

# **Proton Radius**

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- 1) Proton radius puzzle ??**
- 2) Proton radius by electron scattering**
- 3) ULQ2 project**  
**low-energy electron scattering off proton**
- 4) Conclusions**

## **1) Proton radius puzzle ??**

2) Proton radius by electron scattering

3) ULQ2 project

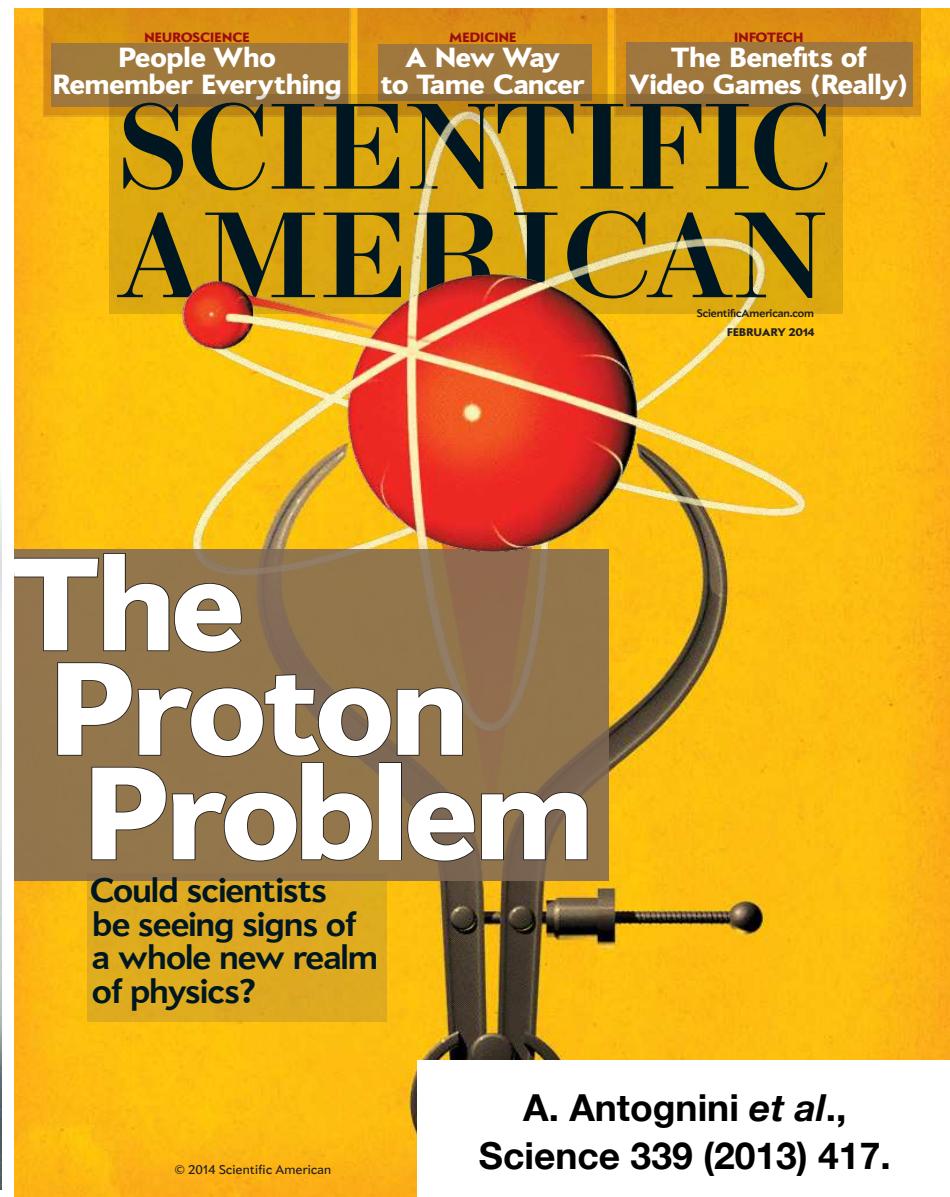
low-energy electron scattering off proton

4) Conclusions

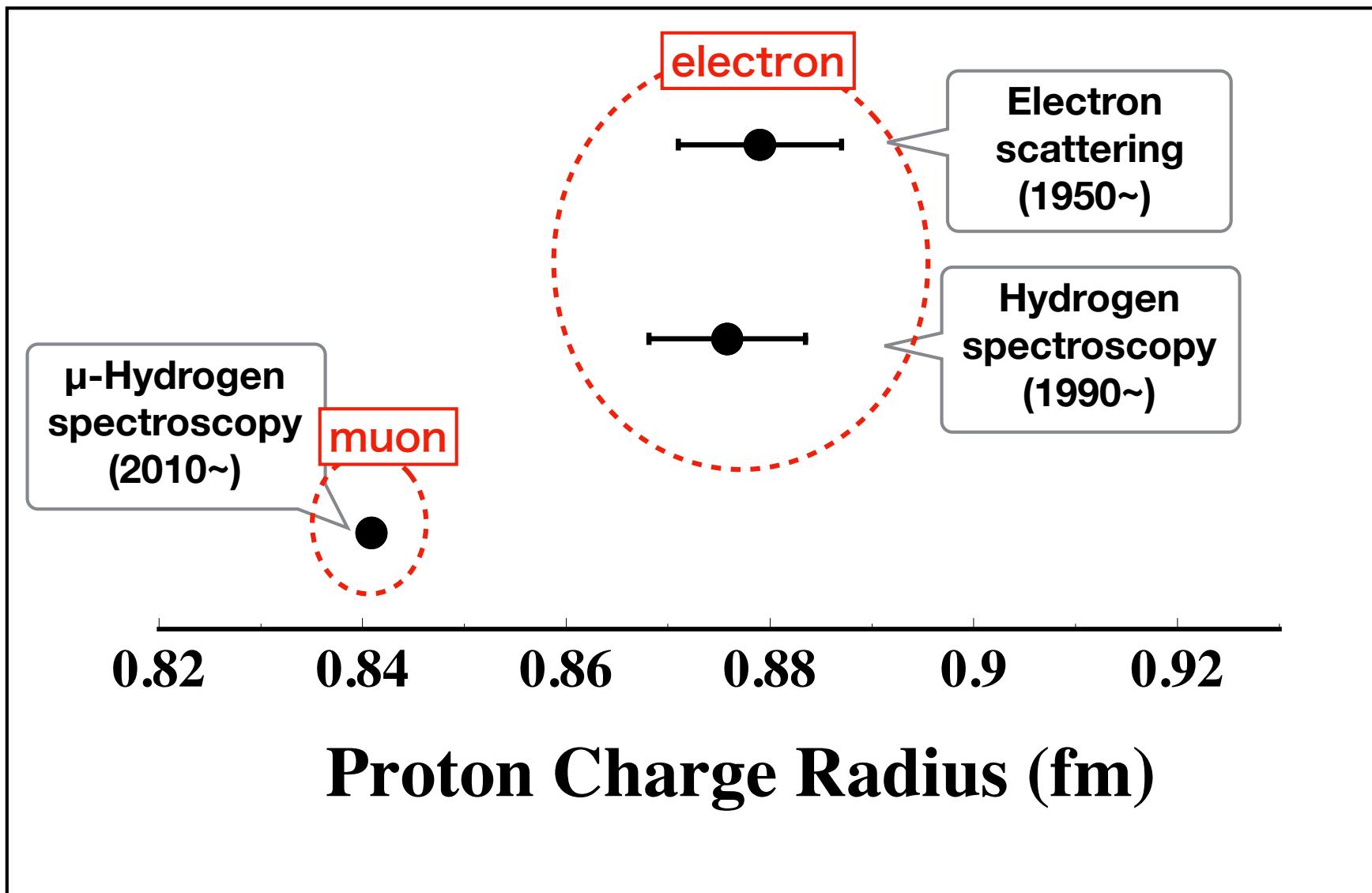
# Proton Radius Puzzle ?

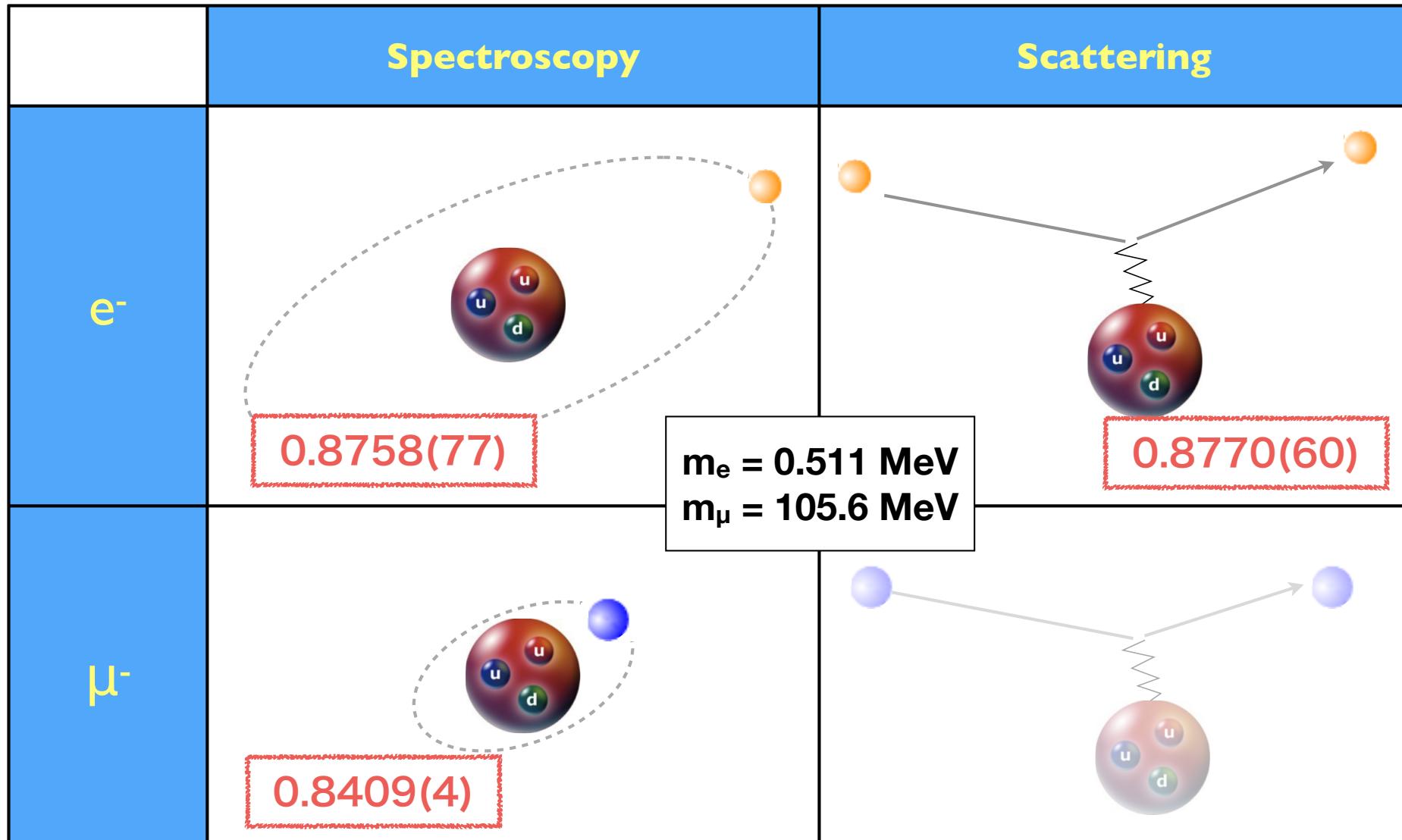
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the puzzle started in 2010



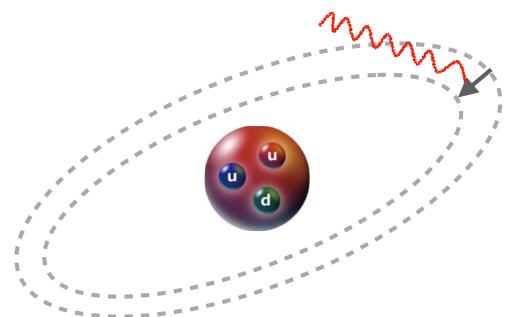
2010 ~





**1) the radius is one of the basic properties of the nucleon**

**2) the radius is strongly correlated to the Rydberg constant**



$$\Delta E = R_{Rydberg} \left( \frac{1}{n^2} - \frac{1}{m^2} \right)$$

$$\Delta E = \alpha \cdot R_{Rydberg} + \beta \cdot \langle r^2 \rangle$$

$$R_\infty = 10973\ 731.568\ \underline{539} \pm 0.000\ 055\ \text{m}^{-1}$$

$r_p$  uncertainty

**3) possible new physics beyond Standard Model (??)**

Lepton Universality ( $e \leftrightarrow \mu$ ) ??

**4) nuclear structure : (e-scatt. for exotic nuclei at RIKEN/SCRIT)**

$$\langle r_c^2 \rangle = \langle r_{pointp}^2 \rangle + \langle r_p^2 \rangle + \frac{N}{Z} \langle r_n^2 \rangle + \text{rel. corr.}$$

exp.      theory      p radius      n radius

# Proton Charge Radius ??

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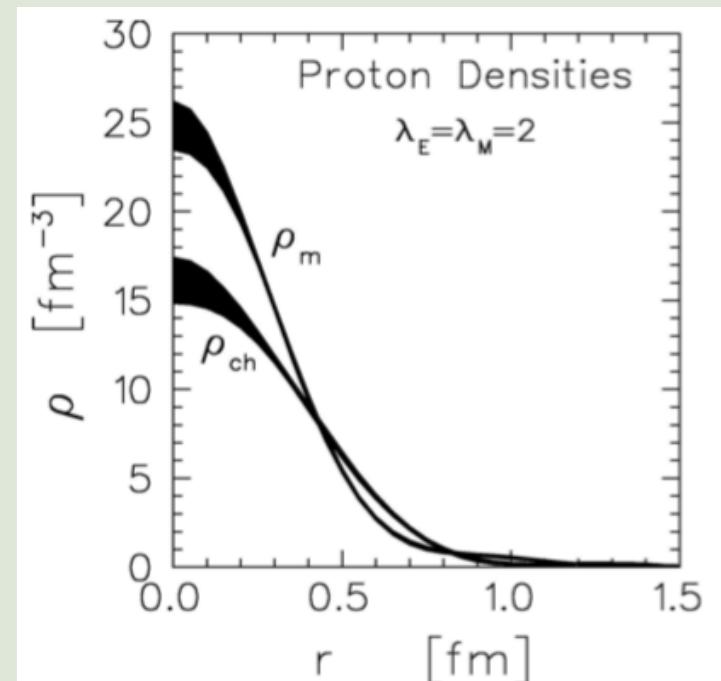
$$r_p^2 = \int r^2 \rho(\vec{r}) d\vec{r}$$

$$F(Q_L^2) = \int \rho(\vec{r}) e^{i \vec{Q}_L \cdot \vec{r}} d\vec{r}$$

$Q_L$  Lab. value of momentum transfer

*“applies in the non-relativistic limit in which  $\rho(r)$  is the static density distribution”*

R. Hofstadter (1951)



J. J. Kelly, Phys. Rev. C70 (2004) 068202

Relativistically proper definition

$$r_p^2 = -6 \frac{dG_E(0)}{dQ^2} \Big|_{Q^2 \rightarrow 0}$$

G. A. Miller Phys. Rev. C99 (2019) 035202

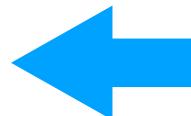
## Hydrogen spectroscopy

- 1) Garching : 2S->4P (Science 358 (2017) 79.)
- 2) Paris : 1S->3S (PRL 120 (2018) 183001.)
- 3) Tronto : 2S->2P (Science 365 (2019) 1007.)

## Electron scattering

- 1) Mainz : PRC90 (2014) 15206.
- 2) PRad@JLAB : Nature 575 (2019) 147.

ULQ2 at Tohoku (2021 ~)



e-p scattering at MESA

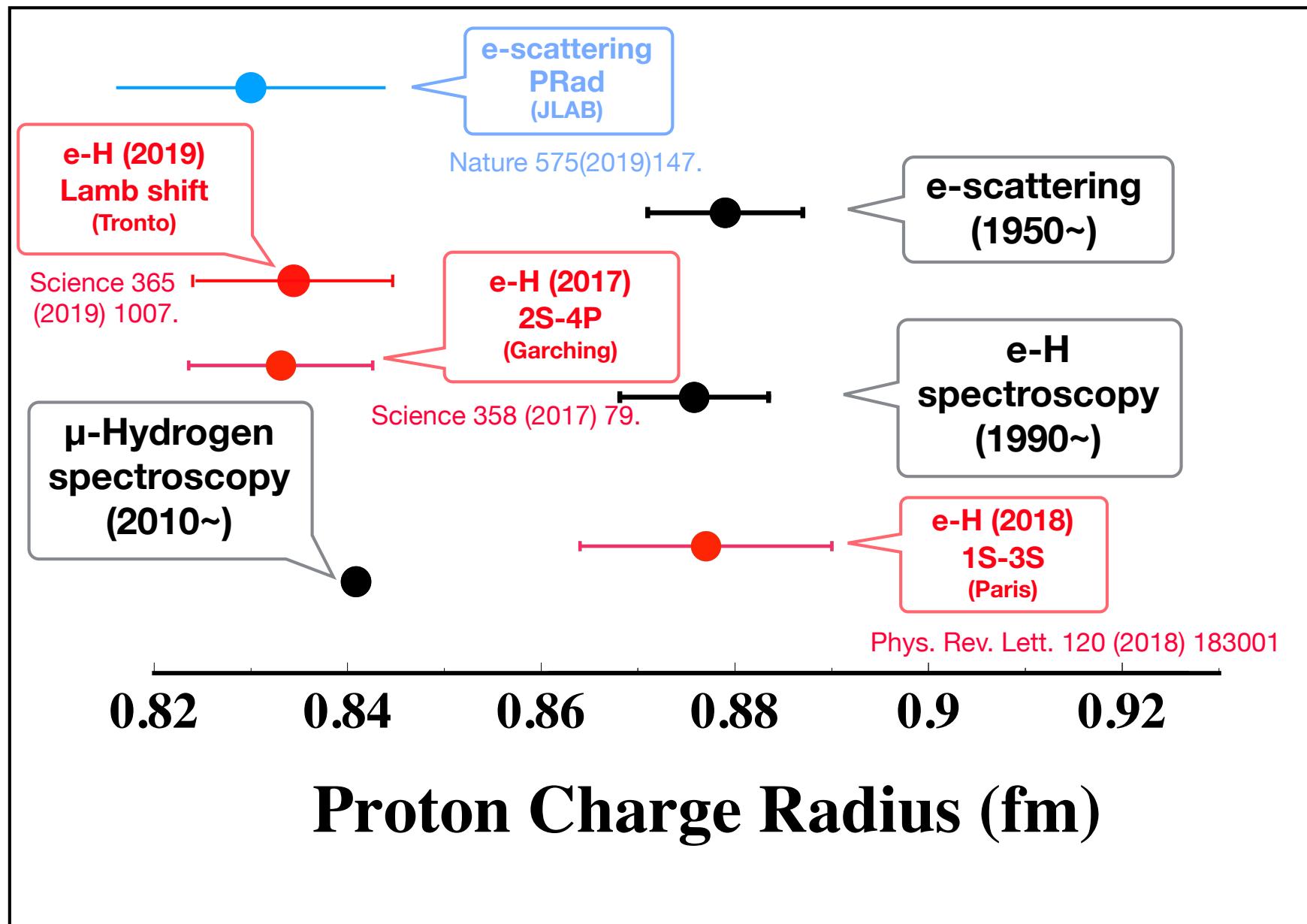
## Muon scattering

MUSE@PSI (2020~)

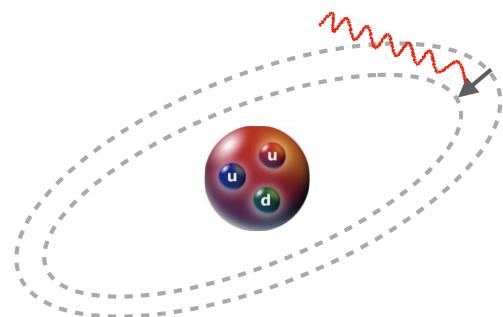
LowQ2- $\mu$ p@COMPASS (proposal)

# Proton radius as of today

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- 1) the radius is one of the basic properties of the nucleon
- 2) the radius is strongly correlated to the Rydberg constant



$$\Delta E = R_{Rydberg} \left( \frac{1}{n^2} - \frac{1}{m^2} \right)$$

$$\Delta E = \alpha \cdot R_{Rydberg} + \beta \cdot \langle r^2 \rangle$$

$$R_\infty = 10973\ 731.568\ \underline{539} \pm 0.000\ 055\ \text{m}^{-1}$$

$r_p$  uncertainty

- 3) possible new physics beyond Standard Model (??)

Lepton Universality ( $e \leftrightarrow \mu$ ) ??

???

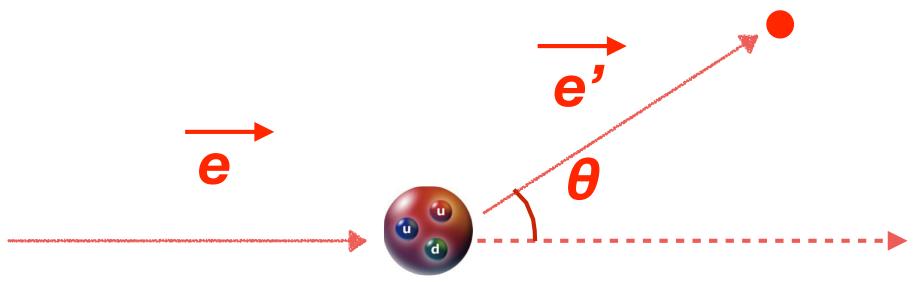
- 4) nuclear structure : (e-scatt. for exotic nuclei at RIKEN/SCRIT)

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# Electron scattering

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**momentum transfer**

$$\vec{q} = \vec{e} - \vec{e}'$$

**energy transfer**

$$\omega = e - e'$$

**4 momentum transfer**

$$Q^2 = q^2 - \omega^2$$

$$= 4 e e' \sin^2(\theta/2)$$

Charge FF      Magnetic FF

$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{Mott} \frac{G_E^2(Q^2) + \frac{\tau}{\epsilon} G_M^2(Q^2)}{1 + \tau}$$

$$\left( \frac{d\sigma}{d\Omega} \right)_{Mott} = \frac{z^2 \alpha^2}{4e^2} \frac{\cos^2(\theta/2)}{\sin^4(\theta/2)} \propto \frac{e^2}{q^4}$$

$$\epsilon = \frac{1}{1 + 2(1 + \tau) \tan^2 \frac{\theta}{2}}$$

$$\tau = \frac{Q^2}{4m_p^2}$$

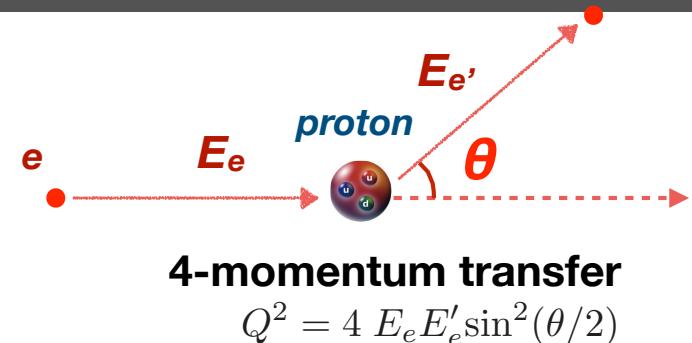
# Proton radius by electron scattering

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## elastic cross section for e-p

$$\frac{d\sigma}{d\Omega} \propto G_E^2(Q^2) + \alpha(\theta) G_M^2(Q^2)$$

Charge FF                      Magnetic FF



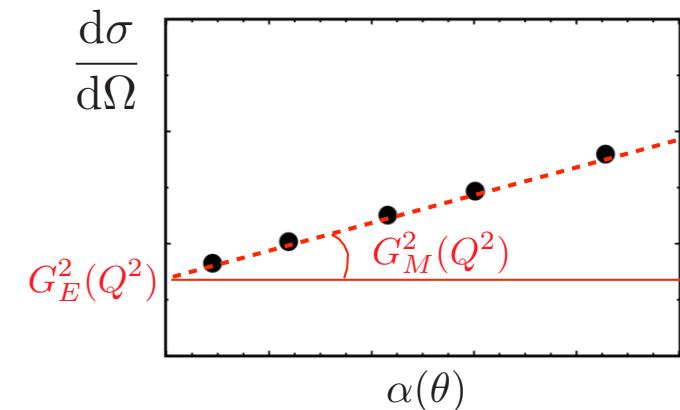
## $G_E(Q^2)$ extraction from cross section

vary  $\theta$  under fixed  $Q^2$

$$Q^2 = 4 E_e E'_e \sin^2(\theta/2)$$

Rosenbluth separation

Frequent change of  $E_e$   
("small" accelerator)

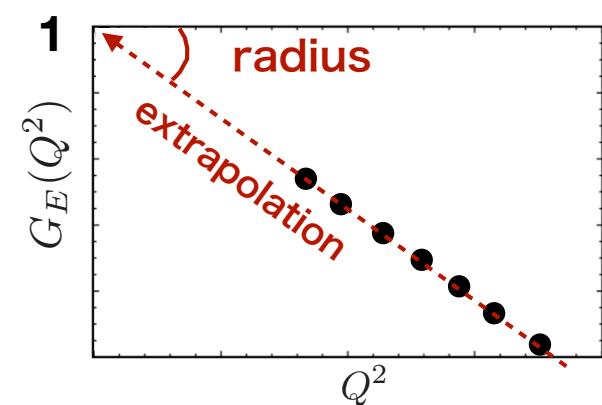


## Proton charge radius

$$\langle r^2 \rangle \equiv -6 \frac{dG_E(Q^2)}{dQ^2} \Big|_{Q^2 \rightarrow 0}$$

low  $Q^2$  region as possible

low- $E_e$  (or small  $\theta_e$ )

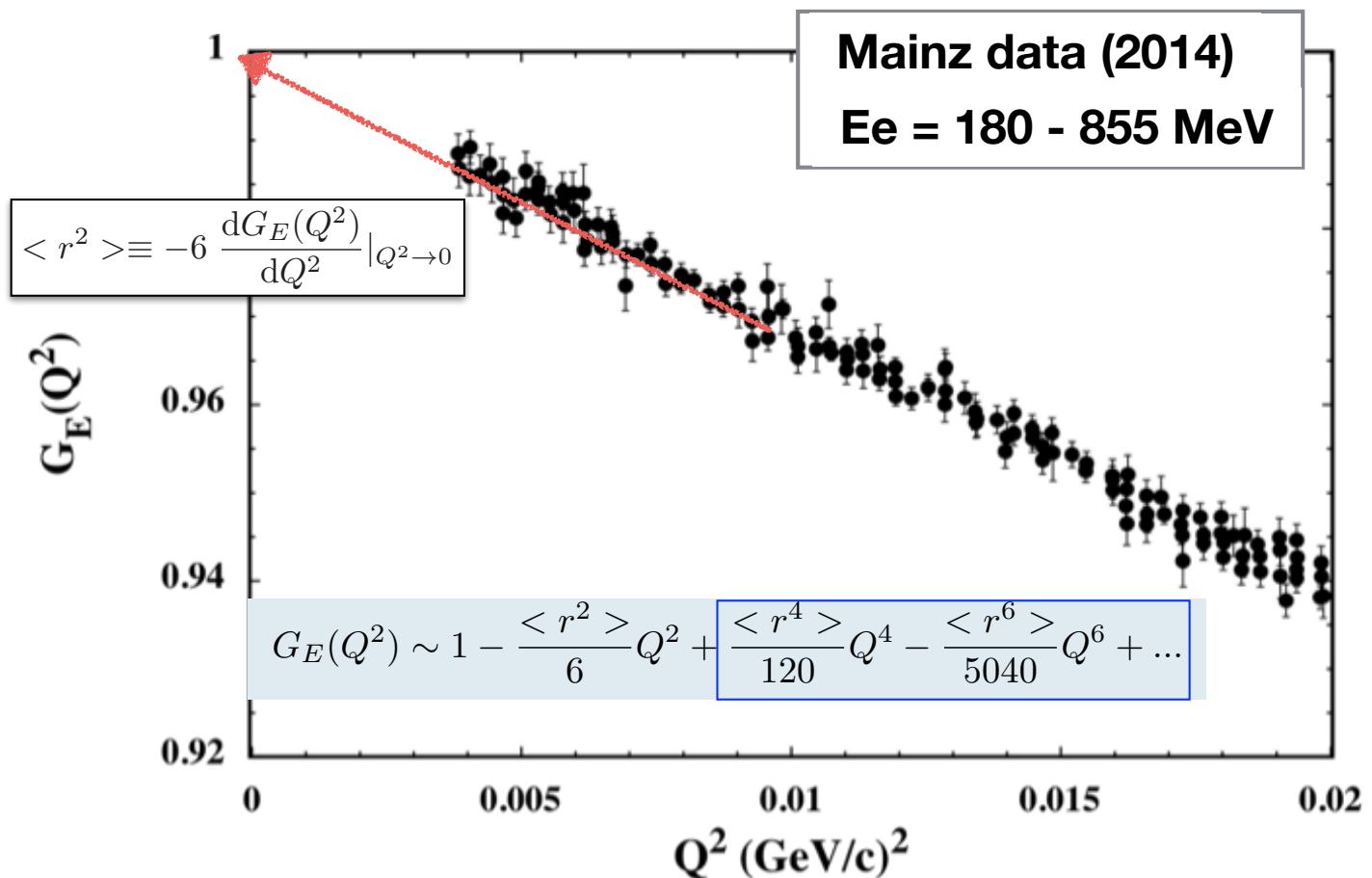


same for magnetic radius

$$\langle r_M^2 \rangle \equiv -6 \frac{dG_M(Q^2)}{dQ^2} \Big|_{Q^2 \rightarrow 0}$$

# Recent Mainz data (2014)

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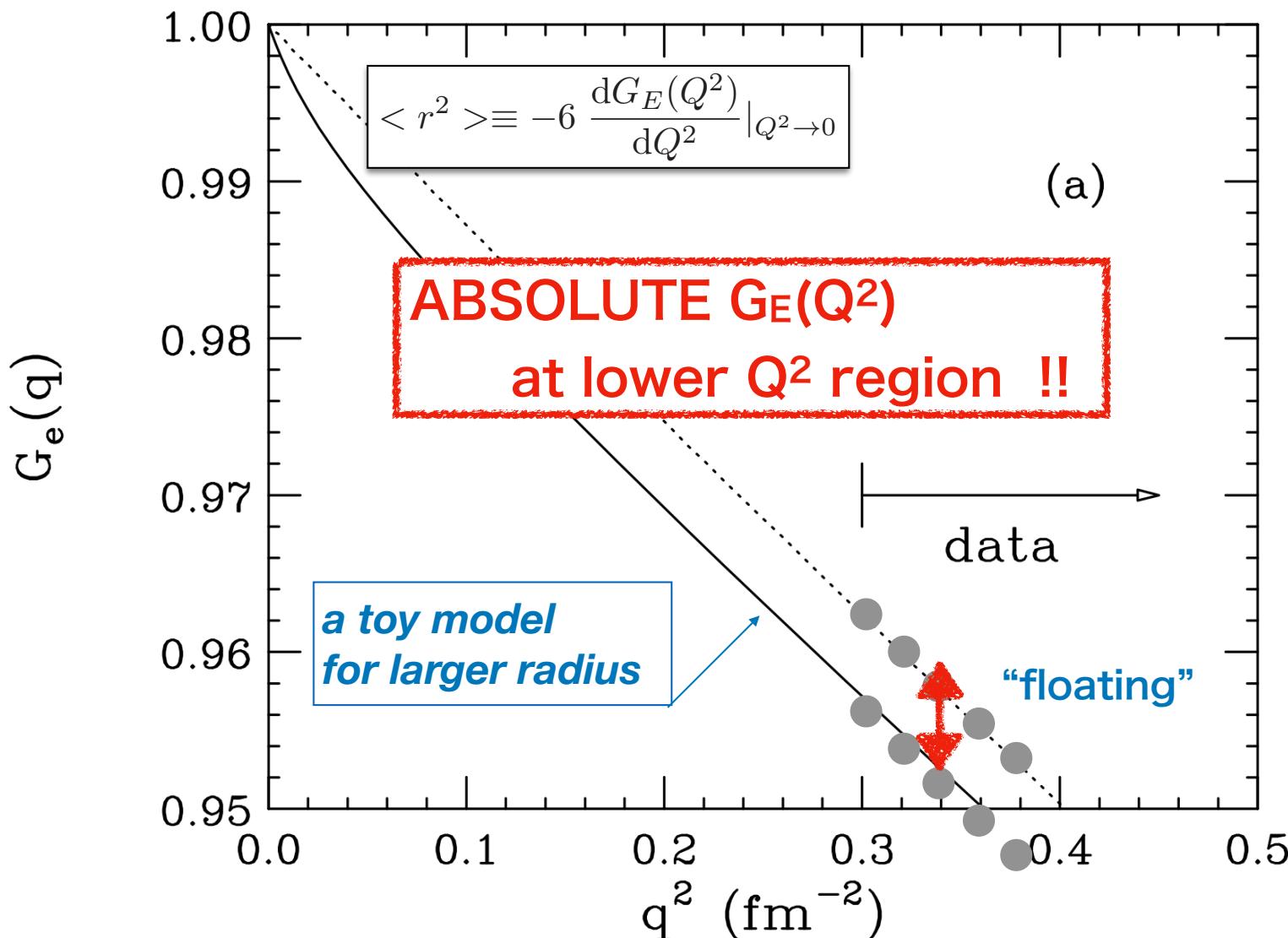


no “ultra-“ low $Q^2$ data	min. $E_e = 180 \text{ MeV}$
no Rosenbluth separation	no frequent change of $E_e$
no absolute cross section	liq. $H_2$ target + spectrometer

# Absolute $G_E(Q^2)$ at lower $Q^2$ region

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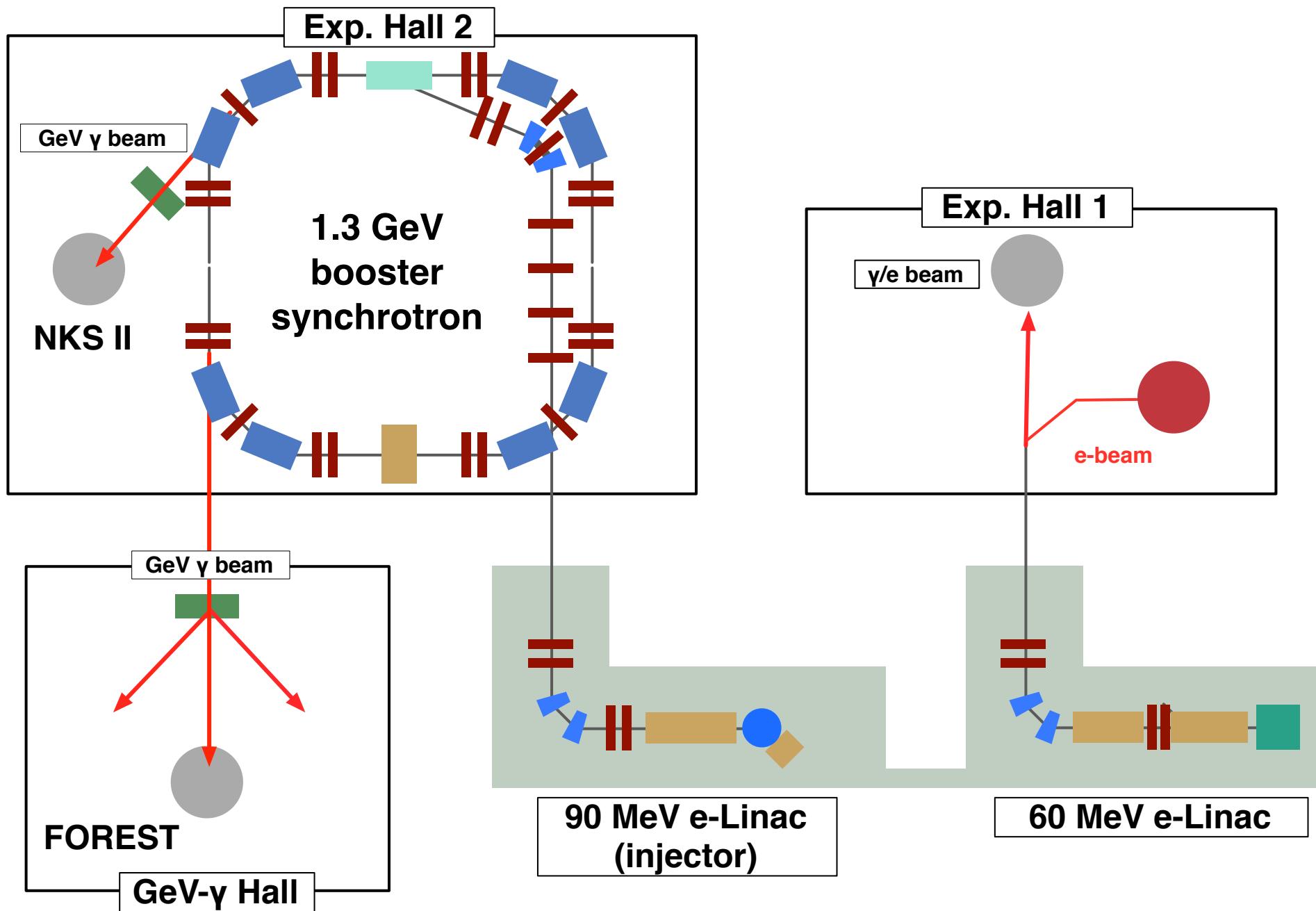
- 1) no absolute  $G_E(Q^2)$  (“floating”)
- 2)  $\chi^2$  is quite similar



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- 3) **ULQ2 project**  
**low-energy electron scattering off proton**
- 4) Conclusions

## ULQ<sup>2</sup> collaboration (Ultra-Low Q<sup>2</sup>)





## 研究基盤装置：電子加速器

## 全国共同利用・共同研究拠点



国内最大級ビームパワー ~10 kW

大学施設としては国内最大エネルギー

## 現状

### 全国共同利用・共同研究拠点

年間延べ 1000 人以上の電子光ビームユーザー（ハドロン・原子核、RI）

- 1) ~ 60 MeV 制動輻射ガンマ線： RI 生成
- 2) ~ 1 GeV 单色ガンマ線、電子（陽電子）ビーム：ハドロン物理、検出器開発
- 3) ~ 60 MeV 電子散乱（世界唯一）：原子核研究 => 近い将来、共同利用に提供



## 研究

1.3 GeV : ハドロン物理 : ダイバリオン、ハイパー核、検出器開発

60 MeV : 原子核物理 : 陽子電荷半径

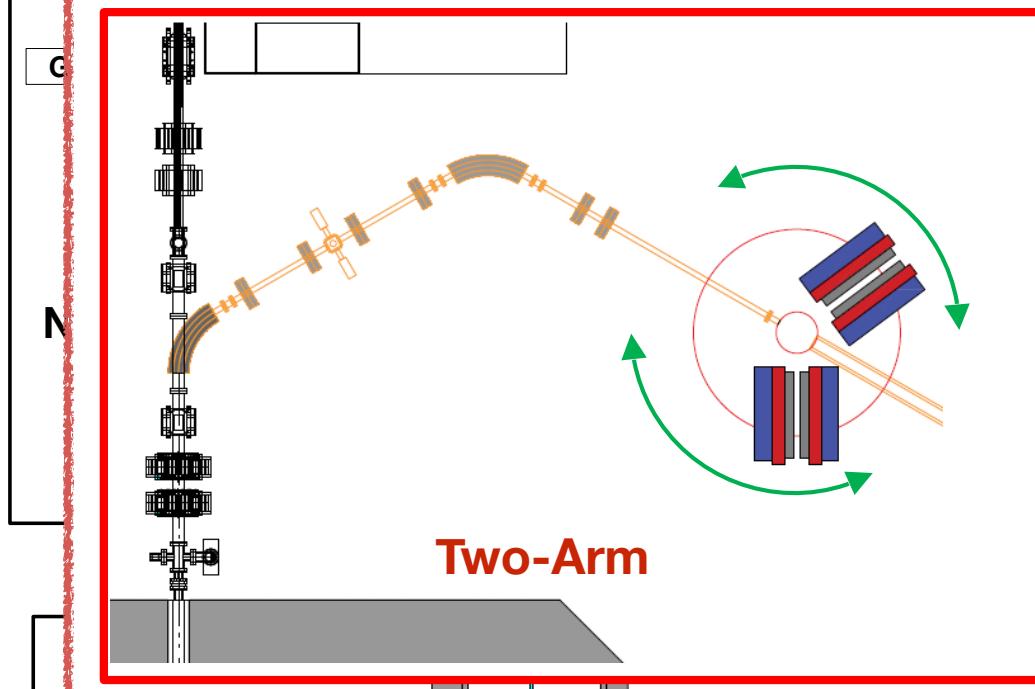
RI : 核医学用有用RI を含む RI 光生成 (イオンビームと相補的)



Low energy electron beam :  $E_e = 20 - 60 \text{ MeV}$

the lowest- $E_e$  ever employed for electron scattering off proton

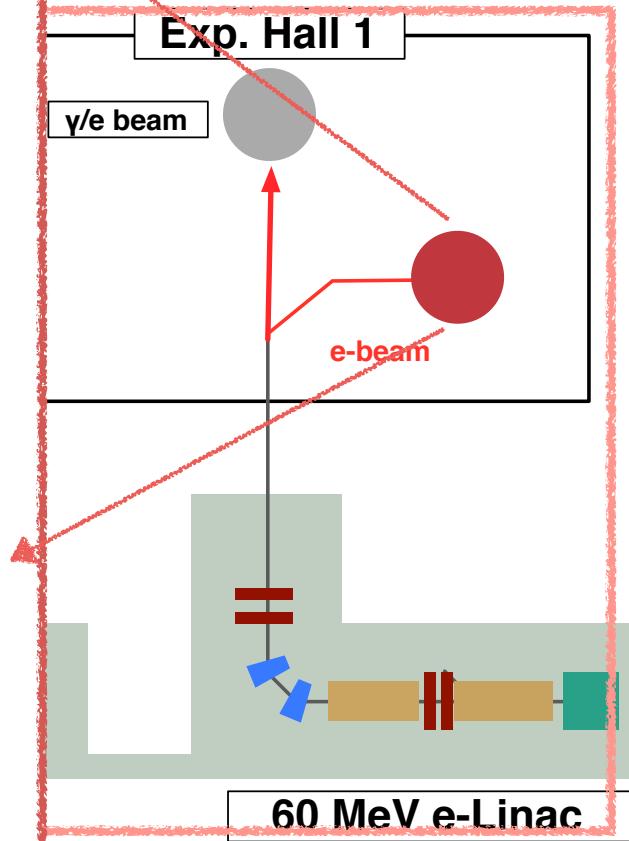
## New beam line + Spectrometers



$E_e = 20 - 60 \text{ MeV}$   
 $I_e = 1 \text{ nA} - 0.1 \mu\text{A}$   
beam size on target  $\leq 1 \text{ mm}$   
 $\Delta p/p \leq 10^{-3}$

New beam line  
New spectrometer

for ULQ2 exp.

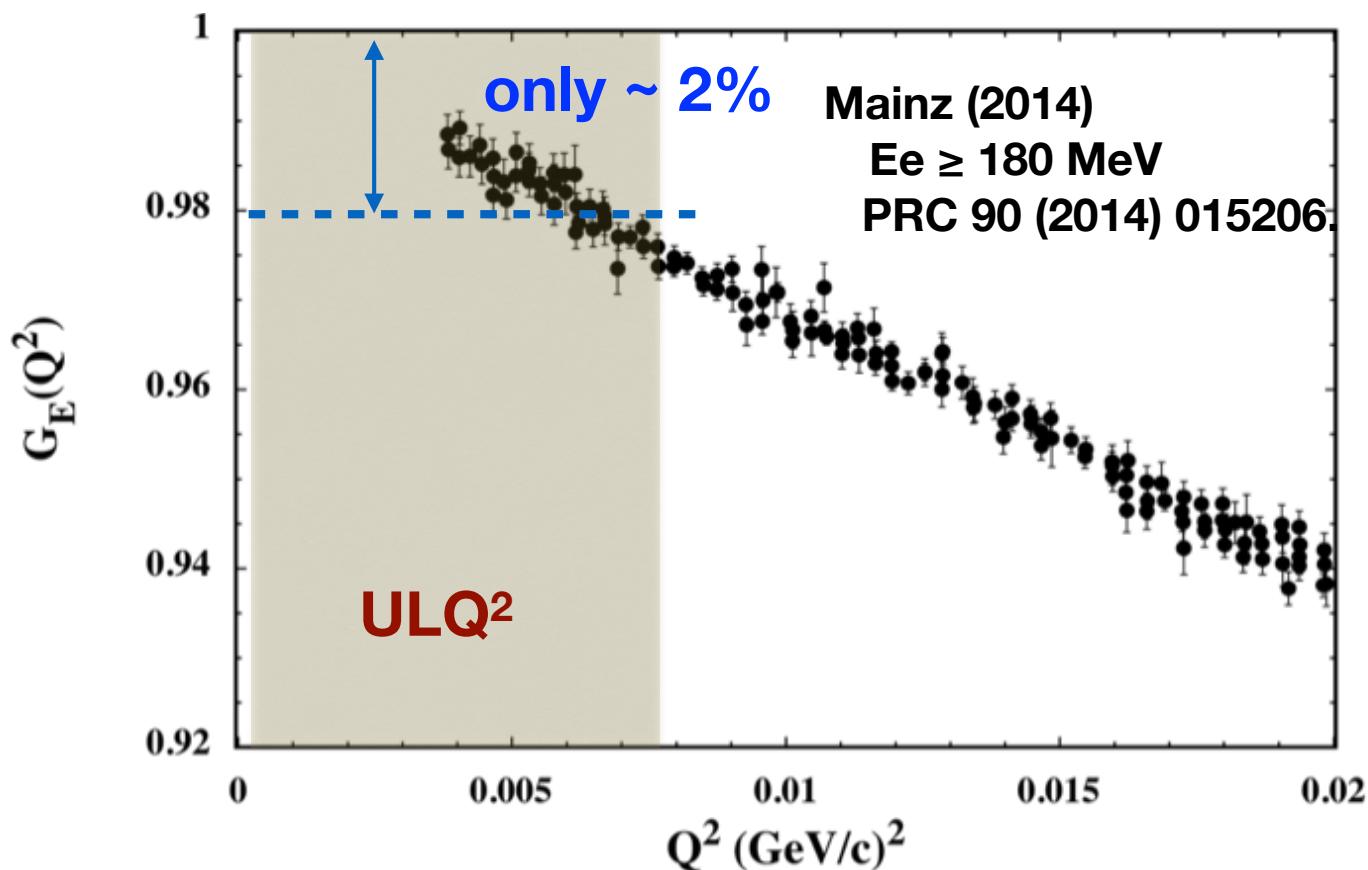


1)  $G_E(Q^2)$  measurements at  $0.0003 \leq Q^2 \leq 0.008 (\text{GeV}/c)^2$

2) Absolute cross section measurement with  $10^{-3}$  precision

3) Rosenbluth separated  $G_E(Q^2)$ ,  $G_M(Q^2)$

Exp. @ Tohoku Low-Energy Electron Linac ( $E_e = 20 - 60 \text{ MeV}$ )



# e-scattering off proton at ultra-low $Q^2$ region

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## Goal of our experiment

**$G_E(Q^2)$  measurements in  $0.0003 \leq Q^2 \leq 0.008 \text{ (GeV/c)}^2$**

## Our experiments

**Low-energy electron scattering**

**Absolute cross section measurement**

**Rosenbluth separation ( $G_E(Q^2)$ ,  $G_M(Q^2)$ )**

## accelerator, instruments

**Tohoku low-energy electron linac + experimental hall**

**$20 \leq E_e \leq 60 \text{ MeV}$**

**$30 \leq \theta \leq 150^\circ$**

**$\Delta p/p \sim 10^{-3}$**

**new beam line + double-arm spectrometer**

## Challenges

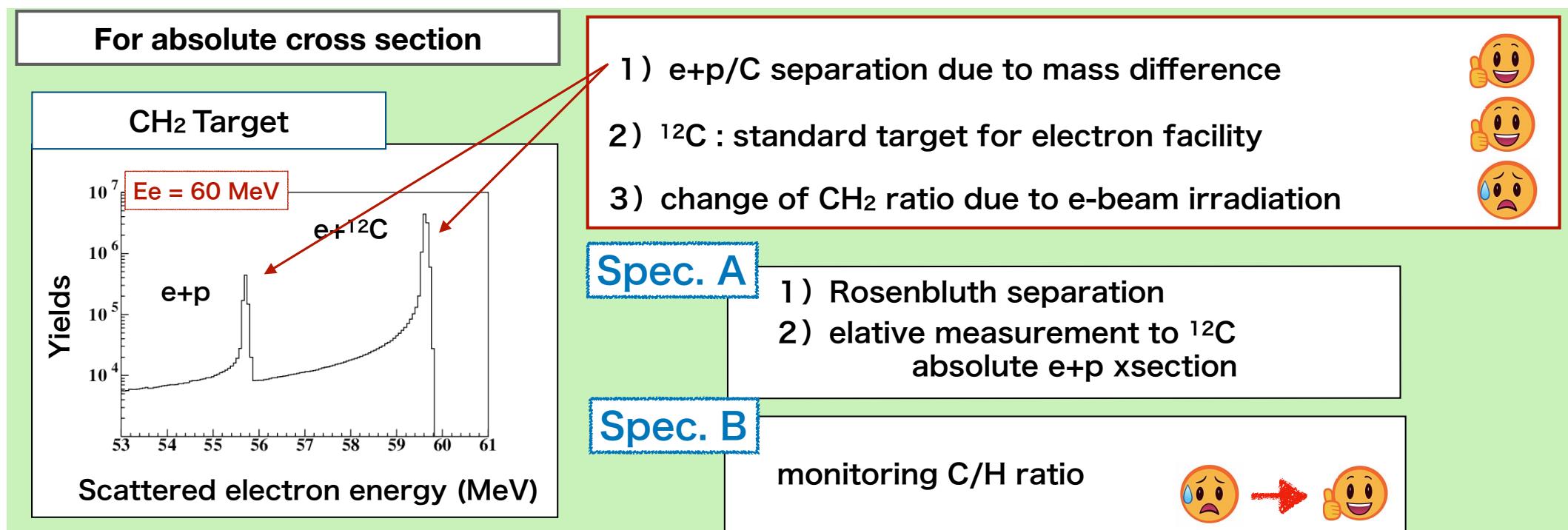
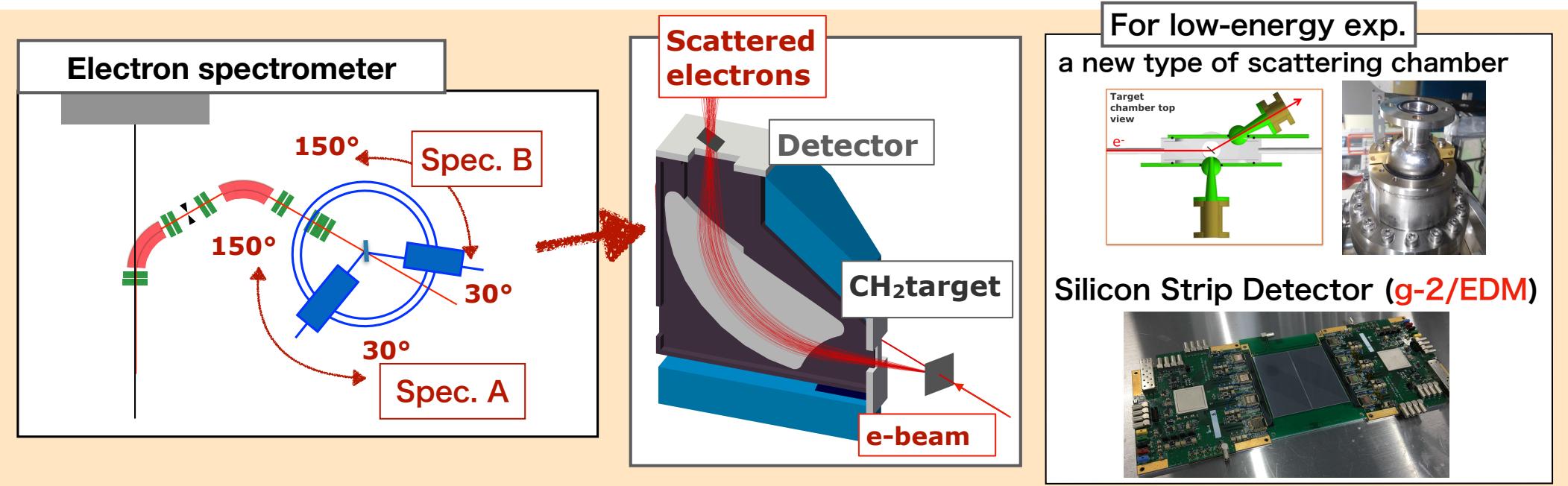
**Absolute cross section ( $G_E(Q^2)$ ) with  $10^{-3}$  accuracy**

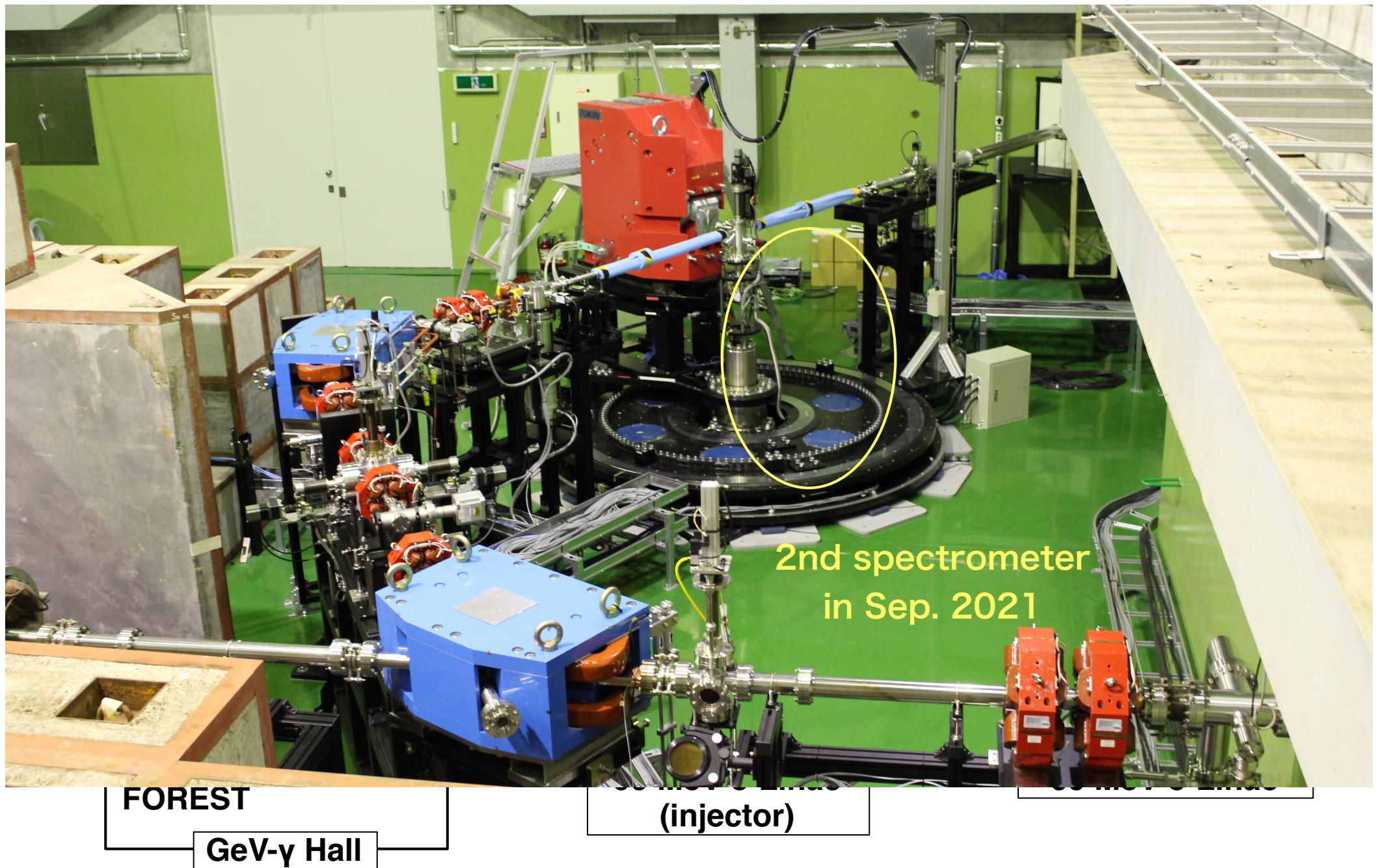
**experimental challenges for measurement**

**theoretical challenges for interpretation**

# Electron Spectrometer

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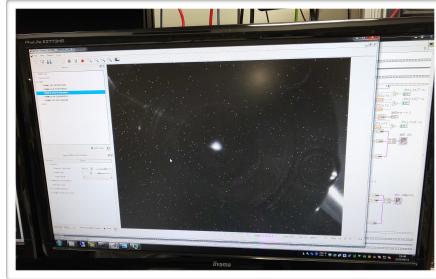




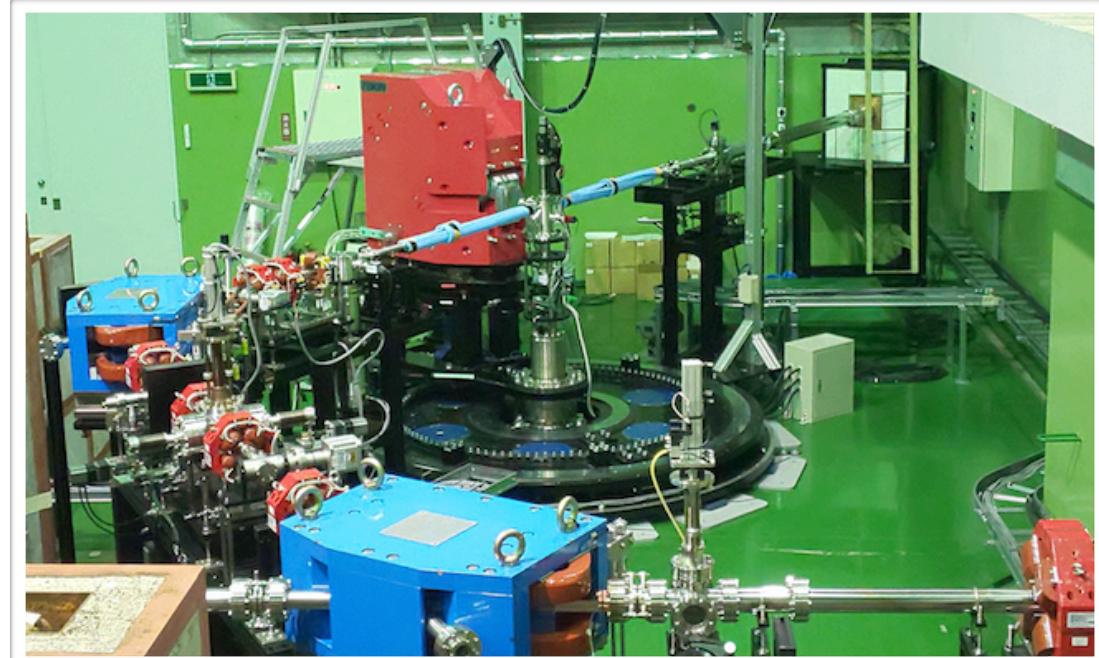
# ULQ2 beam line

# First Beam at the new beam line

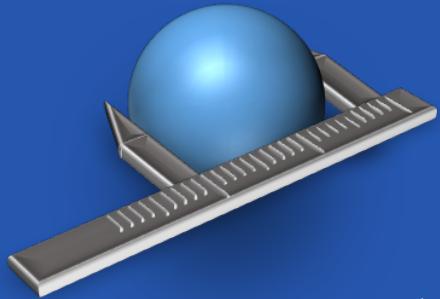
## Sep. 11, 2020



2020年  
9月11日

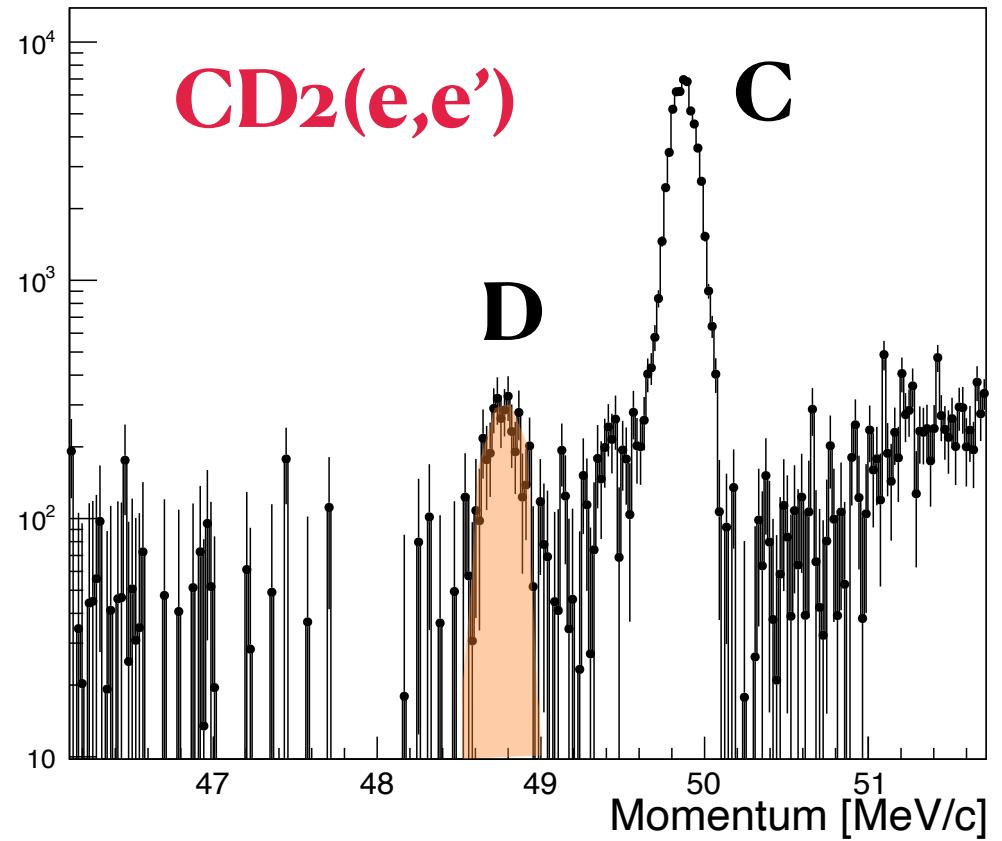
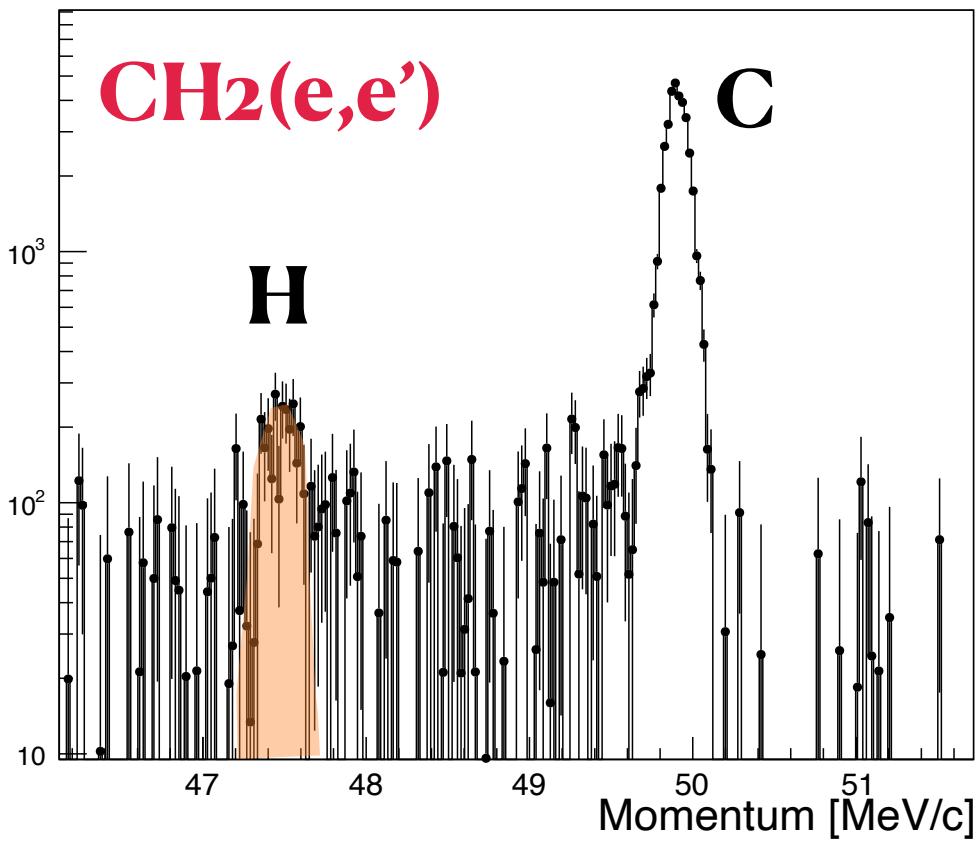


“First-Beam” beer で乾杯



# *First observation of elastic $e+p$ and $e+d$ events*

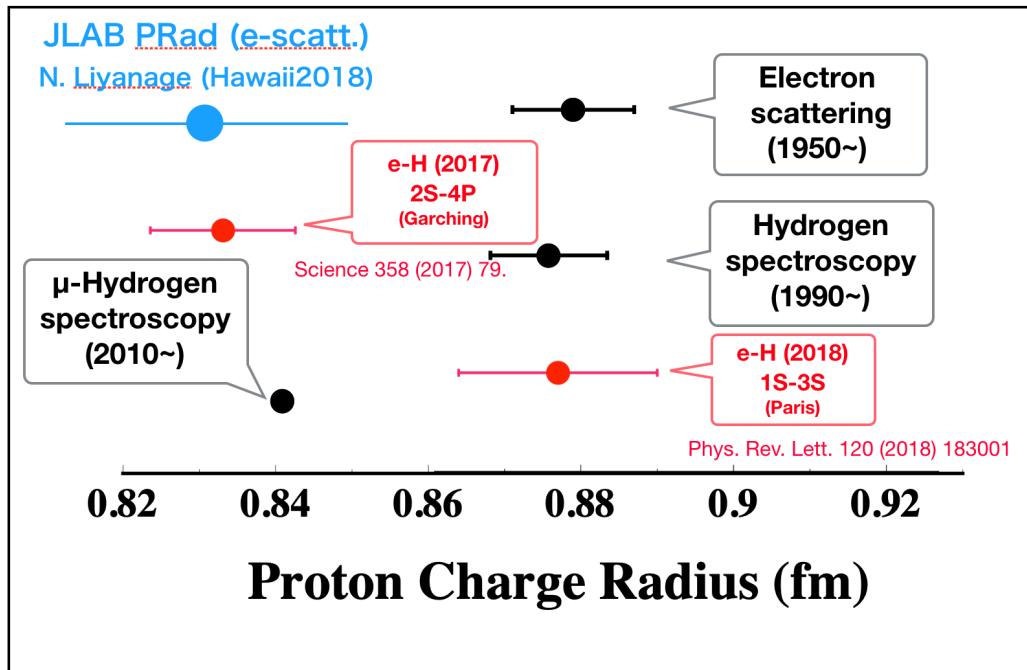
$Ee = 50 \text{ MeV}$ ,  $\theta e = 90^\circ$





Nov. 19, 2020

## Proton Charge Radius Puzzle ??



- disagreements : not yet understood.
- the “correct” proton radius is important.
- further experimental and theoretical efforts.

e-scattering : PRad (JLAB), ULQ2 (Tohoku), MESA (Mainz)  
 $\mu$ -scattering : MUSE (PSI), COMPASS (CERN)