppresses poles of the propagator in the unphysical region.

Regge cuts for π^0 photoproduction

G.R. Goldstein, J.F. Owens III, PRD 7 (1973) 865.

I.S. Barker, J.K. Storrow, NP B137 (1978) 413.

A. Donnachie, Yu.S. Kalashnikova, PRC 93 (2016) 025203.

Regge cuts arise from rescattering two Reggeons R_1 and R_2 (or more).

The exchange of two Reggeons with linear trajectories:

$$\alpha_i(t) = \alpha_i(0) + \alpha'_i t, i = 1, 2 \quad (3)$$

yields a cut with a linear trajectory $\alpha_c(t)$:

$$\alpha_c(t) = \alpha_c(0) + \alpha'_c t \quad (4)$$

were

$$\begin{aligned} \alpha_c(0) &= \alpha_1(0) + \alpha_2(0) - 1 \\ \alpha'_c &= \frac{\alpha'_1 \alpha'_2}{\alpha'_1 + \alpha'_2} \end{aligned} \quad (5)$$

Regge cuts for π^0 photoproduction

Donnachie and Kalashnikova assumed:

linear ρ and ω trajectories:

$$\alpha_\rho = 0.55 + 0.8t$$

$$\alpha_\omega = 0.44 + 0.9t$$

secondary linear Pomeron (P) and f_2 trajectories:

$$\alpha_P \sim 1.08 + 0.25t$$

$$\alpha_{f_2} = 0.672 + 0.817t$$

trajectory of the associated $\rho - P$ and $\omega - P$ cuts:

$$\alpha_{\rho-P}^c = 0.64 + 0.160t$$

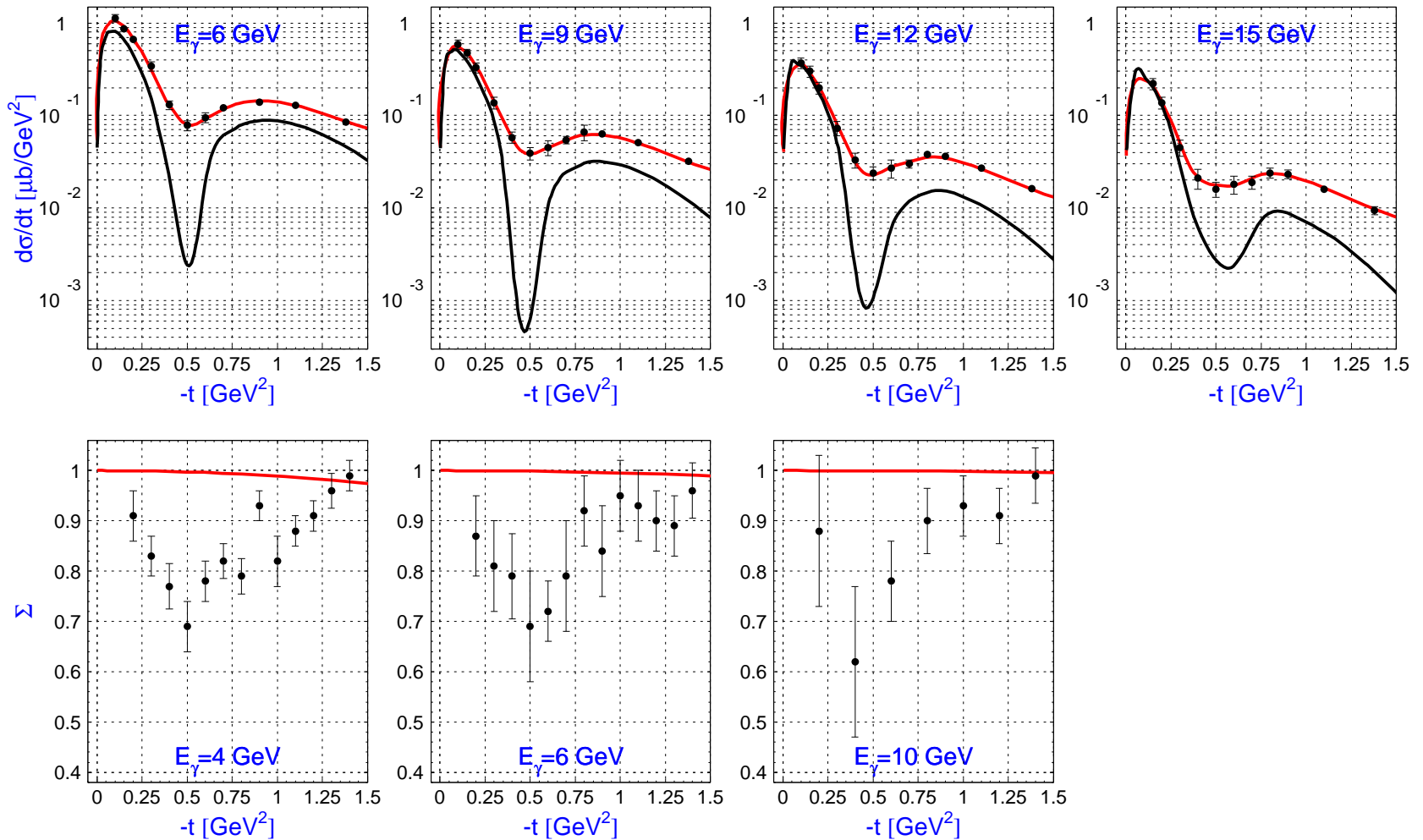
$$\alpha_{\omega-P}^c = 0.52 + 0.196t$$

trajectories of the associated $\rho - f_2$ and $\omega - f_2$ cuts:

$$\alpha_{\rho-f_2}^c = 0.222 + 0.404t$$

$$\alpha_{\omega-f_2}^c = 0.112 + 0.428t$$

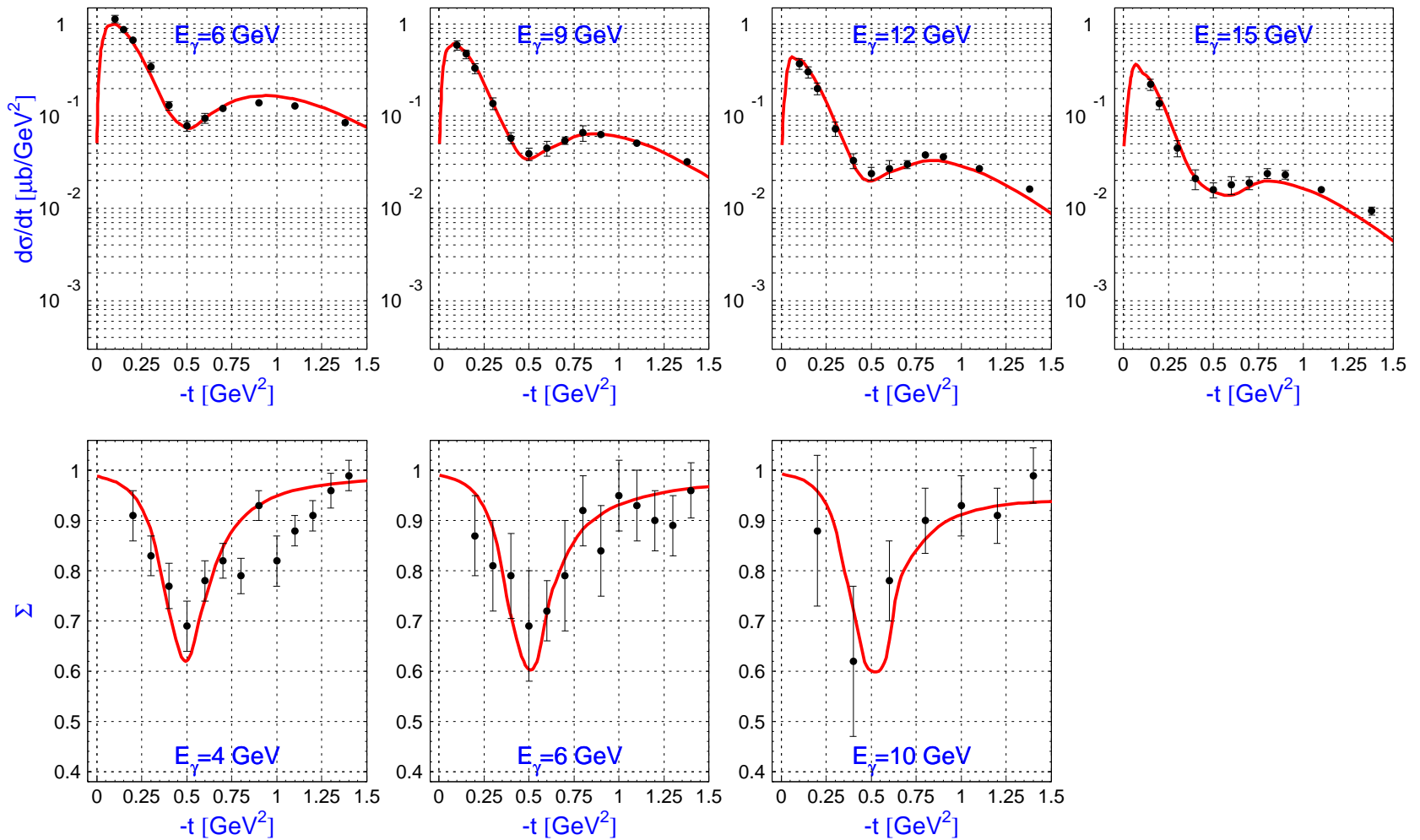
Regge cuts for π^0 photoproduction



Red lines: fit results with Regge cuts of ρ -P, ω -P, ρ - f_2 , ω - f_2 .

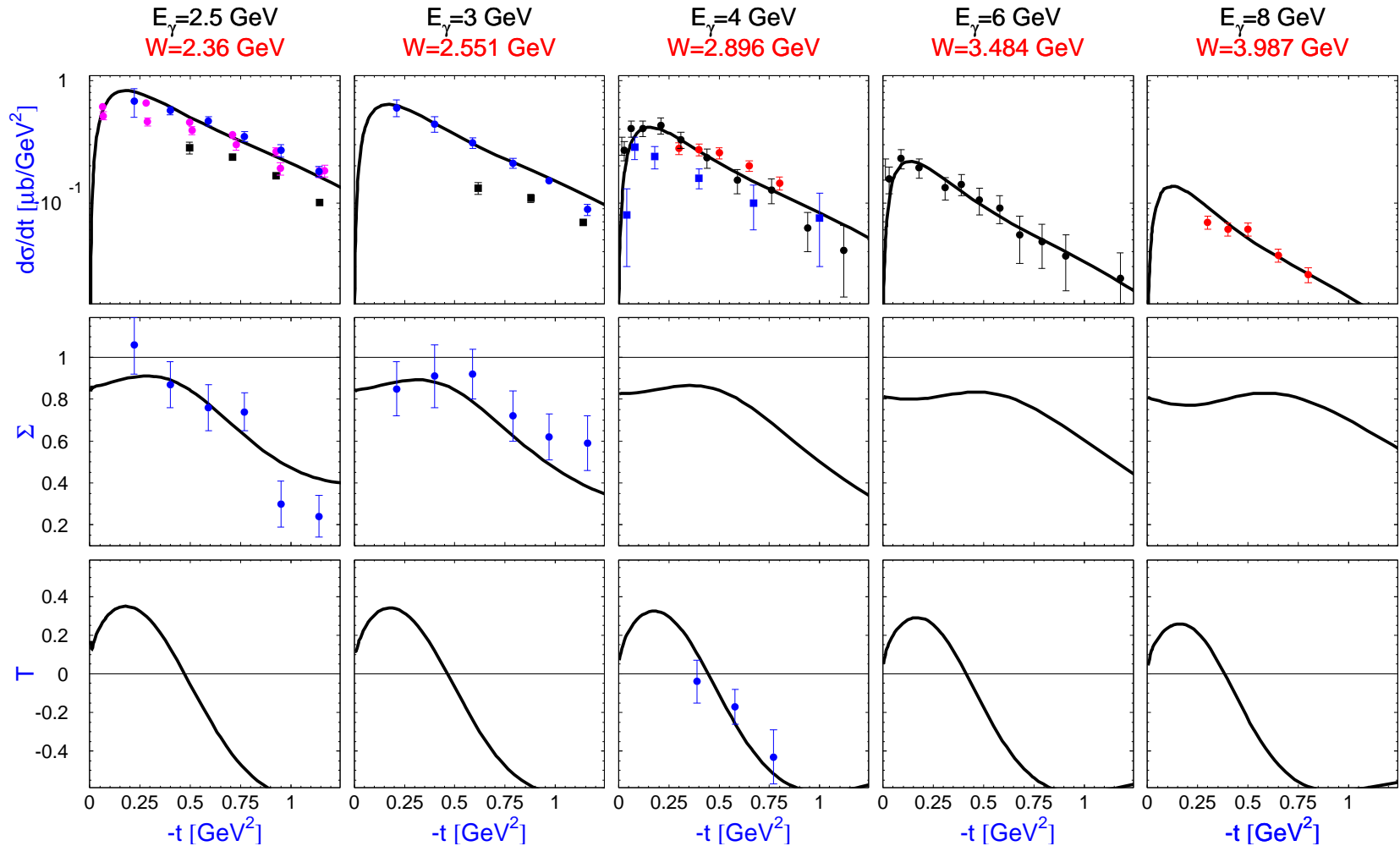
Black lines: without the cuts. Black circles: SLAC-1971 data

Regge cuts for π^0 photoproduction



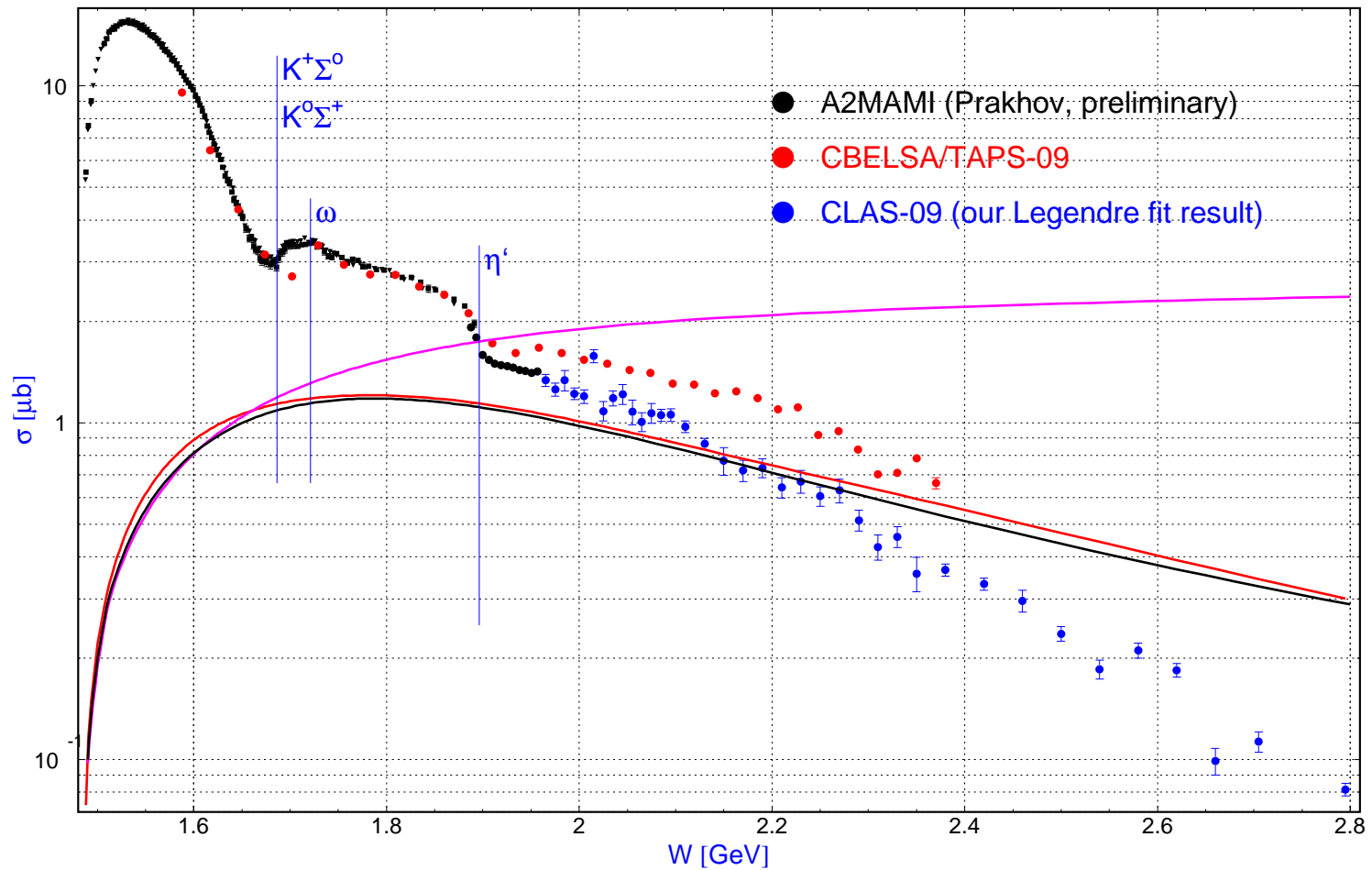
Red lines: fit results with vector and axial-vector (b_1) mesons.

Regge cuts: adaptation to η photoproduction



Black lines: fit results. Circles: black DESY-70, red WLS-71, blue Daresbury-76,80, magenta CBELSA/TAPS-2009. Squares: black CLAS-09, blue CEA-68.

Regge cuts: adaptation to η photoproduction



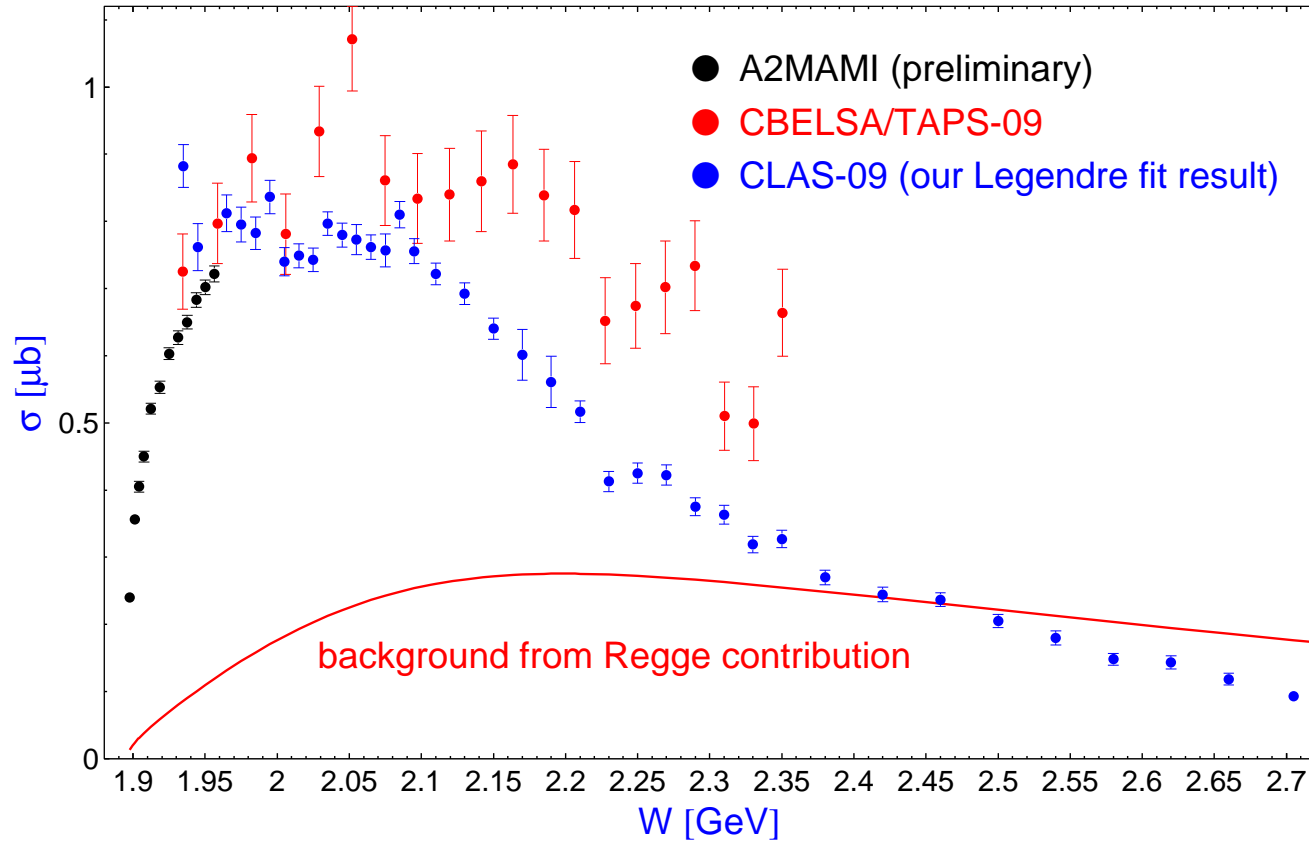
Background contributions:

Red line: present solution, black: η MAID2003 Regge, magenta: vector mesons as poles.

Regge cuts: adaptation to η' photoproduction

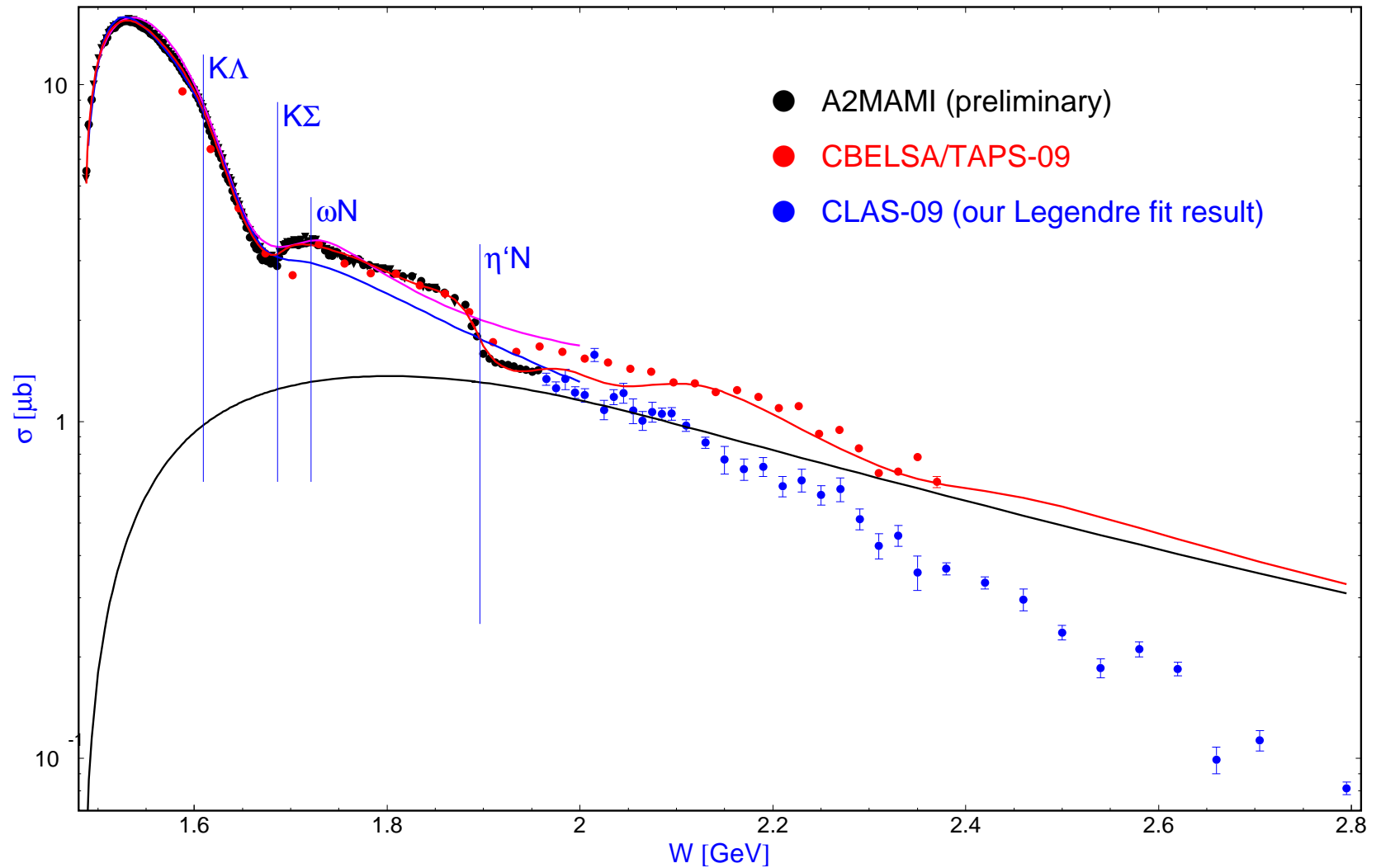
Electromagnetic coupling constants: $\lambda_{\rho\eta'\gamma} = 1.05$ and $\lambda_{\omega\eta'\gamma} = 0.36$.

All other parameters are the same as for η photoproduction.



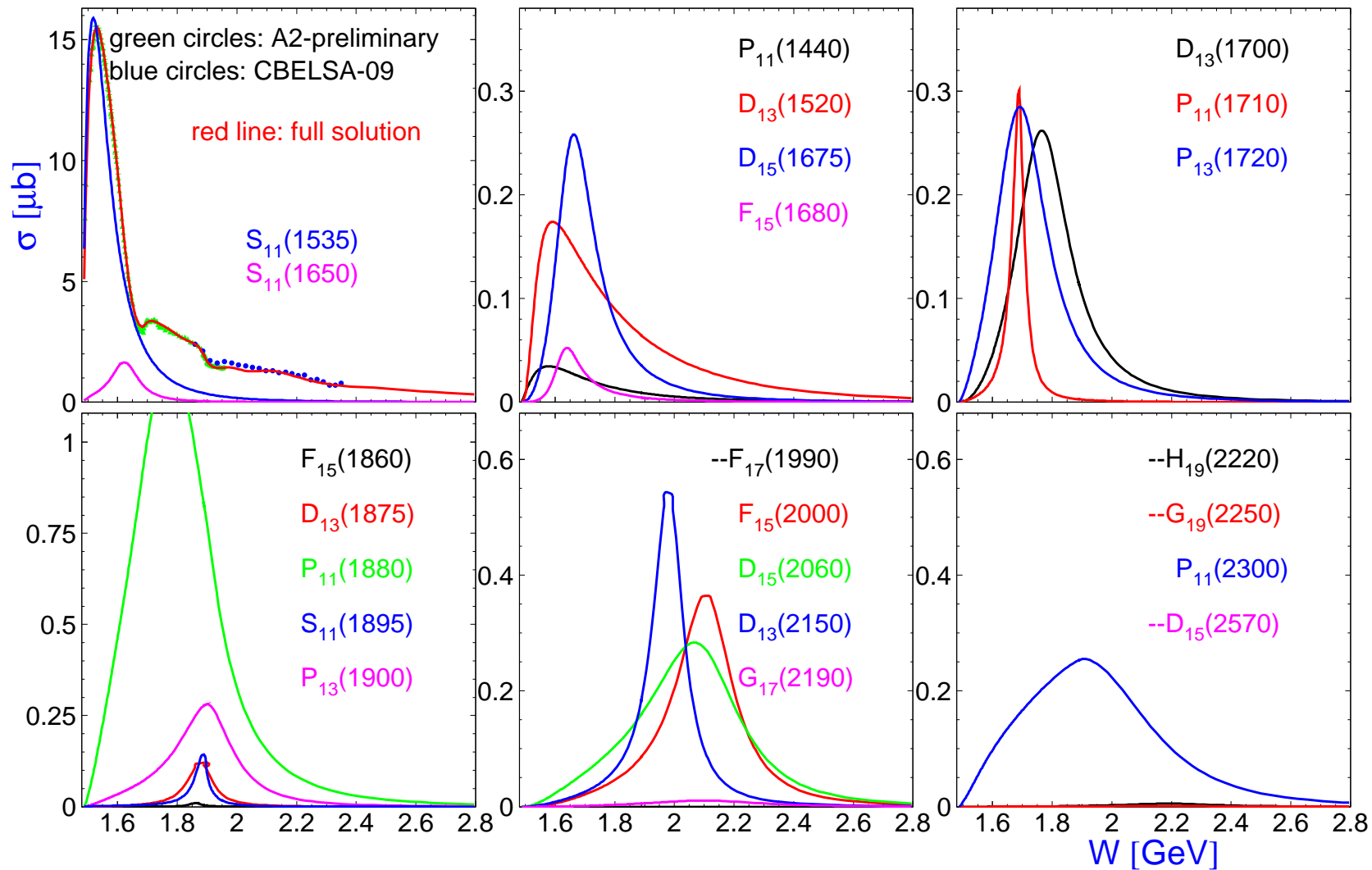
Regge+Resonances for $\gamma p \rightarrow \eta p$

Lines: background + resonances, black: background, η MAID-2003, η MAID-2003 Regge.



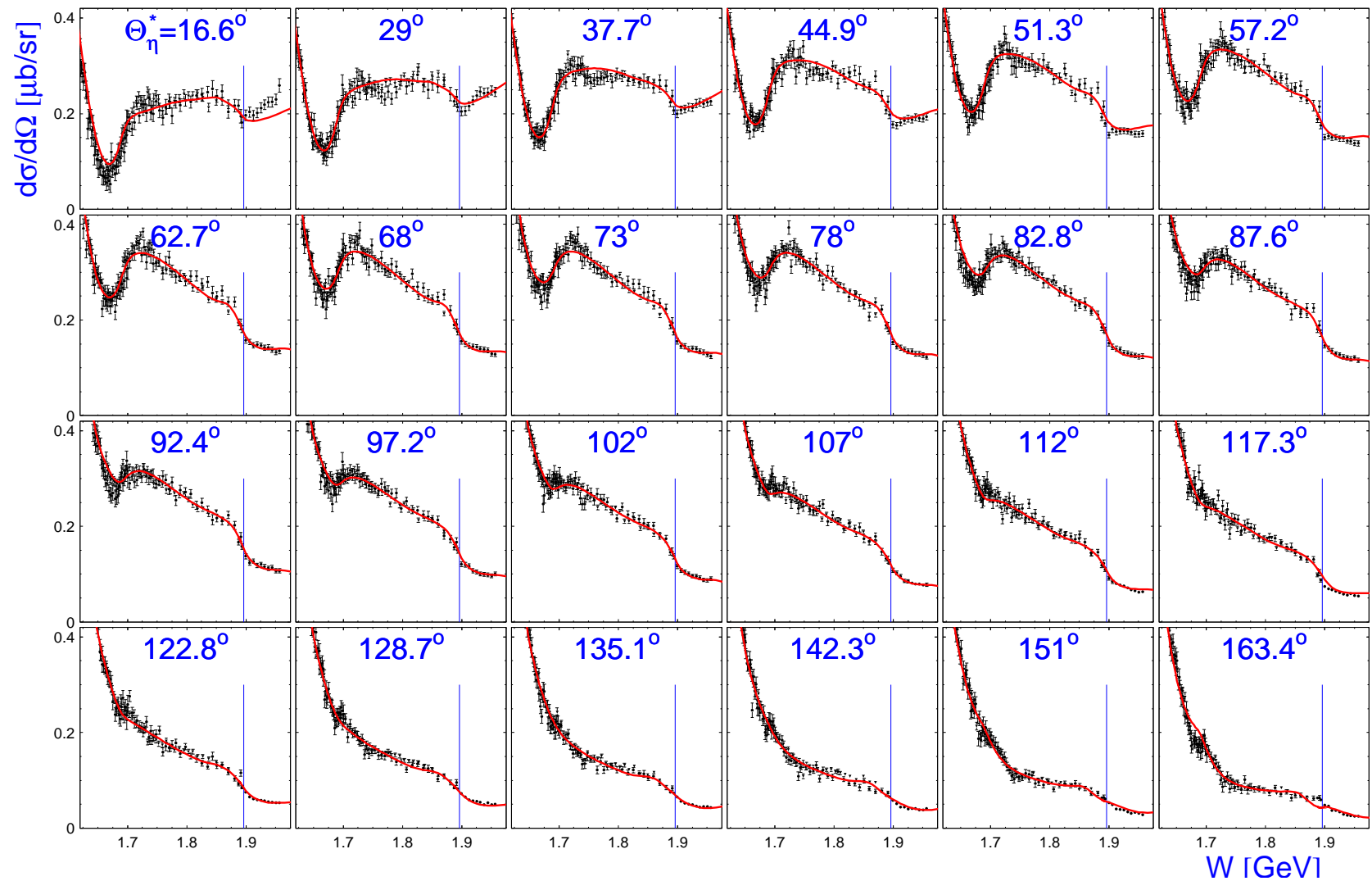
Regge+Resonances for $\gamma p \rightarrow \eta p$

Individual resonance contribution to total cross section.



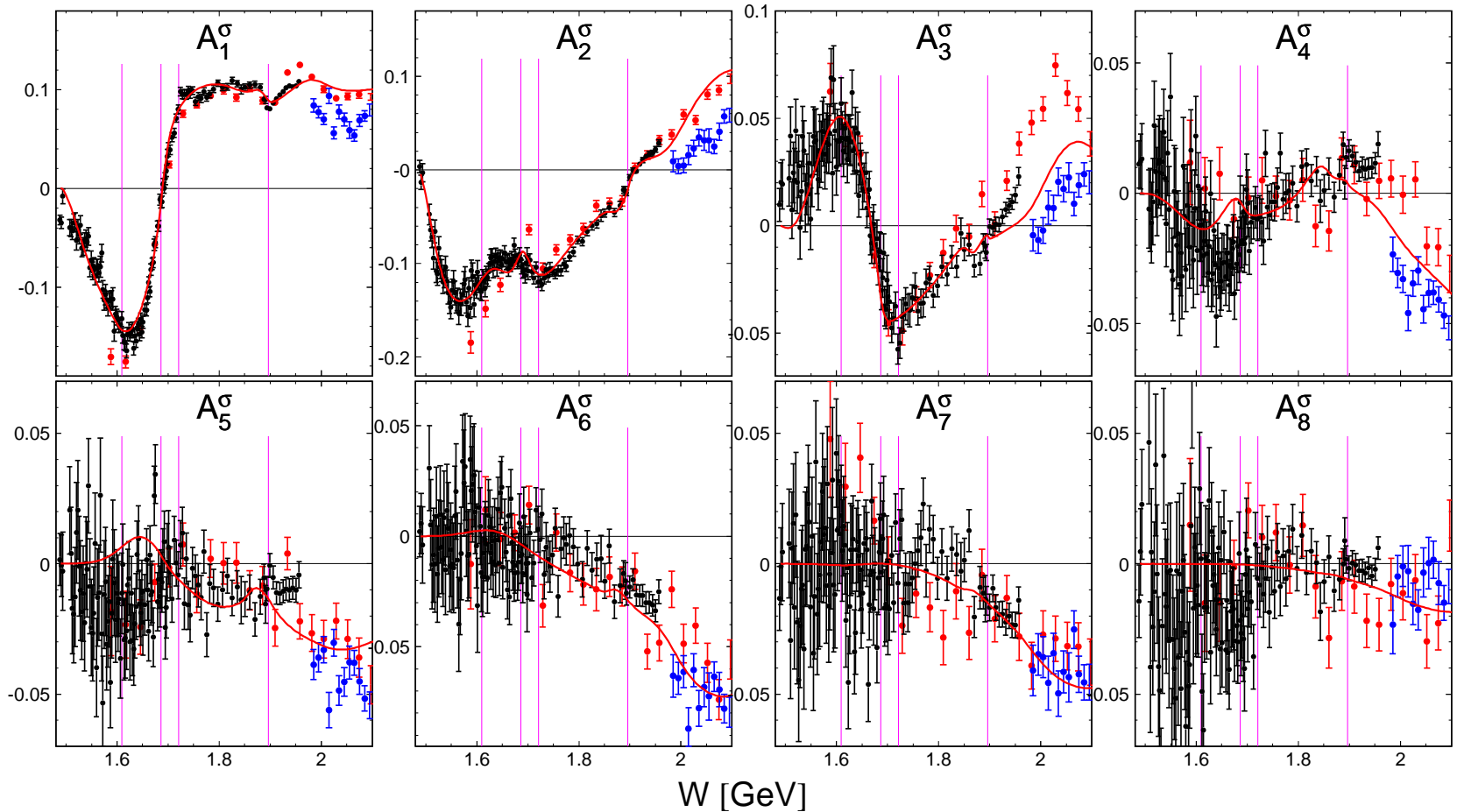
Regge+Resonances for $\gamma p \rightarrow \eta p$

Excitation function. Data: A2MAMI (preliminary). Red lines: full solution.



Legendre coefficients. $\gamma p \rightarrow \eta p$

Fit with $l_{max} = 8$. Red: A2MAMI, black: CBELSA-09, blue: CLAS-09 Magenta lines: thresholds of $K\Lambda$, $K\Sigma$, ωN , $\eta' N$ decay channels consistently.



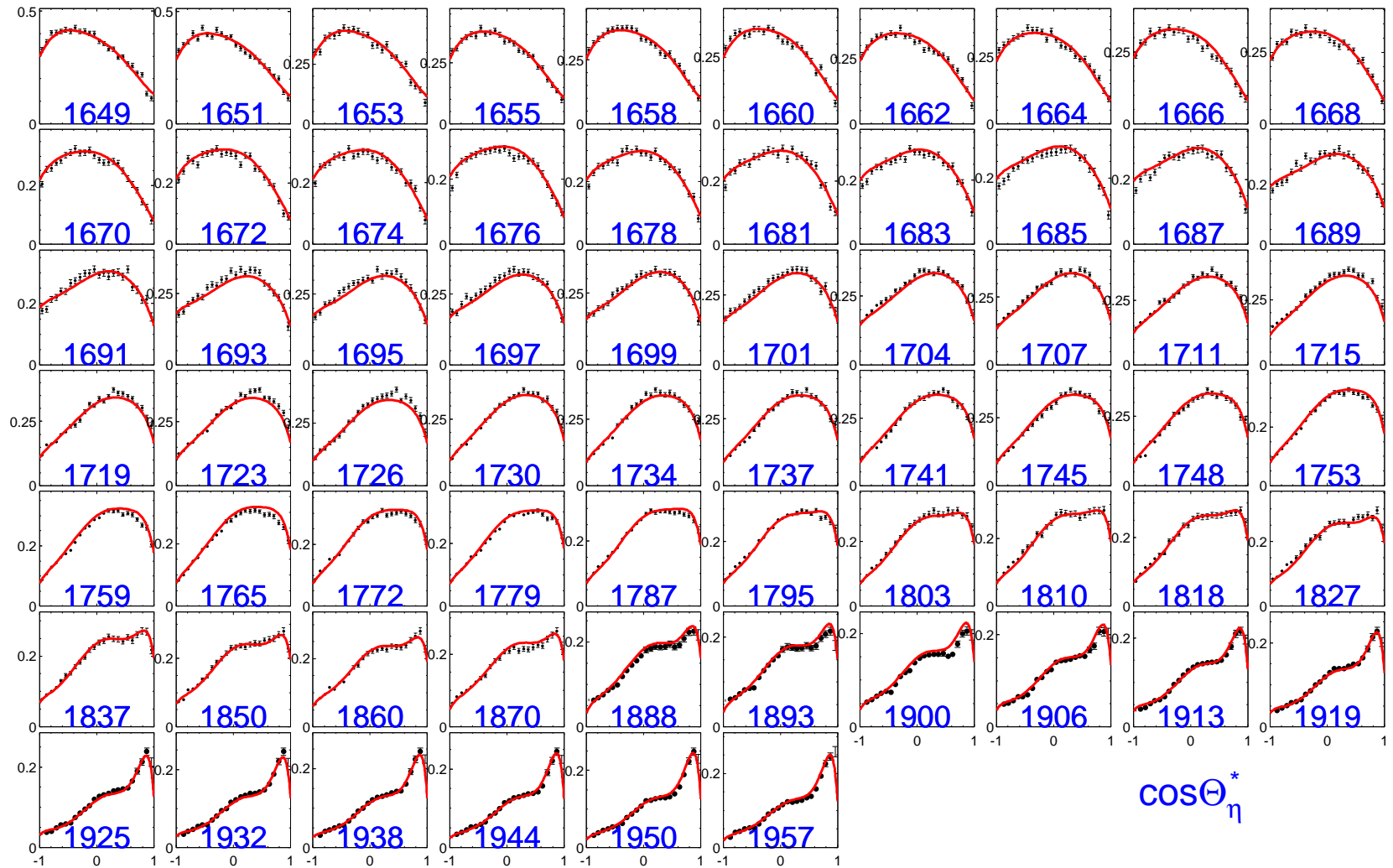
Regge+Resonances for $\gamma p \rightarrow \eta p$

Data: A2MAMI (preliminary). Red lines: full solution.



Regge+Resonances for $\gamma p \rightarrow \eta p$

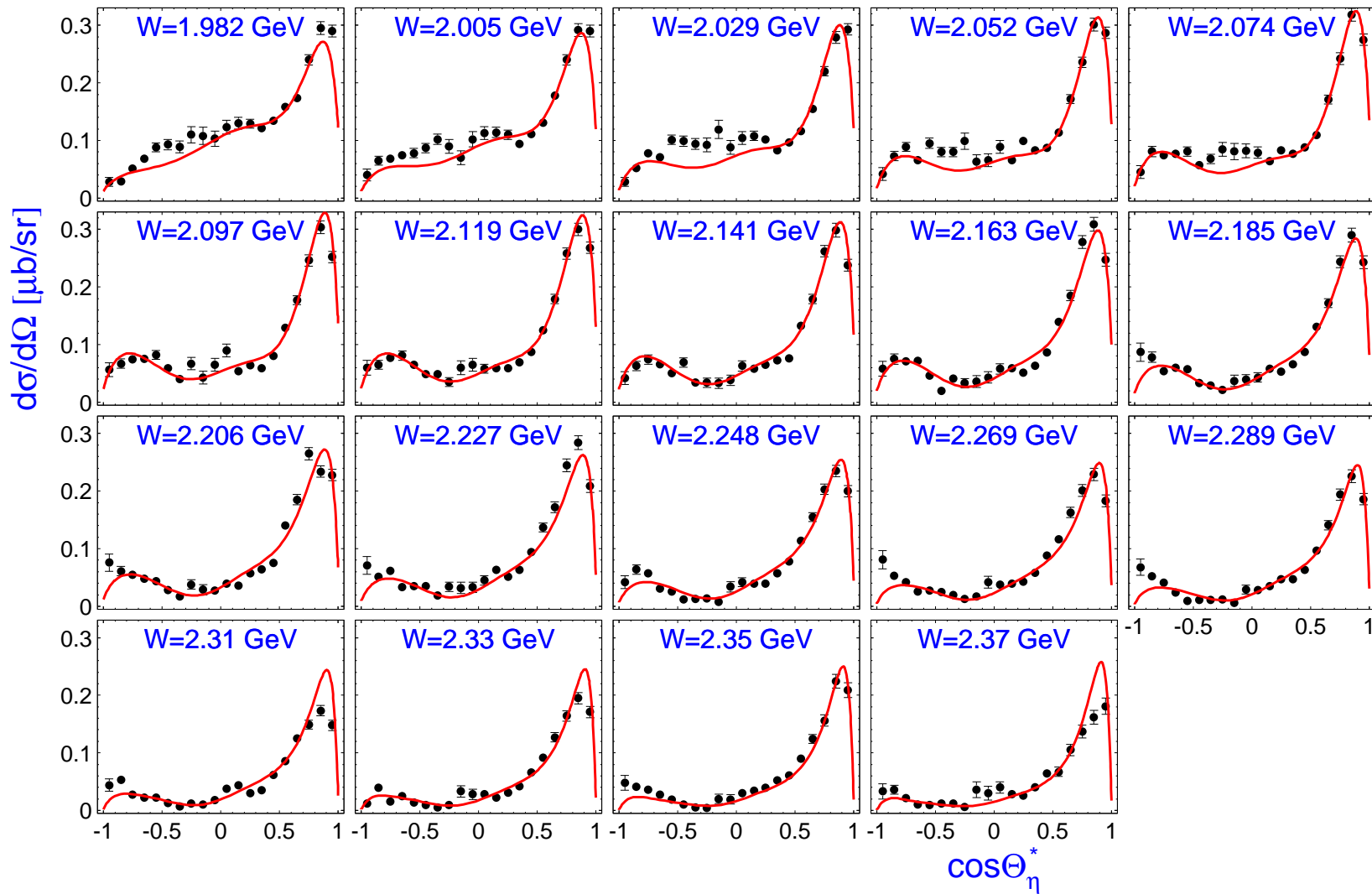
data: A2MAMI (preliminary). Red lines: full solution.



$\cos\Theta_{\eta}^*$

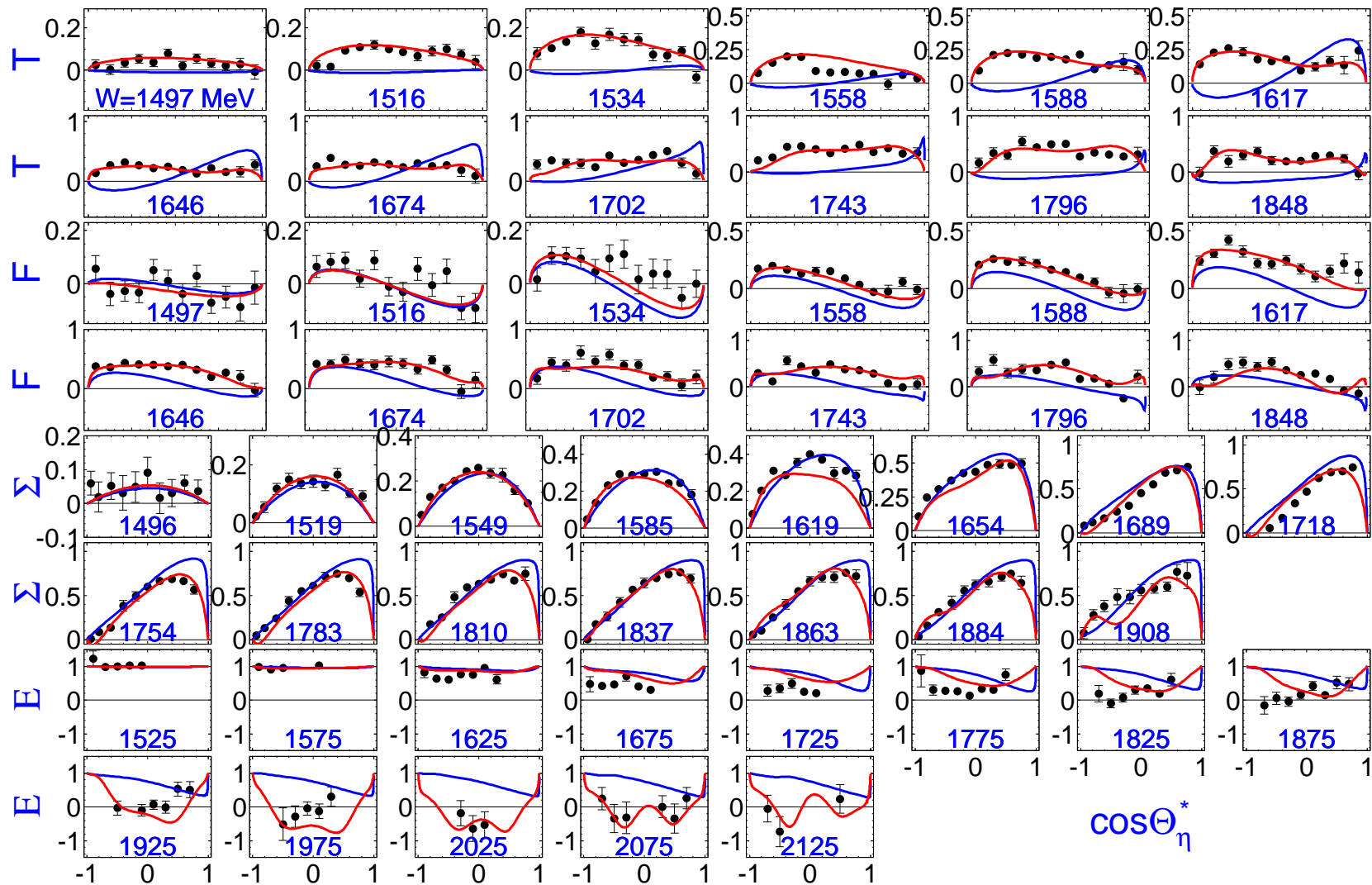
Regge+Resonances for $\gamma p \rightarrow \eta p$

Data: CBELSA/TAPS-09. Red lines: full solution.



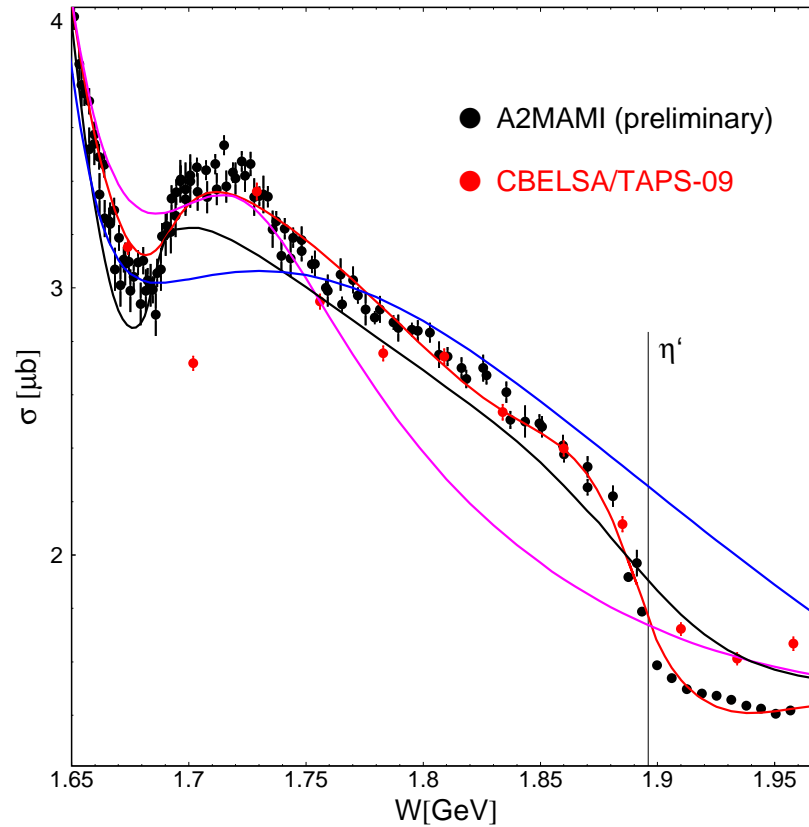
Regge+Resonances for $\gamma p \rightarrow \eta p$

data: A2MAMI-15 (T,F), GRAAL-07 (Σ), CLAS-15 (E). Red: full solution, blue: η MAID03.



Regge+Resonances for $\gamma p \rightarrow \eta p$

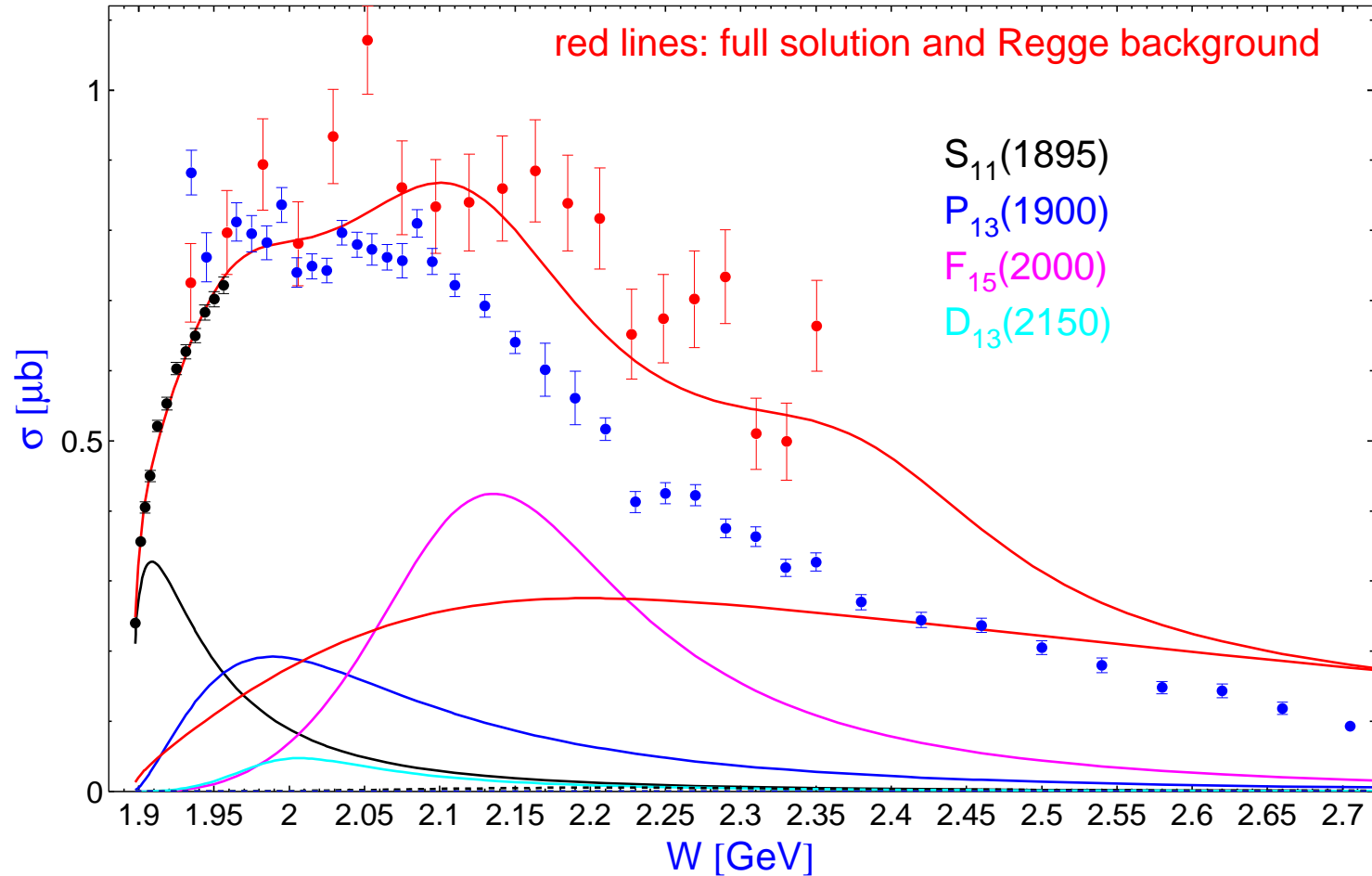
Lines: present solution, η MAID-2003, BG2014-2, SAID GE09.



Regge+Resonances for $\gamma p \rightarrow \eta' p$

Total cross section and individual resonance contributions.

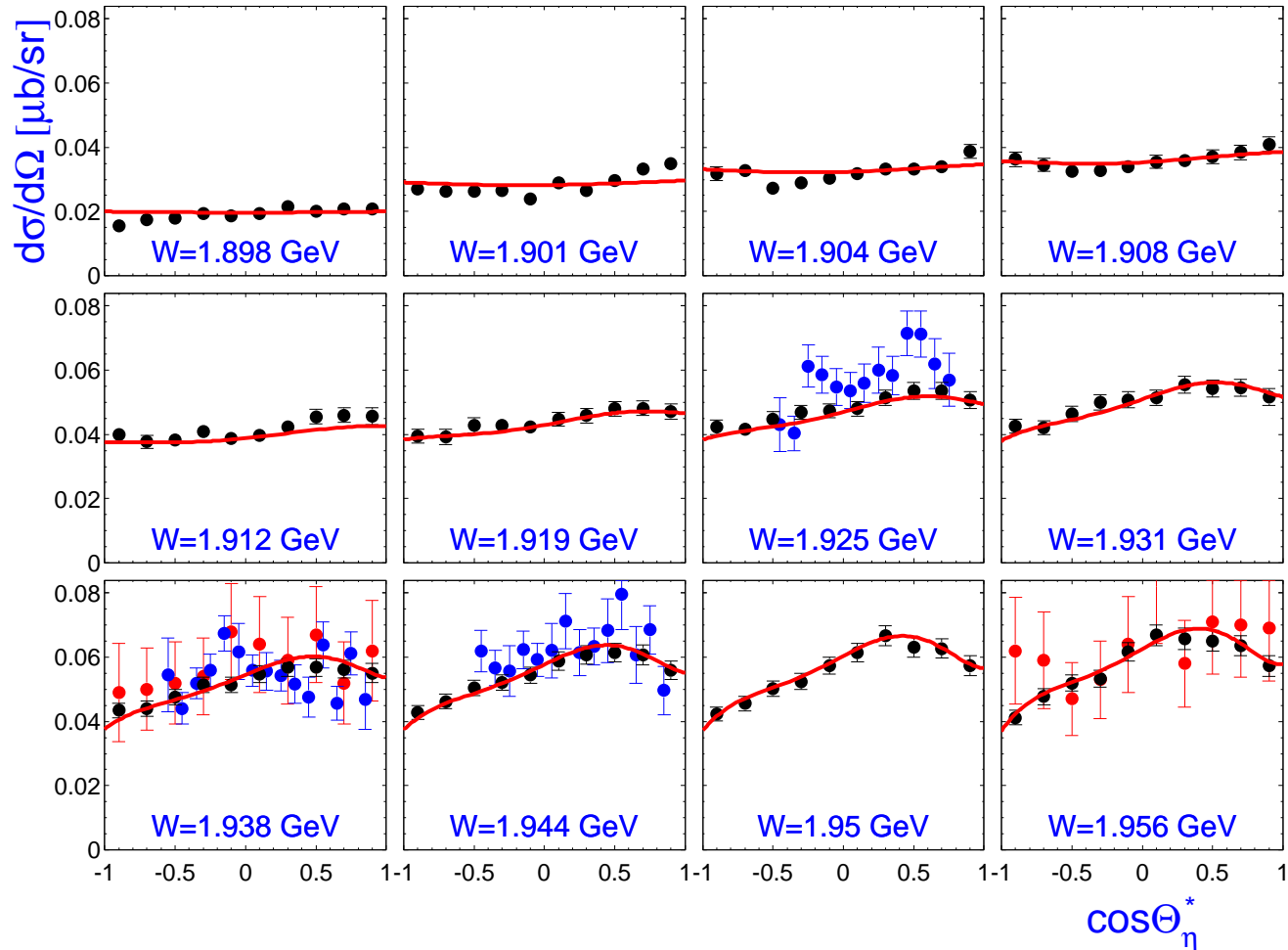
Data: A2MAMI (preliminary), CBELSA/TAPS-09, CLAS-09 (our Legendre fit).



Regge+Resonances for $\gamma p \rightarrow \eta' p$

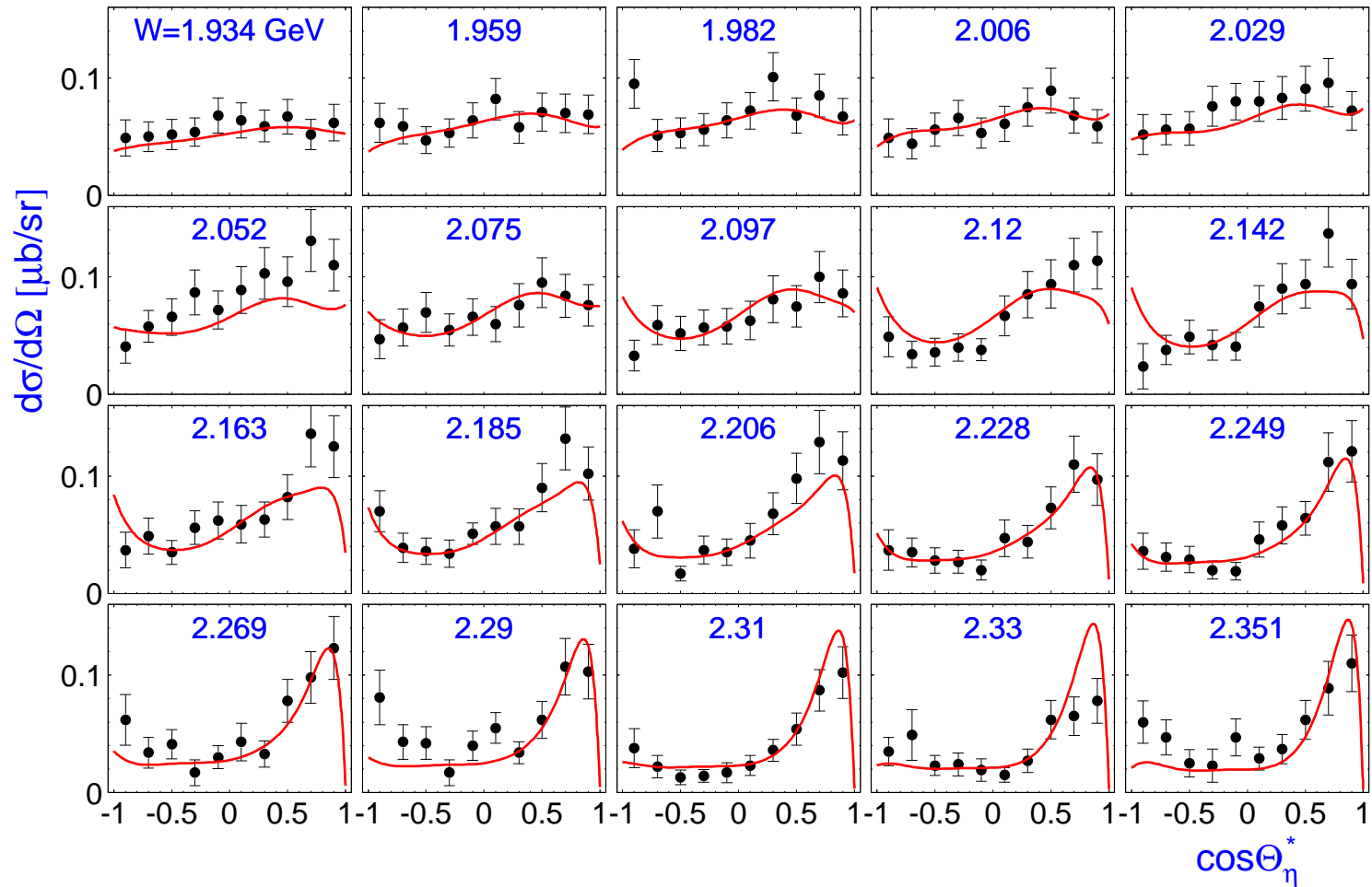
Data: A2MAMI-preliminary (black), CBELSA/TAPS-09, CLAS-09.

Red lines: full solution.



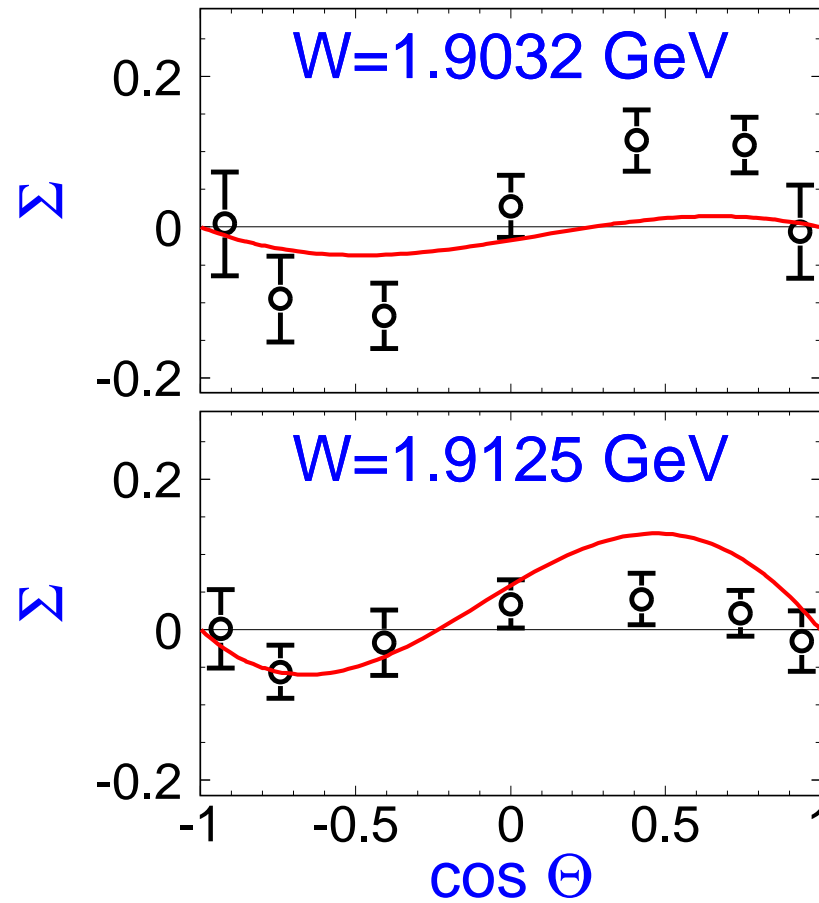
Regge+Resonances for $\gamma p \rightarrow \eta' p$

Data: CBELSA/TAPS-2009. Red lines: full solution.



Regge+Resonances for $\gamma p \rightarrow \eta' p$

Data: GRAAL-2015. Red lines: full solution.



Summary and Outlook

- A new version of the reggezed model for η and η' photoroduction on nucleons was presented. At energy below $W=2.5$ GeV dominate nucleon resonances. To decribe the data in this region we increased the N^* resonances from 8 in the original MAID now up to 23.
- At high energies Regge trajectories of ρ, ω, b_1 and Regge cuts of ρ -P, ω -P, ρ - f_2 , ω - f_2 were used. The obtained solution describes very well the data up to $E_\gamma=8$ GeV.
- Cusp in the total cross section in $\gamma p \rightarrow \eta p$ is explained as a threshold effect due to opening the $\eta' p$ decay channel of the $N(1895)1/2^-$ resonance.
- Breit-Wigner parameters of the resonances were determined. Next step is determination of pole positions and residues.
- A dispersion relation approach is in progress to reduce the model dependence.
- A model independent single-energy PWA is in progress with analytical constrains, similar to the Karlsruhe-Helsinki πN PWA.
- New reaction channels $\gamma N \rightarrow K\Lambda, K\Sigma, \omega N$ will be added to analysis.

Collaboration

- **Mainz:** Lothar Tiator, Michael Ostrick, Kirill Nikonov, and A2 Collaboration at MAMI.
- **Tuzla:** Jugoslav Stahov, Hedim Osmanovic, Mirza Hadzimehmedovic, Rifat Omerovic.
- **Zagreb:** Alfred Svarc.

Donnachie and Kalashnikova:

As a physical mass cannot be associated with a cut, the simplest form of amplitude for a cut term is

$$A_c(s, t) = C_c D_c(s, t) \quad (6)$$

where C_c is a constant and

$$D_c(s, t) = e^{d_c t} e^{-i \frac{1}{2} \pi \alpha_c(t)} s^{\alpha_c(t) - 1}. \quad (7)$$

where we have retained only the Regge phase and absorbed the rest of the t -dependence in the exponential, $\alpha_c(t)$ is the cut trajectory and the constants C_c and d_c for each cut term are obtained by fitting data.

We need a mechanism to allow us to transfer the π^0 cut model to scalar the dominant ω and ρ exchanges, retaining the kinematical structure and replacing $\lambda_{V\pi^0\gamma} g_{VNN} D_V(s, t)$,

$V = \rho, \omega$ by

$$\lambda_{V\pi^0\gamma} g_{VNN} (D_V(s, t) + C_n^{V-P} D_c^{V-P}(s, t) + C_n^{V-f_2} D_c^{V-f_2}(s, t)), \quad (8)$$

where C_n^{V-P} and $C_n^{V-f_2}$ are respectively the natural-parity constants for the $V-P$ and $V-f_2$ cuts.

Donnachie and Kalashnikova:

These cuts also feed into the unnatural-parity exchange term and are much larger than any cuts generated by $b_1(1235)$ exchange due to its small contribution. So b_1 pole term

$\lambda_{b_1\pi^0\gamma}g_{b_1NN}D_b(s, t)$ is replaced by

$$\lambda_{b_1\pi^0\gamma}g_{b_1NN}D_b(s, t) + \sum_V \lambda_{V\pi^0\gamma}g_{VNN}(C_u^{V-P}D_c^{V-P}(s, t) + C_u^{V-f_2}D_c^{V-f_2}(s, t)), \quad (9)$$

where the C_u^{V-P} and $C_u^{V-f_2}$ are the unnatural-parity constants. It turns out that the cuts dominate unnatural parity exchange so in practice the b_1 pole term could be omitted.

The parameters for ρ and ω were taken to be the same:

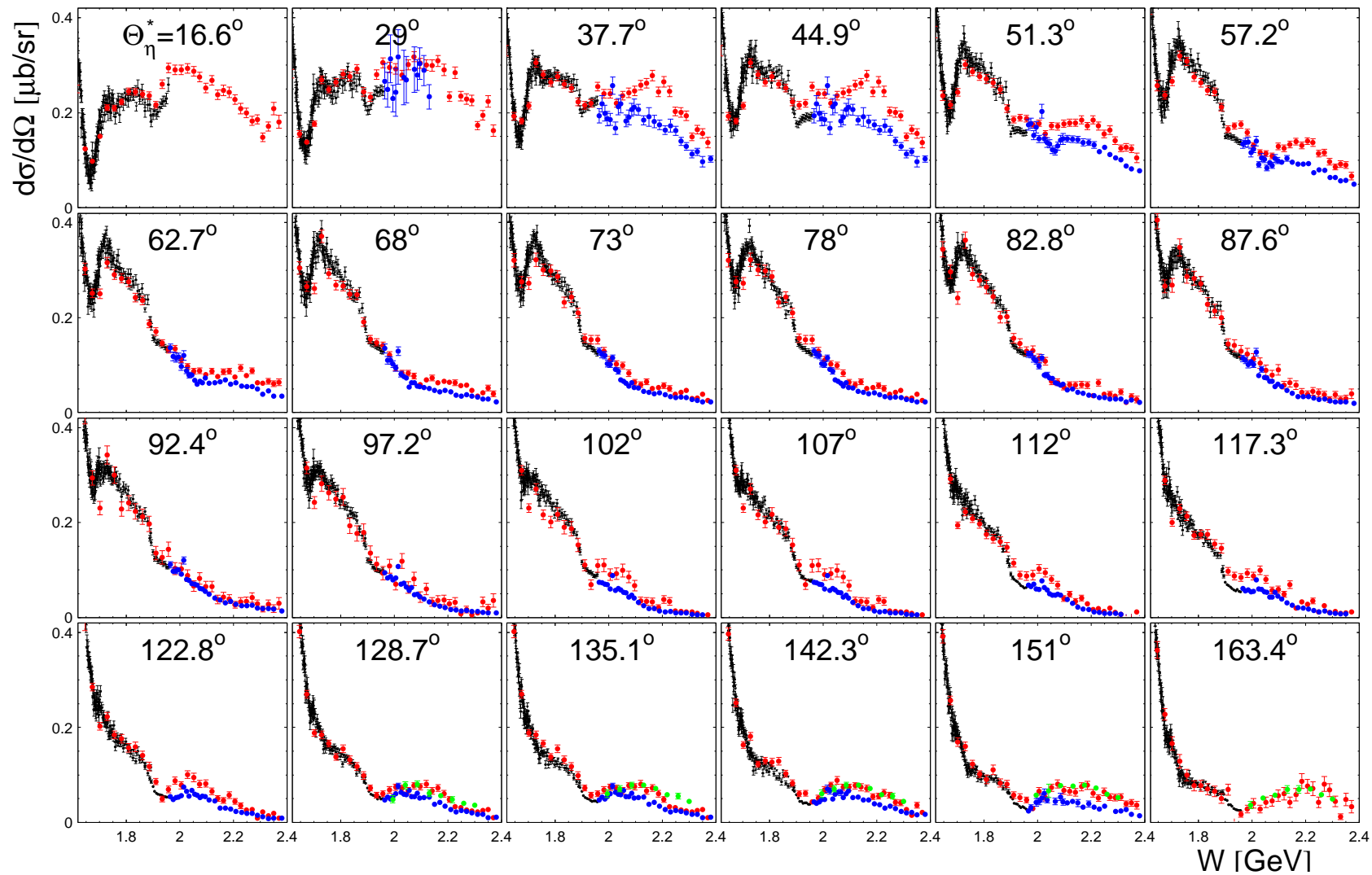
$$C_n^{\rho-P} = C_n^{\omega-P}, \quad C_n^{\rho-f_2} = C_n^{\omega-f_2},$$

$$C_u^{\rho-P} = C_u^{\omega-P}, \quad C_u^{\rho-f_2} = C_u^{\omega-f_2}.$$

d_c of the exponential also was taken to be the same for all terms.

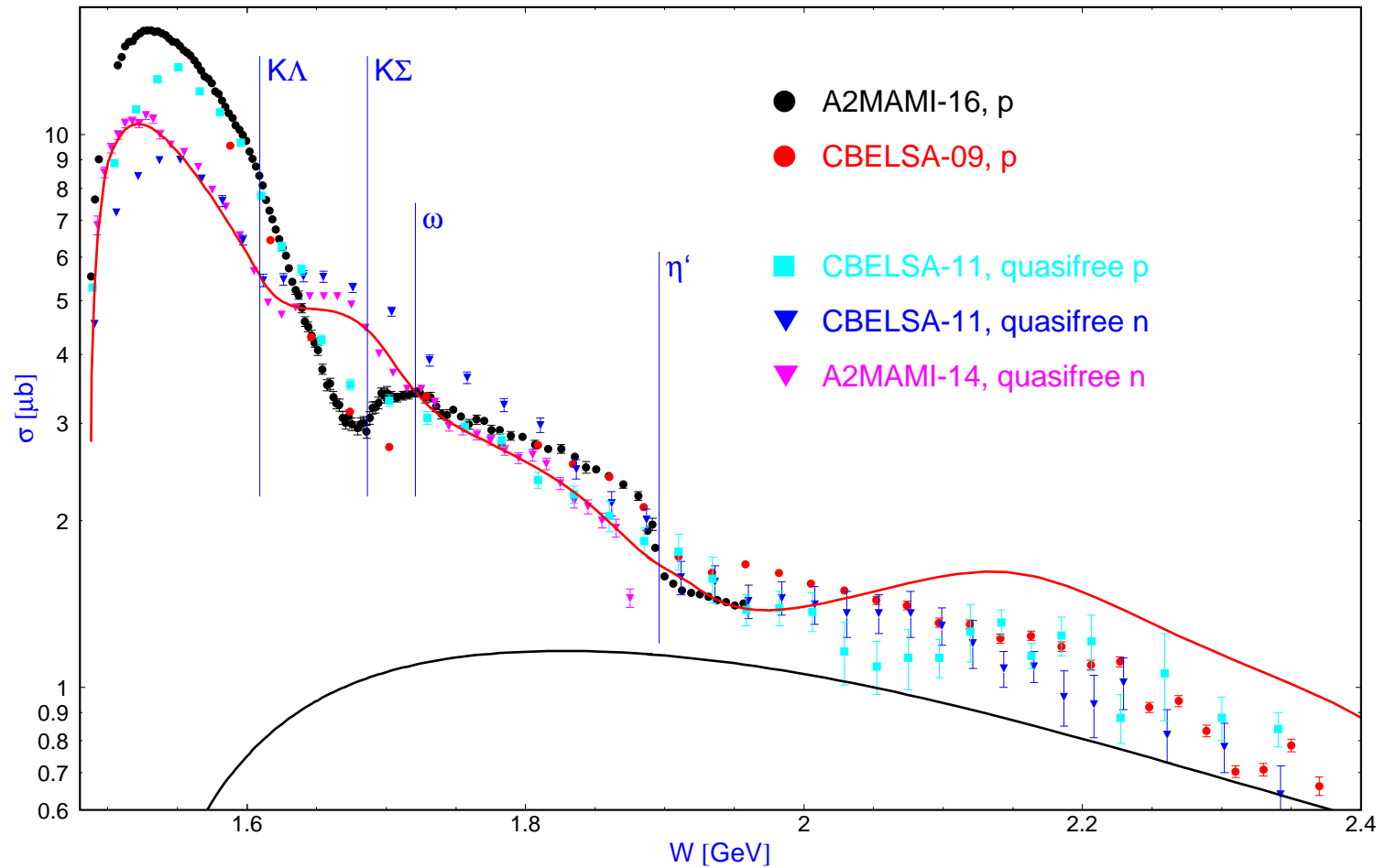
So in practice we have only five free parameters to describe π^0 photoproduction.

Excitation function. Data: A2MAMI, CBELSA-09, CLAS-09



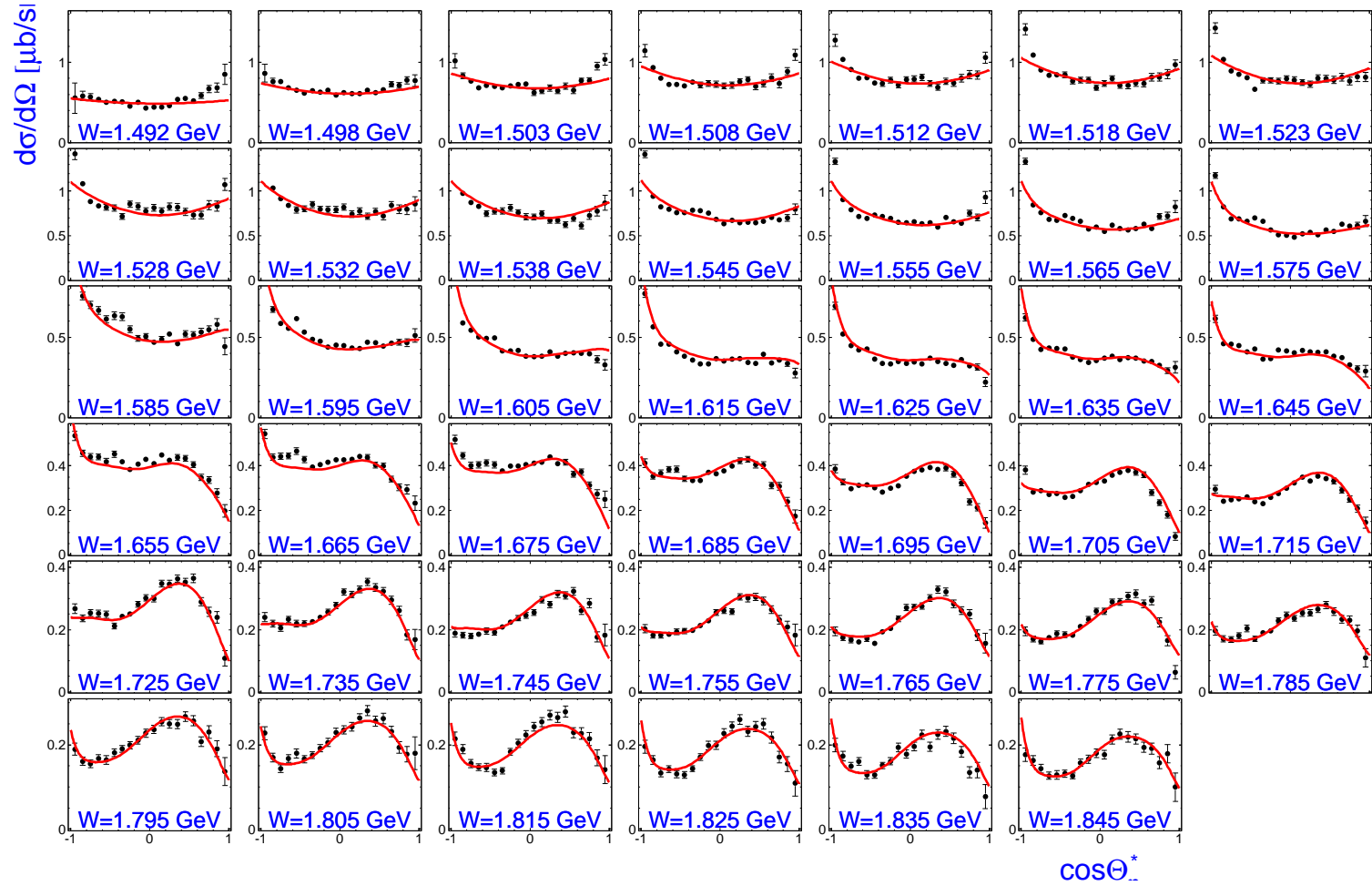
Regge+Resonances for $\gamma n \rightarrow \eta n$

Total cross section. **Red line: full solution**, black line: background.



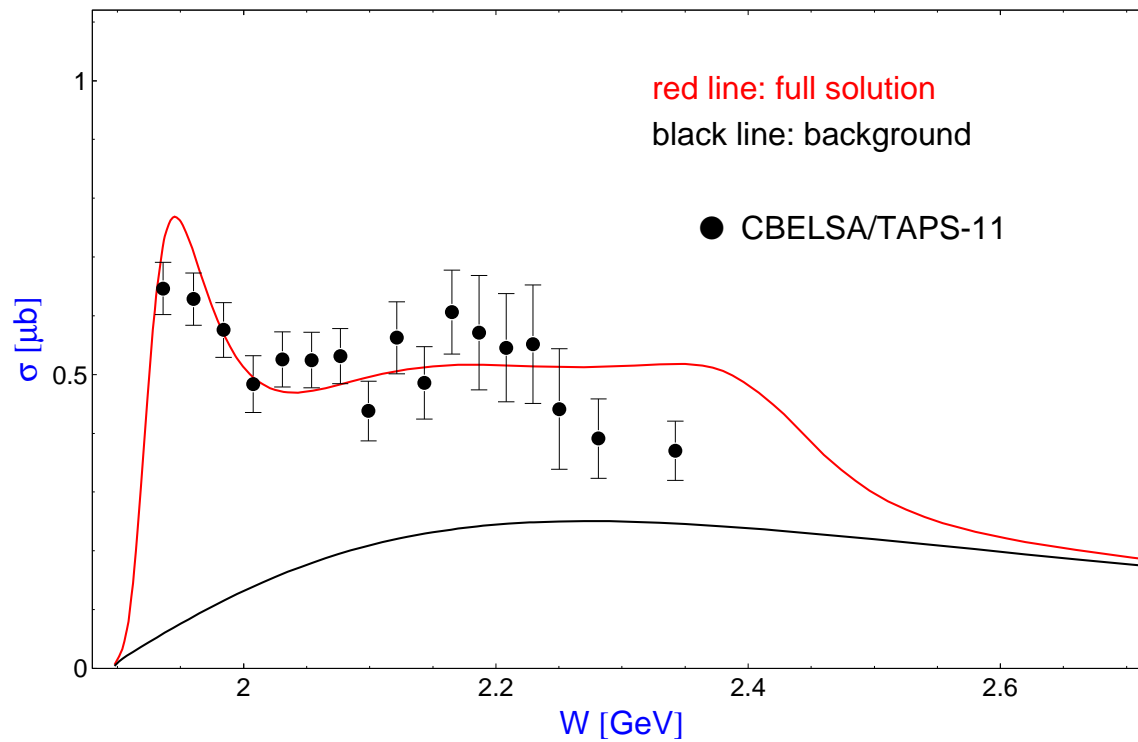
Regge+Resonances for $\gamma n \rightarrow \eta n$

Differential cross sections. Data: A2MAMI-14. Red lines: full solution.



Regge+Resonances for $\gamma n \rightarrow \eta' n$

Total cross section.



Regge+Resonances for $\gamma n \rightarrow \eta' n$

Differential cross sections. Data: CBELSA/TAPS-11 . Red lines: full solution.

