

Dynamics of kaonic nuclei in an improved quark mass density-dependent model

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- 2 Theoretical framework for kaonic nuclei
- 3 Results and discussion
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Introduction to the improved quark mass density-dependent model

● Self-consistent mean-field models for nuclear structure

- Hartree-Fock-Bogoliubov method (**HFB**)
H. J. Mang, Phys. Rep. 18, 325 (1975).
- Relativistic mean-field model (**RMF**)
J. Walecka, Annals of Physics 83, 491 (1974).
P. Ring, Prog. Part. Nucl. Phys. 37, 193 (1996).

● Extended Relativistic mean-field models

- The quark-meson coupling model (**QMC**)
P. A. M. Guichon, Physics Letters B 200, 235 (1988).
- The quark mean field model (**QMF**)
H. Toki, U. Meyer, A. Faessler, and R. Brockmann, Phys. Rev. C 58, 3749 (1998).

Introduction to IQMDD

According to the QMDD model, suggested by Fowler et al. , the masses of u , d quarks and strange quarks depend on the baryon number density n_B .

$$m_q = \frac{B}{3n_B} (q = u, d, \bar{u}, \bar{d}), m_{s,\bar{s}} = m_{s_0} + \frac{B}{3n_B}$$

G. N. Fowler et al.,
Z. Phys. C 9, 271
(1981)

● The IQMDD Lagrangian density at hadronic level

$$\begin{aligned} L = & \bar{\phi}[i\gamma^\mu \partial_\mu - M_N^*(\sigma) - g_\omega \gamma^\mu \omega_\mu - \frac{g_\rho}{2} \gamma^\mu \tau \cdot \rho_\mu - \frac{e}{2} \gamma^\mu (1 + \tau_3) A_\mu \\ & + \frac{f_\omega g_\omega}{2M_N} \sigma^{\mu\nu} \partial_\nu \omega_\mu] \phi + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma - U(\sigma) - \frac{1}{4} \Omega^{\mu\nu} \Omega_{\mu\nu} + \frac{1}{2} m_\omega^2 \omega^\mu \omega_\mu \\ & - \frac{1}{4} G^{\mu\nu} G_{\mu\nu} + \frac{1}{2} m_\rho^2 \rho^\mu \rho_\mu + \eta(g_\rho^2 \rho_\mu \rho^\mu)(g_\omega^2 \omega_\mu \omega^\mu) - \frac{1}{4} F^{\mu\nu} F_{\mu\nu} \end{aligned}$$

Introduction to IQMDD

The effective nucleon mass is obtained from the bag energy which reads

$$M_N^* = \sum_q E_q = \sum_q \frac{4}{3} \pi R^3 \frac{\Gamma_q}{(2\pi)^3} \int_0^{K_F^q} \sqrt{m_q^{*2} + k^2} \left(\frac{dN_q}{dk} \right) dk$$

where, $m_q^* = m_q - g_\sigma^q \sigma$

The bag radius R can be determined by using the equilibrium condition for the nucleon bag

$$\frac{\delta M_N^*}{\delta R} = 0$$

Introduction to IQMDD

While the expression of M_N^* for RMF is taken as

$$M_N^* = M_N - g_\sigma \sigma$$

IQMDD model has a nonlinear relationship with the σ field rather than RMF model

$$\left(\frac{\partial M_N^*}{\partial \sigma} \right)_R = -g_\sigma \times \begin{pmatrix} 1 \\ c(\sigma) \end{pmatrix} \text{ for } \begin{pmatrix} \text{RMF(NL3,FSU,...)} \\ \text{IQMDD} \end{pmatrix}$$

Theoretical framework for kaonic nuclei in IQMDD

Theoretical framework for kaonic nuclei

Formulas of the IQMDD model for kaonic nuclei

$$\begin{aligned} L = & L_N + \partial_\mu \bar{K} \partial^\mu K - m_K^2 \bar{K} K + g_{\sigma K} m_K \bar{K} K \sigma \\ & + \left(i g_{\omega K} \omega_\mu + i g_{\rho K} \tau \cdot \rho_\mu + i \frac{e}{2} (1 + \tau_3) A_\mu \right) \left(K \partial^\mu \bar{K} - \bar{K} \partial^\mu K \right) \\ & + \left[g_{\omega K} \omega_\mu + g_{\rho K} \tau \cdot \rho_\mu + \frac{e}{2} (1 + \tau_3) A_\mu \right]^2 \bar{K} K \end{aligned}$$

Using the Euler-Lagrange equation one obtains the Dirac equation for nucleons as follow

Theoretical framework for kaonic nuclei

$$\left[i\gamma^\mu \partial_\mu - M_N^* - g_\omega \gamma^0 \omega_0 - \frac{g_\rho}{2} \gamma^0 \tau_3 \rho_0 + \frac{f_\omega g_\omega}{2M_N} \sigma^{0i} \partial_i \omega_0 - \frac{e}{2} \gamma^0 (1 + \tau_3) A_0 \right] \varphi = 0 \quad (1)$$

The equations of motion for the mesons and photon can be written as

$$(-\Delta + m_\sigma^2) \sigma = -\frac{\partial M_N^*}{\partial \sigma} \rho_s - b \sigma^2 - c \sigma^3 + g_{\sigma K} m_K \bar{K} K \quad (2)$$

$$(-\Delta + m_\omega^2) \omega_0 = g_\omega \rho_v + \frac{f_\omega g_\omega}{2M_N} \rho_0^T - g_{\omega K} \rho_{K^-} - 2\eta g_\rho^2 g_\omega^2 \rho_0^2 \omega_0 \quad (3)$$

Theoretical framework for kaonic nuclei

$$(-\Delta + m_\rho^2) \rho_0 = \frac{g_\rho}{2} \rho_3 - g_{\rho K} \rho_{K^-} - 2\eta g_\rho^2 g_\omega^2 \rho_0 \omega_0^2 \quad (4)$$

$$-\Delta A_0 = e \rho_p - e \rho_{K^-} \quad (5)$$

The density of K^- meson ρ_{K^-} is given by

$$\rho_{K^-} = 2 \left[\text{Re } E_{K^-} + g_{\omega K} \omega_0 + g_{\rho K} \rho_0 + e A_0 \right] \bar{K} K \quad (6)$$

The integration of ρ_{K^-} over the whole volume is normalized to the number of antikaon, which is one in our calculation.

Theoretical framework for kaonic nuclei

The Klein-Gordon equation of motion for the K^- meson acquires the form

$$[-\Delta + (m_K^2 - E_{K^-}^2) + \tilde{\Pi}] \bar{K} = 0 \quad (7)$$

● K^- meson absorption in the nuclear medium

To evaluate the K^- decay width, one allows the self-energy to become complex

$$\begin{aligned} \tilde{\Pi} &= \text{Re } \tilde{\Pi} - i \text{Im } \tilde{\Pi} \\ &= -g_{\sigma K} m_K \sigma - 2(\text{Re } E_{K^-}) [g_{\omega K} \omega_0 + g_{\rho K} \rho_0 + e A_0] \\ &\quad - [g_{\omega K} \omega_0 + g_{\rho K} \rho_0 + e A_0]^2 - i \text{Im } \tilde{\Pi} \end{aligned}$$

Theoretical framework for kaonic nuclei

The complex eigenenergy is given as

$$E_{K^-} = \text{Re } E_{K^-} - i\Gamma_{K^-} / 2$$

Two kinds of antikaonic absorption in the nuclear medium are considered.



Then the imaginary part of the potential $\text{Im} \tilde{\Pi}$ is written as

$$\begin{aligned} \text{Im} \tilde{\Pi} &= \text{Im} \tilde{\Pi}^{(1)} + \text{Im} \tilde{\Pi}^{(2)} = 2 \left(\text{Re } E_{K^-} \right) f_1 V_0 \frac{\rho_\nu(r)}{\rho_0} \\ &+ 2 \left(\text{Re } E_{K^-} \right) f_2 V_0 \frac{\rho_\nu^2(r)}{\rho_0^2} \end{aligned}$$

Theoretical framework for kaonic nuclei

The mesonic and nonmesonic decay channels are dominated by the final Σ states

$$f_1 = 0.8f_{1\Sigma}, \quad f_2 = 0.2f_{2\Sigma}$$

$$f_1 = 0.7f_{1\Sigma} + 0.1f_{1\Lambda}, \quad f_2 = 0.2f_{2\Sigma}$$

C. Vander Velde-Wilquet, J. Sacton, J. H. Wickens, D. N. Tovee, and D. H. Davis, Nuovo Cimento A **39**, 538 (1977).

J. Yamagata, H. Nagahiro, Y. Okumura et al., Prog. Theor. Phys. **114**, 301 (2005).

T. Sekihara, J. Yamagata-Sekihara, D. Jido, Y. Kanada-En'yo, Phys. Rev. C **86**, 065205 (2012).

Theoretical framework for kaonic nuclei

The imaginary potential depth V_0 strongly depends on the model adopted.

E. Friedman, A. Gal, C.J. Batty, Phys. Lett. B 308, 6 (1993).

E. Friedman, A. Gal, J. Mares, A. Cieply,
Phys. Rev. C 60, 024314 (1999).

$$V_0 \sim 50\text{MeV}$$

A. Ramos et al., Nucl. Phys. A 691, 258 (2001).

$$V_0 \sim 15\text{MeV}$$

The imaginary potential depth V_0 is set to be in the range of 15 ~ 50 MeV.

Theoretical framework for kaonic nuclei

● K^- optical potential

The difference in K^- potential depths between different approaches

T.Waas, W. Weise, Nucl. Phys. A 625, 287 (1997).

$$U_{K^-}(\rho_0) \sim -120 \text{ MeV}$$

V. Koch, Phys. Lett. B 337, 7 (1994).

$$U_{K^-}(\rho_0) \sim -100 \text{ MeV}$$

A. Cieply, E. Friedman, A. Gal,
and J. Mares, Nucl. Phys. A 696, 173 (2001)

$$U_{K^-}(\rho_0) \approx -60 \sim -50 \text{ MeV}$$

Theoretical framework for kaonic nuclei

- The ω -K and ρ -K coupling constants are adopted from the SU(3) relation assuming ideal mixing

$$2g_{\omega K} = 2g_{\rho K} = 6.04$$

J. Schaffner, I.N. Mishustin,
Phys. Rev. C 53, 1416 (1996).

- The σ -K coupling is fixed by varying the optical potential from **-80MeV** to **-120MeV**.

A. Martinez Torres, K.P. Khemchandani, E. Oset,
Eur. Phys. J. A 36, 211 (2008)

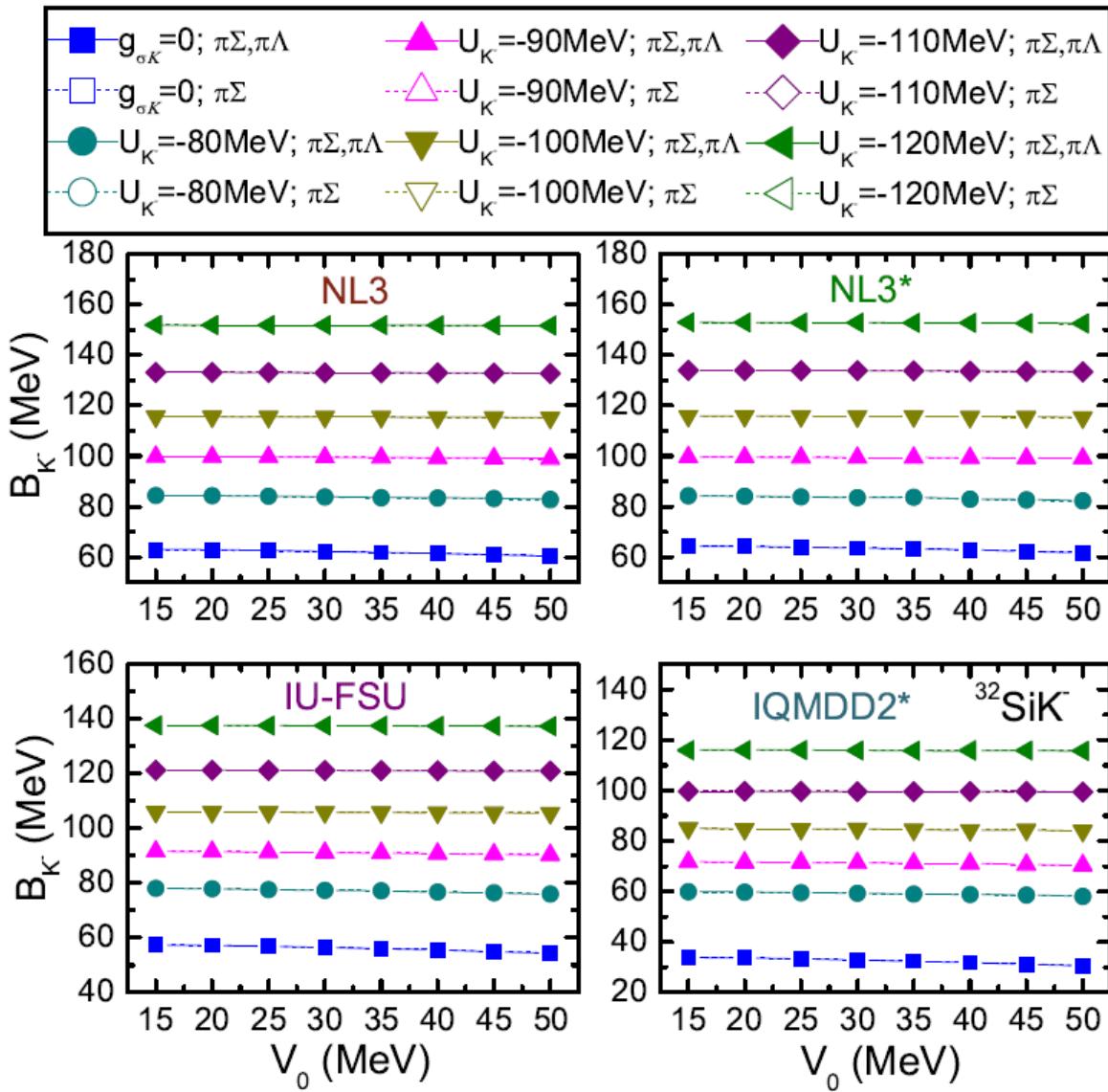
$$g_{\sigma K} = 0$$

$$U_{K^-}(\rho_0) \approx -70 \sim -50 \text{ MeV}$$

(NL3, NL3*,
IU-FSU, IQMDD2*)

Results and discussion

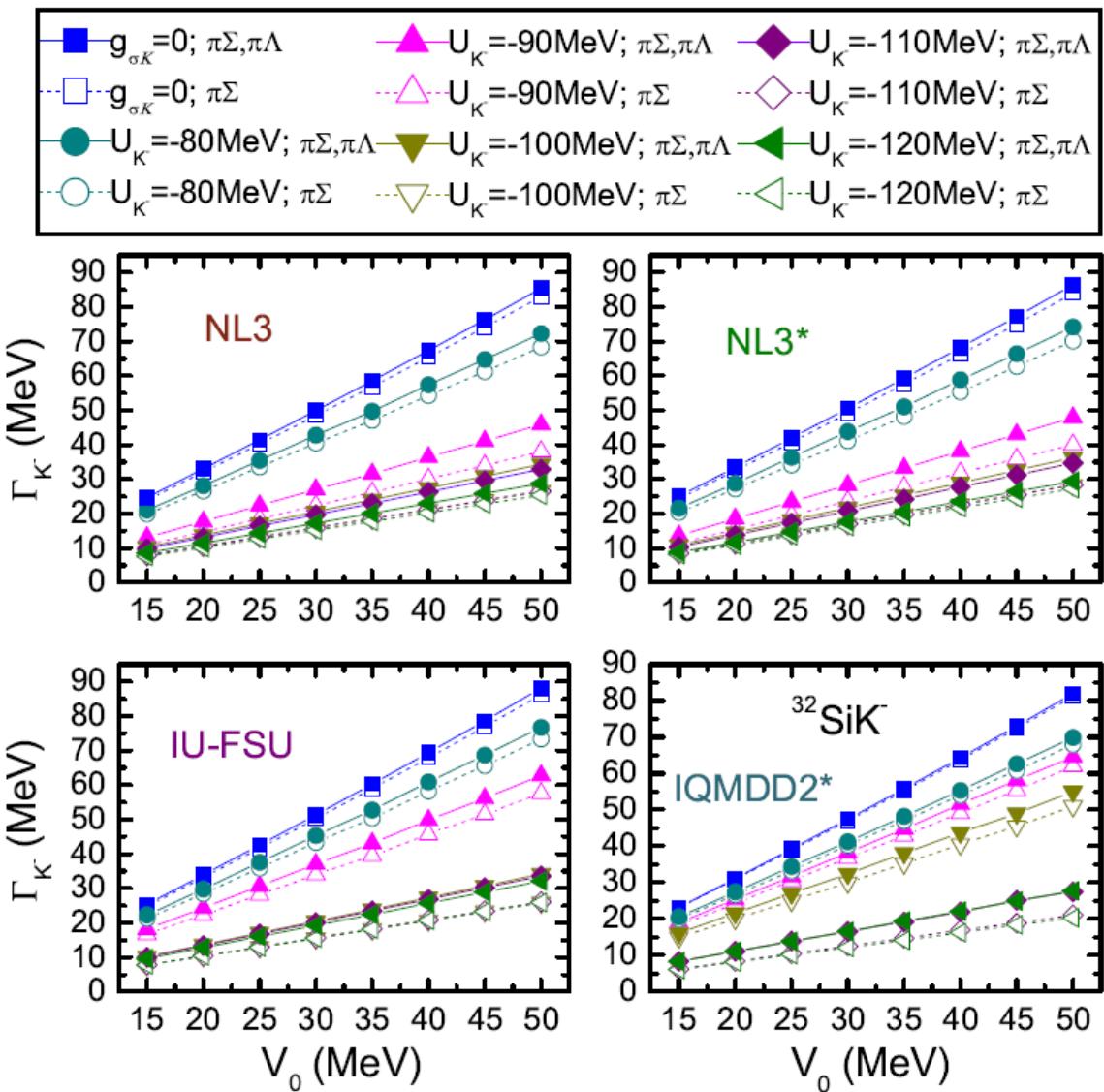
1. K^- binding energy



The calculated K^- binding energies of the 1s nuclear state in the $^{32}\text{Si}K^-$ nucleus by using the IQMDD model (IQMDD2*) and RMF models (NL3, NL3* and IUFSU).

2. decay widths

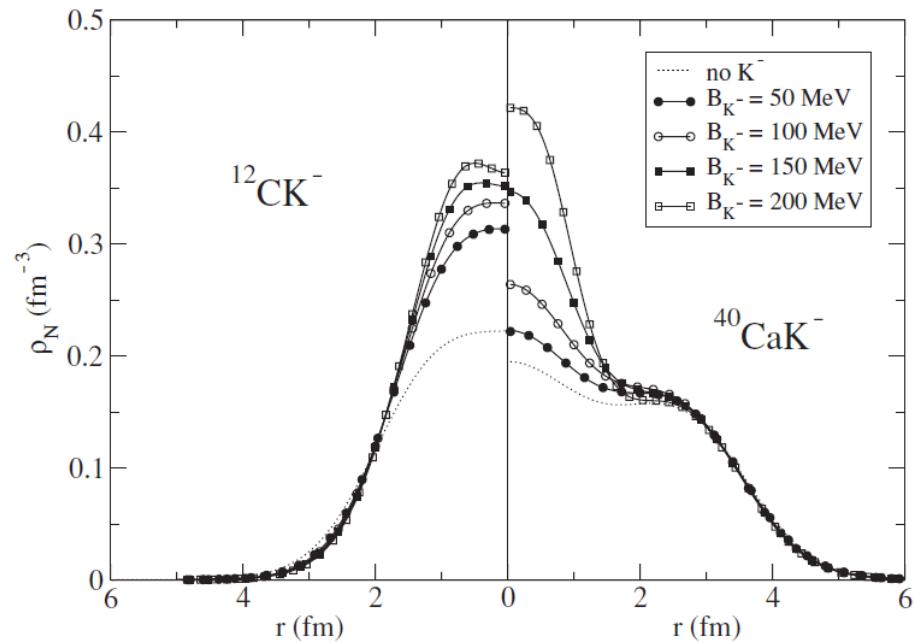
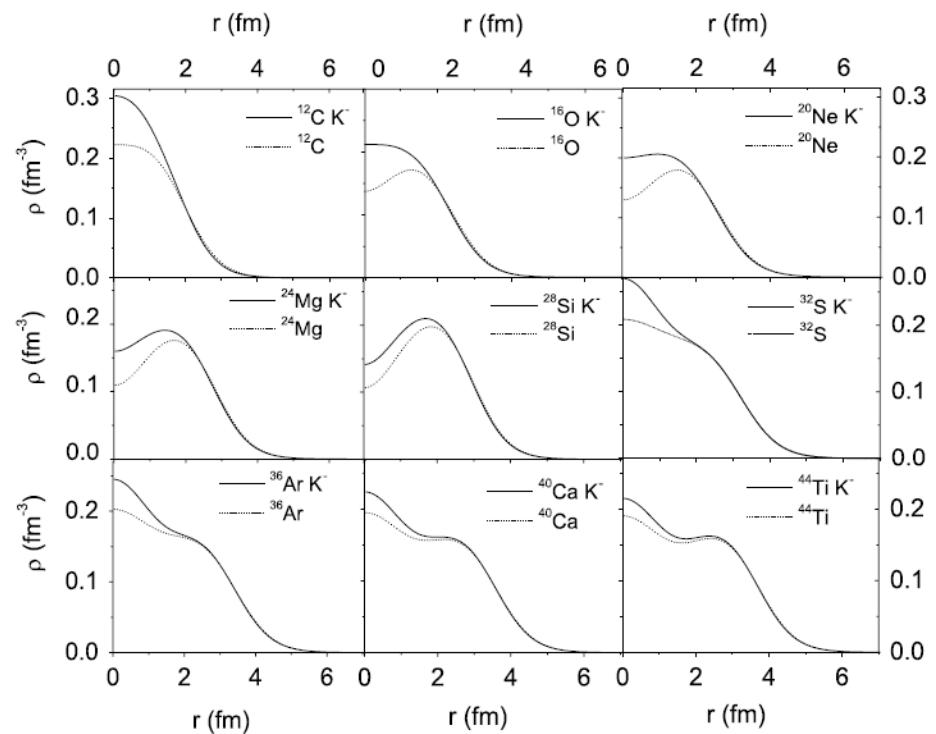
The widths (Γ_{K^-}) of the 1s K^- -nuclear state in the $^{32}\text{Si}K^-$ nucleus as a function of the imaginary potential depth by using the IQMDD model (IQMDD2*) and other RMF models (NL3, NL3* and IU-FSU) for different absorption.



D. Gazda, E. Friedman, A. Gal, J. Mares, Phys. Rev. C 76, 055204 (2007).

3. nuclear density distribution

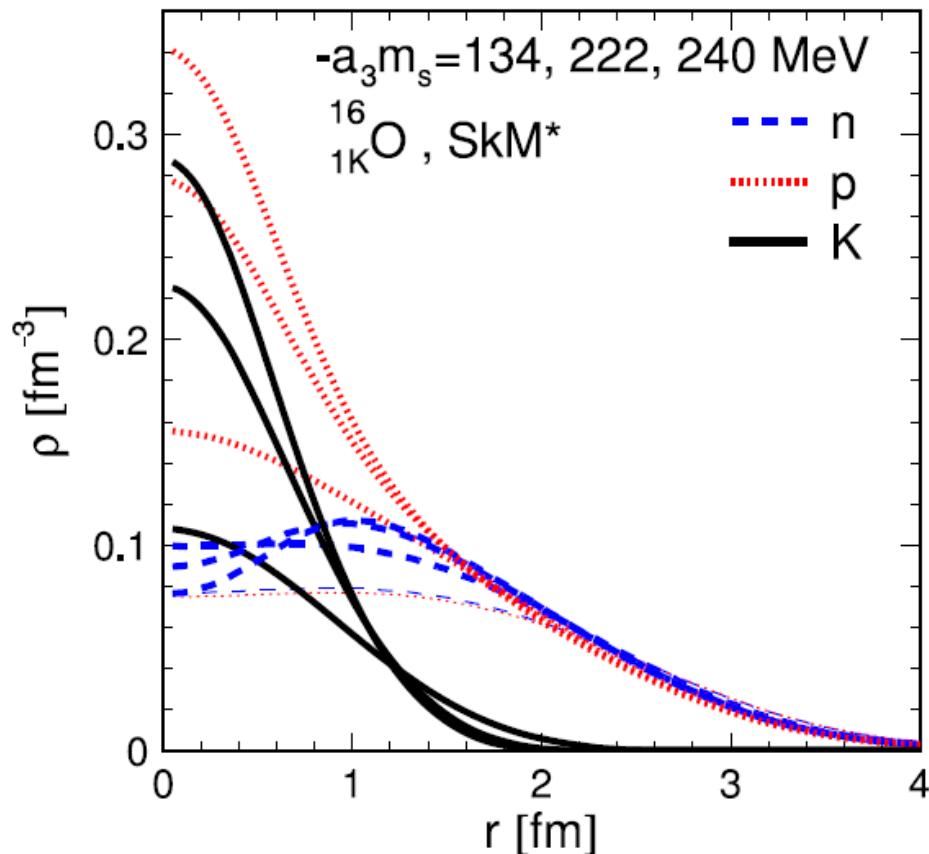
• The shrinkage effects for the kaonic nuclei



X.H. Zhong, G.X. Peng, L. Li, P.Z. Ning, Phys. Rev. C 74, 034321 (2006).

D. Gazda, E. Friedman, A. Gal, J. Mares, Phys. Rev. C 76, 055204 (2007).

3. nuclear density distribution

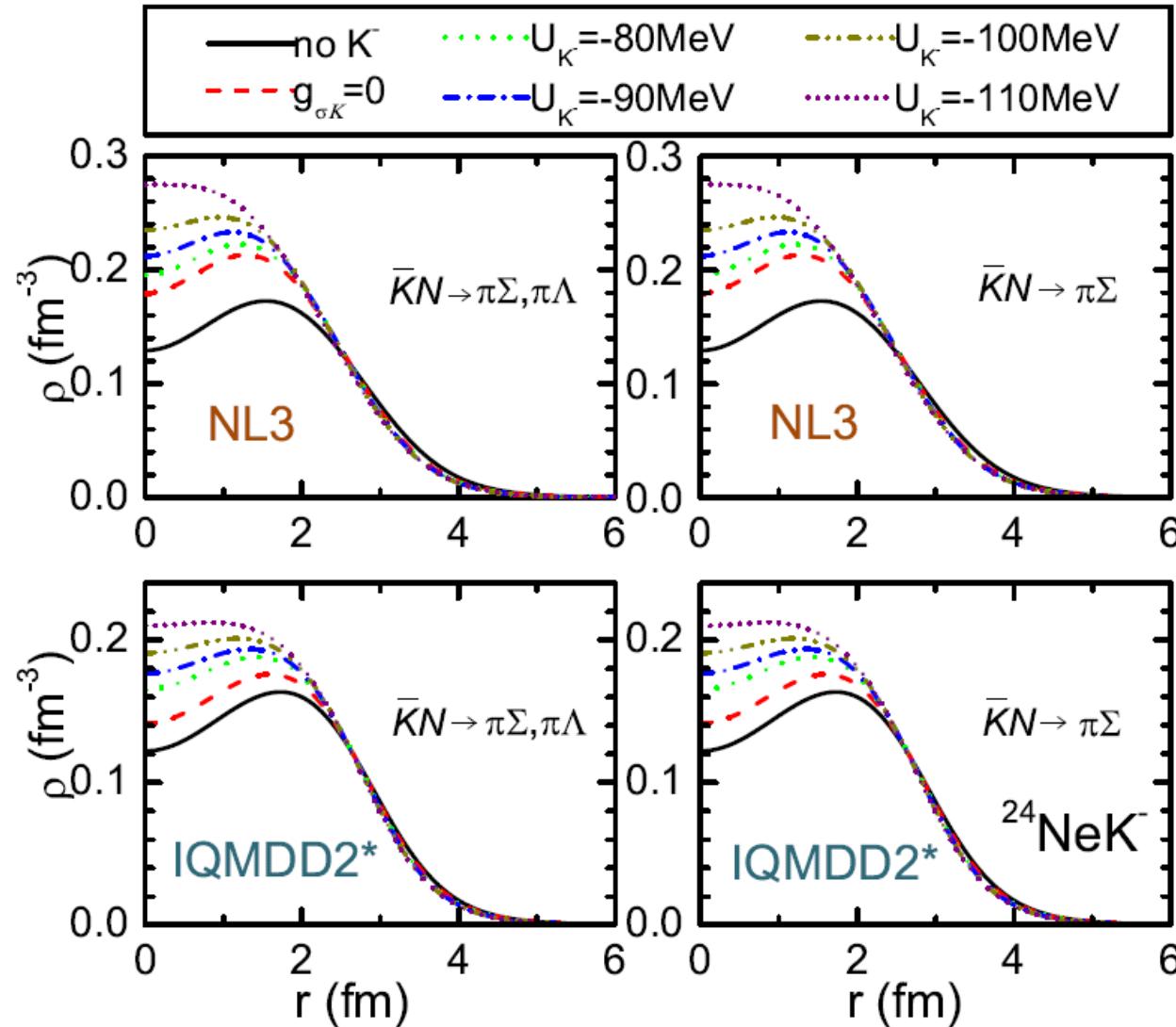


Kaon and nucleon densities of $^{16}\text{O}K^-$ for various interaction parameters a_3 . Increasing absolute a_3 values correspond to increasing curves. The thin curves represent the core nucleus.

X.-R. Zhou, H.-J. Schulze, Nucl. Phys. A 914, 332 (2013).

3. nuclear density distribution

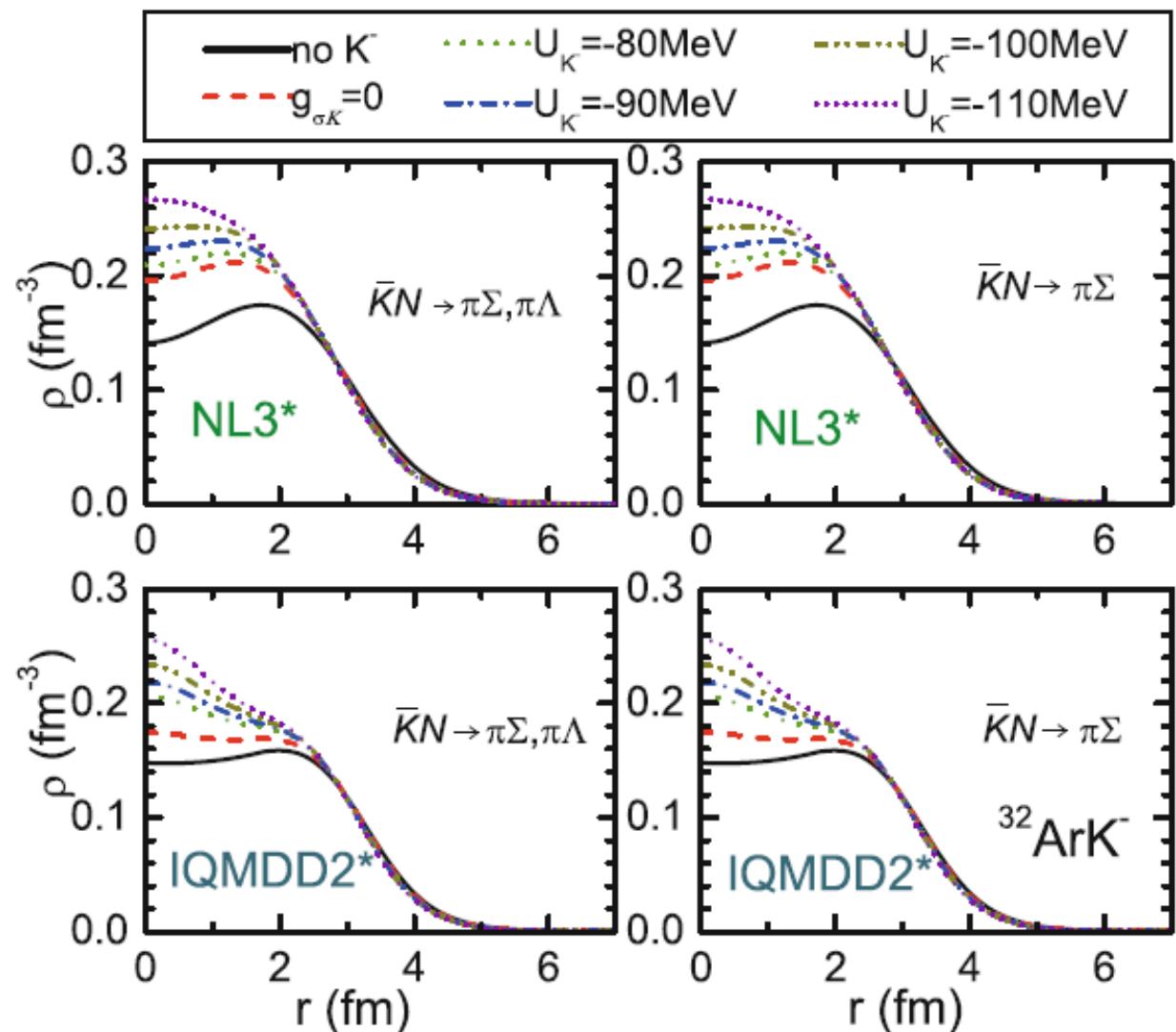
The effects of K^- meson on the properties of bubble nuclei in the light mass region.



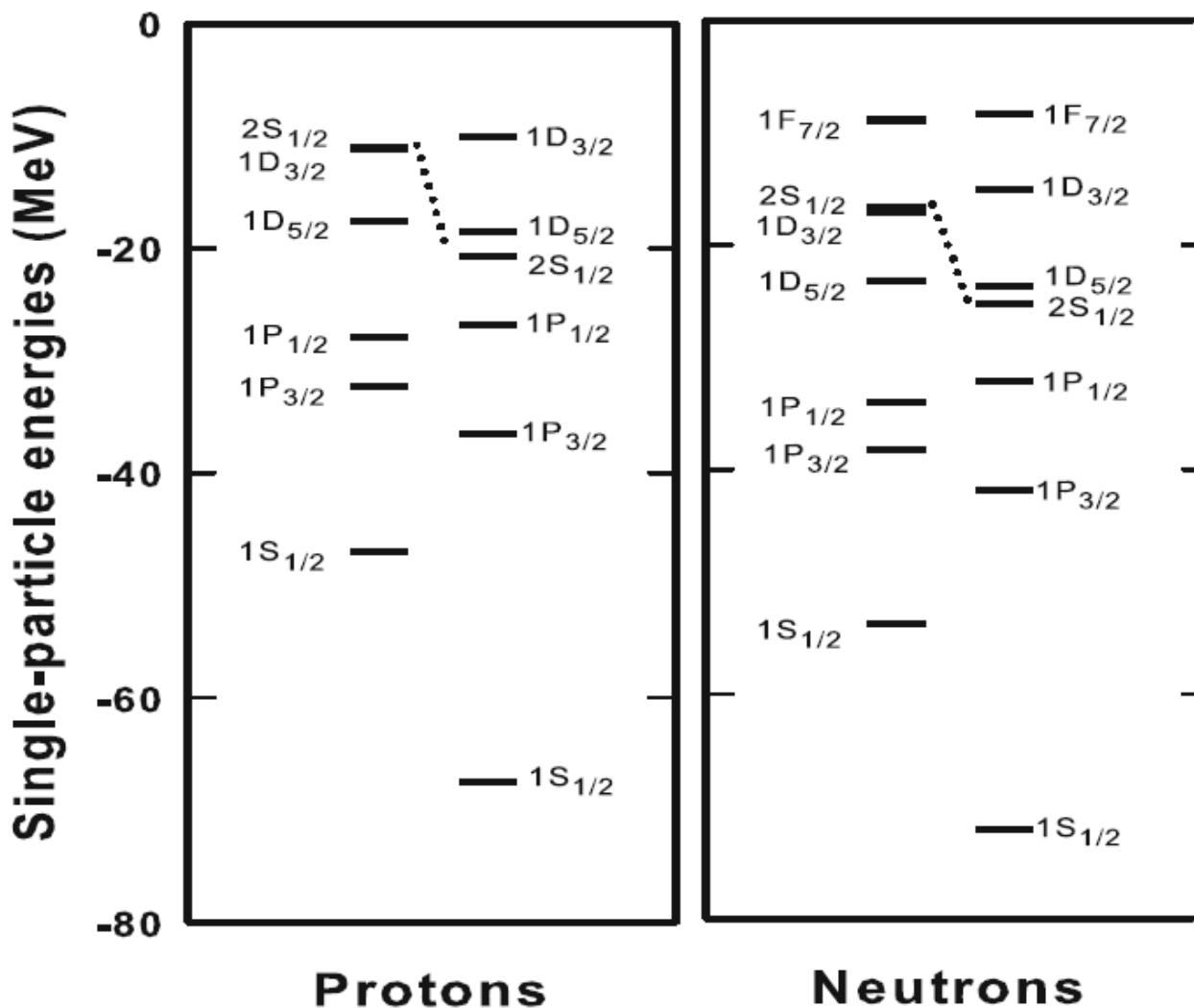
The nuclear density of ^{24}Ne and $^{24}\text{NeK}^-$ nuclei for 1s K^- -nuclear state in the NL3 and the IQMDD model.

3. nuclear density distribution

The nuclear density of ^{32}Ar and $^{32}\text{ArK}^-$ nuclei for 1s K^- -nuclear state in the NL3* and the IQMDD model , with or without the secondary $\pi\Lambda$ decay mode for absorption through the $\bar{K}N \rightarrow \pi\Sigma$.

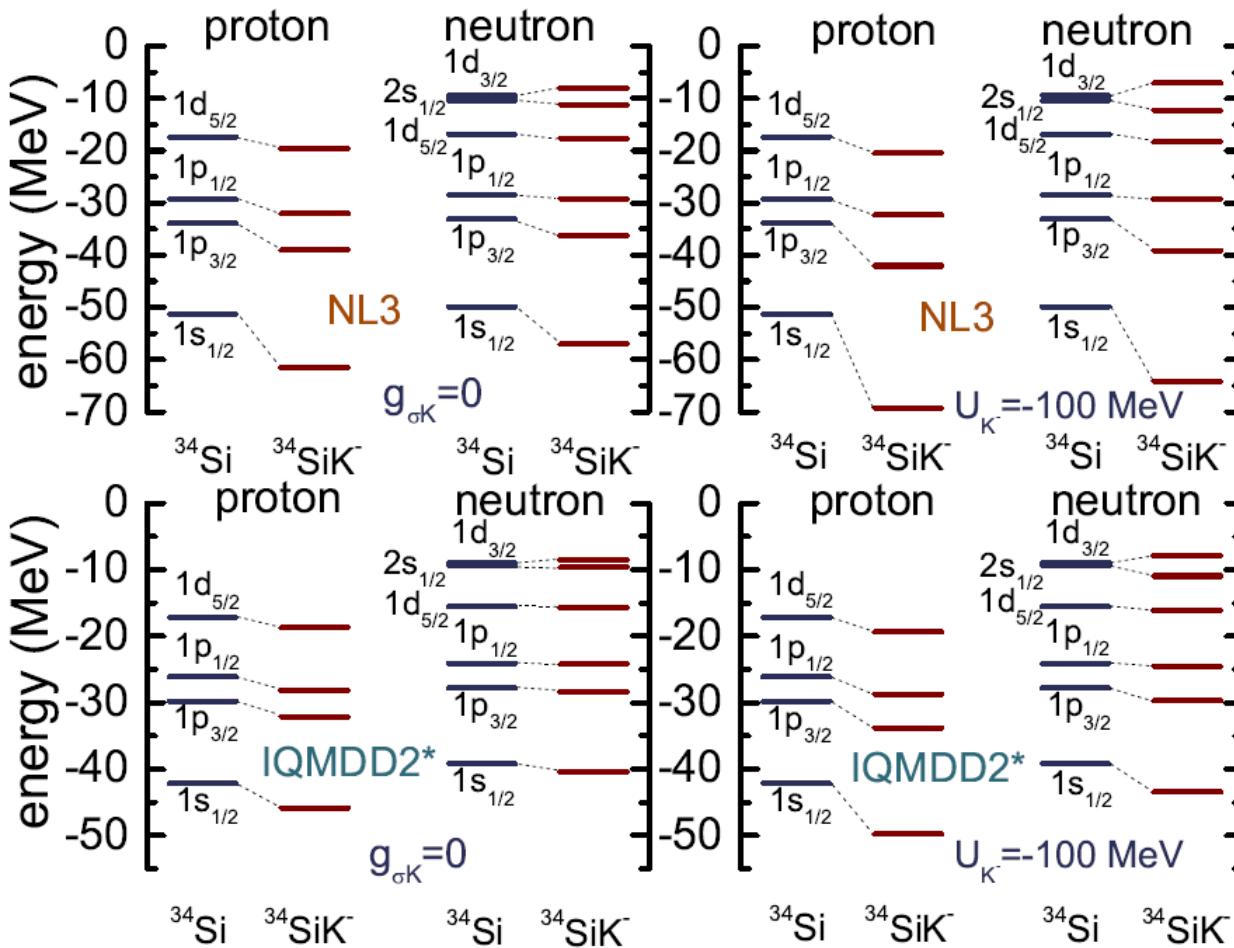


3. pseudospin orbit splitting



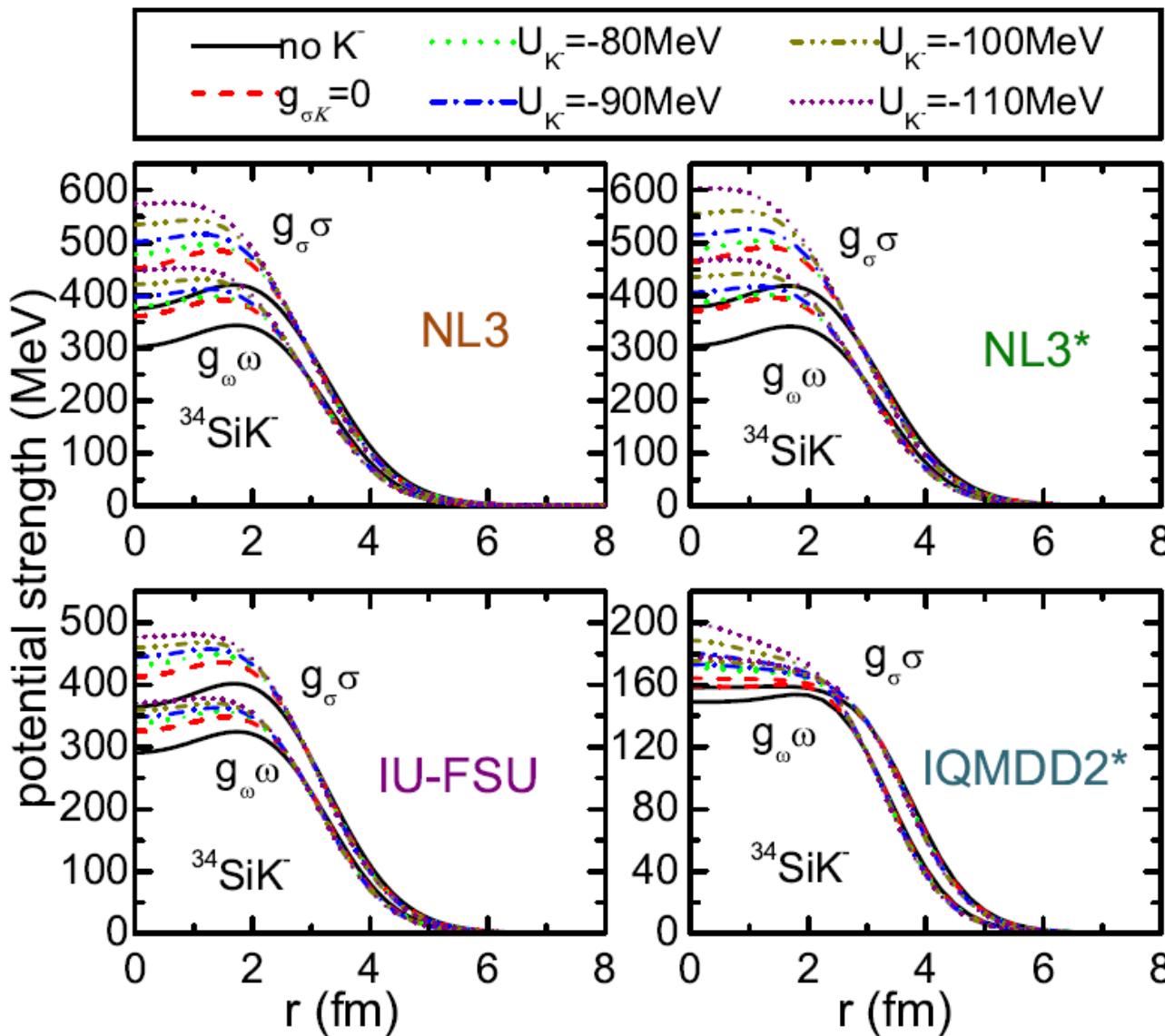
Single-particle energies in ^{42}Ca and $^{42}\text{CaK}^-$. The left column in each panel represents energy levels for ^{42}Ca , while the right ones are for $^{42}\text{CaK}^-$.

3. pseudospin orbit splitting



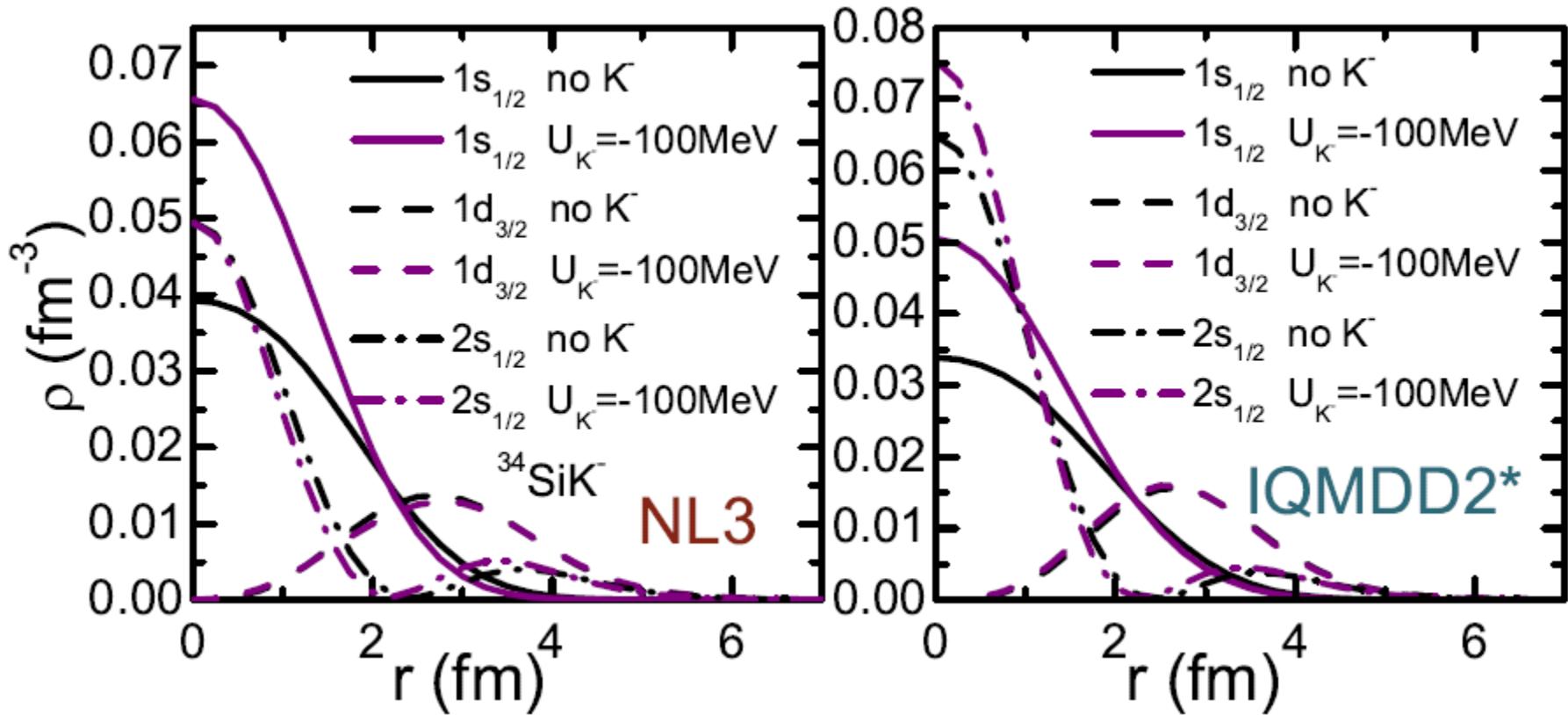
Nucleon single-particle energies of ^{34}Si and $^{34}\text{SiK}^-$ nuclei in the NL3 and the IQMDD model by taking $g_{\sigma K} = 0$ and $U_{K^-}(\rho_0)$ to be -100 MeV .

3. pseudospin orbit splitting



The calculated scalar and vector potentials of nucleon of 1s K^- -nuclear state in ^{34}Si and $^{34}\text{SiK}^-$ nuclei by using NL3, NL3*, IU-FSU and IQMDD models.

3. pseudospin orbit splitting



The density distribution of $1s_{1/2}$, $2s_{1/2}$ and $1d_{3/2}$ neutron states of ^{34}Si and $^{34}\text{SiK}^-$ nuclei in $1s$ K^- -nuclear state by using the NL3 and the IQMDD model, one assumes $U_{K^-}(\rho_0) = -100\text{MeV}$.

Summary

1. The antikaon optical potential $U_{K^-}(\rho_0)$ has a sizable effect on the K^- binding energy. It is found that the K^- binding energy B_{K^-} increases when the antikaon optical potential $U_{K^-}(\rho_0)$ becomes deeper.
2. The antikaon optical potential $U_{K^-}(\rho_0)$ also has a significant effect on the decay width Γ_{K^-} . When the antikaon optical potential becomes deeper, the calculated width Γ_{K^-} decreases.

Summary

3. When the antikaon optical potential $U_{K^-}(\rho_0)$ becomes more negative, the central nuclear density in kaonic nuclei increases. As a result, the nucleon bubble may disappears by embedding the K^- meson in the possible bubble nuclei.
4. the K^- embedment can lead to the pseudospin orbit splitting, and result in the pseudospin symmetry breaking in kaonic nuclei.

Acknowledgement

Special thanks to the valuable discussions from

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X.H. Zhong

Thank you

The phase-space suppression factor corresponding to mesonic decay channel is written as

$$f_{1Y} = \frac{M_{01}^3}{M_1^3} \sqrt{\frac{[M_1^2 - (m_\pi + m_Y)^2][M_1^2 - (m_\pi - m_Y)^2]}{[M_{01}^2 - (m_\pi + m_Y)^2][M_{01}^2 - (m_\pi - m_Y)^2]}} \\ \times \Theta(M_1 - m_\pi - M_Y)$$

Where,

$$M_{01} = m_K + M_N$$

$$M_1 = \text{Re } E_{K^-} + M_N$$

The phase-space suppression factor corresponding to nonmesonic decay channel is written as

$$f_{2Y} = \frac{M_{02}^3}{M_2^3} \sqrt{\frac{[M_2^2 - (m_N + m_Y)^2][M_2^2 - (m_N - m_Y)^2]}{[M_{02}^2 - (m_N + m_Y)^2][M_{02}^2 - (m_N - m_Y)^2]}} \\ \times \Theta(M_2 - m_N - M_Y)$$

Where,

$$M_{02} = m_K + 2M_N$$

$$M_2 = \text{Re } E_{K^-} + 2M_N$$

assuming $U_{K^-}(\rho_0) = -100\text{MeV}$ in the NL3 model, the strength of the scalar and vector potential of a nucleon at the center of the $^{34}\text{SiK}^-$ increase about **160 MeV** and **118MeV**, respectively, compared to those in the ^{34}Si .

