

Unfolding P_T dependence of A_N for Forward Neutron Production in Polarized $p + p$ Collisions at $\sqrt{s} = 200$ GeV

Spin PWG Meeting
2020/07/30
9:00 AM (KST/JST)



Benard Mulilo (KU/RIKEN)



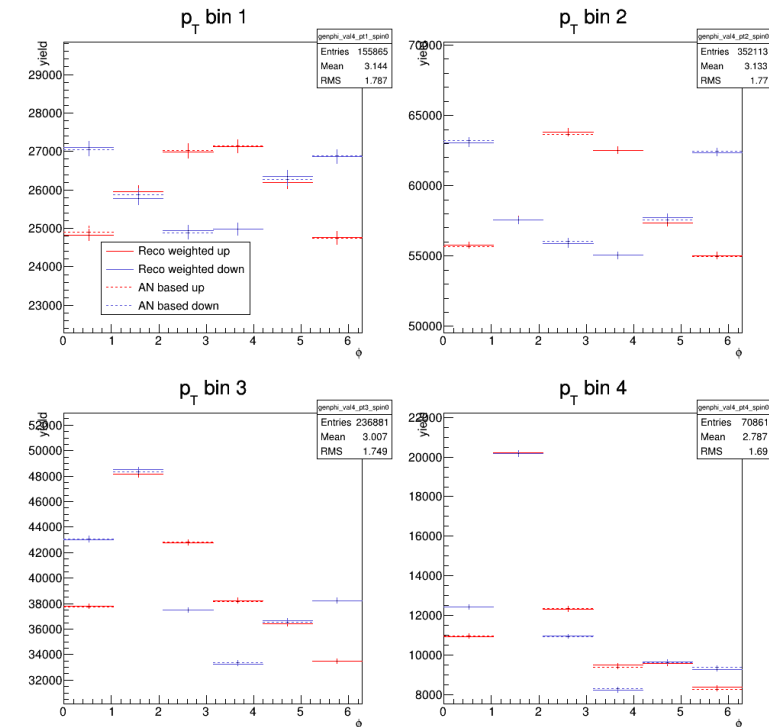
Last Update in Spin PWG Meeting - Asymmetry Extraction Strategy

[2020-06-18 (9 AM, JST/KST)]

- ❖ **Translation:** Measured Asymmetries (Minjung) are translated into 2D yields.
- ❖ **Unfolding:** Unfolding of the two-dimensional yields is executed.
- ❖ **Extraction:** Unfolded asymmetries obtained based on the unfolded yields by calculating asymmetries.

(Minjung's)

P_T dependent A_N 's → translate into 2D yields → Unfold → Get unfolded A_N 's



Asymmetry Weighting and Extraction - Different Functional Forms

For MC sample:

- ❖ Create spin up or down state (ispin 0, 1) for each event.

Create spin dependent weight according to some functional form:

- ❖ Polynomial (w_{pol3}) function:

$$w_{pol3} = 1 + (a + b * P_{T,T} + c * P_{T,T}^2 + d * P_{T,T}^3) * \cos(\Phi_{T,T} + spin * \pi)$$

- ❖ Power function (w_{pow}):

$$w_{pow} = 1 + (\alpha + \beta * P_{T,T}^\gamma) * \cos(\Phi_{T,T} + spin * \pi)$$

- ❖ Exponential function (w_{exp}):

$$w_{exp} = 1 + \left(\omega + \sigma * (1 - \exp(\eta * P_{T,T})) \right) * \cos(\Phi_{T,T} + spin * \pi)$$

a = constant part

b = linear part scanned over a wide range $b_{min} < b < b_{max}$

c = quadratic part scanned over a wide range between $c_{min} < c < c_{max}$

d = cubic part scanned over a wide range between $d_{min} < d < d_{max}$

s = spin ($\uparrow\downarrow$)

$P_{T,T}$ is the true transverse momentum and $\Phi_{T,T}$ is the true azimuthal angle distributions.

f = $\alpha, \beta, \gamma, \omega, \sigma, \eta$ are parameters.

Use these weights based on generated variables in all events and reconstructed variables, etc....

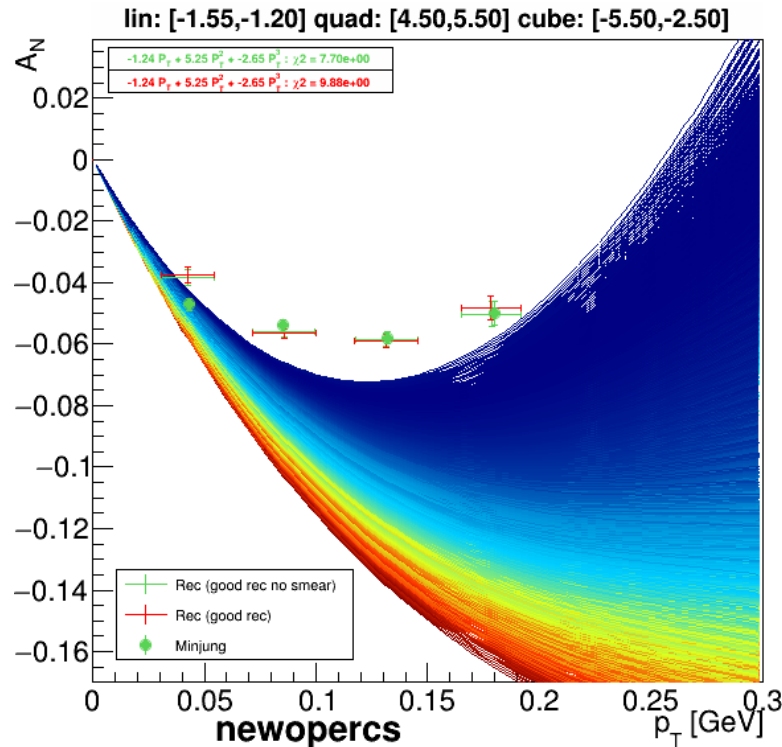
Asymmetries and Best Parameter Scanning – Minimum Chi-Square Search

Calculate Chi-Square based on reconstructed asymmetries and experimental data asymmetries (Minjung):

$$\chi_{min}^2 = \sum_i \frac{(A_{N,i}^{Minjung} - A_{N,i}^{wgt,reco})^2}{\Delta A_{N,i}^{2,Minjung} + \Delta A_{N,i}^{2,wgt,reco}}$$

Best parameter is found (i.e. parameter with lowest Chi-Square for each functional form).

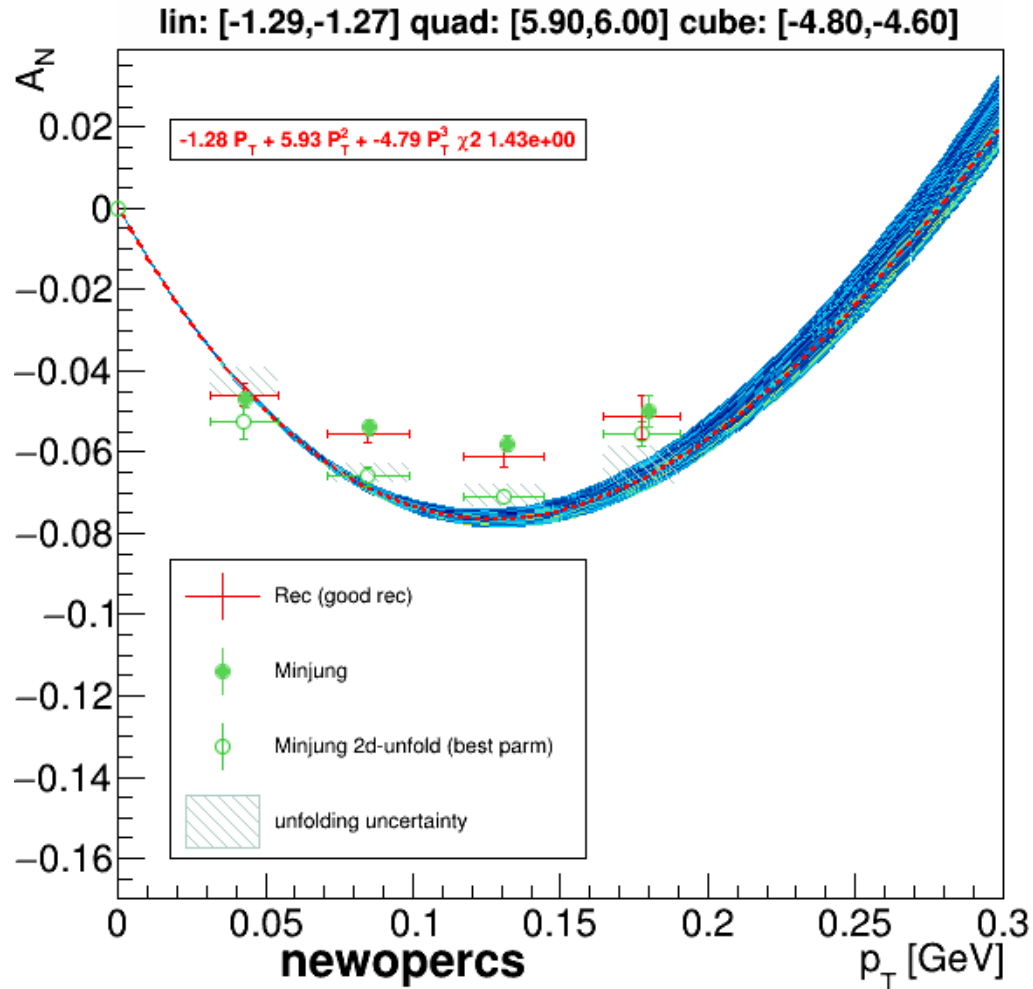
Reconstructed Asymmetries and Minimum Chi-Square Search – Coarse Scanning



- **Green points:** introduced asymmetries based on reco variables without crosstalk (not required)
- **Red points:** Introduced asymmetries based on smeared reco variables.
- Before unfolding, need best Chi-Square (minimum Chi-Square).
- Zoom in (coarse scanning to fine scanning) to find best minimum one.

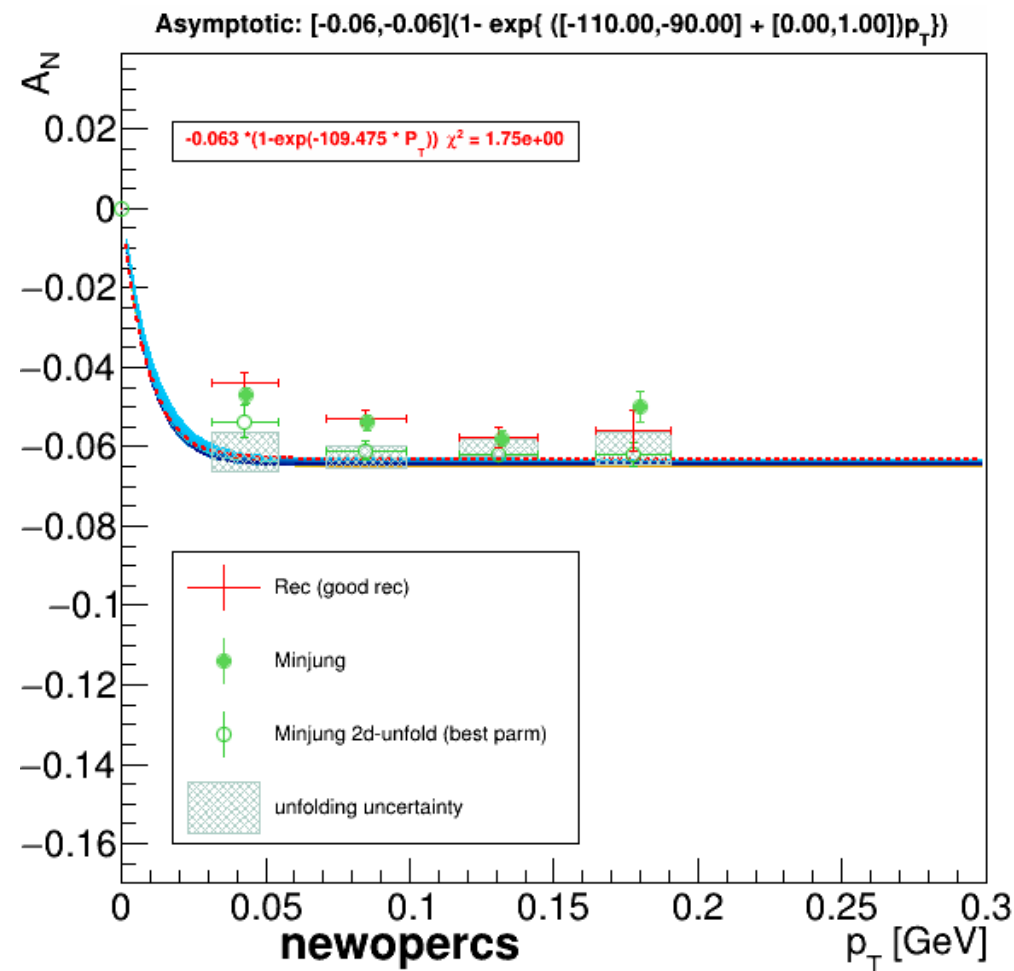
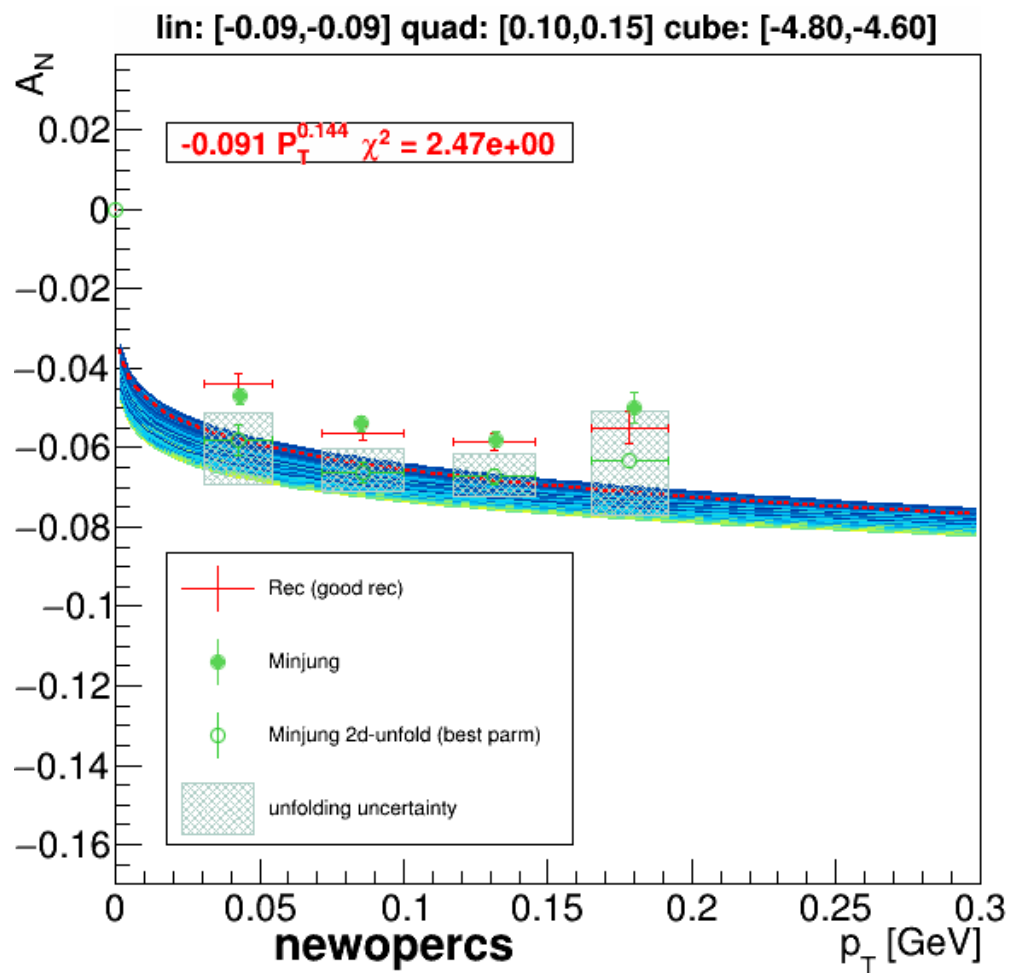
Reconstructed A_N 's	Linear			Quadratic			Cubic			Chi-Square (best)
	Min	Max	Best	Min	Max	Best	Min	Max	Best	
Green cross	-1.55	-1.20	-1.24	4.50	5.50	5.25	-5.5	-2.50	-2.65	7.70
Red cross	-1.25	-1.20	-1.24	4.50	5.50	5.25	-5.5	-2.50	-2.65	9.88

Asymmetries based on a 3rd order polynomial (pol3) function – Fine Scanning



- Fine scanning around best value based on Pol3.
- Shaded curve obtained from the spread of all unfolded A_N 's
- Red broken line is best parametrization in range used for the unfolding (input curve).

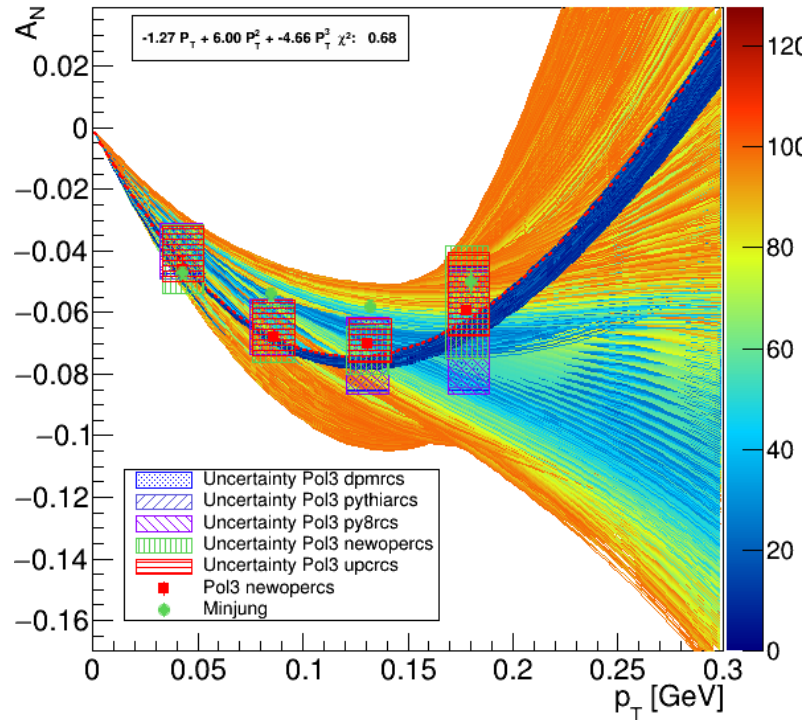
Fine Scanning for other Functional Forms – Power Law and Exponential



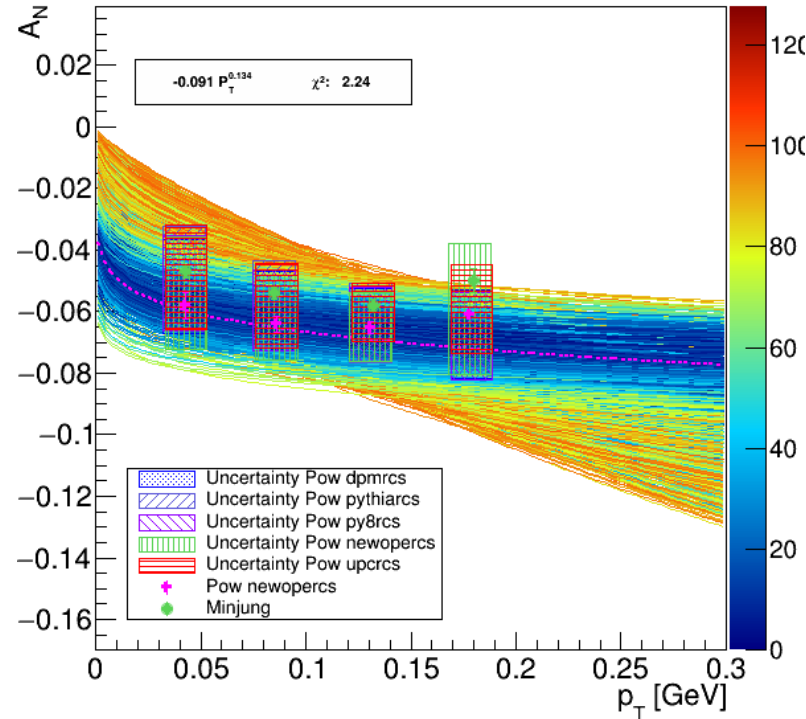
Both functions with somewhat larger Chi-Square than polynomial function (i.e. less flexible)

All Three Parameterizations with Coarse and Fine Scanning Ranges

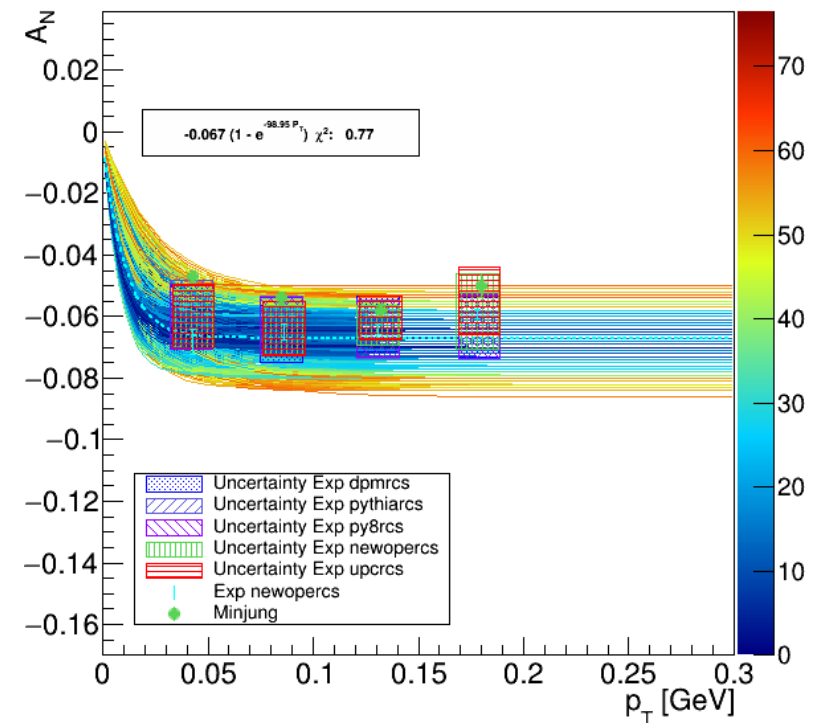
Pol3 dependence



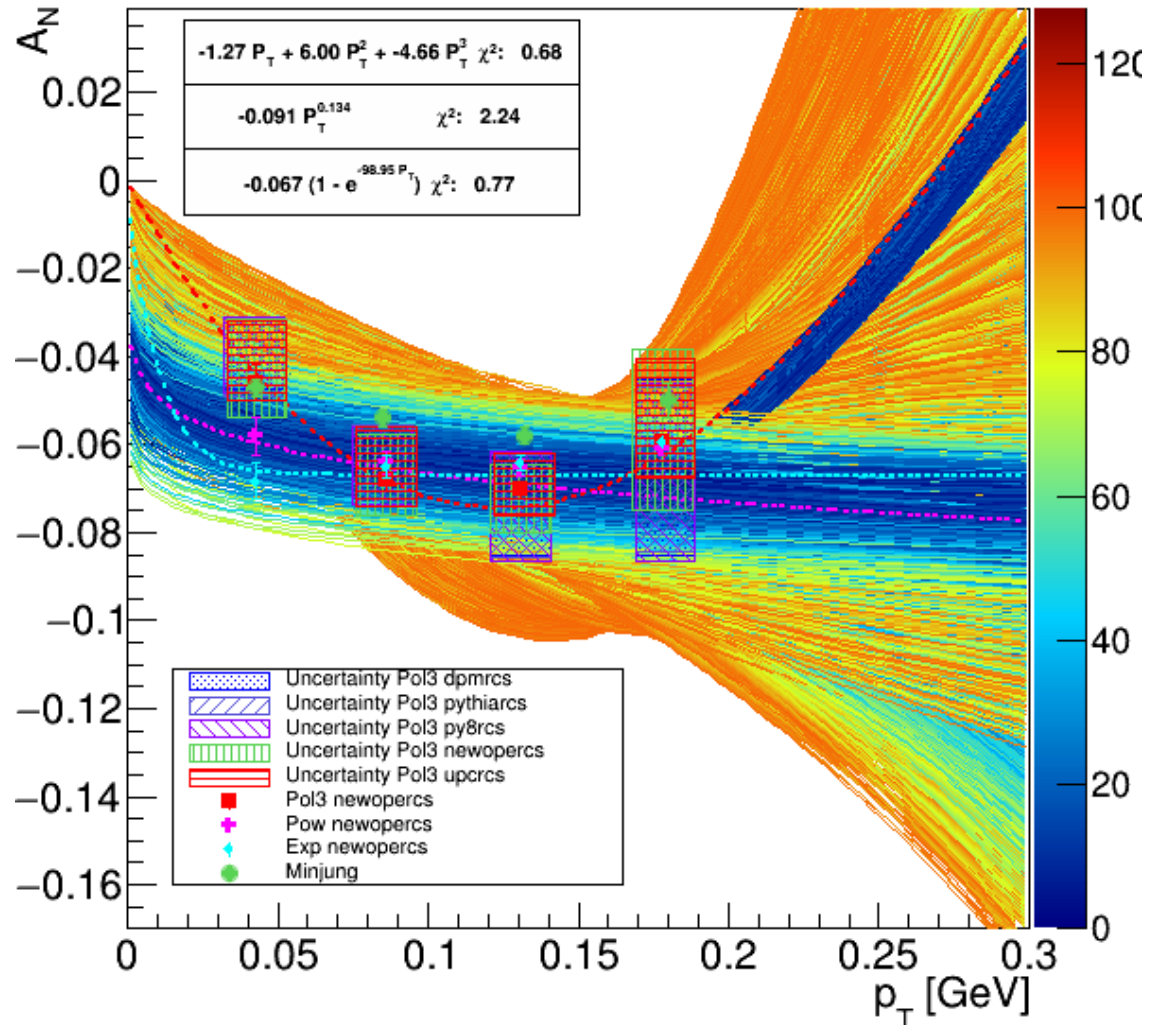
Power law dependence



1-exp dependence



Unfolded Asymmetries – Pol3, Power & Exponential Dependence



➤ Unfolded asymmetries for both coarse and fine ranges.

All show reasonable χ^2 in comparison to measured asymmetries (Minjung).

➤ Pol3 Chi2 = 0.68 : $b = -1.27$, $c = 6.00$, $d = -4.66$

➤ Powr Chi2 = 2.24 : $b = -0.091$, $c = +0.134$

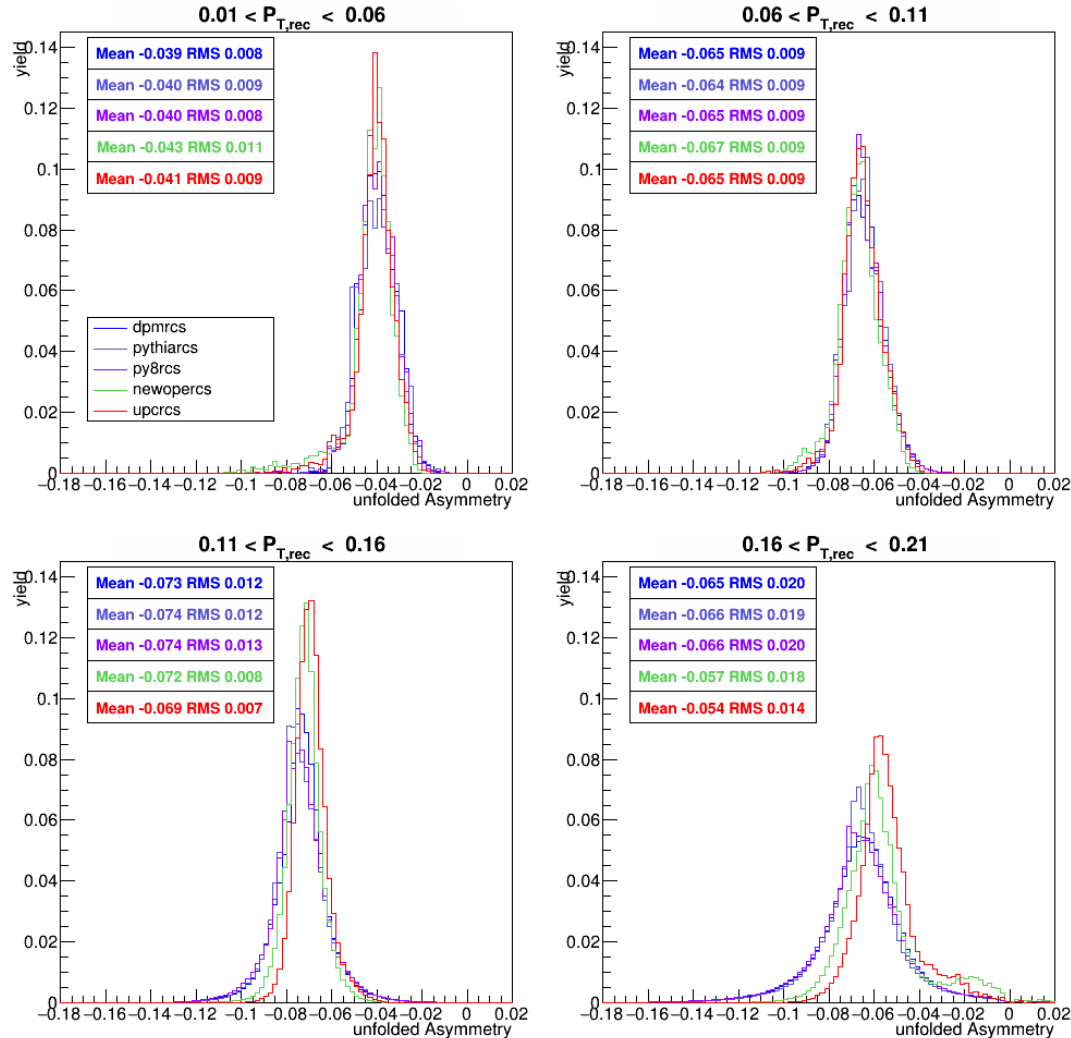
➤ Expo Chi2 = 0.77 : $b = -0.067$, $f = -98.95$

Lowest unfolded result for each parameterization displayed as points.

RMS ranges of unfolded points shown for all the MCs -

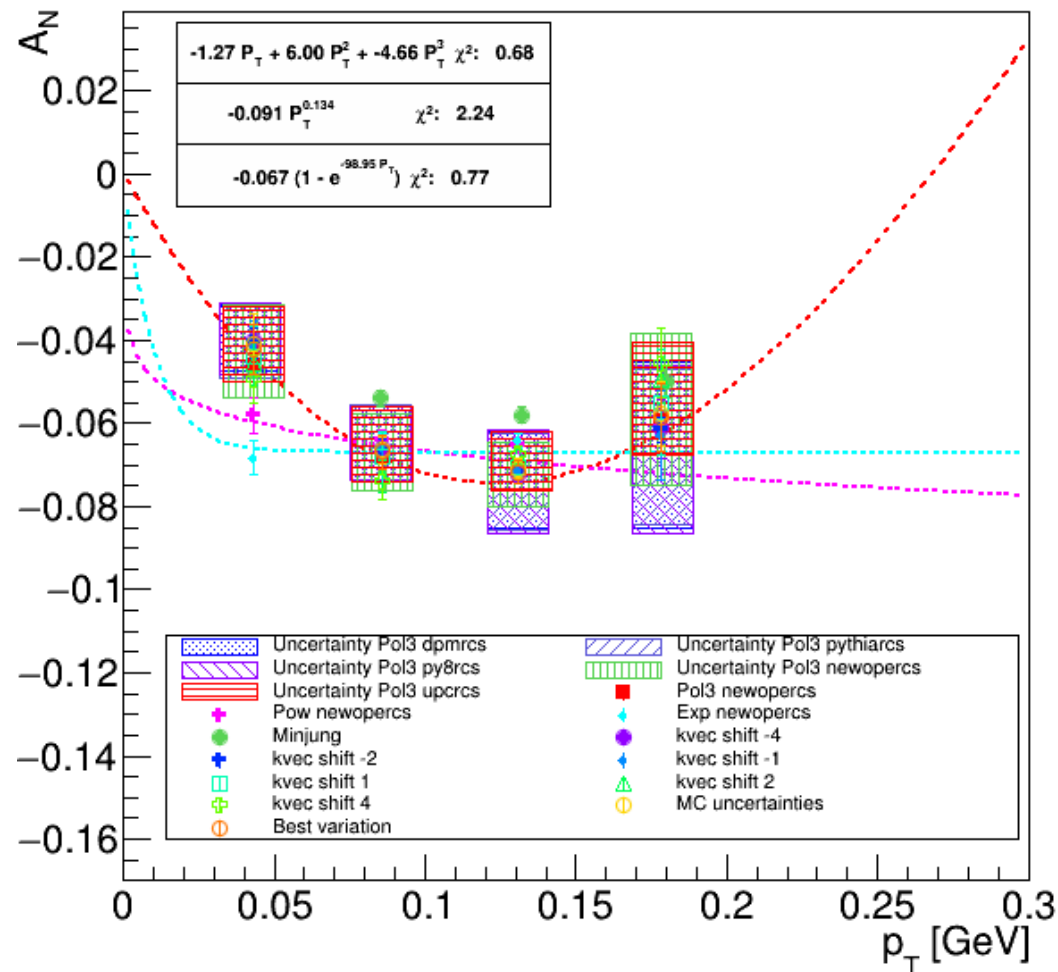
➤ Dpmjet, Pythia6, Pythia8, Ope & Upc for polynomial.

Variation of Unfolded Asymmetry Results for all Monte Carlo Samples



- Distributions of unfolded asymmetries for Dpmjet, Pythia6, Pythia8, Ope and Upc MC samples.
- Spread of unfolded results for all MC's more prominent in higher pt bins.
- The width of the RMS is to be assigned as systematic uncertainties – next slide.

Unfolded Inclusive Result Summary with **Systematic Uncertainties**



- ❖ Variation of best regularization parameter in the TSVD unfolding (**kvec shifts** $\rightarrow \pm 1, \pm 2, \pm 4$).
- ❖ Addition of uncertainties due to MC statistical uncertainties in unfolding covariance matrix via GetAdetCovMatrix (**MC uncertainties**).
- ❖ Repetition of best parametrization many times (**best variation**).
- ❖ Systematic uncertainties show the mean and Root Mean Square (RMS) for all MC repetitions.

Summary:

- ❖ Unfolding worked reasonably well with best parametrization.
- ❖ Enhancement of asymmetries has been observed.

Systematic Uncertainties studied via:

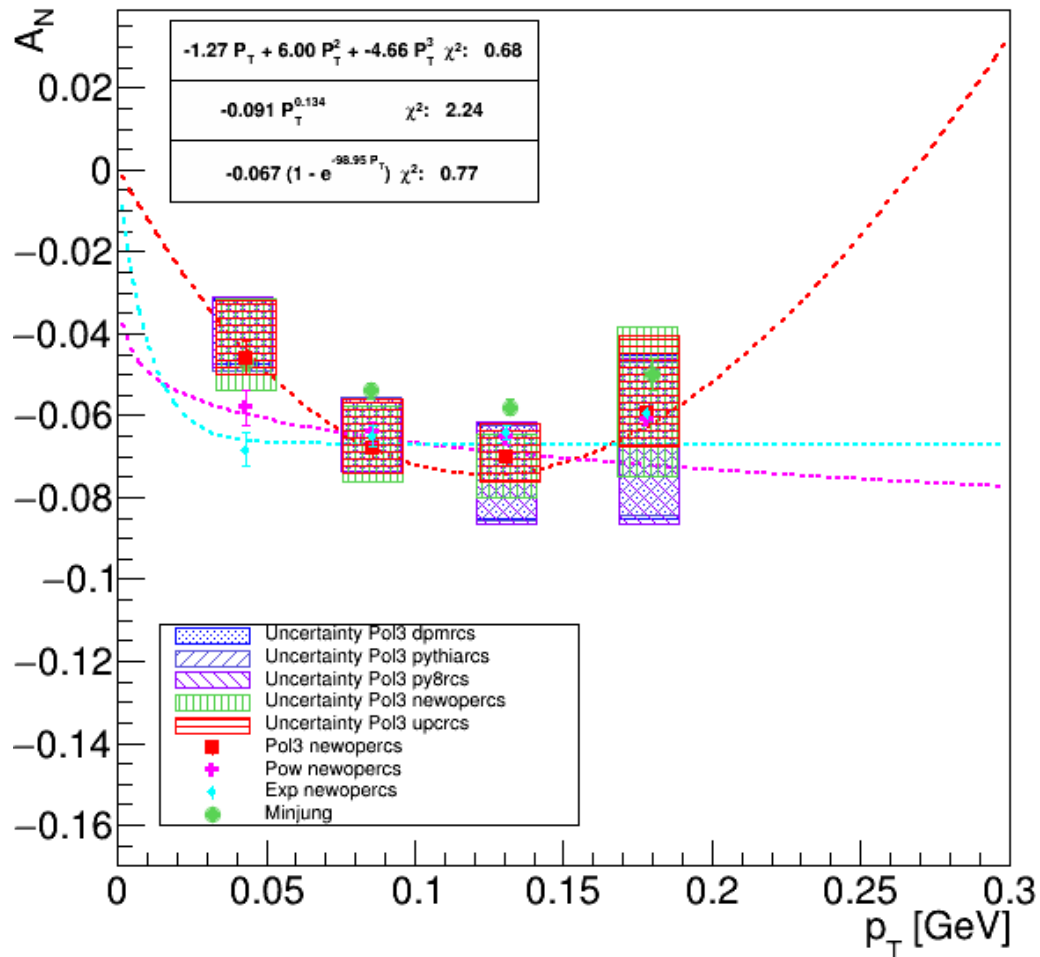
- ❖ Variation of best regularization parameter for the unfolding.
- ❖ Response matrix (MC uncertainties).
- ❖ Repetition of the best parametrizations.

- ❖ Systematic uncertainties display the mean and RMS for all MC repetitions.



BACKUP

Overall Unfolded Inclusive Result - Polynomial, Power & Exponential



➤ Overall unfolded asymmetry result

Best Chi-Square and parameters:

➤ Pol3 Chi2 = 0.68 : $b = -1.27$, $c = 6.00$, $d = -4.66$

➤ Powr Chi2 = 2.24 : $b = -0.091$, $c = +0.134$

➤ Expo Chi2 = 0.77 : $b = -0.067$, $f = -98.95$

All show reasonable χ^2 with respect to Minjung's asymmetry results.

MC uncertainties:

➤ Shown for Pol3 Dpmjet, Pythia6, Pythia8, Ope & Upc.

Algorithm

1. Create two spin states using TRandom Number Generator:
Spin up (0)
Spin down (1)
2. Create spin depended weight:

$$w = 1 + (a + b * P_{T,T} + c * P_{T,T}^2 + d * P_{T,T}^3) \cos(\varphi_T + spin * \pi)$$

the parameters are:

a = constant

b = linear

c = quadratic

d = cube

spin * pi = phase shift

spin = 0 (up)

1 (down)

Note: Other functional forms can also be scanned and tried to describe data asymmetries.

Algorithm...

3. Scan parameters for different functional forms over a wide range using chi-square based on the reconstructed asymmetries from pp collision monte carlo samples and run 15 pp asymmetry results (Minjung's result) to find the best parameter, i.e. parameter with lowest,

$$\chi^2 = \sum_i \frac{(A_{N,i}^{Minjung} - A_{N,i}^{w,reco})^2}{(\Delta A_{N,i}^{2,Minjung} + \Delta A_{N,i}^{2,w,reco})}$$

4. Extract the asymmetry using the best Chi-squared parameters,

$$A_N = \frac{N_{\Phi\uparrow} - N_{\Phi\downarrow}}{N_{\Phi\uparrow} + N_{\Phi\downarrow}}$$