
Two-photon Physics at Belle, KEKB

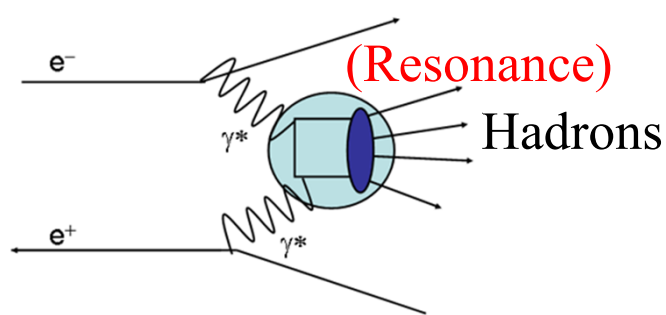


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Belle Collaboration



第12回 高エネルギー QCD・核子構造 勉強会
July 7, 2017

Two-photon Physics at e^+e^- collider



$Q = 0$, $C = +$,

for **real two-photon** system,

$J^P = 0^+, 0^-, 2^+, 2^-, 3^+, 4^+, 4^-, 5^+ \dots$ **(even) $^\pm$, (odd $\neq 1$) $^+$**

Strict constraints for quantum numbers \rightarrow **Determination of J^P by PWA**

$\Gamma_{\gamma\gamma}$: The cross section is proportional to the **two-photon partial decay width** of the resonance, useful information to explore **meson's internal structure**

Decay properties of the resonance

Searches/Discoveries of **new resonances**

Isospin mixing, interference effects among various processes

Form factors, Test of QCD (including a use of **highly virtual photons**)



KEKB Accelerator and Belle Detector

- Asymmetric $e^- e^+$ collider
8 GeV e^- (HER) x 3.5 GeV e^+ (LER)

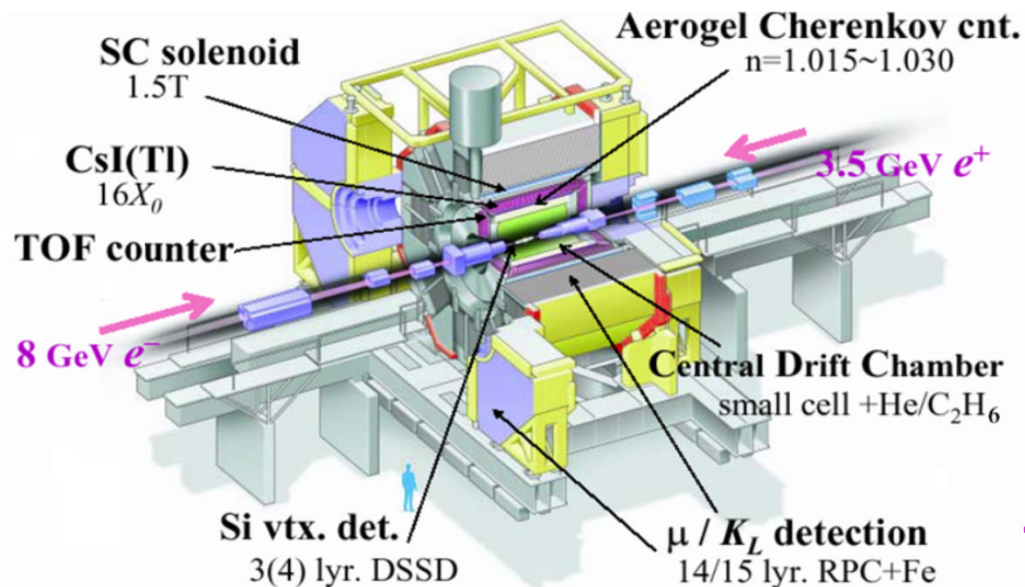
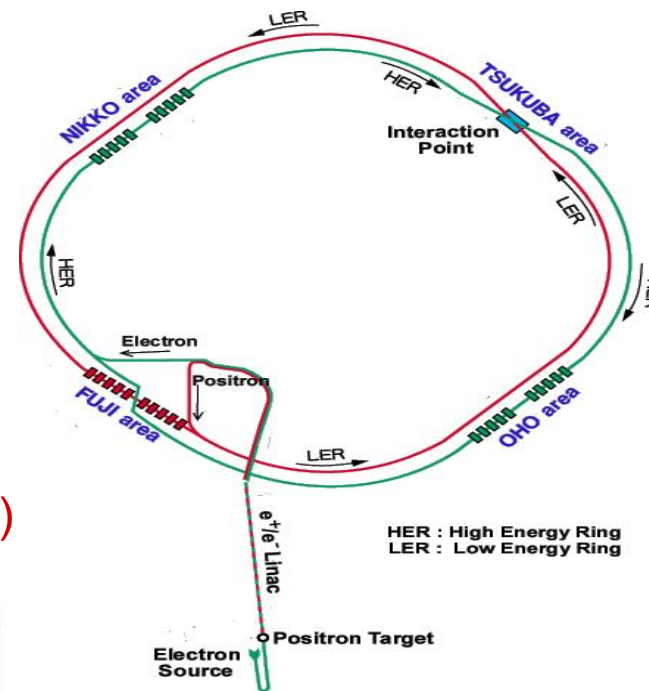
\sqrt{s} = around 10.58 GeV $\Leftrightarrow \Upsilon(4S)$

Beam crossing angle: 22mrad

- World-highest Luminosity

$$L_{\max} = 2.1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$$

$$\int L dt \sim 1040 \text{ fb}^{-1} \text{ (Completed in Jun.2010)}$$



High momentum/energy resolutions

CDC+Solenoid, CsI

Vertex measurement – Si strips

Particle identification

TOF, Aerogel, CDC-dE/dx,

RPC for K_L /muon

Published Two-photon Results from Belle

Process	Reference	Int. Lum.	$\gamma\gamma$ c.m. energy	Light Mesons	Charm.
$p p K^+ K^-$	PRD93,112017(2016)	980 fb ⁻¹	3.2-5.6 GeV	$\Lambda(1520), \theta(11540)$	$\chi_{c0}, c2$
$\gamma^* \gamma \rightarrow \pi^0 \pi^0$	PRD93, 032003 (2016)	759 fb ⁻¹	$Q^2 < 30$ GeV ²	$f_0(980), f_2(1270)$	
$K_S^0 K_S^0$	PTEP 2013, 123C01 (2013)	972 fb ⁻¹	1.05-4.0 GeV	$f_2(1270), a_2(1320), f_0(2500)$ $f_2'(1525), f_2(2200), f_0(1710)$	$\chi_{c0}, c2$ η_c
$\eta^+ \pi^+ \pi^-$	PRD 86, 052002 (2012)	673 fb ⁻¹	1.4-3.4 GeV	$\eta(1760), X(1835)$	η_c
$\gamma\gamma^* \rightarrow \pi^0$	PRD 86, 092007 (2012)	759 fb ⁻¹	$4 < Q^2 < 40$ GeV ²		
$\omega\phi, \phi\phi, \omega\omega$	PRL 108, 232001 (2012)	870 fb ⁻¹	< 4.0 GeV		$\chi_{c0}, c2$ η_c
$\eta\eta$	PRD82,114031(2010)	393 fb ⁻¹	1.096-3.8 GeV	$f_2(1270), f_2'(1525)$	$\chi_{c0}, c2$
$\omega J/\psi$	PRL 104, 092001 (2010)	694 fb ⁻¹	3.9-4.2 GeV		$\chi(3915)$
$\phi J/\psi$	PRL 104, 112004 (2010)	825 fb ⁻¹	4.2-5.0 GeV		$\chi(4350)$ 21
$\eta\pi^0$	PRD80:032001, 2009	223 fb ⁻¹	0.84-4.0 GeV	$a_0(980), a_0(1450), a_2(1320)$	
$\pi^0\pi^0$	PRD79:052009,2009	223 fb ⁻¹	0.6-4.1 GeV	$f_4(2050), f_2(1950)$	$\chi_{c0}, c2$
$\pi^0\pi^0$	PRD78:052004,2008	972 fb ⁻¹	0.6-4.0 GeV	$f_2(1270), f_0(980), f_2'(1525)$	$\chi_{c0}, c2$ η_c
four-meson	EPJC53,1(2008)	395 fb ⁻¹	1.4-3.4 GeV		$\chi_{c0}, c2, \eta_c,$ $\eta_c(2S)$
$K_S^0 K_S^0$	PLB 651, 15 (2007)	397.6 fb ⁻¹	2.4-4.0 GeV		$\chi_{c0}, c2$
$\pi^+ \pi^-$	PRD 75, 051101(2007)	85.9 fb ⁻¹	0.8-1.5 GeV	$f_0(980), f_2(1270), \eta'(958)$	
DD	PRL 96, 082003 (2006)	395 fb ⁻¹			χ'_{c2}
pp	PLB 621, 41 (2005)	89 fb ⁻¹	2.03-4.0 GeV		η_c
$\pi^+ \pi^- / K^+ K^-$	PLB 615, 39 (2005)	87.7 fb ⁻¹	2.4-4.1 GeV		$\chi_{c0}, c2$
$K^+ K^-$	EPJC32,323(2003)	67 fb ⁻¹	1.4-2.4 GeV	$f_2'(1525)$	
$\gamma J/\psi$	PLB 540, 33 (2002)	32.6 fb ⁻¹	3.2-3.8 GeV		χ_{c2} 22

Comments

Pentaquarks

Single tag, scalar and tensor meson TFF

Neutral P-meson pair

P-, PT- mesons

Single tag, pi0 TFF

Neutral V-meson pairs

Neutral P-meson pair

Exotic charmonium-like

Exotic charmonium-like

Neutral P-meson pair

Neutral P-meson pair

Neutral P-meson pair

Charmonium decays

Neutral P-meson pair

Charged P-meson pair

New charmonium

Baryon pair

Charged P-meson pair

Radiative decay of charmonium

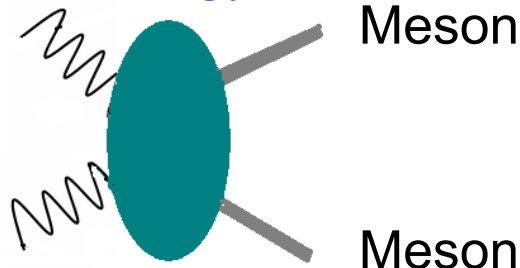


QCD test at high-energy region

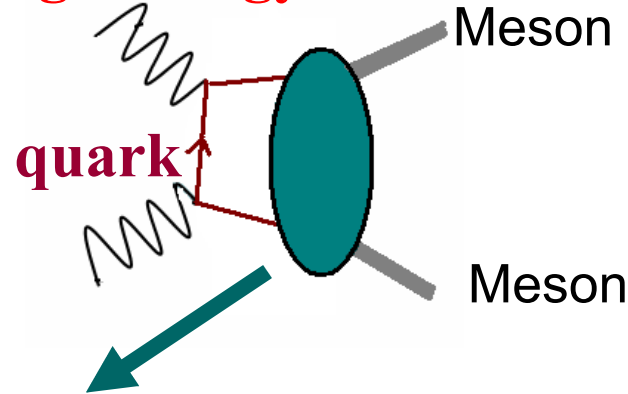


Meson-pair production and QCD

Low energy

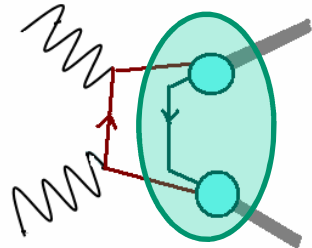


High energy



High energy

Brodsky and Lepage



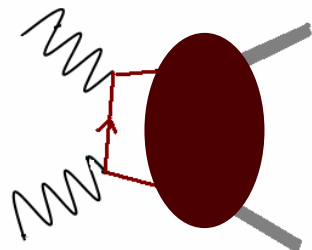
Perturbative QCD approach

for exclusive meson production

Works with refined **form factors**

S.J.Brodsky, G.P.Lepage, PRD 24, 1808 (1981)

M.Benayoun, V.L.Chernyak, NPB329,209(1990)



Kroll, Diehl and Vogt

Handbag model

with soft hadron exchange

Predicts...

Scattering-angle
(of meson)
distribution,


Energy -dependence

Cross section ratios
under SU(3) sym.

M.Diehl, P.Kroll, and C. Vogt, PLB 532, 99 (2002)
M.Diehl, P.Kroll, PLB 683, 165 (2010)

“ $\gamma\gamma \rightarrow$ Pseudoscalar-meson pair” from Belle

10 papers for 6 processes

Process	Reference		Int.Lum. (fb ⁻¹)	$\gamma\gamma$ c.m. Energy (GeV)	Light Mesons	QCD	Char- monia
$\pi^+\pi^-$	PLB 615, 39 (2005)		87.7	2.4 - 4.1		√	√
	PRD 75, 051101(R) (2007)		85.9	0.8 - 1.5	√		
	J. Phys. Soc. Jpn. 76, 074102 (2007)		85.9	0.8 - 1.5	√		
K^+K^-	EPJC 32, 323 (2003)		67	1.4 - 2.4	√		
	PLB 615, 39 (2005)		87.7	2.4 - 4.1		√	√
$\pi^0\pi^0$	PRD 78, 052004 (2008)		95	0.6 - 4.0	√		
	PRD 79, 052009 (2009)		223	0.6 - 4.0	√	√	√
$K_S^0 K_S^0$	PLB 651, 15 (2007)		397.1	2.4 - 4.0		√	√
	PTEP 2013, 123C01 (2013)		972	1.05 - 4.0	√	√	√
$\eta\pi^0$	PRD 80, 032001 (2009)		223	0.84 - 4.0	√	√	
$\eta\eta$	PRD 82, 114031 (2010)		393	1.1 - 3.8	√	√	√

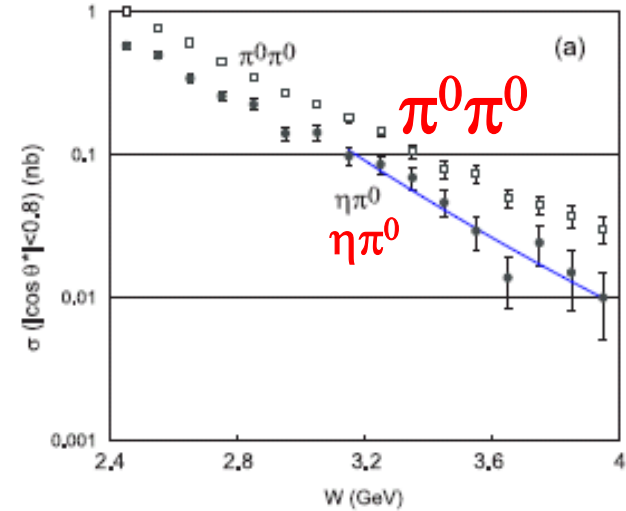
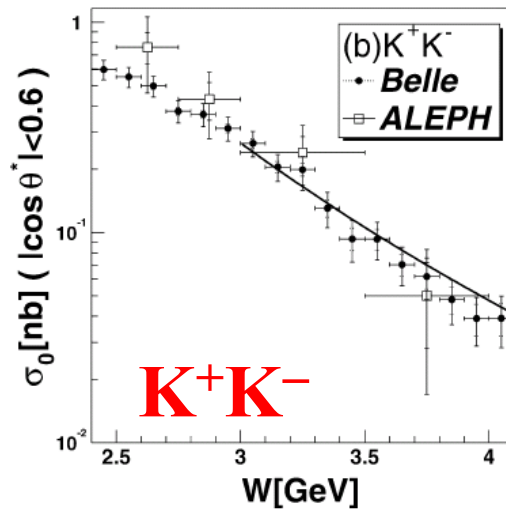
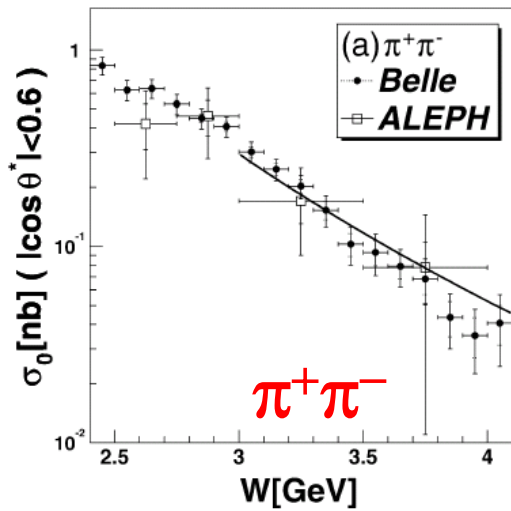
Differential cross section $d\sigma/d|\cos\theta^*|$ for these processes are measured.



W-dependences at high energies

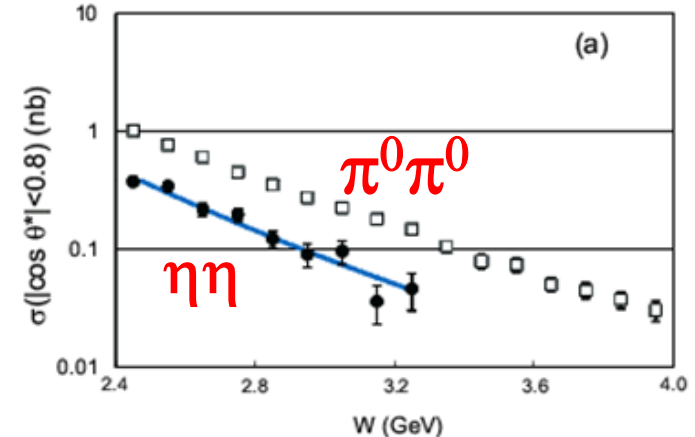
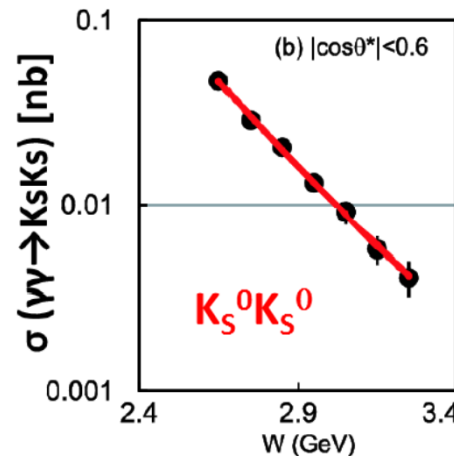
$$W \equiv W_{\gamma\gamma} \equiv \sqrt{s_{\gamma\gamma}} \quad \text{Collision's c.m. energy}$$

Assume or expect $\sigma(W) \sim W^{-n}$



Fitted and reproduced
Slope parameter **n** different
among the reactions

Charmonium contributions
not included/removed



Cross sections and their ratios

Process	n	$W(\text{GeV})$	$ \cos \theta^* $	BL	BC	DKV
$K_S^0 K_S^0$	$11.0 \pm 0.4 \pm 0.4$	$2.4 - 4.0^\dagger$	< 0.8		10	
$\pi^+ \pi^-$	$7.9 \pm 0.4 \pm 1.5$	$3.0 - 4.1$	< 0.6	6	6	
$K^+ K^-$	$7.3 \pm 0.3 \pm 1.5$	$3.0 - 4.1$	< 0.6	6	6	
$\pi^0 \pi^0$	$8.0 \pm 0.5 \pm 0.4$	$3.1 - 4.1^\dagger$	< 0.8		10	
$\eta \pi^0$	$10.5 \pm 1.2 \pm 0.5$	$3.1 - 4.1$	< 0.8		10	
$\eta \eta$	$7.8 \pm 0.6 \pm 0.4$	$2.4 - 3.3$	< 0.8		10	
Process	σ_0 ratio	$W(\text{GeV})$	$ \cos \theta^* $	BL	BC	DKV
$K^+ K^- / \pi^+ \pi^-$	$0.89 \pm 0.04 \pm 0.15$	$3.0 - 4.1$	< 0.6	2.3	1.06	
$K_S K_S / K^+ K^-$	~ 0.10 to ~ 0.03	$2.4 - 4.0$	< 0.6		0.005	2/25
$\pi^0 \pi^0 / \pi^+ \pi^-$	$0.32 \pm 0.03 \pm 0.06$	$3.1 - 4.1$	< 0.6		0.04-0.07	0.5
$\eta \pi^0 / \pi^0 \pi^0$	$0.48 \pm 0.05 \pm 0.04$	$3.1 - 4.0$	< 0.8		$0.24 R_f (0.46 R_f)^\ddagger$	
$\eta \eta / \pi^0 \pi^0$	$0.37 \pm 0.02 \pm 0.03$	$2.4 - 3.3$	< 0.8		$0.36 R_f^2 (0.62 R_f^2)^\ddagger$	

† Exclude χ_{cJ} region, 3.3 - 3.6 GeV.

‡ Assuming η is a member of SU(3) octet (superposition of octet and singlet with mixing angle of $\theta_p = -18^\circ$).

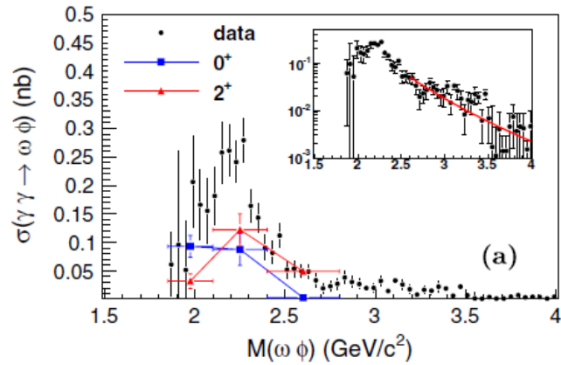
R_f is a ratio of decay constants, $f_\eta^2 / f_{\pi^0}^2$.

- n ranges 7 to 11. Close or not far from QCD prediction of 6 and 10.
- Cross section ratios tend to be constant above 3 GeV.

Summarized by H.Nakazawa
Hadron2013

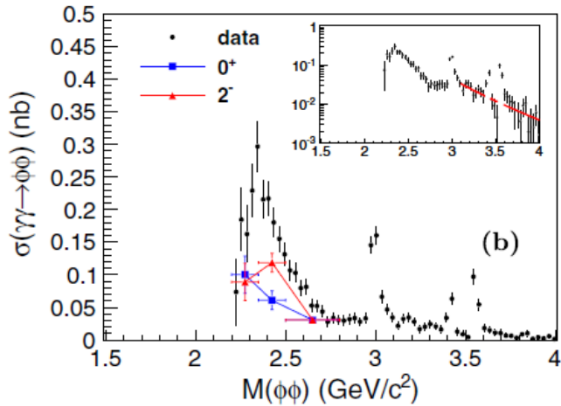


$\gamma\gamma \rightarrow$ Vector-meson pair



$\omega\phi$

Belle, PRL 108, 232001 (2012)



$\phi\phi$

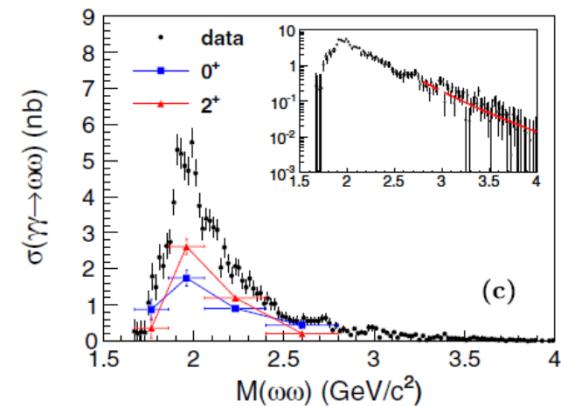
Discussion of the Cross-section sizes
by V. Chernyak
(arXiv:1212.1304[hep-ph])

Slope parameters for high W:

$$n = 7.2 \pm 0.6 (\omega\phi)$$

$$8.4 \pm 1.1 (\phi\phi)$$

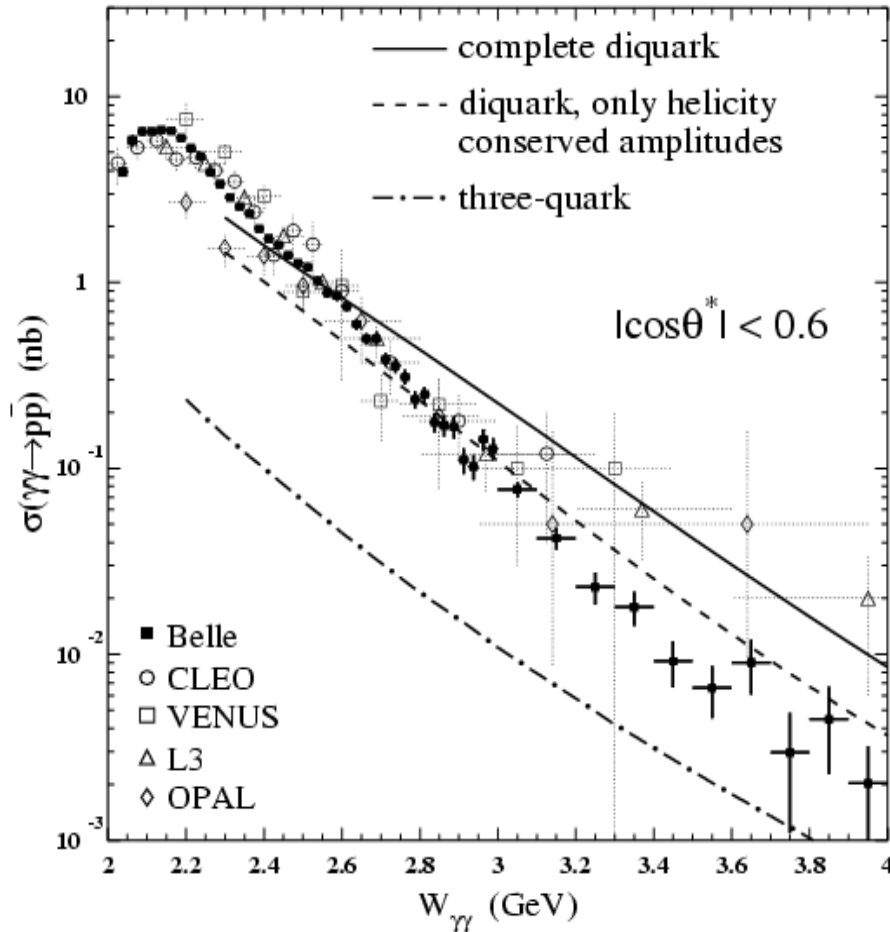
$$9.1 \pm 0.6 (\omega\omega)$$



$\omega\omega$



$p\bar{p}$ final-state cross sections



PLB 621, 41 (2005)

$W_{\gamma\gamma}^{-n}$ dependence

$$n = 15.1 \pm_{1.1}^{0.8} \quad @ \quad 2.5 - 2.9 \text{ GeV}$$

$$n = 12.4 \pm_{2.3}^{2.4} \quad @ \quad 3.2 - 4.0 \text{ GeV}$$

Might agree with a

QCD prediction $n = 10$

at some energy above 3.1 GeV

Slope – steeper than meson pairs

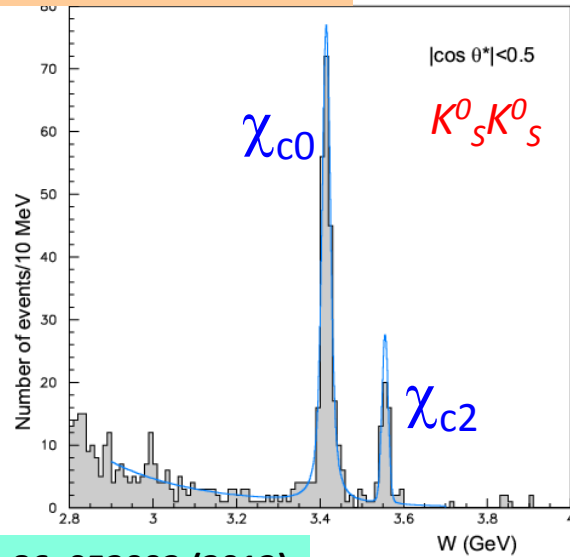


C-even Charmonium(-like) states



Most beautiful signals

PTEP 2013, 123C01 (2013)



Yield

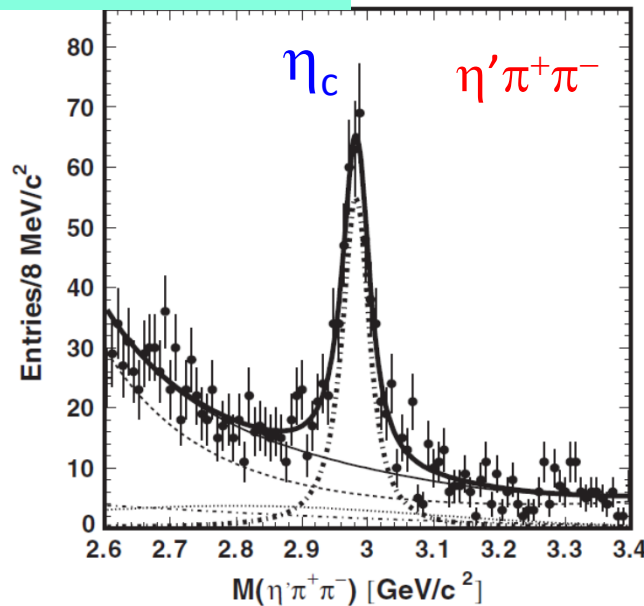
Interference	$N_{\chi_{c0}}$	$N_{\chi_{c2}}$	$-2 \ln \mathcal{L}/ndf$
not included	$248.3^{+17.9}_{-17.2}$	$53.0^{+8.1}_{-7.4}$	57.34/73
included	266 ± 53	53^{+14}_{-12}	57.22/71

* Interference between χ_{c0} and continuum

Product of two-photon decay width and $B(K_S^0 K_S^0)$

Interference	$\Gamma_{\gamma\gamma} \mathcal{B}(\chi_{c0})$ (eV)	$\Gamma_{\gamma\gamma} \mathcal{B}(\chi_{c2})$ (eV)
not included	$8.09 \pm 0.58 \pm 0.83$	$0.268^{+0.041}_{-0.037} \pm 0.028$
included	$8.7 \pm 1.7 \pm 0.9$	$0.27^{+0.07}_{-0.06} \pm 0.03$
Belle 2007	$7.00 \pm 0.65 \pm 0.71$	$0.31 \pm 0.05 \pm 0.03$
PDG 2012	7.3 ± 0.5	0.297 ± 0.026

PRD 86, 052002 (2012)



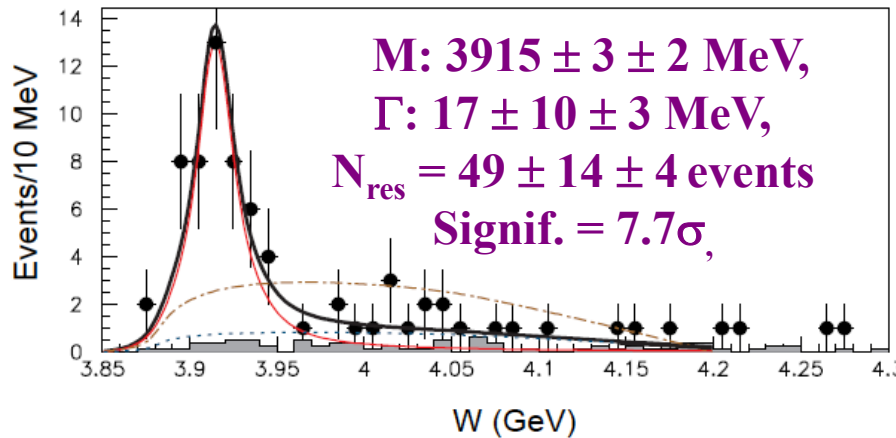
$\eta_c(1S) \rightarrow \eta' \pi^+ \pi^-$; $\Gamma_{\gamma\gamma} \mathcal{B}$ is the product of the two-photon decay width and the branching fraction. The world-average values are shown for comparison.

Parameters	This work	PDG
Y	$486^{+40}_{-39} \pm 53$	
$M, \text{MeV}/c^2$	$2982.7 \pm 1.8 \pm 2.2$	2980.3 ± 1.2
$\Gamma, \text{MeV}/c^2$	$37.8^{+5.8}_{-5.3} \pm 2.8$	26.7 ± 3
$\Gamma_{\gamma\gamma} \mathcal{B}, \text{eV}/c^2$	$50.5^{+4.2}_{-4.1} \pm 5.6$	194 ± 97
$\mathcal{B}, \%$	0.87 ± 0.20	2.7 ± 1.1



Peak of X(3915) in $\gamma\gamma \rightarrow \omega J/\psi$ and $\chi_{cJ}(2P)$

694 fb⁻¹ Belle, PRL 104, 092001 (2010)



The peak is confirmed by BaBar

BaBar, PRD 86, 072002 (2012)

M: 3919.4 ± 2.2 ± 1.6 MeV,
 Γ: 13 ± 6 ± 3 MeV,

Is X(3915) ≡ Y(3940) = $\chi_{c0}(2P)$?

It is believed as two-photon production of Y(3940) discovered in B decays, but the spin=0 is not finally confirmed, yet.

X(3915)
 was $\chi_{c0}(3915)$

$$J^G(J^{PC}) = 0^+(0 \text{ or } 2^{++})$$

Mass $m = 3918.4 \pm 1.9$ MeV
 Full width $\Gamma = 20 \pm 5$ MeV (S = 1.1)

X(3915) DECAY MODES	Fraction (Γ_i/Γ)	p (MeV/c)
$\omega J/\psi$	seen	222
$\pi^+ \pi^- \eta_c(1S)$	not seen	785
$\eta_c \eta$	not seen	665
$\eta_c \pi^0$	not seen	815
$K \bar{K}$	not seen	1896
$\gamma\gamma$	seen	1050

The first 2P charmonium state discovered in two-photon by Belle PRL 96, 082003 (2006)

$\chi_{c2}(2P)$

Mass $m = 3927.2 \pm 2.6$ MeV
 Full width $\Gamma = 24 \pm 6$ MeV

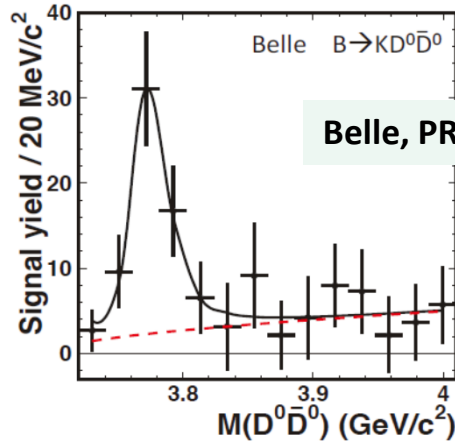
The mass is different, a little.

$\chi_{c2}(2P)$ DECAY MODES	Fraction (Γ_i/Γ)	p (MeV/c)
$\gamma\gamma$	seen	1964
$D \bar{D}$	seen	615
$D^+ D^-$	seen	600
$D^0 \bar{D}^0$	seen	615
$\pi^+ \pi^- \eta_c(1S)$	not seen	793
$K \bar{K}$	not seen	1901

Any $\chi_{c0}(2P) \rightarrow D\bar{D}$ seen?

It is expected that $\chi_{c0}(2P)$ has a large coupling to $D\bar{D}$

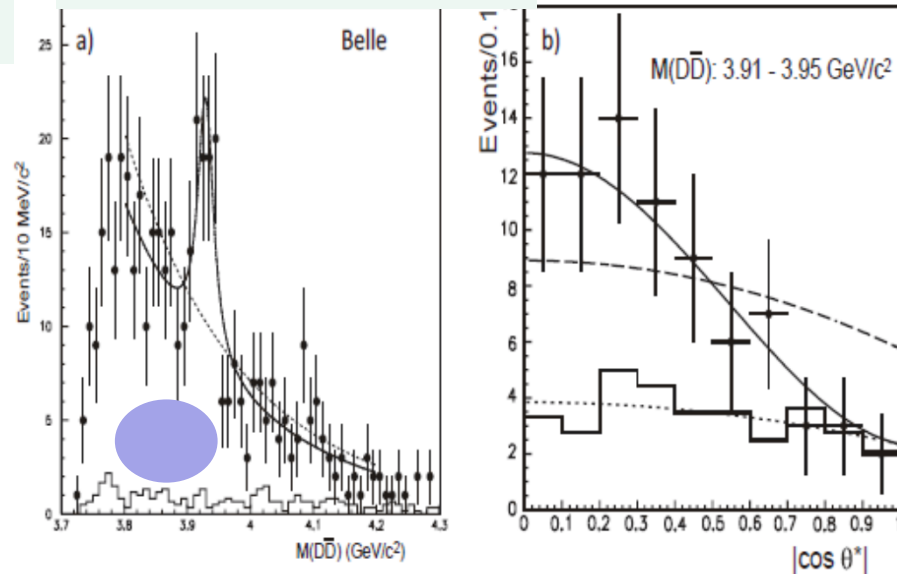
No signature of X(3915) in $B \rightarrow D\bar{D}K$



Belle, PRL 100, 092001 (2008)

$\gamma\gamma \rightarrow \chi_{c2}(2P)$ ($M=3927\text{MeV}$) $\rightarrow D\bar{D}$ is discovered
But no Scalar component is found.

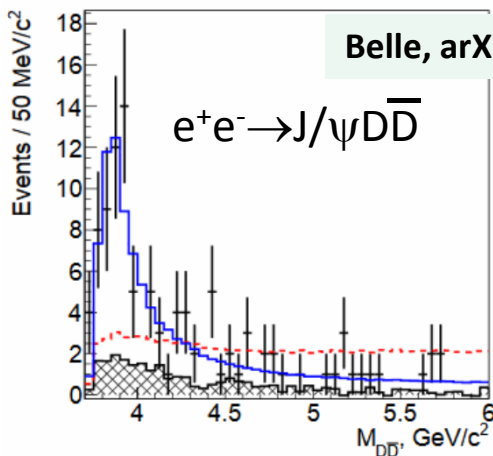
Belle, PRL 96, 082003 (2006)



↑ The 3.8 GeV region is contaminated by $D\bar{D}^*$ production, according to the p_t distribution

← From double-charmonium production study

$\chi_{c0}(2P)$ is lighter (3800-3900MeV) and much broader?



Belle, arXiv 1704.01872(2017)



See S.L. Olsen, PRD 91, 057501 (2015)

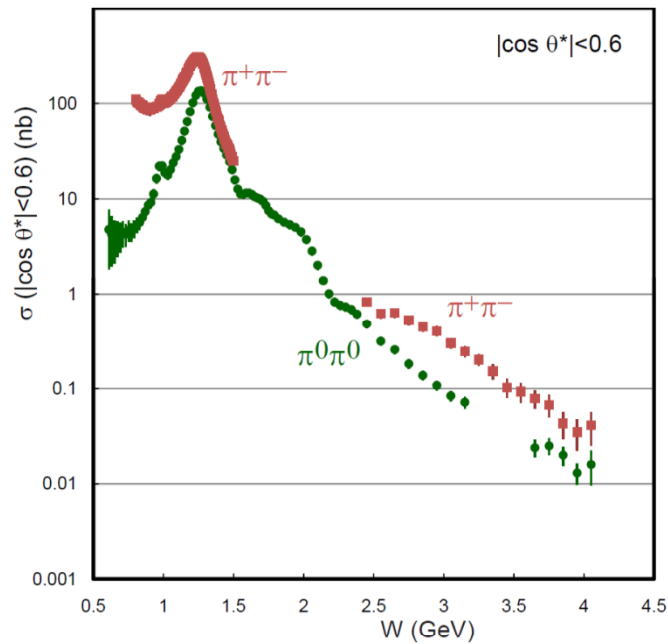
S.Uehara, KEK, Jul. 2017

Light-meson spectroscopy



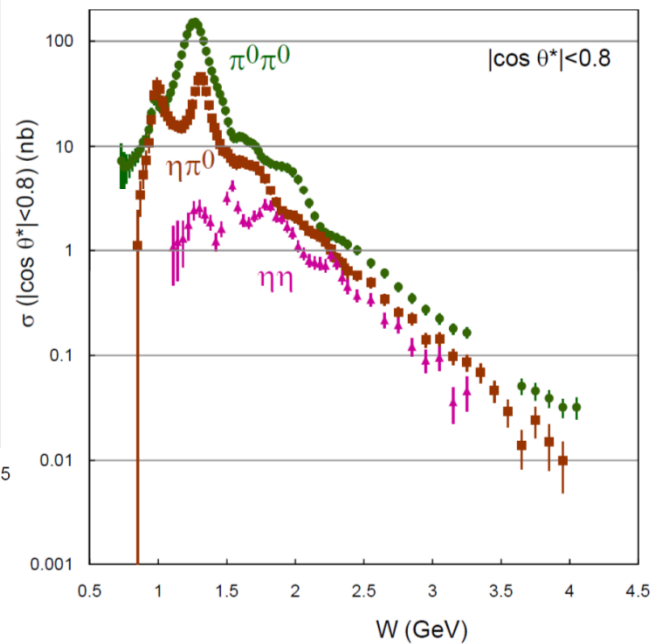
The six processes; in total ~20 peaks

Charged vs Neutral $\pi\pi$

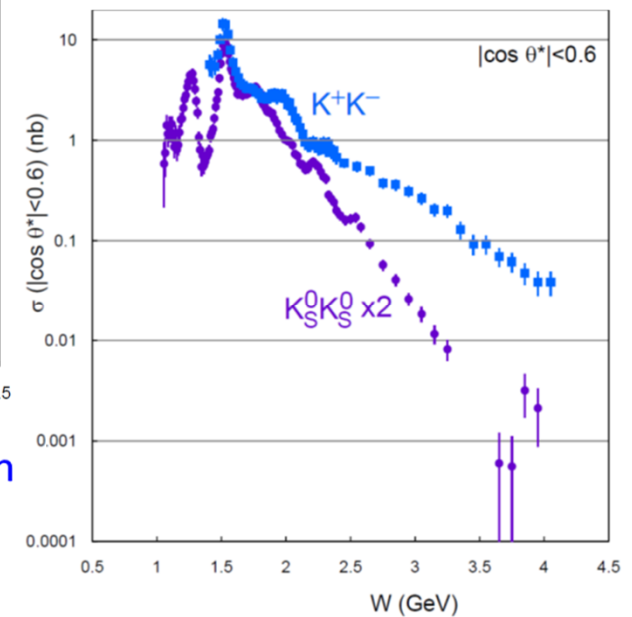


Three neutral-pair processes

$\pi^0\pi^0$, $\eta\pi^0$, $\eta\eta$



Charged vs Neutral $K\bar{K}$



Horizontal axis:

W -- $\gamma\gamma$ c.m. energy = invariant mass of the two-meson system

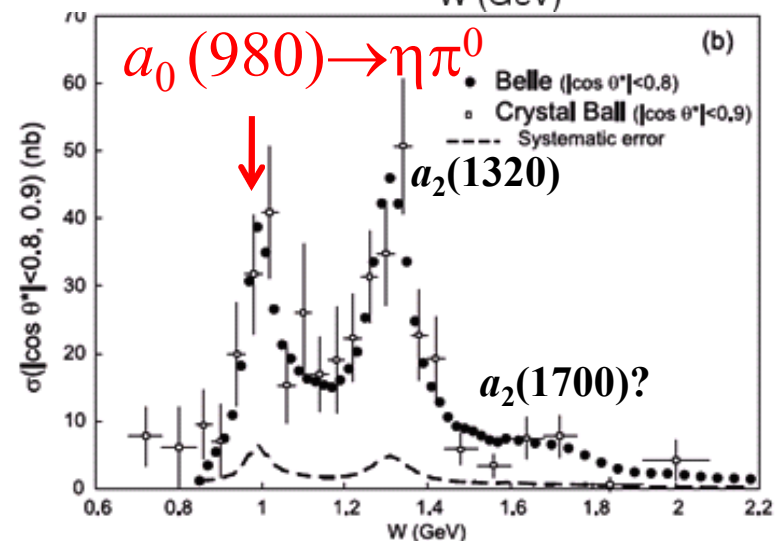
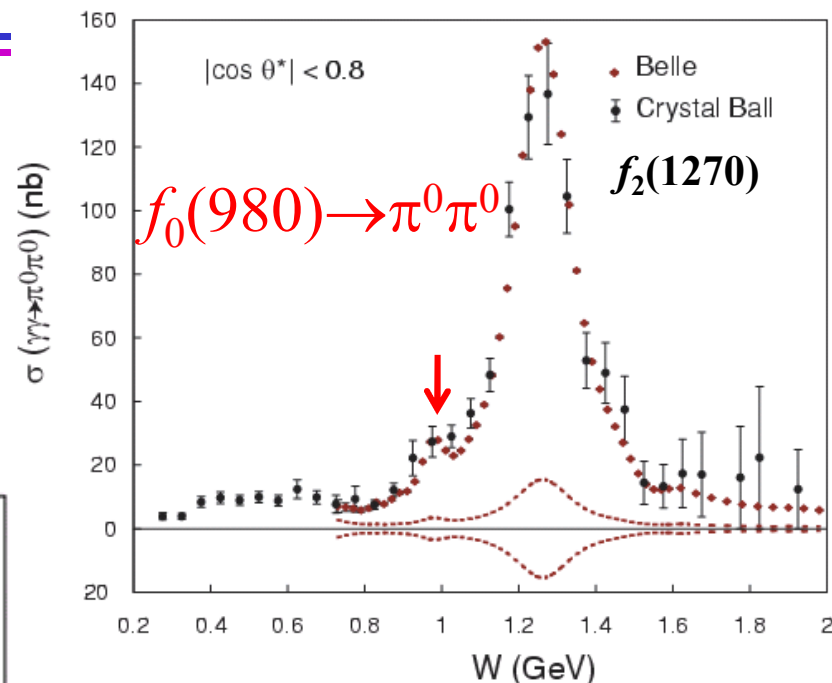
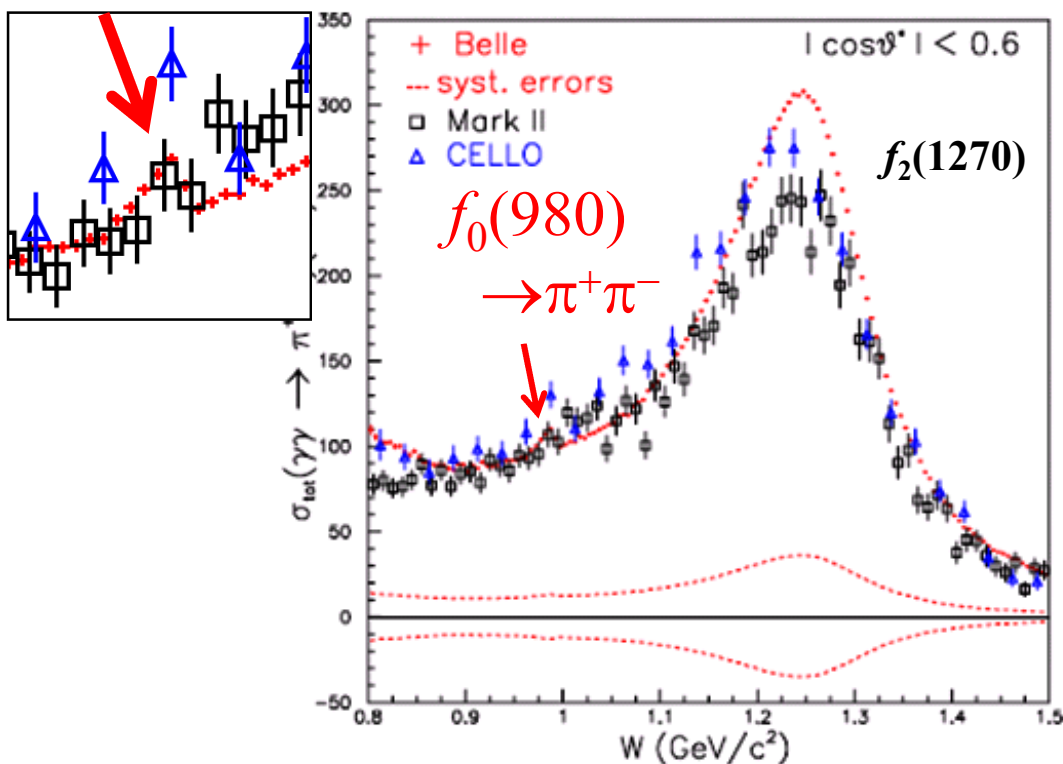
$W < \sim 2.5$ GeV: Dominated by resonances

$W > \sim 2.5$ GeV: (Netnegative) Power law works + (χ_c charmonia)

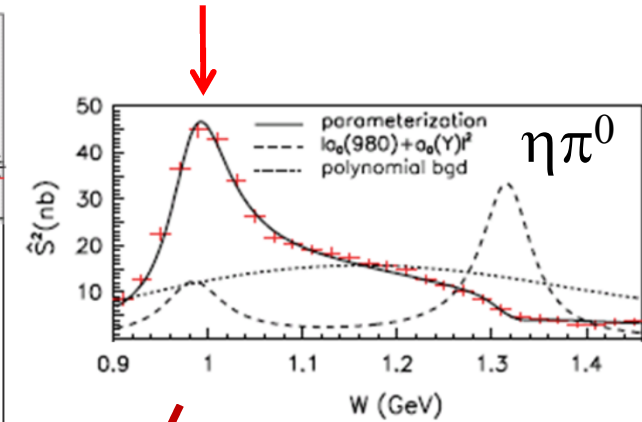
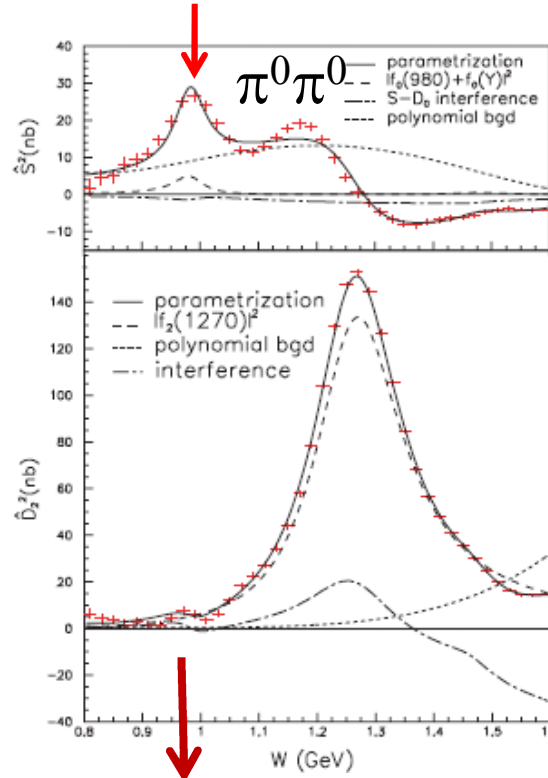
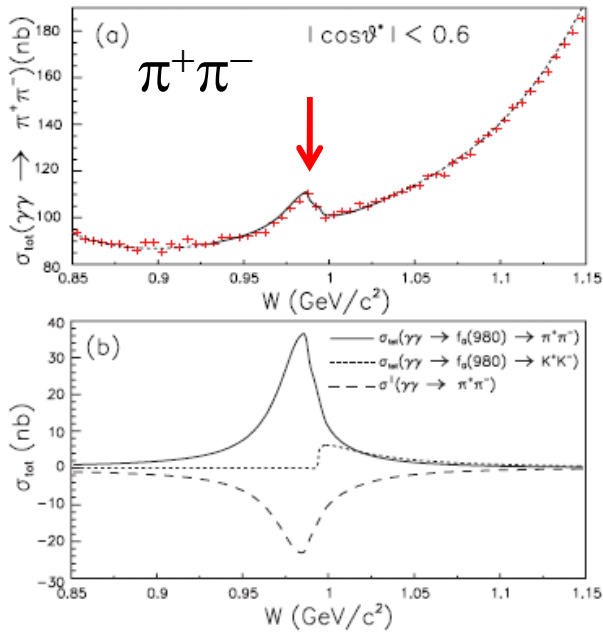


Confirmation of $f_0(980)$ and $a_0(980)$ formations

$f_0(980)$ and $a_0(980)$:
Observed as a peak very clearly in two-photon production, for the first time.



Two-photon decay width of $f_0(980)$ and $a_0(980)$



Predictions for $f_0(980)$

Meson	$f_0(980)$	$f_0(980)$	$a_0(980)$
M[MeV/c ²]	985.6 ^{+1.2+1.1} _{-1.5-1.6}	982.2 ± 1.0 ^{+8.1} _{-8.0}	982.3 ^{+0.6+3.1} _{-0.7-4.7}
$\Gamma_{\pi\pi/\text{tot}}$ [MeV]	51.3 ^{+20.9+13.2} _{-17.7-3.8}	66.9 ^{+13.9+8.8} _{-11.8-2.5}	75.6 ± 1.6 ^{+17.4} _{-10.0} (Γ_{tot})
$\Gamma_{\gamma\gamma}$ [eV]	205 ⁺⁹⁵⁺¹⁴⁷ ₋₈₃₋₁₁₇	286 ± 17 ⁺²¹¹ ₋₇₀	128 ⁺³⁺⁵⁰² ₋₂₋₄₃ / $\mathcal{B}_{\pi^0\eta}$

Model	$\Gamma_{\gamma\gamma}$ [eV]
<i>uubar, ddbar</i>	1300 – 1800
<i>ssbar</i>	300 – 500
KKbar molecule	200 – 600
Four-quark	270

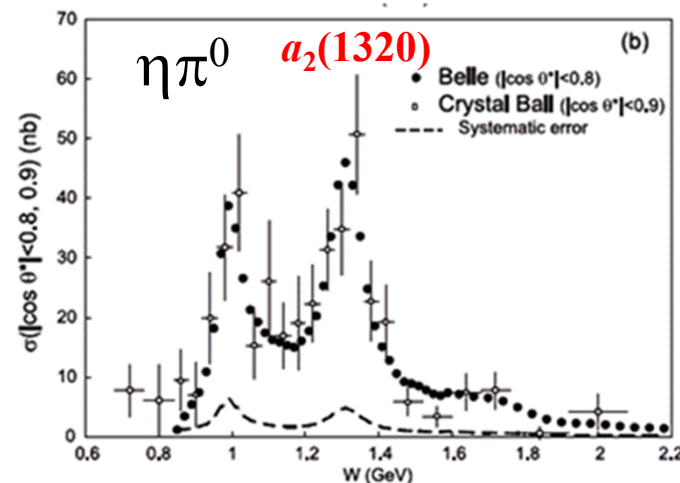
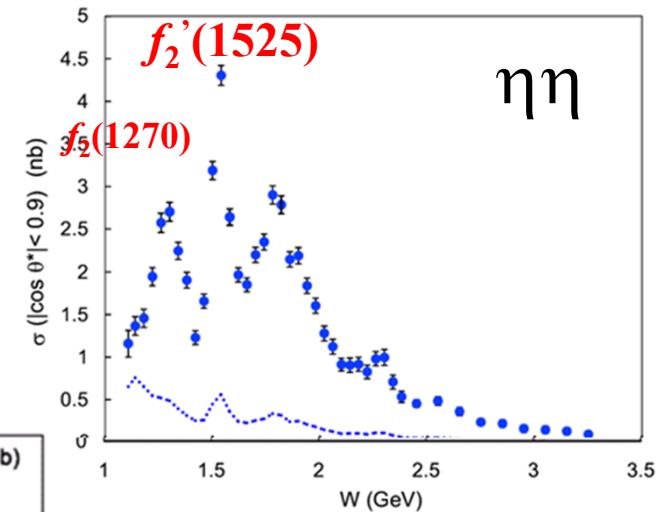
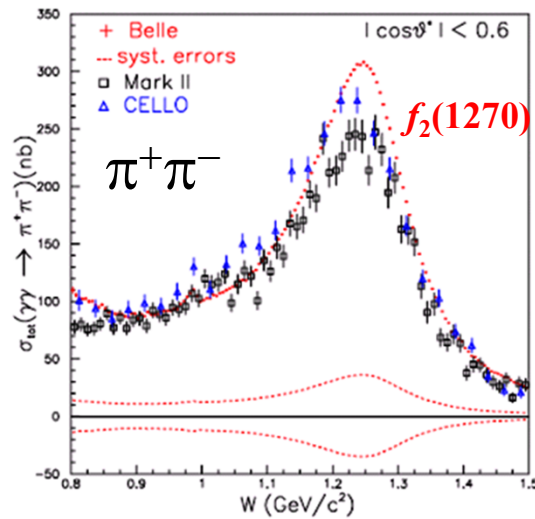


The tensor-meson triplet, $f_2(1270)$, $a_2(1320)$, $f_2'(1525)$

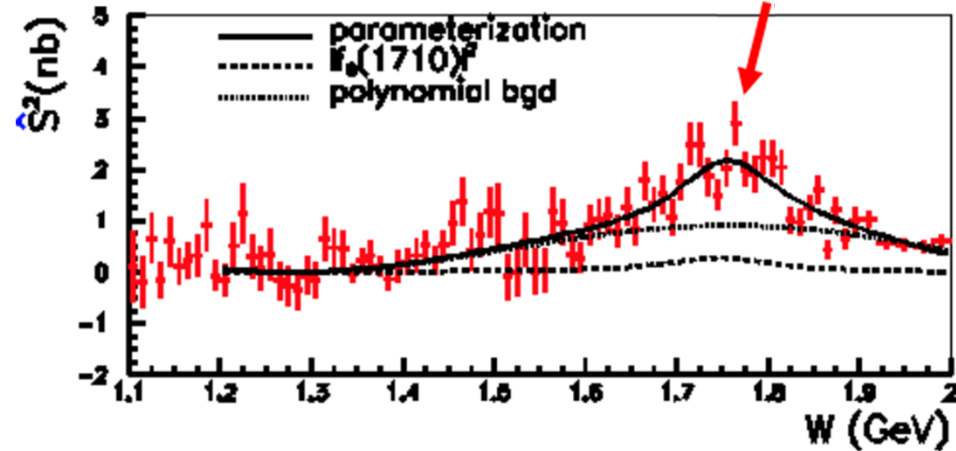
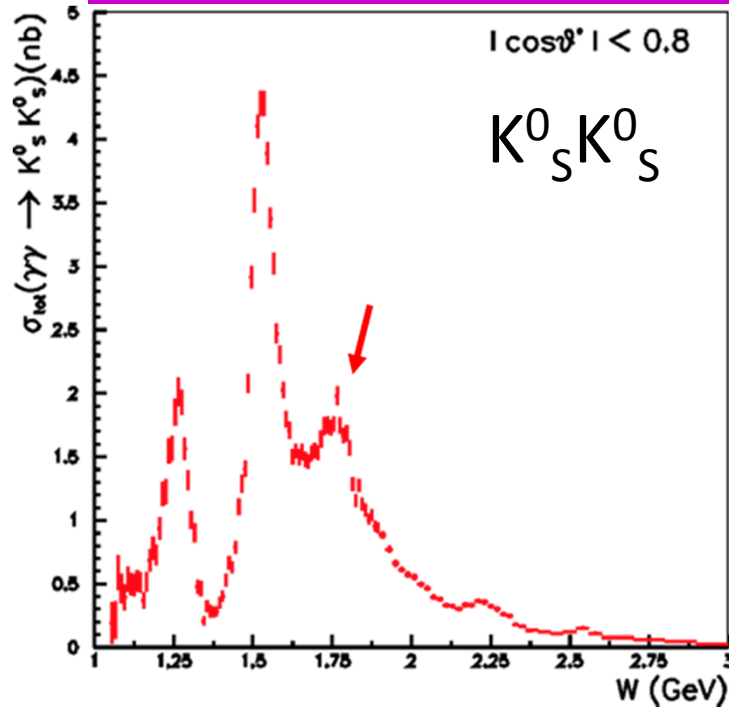
$f_2(1270)$: The largest peak in $\pi^+\pi^-$ and $\pi^0\pi^0$. Also seen in $\eta\eta$

$a_2(1320)$: Large peak in $\eta\pi^0$

$f_2'(1525)$: Large peak in $\eta\eta$, K^+K^- , and $K_S^0K_S^0$



$f_0(1710)$ formation in $K_S^0 K_S^0$



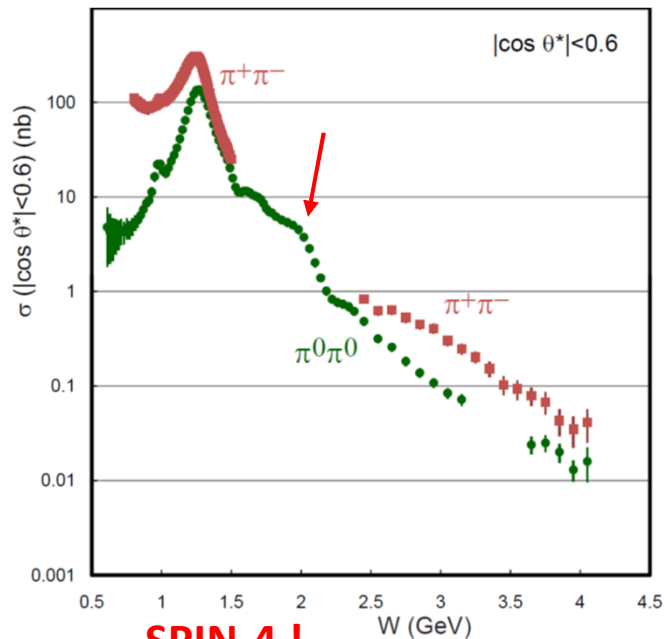
Assuming a single resonance,
 $J = 0$ or 2 ? $J = 0$ is much preferred.

Parameter	$f_0(1710)$ fit				$f_2(1710)$ fit	
	fit-H	fit-L	H,L combined	PDG	fit-H	fit-L
$f_J(1710)$						
χ^2/ndf	694.2/585	701.6/585	Two solutions of interference		796.3/585	831.5/585
Mass(f_J) (MeV/ c^2)	1750^{+5+29}_{-6-18}	1749^{+5+31}_{-6-42}	1750^{+6+29}_{-7-18}	1720 ± 6	1750^{+6}_{-7}	1729^{+6}_{-7}
$\Gamma_{\text{tot}}(f_J)$ (MeV)	138^{+12+96}_{-11-50}	145^{+11+31}_{-10-54}	139^{+11+96}_{-12-50}	135 ± 6	132^{+12}_{-11}	150 ± 10
$\Gamma_{\gamma\gamma} \mathcal{B}(K\bar{K})_{f_J}$ (eV)	12^{+3+227}_{-2-8}	21^{+6+38}_{-4-26}	12^{+3+227}_{-2-8}	unknown	$2.1^{+0.5}_{-0.3}$	1.6 ± 0.2

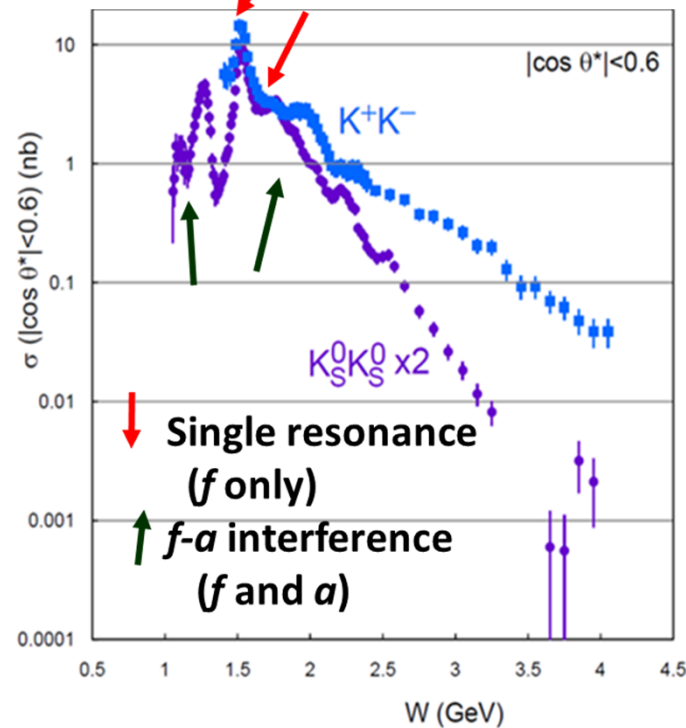
$f_0(1710) \rightarrow K_S^0 K_S^0$ is confirmed in two-photon process.

The 1.8 – 2.2 GeV region

- $f_2(1950) \rightarrow \pi^0\pi^0$ shows a broad structure
- Similar structure exists in K^+K^- (but, they can be different states)
- No peak in $\eta\pi^0$, $\eta\eta$ and $K_S^0 K_S^0$ in this mass region



$I=0$ (f) and $I=1$ (a) interference in $K\bar{K}$



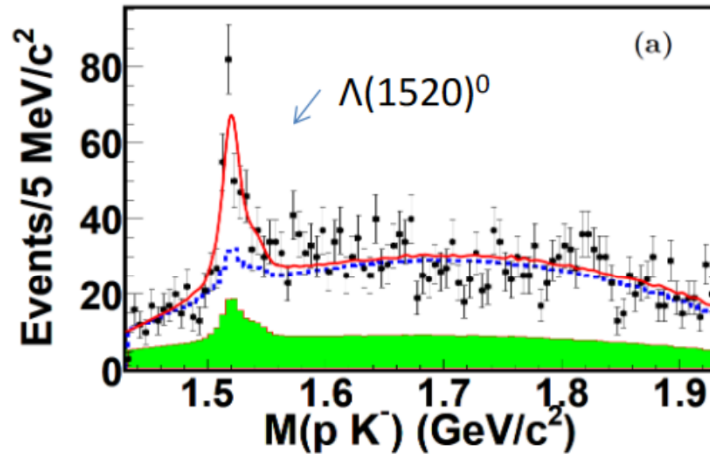
Parameter	$f_4(2050)$	" $f_2(1950)$ "	Unit
Mass	$1885^{+14}_{-13} +^{+218}_{-25}$	$2038^{+13}_{-11} +^{+12}_{-73}$	MeV/c^2
Γ_{tot}	$453 \pm 20 +^{+31}_{-129}$	$441^{+27}_{-25} +^{+28}_{-192}$	MeV
$\Gamma_{\gamma\gamma} \mathcal{B}(\pi^0\pi^0)$	$7.7^{+1.2}_{-1.1} +^{+23.5}_{-5.2}$	$54^{+23}_{-14} +^{+379}_{-68}$	eV

$\chi^2(ndf)$ 323.2 (311)

Search for exotic baryons (Pentaquarks)

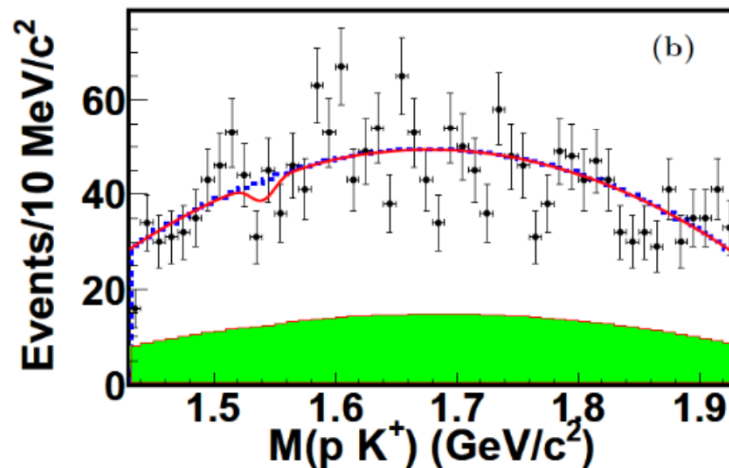


PRD 93, 1120137(2016)



Simultaneous fit: $\Lambda(1520)^0$ and $\Theta(1540)^0$ signal are included.

The shaded histogram: $\sum Pt^*$ sideband
 $288 \pm 48 \Lambda(1520)^0$ events, 8.6σ
 $22 \pm 34 \Theta(1540)^0$ events, 1.4σ



Similar simultaneous fit: $\Theta(1540)^{++}$ signal
 Solid line: the simultaneous fit

The dotted curve: background estimate
 The shaded histogram: $\sum Pt^*$ sideband
 $-16 \pm 34 \Theta(1540)^{++}$ events



Single-tag measurement and meson TFFs

TFF: transition form factor

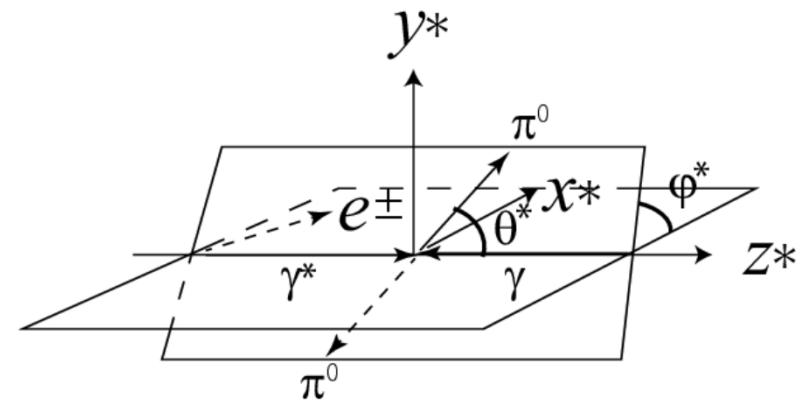
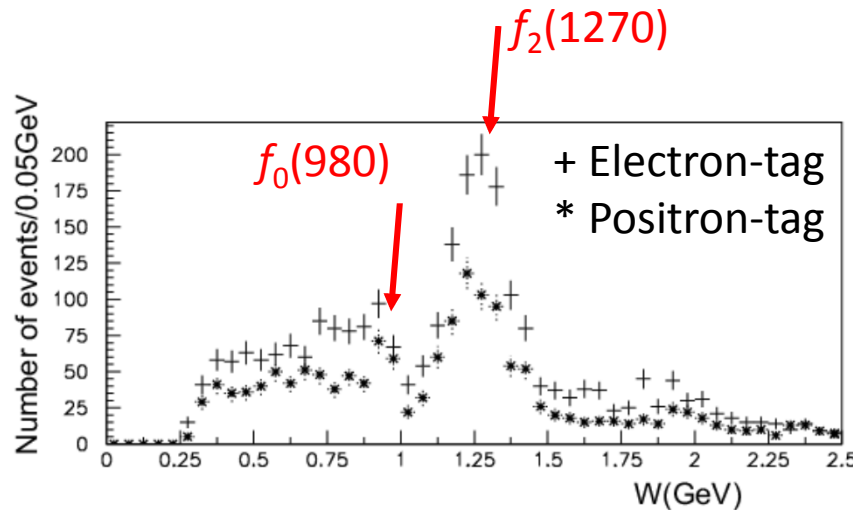
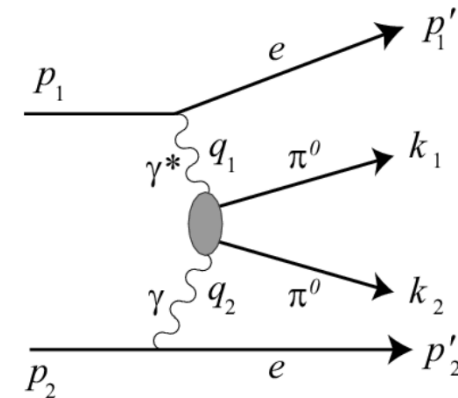


$\gamma^*\gamma \rightarrow \pi^0\pi^0 : f_0(980) \text{ and } f_2(1270) \text{ TFF's}$

Physics motivations:

- Q^2 dependence of TFF for scalar and tensor mesons
(This is the first measurement)
- Test of QCD of $q\bar{q}$ meson model
- Light-by-Light – hadronic contribution for $g-2|_\mu$

PRD 93, 032003 (2016)



The f_0/f_2 ratio is larger than in the no-tag case.



Formalism of PWA

$$|F(Q^2)| = \sqrt{\frac{\sigma_R^\lambda(Q^2)}{\sigma_R^\lambda(0)(1 + \frac{Q^2}{M^2})}}$$

TFF is defined for each resonance R produced with each helicity λ

To obtain the resonance amplitudes:

Perform PWA, parameterizing W dependence of the resonance and continuum components of each helicity amplitude, e.g.,

$$\frac{d\sigma(\gamma^*\gamma \rightarrow \pi^0\pi^0)}{d\Omega} = \sum_{n=0}^2 t_n \cos(n\varphi^*),$$

$$t_0 = |M_{++}|^2 + |M_{+-}|^2 + 2\epsilon_0 |M_{0+}|^2,$$

$$t_1 = 2\epsilon_1 \Re((M_{+-}^* - M_{++}^*)M_{0+}),$$

$$t_2 = -2\epsilon_0 \Re(M_{+-}^* M_{++}),$$

$$M_{++} = S + D_0,$$

$$S = B_S(W) + A_{f_0}(W)$$

$$D_0 = 4\pi [B_{D_0}(W) + A_{f_2}(W)\sqrt{r_{20}}] Y_2^0$$

etc.

Determine each component as well as the relative phase by a fit

++ etc. --- Helicity state of the incident photons

S, D_0 etc. -- Partial-wave amplitude in $\pi^0\pi^0$ scattering

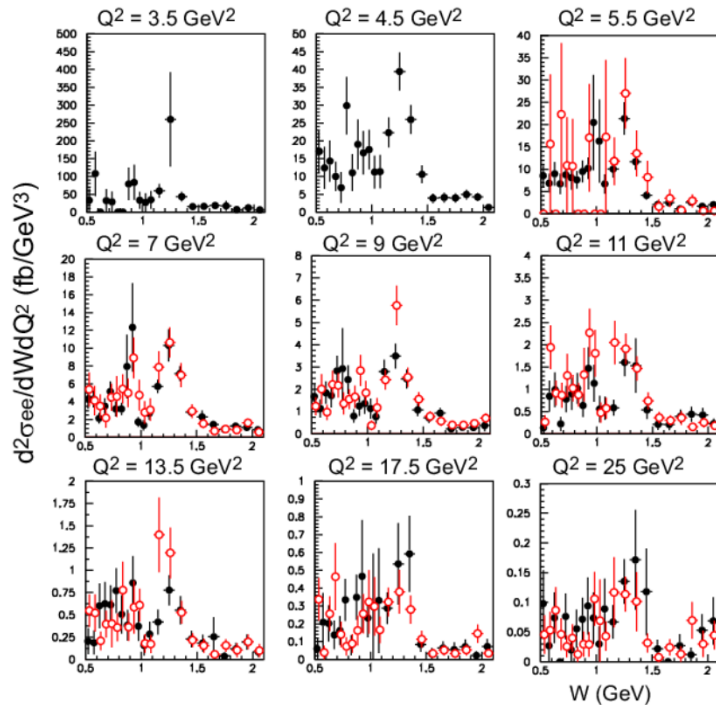
B, A_f -- Background and f -resonance components.

ϵ_0, ϵ_1 --- A spin-dependent flux factor ratio for the virtual-photons

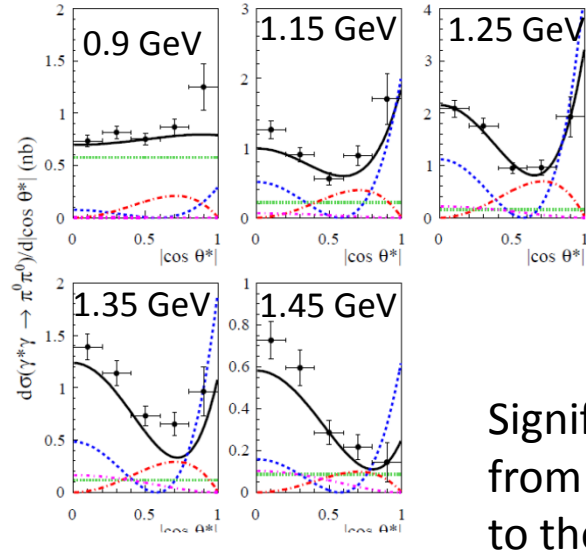


Cross-section results and fit

Consistency check between
electron-tag(●) and positron-tag(○)



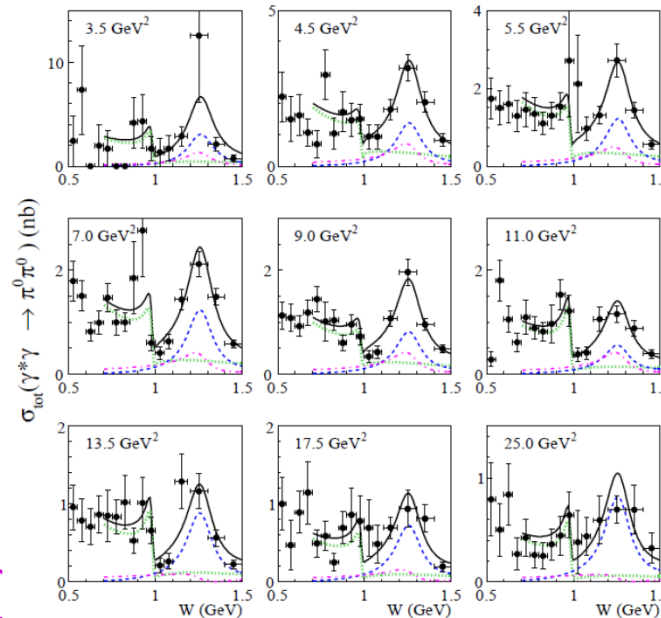
The curves are PWA fit constructed by parameterized resonant ($f_0(980)$ and $f_2(1270)$) and continuum amplitudes.



$|\cos \theta^*|$ dependence
for $Q^2 = 9 \text{ GeV}^2$ and
different W bins

lines: solid= total,
dotted= $|S|^2$, dashed= $|D_0|^2$,
and dash-dotted= $|D_2|^2$

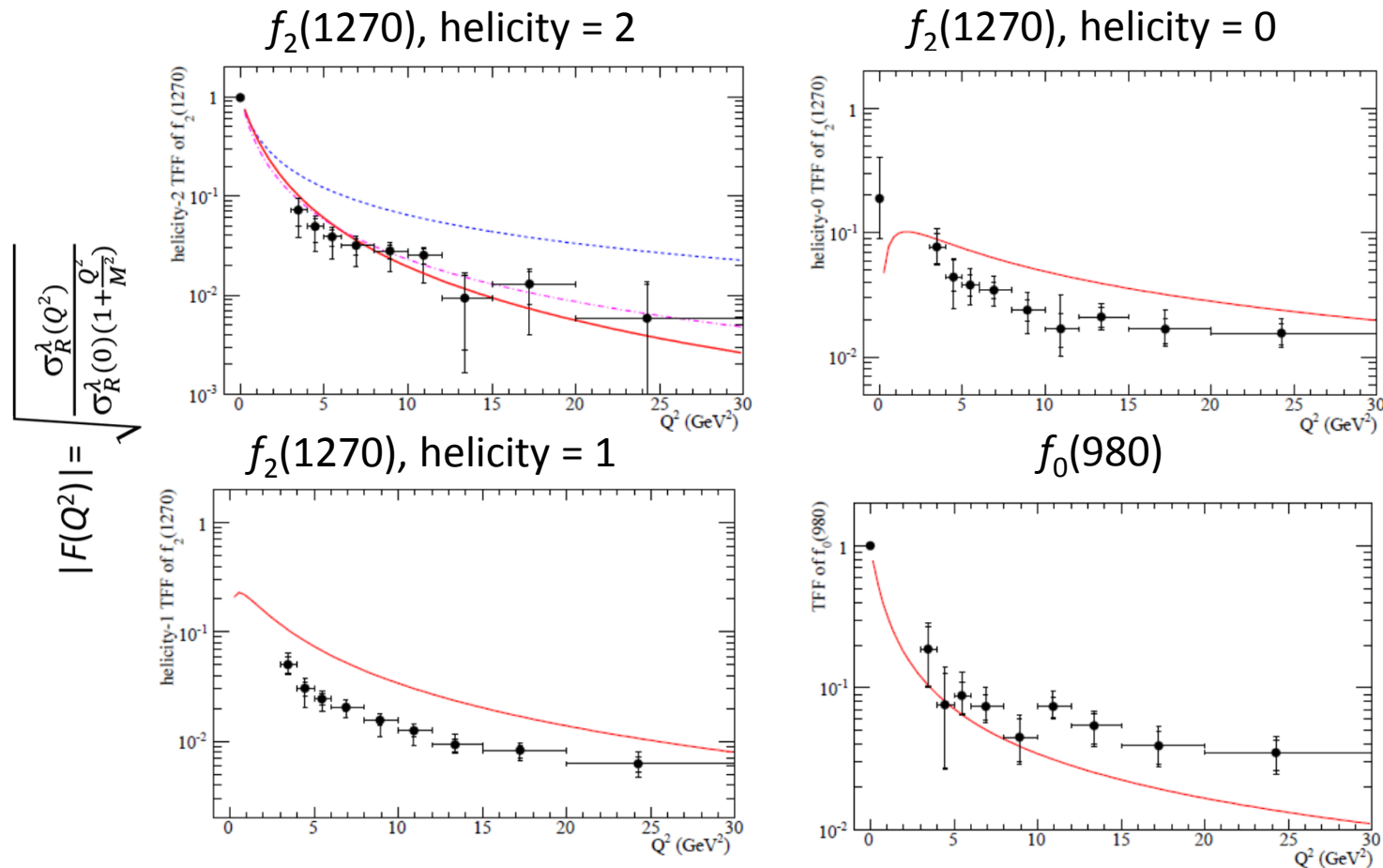
Significant contributions
from hel.=0 and 1 in contrast
to the no-tag ($Q^2=0$) case



Final result of
 $\gamma^*\gamma$ cross sections
and PWA fits



Q² dependence of resonant amplitudes



Theoretical predictions:

- Schuler, Berends, van Gulik, a heavy quark approx. NPB 523, 423 (1998)
- ⋯ Pascalutes, Pauk, Vanderhaeghen, saturated sum rule, PRD 85, 116001 (2012), η 's
- - - ibid., axial-vector mesons



Summary

Highlights of Two-photon physics results from Belle

- Systematic QCD test with many kinds of meson pair channels @ 3 – 4 GeV
- Discovery/observations of new charmonium(like) states $\chi_{c2}(2P)$, X(3915) etc.
- Precise determination of $\Gamma_{\gamma\gamma}$ and BF for the charmonium ground states
- Comprehensive light-meson spectroscopy
 - Observation of scalar states
 - Discrimination of tensor mesons in the couplings to two photons
 - Confirmation of isospin (0 and 1)mixing
- Studies related to glueball, tetraquark, and pentaquark exotic systems
- First measurement of scalar and tensor-meson TFFs

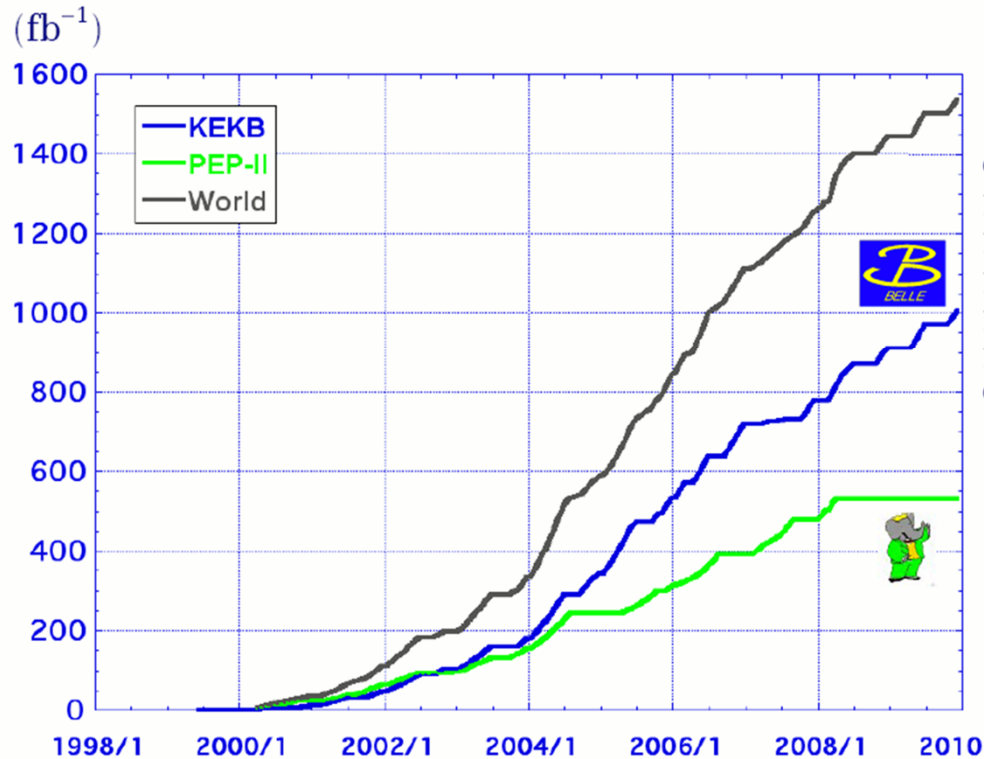


Backup



History of integrated luminosity at Belle

Luminosity at B factories



> 1 ab⁻¹

On resonance:

Y(5S): 121 fb⁻¹

Y(4S): 711 fb⁻¹

Y(3S): 3 fb⁻¹

Y(2S): 24 fb⁻¹

Y(1S): 6 fb⁻¹

Off reson./scan:

~ 100 fb⁻¹

~ 550 fb⁻¹

On resonance:

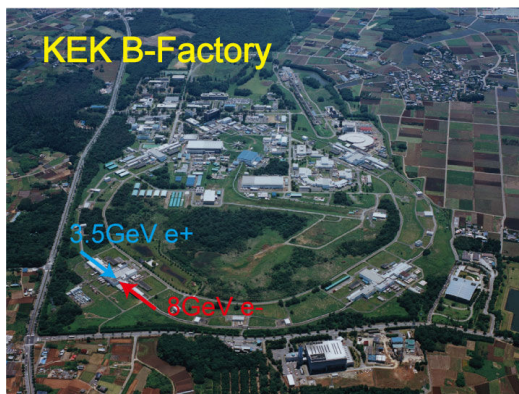
Y(4S): 433 fb⁻¹

Y(3S): 30 fb⁻¹

Y(2S): 14 fb⁻¹

Off resonance:

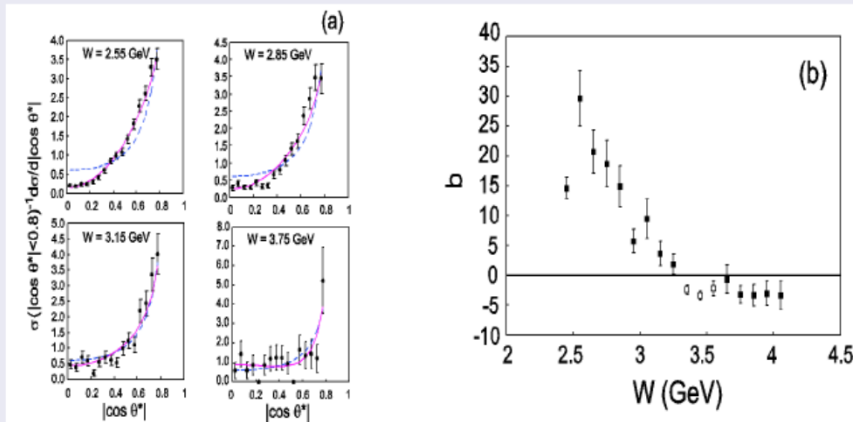
~ 54 fb⁻¹



- 1999 The Belle experiment started
- 2001 CP violation in B mesons was verified and the KEKB accelerator achieved the world's highest luminosity
- 2002 Anomalous CP violation in $b \rightarrow s$ was measured
- 2003 The $B \rightarrow Kll$ decay was discovered
- 2004 The New particle X (3872) was discovered
- 2005 Direct violation of CP in $B \rightarrow K\pi$ was found. The $B \rightarrow \rho\gamma$ decay was discovered
- 2006 $B \rightarrow \tau\nu$ was observed
- 2007 D meson mixing was discovered. A new particle composed of 4 quarks Z (4430) + was discovered
- 2008 Dr. Makoto Kobayashi and Dr. Toshihide Maskawa were awarded the Nobel Prize in Physics
- 2010 The Belle experiment was completed

Angular dependence

$$\gamma\gamma \rightarrow \pi^0\pi^0$$



$d\sigma/d|\cos\theta^*| \propto \sin^{-4}\theta^*$ is predicted by $q\bar{q}$ -meson model and perturbative QCD

- Fit to $\sin^{-4}\theta^* + b \cos\theta^*$
- b becomes constant above 3.2 GeV.

mode	α in $\sin^{-\alpha}\theta^*$	GeV	$ \cos\theta^* $
$K_S K_S$	3 - 8	2.6 - 3.3	< 0.8
$\pi^+ \pi^-$	Good agreement with 4	3.0 - 4.1	< 0.6
$K^+ K^-$	Good agreement with 4	3.0 - 4.1	< 0.6
$\pi^0 \pi^0$	Better agreement with $\sin^{-4}\theta^* + b \cos\theta^*$ Approaches $\sin^{-4}\theta^*$ above 3.1 GeV	2.4 - 4.1 [†]	< 0.8
$\eta\pi^0$	Good agreement with 4 above 2.7 GeV	3.1 - 4.1	< 0.8
$\eta\eta$	Poor agreement with 4 Close to 6 above 3 GeV	2.4 - 3.3	< 0.9

Summarized by H.Nakazawa
Hadron2013

Exclude $\dagger \chi_{c\omega}$ region, 3.3 - 3.6 GeV

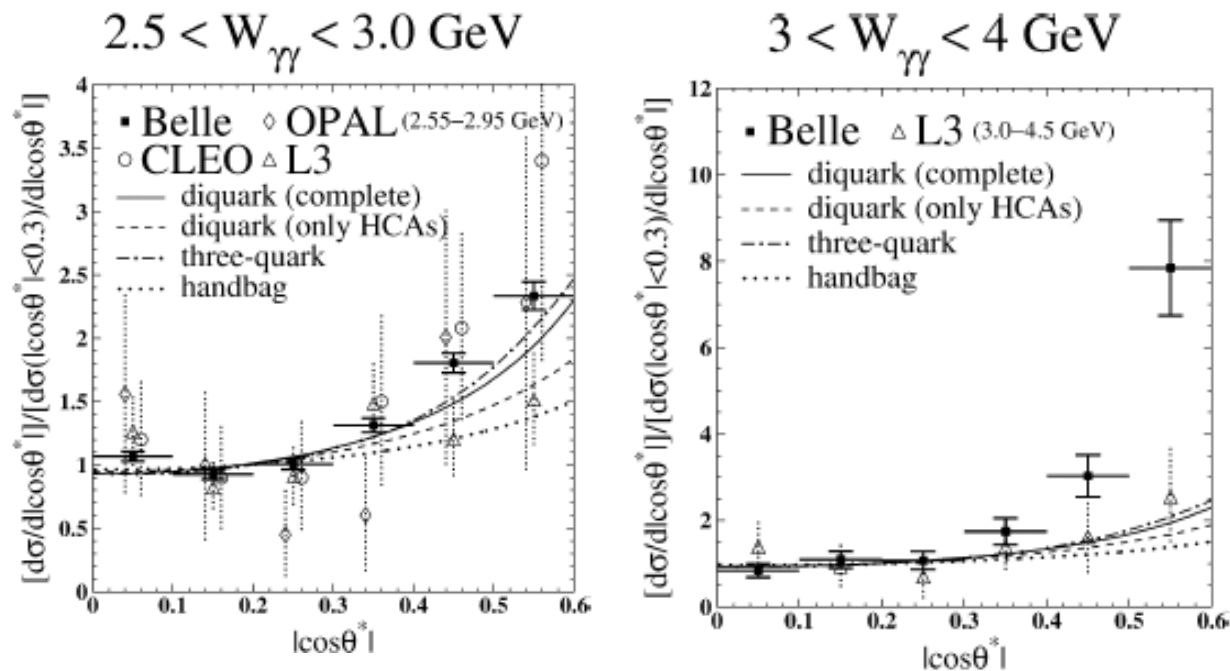
KEK, Jul. 2017

Angular dependence: $\gamma\gamma \rightarrow p\bar{p}$

Baryon production mechanism

Couple with a **single quark?**.. or a **diquark?**

Angular and W dependences, Cross-section size



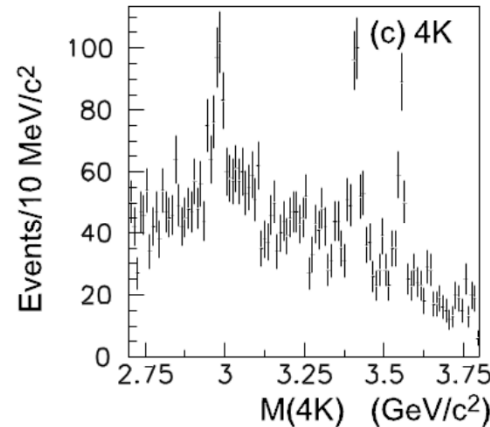
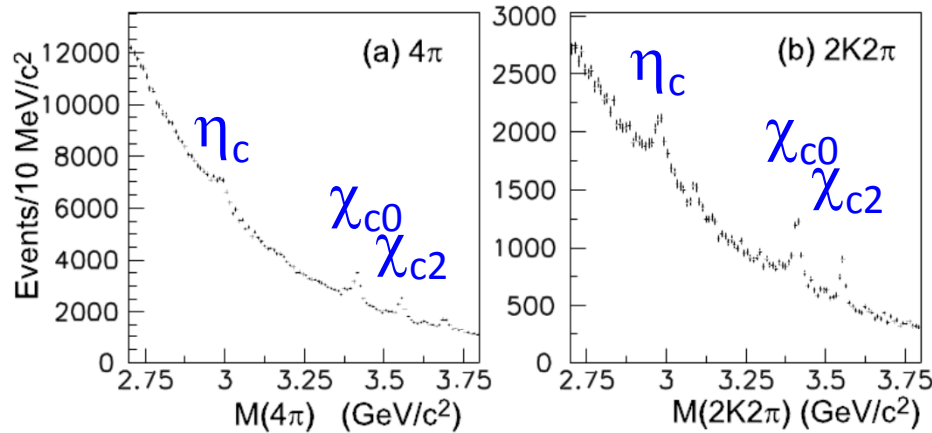
Model predictions are normalized for $|\cos\theta^*| < 0.3$.

Agreement is not very good in $W > 3$ GeV



Three C-even charmonium states

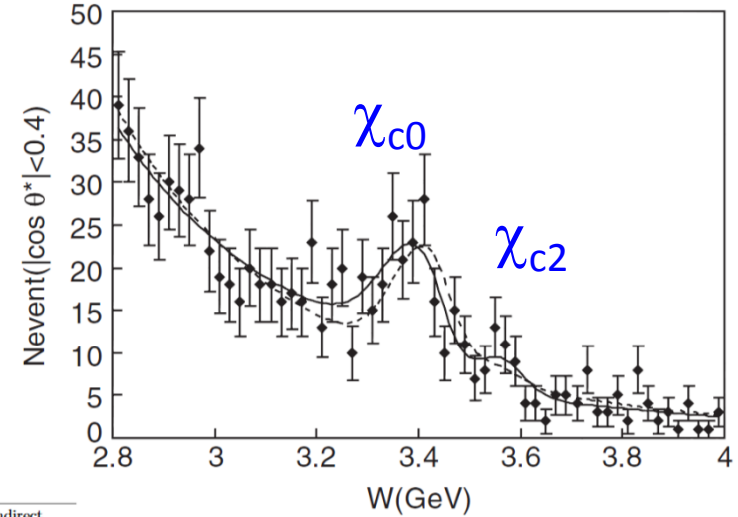
Four-charged-meson final states



EPJ C 53, 1 (2008)

Process	Isospin · BF factor	This paper G (eV)	Direct G (eV)	Indirect G (eV)
$\eta_c \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	1.0	$40.7 \pm 3.7 \pm 5.3$	$180 \pm 70 \pm 20$	83 ± 24
$\eta_c \rightarrow K^+ K^- \pi^+ \pi^-$	1.0	$25.7 \pm 3.2 \pm 4.9$	210 ± 70	102 ± 30
$\eta_c \rightarrow K^+ K^- K^+ K^-$	1.0	$5.6 \pm 1.1 \pm 1.6$	280 ± 70	11 ± 5
$\eta_c \rightarrow \rho\rho$	0.333	< 39	—	130 ± 43
$\eta_c \rightarrow f_2 f_2$	0.320	$69 \pm 17 \pm 12$	—	74 ± 36
$\eta_c \rightarrow K^* K^*$	0.333	$32.4 \pm 4.2 \pm 5.8$	—	66 ± 22
$\eta_c \rightarrow f_2 f_2'$	0.251	$49 \pm 9 \pm 13$	—	—
$\eta_c \rightarrow \phi\phi$	0.243	$6.8 \pm 1.2 \pm 1.3$	—	19 ± 5
$\chi_{c0} \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	1.0	$44.7 \pm 3.6 \pm 4.9$	$75 \pm 13 \pm 8$	69 ± 13
$\chi_{c0} \rightarrow K^+ K^- \pi^+ \pi^-$	1.0	$38.8 \pm 3.7 \pm 4.7$	—	53 ± 12
$\chi_{c0} \rightarrow K^+ K^- K^+ K^-$	1.0	$7.9 \pm 1.3 \pm 1.1$	—	7.8 ± 1.6
$\chi_{c0} \rightarrow K^{*0} K^- \pi^+ \text{ or c.c.}$	0.667	$16.7 \pm 6.1 \pm 3.0$	—	34 ± 13
$\chi_{c0} \rightarrow \rho\rho$	0.333	< 12	—	—
$\chi_{c0} \rightarrow K^* K^*$	0.333	< 18	—	5.1 ± 1.9
$\chi_{c0} \rightarrow \phi\phi$	0.243	$2.3 \pm 0.9 \pm 0.4$	—	2.7 ± 0.8
$\chi_{c2} \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	1.0	$5.01 \pm 0.44 \pm 0.55$	$6.4 \pm 1.8 \pm 0.8$	7.2 ± 1.2
$\chi_{c2} \rightarrow K^+ K^- \pi^+ \pi^-$	1.0	$4.42 \pm 0.42 \pm 0.53$	—	5.8 ± 2.1
$\chi_{c2} \rightarrow K^+ K^- K^+ K^-$	1.0	$1.10 \pm 0.21 \pm 0.15$	—	1.03 ± 0.18
$\chi_{c2} \rightarrow \rho^0 \pi^+ \pi^-$	1.0	$3.2 \pm 1.9 \pm 0.5$	—	3.9 ± 2.3
$\chi_{c2} \rightarrow \rho\rho$	0.333	< 7.8	—	—
$\chi_{c2} \rightarrow K^* K^*$	0.333	$2.4 \pm 0.5 \pm 0.8$	—	2.2 ± 0.5
$\chi_{c2} \rightarrow \phi\phi$	0.243	$0.58 \pm 0.18 \pm 0.16$	—	1.0 ± 0.3
$\eta_c(2S) \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	1.0	< 6.5	—	—
$\eta_c(2S) \rightarrow K^+ K^- \pi^+ \pi^-$	1.0	< 5.0	—	—
$\eta_c(2S) \rightarrow K^+ K^- K^+ K^-$	1.0	< 2.9	—	—

$\pi^0 \pi^0$ final state



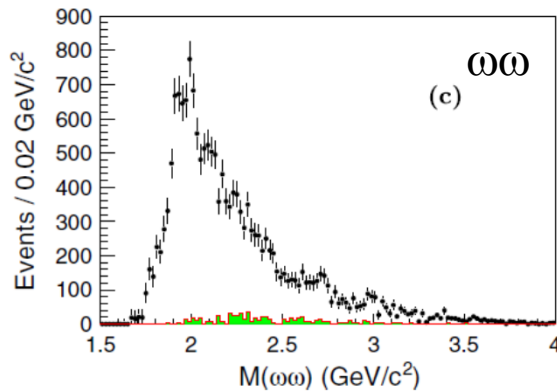
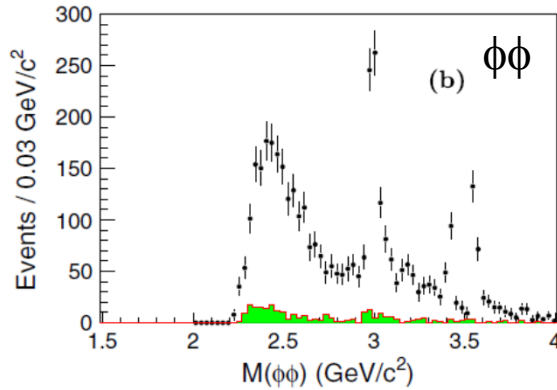
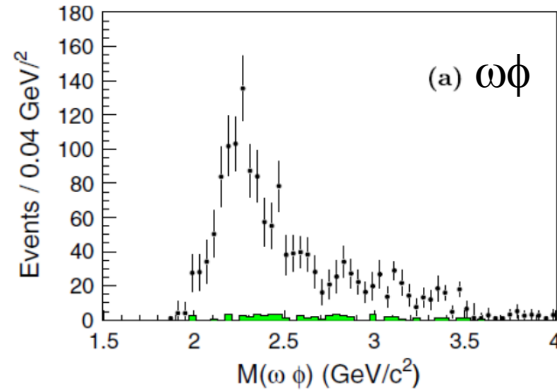
Interference	$N_{\chi_{c0}}$	k	ϕ	$N_{\chi_{c2}}$
Without	100 ± 16	13^{+11}_{-10}
With	103^{+60}_{-42}	$0.82^{+0.18}_{-0.48}$	$(1.1 \pm 0.3)\pi$	34 ± 13

Interference	$\Gamma_{\gamma\gamma} \mathcal{B}(\chi_{c0})$ (eV)	$\Gamma_{\gamma\gamma} \mathcal{B}(\chi_{c2})$ (eV)
Without	$9.7 \pm 1.5 \pm 1.2$	$0.18^{+0.15}_{-0.14} \pm 0.08$
With	$9.9^{+5.8}_{-4.0} \pm 1.6$	$0.48 \pm 0.18 \pm 0.07 \pm 0.14$



Decays to Vector-meson pair

PRL 108, 232001 (2012)



$\Gamma_{\gamma\gamma} \mathcal{B}(X \rightarrow VV)$ (eV) and the numbers of events (in brackets) for η_c , χ_{c0} and χ_{c2}

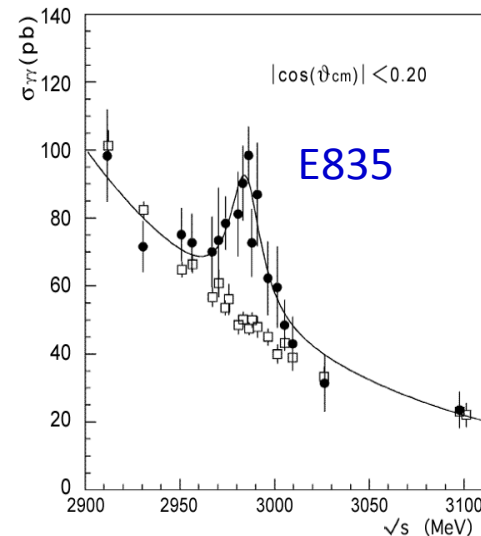
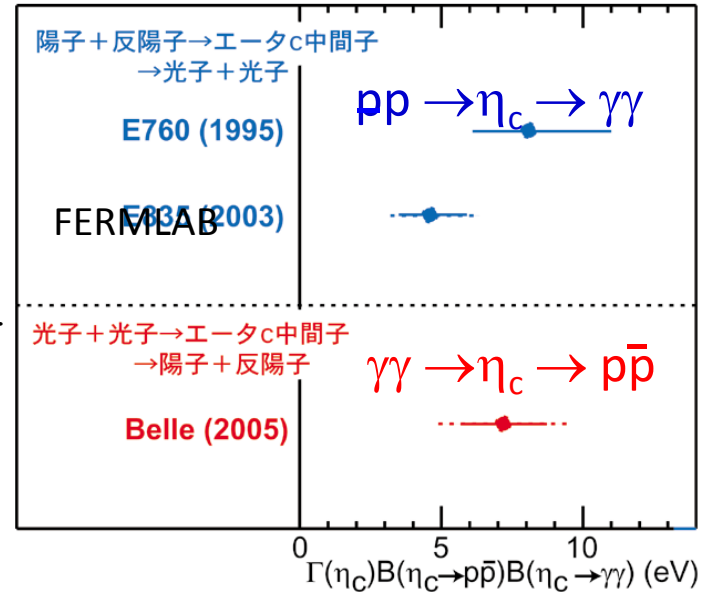
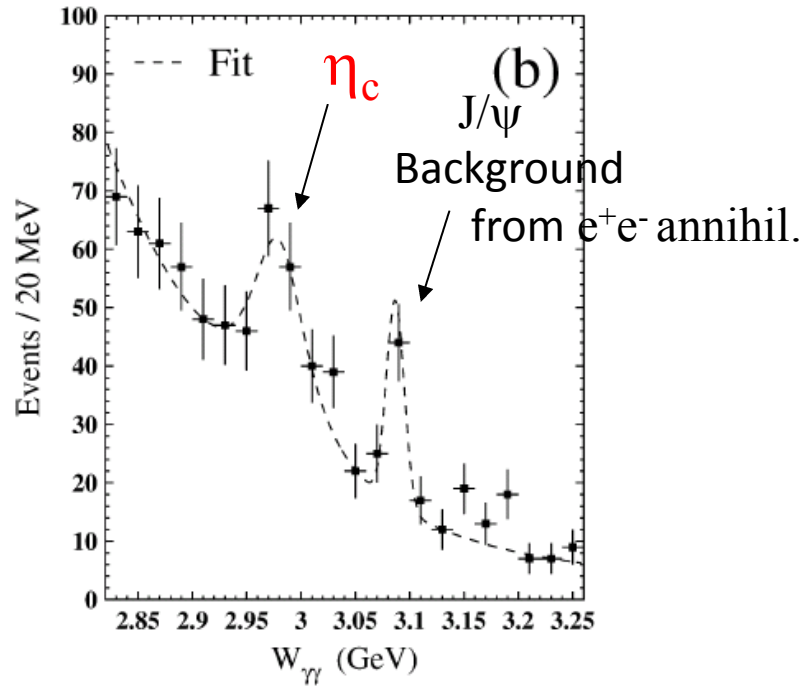
Mode	$\omega\phi$	$\phi\phi$
η_c	<0.49 [< 7.9]	$7.75 \pm 0.66 \pm 0.62$ [386 \pm 31]
χ_{c0}	<0.34 [< 4.3]	$1.72 \pm 0.33 \pm 0.14$ [56 \pm 11]
χ_{c2}	<0.04 [< 2.4]	$0.62 \pm 0.07 \pm 0.05$ [89 \pm 11]

$\omega\omega$
$8.67 \pm 2.86 \pm 0.96$ [85 \pm 29]
<3.9 [< 35]
<0.64 [< 28]



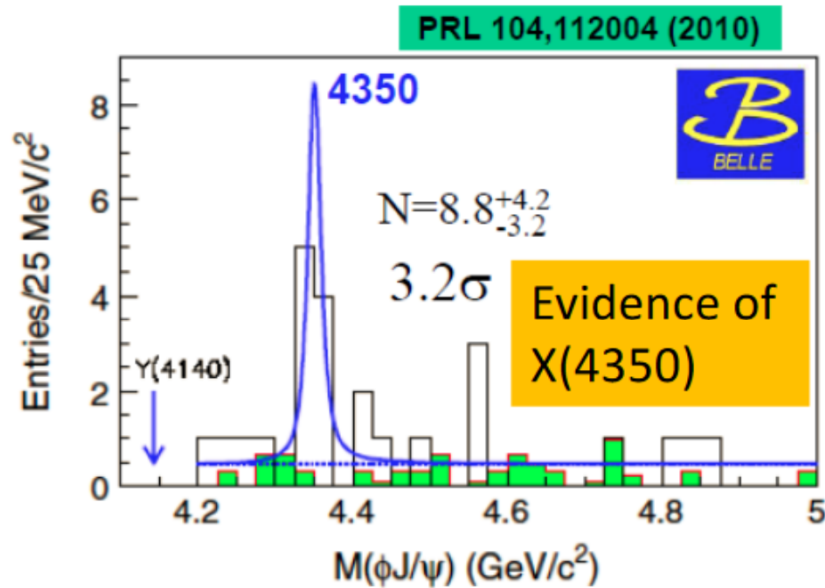
Baryon pair: $\gamma\gamma \rightarrow p\bar{p}$

PLB 621, 41 (2005)

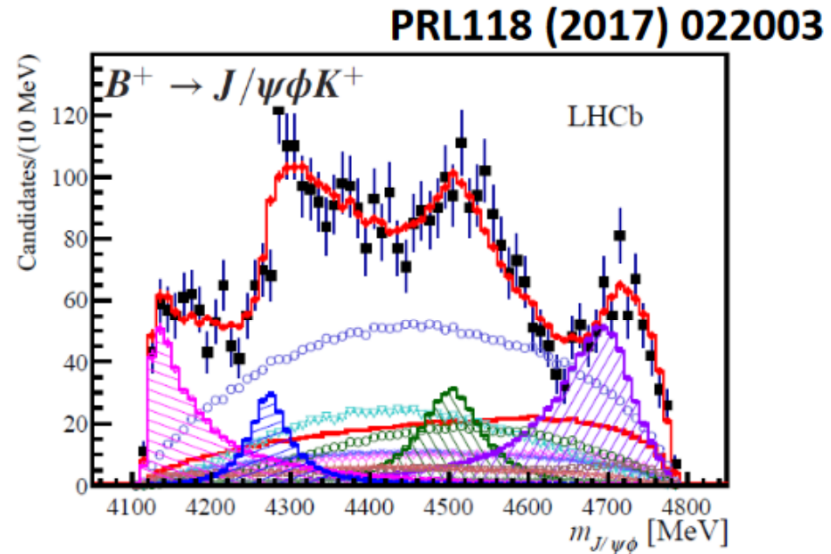


Evidence of $X(4350)$ in $\phi J/\psi$

Two-photon



B decays



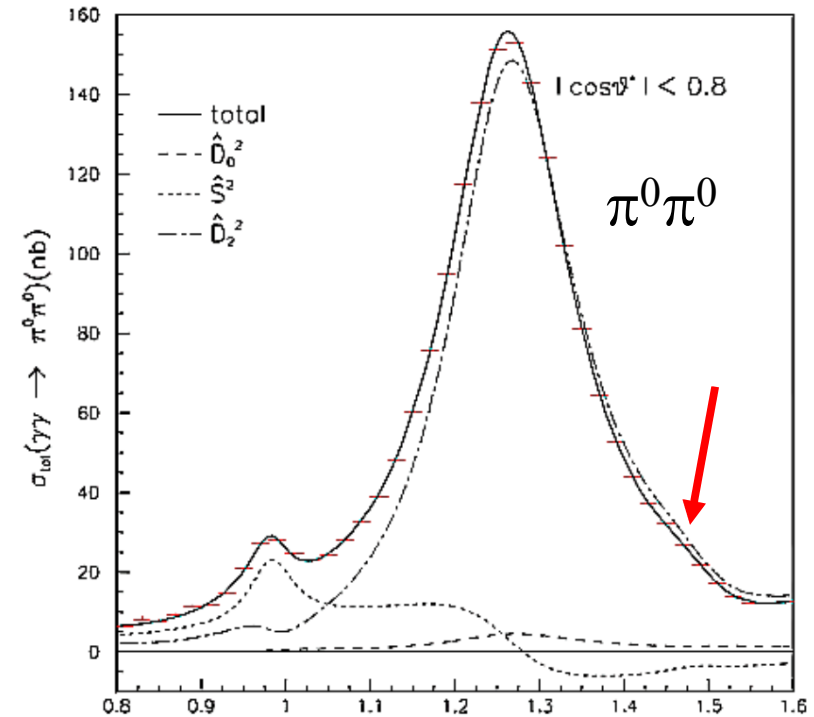
X(4140), X(4274), X(4500), and X(4700)



Scalars in the 1.2 – 1.6 GeV region

- Hadron experiments report a wide $f_0(1370)$ and a narrow $f_0(1500)$.
- Some of previous two-photon measurements provide a hint of $f_0(1100-1400) \rightarrow \pi\pi$ under the huge peak of $f_2(1270)$
- Belle's $\pi^0\pi^0$ measurement reports $f_0(1470)$.
May be visible in the line shape.
 → favorable to the narrow $f_0(1500)$,
 but also consistent with $f_0(1370)$.

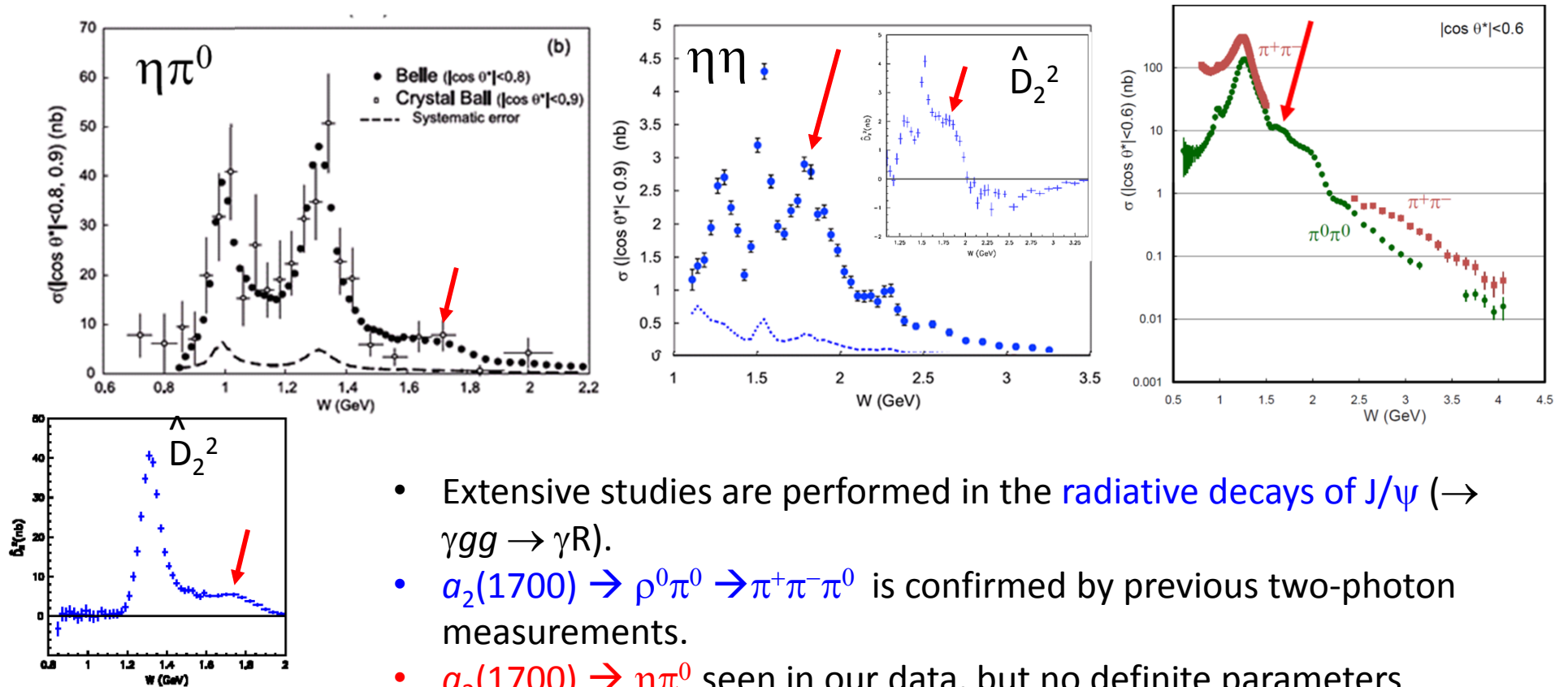
$f_0(1370)$ [i]	$I^G(J^{PC}) = 0^+(0^{++})$		
Mass $m = 1200$ to 1500 MeV Full width $\Gamma = 200$ to 500 MeV			
$f_0(1370)$ DECAY MODES	Fraction (Γ_i/Γ)	p (MeV/c)	
$\pi\pi$	seen	672	
$f_0(1500)$ [n]	$I^G(J^{PC}) = 0^+(0^{++})$		
Mass $m = 1505 \pm 6$ MeV ($S = 1.3$) Full width $\Gamma = 109 \pm 7$ MeV			
$f_0(1500)$ DECAY MODES	Fraction (Γ_i/Γ)	Scale factor	p (MeV/c)
$\pi\pi$	$(34.9 \pm 2.3) \%$	1.2	741



Parameter	Belle ($\pi^0\pi^0$)	Crystal Ball	Unit
Mass	1470^{+6+72}_{-7-255}	1250	MeV/c ²
Γ_{tot}	90^{+2+50}_{-1-22}	268 ± 70	MeV
$\Gamma_{\gamma\gamma} \mathcal{B}(\pi^0\pi^0)$	11^{+4+603}_{-2-7}	430 ± 80	eV



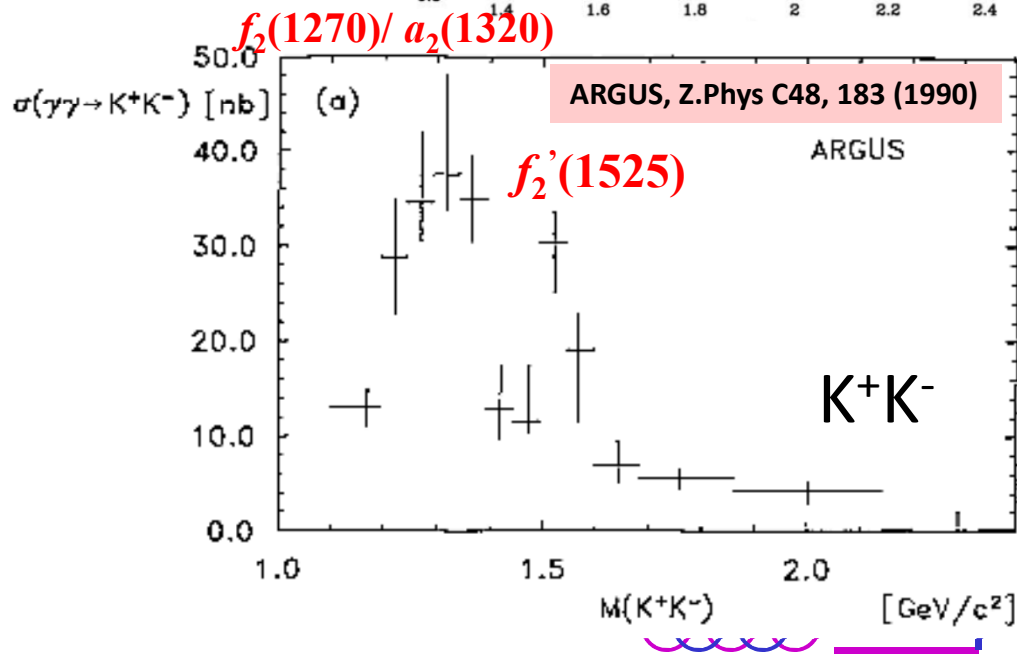
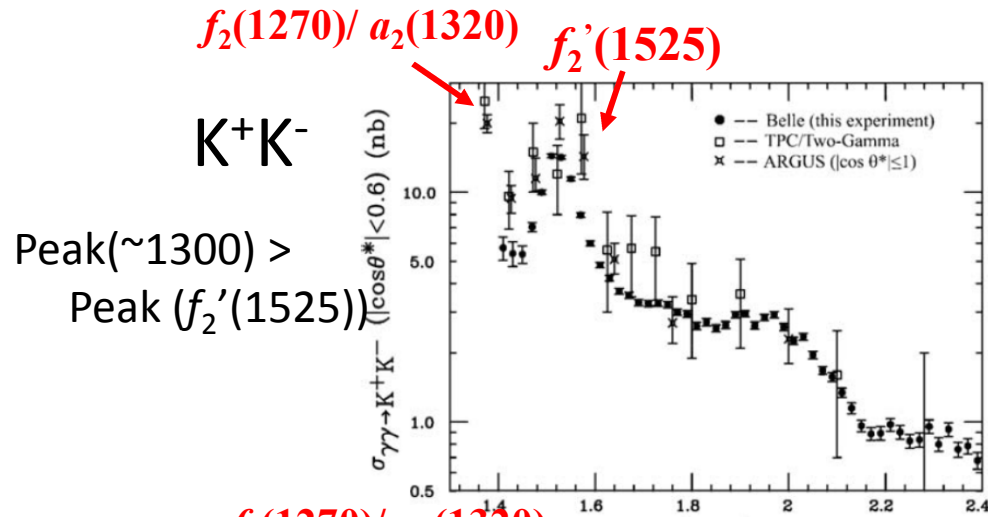
1.6 – 1.8 GeV: Mass region of the greatest difficulty



- Extensive studies are performed in the radiative decays of J/ψ ($\rightarrow \gamma g g \rightarrow \gamma R$).
- $a_2(1700) \rightarrow \rho^0\pi^0 \rightarrow \pi^+\pi^-\pi^0$ is confirmed by previous two-photon measurements.
- $a_2(1700) \rightarrow \eta\pi^0$ seen in our data, but no definite parameters obtained.
- $f_2(1810) \rightarrow \eta\eta$ is confirmed in two-photon process.
- An unidentified structure around ~ 1.6 GeV is seen in $\pi^0\pi^0$. But, its correspondence to a single resonance of the mass is not sure.



$f_2(1270)$ - $a_2(1320)$ interference in $K\bar{K}$



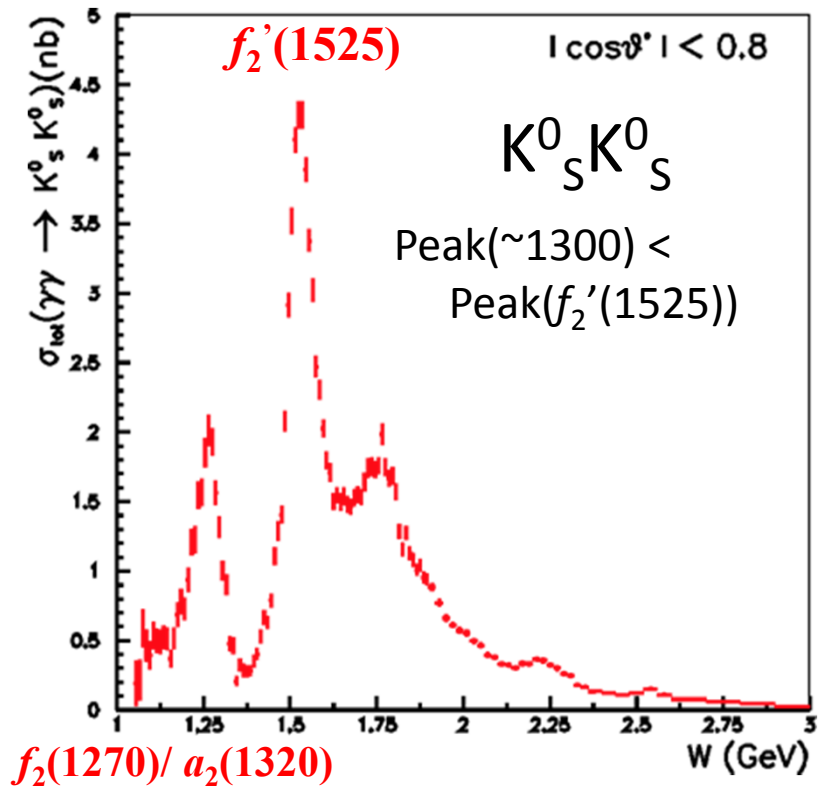
Constructive interference

$f_2(1270)+a_2(1320)$ in K^+K^-

Destructive interference

$f_2(1270)-a_2(1320)$ in $K_S^0 K_S^0$

Explained by a phase relation in isospin composition



The 2.2 – 2.6 GeV region

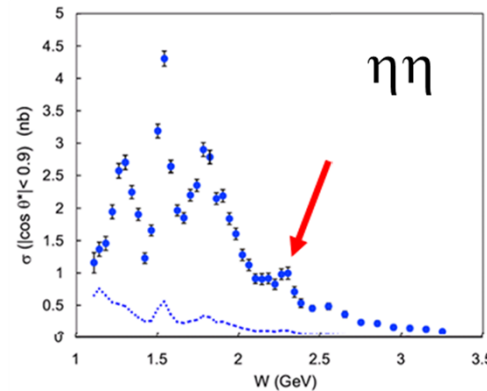
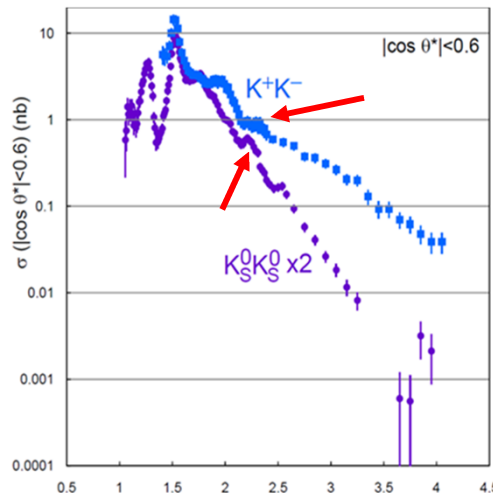
- The **very narrow $f_J(2220)$** (was $\xi(2220)$) and **a wide $f_2(2300)$** are suggested.

Do the both exist? Really narrow?

- Our $\pi^0\pi^0$ result does not need $f(\sim 2300)$; the high mass $f_2(1950)$ can explain the observed line shape.

- Surely something narrow(?) peaks are found in K^+K^- , $K_S^0K_S^0$ and $\eta\eta$.

An $\bar{s}s$ state or a glueball flavor insensible?



$f_J(2220)$		$I^G(J^{PC}) = 0^+(2^{++} \text{ or } 4^{++})$			
OMITTED FROM SUMMARY TABLE Needs confirmation. See our mini-review in the 2004 edition of this Review, PDG 04.					
$f_J(2220)$ MASS					
VALUE (MeV)	EVTs	DOCUMENT ID	TECN	COMMENT	
2231.1 ± 3.5	OUR AVERAGE				
$f_J(2220)$ WIDTH					
VALUE (MeV)	CL%	EVTs	DOCUMENT ID	TECN	COMMENT
23_{-7}^{+8}		8			OUR AVERAGE
$f_J(2220)$ DECAY MODES					
Mode	Fraction (Γ_i/Γ)				
Γ_1 $\pi\pi$	seen				
Γ_2 $\pi^+\pi^-$	seen				
Γ_3 $K\bar{K}$	seen				
Γ_4 $p\bar{p}$					
Γ_5 $\gamma\gamma$	not seen				
Γ_6 $\eta\eta'(958)$	seen				
Γ_7 $\phi\phi$	not seen				
Γ_8 $\eta\eta$	not seen				

$f_2(2300)$		$I^G(J^{PC}) = 0^+(2^{++})$	
Mass $m = 2297 \pm 28$ MeV			
Full width $\Gamma = 149 \pm 40$ MeV			
$f_2(2300)$ DECAY MODES	Fraction (Γ_i/Γ)	p (MeV/c)	
$\phi\phi$	seen	529	
$K\bar{K}$	seen	1037	
$\gamma\gamma$	seen	1149	

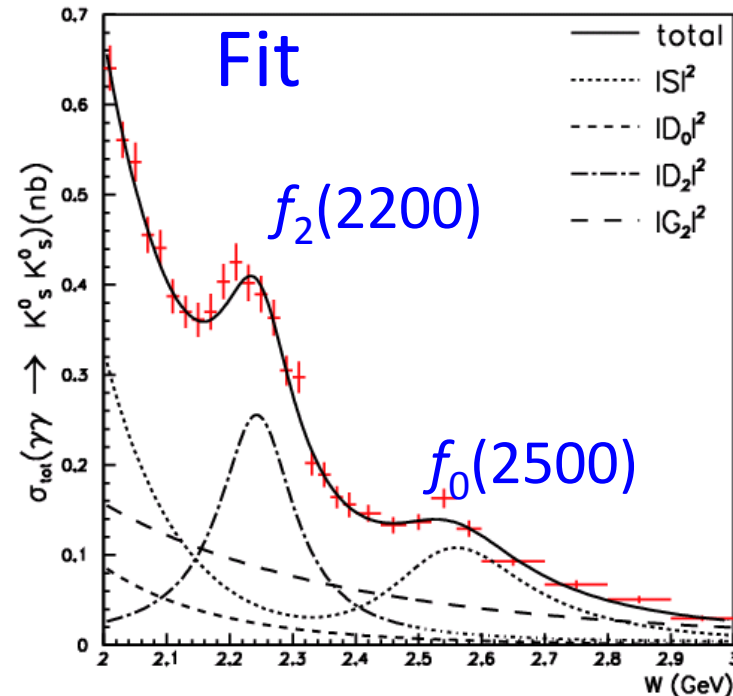
Fit Results for resonances in $K^0_S K^0_S$

$f_2(2200)-f_0(2500)$ is the best solution (in all the J= 0, 2, 4 combinations)

Parameter	$f_2(2200)$	$f_0(2500)$
Mass (MeV/ c^2)	2243^{+7+3}_{-6-29}	$2539 \pm 14^{+38}_{-14}$
Γ_{tot} (MeV)	$145 \pm 12^{+27}_{-34}$	$274^{+77+126}_{-61-163}$
$\Gamma_{\gamma\gamma} \mathcal{B}(K\bar{K})$ (eV)	$3.2^{+0.5+1.3}_{-0.4-2.2}$	40^{+9+17}_{-7-40}

Significances

- 3.4σ for $f_2(2200)$ over $f_0(2200)$
- 4.3σ for $f_0(2500)$ over $f_2(2500)$



- There can be an only wide state around 2240 MeV.
- Narrow appearances in previous measurements may be due to an interference effect and/or statistical fluctuation.
- A high-mass state at 2.5 GeV may be the heaviest light-quark scalar meson so far found.



$\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$

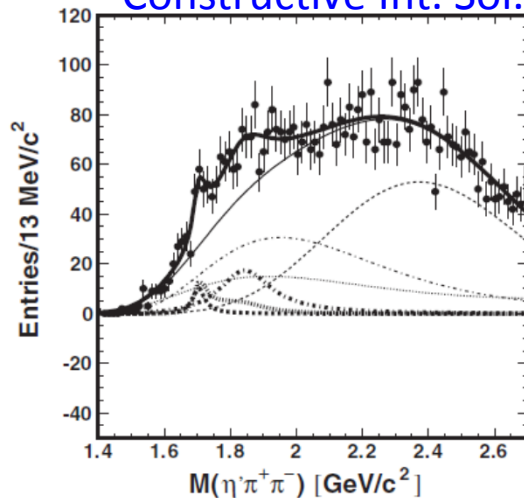
Production of light-quark mesons decaying to the **three pseudoscalar meson final state**. (The η_c production is also presented.)

Belle, PRD 86, 052002 (2012)

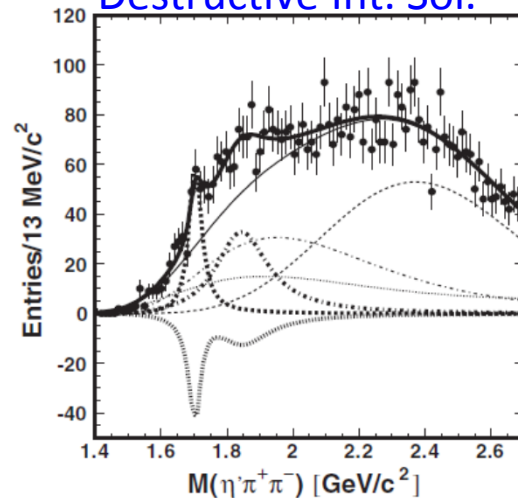
X(1835) is an exotic resonance candidate found in the radiative decay of J/ψ by BES. Is it gluon-rich, or $q\bar{q}$ -rich?

A hint of X(1835) – 2.8σ ,
but it is not very significant.

$\eta(1760) + X(1835) + \text{Non-Res} + \text{Backgrounds}$
Constructive Int. Sol.



Destructive Int. Sol.

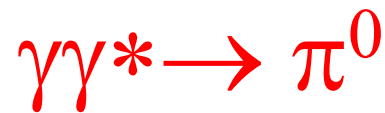


Parameter	Two interfering resonances		Reference
	Solution I	Solution II	
	X(1835)		
$M, \text{ MeV}/c^2$	1836.5 (fixed)		$1836.5 \pm 3.0^{+5.6}_{-2.1}$
$\Gamma, \text{ MeV}/c^2$	190 (fixed)		$190 \pm 9^{+38}_{-36}$
$\Gamma_{\gamma\gamma} \mathcal{B}, \text{ eV}/c^2$	$18.2^{+7.7}_{-6.7} \pm 4.0$	$35^{+12}_{-13} \pm 8$	
$(\Gamma_{\gamma\gamma} \mathcal{B})_{90} \text{ eV},$	<35.6	<83	
S, σ	2.8		
	$\eta(1760)$		
$M, \text{ MeV}/c^2$	$1703^{+12}_{-11} \pm 1.8$		1756 ± 9
$\Gamma, \text{ MeV}/c^2$	$42^{+36}_{-22} \pm 15$		96 ± 70
$\Gamma_{\gamma\gamma} \mathcal{B}, \text{ eV}/c^2$	$3.0^{+2.0}_{-1.2} \pm 0.8$	$18^{+13}_{-10} \pm 5$	
S, σ	4.1		
ϕ	$(287^{+42}_{-51})^\circ$	$(139^{+19}_{-9})^\circ$	

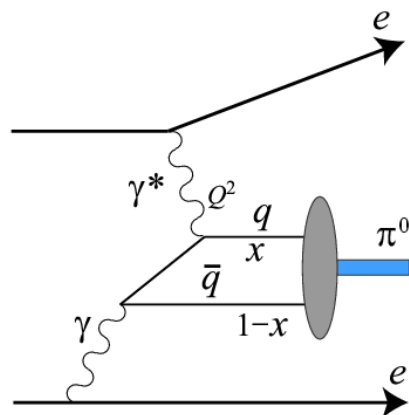


π^0 Transition Form Factor (TFF)

PRD 86, 092007 (2012)



Coupling of neutral pion with two photons
Good test for QCD at high Q^2



Single-tag π^0 production in two-photon process with a large- Q^2 and a small- Q^2 photon

Theoretically calculated from pion distribution amplitude and decay constant

$$F(Q^2) = \frac{\sqrt{2}f_\pi}{3} \int T_H(x, Q^2, \mu) \phi_\pi(x, \mu) dx$$

BaBar has reported a significant deviation from the expectation.

Measurement:

$$|F(Q^2)|^2 = |F(Q^2, 0)|^2 = (d\sigma/dQ^2) / (2A(Q^2)) \quad A(Q^2) \text{ is calculated by QED}$$

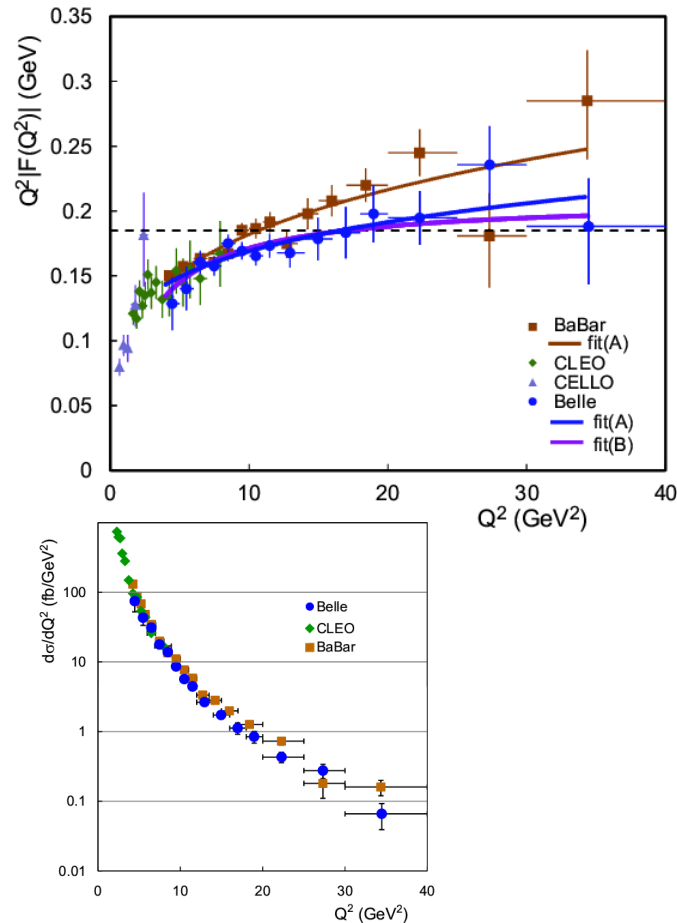
$$|F(0, 0)|^2 = 64\pi\Gamma_{\gamma\gamma} / \{(4\pi\alpha)^2 m_R^3\}$$

Detects e (tag side) and π^0

$Q^2 = 2EE'(1 - \cos \theta)$ from energy and polar angle of the tagged electron



Comparisons with Previous Measurements and Fits



No rapid growth above $Q^2 > 9 \text{ GeV}^2$ is seen in Belle result.

$\sim 2.3\sigma$ difference between Belle and BaBar in $9 - 20 \text{ GeV}^2$

Fit A (suggested by BaBar)

$$Q^2|F(Q^2)| = A (Q^2/10\text{GeV}^2)^\beta$$

BaBar: —

$$A = 0.182 \pm 0.002 (\pm 0.004) \text{ GeV}$$

$$\beta = 0.25 \pm 0.02$$

BaBar, PRD 80, 052002 (2009)

Belle: —

$$A = 0.169 \pm 0.006 \text{ GeV}$$

$$\beta = 0.18 \pm 0.05$$

$$\chi^2/\text{ndf} = 6.90/13 \quad \sim 1.5\sigma \text{ difference from BaBar}$$

Fit B (with an asymptotic parameter)

$$Q^2|F(Q^2)| = BQ^2/(Q^2+C)$$

Belle: —

$$B = 0.209 \pm 0.016 \text{ GeV}$$

$$C = 2.2 \pm 0.8 \text{ GeV}^2$$

$$\chi^2/\text{ndf} = 7.07/13$$

B is consistent with the QCD value (0.185 GeV)



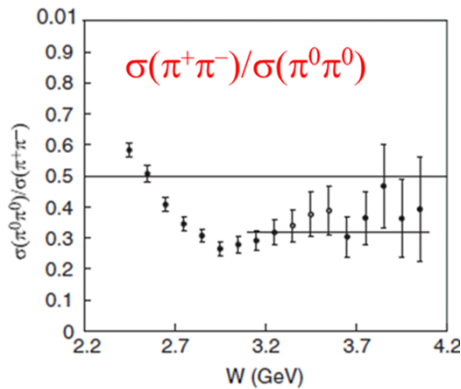
Physics at Belle II, SuperKEKB



Physics of High W

- W-dependence of hadron-pair production $\sigma \propto W^{-n}$

Predictions: $n = 6$ (charged mesons), $n=10$ (neutral mesons) $n=10$ (proton)



W is still not high enough?

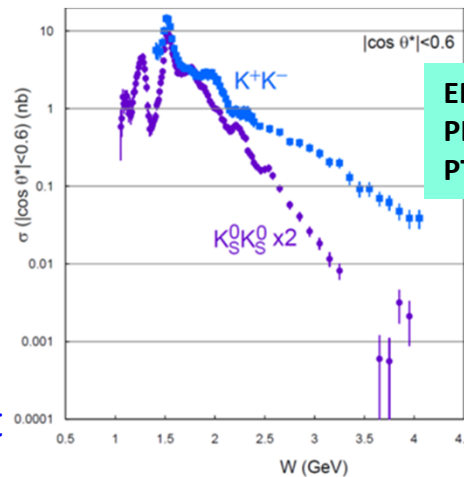
Final-state interaction important for $\pi\pi$ even in high W?

Baryon-pair production processes are statistically limited (because of large n)

Proton pair, Hyperon (Λ , Σ) pair, Δ pair

$\sigma(\Lambda\Lambda)/\sigma(pp) \sim 1$ at high W?

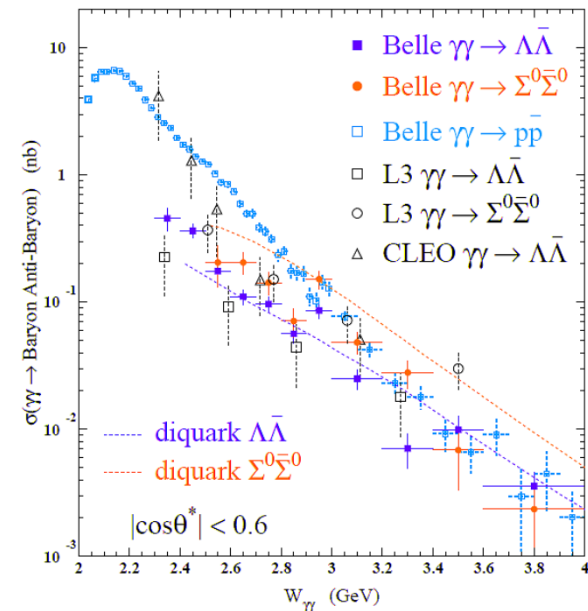
at W High Enough. (We don't know where is "high enough".)



EPJC 32, 323 (2003)
PLB 615, 39 (2005)
PTEP 2013, 123C01 (2013)

$\bar{K}\bar{K}$ is different and agrees with prediction

PLB 621, 41 (2005)
hep-ex/0609048 (Unpublished)



Analysis of $D\bar{D}$ at around 3.80 GeV

Search for $\chi_{c0}(2P) \rightarrow D^0\bar{D}^0 / D^+D^-$

The target is enhancements around 3.80 – 3.85 GeV?

Possible backgrounds:

A difference between charged pair and neutral pair seems to indicate the contribution of $D^*\bar{D}$ which has a charge (isospin) asymmetry in D^* decay

$\chi_{c2}(2P) \rightarrow D^*\bar{D}$, then $M(D\bar{D}) \sim 3.80$ GeV

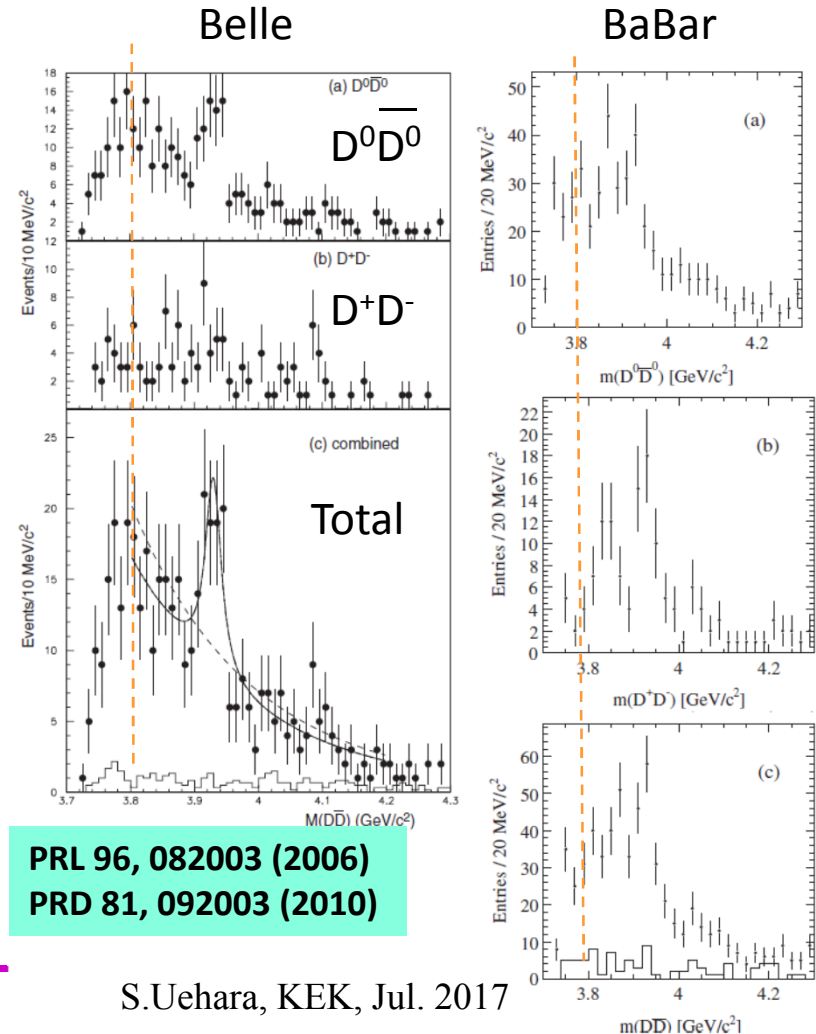
Backgrounds systematically to be solved

$$\chi_{c2}(2P) \rightarrow D^{*0}\bar{D}^0 \rightarrow D^0\bar{D}^0(\pi^0/\gamma)$$

$$\chi_{c2}(2P) \rightarrow D^{*+}D^- \rightarrow D^+D^-(\pi^0)$$

$$\chi_{c2}(2P) \rightarrow D^{*+}D^- \rightarrow D^0D^-(\pi^+)$$

A small P_t -unbalance for $D\bar{D}$ is also important information as a sign of the extra π/γ .



Single-tag TFF's for π^0 , K_S^0 , K_S^0 , etc.

Stat. error estimation for π^0 -TFF measurement in the high Q^2 region

Assumptions:

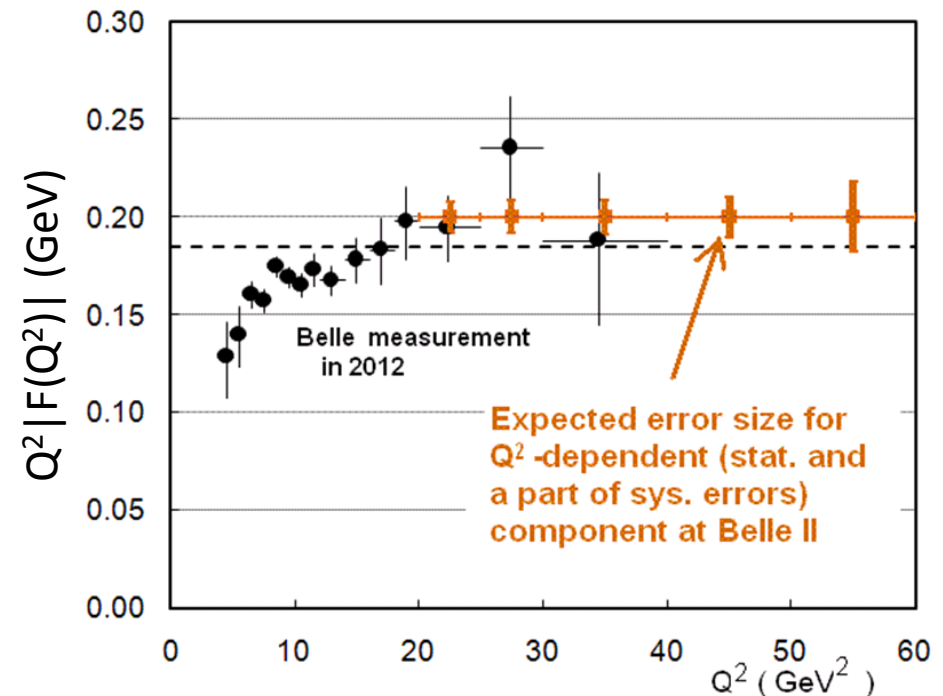
- Integrated luminosity 50 ab^{-1} (x 66)
- No large Bhabha-Veto inefficiency (x 2.5 @ high Q^2)
- Systematic errors from π^0 -fit and trigger can be reduced
- Other systematics stay the same

$Q^2 > 60 \text{ GeV}^2$

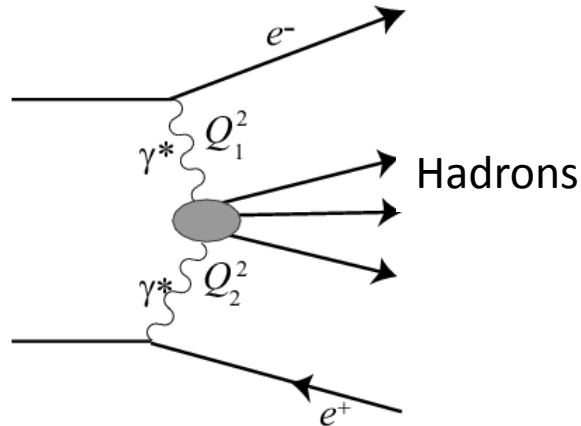
Close to back-to-back topology
of $e\pi^0$ in e^+e^- c.m. frame

Huge background from Bhabha

$K_S^0 K_S^0$ about 200 events to be observed for Belle.
More than 10,000 events expected for Belle II.

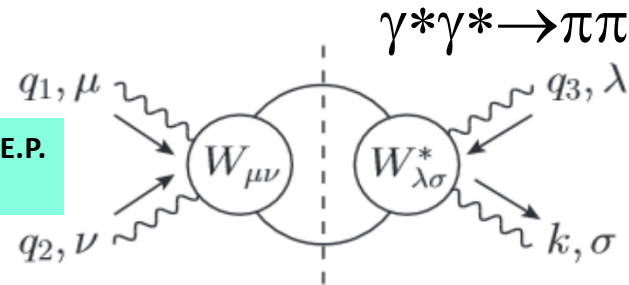


Double-tag processes



Hadronic Light-by-Light (hLbL) contribution is important for muon g-2 theoretical cal.

G.Colangelo et al., J.H.E.P. 1409, 091 (2014)



At the present, the error from the hLbL contribution is the same order of that of the experiment of muon g-2. In near future, an improvement is needed.

Test of QCD

M.Diehl et al., EPJ C22, 439 (2001)

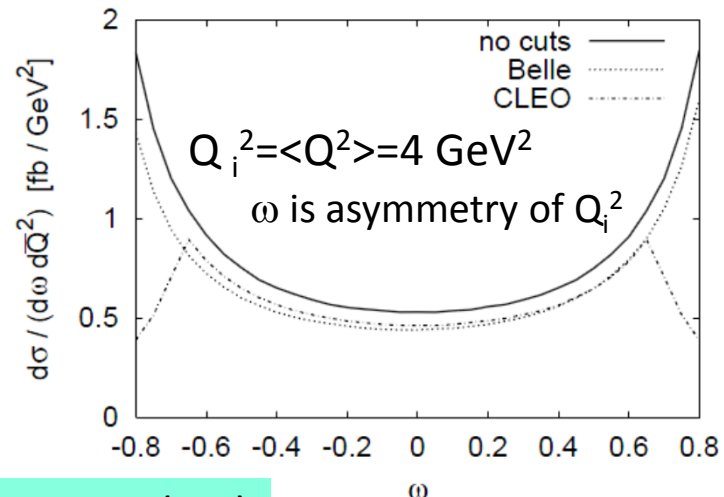
$$\gamma^* \gamma^* \rightarrow \pi^0$$

$$Q_1^2 \sim Q_2^2$$

Dependence on Distribution Amplitude is small

The ee-based cross section $\sim O(0.1\text{fb})$

Feasible at Belle II



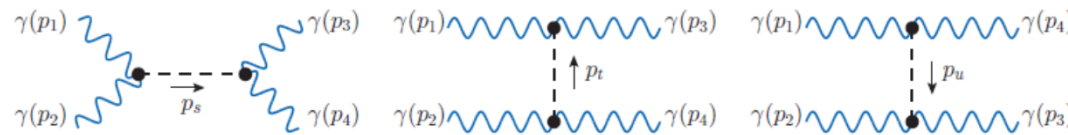
M. Diehl, et al., Eur. Phys. J. C 22, 439 (2001)

S. Ohnara, KEK, Jul. 2017

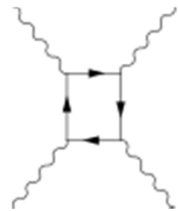
The elastic scattering

- $\gamma\gamma \rightarrow \gamma\gamma$ So far, it is observed only at the peaks of π^0 , η and η' .
- Interference with lepton's and quark's box diagrams may be seen near η_c peak. $\text{BF}(\eta_c \rightarrow \gamma\gamma) = 1.5 \times 10^{-4}$ is known.
- At an e^+e^- collider, the Double-Radiation Bhabha process is also unseparated and interfering background.

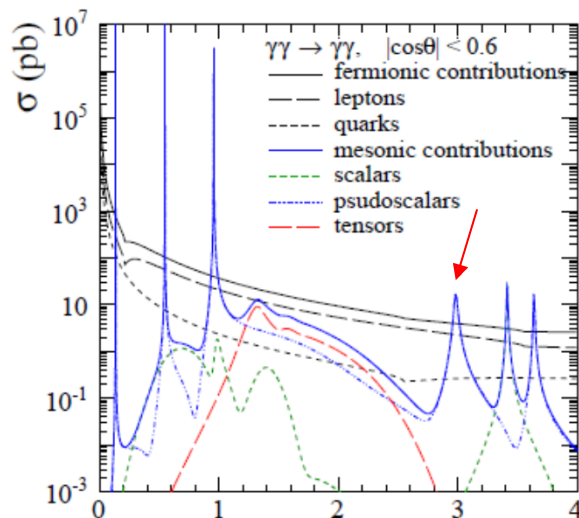
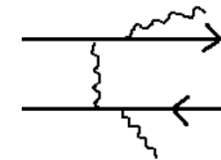
Resonant (s,t,u):



Non-resonant:



Double radiation:



We will need $O(10 \text{ ab}^{-1})$ to overcome background fluctuation in the continuum component.

P.Lebiedowicz and A. Szczurek
arXiv 1705.06535[hep-ph]

