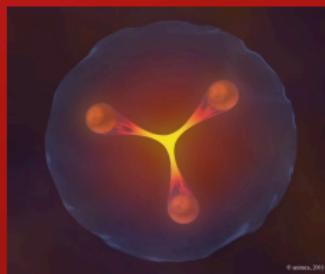


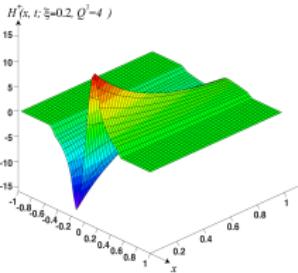
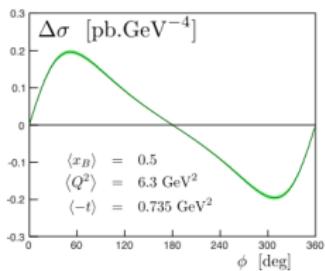
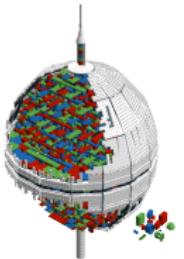
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Proton mechanical properties from DVCS: phenomenology assessment



SPIN2021 | Hervé MOUTARDE

Oct. 20, 2021

This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093.

université
PARIS-SACLAY

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- Is it well-defined?
- Can it be measured?
- What are the needed theory inputs?

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- Is it well-defined? Yes!
- Can it be measured? Yes!
- What are the needed theory inputs? GPD functional shape! Perhaps x or t -dependence at a given scale is enough.

Expect valuable inputs from lattice or continuum QCD. Wait for future measurements

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■ Matrix element in the Breit frame ($a = q, g$):

$$\left\langle \frac{\Delta}{2} |T_a^{\mu\nu}(0)| - \frac{\Delta}{2} \right\rangle = M \left\{ \eta^{\mu 0} \eta^{\nu 0} \left[A_a(t) + \frac{t}{4M^2} B_a(t) \right] + \eta^{\mu\nu} \left[\bar{C}_a(t) - \frac{t}{M^2} C_a(t) \right] + \frac{\Delta^\mu \Delta^\nu}{M^2} C_a(t) \right\}$$

■ Anisotropic fluid in relativistic hydrodynamics:

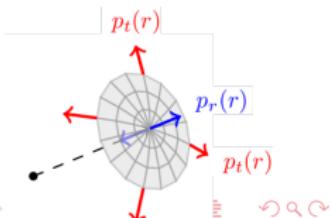
$$\Theta^{\mu\nu}(\vec{r}) = [\varepsilon(r) + p_t(r)] u^\mu u^\nu - p_t(r) \eta^{\mu\nu} + [p_r(r) - p_t(r)] \chi^\mu \chi^\nu$$

where u^μ and $\chi^\mu = x^\mu/r$.

- Define **isotropic pressure** and **pressure anisotropy**:

$$p(r) = \frac{p_r(r) + 2 p_t(r)}{2}$$

$$s(r) = p_r(r) - p_t(r)$$



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- Write dictionary between quantum and fluid pictures:

$$\frac{\varepsilon_a(r)}{M} = \int \frac{d^3 \vec{\Delta}}{(2\pi)^3} e^{-i\vec{\Delta} \cdot \vec{r}} \left\{ A_a(t) + \bar{C}_a(t) + \frac{t}{4M^2} [B_a(t) - 4C_a(t)] \right\}$$

$$\frac{p_{r,a}(r)}{M} = \int \frac{d^3 \vec{\Delta}}{(2\pi)^3} e^{-i\vec{\Delta} \cdot \vec{r}} \left\{ -\bar{C}_a(t) - \frac{4}{r^2} \frac{t^{-1/2}}{M^2} \frac{d}{dt} \left(t^{3/2} C_a(t) \right) \right\}$$

$$\frac{p_{t,a}(r)}{M} = \int \frac{d^3 \vec{\Delta}}{(2\pi)^3} e^{-i\vec{\Delta} \cdot \vec{r}} \left\{ -\bar{C}_a(t) + \frac{4}{r^2} \frac{t^{-1/2}}{M^2} \frac{d}{dt} \left[t \frac{d}{dt} \left(t^{3/2} C_a(t) \right) \right] \right\}$$

$$\frac{p_a(r)}{M} = \int \frac{d^3 \vec{\Delta}}{(2\pi)^3} e^{-i\vec{\Delta} \cdot \vec{r}} \left\{ -\bar{C}_a(t) + \frac{2}{3} \frac{t}{M^2} C_a(t) \right\}$$

$$\frac{s_a(r)}{M} = \int \frac{d^3 \vec{\Delta}}{(2\pi)^3} e^{-i\vec{\Delta} \cdot \vec{r}} \left\{ -\frac{4}{r^2} \frac{t^{-1/2}}{M^2} \frac{d^2}{dt^2} \left(t^{5/2} C_a(t) \right) \right\}$$

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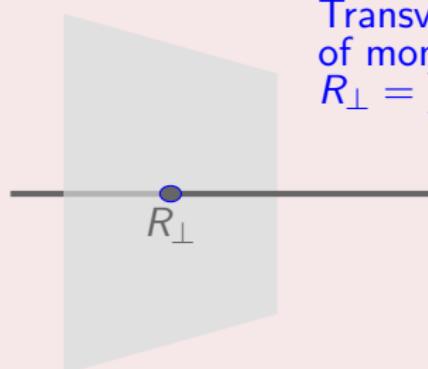
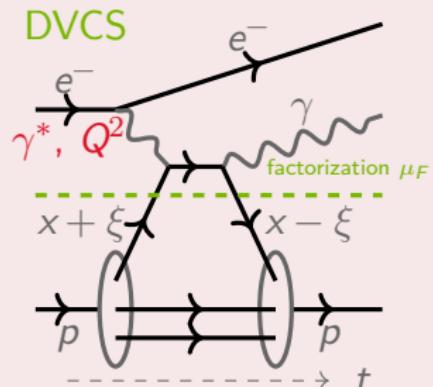
■ Link between GPDs and GFFs

$$\int dx x H^q(x, \xi, t) = A^q(t) + 4\xi^2 C^q(t)$$

$$\int dx x E^q(x, \xi, t) = B^q(t) - 4\xi^2 C^q(t)$$

↳ Ji (1997), ↳ Goeke (2001)

Deeply Virtual Compton Scattering (DVCS)



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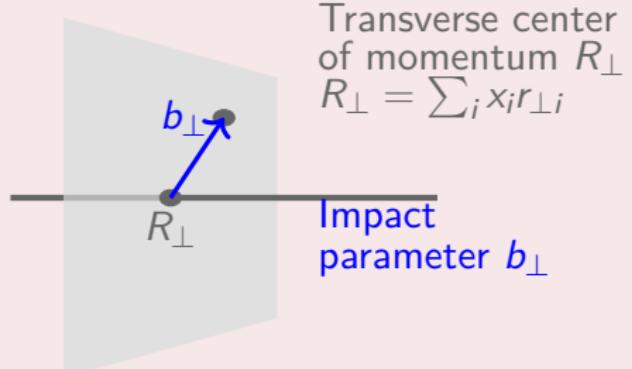
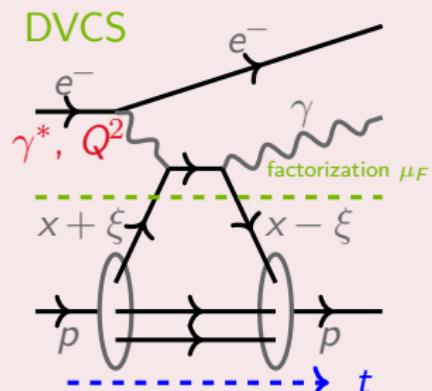
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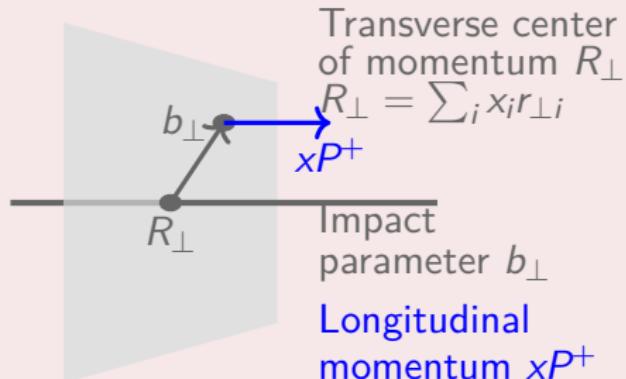
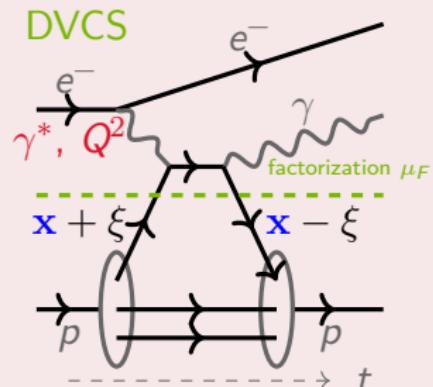
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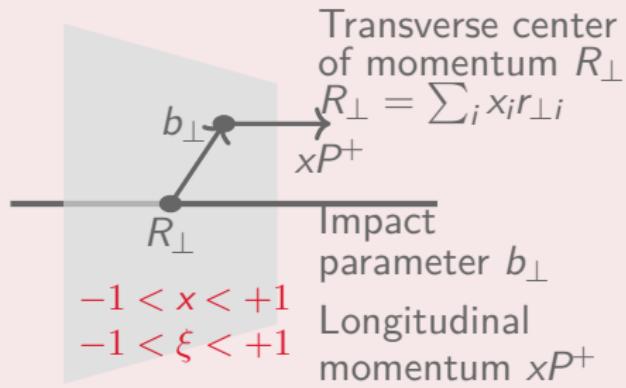
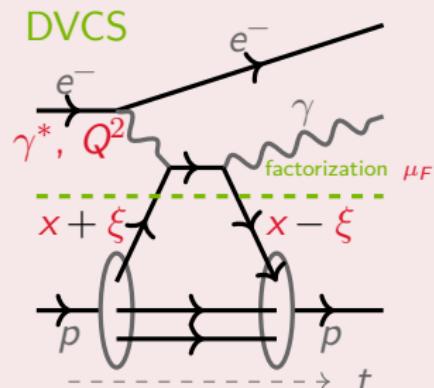
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Bjorken regime : large Q^2 and fixed $xB \simeq 2\xi/(1 + \xi)$

- Partonic interpretation relies on **factorization theorems**.
 - All-order proofs for DVCS.
 - GPDs depend on a (arbitrary) factorization scale μ_F .
 - **Consistency** requires the study of **different channels**.
-
- GPDs enter DVCS through **Compton Form Factors** :

$$\mathcal{F}(\xi, t, Q^2) = \int_{-1}^1 dx T\left(x, \xi, \alpha_S(\mu_F), \frac{Q}{\mu_F}\right) F(x, \xi, t, \mu_F)$$

for a given GPD F .

- CFF \mathcal{F} is a **complex function**.

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1 Expand D-term on Gegenbauer polynomials

$$D_{\text{term}}^q(z, t, \mu_F^2) = (1 - z^2) \sum_{\text{odd } n} d_n^q(t, \mu_F^2) C_n^{3/2}(z)$$

2 Write dispersion relation for CFF (true at all pQCD orders)

$$\mathcal{C}_H(t, Q^2) = \text{Re}\mathcal{H}(\xi) - \frac{1}{\pi} \int_0^1 d\xi' \text{Im}\mathcal{H}(\xi') \left(\frac{1}{\xi - \xi'} - \frac{1}{\xi + \xi'} \right)$$

3 Compute subtraction constant

$$\mathcal{C}_H^{q,g}(t, Q^2) = \frac{2}{\pi} \int_1^{+\infty} d\omega \text{Im} T^{q,g}(\omega) \int_{-1}^1 dz \frac{D^{q,g}(z)}{\omega - z}$$

Diehl & Ivanov (2007)

4 Retrieve GFF

$$d_1^q(t, \mu_F^2) = 5 C_q(t, \mu_F^2)$$

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3 Compute subtraction constant at LO

$$\mathcal{C}_H(t, Q^2) = 4 \sum_q e_q^2 \sum_{\text{odd } n} d_n^q(t, \mu_F^2 \equiv Q^2)$$

Diehl & Ivanov (2007)

4 Retrieve GFF

$$d_1^q(t, \mu_F^2) = 5 C_q(t, \mu_F^2)$$

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GFF C
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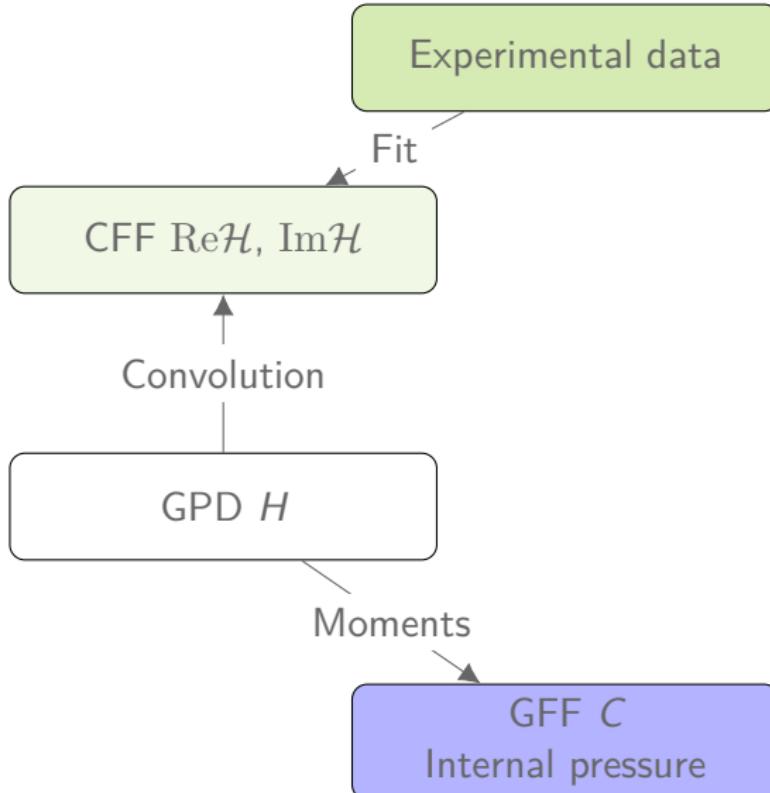
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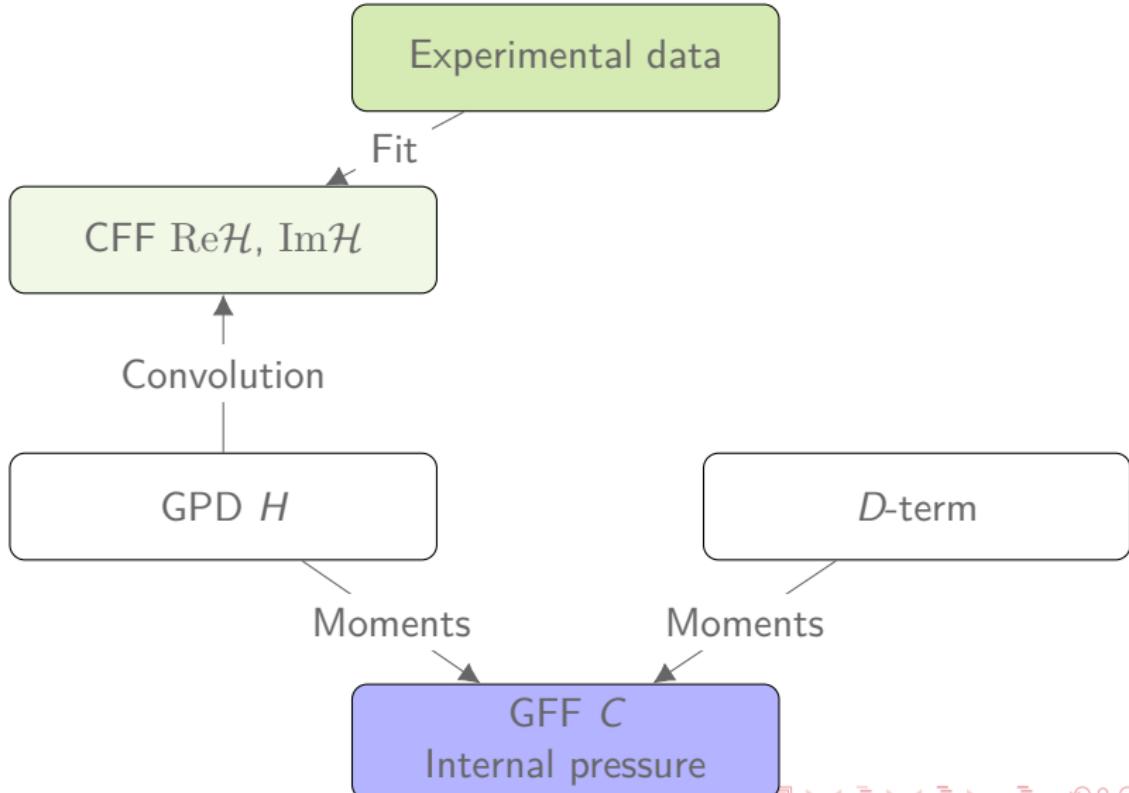
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Extracting chain.

Implementing this first-principle connection.

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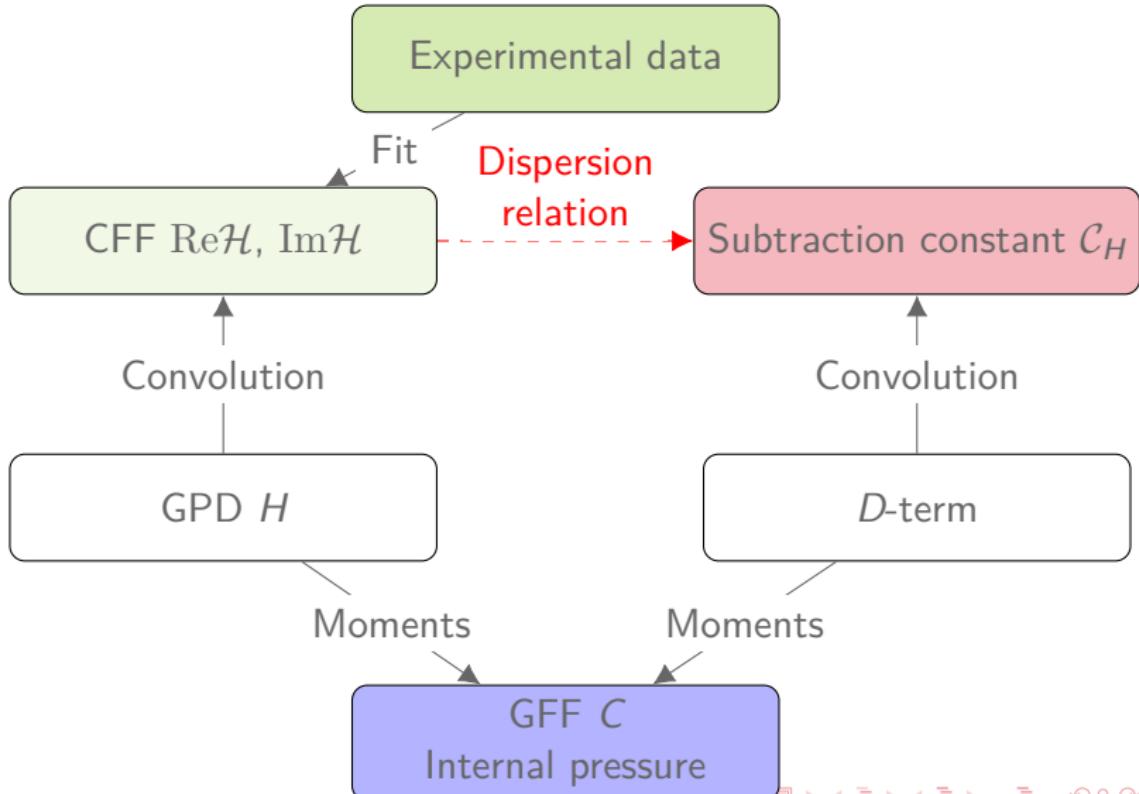
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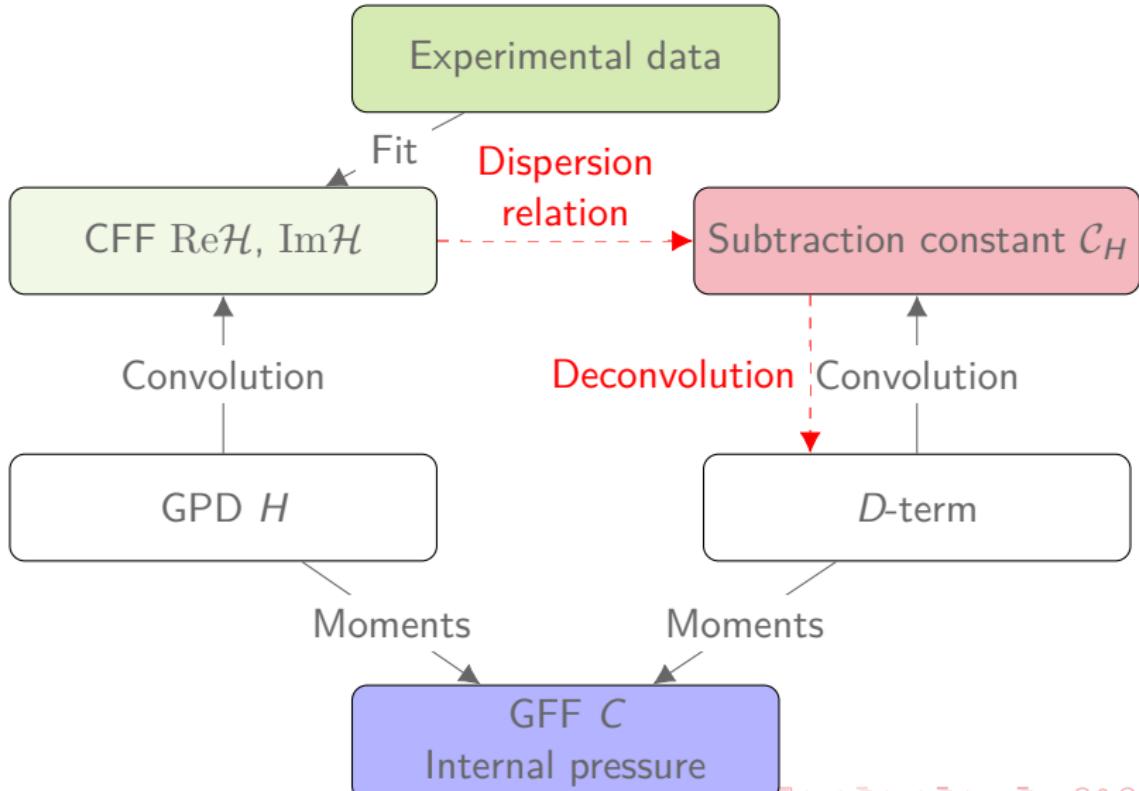
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Almost all existing DVCS data sets.

2600+ measurements of 30 observables published during 2001-17.

	No.	Collab.	Year	Ref.	Observable	Kinematic dependence	No. of points used / all
Proton mechanical properties	1	HERMES	2001	[40]	A_{LU}^+	ϕ	10 / 10
	2		2006	[41]	$A_C^{\cos i\phi}$	$i = 1$	4 / 4
	3		2008	[42]	$A_C^{\cos i\phi}$	$i = 0, 1$	x_{Bj} 18 / 24
Theoretical framework	4		2009	[43]	$A_{UT,DVCS}^{\sin(\phi-\phi_S) \cos i\phi}$	$i = 0$	
Gravitational form factors					$A_{UT,I}^{\sin(\phi-\phi_S) \cos i\phi}$	$i = 0, 1$	
Pressure	5		2010	[44]	$A_{UT,I}^{\cos(\phi-\phi_S) \sin i\phi}$	$i = 1$	
GPDs	6		2011	[45]	$A_{LU,I}^{\sin i\phi}$	$i = 1, 2$	x_{Bj} 35 / 42
Phenomenology					$A_{LU,DVCS}^{\sin i\phi}$	$i = 1$	
CFF global fit					$A_C^{\cos i\phi}$	$i = 0, 1, 2, 3$	
Pressure forces	7		2012	[46]	A_{UL}^+	$i = 1, 2, 3$	
Models: systematic uncertainties					$A_{UL}^{+, \cos i\phi}$	$i = 0, 1, 2$	
Maximize theory input	8	CLAS	2001	[47]	$A_{LT,DVCS}^{\cos(\phi-\phi_S) \cos i\phi}$	$i = 0, 1$	
Deconvolution problem	9		2006	[48]	$A_{LT,DVCS}^{\sin(\phi-\phi_S) \sin i\phi}$	$i = 1$	
Ecosystem	10		2008	[49]	$A_{LT,I}^{\cos(\phi-\phi_S) \cos i\phi}$	$i = 0, 1, 2$	
Design	11		2009	[50]	$A_{LT,I}^{\sin(\phi-\phi_S) \sin i\phi}$	$i = 1, 2$	
EpiC event generator	12		2015	[51]	$A_{LU}^-, A_{UL}^-, A_{LL}^-$	$i = 1, 2$	— 0 / 2
GPD evolution	13		2015	[52]	$d^4\sigma_{UU}^-$	$i = 1, 2$	— 2 / 2
Conclusion	14	Hall A	2015	[34]	$\Delta d^4\sigma_{LU}^-$	ϕ	283 / 737
Abbreviations	15		2017	[35]	$\Delta d^4\sigma_{LU}^-$	ϕ	22 / 33
	16	COMPASS	2018	[36]	$d^3\sigma_{UU}^-$	ϕ	311 / 497
	17	ZEUS	2009	[37]	$d^3\sigma_{UU}^+$	ϕ	1333 / 1933
	18	H1	2005	[38]	$d^3\sigma_{UU}^+$	ϕ	228 / 228
	19		2009	[39]	$d^3\sigma_{UU}^\pm$	ϕ	276 / 358
						t	2 / 4
						t	4 / 4
						t	7 / 8
						t	12 / 12

SUM: 2624 / 3996

Almost all existing DVCS data sets. 2600+ measurements of 30 observables published during 2001-17.

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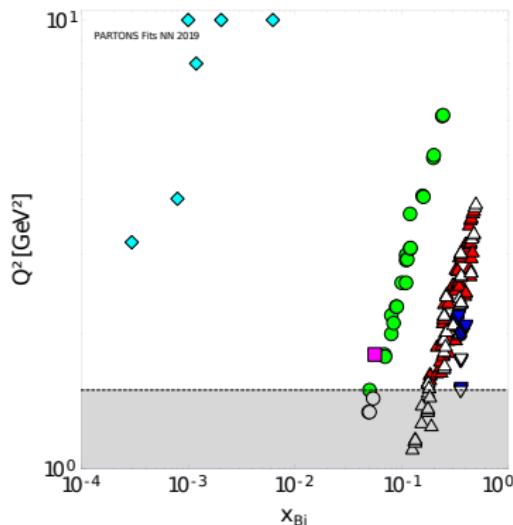
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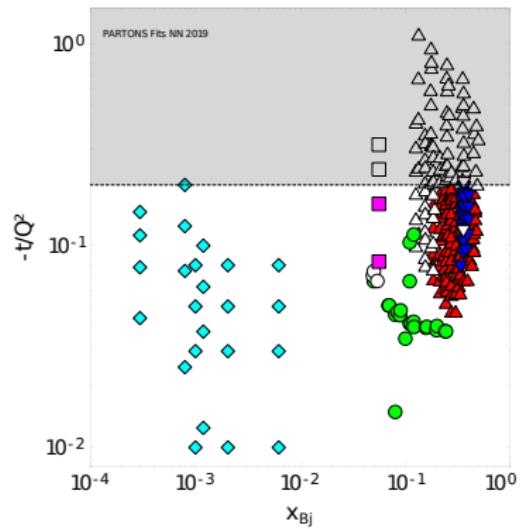
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▼ Hall A
▲ CLAS

● HERMES
◆ H1 and ZEUS



■ COMPASS

Moutarde *et al.* (2019)

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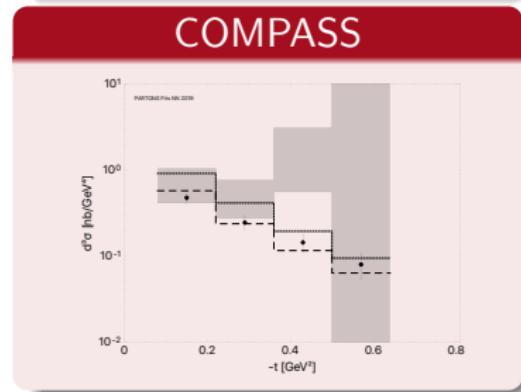
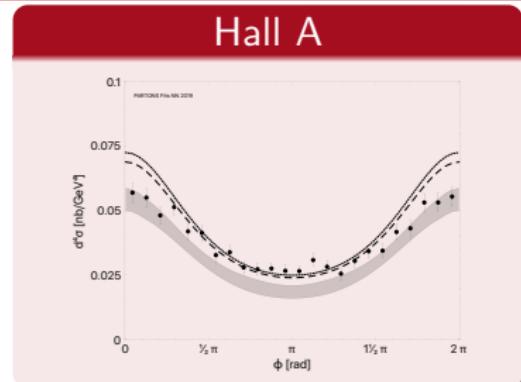
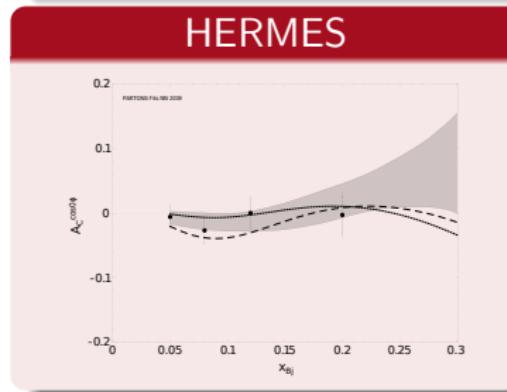
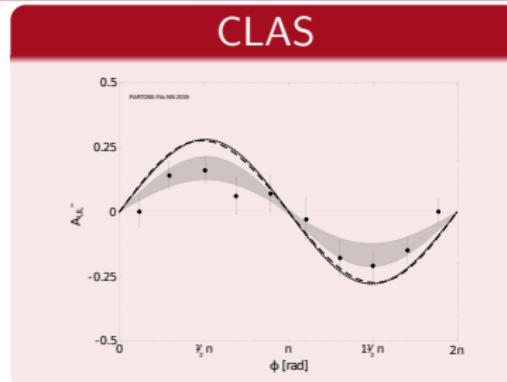
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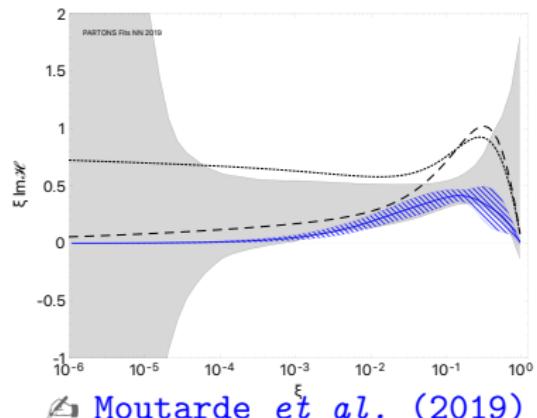
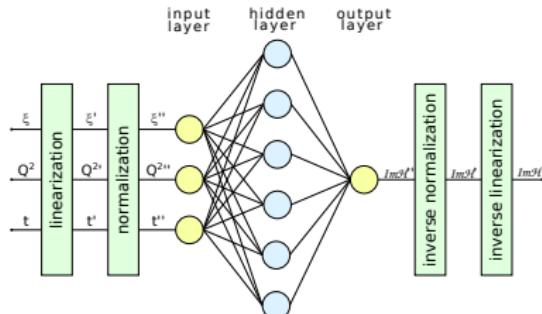
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- Real and imaginary parts of CFFs parameterized by **neural networks**.
- Propagation of uncertainties through **replica method** and evaluation of 68 % **confidence levels**.



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Range of kinematic variables in neural networks

$$\begin{aligned} 10^{-6} &< \xi &< 1 \\ 0 &< -t &< 1 \text{ GeV}^2 \\ 1 &< Q^2 &< 100 \text{ GeV}^2 \end{aligned}$$

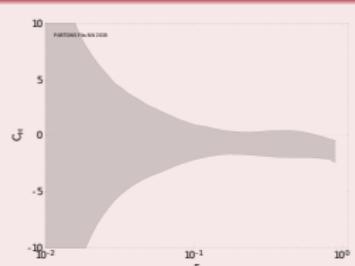
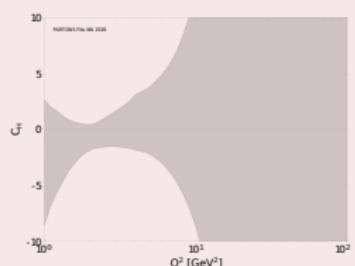
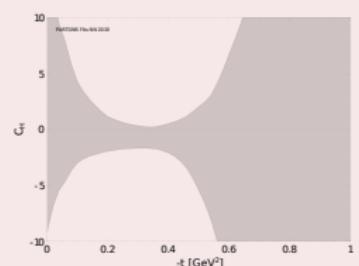
Implement DVCS dispersion relation

$$\mathcal{C}_H(t, Q^2) = \text{Re}\mathcal{H}(\xi) - \frac{1}{\pi} \int_{10^{-6}}^1 d\xi' \text{Im}\mathcal{H}(\xi) \left(\frac{1}{\xi - \xi'} - \frac{1}{\xi + \xi'} \right)$$

$$\begin{aligned} \xi &= 0.2 \\ Q^2 &= 2 \text{ GeV}^2 \end{aligned}$$

$$\begin{aligned} \xi &= 0.2 \\ t &= -0.3 \text{ GeV}^2 \end{aligned}$$

$$\begin{aligned} t &= -0.3 \text{ GeV}^2 \\ Q^2 &= 2 \text{ GeV}^2 \end{aligned}$$



 Moutarde et al. (2019)

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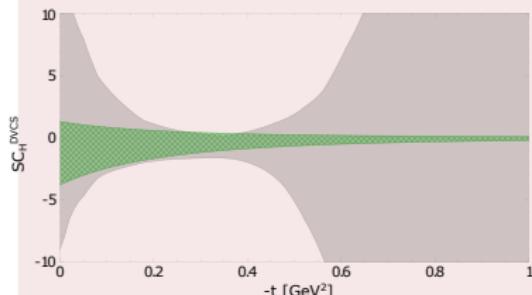
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- 1 Subtraction constant assumed equal to d_1 .
- 2 Equal values for light quark contributions d_1^{uds} .
- 3 Radiative generation of gluon d_1^g and charm d_1^c contributions.
- 4 Tripole Ansatz for the t -dependence of d_1 .

Tripole Ansatz



Parameter	Value
$d_1^{uds}(\mu_F^2)$	-0.45 ± 0.92
$d_1^c(\mu_F^2)$	-0.0020 ± 0.0041
$d_1^g(\mu_F^2)$	-0.6 ± 1.3

Dutrieux et al. (2021)

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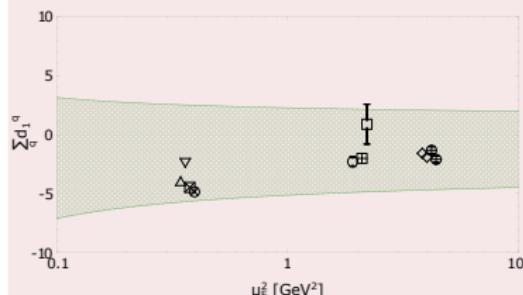
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 d_1 from DVCS data

Parameter	Value
$d_1^{uds}(\mu_F^2)$	-0.45 ± 0.92
$d_1^c(\mu_F^2)$	-0.0020 ± 0.0041
$d_1^g(\mu_F^2)$	-0.6 ± 1.3

Dutrieux et al. (2021)

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Summary of existing determinations

No.	Marker in Fig. 3	$\sum_q d_1^q(\mu_F^2)$	μ_F^2 in GeV^2	# of flavours	Type	Ref.
1	○	$-2.30 \pm 0.16 \pm 0.37$	2.0	3	from experimental data	[13]
2	□	0.88 ± 1.69	2.2	2	from experimental data	[14]
3	◊	-1.59	4	2	t -channel saturated model	[55]
		-1.92	4	2	t -channel saturated model	[55]
4	△	-4	0.36	3	χ QSM	[30]
5	▽	-2.35	0.36	2	χ QSM	[10]
6	⊗	-4.48	0.36	2	Skyrme model	[56]
7	田	-2.02	2	3	LFWF model	[57]
8	⊗	-4.85	0.36	2	χ QSM	[58]
9	⊕	-1.34 ± 0.31	4	2	lattice QCD ($\overline{\text{MS}}$)	[59]
		-2.11 ± 0.27	4	2	lattice QCD (MS)	[59]

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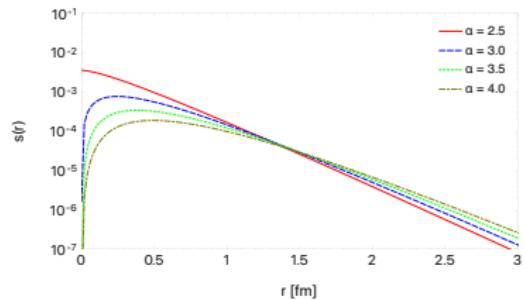
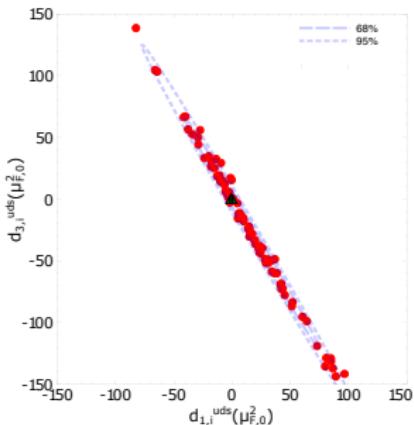
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- No justification to truncate the subtraction constant expansion to its first term and assume that it is the d_1 coefficient related to the energy-momentum tensor.
- Shape of pressure profile is fixed by multipole Ansatz. Actual value is extremely sensitive to its parameters.



Dutrieux et al. (2021)

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- Reduction to PDFs or elastic form factors.
- Implement *a priori* positivity and polynomiality. Still uncommon in many models or parameterizations used for phenomenology.

See P. Sznajder's talk at 17:20 and J.-M. Morgado Chavez's talk at 17:40 (today)

- General solution starting from overlap of (potentially effective) light front wave functions.
 Chouika et al. (2017)
- Use of evolution equations to implement further constraints on the GPD functional form.
- Work beyond leading-order and depart from the parton model...
- Systematic impact study or use of kinematic corrections still missing.

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- Assume CFF \mathcal{H} is perfectly known. Solve inverse problem?

$$\mathcal{H}^q(\xi, Q^2) = \int_{-1}^1 \frac{dx}{\xi} T^q \left(\frac{x}{\xi}, \frac{Q^2}{\mu^2}, \alpha_s(\mu^2) \right) H^q(x, \xi, \mu^2)$$

- Question raised about 20 years ago and has remained essentially open. Evolution proposed as a crucial element.

 Freund (2000)

- There exist **non-zero GPDs with vanishing forward limit** and **vanishing CFF up to order α_s^2** .
- The DVCS deconvolution problem is **ill-posed**.

 Bertone et al. (2021)

- Same conclusion holds** for several other hard exclusive processes. See H. Dutrieux's talk on Monday at 20:
- Define and implement** further criterions in fitting strategies to select one solution among infinitely many.

The PARTONS ecosystem



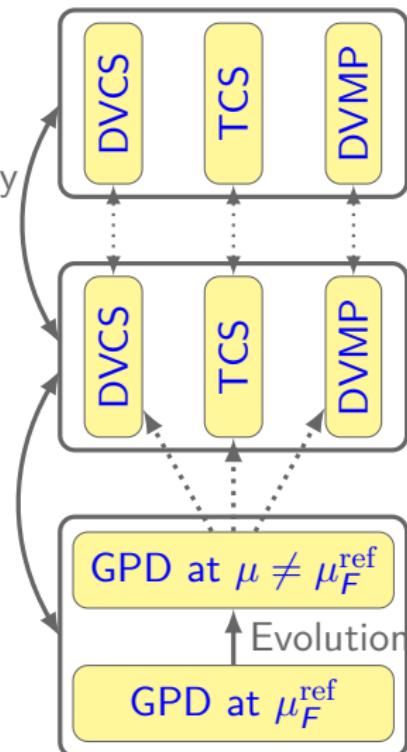
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Computing chain design.

Differential studies: physical models and numerical methods.

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- Full processes**
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- Computation of amplitudes
- Large distance**
- First principles and fundamental parameters



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- Perturbative approximations.
- Physical models.
- Fits.
- Numerical methods.
- Accuracy and speed.

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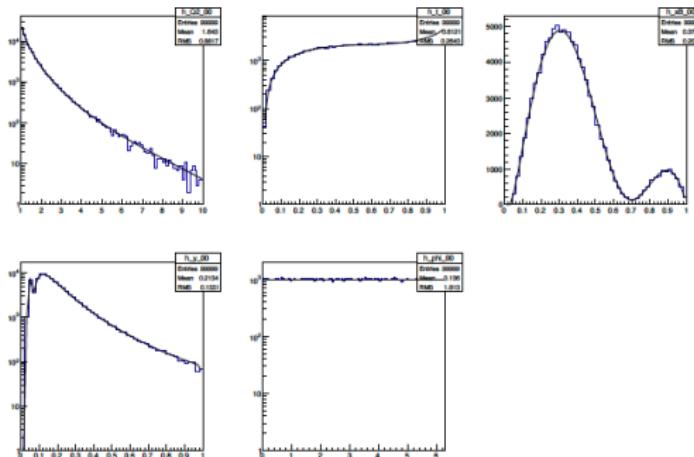
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EpIC – DVCS

Longitudinally polarized target, $E_e = 10 \text{ GeV}$, $E_p = 1 \text{ GeV}$



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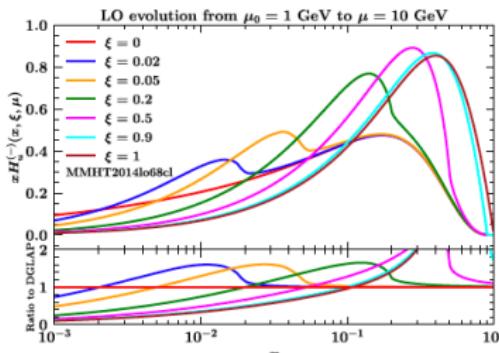
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Forward limit and DGLAP equations



- When $\kappa \rightarrow 0$, one recovers the forward DGLAP equations
 - Only the $\Theta(1-y)\mathcal{P}_1^{-(0)}(y; \kappa)$ term contributes to the evolution
 - No spurious singularity as $x < y < 1 < 1/\kappa$



- no ξ dependence in input
- Excellent agreement with native Apfel++ DGLAP evolution (red curve)
- Strong ξ dependence generated
- Continuity guaranteed at $x = \xi$ (cusp ?)

First validations

$x = \xi$ continuity, DGLAP limit and spurious divergences handling

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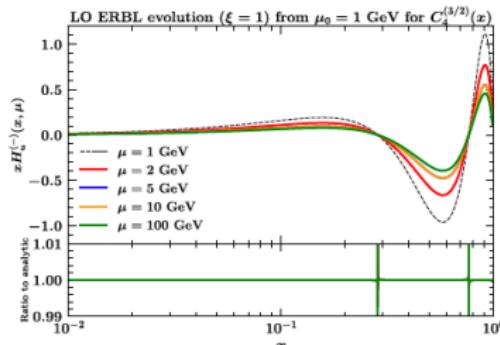
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ERBL Limit and Gegenbauer polynomials



- When $\kappa \rightarrow 1/x$ (i.e. $\xi \rightarrow 1$) one recovers the ERBL kernel
 - Eigen basis known $\rightarrow 3/2$ -Gegenbauer Polynomials
 - Direct (albeit restricted to $\xi = 1$) comparison between x-space and conformal space evolution



- $H(x, 1) \propto (1 - x^2) C_4^{(3/2)}(x)$
- $\frac{H(x, 1, \mu)}{H(x, 1, \mu_0)} = \left(\frac{\alpha_S(\mu)}{\alpha_S(\mu_0)} \right)^{\gamma_A/\beta_0}$
- Ratio is independent of x
- Excellent agreement between Apfel++ and conformal evolution in the ERBL limit

Additional validations

conformal evolution when $\xi \rightarrow 1$ guaranteeing the ERBL limit

Cédric Mezrag (Irfu-DPhN)

Apfel ++

May 31st, 2021

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Bertone et al., in progress

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- Concept **well-defined** and suitable for phenomenological analysis.
- Strong **first-principle connection** between concept and experimental data.
- The GPD deconvolution problem is **ill-posed**.
- Need for **multi-channel** analysis **beyond LO**.
- **Huge sensitivity** to numerical noise or experimental uncertainties.
- Benefiting from new inputs or constraints from **nonperturbative QCD** is highly desirable!
- Need for **coordinated effort** involving fits, computing chains e.g. PARTONS and continuum or lattice QCD to make the best from experimental data.

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ANN	artificial neural network
APFEL	a PDF evolution library
CFF	Compton form factor
DGLAP	Dokshitzer-Gribov-Lipatov-Altarelli-Parisi
DVCS	deeply virtual Compton scattering
DVMP	deeply virtual meson production
EIC	electron-ion collider
ERBL	Efremov-Radyushkin-Brodsky-Lepage
GFF	gravitational form factor
GPD	generalized parton distribution
LO	leading order
NLO	next-to-leading order
PDF	parton distribution function
TCS	timelike Compton scattering

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