

# ***BigRIPS as a high resolution spectrometer for pionic atoms***

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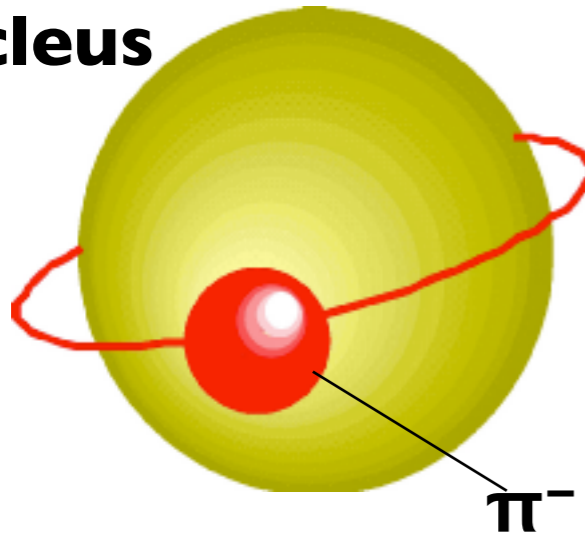
**for Pionic Atom Factory Project**

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R.S. Hayano, N. Inabe<sup>B</sup>, K. Itahashi<sup>B</sup>, S. Itoh, D. Kameda<sup>B</sup>, K. Okochi,  
T. Kubo<sup>B</sup>, H. Matsubara<sup>B</sup>, S. Michimasa<sup>B</sup>, K. Miki<sup>E</sup>, H. Miya, M. Nakamura<sup>B</sup>,  
Y. Murakami, N. Nakatsuka<sup>C</sup>, S. Noji<sup>F</sup>, S. Ota, H. Suzuki<sup>B</sup>, K. Suzuki<sup>G</sup>, M.  
Takagi, H. Takeda<sup>B</sup>, Y. K. Tanaka, K. Todoroki, K. Tsukada<sup>H</sup>, T. Uesaka<sup>B</sup>, Y.  
Watanabe, H. Weick<sup>D</sup>, H. Yamada, and K. Yoshida<sup>B</sup>

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GSI<sup>D</sup>, Osaka Univ.<sup>E</sup>, Michigan State Univ.<sup>F</sup>, SMI<sup>G</sup>, Tohoku Univ.<sup>H</sup>**

# deeply-bound Pionic Atom

**Nucleus**

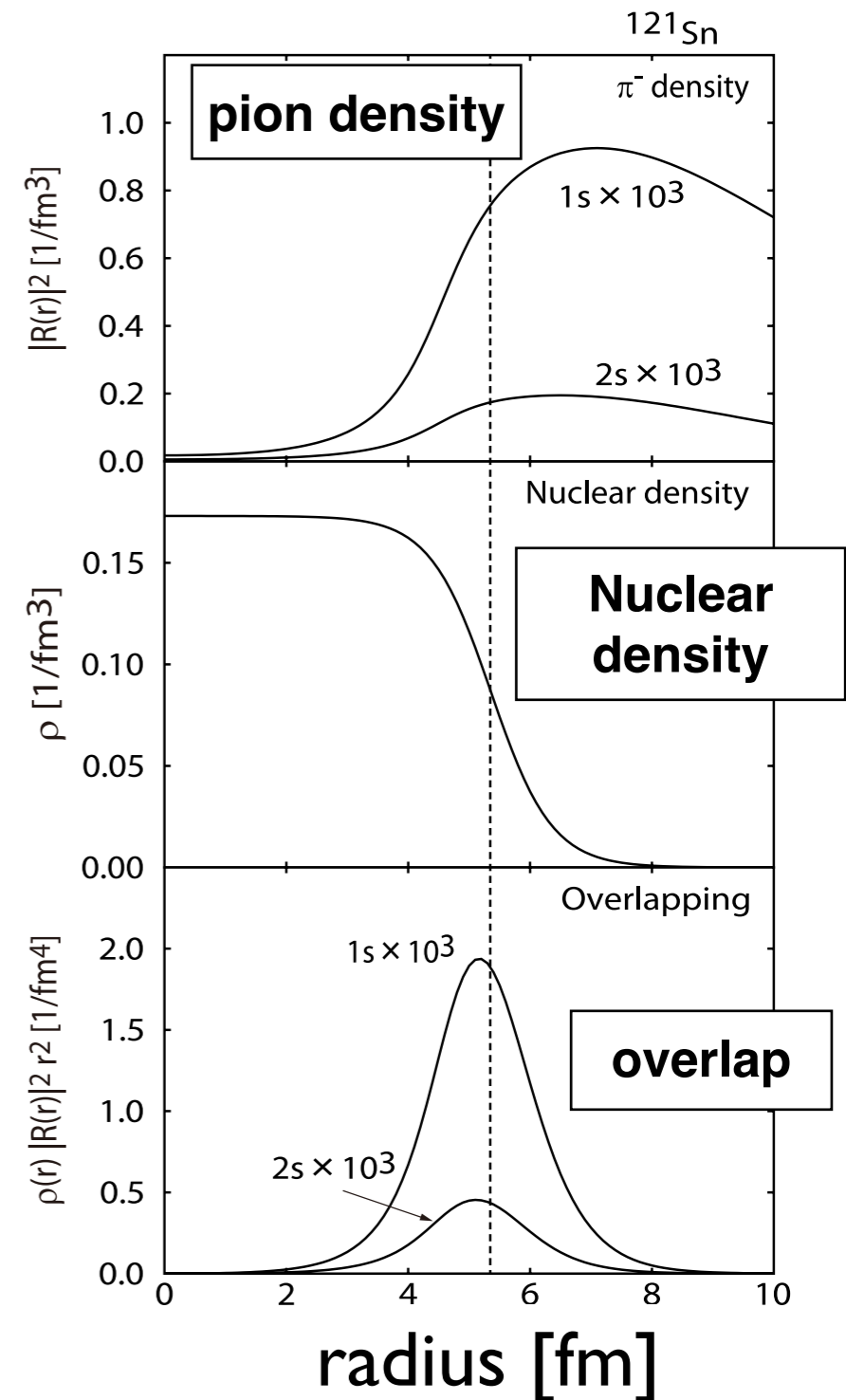


Coulomb  
+  
Strong

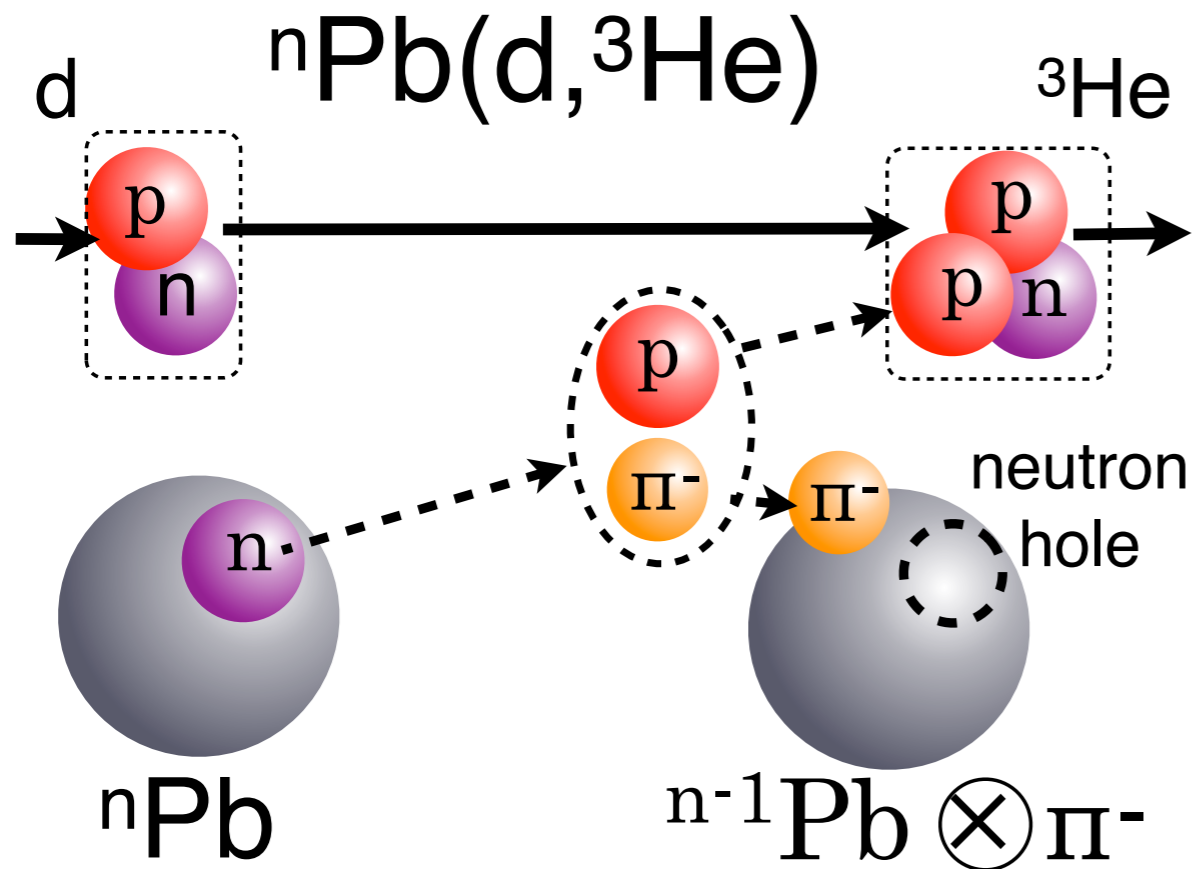
Large overlap between  
pion and nucleus

→ probe for QCD in finite density

density [fm<sup>-3</sup>]

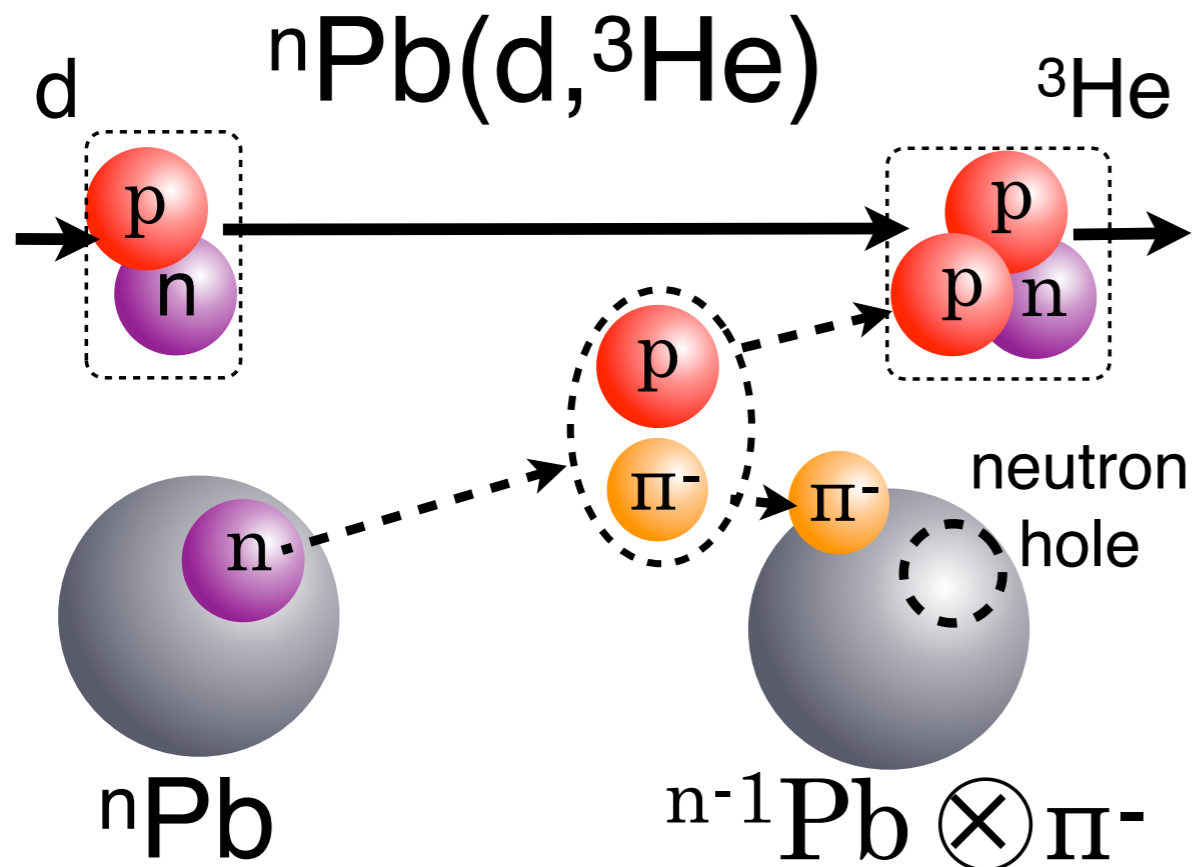


# $(d, ^3\text{He})$ reaction



Missing mass spectroscopy

# $(d, {}^3\text{He})$ reaction



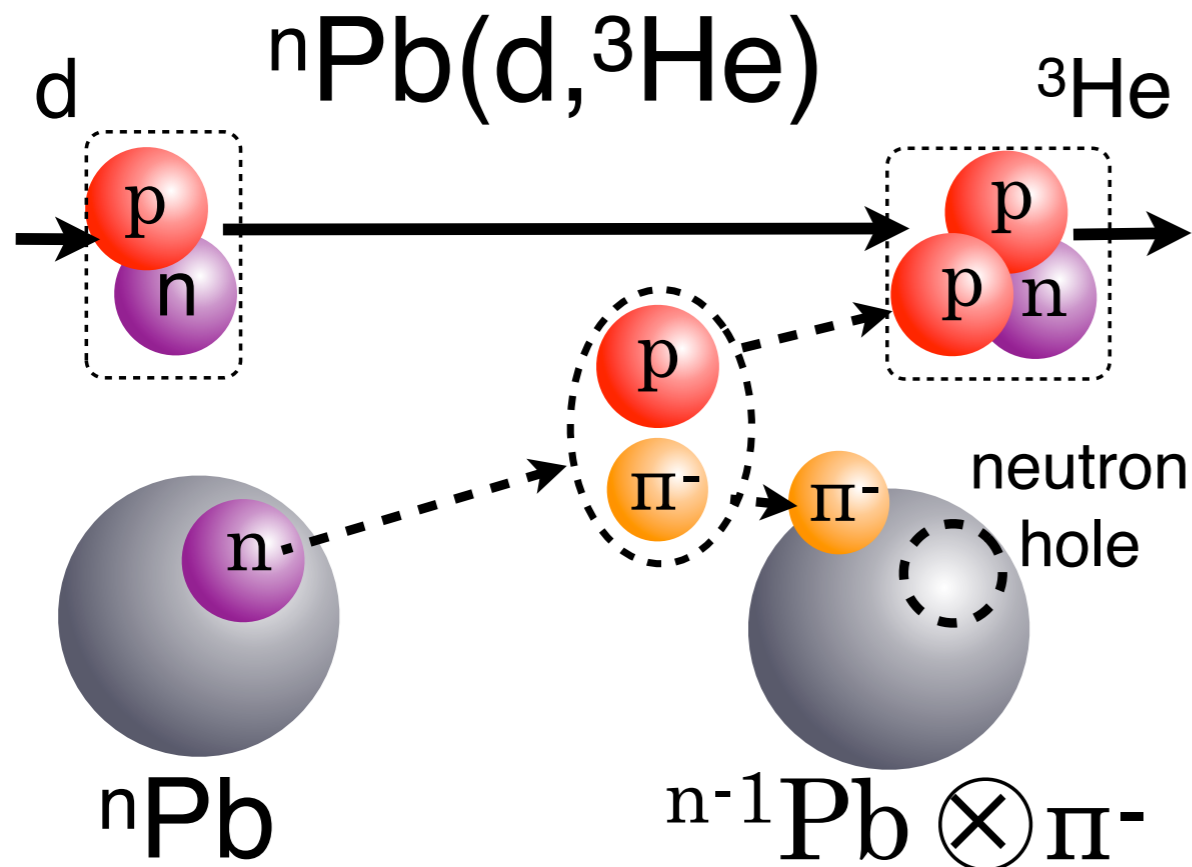
2 body kinematics

→ mass of the pionic atom  
can be calculated from **Q-value**

Calculated from  $E_d$ ,  $E_{{}^3\text{He}}$

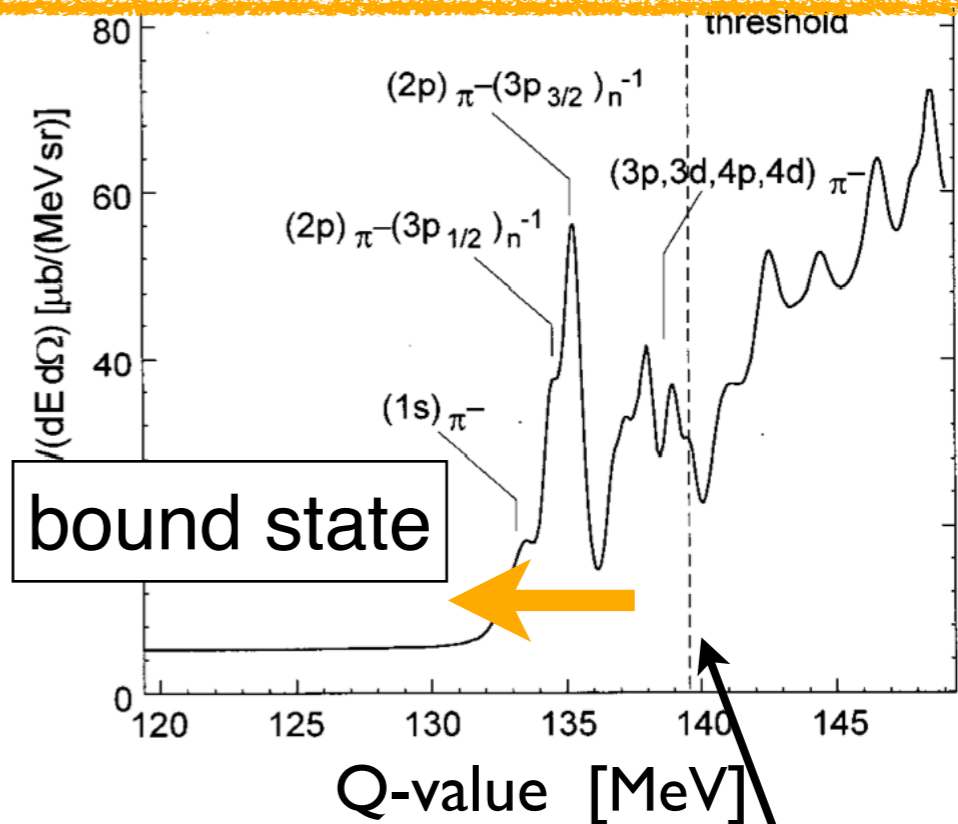
Missing mass spectroscopy

# $(d, ^3\text{He})$ reaction



Missing mass spectroscopy

Theoretical spectrum pionic  $\text{Pb}^{207}$   
couple of pion and neutron hole state

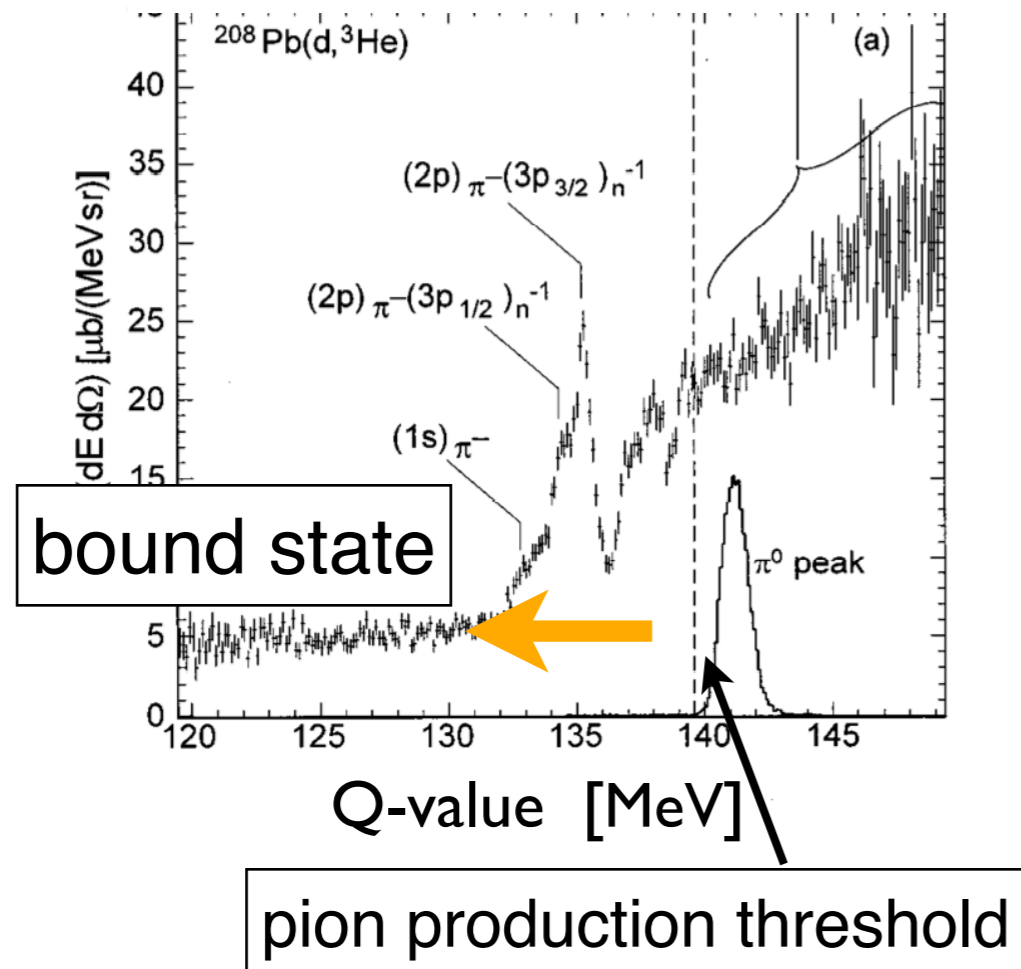


pion production threshold

S. Hirenzaki, H. Toki, T. Yamazaki,  
Phys. Rev. C44 (1991) 2472

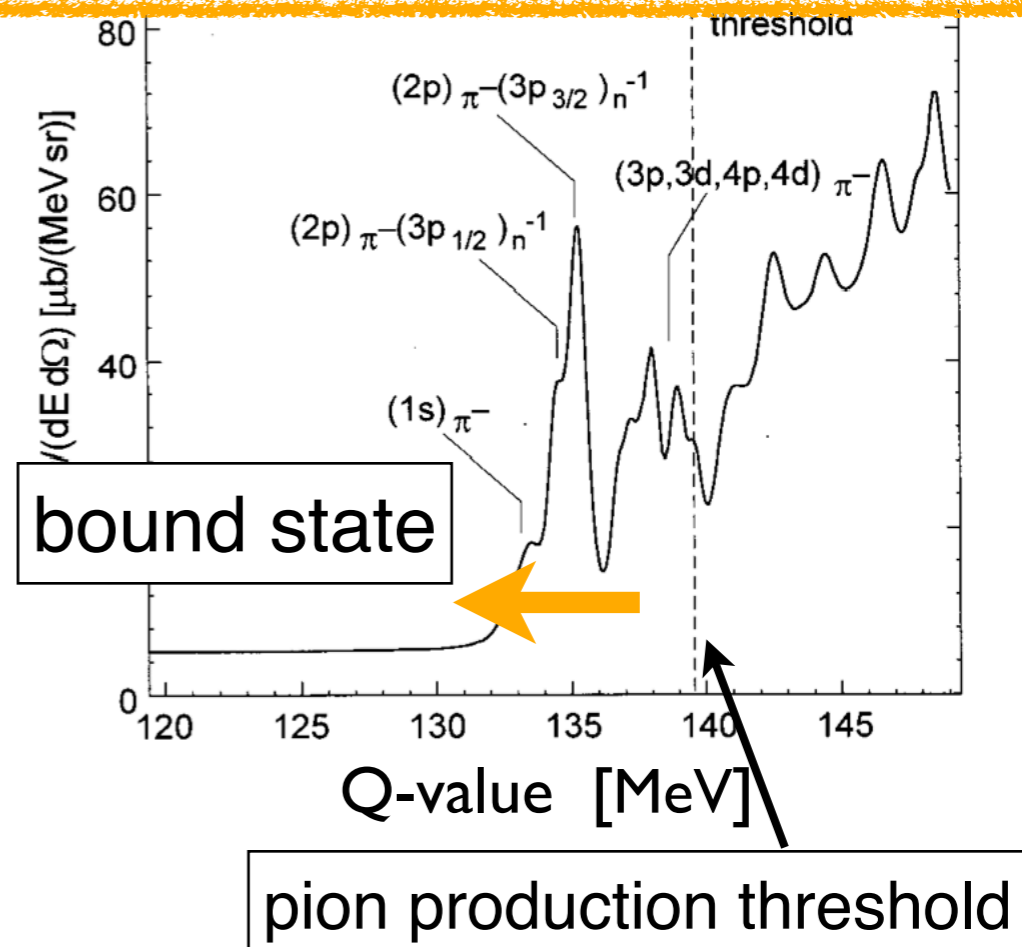
# $(d, ^3\text{He})$ reaction

experimental spectrum  
for pionic  $\text{Pb}^{207}$  @GSI



K. Itahashi, et al.,  
Phys. Rev. C62 (2000) 025202

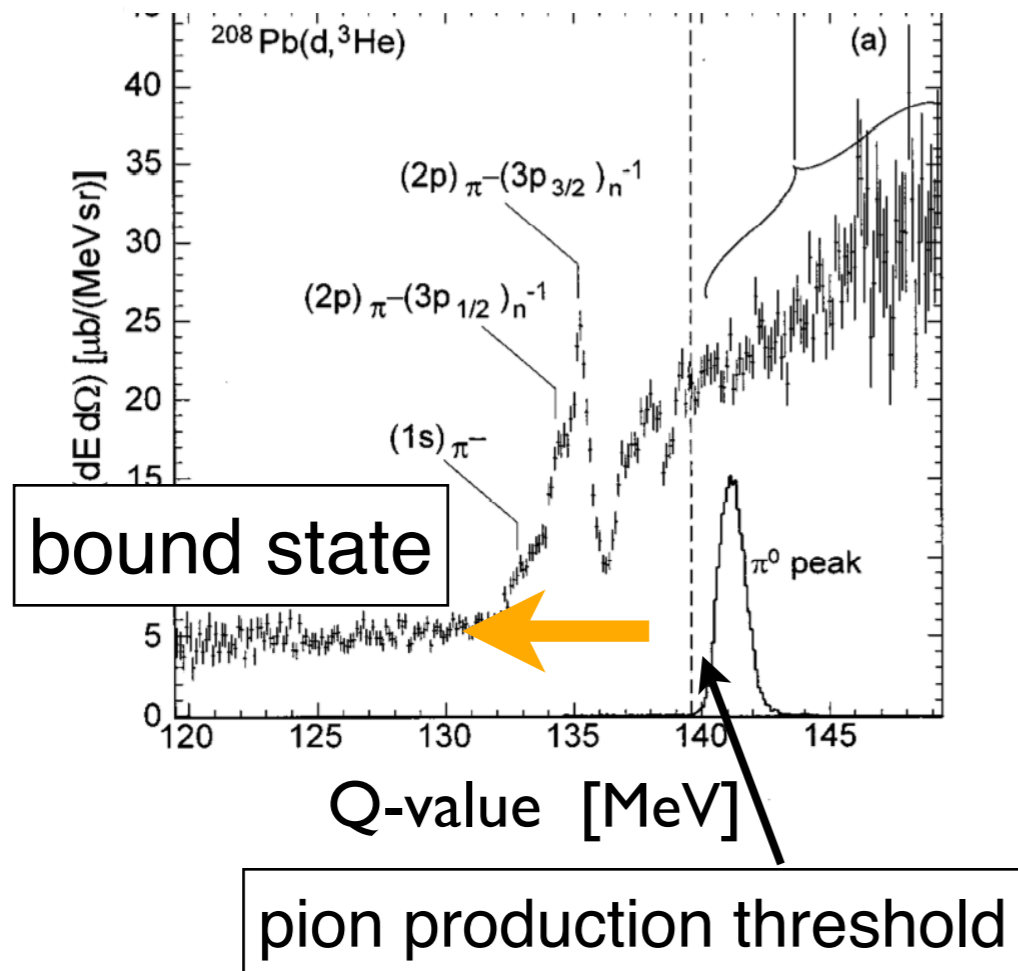
Theoretical spectrum pionic  $\text{Pb}^{207}$   
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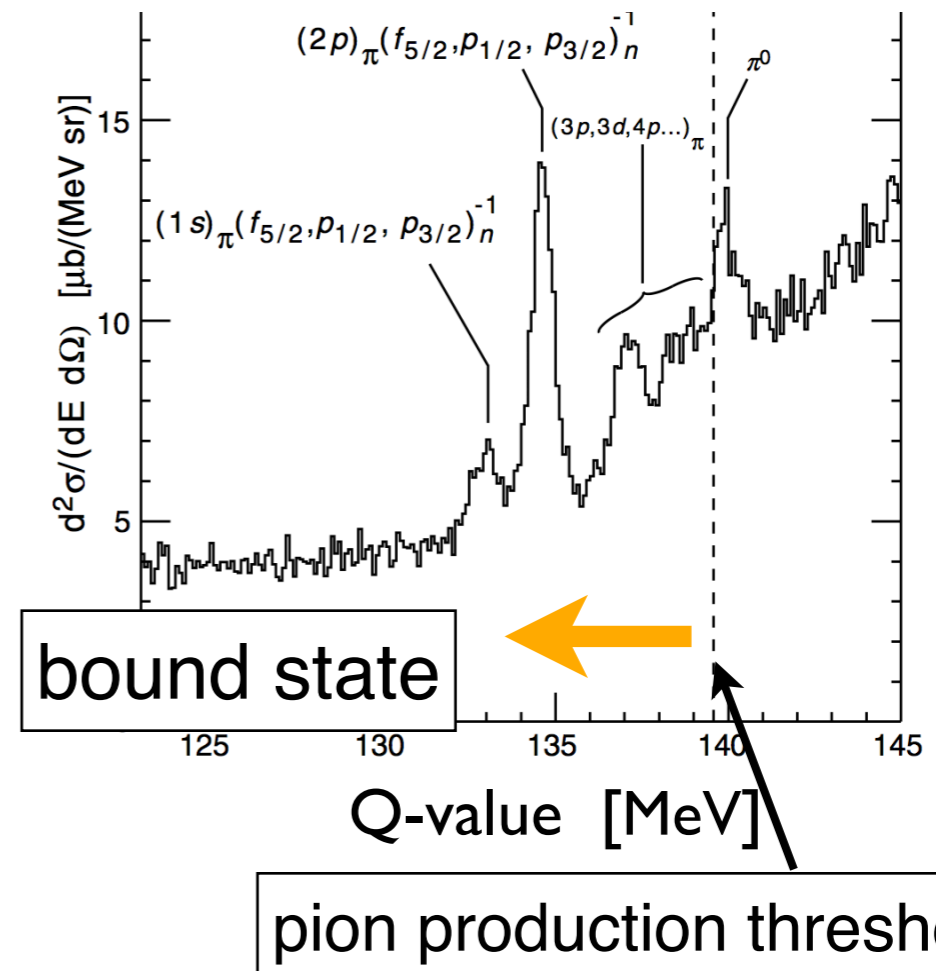
# $(d, {}^3\text{He})$ reaction

experimental spectrum  
for pionic  $\text{Pb}^{207}$  @GSI



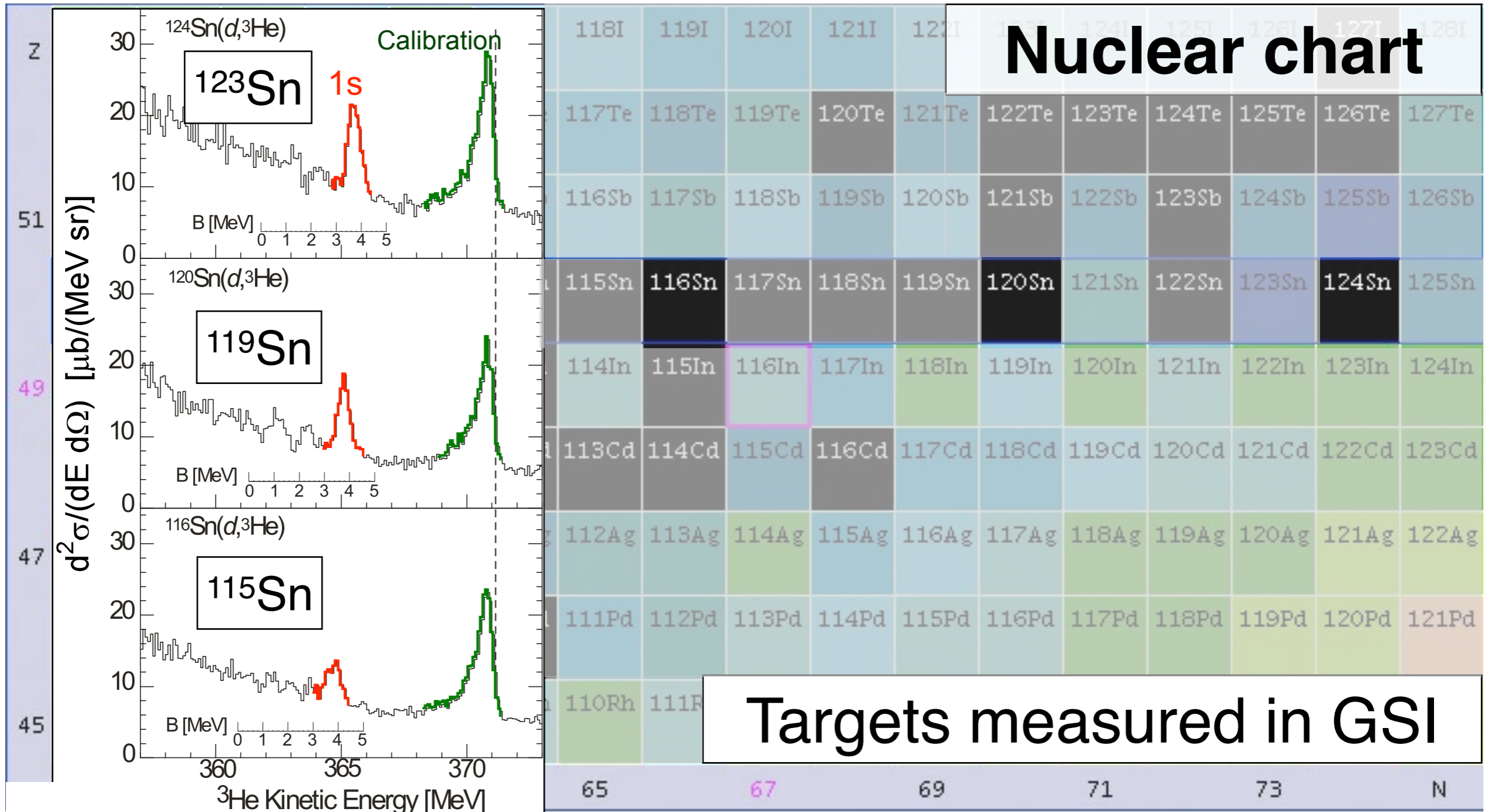
K. Itahashi, et al.,  
Phys. Rev. C62 (2000) 025202

experimental spectrum  
for pionic  $\text{Pb}^{205}$  @GSI



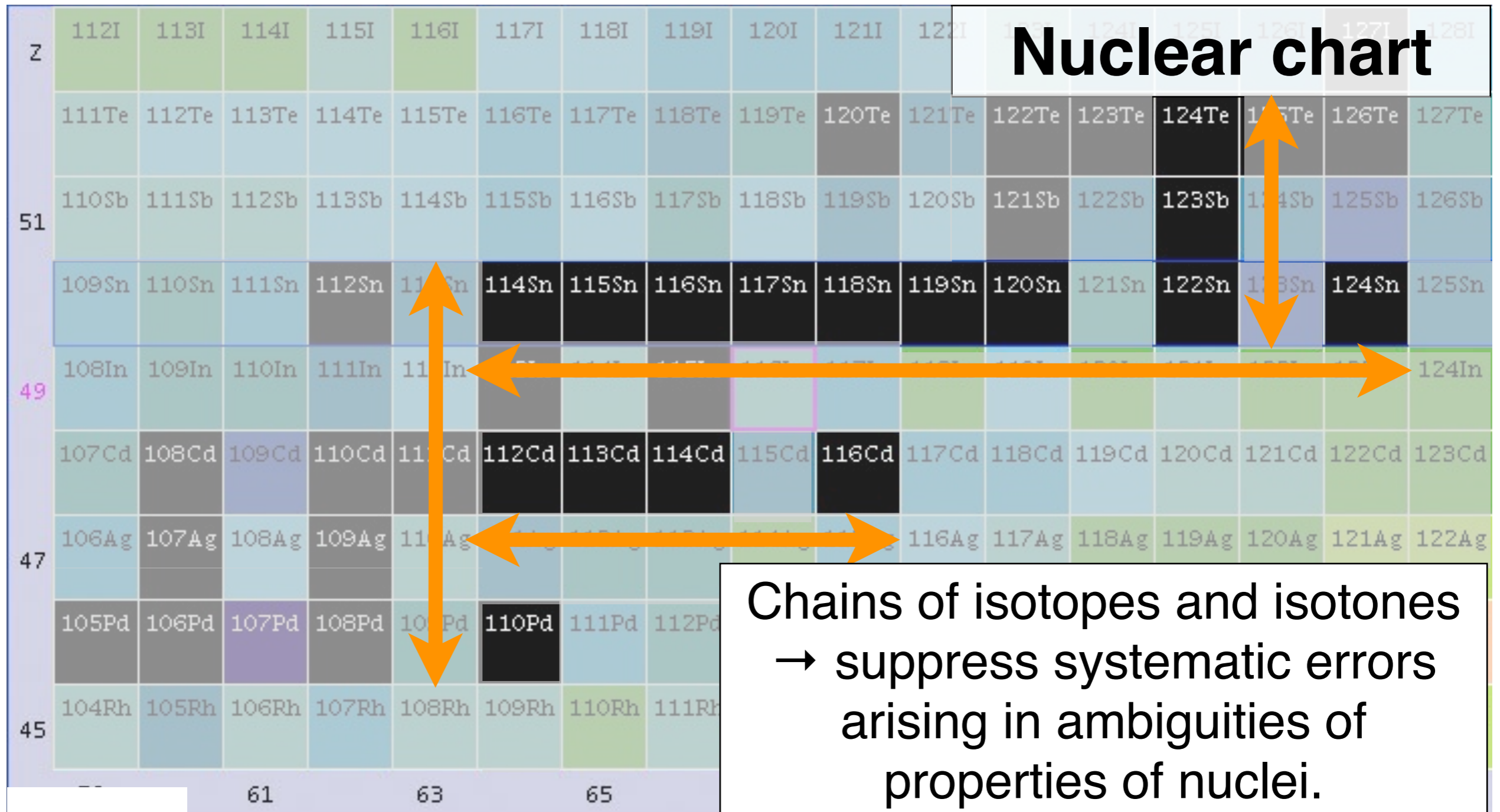
S. Hirenzaki, H. Toki, T. Yamazaki,  
Phys. Rev. C44 (1991) 2472

# The experiment at GSI





# Spectroscopy of Pionic Atom at RIBF



# Comparison with GSI

	GSI	RIBF	
intensity	$\sim 10^{11}/\text{spill}$	$\sim 10^{12}/\text{s}$	$\times 50$
Target	20 mg/cm <sup>2</sup>	10 mg/cm <sup>2</sup>	$\times 0.5$
angular acceptance	$\sim 10$ mrad	40 / 60 mrad	$\times 20$
$\Delta p_d / p_d$ (FWHM)	0.03%	0.1%	$\times 3$
resolution (FWHM)	400 keV	$\sim 850$ keV	

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intensity	$\sim 10^{11}/\text{spill}$	$\sim 10^{12}/\text{s}$	<b>x50</b>
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# Comparison with GSI

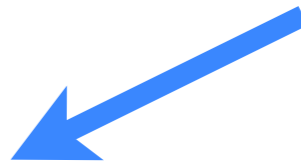
	GSI	RIBF	
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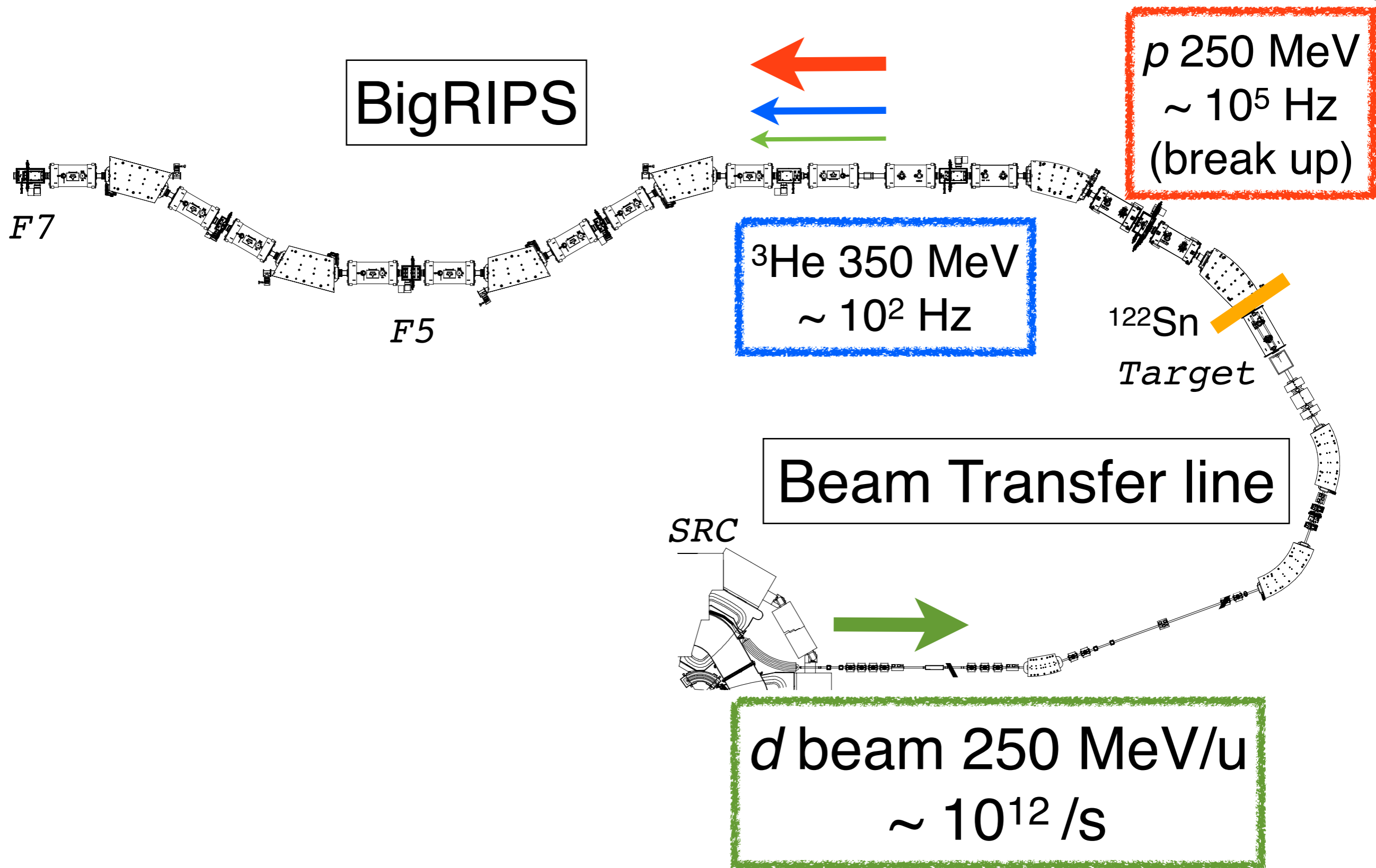


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$\Delta p_d / p_d$ (FWHM)	0.03%	0.1%	$\times 3$
resolution (FWHM)	400 keV	<b>200~300 keV</b>	factor 1.3 ~ 2

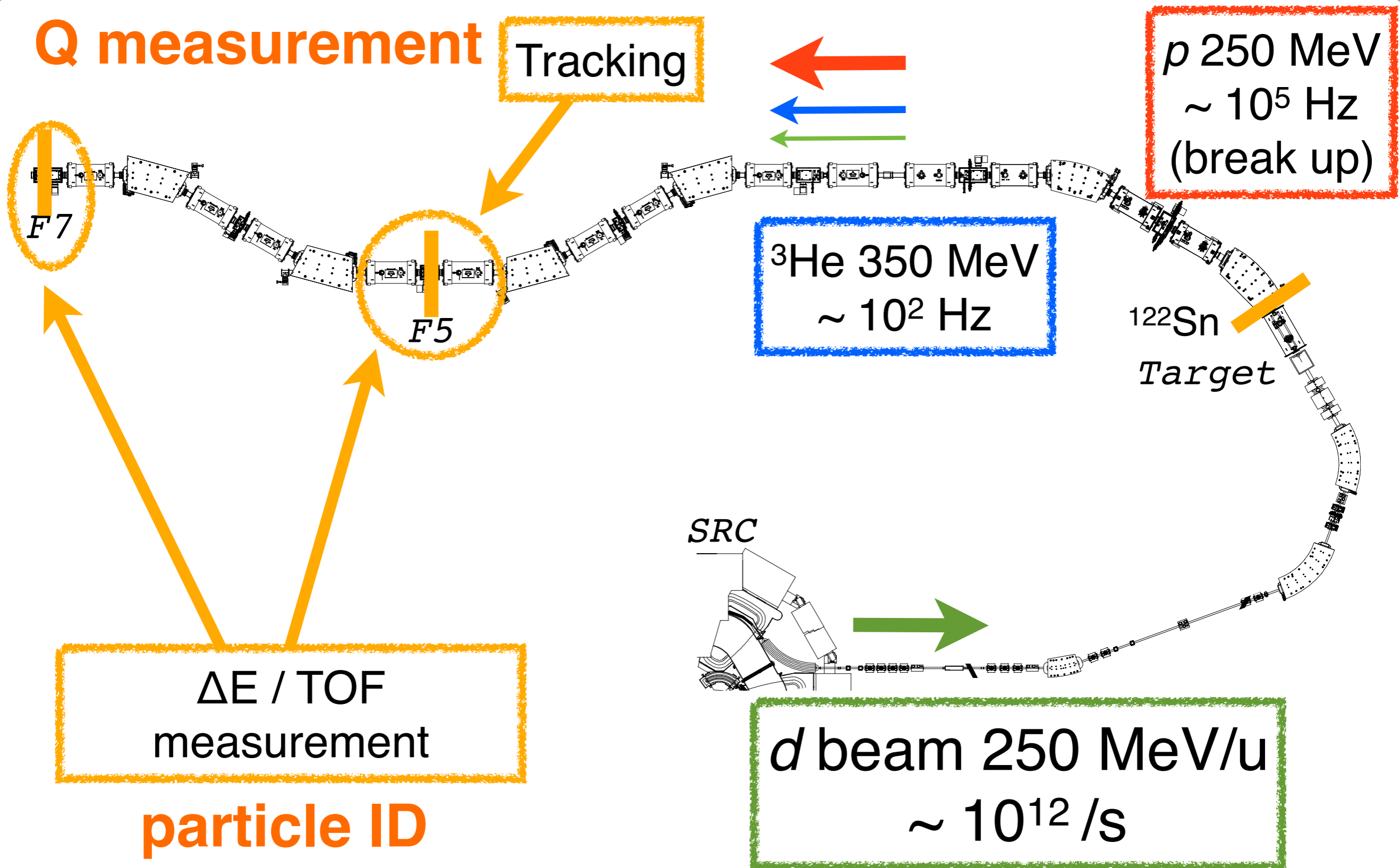
eliminate the effect of  $\Delta p_d / p_d$   
using dispersion matching

# Experimental Setup





# Experimental Setup



# Dispersion Matching

Eliminate contribution of beam momentum spread  
to the resolution

$$\begin{array}{c} \left( \begin{array}{c} x_{fp} \\ \theta_{fp} \\ \delta p_{fp} \end{array} \right) \end{array} = \begin{array}{c} \boxed{\begin{array}{c} \text{Spectrometer} \\ \text{(BigRIPS)} \end{array}} \\ \left( \begin{array}{ccc} S_{11} & S_{12} & S_{16} \\ S_{21} & S_{22} & S_{26} \\ 0 & 0 & 1 \end{array} \right) \end{array} \begin{array}{c} \boxed{\text{reaction}} \\ \left( \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & C \end{array} \right) \end{array} \begin{array}{c} \boxed{\begin{array}{c} \text{Analyzer} \\ \text{(Beam Transfer Line)} \end{array}} \\ \left( \begin{array}{ccc} A_{11} & A_{12} & A_{16} \\ A_{21} & A_{22} & A_{26} \\ 0 & 0 & 1 \end{array} \right) \end{array} \begin{array}{c} \left( \begin{array}{c} x_0 \\ \theta_0 \\ \delta p_0 \end{array} \right) \end{array}$$

\*C: kinematical factor = 1.31

$$\begin{aligned}
 x_{fp} &= (S_{11}A_{11} + S_{12}A_{21})x_0 \\
 &+ (S_{11}A_{12} + S_{12}A_{22})\theta_0 \\
 &+ \underline{(S_{11}A_{16} + S_{12}A_{26} + CS_{16})\delta p_0}
 \end{aligned}$$

# Dispersion Matching

Eliminate contribution of beam momentum spread to the resolution

$$\begin{array}{c}
 \begin{array}{|c|} \hline \text{Spectrometer} \\ \hline \text{(BigRIPS)} \\ \hline \end{array}
 \end{array}
 \begin{array}{c}
 \begin{array}{|c|} \hline \text{reaction} \\ \hline \end{array}
 \end{array}
 \begin{array}{c}
 \begin{array}{|c|} \hline \text{Analyzer} \\ \hline \text{(Beam Transfer Line)} \\ \hline \end{array}
 \end{array}
 \begin{array}{c}
 \begin{pmatrix} x_{fp} \\ \theta_{fp} \\ \delta p_{fp} \end{pmatrix} = \begin{pmatrix} S_{11} & S_{12} & S_{16} \\ S_{21} & S_{22} & S_{26} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & C \end{pmatrix} \begin{pmatrix} A_{11} & A_{12} & A_{16} \\ A_{21} & A_{22} & A_{26} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x_0 \\ \theta_0 \\ \delta p_0 \end{pmatrix}
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 x_{fp} = & (S_{11}A_{11} + S_{12}A_{21})x_0 \\
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 \end{aligned}$$

→ 0 by focusing

# Dispersion Matching

Eliminate contribution of beam momentum spread to the resolution

$$\begin{pmatrix} x_{fp} \\ \theta_{fp} \\ \delta p_{fp} \end{pmatrix} = \begin{pmatrix} S_{11} & S_{12} & S_{16} \\ S_{21} & S_{22} & S_{26} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & C \end{pmatrix} \begin{pmatrix} A_{11} & A_{12} & A_{16} \\ A_{21} & A_{22} & A_{26} \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x_0 \\ \theta_0 \\ \delta p_0 \end{pmatrix}$$

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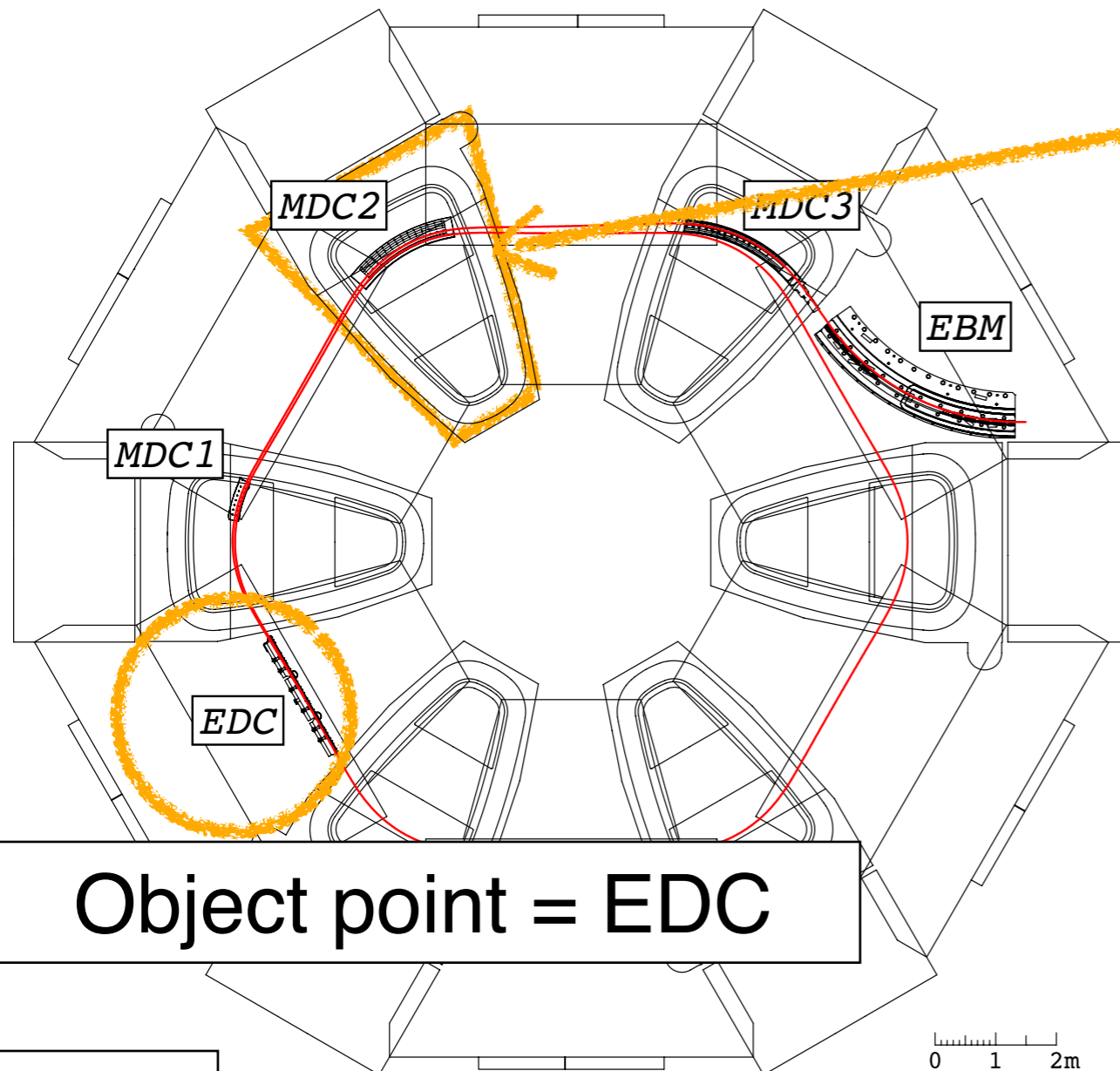
$$\begin{aligned} x_{fp} = & (S_{11}A_{11} + S_{12}A_{21})x_0 \\ & + (S_{11}A_{12} + S_{12}A_{22})\theta_0 \\ & + (S_{11}A_{16} + S_{12}A_{26} + CS_{16})\delta p_0 \end{aligned} \quad \rightarrow 0 \text{ by focusing}$$

$$A_{16} = -CS_{16}/S_{11}$$

matching condition realized by adjusting  $A_{16}$  = dispersion of Analyzer

# Ion Optics

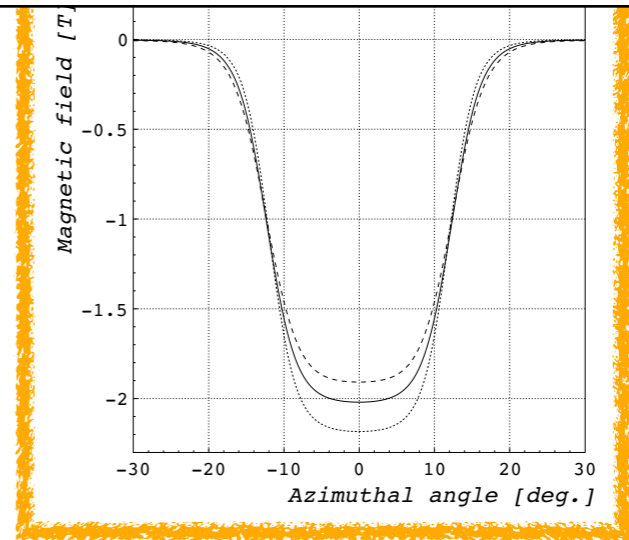
## Dispersion matching using primary beam



Object point = EDC

SRC

magnetic field in the magnet



calculate the transfer matrix using Runge-Kutta method

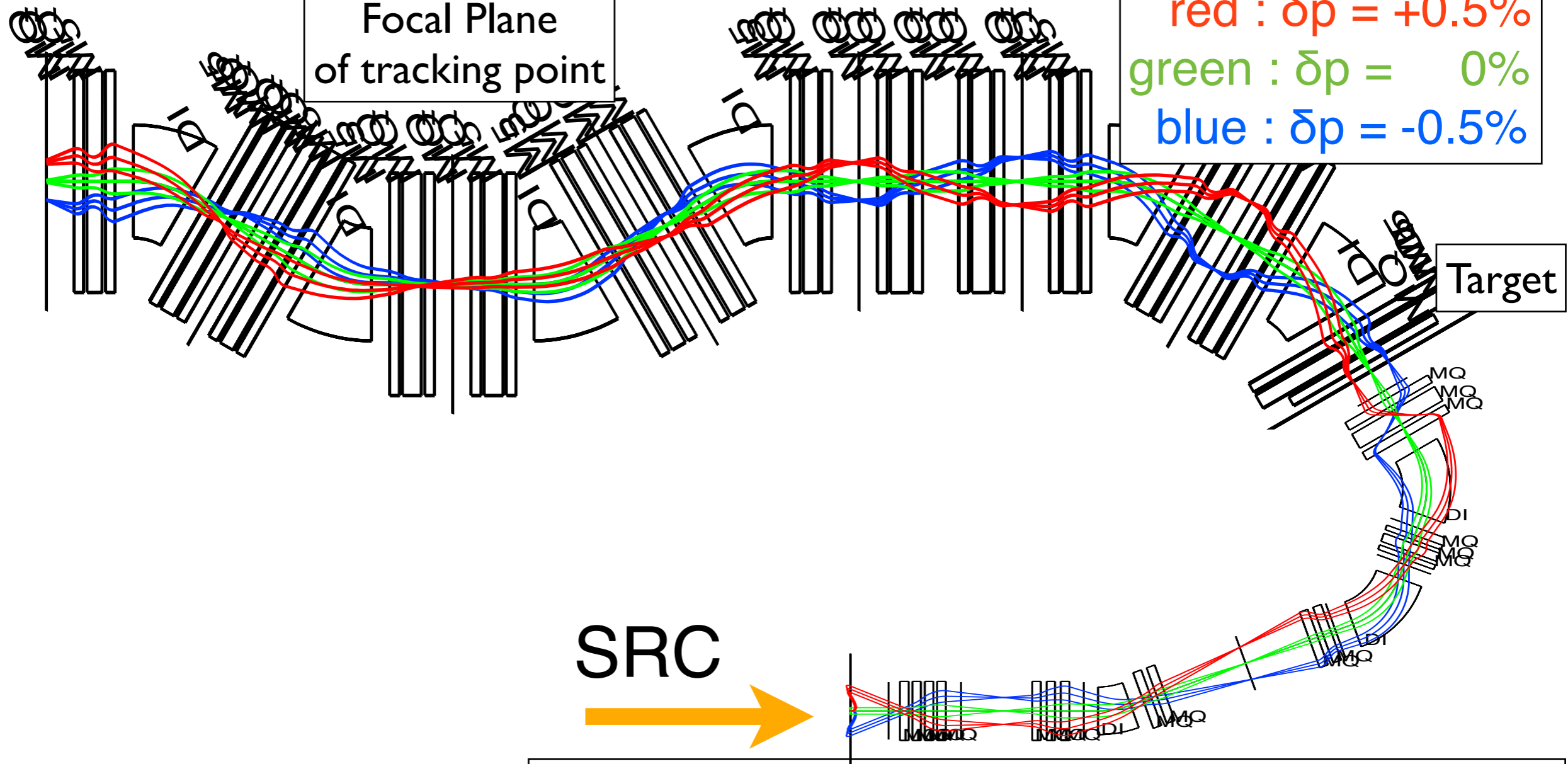
$$\begin{pmatrix} (x|x) & (x|a) & (x|y) & (x|b) & (x|\delta) \\ (a|x) & (a|a) & (a|y) & (a|b) & (a|\delta) \\ (y|x) & (y|a) & (y|y) & (y|b) & (y|\delta) \\ (b|x) & (b|a) & (b|y) & (b|b) & (b|\delta) \end{pmatrix}_{\text{EDC} \rightarrow \text{EBM}} = \begin{pmatrix} -1.00 & -3.35 & 0.0 & 0.0 & 76.9 \\ 0.30 & -0.01 & 0.0 & 0.0 & -25.4 \\ 0.0 & 0.0 & -1.03 & -1.75 & 0.0 \\ 0.0 & 0.0 & -0.09 & -1.12 & 0.0 \end{pmatrix}$$

# Ion Optics

BigRIPS = Spectrometer

Focal Plane  
of tracking point

red :  $\delta p = +0.5\%$   
green :  $\delta p = 0\%$   
blue :  $\delta p = -0.5\%$



SRC



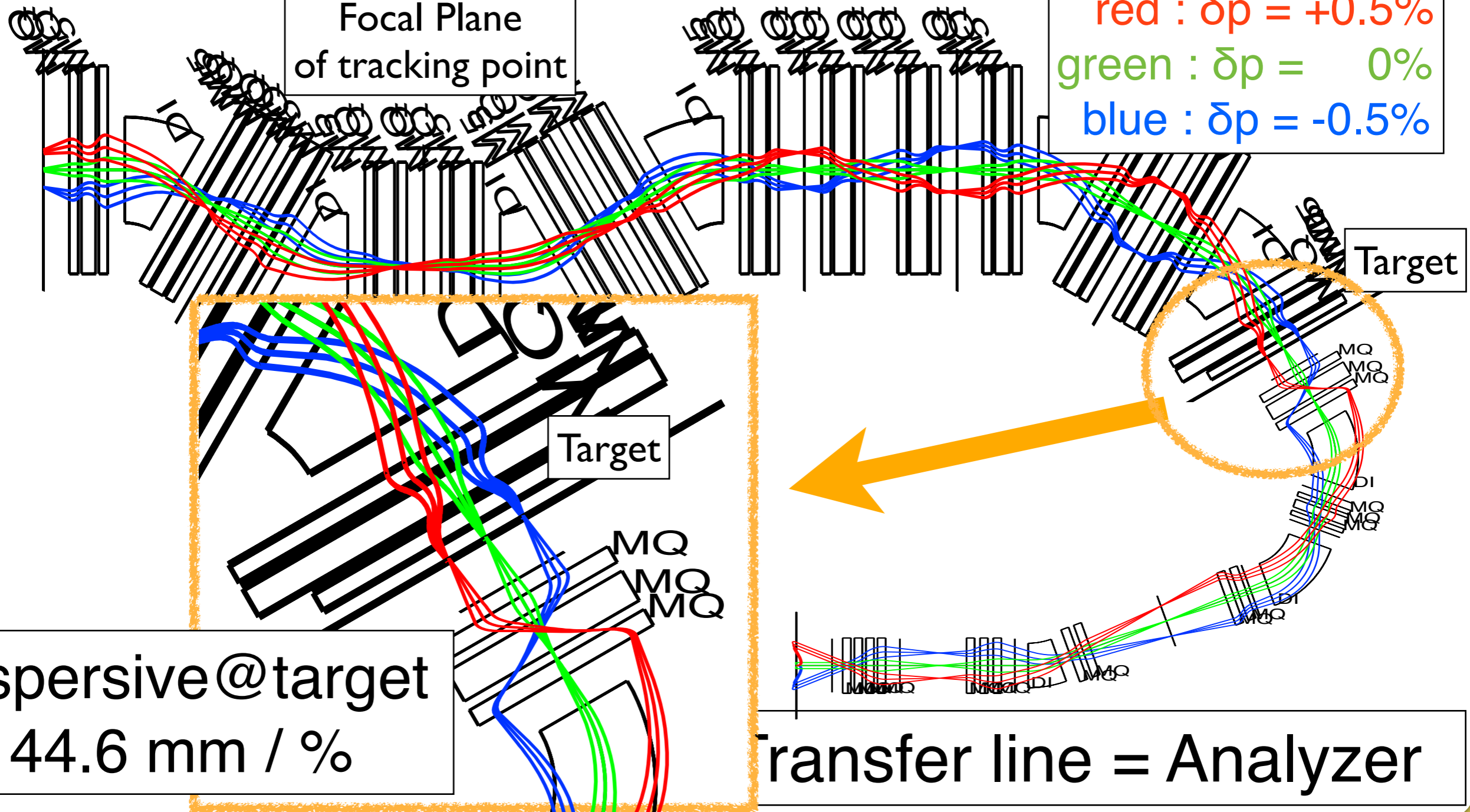
Beam Transfer line = Analyzer

# Ion Optics

BigRIPS = Spectrometer

Focal Plane  
of tracking point

red :  $\delta p = +0.5\%$   
green :  $\delta p = 0\%$   
blue :  $\delta p = -0.5\%$



dispersive @ target  
44.6 mm / %

transfer line = Analyzer

# Ion Optics

BigRIPS = Spectrometer

Focal Plane  
of tracking point

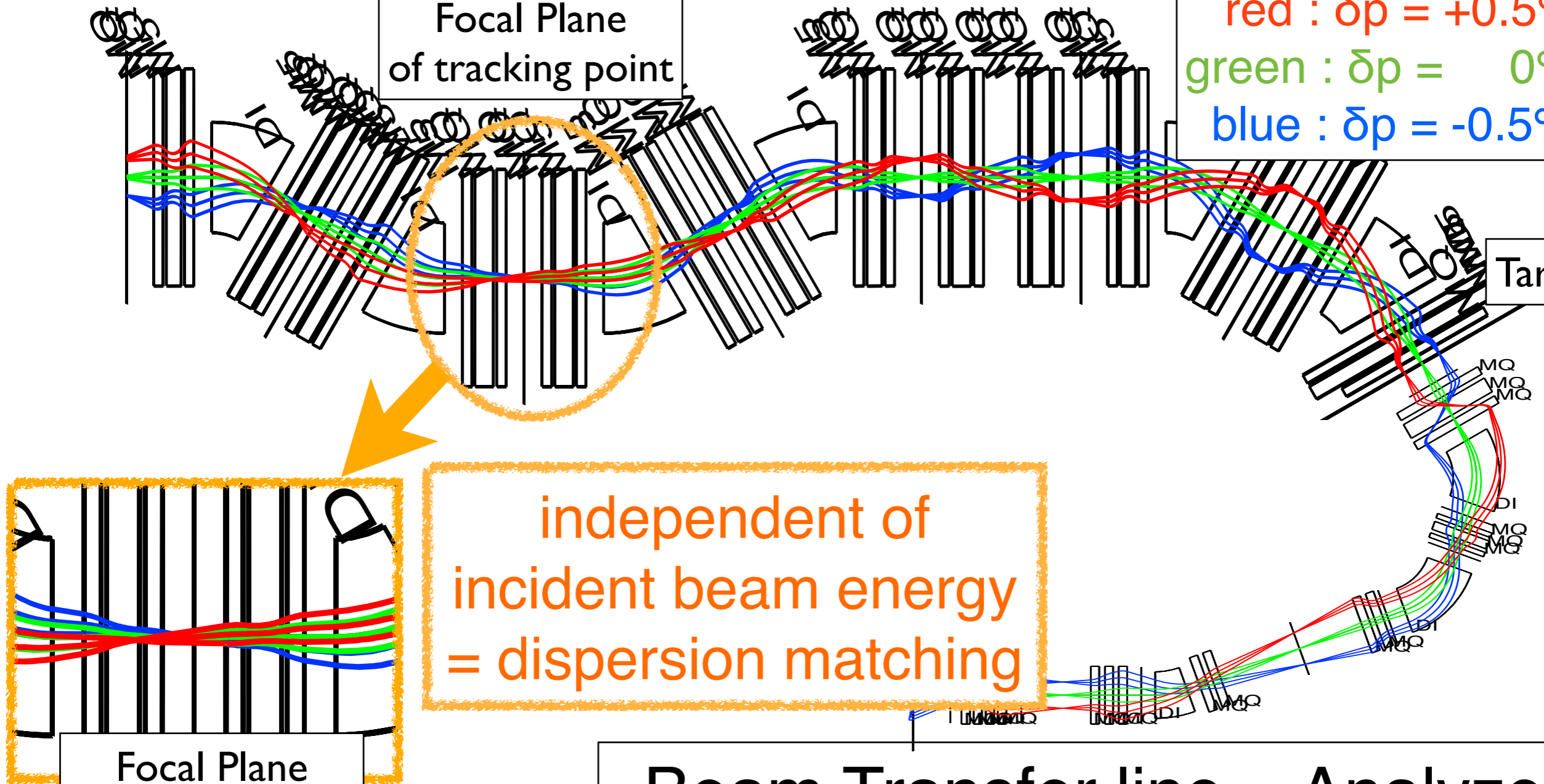
red :  $\delta p = +0.5\%$   
green :  $\delta p = 0\%$   
blue :  $\delta p = -0.5\%$

Target

independent of  
incident beam energy  
= dispersion matching

Focal Plane  
of tracking point

Beam Transfer line = Analyzer





# Ion Optics

BigRIPS = Spectrometer

Focal Plane  
of tracking point

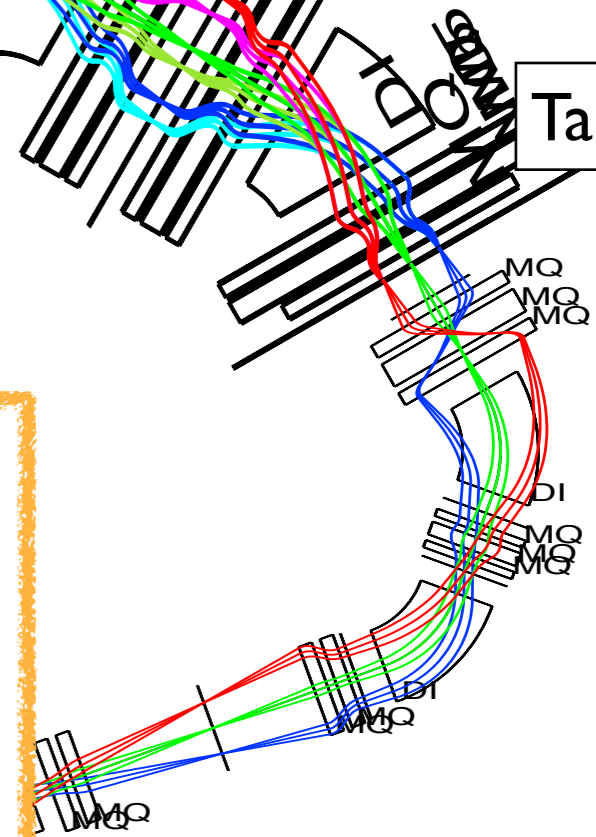
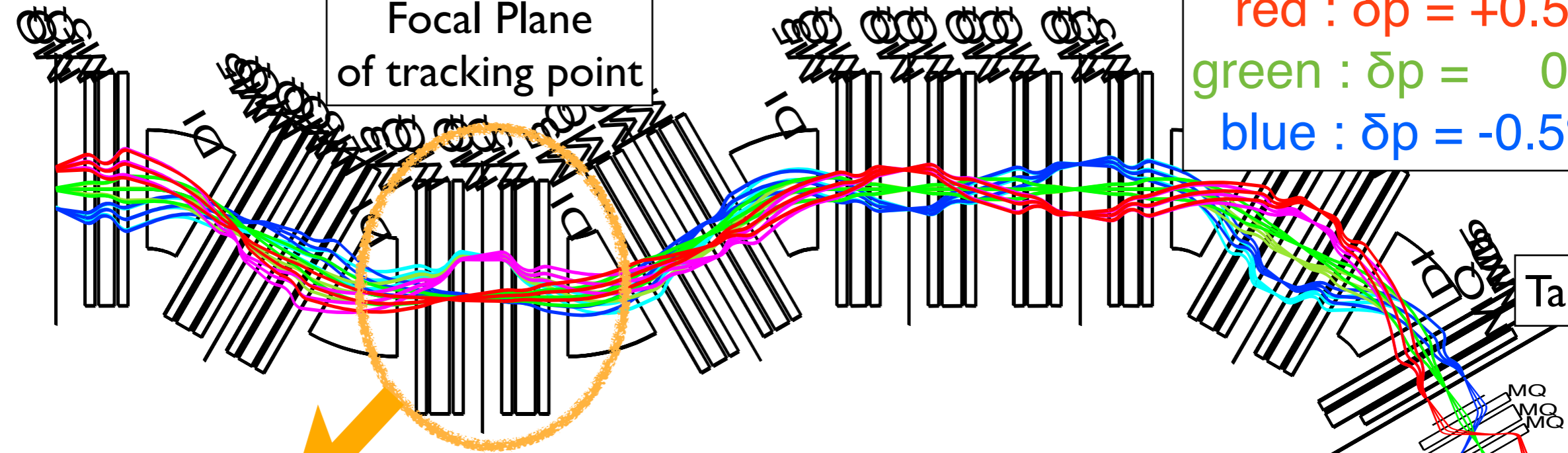
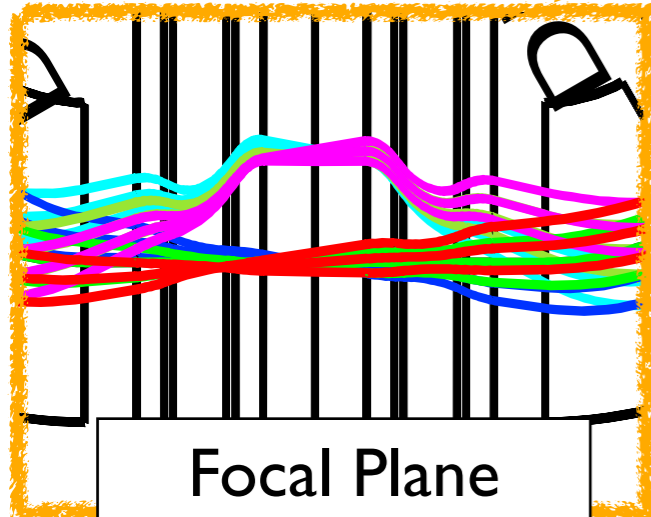
red :  $\delta p = +0.5\%$   
green :  $\delta p = 0\%$   
blue :  $\delta p = -0.5\%$

Target

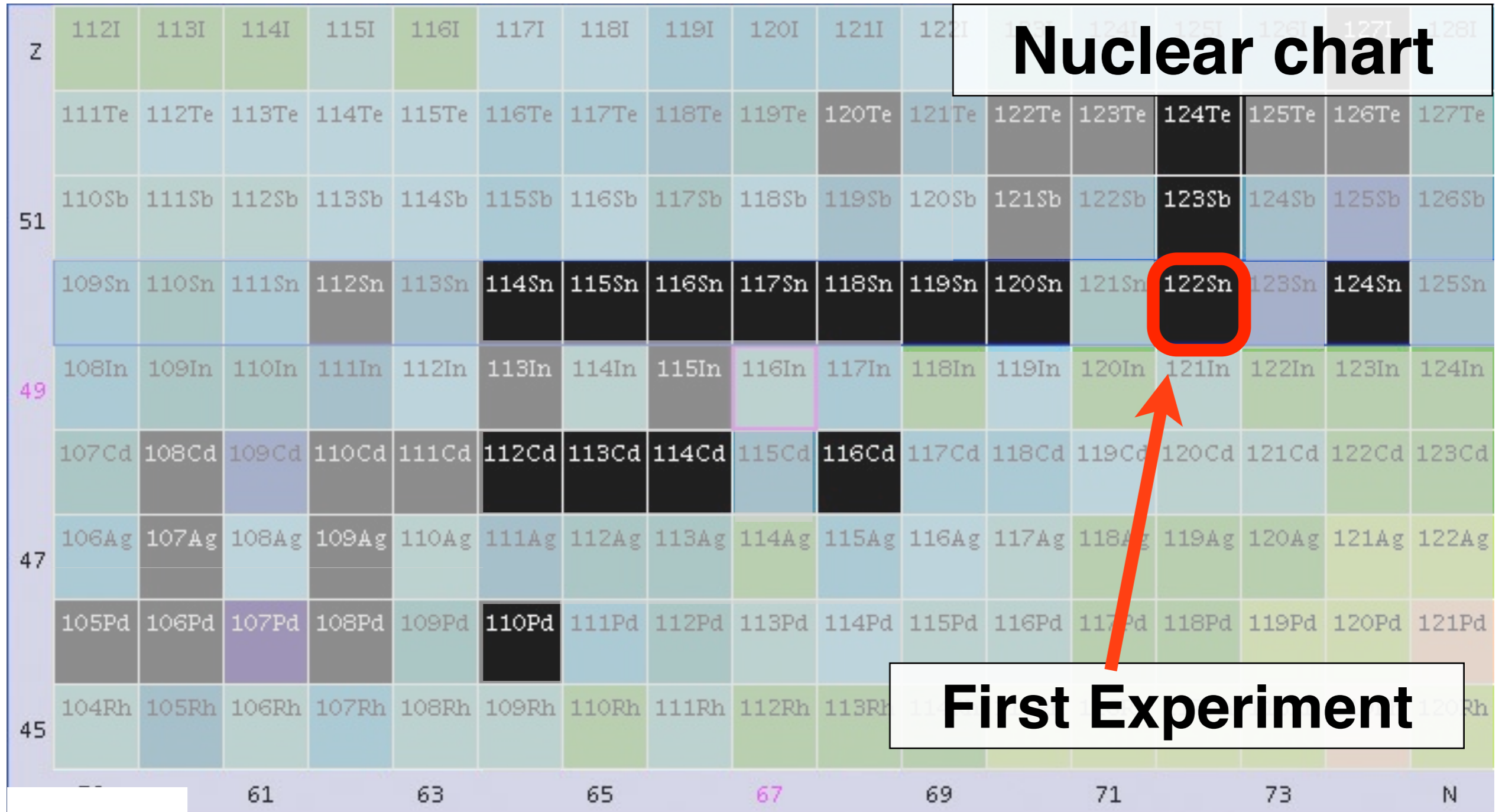
realize high precision  
spectroscopy  
dispersion 62 mm / %  
 $p/\Delta p \sim 6000$

Focal Plane  
of tracking point

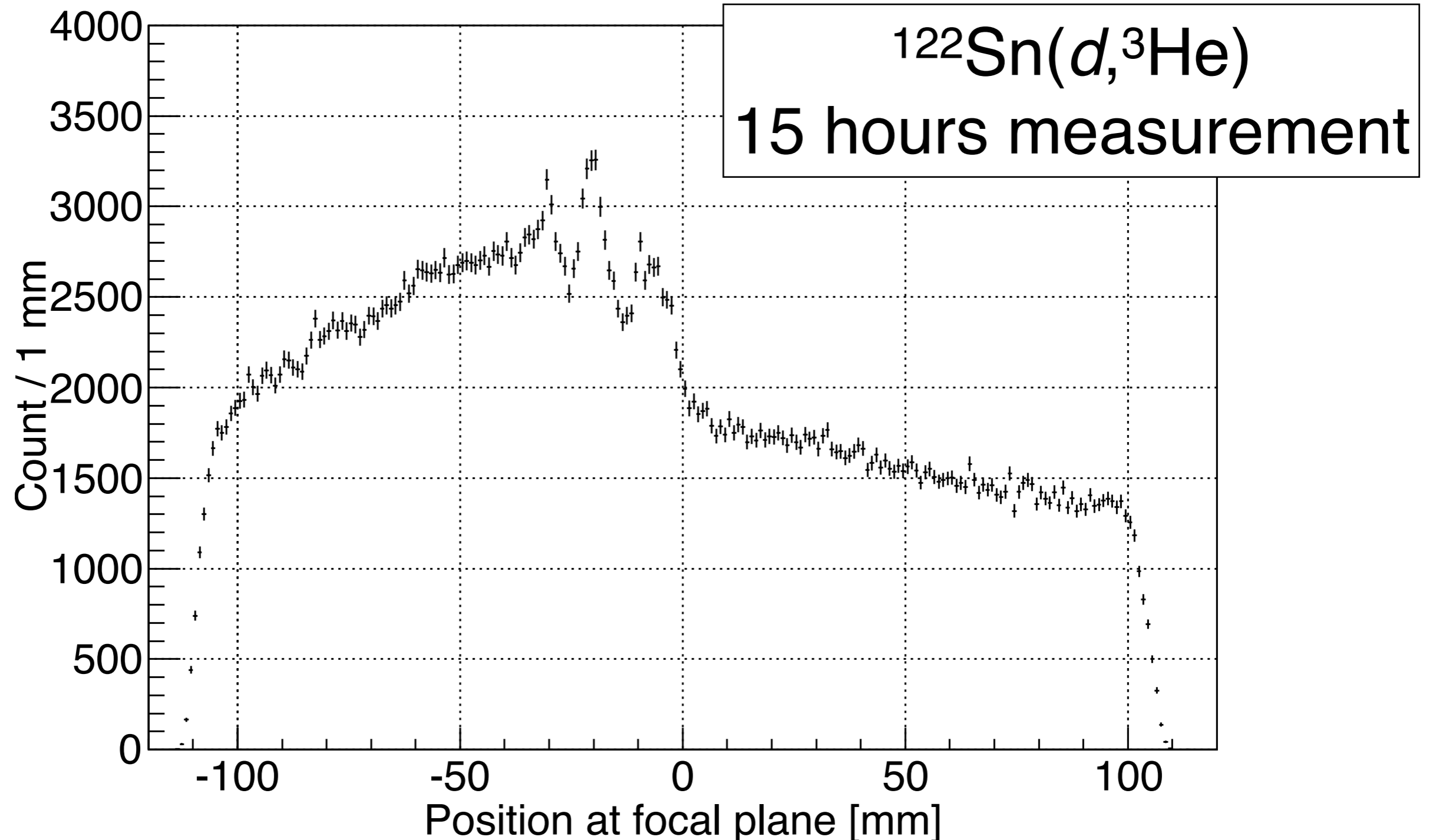
Beam Transfer line = Analyzer



# The pilot experiment

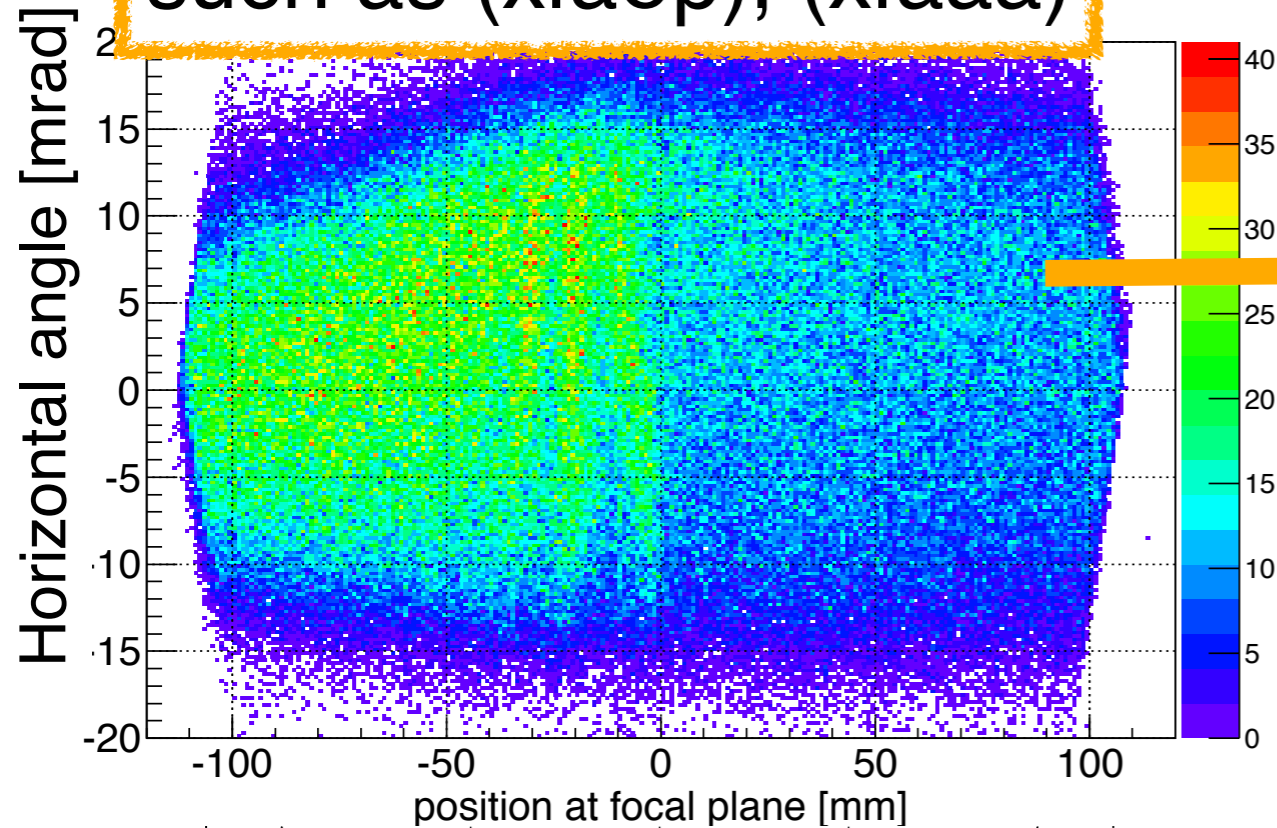


# *The result of pilot experiment*

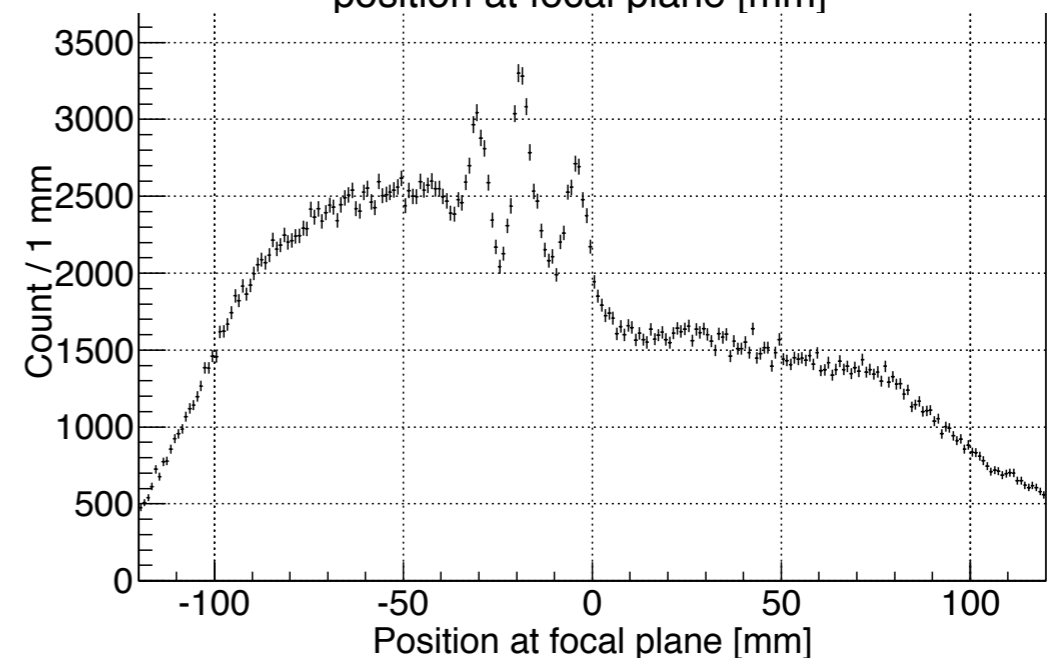
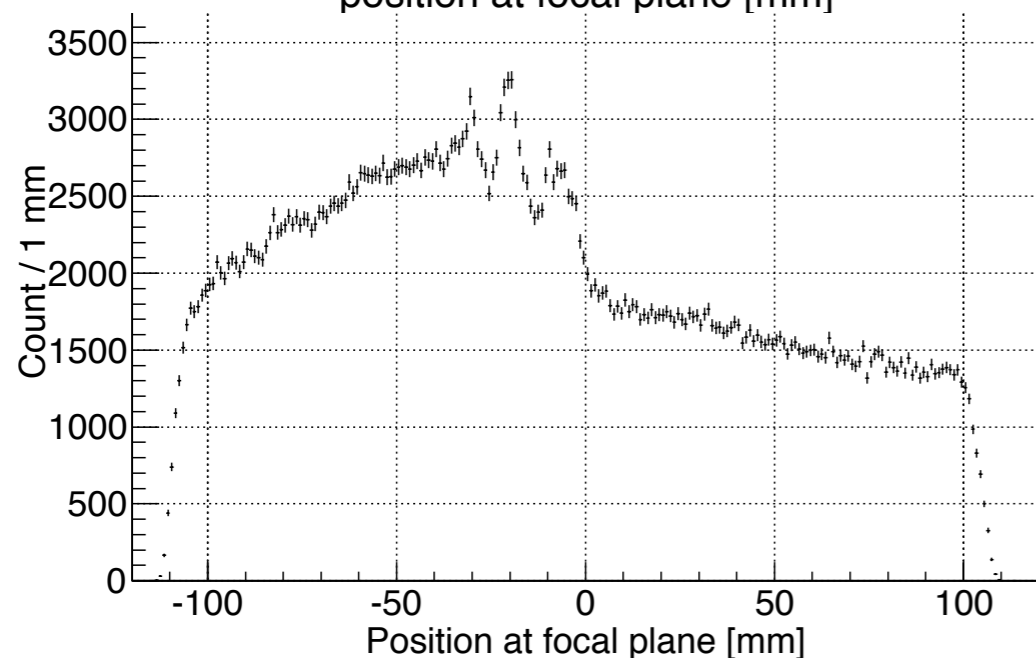
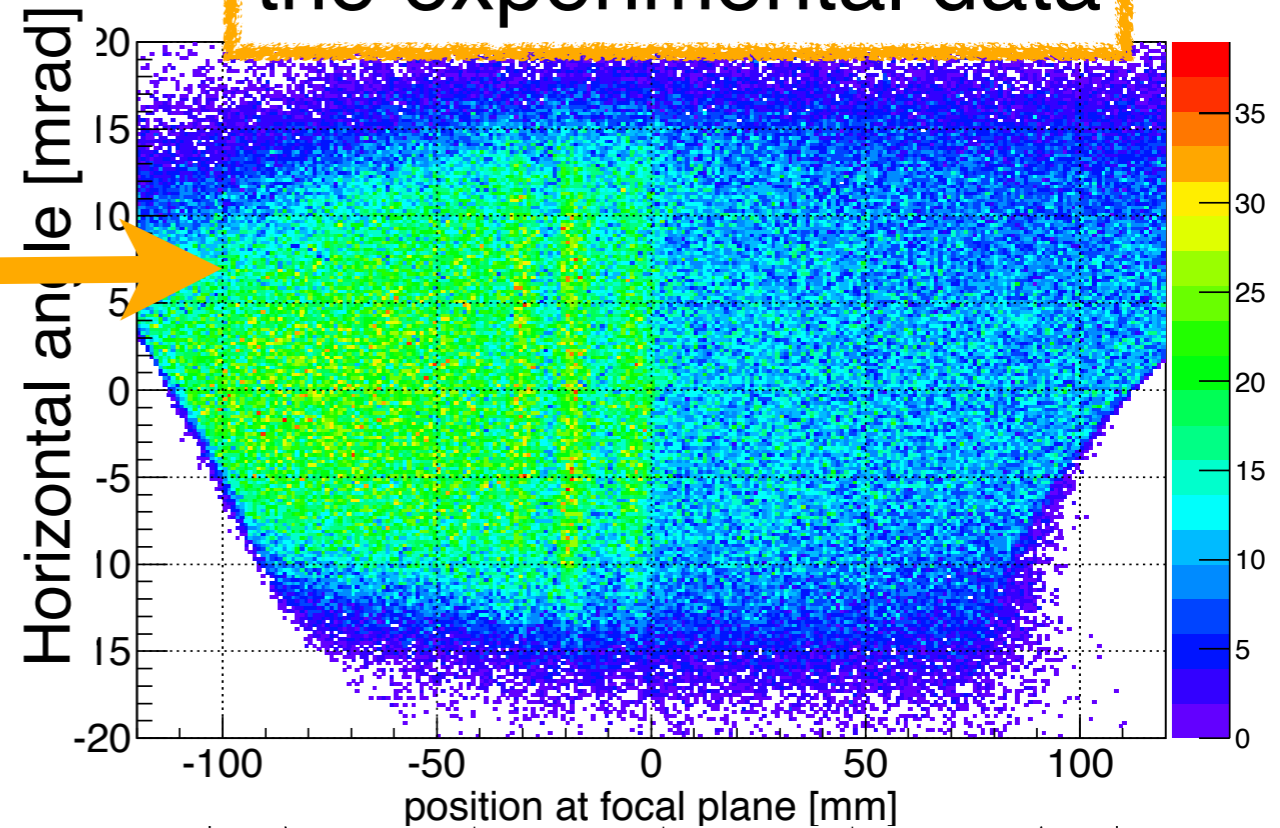


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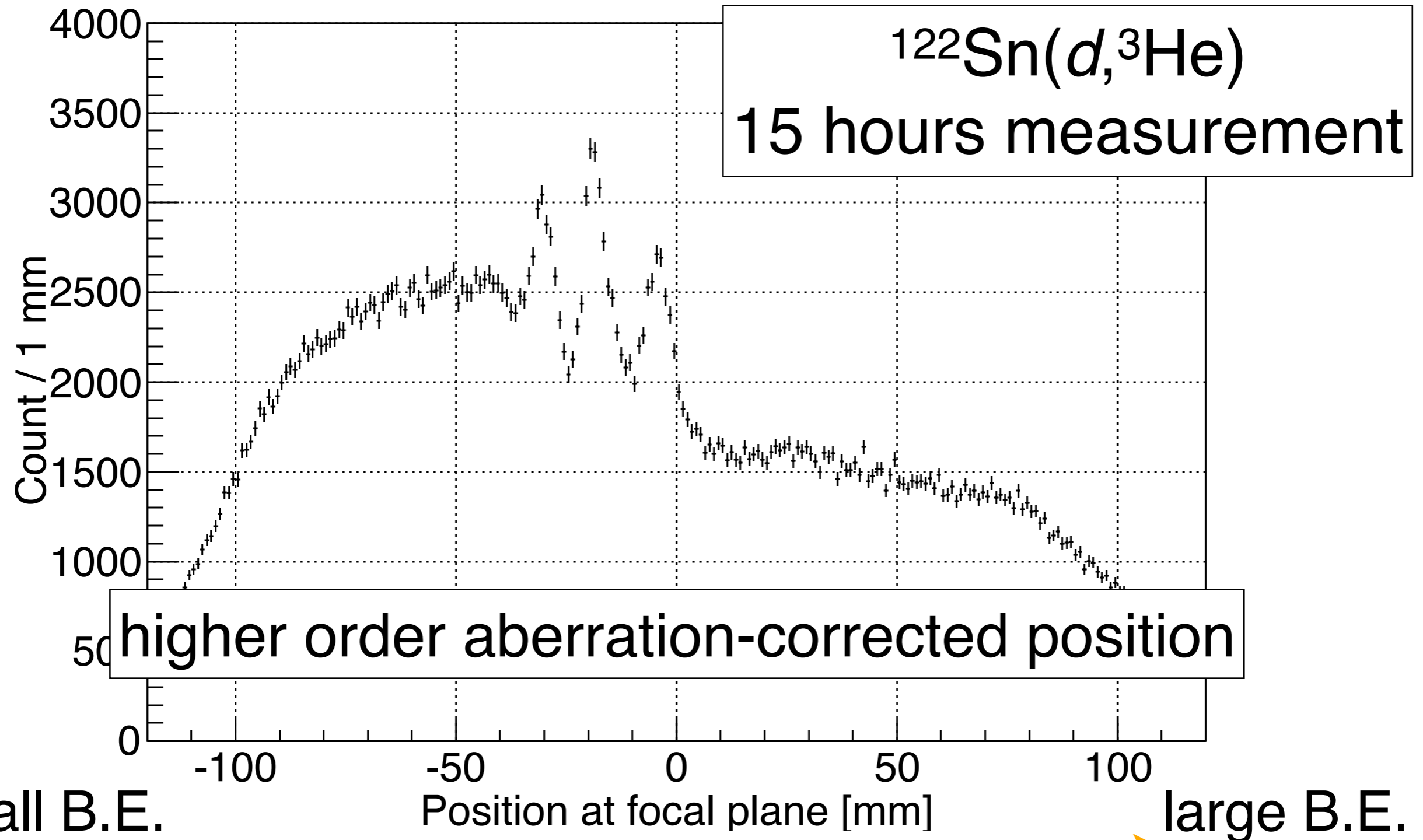
higher order aberration  
such as  $(\chi_{la\delta\rho})$ ,  $(\chi_{laaa})$



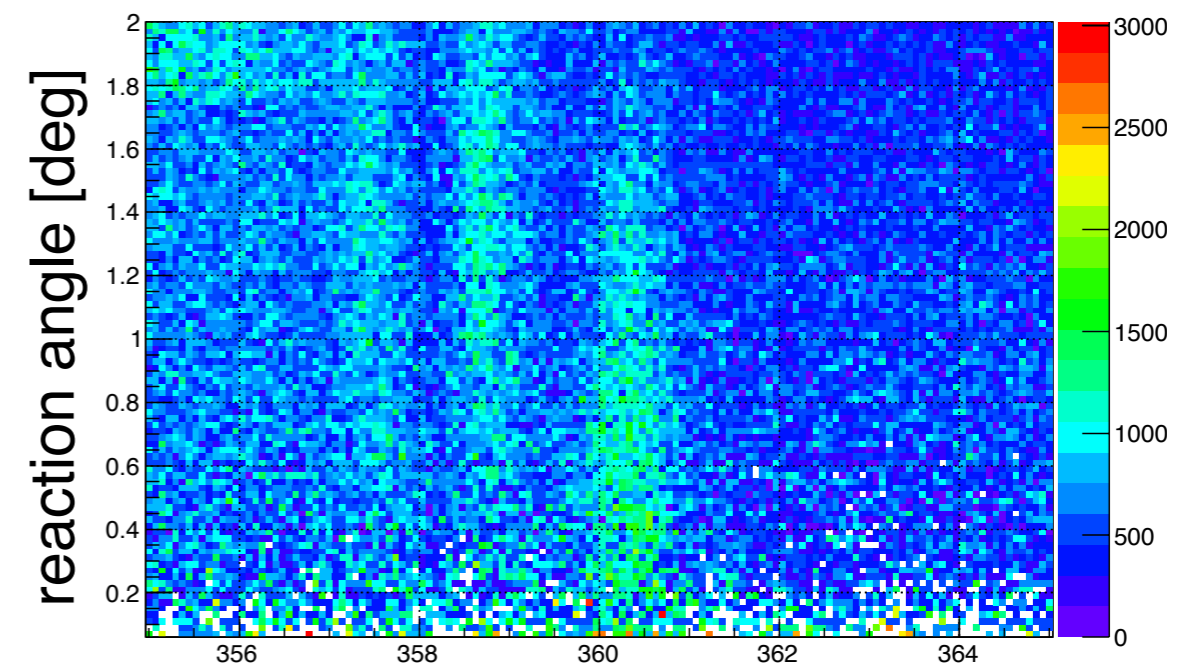
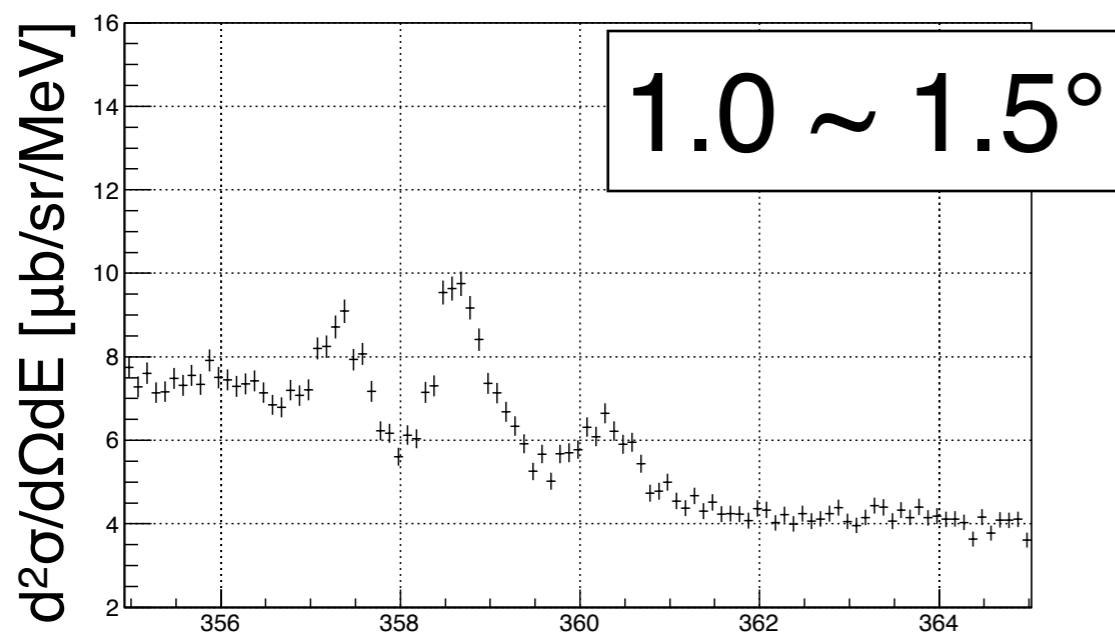
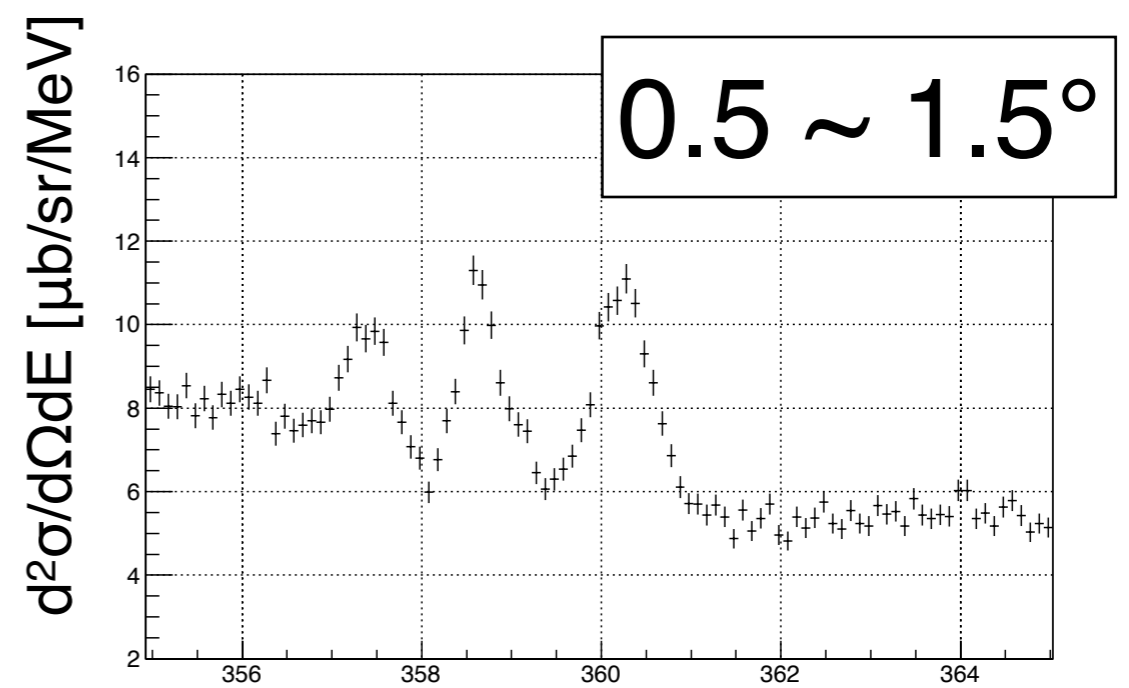
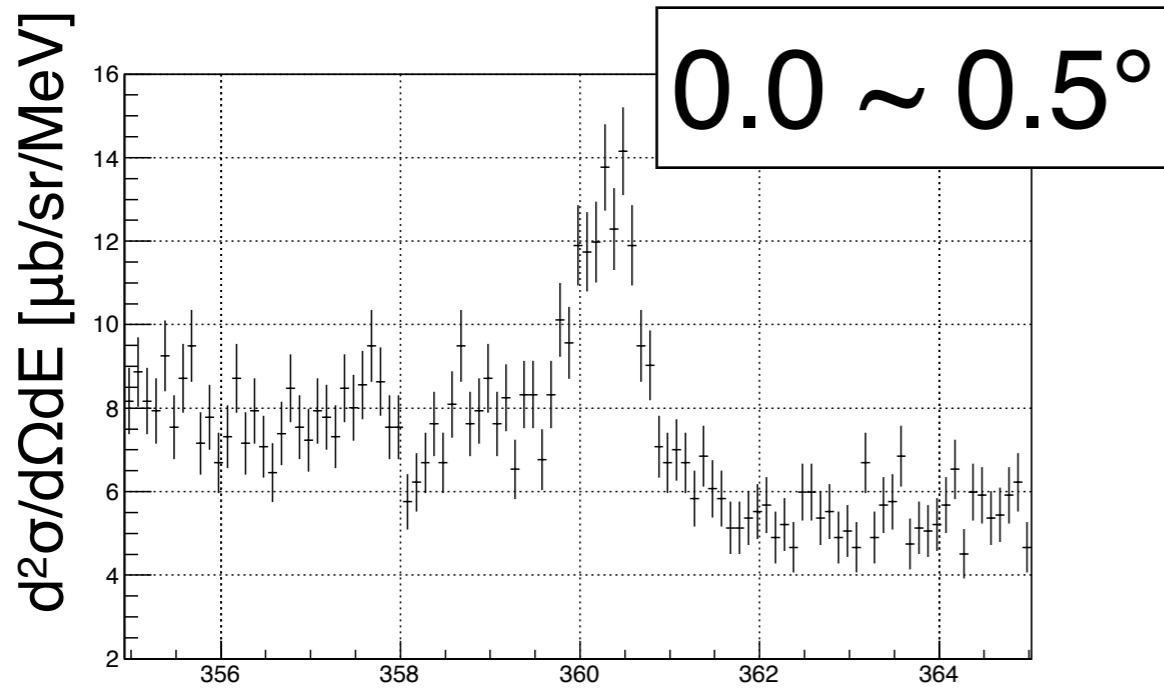
corrected by  
the experimental data



# *The result of pilot experiment*



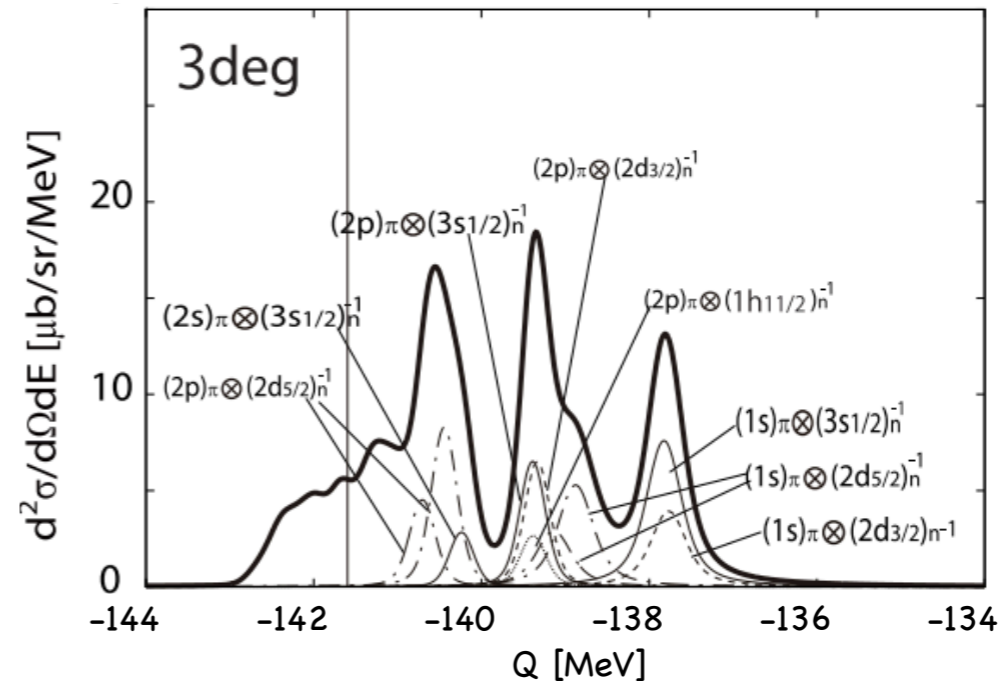
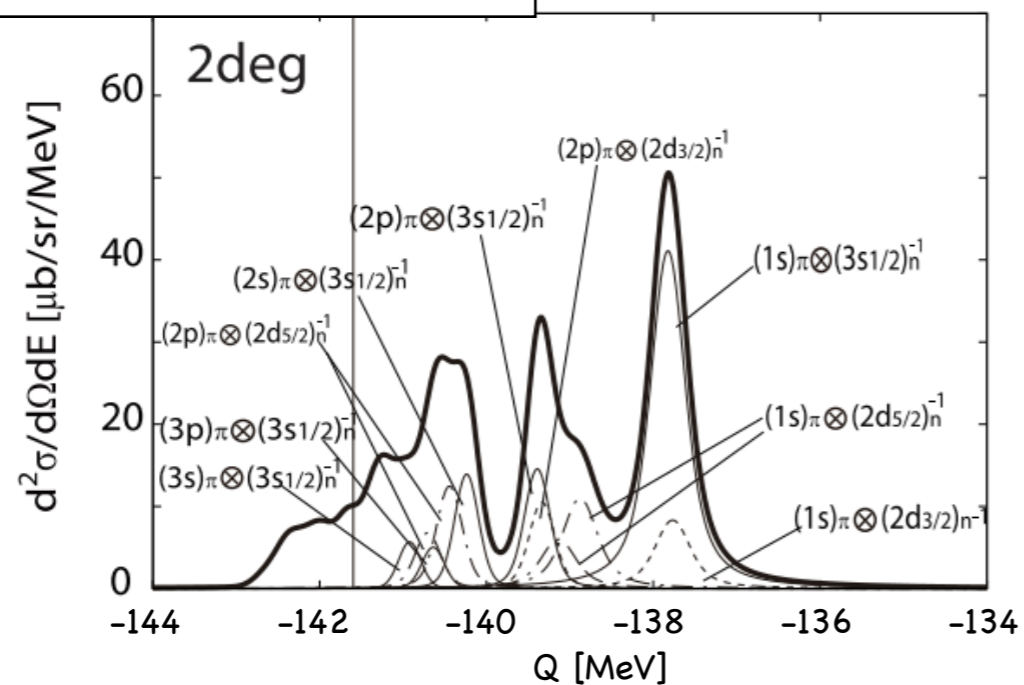
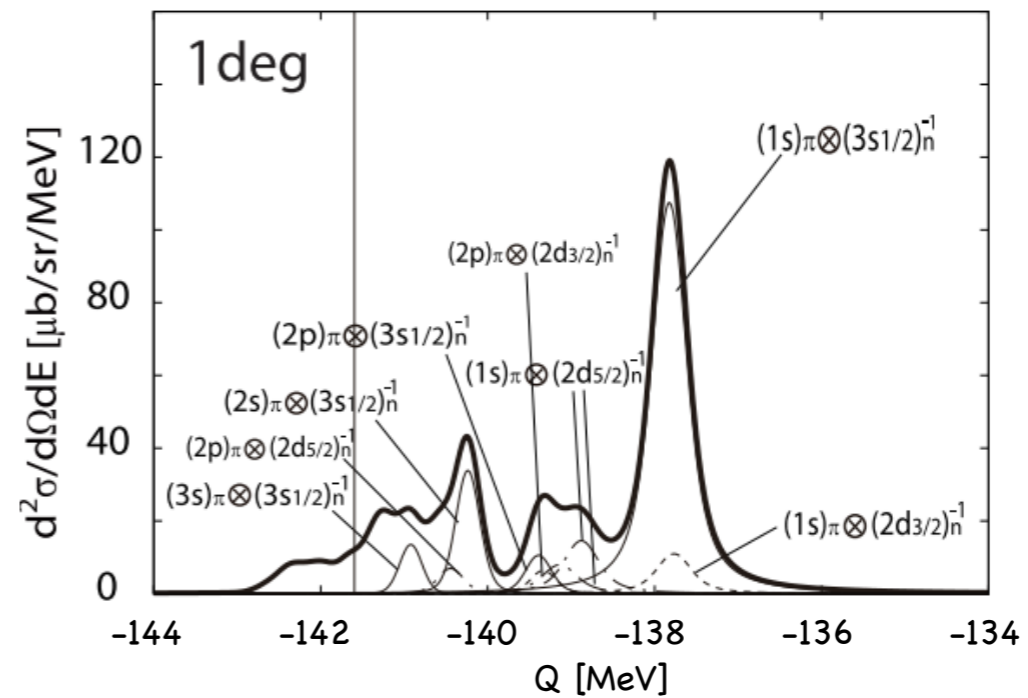
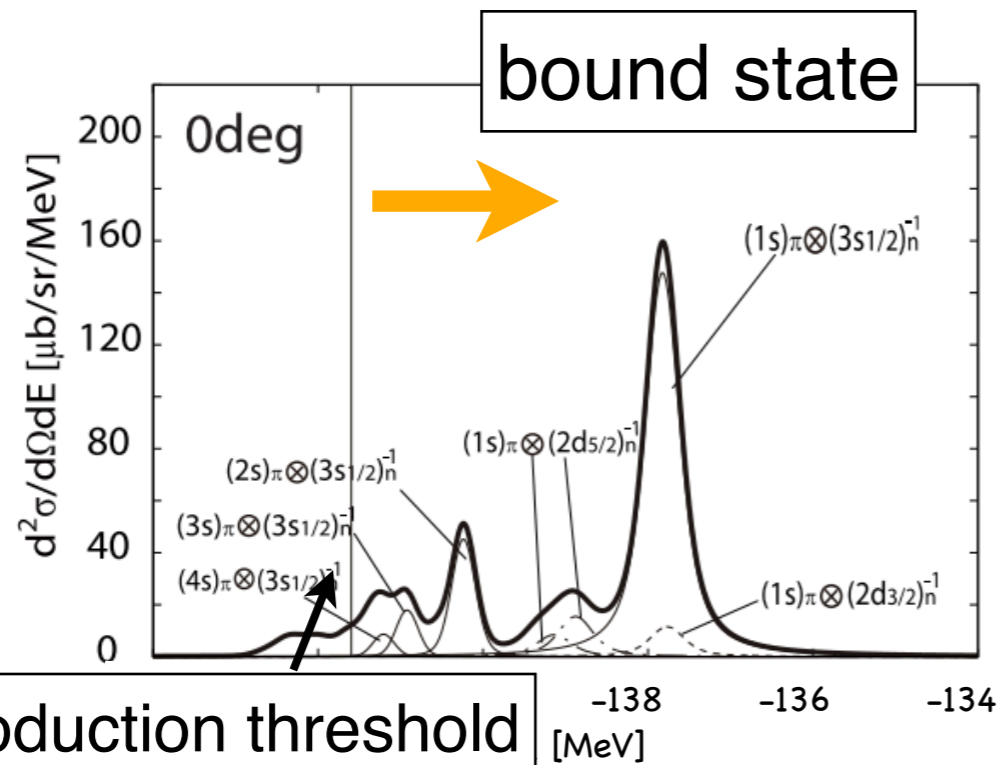
# $d^2\sigma/d\Omega dE$ vs $T_{He}$ Spectra



kinetic energy of  ${}^3\text{He}$  [MeV]

kinetic energy of  ${}^3\text{He}$  [MeV]

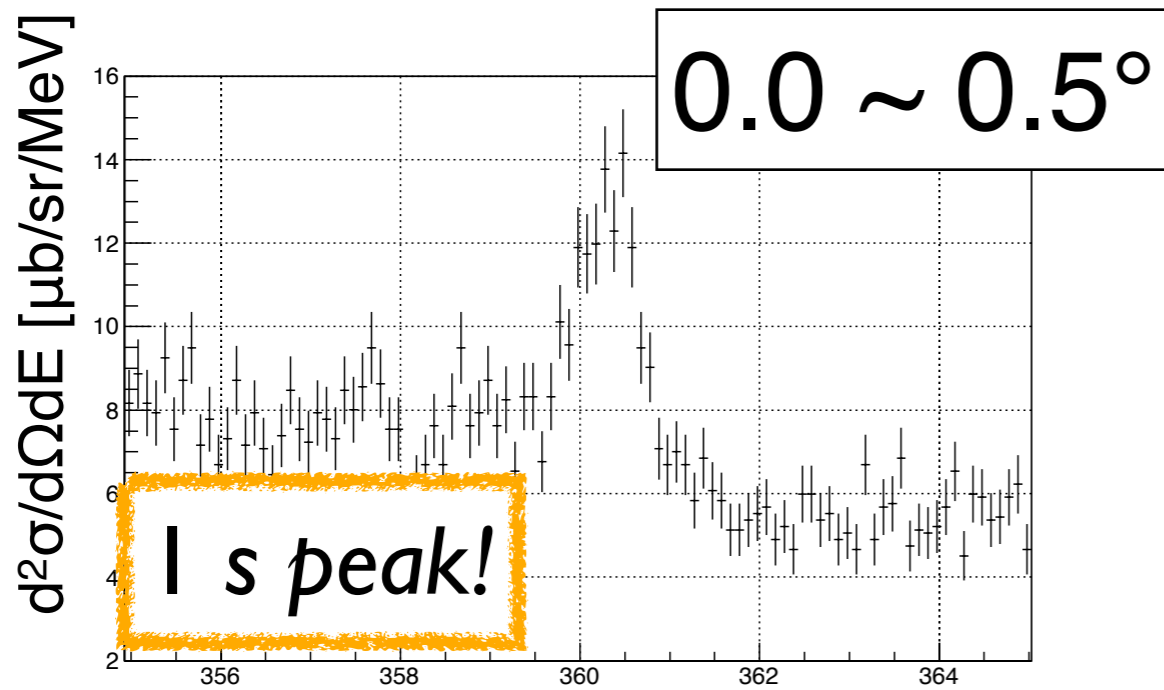
# Theoretical calculated spectrum



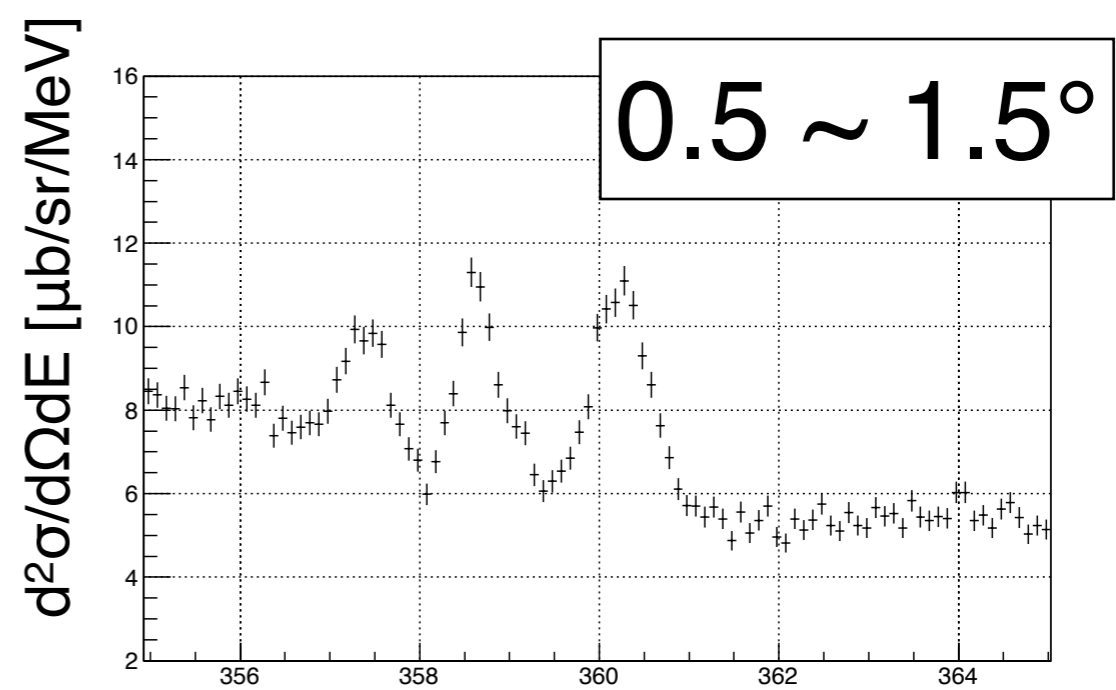
resolution  $\sim 300$  keV

\*N. Ikeno et al., Eur. Phys. J. A 47, 161 (2011)

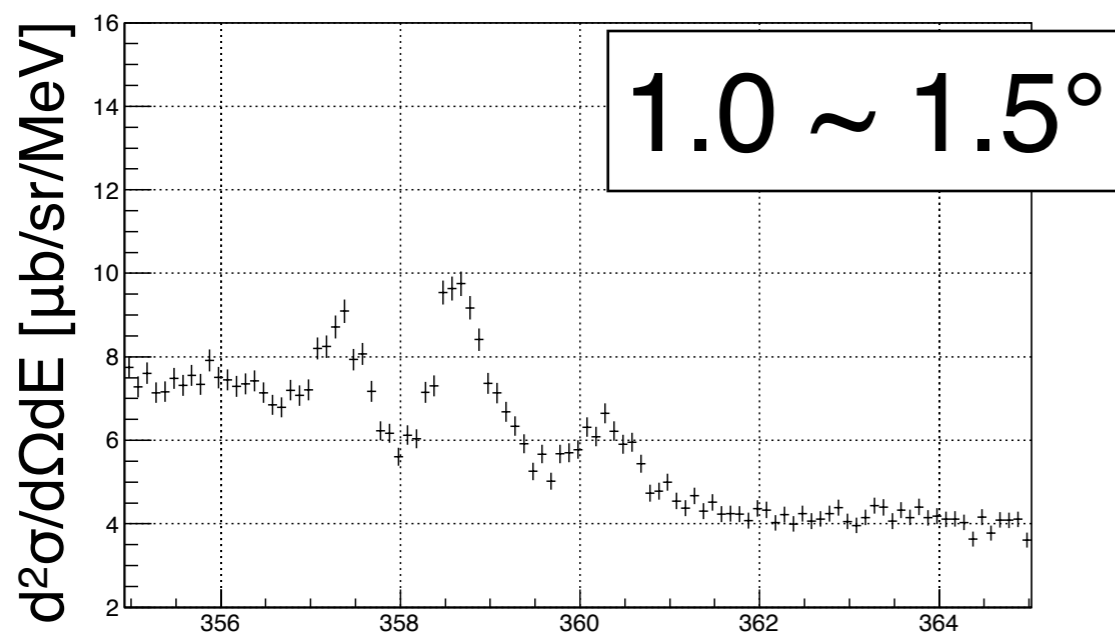
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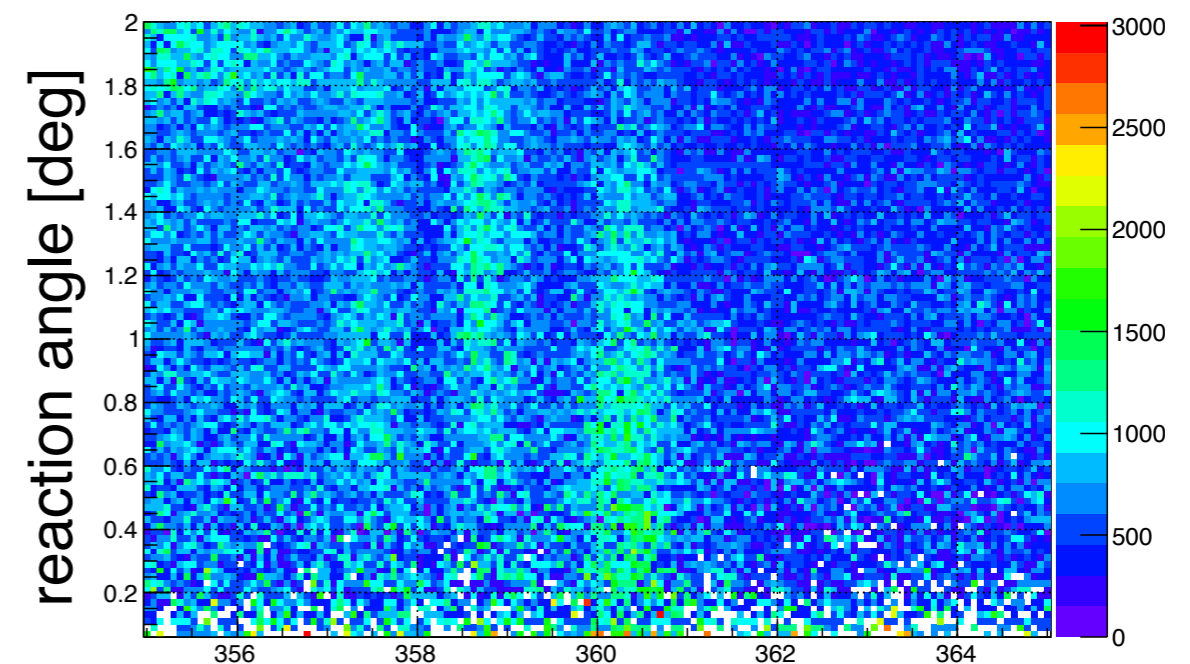
kinetic energy of  ${}^3\text{He}$  [MeV]



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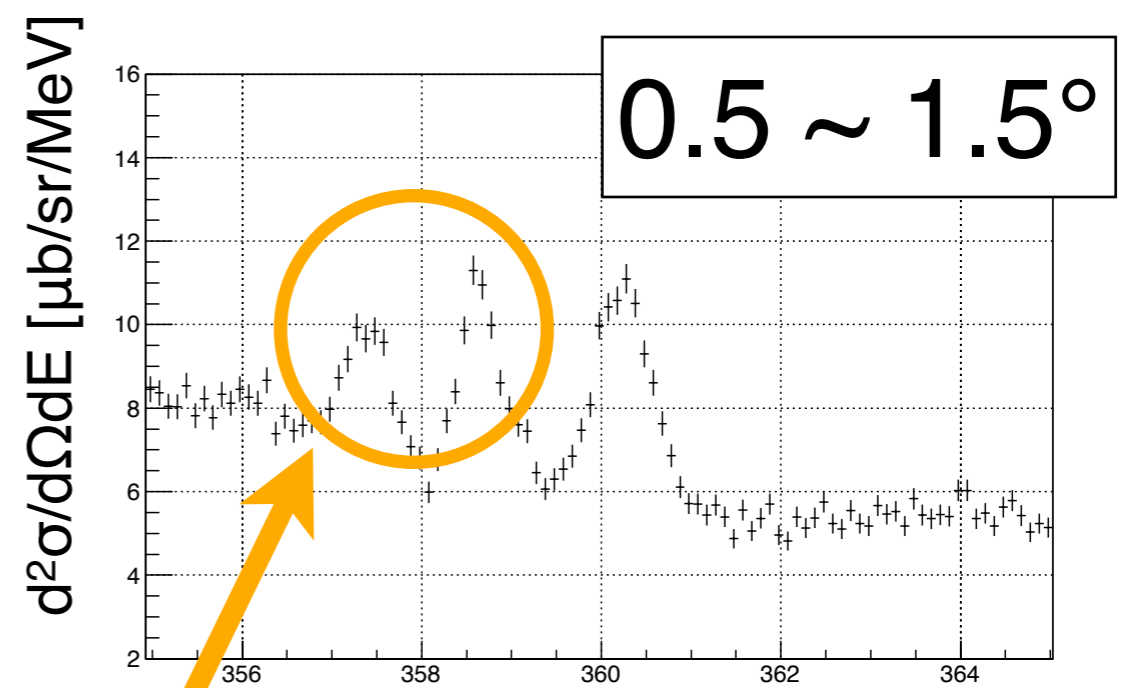
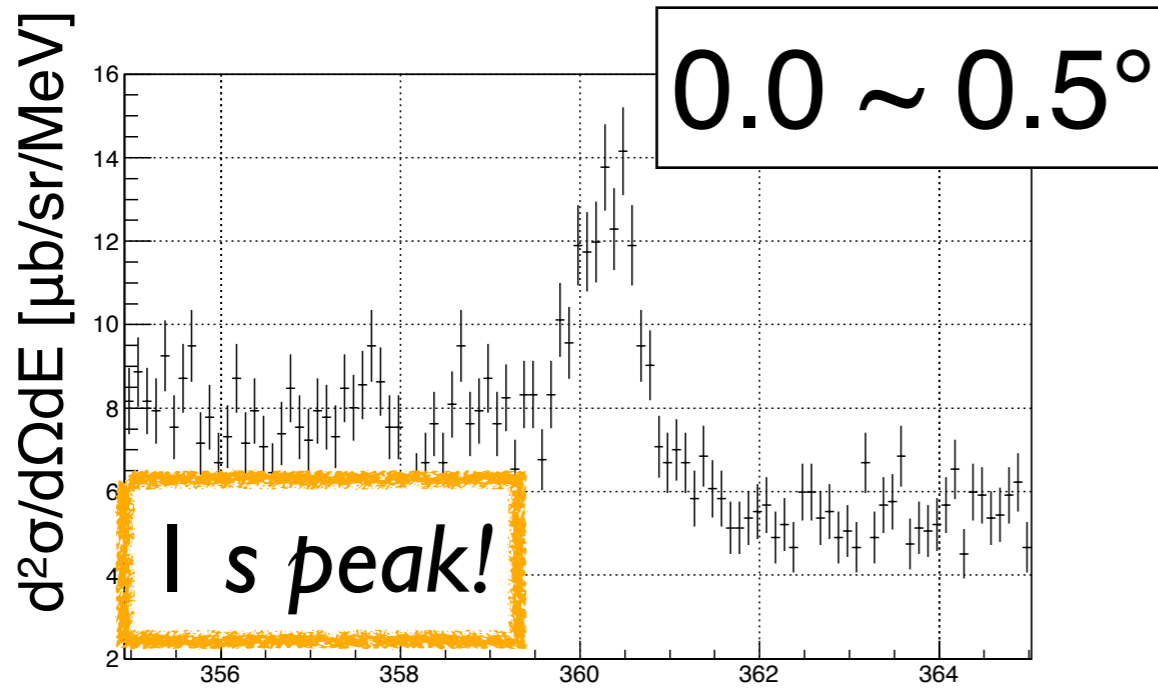
kinetic energy of  ${}^3\text{He}$  [MeV]



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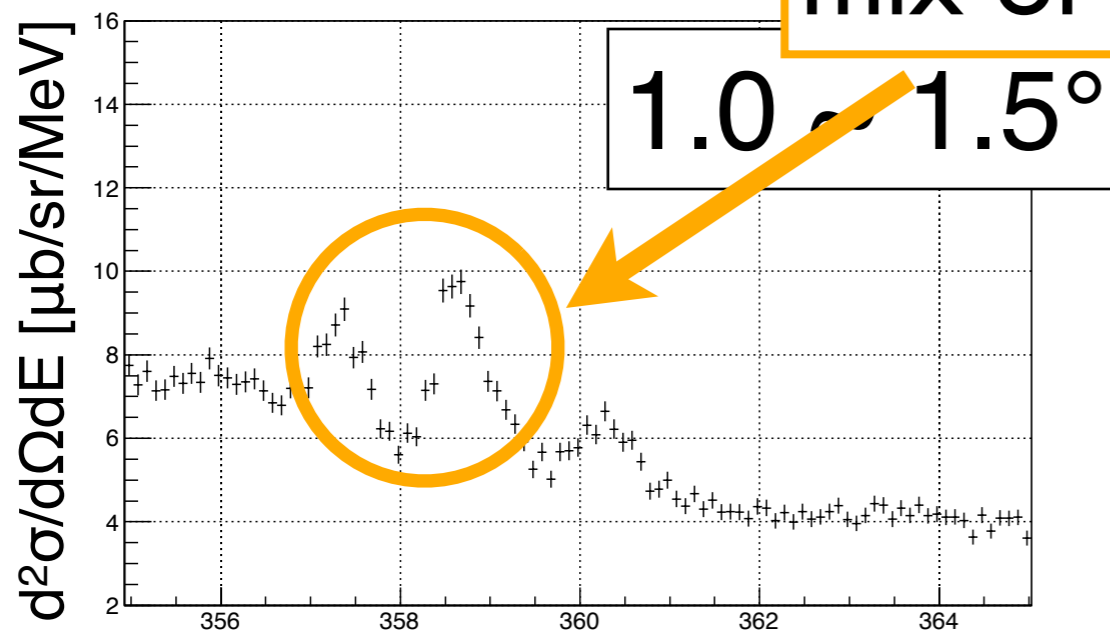


# $d^2\sigma/d\Omega dE$ vs $T_{He}$ Spectra

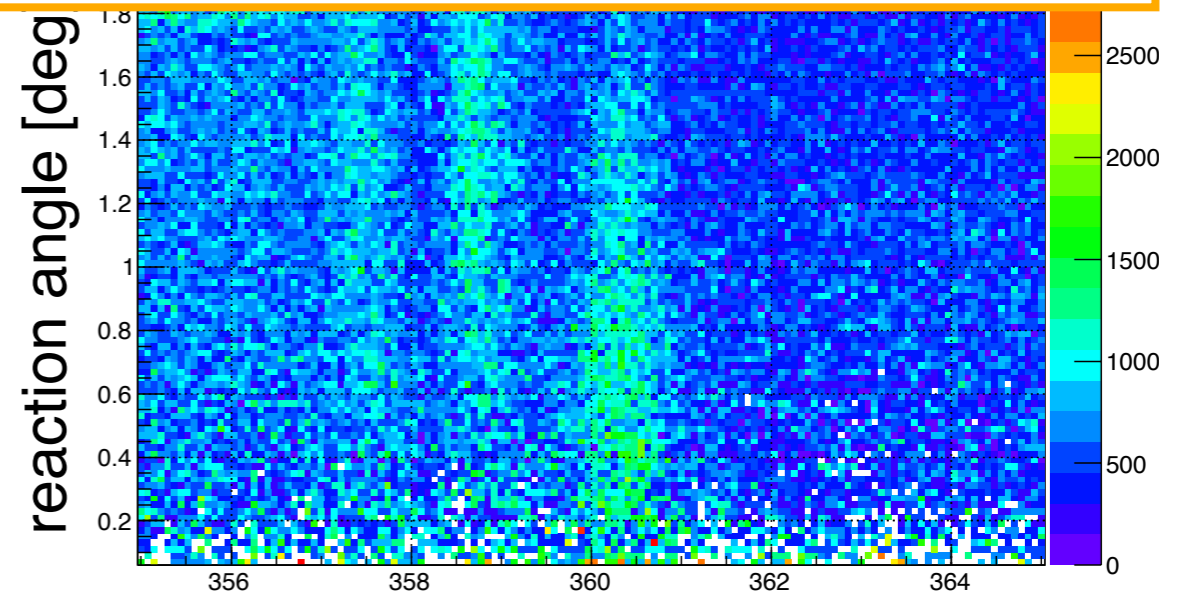


kinetic energy of  $^3\text{He}$

mix of  $(2s, 2p)_\pi \otimes (2d_{\frac{3}{2}}, 2d_{\frac{5}{2}}, 3s_{\frac{1}{2}})_{n-1}$

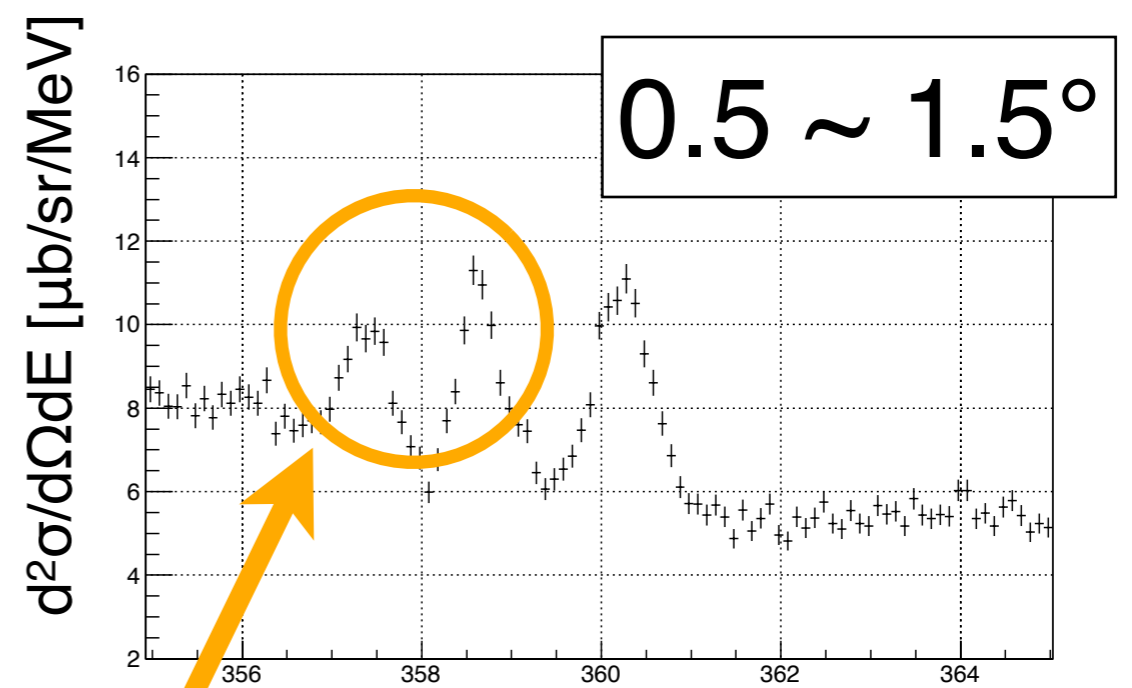
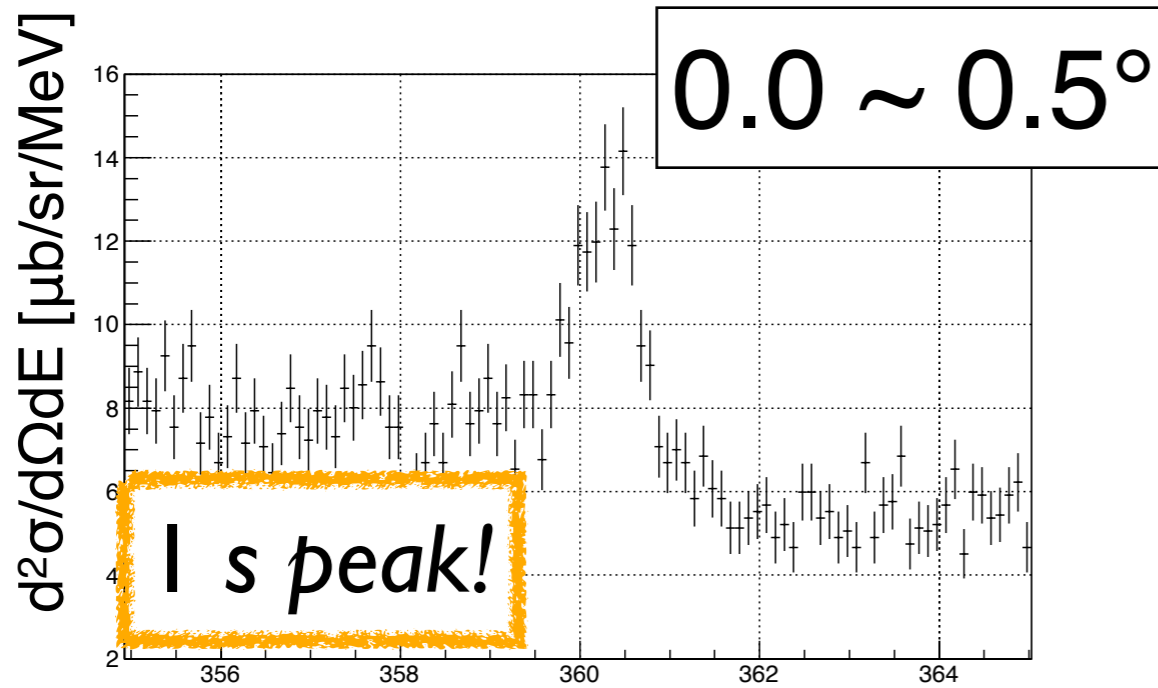


kinetic energy of  $^3\text{He}$  [MeV]

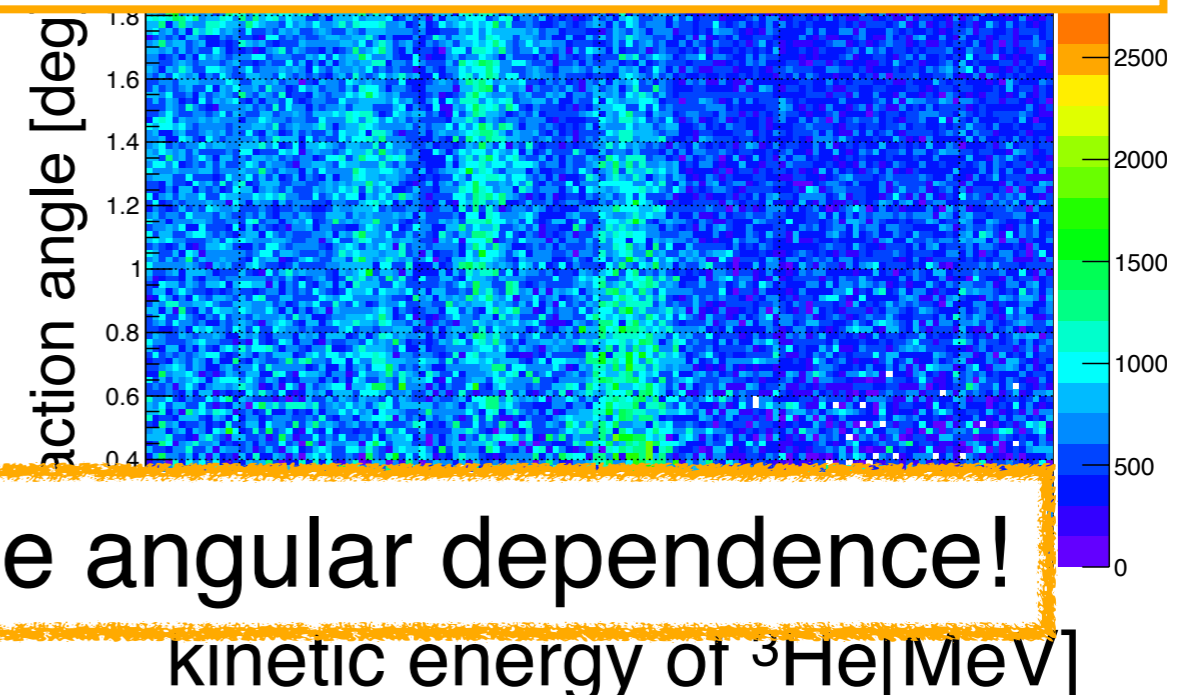
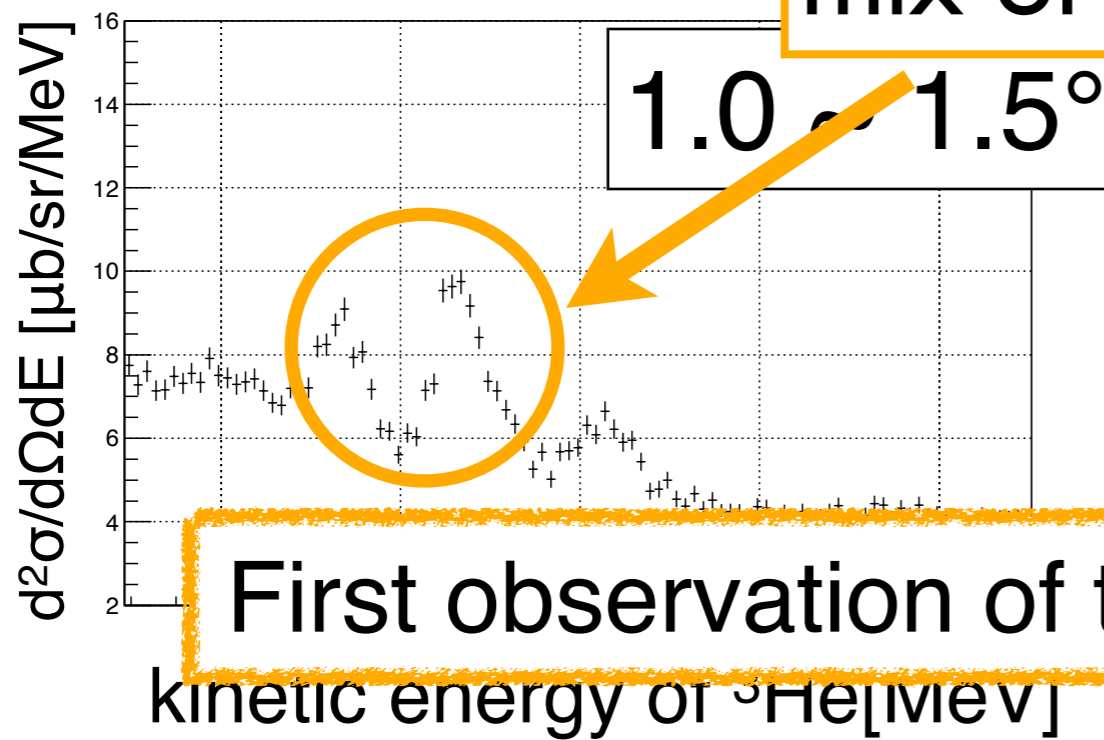


kinetic energy of  $^3\text{He}$  [MeV]

# $d^2\sigma/d\Omega dE$ vs $T_{He}$ Spectra

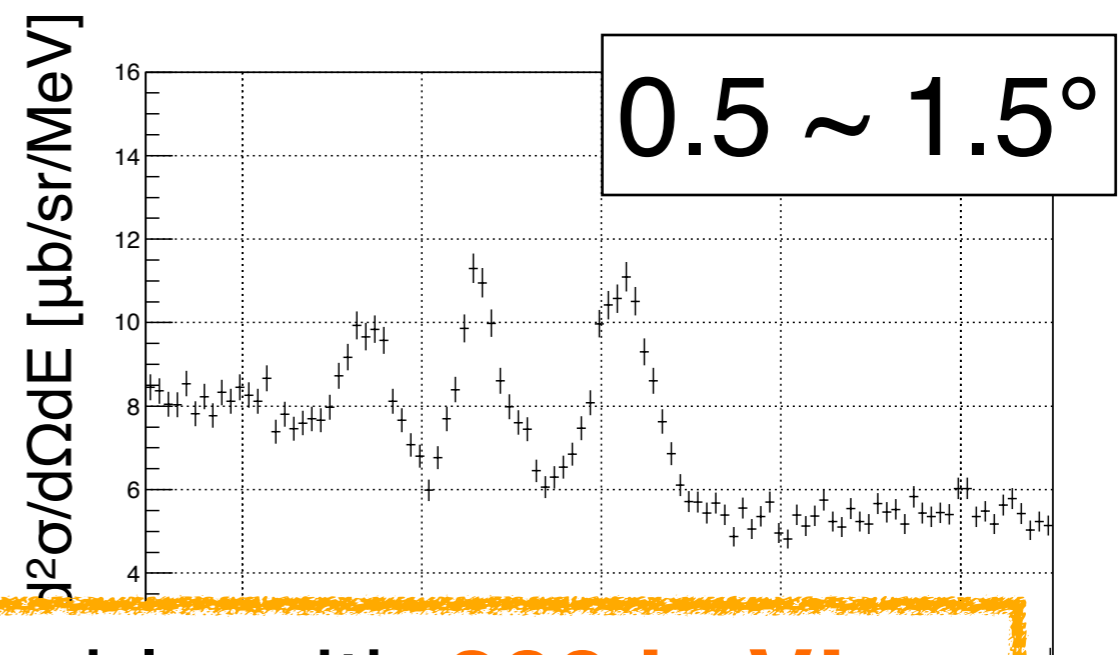
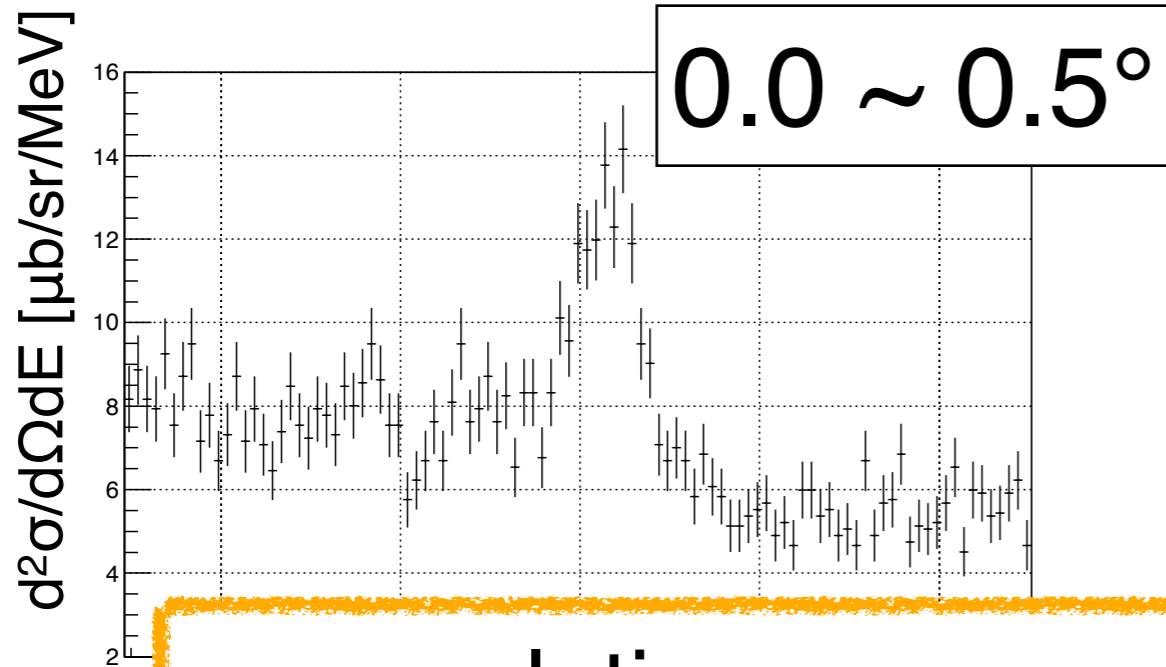


**mix of  $(2s, 2p)_\pi \otimes (2d_{\frac{3}{2}}, 2d_{\frac{5}{2}}, 3s_{\frac{1}{2}})_{n-1}$**

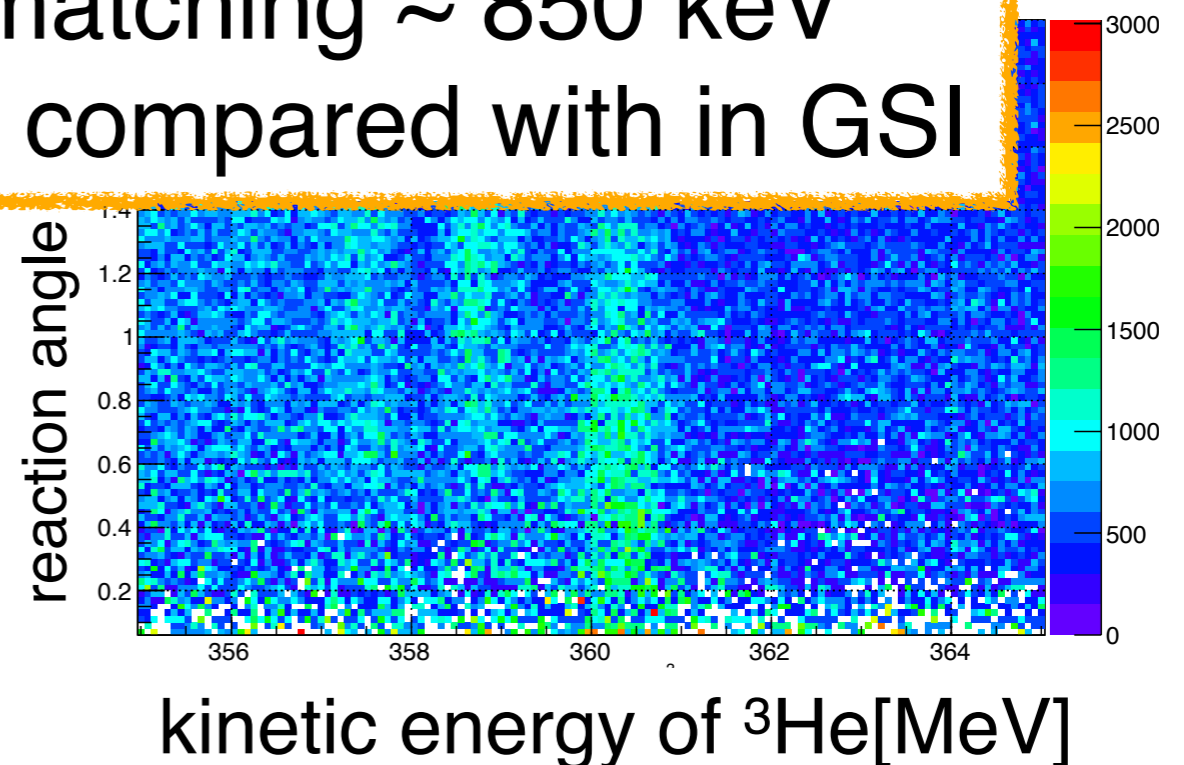


**First observation of the angular dependence!**

# $d^2\sigma/d\Omega dE$ vs $T_{He}$ Spectra



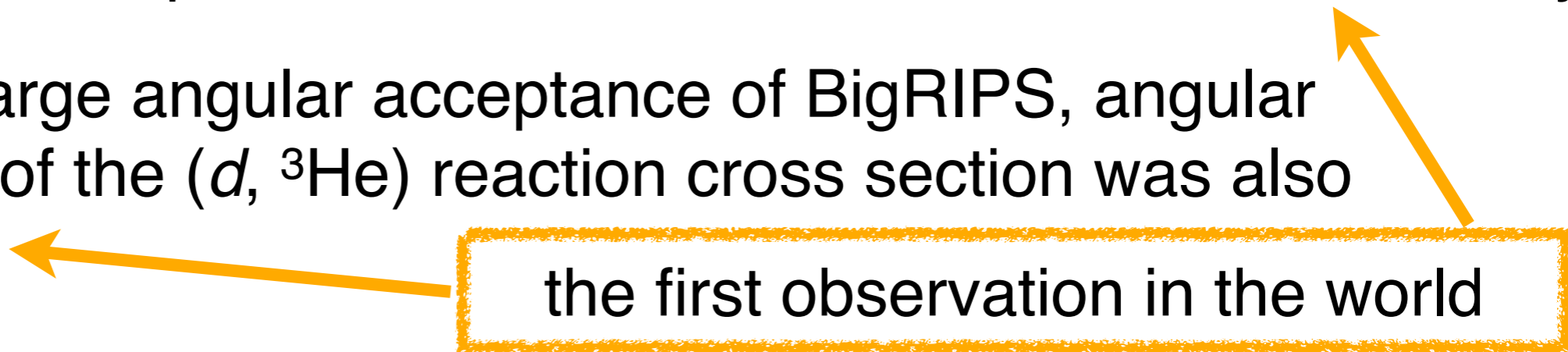
resolution ~ comparable with **300 keV!**  
cf.) w/o dispersion matching ~ 850 keV  
in 1/7 short beam time compared with in GSI



# *Summary and future works*

- We constructed new optics using dispersion matching with primary beam at RIBF, RIKEN for deeply-bound pionic atom experiment.
- We performed the pilot experiment with the target of  $^{122}\text{Sn}$ .
- The deeply bound pionic states in  $^{121}\text{Sn}$  was observed successfully.
- Thanks for large angular acceptance of BigRIPS, angular dependence of the  $(d, ^3\text{He})$  reaction cross section was also observed.
- Now we are finalizing the result of the pilot experiment to extract binding energy and width of deeply bound pionic states.
- In the main experiment, we will optimize the dispersion matching condition and improve the resolution.

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# *Ongoing other projects in our group*

Feasibility study of inverse kinematics  
for pionic atom  $\rightarrow$  pionic unstable nuclei

$\eta'$  mesic nuclei by using  $C(p,d)$  reaction  
@GSI

(2.5 GeV proton / high resolution spectrometer)