

LHC Physics and EIC

Shima Shimizu (KEK 協力研究員)

Many thanks to Julia Furletova and Rik Yoshida, for their help!

Disclaimer:

I am **not** in the EIC community.

Your inputs for a discussion are very welcome!

LHC (Large Hadron Collider)

Mont Blanc

Lake Leman

Geneva city

←Geneva Airport

LHCb

pp collision ATLAS →

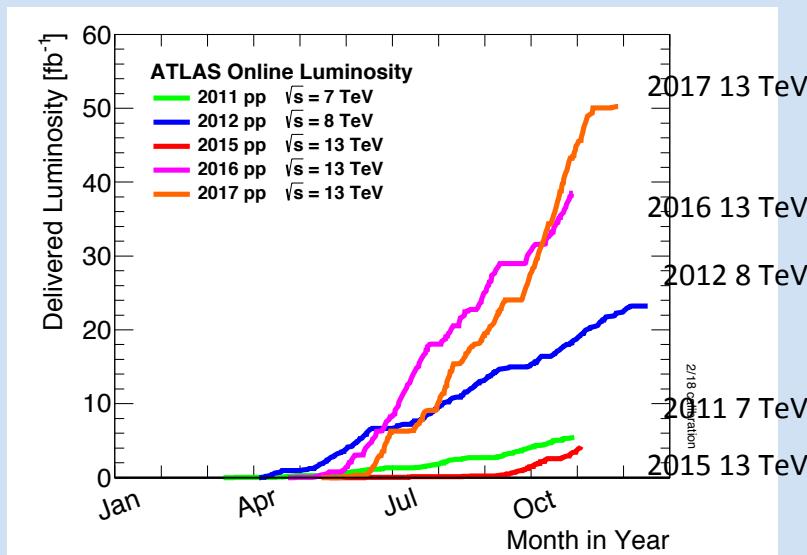
CERN

←pp collision: CMS

France

LHC (Large Hadron Collider)

Since 2009, LHC provided high energy proton-proton collisions at $\sqrt{s}=0.9$ TeV, 2.76 TeV, 7 TeV, 8 TeV, and 13 TeV.



Mont Blanc

Geneva city

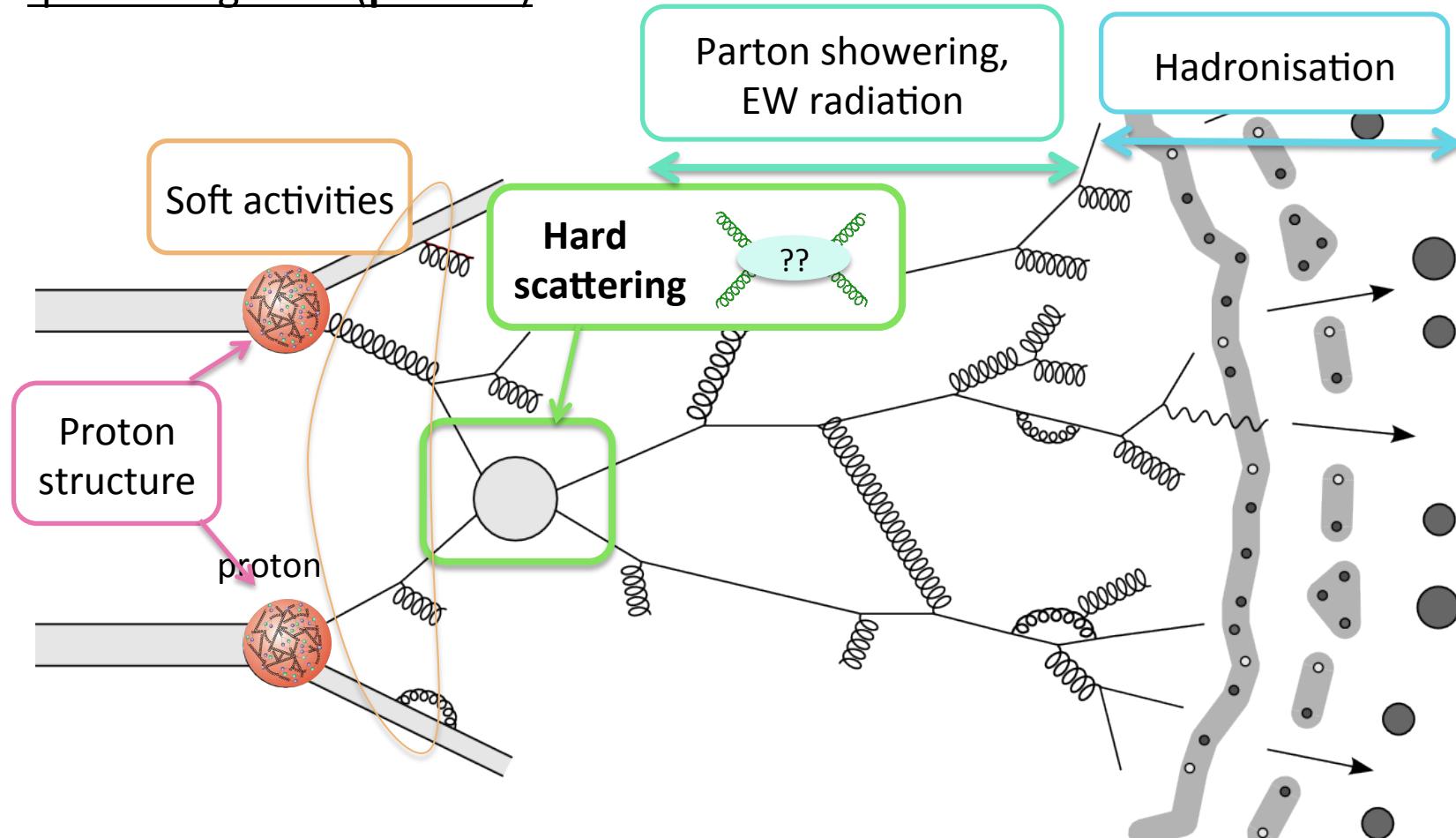
←Geneva Airport

CERN

- ◆ Search of new physics beyond the Standard Model.
- ◆ Precise measurement of the Standard Model physics.
e.g. Higgs, top...

Proton-proton collision

ATLAS and CMS look for new physics from hard scattering of quarks or gluons (**partons**).



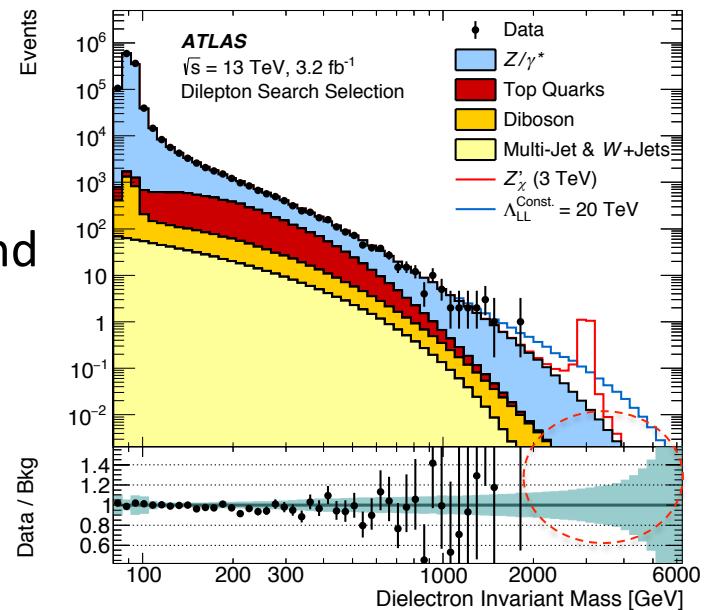
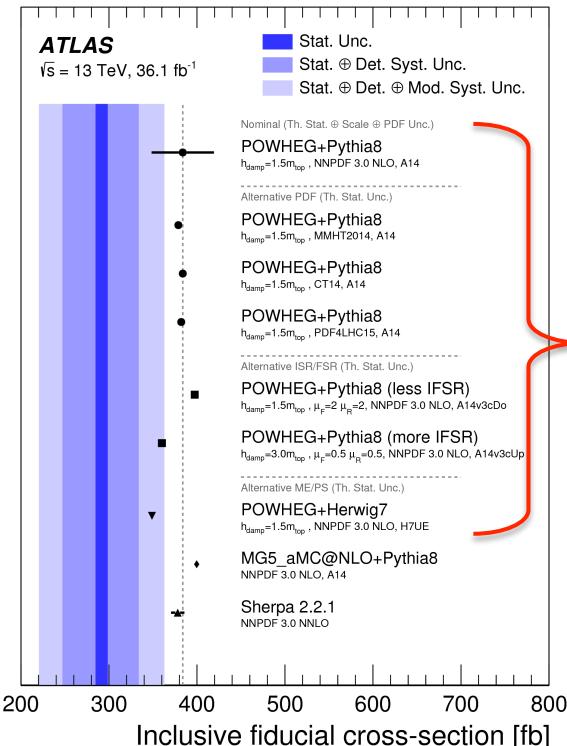
... and there are a lot of QCD to be understood.

Examples

Dilepton search

- Increasing uncertainties on background (SM predictions) at high mass region.
← From proton parton distribution functions (PDFs).

arXiv: 1801.02052



t anti-t cross section measurement

Predictions are given by

Matrix Element MC + Parton Shower MC

(Matrix Element → Calculation of the hard scattering.)

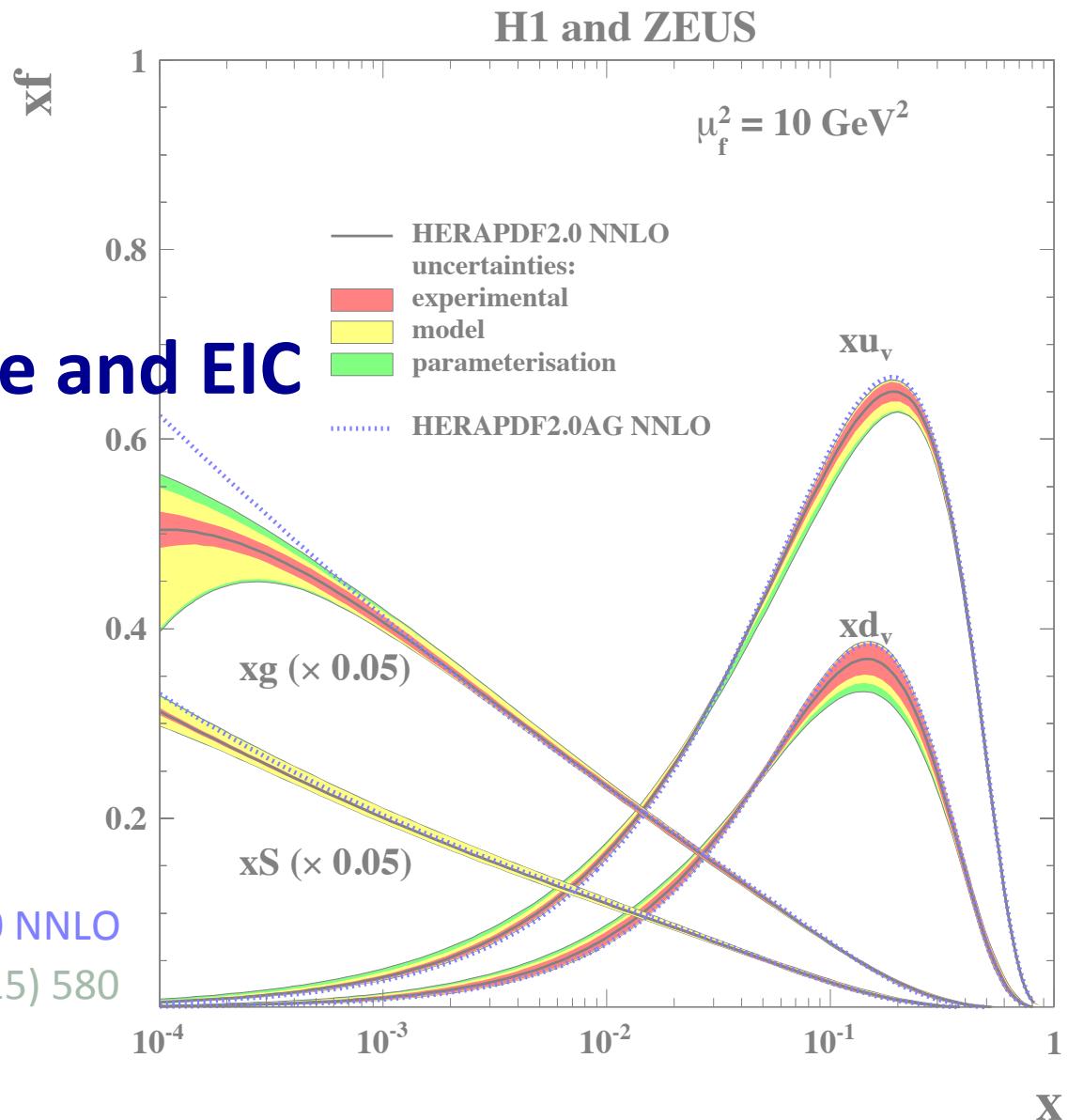
All using the same Matrix Element in POWHEG

- Differences come from
 - More/Less radiations
 - Different parton shower MCs

Can EIC give better understanding of them?

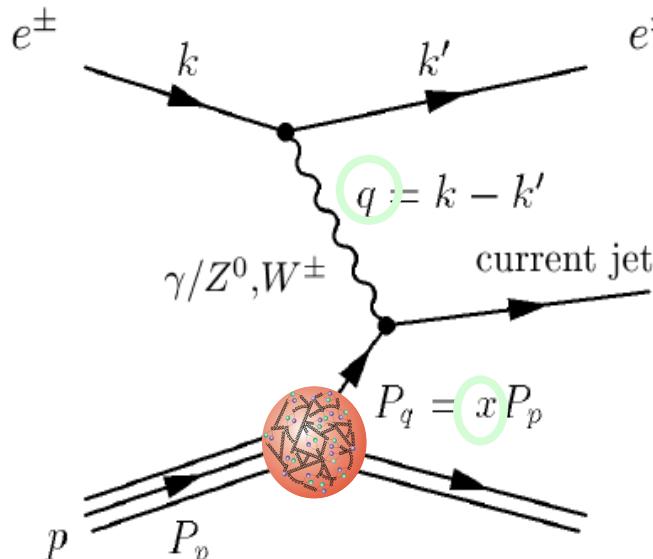
Proton structure and EIC

HERAPDF2.0 NNLO
EPJC 75 (2015) 580



Deep Inelastic Scattering (DIS)

ep DIS at HERA played a crucial role in understanding of the proton structure.



$$Q^2 = sxy$$

$$Q^2 = -q^2 = -(k - k')^2$$

$$x = \frac{Q^2}{2p \cdot q}$$

$$y = \frac{p \cdot q}{p \cdot k}$$

- ◆ Kinematic variables to describe DIS

Q²: Virtuality

→ probing power

x : Bjorken scaling variable

→ momentum fraction of the struck quark

y : Inelasticity

\sqrt{s} : center of mass energy

- Inclusive DIS cross sections can be written with structure functions.

$$\frac{d^2\sigma(e^\pm p)}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4} Y_+ \left[F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) \mp \frac{Y_-}{Y_+} x F_3(x, Q^2) \right] \quad Y_\pm = 1 \pm (1-y)^2$$

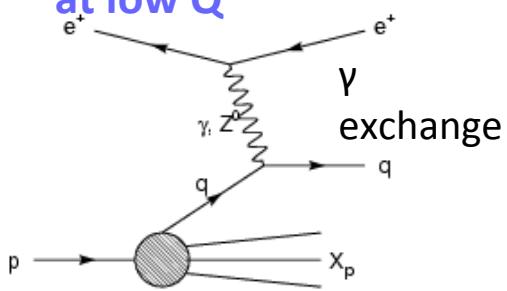
cross section of
point-like particles

Structure functions reflect momentum distribution of partons in the proton.

DIS and PDFs

The proton structure is parameterised by Parton Distribution Functions (PDFs), $q(x, Q^2)$ and $g(x, Q^2)$.
 They are determined from a fit on DIS cross sections.

Neutral current DIS (NC) at low Q^2



$$\gamma \rightarrow F_2 = \sum A_q x(q + \bar{q})$$

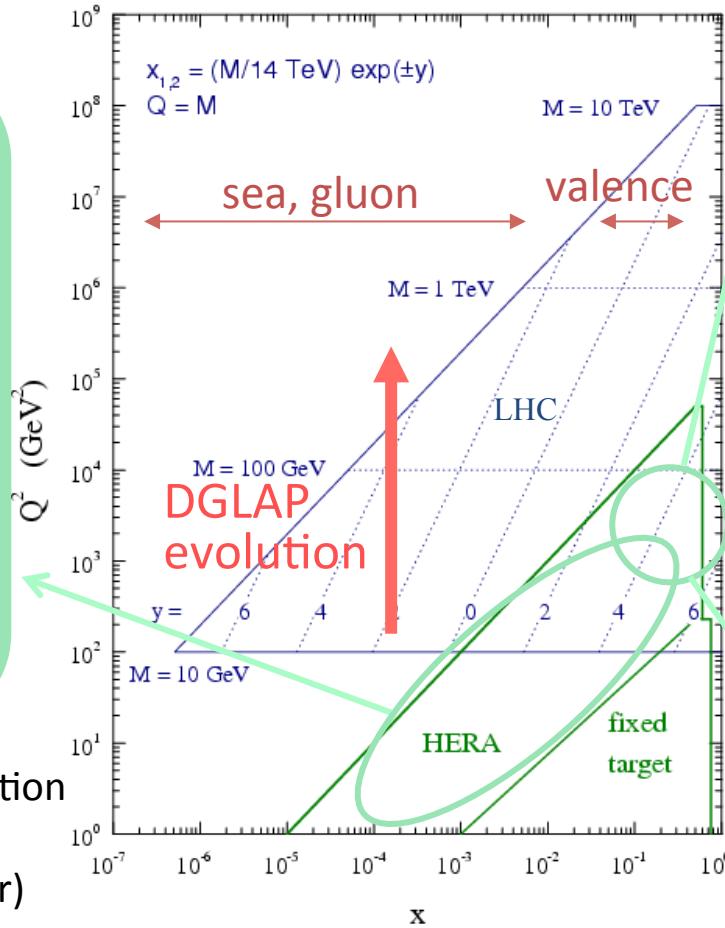
Sea + valence quark

$$\frac{\partial F_2}{\partial \ln Q^2} \propto x g$$

gluon

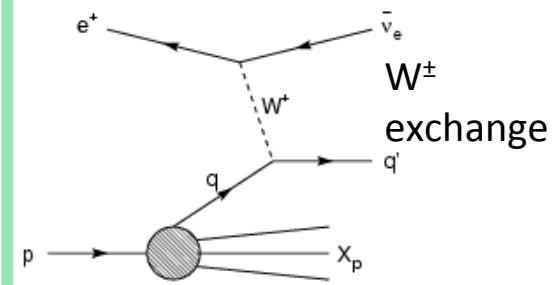
F_L : longitudinal structure function
 \rightarrow gluon

sizable only at high- y (see later)



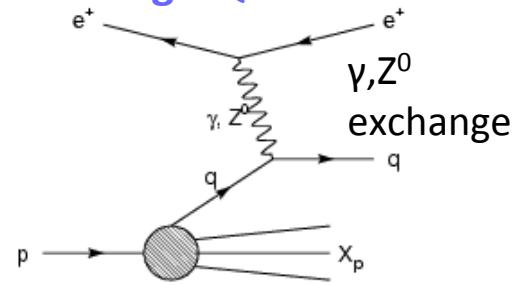
The Q^2 evolution can be described by perturbative QCD, using DGLAP equation.

Charged current DIS (cc)



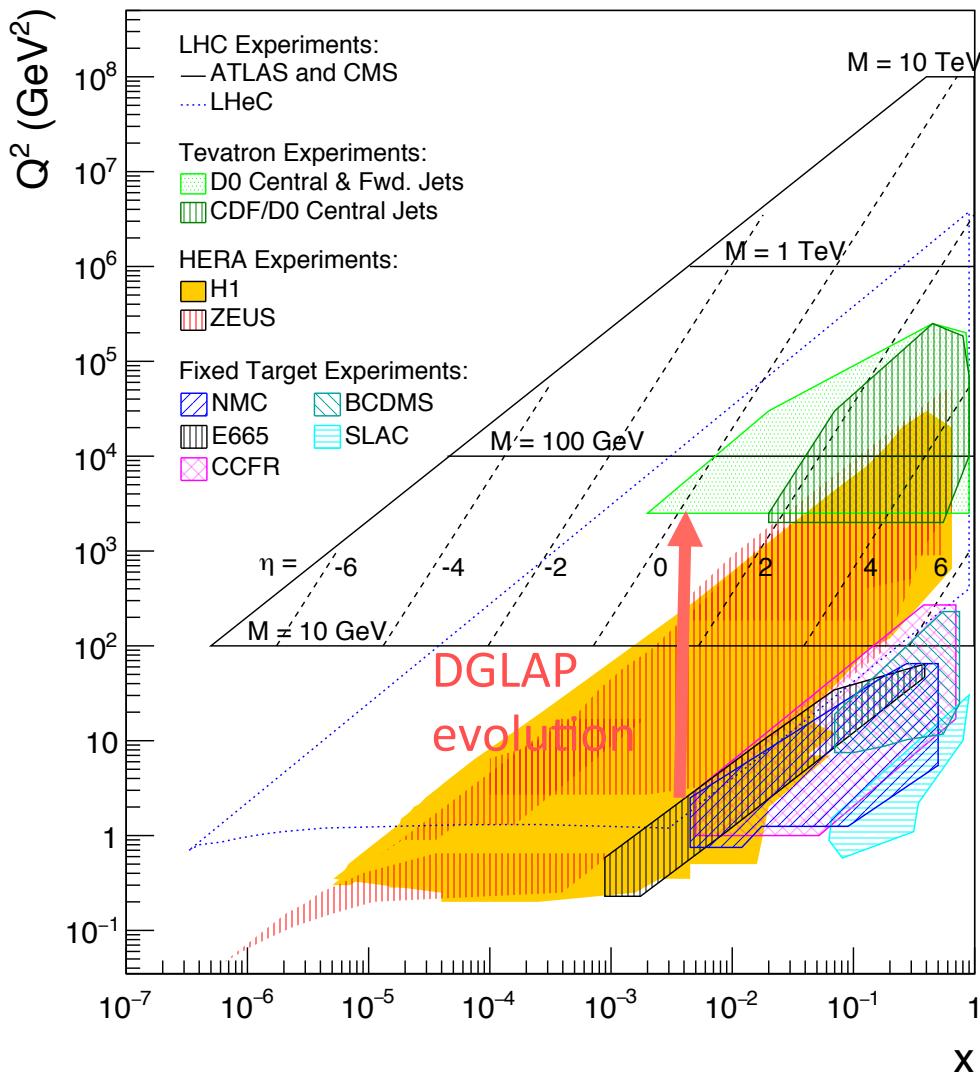
Charge selective interaction
 e^- : u quark e^+ : d quark

Neutral current DIS (NC) at high Q^2

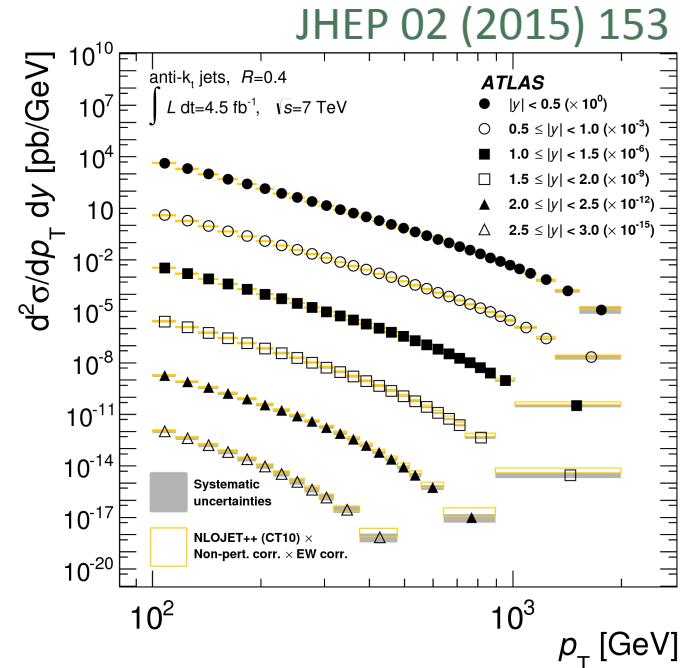


F_2 : Sea + valence quark
 Z^0 introduces parity violation.
 $\rightarrow x F_3 = \sum B_q x(q - \bar{q})$
 valence quark

DGLAP works well...



pre-LHC PDFs succeed to describe LHC data in general.



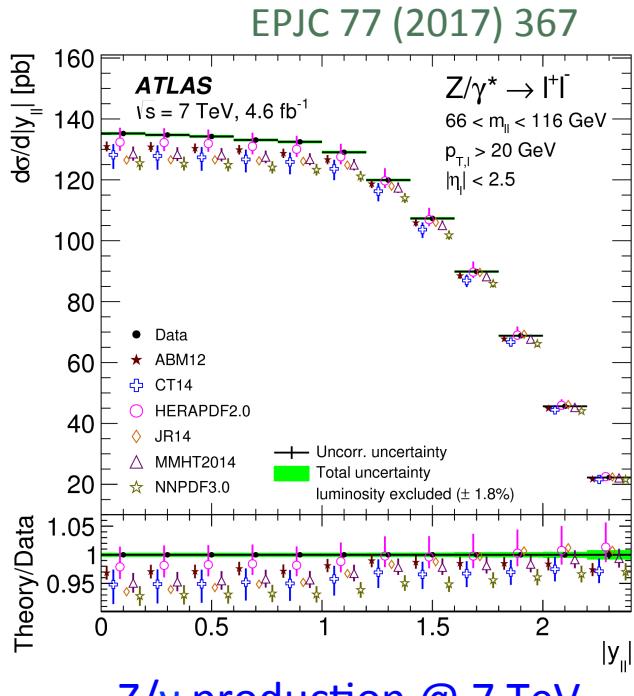
Inclusive jet cross section vs. prediction using CT10 PDFs

CT10 PDF: HERA DIS, Fixed target, Tevatron W/Z, jets

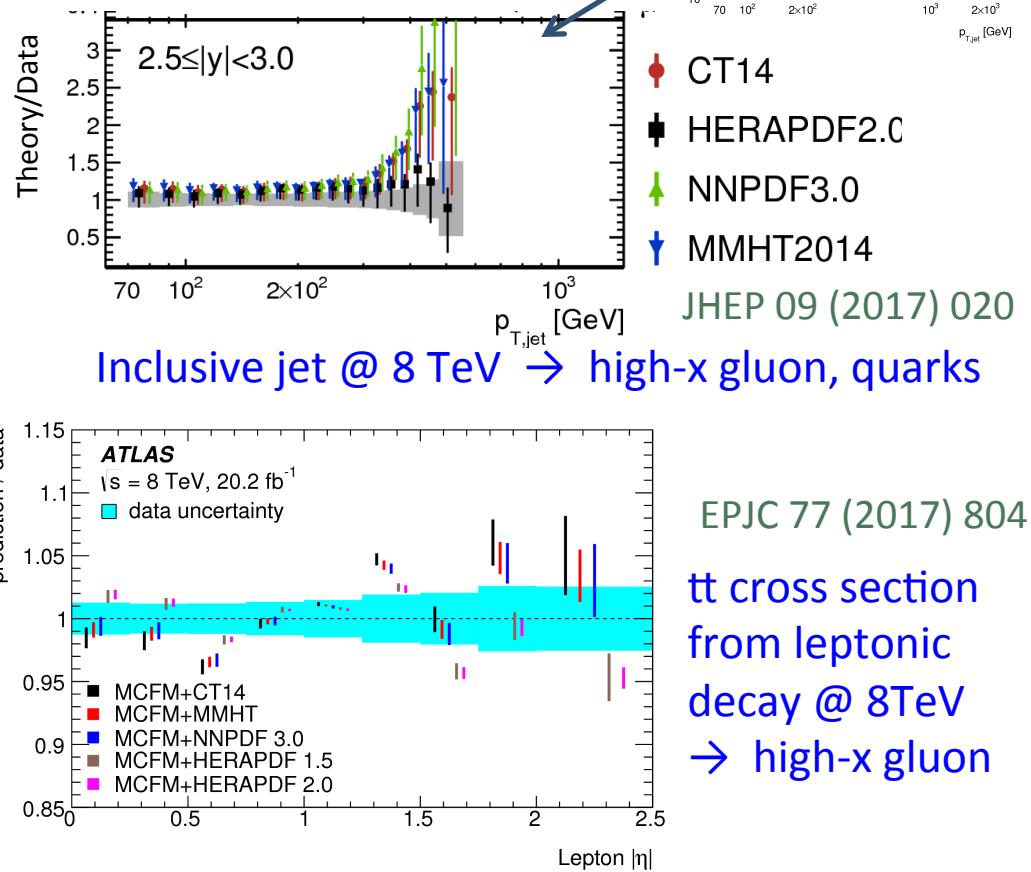
LHC provides more input

LHC measurements show their own preferences of PDF sets.

→ Good inputs for further constraints on PDFs.



Z/γ production @ 7 TeV
→ quark distributions

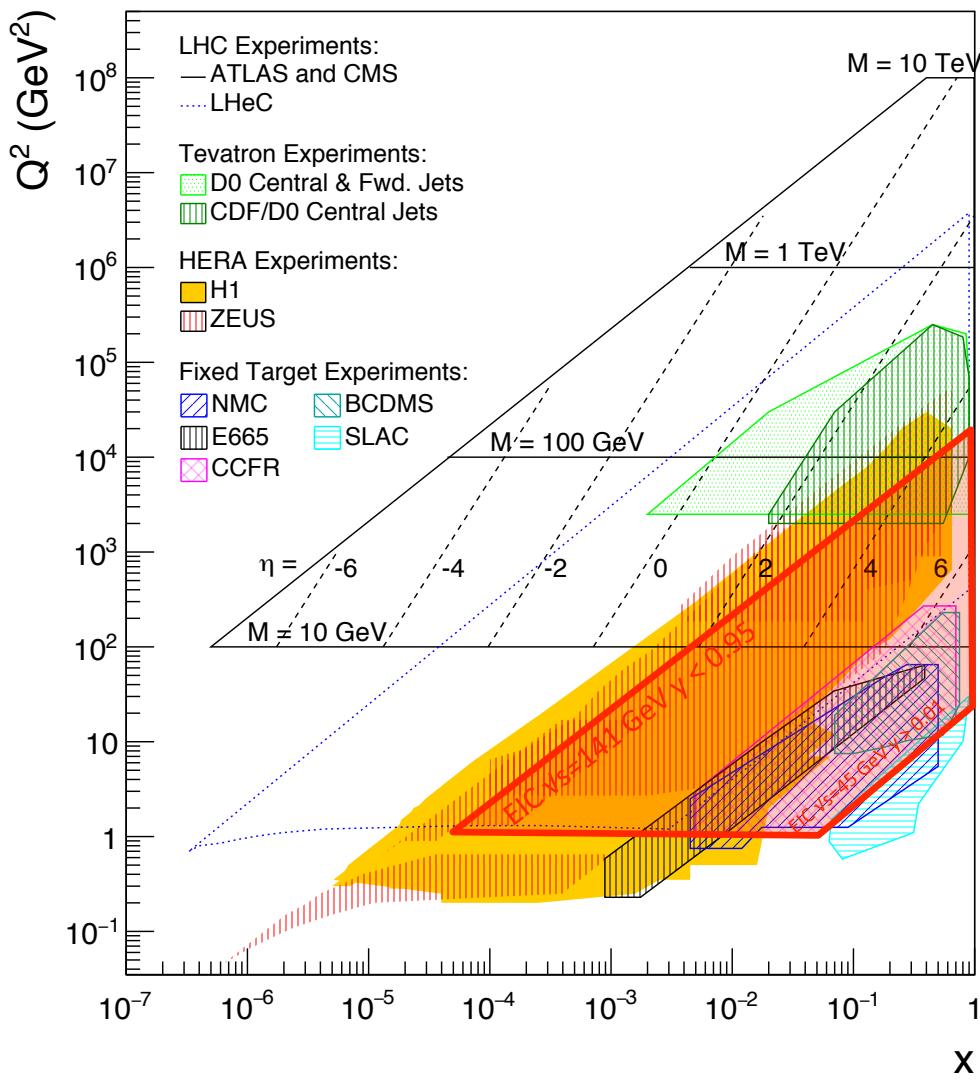


However, it is not ideal situation for LHC searches.

- Looking for deviations from the SM, but SM uses PDFs with LHC feedbacks.

→ Great to have other cross checks and/or more inputs from other experiments.

EIC provides opportunity for improvement



With \sqrt{s} up to 141 GeV, EIC ep has a decent coverage of kinematic region.

- ◆ Free from target correction and nuclear effect.
- ◆ Free from unknown physics at TeV scale.
- ◆ In a region where DGLAP is (probably) applicable.

EIC aims 10-100 fb⁻¹/year of data.

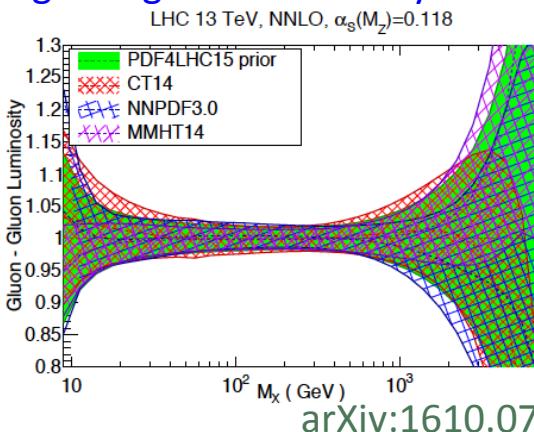
c.f. HERA: $\sim 0.5 \text{ fb}^{-1}$ in total,
for each experiment.

- Can provide useful and powerful inputs for PDF determination.
- High-x measurements
 - Charged Current DIS
 - F_L measurement

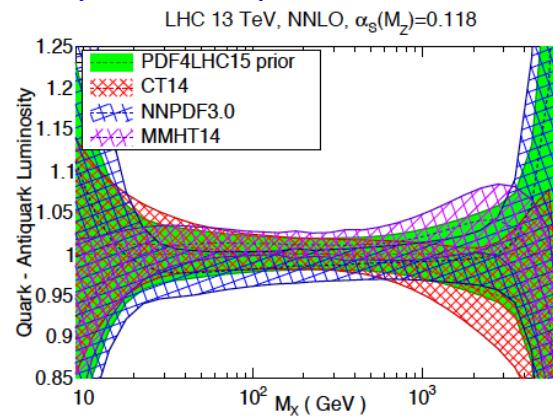
Why is high-x important?

- As a search goes higher mass, more precision at **high-x** is needed.
 - Uncertainties are large.

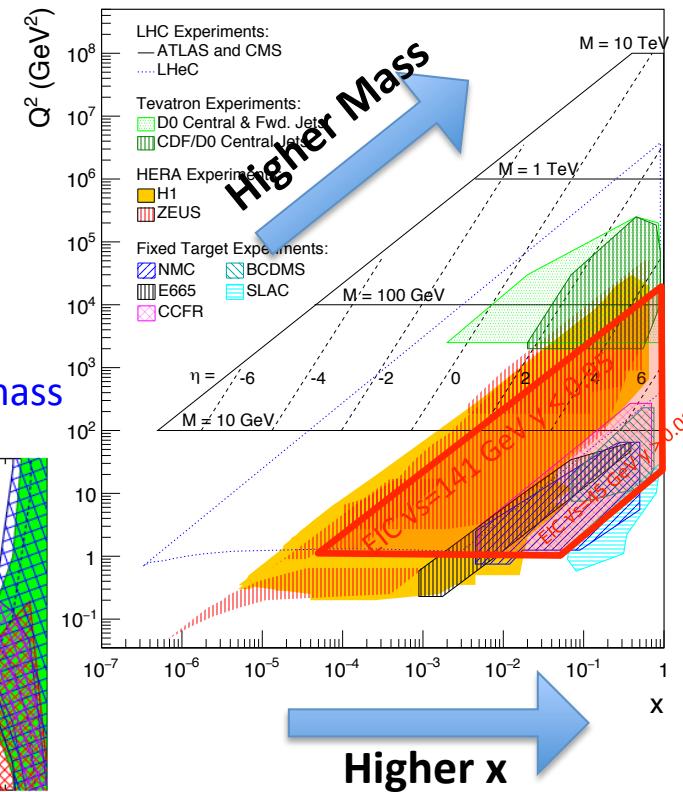
Comparison of
gluon-gluon luminosity vs mass



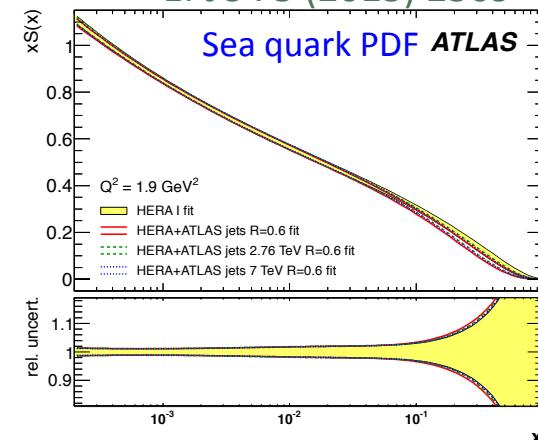
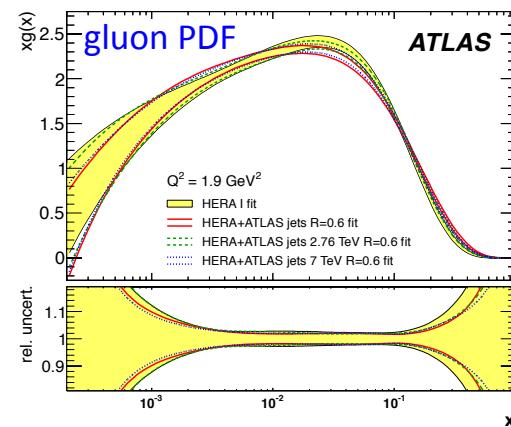
Comparison of
quark-antiquark lumi. vs mass



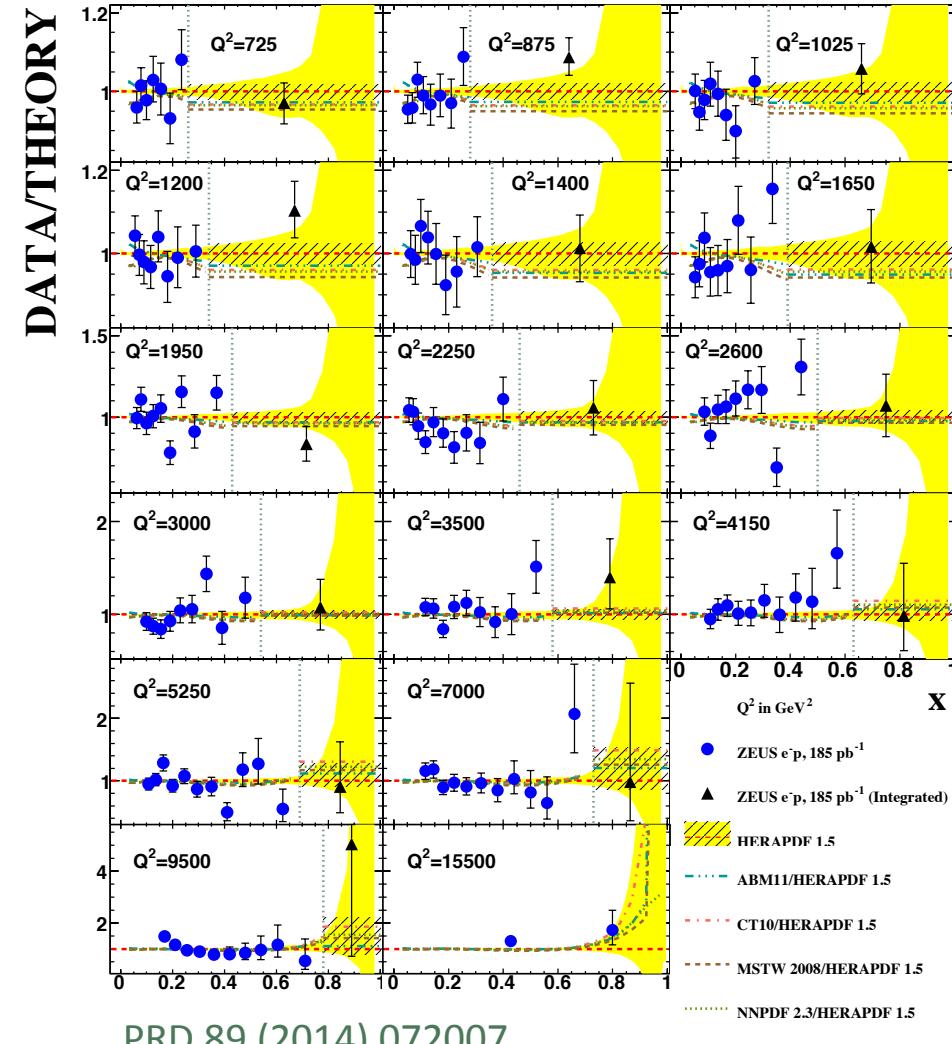
- High-x determination from HERA still has a room for improvement.
 - Shape of gluon and sea-quark PDFs can move with ATLAS jet data.



EPJC 73 (2013) 2509

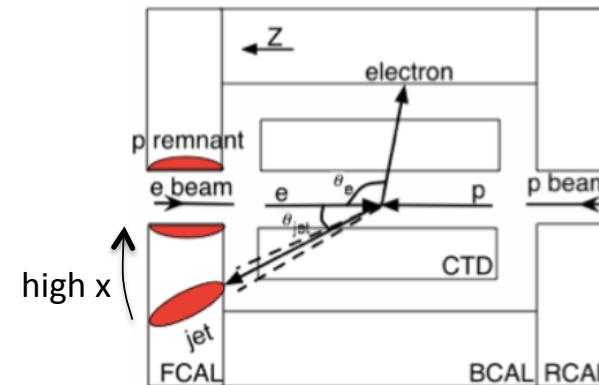


High-x measurement from HERA



ZEUS high-x measurement (Not in the PDF fit)

- Measured at relatively high Q^2
- At very high x , struck quark escapes from the beam pipe
- Highest- x bin ($x > x_{\text{edge}}$) shows the integrated cross section.



Stat. error dominant
→ Does EIC allow a better measurement?

HERA vs EIC for high-x measurement

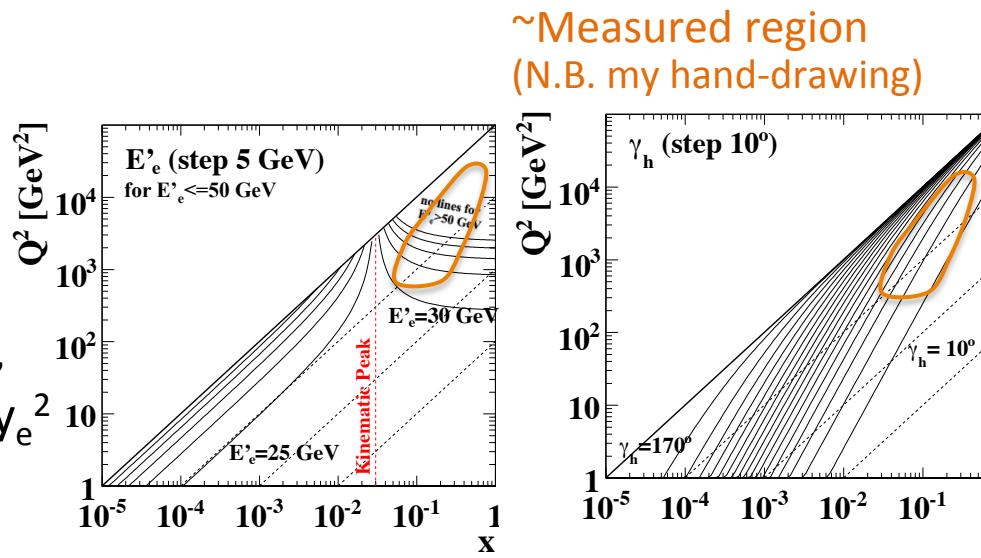
In the ZEUS measurement:

Kinematic reconstruction

- Q^2 from the scattered electron

$$Q^2 = 2E_e E'_e (1 + \cos \theta_e)$$

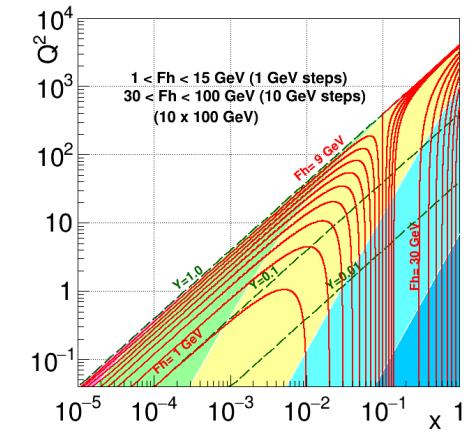
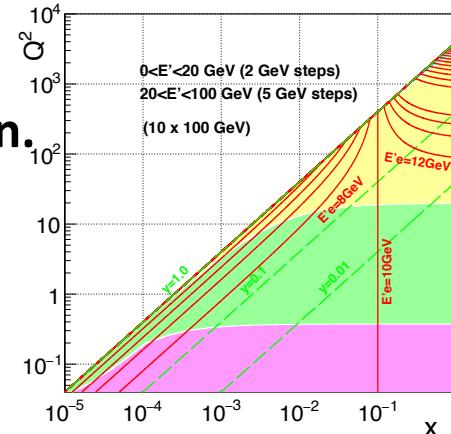
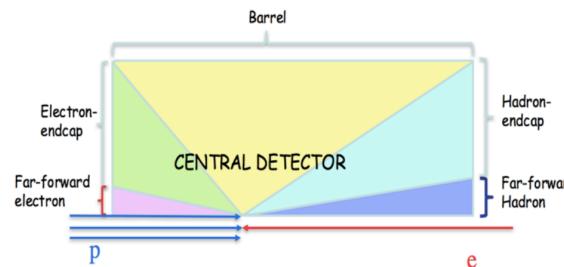
- x from jet* energies and angles (γ_h), to avoid large uncert. from $\Delta x/x \sim 1/y_e^2$
 - if e and jet balance, E'_{eT} and jet angle are used.



*jet ~ hadrons from scattered quark

At EIC:

- Scattered electron will be well in the central region.
- How about the scattered quark??
- Need good energy/angle measurement in the forward region.**



HERA vs EIC for high-x measurement

In the ZEUS measurement:

Kinematic reconstruction

- Q^2 from the scatter

$$Q^2 = 2E_e E'_e (1 + \cos\theta)$$

- x from jet* energies

to avoid large uncertainties

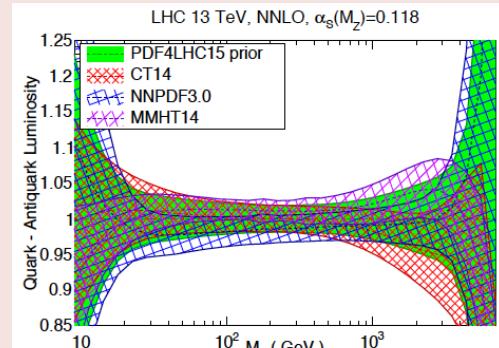
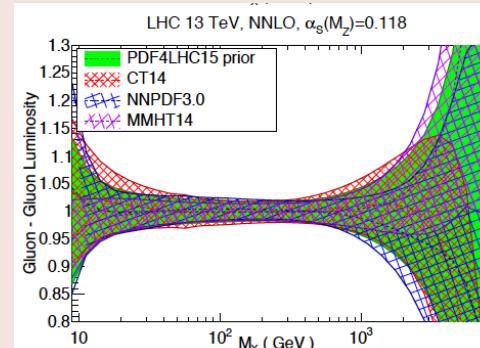
- if e and jet balanced

$$E'_{eT} \text{ and jet angle}$$

At EIC:

- Scattered electron

If it is achieved, EIC *might* improve these uncertainties

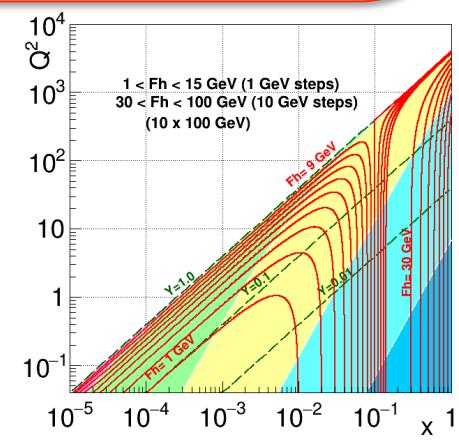
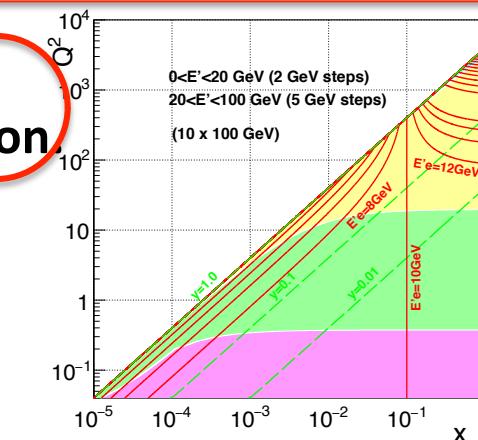
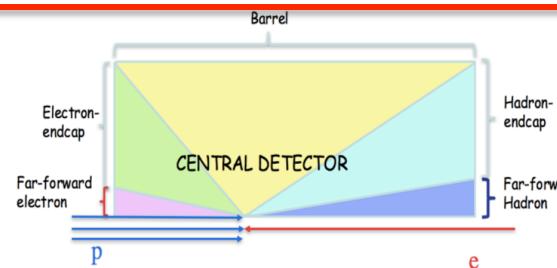


from its advantage of large statistics.

might: need to know kinematic coverage and precision.

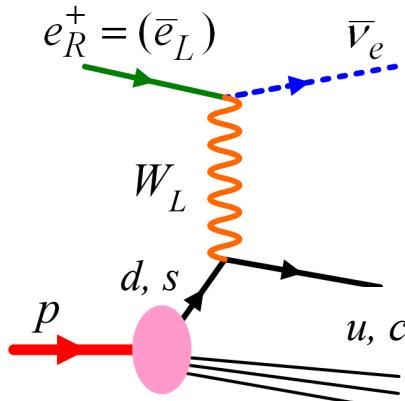
- How about the scattered quarks?

- Need good energy/angle measurement in the forward region**



Charged Current DIS

Charge selective interaction via W exchange



$$e^- q^{(+)} \rightarrow \nu q^{(-)}$$

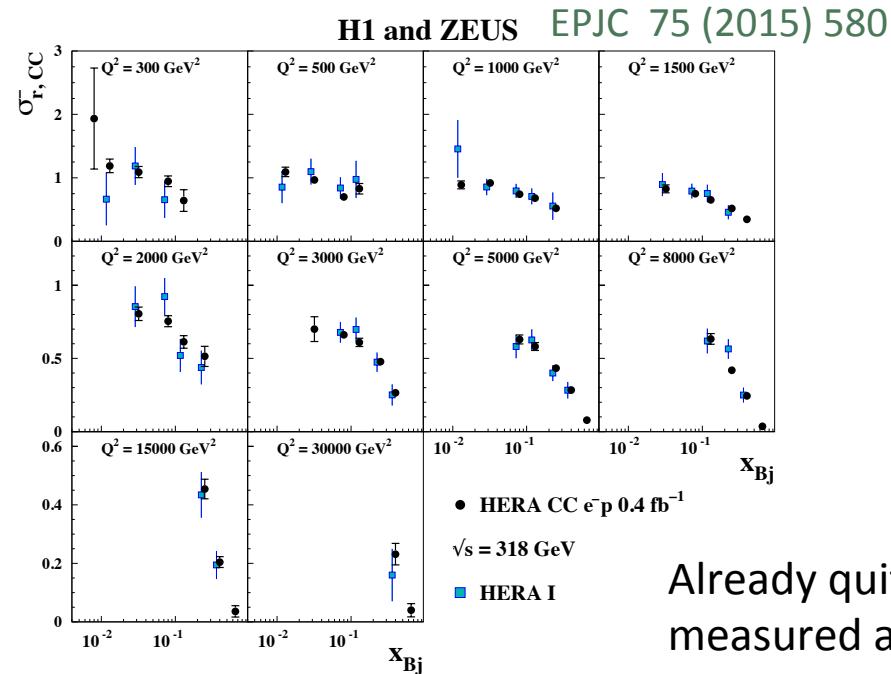
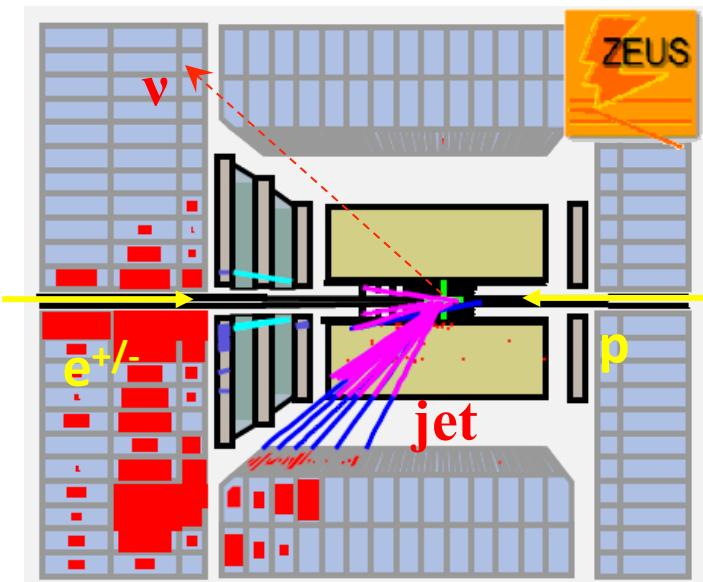
$$e^+ q^{(-)} \rightarrow \bar{\nu} q^{(+)}$$

Neutrinos at the final state
= **no scattered electron**

Electron/Positron beams give flavour separation of PDFs

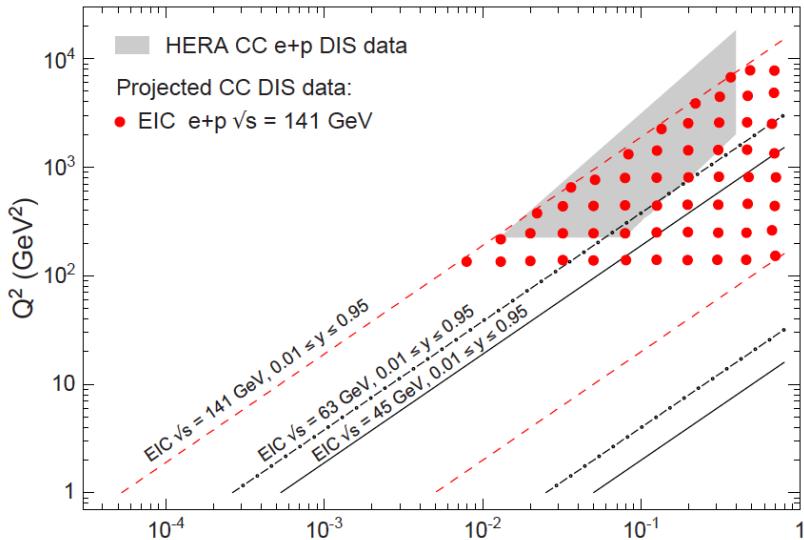
$$\tilde{\sigma}(e^+ p) \propto [(\bar{u} + \bar{c}) + (1 - y)^2 (\bar{d} + \bar{s})]$$

$$\tilde{\sigma}(e^- p) \propto [(u + c) + (1 - y)^2 (d + s)]$$



Already quite well measured at HERA

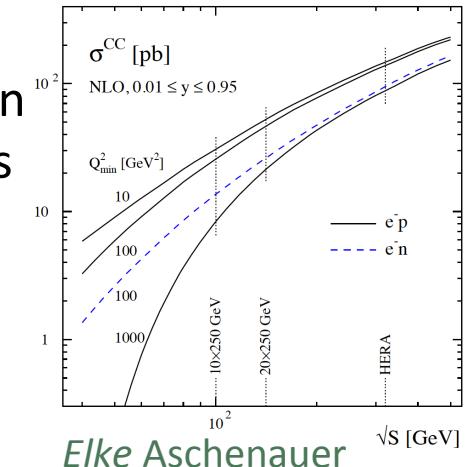
Charged Current DIS at EIC?



EIC may extend the measurement to higher x .

- Small cross section but large statistics would help.

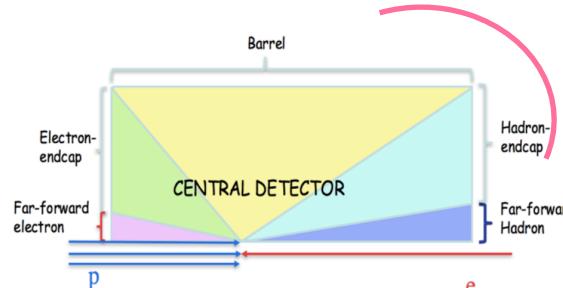
[arXiv:1708.01527](https://arxiv.org/abs/1708.01527)



Elke Aschenauer

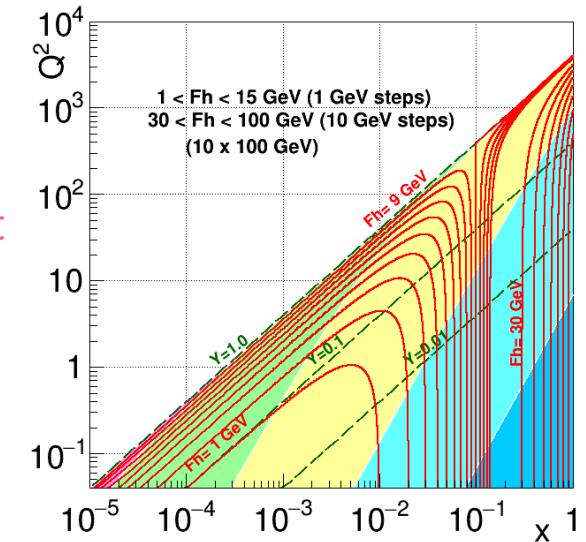
A neutrino at the final state: Large p_T^{Miss} , No scattered electron.

→ Kinematic variables should be reconstructed from **hadron activities** (γ_h , E_h).



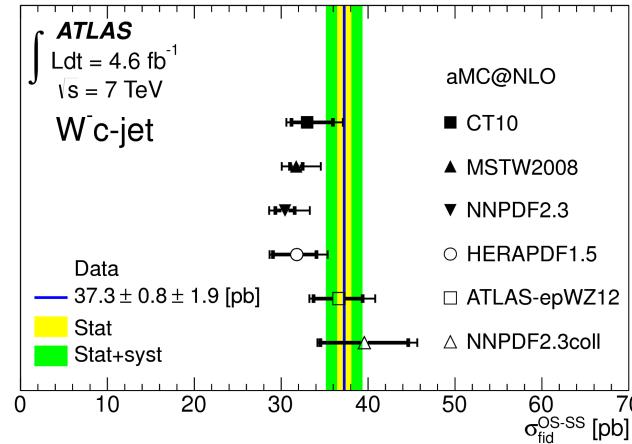
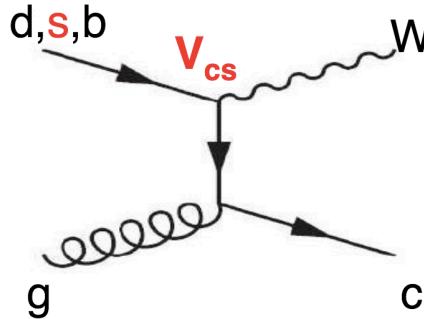
Good measurement of hadronic energy in this region.

A study requires decent description by Monte Carlo.

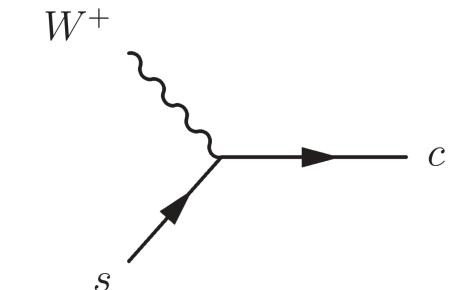


Charm-tagged Charged Current DIS

- ◆ If a charm is tagged in CC DIS, the cross section has a sensitivity to the intrinsic strange.
- ◆ Strange quark distribution is not well determined.
 - ATLAS data prefers more strangeness than fixed target data?

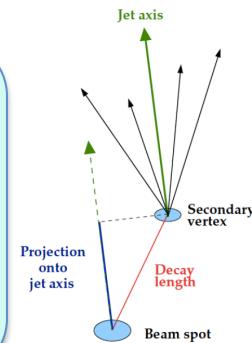


- ◆ Charm-tagged CC DIS at EIC would be interesting.
 - Free from the nuclear/target correction.
 - Requires charm tagging in the Central-Forward region.



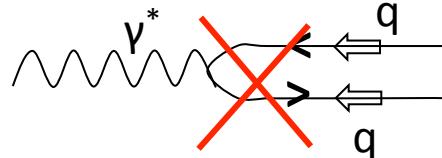
Y. Furletova

At EIC
 $(\sqrt{s} \sim 70 \text{ GeV}, Q^2 > 100 \text{ GeV}^2)$:
 $\sigma(e^+ p \rightarrow e^- + c + X) \sim 0.1 \text{ pb}$
 $\Rightarrow \text{with } 10 \text{ fb}^{-1} / \text{year}$
 $\Rightarrow \sim 1000 \text{ events/year}$



Longitudinal structure function F_L

- F_L is proportional to the cross section of longitudinal photon interacting with proton. $F_L \propto \sigma_L$
- In naïve Quark Parton Model, proton has co-linear spin $\frac{1}{2}$ quarks only.

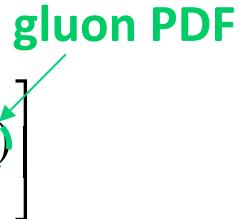


Longitudinal photon cannot interact with a quark $\rightarrow F_L = 0$

- Gluon emission in the proton $\rightarrow F_L \neq 0$

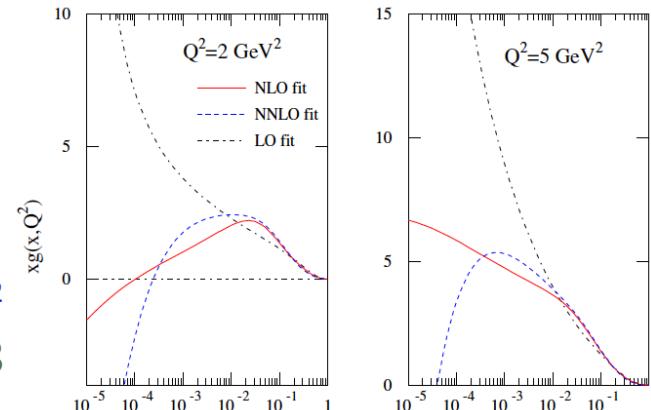
i.e. F_L directly reflects gluon dynamics in the proton.

$$\text{In perturbative QCD: } F_L = \frac{\alpha_s}{4\pi} x^2 \int_x^1 \frac{dz}{z^3} \left[\frac{16}{3} F_2 + 8 \sum_q e_q^2 \left(1 - \frac{x}{z} \right) z g(z) \right]$$



F_L provides another validity check of the gluon PDFs and even the DGLAP framework at low Q^2 .

Instability of gluon PDF at low Q^2
R. Throne DIS2008



F_L measurement from HERA

Reduced DIS cross section at low Q^2
(xF_3 is ignored)

$$\tilde{\sigma} = \frac{Q^2 Y_+}{2\pi\alpha^2} \frac{d\sigma^2}{dx dQ^2} = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2)$$

F_L measurement requires

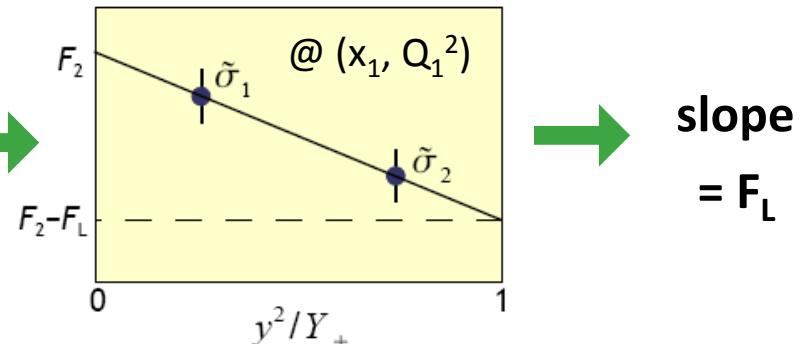
- ◆ large y to see F_L contribution
- ◆ Comparison at the same (x, Q^2) but the different y

$$y = \frac{Q^2}{sx} \rightarrow \text{multiple beam energies}$$

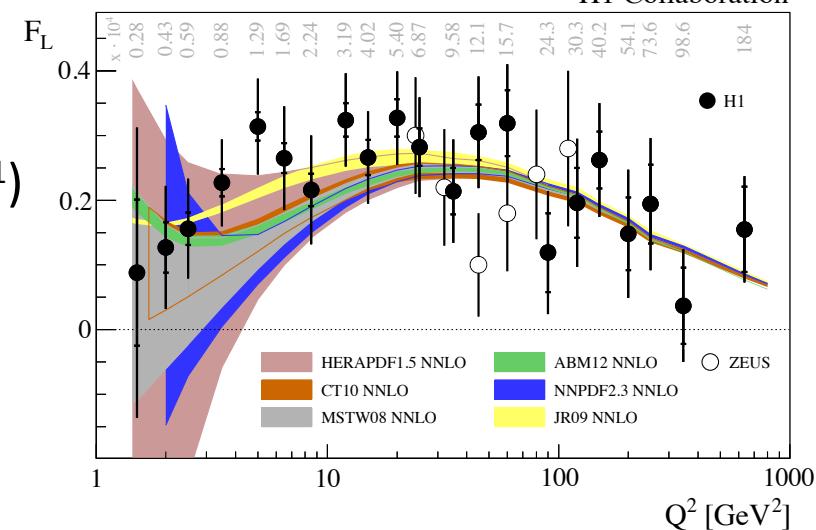
Dedicated data taking
with **lowered proton beam energies**
(920 GeV \rightarrow 460 GeV 14 pb $^{-1}$, 575 GeV 8 pb $^{-1}$)
at the last 3 months of HERA

→ First direct F_L measurement
at collider experiments

$$0 < y < 1, \quad Y_+ = 1 + (1 - y)^2 \rightarrow 1 < Y_+ < 2$$



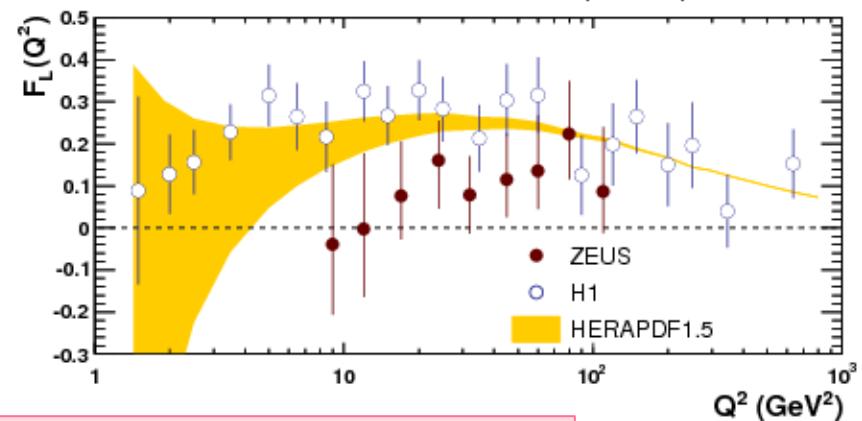
EPJC 74 (2014) 2814



What was the difficulty?

Q: H1 did a better job. Why?

A: Detector!

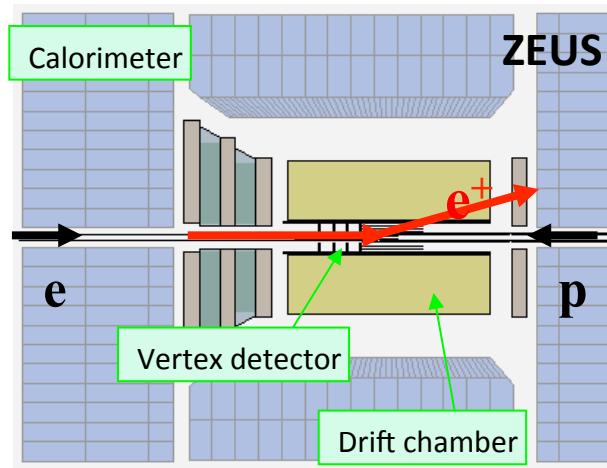
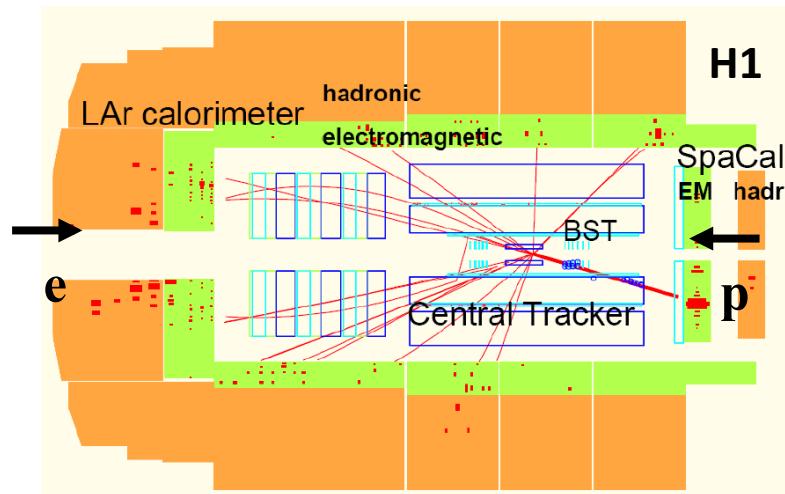


$$y_{el} = 1 - \frac{E'_e}{2E_e}(1 - \cos \theta_e)$$

$$Q_{el}^2 = 2E_e E'_e (1 + \cos \theta_e)$$

Low Q^2 : Lower electron angle
High y : Lower electron energy

If electron ID fails, large amount of background (photoproduction) comes in.



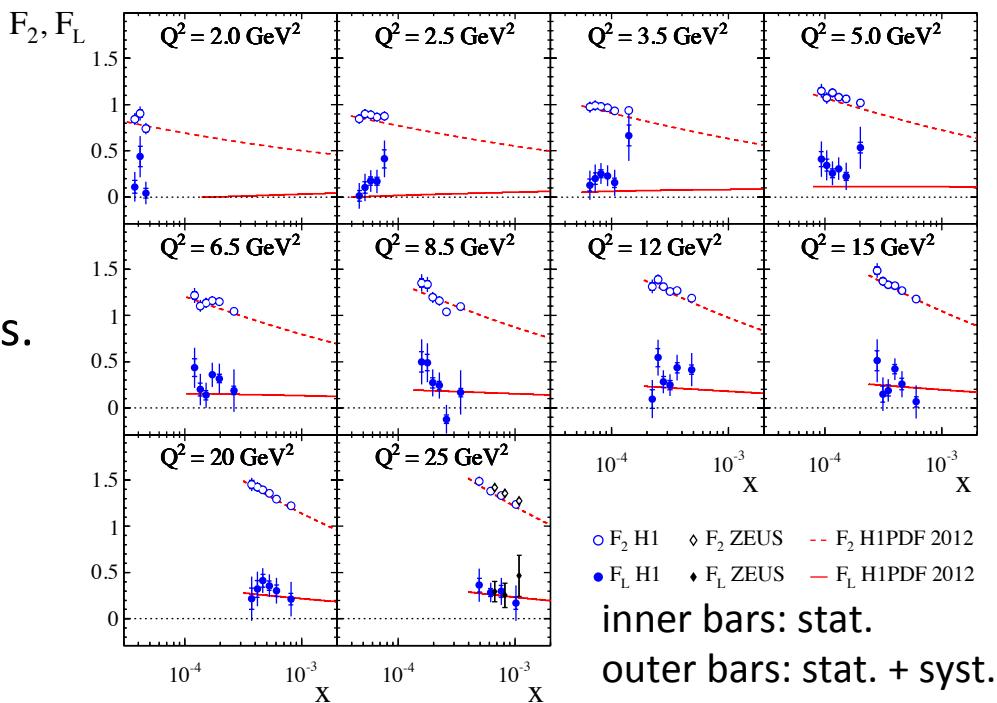
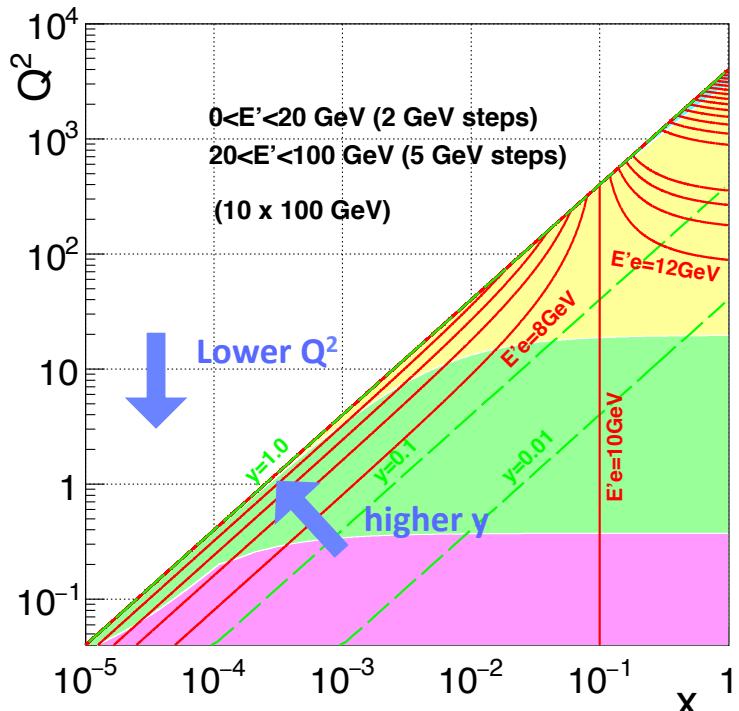
Measured at:
H1 $E'_e > 3.4 \text{ GeV}$
ZEUS $E'_e > 6 \text{ GeV}$

H1 was equipped with detectors for good electron identification in rear side.

Can EIC do better job?

Advantages of EIC

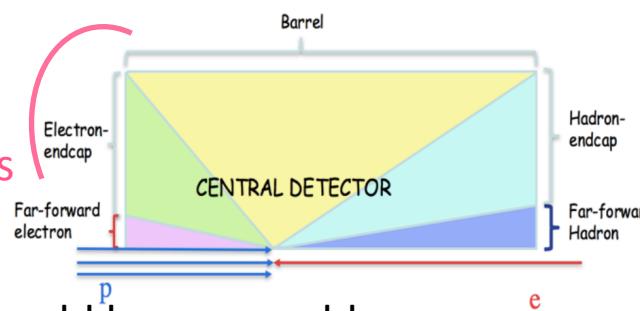
- ◆ Variable centre of mass energies.
- ◆ High luminosity
- ◆ (Better systematics?)



inner bars: stat.
outer bars: stat. + syst.

EIC: $Q^2 \sim 5 \text{ GeV}$ gives $x \sim 10^{-3}-10^{-2}$
(depends on how CM energies varies)
→ Would be interesting to see gluons

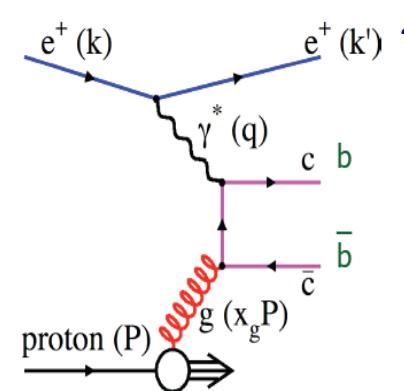
How well can
electrons be
measured in this
region?



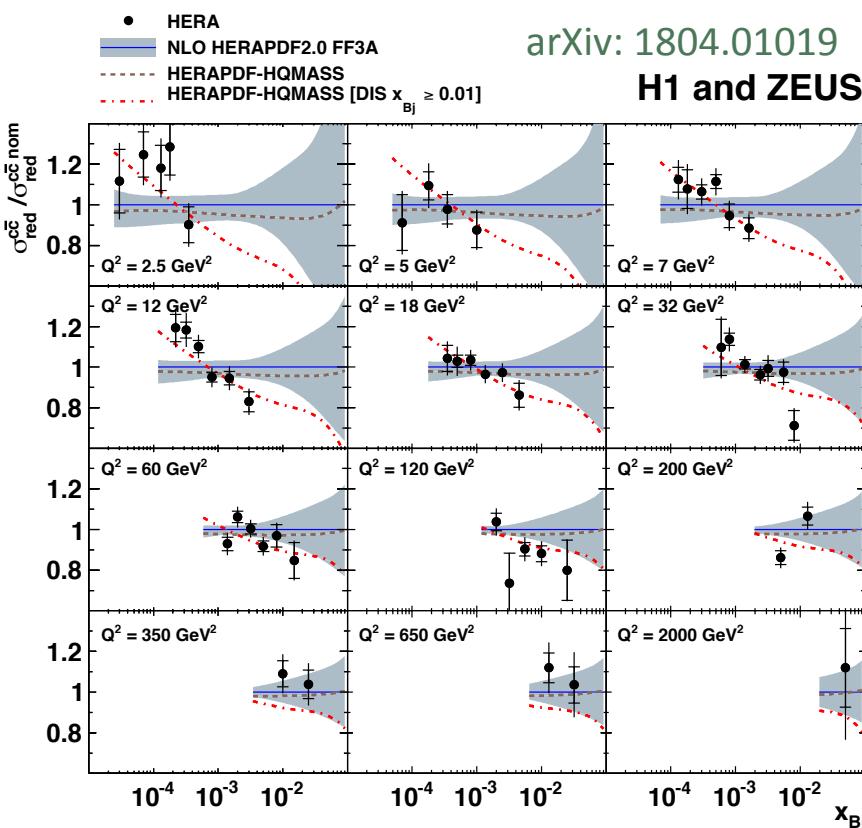
Also, hadrons should be reasonably measured for identification of DIS events.

σ^{cc} , σ^{bb}

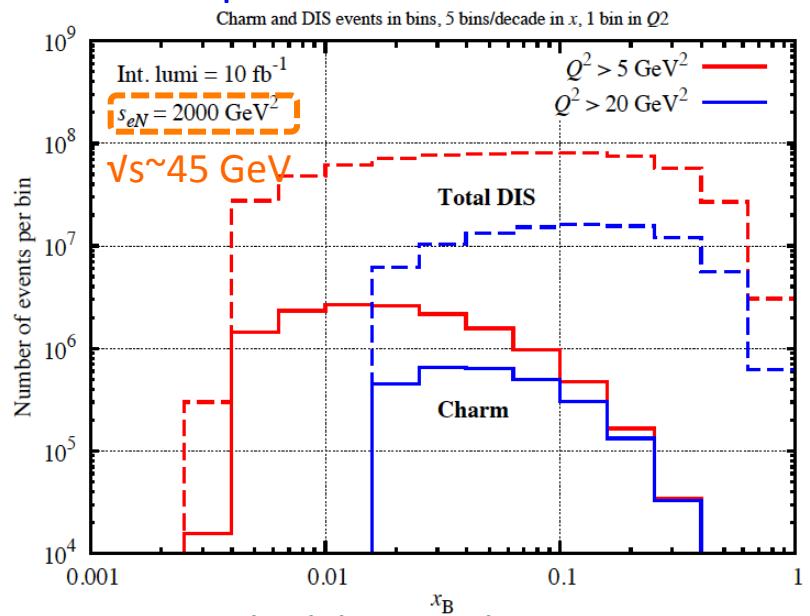
- ◆ Cross section with heavy-flavoured quark pair (cc, bb).
- ◆ Sensitive to gluons,
but the description of heavy flavour production is complicated.



Latest HERA results show some difficulty in describing both σ^{cc} and low- x $\sigma^{\text{inc. DIS}}$.



Charm production rate at low \sqrt{s} vs eN



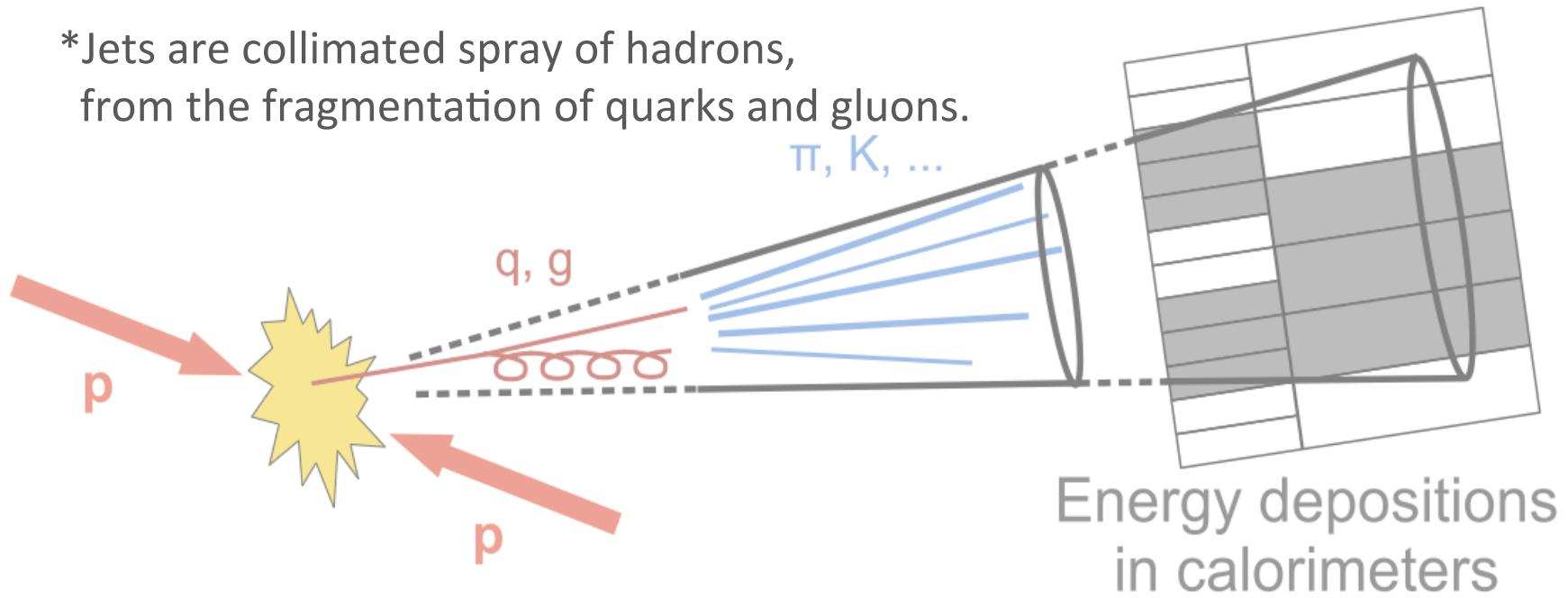
E. Chudakov et. al. arXiv: 1610.08536

With $\sqrt{s} \sim 100$ GeV and large stat., perhaps EIC can clarify the situation.

Jet physics at EIC?



*Jets are collimated spray of hadrons,
from the fragmentation of quarks and gluons.



Energy depositions
in calorimeters

Description of jet physics at LHC

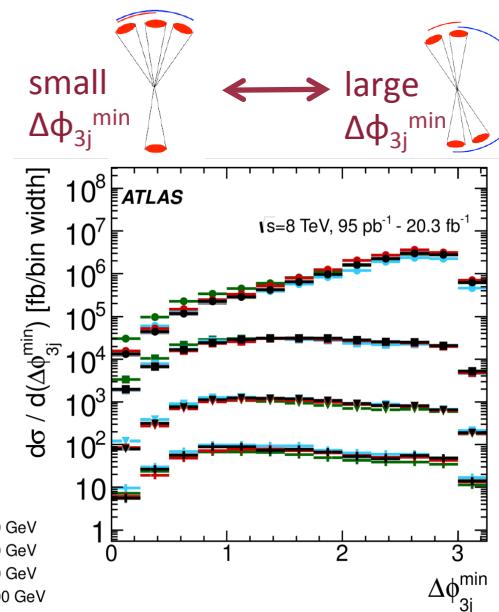
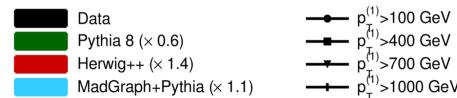
Understanding and description of jet production is quite important at LHC.

- Multijet is a severe background in searches and measurements.
- Hard radiation gives one of the major uncertainties in a precise measurement of e.g. top quarks.

Several MCs are tested in various measurements using various observables.

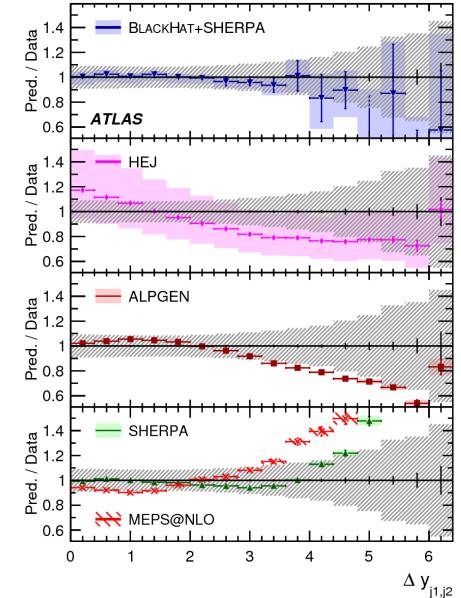
- LO $2 \rightarrow 2$ MCs with parton shower models.
 - Easy event generation to test analysis methods.
- Multi-leg ($2 \rightarrow N$) LO MCs
- NLO MCs, matched to parton shower MCs.
- MC with all-order sum of wide angle QCD radiation.

JHEP 12 (2015) 105
ATLAS 4jets, $\Delta\phi_{3j}$



ATLAS W+2jets, $\Delta y_{j1, j2}$
 $\sqrt{s}=7$ TeV, 4.6 fb^{-1}

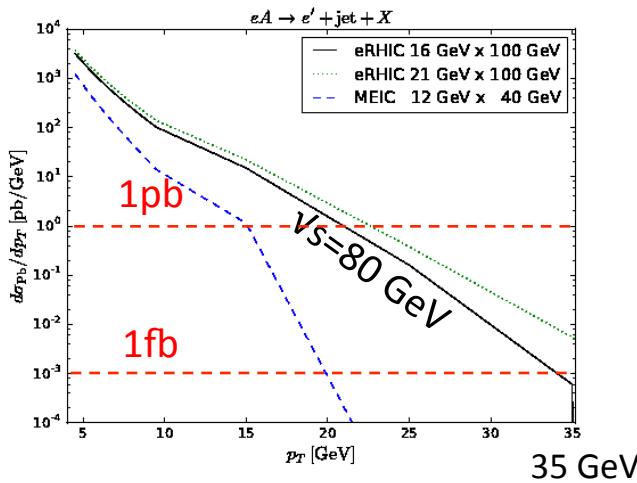
EPJC 75(2015) 82



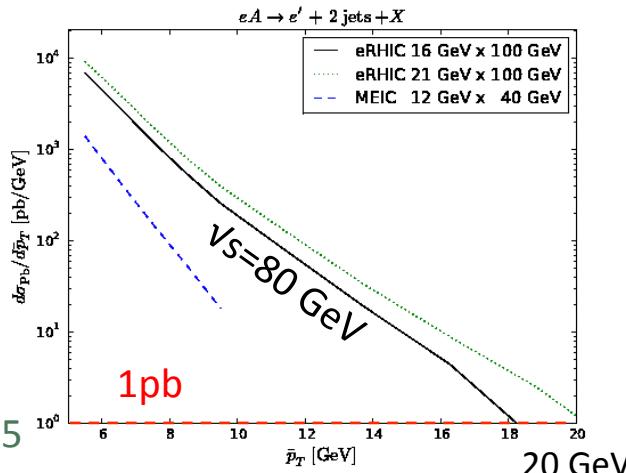
Jet production at EIC

- ◆ ep colliders give a cleaner circumstance than pp.
- ◆ How limited is the p_T reach?

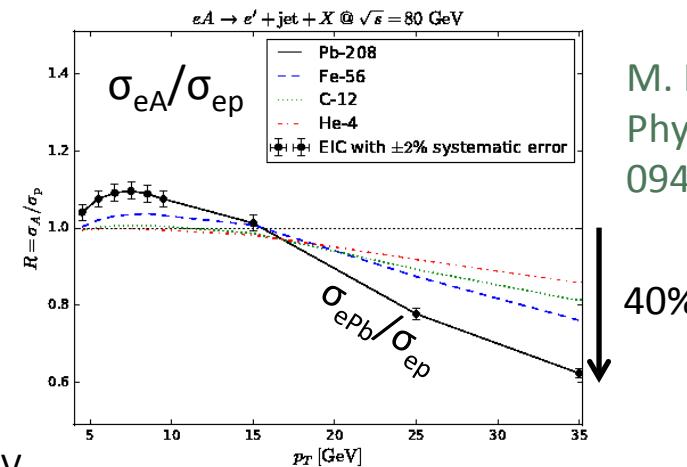
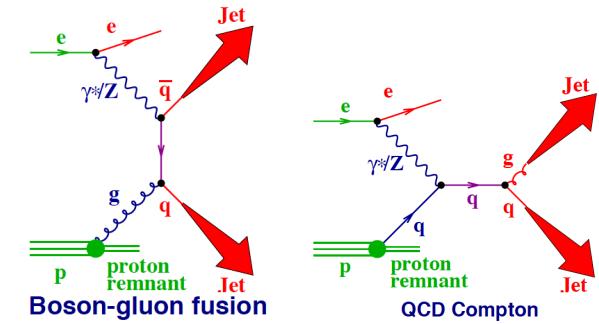
inclusive jet
 $d\sigma/dp_T$
@ePb DIS



dijet $d\sigma/dp_T$
@ ePb
photo-
production



M. Klasen,
K.Kovarik
arXiv 1803.10985



M. Klasen et al.,
Phys. Rev. D 95,
094013 (2017)

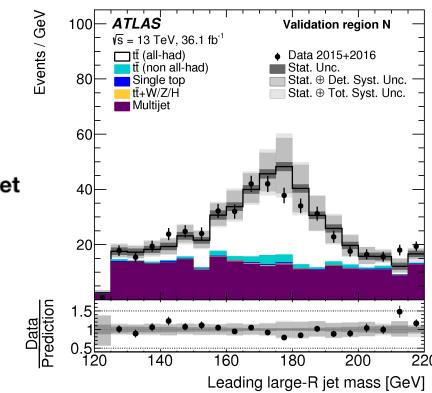
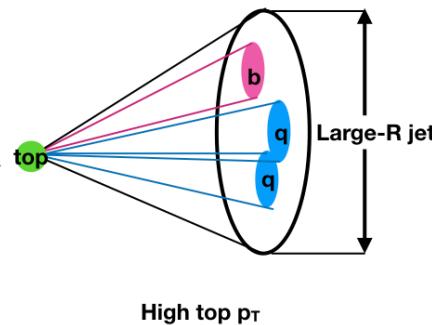
Probably jets with $p_T \sim O(10) \text{ GeV}$
(or more?) can be studied at EIC ep collisions.

- Higher \sqrt{s} or larger stat. allow higher p_T reach.

Jet substructure measurements?

- ◆ Quite a progress in understanding of jet substructure during the LHC era.
- ◆ Jet substructure is an important tool to identify boosted objects at LHC.

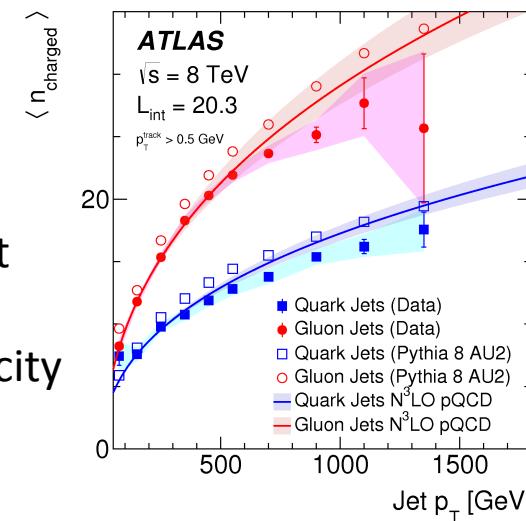
High p_T top or W/Z bosons decaying hadronically can be observed as large size jets.



arXiv:
1801.02052
Mass of
large-R jets
in ttbar
cross section
measurement

- ◆ Several observables are measured at LHC.
 - Jet mass, k_T splitting, jet charge, charged particle multiplicity.

Gluon/quark-initiated jets have different rapidity dependence.
 → Studies of charged particle multiplicity accesses to the origin of jets.



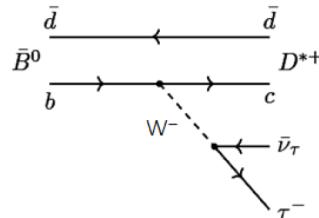
Are they interesting at EIC as well?

Leptoquark search

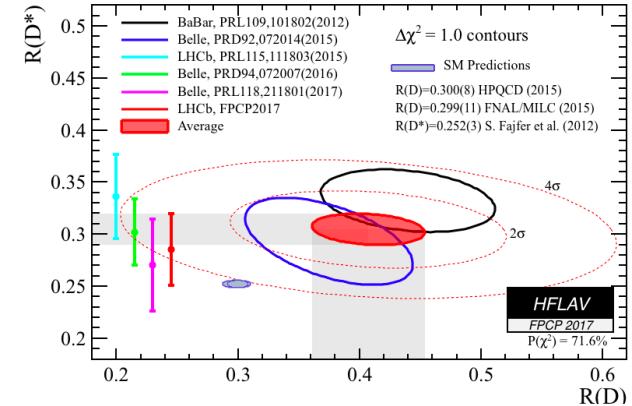
Particular attention on leptoquarks

Anomalies seen in B physics invoke a lot of interest on leptoquarks.

- ◆ Larger branching fraction of $B \rightarrow D^{(*)}\tau\nu_\tau$. ($\sim 4\sigma$)
 - Seen by Belle, Babar, LHCb.

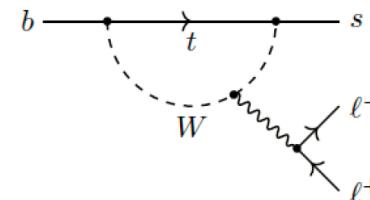


$$R_{D^{(*)}} = \frac{\text{Br}(B \rightarrow D^{(*)}\tau\nu_\tau)}{\text{Br}(B \rightarrow D^{(*)}l\nu_l)}$$

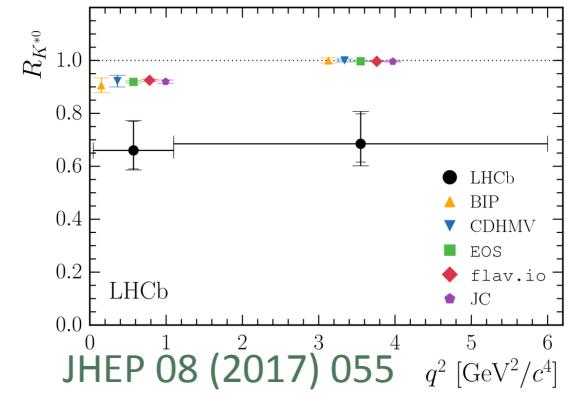


- ◆ Smaller branching fraction of $b \rightarrow s\mu^+\mu^-$ process.

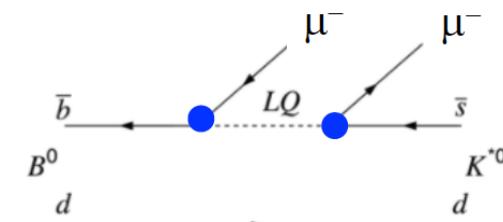
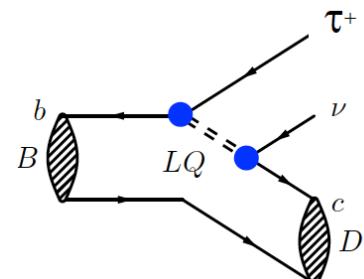
- LHCb driven.
- Smaller than $b \rightarrow se^+e^-$ ($\sim 2.5\sigma$)
- Analyses of decay angles show tensions. ($\sim 3.4\sigma$)



$$R_{K^{(*)}} = \frac{\text{Br}(B \rightarrow K^{(*)}\mu^+\mu^-)}{\text{Br}(B \rightarrow K^{(*)}e^+e^-)}$$



Leptoquarks can explain the both anomalies.



LHC Leptoquark searches

- ◆ Searches are done through LQ pair production or single production.
- ◆ Limits depend on branching ratio (β or $1-\beta$). (shown for specific β (1, 0, or 0.5))
- ◆ Single production has a dependence on the coupling λ .

CMS summary

$LQ \rightarrow$ 1st gen. 2nd. gen. 3rd gen. Full 2016 dataset

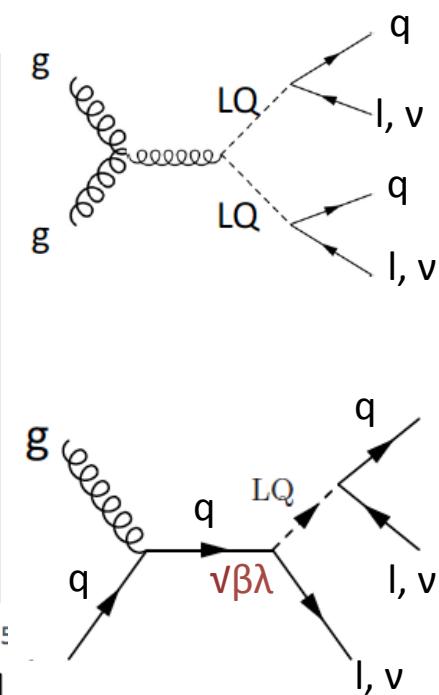
Scalar LQ



Vector LQ
(LQ model used: 1706.07641)



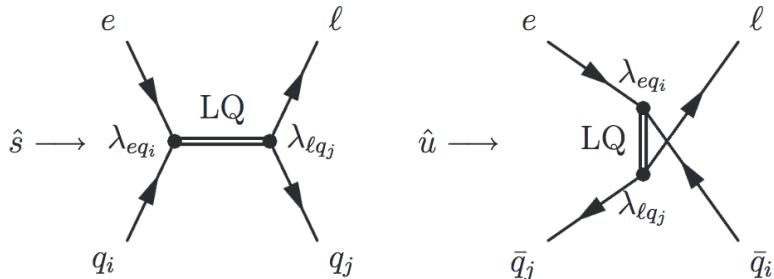
Y. Takahashi, Moriond2018



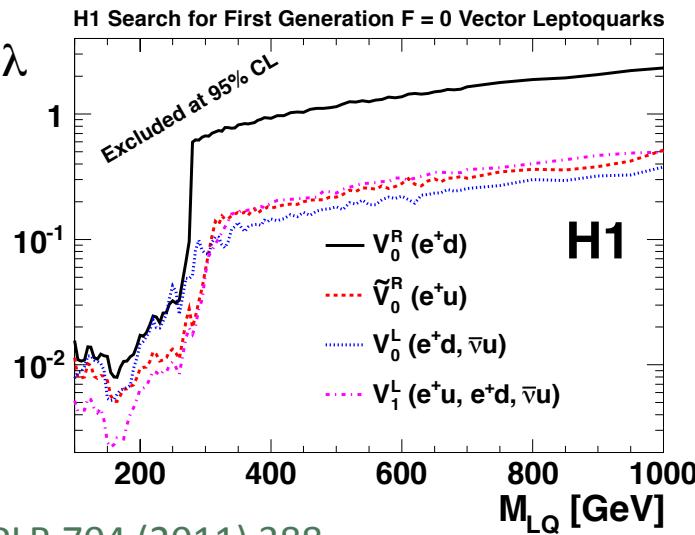
$M_{LQ} < \sim O(1) \text{ TeV}$
are excluded.

Leptoquark search at ep collider

14 categories of leptoquarks via s-channel or u-channel are looked for, in $ep \rightarrow lX$



Limits are set on $\frac{\lambda_{eq_i} \lambda_{lq_j}}{M_{\text{LQ}}^2}$



LQ type	J	F	Q	Production and decay modes	Coupling	β_ℓ
S_0^L	0	2	-1/3	$e_L^- u_L \rightarrow \begin{cases} \ell^- u \\ \nu_\ell d \end{cases}$	λ_L	1/2
S_0^R	0	2	-1/3	$e_R^- u_R \rightarrow \ell^- u$	λ_R	1
\tilde{S}_0^R	0	2	-4/3	$e_R^- d_R \rightarrow \ell^- d$	λ_R	1
S_1^L	0	2	-1/3	$e_L^- u_L \rightarrow \begin{cases} \ell^- u \\ \nu_\ell d \end{cases}$	$-\lambda_L$	1/2
			-4/3	$e_L^- d_L \rightarrow \ell^- d$	$-\sqrt{2}\lambda_L$	1
$V_{1/2}^L$	1	2	-4/3	$e_L^- d_R \rightarrow \ell^- d$	λ_L	1
$V_{1/2}^R$	1	2	-1/3	$e_R^- u_L \rightarrow \ell^- u$	λ_R	1
			-4/3	$e_R^- d_L \rightarrow \ell^- d$	λ_R	1
$\tilde{V}_{1/2}^L$	1	2	-1/3	$e_L^- u_R \rightarrow \ell^- u$	λ_L	1
V_0^L	1	0	+2/3	$e_R^+ d_L \rightarrow \begin{cases} \ell^+ d \\ \bar{\nu}_\ell u \end{cases}$	λ_L	1/2
V_0^R	1	0	+2/3	$e_L^+ d_R \rightarrow \ell^+ d$	λ_R	1
\tilde{V}_0^R	1	0	+5/3	$e_L^+ u_R \rightarrow \ell^+ u$	λ_R	1
V_1^L	1	0	+2/3	$e_R^+ d_L \rightarrow \begin{cases} \ell^+ d \\ \bar{\nu}_\ell u \end{cases}$	$-\lambda_L$	1/2
			+5/3	$e_R^+ u_L \rightarrow \ell^+ u$	$\sqrt{2}\lambda_L$	1
$S_{1/2}^L$	0	0	+5/3	$e_R^+ u_R \rightarrow \ell^+ u$	λ_L	1
$S_{1/2}^R$	0	0	+2/3	$e_L^+ d_L \rightarrow \ell^+ d$	$-\lambda_R$	1
			+5/3	$e_L^+ u_L \rightarrow \ell^+ u$	λ_R	1
$\tilde{S}_{1/2}^L$	0	0	+2/3	$e_R^+ d_R \rightarrow \ell^+ d$	λ_L	1

Charged lepton flavour violation (CLFV)

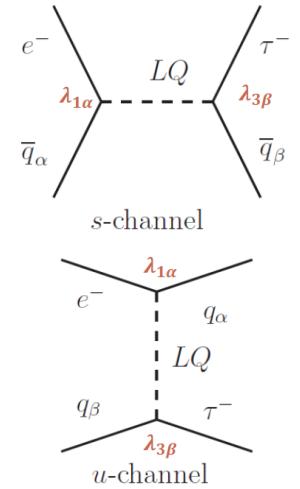
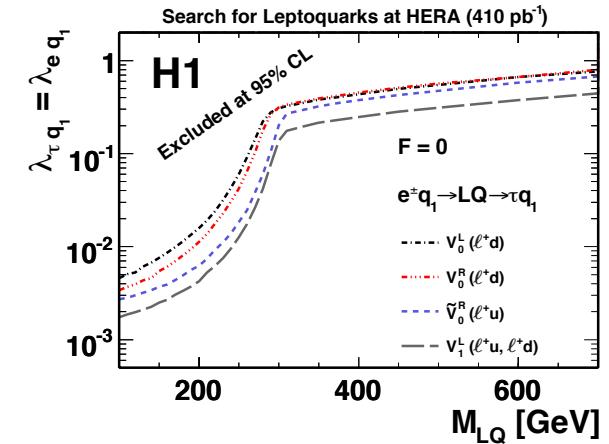
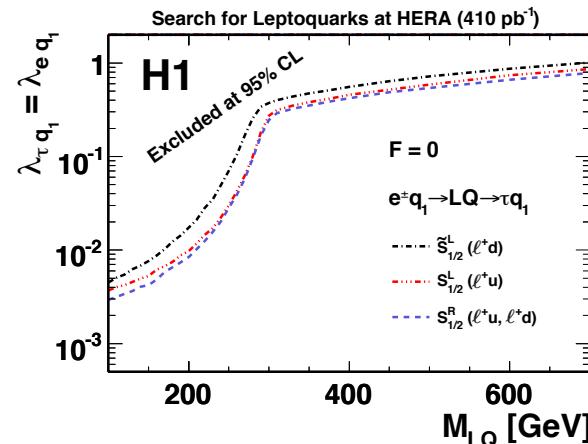
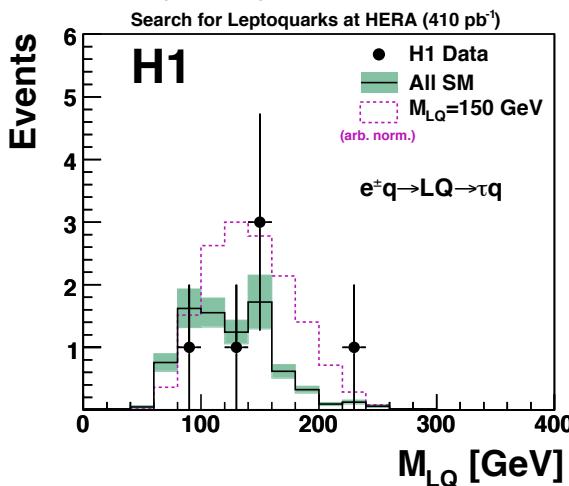
Neutrino oscillation means lepton flavour violations in the neutrinos.
 → Why not in the charged lepton?

ep colliders can search for CLFV (1,3) in DIS from $ep \rightarrow \tau X$

- Much less background compared to $ep \rightarrow eX$
- Less constraint compared to CLFV (1,2). cf $\mu \rightarrow e\gamma$

$ep \rightarrow \tau X$ can be interpreted as a process via leptoquarks.

PLB 701 (2010) 20



Sensitivities at EIC vs HERA

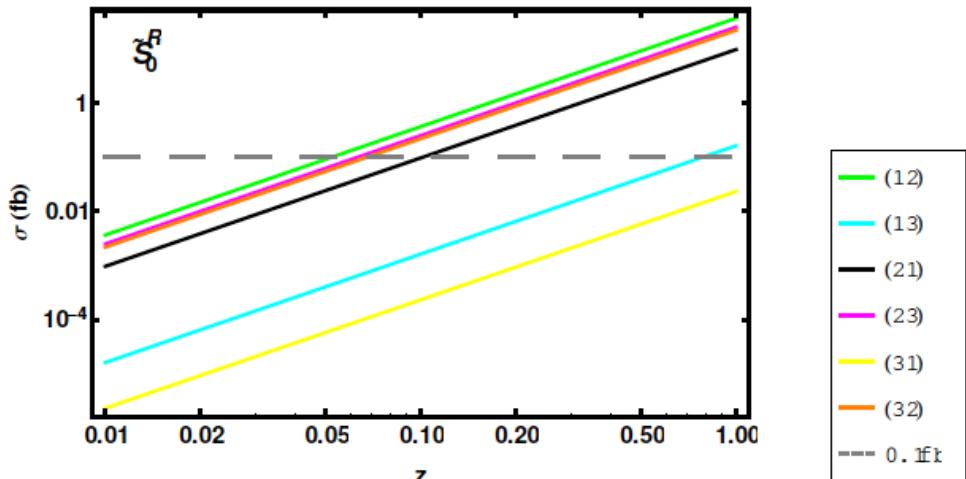
EIC@ $\sqrt{s}=90\text{GeV}$, compared to HERA*.

M. Gonderinger, M. J. Ramsey-Musolf
JHEP 05 (2012) 047

*ZEUS EPJC 44 (2005) 463,
H1 EPJC 52 (2007) 833

$$z = \frac{(\lambda_{1\alpha}\lambda_{3\beta})/M_{\text{LQ}}^2}{[(\lambda_{1\alpha}\lambda_{3\beta})/M_{\text{LQ}}^2]_{\text{HERA limit}}}$$

Assuming the same acceptance and τ tagging efficiency as HERA.



- ◆ With 10 fb^{-1} data, EIC can improve HERA limits, which are stringent for (2,3) and (3,2) in case of \tilde{S}_0^R
 - Higher \sqrt{s} gives higher sensitivities.
 - Larger statistics will give further improvement.
 - Polarization of e^-/e^+ beams can increase or suppress the cross section.
→ Distinguish L vs R.

EIC can take a role in leptoquark searches

Summary

- ◆ LHC looks for new physics using pp collisions at $\sqrt{s} = 13$ TeV. LHC physics require:
 - Better determination of the proton parton distribution functions.
 - Good description of jet production.
- ◆ EIC can improve the determination of the parton distribution functions.
 - High- y measurements are very important.
 - F_L can be measured.
 - Require good measurement of hadrons in the forward region and electrons in the rear side.
- ◆ Jet physics at EIC could be also interesting.
- ◆ EIC can play a role in the search of leptoquarks, which get particular attention due to the anomalies in B physics.

And a remark...

As you may notice, there are a lot of room for sensitivity studies.

Rik wrote me:

“these kind of HEP oriented studies are somewhat neglected at the EIC”

- A lot of interest for the EIC from the nuclear physics community.
- Less discussion in the HEP community.

“this is a machine that will run likely concurrently with HL-LHC”

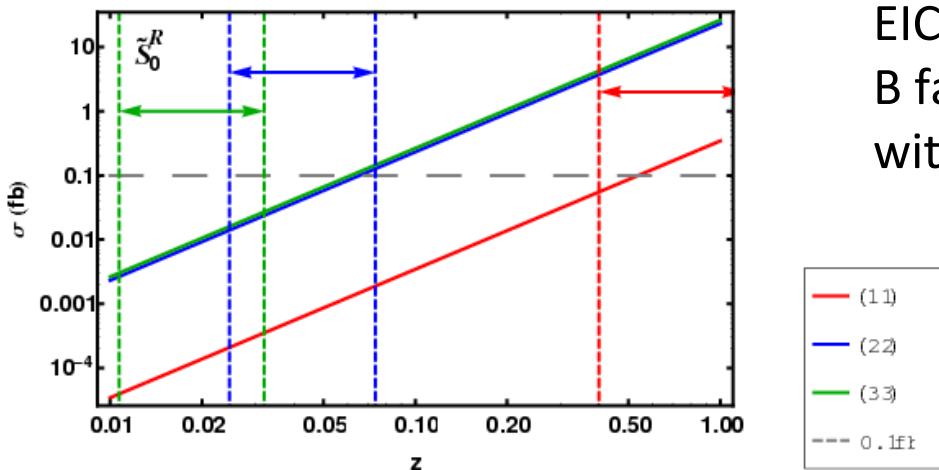
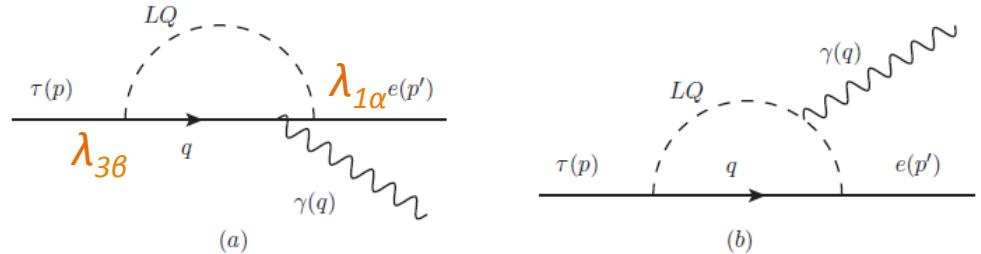
→ Good to consider the HEP-oriented possibilities at EIC.

CLFV EIC vs B factory

- ◆ Rare decay $\tau \rightarrow e\gamma$ at B factories* can set limits for $\alpha = \beta$

*Babar PRL104(2010) 021802
Belle PLB 660 (2008) 154

M. Gonderinger, M. J. Ramsey-Musolf
JHEP 05 (2012) 047



EIC could compete with previous B factories for the 1st generation quarks with large statistics.
Not sure wrt Belle II.

Where HERA ep has sensitivities:

PLB701(2010)20

$ep \rightarrow \tau X$		H1				$F = 0$	
Upper exclusion limits on $\lambda_{eq_i} \lambda_{\tau q_j} / m_{LQ}^2$ (TeV $^{-2}$) for lepton flavour violating leptoquarks at 95% CL							
$q_i q_j$	$S_{1/2}^L$ $\ell^- \bar{U}$ $\ell^+ U$	$S_{1/2}^R$ $\ell^- \bar{U}, \ell^- \bar{D}$ $\ell^+ U, \ell^+ D$	$\tilde{S}_{1/2}^L$ $\ell^- \bar{D}$ $\ell^+ D$	V_0^L $\ell^- \bar{D}$ $\ell^+ D$	V_0^R $\ell^- \bar{D}$ $\ell^+ D$	\tilde{V}_0^R $\ell^- \bar{U}$ $\ell^+ U$	V_1^L $\ell^- \bar{U}, \ell^- \bar{D}$ $\ell^+ U, \ell^+ D$
1 1	$\tau \rightarrow \pi e$ 0.06 1.4	$\tau \rightarrow \pi e$ 0.03 1.2	$\tau \rightarrow \pi e$ 0.06 2.2	$\tau \rightarrow \pi e$ 0.03 1.2	$\tau \rightarrow \pi e$ 0.03 1.3	$\tau \rightarrow \pi e$ 0.03 0.9	$\tau \rightarrow \pi e$ 0.005 0.4
1 2		$\tau \rightarrow K e$ 0.04 1.5	$K \rightarrow \pi \nu \bar{\nu}$ 5.8×10^{-4} 2.2	$\tau \rightarrow K e$ 0.02 1.5	$\tau \rightarrow K e$ 0.02 1.6	$\tau \rightarrow K e$ 1.5 $\times 10^{-4}$ 1.2	$K \rightarrow \pi \nu \bar{\nu}$ 1.5×10^{-4} 0.5
1 3	*	$B \rightarrow \tau \bar{e}$ 0.07 2.2	$B \rightarrow \tau \bar{e}$ 0.07 2.2	$B \rightarrow \tau \bar{e}$ 0.03 1.8	$B \rightarrow \tau \bar{e}$ 0.03 1.8	*	$B \rightarrow \tau \bar{e}$ 0.03 1.8
2 1		$\tau \rightarrow K e$ 0.04 3.4	$K \rightarrow \pi \nu \bar{\nu}$ 5.8×10^{-4} 2.8	$\tau \rightarrow K e$ 0.02 3.9	$\tau \rightarrow K e$ 0.02 1.5	$\tau \rightarrow K e$ 0.02 1.6	$K \rightarrow \pi \nu \bar{\nu}$ 1.5×10^{-4} 1.2
2 2	$\tau \rightarrow 3e$ 0.6 6.4	$\tau \rightarrow 3e$ 0.9 4.2	$\tau \rightarrow 3e$ 1.8 5.0	$\tau \rightarrow 3e$ 0.9 2.7	$\tau \rightarrow 3e$ 0.9 2.8	$\tau \rightarrow 3e$ 0.3 3.5	$\tau \rightarrow 3e$ 0.2 1.4
2 3	*	$B \rightarrow \tau \bar{e} X$ 14.0 5.8	$B \rightarrow \tau \bar{e} X$ 14.0 5.6	$B \rightarrow \tau \bar{e} X$ 7.2 3.6	$B \rightarrow \tau \bar{e} X$ 7.2 4.0	*	$B \rightarrow \tau \bar{e} X$ 7.2 3.6
3 1	*	$B \rightarrow \tau \bar{e}$ 0.07 5.3	$B \rightarrow \tau \bar{e}$ 0.07 4.8	V_{ub} 0.14 1.5	$B \rightarrow \tau \bar{e}$ 0.03 1.7	*	V_{ub} 0.14 1.5
3 2	*	$B \rightarrow \tau \bar{e} X$ 14.0 7.9	$B \rightarrow \tau \bar{e} X$ 14.0 7.6	$B \rightarrow \tau \bar{e} X$ 7.2 2.9	$B \rightarrow \tau \bar{e} X$ 7.2 3.1	*	$B \rightarrow \tau \bar{e} X$ 7.2 2.9
3 3	*	$\tau \rightarrow 3e$ 0.9 10.1	$\tau \rightarrow 3e$ 1.8 9.1	$\tau \rightarrow 3e$ 0.9 4.7	$\tau \rightarrow 3e$ 0.9 4.9	*	$\tau \rightarrow 3e$ 0.2 4.7

$ep \rightarrow \tau X$		H1				$F = 2$	
Upper exclusion limits on $\lambda_{eq_i} \lambda_{\tau q_j} / m_{LQ}^2$ (TeV $^{-2}$) for lepton flavour violating leptoquarks at 95% CL							
$q_i q_j$	S_0^L $\ell^- U$ $\ell^+ \bar{U}$	S_0^R $\ell^- U$ $\ell^+ \bar{U}$	\tilde{S}_0^R $\ell^- D$ $\ell^+ \bar{D}$	S_1^L $\ell^- U, \ell^- D$ $\ell^+ \bar{U}, \ell^+ \bar{D}$	$V_{1/2}^L$ $\ell^- D$ $\ell^+ \bar{D}$	$V_{1/2}^R$ $\ell^- U, \ell^- D$ $\ell^+ \bar{U}, \ell^+ \bar{D}$	$\tilde{V}_{1/2}^L$ $\ell^- U$ $\ell^+ \bar{U}$
1 1	G_F 0.3 1.6	$\tau \rightarrow \pi e$ 0.06 1.8	$\tau \rightarrow \pi e$ 0.06 2.6	$\tau \rightarrow \pi e$ 0.01 1.0	$\tau \rightarrow \pi e$ 0.03 1.1	$\tau \rightarrow \pi e$ 0.01 0.7	$\tau \rightarrow \pi e$ 0.03 0.8
1 2	$K \rightarrow \pi \nu \bar{\nu}$ 5.8×10^{-4} 1.9	$\tau \rightarrow K e$ 0.04 2.1	$K \rightarrow \pi \nu \bar{\nu}$ 2.9×10^{-4} 2.9	$K \rightarrow \pi \nu \bar{\nu}$ 2.9×10^{-4} 1.1	$K \rightarrow \pi \nu \bar{\nu}$ 2.9×10^{-4} 1.9	$\tau \rightarrow K e$ 0.02 1.3	$\tau \rightarrow K e$ 0.02 1.5
1 3	*	$B \rightarrow \tau \bar{e}$ 0.07 3.0	*	V_{ub} 0.07 1.3	$B \rightarrow \tau \bar{e}$ 0.3 2.2	$B \rightarrow \tau \bar{e}$ 0.03 2.4	*
2 1	$K \rightarrow \pi \nu \bar{\nu}$ 5.8×10^{-4} 2.7		$\tau \rightarrow K e$ 0.04 3.5	$K \rightarrow \pi \nu \bar{\nu}$ 2.9×10^{-4} 1.4	$K \rightarrow \pi \nu \bar{\nu}$ 2.9×10^{-4} 1.2	$\tau \rightarrow K e$ 0.02 0.7	$\tau \rightarrow K e$ 0.02 0.9
2 2	$\tau \rightarrow 3e$ 0.6 6.3	$\tau \rightarrow 3e$ 0.6 6.8	$\tau \rightarrow 3e$ 1.8 5.4	$\tau \rightarrow 3e$ 1.5 2.3	$\tau \rightarrow 3e$ 0.9 2.7	$\tau \rightarrow 3e$ 0.5 2.2	$\tau \rightarrow 3e$ 0.3 3.4
2 3	*		*	$B \rightarrow \tau \bar{e} X$ 14.0 5.8	$B \rightarrow \tau \bar{e} X$ 7.2 2.7	$B \rightarrow \tau \bar{e} X$ 7.2 3.6	*
3 1	*	*	*	$B \rightarrow \tau \bar{e}$ 0.07 4.0	$B \rightarrow \tau \bar{e}$ 0.03 2.0	$B \rightarrow \tau \bar{e}$ 0.03 1.2	*
3 2	*	*	*	$B \rightarrow \tau \bar{e} X$ 14.0 7.9	$B \rightarrow \tau \bar{e} X$ 7.2 3.7	$B \rightarrow \tau \bar{e} X$ 7.2 2.9	*
3 3	*	*	*	$\tau \rightarrow 3e$ 1.8 10.1	$\tau \rightarrow 3e$ 1.5 4.6	$\tau \rightarrow 3e$ 0.9 4.7	*