

24th International Spin Symposium October 18 -22, 2021



# **Nuclear Spin-Isospin Responses Studied by Nuclear Reactions:** A tribute to Munetake Ichimura



Tomotsugu Wakasa Department of Physics Kyushu University

1938 - 2020

Dedicated to Ichimura-san

with deep gratitude

## Ichimura-san and the spin-isospin problems

Ichimura-san made a significant contribution to nuclear physics, especially:

Solve the spin-isospin problems such as

- Quenching of Gamow-Teller strength
- *Enhancement* of spin-longitudinal  $\pi$ -mode

Give a unified understanding of spin-isospin responses in wide  $(q, \omega)$  region

	Available online at www.sciencedirect.com SCIENCE DIRECT ELSEVIER Progress in Particle and Nuclear Physics 56 (2006) 446–531	Progress in Particle and Nuclear Physics www.elsevier.com/locate/ppnp		
Review				
Spin–isospin responses via $(p, n)$ and $(n, p)$ reactions				
	M. Ichimura <sup>a,*</sup> , H. Sakai <sup>b</sup> , T. Wakasa <sup>c</sup>			
	<sup>a</sup> Faculty of Computer and Information Sciences, Hosei University, Koganei, Tokyo 184-8584, Japan <sup>b</sup> Department of Physics, The University of Tokyo, Bunkyo, Tokyo 113-0033, Japan <sup>c</sup> Department of Physics, Kyushu University, Higashi, Fukuoka 812-8581, Japan			
	GT and pionic spin-longitudinal response			
	Recent progress for unstable nuclei			



# **GT Response Function R<sub>GT</sub>(ω)**

### **Gamow-Teller (GT) transition operator**

• Nucleon (N) space

$$O_{\rm GT} = t\boldsymbol{\sigma} = \frac{1}{2}\boldsymbol{\tau}\boldsymbol{\sigma}$$

Extend to N+
$$\Delta$$
 space  

$$O_{\text{GT}}^{\pm} = \mp \frac{1}{\sqrt{2}} \sum_{k=1}^{A} \left\{ \tau_{k,\pm 1} \boldsymbol{\sigma}_{k} + \frac{g_{A}^{N\Delta}}{g_{A}} (T_{k,\pm 1} S_{k} - T_{k,\mp 1}^{\dagger} S_{k}^{\dagger}) \right\}$$

**GT** response function

isospin operator from N to 
$$\Delta$$

\*q=q'=0 and  $\omega \sim 0$  for GT transition

## **Pionic (Spin-Longitudinal) Response Function**

**Isovector spin-longitudinal transition operator** 

$$O_L^{\lambda}(\boldsymbol{q}) = \sum_{k=1}^A \left\{ \tau_{k,\lambda} \boldsymbol{\sigma}_k \cdot \hat{\boldsymbol{q}} + \frac{f_{\pi N \Delta}}{f_{\pi N N}} \left( T_{k,\lambda} \boldsymbol{S}_k \cdot \hat{\boldsymbol{q}} + (-1)^{\lambda} T_{k,-\lambda}^{\dagger} \boldsymbol{S}_k^{\dagger} \cdot \hat{\boldsymbol{q}} \right) \right\} e^{i \boldsymbol{q} \cdot \boldsymbol{r}_k}$$

**Isovector spin-longitudinal response function** 

$$R_L^{\lambda}(q,\omega) = \sum_n \left| \langle \Psi_n | O_L^{\lambda}(\boldsymbol{q}) | \Psi_0 \rangle \right|^2 \delta(\omega - (\mathcal{E}_n - \mathcal{E}_0))$$

- Representing  $\pi NN$  and  $\pi N\Delta$  coupling



 $\approx q \sim q' \sim 1.7 \text{ fm}^{-1}$  and  $\omega \sim q^2/2m_N$  for quasi-elastic scattering

## **Contrastive Phenomena**

### Why Ichimura-san and we are especially interested in $R_{\text{GT}}$ and $R_{\text{L}}$ ?

- They show very contrastive phenomena
- Quenching of RGT

 $au\sigma$  :  $q\simeq 0,~\omega < 50\,{
m MeV}$ 

• GT resonance (GTR) region



Enhancement of RL

$$au \sigma \cdot \hat{q} \quad : \ q \simeq q_c \simeq 1.7 \, {
m fm}^{-1}, \quad \omega \simeq rac{q^2}{2m_N}$$

Quasi-elastic scattering (QES) region

# **Quenching of GT Transition I**



C. Gaarde, Nucl. Phys. A 369, 258 (1981).

R.R.Doering et al., Phys. Rev. lett. 35, 1691 (1975).

# **Quenching of GT Transition II**

Extraction of R<sub>GT</sub> (B(GT)) from (p,n) and (n,p) reactions

$$rac{d^2\sigma_{\Delta L=0}(q,\omega)}{d\Omega d\omega} = \hat{\sigma}_{
m GT}F(q,\omega)R_{
m GT}^{\pm}(\omega)$$

**GT** total strength

$$S^{\pm}_{
m GT}(\omega^{\pm}_{
m top}) = \int^{\omega^{\pm}_{
m top}} R^{
m exp}_{\pm,
m GT}(\omega) d\omega$$

GT sum rule

$$S_{eta^-} - S_{eta^+} = 3(N-Z)$$

• Model independent in the nucleon space

**GT** quenching factor

$$Q = rac{S_{ ext{GT}}^-(\omega_{ ext{top}}^-) - S_{ ext{GT}}^+(\omega_{ ext{top}}^+)}{3(N-Z)}$$

• If nucleus is made by nucleons, Q=1.



## **Origin of Quenching of Total GT Strength**

### Quark-degree (Δ-isobar) effect

Coupling between p-h and  $\Delta$ -h is *large (strong repulsion)* 

- Significant GT strengths move to  $\Delta$  region ( $\omega{\sim}300$  MeV)
- GTR strength is quenched

### **Configuration mixing effect**

2nd-order config. mixing is effective for all nuclei

- M.Ichimura and K.Yazaki, NP 63, 401 (1965).
- H.A.Mavromatis, L.Zamick, G.E.Brown, NP 80, 545 (1966).
- K.Shimizu, M.Ichimura, A.Arima, NPA 226, 282 (1974).
- I.S.Towner, F.C.Khanna, PRL 42, 51 (1979).
- I.S.Towner, PR 155, 264 (1987).
- A.Arima et al., Adv. NP, 18, 1 (1987).

Coupling between p-h and Δ-h is *small (weak repulsion)* 

- Strength-shift to  $\Delta$  region is small
- GTR strength is quenched by configuration mixing







## **Dominance of Nuclear Configuration Mixing**



## **Enhancement of Pionic Response**

A precursor phenomenon of pion condensation

Pionic (spin-longitudinal) response R<sub>L</sub> : **Enhanced** and softened

Rho-mesonic (spin-transverse) response R<sub>T</sub> : **Quenched** and hardened

•  $R_L/R_T \gg 1 \rightarrow$  Good signature of pion condensation precursor phenomena



# **Origin of the Enhancement/Quenching**

<u>M. Ichimura</u>, H. Sakai, TW, PPNP 56, 446 (2006). Effective p-h and Δ-h interaction governed by OPEP develops pionic correlation.



## **Experimental Spin-Response Ratio**

Pb(p,p') at  $T_p=500$  MeV and q=1.75 fm<sup>-1</sup>

Measure polarization transfer  $D_{ij} \rightarrow Separate I$  (cross section) into  $ID_L$  and  $ID_T$ 

Use the proportionality relation between  $ID_L$  ( $ID_T$ ) and  $R_L$  ( $R_T$ )

•  $R_L/R_T \sim 1 \rightarrow No evidence$  of theoretically expected enhancement



# **Issues raised by Prof. Ichimura**

**Prof.** Ichimura raised the following issues regarding the " $R_L/R_T$  ratio problem"

- Q1 : Is the method used to extract  $R_L$ ,  $R_T$  from  $D_{ij}$  reasonable?
  - Relation between the polarized cross sections and D<sub>ij</sub>
- Q2 : Are theoretical calculations of  $R_{\rm L}$  and  $R_{\rm T}$  reliable?
  - Fermi gas model calculations
- Q3 : Is the theoretical treatment of the reaction mechanism reasonable?
  - Proportionality between the polarization cross sections and the corresponding response functions

R <sub>L</sub> /R <sub>T</sub> Puzzle を解くための設問			
Q1. D <sub>ij</sub> から R <sub>L</sub> , R <sub>T</sub> を抽出する方法は妥 当か?			
Q2. R <sub>L</sub> , R <sub>T</sub> の理論計算は信頼できるか?			
Q3. 反応メカニズムの理論的取扱いは妥当か?			

Original slide by Prof. Ichimura in the RCNP workshop (1992).

### **Q1 : Is the method used to extract RL, RT from Dij reasonable?**

M. Ichimura and K.Kawahigashi, Phys. Rev. C 45, 1822 (1992).

### **Carey's formula**

• spin-longitudinal (
$$\pi$$
) :  $ID_q = rac{I}{4} \Big[ 1 - D_{NN} + (D_{SS'} - D_{LL'}) \sec heta_{
m lab} \Big] \propto R_I$ 

• spin-transverse (p):  $ID_p = \frac{I}{4} \Big[ 1 - D_{NN} - (D_{SS'} - D_{LL'}) \sec \theta_{\text{lab}} \Big] \propto R_T$ 

This formula is adequate only for NN scattering (NOT for NA scattering)

### Ichimura's correct formula

$$\cdot ID_{q} = \frac{I}{4} \Big[ 1 - D_{NN} + (D_{SS'} - D_{LL'}) \cos(2\theta_{p} - \theta_{\text{lab}} - \Omega) - (D_{LS'} + D_{SL'}) \sin(2\theta_{p} - \theta_{\text{lab}} - \Omega) \Big]$$
$$\cdot ID_{p} = \frac{I}{4} \Big[ 1 - D_{NN} - (D_{SS'} - D_{LL'}) \cos(2\theta_{p} - \theta_{\text{lab}} - \Omega) + (D_{LS'} + D_{SL'}) \sin(2\theta_{p} - \theta_{\text{lab}} - \Omega) \Big]$$



## **Q2 : Are theoretical calculations of R\_L and R\_T reliable?**



### Q3: Is the theoretical treatment of the reaction mechanism reasonable?



 $\omega_{lab}$  (MeV)

Exp. *ID<sub>i</sub>* should be compared with DWIA calc.

# **Unified Analysis**

### Analyzed

- GTGR spectrum
- GT quenching factor Q
- Spin-longitudinal (pionic) ID<sub>q</sub> spectrum

### by the common method

### Continuum RPA

- Δ isobar is included
- Woods-Saxon type mean field
- Local effective mass
- Spreading widths
- DWIA + Two-step processes
  - Fermi motion
  - Off-shell effect, etc.

PHYSICAL REVIEW C 72, 067303 (2005)

#### Unified analysis of spin isospin responses of nuclei

T. Wakasa,<sup>1</sup> M. Ichimura,<sup>2</sup> and H. Sakai<sup>3</sup> <sup>1</sup>Department of Physics, Kyushu University, Higashi, Fukuoka 812-8581, Japan <sup>2</sup>Faculty of Computer and Information Sciences, Hosei University, Koganei, Tokyo 184-8584, Japan <sup>3</sup>Department of Physics, The University of Tokyo, Bunkyo, Tokyo 113-0033, Japan (Received 8 October 2004; published 30 December 2005)

PHYSICAL REVIEW C, VOLUME 63, 044609

Distorted wave impulse approximation analysis for spin observables in nucleon quasielastic scattering and enhancement of the spin longitudinal response

Ken Kawahigashi\* Department of Information Sciences, Kanagawa University, Hiratsuka 259-1293, Japan

Kimiaki Nishida and Atsushi Itabashi Institute of Physics, University of Tokyo, Komaba, Meguro-ku, Tokyo 153-8902, Japan

Munetake Ichimura<sup>†</sup>

Faculty of Computer and Information Sciences, Hosei University, Koganei, Tokyo 184-8584, Japan (Received 27 July 2000; published 23 March 2001)

PHYSICAL REVIEW C 69, 054609 (2004)

#### Pionic enhancement in quasielastic $(\vec{p}, \vec{n})$ reactions at 345 MeV

T. Wakasa,<sup>1,\*</sup> H. Sakai,<sup>2,3</sup> M. Ichimura,<sup>4</sup> K. Hatanaka,<sup>5</sup> M. B. Greenfield,<sup>6</sup> M. Hatano,<sup>2</sup> J. Kamiya,<sup>7</sup> H. Kato,<sup>2</sup> K. Kawahigashi,<sup>8</sup> Y. Maeda,<sup>2</sup> Y. Nakaoka,<sup>-</sup> H. Okamura,<sup>9</sup> T. Ohnishi,<sup>3</sup> H. Otsu,<sup>10</sup> K. Sekiguchi,<sup>3</sup> K. Suda,<sup>11</sup> A. Tamii,<sup>5</sup> T. Uesaka,<sup>12</sup> T. Yagita,<sup>1</sup> and K. Yako<sup>2</sup> <sup>1</sup>Department of Physics, Kyushu University, Higashi, Fukuoka 812-8581, Japan <sup>2</sup>Department of Physics, The University of Tokyo, Bunkyo, Tokyo 113-0033, Japan <sup>3</sup>The Institute of Physical and Chemical Research, Wako, Saitama 351-0198, Japan <sup>4</sup>Faculty of Computer and Information Sciences, Hosei University, Koganei, Tokyo 184-8584, Japan <sup>3</sup>Research Center for Nuclear Physics, Osaka University, Ibaraki, Osaka 567-0047, Japan <sup>6</sup>Division of Natural Science, International Christian University, Mitaka, Tokyo 181-8585, Japan <sup>7</sup>Accelerator Group, Japan Atomic Energy Research Institute, Tokai, Ibaraki 319-1195, Japan <sup>8</sup>Department of Information Sciences, Kanagawa University, Hiratsuka, Kanagawa 259-1293, Japan <sup>9</sup>Cyclotron and Radioisotope Center, Tohoku University, Sendai, Miyagi 980-8578, Japan <sup>10</sup>Department of Physics, Tohoku University, Sendai, Miyagi 980-8578, Japan <sup>11</sup>Department of Physics, Saitama University, Saitama, Saitama 338-8570, Japan <sup>12</sup>Center for Nuclear Study, The University of Tokyo, Bunkyo, Tokyo 113-0033, Japan (Received 14 January 2004; published 25 May 2004)

# **Effective Interaction**

### Key parameters of the *unified/common* analysis

•  $\pi + \rho + g'$  model

$$V_{\rm eff}(\boldsymbol{q},\omega) = V_{\pi}(\boldsymbol{q},\omega) + V_{\rho}(\boldsymbol{q},\omega) + V_{\rm LM}$$

spin-longitudinal ( $\pi$ )

Landau-Migdal (LM) parameters

$$V_{\rm LM} = \frac{f_{\pi NN}^2}{m_{\pi}^2} \left\{ g_{NN}' (\boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2) (\boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2) \right\}$$



A copy of Prof. Ichimura's handwritten slides

$$+\frac{f_{\pi N\Delta}}{f_{\pi NN}}g'_{N\Delta}\left[\left((\boldsymbol{\tau}_{1}\cdot\boldsymbol{T}_{2})(\boldsymbol{\sigma}_{1}\cdot\boldsymbol{S}_{2})+(\boldsymbol{\tau}_{1}\cdot\boldsymbol{T}_{2}^{\dagger})(\boldsymbol{\sigma}_{1}\cdot\boldsymbol{S}_{2}^{\dagger})\right)+(1\leftrightarrow2)\right]\\+\left(\frac{f_{\pi\Delta\Delta}}{f_{\pi NN}}\right)^{2}g'_{\Delta\Delta}\left[\left((\boldsymbol{T}_{1}\cdot\boldsymbol{T}_{2})(\boldsymbol{S}_{1}\cdot\boldsymbol{S}_{2})+(\boldsymbol{T}_{1}\cdot\boldsymbol{T}_{2}^{\dagger})(\boldsymbol{S}_{1}\cdot\boldsymbol{S}_{2}^{\dagger})\right)+\text{h.c.}\right]\right\}\delta(\boldsymbol{r}_{1}-\boldsymbol{r}_{2})$$

 $*g'_{\Delta\Delta}$  is fixed to be 0.5 because its dependence is known to be small.

# **GTGR Spectrum**

### Experiment: <sup>90</sup>Zr(p,n)<sup>90</sup>Nb at 295 MeV

- Prominent GTGR peak
- GT (L=0) contribution is extracted by MDA
- GT strength, B(GT), is deduced with proportionality ansatz

### **Comparison with theory**

- GTGR peak position
  - Strongly depends on g'NN

 $g'_{NN} = 0.6 \pm 0.1$ 

• Weak  $g'_{N\Delta}$  dependence



# **GT Quenching Factor Q**

### GT quenching factor Q

- $Q = 0.86 \pm 0.07 \leftarrow$  from MD analysis
  - 2p2h effects are dominant

### **Q** evaluated in **RPA**

- Determine the coupling to  $\Delta$
- Larger  $g'_{N\Delta} \rightarrow$  Stronger coupling
  - Strength becomes small (quenched)
     [Strength moves to Δ region]
- Q strongly depends on  $g'_{N\Delta}$

 $g'_{N\Delta}=0.35\pm0.16$ 

- Weak  $g'_{NN}$  dependence



## **Spin-Longitudinal (Pionic)** *ID*<sub>q</sub> **Enhancement**

### Experiment ( $q = 1.7 \text{ fm}^{-1}$ )

- <sup>12</sup>C(p,n) at RCNP
  - T<sub>p</sub>=346 MeV and  $\theta$ =22°
- <sup>12</sup>C(p,n) at LAMPF
  - + T<sub>p</sub>=494 MeV and  $\theta$ =18°

### **Comparison with theory**

- DWIA + two-step
- QES peak depends on g'NN
  - g'<sub>NN</sub> = 0.6-0.7
- Enhancement depends on  $g'_{\mathsf{N}\!\Delta}$ 
  - $g'_{N\Delta} = 0.2-0.4$



$$g'_{NN} \approx 0.7, \quad g'_{N\Delta} \approx 0.3 \iff g'_{NN} = 0.6 \pm 0.1, \quad g'_{N\Delta} = 0.35 \pm 0.16$$
 $q \simeq 1.7 \, {\rm fm}^{-1} \qquad \qquad q = 0 \, {\rm fm}^{-1}$ 

# **Ichimura-san's summary in SPIN2004**



In summary, our unified approach leads to a common set of the LM parameters,  $g'_{NN}=0.6-0.7$  and  $g'_{N\Lambda}=0.2-0.4$  for the above contrasting phenomena.

### Unified understanding of nuclear spin responses in wide (q, $\omega$ ) region with just wo parameters, g'<sub>NN</sub> and g'<sub>NA</sub>

trieste october 10 16 2004



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## **Spin-isospin responses for unstable nuclei**



## B(GT) and Landau-Migdal parameter g'<sub>NN</sub> in <sup>132</sup>Sn

J. Yasuda, M. Sasano, TW et al., Phys. Rev. Lett. 121, 132501 (2018).

GT giant resonance (GTGR) is observed for <sup>132</sup>Sn (doubly-magic unstable nuclei)

GTGR peak is sensitive to g'NN

- Ratio of the bump to the main peak is also sensitive to  $g'_{\mbox{\scriptsize NN}}$ 

 $g^\prime_{NN}=0.68\pm0.07$ 

\* g'<sub>NN</sub> is constant for isospin asymmetry (N-Z)/A of 0.11(<sup>90</sup>Zr) to 0.24(<sup>132</sup>Sn)



## **Experimental results**

Gamow-Teller resonances have been *successfully observed* for <sup>8</sup>He and <sup>12</sup>Be



M. Kobayashi et al., JPS Conf. Proc. 1, 013034 (2014). courtesy of K. Yako

### **Collectivity in (N-Z)/A > 0.21; Very neutron-rich nuclei**



Data are consistent with predictions employing g'<sub>NN</sub>=0.6±0.1

 $\rightarrow$  Suggests the constancy of residual interaction for up to (N-Z)/A=0.5 (very neutron-rich)

## **NEW reaction probe for pionic 0- state**



## Ichimura-san's legacy will live on

Ichimura-san's work laid the grounds for

- the unified understanding of spin-isospin responses
- the analysis of experimental data using his computer codes
  - CRDW : DWIA calculation
  - RESPQ : Spin-isospin response calculation



Computer Programs	•.•.
by M.Ichimura	
CRDW is the abbreviation for Continuum RPA + DWIA. for the nucleon induced inelastic and charge exchange	This is a computer program, which perform a DWIA calculation e reactions to continuum final states as well as discrete states.
<ul> <li>Manual (PDF/259kb)</li> <li>Formalism (PDF/211kb)</li> </ul>	

#### RESPQ

#### by M.Ichimura

RESPQ is a computer program, which calculate the isovector spin-scalar, and spin-vector response functions of nuclei as a function of the transferred momentum q and energy  $\omega$  including  $\Delta$  isobar degrees of freedom.

RIKEN Nishina Center for Accelerator-Based Science

Manual (PDF/262kb)
Source codes (65kb)

Source codes (243kb)