

The COMPASS program with the muon beam: past, present and future

Andrea Bressan

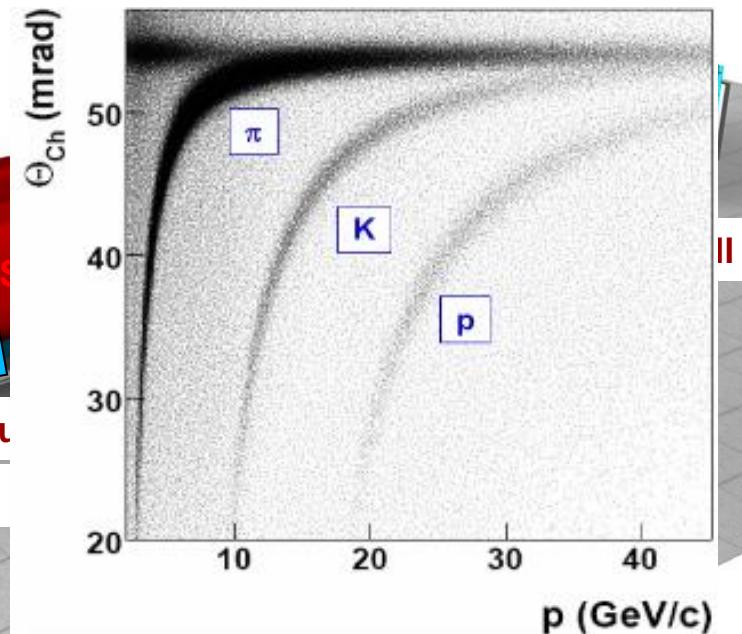
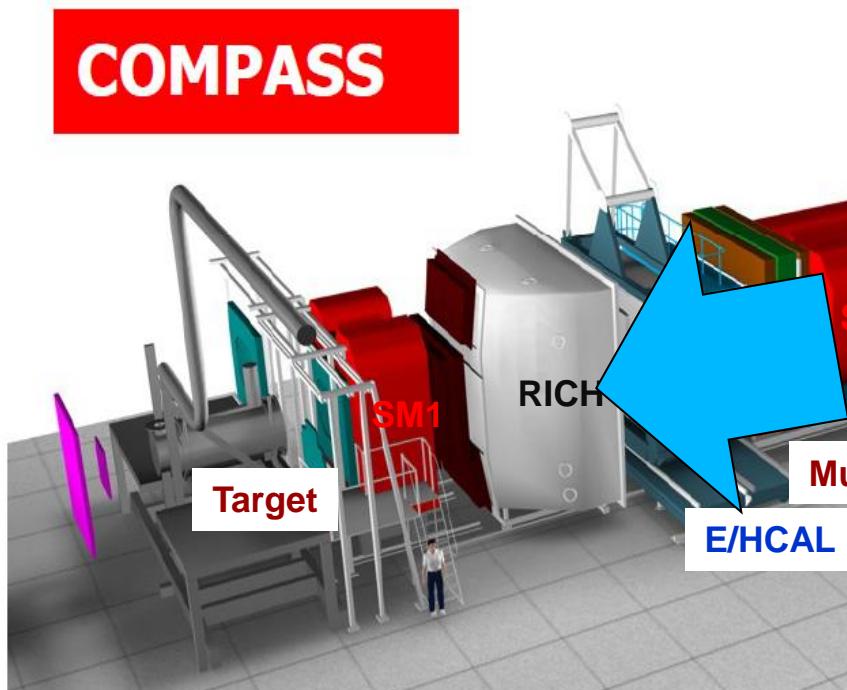
University of Trieste and INFN
(on behalf of the COMPASS Collaboration)

THE HTH CIRCUM-PAN-PACIFIC SYMPOSIUM ON HIGH ENERGY SPIN PHYSICS
27-30 AUGUST 2019, MIYAZAKI, JAPAN

Muon beam: SIDIS setup

- high energy beam
- large angular acceptance
- broad kinematical range

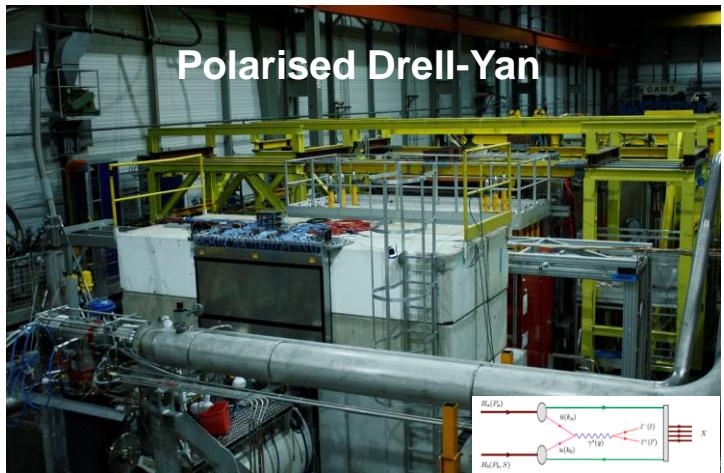
two stages spectrometer
 radiator C₂F₄ + He
 Large Angle Spectrometer (SM)
 K ~ 10 GeV/c
 Small Angle Spectrometer (SM2)



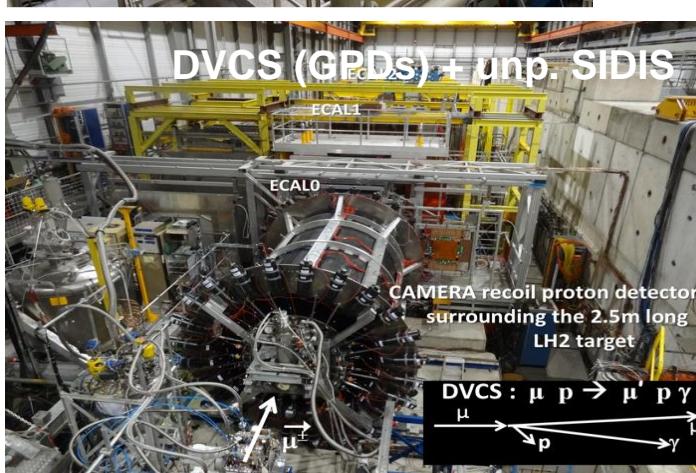
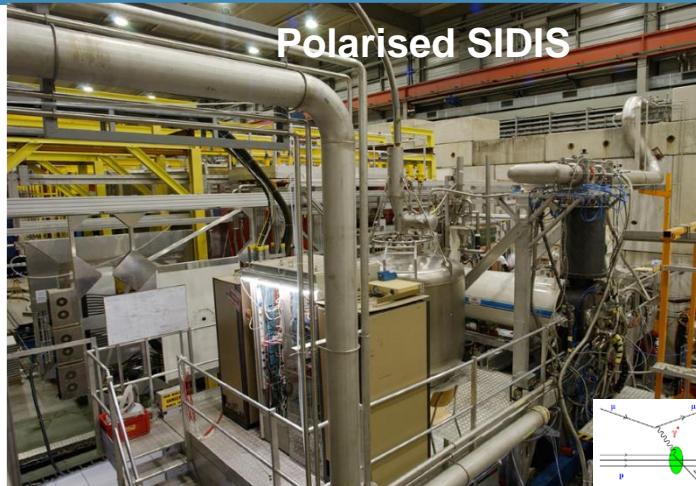
COMPASS target area



COMPASS-I
1997-2011



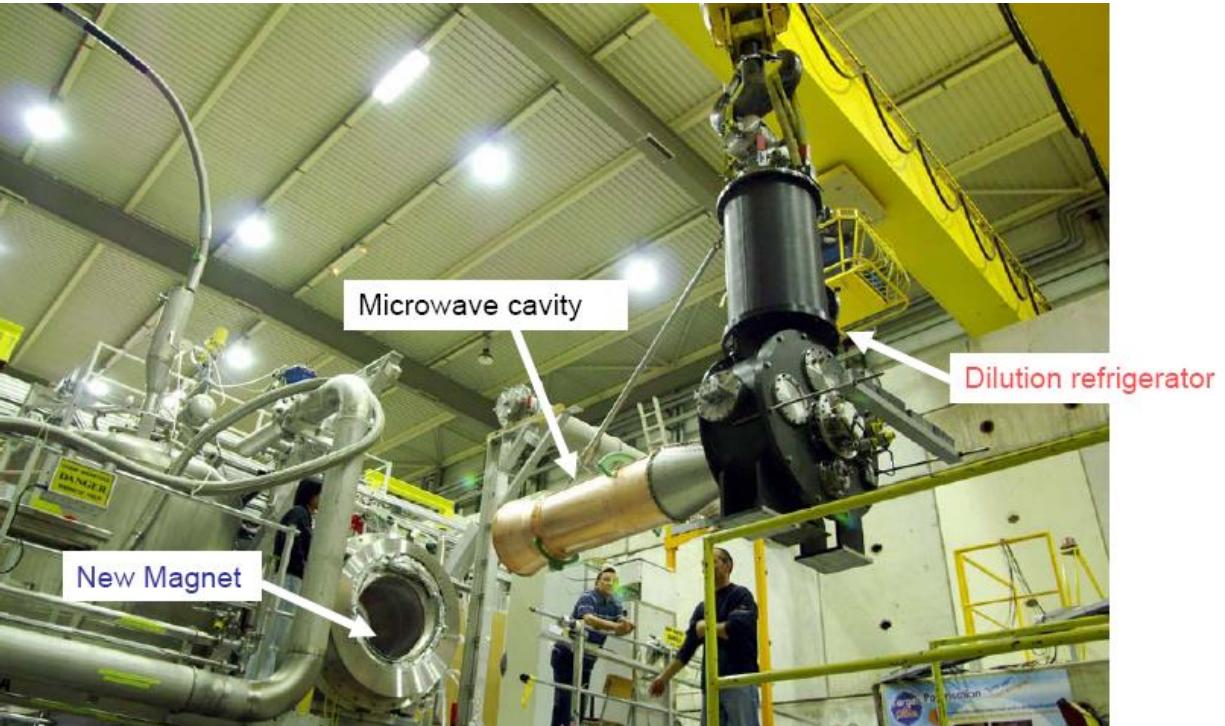
COMPASS-II
2012-2020



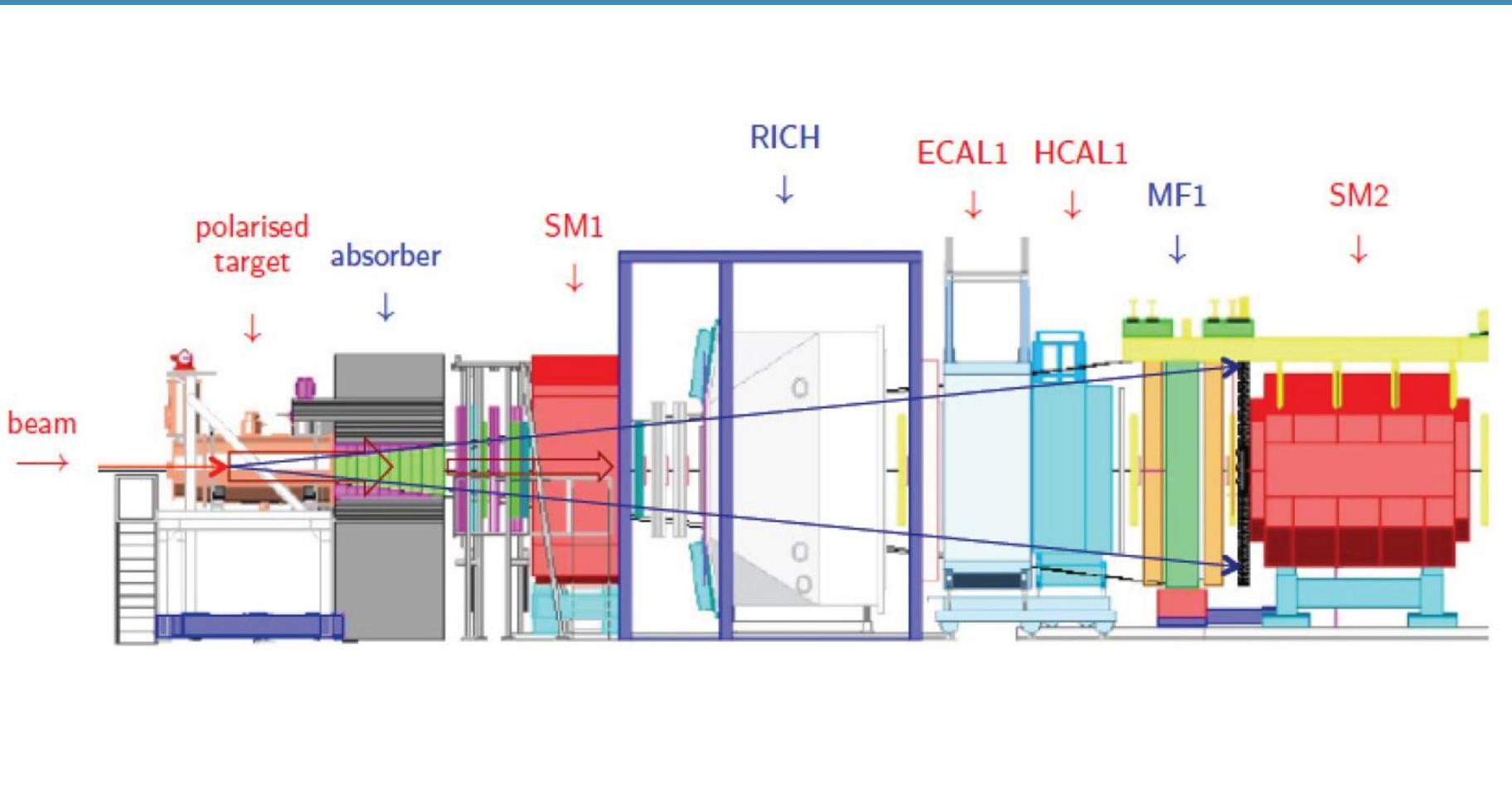
Operations on the target area



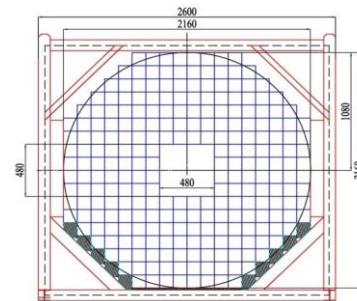
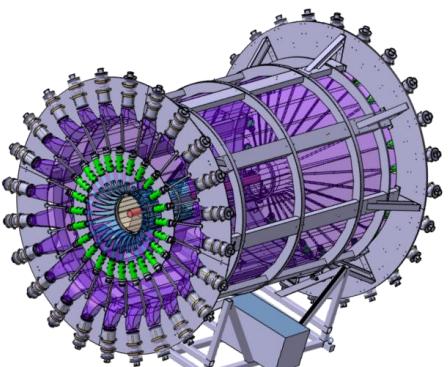
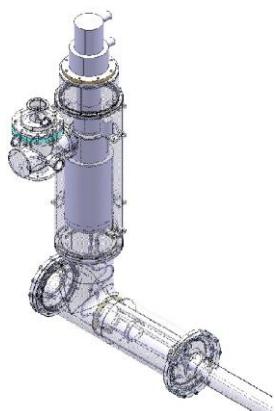
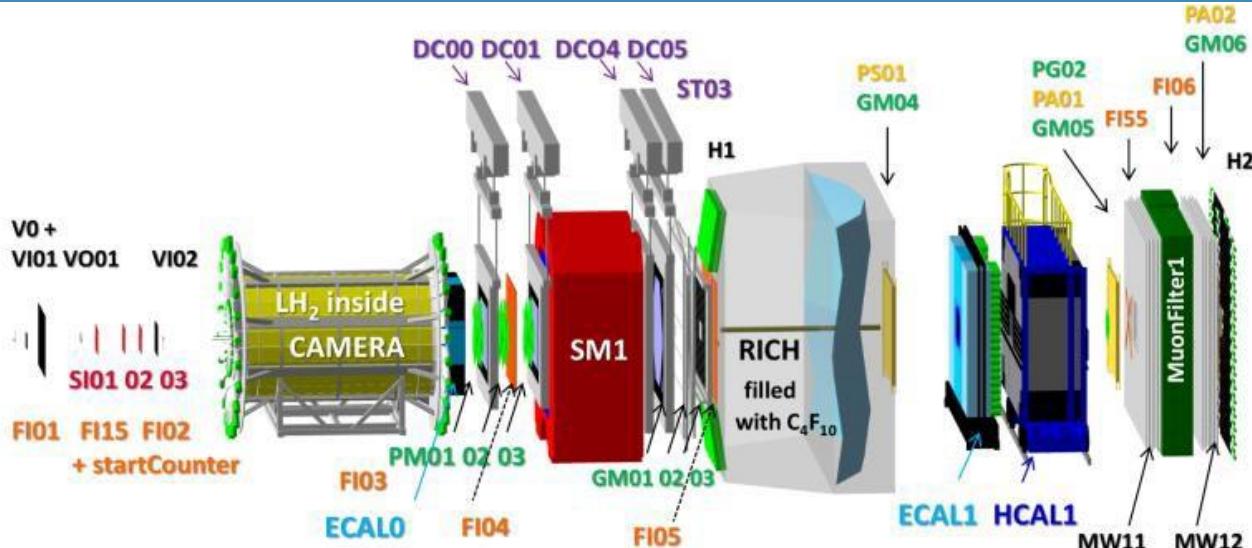
Targets



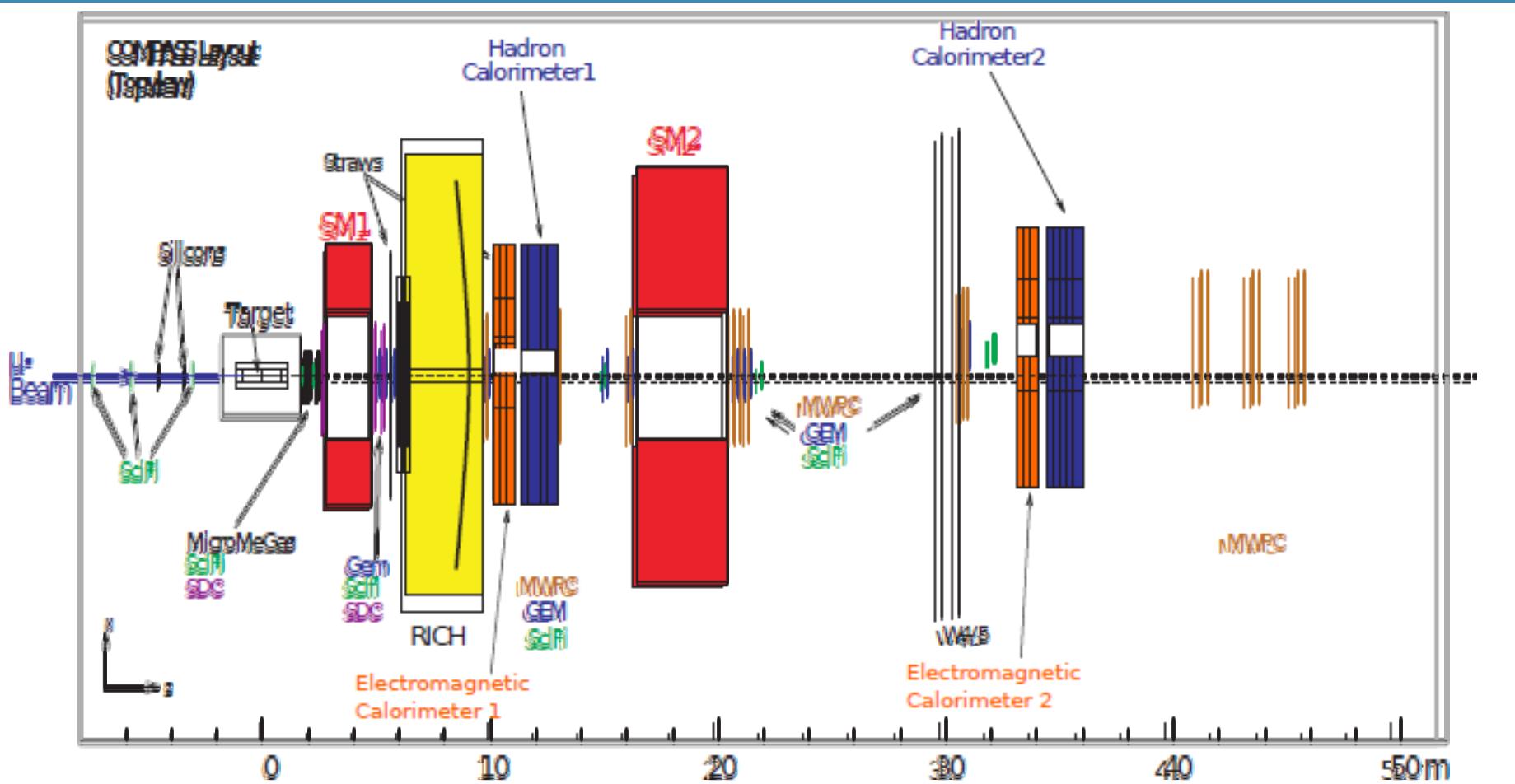
Hadron beam: Drell-Yan setup



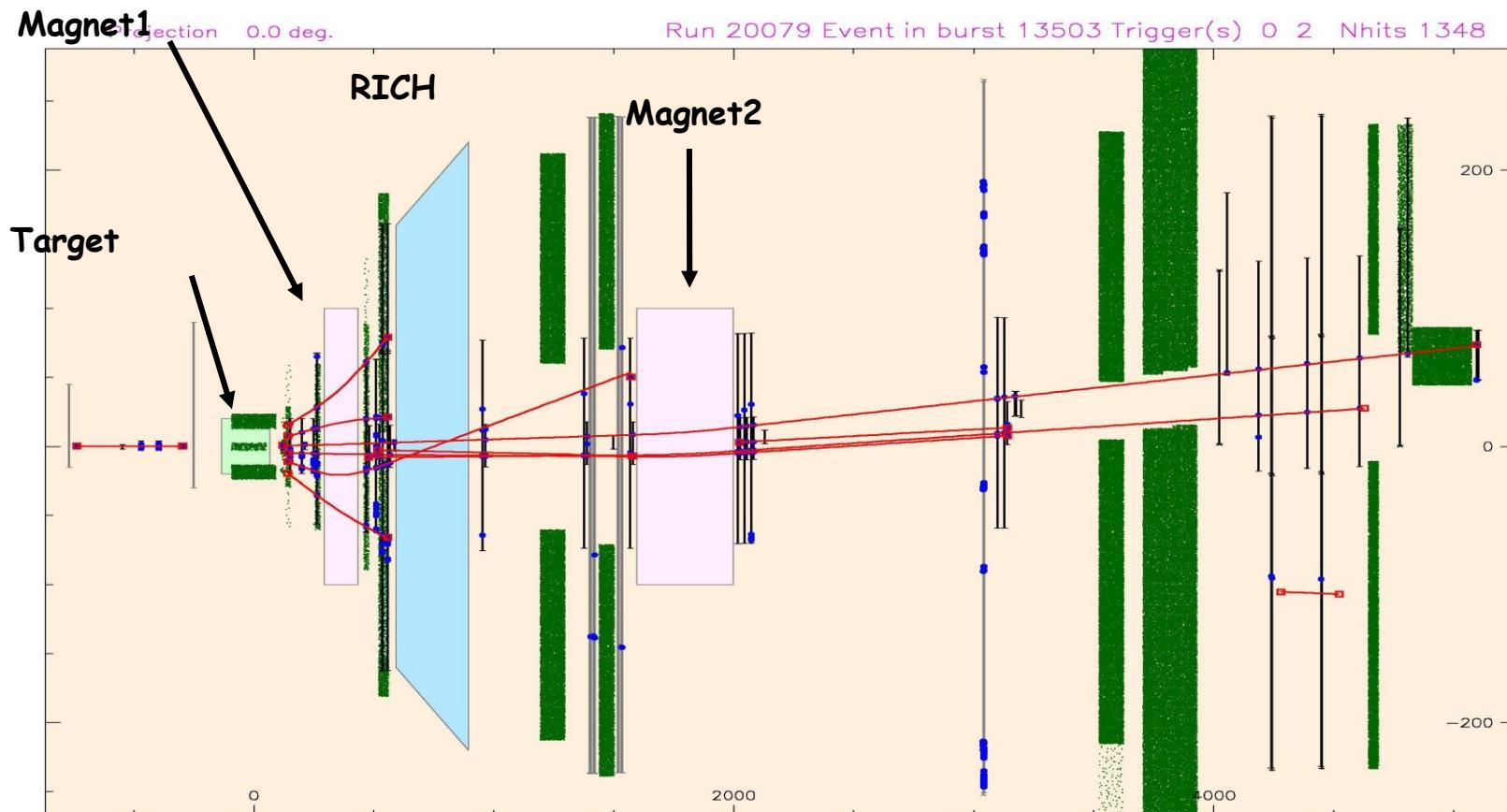
Muon beam – DVCS setup



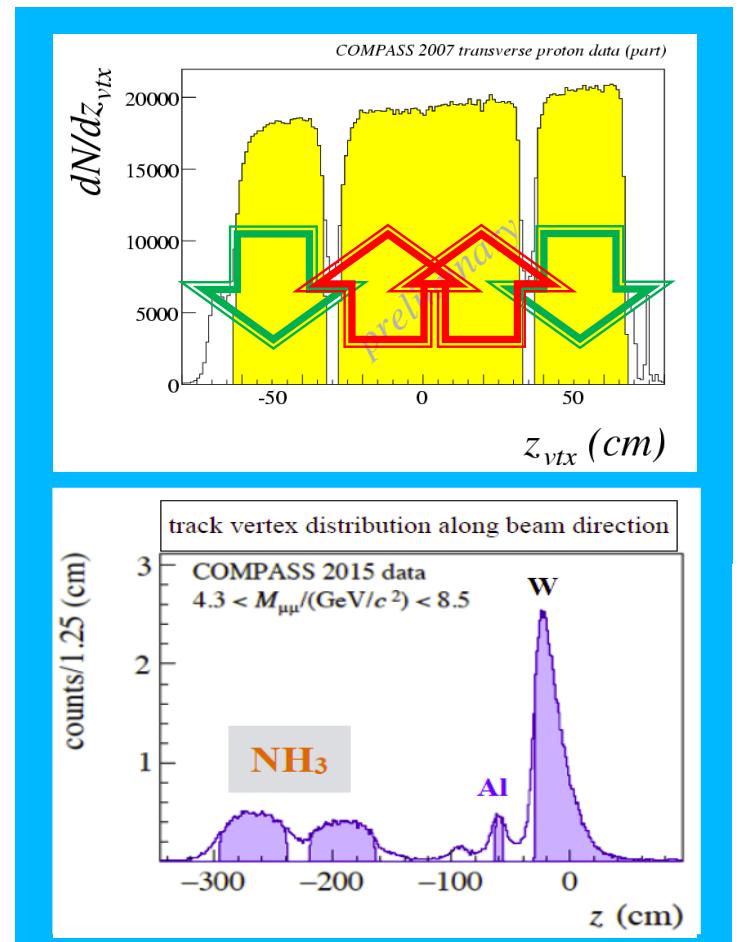
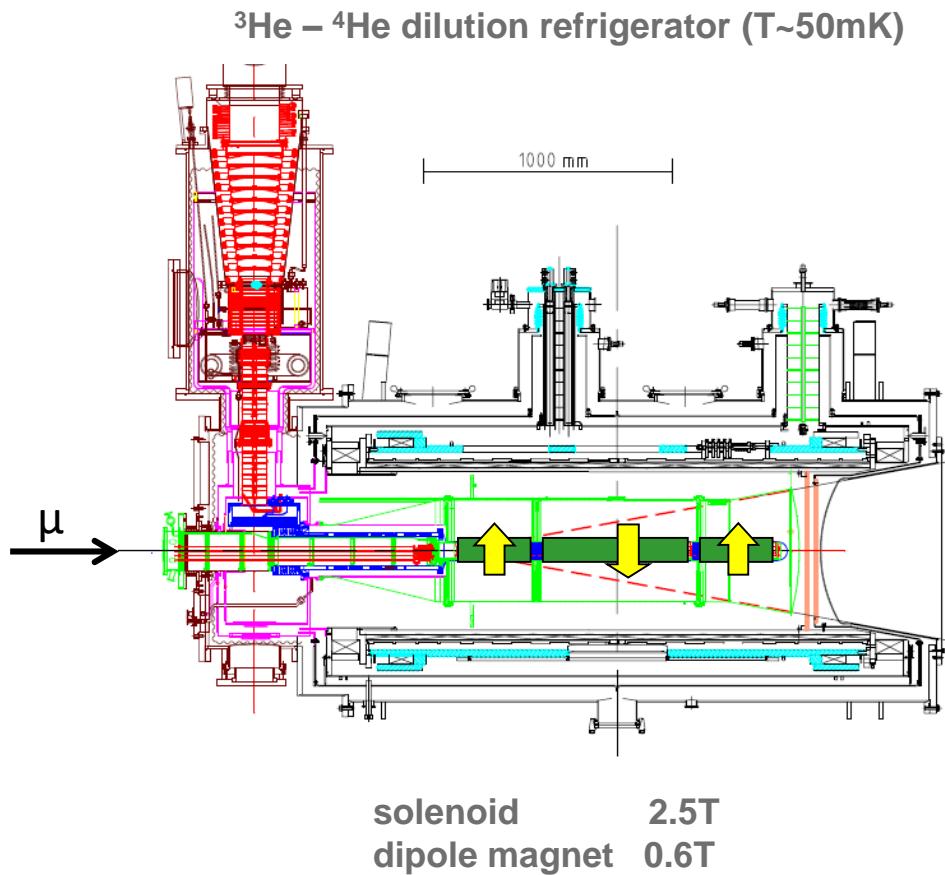
Spectrometer elements



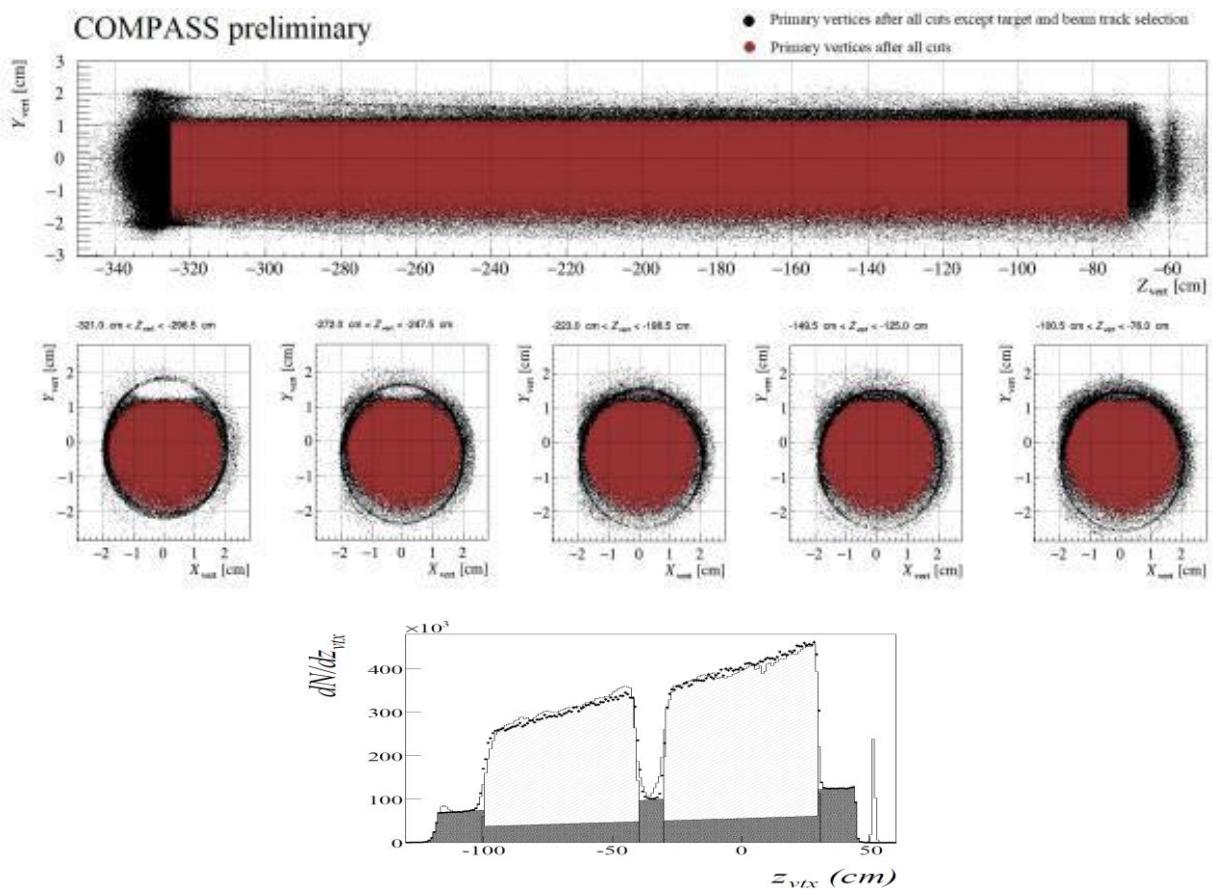
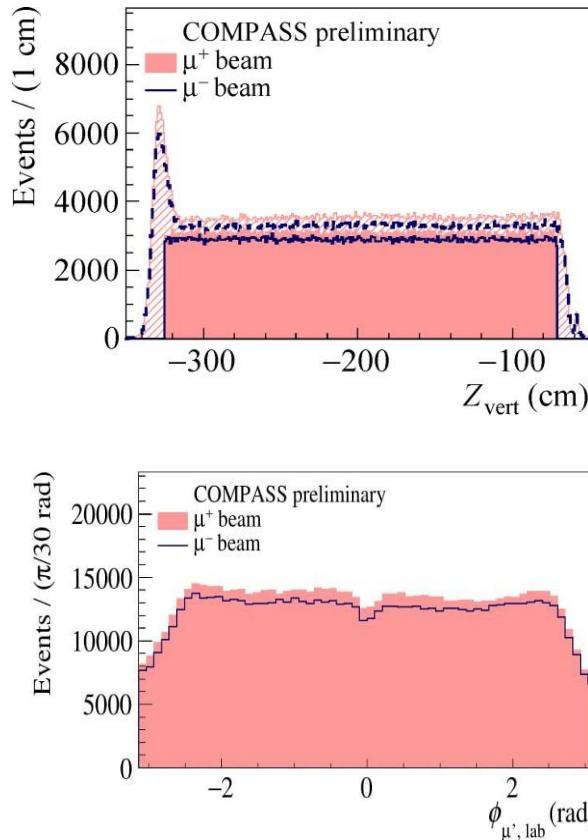
Spectrometer: momentum determination



the polarized target system (>2005)



Vertex determination



COMPASS data taking

muon beam	deuteron (${}^6\text{LiD}$) PT	2002 2003 2004	80% L/20% T target polarisation
		2006	L target polarisation
	proton (NH_3) PT	2007	50% L /50% T target polarisation
Hadron	LH target	2008 2009	
muon beam	proton (NH_3) PT	2010	T target polarisation
		2011	L target polarisation
Hadron	Ni target	2012	Primakoff
muon beam	LH2 target	2012	Pilot DVCS & unpol. SIDIS
Hadron	Proton (NH_3) DT PT	2014 2015 2018	Pilot DY run DY run DY run
muon beam	LH2 target	2016 2017	DVCS & unpol. SIDIS

Measurements with the target longitudinally polarized:



Year	Obs.	
2006	$A_{LL}^{2h}(Q^2 < 0)$	$\Delta g/g$
2007	$g_1^d(x),$	$\Gamma_1^d, \Delta\Sigma$
2008	$A_{1,d}^{h^+ - h^-}$	$\Delta u_v + \Delta d_v$
2009	$A_{1,d}, A_{1,d}^{\pi^\pm}, A_{1,d}^{K^\pm}$	$\Delta u_v + \Delta d_v, \Delta \bar{u} + \Delta \bar{d}, \Delta s (= \Delta \bar{s})$
2010	$g_1^p(x),$	$\Gamma_1^{NS}, g_A/g_V $
2010	$A_{1,d}, A_{1,d}^{\pi^\pm}, A_{1,d}^{K^\pm}, A_{1,p}, A_{1,p}^{\pi^\pm}, A_{1,p}^{K^\pm}$	$\Delta u, \Delta d, \Delta \bar{u}, \Delta \bar{d}, \Delta \bar{d}, \Delta s, \Delta \bar{s}$
2010	$\sin \phi, \sin 2\phi, \sin 3\phi, \cos \phi$ asymms	$h_L, f_L^\perp, h_1, f_{1T}^\perp, h_{1L}^\perp, h_{1T}^\perp, h_{1L}^\perp, g_L^\perp, g_{1T}$
2013	A_{LL}^{2h}	$\Delta g/g$
2013	$A_D^{\gamma N}$	$\Delta g/g$ in LO and NLO
2015	$g_1^p(x)$	$\Gamma_1^{NS}, \Delta\Sigma, \Delta u + \Delta \bar{u} \dots$
2015	A_{LL}^p	NLO QCD fits for $\Delta g/g$
2016	$A_{UL}^{\sin \phi_h}, A_{UL}^{\sin 2\phi_h}, A_{UL}^{\cos \phi_h} \dots$	TSA on L polarized NH ₃ target

Measurements with the target transversely polarized:



Year	Obs	
2005	$A_{Siv,d}^h, A_{Col,d}^h$	First ${}^6\text{LiD}$ data
2006	$A_{Siv,d}^h, A_{Col,d}^h$	Full ${}^6\text{LiD}$ statistics
2009	$A_{Siv,d}^{\pi^\pm, K^\pm, K_S^0}, A_{Col,d}^{\pi^\pm, K^\pm, K_S^0}$	Full ${}^6\text{LiD}$ statistics
2010	$A_{Siv,p}^h, A_{Col,p}^h$	2007 NH_3 data
2012	$A_{UT,d}^{\sin\phi_{RS}}, A_{UT,p}^{\sin\phi_{RS}}$	Full ${}^6\text{LiD}$
2012	$A_{Siv,p}^h, A_{Col,p}^h$	Full NH_3 statistics
2012	$A_{UT,d}^{\sin(\phi_\rho - \phi_S)}, A_{UT,p}^{\sin(\phi_\rho - \phi_S)}$	Exclusive ρ^0
2013	$A_{UT,d}^{(\phi_\rho, \phi_S)}, A_{UT,p}^{(\phi_\rho, \phi_S)}$	Exclusive ρ^0 , all asymms.
2014	$A_{UT,d}^{\sin\phi_{RS}}, A_{UT,p}^{\sin\phi_{RS}}$	Full ${}^6\text{LiD}$ and NH_3
2014	$A_{Siv,d}^{\pi^\pm, K^\pm, K_S^0}, A_{Col,d}^{\pi^\pm, K^\pm, K_S^0}$	Full NH_3 statistics
2015	Interplay $A_{UT,p}^{\sin\phi_{RS}}$ vs $A_{Col,p}^h$	Full NH_3 statistics

Measurements with the target transversely polarized :



Year	Obs	
2016	P_{hT} -weighted $A_{Siv,p}^h$	2010 NH ₃ data
2016	$A_{Siv,p}^g, A_{Col,p}^g$	2010 NH ₃ data, gluon Sivers
2017	$P_\Lambda(x, z)$	Transversely transmitted Λ 2010 NH ₃

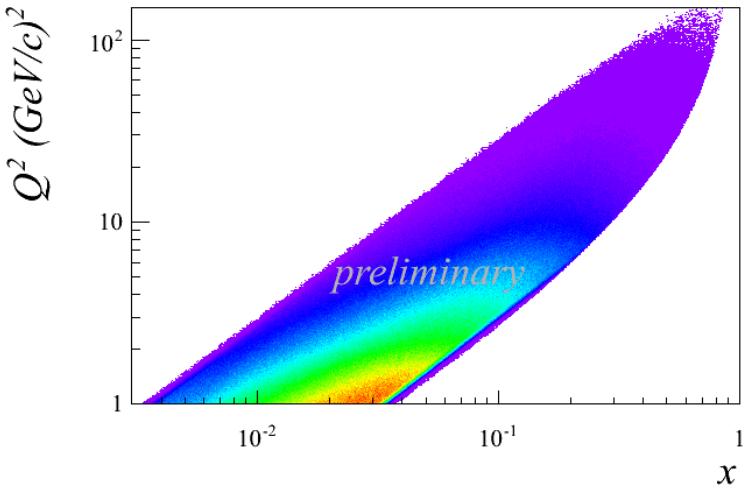
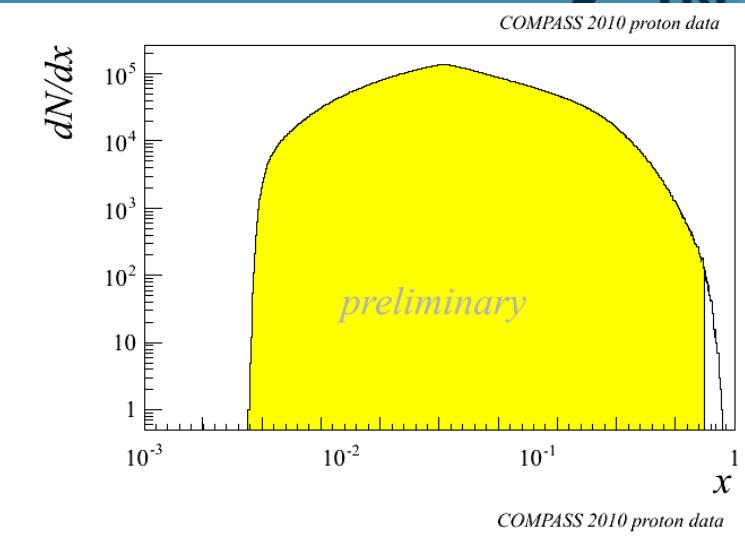
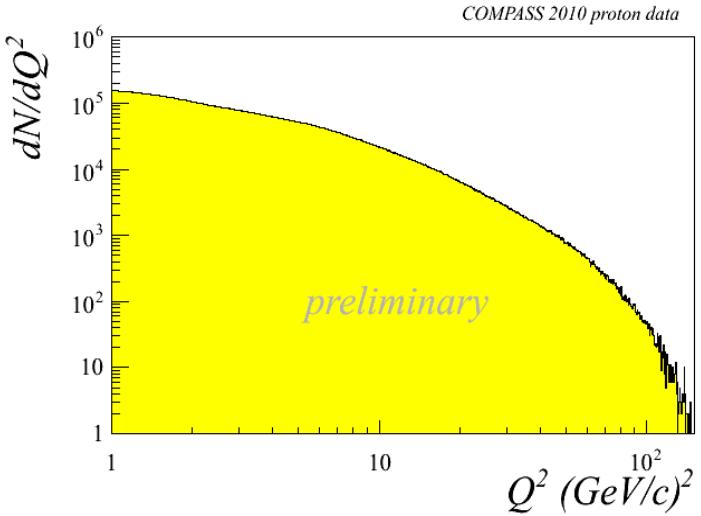
Measurements with unpolarised targets:

Year	Obs	
2013	$dn^h/(dN^\mu dz dp_T^2)$	multiplicities on d, 2004
2014	$A_{UU,d}^{\cos \phi_h}, A_{UU,d}^{\cos 2\phi_h}, A_{LU,d}^{\sin \phi_h}$	2004, part
2016	$dn^\pi/(dN^\mu dz)$	multiplicities on d, 2006
2016	$dn^h/(dN^\mu dz dp_T^2)$	multiplicities on d, 2006
2016	$dn^K/(dN^\mu dz)$	multiplicities on d, 2006
2017	$[dn^{K^+}/(dN^\mu dz)]/[dn^{K^-}/(dN^\mu dz)]$	Multiplicity ratios for k on d, 2006
2018	SDME modulation for ω	Liquid H ₂ , 2012 data
2018	$A_{UU,d}^{\cos \phi_h}, A_{UU,d}^{\cos 2\phi_h}, A_{LU,d}^{\sin \phi_h}$	Liquid H ₂ , 2016 data, part
2019	$dn^{\pi,K,p}/(dN^\mu dz)$	multiplicities on p, 2016
2019	$dn^h/(dN^\mu dz dp_T^2)$	p_T^2 -dep multiplicities on p, 2016

Kinematic distributions

INFN

DIS cuts: $Q^2 > 1 \text{ (GeV/c)}^2$
 $0.1 < y < 0.9$
 $W > 5 \text{ GeV/c}^2$



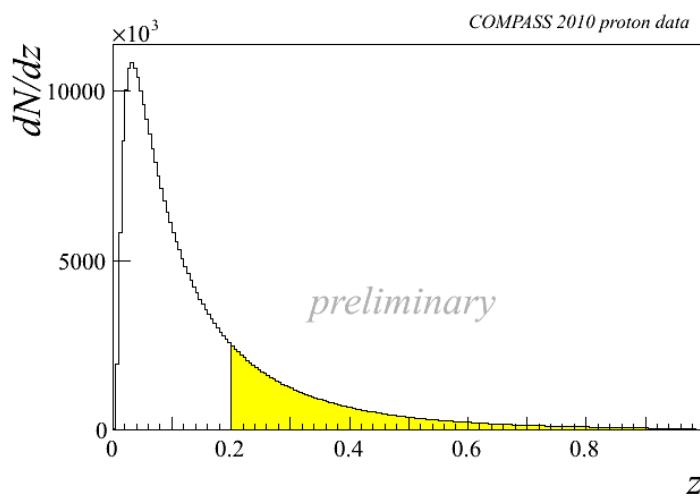
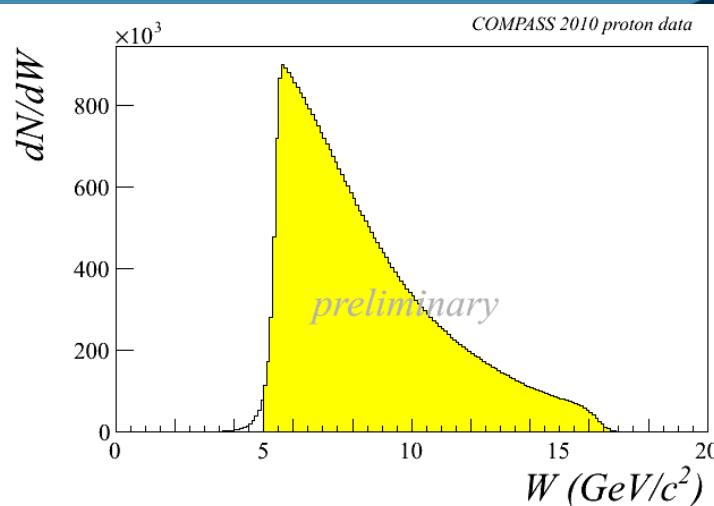
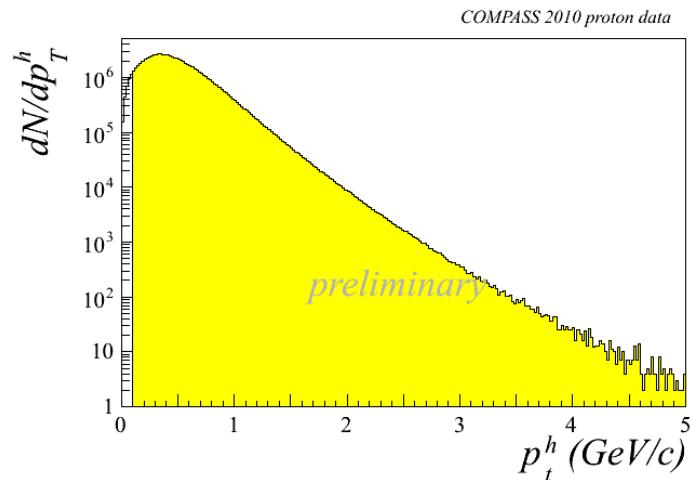
Kinematic distributions - 2

DIS cuts: $Q^2 > 1 \text{ (GeV/c)}^2$

$0.1 < y < 0.9$

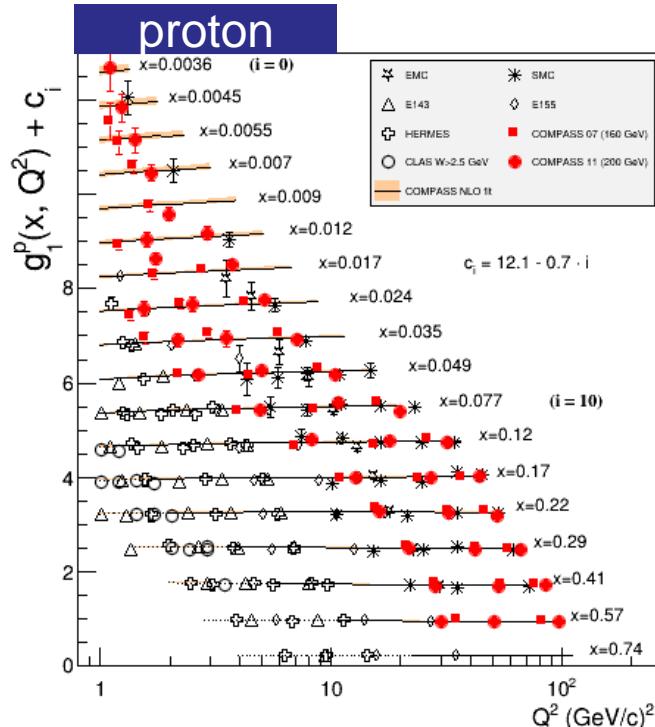
$W > 5 \text{ GeV/c}^2$

hadron selection: $P_{hT} > 0.1 \text{ GeV/c},$
 $z > 0.2$



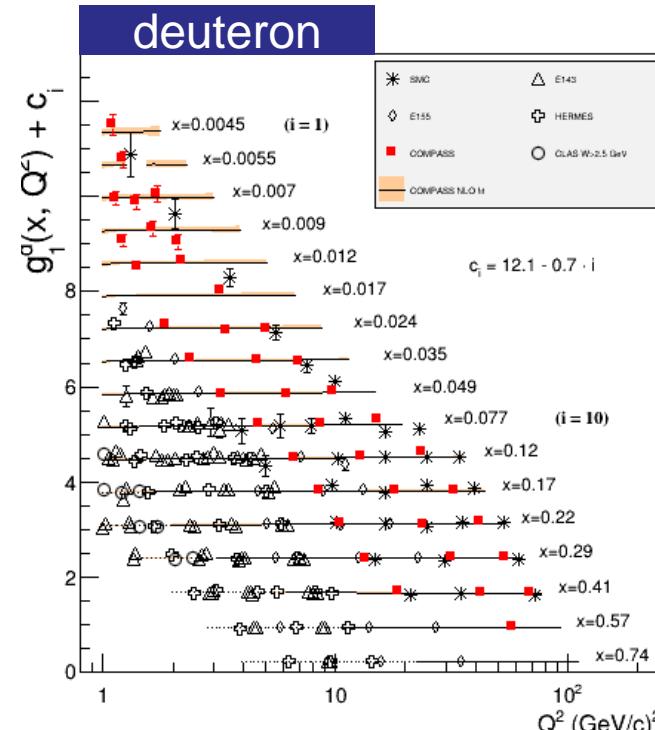
QCD fits- World data on g_1^p and g_1^d

→ $g_1(x, Q^2)$ as input to global QCD fits
for extraction of $\Delta q_f(x)$ and $\Delta g(x)$



x and Q^2 coverage not yet sufficient for precise Δg
Can be improved by constraining from pp data (as DSSV, NNPDF...)

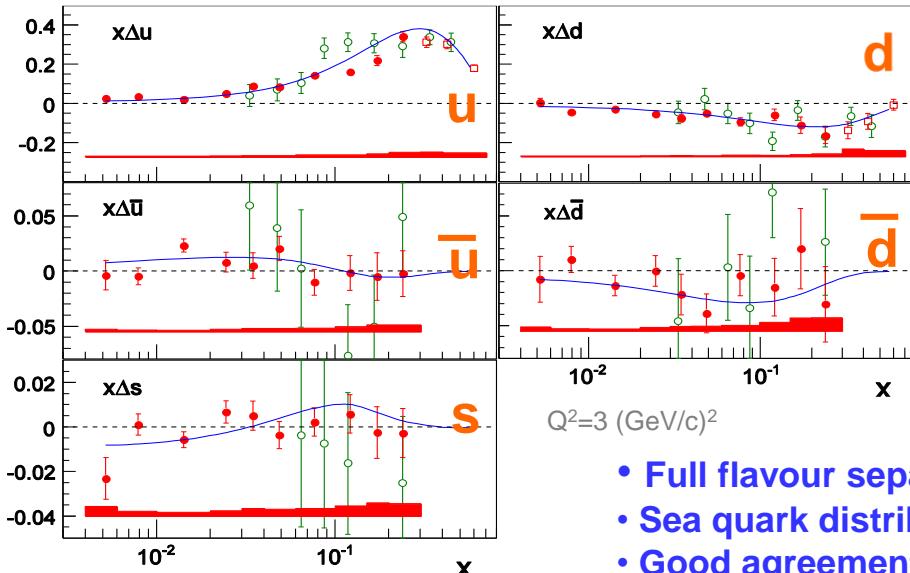
$$\frac{dg_1}{d \ln Q^2} \propto -\Delta g(x, Q^2)$$



PLB753 (2016) 18

Quark helicities from semi-inclusive DIS

Leading order extraction of quark helicities from spin asymmetries:



- **COMPASS**
PLB693(2010)227, using DSS FFs

- **HERMES**
PRD71(2005)012003

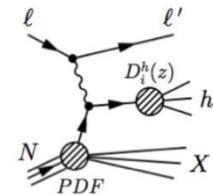
— DSSV at NLO



- Full flavour separation $\rightarrow x \sim 0.004$
- Sea quark distributions \sim zero
- Good agreement with global fits

What about Δs ? Integral is found negative from **inclusive** data, when imposing SU3 while here from **semi-inclusive** data, $x > \sim 0.005$ Δs is compatible with zero.

- NB:**
- The extraction assumes quark Fragmentation Functions known (DSS here)
 - No measurement at lower x

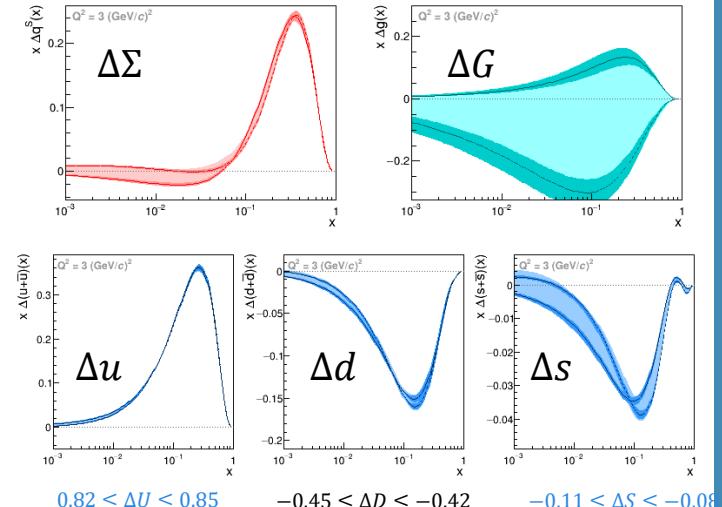


A NLO pQCD fit to g_1 DIS world data

- Assumes functional forms for $\Delta\Sigma$, ΔG and Δq^{NS} and SU3 symmetry
- Use DGLAP equations.
- Fit g_1^p , g_1^d , g_1^n DIS world data

→ Quark spin contribution :

$$\Delta\Sigma = 0.31 \pm 0.05 \text{ at } Q^2 = 3 \text{ (GeV/c)}^2$$



Uncertainties are dominated by the bad knowledge of the functional forms.

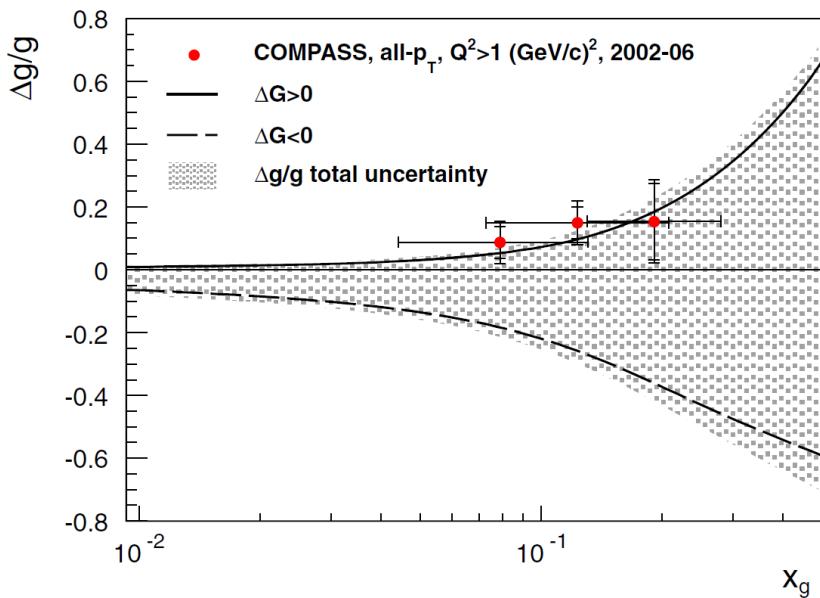
→ Gluon spin contribution: ΔG not well constrained, even the sign, using DIS only

Solution with $\Delta G > 0$ agrees with result from DSSV++ using RHIC pp data

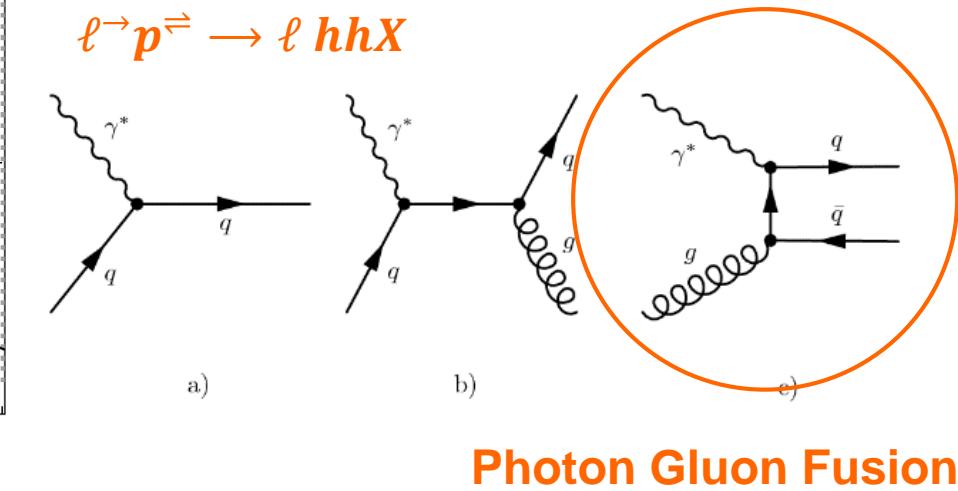
Gluon helicity $\Delta g/g$ from SIDIS

Extraction at LO:

$$\Delta G/G (x = 0.1) = 0.11 \pm 0.04 \pm 0.04$$



EPJC 77 (2017) 209



Photon Gluon Fusion

Summary on nucleon SPIN

$$\frac{1}{2} = \frac{1}{2} (\Delta u_v + \Delta u_v + \Delta q_s) + \Delta G + L_q + L_g$$

Quarks $\frac{1}{2} \Delta \Sigma \sim 0.15$ from g_1 measurements and global analysis at NLO. Largest uncertainty on $\Delta \Sigma$ due to uncertainty on ΔG

Gluons $\Delta G \sim 0.2$ integrated between $0.05 < x < 0.2$: precise result from RHIC. $\Delta G/G$ positive at $x \sim 0.1$ (from data of γg fusion process, at LO). Low- x contribution to integral still unknown. Not enough constrain from g_1 global analysis at NLO.

Orbital momenta: $L_q + L_g = ?$ Ongoing studies of GPDs.

Promising results from lattice QCD calculations:

→ The main question raised in ‘Nucleon spin crisis’ is resolved:

- Quark spin represents a non zero fraction (0.3) of nucleon spin
(measurements and lattice QCD calculations)
- The hypothesis of very large ΔG (2 to 3, associated to $L \sim -2 \div -3$) rejected

→ Puzzle still pending: share between ΔG and L

The spin content of the proton: where we stand



Gluons PDF are accessed using DGLAP! Equations

$$\frac{d}{dt} \Delta\Sigma(x, t) = \frac{\alpha_s(t)}{2\pi} \int_x^1 \frac{dy}{y} \left[P_{qq}^S \left(\frac{x}{y}, \alpha_s(t) \right) \Delta\Sigma(y, t) + 2n_f P_{qg} \left(\frac{x}{y}, \alpha_s(t) \right) \Delta g(y, t) \right]$$

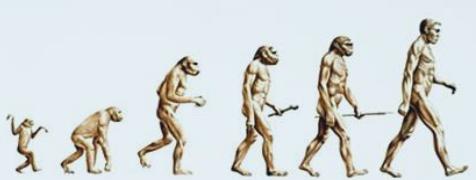
$$\frac{d}{dt} \Delta g(x, t) = \frac{\alpha_s(t)}{2\pi} \int_x^1 \frac{dy}{y} \left[P_{gq} \left(\frac{x}{y}, \alpha_s(t) \right) \Delta\Sigma(y, t) + P_{gg} \left(\frac{x}{y}, \alpha_s(t) \right) \Delta g(y, t) \right]$$

$$\frac{d}{dt} \Delta q_{NS}(x, t) = \frac{\alpha_s(t)}{2\pi} \int_x^1 \frac{dy}{y} P_{qq}^{NS} \left(\frac{x}{y}, \alpha_s(t) \right) \Delta q_{NS}(y, t)$$

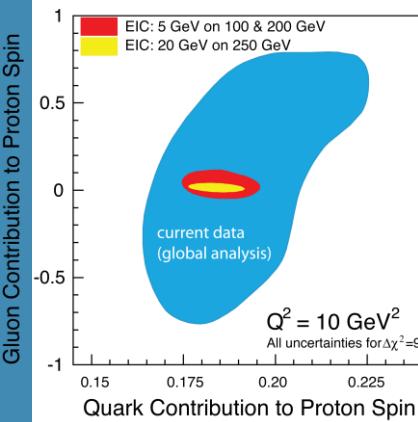
With $t = \ln Q^2/\Lambda^2$, $\Delta\Sigma(x, t) = \sum_{i=1}^{n_f} \Delta q_i$ and $\Delta q_{NS}(x, t) = \sum_{i=1}^{n_f} (e_i^2 / \langle e^2 \rangle - 1) \Delta q_i$,

where $\langle e^2 \rangle = \frac{1}{n_f} \sum_{i=1}^{n_f} e_i^2$

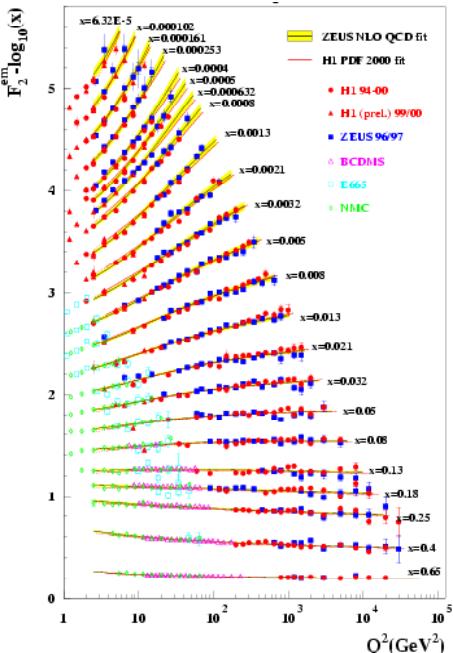
A very powerful tool access Δg , but limited by the present experimentally available phase space



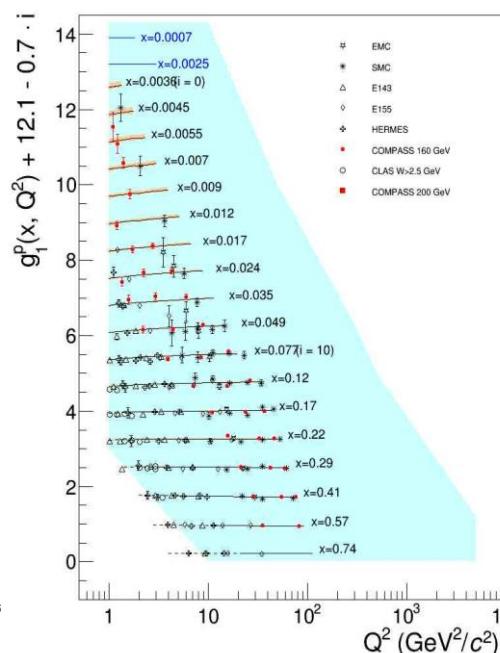
To answer to this we need and EIC



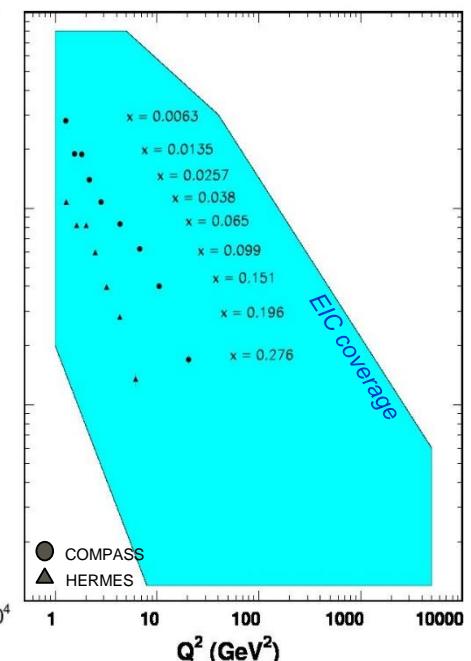
World Data on F_2^p



World Data on g_1^p



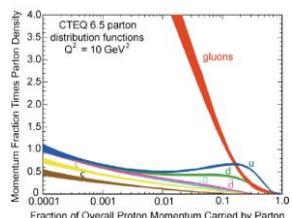
World Data on h_1^p



momentum

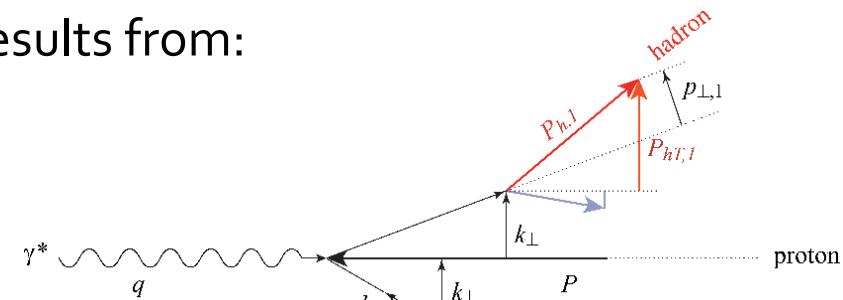
spin

transverse
spin ~ angular
momentum



Importance of unpolarized SIDIS

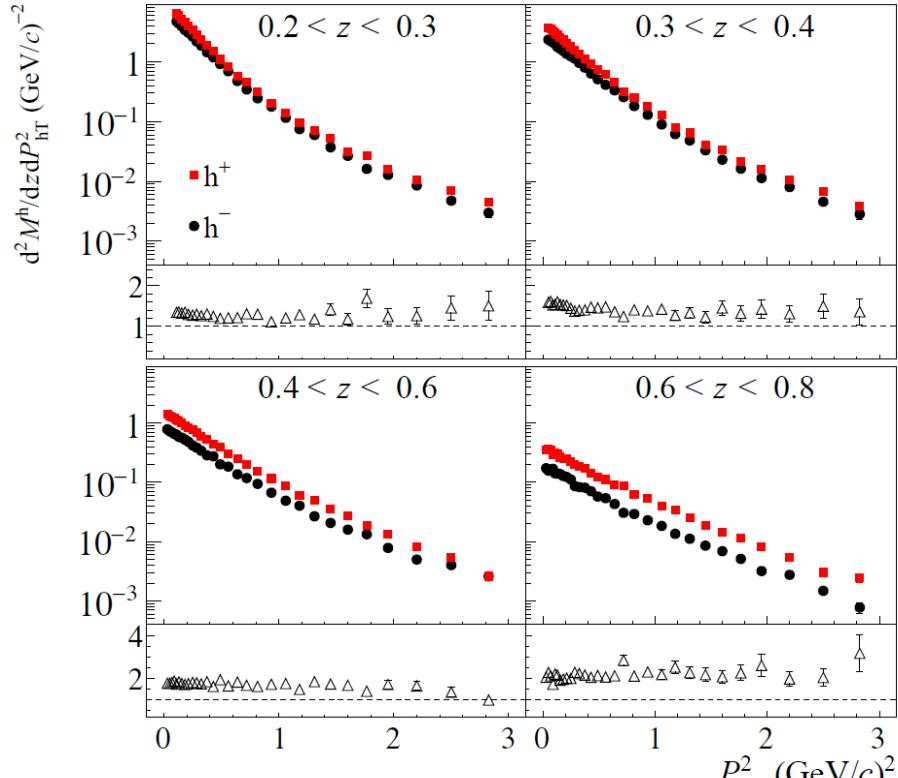
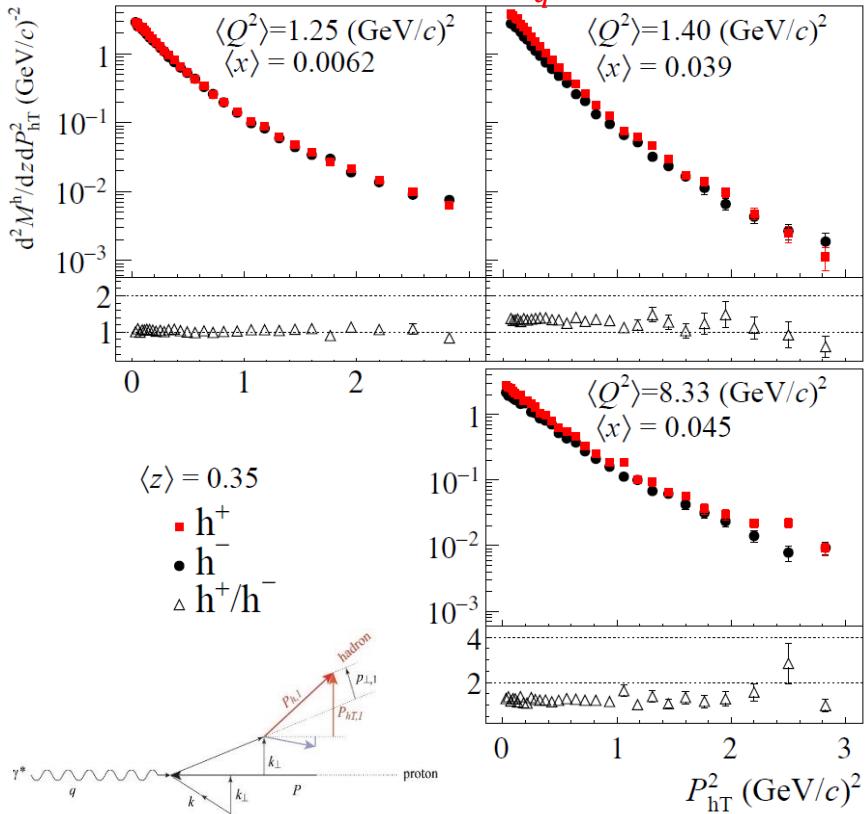
- The cross section dependence from P_{hT} results from:
 - intrinsic k_\perp of the quarks
 - p_\perp generated in the quark fragmentation



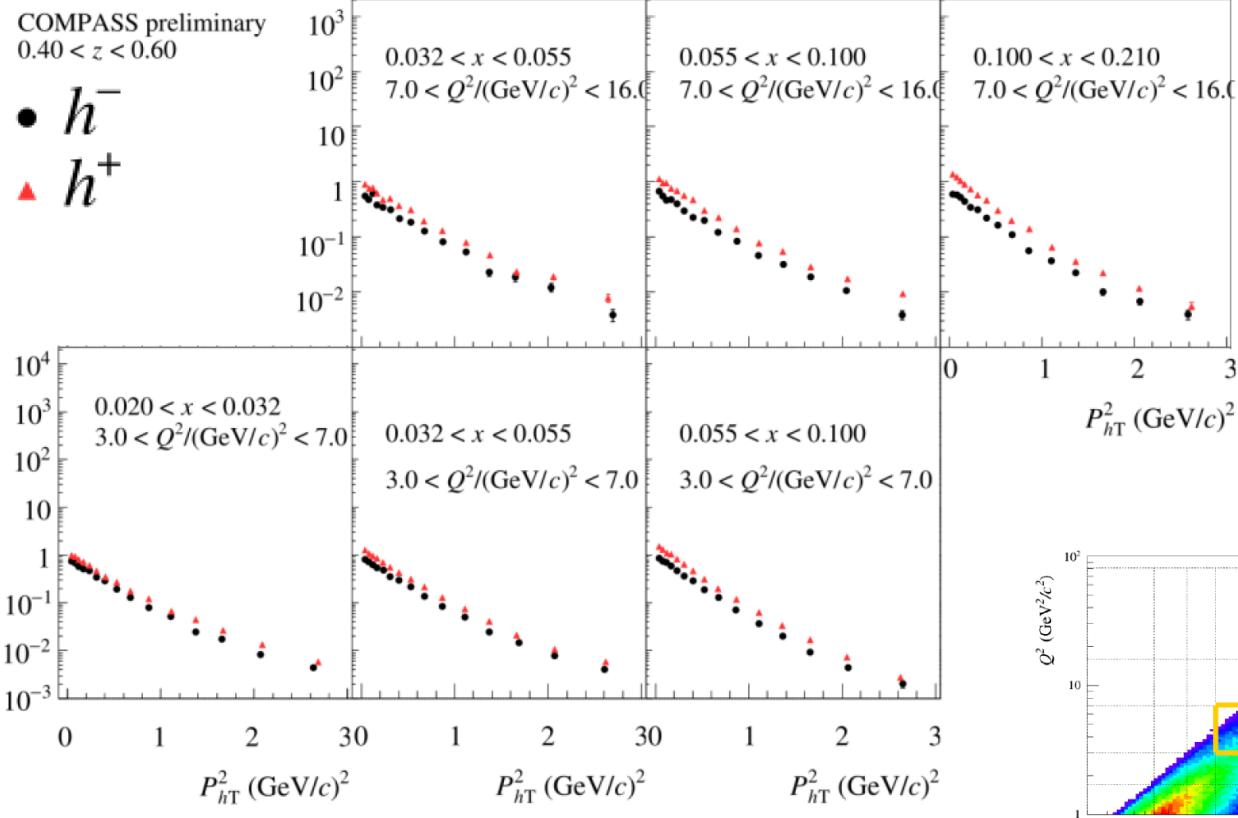
- The azimuthal modulations in the unpolarised cross sections comes from:
 - Intrinsic k_\perp of the quarks
 - The Boer-Mulders PDF
- Difficult measurements were one has to correct for the apparatus acceptance
- COMPASS and HERMES have**
 - results on 6LiD ($\sim d$) and preliminary on p from COMPASS
 - d and p from HERMESS
- ⇒COMPASS-II, measurements on LH_2 in parallel with DVCS**

Positive vs Negative charged hadrons (${}^6\text{LiD}$)

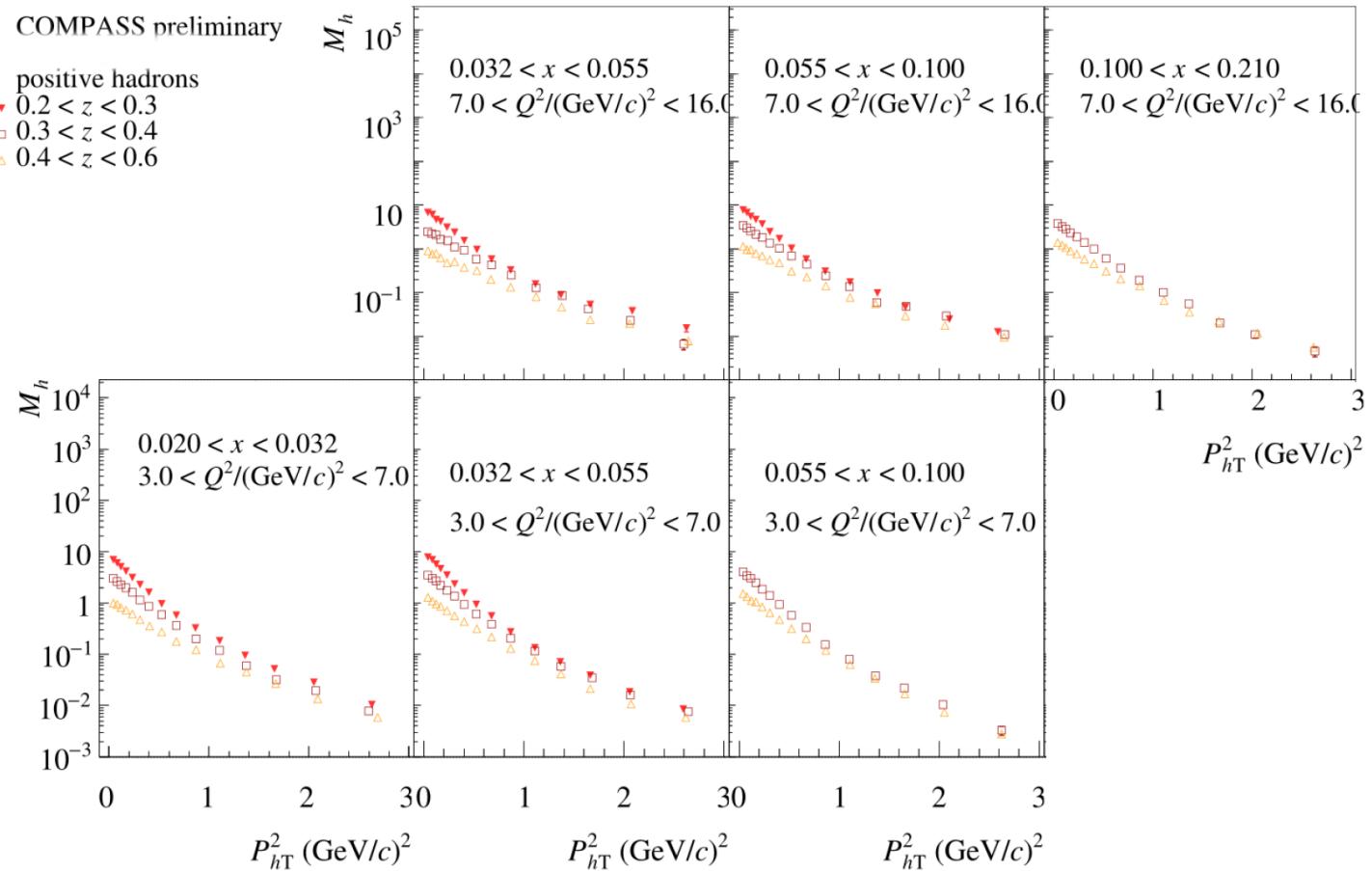
$$F_{UU}^h(x, z, P_{hT}^2; Q^2) = x \sum_q e_q^2 \int d^2 \vec{k}_\perp d^2 \vec{p}_\perp \delta(\vec{p}_\perp + z \vec{k}_\perp - \vec{P}_{hT}) f_1^q(x, k_\perp^2; Q^2) D_1^{q \rightarrow h}(z, p_\perp^2; Q^2)$$



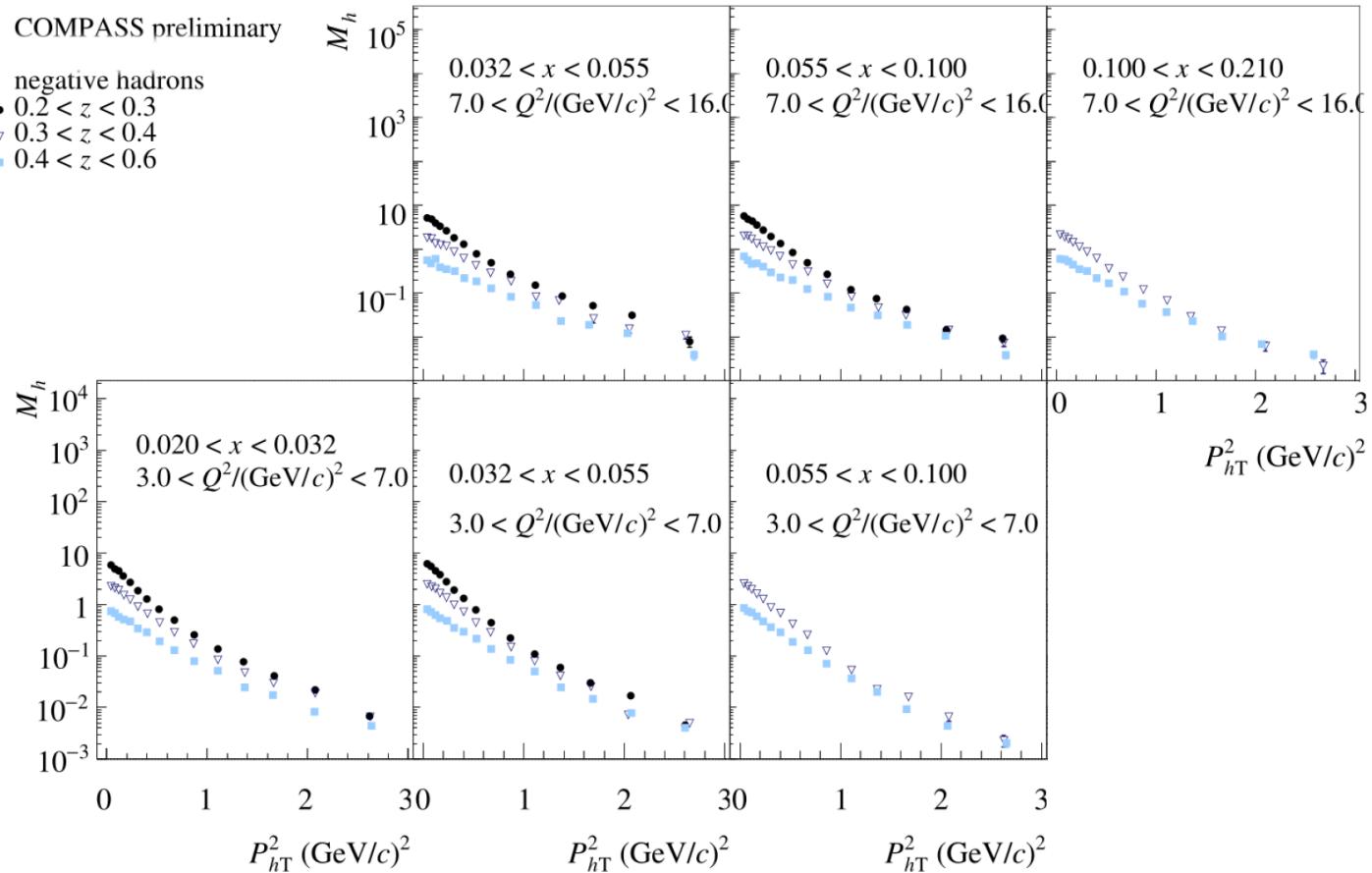
Positive vs Negative charged hadrons (p)



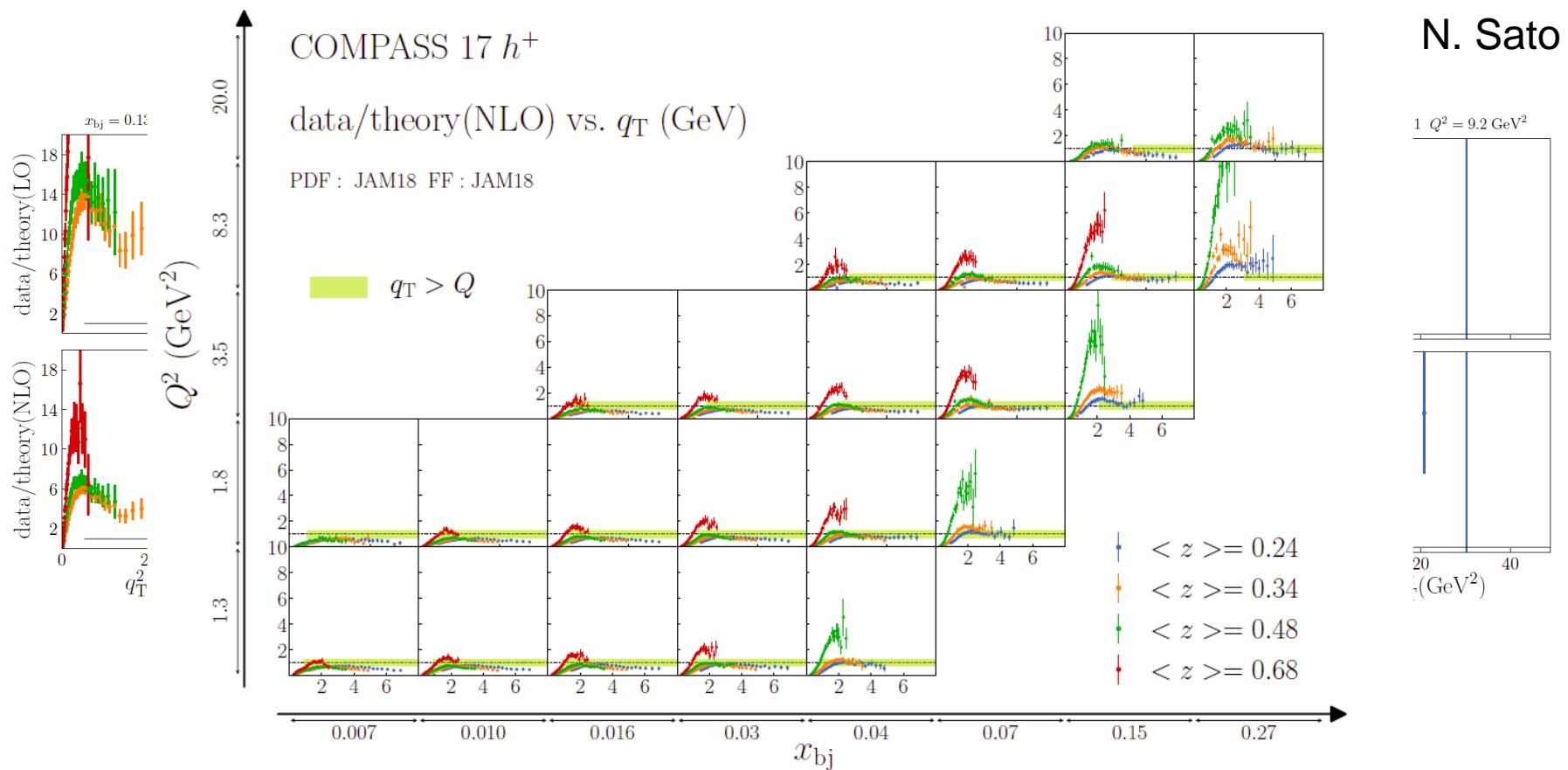
Positive charged hadrons (p)



Negative charged hadrons (p)



The matching problem ($q_T/Q > 1$ region)



Unpolarised Azimuthal Modulation



When looking at the content of the structure functions/modulations in terms of TMD PDFs for the $\cos \phi_h$ and $\cos 2\phi_h$ we can write:

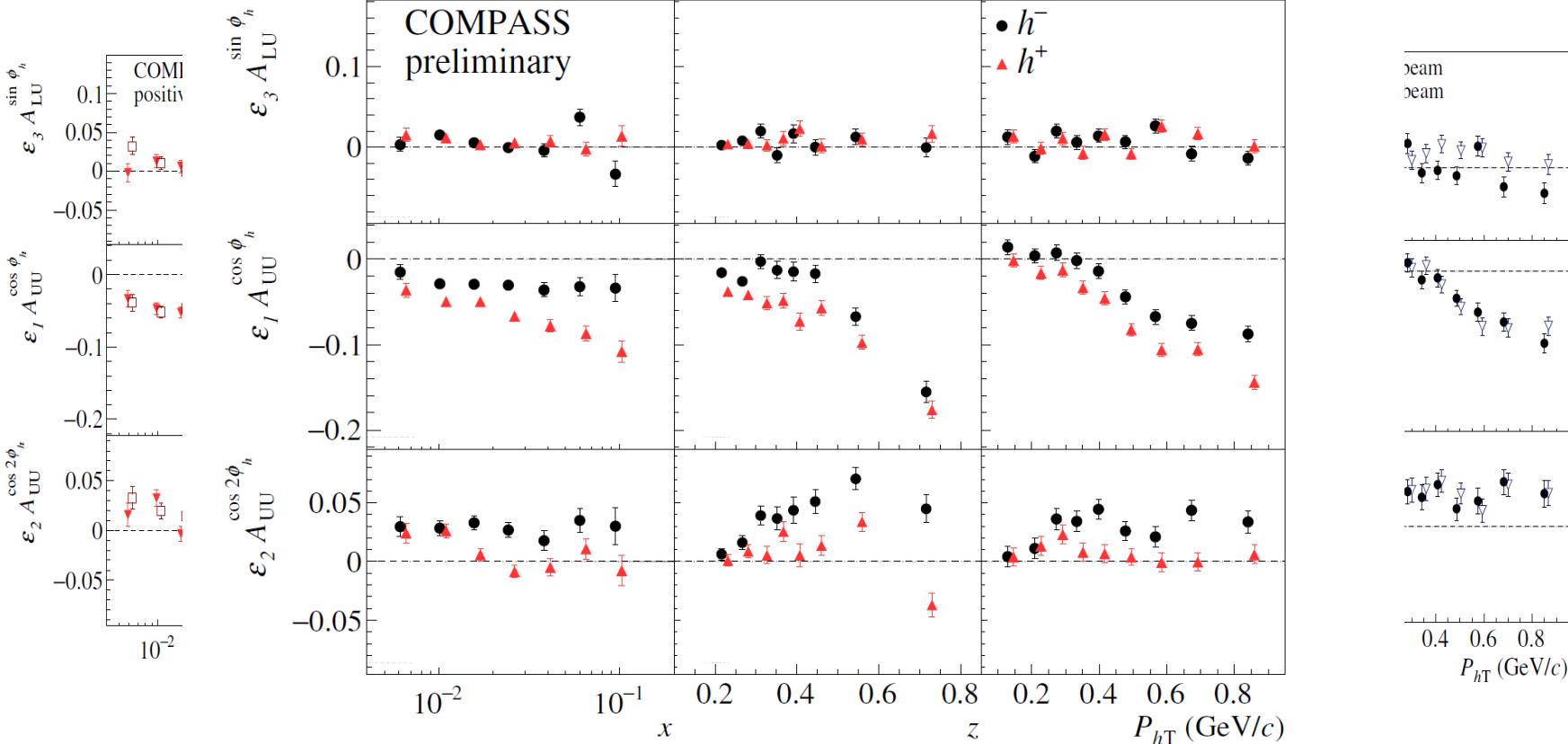
$$F_{UU}^{\cos \phi_h} = -\frac{2M}{Q} C \left[\frac{\hat{h} \cdot \vec{k}_\perp}{M} \mathbf{f}_1 D_1 - \frac{p_\perp k_\perp}{M} \frac{\vec{P}_{hT} - z(\hat{h} \cdot \vec{k}_\perp)}{z M_h M} \mathbf{h}_1^\perp H_1^\perp \right] + \text{twists} > 3$$

$$F_{UU}^{\cos 2\phi_h} = C \left[\frac{(\hat{h} \cdot \vec{k}_\perp)(\hat{h} \cdot \vec{p}_\perp) - \vec{p}_\perp \cdot \vec{k}_\perp}{MM_h} \mathbf{h}_1^\perp H_1^\perp \right] + \text{twists} > 3$$

In the $\cos 2\phi_h$ Cahn effects enters only at twist 4

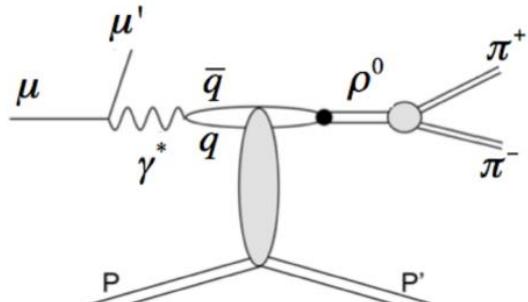
$$F_{\text{Cahn}}^{\cos 2\phi_h} \approx \frac{2}{Q^2} C \left[\left\{ 2(\hat{h} \cdot \vec{k}_\perp)^2 - k_\perp^2 \right\} \mathbf{f}_1 D_1 \right]$$

Azimuthal modulations on p

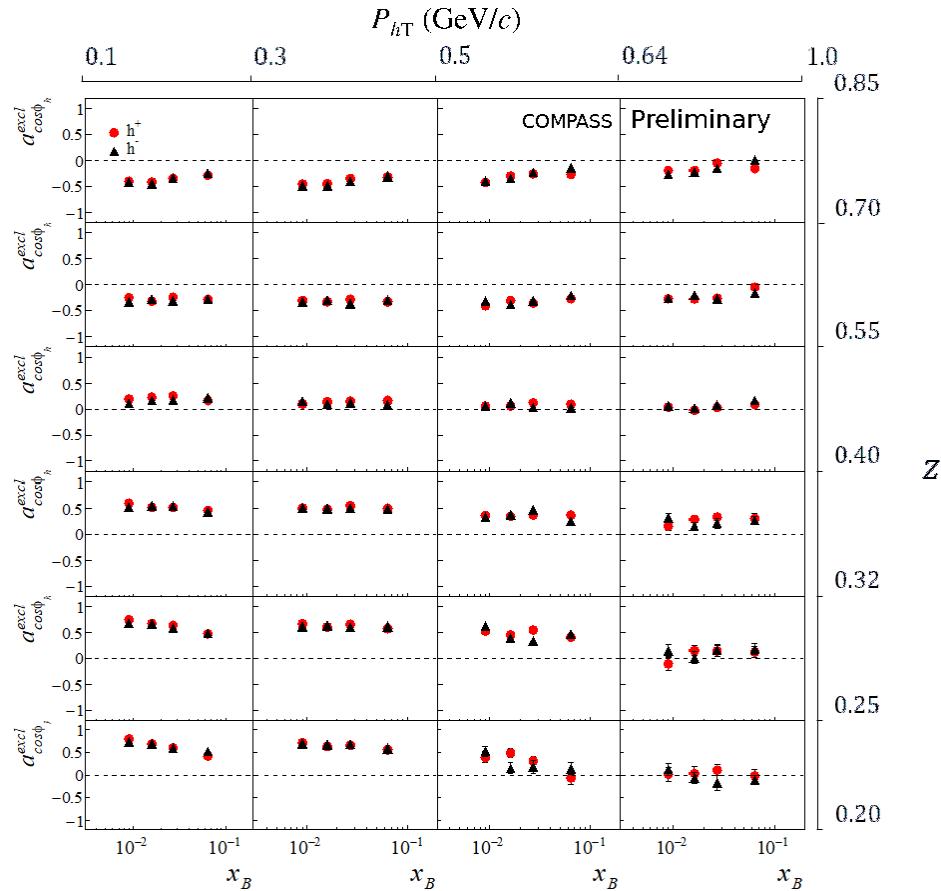


Contribution of diffractive VMs

- Determined from $z_1 + z_2 > 0.95$
- Selecting ρ^0 and ϕ
- Smaller, but not negligible, effect for $\cos 2\phi_h$

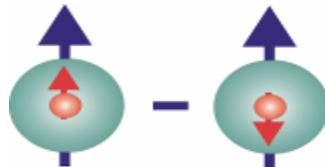


The diffractive ρ^0 production and decay.



Transversity PDF

$$h_1^q(x) = q^{\uparrow\uparrow}(x) - q^{\uparrow\downarrow}(x)$$



$$q = u_v, d_v, q_{\text{sea}}$$

quark with **spin** parallel to the nucleon spin in a transversely polarised nucleon

- probes the relativistic nature of quark dynamics
- no contribution from the gluons \rightarrow simple Q^2 evolution
- Positivity: Soffer bound..... $2|h_1^q| \leq f_1^q + g_1^q$ *Soffer, PRL 74 (1995)*
- first moments: tensor charge..... $\delta q(Q^2) = \int_0^1 dx [h_1^q(x) - h_1^{\bar{q}}(x)]$
- is chiral-odd: decouples from inclusive DIS *Bakker, Leader, Trueman, PRD 70 (04)*

is chiral-odd:

observable effects are given only by the product of $h_1^q(x)$ and an other chiral-odd function

can be measured in SIDIS on a transversely polarised target via “quark polarimetry”

$$\ell \mathbf{N}^\uparrow \rightarrow \ell' \mathbf{h} \mathbf{X}$$

“Collins” asymmetry
“Collins” Fragmentation Function

$$\ell \mathbf{N}^\uparrow \rightarrow \ell' \mathbf{h} \mathbf{h} \mathbf{X}$$

“two-hadron” asymmetry
“Interference” Fragmentation Function

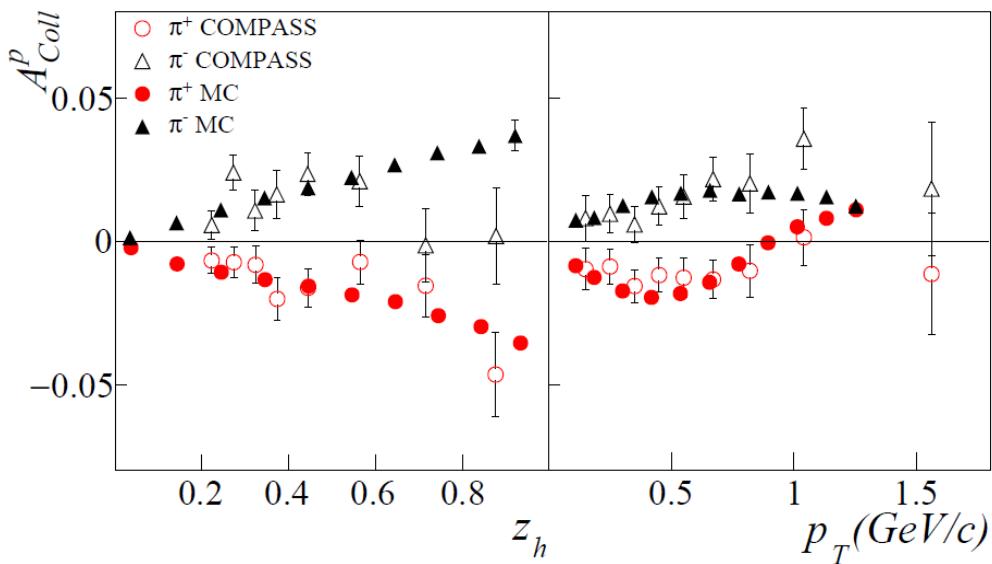
$$\ell \mathbf{N}^\uparrow \rightarrow \ell' \Lambda \mathbf{X}$$

Λ polarisation
Fragmentation Function of $q \uparrow \rightarrow \Lambda$

A_{Coll}^p on proton and 3P_0 model for FF



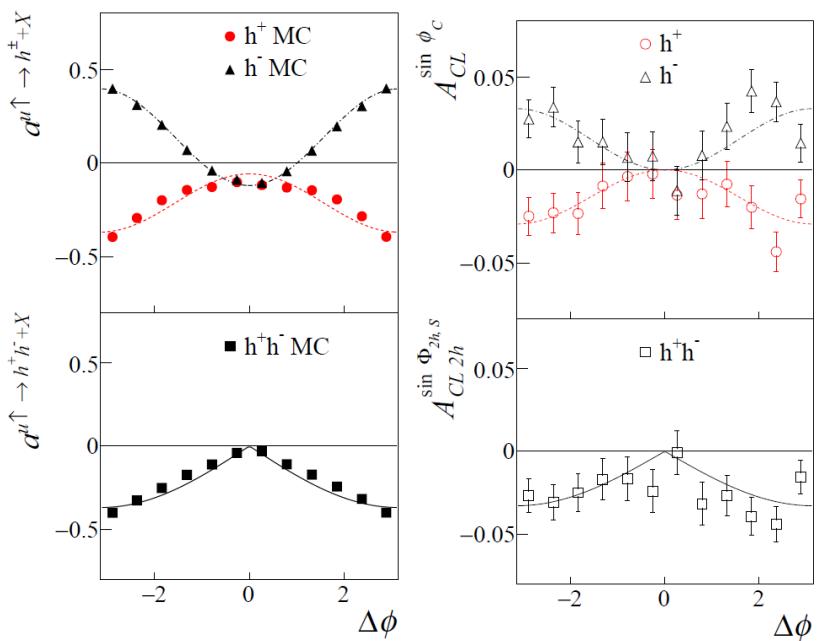
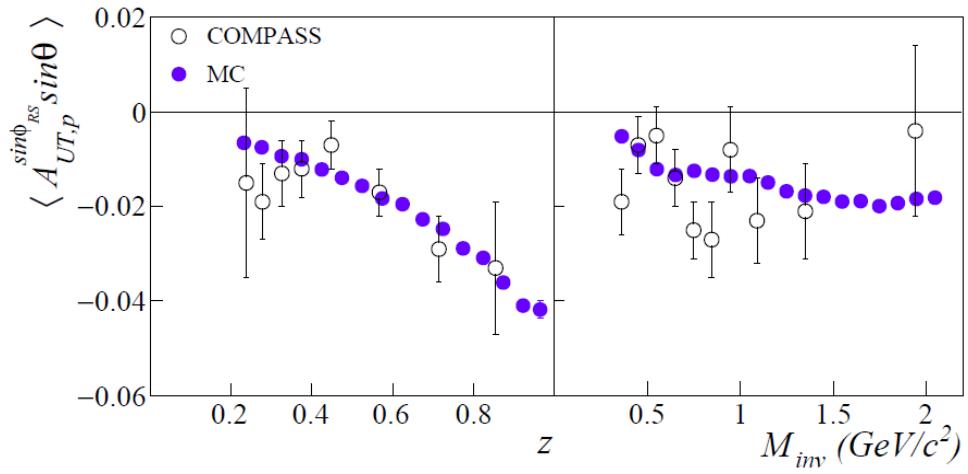
Albi Kerbizi @ DSPIN17 <http://theor.jinr.ru/~spin/2017/>
Phys. Rev. D 97, 074010 (2018)/[arXiv:1802.00962](https://arxiv.org/abs/1802.00962)



- The curves are fits of the Monte Carlo data, scaled by $\lambda \sim \langle h_1^u/f_1^u \rangle \sim 0.055$
- Agreement with the measured Collins asymmetry is quite satisfactory

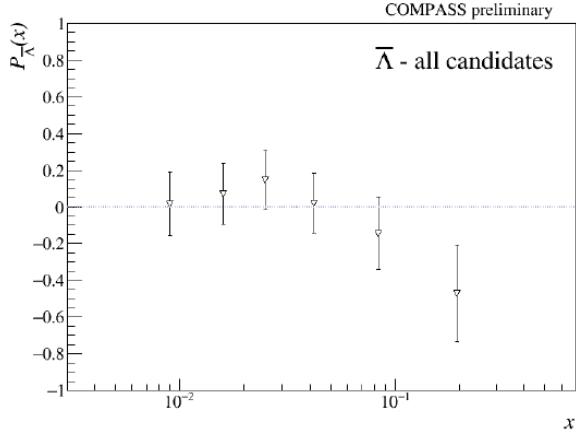
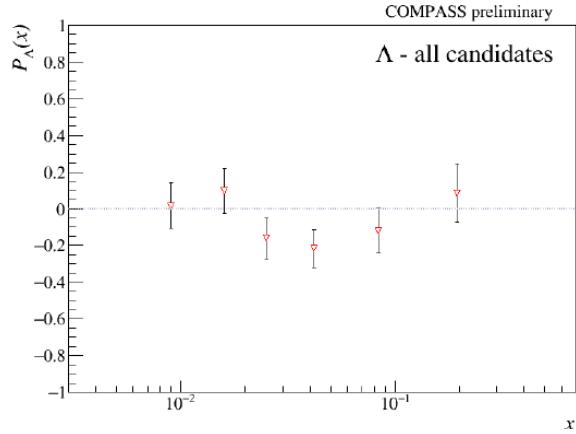
2h asymmetries on p and 3P_0 model for FF

$$A_{UT}^{\sin(\phi_R + \phi_S - \pi)} = \frac{\sum_q e_q^2 h_1^q(x) H_{q \rightarrow h_1 h_2}^4(z, \mathcal{M}_{h_1 h_2}^2)}{\sum_q e_q^2 q(x) D_q^{h_1 h_2}(z, \mathcal{M}_{h_1 h_2}^2)}$$



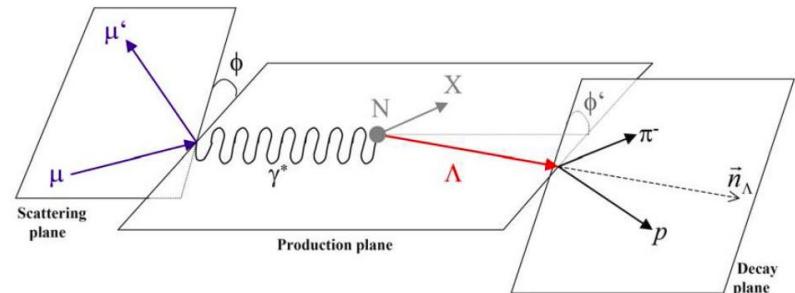
$a_P^{u \uparrow \rightarrow h^+ h^- X} = \langle \sin(\phi_R + \phi_S - \pi) \rangle$ and $\vec{R} = \frac{z_2 \vec{P}_{h_1} - z_1 \vec{P}_{h_2}}{z_1 + z_2}$ and as before $\lambda \sim \langle h_1^u / f_1^u \rangle \sim 0.055$

Λ transverse spin transfer from COMPASS



$$P_{\Lambda(\bar{\Lambda})}(x, z) = \frac{\sum_q e_q^2 h_1^q(x) H_1^{\Lambda(\bar{\Lambda})}(z)}{\sum_q e_q^2 f_1^q(x) D_1^{\Lambda(\bar{\Lambda})}(z)}$$

$$\frac{dN}{d \cos \theta^*} \propto A(1 + \alpha P_{\Lambda(\bar{\Lambda})} \cos \theta^*)$$



Sivers Asymmetry

Sivers: correlates nucleon spin & quark transverse momentum k_T /T-ODD

at LO:

$$A_{Siv} = \frac{\sum_q e_q^2 f_{1Tq}^\perp \otimes D_q^h}{\sum_q e_q^2 q \otimes D_q^h}$$



The Sivers PDF	
1992	Sivers proposes f_{1T}^\perp
1993	J. Collins proofs $f_{1T}^\perp = 0$ for T invariance
2002	S. Brodsky, Hwang and Schmidt demonstrate that f_{1Tq}^\perp may be $\neq 0$ due to FSI
2002	J. Collins shows that $(f_{1T}^\perp)_{DY} = -(f_{1T}^\perp)_{SIDIS}$
2004	HERMES on p: $A_{Siv}^{\pi^+} \neq 0$ and $A_{Siv}^{\pi^-} = 0$
2004	COMPASS on d: $A_{Siv}^{\pi^+} = 0$ and $A_{Siv}^{\pi^-} = 0$
2008	COMPASS on p: $A_{Siv}^{\pi^+} \neq 0$ and $A_{Siv}^{\pi^-} = 0$

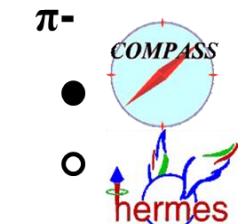
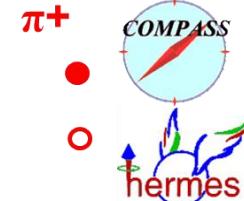
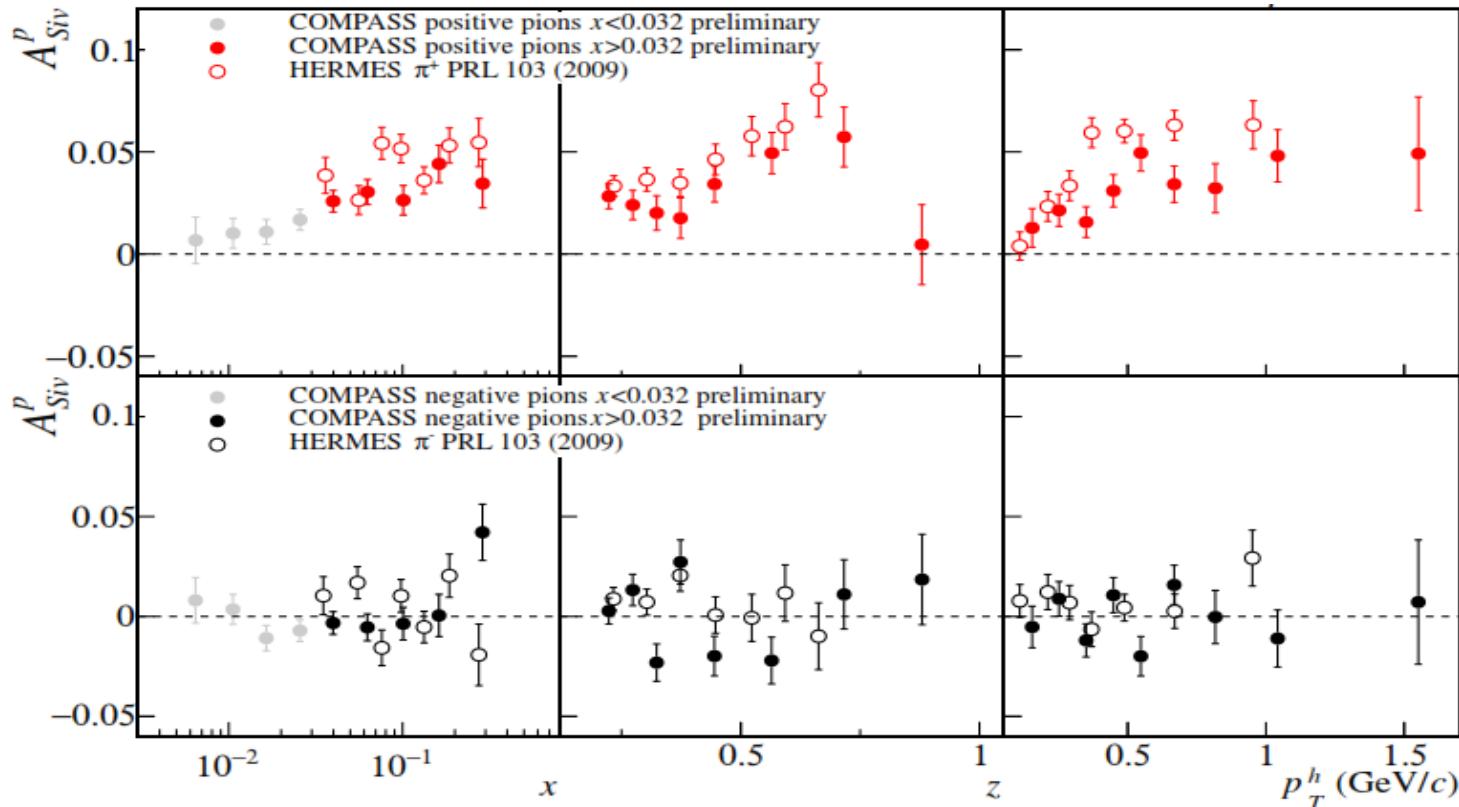
Sivers Asymmetry

$$A_{Siv}(x, z) = \frac{F_{UT}^{\sin\Phi_{Siv}}(x, z)}{F_{UU}(x, z)} = \frac{\sum_q e_q^2 x f_{1T}^{\perp q}(x, k_\perp^2) \otimes D_{1q}^h(z, p_\perp^2)}{\sum_q e_q^2 x f_1^q(x, k_\perp^2) \otimes D_{1q}^h(z, p_\perp^2)}$$

- To evaluate it we need to solve the convolutions (i.e. make hypothesis on the transverse momenta dependences of the TMDs)
- Gaussian ansatz: $f_{1T}^{\perp q}(x) \frac{e^{-k_\perp^2/\langle k_\perp^2 \rangle_S}}{\pi \langle k_\perp^2 \rangle_S} \quad D_{1q}^h(z) \frac{e^{-p_\perp^2/\langle p_\perp^2 \rangle}}{\pi \langle p_\perp^2 \rangle}$
- Leading to: $A_{Siv,G}(x, z) = \frac{\sqrt{\pi} M}{\sqrt{z^2 \langle k_T^2 \rangle_S + \langle p_T^2 \rangle}} \frac{\sum_q e_q^2 x f_{1T}^{\perp(1)q}(x) z D_{1q}^h(z)}{\sum_q e_q^2 x f_1^q(x) D_{1q}^h(z)}$ with $f_{1T}^{\perp(1)q}(x) = \int d^2 \vec{k}_T \frac{k_T^2}{2M^2} f_{1T}^{\perp q}(x, k_T^2)$

Sivers asymmetry on p

charged pions (and kaons), HERMES and COMPASS



The weighted Sivers asymmetry

- If we weight the spin dependent part of the cross-section

$$F_{UT}^{\sin\Phi_{Siv}}(x, z) = \sum_q e_q^2 \int d^2 \vec{P}_T P_T F_q(x, z, P_T^2)$$

- with $w = P_T/zM$, i.e.

$$F_{UT}^{\sin\Phi_{Siv}, w}(x, z) = \sum_q e_q^2 \int d^2 \vec{P}_T \frac{P_T^2}{zM} F_q(x, z, P_T^2) = 2 \sum_q e_q^2 x f_{1T}^{\perp(1)q}(x) D_{1q}^h(z)$$

and $F_q(x, z, P_T^2) = \int d^2 \vec{k}_T \int d^2 \vec{p}_T \delta^2(\vec{P}_T - z \vec{k}_T - \vec{p}_T) \frac{\vec{P}_T \cdot \vec{k}_T}{MP_T^2} x f_{1T}^{\perp q}(x, k_T^2) D_{1q}(z, p_T^2)$

- we have no longer a convolution but a product of two integrals and we can write

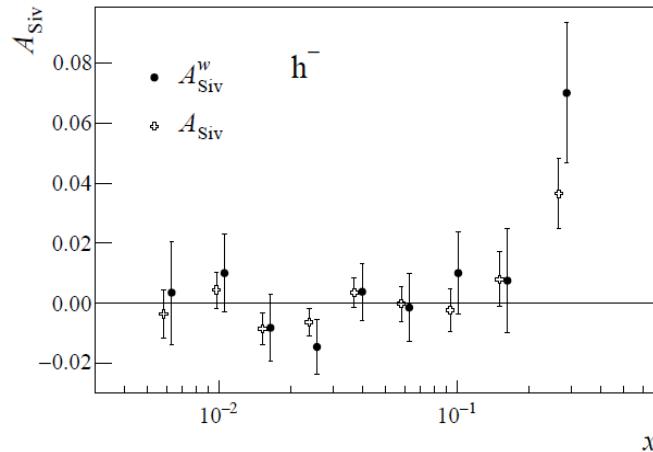
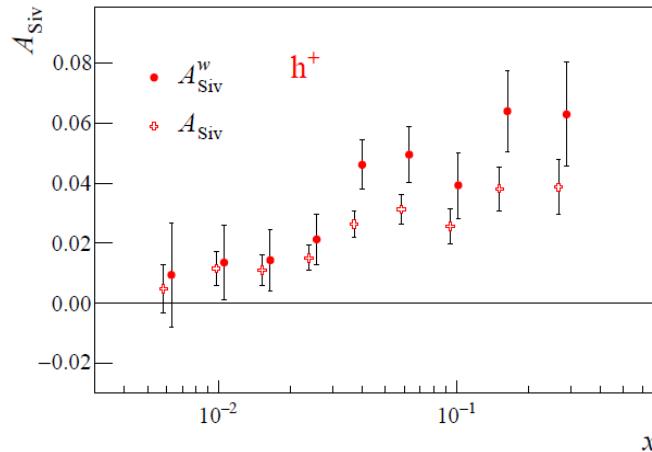
$$A_{Siv}^w(x, z) = \frac{F_{UT}^{\sin\Phi_{Siv}, w}(x, z)}{F_{UU}(x, z)} = 2 \frac{\sum_q e_q^2 x f_{1T}^{\perp(1)q}(x) D_{1q}^h(z)}{\sum_q e_q^2 x f_1^q(x) D_{1q}^h(z)}$$

with $f_{1T}^{\perp(1)q}(x) = \int d^2 \vec{k}_T \frac{k_T^2}{2M^2} f_{1T}^{\perp q}(x, k_T^2)$

The weighted Sivers asymmetry

$$A_{Siv}^w(x) = 2 \frac{\sum_q e_q^2 x f_{1T}^{\perp(1)q}(x) \int D_{1q}^h(z) dz}{\sum_q e_q^2 x f_1^q(x) \int D_{1q}^h(z) dz} \quad w = P_T/zM$$

standard cuts
 $z > 0.2$



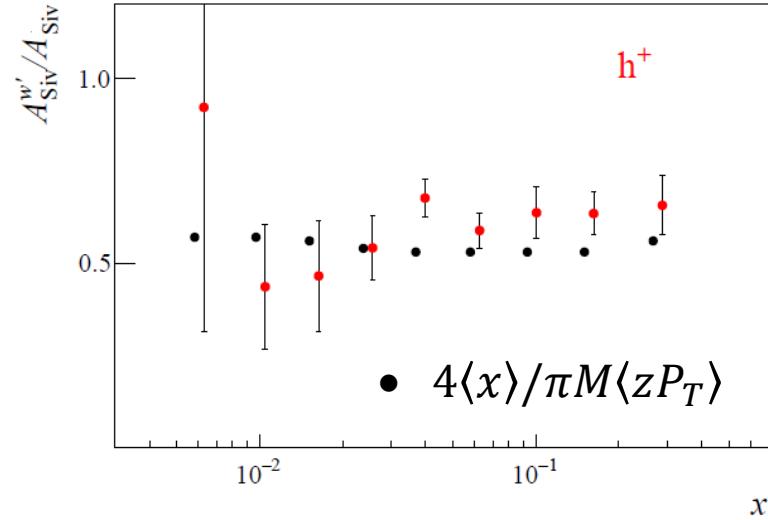
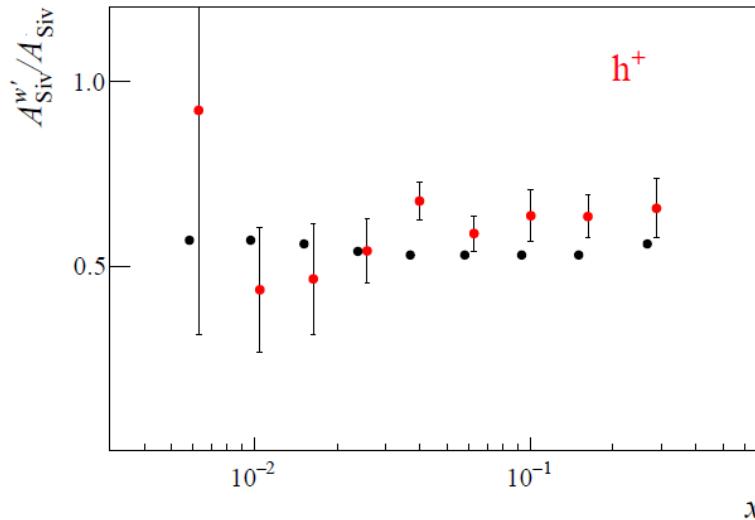
$$\sim 2 \frac{f_{1T}^{\perp(1)u}(x)}{f_1^u(x)}$$

both $f_{1T}^{\perp(1)u}$ and $f_{1T}^{\perp(1)d}$ contribute

The weighted Sivers asymmetry

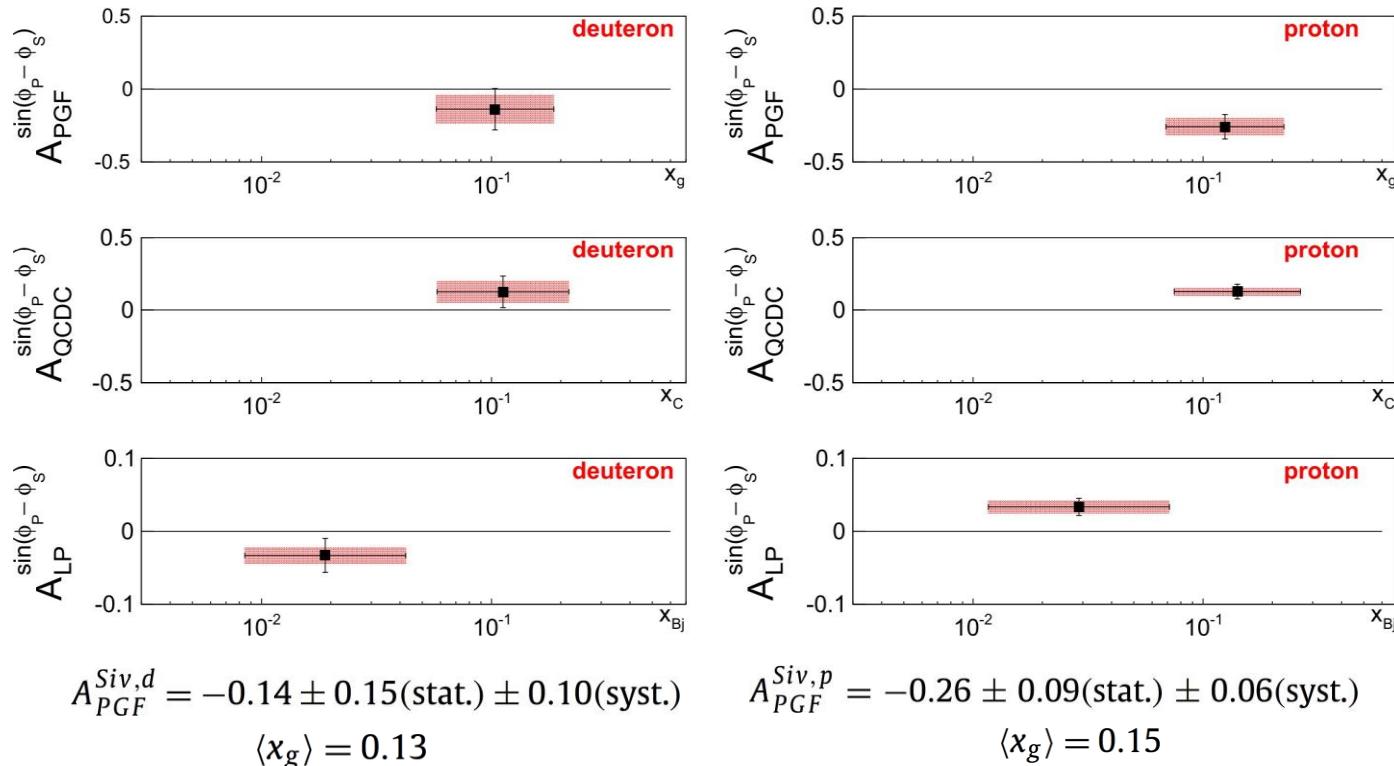
$$A_{Siv}^w(x) = 2 \frac{\sum_q e_q^2 x f_{1T}^{\perp(1)q}(x) \int D_{1q}^h(z) dz}{\sum_q e_q^2 x f_1^q(x) \int D_{1q}^h(z) dz} \quad w = P_T/zM$$

standard cuts
 $z > 0.2$



The ratio between weighted and unweighted Sivers asymmetries follows the average of $4\langle x \rangle / \pi M \langle zP_T \rangle$ of the unpolarised sample

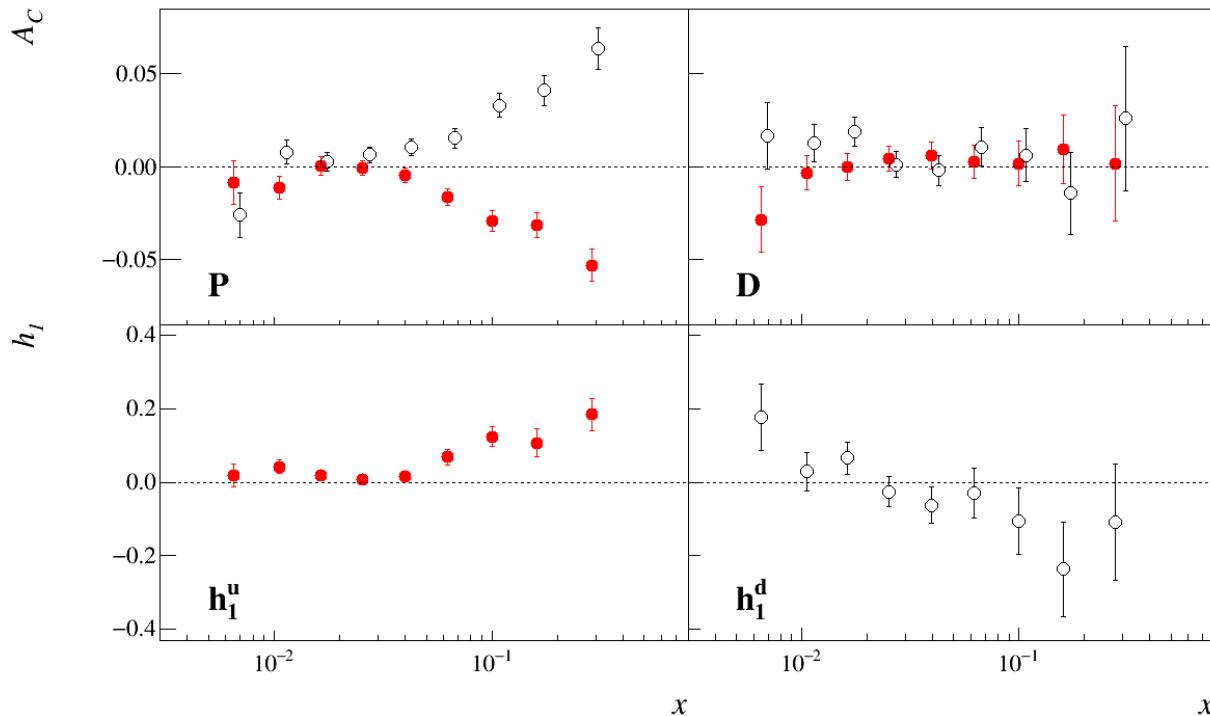
Sivers Asymmetry for Gluon from SIDIS



C. Adolph et al. (COMPASS Collaboration), Phys. Lett. B 772, 854 (2017).

2021 Deuteron run

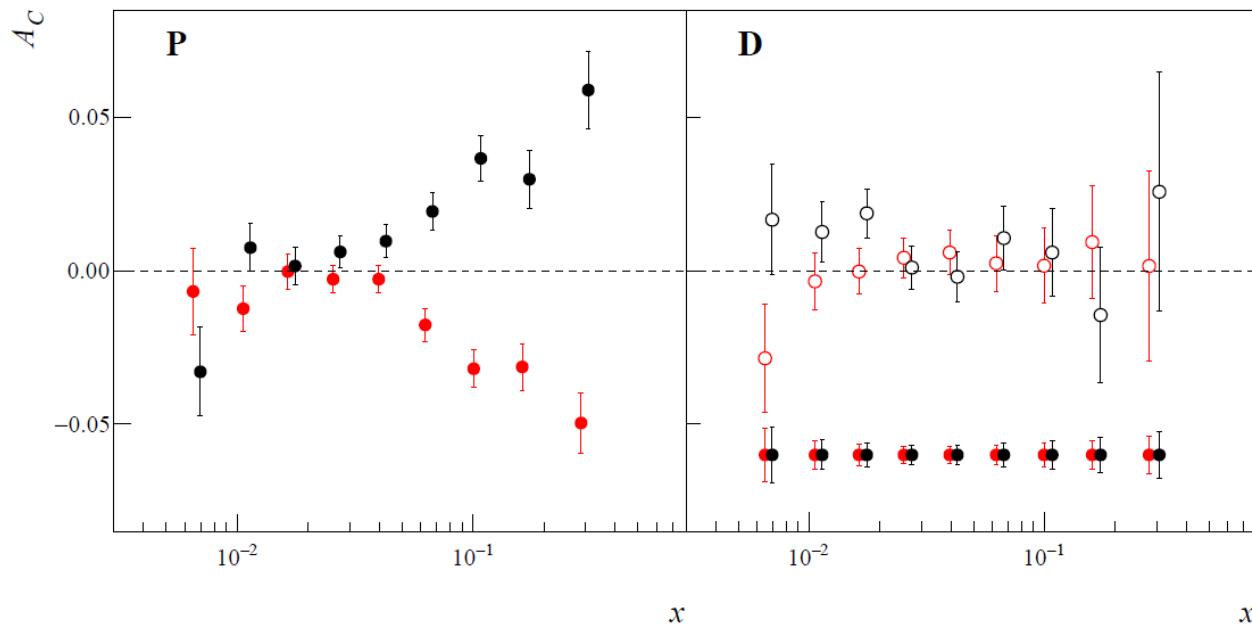
- Benchmark: h_1 extraction from Collins asymmetries



Transversity extracted as in
PRD 91(2015) 014034

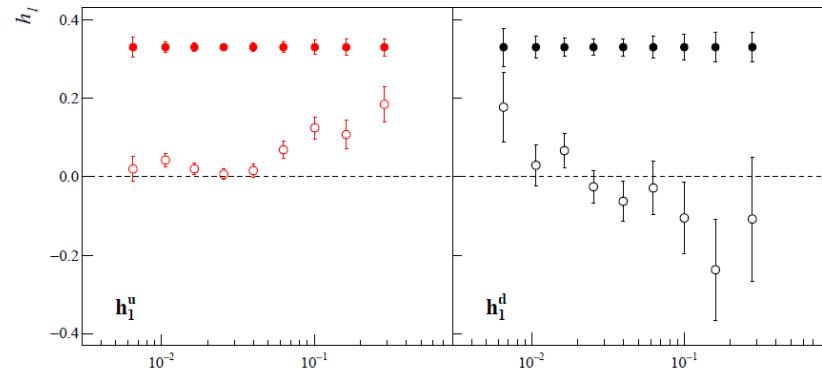
2021 Deuteron Run

- COMPASS proposed to CERN to run a full year with the transversely polarized deuteron target and this proposal has been approved



New deuteron data

- 1 full year (same as 2010). We also gain from $\frac{f_p P_{pT}}{f_D P_{DT}} = \frac{0.155 \times 0.8}{0.40 \times 0.5} = 0.6$



— projected

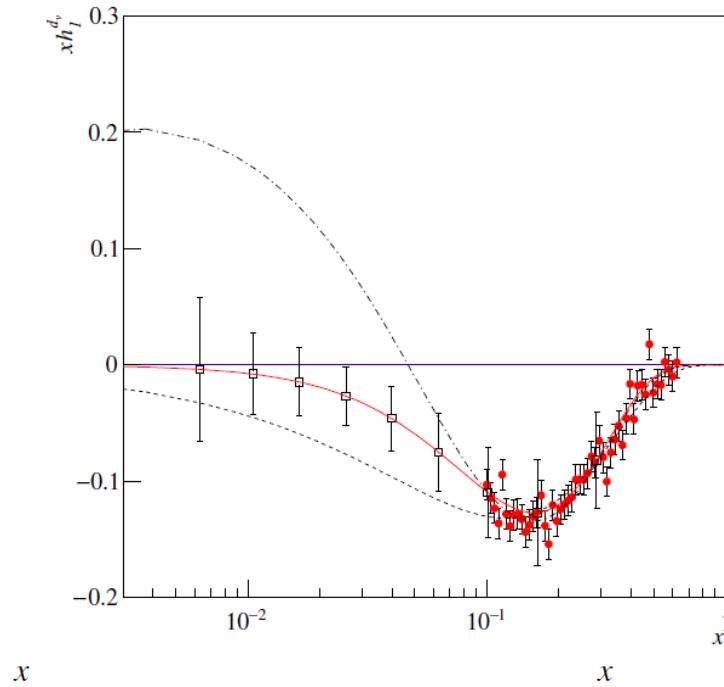
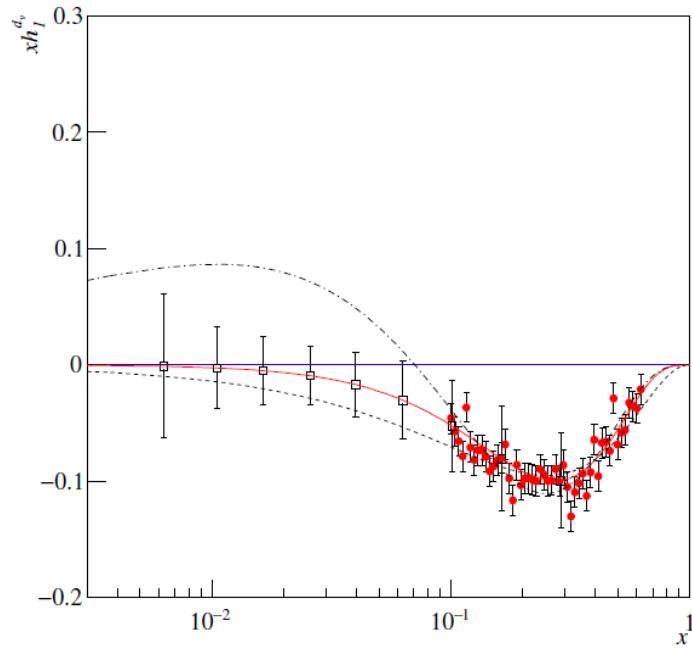
— present

Transversity extracted as in
PRD 91(2015) 014034

COMPASS deuteron data in 2021



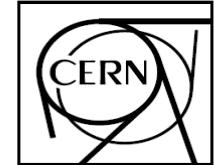
- Expected gain in precision on u- and d-quark transversity



New QCD facility at CERN M2



EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH



CERN-SPSC-2019-XXX
SPSC-P-XXX
May 31, 2019

Proposal for Measurements at the M2 beam line of the CERN SPS
Phase-1: 2022-2024
COMPASS++*/AMBER[†]

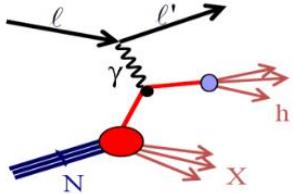
A photograph of a grand, multi-story castle with a light-colored stone facade and several towers, situated on a rocky cliff overlooking the sea. The sky is a vibrant orange and blue at sunset. In the foreground, a paved walkway leads towards the castle, and a wooden dreidel (spinning top) is positioned on the left side of the path.

Thank you

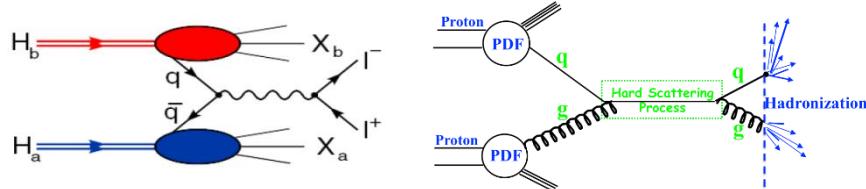
FACTORISATION

- DIS/SIDIS off polarized p, d, n targets

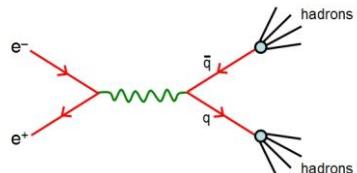
Cern/Hera/Jlab
future: **eN colliders?**



- Drell-Yan/W/jets in Hadron Hadron



- $e^+e^- \rightarrow h_1 h_2$



LEP/SLAC/BELLE/BES

$$\sigma^{\ell p \rightarrow \ell' X} \sim q(x) \otimes \hat{\sigma}^{\gamma q \rightarrow q}$$

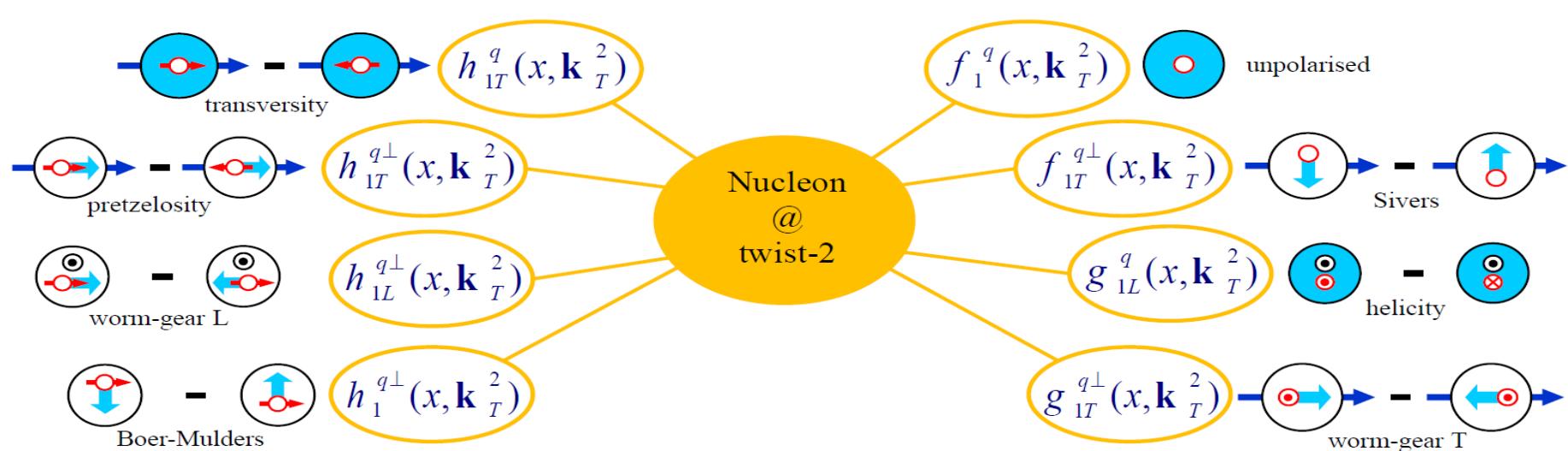
$$\sigma^{\ell p \rightarrow \ell' h X} \sim q(x) \otimes \hat{\sigma}^{\gamma q \rightarrow q} \otimes D_q^h(z)$$

$$\sigma^{hp \rightarrow \mu\mu} \sim \bar{q}_h(x_1) \otimes q_p(x_2) \otimes \hat{\sigma}^{\bar{q}q \rightarrow \mu\mu}(\hat{s})$$

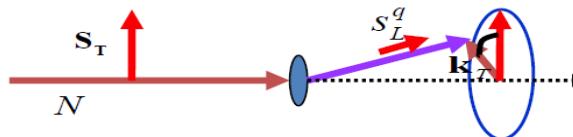
CERN(COMPASS/LHC)/RHIC/FNAL
future: **FAIR, JPark, NICA**

$$\sigma^{e^+e^- \rightarrow h_1 h_2} \sim \hat{\sigma}^{\ell\ell \rightarrow \bar{q}q}(\hat{s}) \otimes D_q^{h_1}(z_1) \otimes D_q^{h_2}(z_2)$$

TMD Distribution Functions

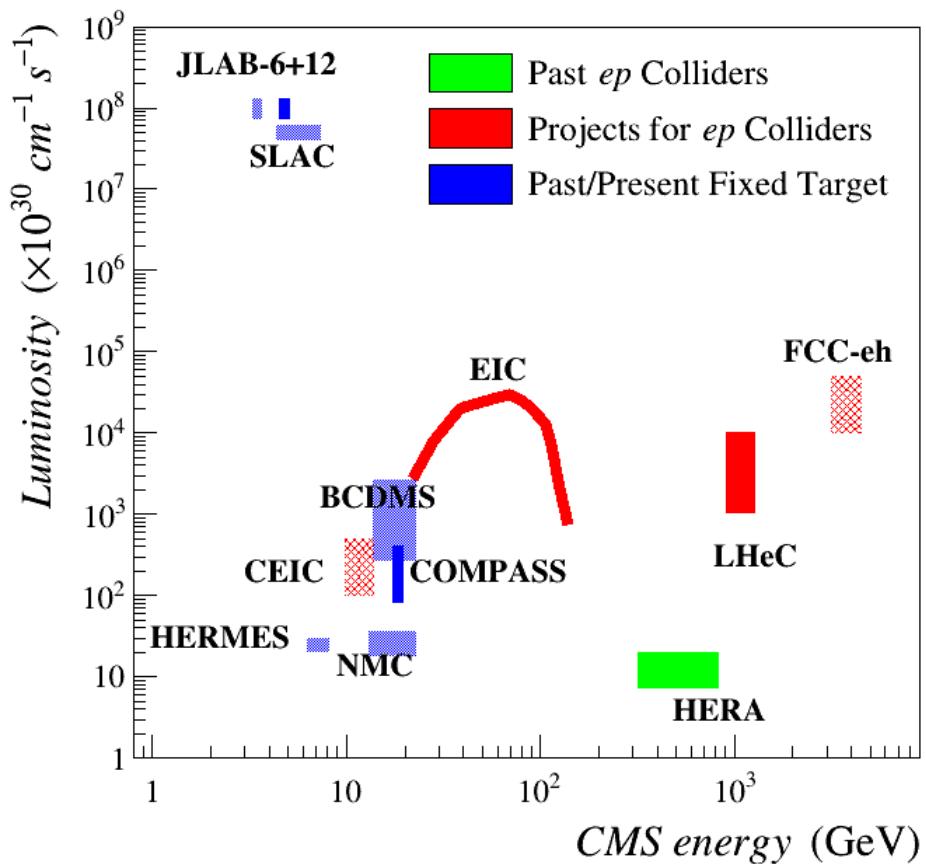


Proton goes out of the screen. Photon goes into the screen

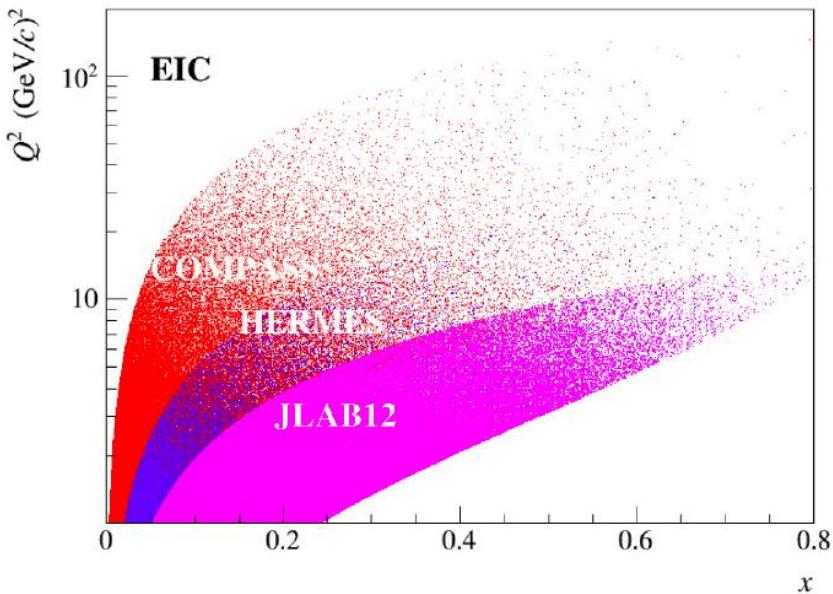
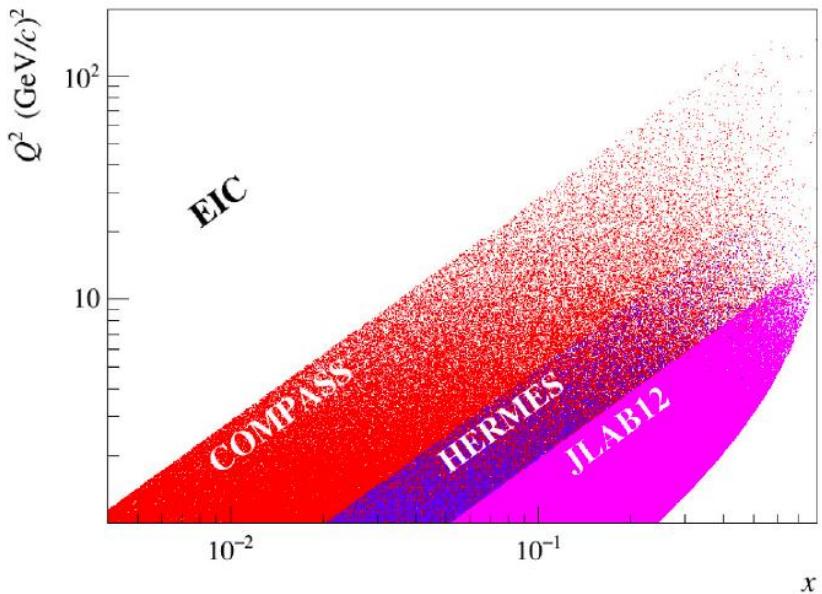


\mathbf{k}_T – intrinsic transverse momentum of the quark

DIS around the world



Kinematic coverage



From Collins asymmetries to transversity



- Following Physical Review D 91, 014034 (2015), in the valence region

$$x h_1^u = \frac{1}{5} \frac{1}{\tilde{\alpha}_P^h(1-\tilde{\alpha})} \left[(x f_p^+ A_p^+ - x f_p^- A_p^-) + \frac{1}{3} (x f_d^+ A_d^+ - x f_d^- A_d^-) \right]$$

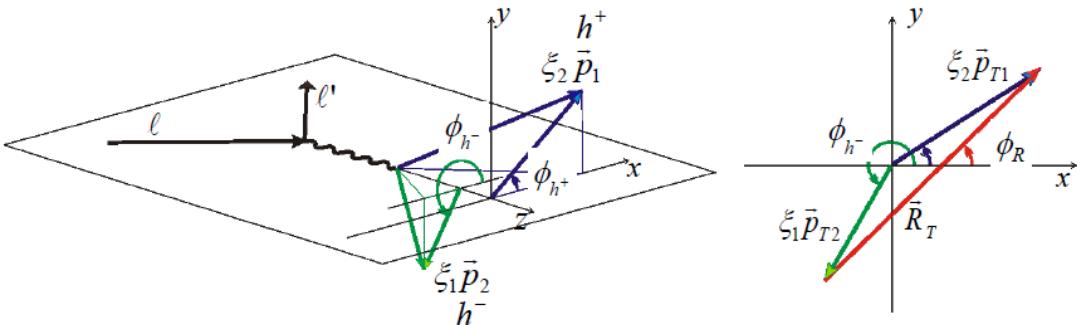
$$x h_1^d = \frac{1}{5} \frac{1}{\tilde{\alpha}_P^h(1-\tilde{\alpha})} \left[\frac{4}{3} (x f_d^+ A_d^+ - x f_d^- A_d^-) - (x f_p^+ A_p^+ - x f_p^- A_p^-) \right]$$

With $\tilde{\alpha}_P^h$ and $\tilde{\alpha}$ constants

$$\pi^+ \text{ in p: } f_p^+ = 4 \left(f_1^u + \frac{\tilde{D}_{unf}}{\tilde{D}_f} f_1^{\bar{u}} \right) + \left(\frac{\tilde{D}_{unf}}{\tilde{D}_f} f_1^d + f_1^{\bar{d}} \right) + \frac{\tilde{D}_{unf}}{\tilde{D}_f} (f_1^s + f_1^{\bar{s}})$$

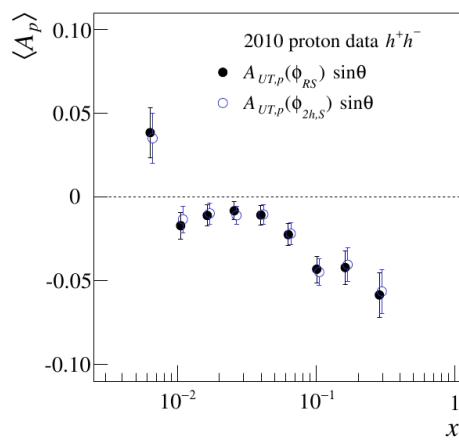
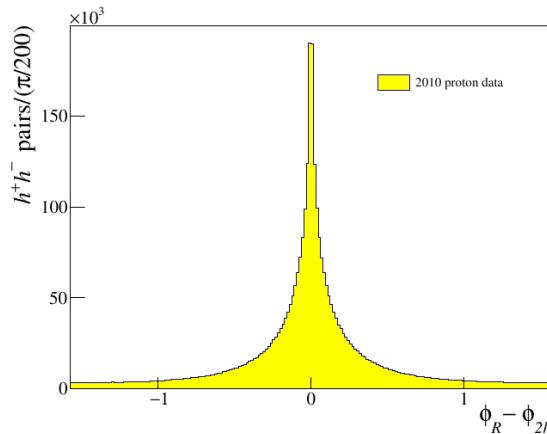
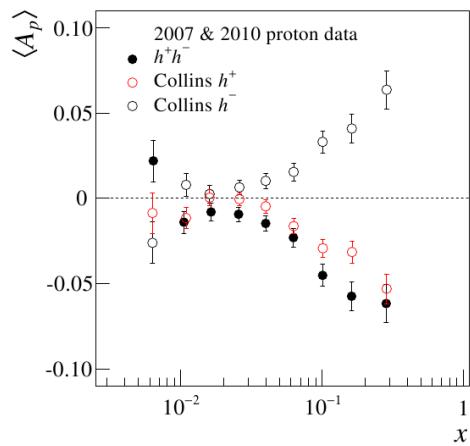
$$\pi^- \text{ in p: } f_p^+ = 4 \left(\frac{\tilde{D}_{unf}}{\tilde{D}_f} f_1^u + f_1^{\bar{u}} \right) + \left(f_1^d + \frac{\tilde{D}_{unf}}{\tilde{D}_f} f_1^{\bar{d}} \right) + \frac{\tilde{D}_{unf}}{\tilde{D}_f} (f_1^s + f_1^{\bar{s}})$$

Hadron correlations

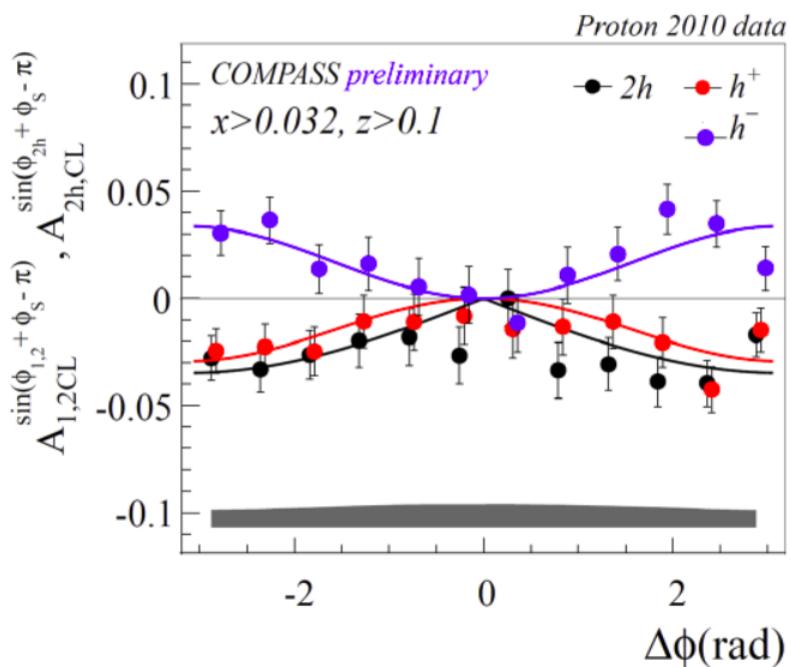


Interplay between
Collins and IFF
asymmetries

common hadron sample for Collins and 2h analysis



Asymmetries for $x > 0.032$ vs $\Delta\phi = \phi_{h^+} - \phi_{h^-}$



$$a = \frac{\sigma_{1C}^{h^+h^-}(\Delta\phi)}{\sigma_U(\Delta\phi)}$$

$$= -\frac{\sigma_{2C}^{h^+h^-}(\Delta\phi)}{\sigma_U(\Delta\phi)}$$

- $a \sqrt{2(1-\cos \Delta\phi)}$
- $a (1-\cos \Delta\phi)$
- $a (1-\cos \Delta\phi)$

$a = -0.017 \pm 0.002, \chi^2/\text{n.d.f.} = 0.98$

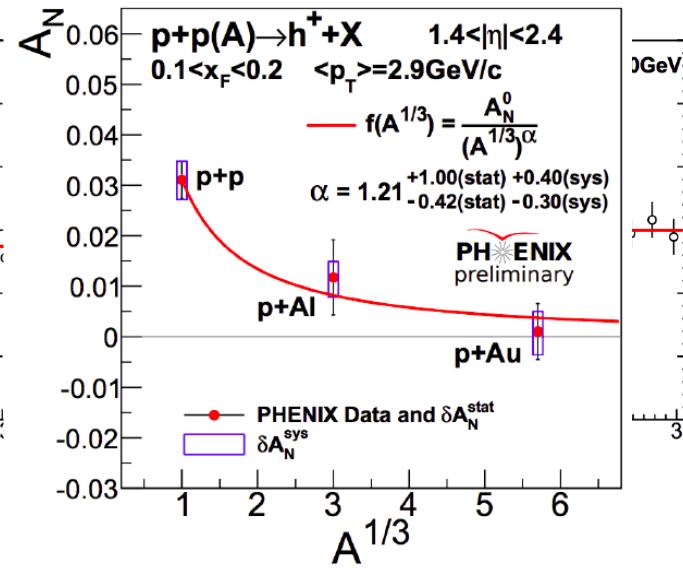
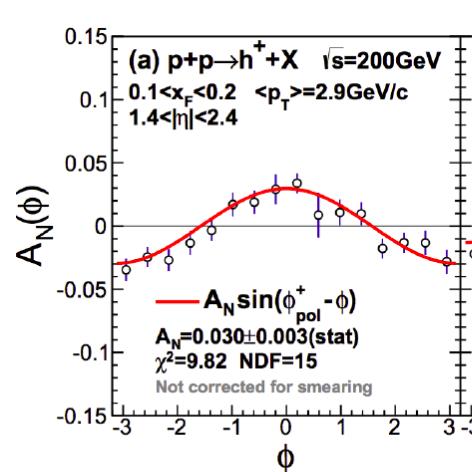
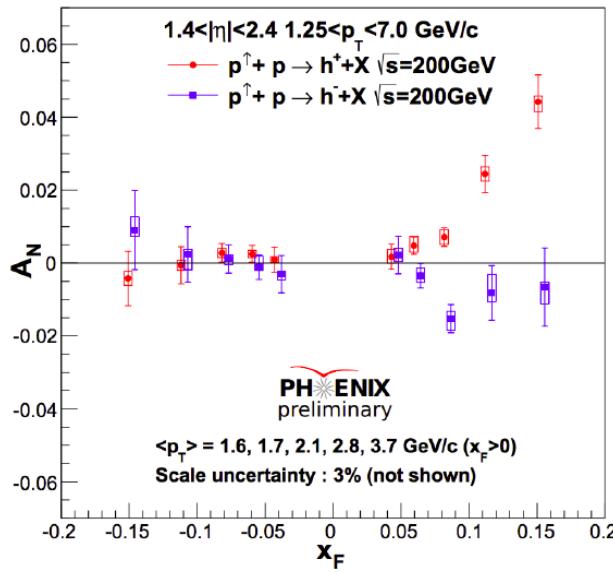
$a = -0.015 \pm 0.003, \chi^2/\text{n.d.f.} = 0.65$

$a = 0.017 \pm 0.003, \chi^2/\text{n.d.f.} = 0.80$

ratio of the integrals compatible with $4/\pi$

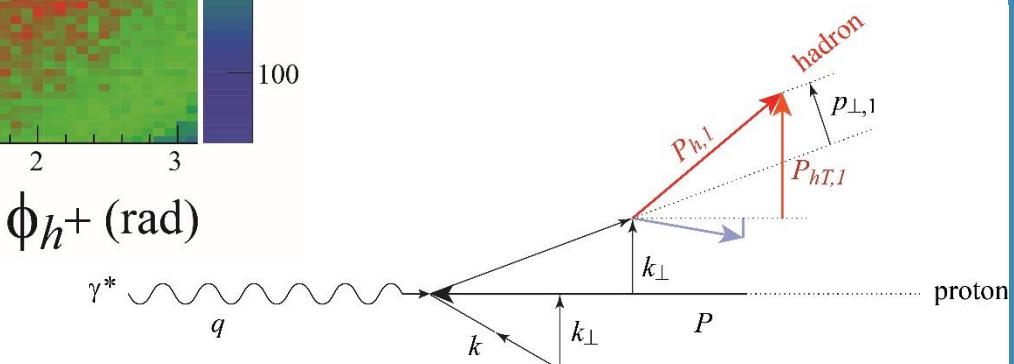
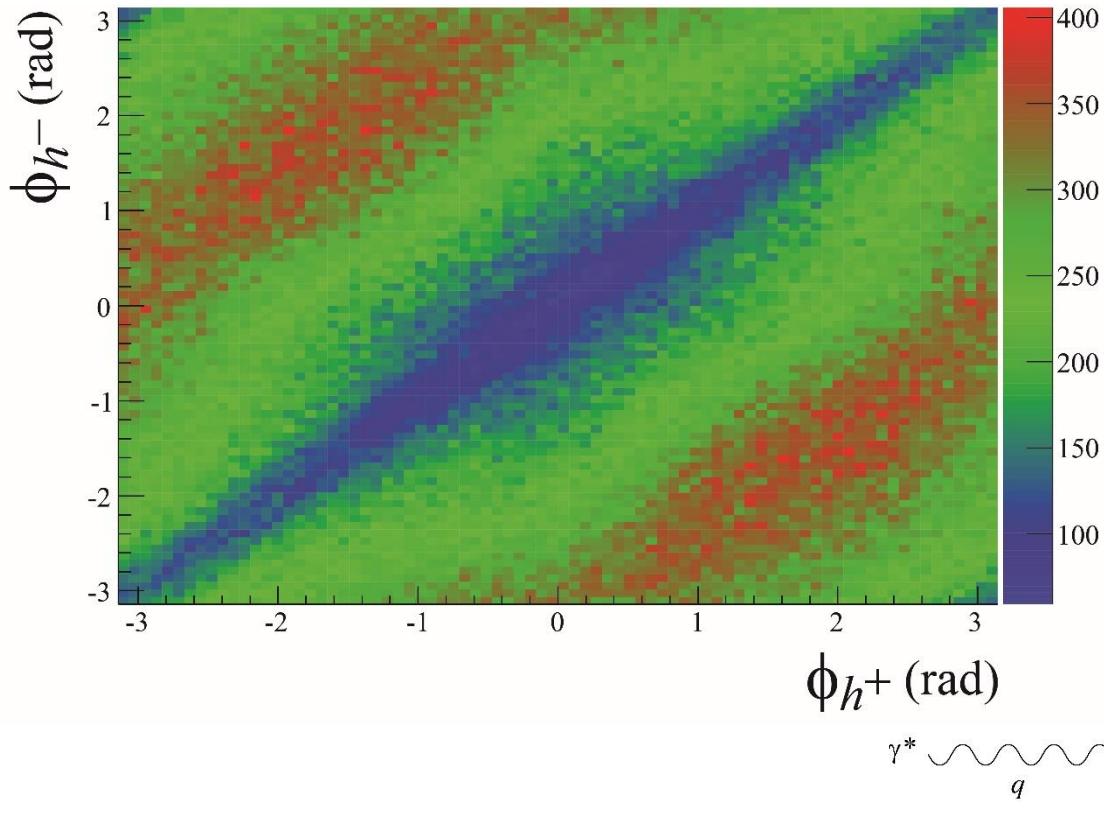
Hints for a common origin of 1h and 2h mechanisms

TSSA A_N studies at PHENIX



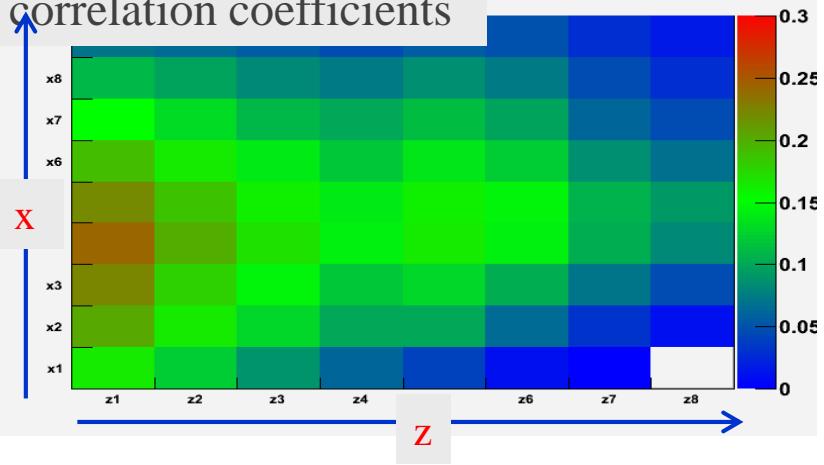
Described by twist 3 collinear approach (1 scale, high p_T)
 Supresion in $p^\uparrow A$ expected by gluon saturation ($\propto A^{1/3}$)
 Hybrid approach: twist-3 and CGC

Is correlation having an impact?



Statistical correlations

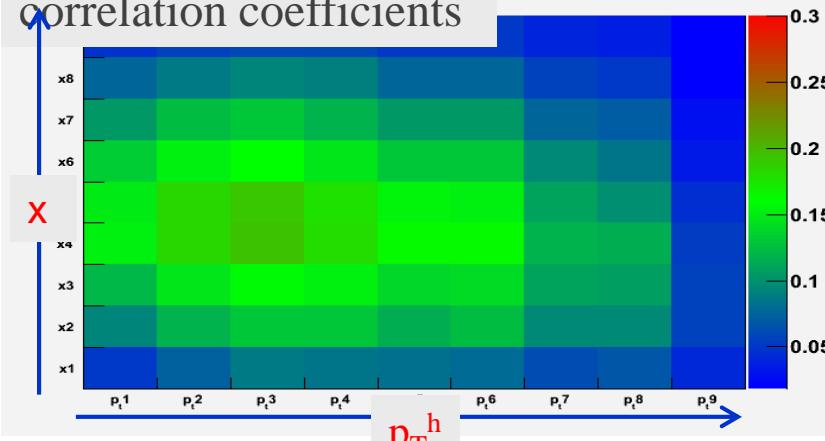
correlation coefficients



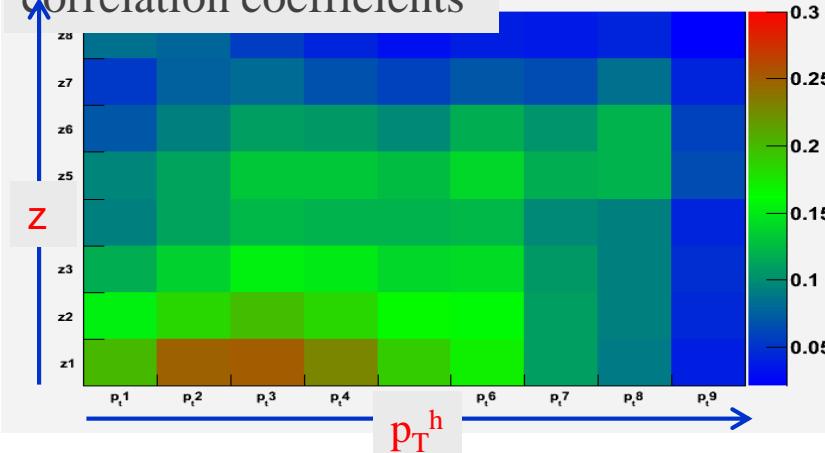
**charged pions
also available for
charged hadrons
charged kaons**

have to be taken into account

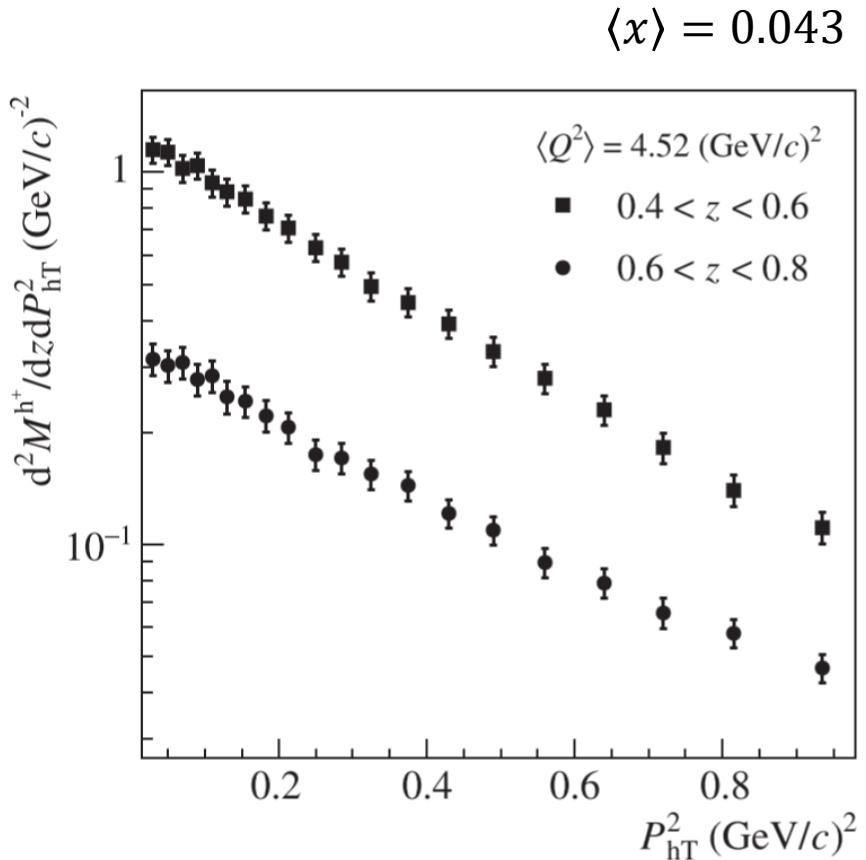
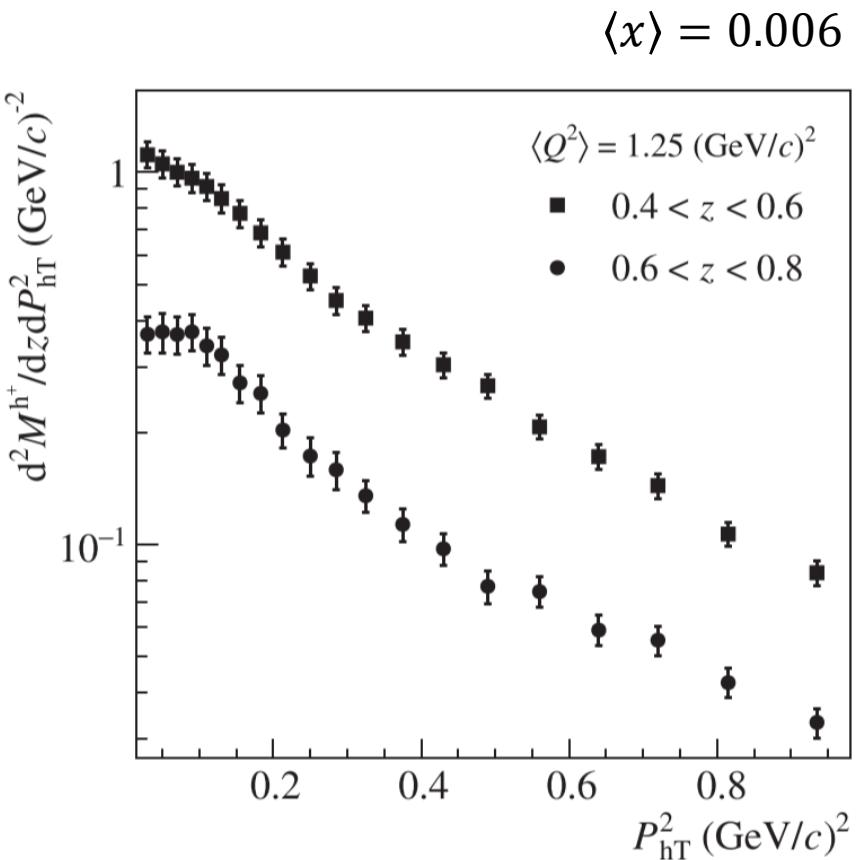
correlation coefficients



correlation coefficients



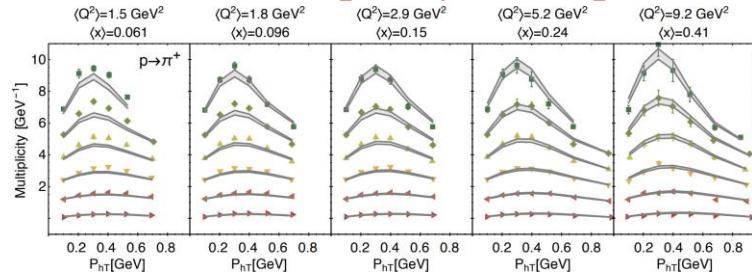
Low P_{hT} behavior



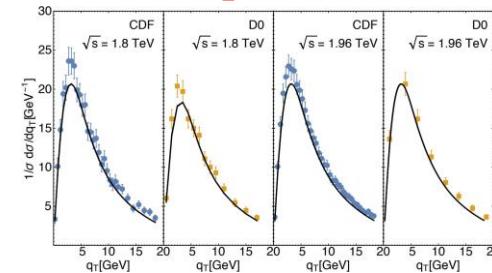
Global Analysis: Unpolarized TMD

Global analysis of semi-inclusive DIS, Drell-Yan and Z production data with TMD evolution

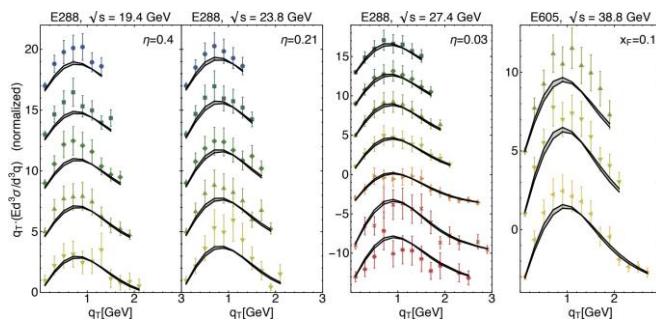
SIDIS multiplicity (example)



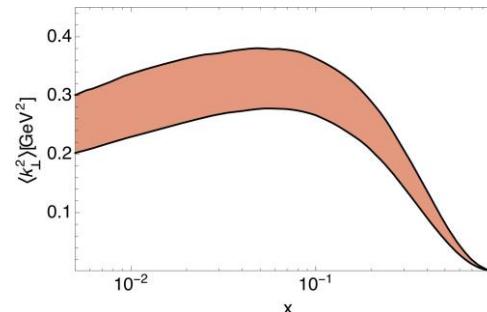
Z production



Drell-Yan cross section



Transverse momentum distribution



A. Bacchetta *et al.*, J. High Energy Phys. 06 (2017) 081.

TMD evolution:



- QCD evolution of TMDs in Fourier space (solution of equation)

$$F(x, b; Q) \approx C \otimes F(x, c/b^*) \exp \left\{ - \int_{c/b^*}^{Q_f} \frac{d\mu}{d} \left(A \ln \frac{Q_f^2}{\mu^2} + B \right) \right\} \times \exp[-S_{\text{non-pert}}(b, Q)]$$

Evolution of longitudinal/collinear part

Evolution of transverse part (Sudakov form factor)

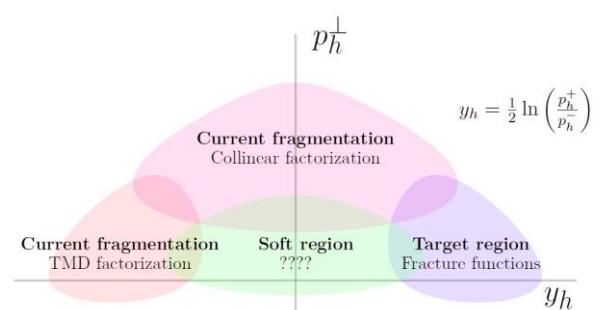
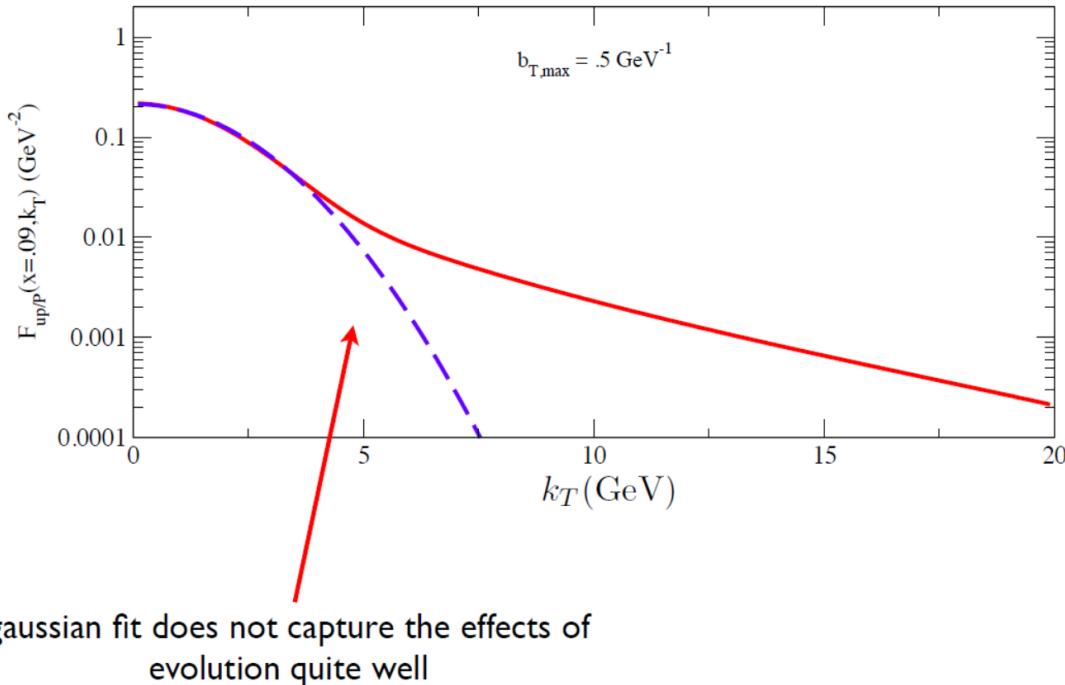
Non-perturbative part has to be fitted to experimental data
The key ingredient is spin-independent

- Polarized scattering data comes as ratio: e.g. $A_{UT}^{\sin(\phi_h - \phi_s)} = F_{UT}^{\sin(\phi_h - \phi_s)} / F_{UU}$
- Unpolarized data is very important to constrain/extract the key ingredient for the non-perturbative part

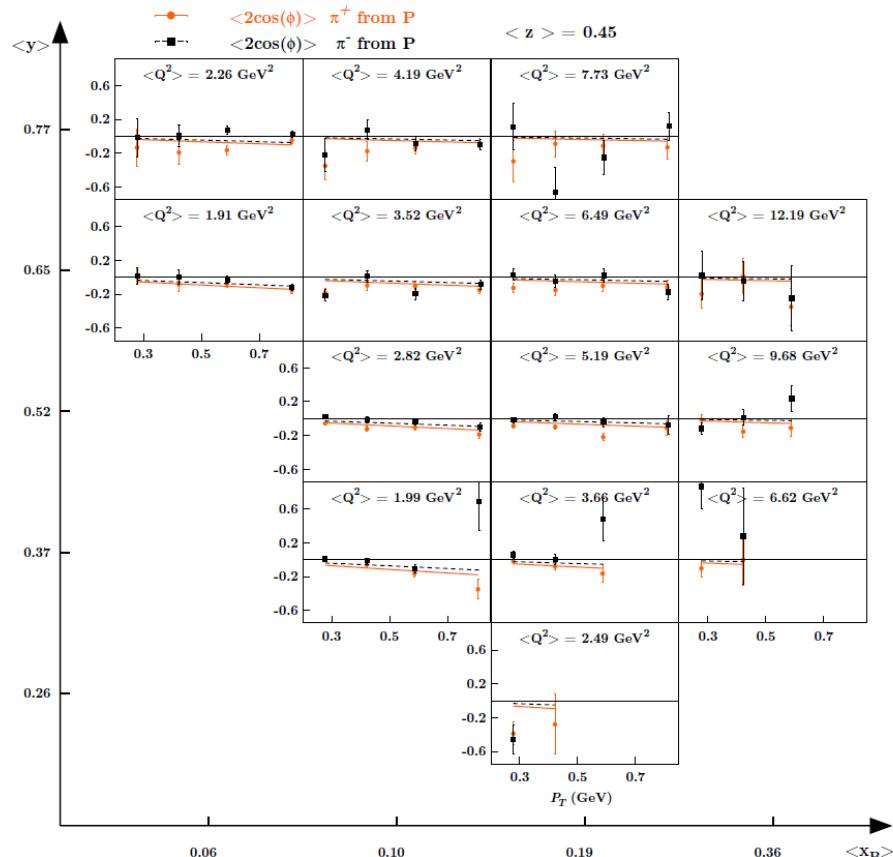
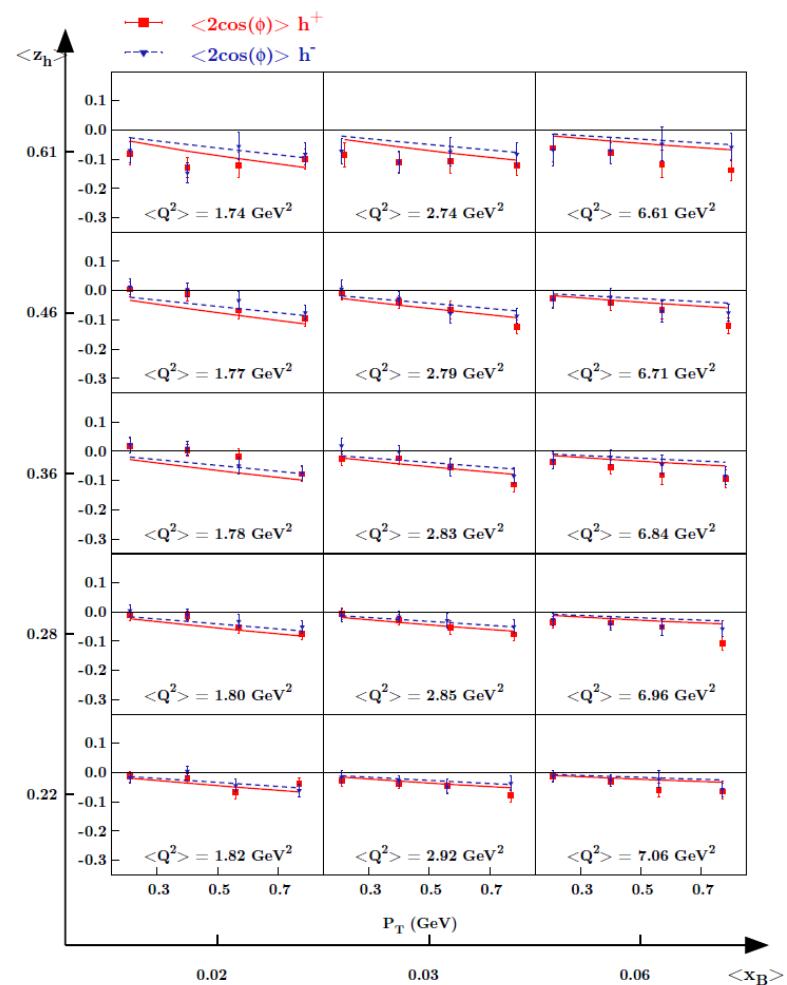
Effect of QCD evolution



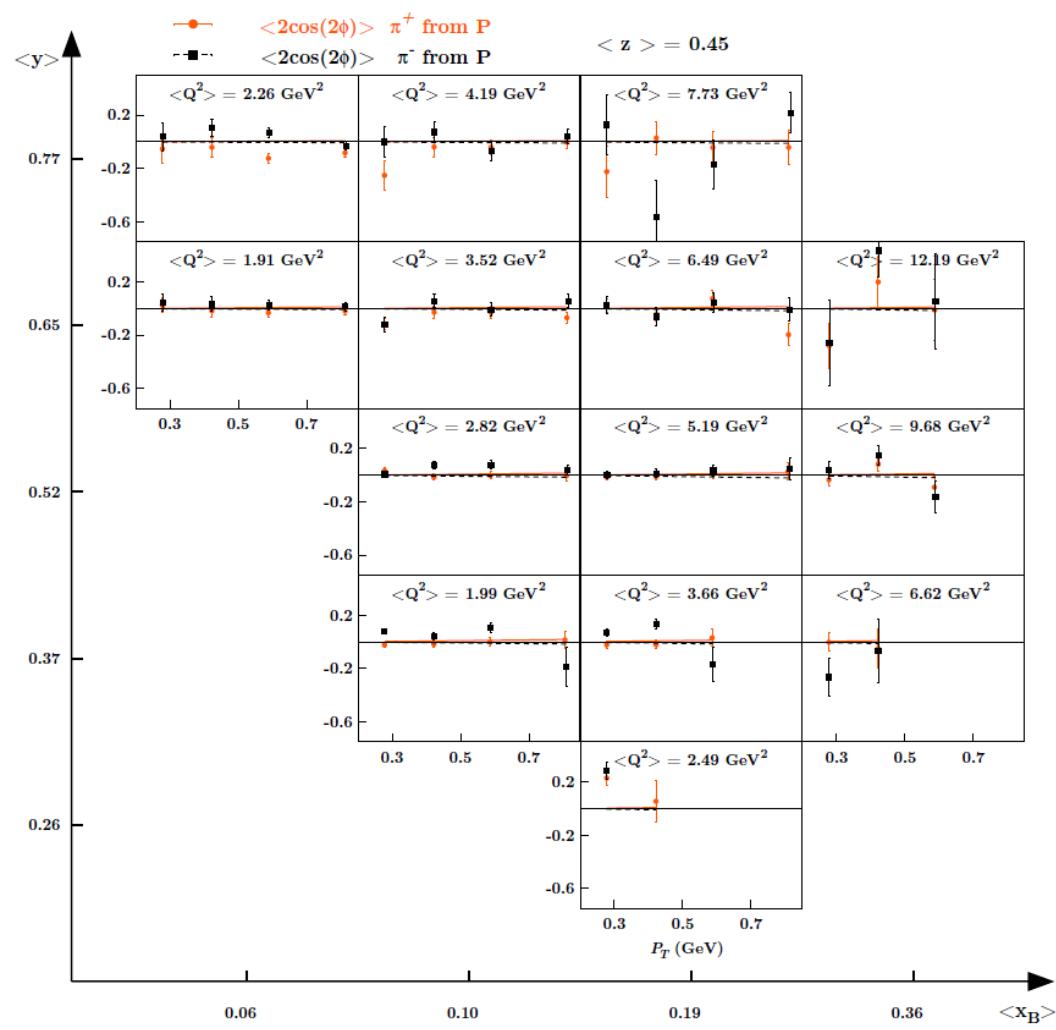
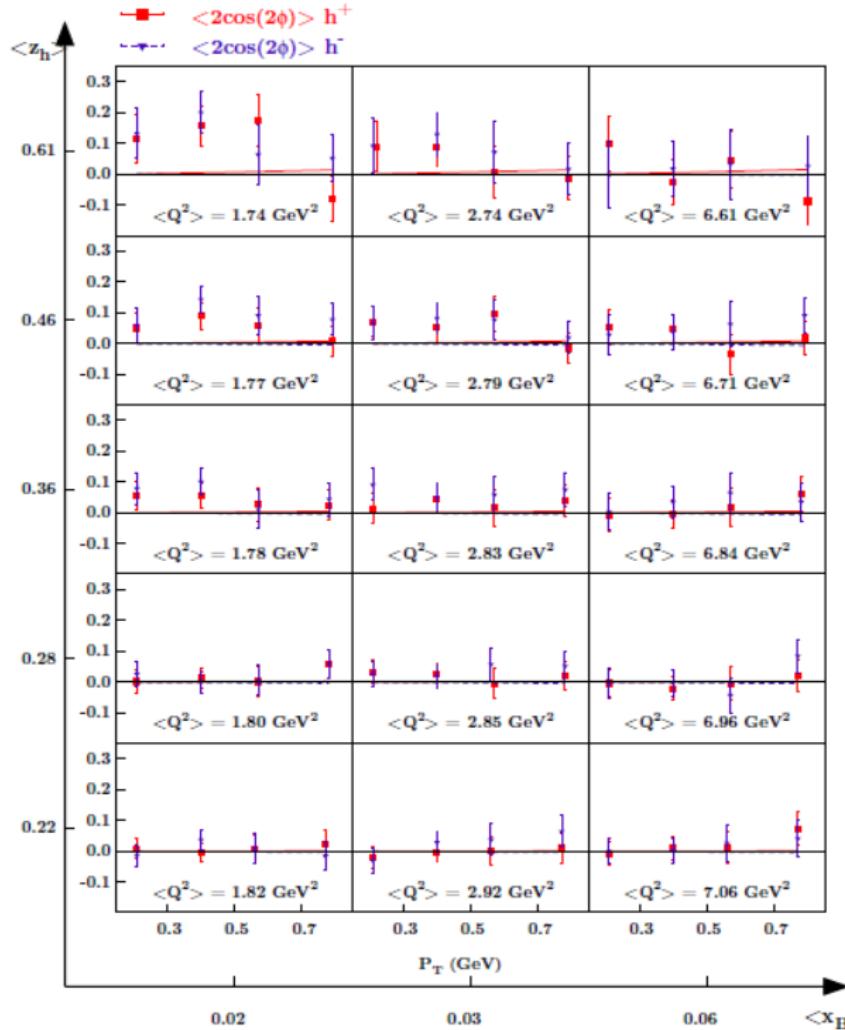
- What evolution does
 - Spread out the distribution to much larger k_T . At low k_T , the distribution decreases due to this spread



$\cos \phi$ modulation



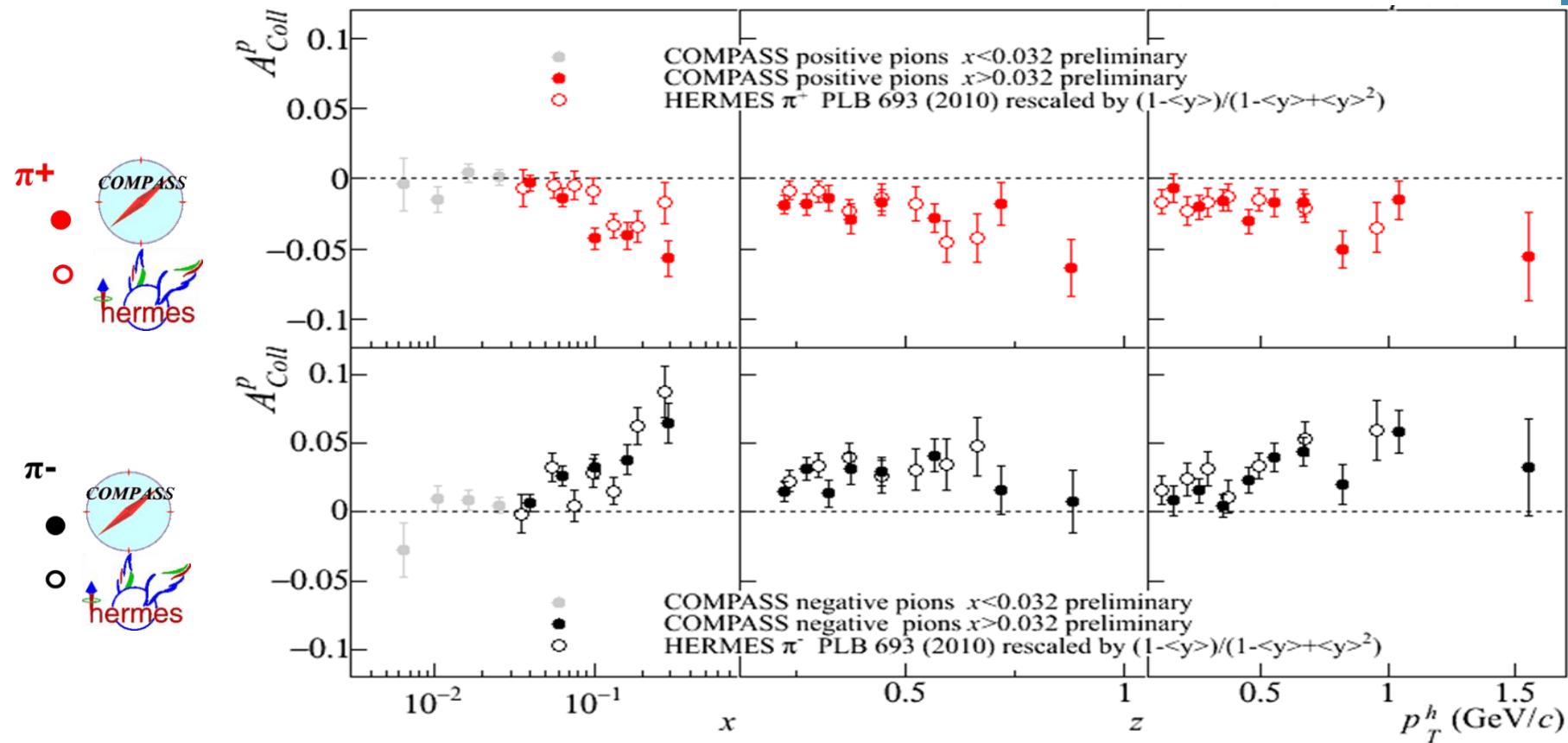
Boer-Mulders in $\cos 2\phi$ and in $\cos \phi$



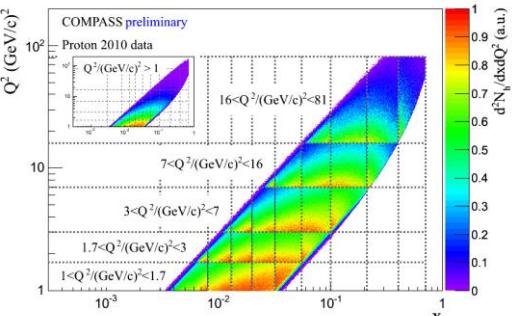
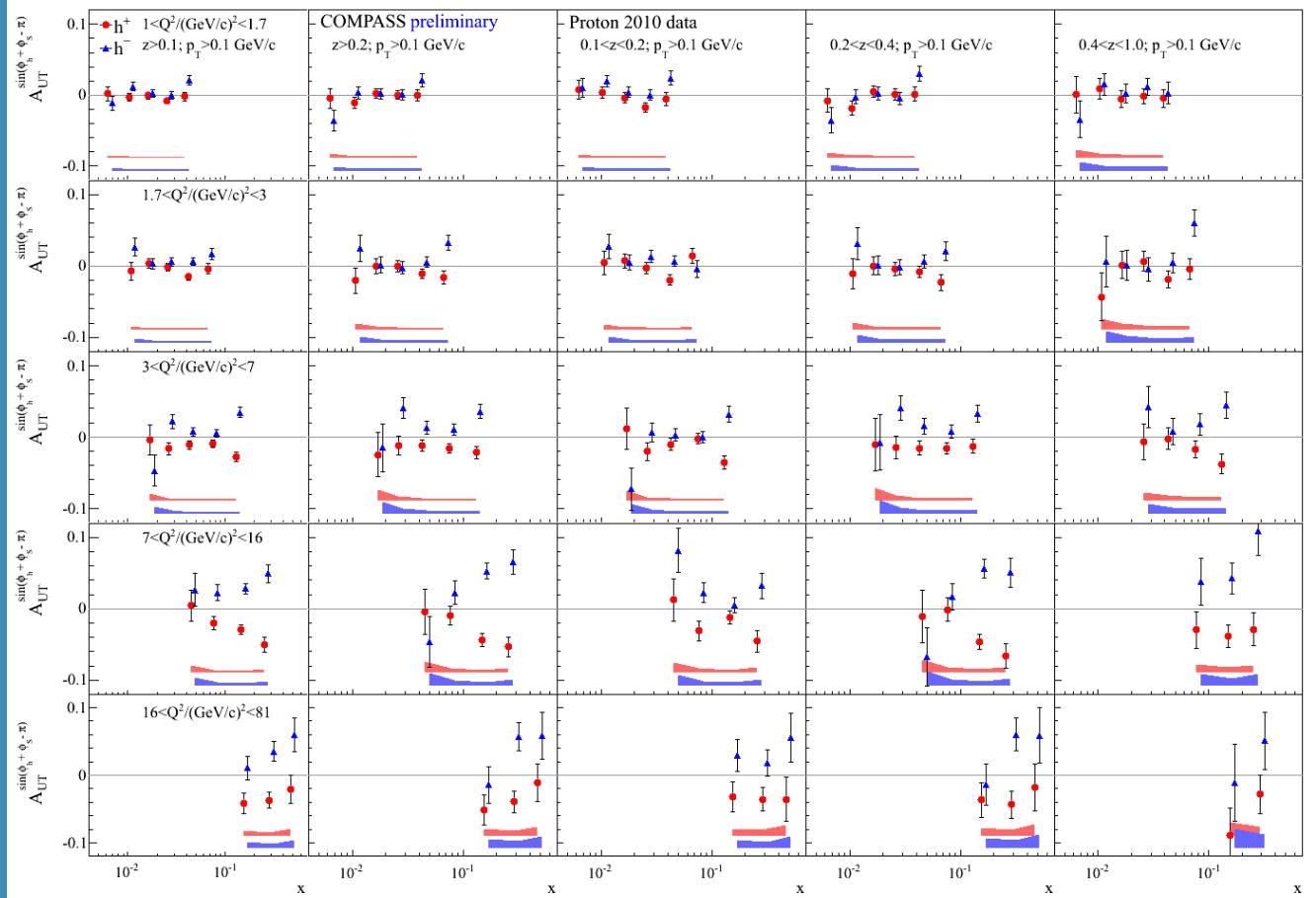
Collins asymmetry on proton

charged pions

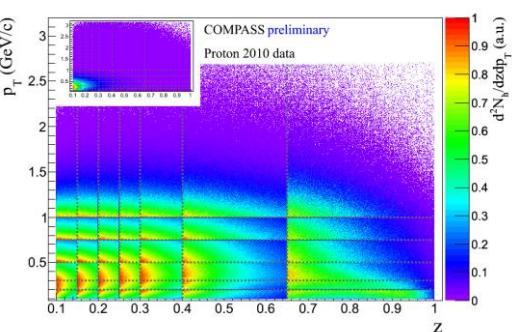
COMPASS and HERMES results



Collins asymmetry on proton. Multidimensional Extraction of TSAs with a Multi-D ($x: Q^2: z: p_T$) approach



One dense plot out
of many



- The theoretical expression of TMDs has a more complicated structure of the gauge link, connecting two space-time points with a transverse separation

$$f_{q/N}(x, \mathbf{k}_\perp) = \frac{1}{8\pi} \int dr^- \frac{dr_\perp^2}{(2\pi)^2} e^{-iMxr^-/2 + i\mathbf{k}_\perp \cdot \mathbf{r}_\perp}$$

$$\langle N(P) | \bar{q}(r^-, \mathbf{r}_\perp) \gamma^+ W[r^-, \mathbf{r}_\perp; 0] q(0) | N(P) \rangle|_{r^+ \sim 1/\nu \rightarrow 0}$$

- The Wilson line W is no longer on the light-cone axis and may introduce a **process dependence**

Parity and Time reversal invariance \Rightarrow

$$(f_{1Tq}^\perp)_{DY} = -(f_{1Tq}^\perp)_{SIDIS}$$

Most critical test to TMD approach to SSA

