

# Heavy quark spin in nuclear medium

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# 1. Multi-flavor nucleus

# Nucleus meets Flavor

HiggsTan.com

charge

1st

2nd

3rd

$Q=+2/3$

up



charm



top



2 MeV

1300 MeV

173000 MeV

$Q=-1/3$

down



strange



bottom



5 MeV

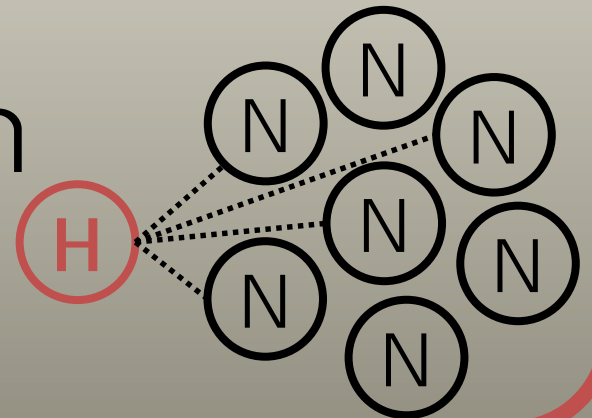
100 MeV

4200 MeV

# 1. Multi-flavor nucleus

## Nucleus meets Flavor

1. Hadron-nucleon interaction
2. Hadron in medium
3. Nuclear structure



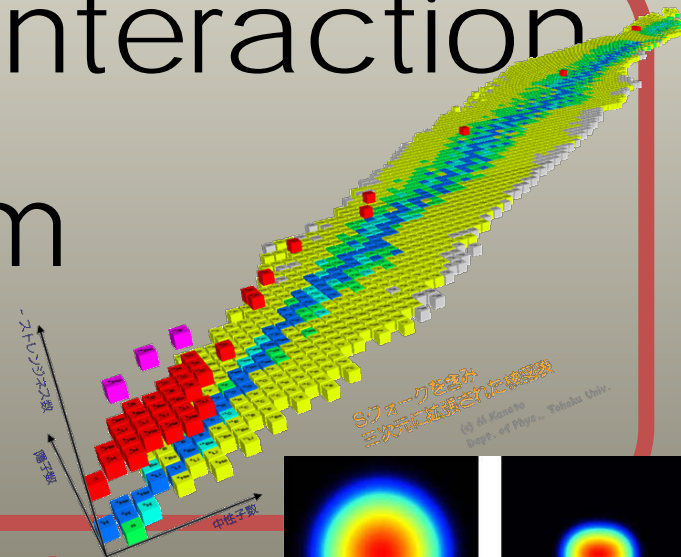
Impurity Physics

# 1. Multi-flavor nucleus

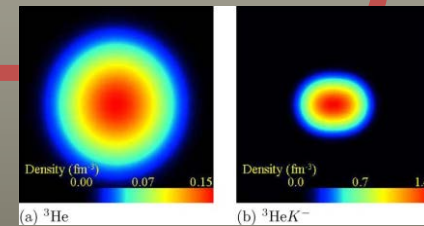


# Nucleus + Strangeness

1. Hadron-nucleon interaction
2. Hadron in medium
3. Nuclear structure



## Impurity Physics



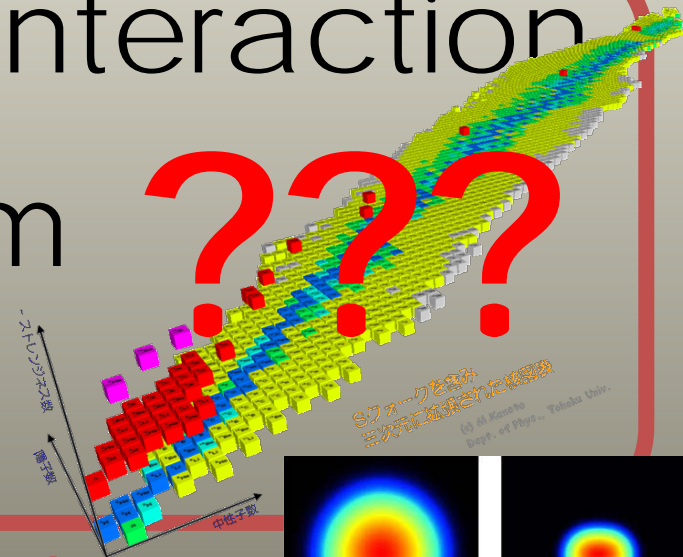
# 1. Multi-flavor nucleus

## Nucleus + Charm

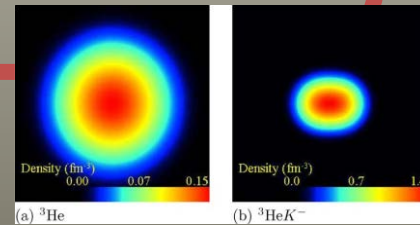


Mass hierarchy ( $m_c \gg \Lambda_{\text{QCD}}$ )  
~1.2 GeV    ~0.2 GeV

1. Hadron-nucleon interaction
2. Hadron in medium
3. Nuclear structure



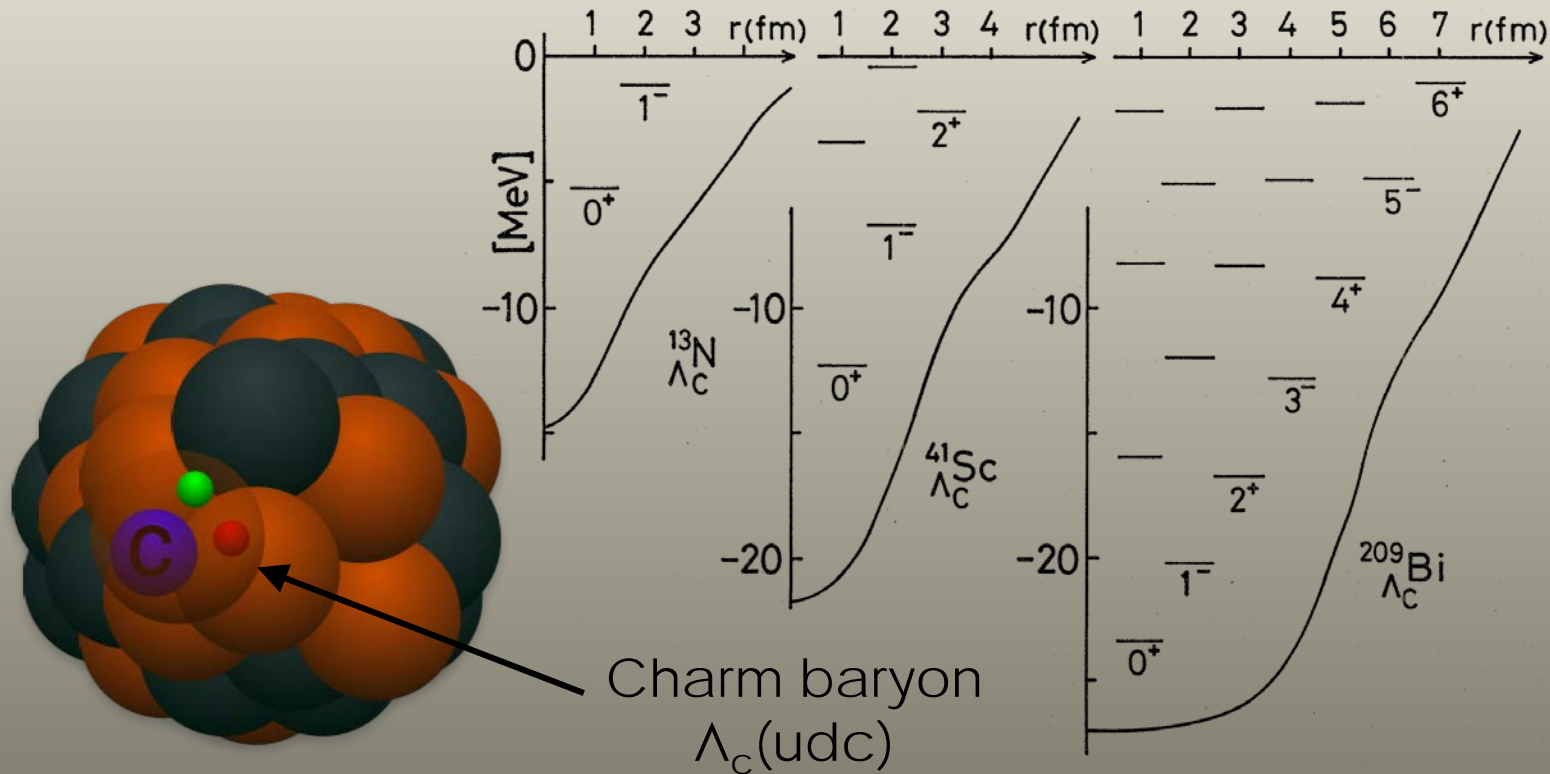
## Impurity Physics



# 1. Multi-flavor nucleus

Strangeness

Charm



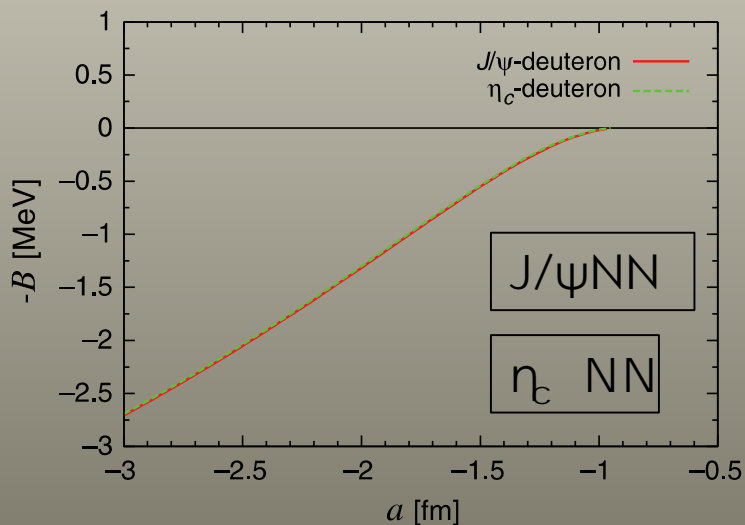
# 1. Multi-flavor nucleus

## Charm/bottom "light" nuclei

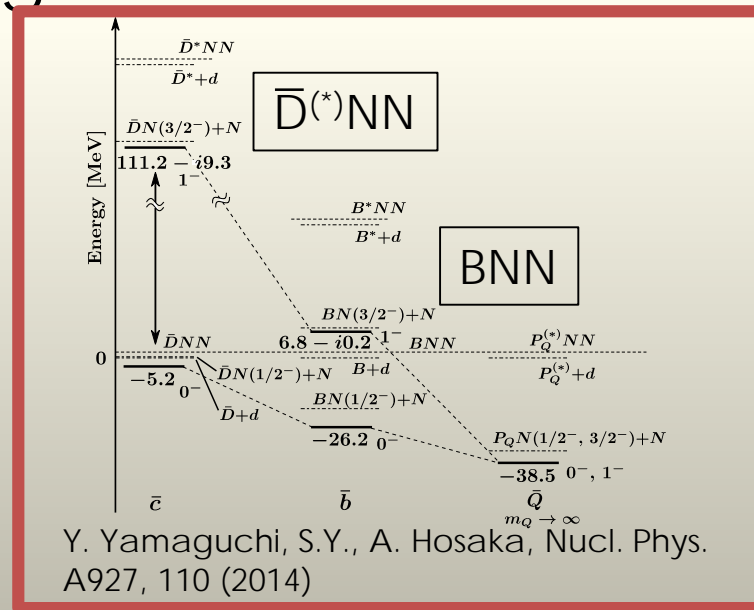
DNN

	HN1R $J = 1$	$J = 0$	Minnesota $J = 0$	Av18 $J = 0$
$B$	Unbound	Bound	Bound	Bound
$M_B$	3537	3520	3494	3536
$\Gamma_{\pi Y_c N}$	—	26	38	22
$E_{\text{kin}}$	338	352	438	335
$V(NN)$	0	-2	19	-5
$V(DN)$	-546	-575	-708	-540
$T_{\text{nuc}}$	113	126	162	117
$E_{NN}$	113	124	181	113
$P(\text{odd})$	75.0%	14.4%	7.4%	18.9%

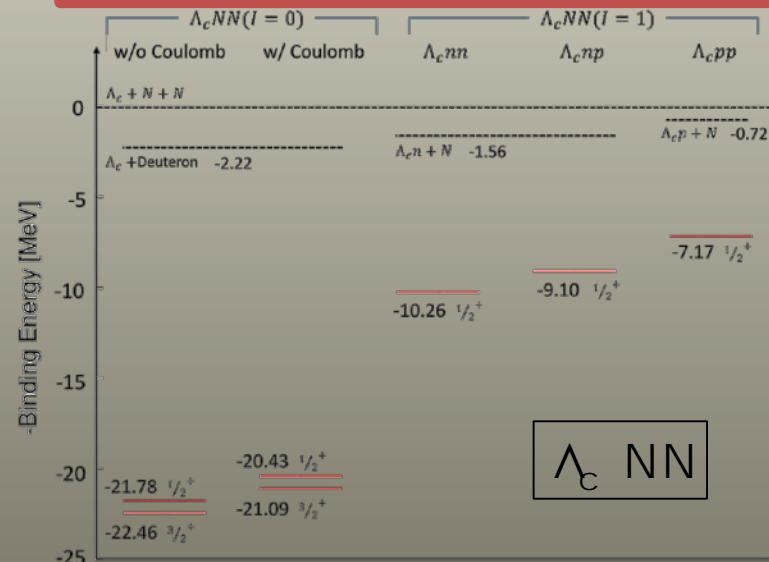
M. Bayer, C. W. Xiao, T. Hyodo, A. Dote, M. Oka, E. Oset, Phys. Rev. C86, 044004 (2012)



A. Yokota, E. Hiyama, M. Oka, Pog. Ther. Exp. Phys. 2013, 113D01



Y. Yamaguchi, S.Y., A. Hosaka, Nucl. Phys. A927, 110 (2014)

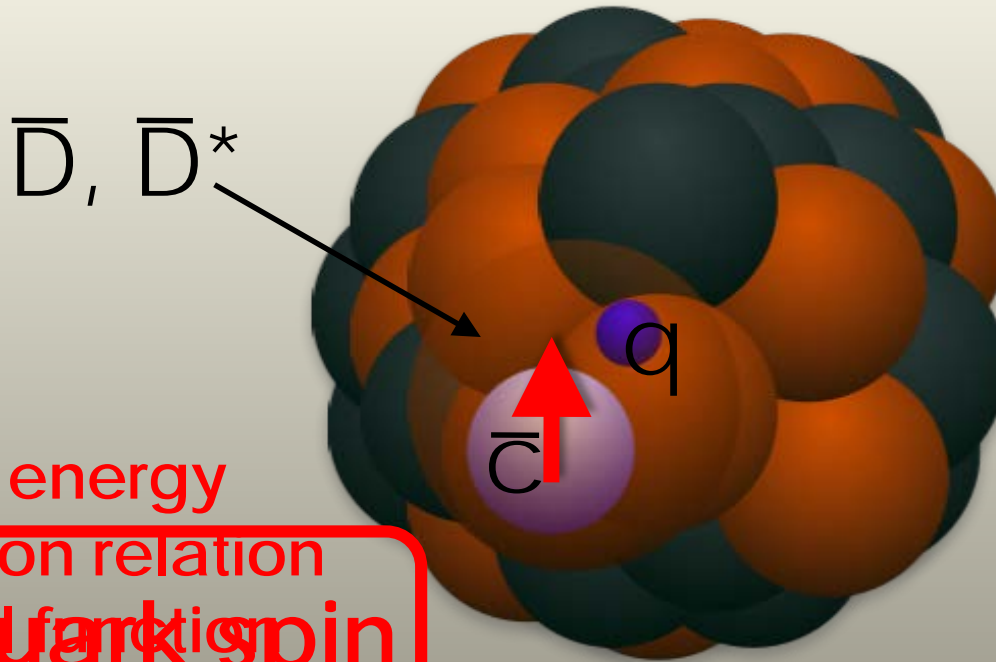


S. Maeda, M. Oka, A. Yokota, E. Hiyama, Y-R. Liu, Pog. Ther. Exp. Phys. 2016, 023D02

# 1. Multi-flavor nucleus

## $\bar{D}$ ( $B$ ) meson in nuclear matter

Quark-meson coupling model, QCD sum rules, hadronic interactions (mean-field approach, channel coupling, pion interaction), ...



- Binding energy

- Dispersion relation

Heavy quark spin

- Reaction

- Restoration of  $\chi$ SB

- Nuclear structure

- etc.

Nucleus

Charm nucleus mass spectroscopy



# 1. Multi-flavor nucleus

## $\bar{D}$ (B) meson in nuclear matter

Quark-meson coupling model, QCD sum rules, hadronic interactions (mean-field approach, channel coupling, pion interaction), ...

Binding energy in nuclear matter [MeV]

	Quark-meson coupling model	QCD sum rule	Hadron dynamics		
			Mean field	WT-type coupling	$\pi$ exchange
$\bar{D}$ meson	$-(10-35)$ (in $^{208}\text{Pb}$ ) [6] $\simeq +20$ [7]	$+(65-75)$ [15] $-50$ MeV [27] $+30$ MeV [28] $-66$ MeV [29]	$\simeq -(100-180)$ [18] $-30$ [21] $-27$ [22, 24]	$+18$ [19] $+(11-20)$ [20] $+(27-35)$ [23] $\simeq -(20-27)$ [25]	$-35.1$ [26]
$D^*$ meson					$-153.9 - i170.1$
B meson		$+(125-155)$ [15]			$-106.9$
$B^*$ meson					$-203.3 - i117.5$

**~ a few ten MeV**  
**(Repulsive? Attractive?)**

[6] K. Tsushima, D. -H. Lu, A. W. Thomas, K. Saito and R. H. Landau, Phys. Rev. C 59, 2824 (1999).

[7] A. Sibirtsev, K. Tsushima and A. W. Thomas, Eur. Phys. J. A 6, 351 (1999).

[15] T. Hilger, R. Thomas and B. Kampfer, Phys. Rev. C 79, 025202 (2009).

[16] T. Hilger, R. Schulze and B. Kampfer, J. Phys. G G 37, 094054 (2010).

[17] Z. -G. Wang and T. Huang, Phys. Rev. C 84, 048201 (2011).

[18] A. Mishra, E. L. Bratkovskaya, J. Schaffner-Bielich, S. Schramm and H. Stoecker, Phys. Rev. C 69, 015202 (2004).

[19] M. F. M. Lutz and C. L. Korpa, Phys. Lett. B 633, 43 (2006).

[20] L. Tolos, A. Ramos and T. Mizutani, Phys. Rev. C 77, 015207 (2008).

[21] A. Mishra and A. Mazumdar, Phys. Rev. C 79, 024908 (2009).

[22] A. Kumar and A. Mishra, Phys. Rev. C 81, 065204 (2010).

[23] C. E. Jimenez-Tejero, A. Ramos, L. Tolos and I. Vidana, Phys. Rev. C 84, 015208 (2011).

[24] A. Kumar and A. Mishra, Eur. Phys. J. A 47, 164 (2011).

[25] C. Garcia-Recio, J. Nieves, L. L. Salcedo and L. Tolos, Phys. Rev. C 85, 025203 (2012).

[26] S. Yasui, K. Sudoh, Phys. Rev. C 87, 015202 (2013).

[27] A. Hayashigaki, Phys. Lett. B 487, 96 (2000).

[28] K. Suzuki, P. Gubler, M. Oka, Pos Hadron2013, 179 (2014).

[29] K. Azzi, N. Er, H. Sundu, Eur. Phys. J. C 74, 3021 (2014).

# 1. Multi-flavor nucleus

## $\bar{D}$ (B) meson in nuclear matter

Quark-meson coupling model, QCD sum rules, hadronic interactions (mean-field approach, channel coupling, pion interaction), ...

Heavy quark symmetry

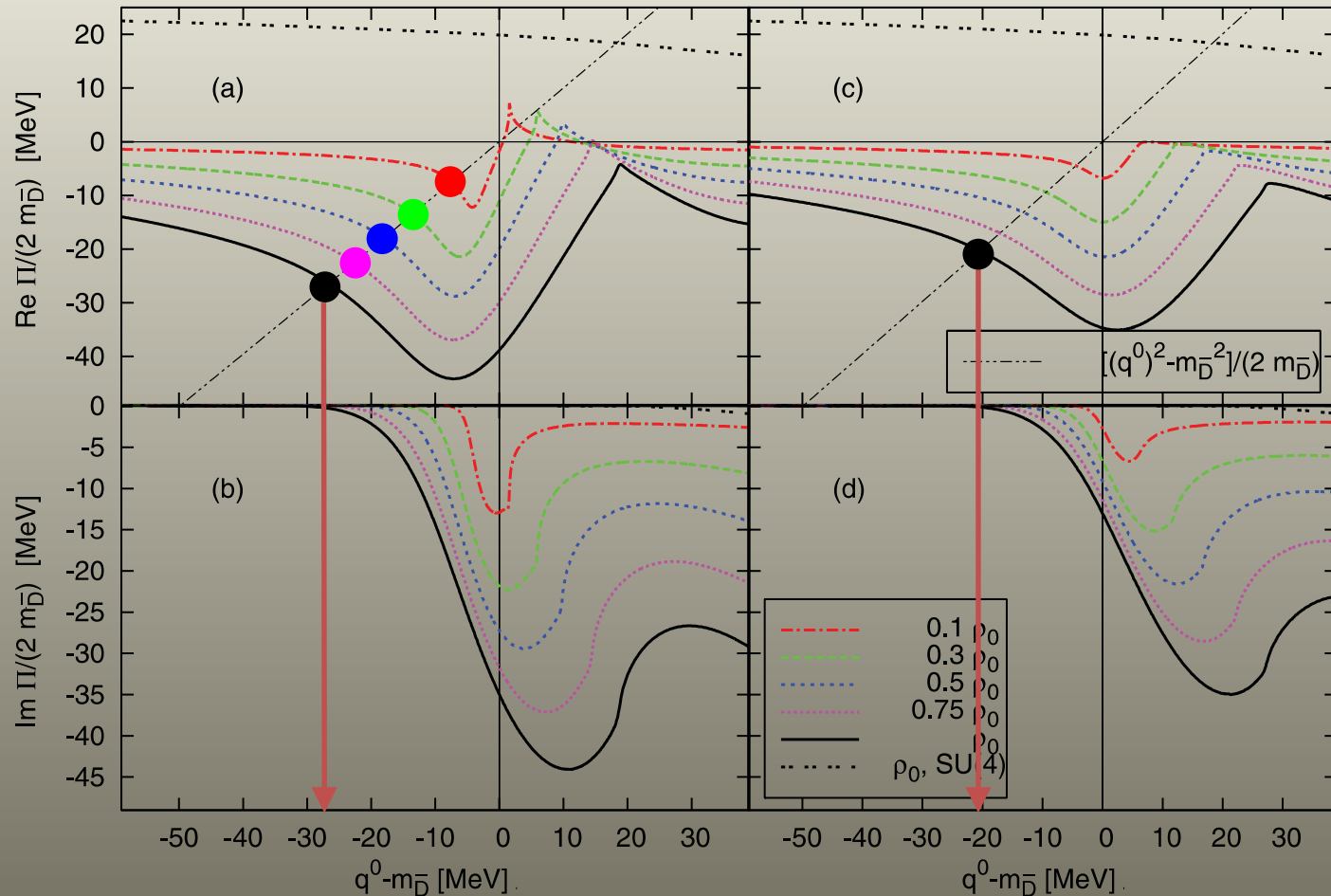
$$\bar{D}N \rightleftharpoons \bar{D}^*N$$

Hadronic model

C. Garcia-Recio, J. Nieves, L. L. Salcedo, L. Tolos, Phys. Rev. C 85, 025203 (2012)

$$\mu^2 = m_{th}^2 + M_{th}^2$$

$$\mu^2 = 1.2 (m_{th}^2 + M_{th}^2)$$



# 1. Multi-flavor nucleus

## $\bar{D}$ (B) meson in nuclear matter

Quark-meson coupling model, QCD sum rules, hadronic interactions (mean-field approach, channel coupling, pion interaction), ...

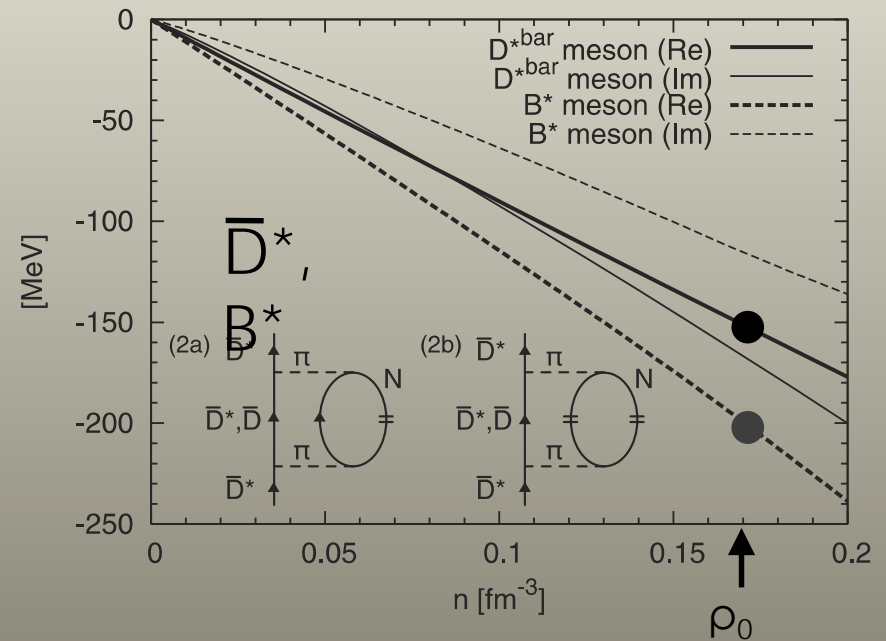
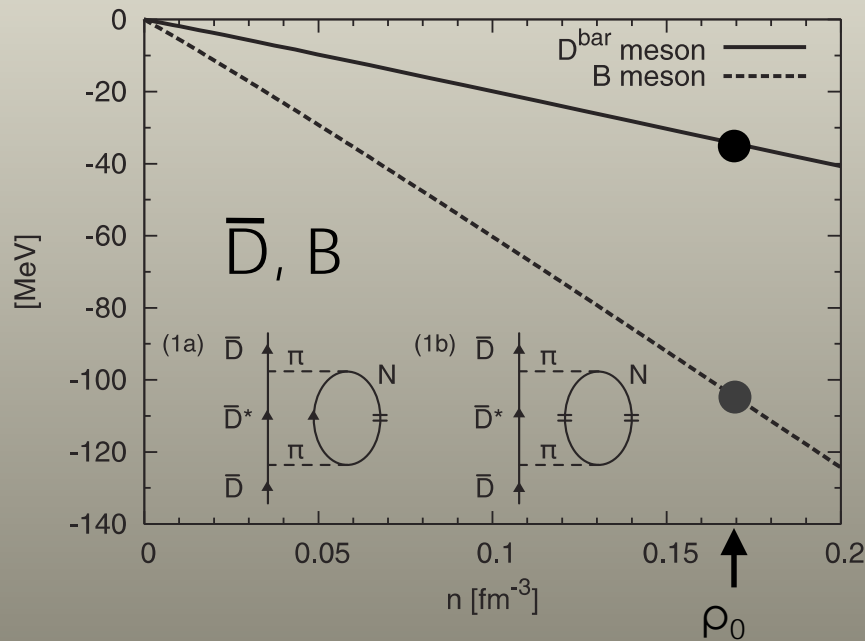
Heavy quark symmetry

$$\bar{D}N \rightleftharpoons \bar{D}^*N$$

Hadronic model

S. Y. , K. Sudoh, Phys Rev. C87, 015202 (2013)

$\pi$  meson exchange between  $\bar{D}$  ( $\bar{D}^*$ ) and N

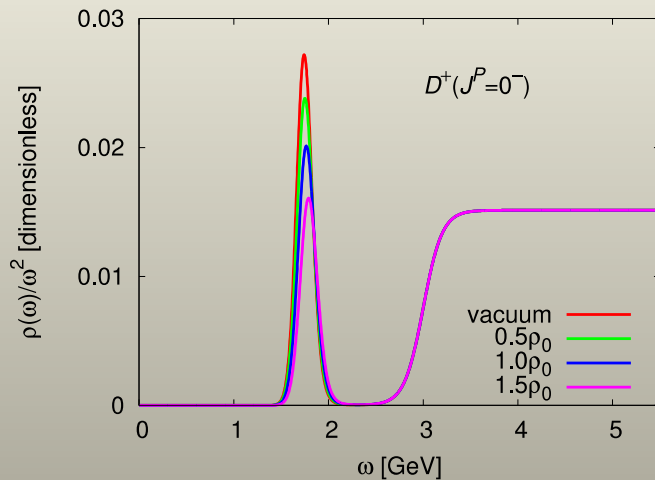


# 1. Multi-flavor nucleus

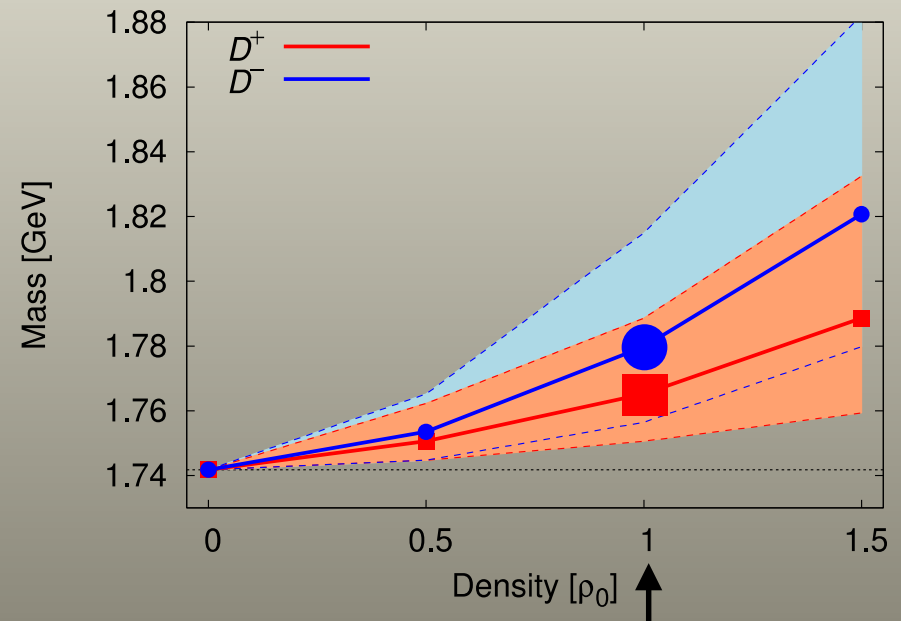
## $\bar{D}$ ( $B$ ) meson in nuclear matter

Quark-meson coupling model, QCD sum rules, hadronic interactions (mean-field approach, channel coupling, pion interaction), ...

### QCD sum rule



K. Suzuki, P. Gubler, M. Oka, arXiv:1511.04513 [hep-ph]



Cf. Quark confinement picture  
A. Park, P. Gubler, M. Harada, S. H. Lee, C. Nonaka,  
W. Park, arXiv:1602.01250 [nucl-th]

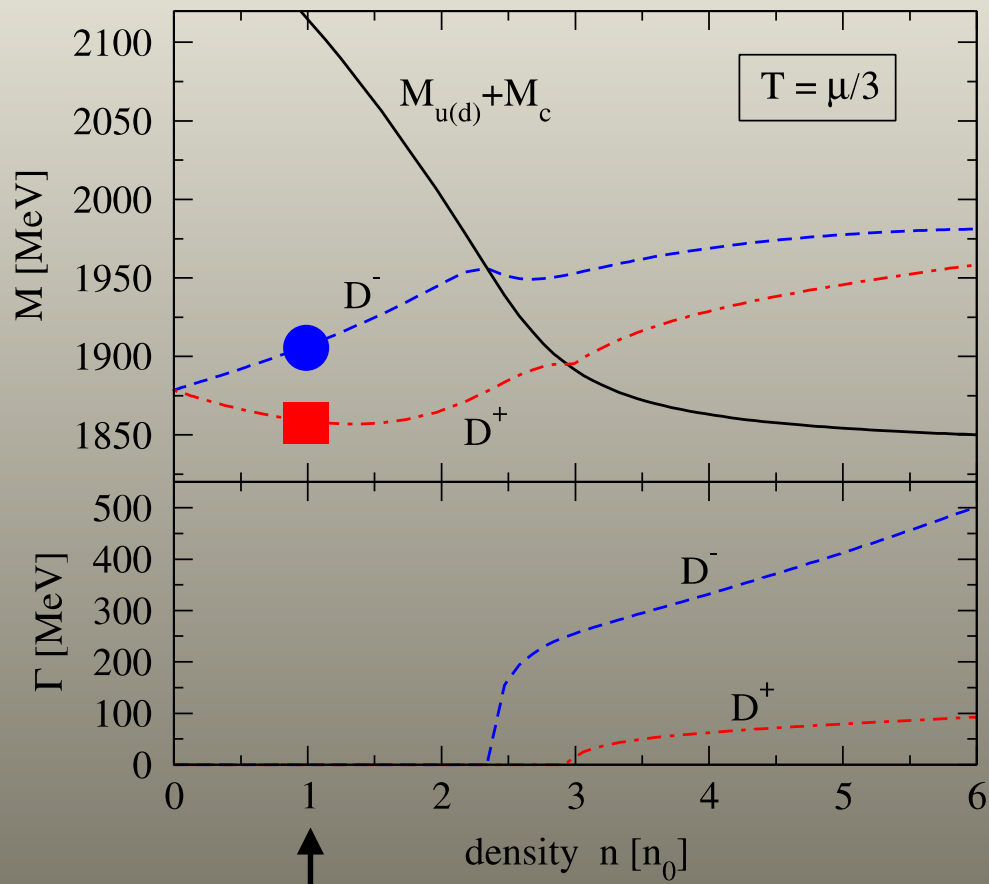
# 1. Multi-flavor nucleus

## $\bar{D}$ (B) meson in nuclear matter

Quark-meson coupling model, QCD sum rules, hadronic interactions (mean-field approach, channel coupling, pion interaction), ...

PNJL model

D. Blaschke, P. Costa, Y-L. Kalinovsky,  
Phys. Rev. D85, 034005 (2012)



# Contents

1. Multi-flavor nucleus
2. Heavy quark symmetry
3. Application 1: Leading order in  $1/m_Q$  expansion
4. Application 2: Next-to-Leading order in  $1/m_Q$  expansion
5. Conclusion

## 2. Heavy quark symmetry

Introduction to “velocity-frame”



$$p = m_Q v + k$$

$$v^2 = 1 \quad v^\mu = (1, 0, 0, 0)$$

Propagator:

$$\begin{aligned} & \frac{i}{\not{p} - m_Q + i\varepsilon} = \frac{i(\not{p} + m_Q)}{p^2 - m_Q^2 + i\varepsilon} \\ &= \frac{i(m_Q \not{v} + \not{k} + m_Q)}{(m_Q v + k)^2 - m_Q^2 + i\varepsilon} \\ &= \frac{i(m_Q \not{v} + \not{k} + m_Q)}{2m_Q v \cdot k + k^2 + i\varepsilon} \\ &= \frac{i(\not{v} + \not{k}/m_Q + 1)}{2v \cdot k + k^2/m_Q + i\varepsilon} \\ &= \frac{\not{v} + 1}{2} \frac{i}{v \cdot k + i\varepsilon} + \mathcal{O}(1/m_Q) \end{aligned}$$

## 2. Heavy quark symmetry

$$\mathcal{L}_{\text{heavy quark}} = \bar{Q}(i\not{D} - m_Q)Q \quad D_\mu = \partial_\mu - igA_\mu^a T^a$$

$\downarrow$  **1/m<sub>Q</sub> expansion**  
 (positive energy state Q<sub>v</sub> with velocity v)

$$Q_v = e^{im_Q v \cdot x} \frac{1 + \not{v}}{2} Q$$

Manohar, Wise, Luke, Grinstein, ...

$$\mathcal{L}_{\text{HQET}} = \boxed{\bar{Q}_v v \cdot iD Q_v} + \bar{Q}_v \frac{(iD_\perp)^2}{2m_Q} Q_v - g_s \bar{Q}_v \frac{\sigma_{\mu\nu} G^{\mu\nu}}{4m_Q} Q_v + \mathcal{O}(1/m_Q^2)$$

LO

$$\gamma^\mu \rightarrow \frac{1 + \not{v}}{2} \gamma^\mu \frac{1 + \not{v}}{2} = v^\mu \frac{1 + \not{v}}{2} \rightarrow v^\mu$$



Heavy quark spin in  $m_Q \rightarrow \infty$  is conserved.

# Heavy quark symmetry (HQS)



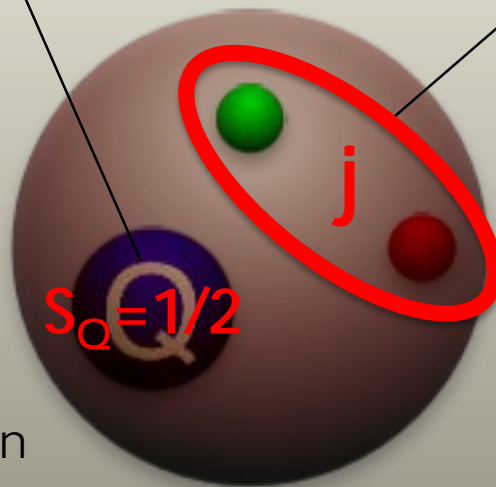
## 2. Heavy quark symmetry

# Heavy quark symmetry (HQS)

Normal hadrons, exotic hadrons, hadronic molecules, exotic nuclei, ...

Heavy quark spin × Light quark and gluon total spin

*Brown muck*  
(Spin-complex)



Heavy hadron

small spin-spin ( $S_Q \cdot j$ ) interaction  
 $\sim \Lambda_{\text{QCD}}/m_Q \ll 1$



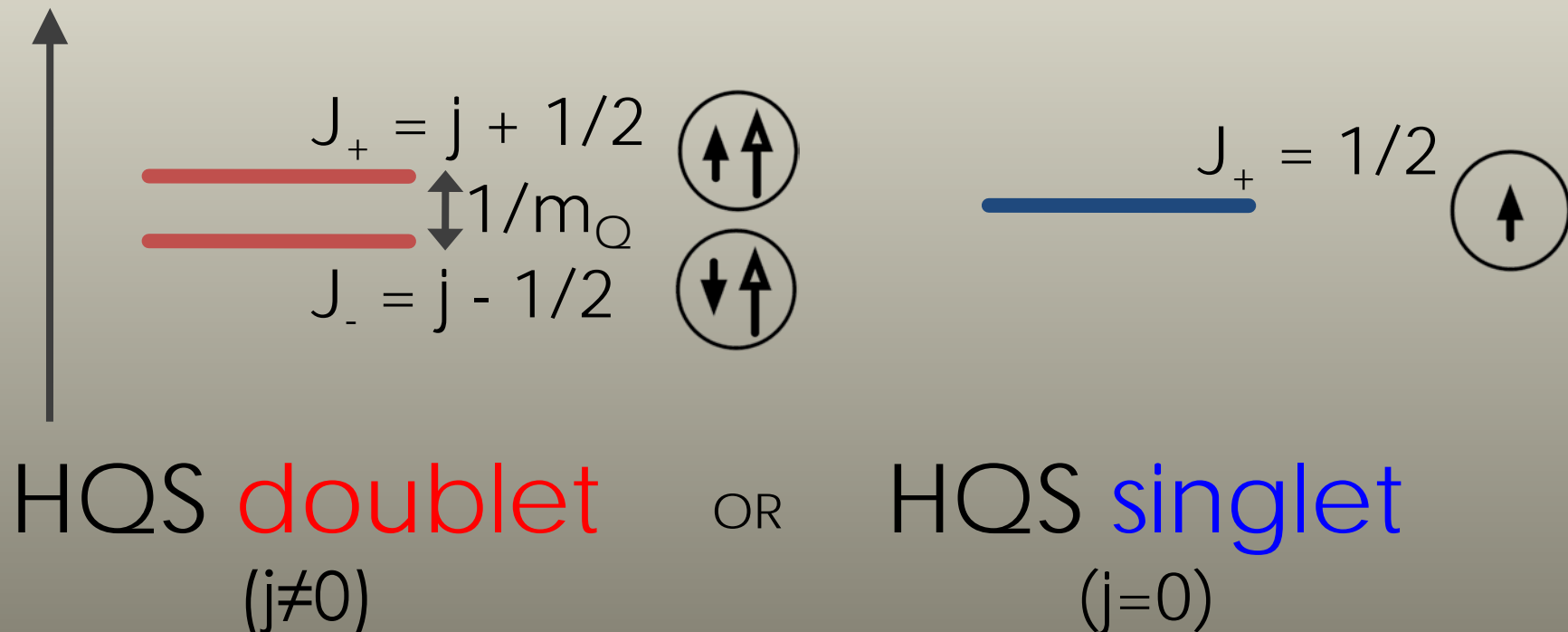
Total spin =  $j \pm 1/2$ : degenerate

## 2. Heavy quark symmetry

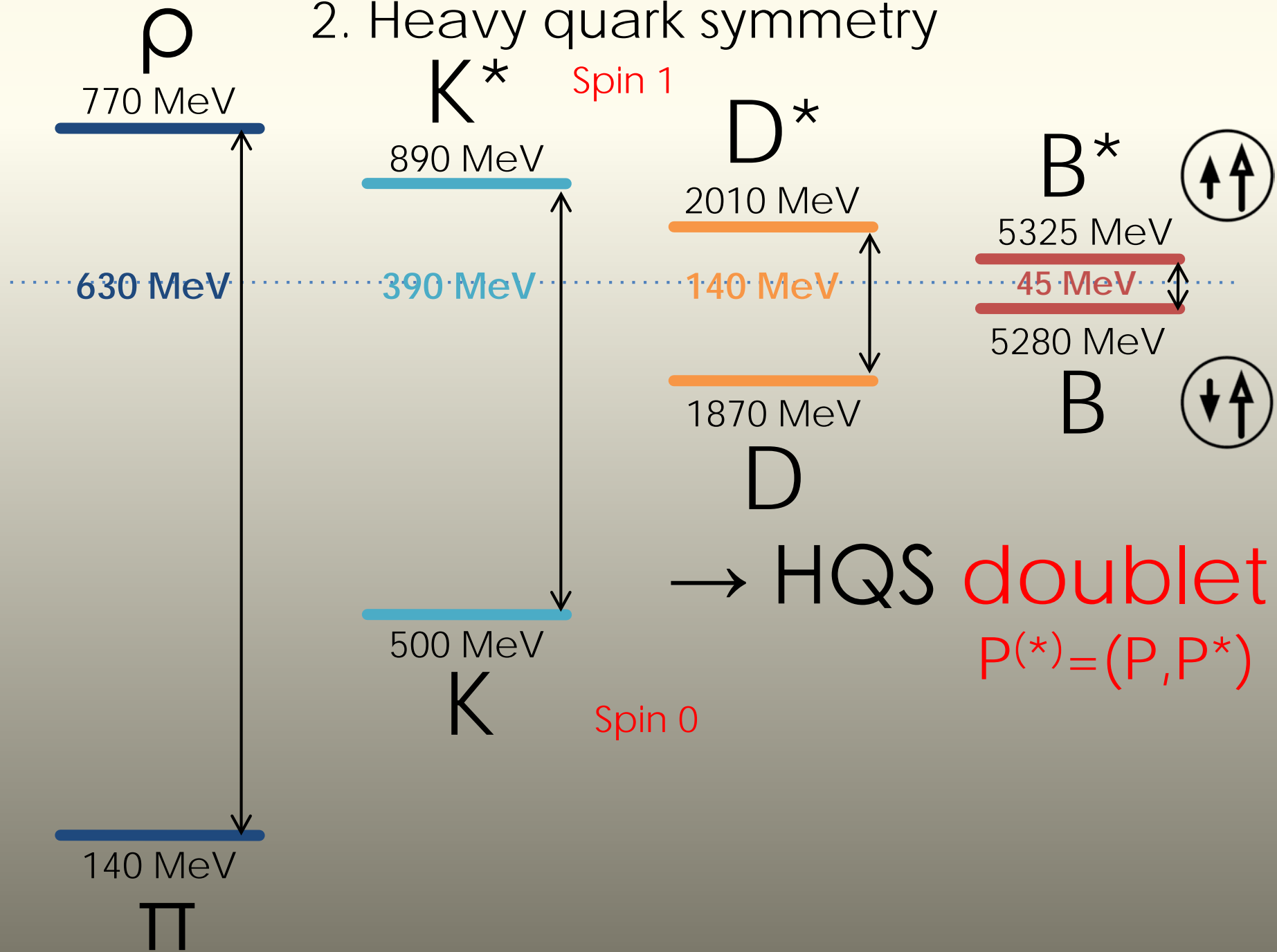
# Heavy quark symmetry (HQS)

Normal hadrons, exotic hadrons, hadronic molecules, exotic nuclei, ...

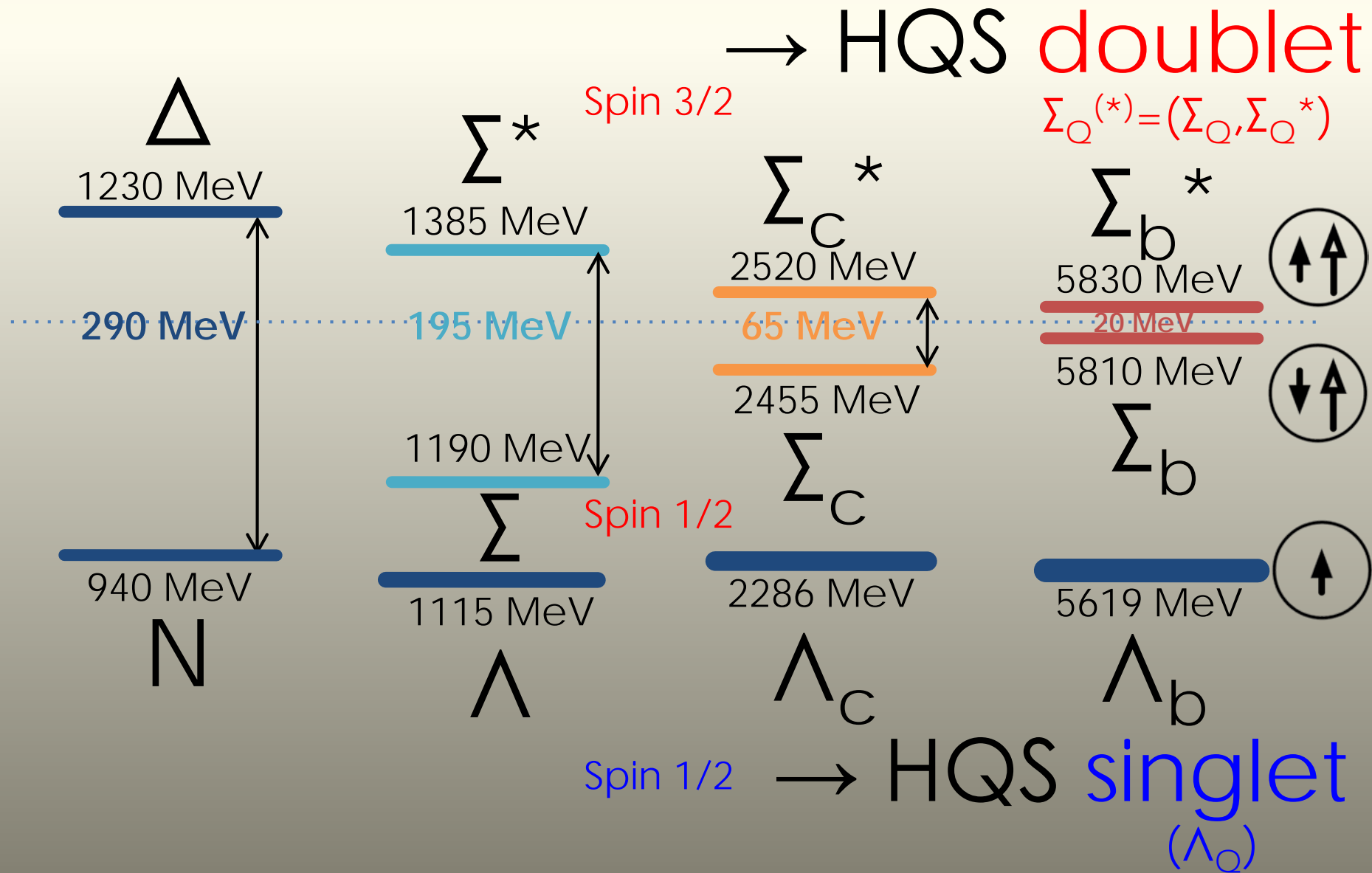
Hadron mass



## 2. Heavy quark symmetry

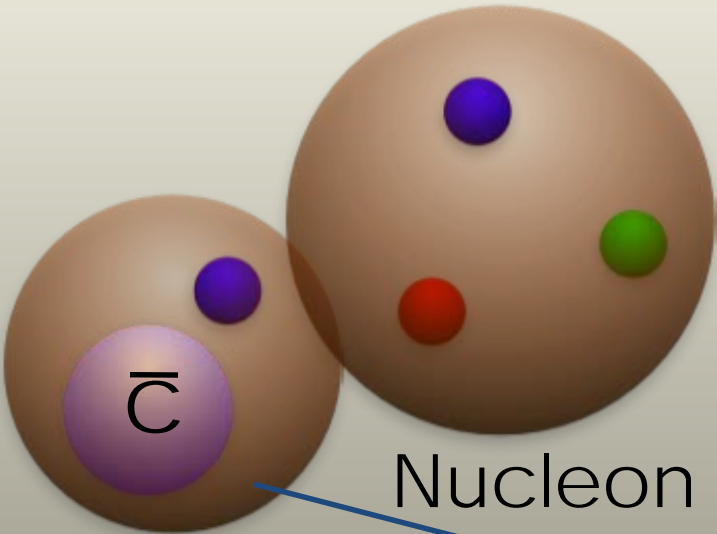


## 2. Heavy quark symmetry



# Question

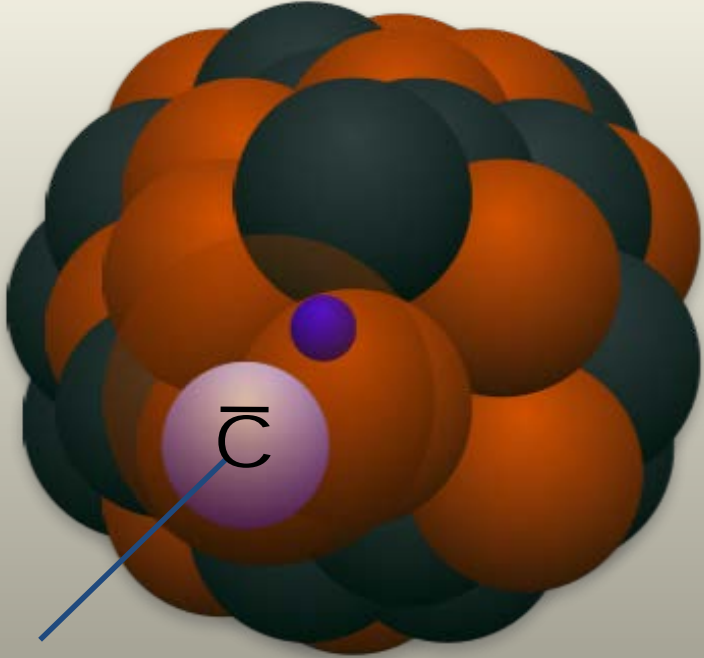
Charm (bottom) exotic hadrons and nuclei



Nucleon

$\bar{D}$  meson

Hadronic molecule (A=1)



Nucleus (A: large)

Answer

HQS doublet or singlet?  
HQS doublet!!

### 3. Application 1: Leading order in $1/m_Q$ expansion

Heavy **hadron** effective theory

**LO** in  $1/m_Q$  expansion

### 3. Application 1: Leading order in $1/m_Q$ expansion

$$Q\bar{q}$$


A diagram showing a quark  $Q$  and an antiquark  $\bar{q}$ . Below the  $Q$  are two red arrows: one pointing up and one pointing down. Below the  $\bar{q}$  is a black arrow pointing up.

$$P^{(*)} = P^* \begin{matrix} \uparrow \uparrow \\ 1^- \end{matrix} \quad \text{or} \quad P \begin{matrix} \downarrow \uparrow \\ 0^- \end{matrix}$$

same mass

$$Q=b \quad \bar{B}^{**} \quad \bar{B}$$

### 3. Application 1: Leading order in $1/m_Q$ expansion

$Q\bar{q}$

$$H_v(x) = \frac{1 + \psi}{2} \left[ \frac{1 + \psi}{2} P_{1^-}^*(x) + i\gamma_5 \frac{1 + \psi}{2} P_{0^-}(x) \right] P_v$$

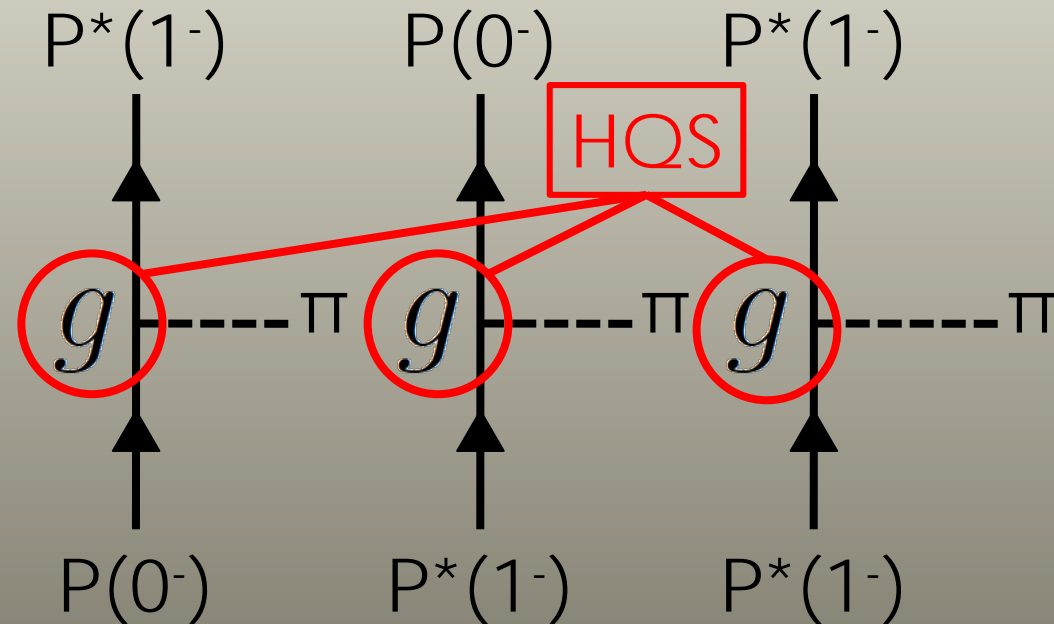


### 3. Application 1: Leading order in $1/m_Q$ expansion

Interaction of  $P(0^-)$ ,  $P^*(1^-)$  meson and pion field with chiral symmetry + HQS

$$\mathcal{L}_{\text{HMET}}^{(0)} = \underbrace{-\text{Tr} \bar{H}_v v \cdot i D H_v}_{\text{kinetic term}} + \underbrace{g \text{Tr} \bar{H}_v H_v \gamma_\mu \gamma_5 A^\mu}_{\text{interaction with pion}} + \mathcal{O}(1/M)$$

$A_\mu = -\partial_\mu \pi$

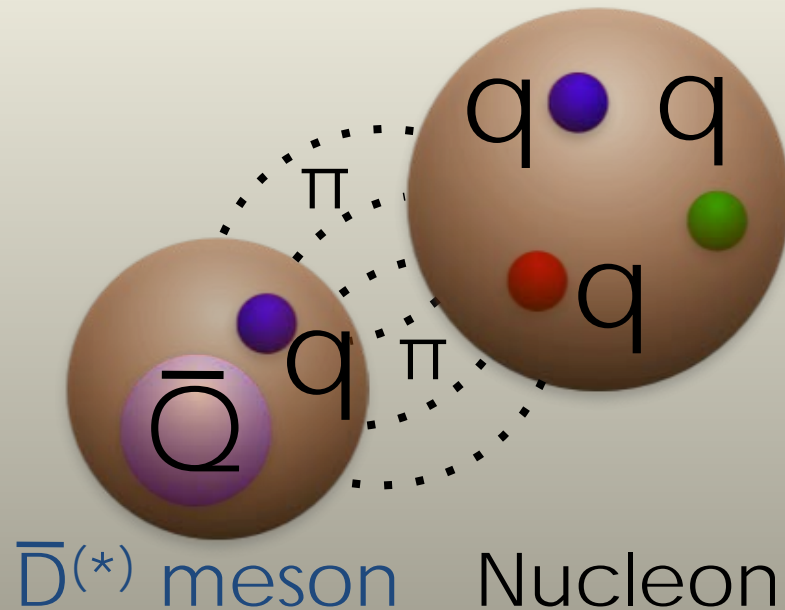


H.Georgi, Phys. Lett. B240, 447 (1990)

A.F.Falk, H.Georgi, B.Grinstein, Nucl. Phys. B343, 1 (1990)

### 3. Application 1: Leading order in $1/m_Q$ expansion

$$\bar{Q}q = \bar{P}^{(*)}$$



Hadronic molecule

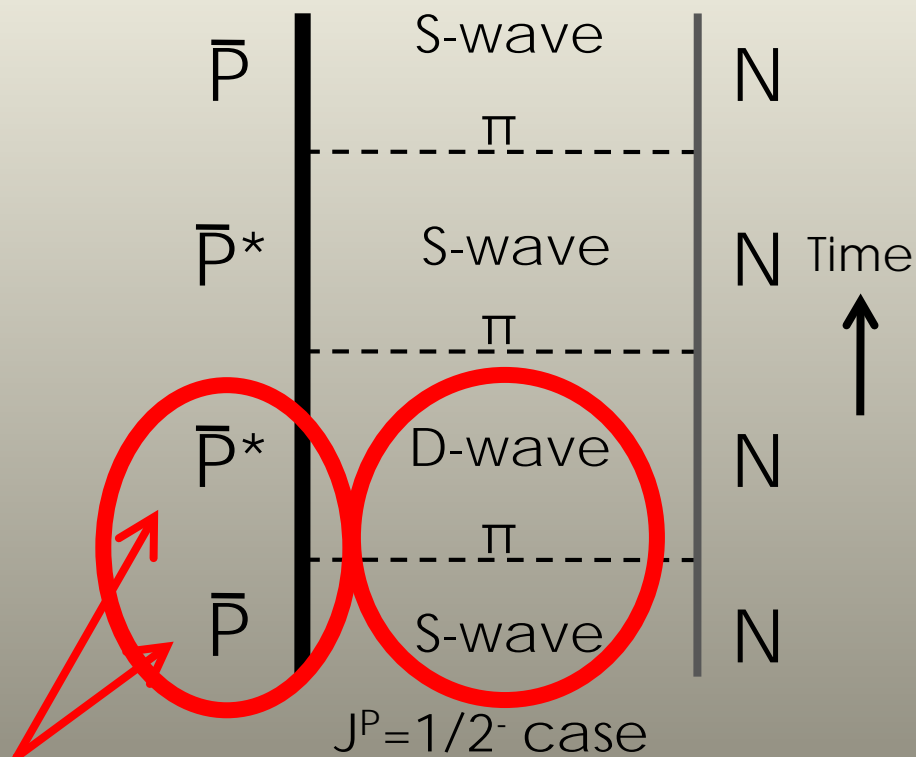
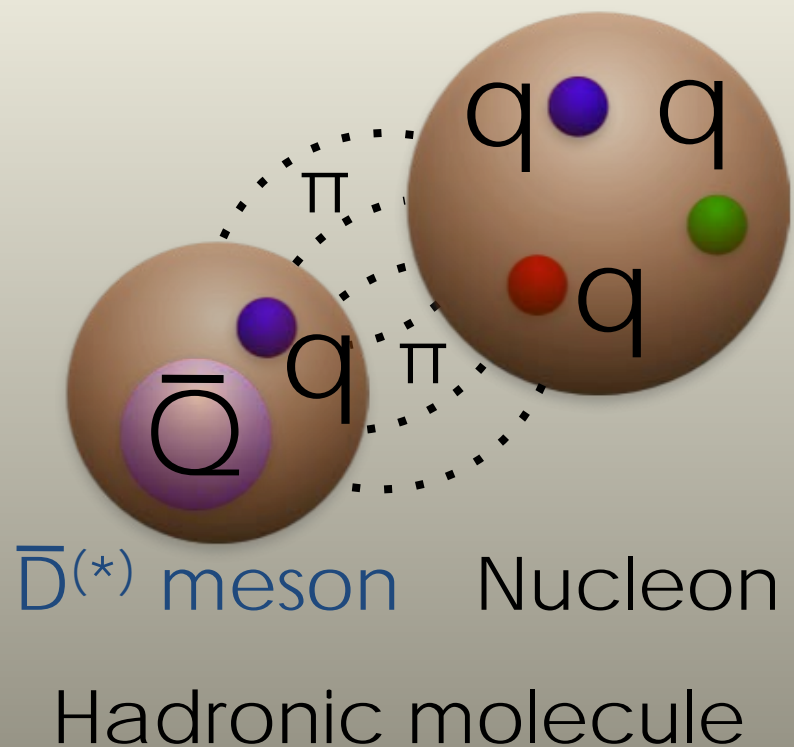
① No *quark-antiquark* annihilation  
(very simple system!)

② Relation for interaction vertices:  
 $g_{PP^*\pi} = g_{P^*P^*\pi}$  (heavy quark symmetry)

HQS **doublet** or **singlet**?

### 3. Application 1: Leading order in $1/m_Q$ expansion

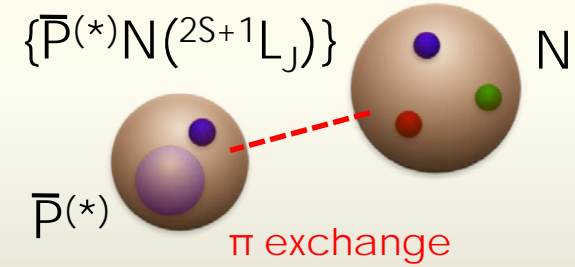
$$\bar{Q}q = \bar{P}^{(*)} \quad \vdots$$



$\bar{P}(0^-) - \bar{P}^*(1^-)$  mixing are important!  
 (mixing of S-wave and D-wave, like in deuteron)

# 3. Application 1: Leading order in $1/m_Q$ expansion

$$J^P = 1/2^-, 3/2^-$$



$$J^P = 1/2^- : \{\bar{P}N(2S_{1/2}), \bar{P}^*N(2S_{1/2}), \bar{P}^*N(4D_{1/2})\}$$

HQS singlet

$$H_{1/2^-} = \begin{pmatrix} K_0 & \sqrt{3}C & -\sqrt{6}T \\ \sqrt{3}C & K_0 - 2C & -\sqrt{2}T \\ -\sqrt{6}T & -\sqrt{2}T & K_2 + (C - 2T) \end{pmatrix} \rightarrow \begin{pmatrix} K_0 - 3C & 0 & 0 \\ 0 & K_0 + C & -2\sqrt{2}T \\ 0 & -2\sqrt{2}T & K_2 + (C - 2T) \end{pmatrix}$$

Unitary transformation  
(Heavy quark + Brown muck)

**HQS doublet**  
(tensor potential)

$$J^P = 3/2^- : \{\bar{P}N(2D_{3/2}), \bar{P}^*N(4S_{3/2}), \bar{P}^*N(4D_{3/2}), \bar{P}^*N(2D_{3/2})\}$$

$$H_{3/2^-} = \begin{pmatrix} K_2 & \sqrt{3}T & -\sqrt{3}T & \sqrt{3}C \\ \sqrt{3}T & K_0 + C & 2T & T \\ -\sqrt{3}T & 2T & K_2 + C & -T \\ \sqrt{3}C & T & -T & K_2 - 2C \end{pmatrix} \rightarrow \begin{pmatrix} K_0 + C & 2\sqrt{2}T & 0 & 0 \\ 2\sqrt{2}T & K_2 + (C - 2T) & 0 & 0 \\ 0 & 0 & K_2 - 3C & 0 \\ 0 & 0 & 0 & K_2 + (C + 2T) \end{pmatrix}$$

Unitary transformation  
(Heavy quark + Brown muck)

$K_L$ : kinetic term

(angular momentum L)

C: central potential

T: tensor potential

1/2<sup>-</sup> and 3/2<sup>-</sup> are degenerate in mass.

**HQS doublet**

### 3. Application 1: Leading order in $1/m_Q$ expansion

$\bar{P}^{(*)}N$

Mass

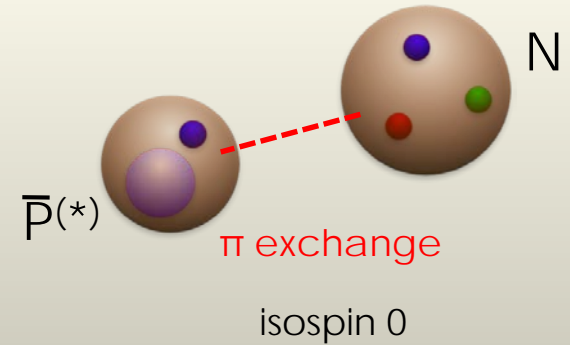
$\bar{D}^*N$  142 MeV

$B^*N$  46 MeV

$\bar{D}N$  0 MeV

$BN$  0 MeV

$\bar{P}N, \bar{P}^*N$  0 MeV

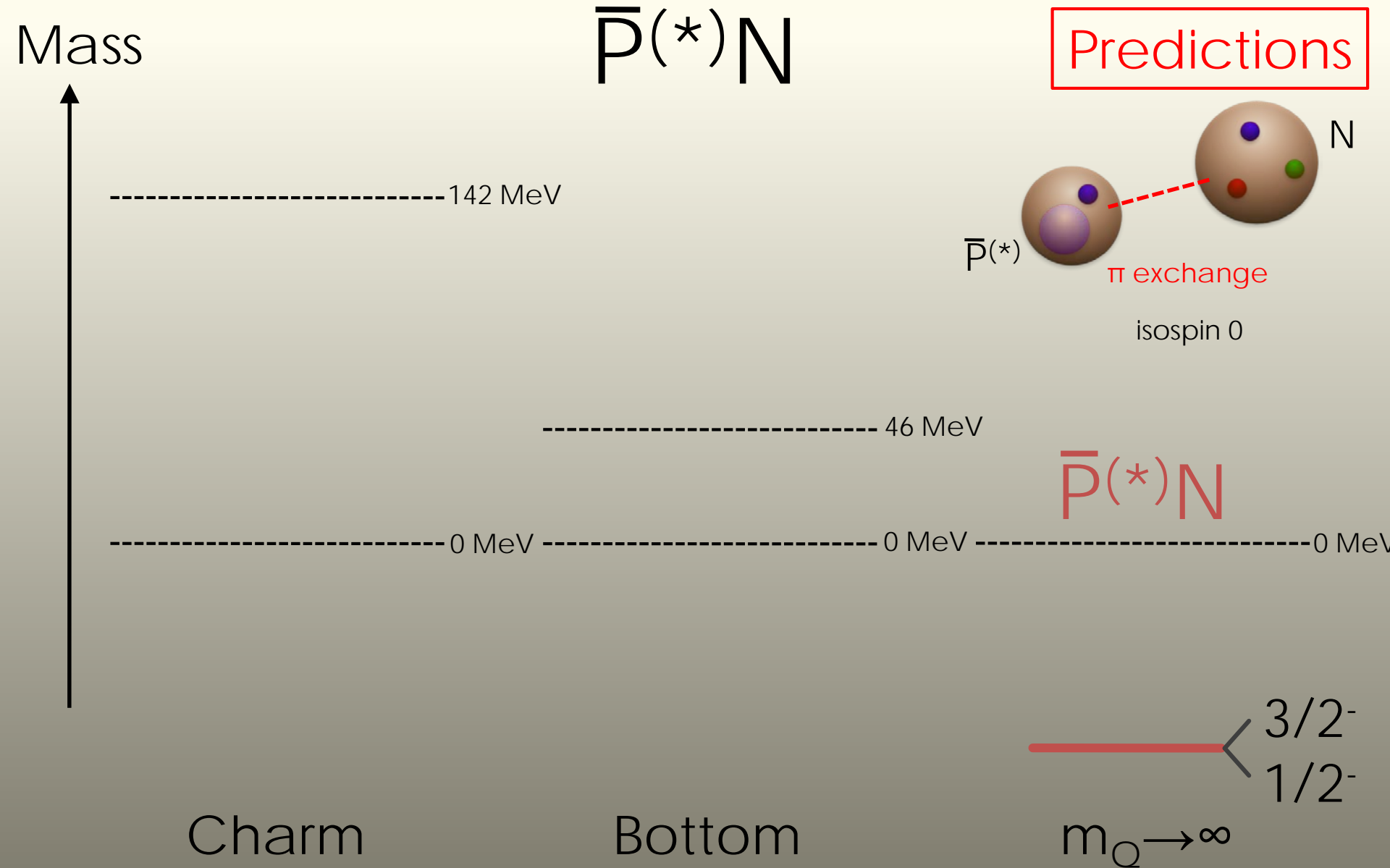


Charm

Bottom

$m_Q \rightarrow \infty$

### 3. Application 1: Leading order in $1/m_Q$ expansion



### 3. Application 1: Leading order in $1/m_Q$ expansion

Mass

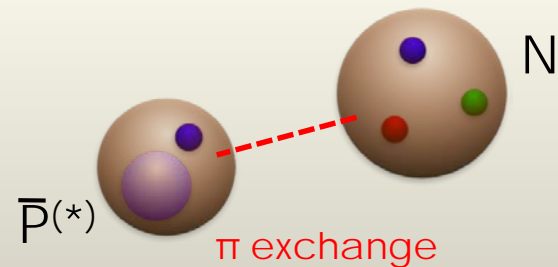
$\bar{P}^{(*)}N$

Predictions

$\bar{D}^{(*)}N$

----- 142 MeV

3/2<sup>-</sup>



$\pi$  exchange

isospin 0

Feshbach resonance ( $\Gamma=18$  MeV)

$J^P=3/2^- : \{\bar{P}N(^2D_{3/2}), \bar{P}^*N(^4S_{3/2}), \bar{P}^*N(^4D_{3/2}), \bar{P}^*N(^2D_{3/2})\}$

----- 0 MeV

3/2<sup>-</sup>

----- 0 MeV

----- 0 MeV

1/2<sup>-</sup>

1/2<sup>-</sup>

HQS doublet

3/2<sup>-</sup>

1/2<sup>-</sup>

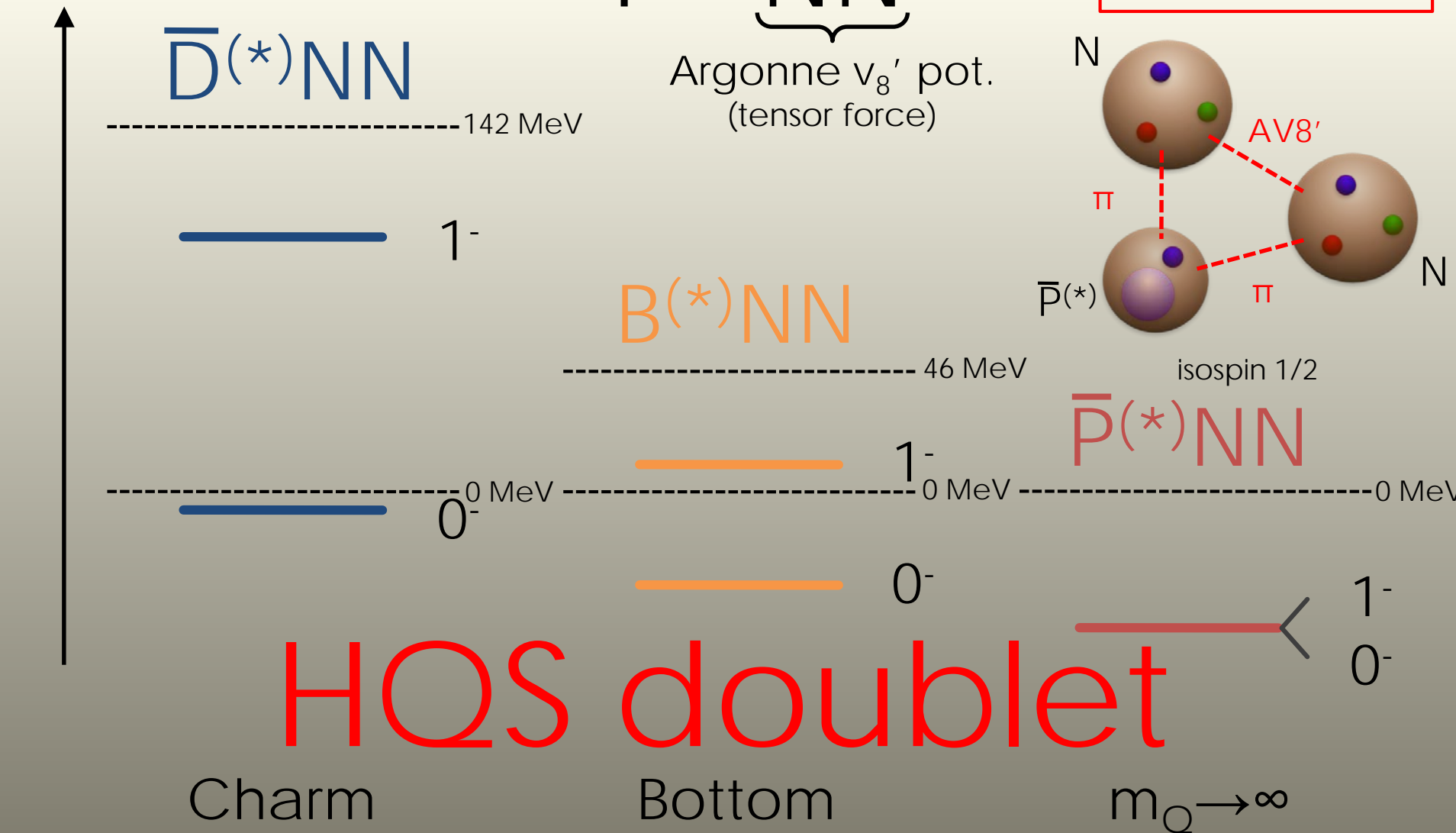
Charm

Bottom

$m_Q \rightarrow \infty$

### 3. Application 1: Leading order in $1/m_Q$ expansion

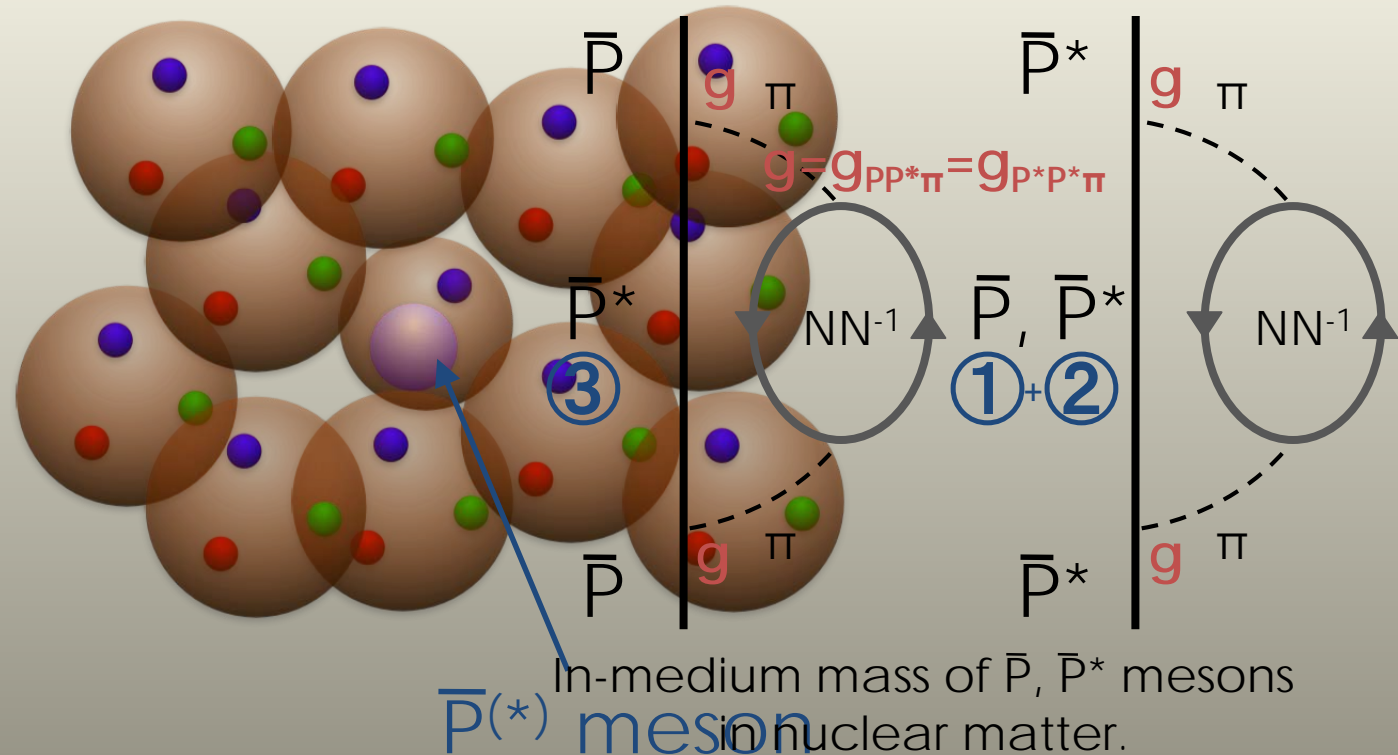
Mass





### 3. Application 1: Leading order in $1/m_Q$ expansion

## $\bar{P}^{(*)}$ in nuclear matter



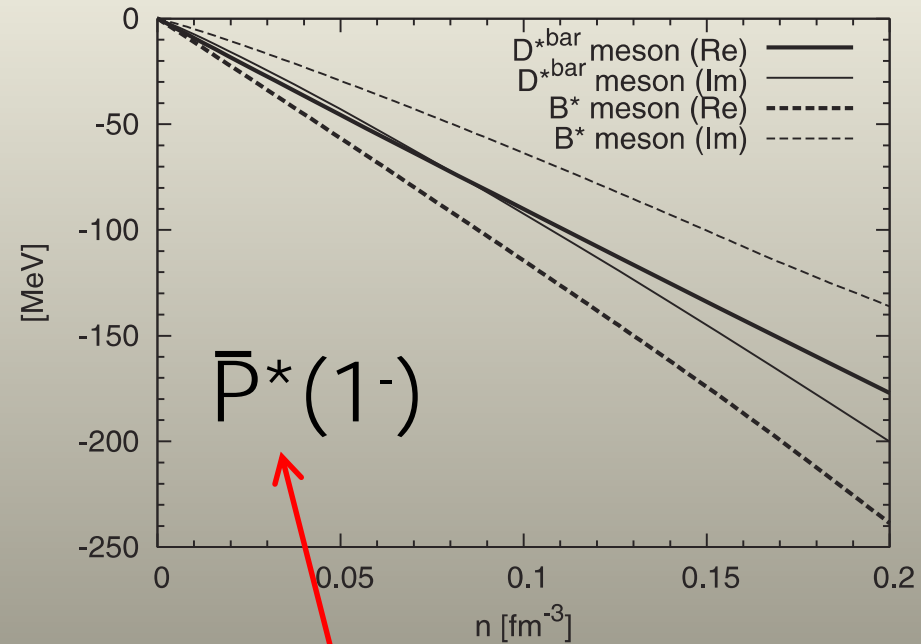
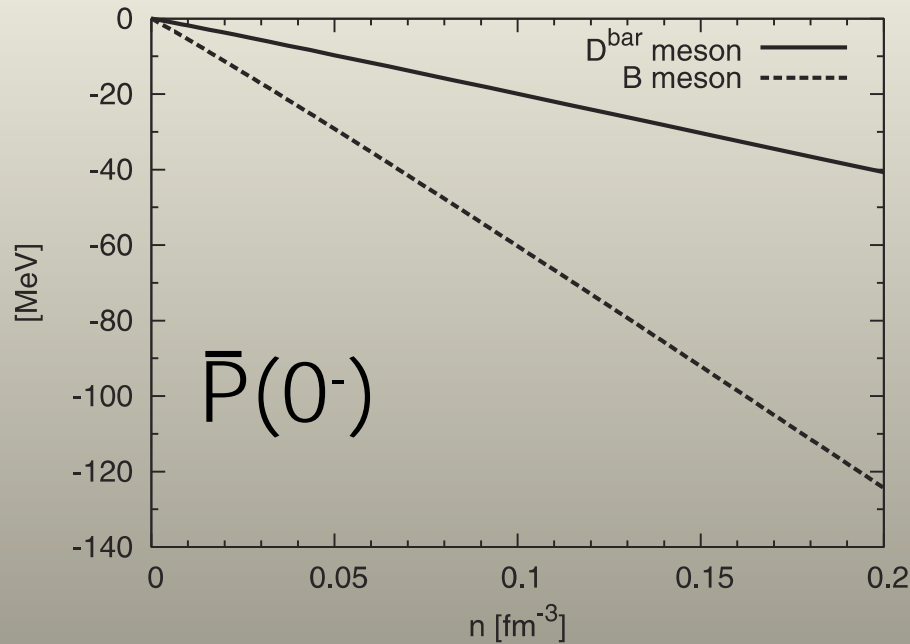
~~$$\text{Mass}(\bar{P}) = \text{Mass}(\bar{P}^*)$$~~

Cf. HQS [singlet](#) in "pion condensate" (Suenaga, He, Ma, Harada, PRC89, 068201 (2014))

### 3. Application 1: Leading order in $1/m_Q$ expansion

Numerical results for cutoff momentum 800 MeV

$P(0^-)$ ,  $P^*(1^-)$  self-energy in nuclear medium



1. Imaginary parts
2. Large mass drop

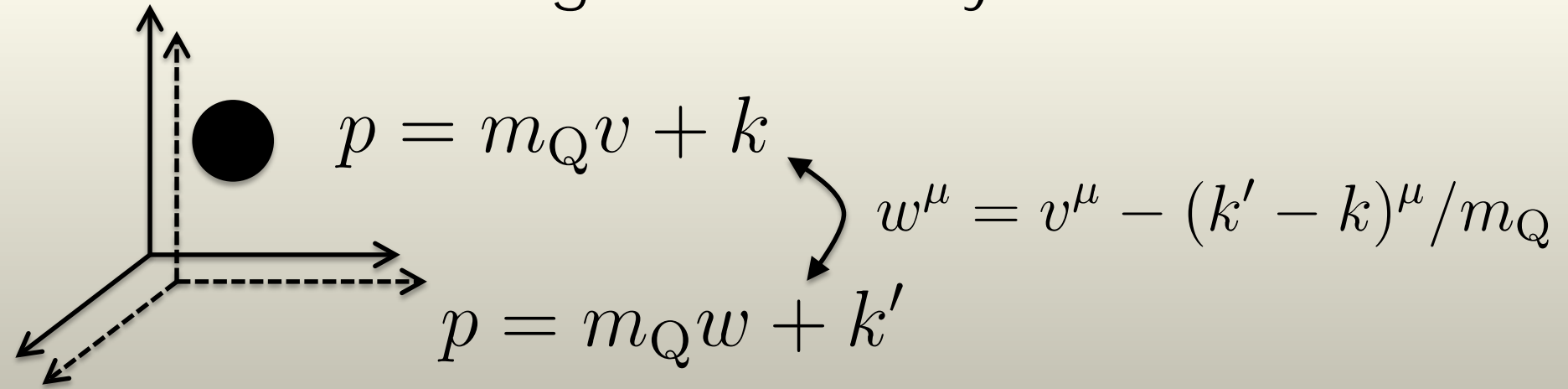
## 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

$1/m_Q$  expansion

LO + NLO

# 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

Change of "velocity-frame"



velocity-rearrangement

Effective field

$$v \rightarrow v + q/m_Q \quad \Rightarrow \quad Q_v \rightarrow e^{iq \cdot x} \left( 1 + \frac{\not{q}}{2m_Q} \right) Q_v$$

Ex. Heavy Quark Effective Theory

$$\mathcal{L}_0 = \bar{Q}_v i v \cdot D Q_v \quad \mathcal{L}_1 = \bar{Q}_v \frac{(iD_\perp)^2}{2m_Q} Q_v - g_s \bar{Q}_v \frac{\sigma_{\mu\nu} G^{\mu\nu}}{4m_Q} Q_v$$

$$\mathcal{L}_0 \rightarrow \mathcal{L}_0 + \frac{1}{m_Q} \bar{Q}_v i q \cdot D Q_v \quad \mathcal{L}_1 \rightarrow \mathcal{L}_1 - \frac{1}{m_Q} \bar{Q}_v i q \cdot D Q_v$$

$L_0 + L_1$ : invariant

# 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

Heavy hadron mass "parametrization"

$$M_H(\rho) = m_Q + \Lambda(\rho) + \frac{\lambda_1(\rho)}{2m_Q} + 4\vec{S} \cdot \vec{j} \frac{\lambda_2(\rho; m_Q)}{2m_Q} + \mathcal{O}(1/m_Q^2)$$

$\rho$ : nuclear matter density

at NLO

$$\frac{\lambda_1(\rho)}{m_Q} = - \langle H_{v_r}(\rho) | \bar{Q}_{v_r} g_s \vec{x} \cdot \vec{E} Q_{v_r} | H_{v_r}(\rho) \rangle$$

M. Neubert, Phys. Lett. B322, 419 (1994)

Color electric gluon

$$8\vec{S} \cdot \vec{j} \lambda_2(\rho; m_Q) = \frac{1}{2} c(\mu) \langle H_{v_r}(\rho) | \bar{Q}_{v_r} g_s \vec{\sigma} \cdot \vec{B} Q_{v_r} | H_{v_r}(\rho) \rangle$$

Color magnetic gluon

"Non-perturbative" gluon

## 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

Can we calculate hadron w.f.  
in nuclear medium from **QCD**?

Very difficult, but...

## 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

$$M_H(\rho) = m_Q + \bar{\Lambda}(\rho) - \frac{\lambda_1(\rho)}{2m_Q} + 4\vec{S} \cdot \vec{j} \frac{\lambda_2(\rho; m_Q)}{2m_Q} + \mathcal{O}(1/m_Q^2)$$

Heavy **hadron** effective theory

LO + NLO

$1/m_Q$  expansion in **quark**  $\Leftrightarrow$   $1/M$  expansion in **hadron**

$$M = m_Q + \bar{\Lambda}(\rho) - \frac{\lambda_1(\rho)}{2m_Q} + 4\vec{S} \cdot \vec{j} \frac{\lambda_2(\rho; m_Q)}{2m_Q} + \mathcal{O}(1/m_Q^2)$$

Question: what is NLO?

# 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

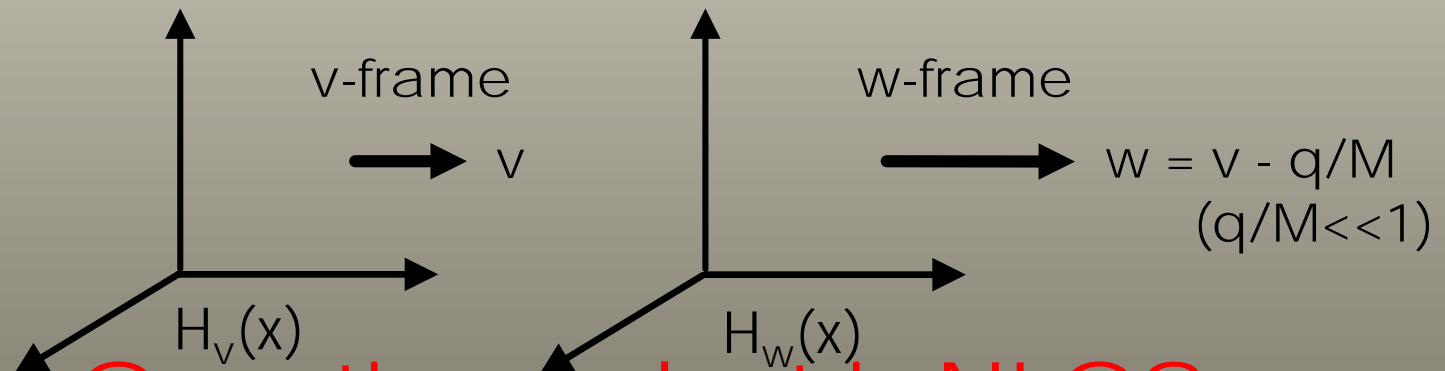
## How to construct effective Lagrangian?

1. Heavy quark symmetry is conserved at  $O(1)$ .



2. Invariance under Lorentz boost at  $O(1)+O(1/M)$ .

Luke, Manohar, PLB286, 348 (1992), Kitazawa, Kurimoto, PLB323, 65 (1994)



Question: what is NLO?

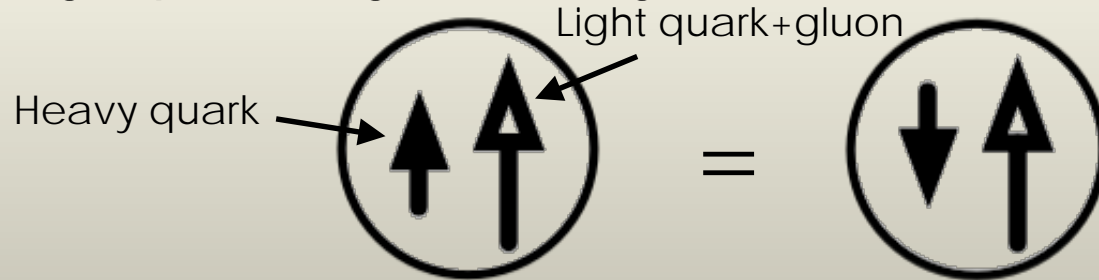
Lorentz boost (velocity-rearrangement)



## 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

# How to construct effective Lagrangian?

1. Heavy quark symmetry is conserved at  $O(1)$ .



2. Invariance under Lorentz boost at  $O(1)+O(1/M)$ .

Luke, Manohar, PLB286, 348 (1992), Kitazawa, Kurimoto, PLB323, 65 (1994)

3. Heavy quark symmetry breaking terms at  $O(1/M)$ .



# 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

Kitazawa, Kurimoto, PLB323, 65 (1994)

Heavy meson effective theory with  $1/M$  corrections

$\bar{P}(0^-), \bar{P}^*(1^-)$



$\Pi$

$g$  (LO),  $g/M$ ,  $g_1/M$ ,  $g_2/M$  (NLO)

$\bar{P}(0^-), \bar{P}^*(1^-)$

$$\mathcal{L}_{\text{HMET}}^{\text{LO+NLO}} = -\text{Tr} \bar{\mathcal{H}}_v v \cdot i D \mathcal{H}_v + \frac{\lambda}{M} \text{Tr} \bar{\mathcal{H}}_v \sigma^{\mu\nu} \mathcal{H}_v \sigma_{\mu\nu} \text{spin-flip } (1/M)$$

$$+ \left( g + \frac{g_1}{M} \right) \text{Tr} \bar{\mathcal{H}}_v \mathcal{H}_v \gamma_\mu \gamma_5 A^\mu + \frac{g_2}{M} \text{Tr} \bar{\mathcal{H}}_v \gamma_\mu \gamma_5 \mathcal{H}_v A^\mu$$

$$+ \mathcal{O}(1/M^2)$$

"Covariant" field for velocity-rearrangement

$$\mathcal{H}_v = H_v + \frac{1}{2M} (i \overleftrightarrow{D} H_v - H_v i \overleftarrow{D} - 2v i D H_v) + \mathcal{O}(1/M^2)$$

# 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

$$M_H(\rho) = m_Q + \bar{\Lambda}(\rho) - \frac{\lambda_1(\rho)}{2m_Q} + 4\vec{S} \cdot \vec{j} \frac{\lambda_2(\rho; m_Q)}{2m_Q} + \mathcal{O}(1/m_Q^2)$$

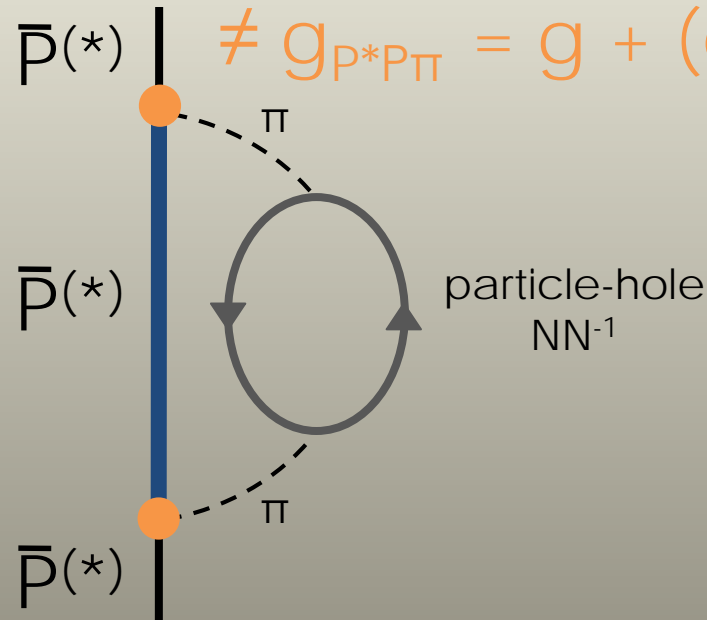
$\bar{p}^{(*)}$  with breaking of HOs

$$g_{P^*P^*\pi} = g + (g_1 + g_2)/M$$

$$\neq g_{P^*P\pi} = g + (g_1 - g_2)/M$$

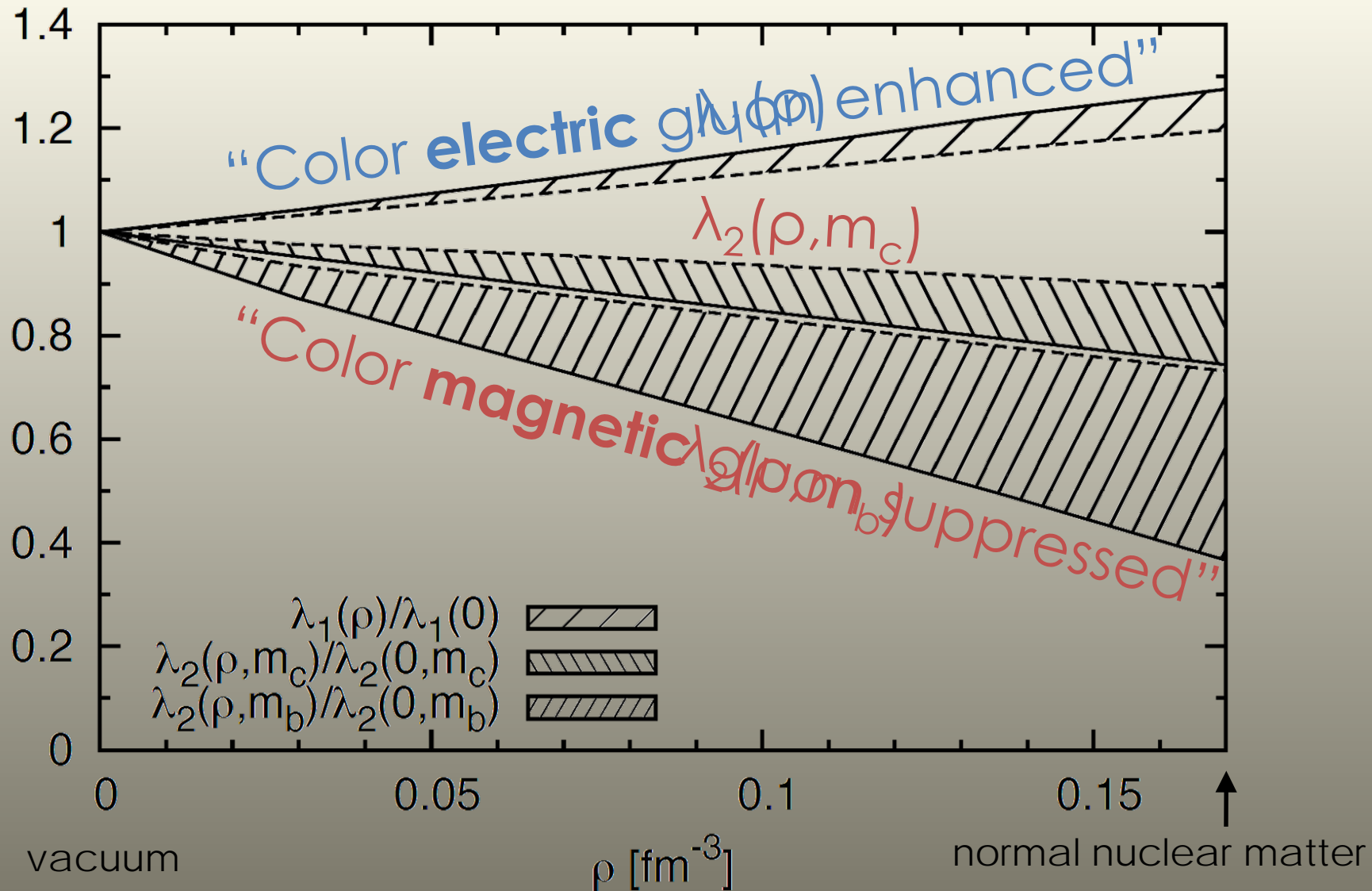
$$M_{P^*} = M - 2\lambda/M$$

$$\neq M_P = M + 6\lambda/M$$

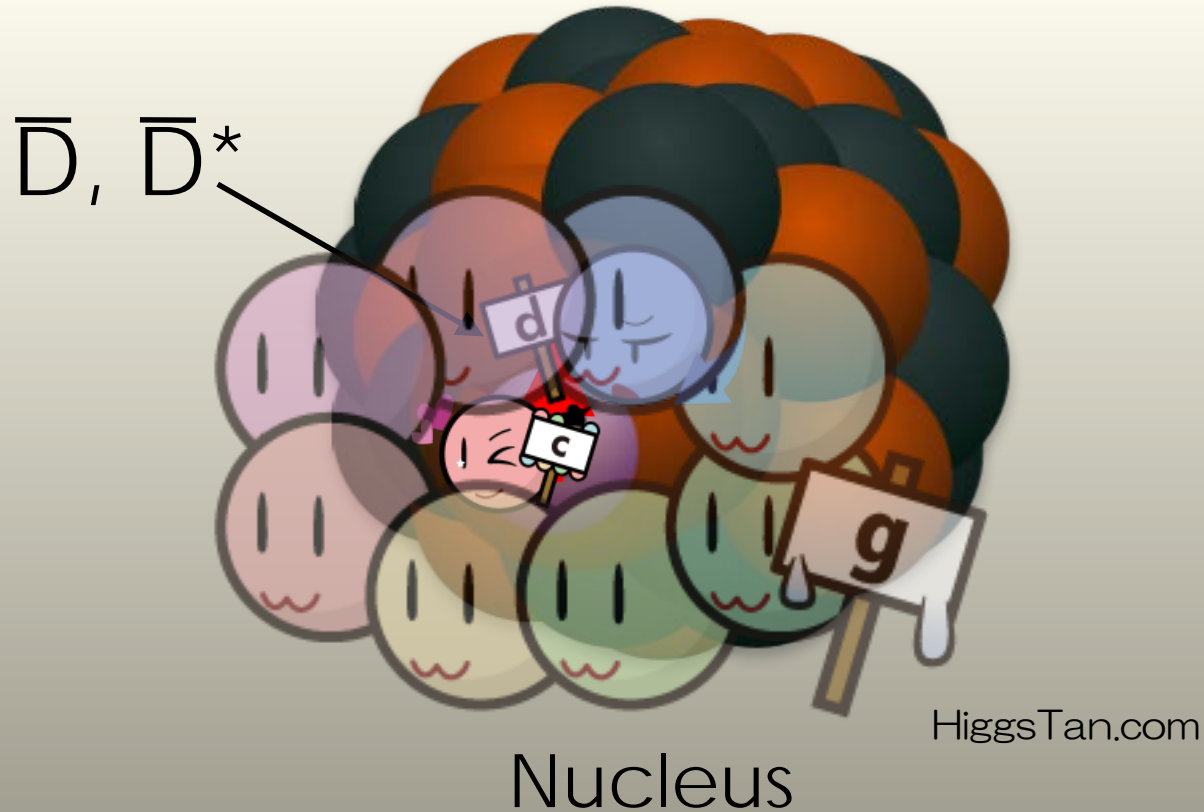


# 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion

$$M_H(\rho) = m_Q + \bar{\Lambda}(\rho) - \frac{\lambda_1(\rho)}{2m_Q} + 4\vec{S} \cdot \vec{j} \frac{\lambda_2(\rho; m_Q)}{2m_Q} + \mathcal{O}(1/m_Q^2)$$



# 4. Appl.2: Next-to-Leading order in $1/m_Q$ expansion



Charm hadron



Probing gluon fields

## 5. Conclusion

1. We discuss heavy quark symmetry (HQS) at LO in  $1/m_Q$  expansion.
2. HQS gives doublet/singlet in mass spectrum in exotic heavy hadrons and nuclei.
3. Mass modifications and splitting of  $\bar{D}$  and  $\bar{D}^*$  mesons are concerned with gluon in medium.
4. Toward experiments at J-PARC, GSI-FAIR, LHC, RHIC, etc.!!

# 5. Conclusion

## Many open problems...

- Relation to other fundamental aspects of QCD ?  
(Dynamical breaking of chiral symmetry, Quark Confinement, ...)
- Hadron-nucleon interaction ? Many-body physics ?  
(Pion exchange, Mean field approximation, Symmetry restoration, ...)
- What about atomic nucleus with charm ?
- Lattice QCD: what QCD says about charm nucleus ?
- Production cross sections of charm nucleus ?
- etc.

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