

Matsue, June 4-8

Direct Reactions with Exotic Beams (DREB2018)

Linking structure and dynamics in (p, pN) reactions induced by Borromean nuclei

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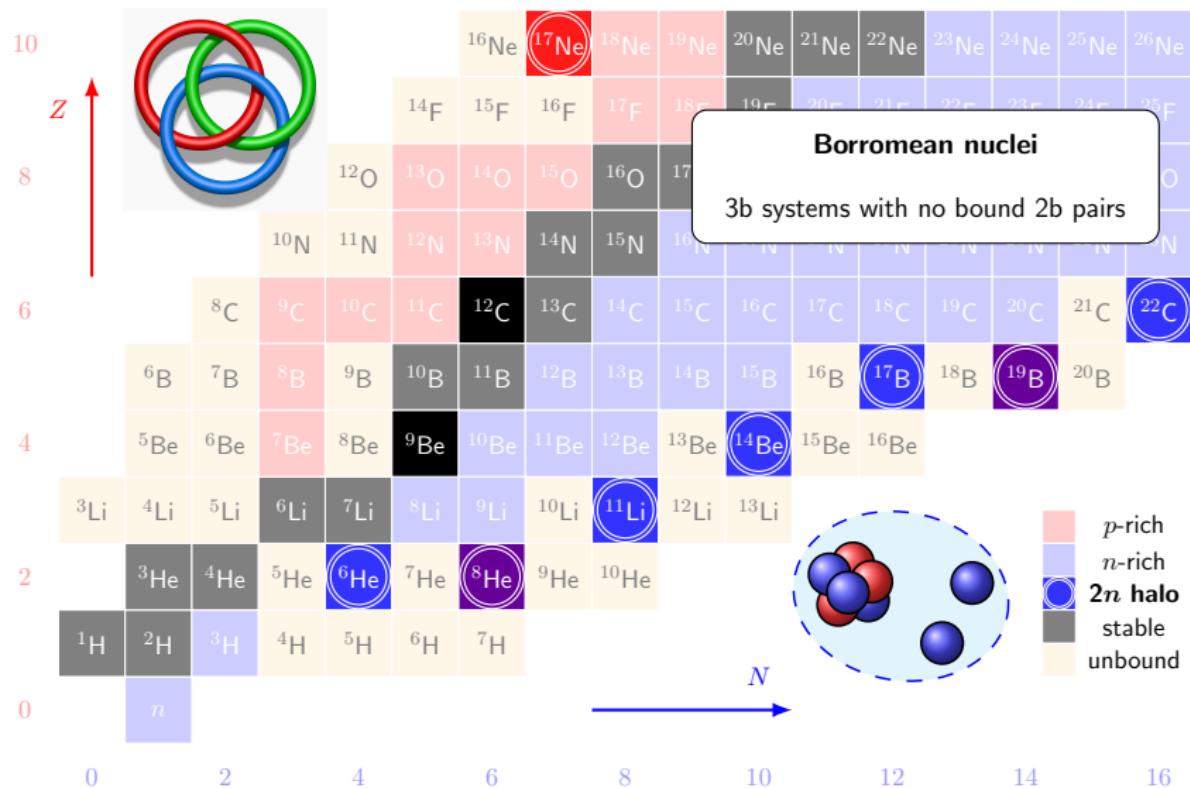


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Universidad de Sevilla, Spain



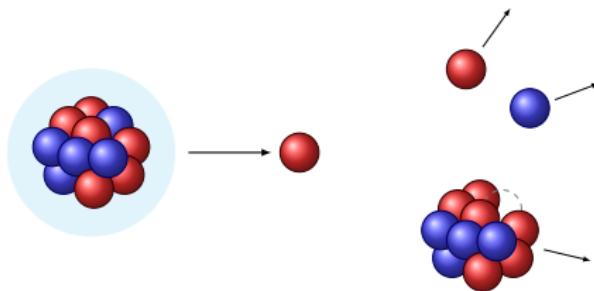


(p, pN) reactions in inverse kinematics

"quasifree" 1*N* removal; *p*-target knockout

- Fast-moving projectile on a proton target

One nucleon is removed, leaving the residue in ground or excited state



- High energies to increase mean free path of nucleon inside nucleus
- Structure information inferred from total 1*N* removal cross sections, momentum distributions, γ and particle decay of the residue ...

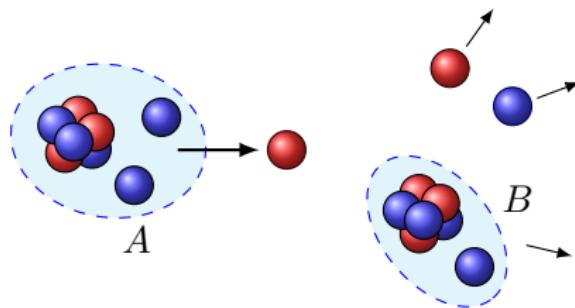
(p, pN) reactions in inverse kinematics

"quasifree" 1*N* removal; *p*-target knockout

Borromean

- Fast-moving projectile on a proton target

One nucleon is removed, leaving the residue in ground or excited state



- If *A* is Borromean, the unbound subsystem *B* will eventually decay
- Probe the continuum wave function of the unbound subsystem

Transfer to the Continuum (TC)

- No IA assumed
- No factorization approximation
- 3-body structure explicitly included

➢ Prior-form T-matrix Participant (N_1) / Spectator (B) approach

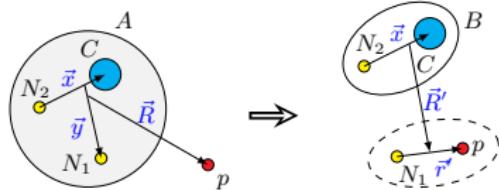
$$\mathcal{T}_{if} = \left\langle \varphi_B^{2b}(\vec{q}, \vec{x}) \Psi_f^{(-)}(\vec{r}', \vec{R}') \middle| V_{pN_1} + U_{pB} - U_{pA} \middle| \Phi_A^{3b}(\vec{x}, \vec{y}) \chi_{pA}^{(+)}(\vec{R}) \right\rangle$$

φ_B^{2b} \equiv continuum wave function of the **binary subsystem B**

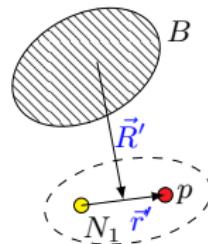
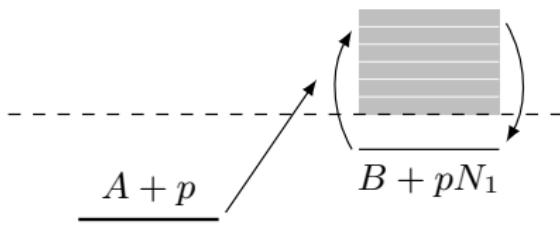
Ψ_f \equiv final $(p + N_1) + B$ wave function

Φ_A^{3b} \equiv g.s. wave function of the initial **3-body projectile A**

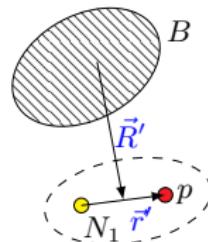
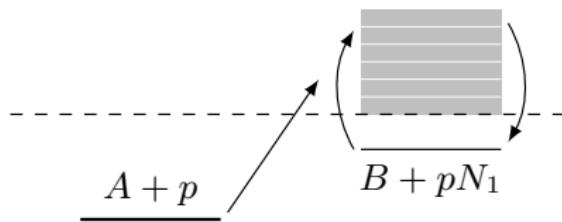
χ_{pA} \equiv distorted p - A wave



$\Psi_f(\vec{r}', \vec{R}')$ expanded in discretized pN states (CDCC-like)



$\Psi_f(\vec{r}', \vec{R}')$ expanded in discretized pN states (CDCC-like)



→ Assume $(V_{pN_1} + U_{pB} - U_{pA})$ does not change the state of B

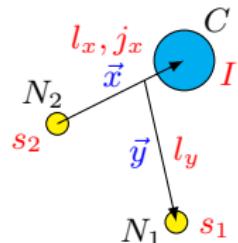
Define **overlaps** $\psi_{LJJ_T M_T}(q, \vec{y}) = \int \varphi_{B, LJJ_T M_T}^{2b}(q, \vec{x}) \Phi_A^{3b}(\vec{x}, \vec{y}) d\vec{x}$

Cross section from auxiliary amplitudes:

$$\mathcal{T}_{if}^{LJJ_T M_T} \equiv \langle \Psi_f^{(-)}(\vec{r}', \vec{R}') | V_{pN_1} + U_{pB} - U_{pA} | \psi_{LJJ_T M_T}(q, \vec{y}) \chi_{pA}^{(+)} \rangle$$

$$\frac{d\sigma^2}{d\Omega_B dq} \propto \sum \left| \mathcal{T}_{if}^{LJJ_T M_T} \right|^2$$

3-body g.s. wave function of $A \Rightarrow$ HH expansion



$$\beta \equiv \{K, l_x, j_x, j_1, l_y, j_2\}$$

$$\vec{l}_x + \vec{s}_2 = \vec{j}_x, \quad \vec{j}_x + \vec{I} = \vec{j}_1$$

$$\vec{l}_y + \vec{s}_1 = \vec{j}_2, \quad \vec{j}_1 + \vec{j}_2 = \vec{j}$$

Diagonalize \mathcal{H}_{3b} using:

[PRC 88 (2013) 014327]

- Binary interactions $C-N_i, N_1-N_2$
- Three-body force to fine-tune g.s. energy

$$\Phi_A^{j\mu}(\vec{x}, \vec{y}) = \sum_{\beta} w_{\beta}^j(x, y) \left\{ [\mathcal{Y}_{l_x s_2 j_x}(\widehat{x}) \otimes \kappa_I]_{j_1} \otimes [Y_{l_y}(\widehat{y}) \otimes \kappa_{s_1}]_{j_2} \right\}_{j\mu}$$

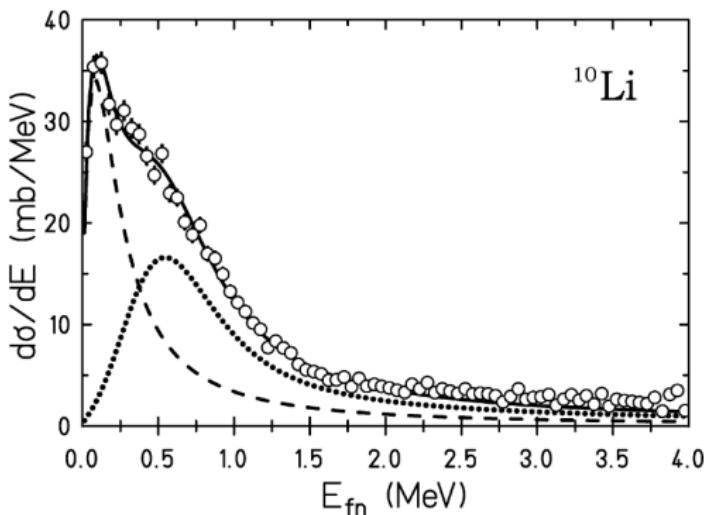
2-body continuum φ_B^{2b} computed with the same $C-N$ potential

$^{11}\text{Li}(p, pn)^{10}\text{Li}$

in inverse kinematics at 280 MeV/u *

ALADIN-LAND setup at GSI

[Aksyutina *et al.* PLB 666 (2008) 430]



$l = 0$ virtual state ($s_{1/2}$)
 $l = 1$ resonance ($p_{1/2}$)

spectroscopic information
extracted through fitting
with assumed shapes
(e.g.: Breit-Wigner)

reaction dynamics
not considered

* More recent data from RIKEN is coming

spin-spin splitting:

$$s_{1/2} \Rightarrow 1^-, 2^-$$

$$p_{1/2} \Rightarrow 1^+, 2^+$$

Model: P1I:

- ^{10}Li :

$$a = -37.9 \text{ fm } (2^-)$$

res. at 0.37, 0.61 MeV

- ^{11}Li :

$3/2^-$ g.s. at -0.37 MeV

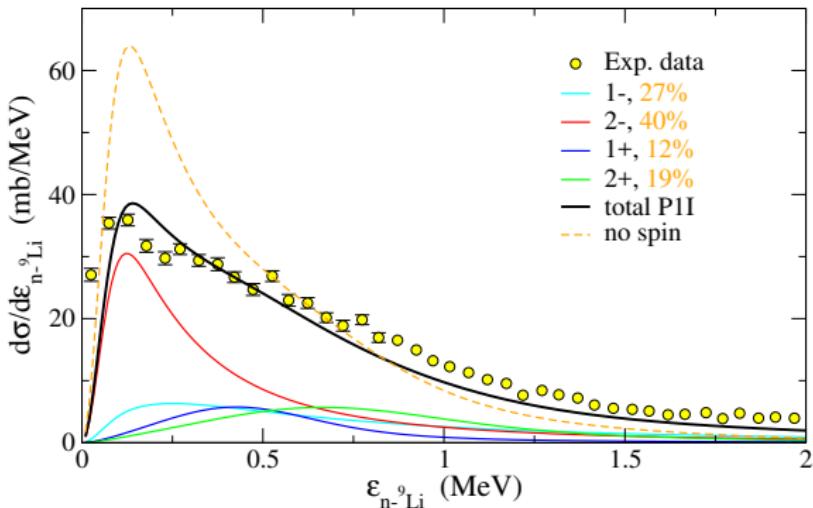
$$r_{mat} = 3.2 \text{ fm}$$

$$r_{ch} = 2.41 \text{ fm}$$

67% s, 31% p

Include spin of ^9Li ; $I^\pi = 3/2^-$

[PLB 772 (2017) 115]

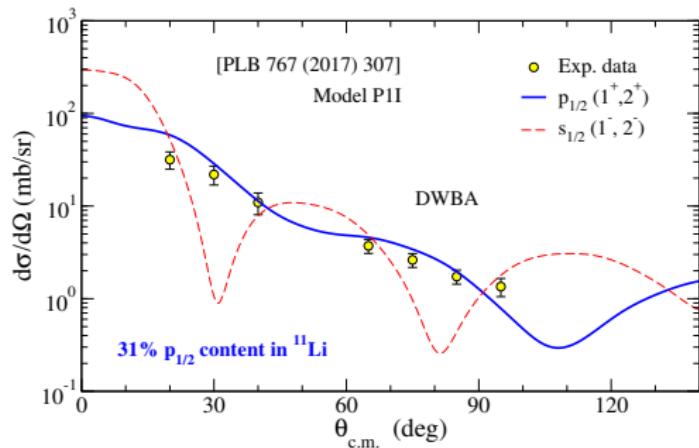
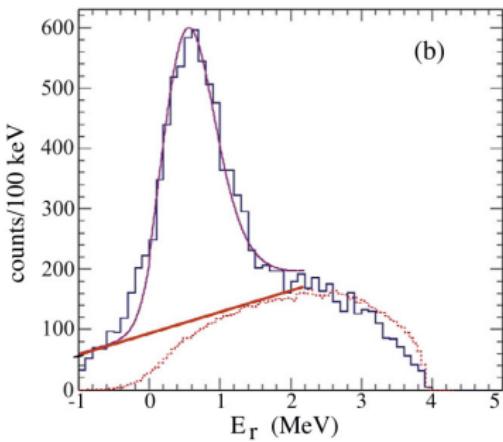


Data from Aksyutina *et al.* [PLB 666 (2008) 430]

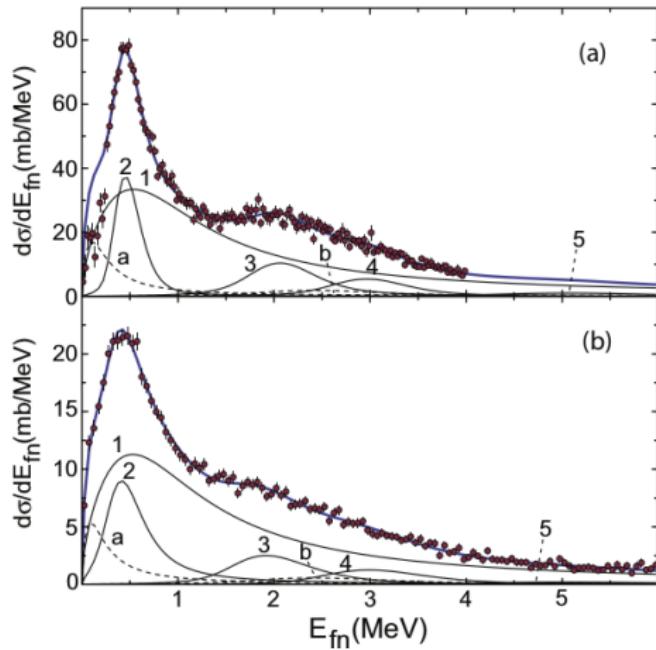
Transfer reaction $^{11}\text{Li}(p, d)^{10}\text{Li}$

IRIS at TRIUMF, 5.7 AMeV

Sanetullaev *et al.* [PLB 755 (2016) 481]



➤ Same model gives good agreement on (p, pn) and (p, d) reactions



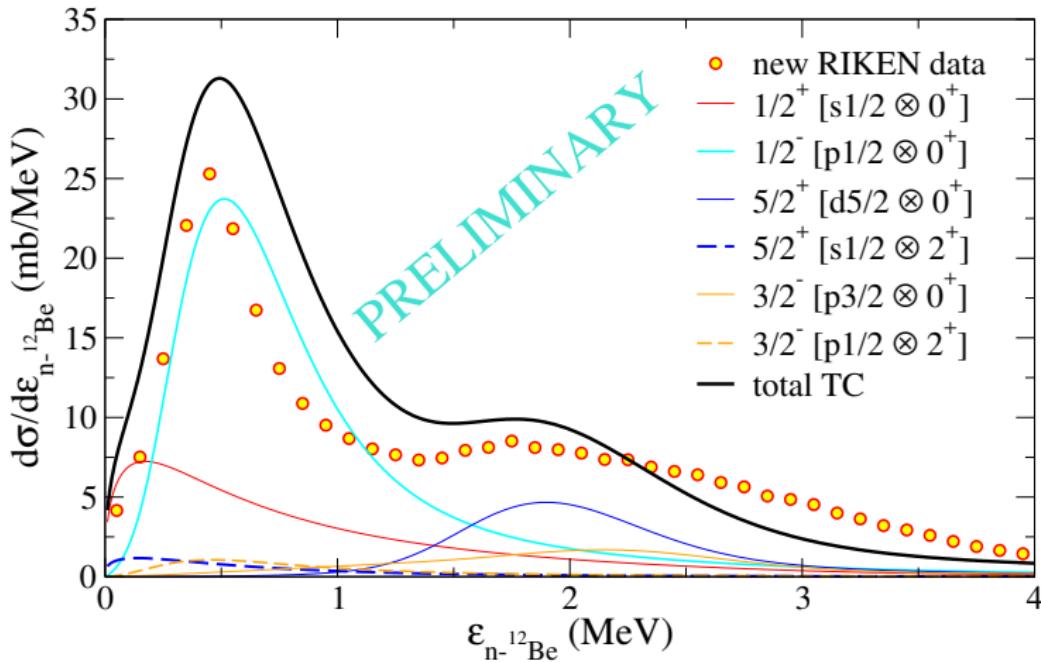
$^{14}\text{Be}(p, pn)^{13}\text{Be}$

- a) Kondo et al. 69 MeV/u
PLB 690 (2010) 245
b) Aksyutina et al. 304 MeV/u
PRC 87 (2013) 064316

- 1) $l = 0, 1/2^+$
 - 2) $l = 1, 1/2^-$
 - 3) $l = 2, 5/2^+$
 - 4) $l = 1, 1/2^-$
 - 5) $l = 2, ?$
- a) decay $5/2^+ \rightarrow ^{12}\text{Be}(2^+)$
b) decay into $^{12}\text{Be}(1^-)$

$^{14}\text{Be}(p, pn)^{13}\text{Be}$ @ 250 MeV/u

new data from RIKEN (A. Corsi)

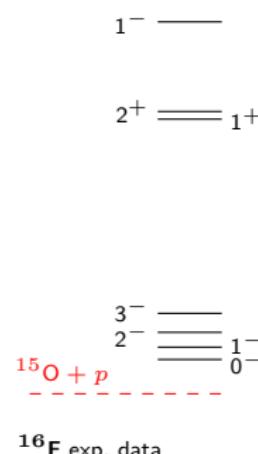
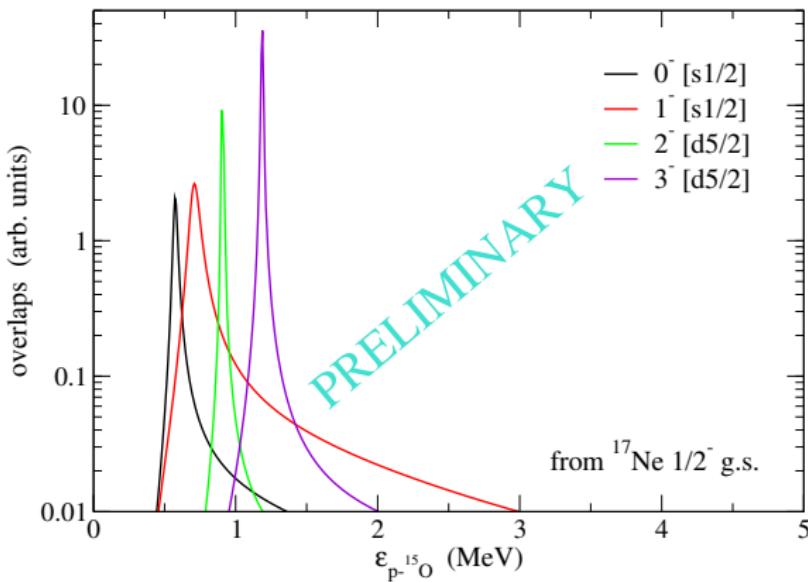


Spectrum governed by low-lying $1/2^-$ resonance

$^{17}\text{Ne}(p, 2p)^{16}\text{F}$

measured at GSI @ 500 MeV/u ...

$^{15}\text{O} + p + p$ model from [PRC 94 (054622) 2016]: **30% s-wave protons**



● Transfer to Continuum (TC)

To describe (p, pN) reactions induced by 3b projectiles.

- Structure information contained in $\langle \varphi_{2b}^q | \Phi_{3b}^{g.s.} \rangle$ overlaps.
- Provides absolute cross sections.

● $^{11}\text{Li}(p, pn)^{10}\text{Li}$

- Including the spin of ${}^9\text{Li}$ improves agreement.
- Same model gives good agreement for ${}^{11}\text{Li}(p, d){}^{10}\text{Li}$.
- Our model: 31% of p -waves in ${}^{11}\text{Li}$.

● ${}^{14}\text{Be}(p, pn){}^{13}\text{Be}$

- Core excited components in a collective model.
- The analysis is ongoing.

- ➡ This is a lot of work! ${}^{14}\text{Be}$; also ${}^{17}\text{Ne}$, ${}^8\text{He}$, ${}^{17}\text{B}$...
- ➡ Other observables: momentum distributions, profile functions, ...



Project No.

FIS2014-53448-c2-1-P

FIS2017-88410-P



Project No.

P11-FQM-7632



Horizon 2020 No. 654002

Introduction
Formalism
Applications
Summary

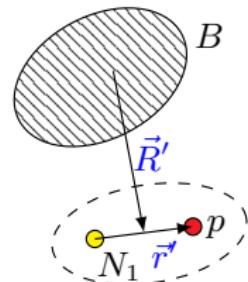
Conclusions
Acknowledgments

- Understanding the structure of **3-body Borromean nuclei** requires:
 - A proper knowledge of the corresponding **2-body subsystems**
 - Information on **excitations/correlations of the core**
- Different reaction **observables** probe different properties
 - E.g.: for ^{11}Li :
 - **breakup** $^{11}\text{Li} + A \rightarrow {}^9\text{Li} + n + n + A$
 - **1n transfer** $^{11}\text{Li}(p, d){}^{10}\text{Li}^*$
 - **2n transfer** $^{11}\text{Li}(p, t){}^9\text{Li}^*$
 - **knockout** $^{11}\text{Li} + A \rightarrow {}^{10}\text{Li}^* + X \rightarrow {}^9\text{Li} + n + X$
 - **1n removal** $^{11}\text{Li}(p, pn){}^{10}\text{Li}^*$
 - ...
 - In all these processes, a crucial aspect is how the **structure input** is **linked** to the **reaction observables**

Final wave function

Expanded in proton-nucleon states (CDCC)

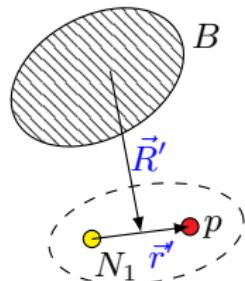
$$\Psi_f(\vec{r}', \vec{R}') \simeq \sum_{n\mathcal{J}\Pi} \phi_n^{\mathcal{J}\Pi}(k_n, \vec{r}') \chi_n^{\mathcal{J}\Pi}(\vec{K}', \vec{R}')$$



Final wave function

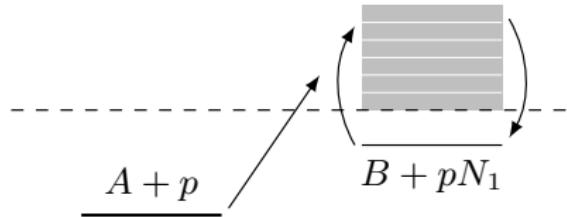
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Basis of N discretized bins

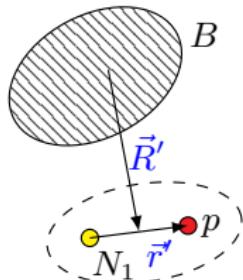
$$\phi_n^{\mathcal{J}\Pi}(k_n, \vec{r}') = \sqrt{\frac{2}{\pi N}} \int_{k_{n-1}}^{k_n} \phi_{pN_1}^{\mathcal{J}\Pi}(k, \vec{r}') dk.$$



Final wave function

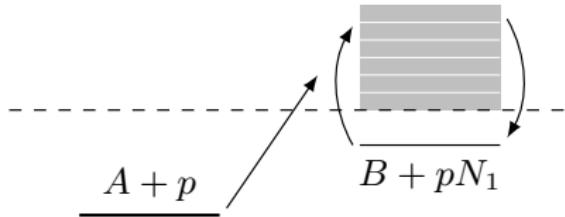
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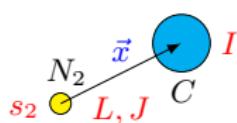
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If we select the (p, d) channel
TC reduces to DWBA

$$\Psi_f(\vec{r}', \vec{R}') \simeq \phi_d(\vec{r}') \chi_{d-B}(\vec{R}')$$

2b continuum state of fragment B

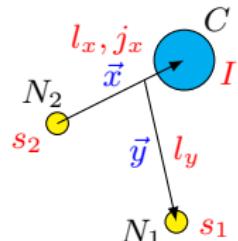


$$\varphi_{\vec{q}, \sigma_2, \iota}^{(+)}(\vec{x}) = \frac{4\pi}{qx} \sum_{LJJ_T M_T} i^L Y_{LM}^*(\hat{q}) \langle LM s_2 \sigma_2 | JM_J \rangle \\ \times \langle JM_J I \iota | J_T M_T \rangle f_{LJ}^{J_T}(qx) [\mathcal{Y}_{Ls_2 J}(\hat{x}) \otimes \kappa_I]_{J_T M_T}$$

Coupling order: $\vec{L} + \vec{s}_2 = \vec{J}$, $\vec{J} + \vec{I} = \vec{J}_T$

Obtain solution for each $(L, J) J_T$:

$$f_{LJ}^{J_T}(qx) \longrightarrow \frac{i}{2} e^{i\sigma_L} \left[H_L^{(-)}(qx) - S_{LJ}^{J_T} H_L^{(+)}(qx) \right]$$

3b g.s. wave function of A 

$$\beta \equiv \{K, l_x, j_x, j_1, l_y, j_2\}$$

$$\vec{l}_x + \vec{s}_2 = \vec{j}_x, \quad \vec{j}_x + \vec{I} = \vec{j}_1$$

$$\vec{l}_y + \vec{s}_1 = \vec{j}_2, \quad \vec{j}_1 + \vec{j}_2 = \vec{j}$$

Diagonalize \mathcal{H}_{3b} using:

[PRC 88 (2013) 014327]

- Binary interactions $C-N_i$, N_1-N_2
- Three-body force to fine-tune g.s. energy

$$\Phi_A^{j\mu}(\vec{x}, \vec{y}) = \sum_{\beta} w_{\beta}^j(x, y) \left\{ [\mathcal{Y}_{l_x s_2 j_x}(\hat{x}) \otimes \kappa_I]_{j_1} \otimes [Y_{l_y}(\hat{y}) \otimes \kappa_{s_1}]_{j_2} \right\}_{j\mu}$$

Consistent with 2b wave function: same potential and couplings

- Assume $(V_{pN_1} + U_{pB} - U_{pA})$ does not change the state of B
- Define overlaps $\langle 2b|3b \rangle$:

$$\psi_{LJJ_T M_T}(q, \vec{y}) = \int \frac{f_{LJ}^{J_T}(qx)}{x} [\mathcal{Y}_{Ls_2 J}(\hat{x}) \otimes \psi_I]_{J_T M_T} \Phi_A^{j\mu}(\vec{x}, \vec{y}) d\vec{x}$$

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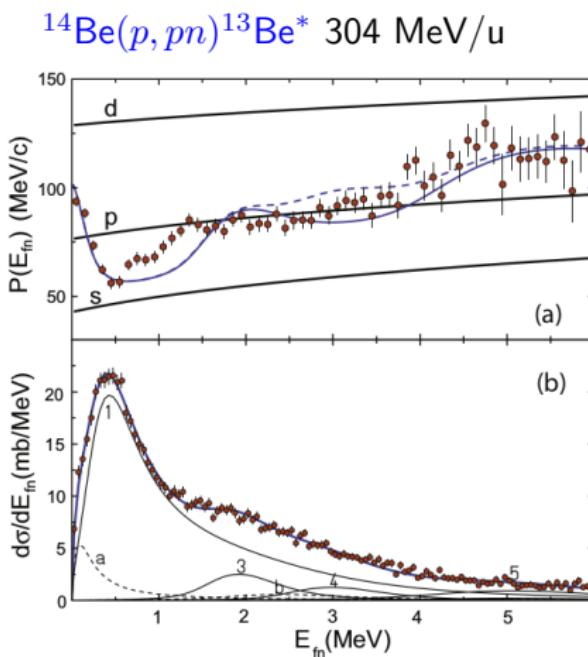
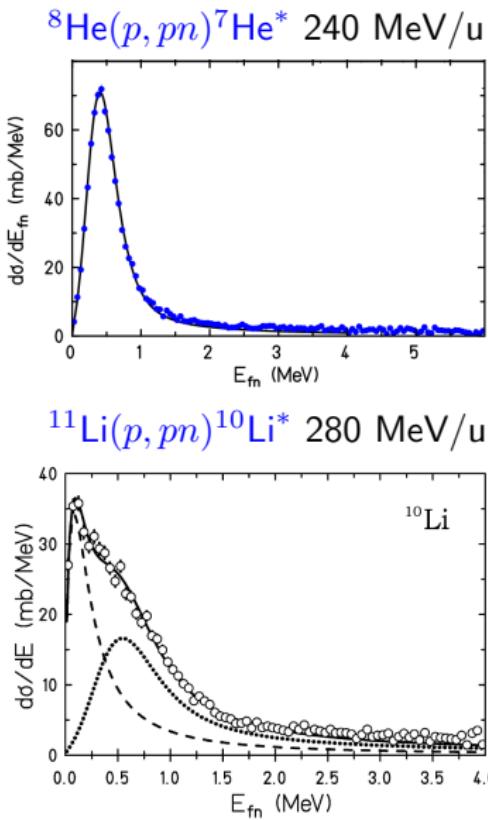
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- Auxiliary amplitudes for each 2b configuration $\{(L, s_2)J, I\}J_T$:

$$\mathcal{T}_{if}^{LJJ_T M_T} \equiv \langle \Psi_f^{(-)}(\vec{r}', \vec{R}') | V_{pN_1} + U_{pB} - U_{pA} | \psi_{LJJ_T M_T}(q, \vec{y}) \chi_{pA}^{(+)} \rangle$$

⇒ Cross sections

$$\frac{d\sigma_n^2}{d\Omega_B d\varepsilon_x} \propto \sum \left| \mathcal{T}_{if}^{LJJ_T M_T} \right|^2$$



Aksyutina et al. (2008,2009,2013) GSI

TC calculations [spin of ^9Li ignored, $I^\pi = 0^+$]

- ^{10}Li ($^9\text{Li} + n$)

$2s_{1/2}$ virtual state: $a = -20.9$ fm

$1p_{1/2}$ resonance at ~ 0.5 MeV

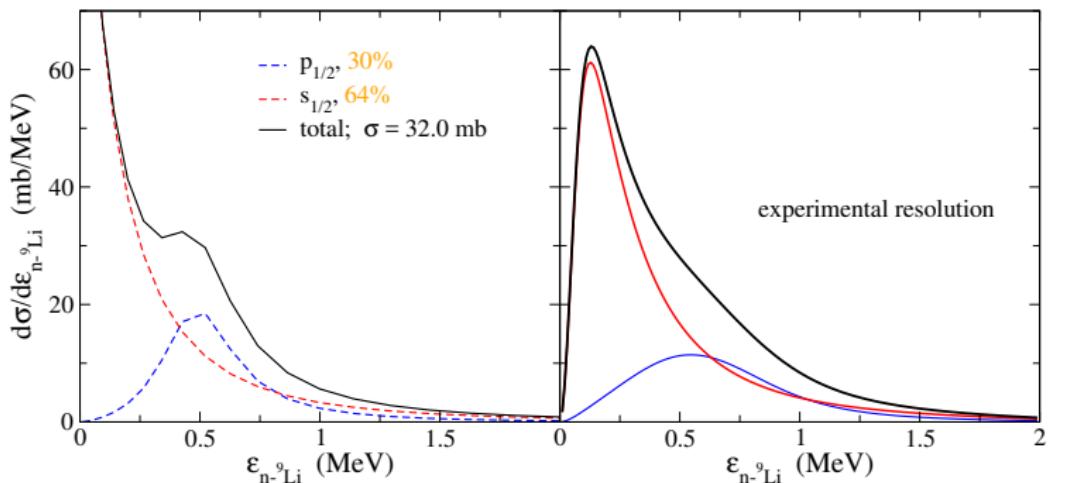
$1d_{5/2}$ state around 4.5 MeV

- ^{11}Li ($^9\text{Li} + n + n$)

0^+ g.s. at -0.37 MeV

$r_{mat} = 3.55$ fm, $r_{ch} = 2.48$ fm

64% $s_{1/2}$, 30% $p_{1/2}$, 3% $d_{5/2}$



TC calculations [spin of ^9Li ignored, $I^\pi = 0^+$]• ^{10}Li ($^9\text{Li} + n$)

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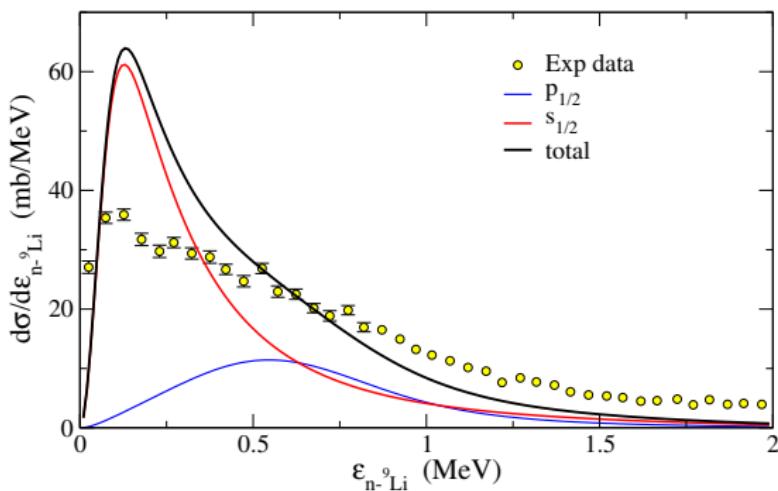
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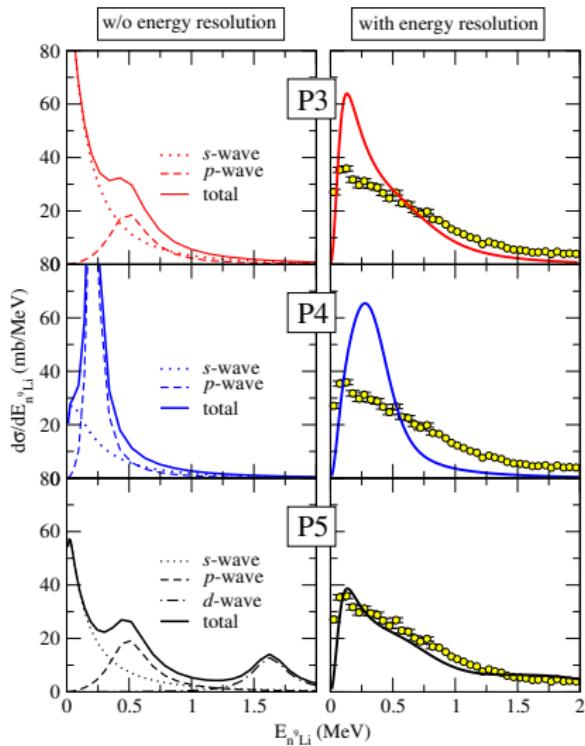
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$r_{mat} = 3.55$ fm, $r_{ch} = 2.48$ fm

64% $s_{1/2}$, 30% $p_{1/2}$, 3% $d_{5/2}$





Sensitivity to the structure model

- P3: reference model
- P4: virtual state at higher E
 p resonance at lower E
- P5: with d resonance ~ 1.5 MeV

	a	$E_r[p_{1/2}]$	$E_r[d_{5/2}]$
P3	-29.8	0.50	4.3
P4	-16.2	0.23	4.3
P5	-29.8	0.50	1.5
	(fm)	(MeV)	(MeV)
	$\%s_{1/2}$	$\%p_{1/2}$	$\%d_{5/2}$
P3	64	30	3
P4	27	67	3
P5	39	35	23

Factorization of the cross section

$$\frac{d\sigma^{LJJ_T}}{d\varepsilon_x} \simeq C^{LJJ_T} K(E) \eta^{LJJ_T}(E)$$

Structure form factors (SF):

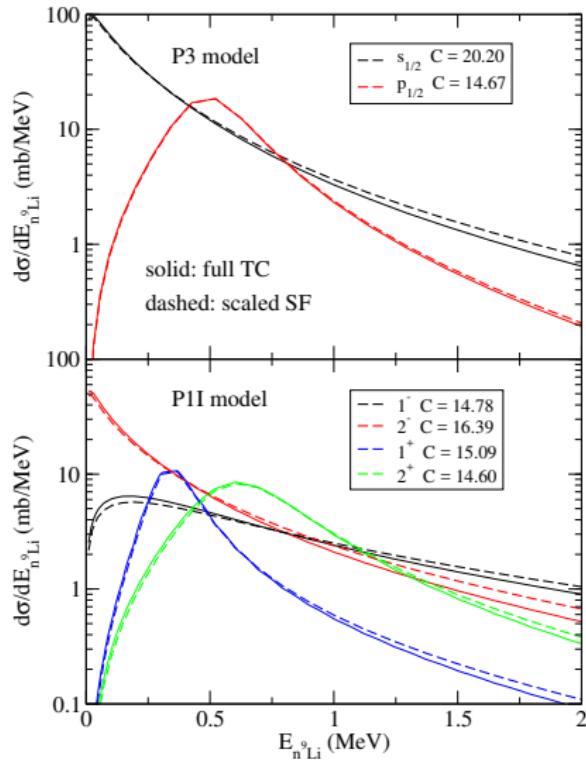
$$\eta^{LJJ_T}(E) \equiv \int d\vec{y} |\psi_{LJJ_T M_T}(E, \vec{y})|^2$$

Correct up to certain extent

BUT!!

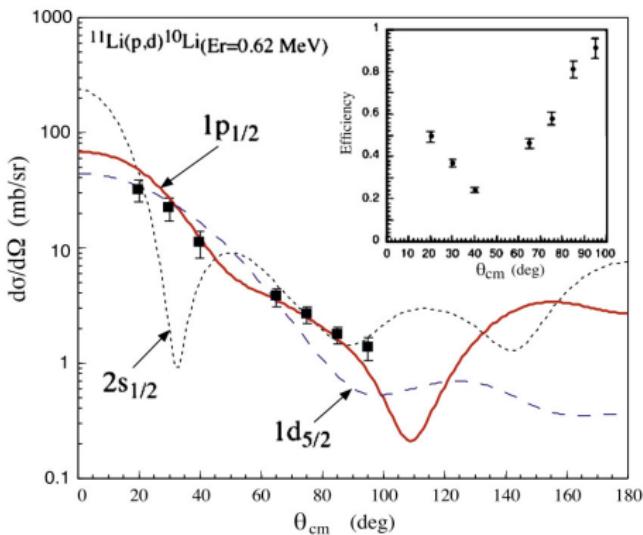
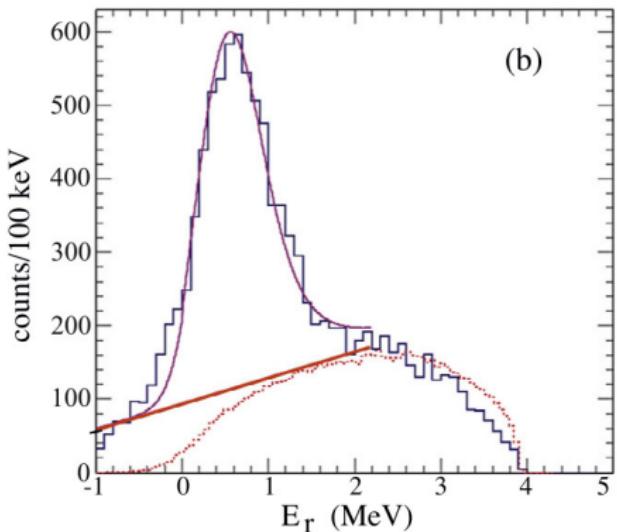
ratio depends on L, J, J_T

reaction calc. to obtain relative weights
less ambiguous than fitting

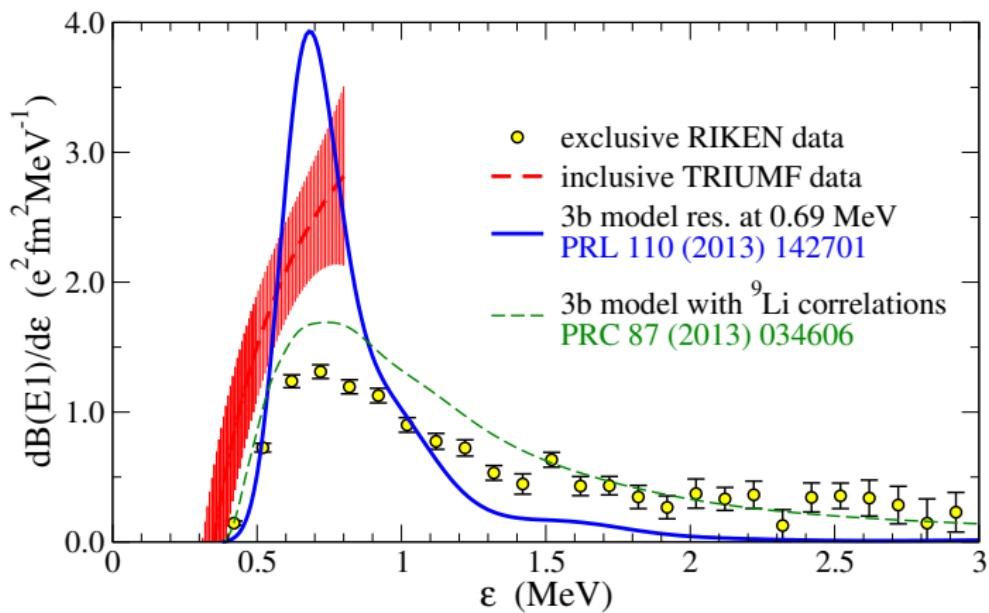


Transfer reaction $^{11}\text{Li}(p, d)^{10}\text{Li}$

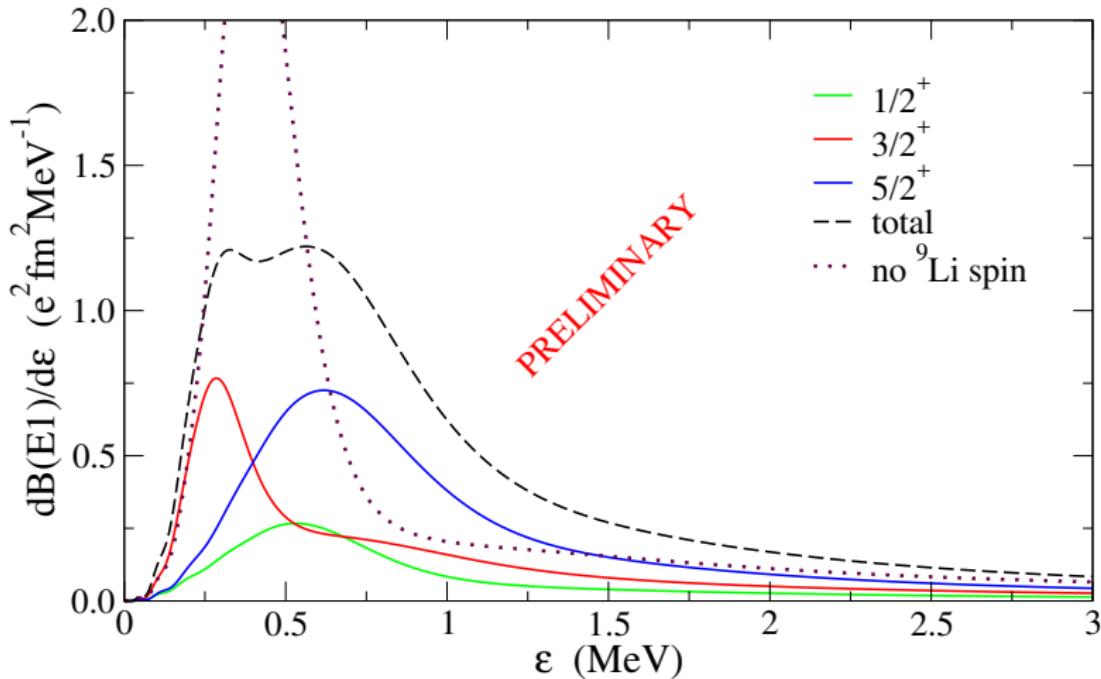
IRIS at TRIUMF, 5.7 AMeV

Sanetullaev *et al.* [PLB 755 (2016) 481]weight $p_{1/2}$: 33%

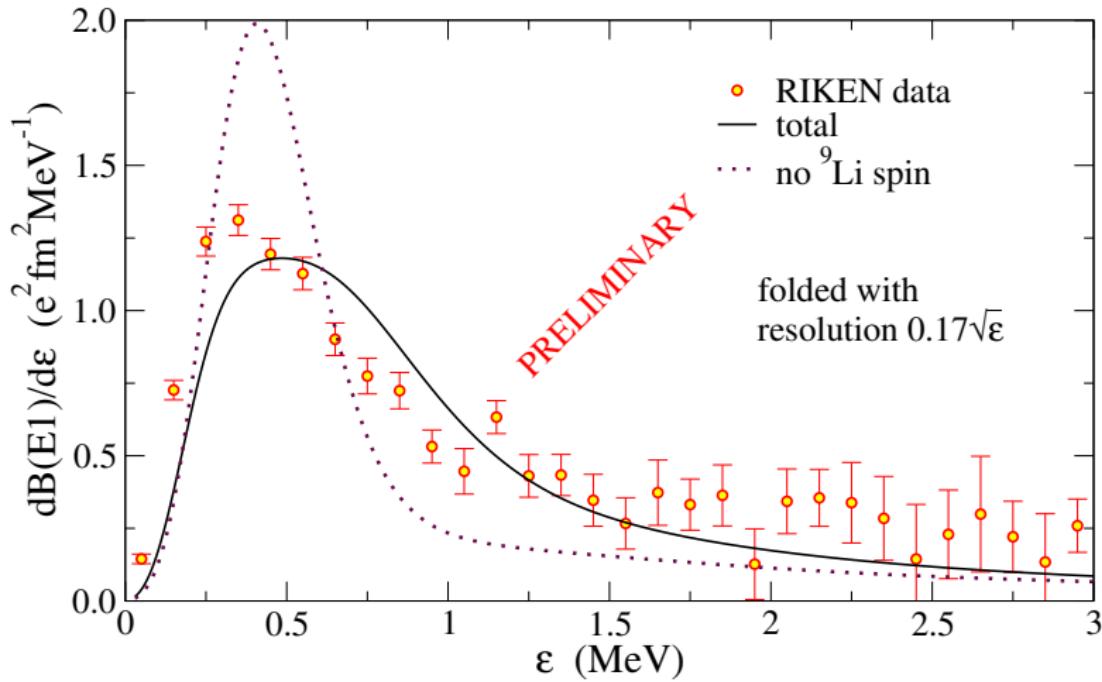
Continuum of ^{11}Li : Dipole response



Large discrepancies between experiments and theory



Again same model P1I seems reasonable



Again same model P1I seems reasonable

Structure model

Deformed $^{12}\text{Be} + n$ potential with core couplings in a collective model

- Only $0^+(\text{g.s.})$ and $2^+(2.1 \text{ MeV})$ of ^{12}Be included.

Deformation parameter $\beta_2 = 0.8$ [Tarutina *et al.* NPA 733 (2004) 53]

- $V(l = 0, 2)$ and V_{ls} adjusted to give:

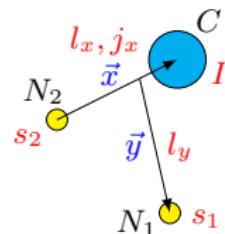
- near-threshold $1/2^+$ state
- $5/2^+$ resonance at ~ 2 MeV

- Shallow $V(l = 1)$ for simplicity

- Three-body calculations:

^{14}Be ($^{12}\text{Be} + n + n$) 0^+ g.s. fixed at $S_{2n}(\text{exp}) \simeq 1.3$ MeV

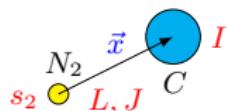
About 60% of $l_x = 0$ and 35% of $I = 2^+$



Multichannel problem

Two-body coupling order: $\underbrace{\{(L, s_2)J, I\}J_T}_{\text{s.p.}} \iff \{L_J \otimes I\}J_T$

Example:



$^{13}\text{Be}(5/2^+)$: $\{d_{5/2} \otimes 0^+\}$, $\{s_{1/2} \otimes 2^+\}$, $\{d_{3/2} \otimes 2^+\}$, $\{d_{5/2} \otimes 2^+\}$

- So (up to $L_{max} = 2$) we have 4 asymptotic channels
- The w.f. for each channel comprises 4 components
- $\langle 2b|3b \rangle$ overlaps mix them

One contribution to the cross section for each asymptotic channel

Similar for other J_T configurations

Aksyutina et al.
PRC 87 (2013) 064316

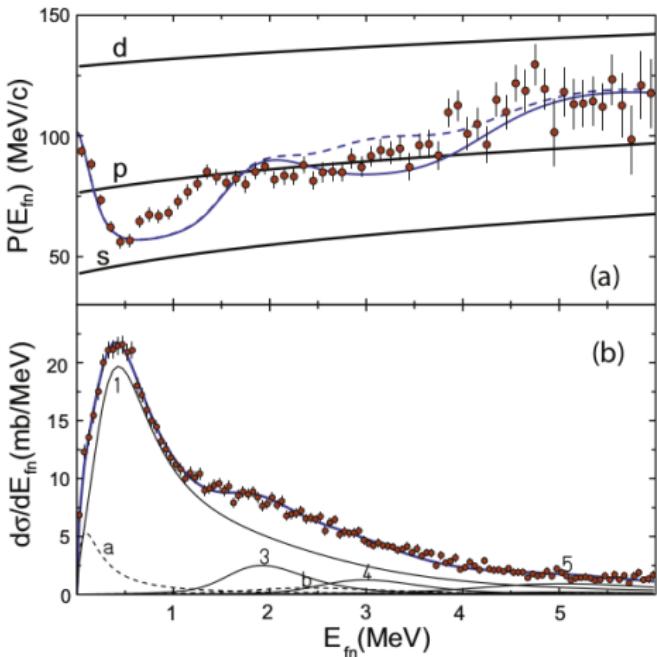
1) using two $1/2^+$ states

No low-energy $1/2^-$ resonance required

Momentum profile gives an average: mostly $l = 0, l = 2$

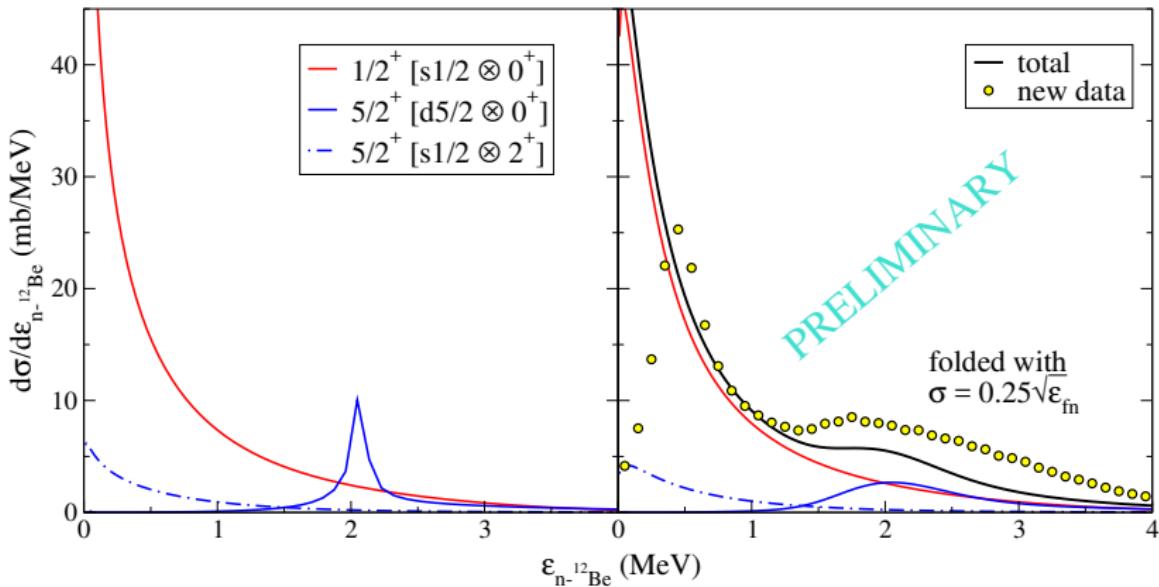
^{13}Be structure not clear

New data from RIKEN, 250 MeV/u. Anna Corsi *et al.*



$^{14}\text{Be}(p, pn)^{13}\text{Be}$ @ 250 MeV/u

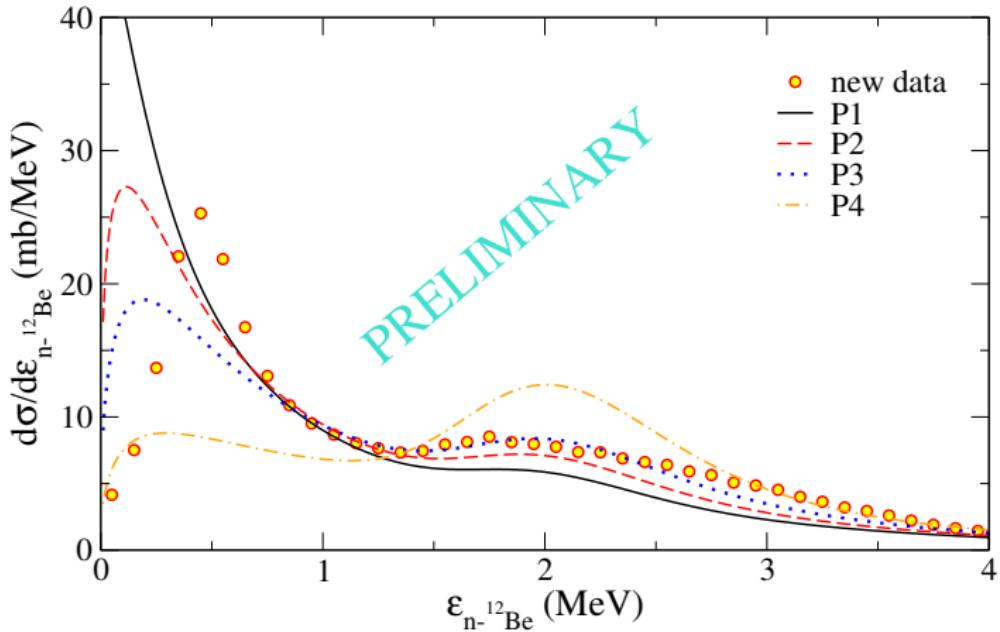
new data from RIKEN (A. Corsi)



Virtual state does not fit - too large scattering length
Missing cross section at high ε

$^{14}\text{Be}(p, pn)^{13}\text{Be}$ @ 250 MeV/u

new data from RIKEN (A. Corsi)



The $1/2^+$ state cannot account for the low-energy peak