



# パルサー星雲電波放射の 乱流加速モデル

Shuta J. Tanaka  
Aoyama Gakuin Univ.

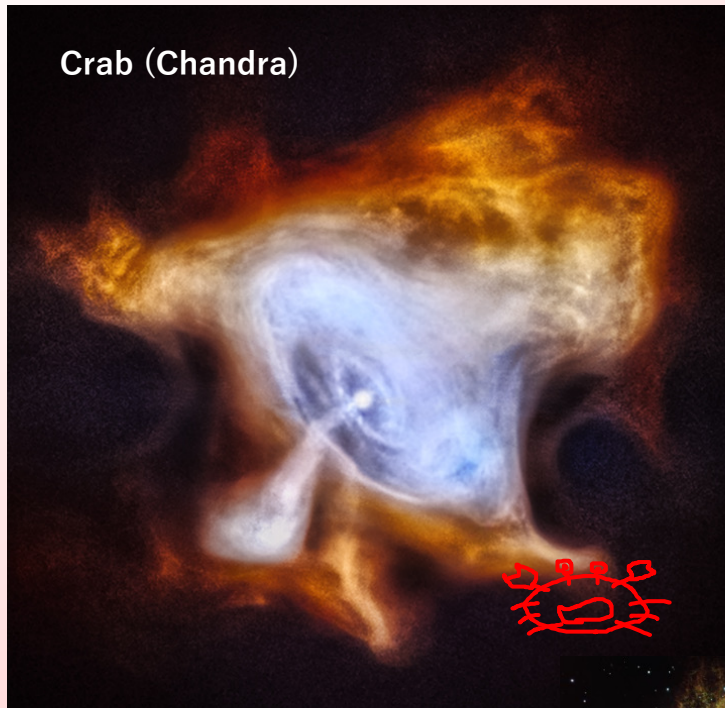
# Introduction

# PSR/PWN/SNR systems

pulsars

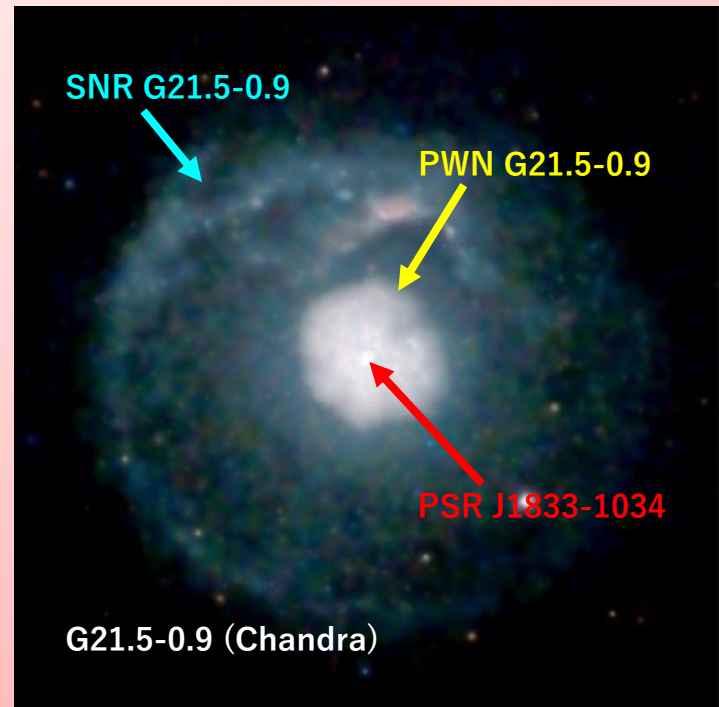
pulsar  
wind  
nebula

supernova  
remnant



Crab (Chandra)

powered by pulsars



SNR G21.5-0.9

PWN G21.5-0.9

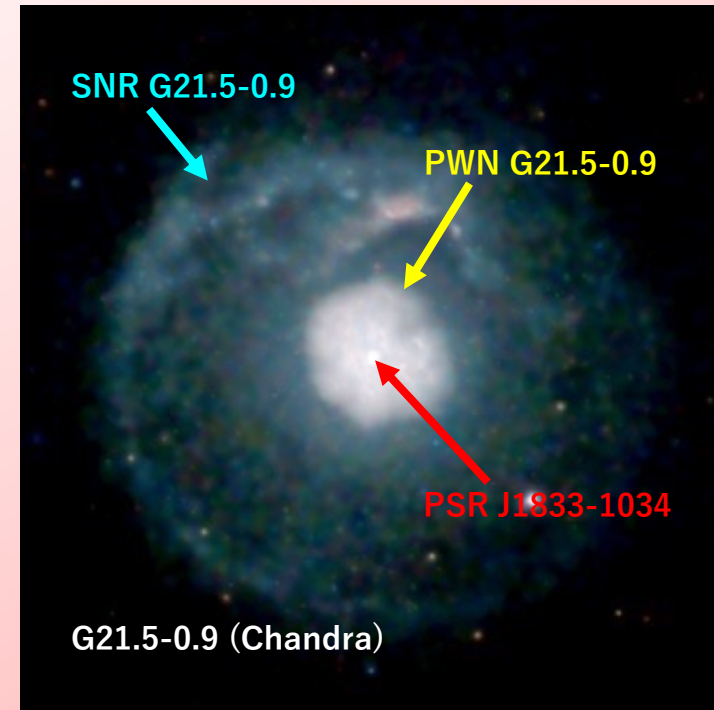
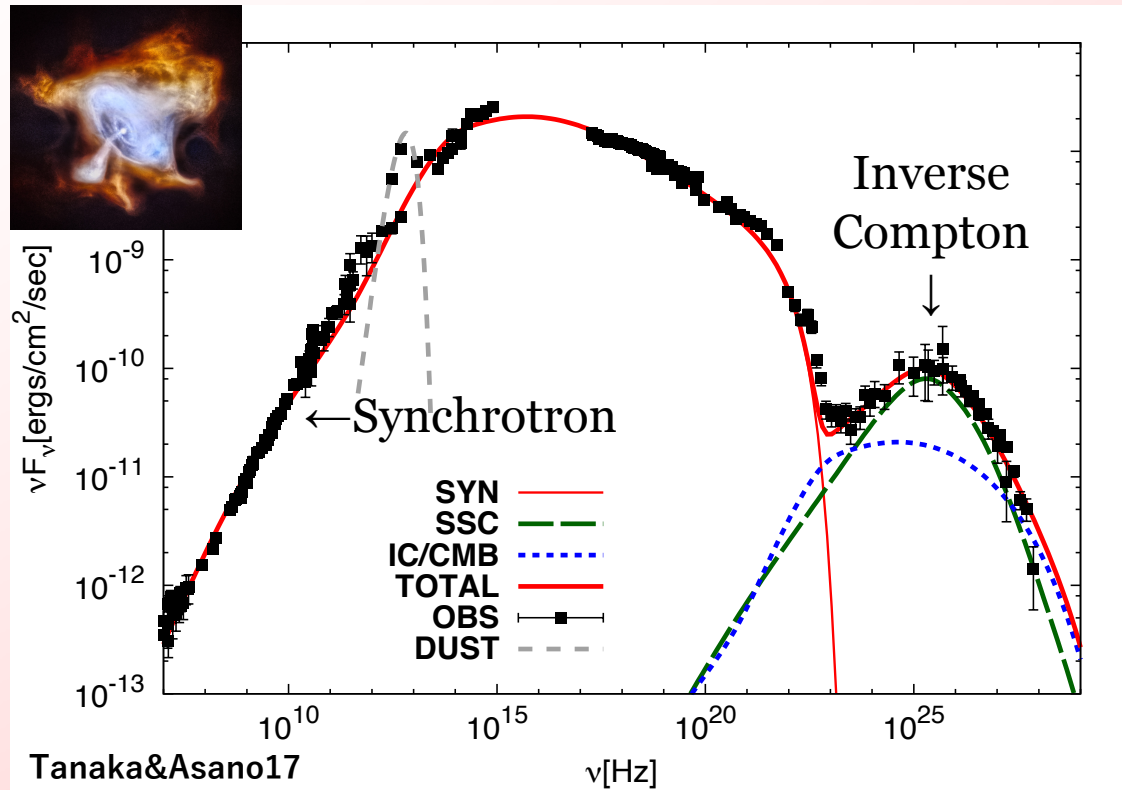
PSR J1833-1034

G21.5-0.9 (Chandra)

confined by SNR

# PWN as Particle Accelerator

Broadband emission from radio to TeV.



Typical electron energy @  
optical peak is  $\sim$  TeV

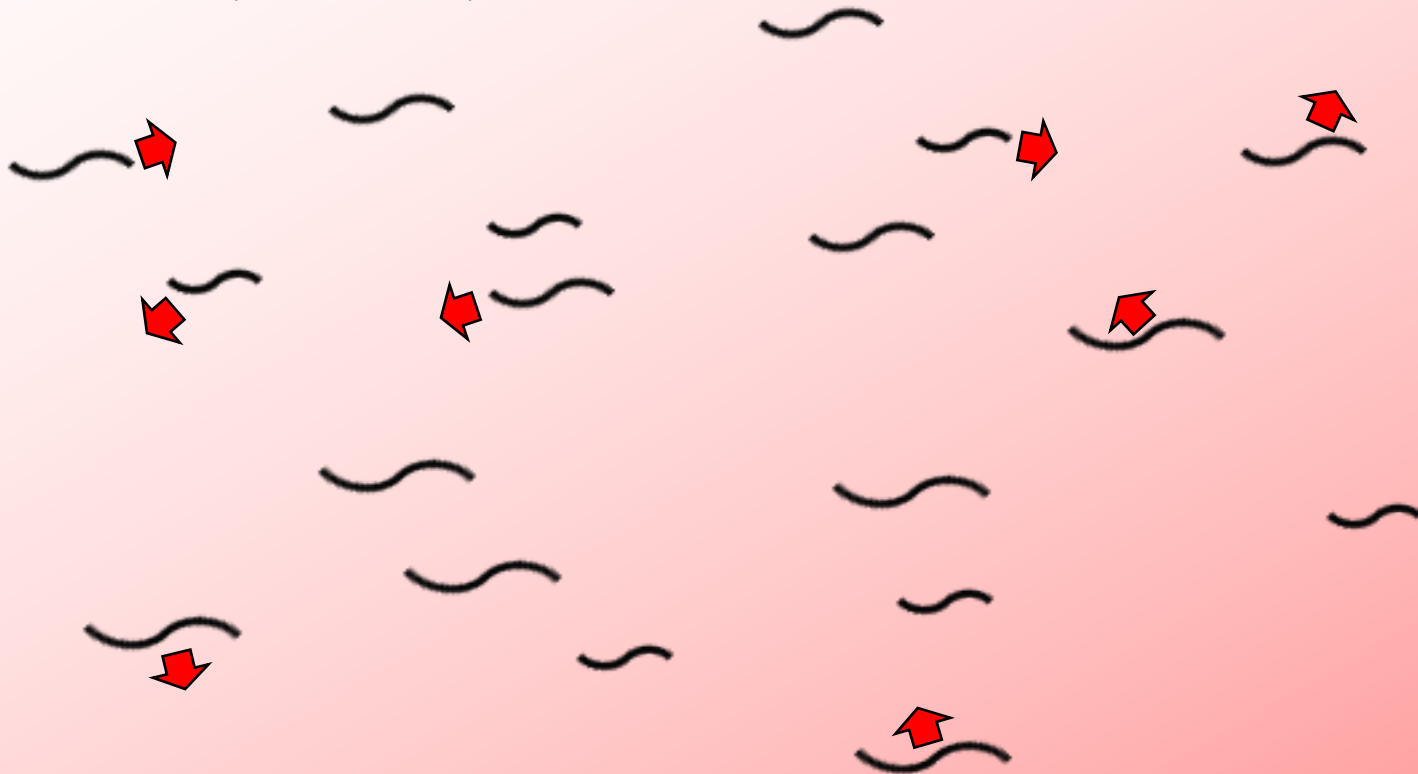


extremely hot (energetic)  
and rarefied plasma cloud  
( $n_{\text{PWN}} < 10^{-6} \text{ cm}^{-3}$ )

**Closest relativistic object**

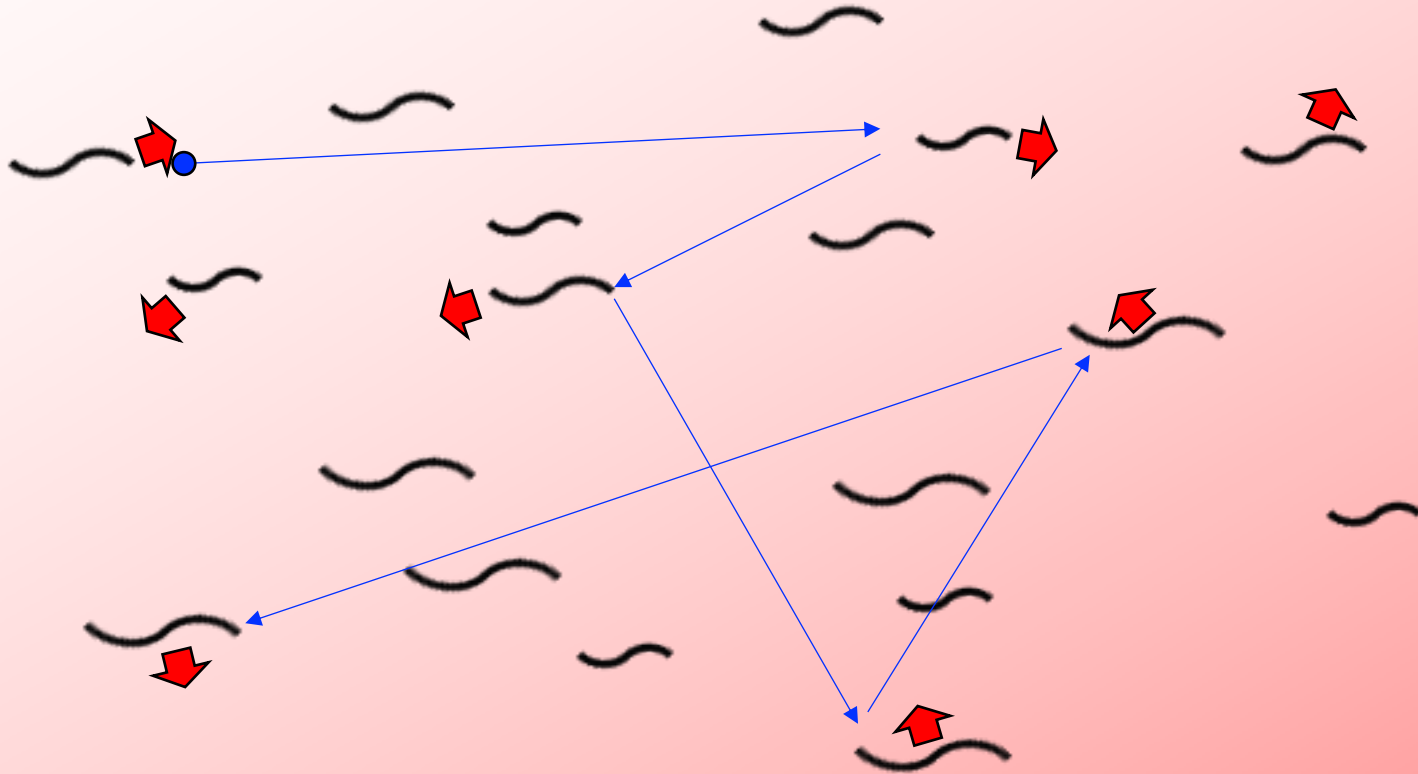
# Particle Acceleration = Mechanism to form non-thermal particle distribution

Stochastic Acceleration  
(2<sup>nd</sup> order Fermi acceleration)  
by random waves (turbulence)



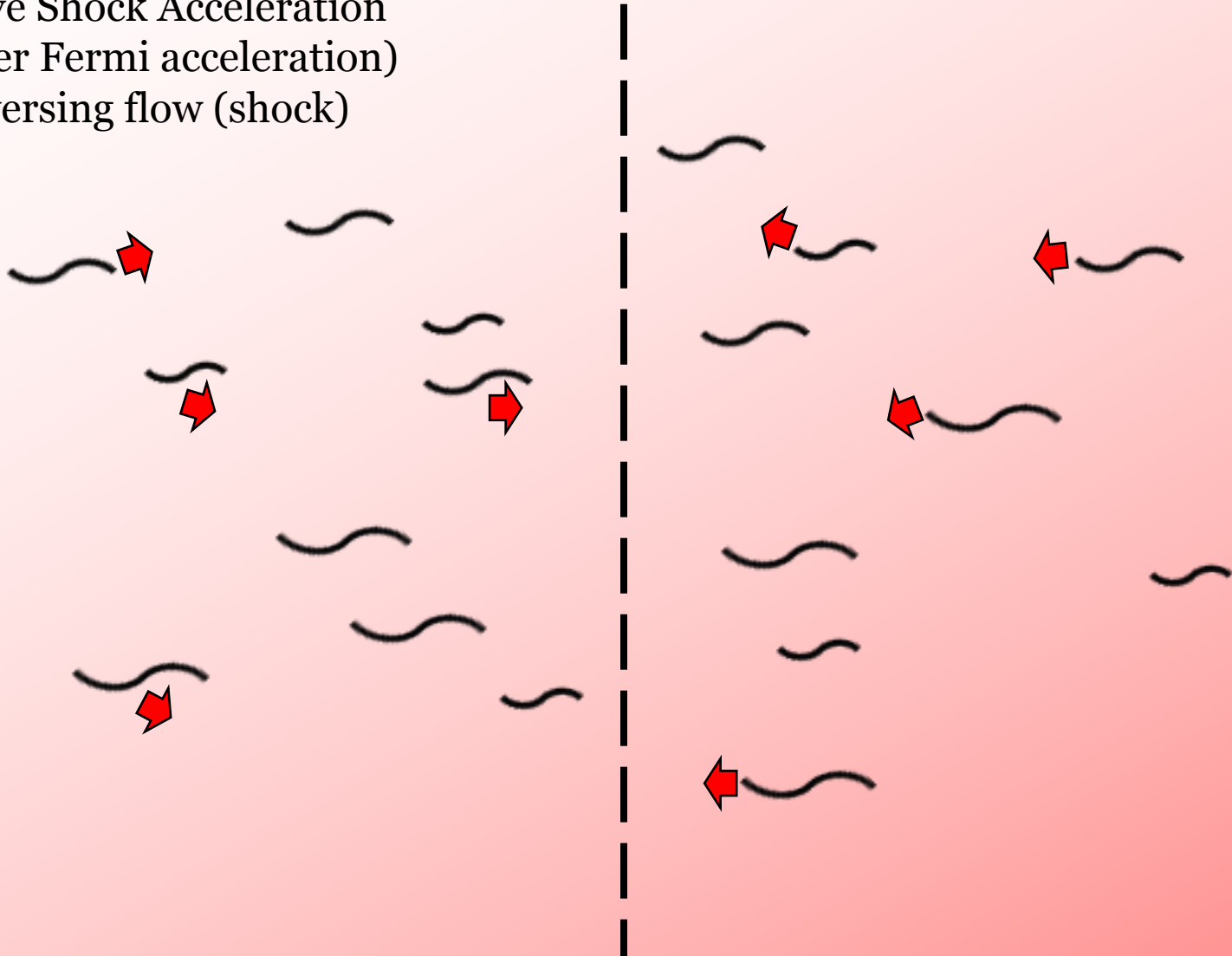
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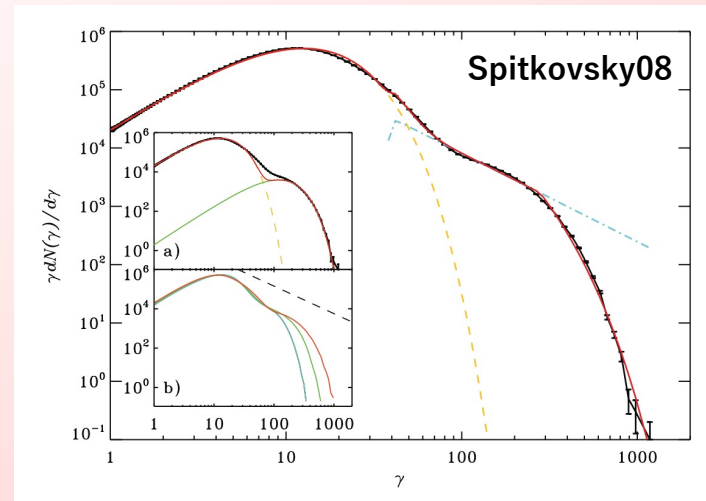
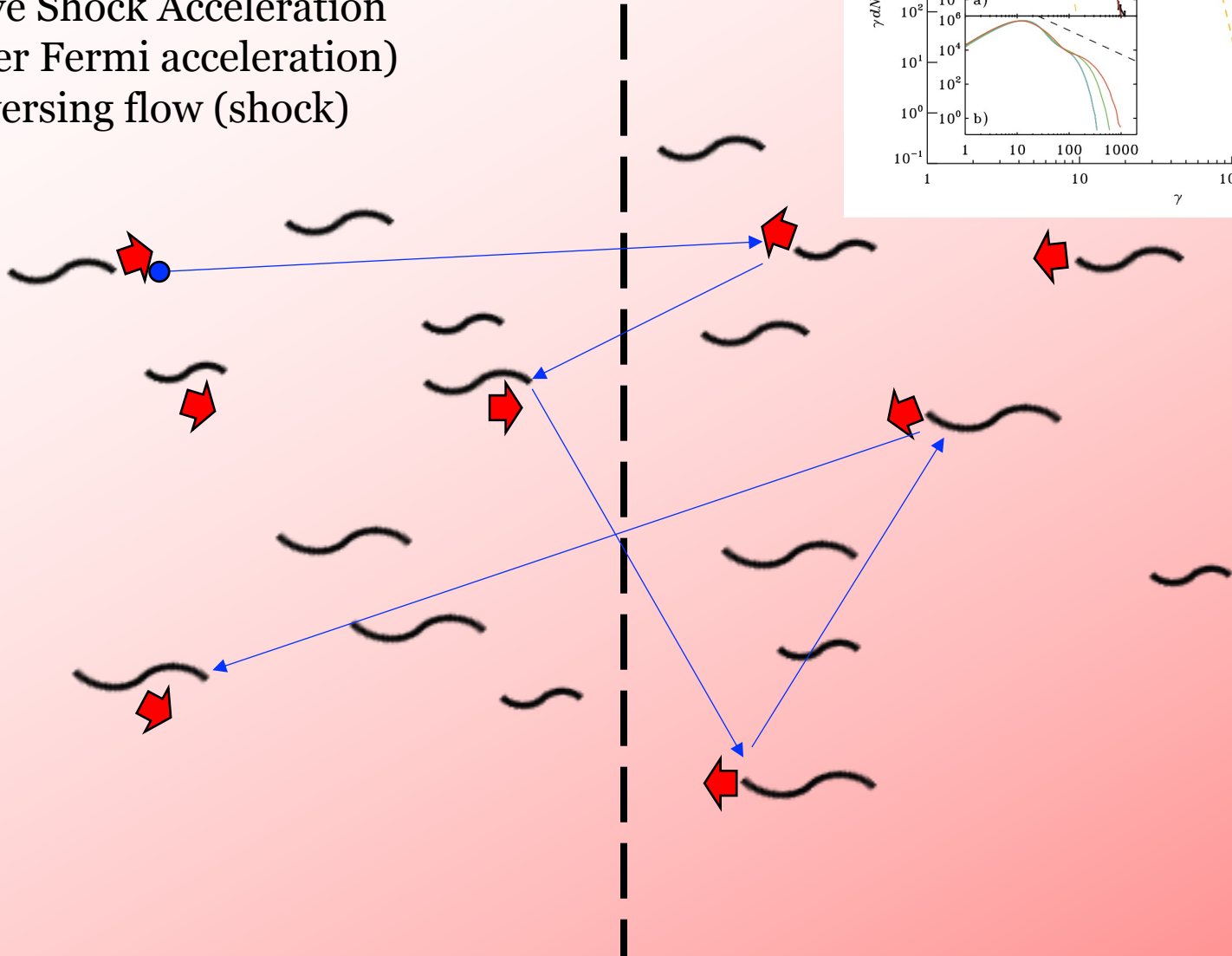
# Particle Acceleration

Diffusive Shock Acceleration  
(1<sup>st</sup> order Fermi acceleration)  
by converging flow (shock)



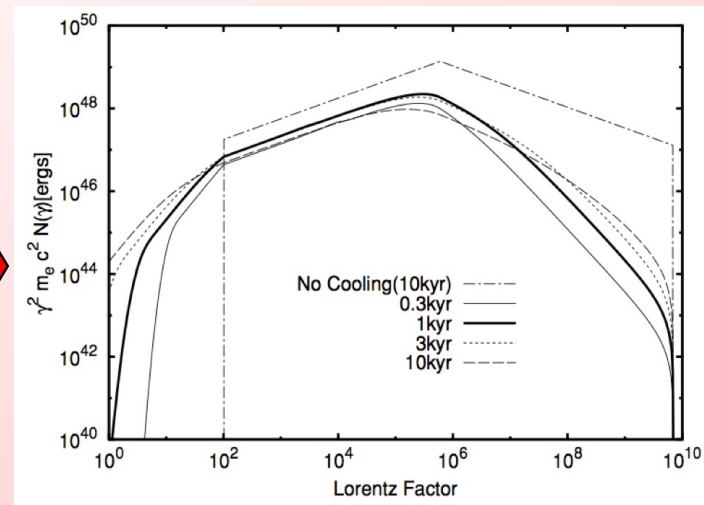
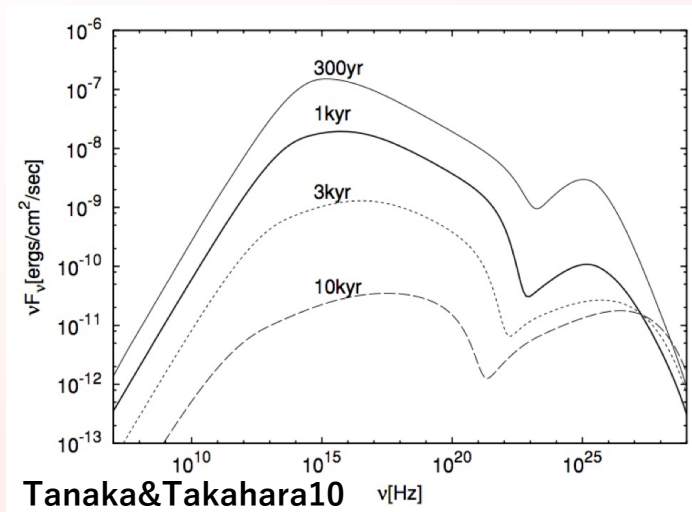
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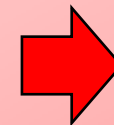




# Origin of Radio Emission



- Standard acceleration model (e.g., shock accel.) forms single power-law distribution.
- Radio obs. indicate very hard spectrum.
- Radio emitting particle dominate in # ( $\kappa$ -problem)
- PWNe are in turbulent state.

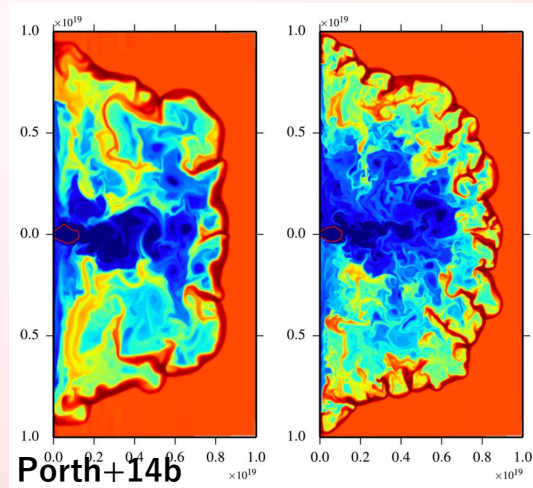
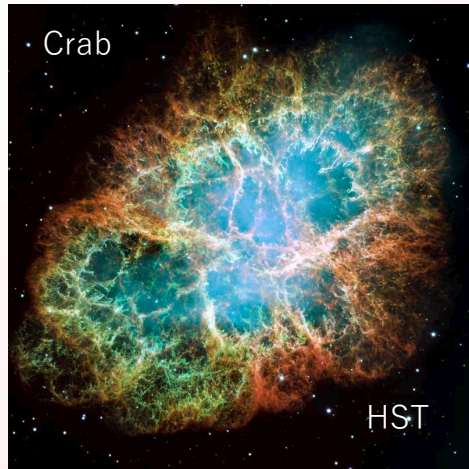


Single power-law injection from central pulsar @ high energy & **external particle injection** + stochastic accel.

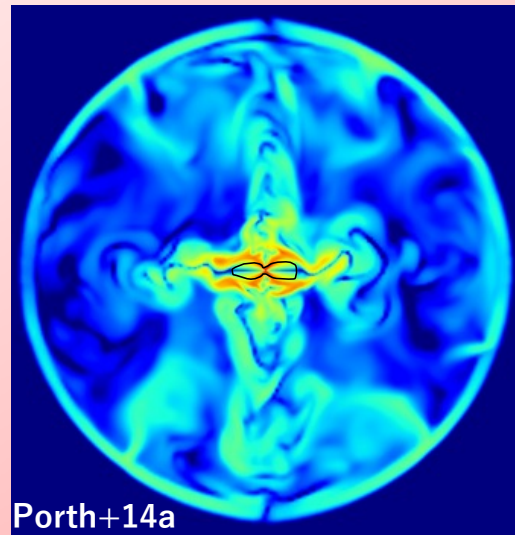
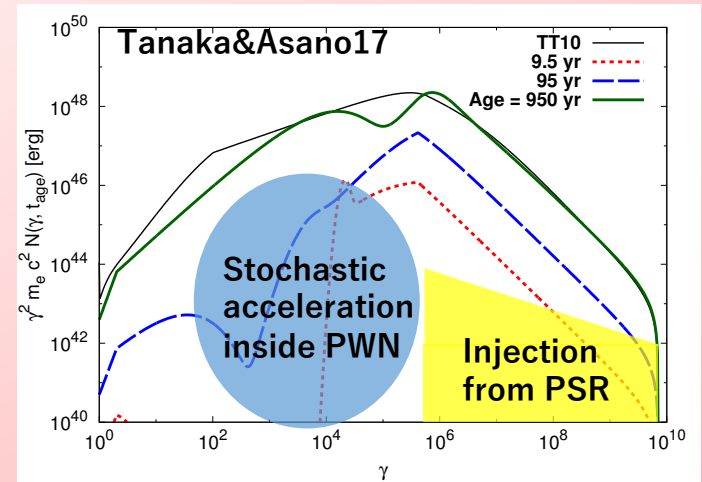
Tanaka&Asano17

Model

# Turbulence in PWNe



## Stochastic acceleration model

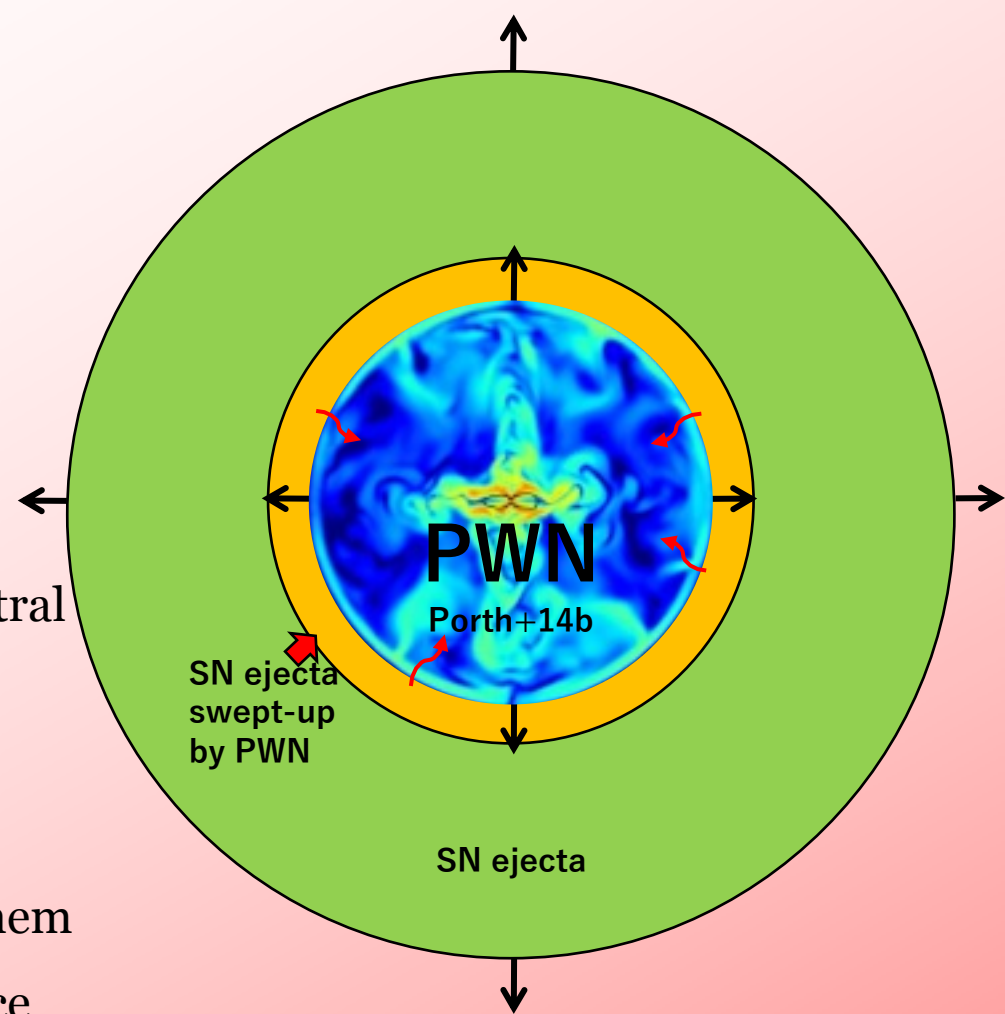


- Standard single PL injection + stochastic acceleration
- Radio-emitting particles increase more rapidly than broken PL model

# One-zone Model

One-zone approx. for PWN

- Expanding PWN inside expanding SN ejecta e.g., Gelfand+09, Bandiera+20
- Supplying accelerated  $e^\pm$  & B from central PSR e.g., Pacini&Salvati73, Kennel&Coroniti84
- Seeding low-energy electrons from SN ejecta and stochastically accelerating them to radio-emitting particles by turbulence Tanaka&Asano17



- B-field evolution of  $\frac{4\pi}{3} R_{\text{PWN}}^3(t) \frac{B^2(t)}{8\pi} = \eta_B \int_0^t L_{\text{spin}}(t') dt'$  Tanaka&Takahara10

$$L_{\text{spin}} = (\eta_e + \eta_B + \eta_{\text{turb}}) L_{\text{spin}}$$

# Stochastic Acceleration

$$\frac{\partial}{\partial t} N(\gamma, t) + \frac{\partial}{\partial \gamma} \left[ \left( \underbrace{\dot{\gamma}_{\text{cool}}(\gamma, t)}_{\text{cooling effects}} - \underbrace{\gamma^2 D_{\gamma\gamma}(\gamma, t)}_{\text{stochastic accel.}} \frac{\partial}{\partial \gamma} \frac{1}{\gamma^2} \right) N(\gamma, t) \right] = \underbrace{Q_{\text{PSR}}(\gamma, t)}_{\text{from pulsar}} + \underbrace{Q_{\text{ext}}(t)}_{\text{Extra injection}}$$

$$D_{\gamma\gamma} = \frac{\gamma_{\text{min}}^2}{2\tau_{\text{acc,m}}} \left( \frac{\gamma}{\gamma_{\text{min}}} \right)^2 \exp\left(-\frac{t}{\tau_{\text{turb}}}\right)$$

Tanaka&Asano17

- $\tau_{\text{acc,m}}$ : acceleration time normalized at  $\gamma_{\text{min}}$
- $\tau_{\text{turb}}$ : decay time-scale of turbulence

$$Q_{\text{ext}}(\gamma, t) = f_{\text{inj}} 4\pi R_{\text{PWN}}^2(t) v_{\text{PWN}}(t) n_{\text{ej}}(R_{\text{PWN}}(t)) \delta(\gamma - \gamma_{\text{inj}})$$

- $f_{\text{inj}}$ : injection efficiency  
 $f_{\text{inj}} \ll 1$  ( $O(10^{-5})$ )
- $\gamma_{\text{inj}}$ : injection energy  
 $\gamma_{\text{inj}} \sim 1$

# Stochastic Acceleration

$$\frac{\partial}{\partial t} N(\gamma, t) + \frac{\partial}{\partial \gamma} \left[ \underbrace{\dot{\gamma}_{\text{cool}}(\gamma, t)}_{\text{cooling effects}} - \underbrace{\gamma^2 D_{\gamma\gamma}(\gamma, t)}_{\text{stochastic accel.}} \frac{\partial}{\partial \gamma} \frac{1}{\gamma^2} \right] N(\gamma, t) = \underbrace{Q_{\text{PSR}}(\gamma, t)}_{\text{from pulsar}} + \underbrace{Q_{\text{ext}}(t)}_{\text{Extra injection}}$$

$$D_{\gamma\gamma} = \frac{\gamma^2}{\tau_{\text{acc}}} \left( \frac{E_{\delta}}{E_{\text{rot}}} \right)$$

This study

- $\tau_{\text{acc}}$ : parameter determines time-scale
- $E_{\text{rot}}$ : total spin-down energy
- $E_{\delta}$ : energy of turbulence injection from spin-down & decreasing for stochastic accel.

$$Q_{\text{ext}}(\gamma, t) = f_{\text{inj}} 4\pi R_{\text{PWN}}^2(t) v_{\text{PWN}}(t) n_{\text{ej}}(R_{\text{PWN}}(t)) \delta(\gamma - \gamma_{\text{inj}})$$

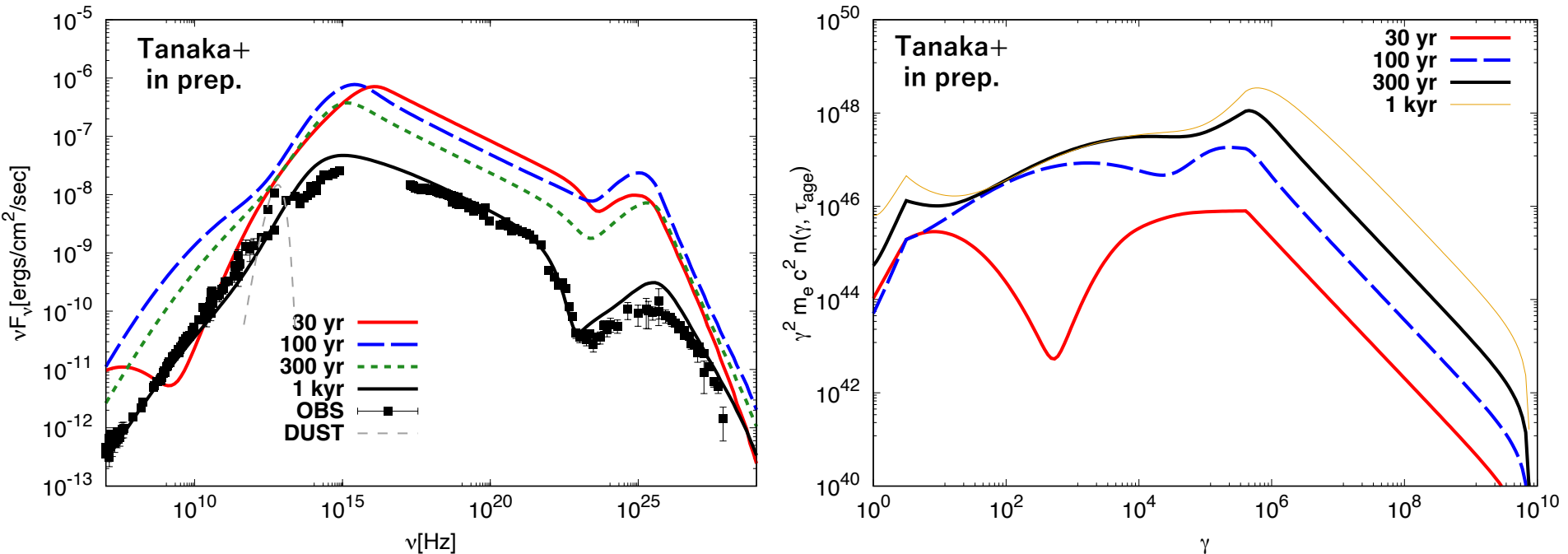
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# Results & Conclusion



# Results

Application to the Crab Nebula ( $\tau_{\text{acc}} \sim 1 \text{ yr}$ )

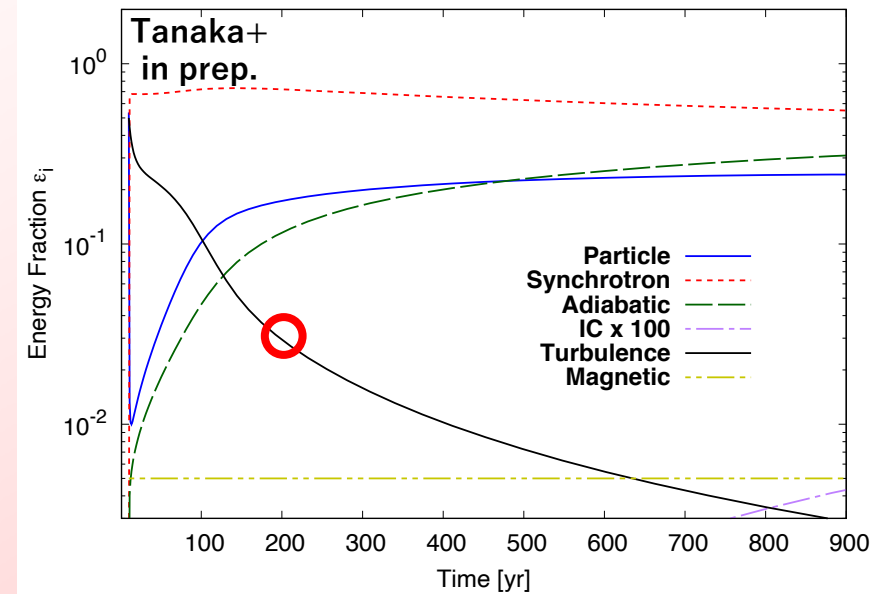


A preliminary result shows that the hard radio spectrum can be reproduced with the current model



# Conclusions

Stochastic acceleration model of radio emission from the Crab Nebula is improved considering the evolution of turbulent energy.



- Origin of the radio-emitting particles of PWNe is unknown.
- Studied the external particle origin scenario with stochastic acceleration model by Tanaka & Asano (2017) improved by excluding artificial decaying behavior of the turbulent.
- The radio spectrum of the Crab Nebula is reproduced with the current model which has no artificial decaying term.