

Accessing TMD fracture functions in back-to-back hadron production at CLAS12

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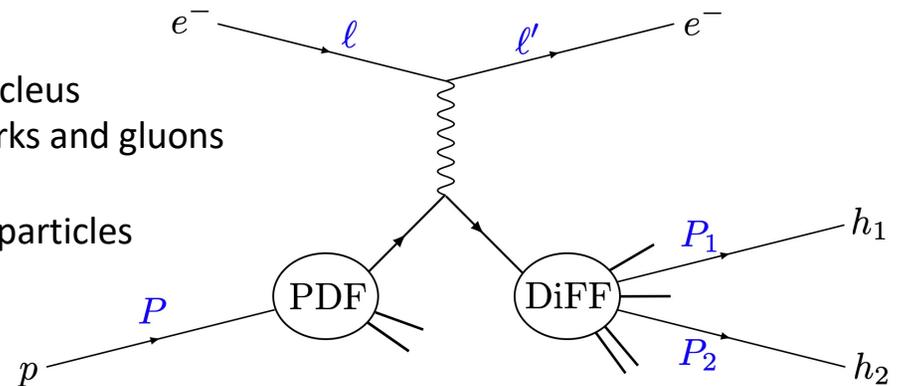
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Accessing 3D nucleonic structure

- Decades of study have led to detailed mappings of the momentum distribution of the nucleon in terms of 1-D parton distribution functions (PDFs).
- Theoretical advances have led to a framework in which information on the confined motion of the partons inside a nucleon are matched to 3-D transverse momentum dependent parton distribution functions (TMDs).

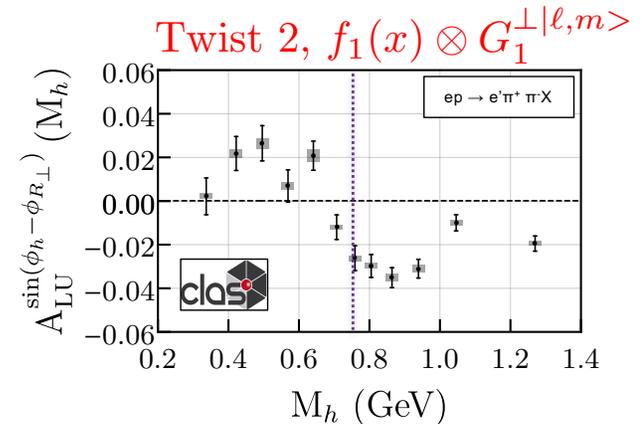
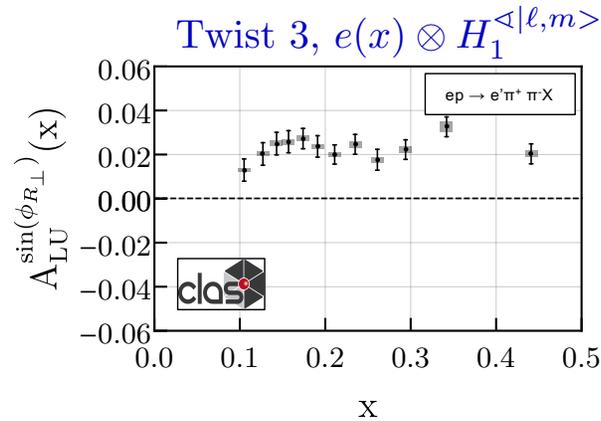
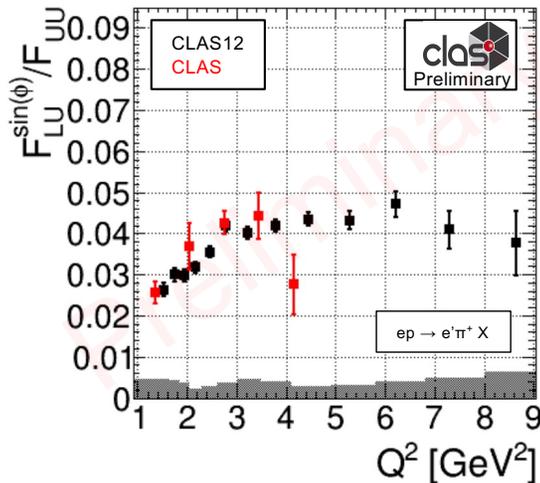
- TMDs/PDFs
 - Confined motion of quarks and gluons inside the nucleus
 - Orbital motion of quarks, correlations between quarks and gluons
- Fragmentation Functions
 - Probability for a quark to form particular final state particles
 - Insight into transverse momenta and polarization



TMD-sensitive CLAS12 Measurements

- CLAS12, with its high luminosity, wide acceptance and low Q^2 (for higher twist measurements) is an ideal place to study numerous physics observables which access these 3-D dependent quantities... Measurements traditionally focus on factorization theorems and assumption that hadrons are produced in current fragmentation.

$$F_{LU}^{\sin\phi_h} = \frac{2M}{Q} C \left[-\frac{\hat{h} \cdot k_T}{M_h} \left(x e H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{h} \cdot p_T}{M} \left(x g^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{E}}{z} \right) \right]$$



T. B. Hayward, C. Dilks, A. Vossen, H. Avakian et al., *Phys. Rev. Lett.*, 126, 152501, (2021), hep:ex/2101.04842

S. Diehl, A. Kim, G. Angelini, K. Joo et al., (2021) hep:ex/2101.03544.

Fracture Functions

- Information on the momentum distribution of quarks and gluons are encoded in TMDs that can be measured in inclusive processes such as SIDIS.
- TMDs have been extensively studied via azimuthal modulations of a final state hadron generated in the fragmentation of a struck quark (CFR).
- Final state hadrons can also form from the left-over target remnant (TFR) whose partonic structure is defined by “fracture functions”: the probability to form a certain hadron given a particular ejected quark.

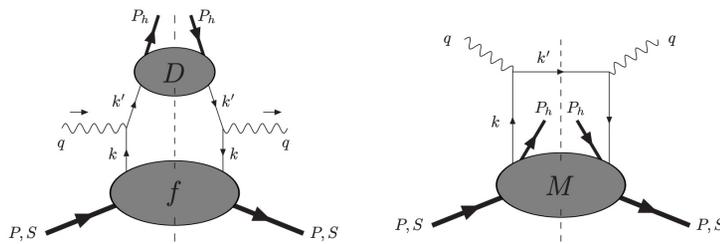


Figure 1: The handbag diagram for the SIDIS hadronic tensor in the current fragmentation region (left) and in the target fragmentation region (right).

Phys. Lett. B. 699 (2011), 108-118, [hep-ph] 1102.4214

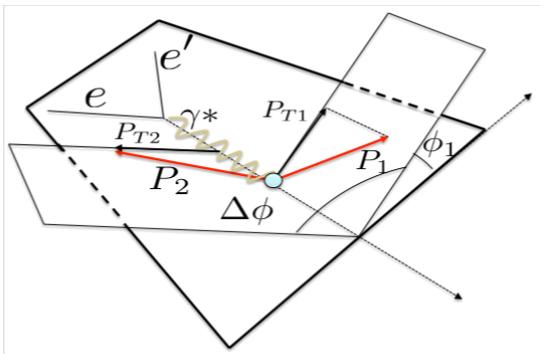
	U	L	T
U	\hat{u}_1	$\hat{l}_1^{\perp h}$	$\hat{t}_1^h, \hat{t}_1^{\perp}$
L	$\hat{u}_{1L}^{\perp h}$	\hat{l}_{1L}	$\hat{t}_{1L}^h, \hat{t}_{1L}^{\perp}$
T	$\hat{u}_{1T}^h, \hat{u}_{1T}^{\perp}$	$\hat{l}_{1T}^h, \hat{l}_{1T}^{\perp}$	$\hat{t}_{1T}, \hat{t}_{1T}^{hh}, \hat{t}_{1T}^{\perp\perp}, \hat{t}_{1T}^{\perp h}$

Back-to-back Formalism

$$\mathcal{F}_{LU}^{\sin(\phi_1 - \phi_2)} = \frac{|\mathbf{P}_{1\perp}| |\mathbf{P}_{2\perp}|}{m_N m_2} c \left[w_5 \hat{l}_1^{\perp h} D_1 \right],$$

$$\mathcal{A}_{LU} = - \frac{y \left(1 - \frac{y}{2}\right)}{\left(1 - y + \frac{y^2}{2}\right)} \frac{\mathcal{F}_{LU}^{\sin \Delta\phi}}{\mathcal{F}_{UU}} \sin \Delta\phi$$

Phys. Lett. B. 713 (2012), 317-320, [hep-ph] 1112.2604



- When two hadrons are produced “back-to-back” with one in the CFR and one in the TFR the structure function contains a convolution of a **fracture function** and a **fragmentation function**.

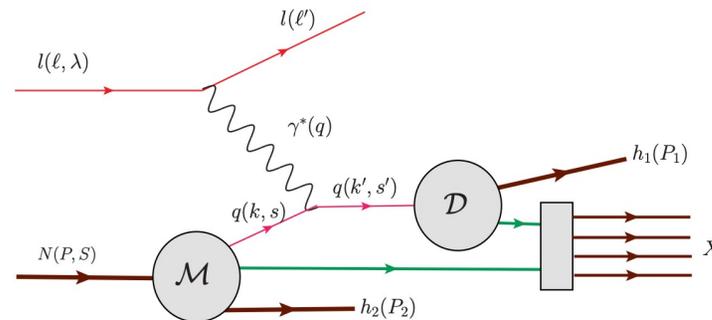


Figure 1: Lepto-production of two hadrons, one in the CFR and one in the TFR.

Phys. Lett. B. 706 (2011), 46-52, [hep-ph] 1109.1132

Additional Modulations

$$\mathcal{F}_{LU} = \frac{|p_\perp^\perp| |p_P^\perp|}{m_p m_\pi} \mathcal{C} \left[w_5 \hat{l}_1^{\perp h} D_1 \right] \longrightarrow$$

Phys. Lett. B. 713 (2012), 317-320, [hep-ph] 1112.2604

Structure functions carry a dependence on $|p_\perp^\perp| |p_P^\perp|$ which introduces a dependence on $\cos \Delta\phi$.

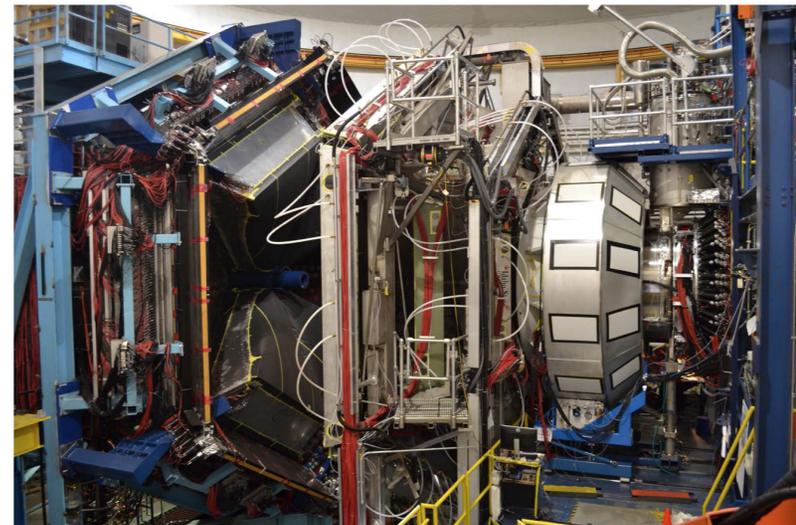
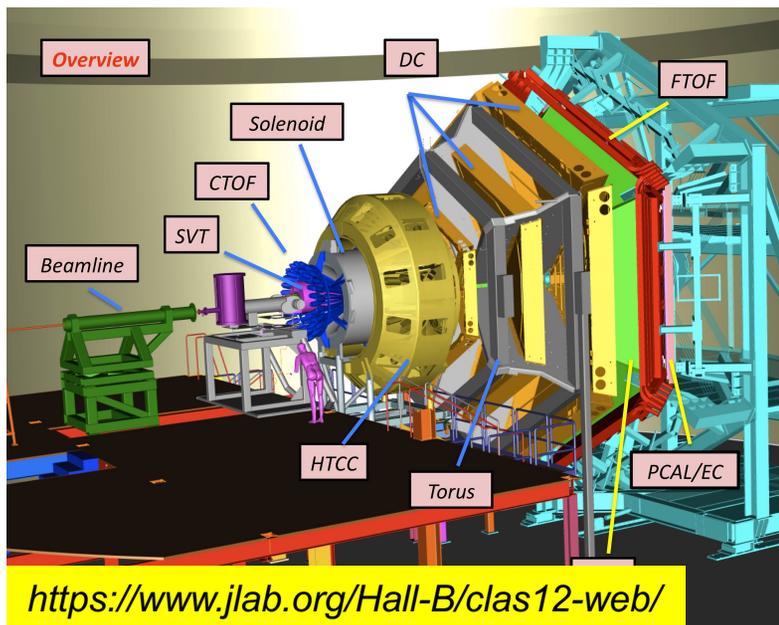
If the correlations are assumed small, the fracture functions can be expanded in powers of $k^\perp \cdot p_P^\perp$.

$$\begin{aligned} \hat{l}_1^{\perp h}(x, \zeta, \mathbf{k}^{\perp 2}, \mathbf{p}_P^{\perp 2}, \mathbf{k}^\perp \cdot \mathbf{p}_P^\perp) \\ \approx a(x, \zeta, \mathbf{k}^{\perp 2}, \mathbf{p}_P^{\perp 2}) \\ + b(x, \zeta, \mathbf{k}^{\perp 2}, \mathbf{p}_P^{\perp 2}) \mathbf{k}^\perp \cdot \mathbf{p}_P^\perp \end{aligned}$$

The term linear in $k^\perp \cdot p_P^\perp$ yields a $\cos \Delta\phi$ which when combined with the already existing $\sin \Delta\phi$ term results in a $\sin 2\Delta\phi$.

$$\mathcal{A}_{LU}(x, \zeta, \mathbf{k}^{\perp 2}, \mathbf{p}_P^{\perp 2}, \Delta\phi) = A(x, \zeta, \mathbf{k}^{\perp 2}, \mathbf{p}_P^{\perp 2}) \sin \Delta\phi + B(x, \zeta, \mathbf{k}^{\perp 2}, \mathbf{p}_P^{\perp 2}) \sin(2\Delta\phi)$$

CLAS12 Experimental Setup



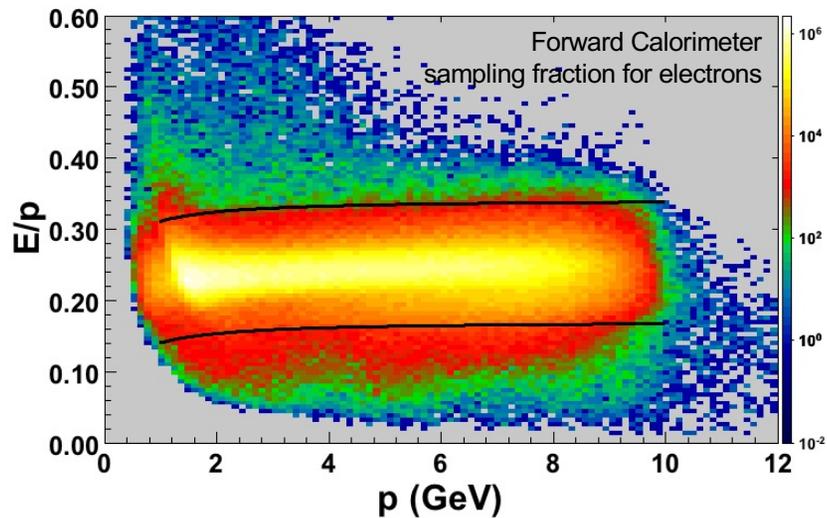
V. Burkert et al., Nucl. Instrum. Meth. A 959 (2020) 163419

- Data taken during Fall 2018 and Spring 2019.
- 10.6 (2018) and 10.2 (2019) GeV longitudinally polarized electron beam with a H₂ target.
- Analyzed data is a small percentage of the total available data.

Particle ID

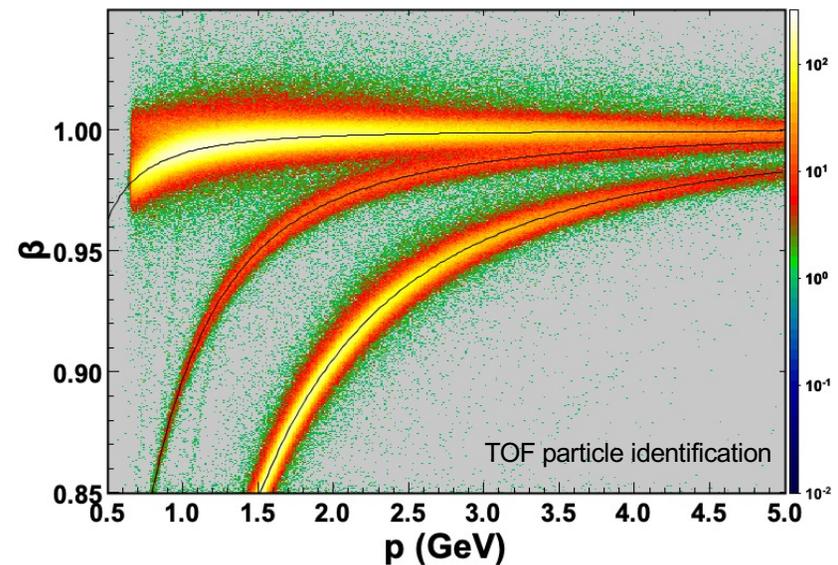
- Electron

- Electromagnetic calorimeter.
- Cherenkov detector.
- Vertex and fiducial cuts.



- Hadron

- β vs p comparison between vertex timing and event start time.
- Vertex and fiducial cuts.



Selecting “back-to-back” events

- Formalism requires one hadron in the CFR and one hadron in the TFR.
- A natural choice for a first analysis are events with a pion (CFR biased) and proton (TFR biased).

PLOTS REMOVED ONLINE (DISTRIBUTIONS OF M_X AND X_F OF PROTON AND PION)

Monte Carlo

- SIDIS MC “clasdis”¹ based on PEPSI² generator, the polarized version of the well-known LEPTO³ generator.
- Parameters changed to reproduce observed distributions include average transverse momentum, fraction of spin-1 light mesons and fraction of spin-1 strange mesons.
- CLAS12 detector system described in “GEMC”⁴, a detailed GEANT4 simulation package.
- Excellent agreement between data and MC!

PLOTS REMOVED ONLINE (Data/MC Comparisons of Q^2 , P^\perp , X_F of pion and $\Delta\phi$)

1. H. Avakian, “clasdis.” <https://github.com/JeffersonLab/clasdis>, 2020.
2. L. Mankiewicz, A. Schäfer, and M. Veltri, “Pepsi: A monte carlo generator for polarized leptonproduction,” *Comput. Phys. Commun.*, vol. 71, pp. 305–318, 1992.
3. G. Ingelman, A. Edin, and J. Rathsman, “LEPTO 6.5: A Monte Carlo generator for deep inelastic 912 lepton - nucleon scattering,” *Comput. Phys. Commun.*, vol. 101, pp. 108–134, 1997.
4. M. Ungaro et al., “The CLAS12 Geant4 simulation,” *Nucl. Instrum. Meth. A*, vol. 959, p. 163422, 2020.

Extracting A_{LU}

- Select $ep \rightarrow e'P \pi^+ + X$.
- Consider all possible hadron pairs.
- Amplitudes are extracted simultaneously via maximizing a likelihood function.
- Unbinned maximum likelihood method:

$$\frac{N_{\pm}(\Delta\phi)}{N(\Delta\phi)} = \frac{1}{2} \frac{L_{\pm} a_{\pm}(\Delta\phi) \eta_{\pm}(\Delta\phi)}{L a(\Delta\phi) \eta(\Delta\phi)} [1 \pm P A_{LU}(\Delta\phi)]$$

- Use MINUIT to minimize the -log likelihood.
- Include relevant beam polarization (~85% at JLab).

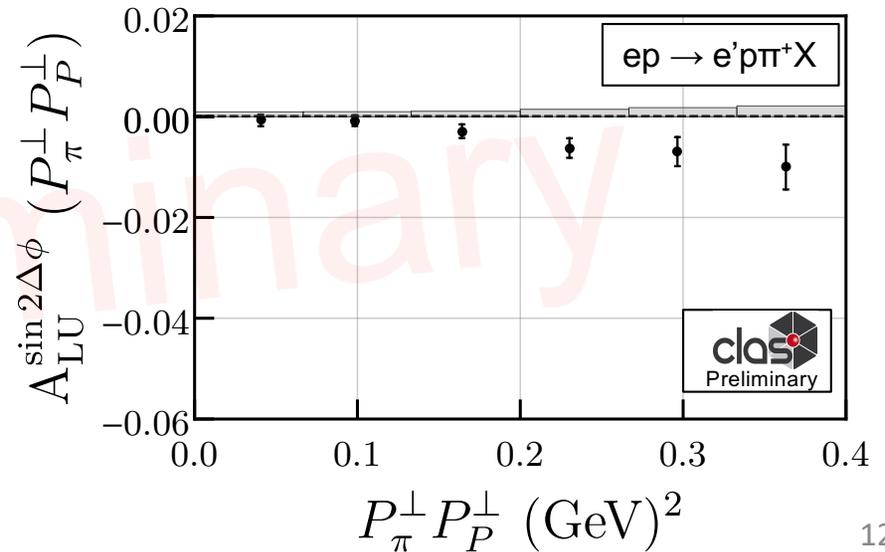
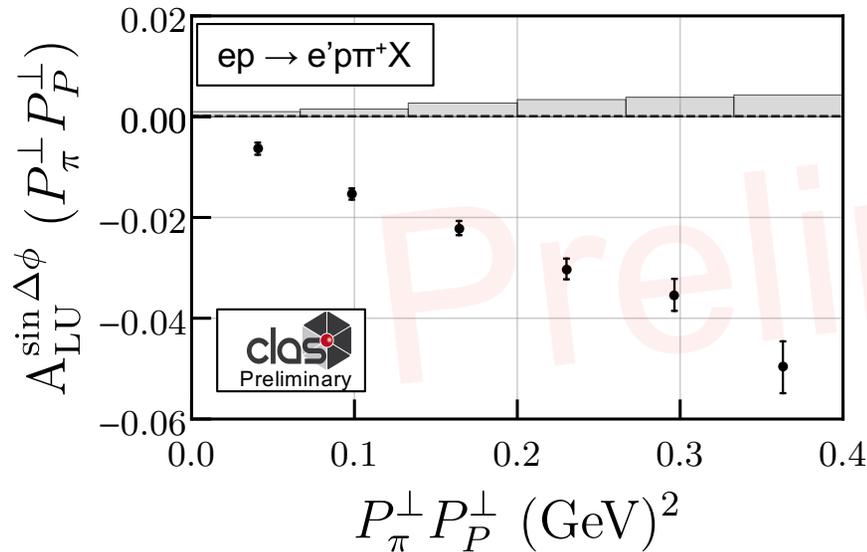
Channel selection

- $Q^2 > 1.0 \text{ GeV}^2$
- $W > 2.0 \text{ GeV}$
- $M_{\text{miss}} > 0.85 \text{ GeV}$
- $y < 0.75$
- $x_{F\pi} > 0$
- $x_{FP} < 0$
- $z_{\pi} > 0.2$

Back-to-back results

- Observed linear dependence on the product of transverse momenta is consistent with expectations.
- Non-zero asymmetries are the first experimental observation of possible spin-orbit correlations between hadrons produced simultaneously in the CFR and TFR.

$$\mathcal{F}_{LU} = \frac{|p_{\pi^+}^\perp| |p_P^\perp|}{m_p m_\pi} \mathcal{C} \left[w_5 \hat{l}_1^\perp h D_1 \right]$$

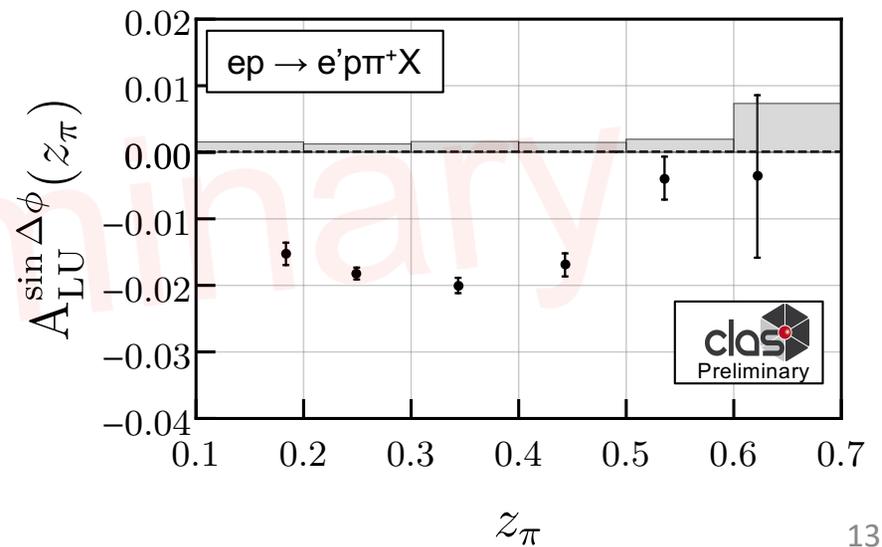
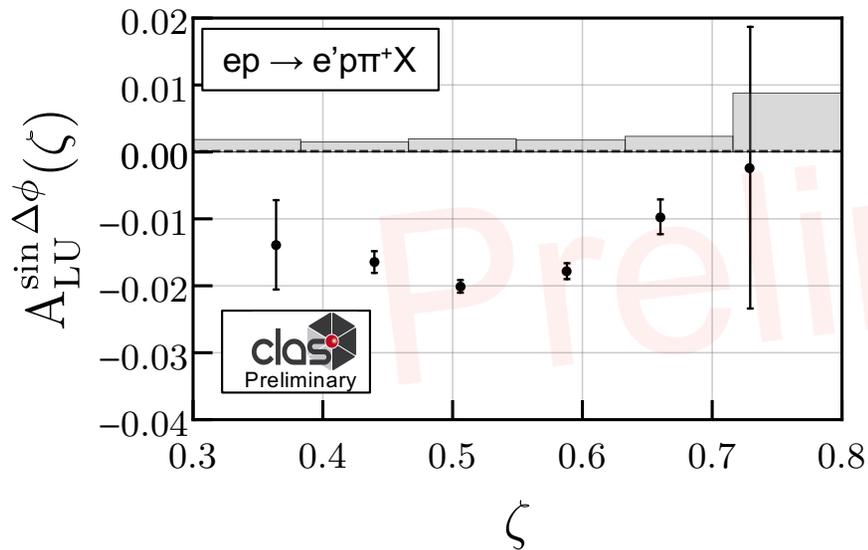


Access to unmeasured fracture function

- Fracture function $\hat{l}_1^{\perp h}$ depends on ζ .
- Fragmentation function D_1 depends on z_π .

$$\mathcal{F}_{LU}^{\sin(\Delta\phi)} = \frac{|p_{\pi^+}^\perp| |p_P^\perp|}{m_P m_{\pi^+}} \mathcal{C} \left[w_5 \hat{l}_1^{\perp h} D_1 \right]$$

$$\zeta = E_P/E \quad z_\pi = E_\pi/\nu$$



Conclusions

- Significant single-spin asymmetries have been observed **for the first time** in back-to-back proton-pion electroproduction.
- Beam-spin asymmetries amplitudes indicate that spin-orbit correlations may exist between hadrons produced simultaneously in the target and current fragmentation regions.
- Analysis in final collaboration review with the aim of submission for publication this year.