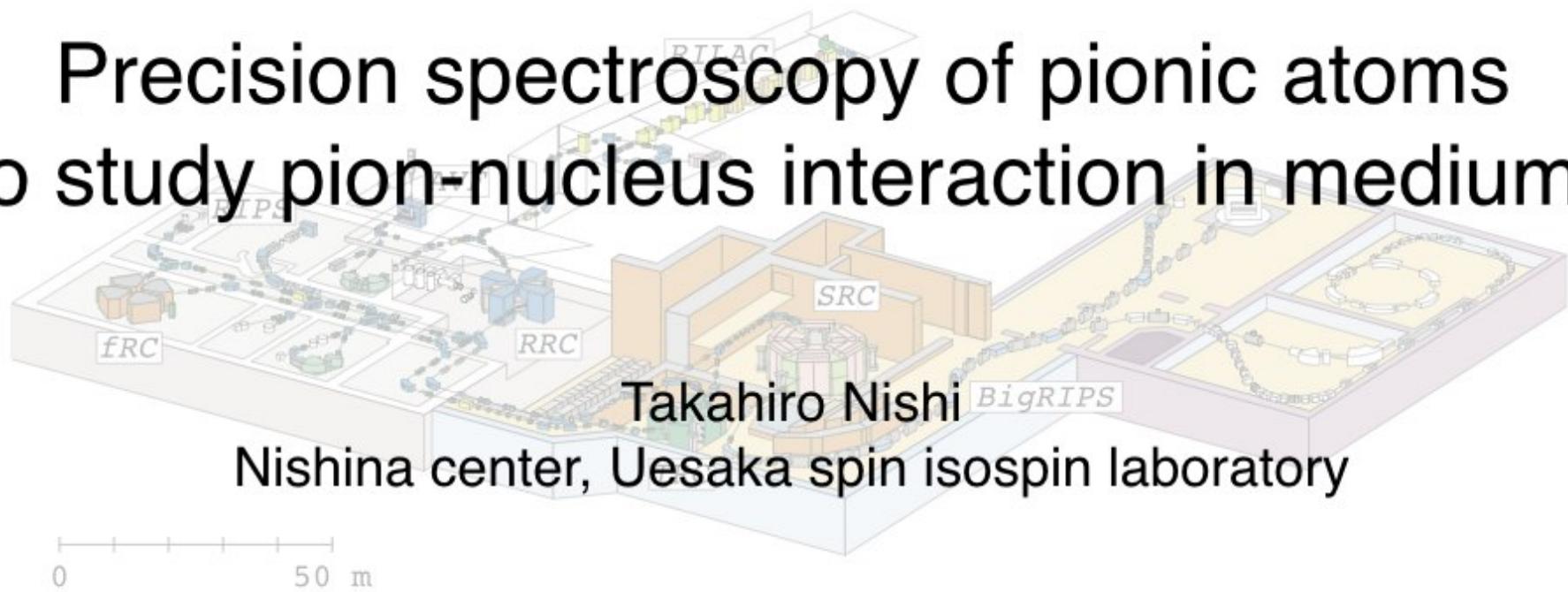


Precision spectroscopy of pionic atoms to study pion-nucleus interaction in medium



Collaborators

DeukSoon Ahn, Georg P.A. Berg, Masanori Dozono, Daijiro Etoh, Hiroyuki Fujioka, Naoki Fukuda, Nobuhisa Fukunishi, Hans Geissel, Emma Haettner, Tadashi Hashimoto, Ryugo S. Hayano, Satoru Hirenzaki, Hiroshi Horii, Natsumi Ikeno, Naoto Inabe, Kenta Itahashi*, Sathoshi Itoh, Masahiko Iwasaki, Daisuke Kameda, Shouichiro Kawase, Keichi Kisamori, Yu Kiyokawa, Toshiyuki Kubo, Kensuke Kusaka, Hiroaki Matsubara, Masafumi Matsushita, Shin'ichiro Michimasa, Kenjiro Miki, Go Mishima, Hiroyuki Miya, Daichi Murai, Yohei Murakami, Hideko Nagahiro, Masaki Nakamura, Megumi Niikura, Takahiro Nishi**, Shumpei Noji, Kota Okochi, Shinsuke Ota, Naruhiko Sakamoto, Kimiko Sekiguchi, Hiroshi Suzuki, Ken Suzuki, Motonobu Takaki, Hiroyuki Takeda, Yoshiki K. Tanaka, Koichi Todoroki, Kyo Tsukada, Tomohiro Uesaka, Yasumori Wada, Yuni N. Watanabe, Helmut Weick, Hiroyuki Yamada, Hiroki Yamakami, Yoshiyuki Yanagisawa and Koichi Yoshida

*spokesperson, ** co-spokesperson

University of Tokyo, RIKEN, Nishina Center, University of Notre Dame, Tohoku University, Kyoto University, GSI Helmholtzzentrum für Schwerionenforschung GmbH, Nara Women's University, Osaka University, Stefan Meyer Institute

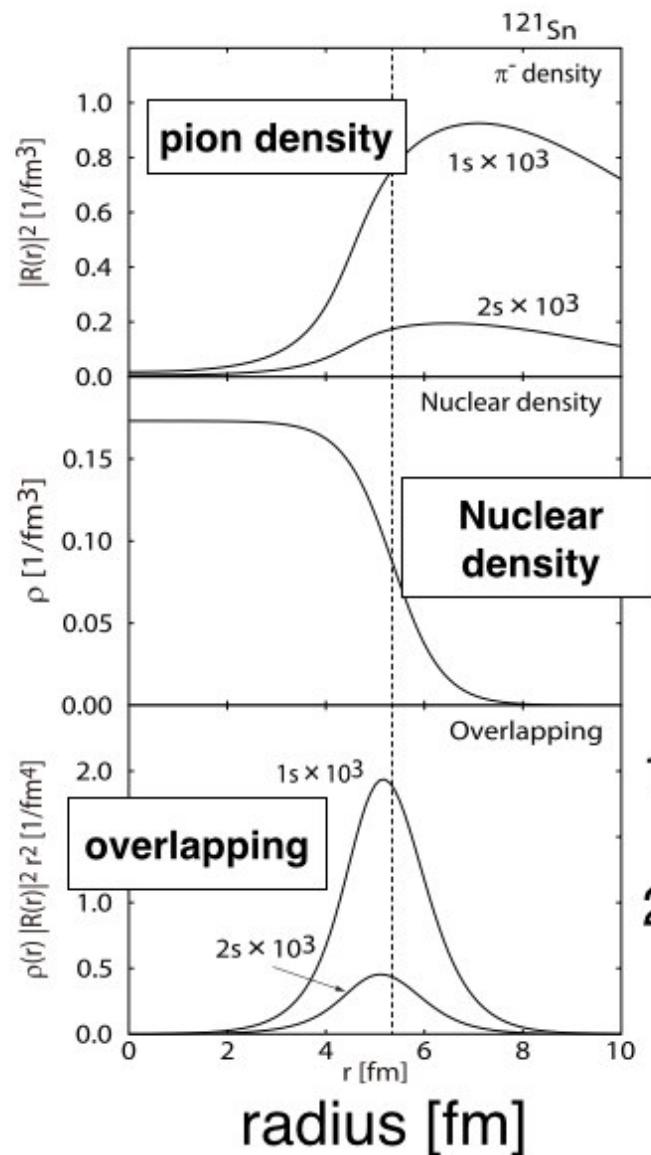
Index

- (i) Motivation and prior research
- (ii) Experiment performed in 2014 at RIKEN
- (iii) Data analysis (pID / optics / decomposition)
- (iv) Summary and future plan

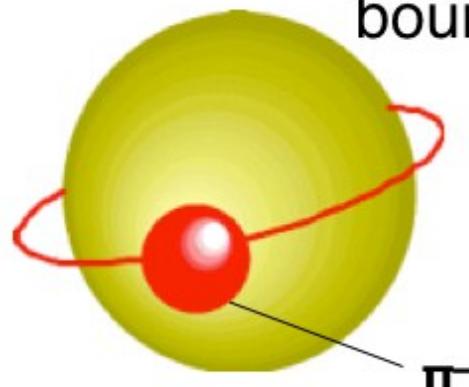
(i) Motivation and prior research

(i) Motivation and prior research

Deeply bound pionic atoms



bound system of π^- & nucleus

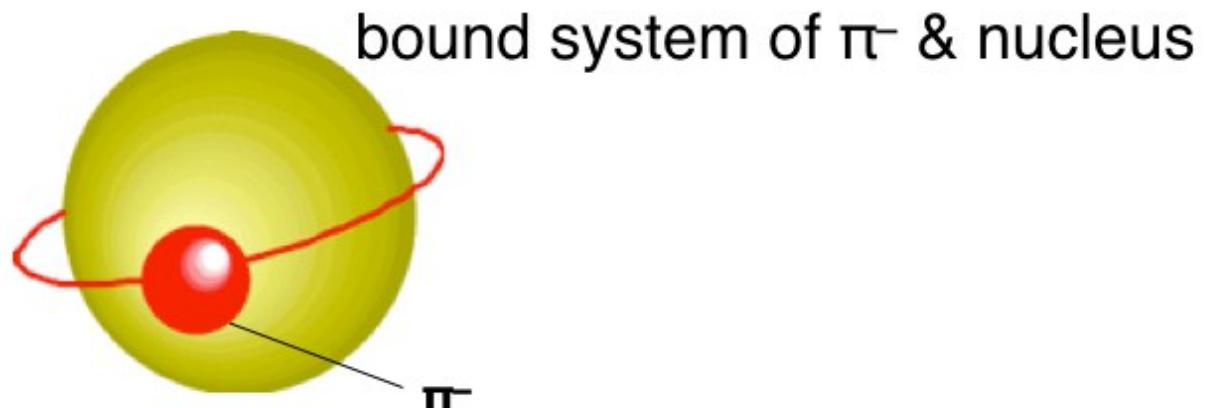
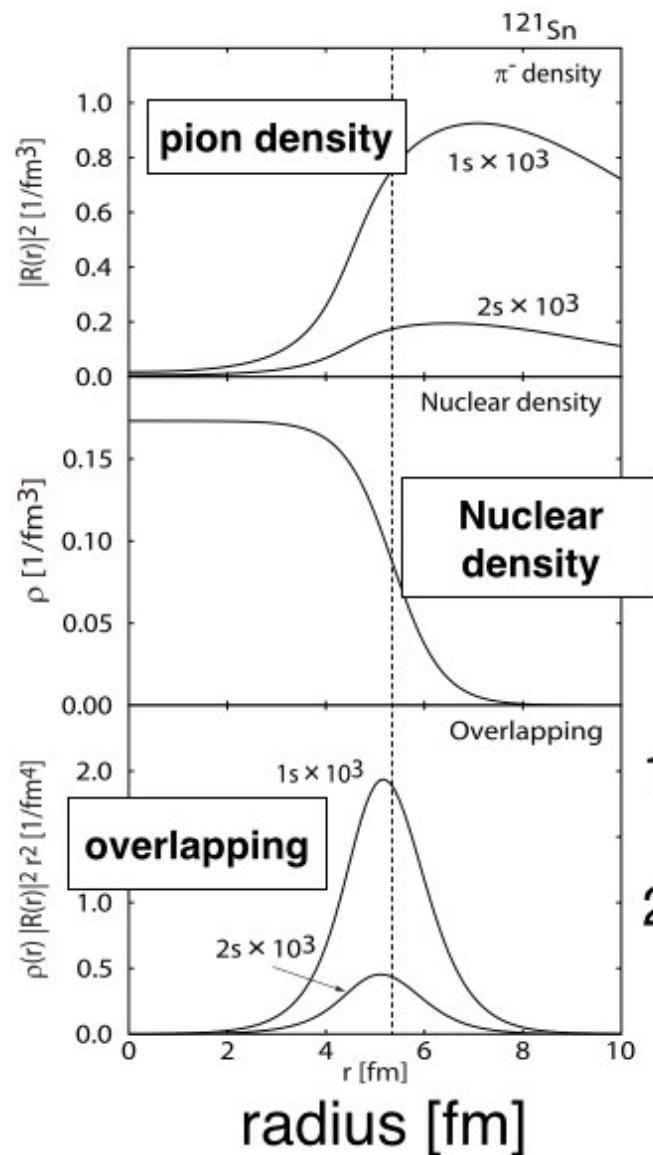


very unique objects in terms of

- 1) Bound system of meson-nucleus
- 2) Quasi-stable state

(i) Motivation and prior research

Deeply bound pionic atoms



bound system of π^- & nucleus

very unique objects in terms of

- 1) Bound system of meson-nucleus
No other “meson in nucleus” system established
- 2) Quasi-stable state
Quantitative evaluation of strong interaction in medium

(i) Motivation and prior research

Deeply bound pionic atoms

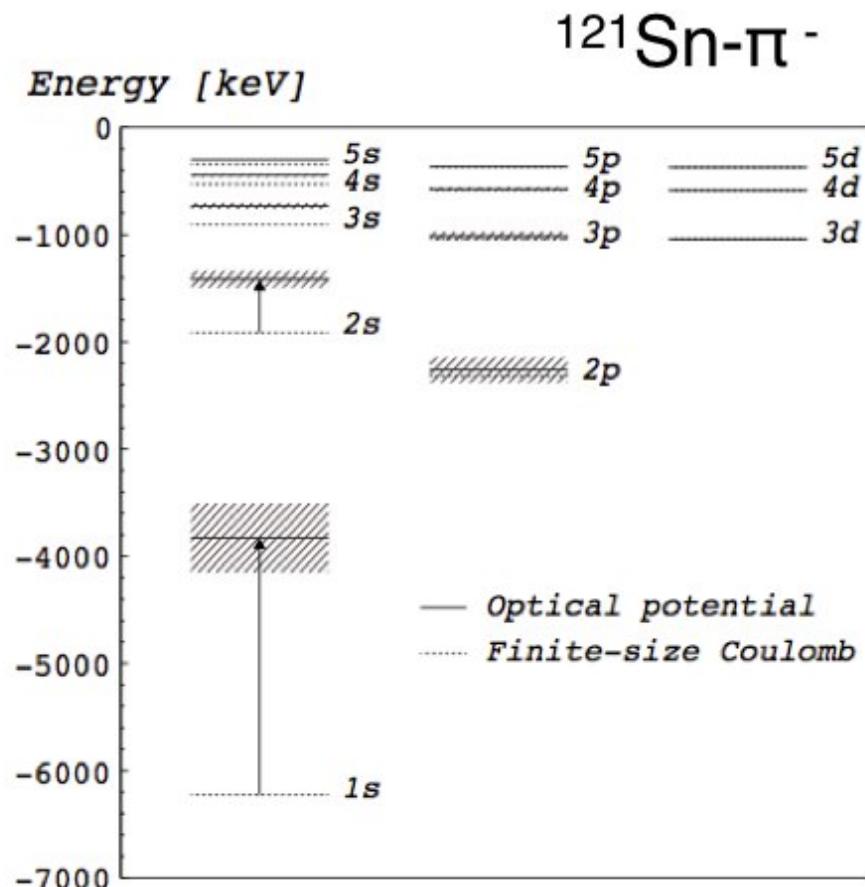
**BE, Γ of 1s pionic state
↔ strong interaction effect**

π -A s-wave optical potential (s-wave)

$$V_s(r) = -\frac{2\pi}{\mu} [\epsilon_1 \{b_0\rho + b_1\delta\rho\} + \epsilon_2 B_0 \rho^2]$$

$$\rho = \rho_p + \rho_n$$

$$\delta\rho = \rho_p - \rho_n$$



N. Ikeda et al., Prog. Theor. Phys. 126 (2011) 483.
S. Itoh, Doctoral Dissertation, Univ. of Tokyo (2011)

(i) Motivation and prior research

Deeply bound pionic atoms

**BE, Γ of 1s pionic state
↔ strong interaction effect**

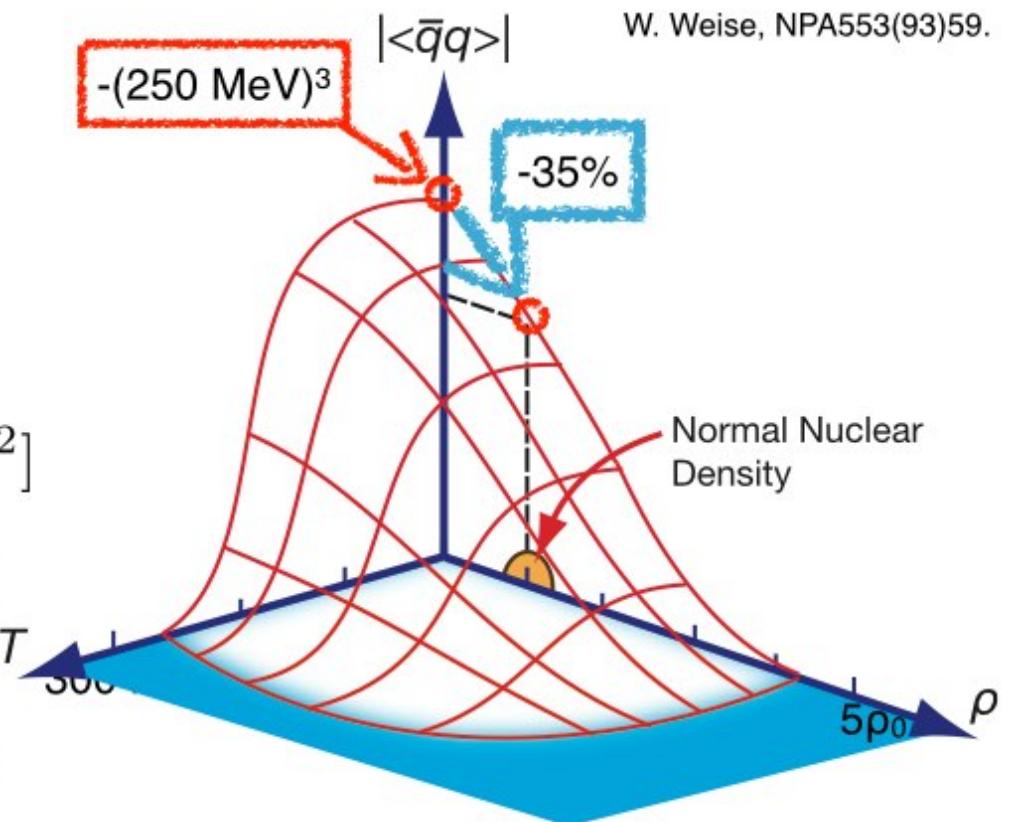
π -A s-wave optical potential (s-wave)

$$V_s(r) = -\frac{2\pi}{\mu} [\epsilon_1 \{b_0\rho + b_1\delta\rho\} + \epsilon_2 B_0 \rho^2]$$

$$\frac{\langle\bar{q}q\rangle_{\rho=\rho_0}}{\langle\bar{q}q\rangle_{\rho=0}} \simeq \left(\frac{m_\pi^*}{m_\pi}\right)^2 \frac{b_1(\rho=0)}{b_1(\rho=\rho_0)}$$

Quantitative evaluation of $\langle\bar{q}q\rangle$

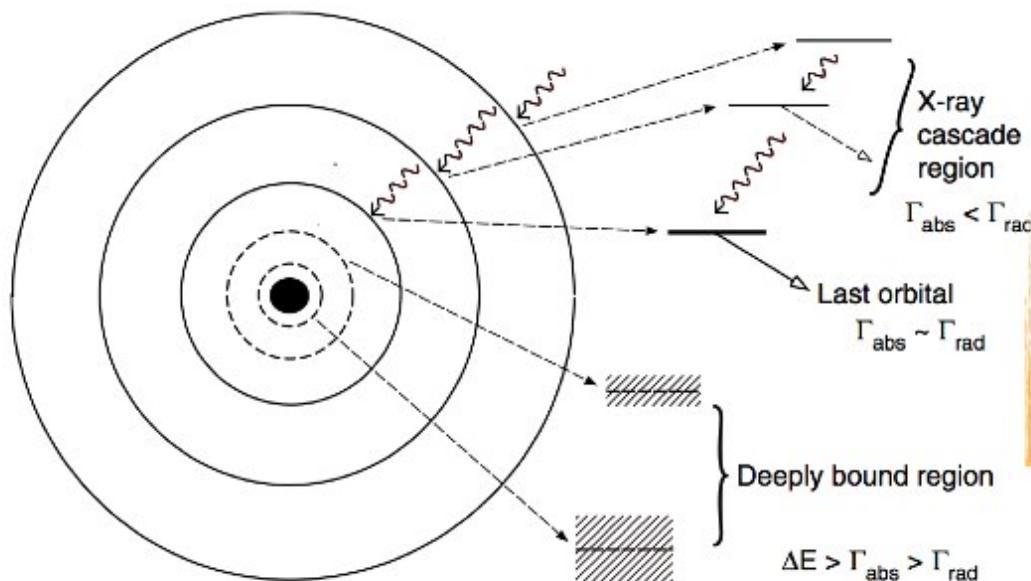
**Order parameter of
chiral symmetry breaking**



W. Weise, NPA553(93)59.

(i) Motivation and prior research

Conventional method: X-ray spectroscopy



Yamazaki *et al.*, Phys. Rep. 514, 1(2012)

x rays during atomic cascade
→ higher orbits / light nuclei
(~ ^{24}Mg for 1s)

pionic 1s state in H
→ b_1 in vacuum

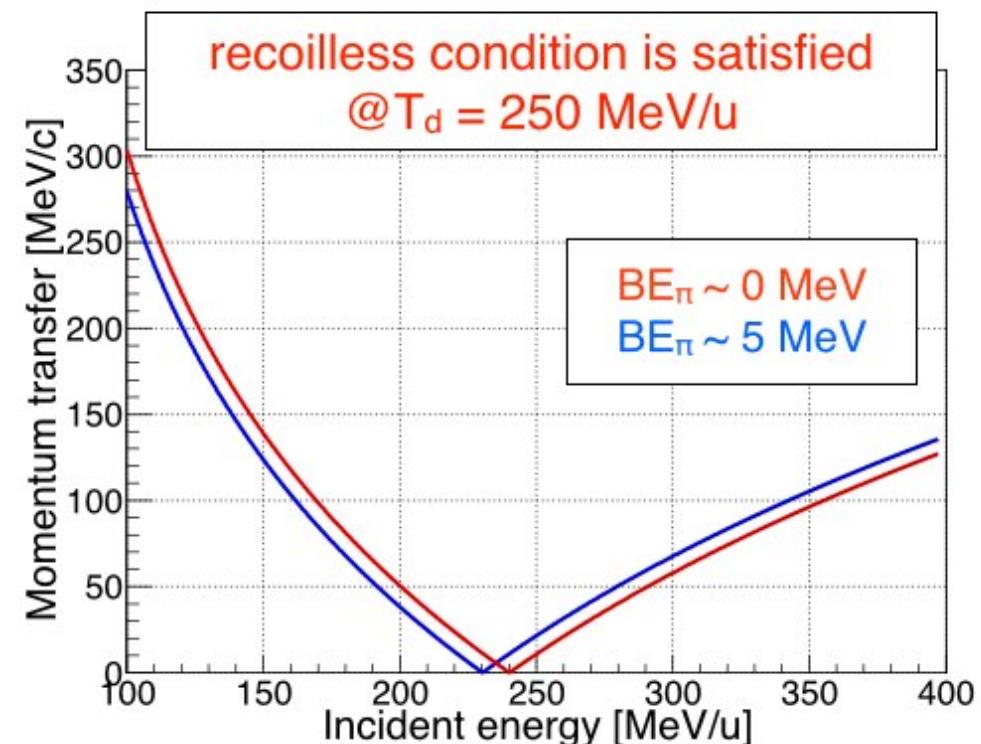
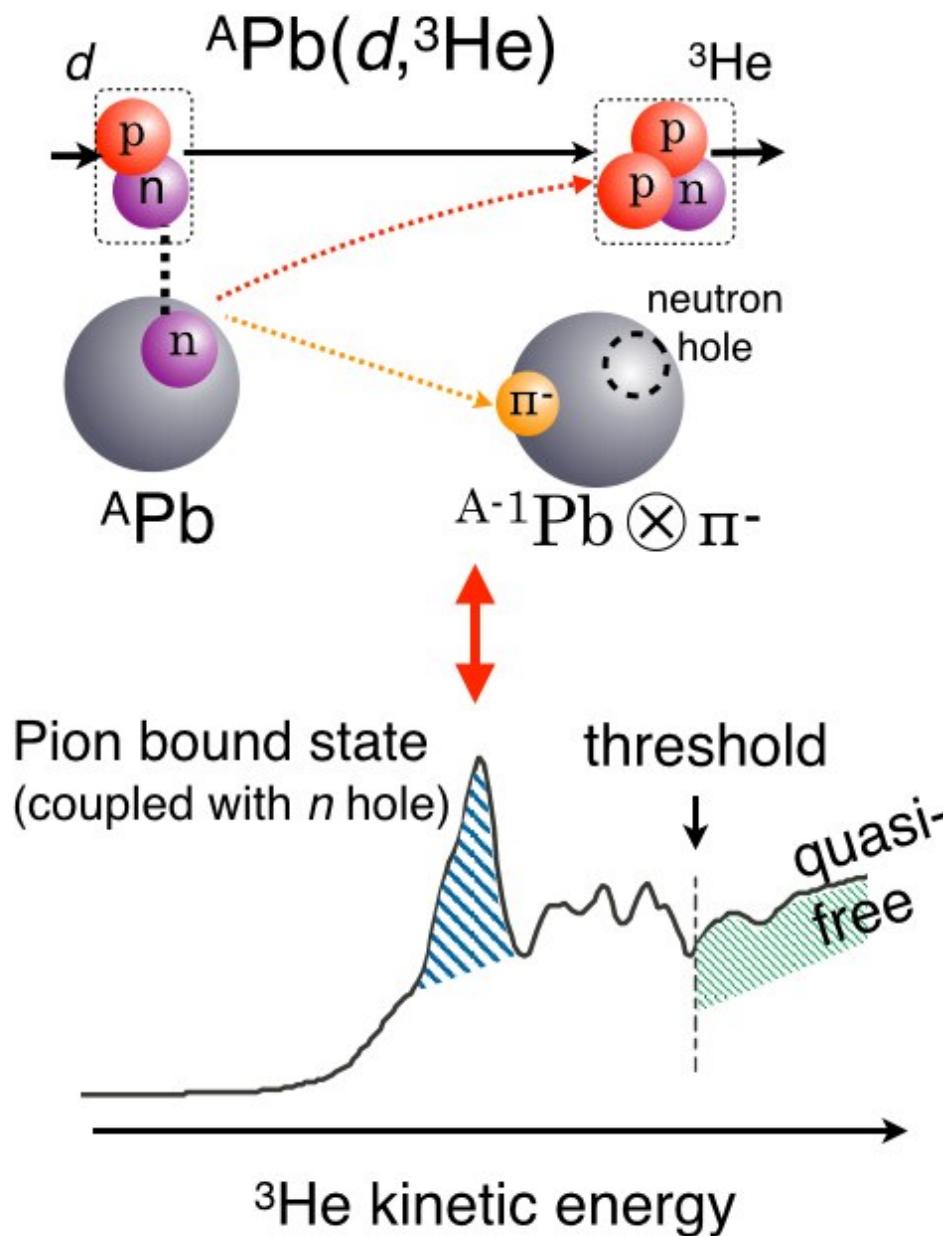
H. Schröder *et al.*, Eur. Phys. J. C 21, 473 (2001).

for deep orbit in heavy nuclei
absorption is faster

This method cannot produce “deeply-bound” pionic atom...

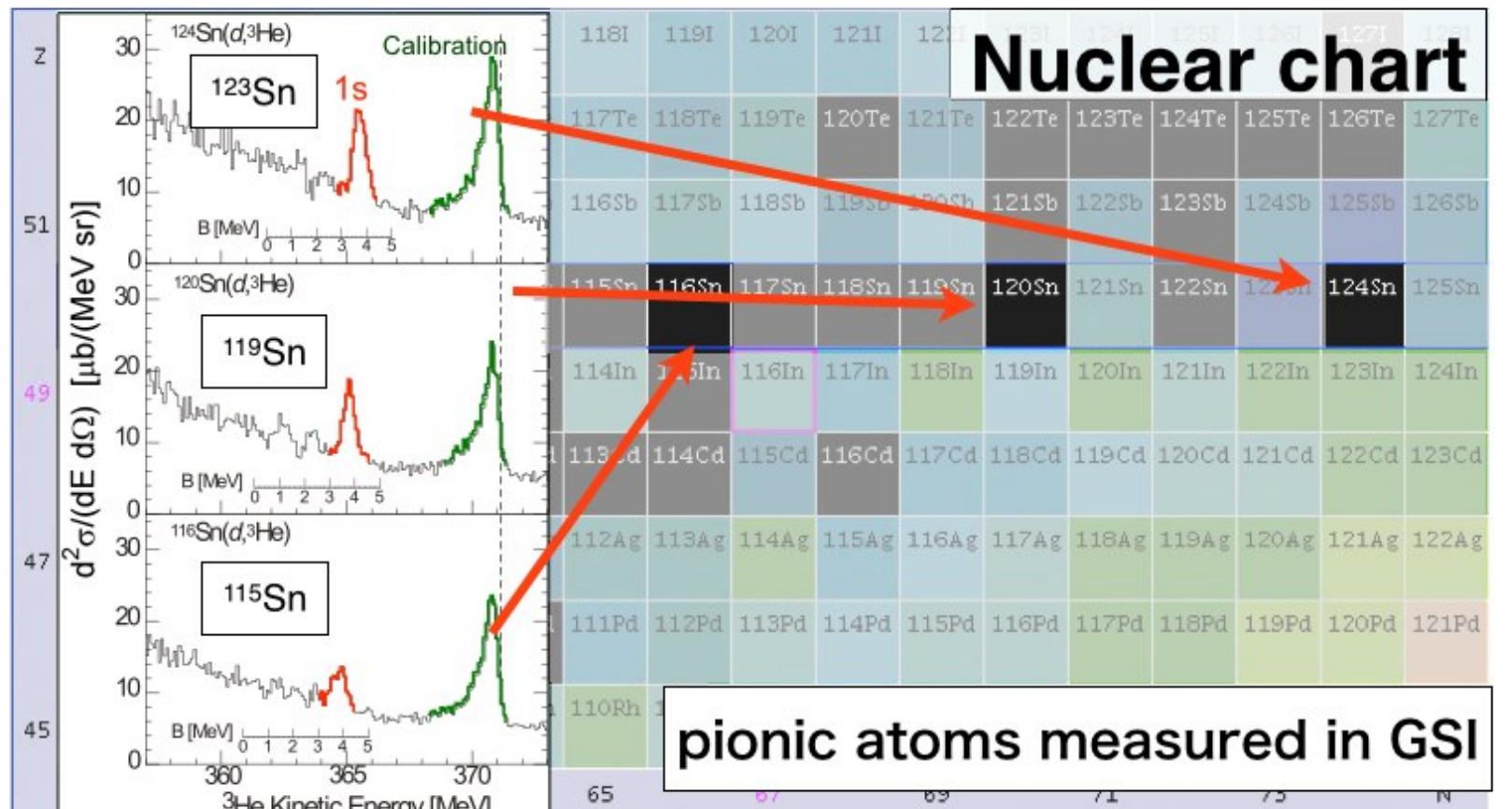
(i) Motivation and prior research

Our method: Missing mass spectroscopy



(i) Motivation and prior research

Prior research: Experiment at GSI



K. Suzuki et al., PRL92 072302 (2004)

NuDat

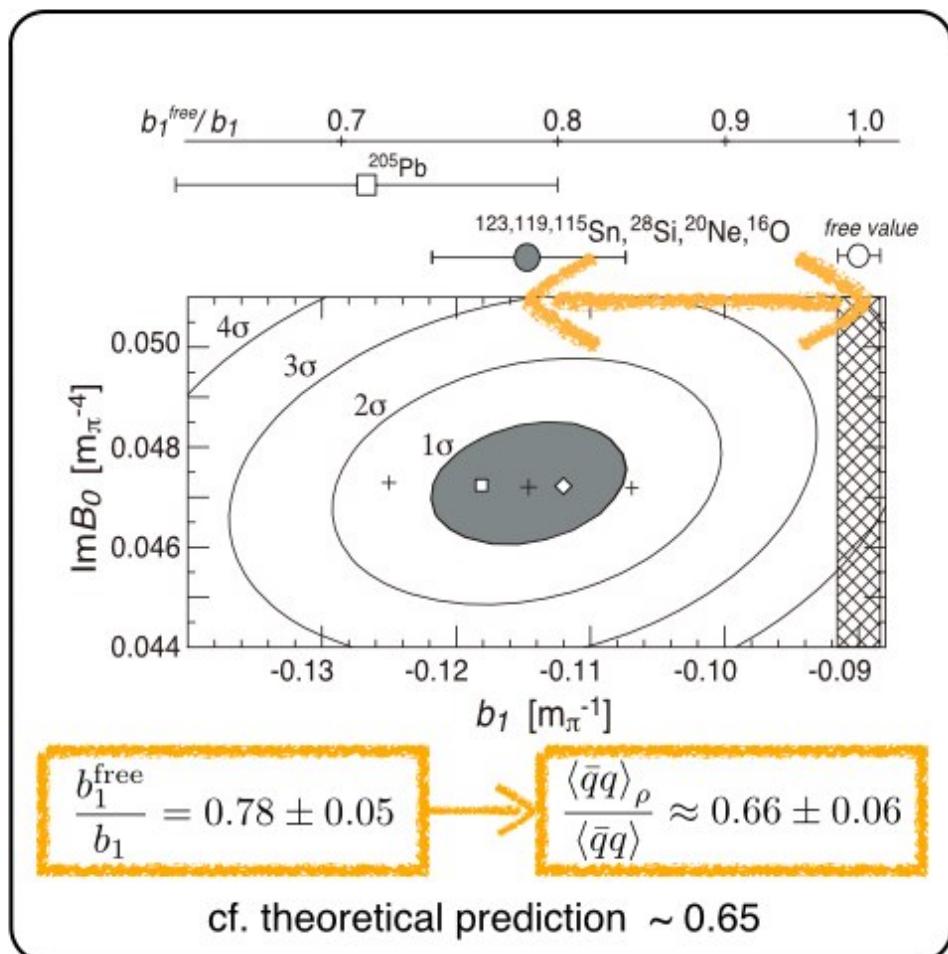
Systematic study of pionic Sn isotopes

~ 3 month measurement for 3 isotopes

(i) Motivation and prior research

Extract b_1 from experimental data at GSI

Contour plot of χ^2



π -A s-wave optical potential

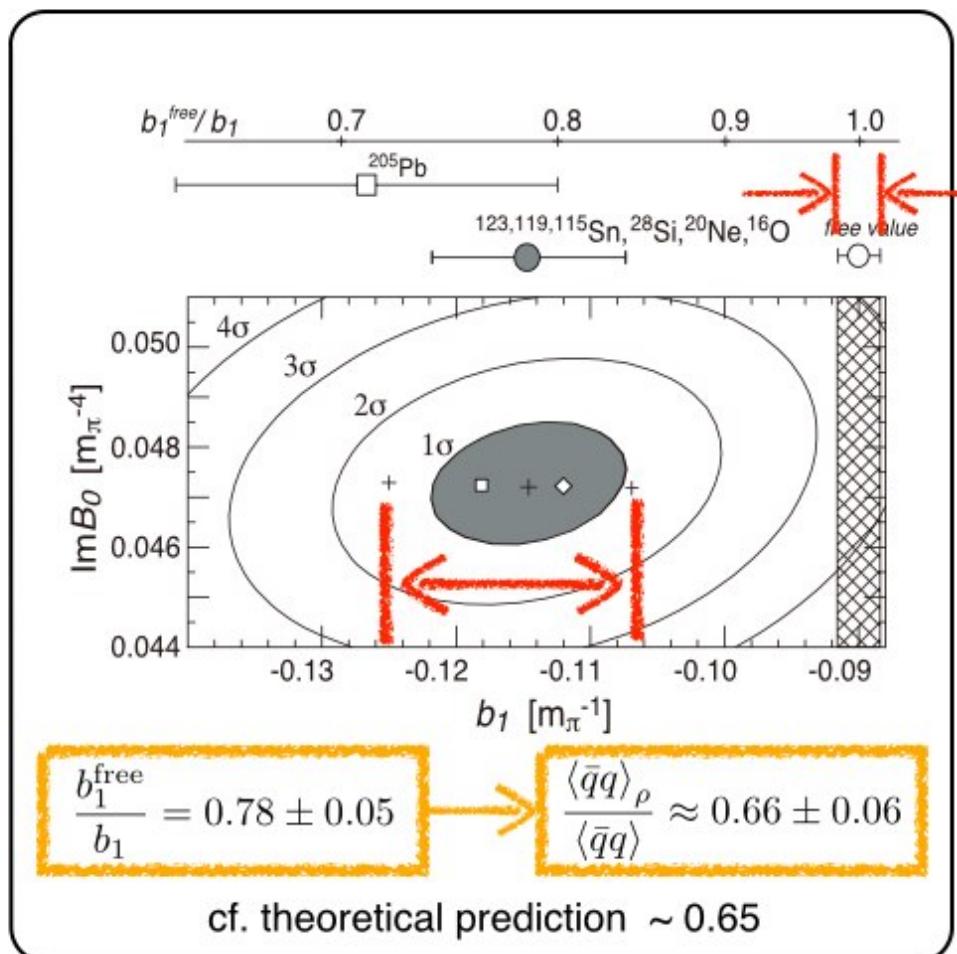
$$V_s(r) = -\frac{2\pi}{\mu} [\epsilon_1 \{b_0 \rho + b_1 \delta \rho\} + \epsilon_2 B_0 \rho^2]$$

* b_0 , $\text{Re}B_0$ are deduced from data of light / symmetric pionic atoms

(i) Motivation and prior research

Extract b_1 from experimental data at GSI

Contour plot of χ^2



π -A s-wave optical potential

$$V_s(r) = -\frac{2\pi}{\mu} [\epsilon_1 \{b_0 \rho + b_1 \delta \rho\} + \epsilon_2 B_0 \rho^2]$$

error of b_1 in medium is still large compared with that in vacuum!!
two main sources are

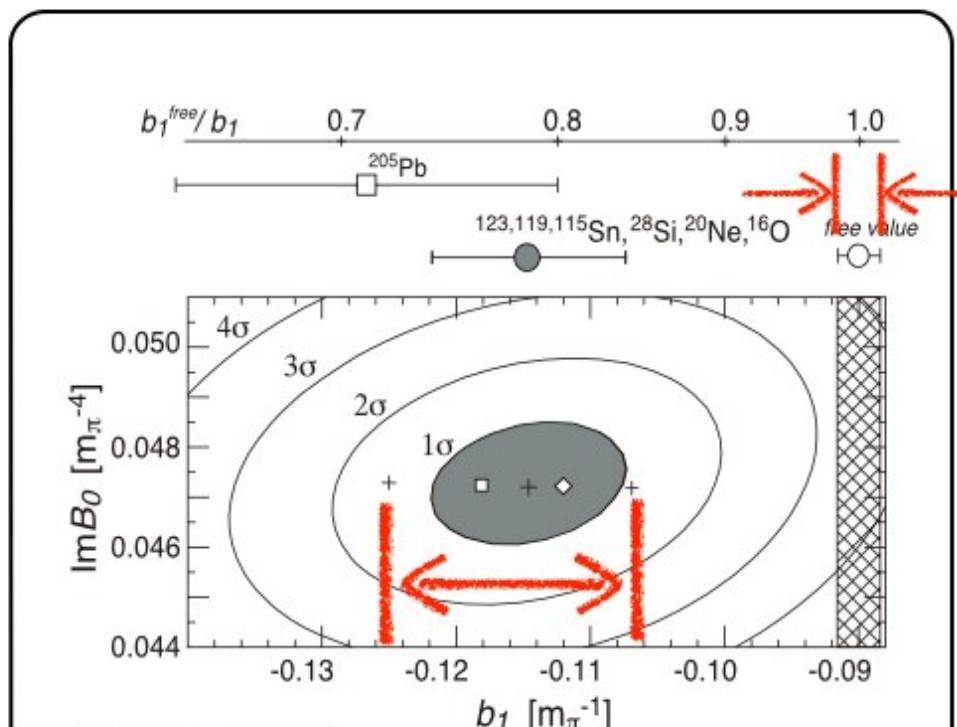
- experimental error
- neutron distribution ambiguities

* b_0 , $\text{Re}B_0$ are deduced from data of light / symmetric pionic atoms

(i) Motivation and prior research

Extract b_1 from experimental data at GSI

Contour plot of χ^2



π -A s-wave optical potential

$$V_s(r) = -\frac{2\pi}{\mu} [\epsilon_1 \{b_0 \rho + b_1 \delta \rho\} + \epsilon_2 B_0 \rho^2]$$

error of b_1 in medium is still large compared with that in vacuum!!
two main sources are

- experimental error
- neutron distribution ambiguities

$$\frac{b_1^{\text{free}}}{b_1} = 0.78 \pm$$

cf. theory

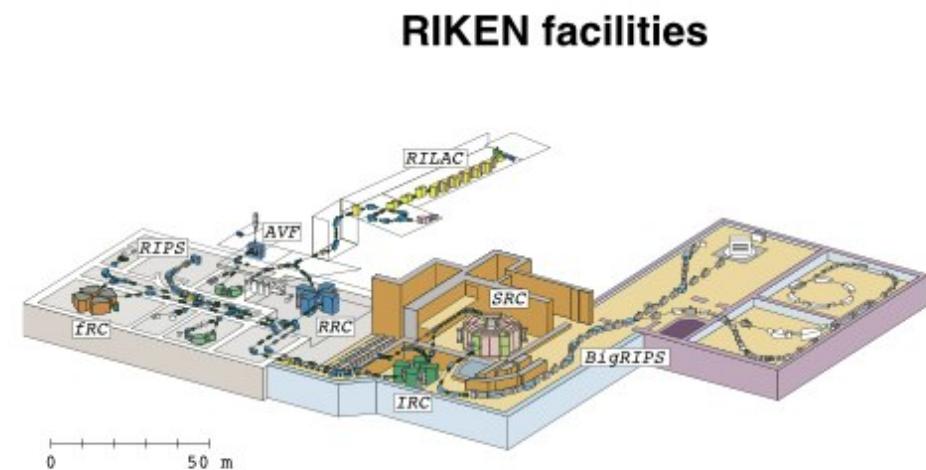
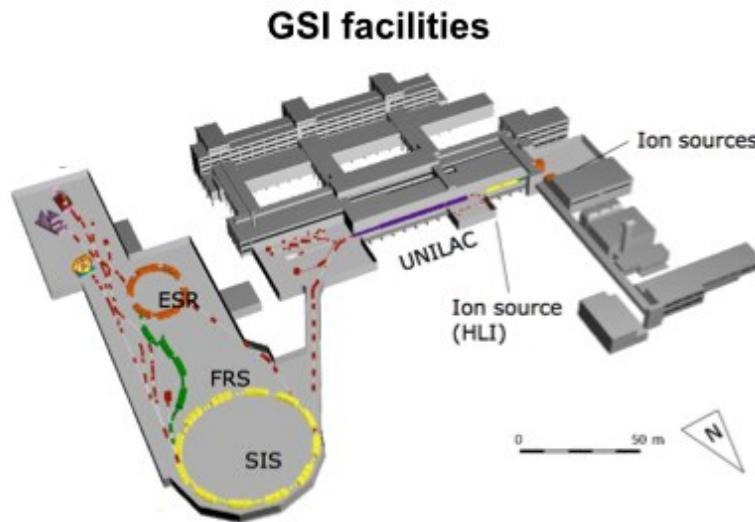
To extract b_1 with higher precision
improve resolution / calibration
More isotopes

(ii) Experiment performed in 2014 at RIKEN

First production experiment in 2014 @ RIKEN (11 days)

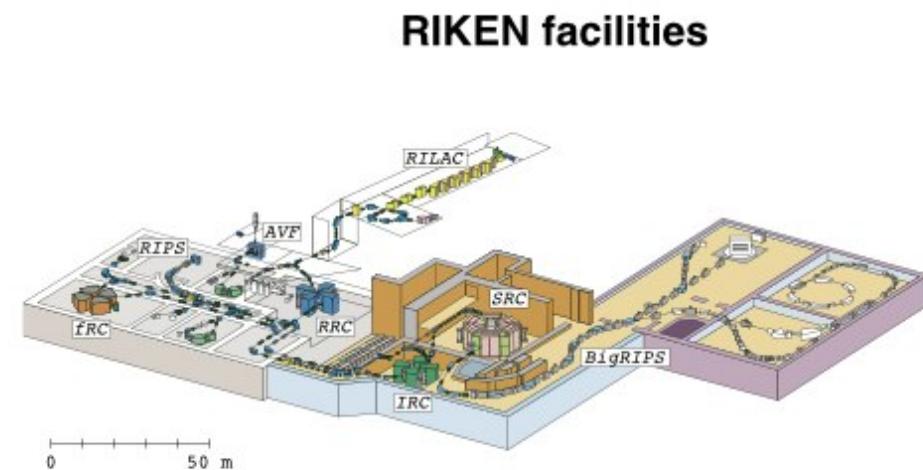
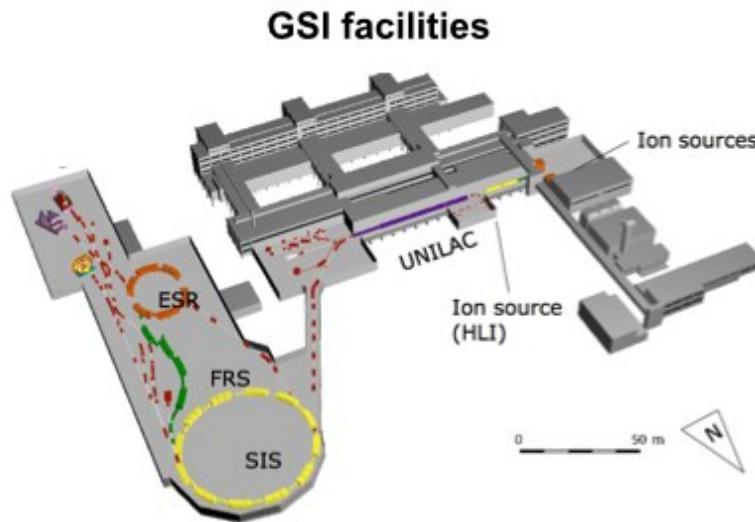


Comparison between RIBF and GSI



	GSI (FRS)	RIBF (BigRIPS)	Improvement
intensity	$\sim 10^{11}/6\text{ s}$ (1 spill)	$\sim 10^{12}/\text{s}$	$\times 60$
angular acceptance (H / V)	15 / 10 mrad	40 / 60 mrad	$\times 16$
resolution (FWHM)	400 keV	$\sim 600 \text{ keV}$	\searrow factor 1.5 ~ 2

Comparison between RIBF and GSI

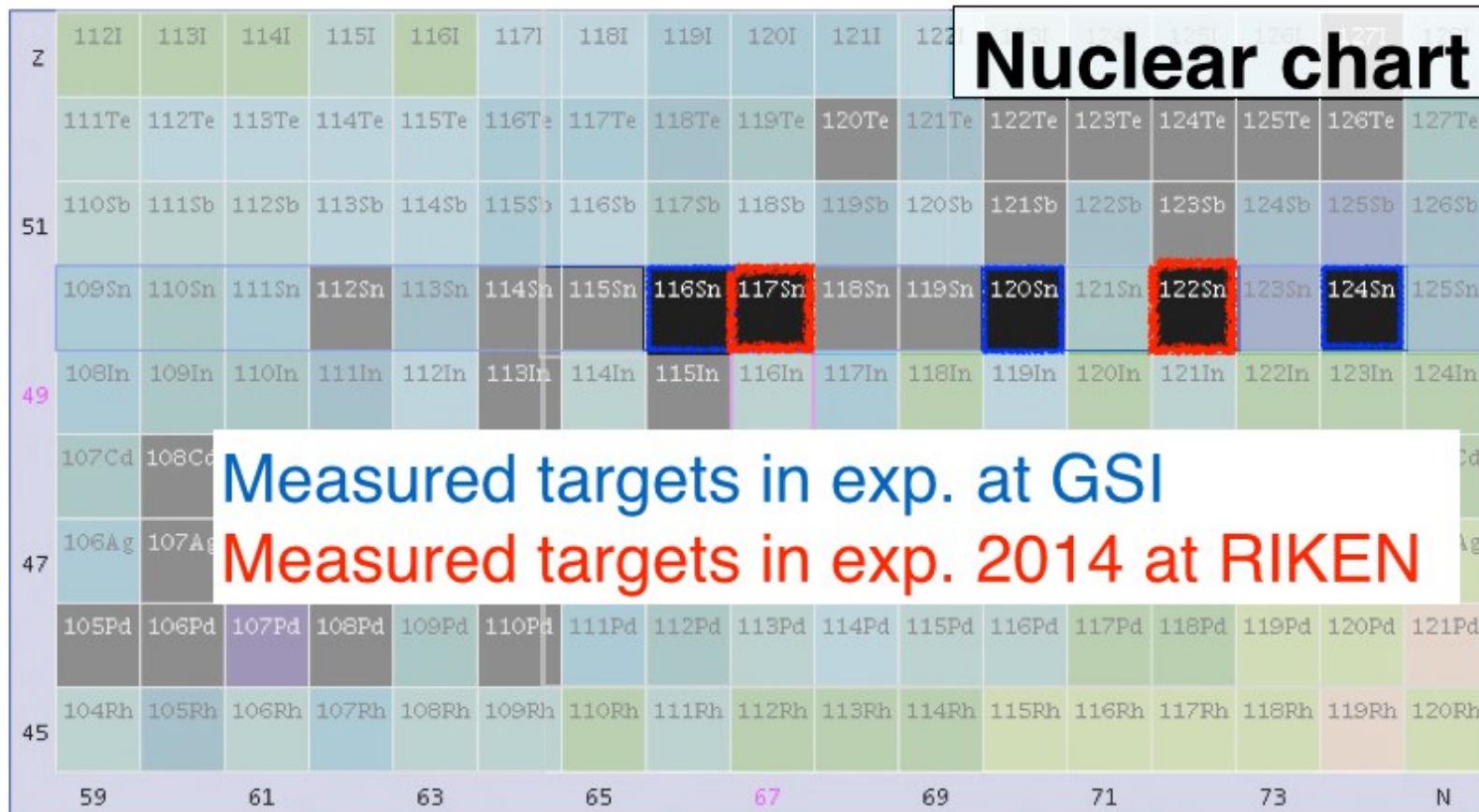


	GSI (FRS)	RIBF (BigRIPS)	Improvement
intensity	$\sim 10^{11} / 6 \text{ s}$ (1 spill)	$\sim 10^{12} / \text{s}$	$\times 60$
angular acceptance (H / V)	15 / 10 mrad	40 / 60 mrad	$\times 16$
resolution (FWHM)	400 keV	200 ~ 300 keV	improve

by dispersion matching optics

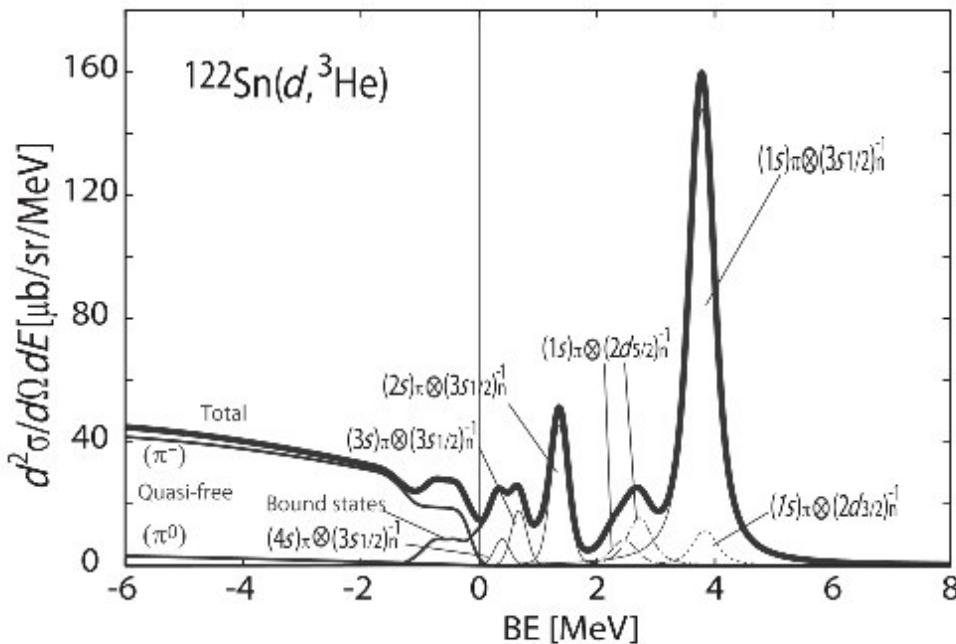
Targets in the experiment at RIKEN

NuDat

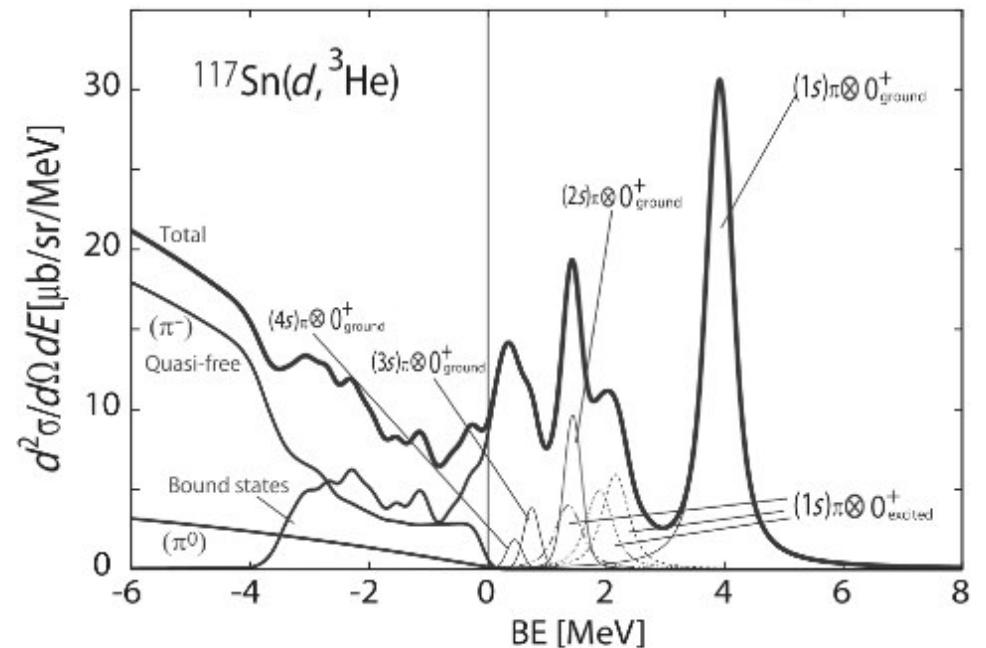


Expected excitation spectra

^{122}Sn : relatively large cross section



^{117}Sn : first odd-A target



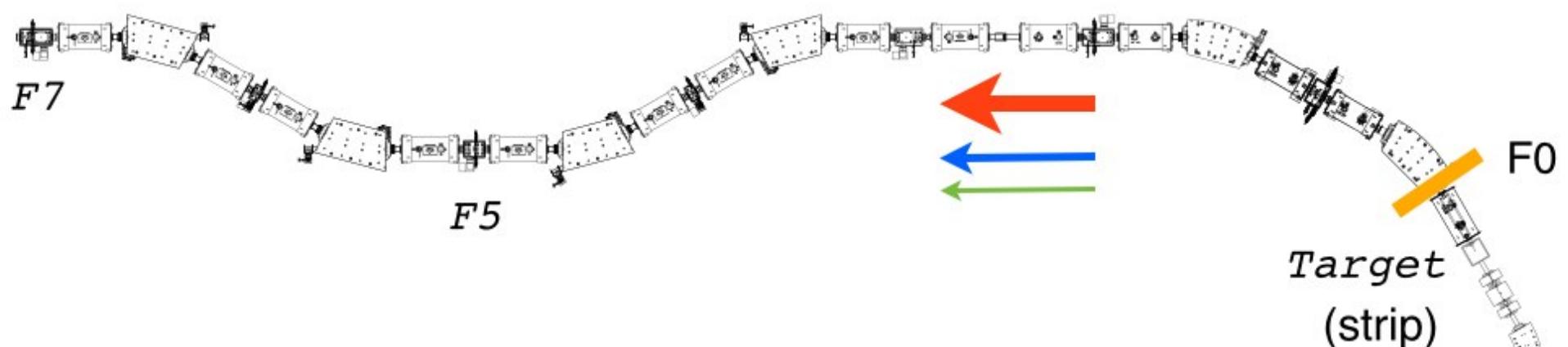
N. Ikeno et al., Prog. Theor. Exp. Phys. (2013) 2013 (6): 063D01.

Experimental setup

RIKEN Fragment Separator
BigRIPS

${}^3\text{He}$ $\sim 10^2$ Hz
(signal)

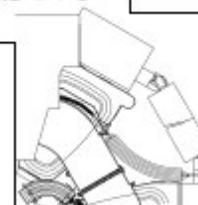
$p \sim 10^5$ Hz
(break up/ background)



SRC

Beam Transfer line

Superconducting
Ring
Cyclotron



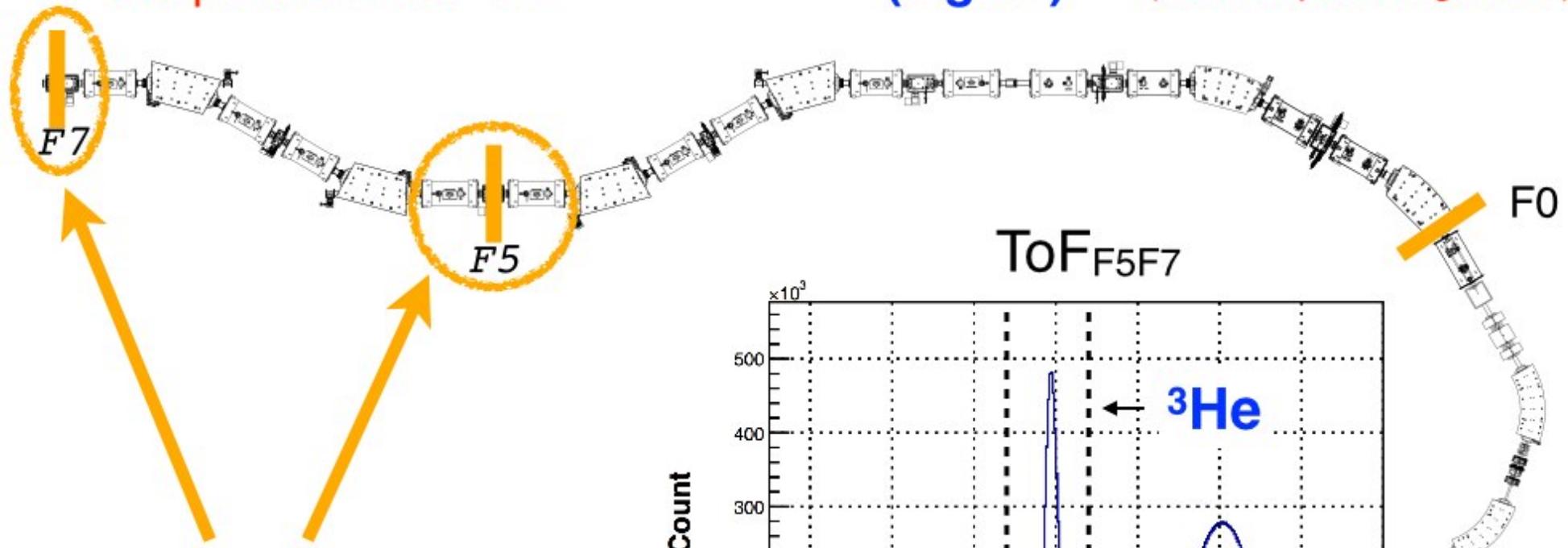
d beam 250 MeV/u
 $\sim 10^{12} / \text{s}$

Experimental setup

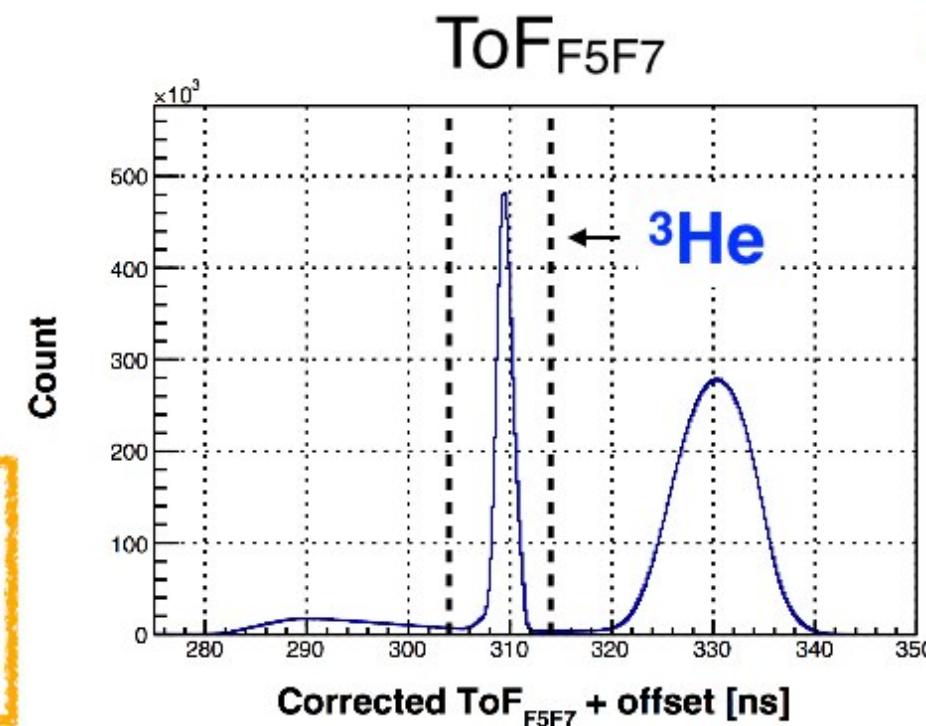
large part of p :
swept out in F5 - F7

${}^3\text{He} \sim 10^2 \text{Hz}$
(signal)

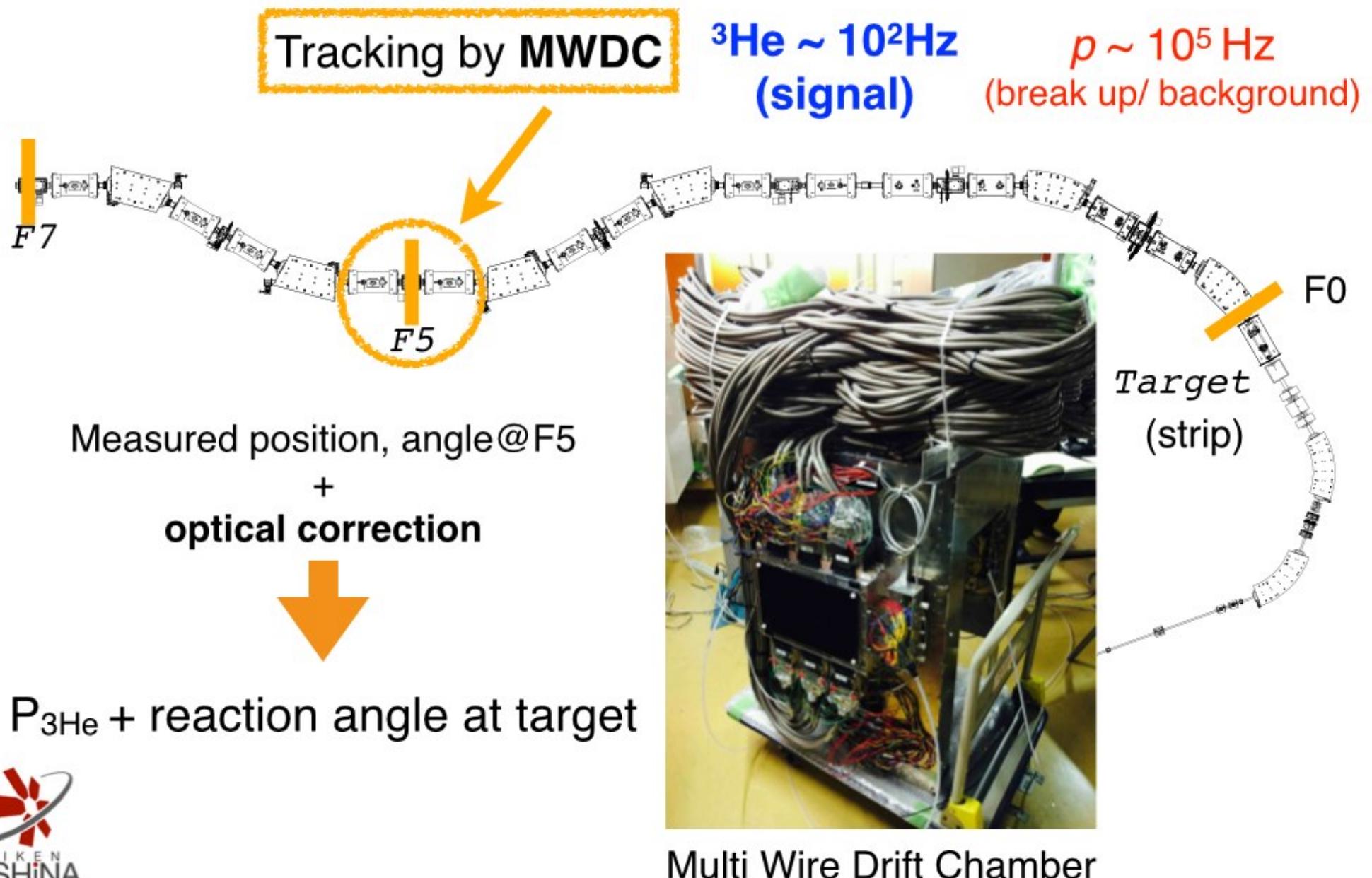
$p \sim 10^5 \text{ Hz}$
(break up/ background)



$\Delta E / \text{TOF measurement}$
(pID, hardware trigger)
by plastic scintillator



Experimental setup



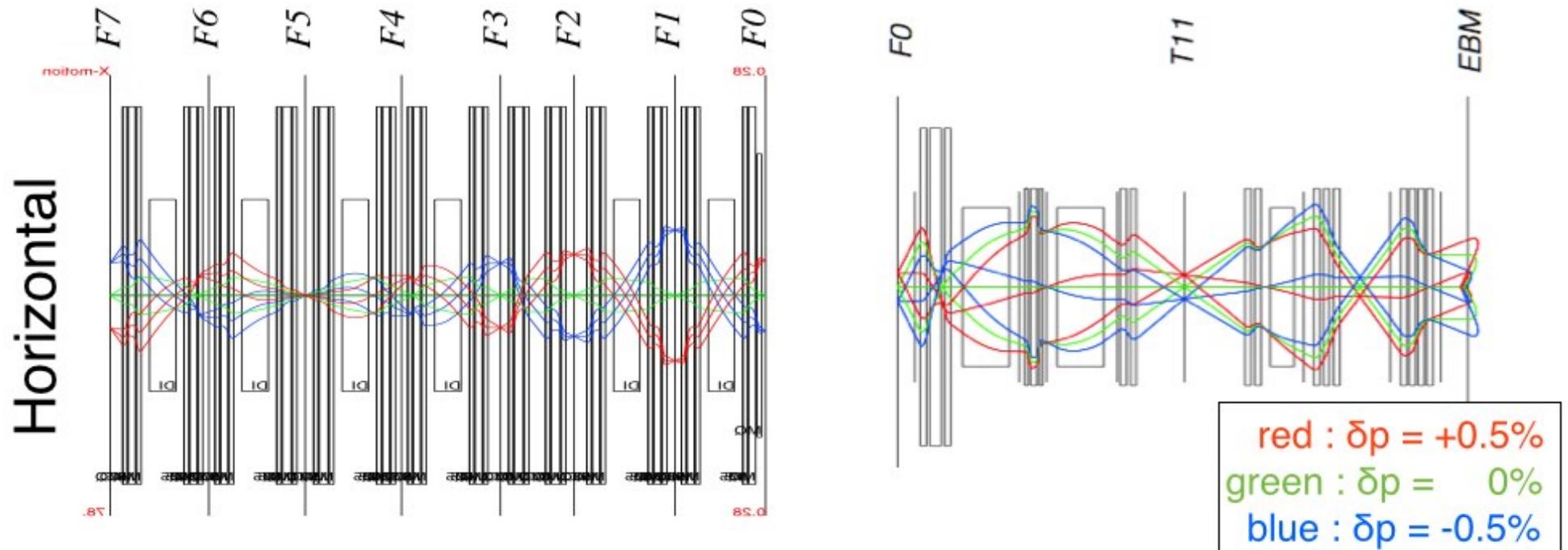
Ion optics (design)

Dispersion matching:
Eliminate contribution of beam momentum spread

Spectrometer (BigRIPS)	reaction	Analyzer (Beam Transfer Line)
$\begin{pmatrix} x_{fp} \\ \theta_{fp} \\ \delta p_{fp} \end{pmatrix} = \begin{pmatrix} S_{11} & S_{12} & S_{16} \\ S_{21} & S_{22} & s_{26} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & C \end{pmatrix} \begin{pmatrix} A_{11} & A_{12} & A_{16} \\ A_{21} & A_{22} & A_{26} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x_0 \\ \theta_0 \\ \delta p_0 \end{pmatrix}$		
F5	*C: kinematical factor = 1.31	inside SRC

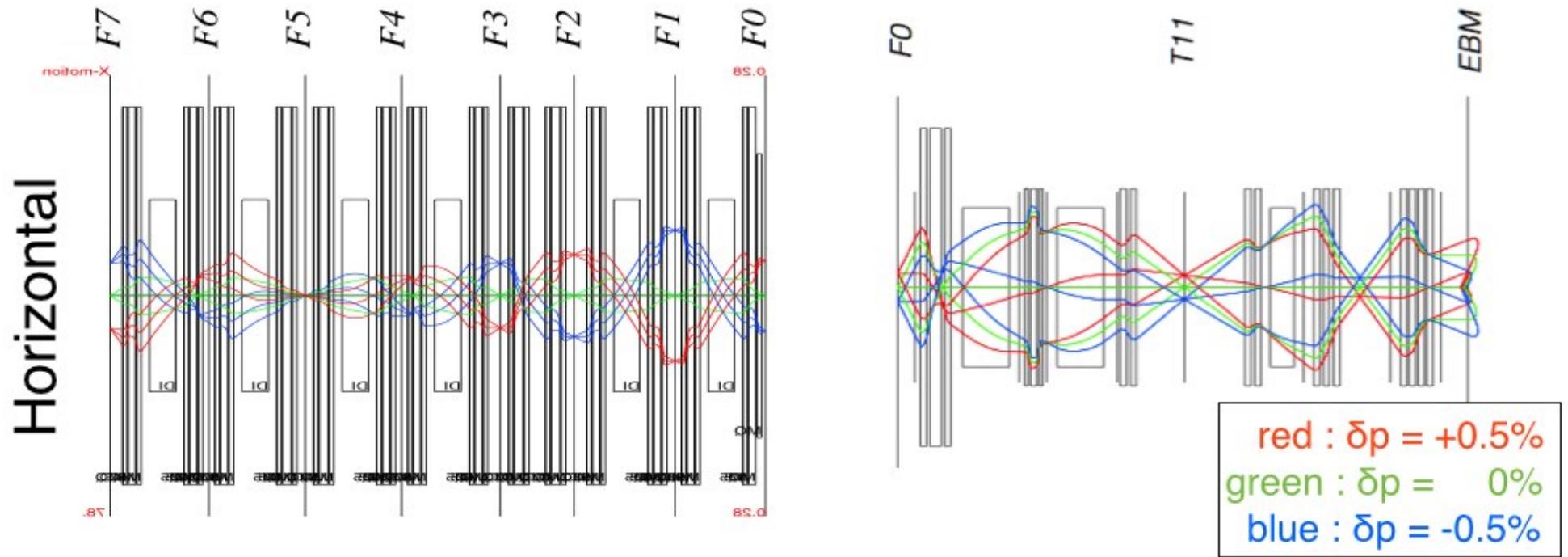
$$x_{fp} = \dots + \underbrace{(S_{11}A_{16} + CS_{16})\delta p_0}_{\text{red line}} + \underbrace{\dots}_{\text{blue line}}$$

Ion optics (design)



$$x_{fp} = \dots + \underbrace{(S_{11}A_{16} + CS_{16})}_{\text{red}} \delta p_0 + \underbrace{\dots}_{\text{blue}}$$

Ion optics (design)

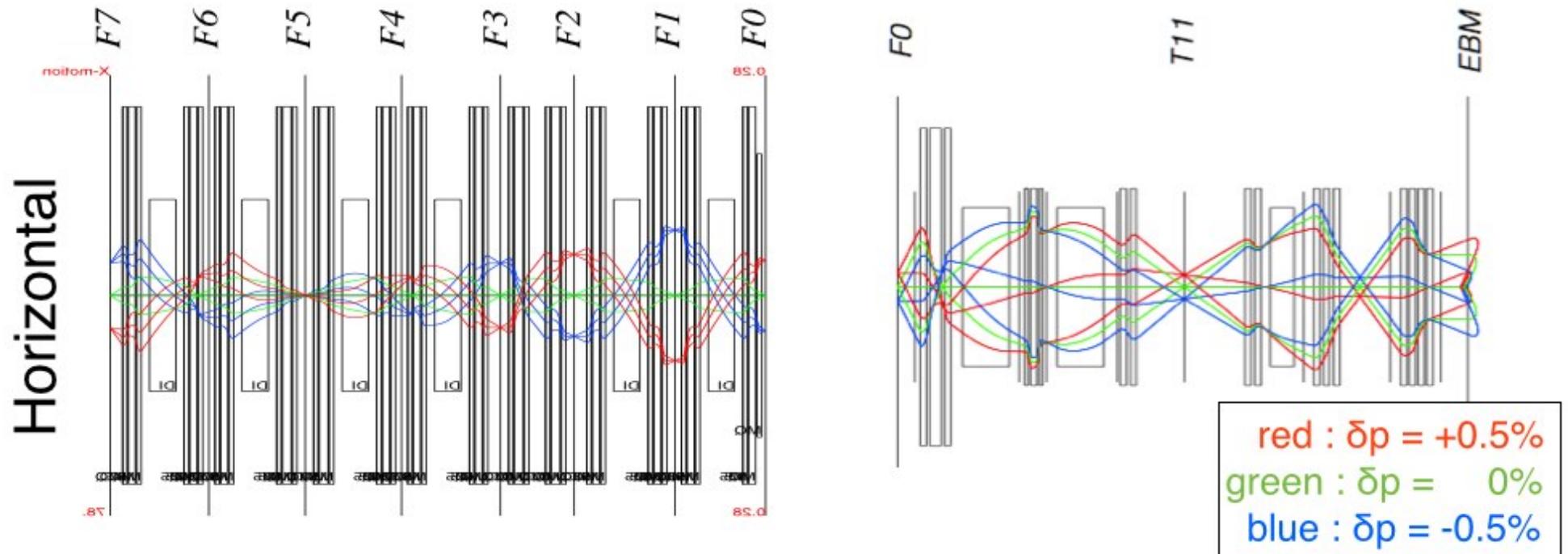


$$x_{fp} = \dots + (S_{11}A_{16} + CS_{16})\delta p_0$$

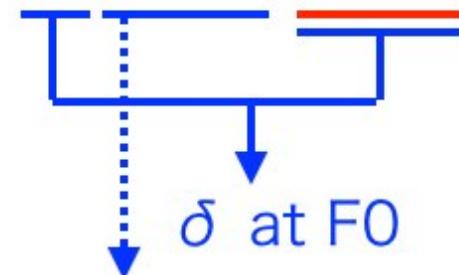
magnification of
BigRIPS

position at F0

Ion optics (design)

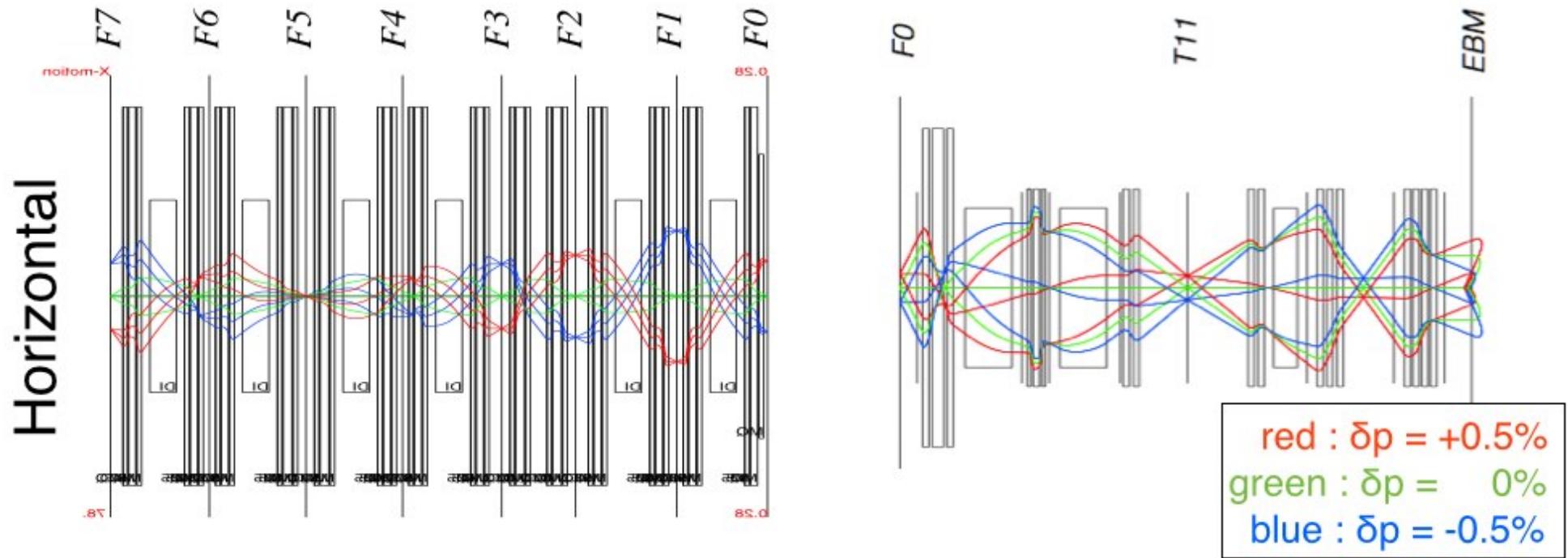


$$x_{fp} = \dots + \underline{(S_{11}A_{16} + CS_{16})\delta p_0}$$



dispersion of BigRIPS

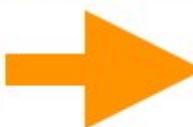
Ion optics (design)



$$x_{fp} = \dots + \underbrace{(S_{11}A_{16} + CS_{16})}_{\text{Cancel out}} \delta p_0$$

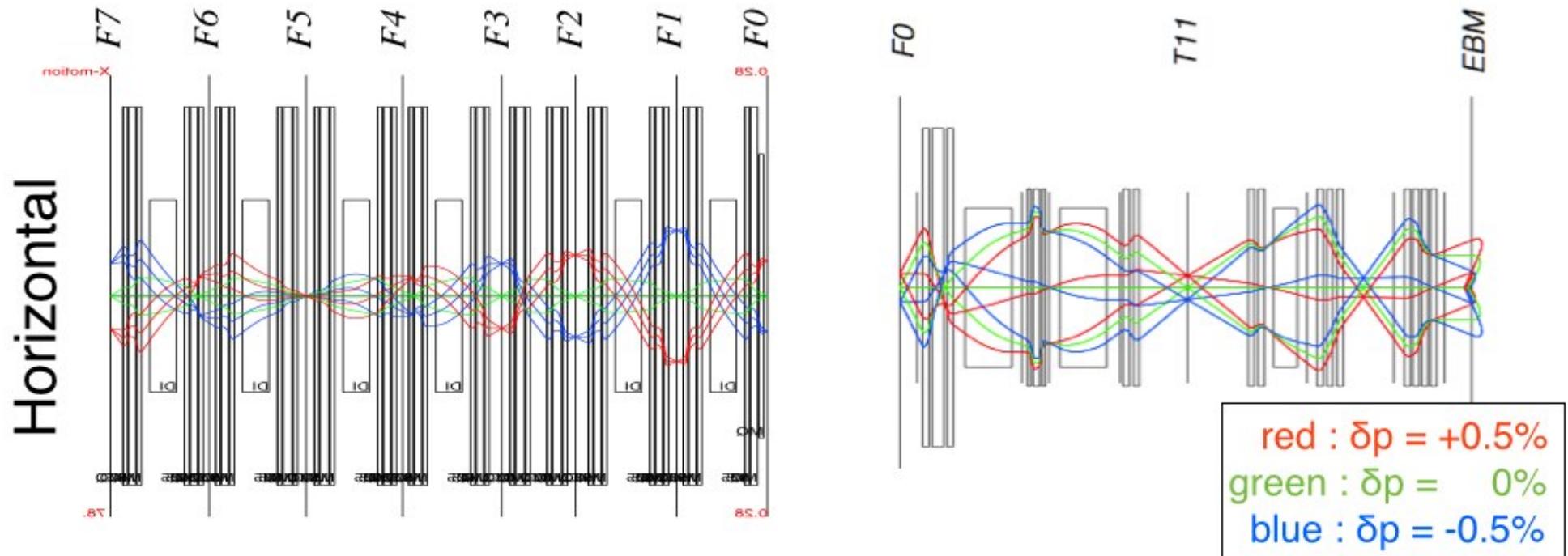
← → Cancel out

same Q value
different primary beam Energy



same position at F5

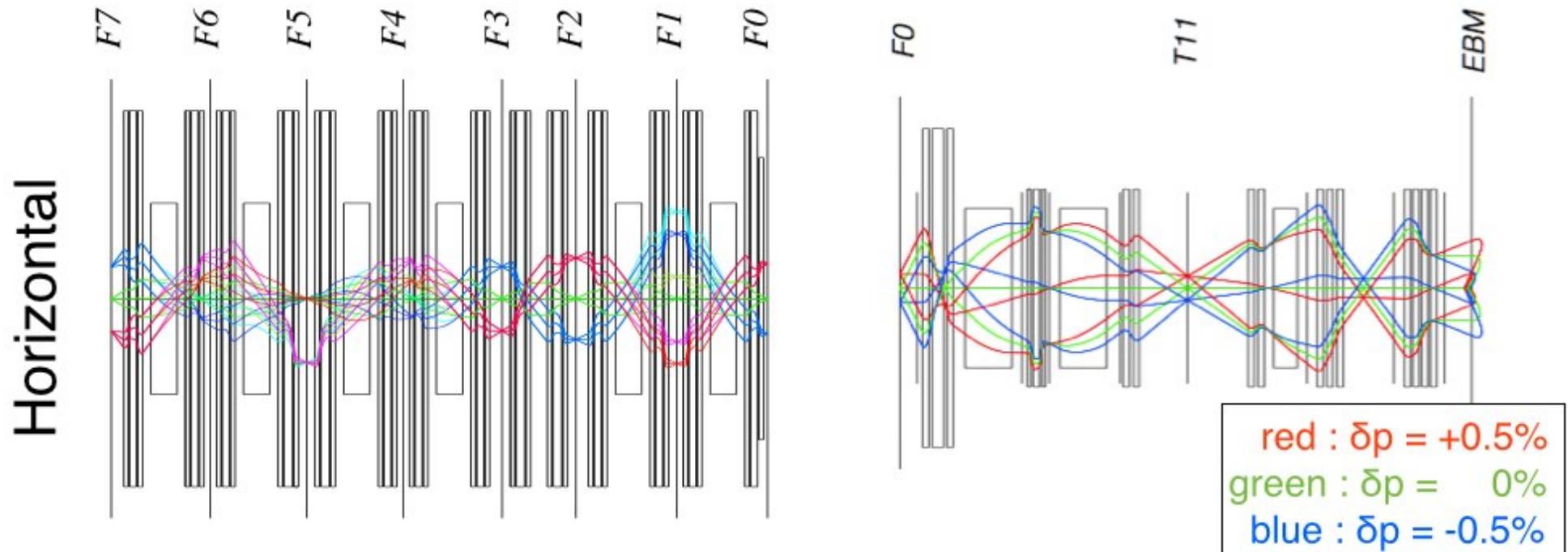
Ion optics (design)



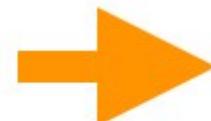
$$x_{fp} = \dots + \underbrace{(S_{11}A_{16} + CS_{16})}_{\text{Red arrow}} \delta p_0 + \underbrace{C}_{\text{Blue arrow}} \delta p_0 \xrightarrow{\text{Cancel out}}$$

design values: $S_{11} = -1.8$ $A_{16} = 44.6 \text{ mm}/\%$
 $C = 1.31$ $S_{16} = 62 \text{ mm}/\%$

Ion optics (design)

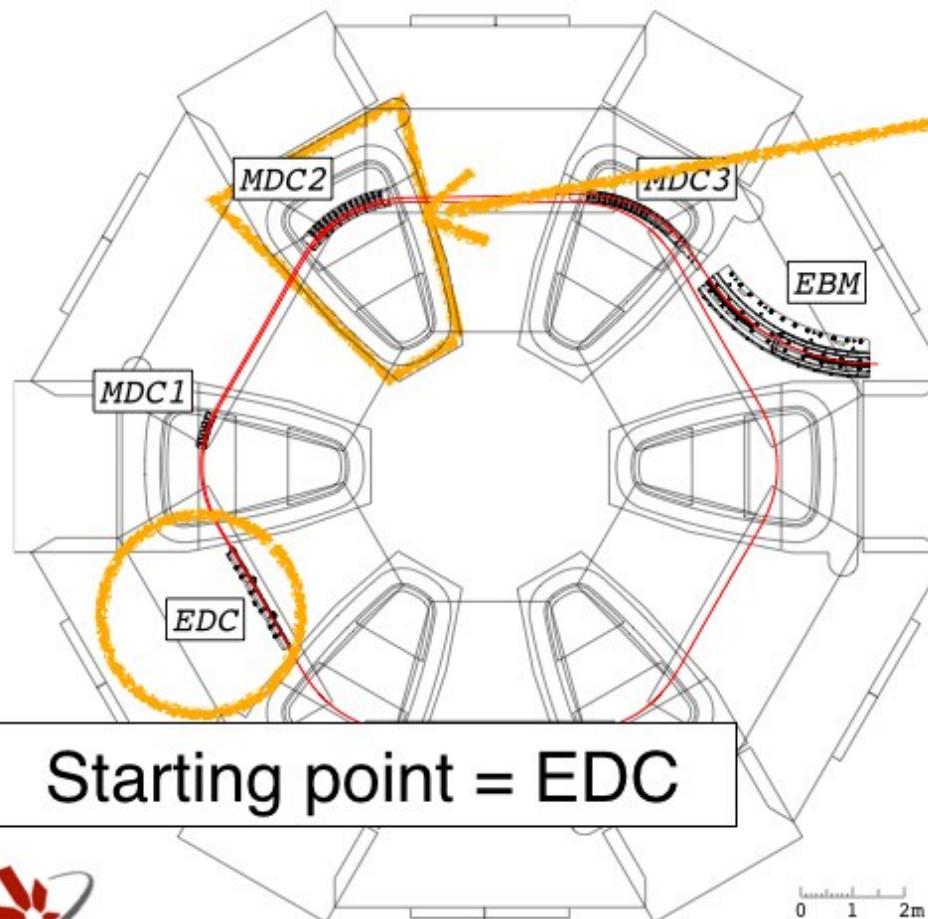


$$x_{fp} = \dots + \underbrace{(S_{11}A_{16} + CS_{16})}_{\text{red}} \delta p_0 + \underbrace{C}_{\text{blue}}$$

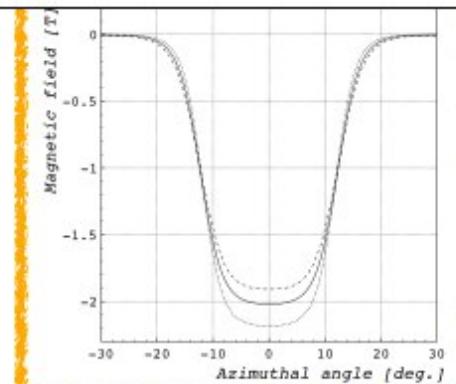


Ion Optics inside SRC (calc.)

Dispersion matching using primary beam



magnetic field in the magnet



calculate the transfer matrix
using Runge-Kutta method

$$\begin{aligned}
 & \begin{pmatrix} (x|x) & (x|a) & (x|y) & (x|b) & (x|\delta) \\ (a|x) & (a|a) & (a|y) & (a|b) & (a|\delta) \\ (y|x) & (y|a) & (y|y) & (y|b) & (y|\delta) \\ (b|x) & (b|a) & (b|y) & (b|b) & (b|\delta) \end{pmatrix}_{\text{EDC} \rightarrow \text{EBM}} \\
 &= \begin{pmatrix} -1.00 & -3.35 & 0.0 & 0.0 & 76.9 \\ 0.30 & -0.01 & 0.0 & 0.0 & -25.4 \\ 0.0 & 0.0 & -1.03 & -1.75 & 0.0 \\ 0.0 & 0.0 & -0.09 & -1.12 & 0.0 \end{pmatrix}
 \end{aligned}$$

Key points of the experiment for better resolution

- ① Tuning of the beam transfer line optics
→ realize dispersion matching
 - ② Reduce the primary beam emittance / δp
- ① × ② ⇒ contribution of δp on resolution

① Tuning of the beam transfer line optics

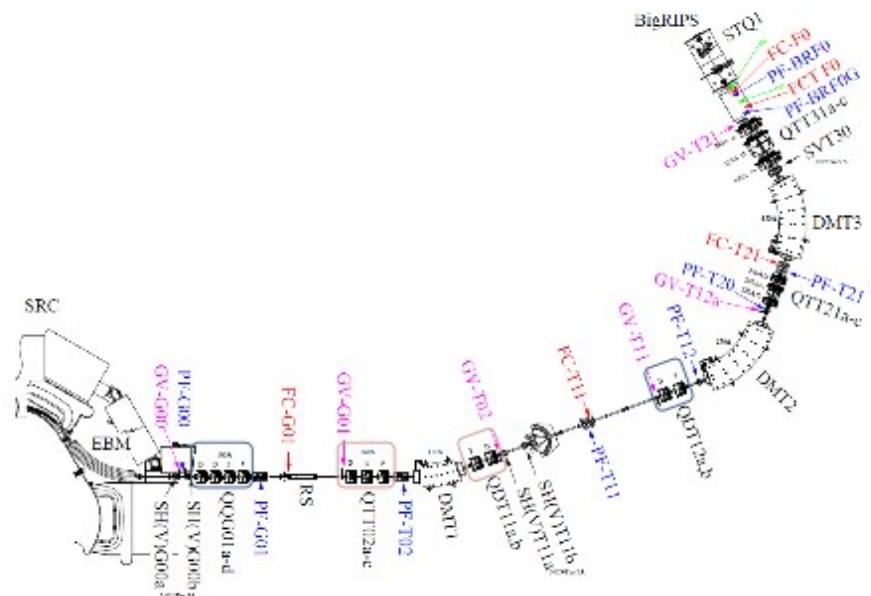
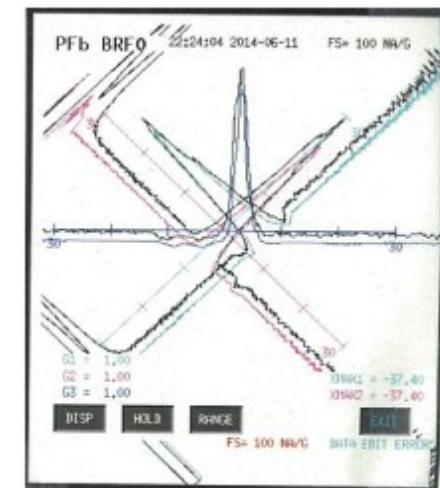
beam envelope measured by profile monitor

Diagnostics in BT line

- ~ 10 profile monitors (wires)
 - **No tracker**



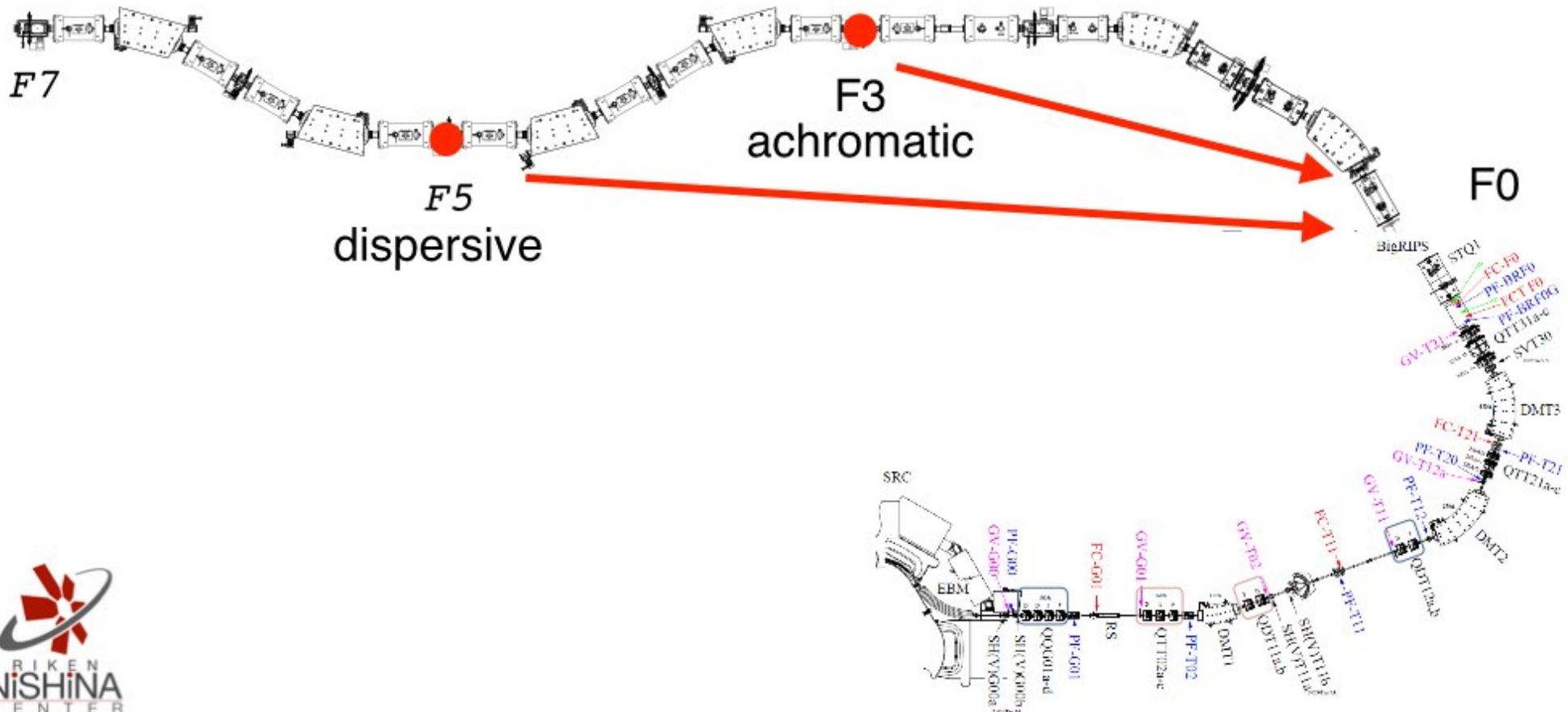
not enough to measure dispersion / other transfer matrix



① Tuning of the beam transfer line optics

Use BigRIPS as a diagnostics of BT line

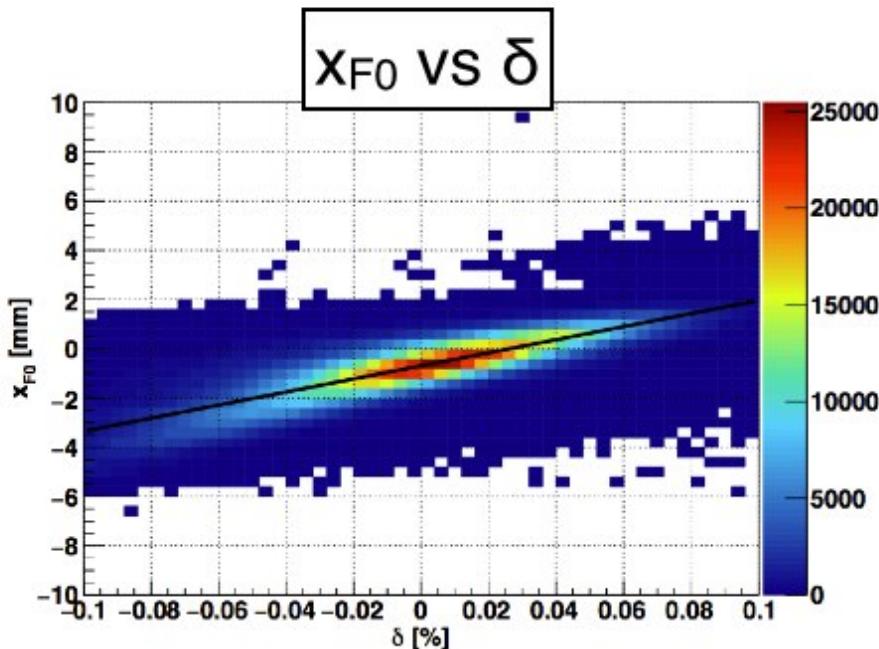
- measure the position / angle at F3 and F5 focal plane
- trace back to F0



① Tuning of the beam transfer line optics

Use BigRIPS as a diagnostics of BT line

- measure the position / angle at F3 and F5 focal plane
- trace back to F0

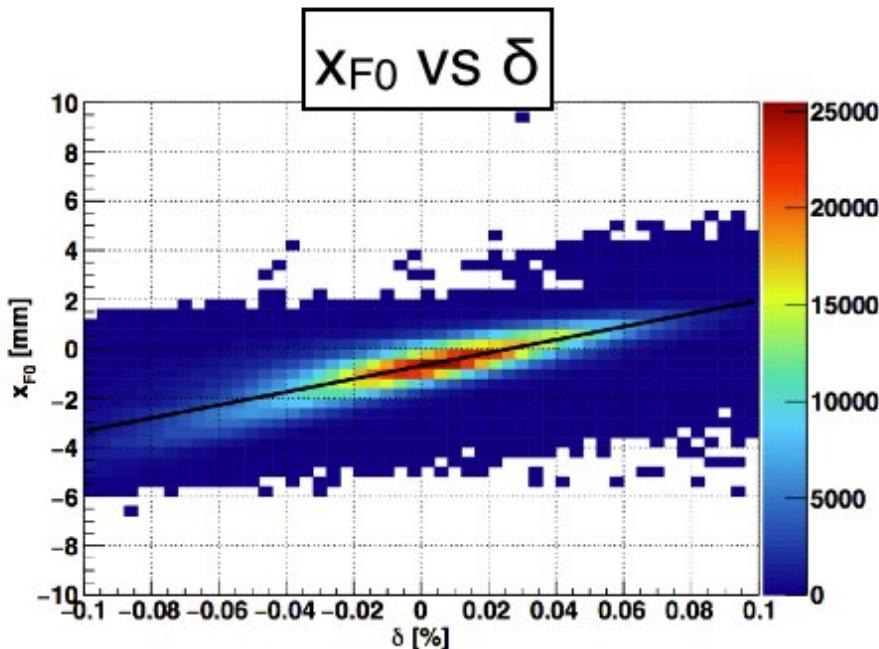


measured dispersion in BT line

① Tuning of the beam transfer line optics

Use BigRIPS as a diagnostics of BT line

- measure the position / angle at F3 and F5 focal plane
- trace back to F0



measured dispersion in BT line
→ 24 mm/% !!!

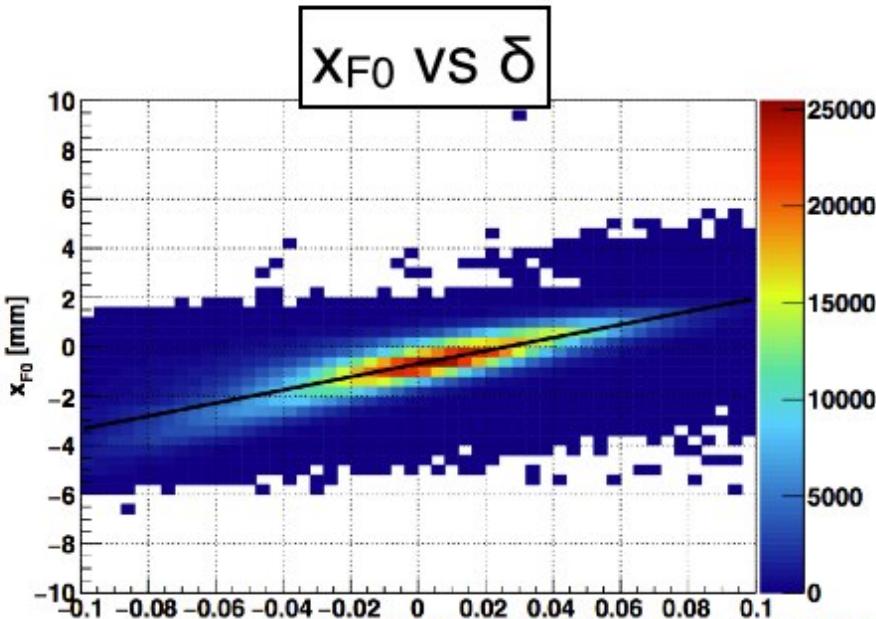
(cf. designed value: 44.6 mm/%)

The difference may be caused
by the optics inside SRC

① Tuning of the beam transfer line optics

Use BigRIPS as a diagnostics of BT line

- measure the position / angle at F3 and F5 focal plane
- trace back to F0



measured dispersion in BT line
→ **24 mm/% !!!**

(cf. designed value: 44.6 mm/%)

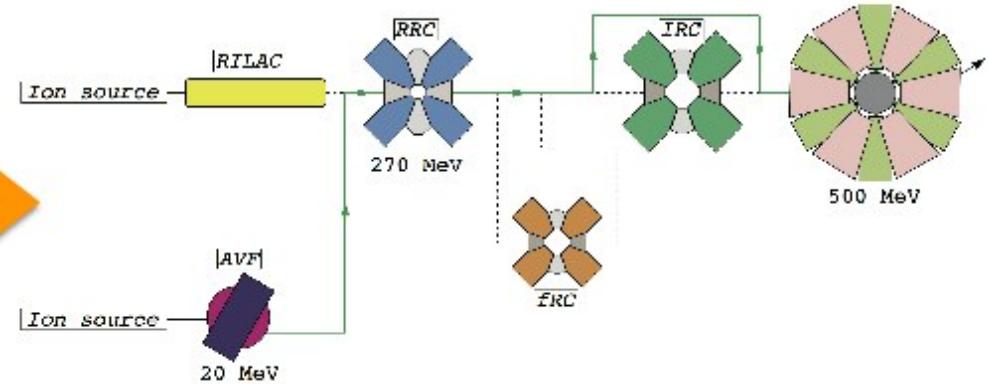
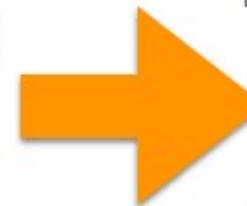
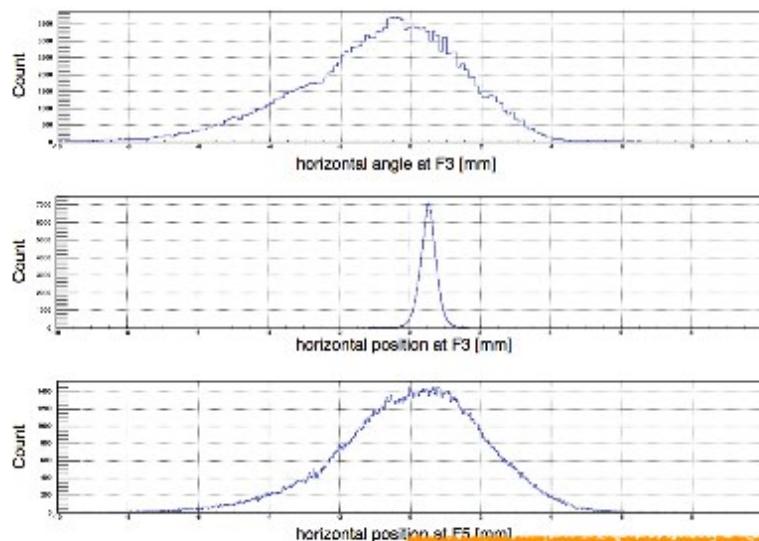
The difference may be caused
by the optics inside SRC

After phenomenological tuning,
dispersion is improved to be **28 mm/%**
↔ reduce the contribution of δp by ~ 50%

② Reduce the primary beam emittance / δp

Use BigRIPS as a diagnostics of Primary beam

- position and angle distribution at achromatic focal plane (F3)
→ beam emittance
- position distribution at dispersive focal plane (F5)
→ δp



feedback to the accelerator team
to tune accelerator parameters / slit condition
achieve **$0.2 \times 2.0 \text{ mm} \cdot \text{mrad} / 0.03 \% (\text{RMS})$**

Contribution of δp on resolution

- ① Tuning of the beam transfer line optics
→ dispersion **28 mm/%** \Leftrightarrow reduce the contribution by **$\sim 50\%$**
- ② Reduce the primary beam emittance / δp
→ achieve **$0.2 \times 2.0 \text{ mm} \cdot \text{mrad} / 0.03\% \text{ (RMS)}$**

$$\textcircled{1} \times \textcircled{2} \Rightarrow \textcolor{red}{\sim 220 \text{ keV (FWHM)}}$$

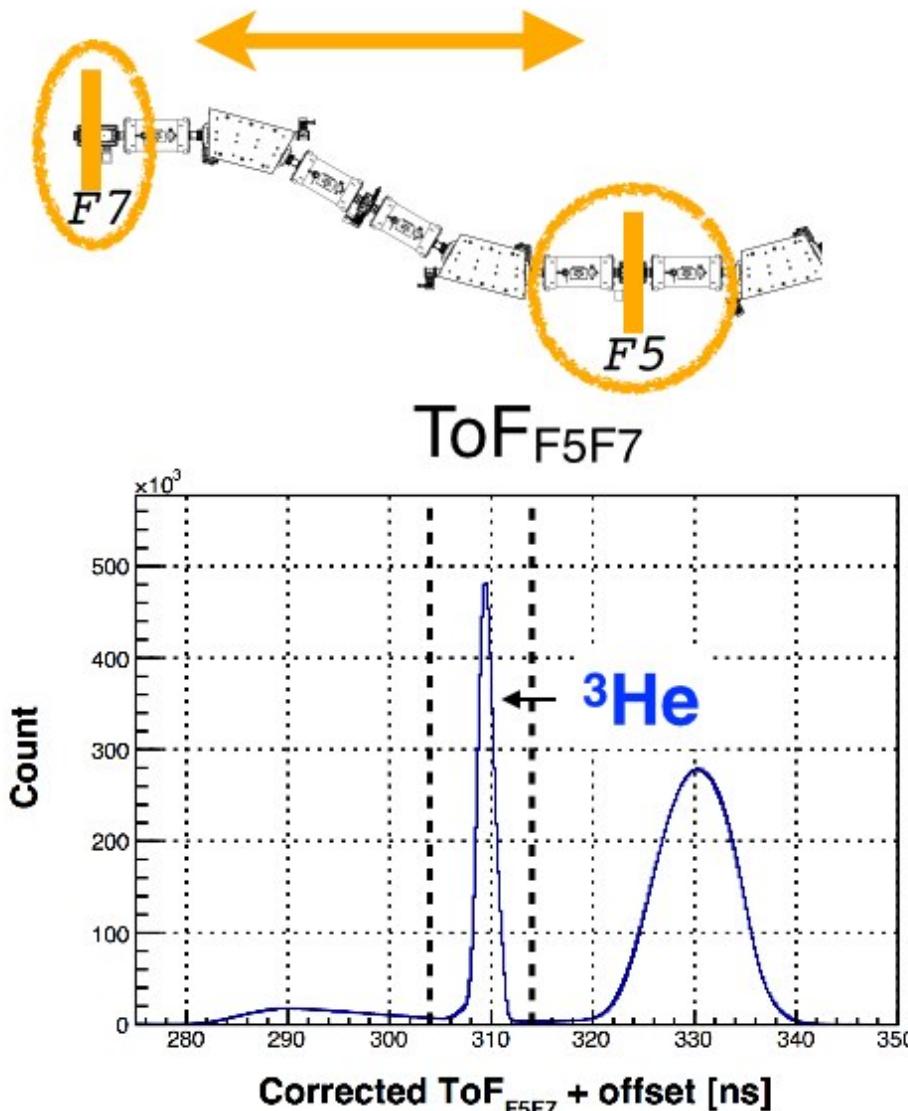
acceptable compared with $\Gamma_{1s} \sim 300 \text{ keV}$

* With other contributions, resolution is estimated
to be $250 \sim 400 \text{ keV}$ (position dependent)

(iii) Data analysis (pID / optics / decomposition)

- Particle identification
- Optics analysis
- Decomposition of Eex spectra

Particle identification



${}^3\text{He}$ is well separated only with ToF.
Using additional information of

- Eloss in MWDC (as ToT)
- relative timing with RF of SRC

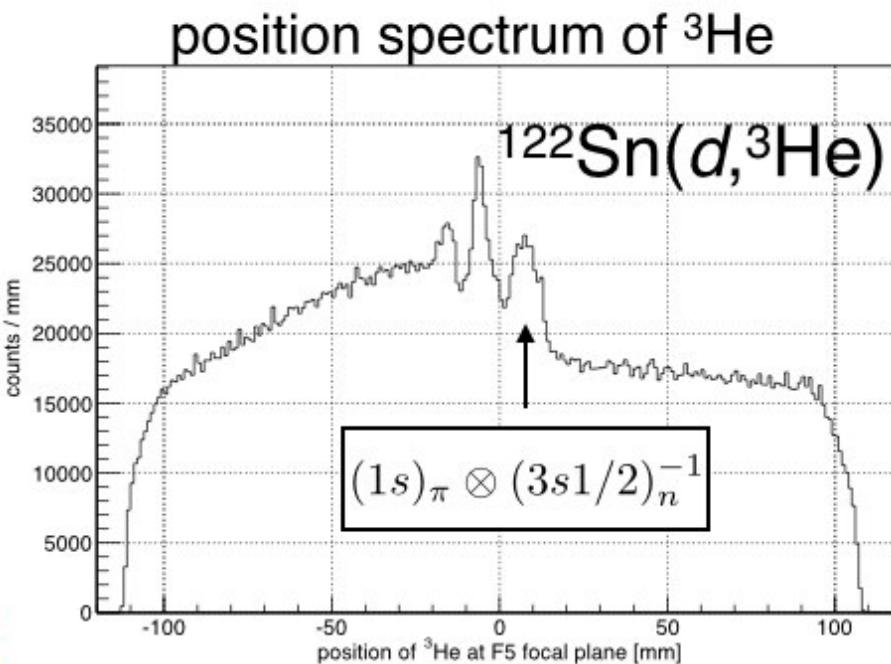
We achieve

efficiency : $\geq 98\%$
purity : $\geq 99.5\%$

Optics analysis

To convert the position spectrum to Eex spectra, we should

- ① measure the **dispersion**
- ② correct the **optical higher order aberration**



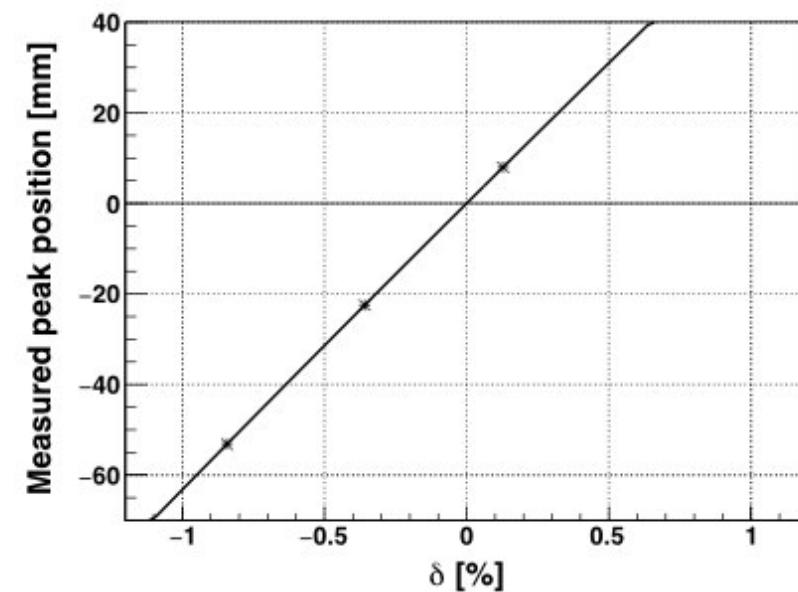
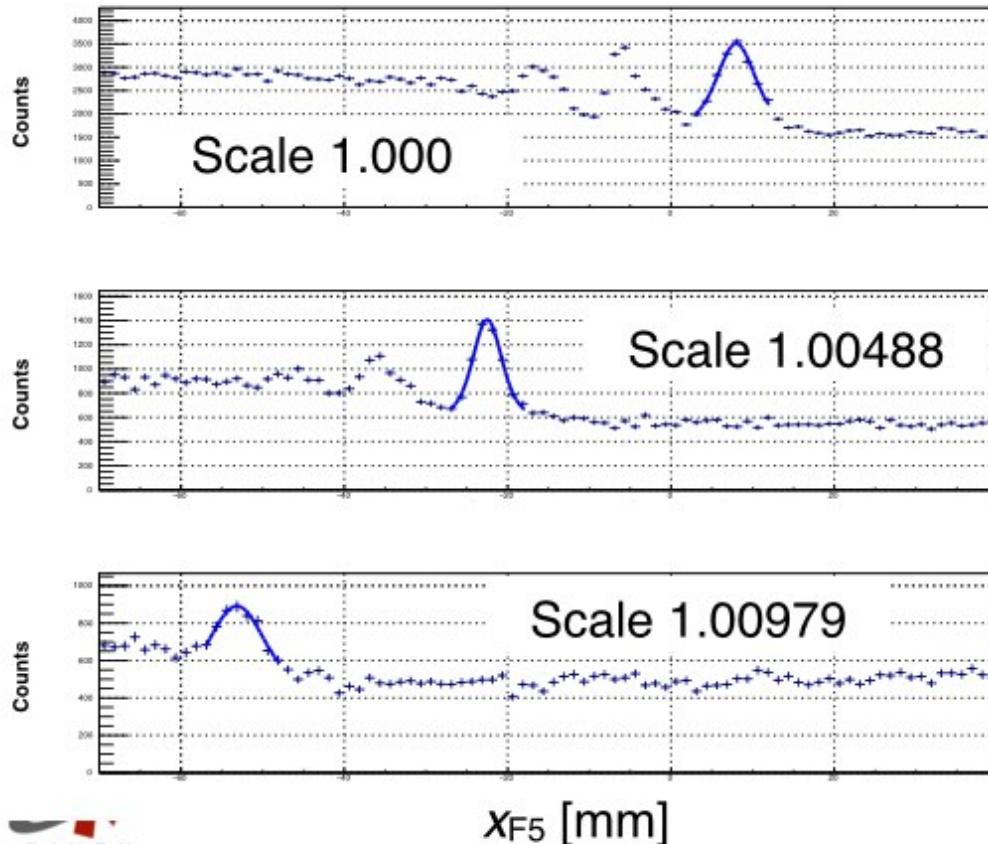
To analyze the optics,
we used the peak of $(1s)_\pi \otimes (3s1/2)_n^{-1}$

- sufficient strength in forward θ
- no angle dependence of Eex

① Dispersion of BigRIPS

$$\delta = (P_{^3He}^{1s} - P_{\text{BigRIPS}})/P_{\text{BigRIPS}} * 100.$$

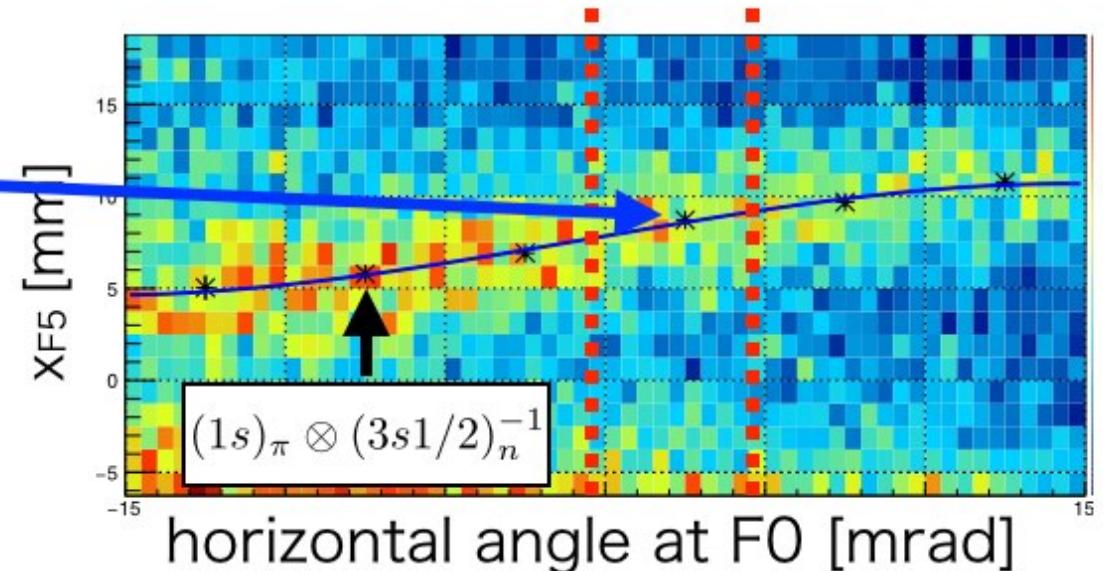
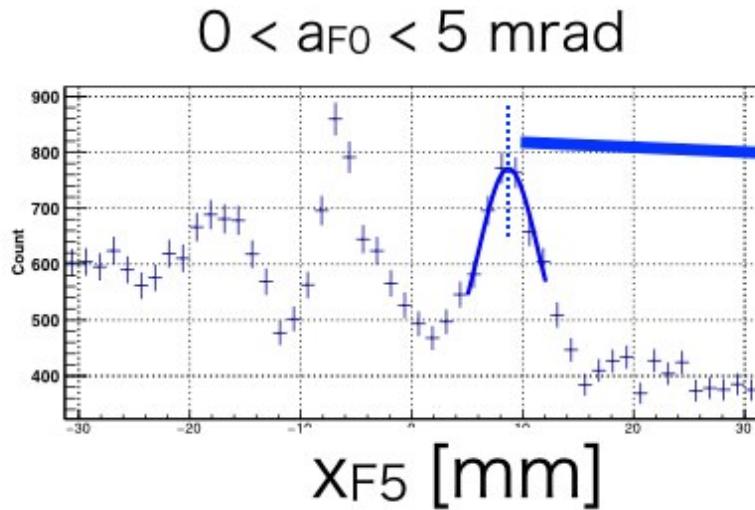
scale BigRIPS by 1.000 (default), 1.00488, 1.00979



$$X_{F5} = \alpha \delta + \beta \delta^2$$

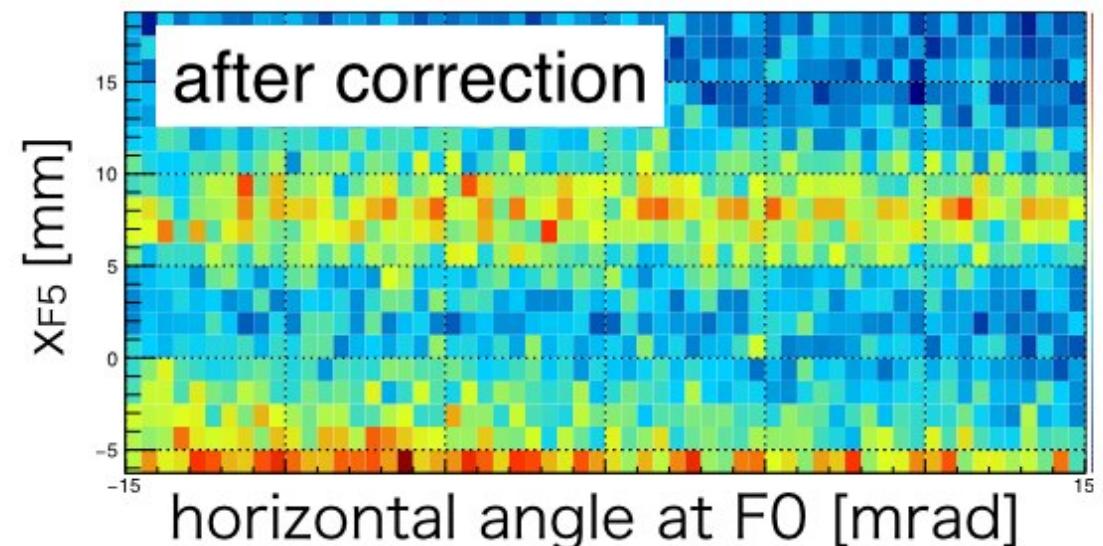
Dispersion

② Correct optical higher order aberration



vertical angular aberration
is also corrected

*data for the evaluation separated
from the production run

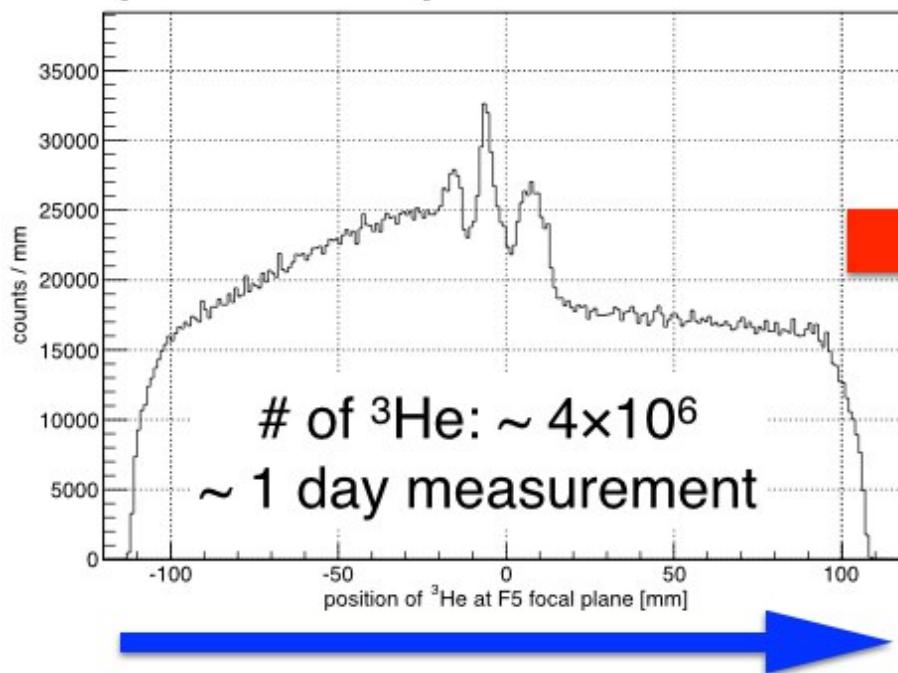


Finally, we include 15 elements of transfer matrix for the analysis.

matrix element	deduced values from exp. data	calculated values
$(x_{F5} a_{F0})$ [mm/mrad]	$(+2.75 \pm 0.2) \times 10^{-1}$	$+1.93 \times 10^{-1}$
$(x_{F5} a_{F0}^2)$ [mm/mrad ²]	$(-9.44 \pm 8.0) \times 10^{-4}$	-1.37×10^{-3}
$(x_{F5} a_{F0}^3)$ [mm/mrad ³]	$(-4.41 \pm 0.9) \times 10^{-4}$	-7.10×10^{-4}
$(x_{F5} b_{F0})$ [mm/mrad]	$(+4.87 \pm 6.1) \times 10^{-3}$	0.00
$(x_{F5} b_{F0}^2)$ [mm/mrad ²]	$(-8.45 \pm 4.0) \times 10^{-4}$	-2.15×10^{-4}
$(x_{F5} a_{F0}b_{F0}^2)$ [mm/mrad ³]	$(-2.53 \pm 0.5) \times 10^{-4}$	-3.01×10^{-4}
$(x_{F5} a_{F0}\delta)$ [mm/mrad/%]	$(+7.83 \pm 0.2) \times 10^{-1}$	8.27×10^{-1}
$(x_{F5} a_{F0}^2\delta)$ [mm/mrad ² /%]	$(+6.74 \pm 1.9) \times 10^{-3}$	$+1.28 \times 10^{-3}$
$(x_{F5} \delta)$ [mm/%]	$+62.42 \pm 0.27$	61.20
$(x_{F5} \delta^2)$ [mm/% ²]	$(-7.84 \pm 4.7) \times 10^{-1}$	-8.34×10^{-1}
$(a_{F5} a_{F0})$ [mrad/mrad]	$(-5.19 \pm 0.5) \times 10^{-1}$	-5.48×10^{-1}
$(b_{F5} b_{F0})$ [mrad/mrad]	$(-5.40 \pm 0.5) \times 10^{-1}$	-6.39×10^{-1}
$(a_{F5} a_{F0}\delta)$ [mrad/mrad/%]	—	-3.72×10^{-2}
$(b_{F5} b_{F0}\delta)$ [mrad/mrad/%]	—	-6.79×10^{-2}
$(b_{F5} b_{F0}\delta^2)$ [mrad/mrad/% ²]	—	$+5.29 \times 10^{-2}$

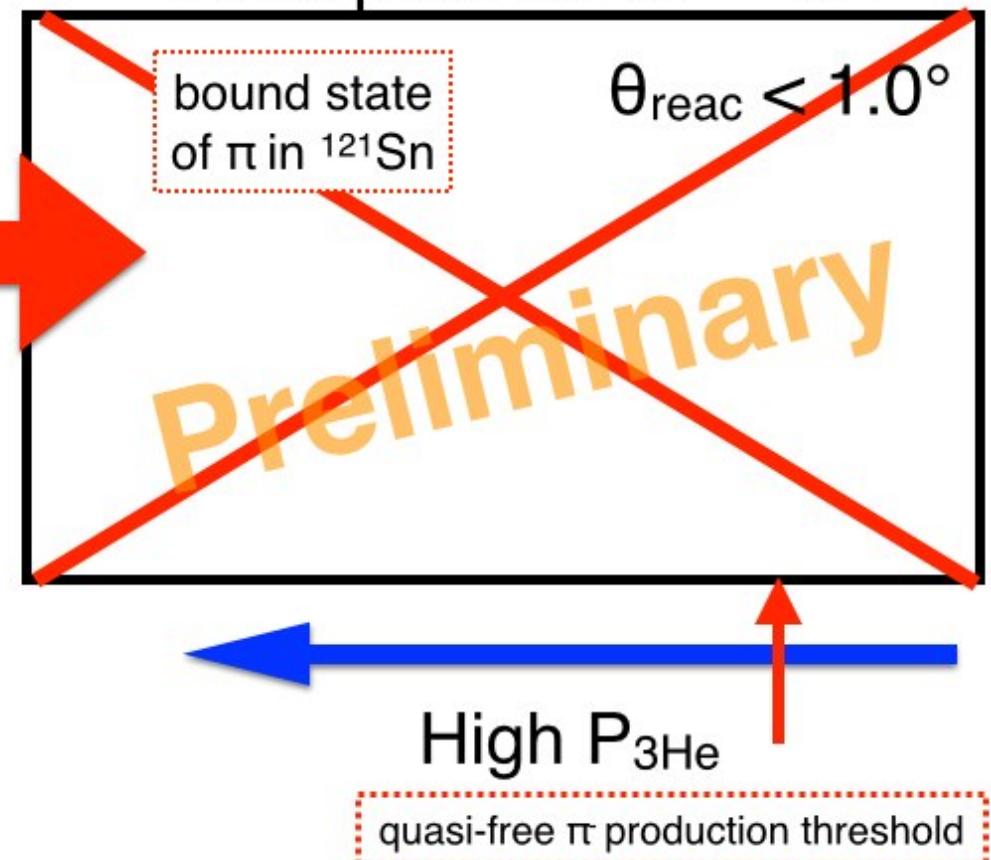
Conversion from position to E_{ex}

position spectrum of ^3He



High $P_{^3\text{He}}$

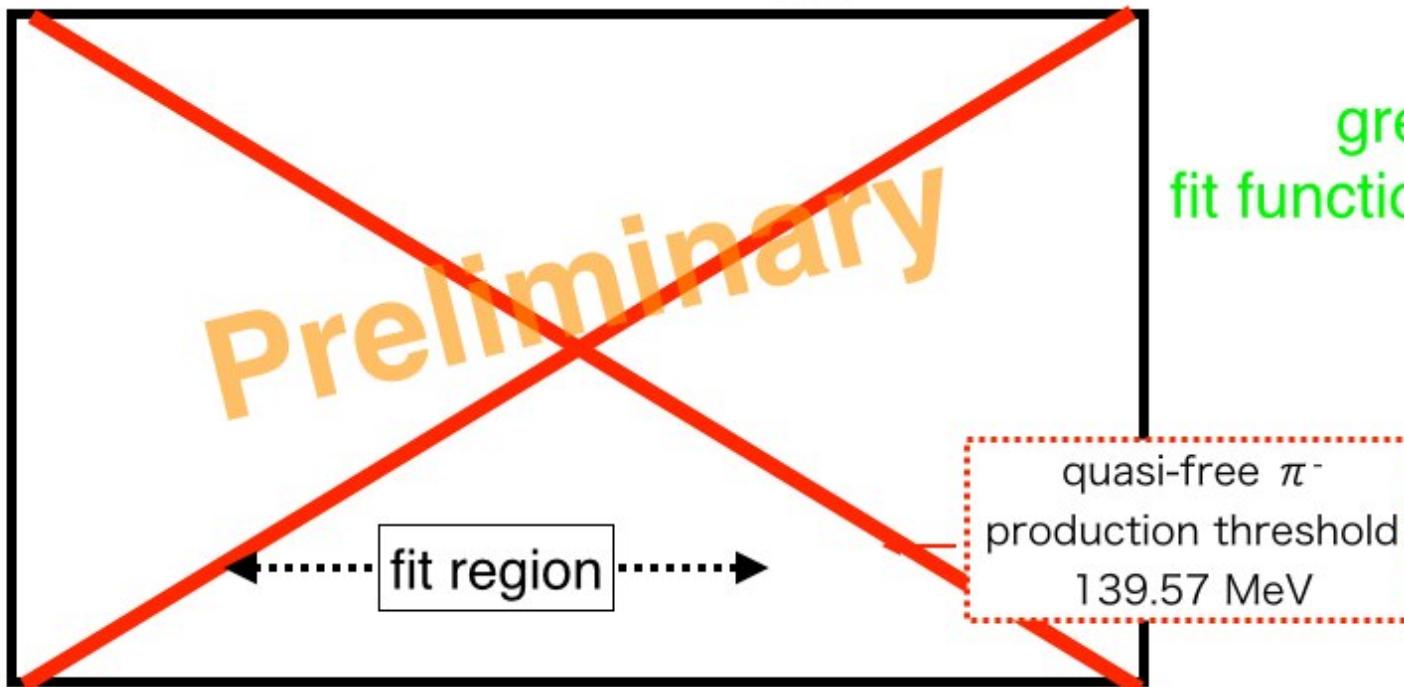
E_{ex} spectrum of ^{121}Sn



The spectrum seems to achieve the best resolution among the past deeply-bound pionic atom experiments.

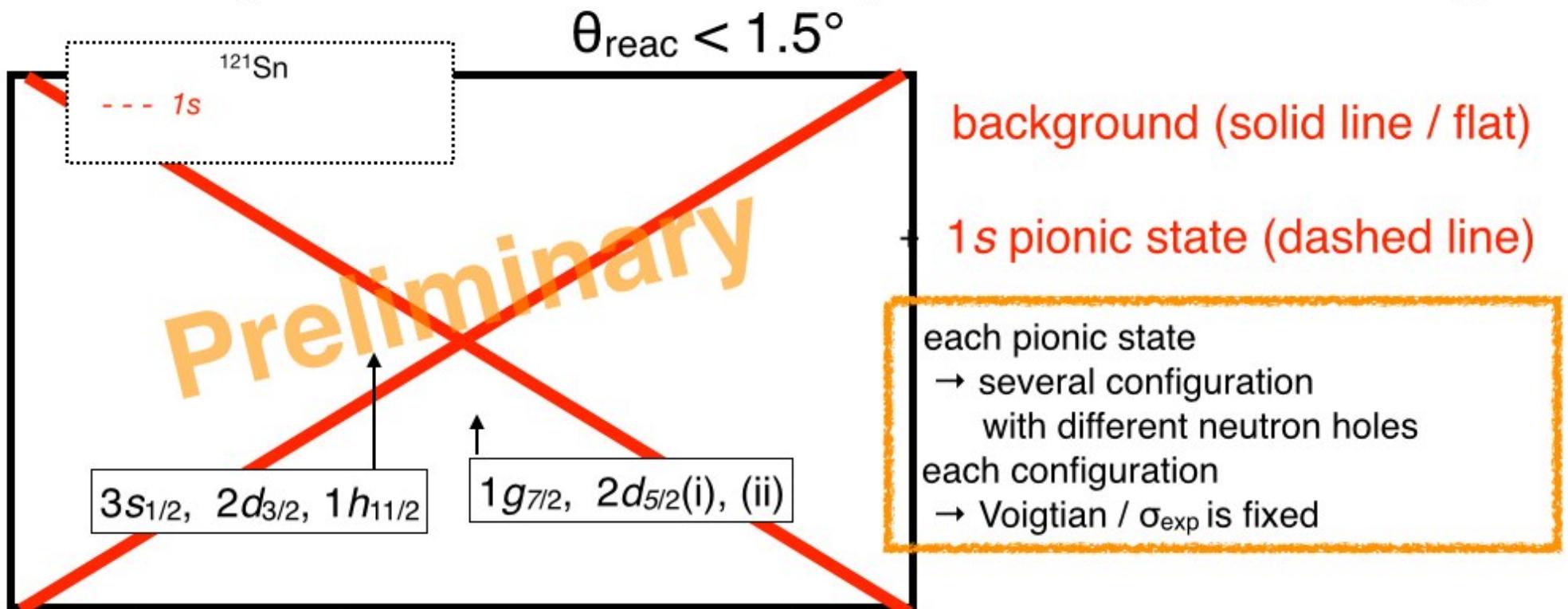
Decomposition of the E_{ex} spectrum : ^{122}Sn target

$\theta_{\text{reac}} < 1.5^\circ$



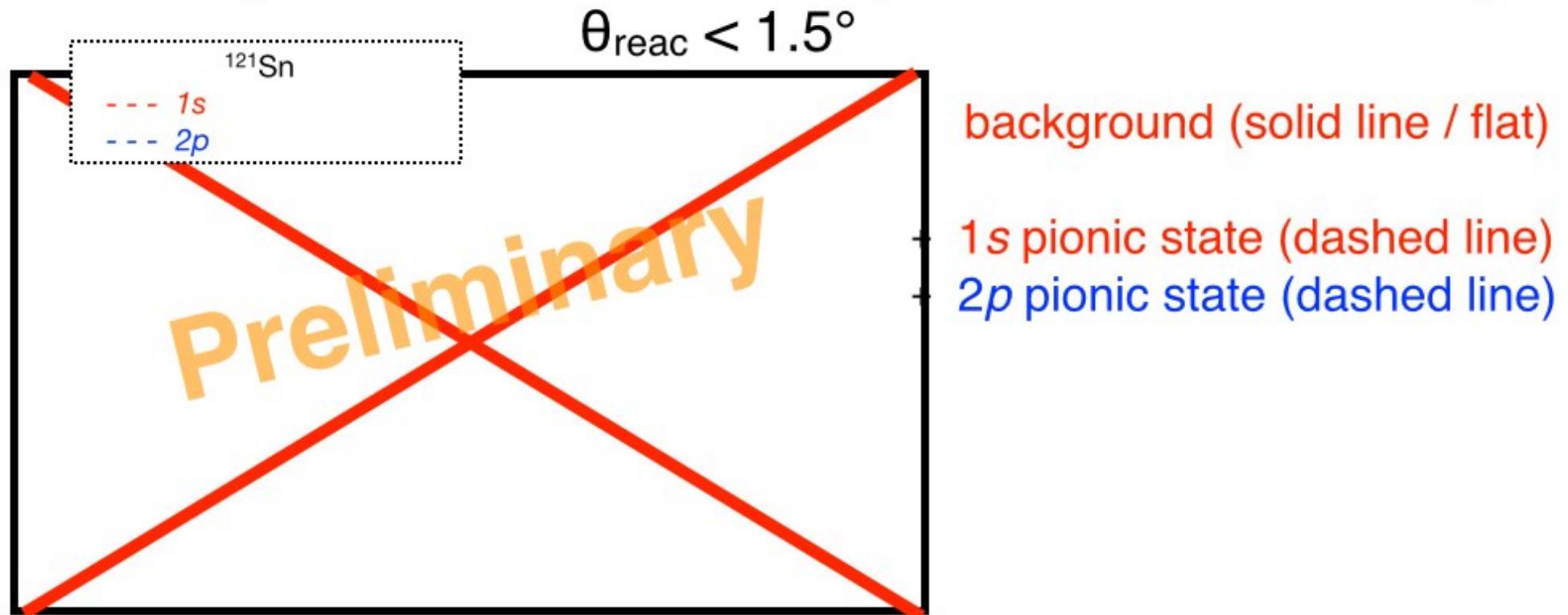
The E_{ex} spectrum is fit by the function with several components
→ deduce binding energies and widths of pionic states

Decomposition of the E_{ex} spectrum : ^{122}Sn target

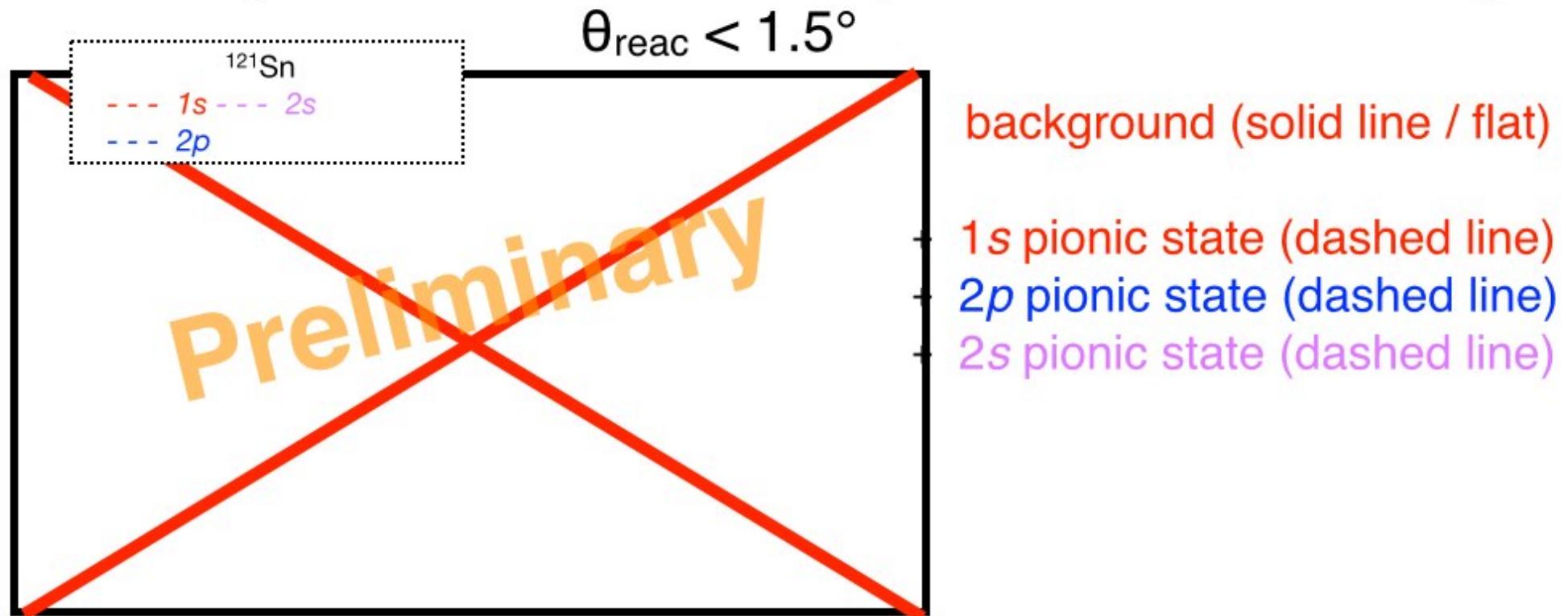


neutron hole	E_{ex} [MeV]	relative strength for pionic 1s state
$2d_{3/2}$	0.000	0.09
$1h_{11/2}$	0.006	0.001
$3s_{1/2}$	0.060	1
$1g_{7/2}$	0.926	0.003
$2d_{5/2} (\text{i})$	1.121	0.12
$2d_{5/2} (\text{ii})$	1.403	0.06

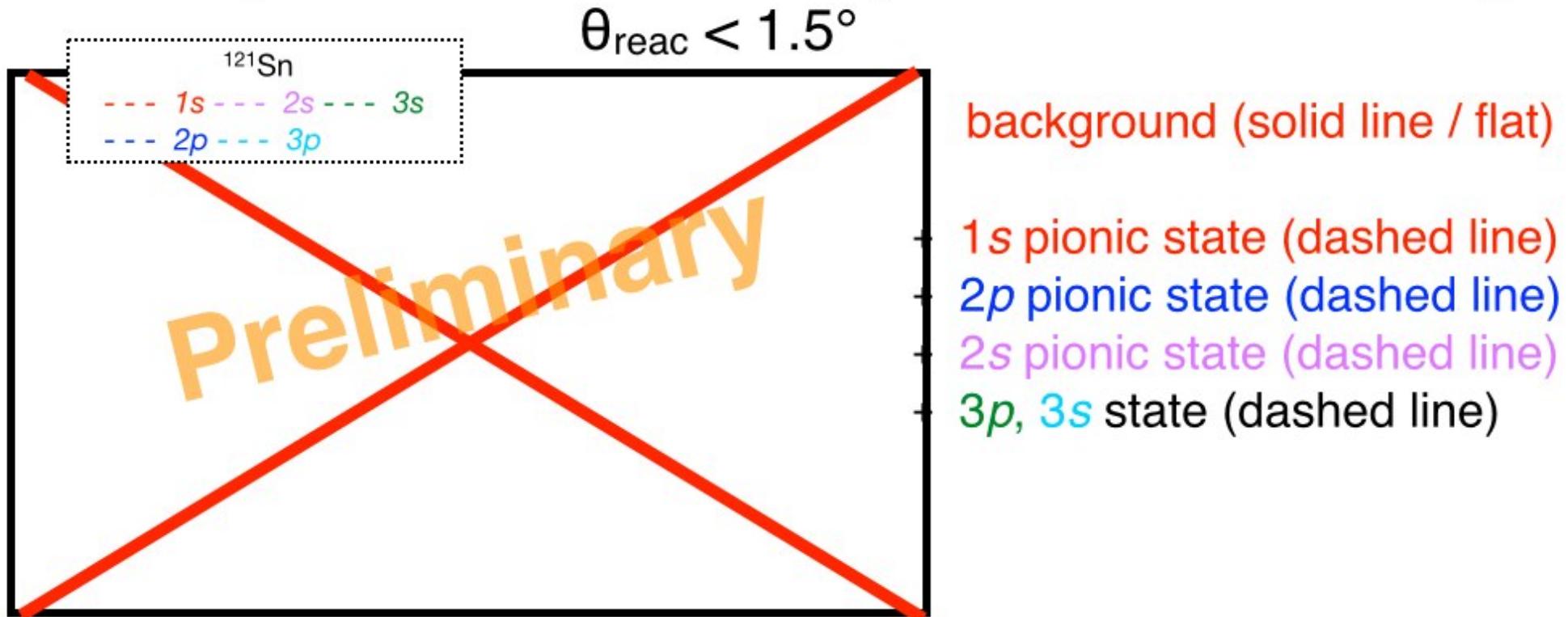
Decomposition of the E_{ex} spectrum : ^{122}Sn target



Decomposition of the E_{ex} spectrum : ^{122}Sn target



Decomposition of the E_{ex} spectrum : ^{122}Sn target



Fitting parameter

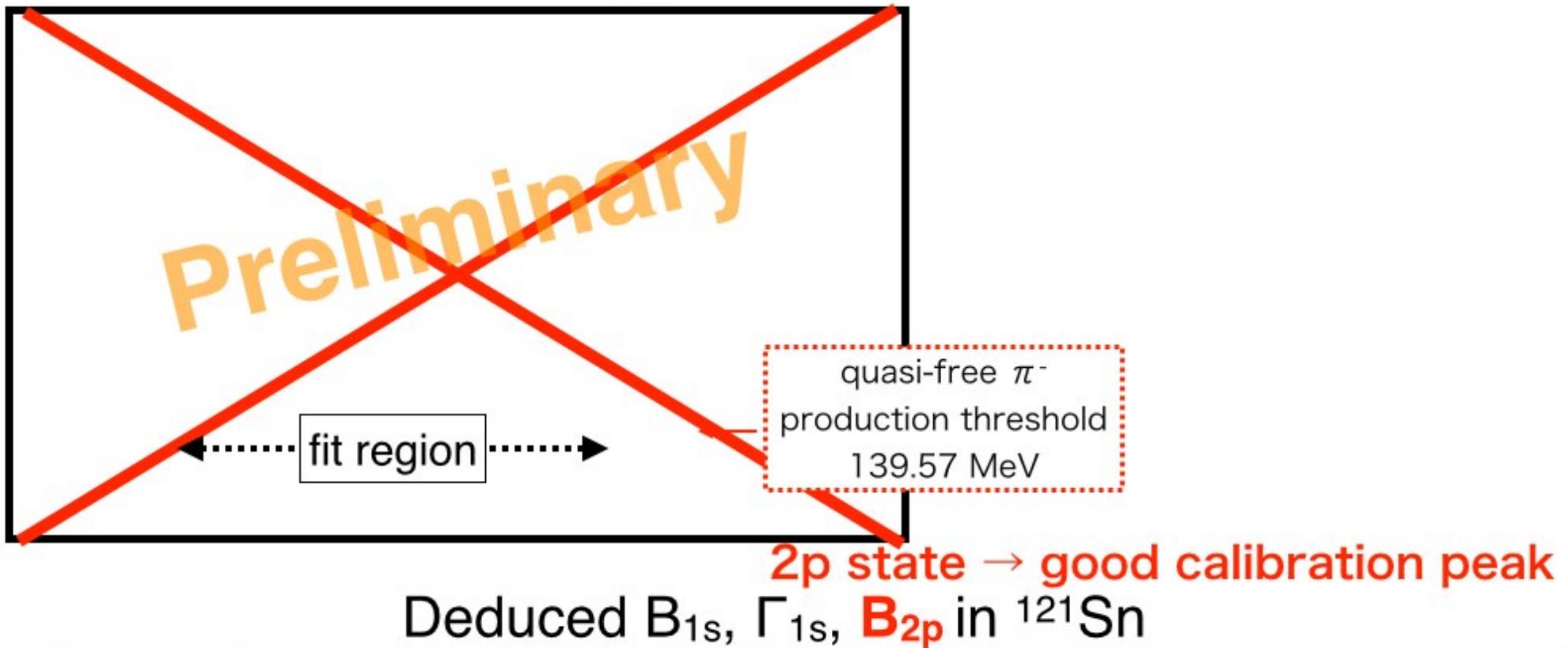
- relative strength of each state
- BE_{1s} , BE_{2p} , BE_{2s}
- Γ_{1s} , Γ_{2p}

Fixed parameter

- BE_{3p} , BE_{3s}
- Γ_{2s} , Γ_{3p} , Γ_{3s}

Decomposition of the E_{ex} spectrum : ^{122}Sn target

$\theta_{\text{reac}} < 1.5^\circ$

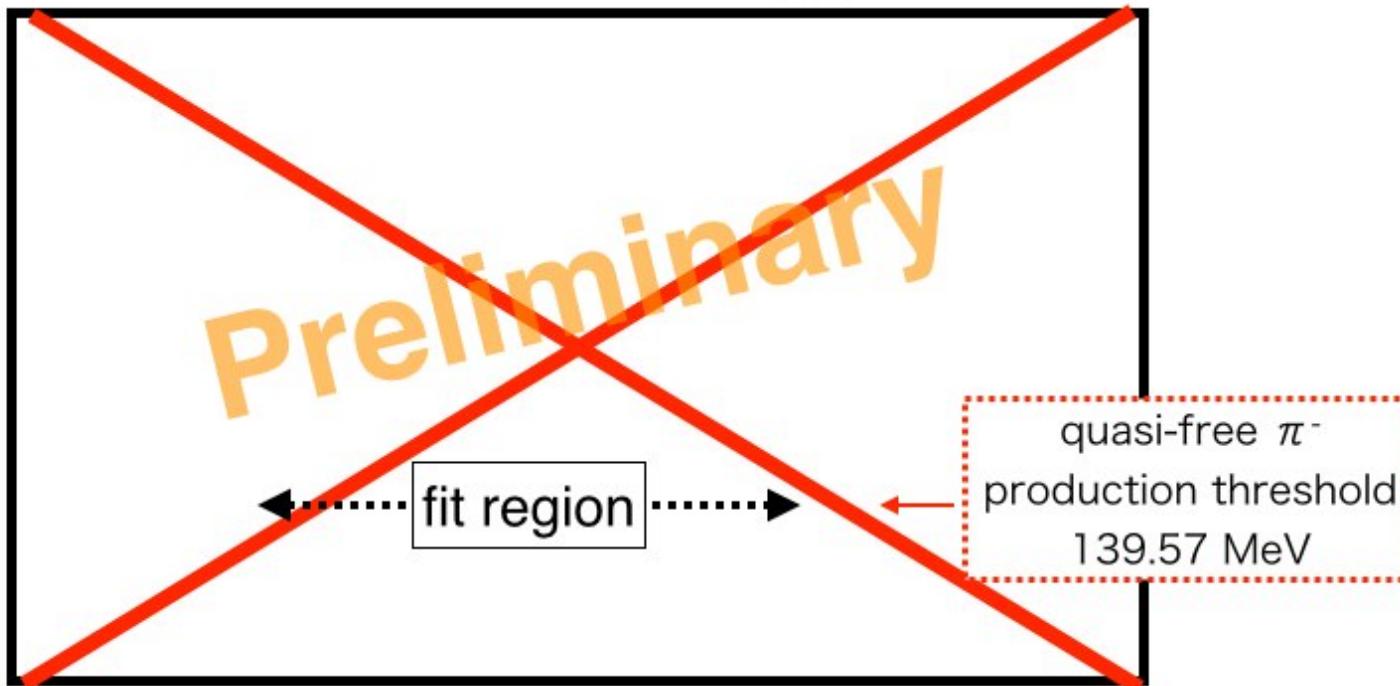


(nl)	B_{nl} [MeV]	Γ_{nl} [MeV]
1s	$XXX \pm XXX$ (stat.) $\pm XXX$ (sys.)	$XXX \pm XXX$ (stat.) $\pm XXX$ (sys.)
2p	$XXX \pm XXX$ (stat.) $\pm XXX$ (sys.)	$XXX \pm XXX$ (stat.) $\pm XXX$ (sys.)
1s - 2p	$XXX \pm XXX$ (stat.)$\pm XXX$ (sys.)	—

Preliminary

Decomposition of the E_{ex} spectrum : ^{117}Sn target

$\theta_{\text{reac}} < 1.5^\circ$



Deduced B_{1s} in ^{117}Sn

(nl)	$B_{nl} [\text{MeV}]$	$\Gamma_{nl} [\text{MeV}]$
1s	$XXX \pm XXX (\text{stat.}, \pm XXX \text{ (sys.)})$	—

Optical potential deduced from B_{1s} , Γ_{1s} , B_{2p} in ^{121}Sn

$$\ast \Delta B = B_{1s} - B_{2p}$$



Calculate likelihood for
each b_1 and $\text{Im}B_0$
→ obtain best value

$$V_s(r) = -\frac{2\pi}{\mu} [\epsilon_1 \{b_0 \rho(r) + b_1 \delta\rho(r)\} + \epsilon_2 B_0 \rho(r)^2].$$

∗ b_0 , $\text{Re}B_0$ are deduced from
data of light / symmetric pionic atoms

	$b_1 [m_{\pi}^{-1}]$	$\text{Im}B_0 [m_{\pi}^{-4}]$
This exp.	XXX ± XXX	XXX ± XXX
GSI	- 0.115 ± 0.007	0.0472 ± 0.0013
In vacuum	- 0.0868 ± 0.0014	–

Optical potential deduced from B_{1s} , Γ_{1s} , B_{2p} in ^{121}Sn

$$\ast \Delta B = B_{1s} - B_{2p}$$



Calculate likelihood for each b_1 and $\text{Im}B_0$
→ obtain best value

$$V_s(r) = -\frac{2\pi}{\mu} [\epsilon_1 \{b_0 \rho(r) + b_1 \delta \rho(r)\} + \epsilon_2 B_0 \rho(r)^2].$$

* b_0 , $\text{Re}B_0$ are deduced from

most precise evaluation the value of b_1 in medium
further evidence that chiral symmetry breaking is partially
restored at finite densities.

This exp.

~~XXX ± XXX~~

~~XXX ± XXX~~

GSI

- 0.115 ± 0.007

0.0472 ± 0.0013

In vacuum

- 0.0868 ± 0.0014

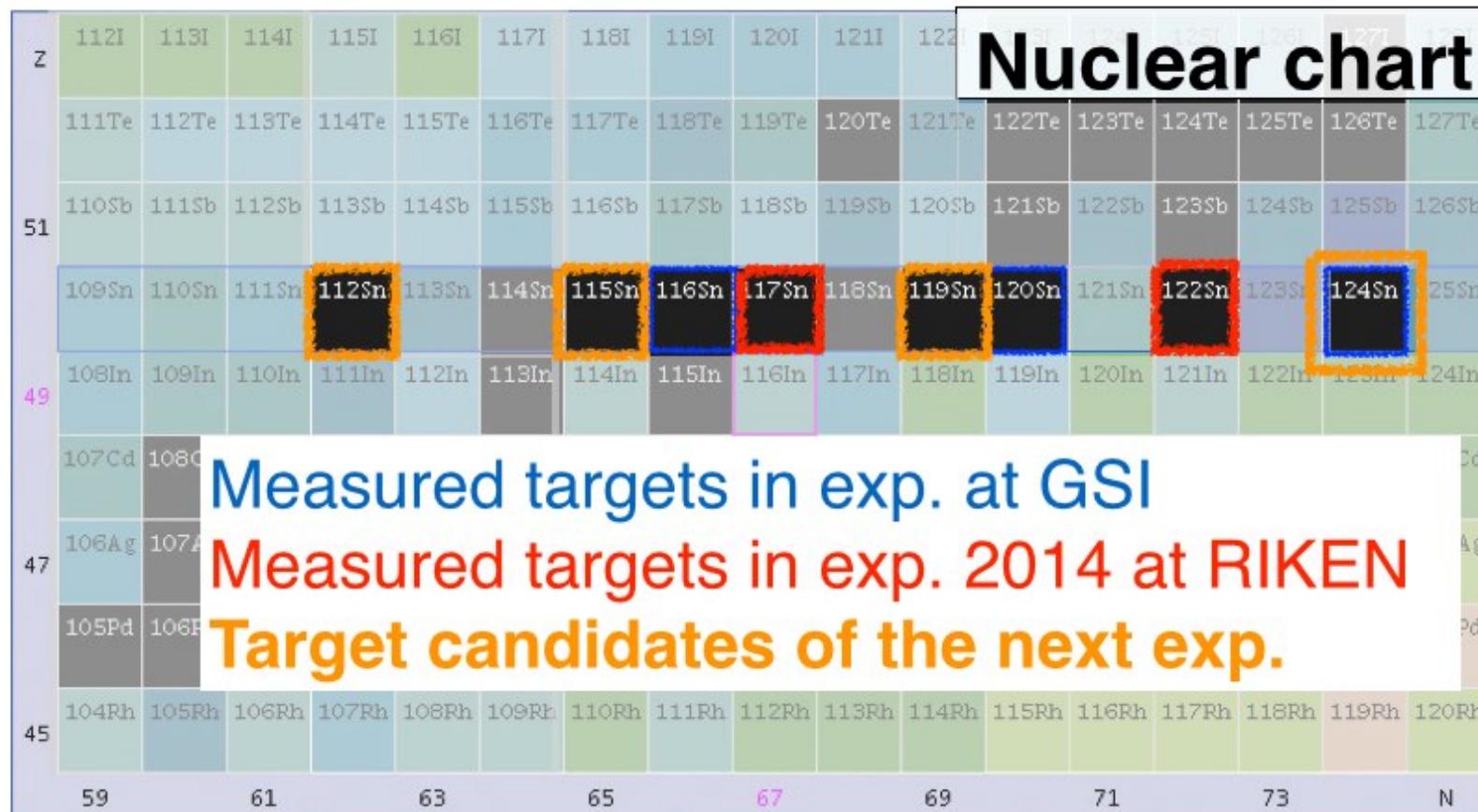
-

Summary

- Deeply-bound pionic atom is good probe for QCD in finite density, especially for quark condensate via b_1 parameter in $\pi - A$ potential.
- To determine the b_1 precisely, experiments of pionic Sn isotopes are on going at RIKEN.
- In the first exp. , we measured with the target of $^{122,116}\text{Sn}$, and succeed in
 - improvement of the resolution,
 - observation of the pionic 1s, 2p and 2s states in $^{121, 116}\text{Sn}$,
- From the obtained binding energies and widths of pionic states, b_1 in medium is evaluated most precisely, which is consistent with the partial restoration of chiral symmetry breaking.

(Near) future works

NuDat



The next exp. are already approved in PAC at RIKEN
with wider range of isotopes.
The exp. will be performed in a few years.