

第16回 高エネルギーQCD・核子構造 勉強会

日時: 2020年2月19日(水)

場所: 東北大学 理学合同AB棟721棟

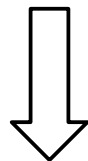


レプトン散乱実験による 一般化パートン分布研究

宮地 義之 (山形大学)

世話人からのリクエスト

*“Transverse extension of partons in the proton probed in the sea-quark range by measuring the DVCS cross section”,
COMPASS, PLB793(2019)188*



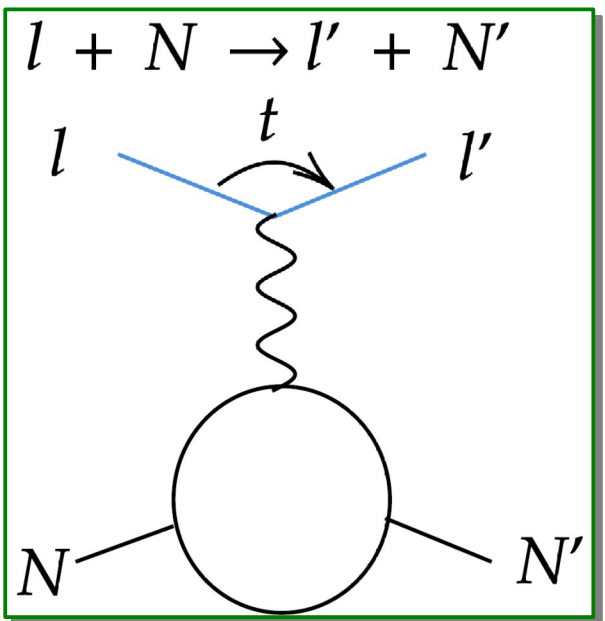
*“Experiments on generalized parton distributions”,
Progress on QCD and nucleon structure in 2019
02/28 – 03/01 in 2019 @ KEK*

をベースに、更新

- Proton Structure and **Generalized Parton Distribution**
 - Total angular momentum of quarks
- Hard Exclusive Production and **GPD**
 - **Deeply Virtual Compton Scattering (DVCS)**
 - Hard Exclusive Meson Production (HEMP)
- Experiments on GPDs
 - Focusing on DVCS measurements
- Summary and Outlook

How to study “Structure of the proton”

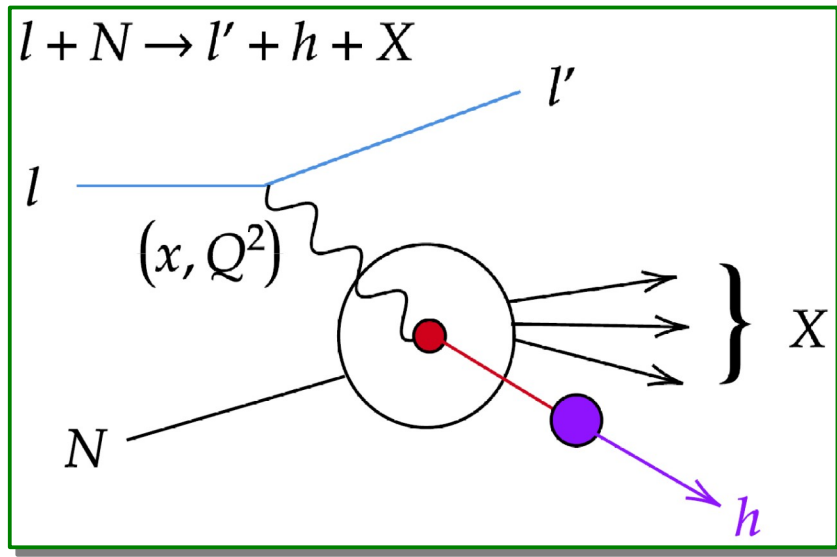
Elastic scattering



Form factors
→ spatial distribution

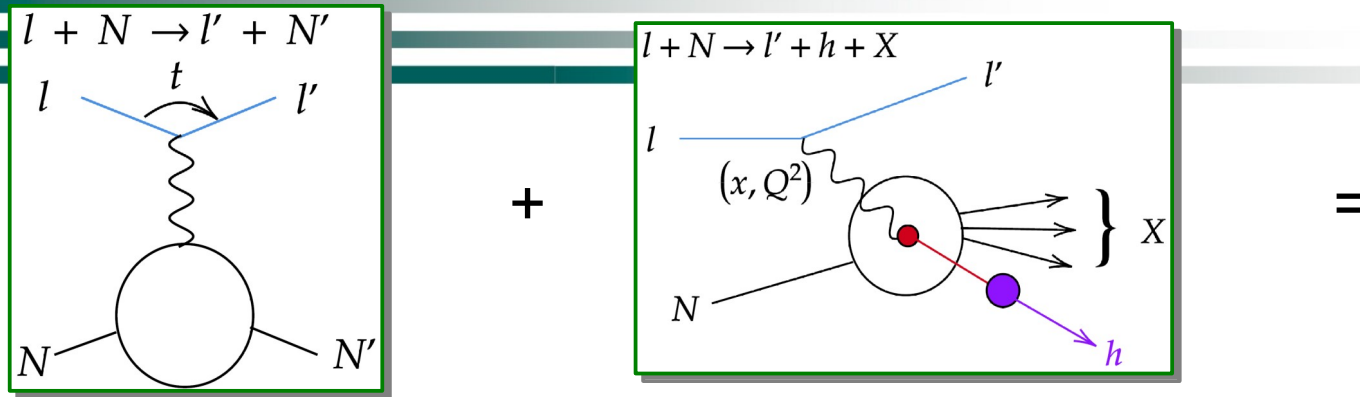
$$\langle r^2 \rangle = -6 \frac{dF(\vec{q})}{dq^2} \Big|_{q^2 \rightarrow 0}$$

Deep Inelastic Scattering

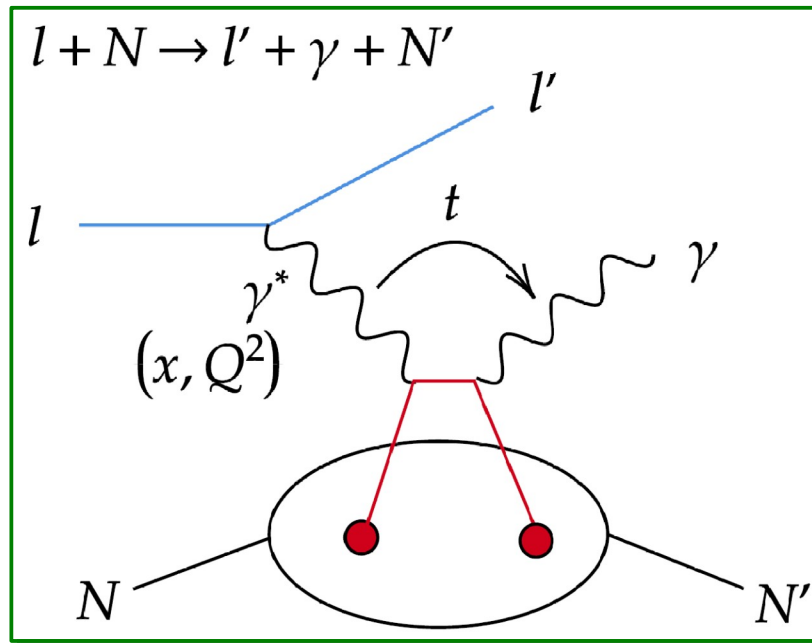


Parton distributions
→ momentum distribution

Proton Structure and Generalized Parton Distributions

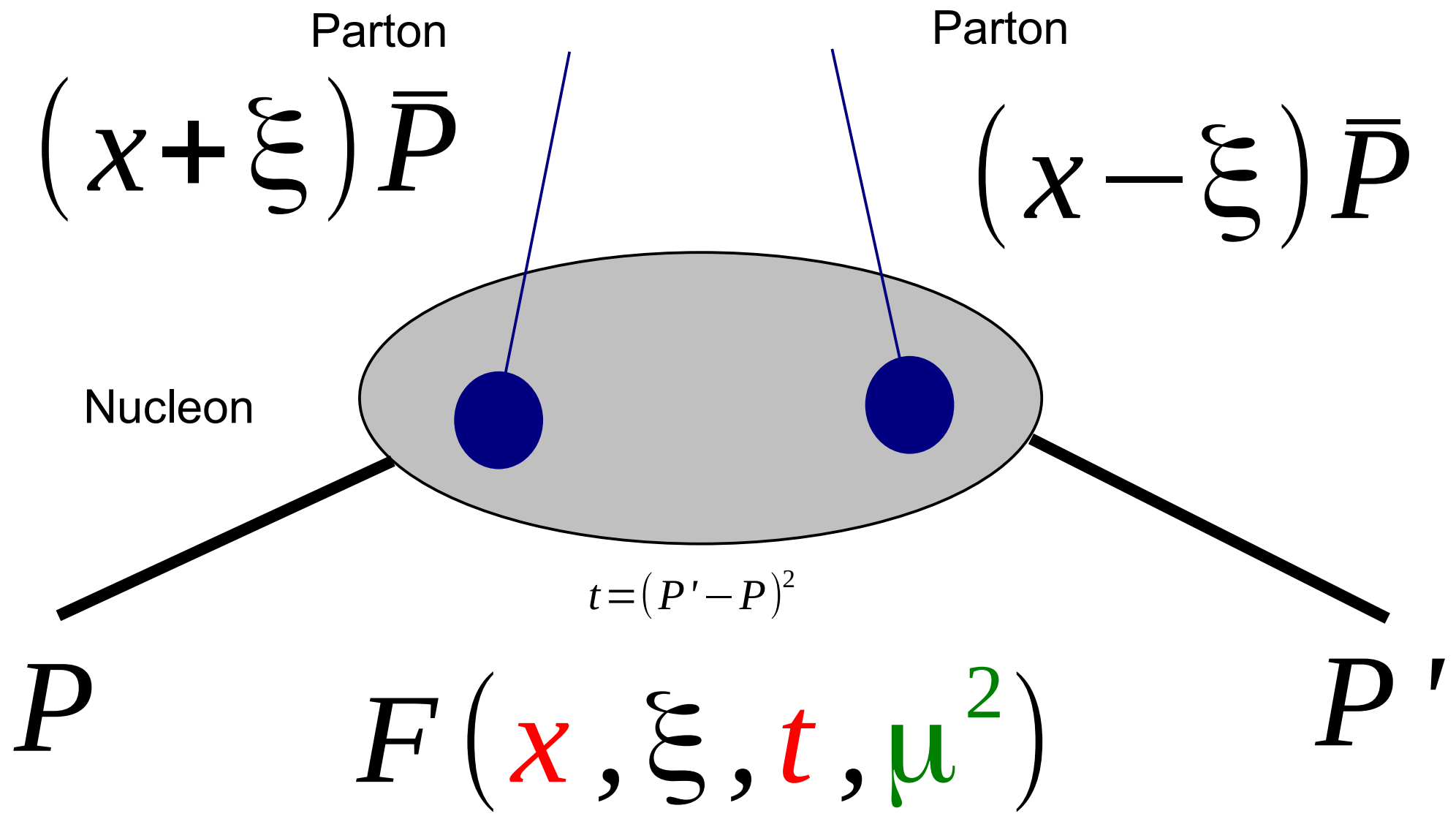


“*virtual photon elastic scattering*”



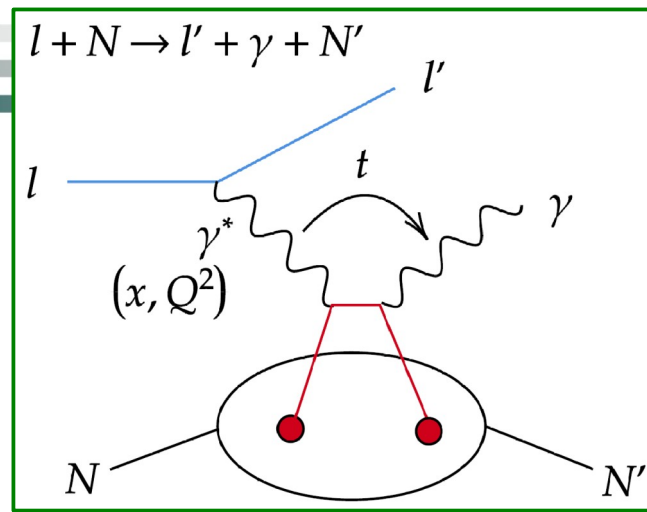
- Virtual photon probes a quark
- Momentum transfer
spatial distribution of quarks

Generalized Parton Distribution

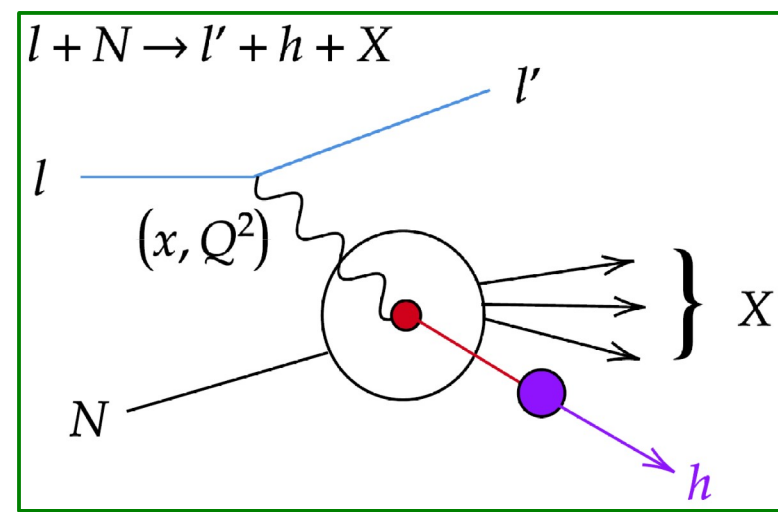
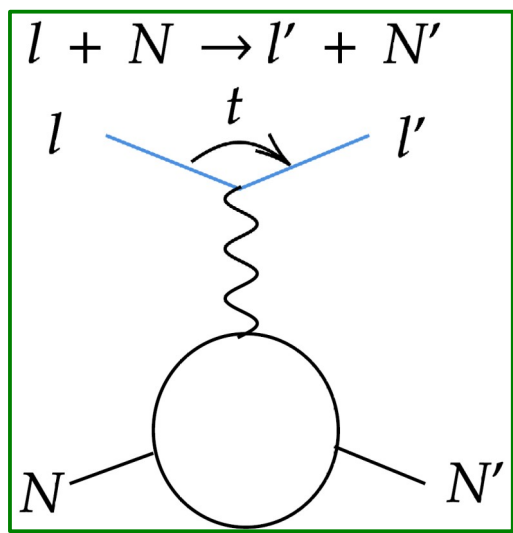


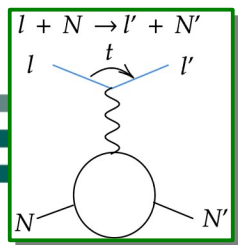
GPDs, Form Factors, PDFs

$\int dx$



$t \rightarrow 0$





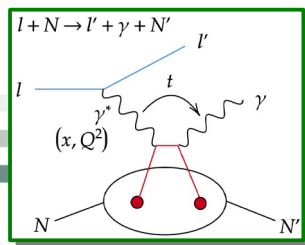
Form Factor

$$F_1(t)$$

$$F_2(t)$$

$$G_A(t)$$

$$G_p(t)$$



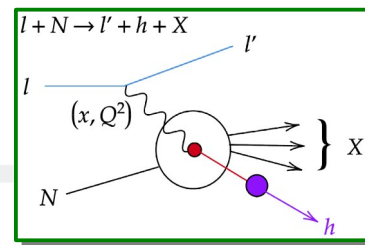
GPD

$$H(x, \xi, t)$$

$$E(x, \xi, t)$$

$$\tilde{H}(x, \xi, t)$$

$$\tilde{E}(x, \xi, t)$$



PDF

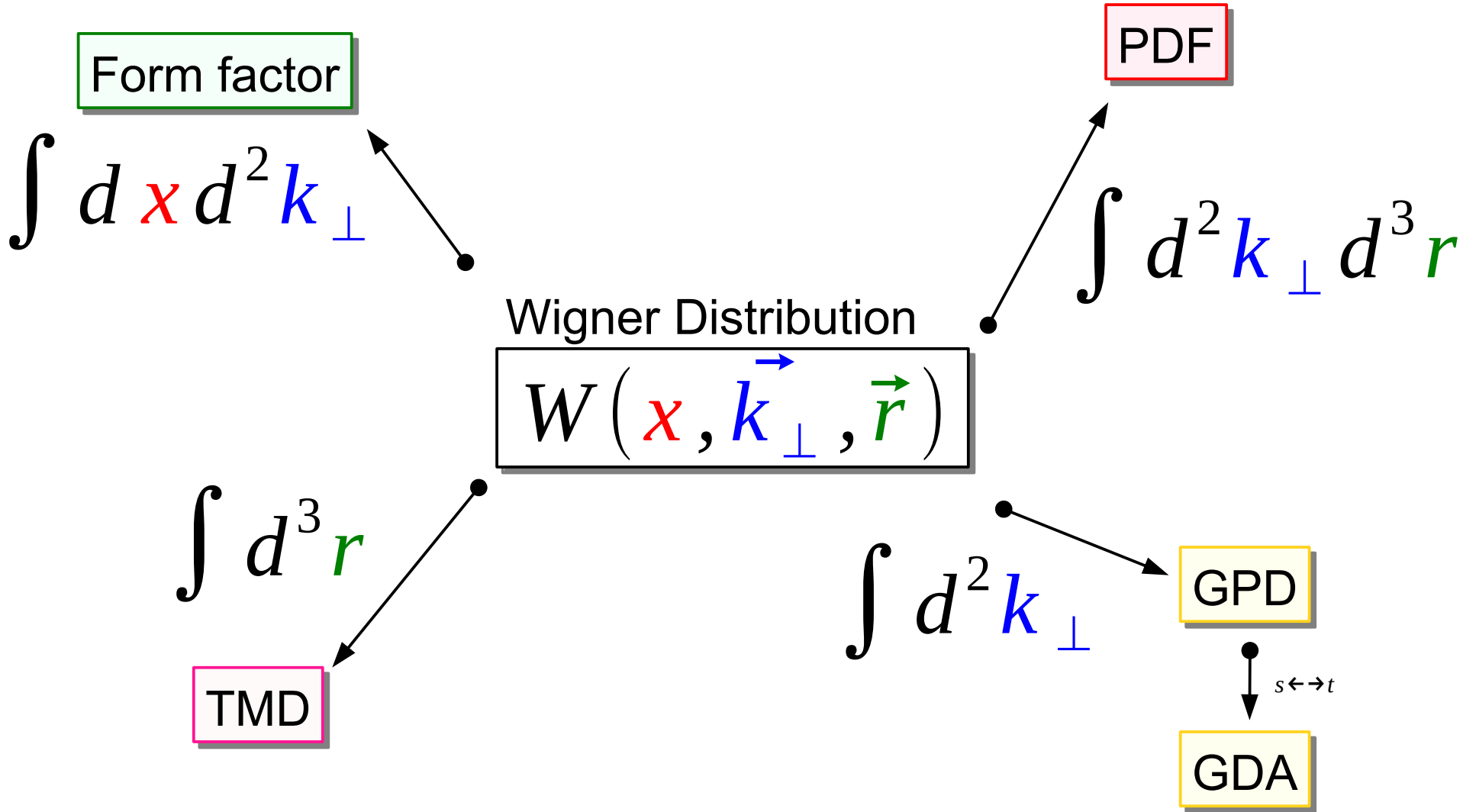
$$f_1 \quad q(x)$$

$$f_{1T}^\perp$$

$$g_1 \quad \Delta q(x)$$

$$g_{1T}$$

Mother distribution of the proton



Total angular momentum of quarks

$$J_N = \underbrace{\sum_{q=u,d,s,c,\dots} \left(\frac{1}{2} \Delta\Sigma_q + L_q \right)} + J_g$$

X.-D. Ji, PRL78(1997)610

$$J_q = \frac{1}{2} \int dx x [H_q(x, 0, 0) + E_q(x, 0, 0)]$$

X.-D. Ji, PRD55(1997)7114

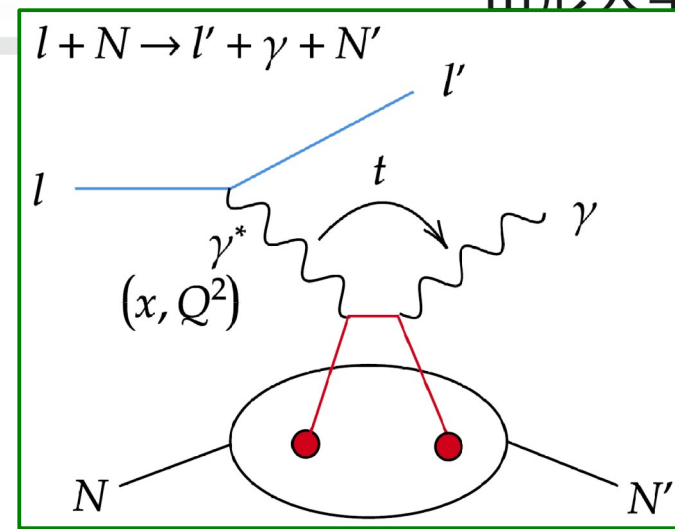


Hard Exclusive Production and GPDs

Deeply Virtual Compton Scattering (DVCS):

$$e + N \rightarrow e' + N' + \gamma$$

Involved GPDs: $H, E, \tilde{H}, \tilde{E}$
clean reaction



Hard Exclusive Meson Production (HEMP)

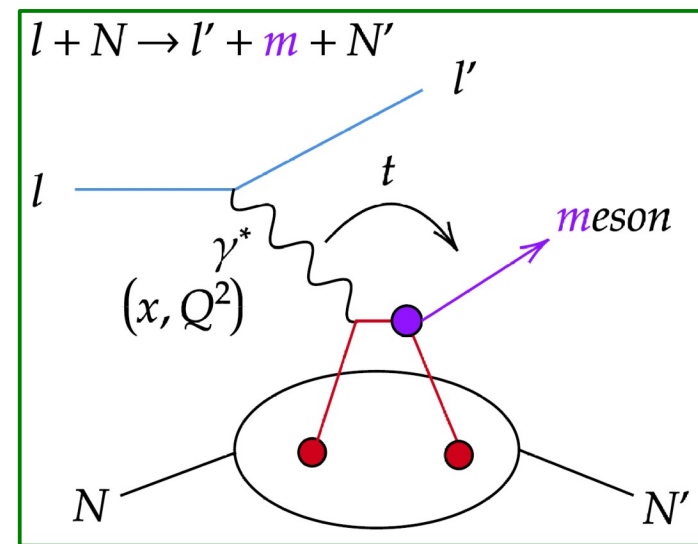
Deeply Virtual Meson Production (DVMP):

$$e + N \rightarrow e' + N' + \{\rho, \pi, \dots\}$$

vector meson: H, E
pseudo-scalar meson: \tilde{H}, \tilde{E}

Quark flavor sensitivity

Meson amplitude involved



Chiral-odd GPDs

DVCS

Chiral-even GPDs

$$H, E, \tilde{H}, \tilde{E}$$

HEMP

Chiral-odd GPDs

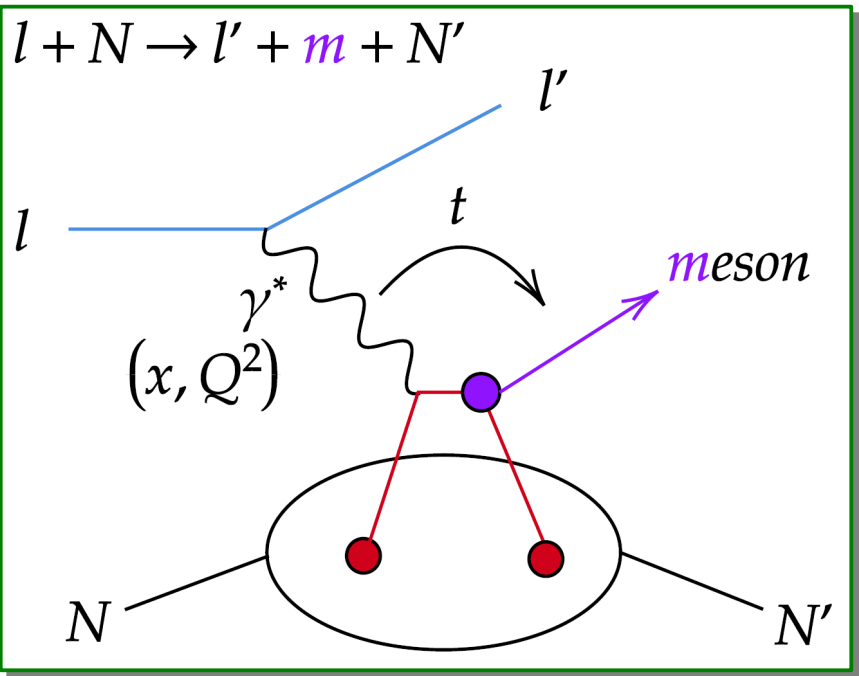
$$H_T, E_T, \tilde{H}_T, \tilde{E}_T$$

$$H_T \longleftrightarrow h_1$$

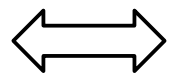
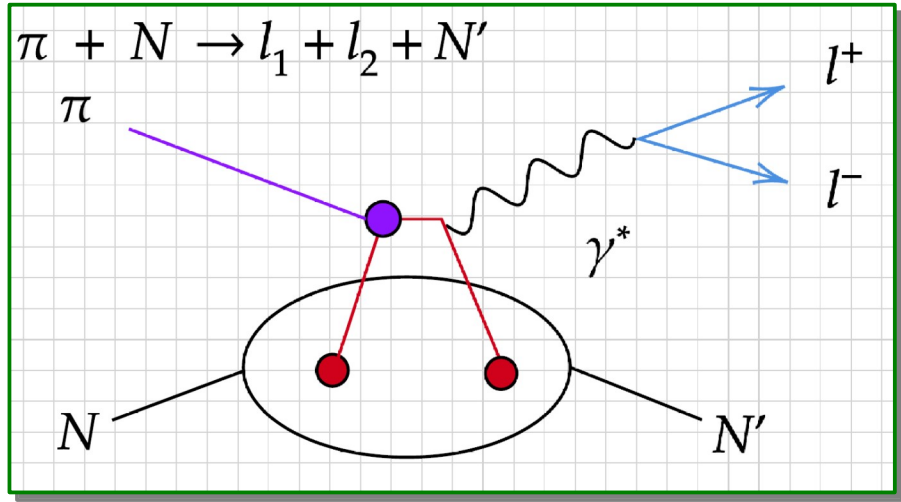
$$2H_T + E_T \longleftrightarrow h_1^\perp$$

Exclusive Process and GPDs

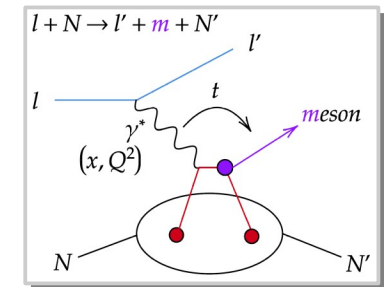
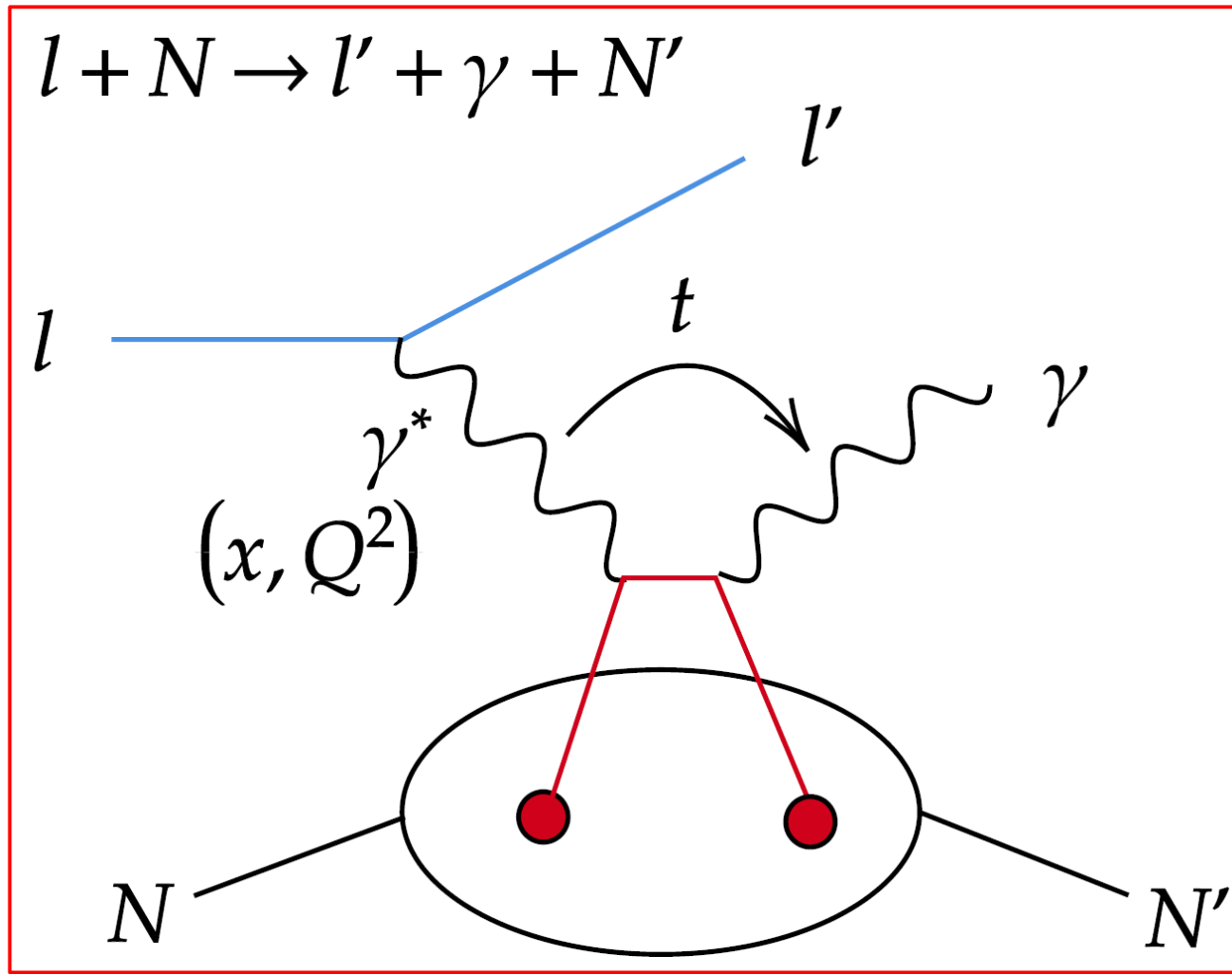
Hard Exclusive Meson Production



Exclusive Drell-Yan Process



Experiments on Deeply Virtual Compton Scattering



Experiments on DVCS

H1, ZEUS σ

COMPASS II

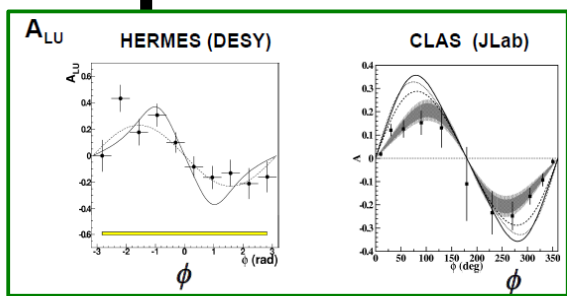
160 GeV μ ,
 σ , **BSA+BCA**

HERMES

26.7 GeV electron, H, D, A
 σ , **BSA**, **BCA**, **TSA(L+T)**

JLab

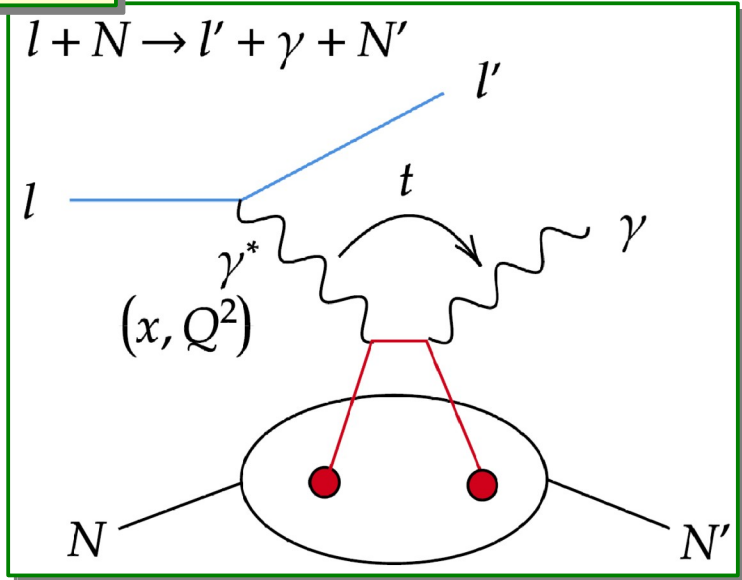
Electron (4 GeV \rightarrow 6 GeV \rightarrow 12 GeV)
 σ , **BSA**



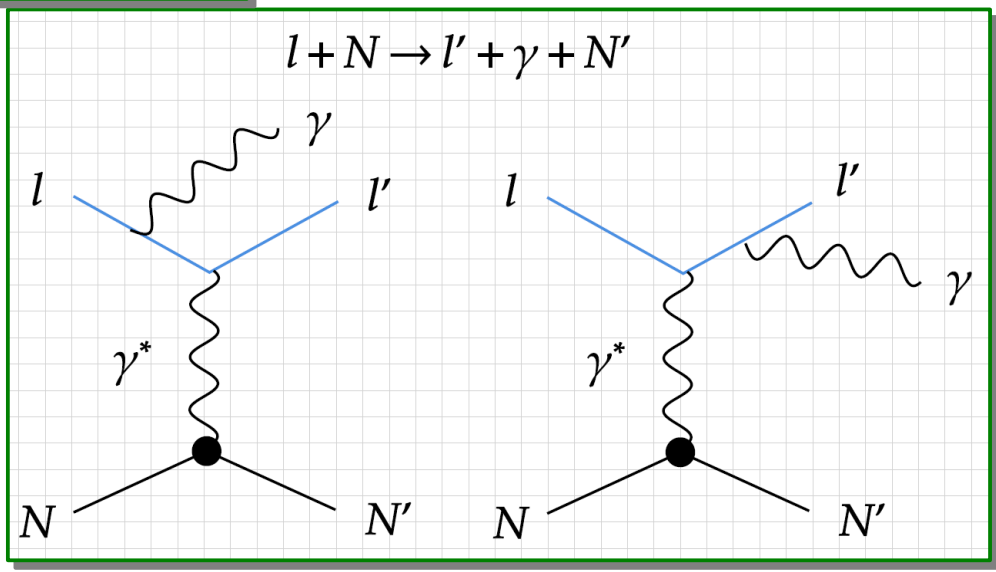
PRL87(2001)

DVCS vs Bethe-Heitler

DVCS



Bethe-Heitler



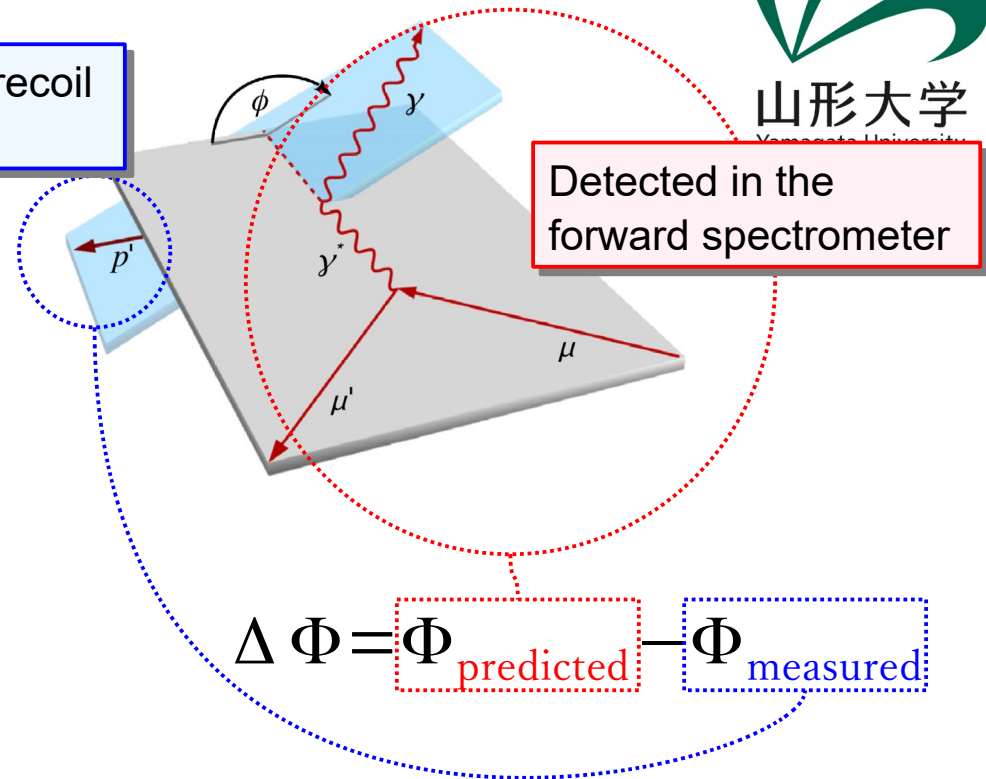
$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi} = \frac{x_B e^6}{32(2\pi)^4 Q^4 \sqrt{1 + \epsilon^2}} |\mathcal{T}_{ep \rightarrow ep\gamma}|^2,$$

$$|\mathcal{T}_{ep \rightarrow ep\gamma}|^2 = |\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2 + \mathcal{I},$$

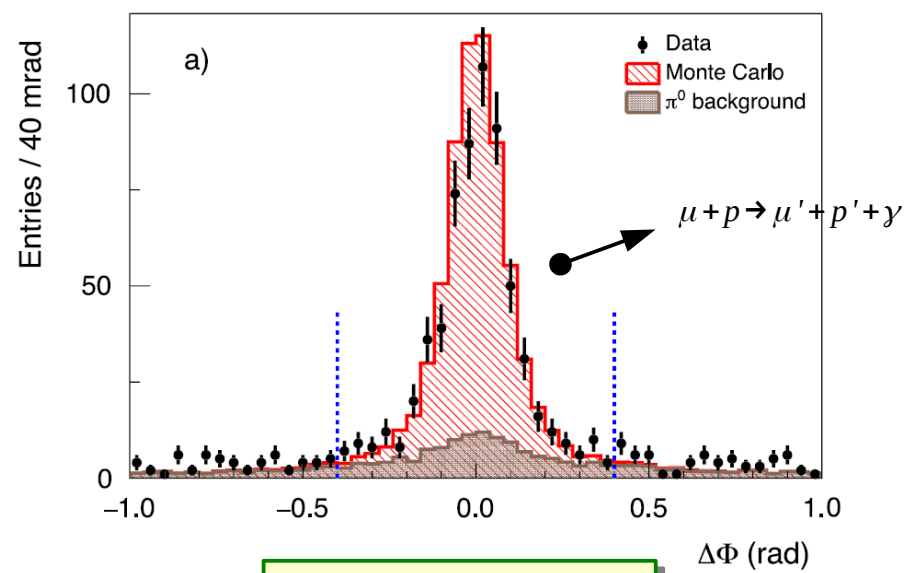
DVCS @ COMPASS II



Detected in the recoil detector

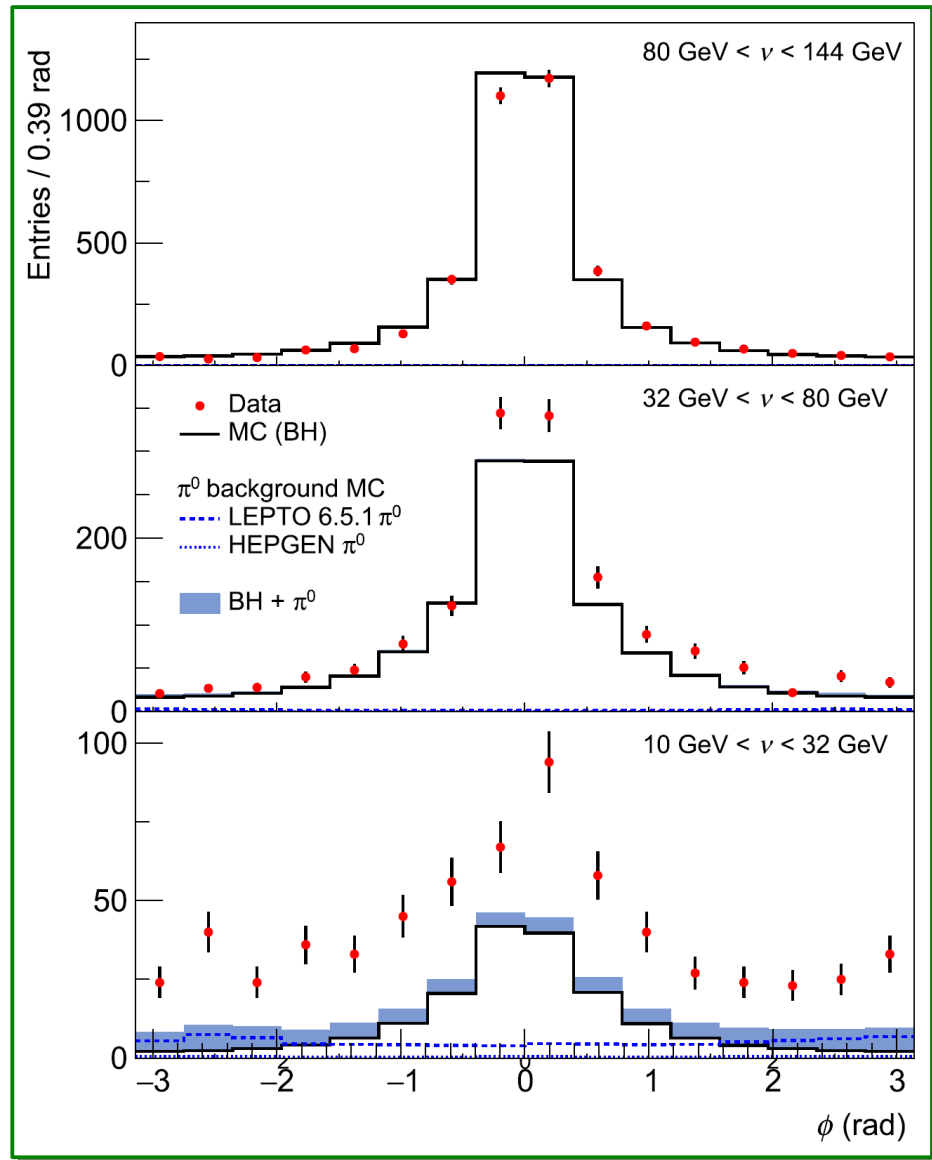


- Liq. H target + Recoil proton detector
- Pol. Muon @ 190 GeV
- Data taking: 2009 (test), 2012 (pilot), 2016-17
 - Results from 2012 data are available.
- Event selection
 - Incoming muon (μ)
 - single outgoing charged particle (μ')
 - One neutral cluster in ECAL (γ)
 - Recoil particle $\Delta\Phi \sim 0$ and $\Delta p_T \sim 0$



PLB793(219)188

DVCS @ COMPASS II



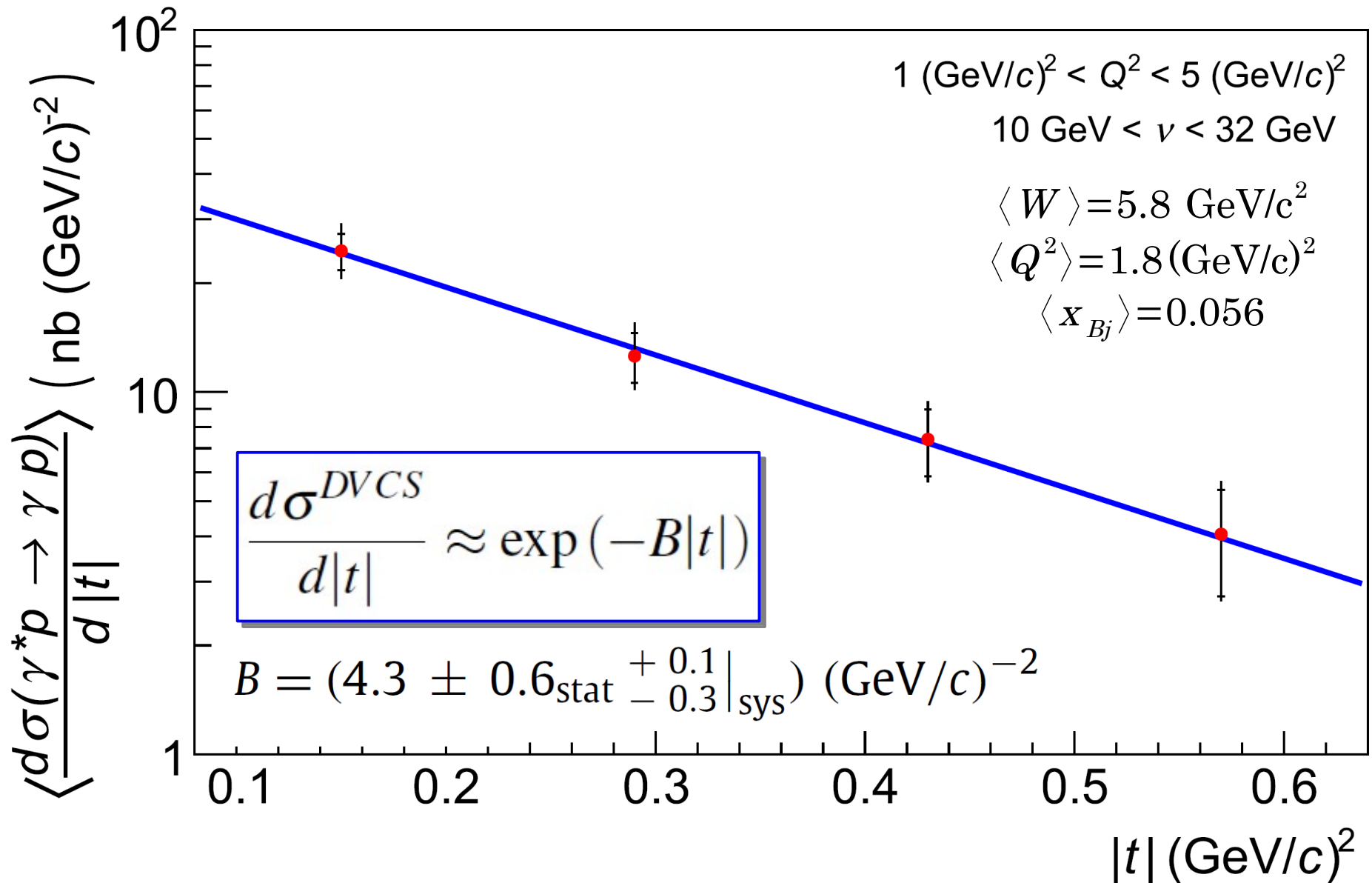
$$1 \text{ (GeV/c)}^2 < Q^2 < 5 \text{ (GeV/c)}^2$$

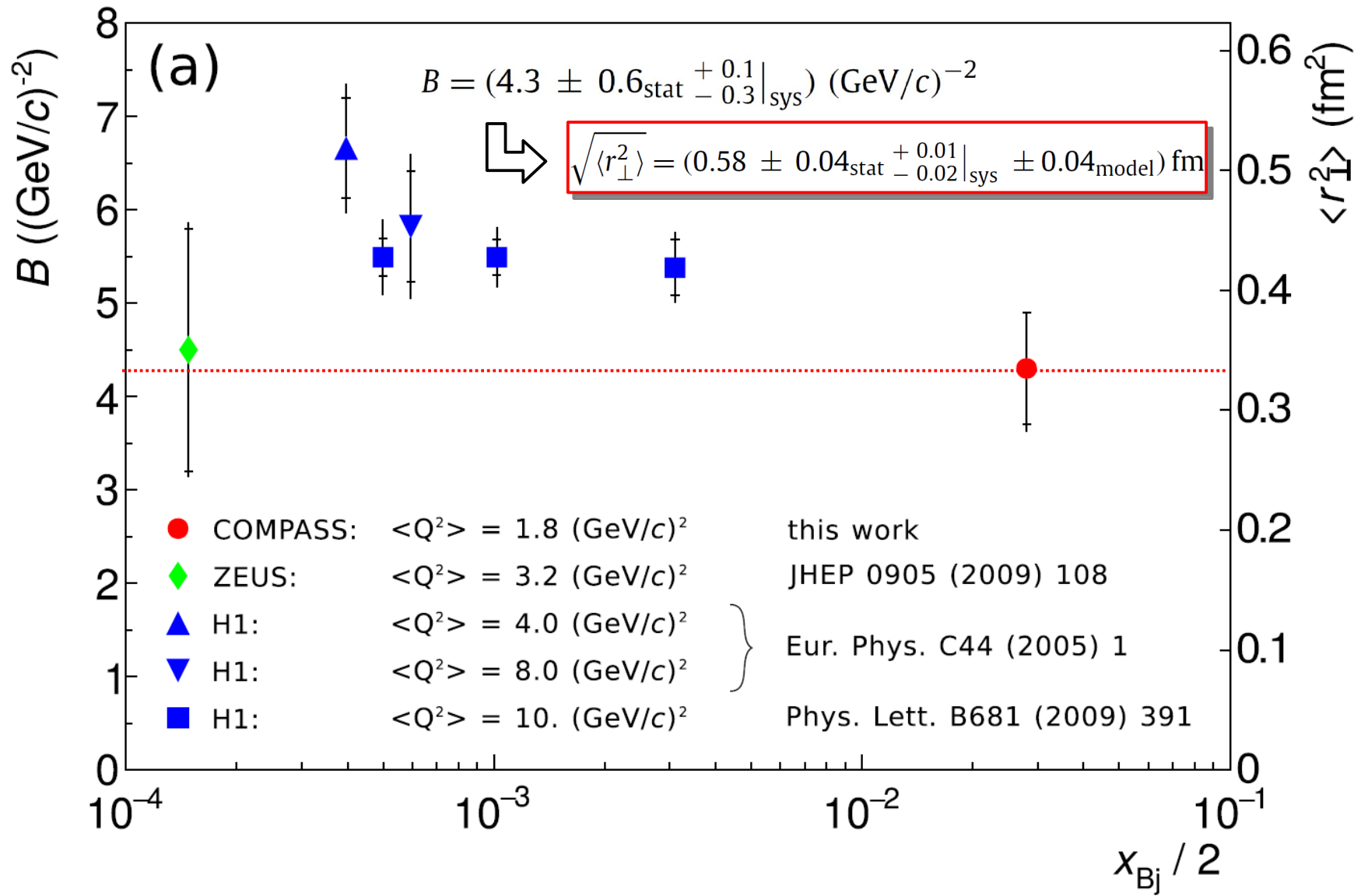
$$0.08 \text{ (GeV/c)}^2 < |t| < 0.64 \text{ (GeV/c)}^2$$

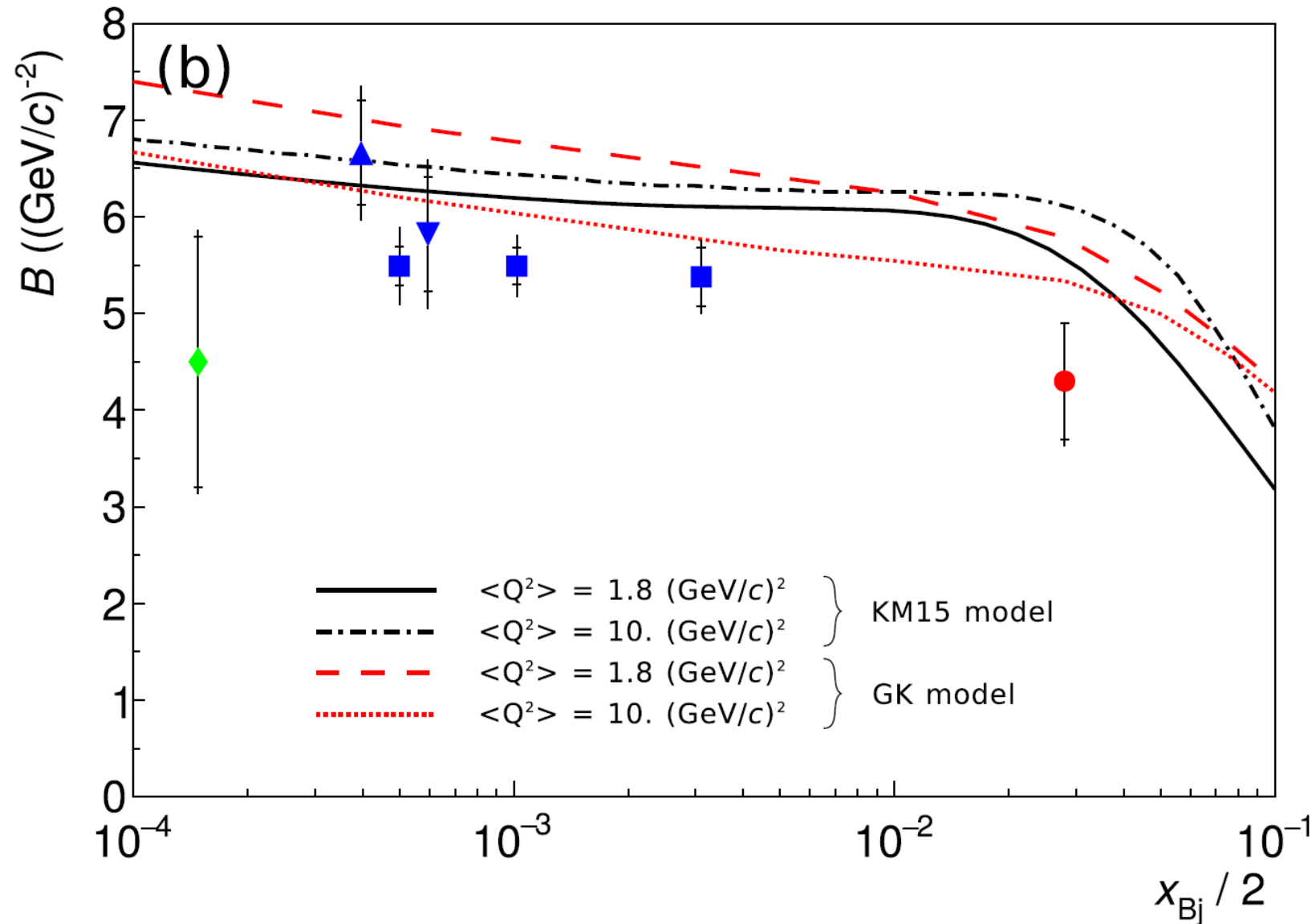
BH Monte Carlo normalization based on integrated luminosity

BH process dominant at the middle and large ν

π^0 background contributing at the small ν



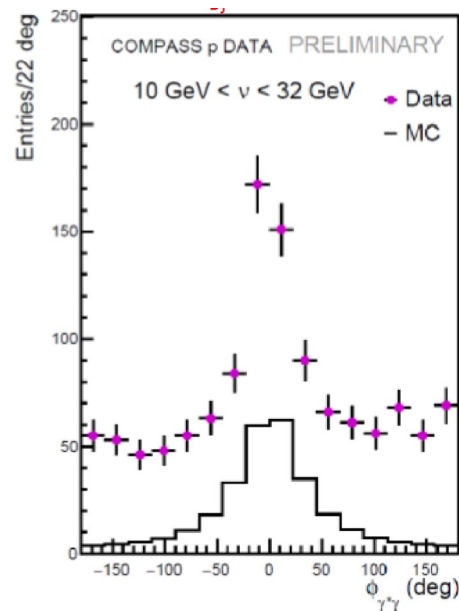
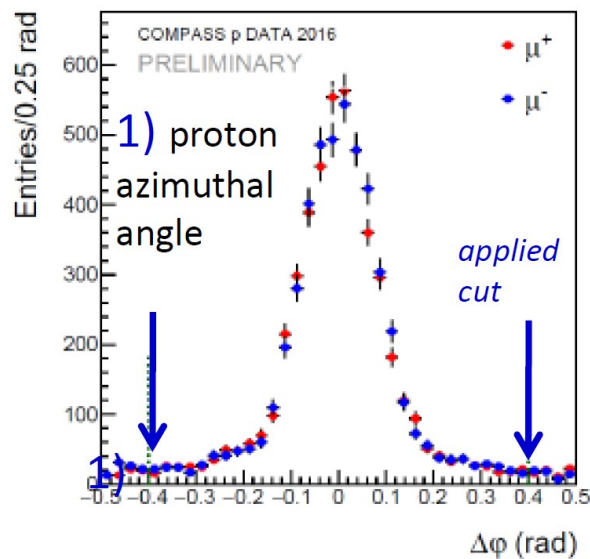




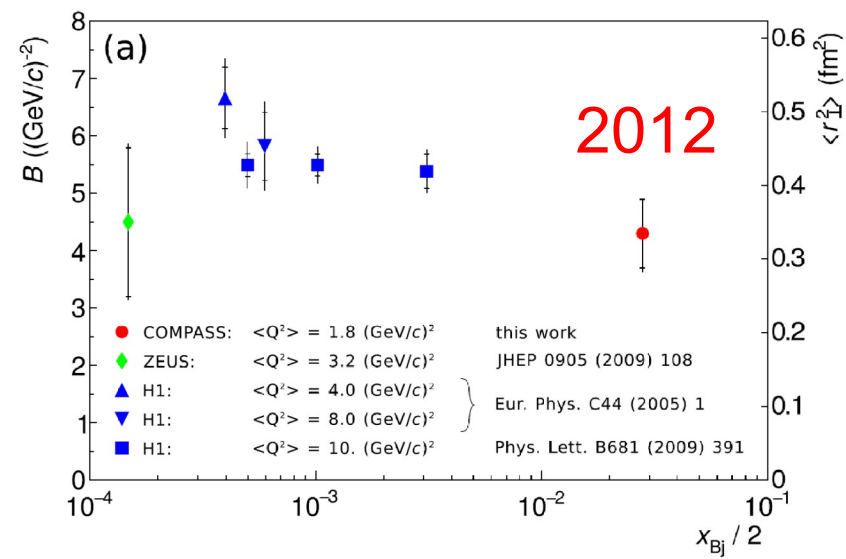
COMPASS 2016 ~ 2017 (2 × 6 months)



10 times more statistics in 2016 ~ 2017



w/ 13% of 2016-2017 data



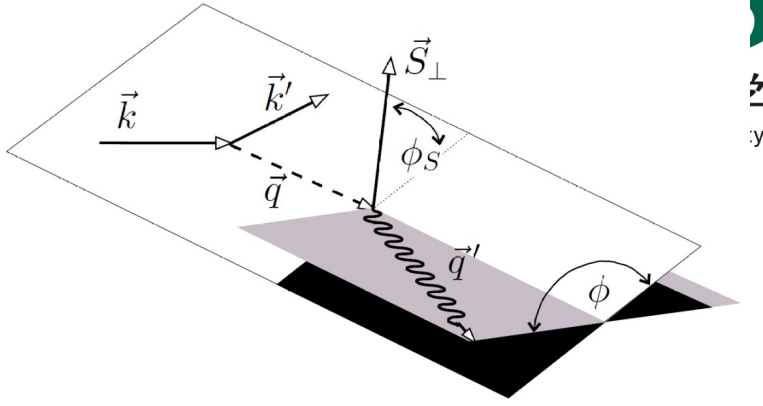
$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi} = \frac{x_B e^6}{32(2\pi)^4 Q^4 \sqrt{1 + \epsilon^2}} |\mathcal{T}_{ep \rightarrow ep\gamma}|^2,$$

$$|\mathcal{T}_{ep \rightarrow ep\gamma}|^2 = |\mathcal{T}_{\text{BH}}|^2 + |\mathcal{T}_{\text{DVCS}}|^2 + \mathcal{I},$$

$$\sigma_{\text{DVCS}} \ll \sigma_{\text{BH}} \quad \text{@HERMES, JLab}$$

Differential cross section

Unpol. target



$$d\sigma \propto |\mathcal{T}_{\text{BH}}|^2 + |\mathcal{T}_{\text{DVCS}}|^2 + \mathcal{I},$$

$$|\mathcal{T}_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left(c_0^{\text{BH}} + \sum_{n=1}^2 c_n^{\text{BH}} \cos(n\phi) \right),$$

$$|\mathcal{T}_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left(c_0^{\text{DVCS}} + \sum_{n=1}^2 c_n^{\text{DVCS}} \cos(n\phi) + \lambda s_1^{\text{DVCS}} \sin \phi \right),$$

$$\mathcal{I} = \frac{-e_l K_{\mathcal{I}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left(c_0^{\mathcal{I}} + \sum_{n=1}^3 c_n^{\mathcal{I}} \cos(n\phi) + \lambda \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right).$$

Beam Charge

Beam helicity

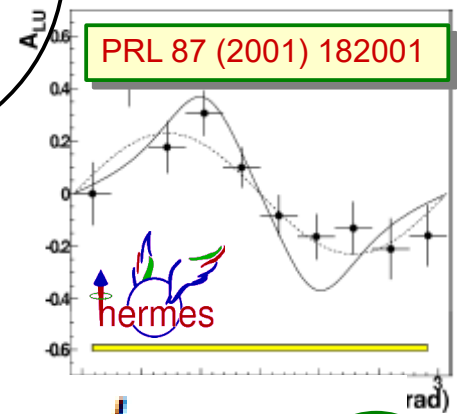
Cross section asymmetries and GPDs

A_C

A_{LU}

$$\mathcal{I} = \frac{-e_{\ell} K_{\mathcal{I}}}{\mathcal{P}_1(\phi) \mathcal{P}_2(\phi)} \left(c_0^{\mathcal{I}} + \sum_{n=1}^3 c_n^{\mathcal{I}} \cos(n\phi) - \lambda \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right)$$

$$s_1^{\mathcal{I}} \approx 8 \frac{\sqrt{-t}}{Q} y(2-y) \Im m(C_{\text{unp}}^{\mathcal{I}}).$$



$$C_{\text{unp}}^{\mathcal{I}} = F_1 \mathcal{H} + \frac{x_B}{2-x_B} (F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4M_p^2} F_2 \mathcal{E}$$

$$C_{\text{unp}}^{\mathcal{I}} = F_1 \mathcal{H} + \frac{x_B}{2 - x_B} (F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4M_p^2} F_2 \mathcal{E}$$

Compton form factors

NPB629 (2002) 323-392

$$\{\mathcal{H}, \mathcal{E}, \mathcal{H}_+^3, \mathcal{E}_+^3, \tilde{\mathcal{H}}_-^3, \tilde{\mathcal{E}}_-^3\}(\xi) = \int_{-1}^1 dx C^{(-)}(\xi, x) \{H, E, H_+^3, E_+^3, \tilde{H}_-^3, \tilde{E}_-^3\}(x, \eta)|_{\eta=-\xi},$$

$$\{\tilde{\mathcal{H}}, \tilde{\mathcal{E}}, \tilde{\mathcal{H}}_+^3, \tilde{\mathcal{E}}_+^3, \mathcal{H}_-^3, \mathcal{E}_-^3\}(\xi) = \int_{-1}^1 dx C^{(+)}(\xi, x) \{\tilde{H}, \tilde{E}, \tilde{H}_+^3, \tilde{E}_+^3, H_-^3, E_-^3\}(x, \eta)|_{\eta=-\xi},$$

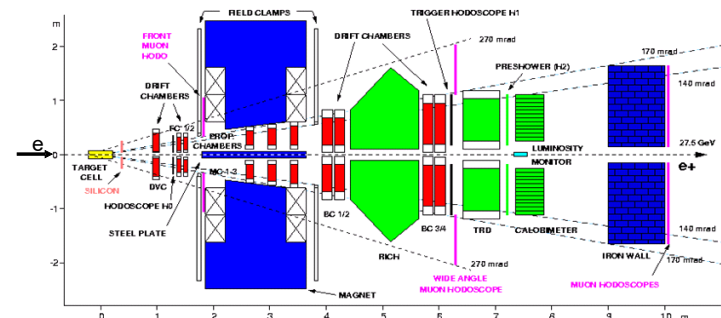
Sum of quark flavors

$$C_{\text{unp}}^{\mathcal{I}} = F_1 \mathcal{H} + \frac{x_B}{2 - x_B} (F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4M_p^2} F_2 \mathcal{E}$$

Negligible

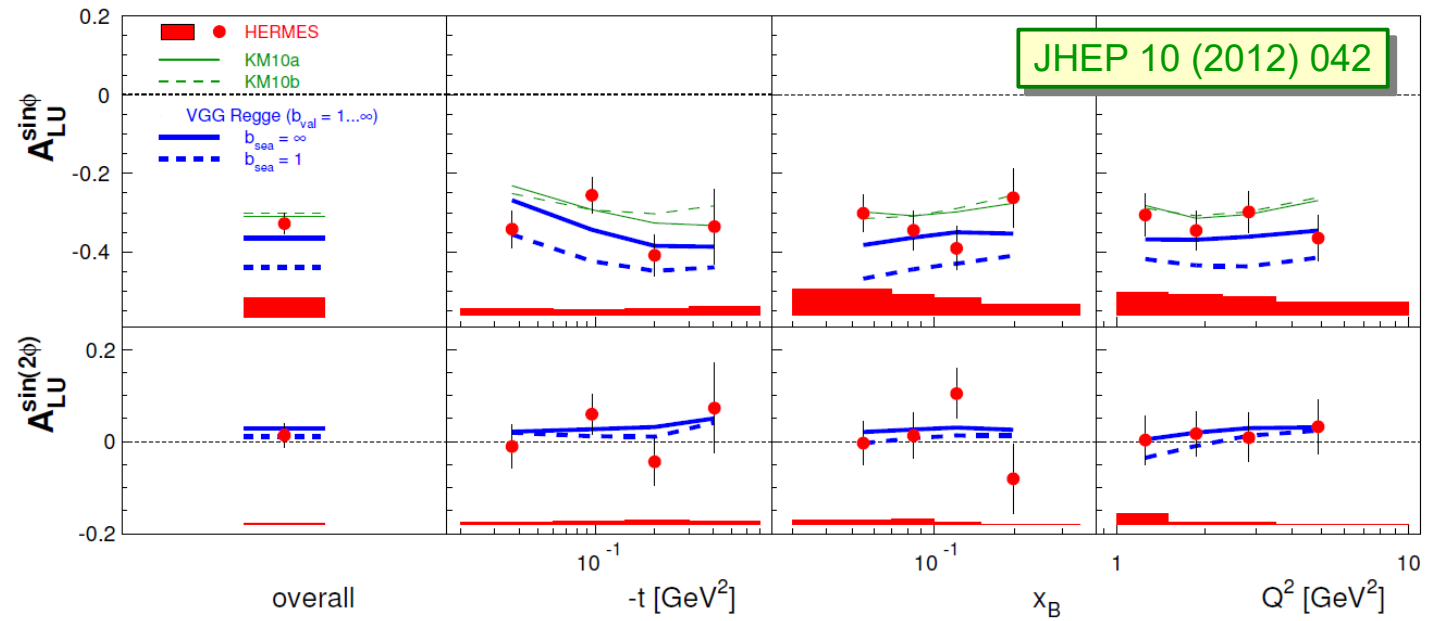
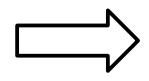
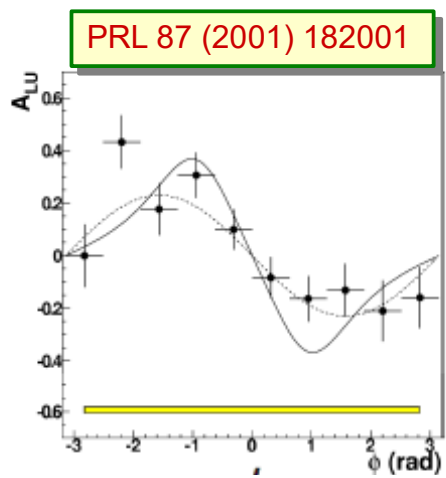
Beam spin asymmetry

$$A_{LU} \rightarrow \propto \sin\phi$$



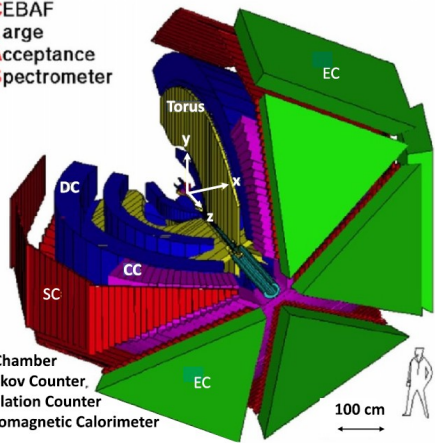
Beam: 27.6 GeV polarized e-/e+ @HERA
 1997 ~ 2005: H, D, L-pol H, L-pol D, T-pol H
 2006 – 2007: H and D w/ recoil detector

w/ recoil proton detection

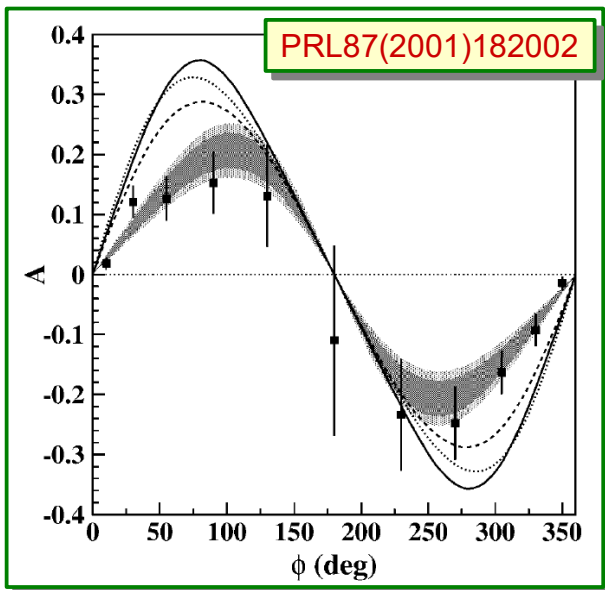


DVCS @ CLAS

CEBAF
Large
Acceptance
Spectrometer

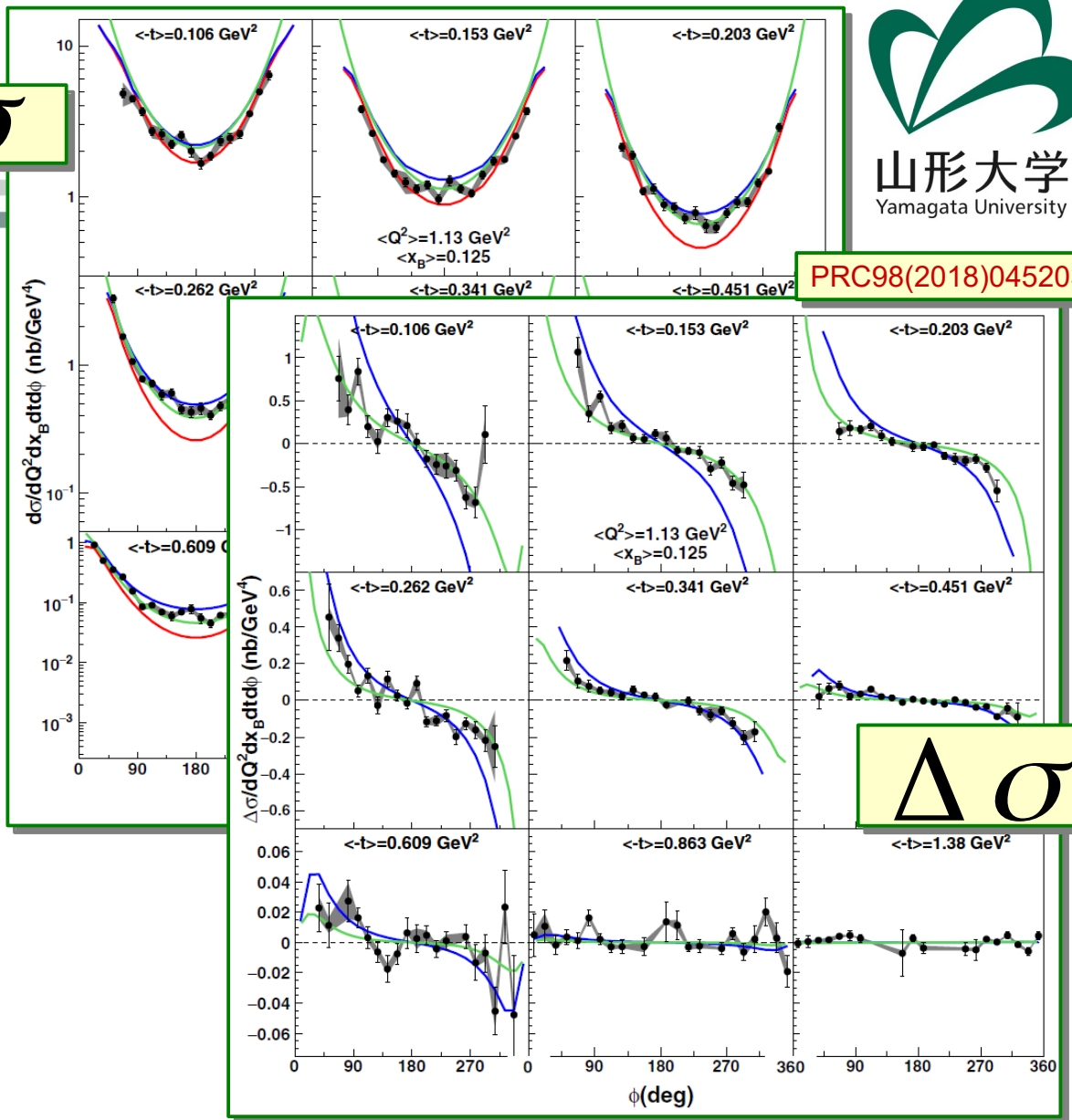


DC: Drift Chamber
CC: Cerenkov Counter
SC: Scintillation Counter
EC: Electromagnetic Calorimeter



Pol. 4 GeV electron

σ



PRC98(2018)045203

$\Delta \sigma$

Pol. 6 GeV electron

$$\langle Q^2 \rangle = 1.13, 1.67, 2.86 \text{ GeV}^2$$

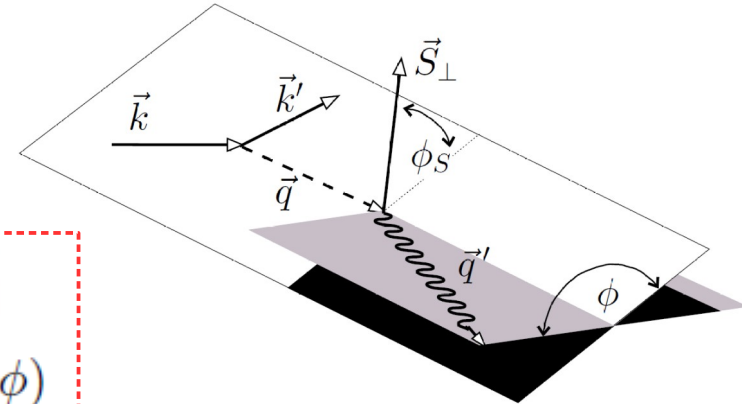
$$\langle x_{Bj} \rangle = 0.125, 0.187, 0.335$$

with a transversely polarized target

$$|T_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left(c_{0,\text{UU}}^{\text{BH}} + \left\{ c_{1,\text{UU}}^{\text{BH}} \cos \phi + \left\{ c_{2,\text{UU}}^{\text{BH}} \cos(2\phi) \right\} \right\} \right),$$

$$|T_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left(c_{0,\text{UU}}^{\text{DVCS}} + c_{2,\text{UU}}^{\text{DVCS}} \cos(2\phi) + \left\{ c_{1,\text{UU}}^{\text{DVCS}} \cos \phi \right. \right. \\ \left. \left. + S_{\perp} \left[c_{0,\text{UT}}^{\text{DVCS}} \sin(\phi - \phi_S) + c_{2,\text{UT}}^{\text{DVCS}} \sin(\phi - \phi_S) \cos(2\phi) \right. \right. \right. \\ \left. \left. + s_{2,\text{UT}}^{\text{DVCS}} \cos(\phi - \phi_S) \sin(2\phi) \right. \right. \\ \left. \left. + \left\{ c_{1,\text{UT}}^{\text{DVCS}} \sin(\phi - \phi_S) \cos \phi + s_{1,\text{UT}}^{\text{DVCS}} \cos(\phi - \phi_S) \sin \phi \right\} \right] \right)$$

$$I = \frac{-K_{\text{I}e_l}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left(c_{1,\text{UU}}^{\text{I}} \cos \phi + c_{3,\text{UU}}^{\text{I}} \cos(3\phi) \right. \\ \left. + \left\{ c_{0,\text{UU}}^{\text{I}} + c_{2,\text{UU}}^{\text{I}} \cos(2\phi) \right\} \right. \\ \left. + S_{\perp} \left[c_{1,\text{UT}}^{\text{I}} \sin(\phi - \phi_S) \cos \phi + s_{1,\text{UT}}^{\text{I}} \cos(\phi - \phi_S) \sin \phi \right. \right. \\ \left. \left. + c_{3,\text{UT}}^{\text{I}} \sin(\phi - \phi_S) \cos(3\phi) + s_{3,\text{UT}}^{\text{I}} \cos(\phi - \phi_S) \sin(3\phi) \right. \right. \\ \left. \left. + \left\{ c_{0,\text{UT}}^{\text{I}} \sin(\phi - \phi_S) + c_{2,\text{UT}}^{\text{I}} \sin(\phi - \phi_S) \cos(2\phi) \right. \right. \right. \\ \left. \left. + s_{2,\text{UT}}^{\text{I}} \cos(\phi - \phi_S) \sin(2\phi) \right\} \right] \right).$$



DVCS with a transversely polarized target

$$c_{0,UT}^{\text{DVCS}} \propto -\frac{\sqrt{-t}}{M} \text{Im} \left\{ \mathcal{H}\mathcal{E}^* - \mathcal{E}\mathcal{H}^* + \xi\tilde{\mathcal{E}}\tilde{\mathcal{H}}^* - \tilde{\mathcal{H}}\xi\tilde{\mathcal{E}}^* \right\},$$

$$c_{1,UU}^{\text{I}} \propto \frac{\sqrt{-t}}{Q} \text{Re} \left\{ F_1\mathcal{H} + \xi(F_1 + F_2)\tilde{\mathcal{H}} - \frac{t}{4M^2}F_2\mathcal{E} \right\},$$

UT → GPD E

$$c_{0,UU}^{\text{I}} \propto -\frac{\sqrt{-t}}{Q} c_{1,UU}^{\text{I}},$$

$$c_{1,UT}^{\text{I}} \propto -\frac{M}{Q} \text{Im} \left\{ \frac{t}{4M^2} \left[(2 - x_B)F_1\mathcal{E} - 4\frac{1 - x_B}{2 - x_B}F_2\mathcal{H} \right] + x_B\xi \left[F_1(\mathcal{H} + \mathcal{E}) - (F_1 + F_2) \left(\tilde{\mathcal{H}} + \frac{t}{4M^2}\tilde{\mathcal{E}} \right) \right] \right\}$$

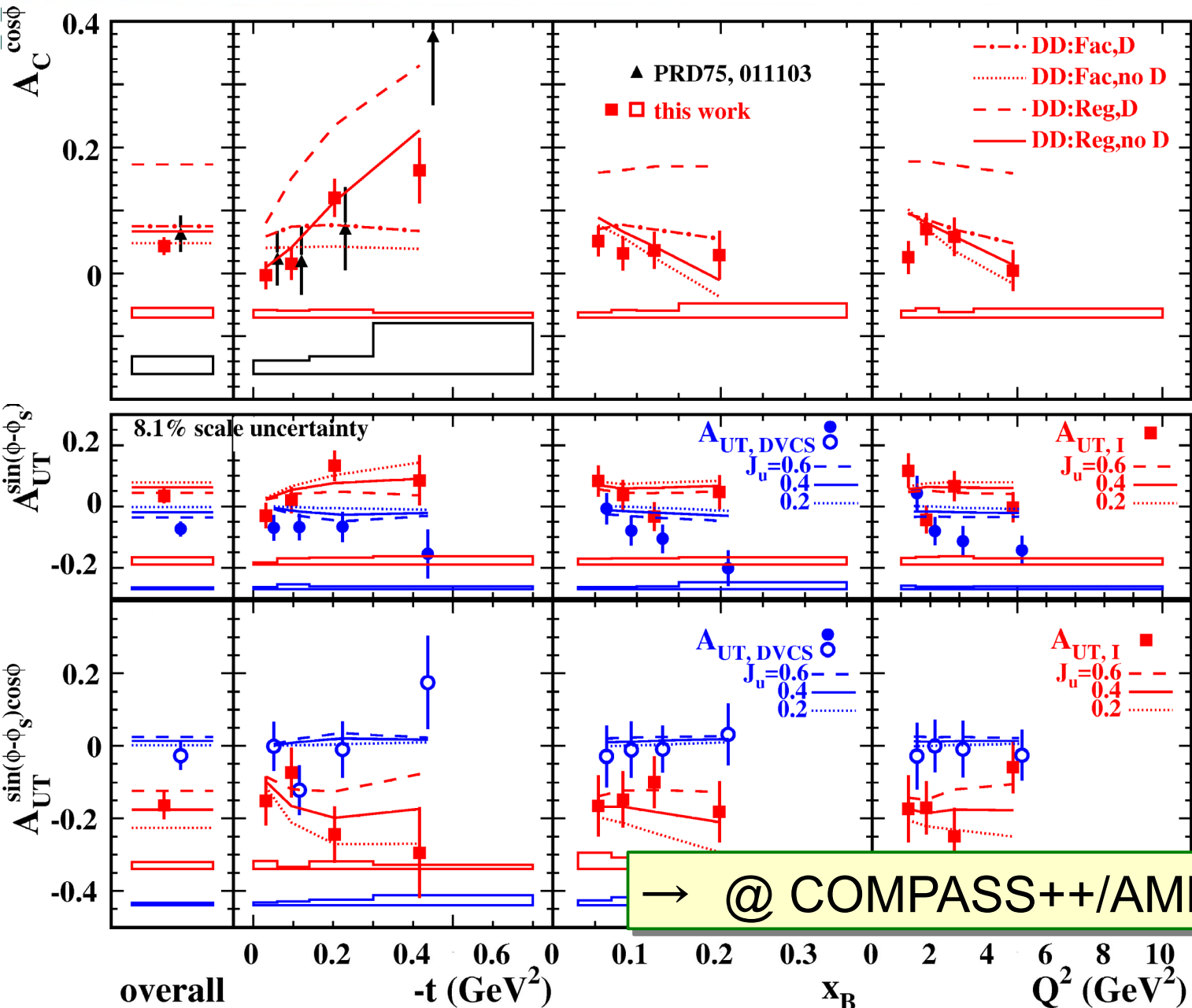
$$c_{0,UT}^{\text{I}} \propto -\frac{\sqrt{-t}}{Q} c_{1,UT}^{\text{I}},$$

$$s_{1,UT}^{\text{I}} \propto -\frac{M}{Q} \text{Im} \left\{ \frac{t}{4M^2} \left[4\frac{1 - x_B}{2 - x_B}F_2\tilde{\mathcal{H}} - (F_1 + \xi F_2)x_B\tilde{\mathcal{E}} \right] + x_B \left[(F_1 + F_2) \left(\xi\mathcal{H} + \frac{t}{4M^2}\mathcal{E} \right) - \xi F_1 \left(\tilde{\mathcal{H}} + \frac{x_B}{2}\tilde{\mathcal{E}} \right) \right] \right\}$$

DVCS with T-pol. H target



HERMES,
JHEP06 (2008) 066



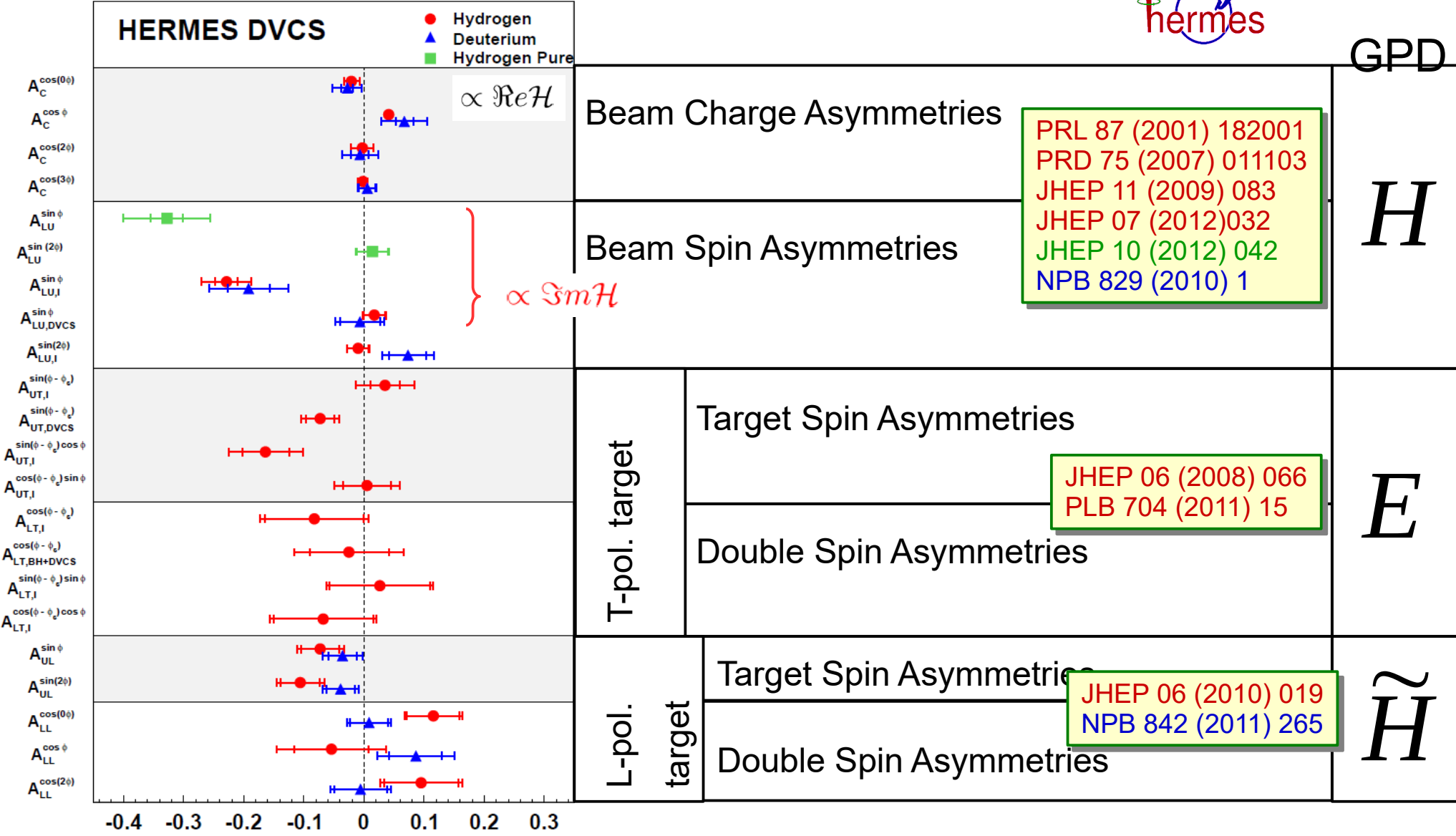
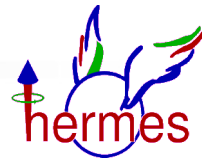
$$A_C^{\cos\phi} \propto \Re [F \mathcal{H}]$$

$$A_{UT,DVCS}^{\sin(\phi-\phi_s)} \propto \Im [\mathcal{H} \mathcal{E}^* - \mathcal{E} \mathcal{H}^* + \xi \tilde{\mathcal{E}} \tilde{\mathcal{H}}^* - \tilde{\mathcal{H}} \xi \tilde{\mathcal{E}}^*]$$

$$A_{UT,I}^{\sin(\phi-\phi_s)} \propto -A_{UT,I}^{\sin(\phi-\phi_s)\cos\phi} \propto \Im [F_1 \mathcal{E} - F_2 \mathcal{H}]$$

→ @ COMPASS++/AMBER, JLab12GeV

Extracted overall asymmetries @ HERMES



-0.4 -0.3 -0.2 -0.1 0 0.1 0.2 0.3

Amplitude Value

"*First Observation of Exclusive Deeply Virtual Compton Scattering in Polarized Electron Beam Asymmetry Measurements*", Phys. Rev. Lett. 87, 182002 (2001)

"*Measurement of Deeply Virtual Compton Scattering with a **Polarized Proton Target***", Phys. Rev. Lett. 97, 072002 (2006)

"*Deeply Virtual Compton Scattering **Beam-Spin Asymmetries***", Phys. Rev. Lett. 100, 162002 (2008)

"***Longitudinal Target-Spin Asymmetries** for Deeply Virtual Compton Scattering*", Phys. Rev. Lett. 114, 032001 (2015)

"***Single and Double Spin Asymmetries** for Deeply Virtual Compton Scattering Measured with CLAS and a **Longitudinally Polarized Proton Target***", Phys. Rev. D 91, 052014 (2015)

"*First Exclusive Measurement of **Deeply Virtual Compton Scattering off 4He**: Toward the 3D Tomography of Nuclei*", Phys. Rev. Lett. 119, 202004 (2017)

"*Measurement of **Unpolarized and Polarized Cross Sections** for Deeply Virtual Compton Scattering on the Proton at Jefferson Laboratory with CLAS*", Phys. Rev. C 98, 045203 (2018)

"*Exploring the Structure of the **Bound Proton** with Deeply Virtual Compton Scattering*", Phys.Rev.Lett. 123 (2019) no.3, 032502



(1) The beam charge & spin sum of cross sections

$$S_{CS,U} \equiv d\sigma^{\leftrightarrow} + d\sigma^{\bar{\leftrightarrow}} = 2(d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + e_{\mu} P_{\mu} \text{Im } I),$$

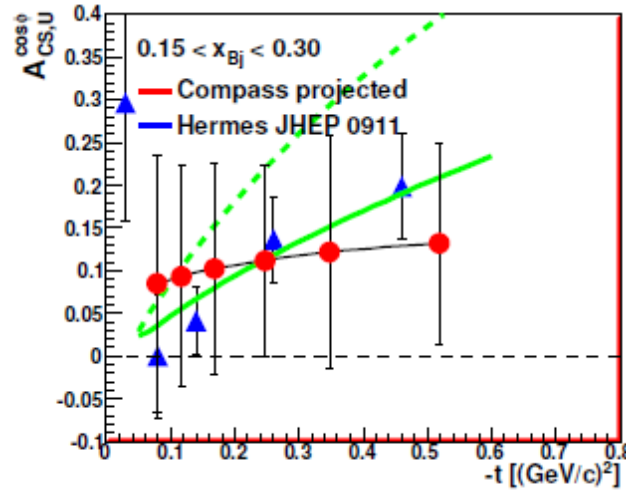
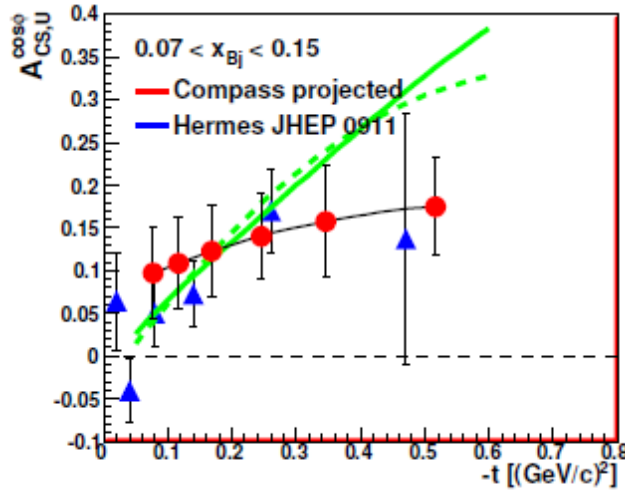
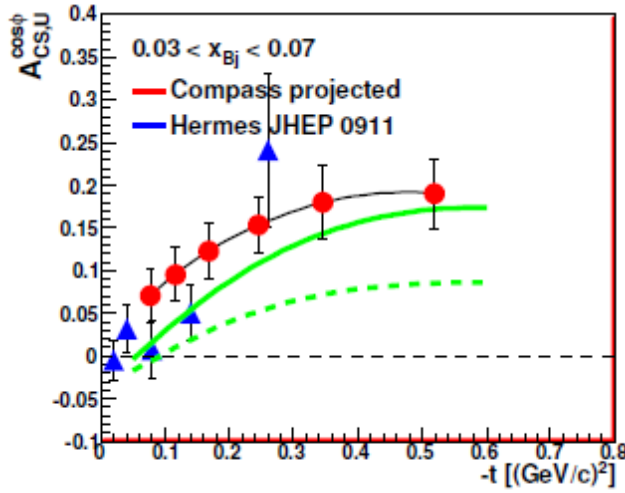
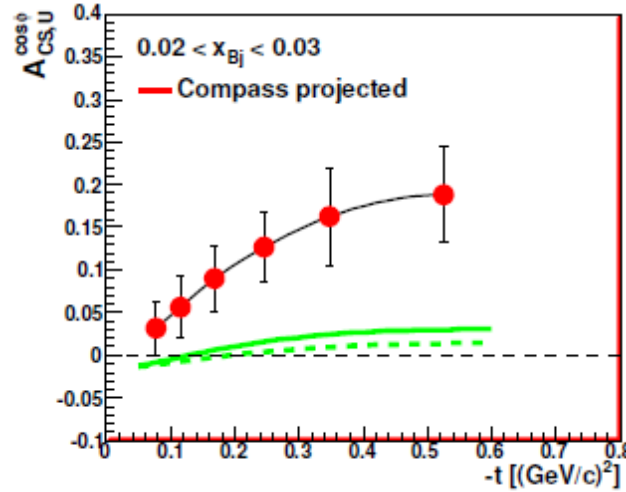
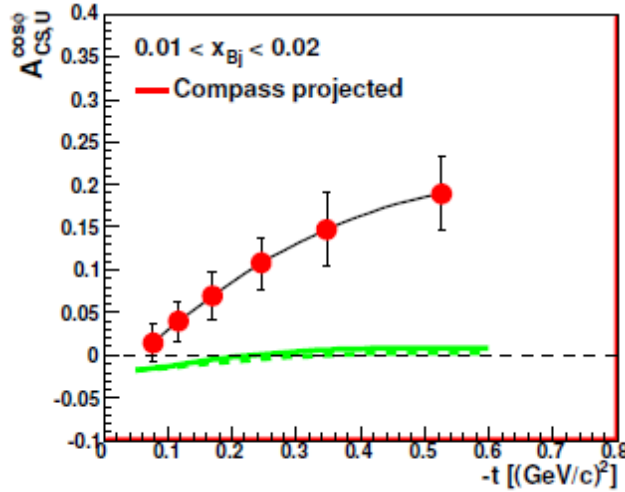
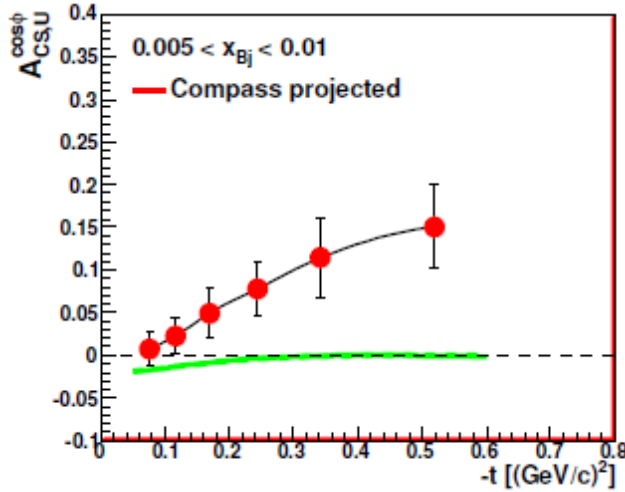
(2) The beam charge & spin difference of cross sections

$$D_{CS,U} \equiv d\sigma^{\leftrightarrow} - d\sigma^{\bar{\leftrightarrow}} = 2(P_{\mu} d\sigma_{pol}^{DVCS} + e_{\mu} \text{Re } I),$$

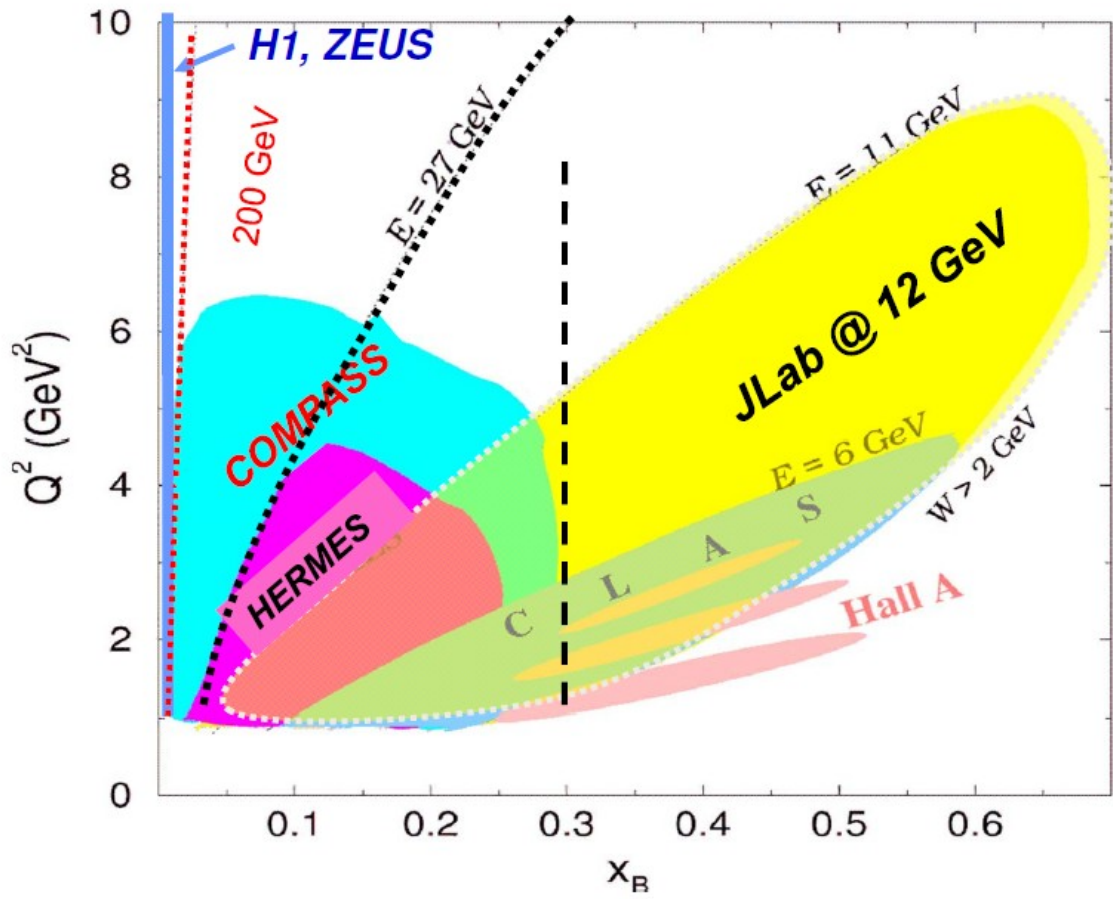
(3) The beam charge & spin asymmetry of cross sections

$$A_{CS,U} \equiv \frac{d\sigma^{\leftrightarrow} - d\sigma^{\bar{\leftrightarrow}}}{d\sigma^{\leftrightarrow} + d\sigma^{\bar{\leftrightarrow}}} = \frac{D_{CS,U}}{S_{CS,U}},$$

Expected beam charge spin asymmetries



DVCS @ JLab 12 GeV





DVCS experiments @ Jlab 12 GeV

Hall-A

E12-06-114 Measurements of Electron-Helicity Dependent Cross Sections of Deeply Virtual Compton Scattering with CEBAF at 12 GeV

Hall-B CLAS12

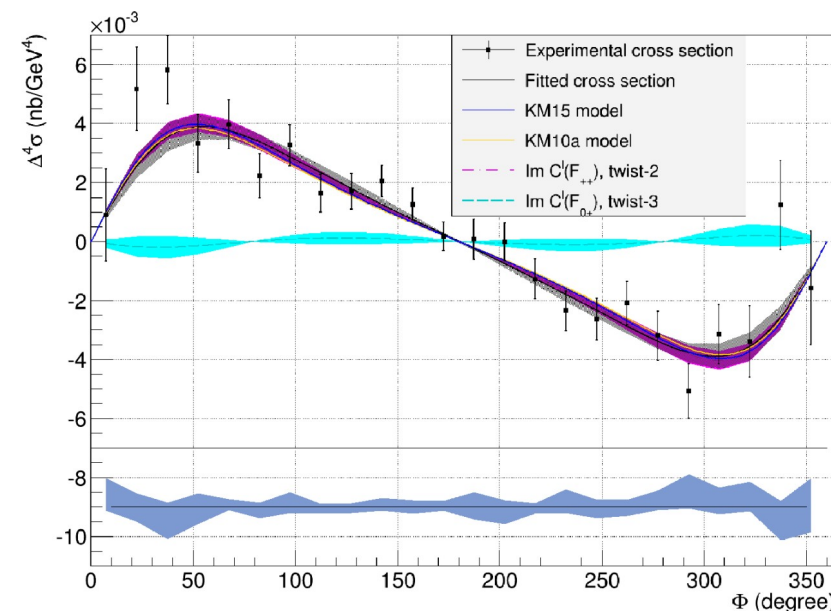
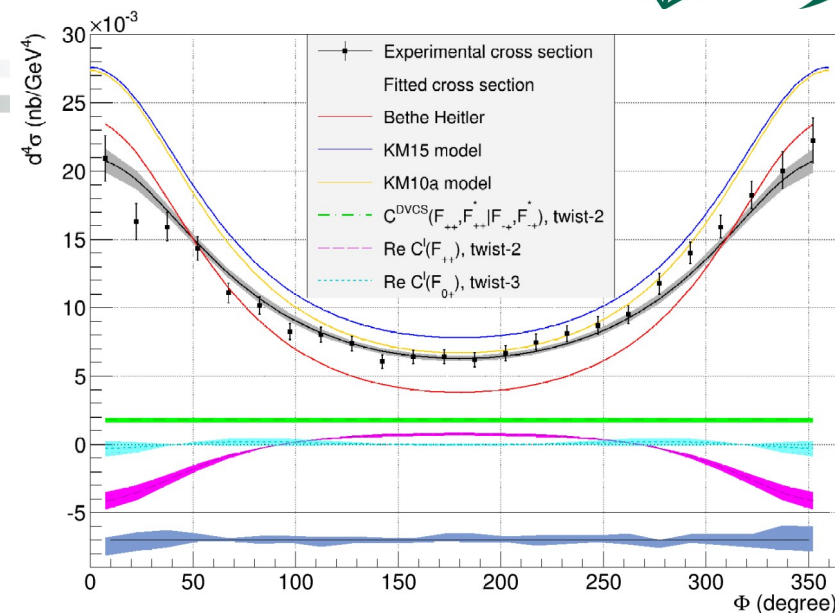
E12-06-119 Deeply Virtual Compton Scattering with CLAS at 11 GeV

E12-11-003 Deeply Virtual Compton Scattering on the Neutron with CLAS12 at 11 GeV

E12-06-109A Deeply virtual Compton scattering on the neutron with a longitudinally polarized deuteron target

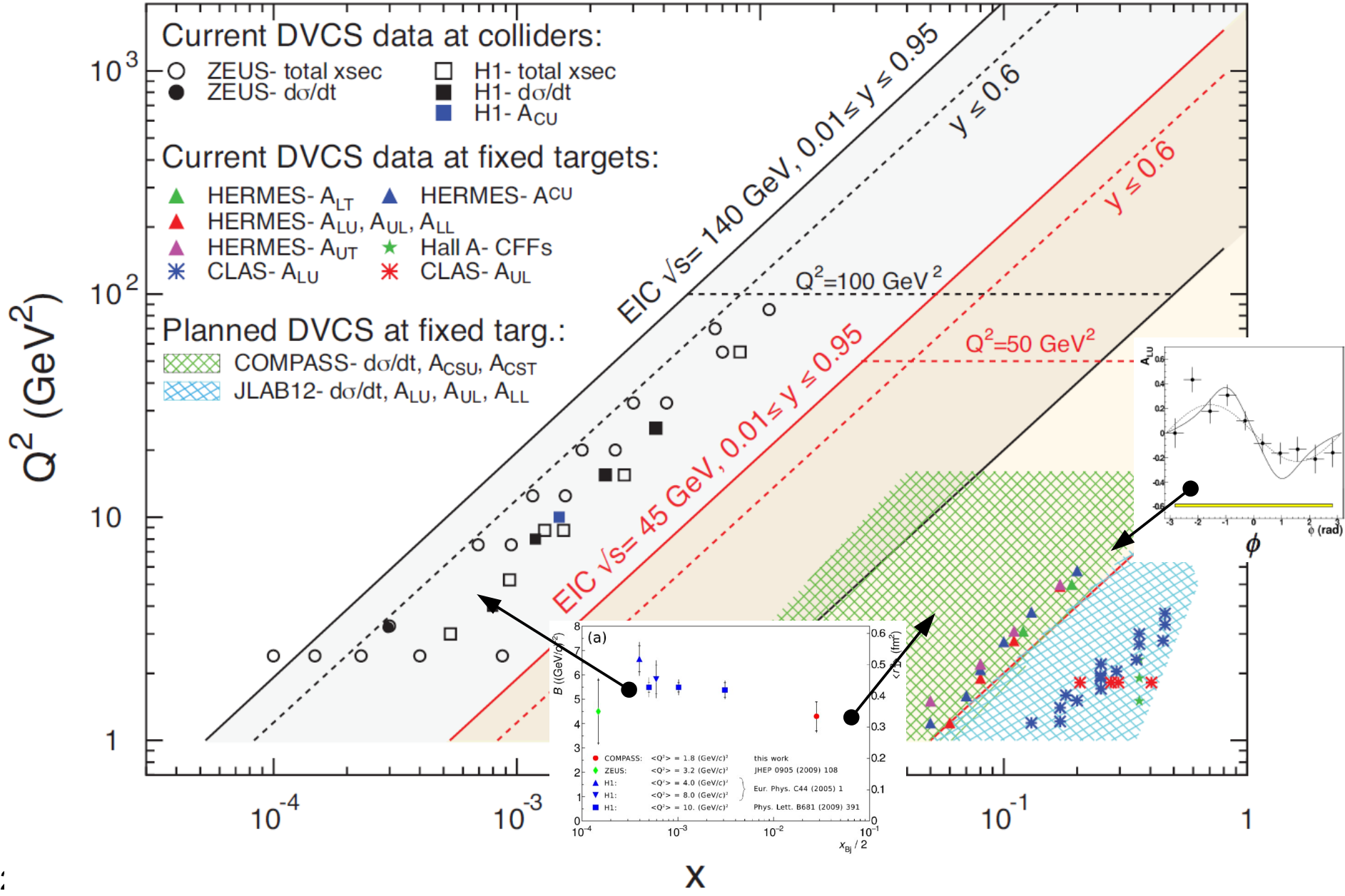
Hall-C

E12-13-010 Exclusive Deeply Virtual Compton and Neutral Pion Cross-Section Measurements in Hall C



E12-06-114 preliminary

DVCS @ Electron Ion Collider



DVCS @ HERMES



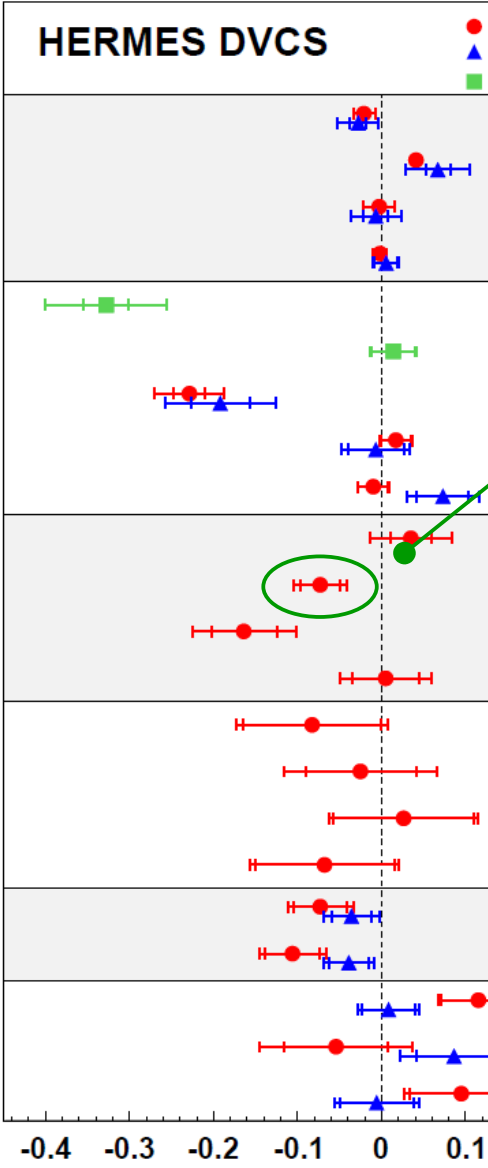
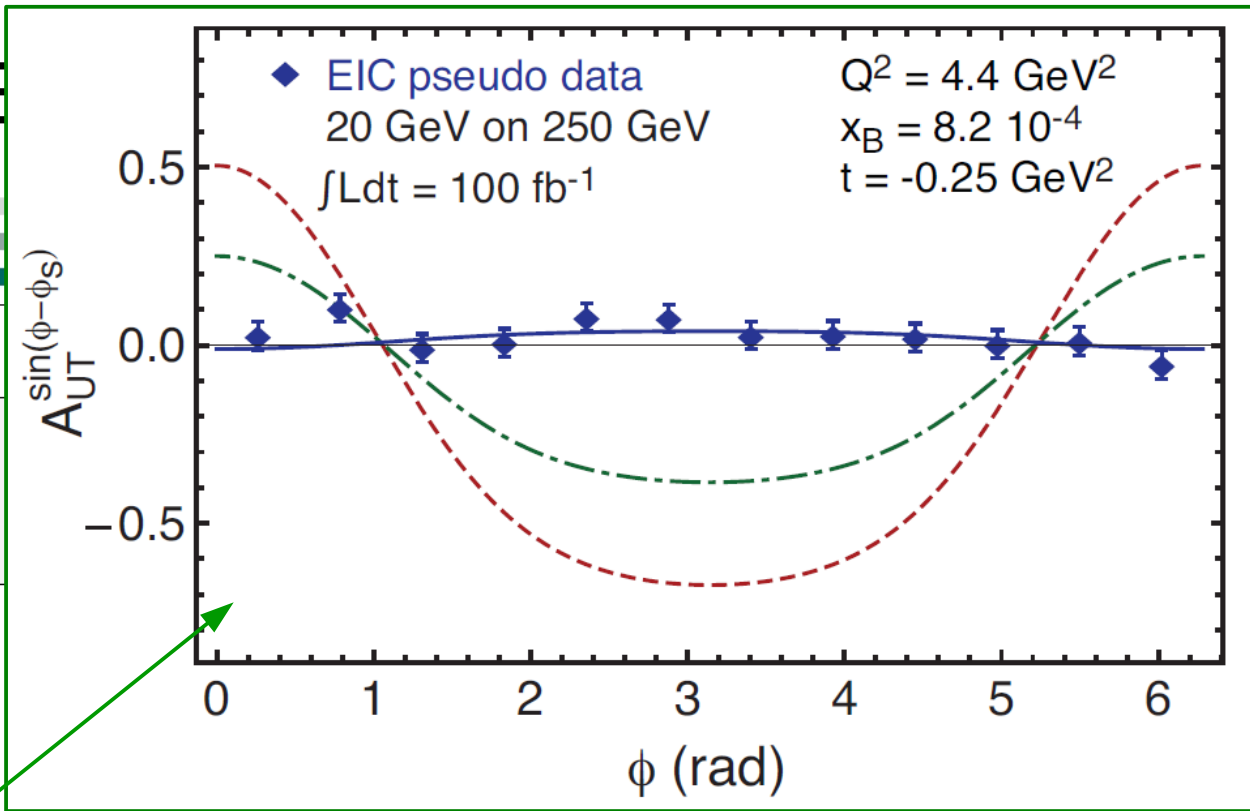
Tohoku University

GPD

H

E

\tilde{H}



$p \uparrow \downarrow$

$p \leftarrow \rightarrow$

Target Spin Asymmetries
 Double Spin Asymmetries
 クォーク全角運動量 \leftrightarrow

JHEP 06 (2008) 066
 PLB 704 (2011) 15

JHEP 06 (2010) 019
 NPB 842 (2011) 265

Amplitude Value

GPD extraction from data

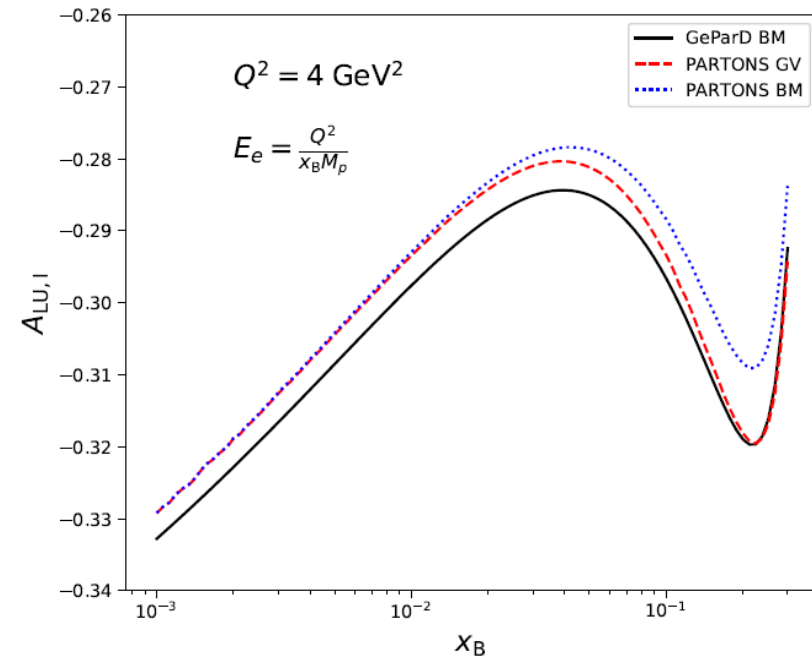
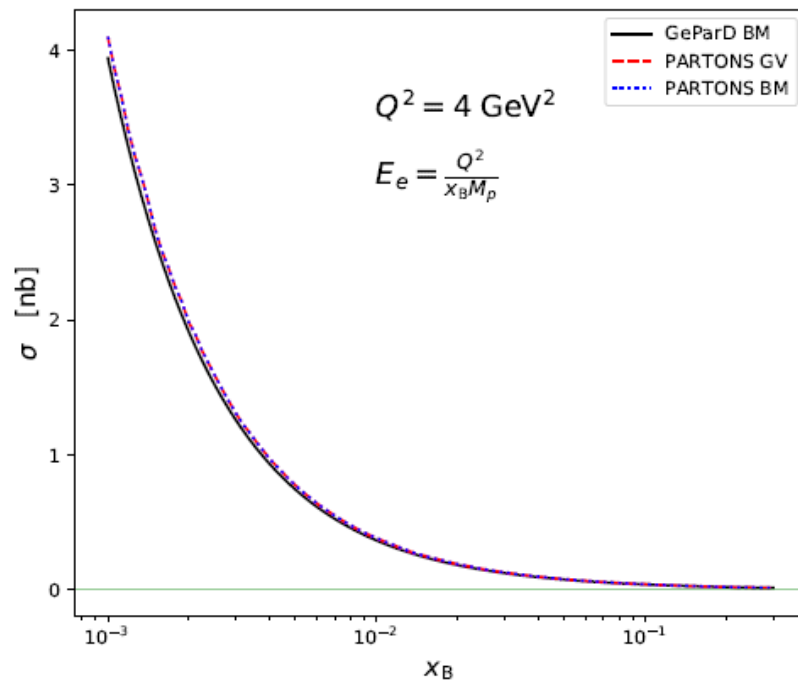
GPD based analysis frameworks:

GeParD

PARTON(EPJC78(2018) 478)

<http://calculon.phy.hr/gpd/>

<https://drf-gitlab.cea.fr/partons/core>



GPD extraction from data

GPD based analysis frameworks:

GeParD <http://calculon.phy.hr/gpd/>

PARTON <http://partons.cea.fr/partons/doc/html/index.html>

[K.K., Müller '09-'15]

Collaboration	Observable	Ref.	n_{pts}	KMM12		KM15	
				χ^2/n_{pts}	pull	χ^2/n_{pts}	pull
ZEUS	σ_{DVCS}	[19][20]	11	0.49	-1.76	0.51	-1.74
ZEUS,H1	$d\sigma_{DVCS}/dt$	[19][21][22]	24	0.97	0.85	1.04	1.37
HERMES	$A_C^{\cos 0\phi}$	[23]	6	1.31	0.49	1.24	0.29
HERMES	$A_C^{\cos \phi}$	[23]	6	0.24	-0.56	0.07	-0.20
HERMES	$A_{LU,1}^{\sin \phi}$	[23]	6	2.08	-2.52	1.34	-1.28
CLAS	$A_{LU}^{\sin \phi}$	[24]	4	1.28	2.09		
CLAS	$A_{LU}^{\sin \phi}$	[4][25]	13			1.24	0.63
CLAS	$\Delta\sigma^{\sin \phi,w}$	[7]	48			0.41	-1.66
CLAS	$d\sigma^{\cos 0\phi,w}$	[7]	48			0.16	-0.21
CLAS	$d\sigma^{\cos \phi,w}$	[7]	48			1.16	6.36
Hall A	$\Delta\sigma^{\sin \phi,w}$	[5]	12	1.06	-2.55		
Hall A	$d\sigma^{\cos 0\phi,w}$	[5]	4	1.21	2.14		
Hall A	$d\sigma^{\cos \phi,w}$	[5]	4	3.49	-0.26		
Hall A	$\Delta\sigma^{\sin \phi,w}$	[6]	15			0.81	-2.84
Hall A	$d\sigma^{\cos 0\phi,w}$	[6]	10			0.40	0.92
Hall A	$d\sigma^{\cos \phi,w}$	[6]	10			2.52	-2.42
HERMES,CLAS	$A_{UL}^{\sin \phi}$	[18][26]	10	1.90	-1.89	1.10	-1.94
HERMES	$A_{LL}^{\cos 0\phi}$	[26]	4	3.44	2.17	3.19	1.99
HERMES	$A_{UT,1}^{\sin(\phi-\phi_2)\cos\phi}$	[27]	4	0.90	0.61	0.90	0.71
CLAS	$A_{UL}^{\sin \phi}$	[4]	10			0.76	0.38
CLAS	$A_{LL}^{\cos 0\phi}$	[4]	10			0.50	-0.22
CLAS	$A_{LL}^{\cos \phi}$	[4]	10			1.54	2.40

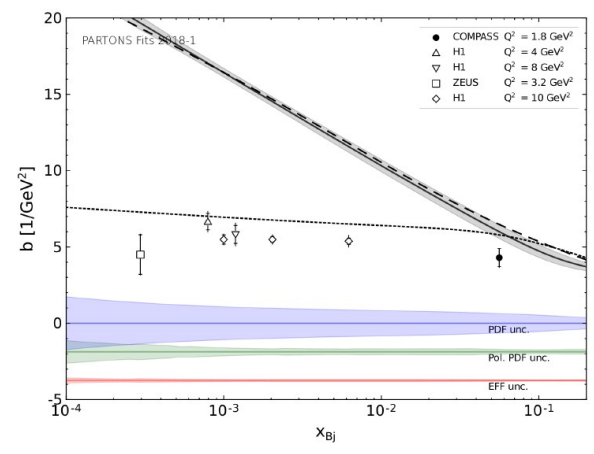
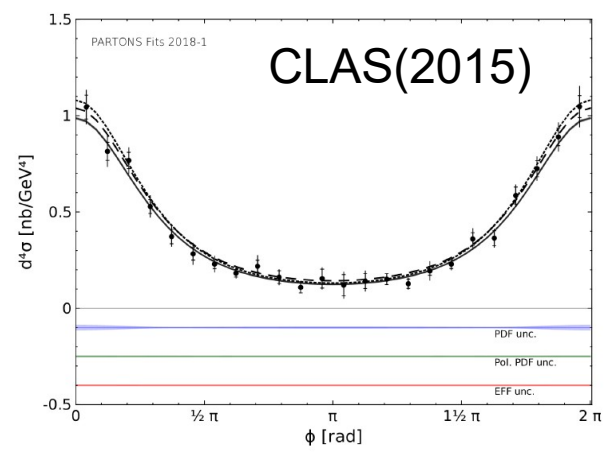
[Moutarde, Sznajder, Wagner, '18]

Data used in global fit

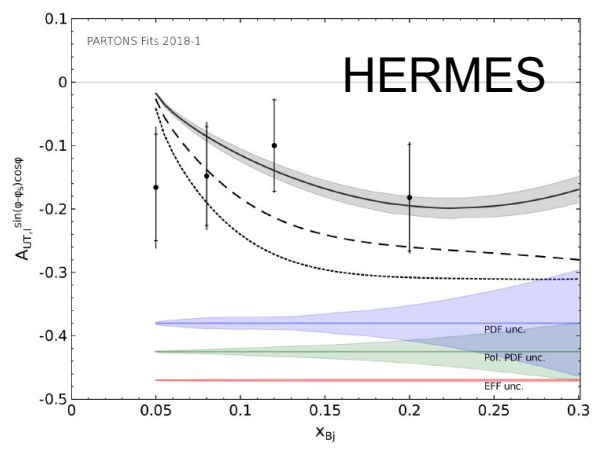
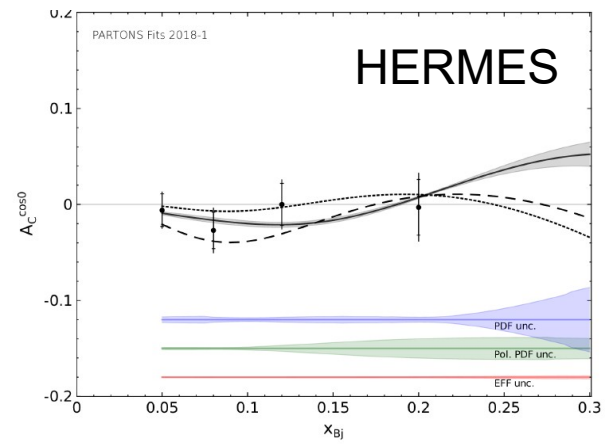
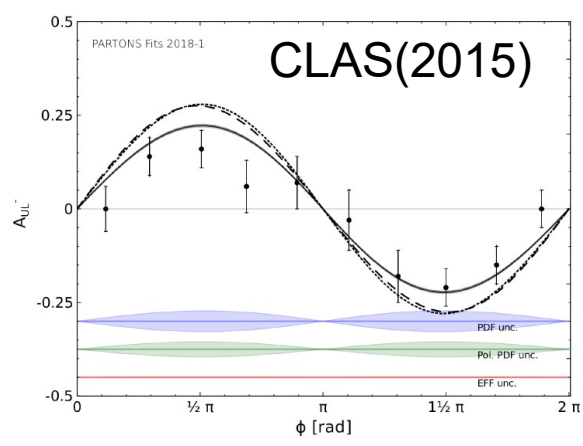
No.	Collab.	Year	Ref.	χ^2	n	χ^2/n
1	HERMES	2001	[13]	9.8	10	0.98
2		2006	[114]	2.9	4	0.72
3		2008	[115]	24.2	18	1.35
4		2009	[116]	40.1	35	1.15
5		2010	[117]	40.3	18	2.24
6		2011	[118]	14.5	24	0.60
7		2012	[119]	25.4	35	0.73
8	CLAS	2001	[14]	—	0	—
9		2006	[120]	0.9	2	0.47
10		2008	[121]	371.1	283	1.31
11		2009	[122]	36.4	22	1.66
12		2015	[123]	351.4	311	1.13
13		2015	[124]	937.9	1333	0.70
14	Hall A	2015	[112]	220.2	228	0.97
15		2017	[113]	258.8	276	0.94
16	COMPASS	2018	[55]	10.7	1	10.67

Fit with PARTONS (arXiv:1807.07620)

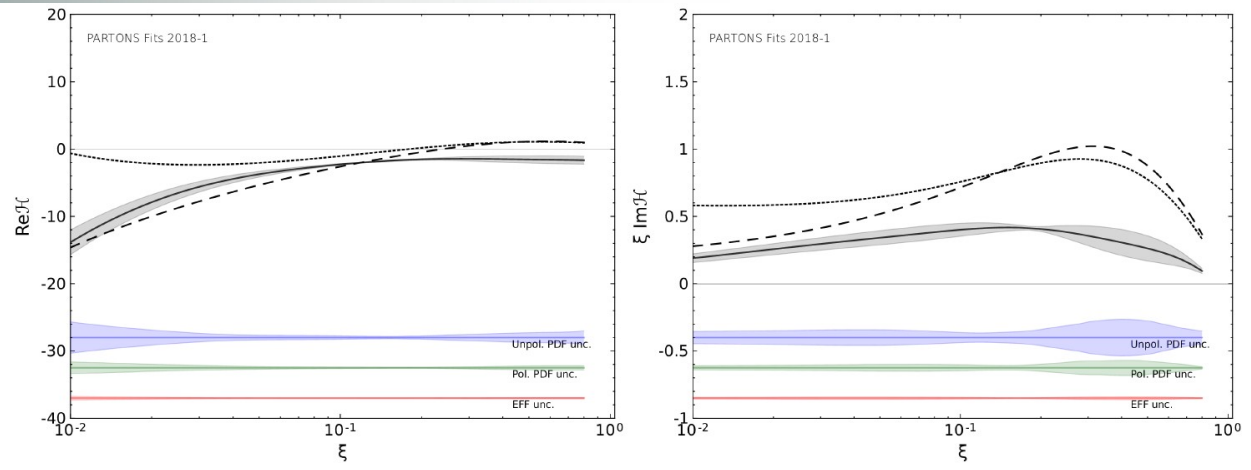
PARTONS18
 GK model
 VGG model



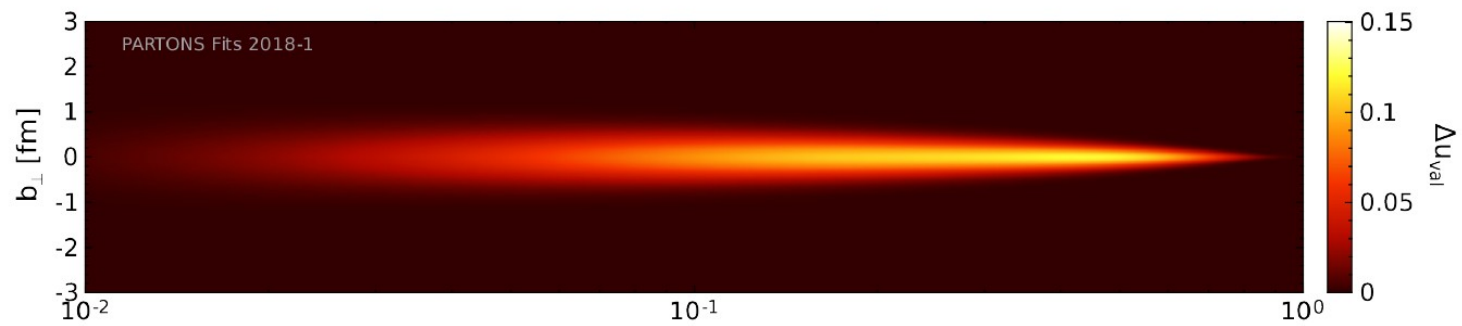
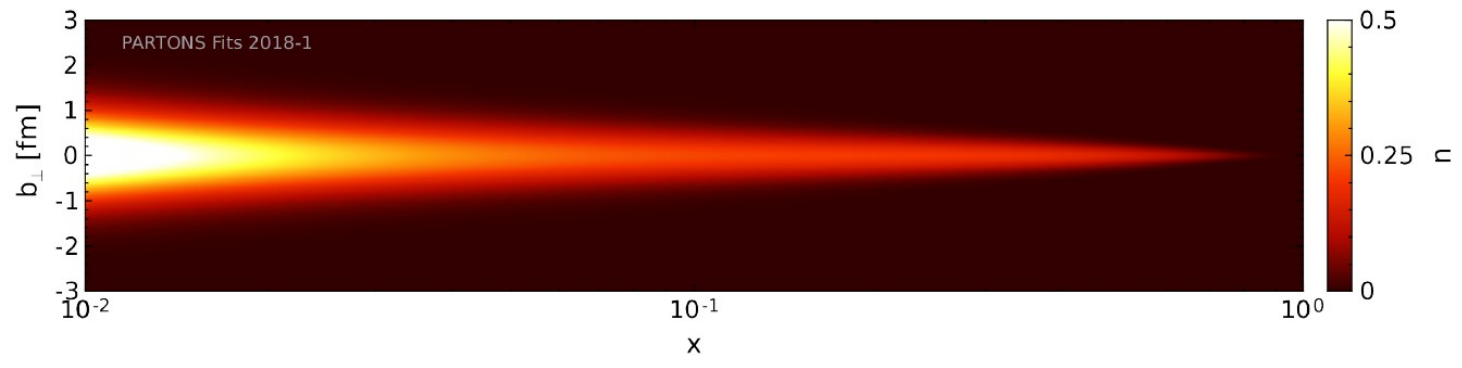
HERA&COMPASS



Fit with PARTONS (arXiv:1807.07620)



$t = -0.3 \text{ GeV}^2, Q^2 = 2 \text{ GeV}^2$



no uncertainties!

Summary and Outlook



H1, ZEUS σ

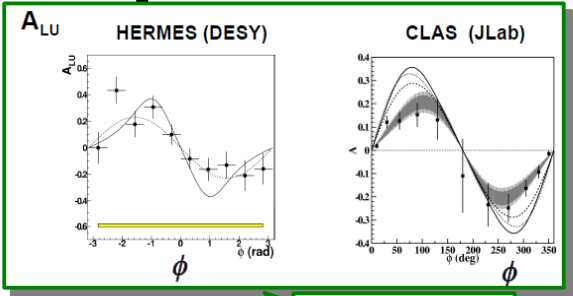
EIC

COMPASS II

COMPASS++/
AMBER

160 GeV μ ,
 σ , **BSA+BCA**

HERMES



PRL87(2001)

26.7 GeV electron, H, D, A
 σ , **BSA**, **BCA**, **TSA(L+T)**

JLab

Electron (4 GeV \rightarrow 6 GeV \rightarrow 12 GeV)
 σ , **BSA**

Precise determination of
GPD

2020/02/19 Observation