

Extraction of ANC via Coulomb breakup

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1) Brief introduction to CDCC

— *M. Kamimura, Yahiro, Iseri, Sakuragi, Kameyama and Kawai, PTP Suppl. 89, 1 (1986);
N. Austern, Iseri, Kamimura, Kawai, Rawitscher and Yahiro, Phys. Rep. 154 (1987) 126.*

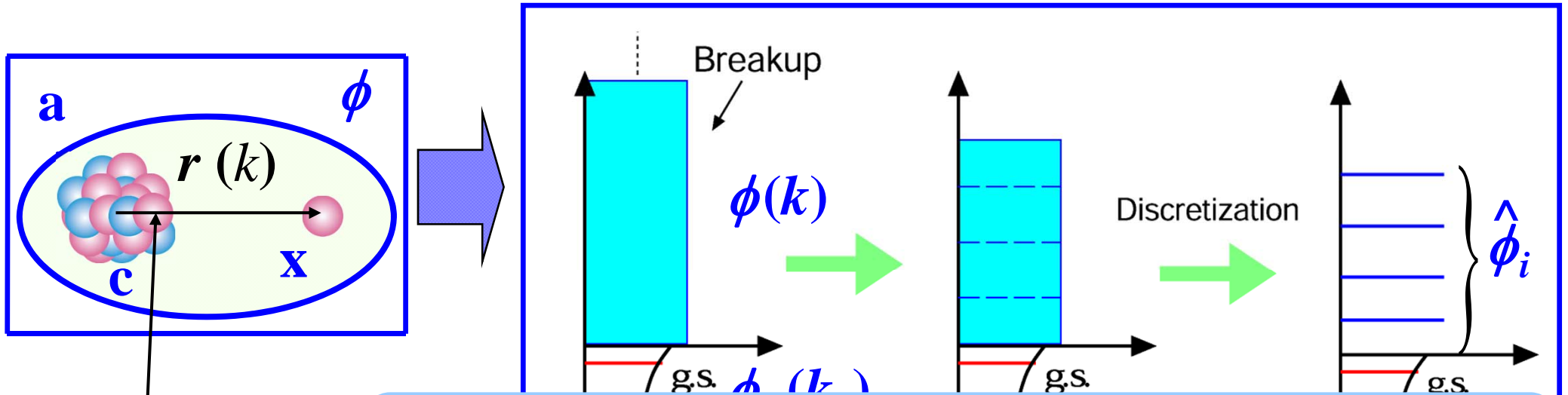
2) Some “new” aspects of our paper on $S_{17}(0)$

— *KO, Hashimoto, Iseri, Kamimura, and Yahiro, PRC73, 024605 (2006).*

3) Some results on breakup of ${}^9\text{C}$

— *KO, Minomo, Bertulani, and Yahiro, in preparation*

The Continuum-Discretized Coupled Channels method (CDCC)



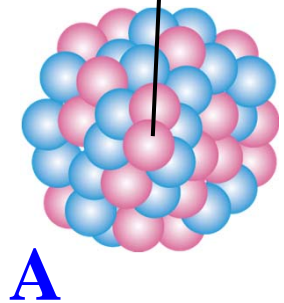
CDCC is just a usual CC calculation with **truncation** and **discretization** of the continuum.

χ $R(K)$

$\psi(\vec{r}, \vec{R}) \cong \phi_0(k_0, \vec{r}) \chi_0(K_0, \vec{R}) + \sum_{i=1}^{i_{\max}} \hat{\chi}(\hat{K}_i, \vec{R}) \int_{k_{i-1}}^{k_i} \phi(k, \vec{r}) dk$

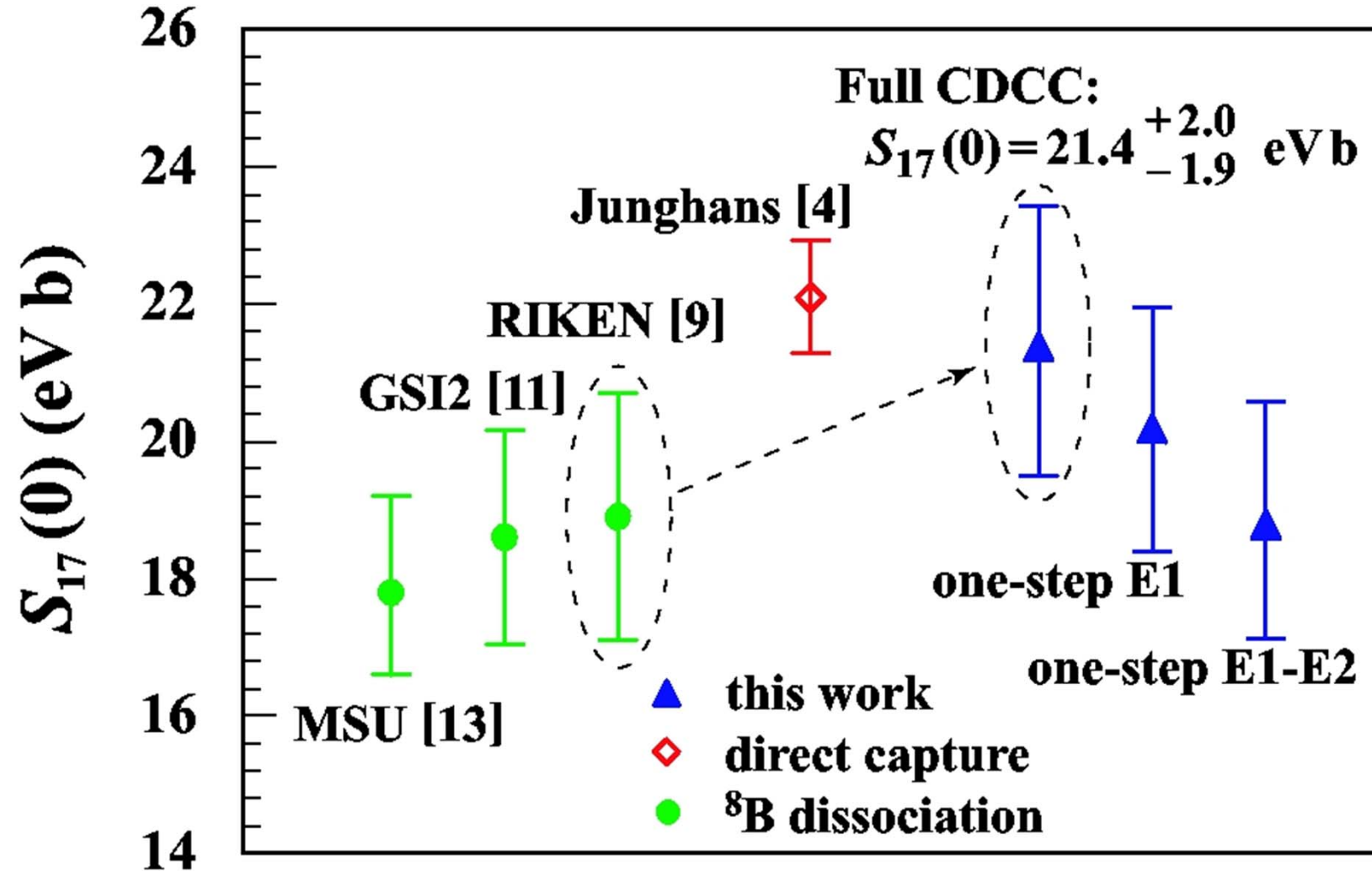
$\psi^{\text{CDCC}}(\vec{r}, \vec{R}) = \sum_{i=0}^{i_{\max}} \hat{\phi}_i(\vec{r}) \hat{\chi}_i(\hat{K}_i, \vec{R})$

Truncation and Discretization



$S_{17}(0)$ extracted from ^8B breakup with CDCC

— KO, Hashimoto, Iseri, Kamimura, and Yahiro, *PRC73*, 024605 (2006).



Three “new” aspects of our S_{17} paper

— *KO, Hashimoto, Iseri, Kamimura, and Yahiro, PRC73, 024605 (2006).*

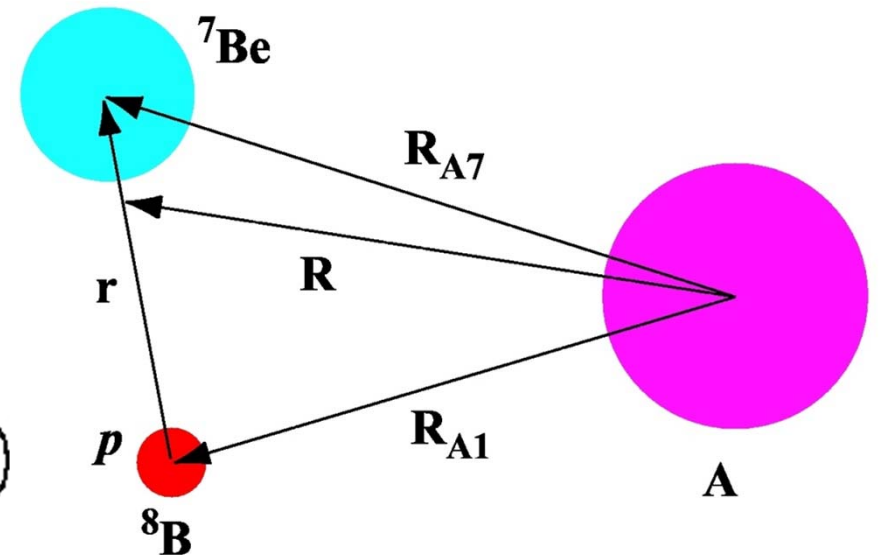
1) The first work to determine ANC from exclusive Coulomb breakup (showing peripherality of Coulomb breakup reaction)

□ Peripherality with respect to R :

$$R \geq R_{\min}$$

□ Property of the E1 operator:

$$\frac{R}{(wr)^2} \theta(wr - R) + \frac{wr}{R^2} \theta(R - wr)$$



Coulomb-dominated breakup is peripheral with respect to r .

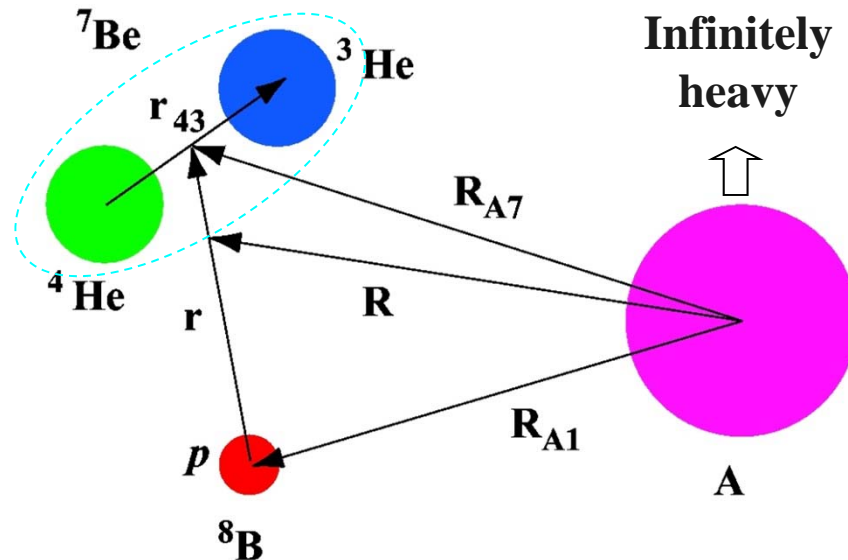
Coulomb breakup ANC method!

c.f. L. Trache, Carstoiu, Gagliardi, and Tribble, PRL87, 271102 (2001).

Three “new” aspects of our S_{17} paper

— KO, Hashimoto, Iseri, Kamimura, and Yahiro, *PRC73*, 024605 (2006).

2) Reduction from 4-body breakup to 3-body breakup



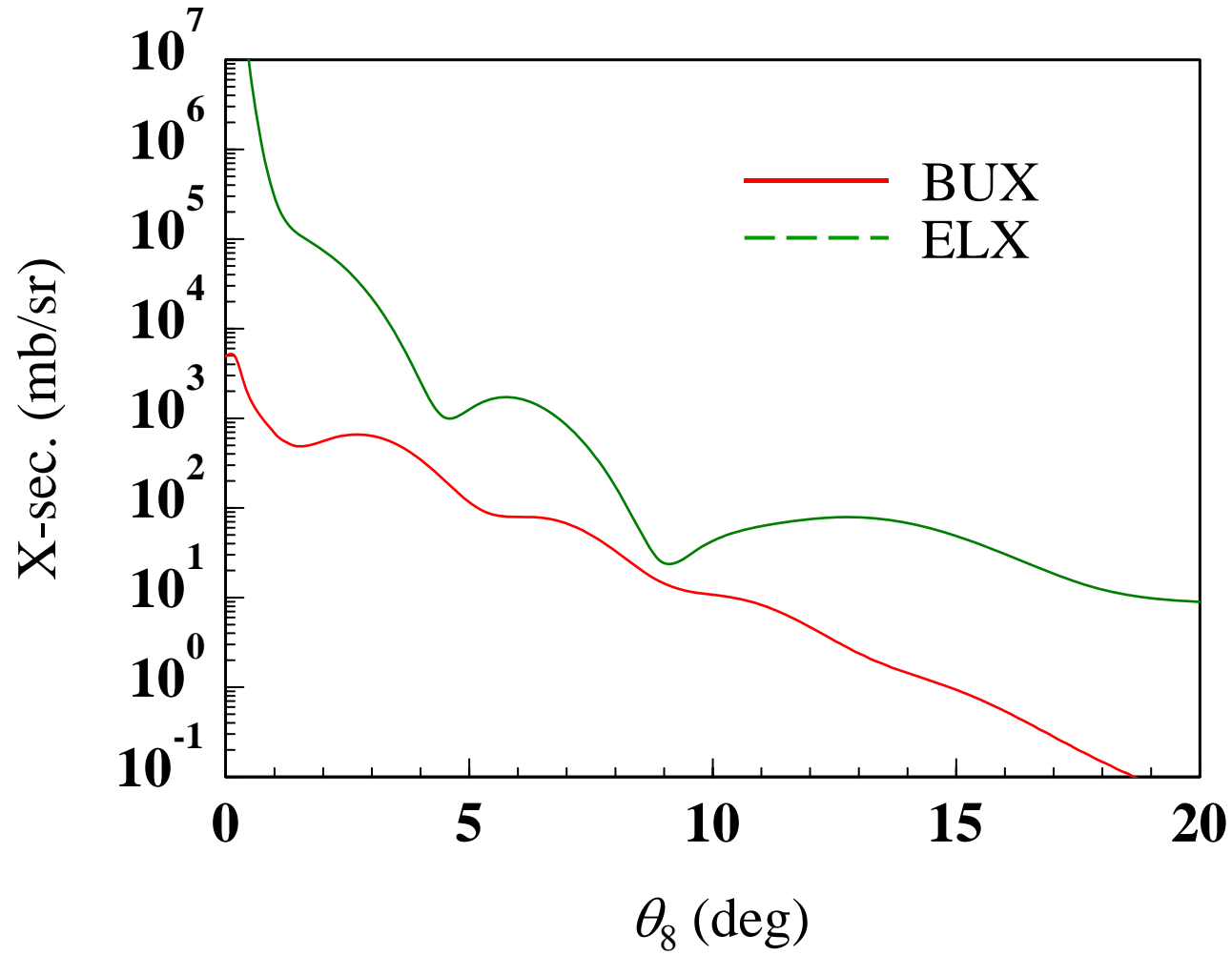
□ The triple-differential cross section for $(^8\text{B}, ^7\text{Be}+p)$ is obtained by

$$C\rho |\mathfrak{X}|^2 \text{ with } \mathfrak{X} = \langle \chi_1 \chi_7 \phi_7^{(0)} | U_{A3} + U_{A4} + U_{A1} + V_{13} + V_{14} | \Psi_{4\text{-body}} \rangle$$

□ ^7Be breakup cross section by ^{208}Pb turned out to be negligibly small for forward-scattering.

$$\Rightarrow \begin{cases} U_{A3} + U_{A4} \approx \langle \phi_7^{(0)} | U_{A3} + U_{A4} | \phi_7^{(0)} \rangle \\ V_{13} + V_{14} \approx \langle \phi_7^{(0)} | V_{13} + V_{14} | \phi_7^{(0)} \rangle \end{cases}$$

^8B scattering from ^9Be at 100 A MeV



Three “new” aspects of our S_{17} paper

— *KO, Hashimoto, Iseri, Kamimura, and Yahiro, PRC73, 024605 (2006).*

3) CDCC cross section is proportional to ANC

$$\begin{aligned} \langle \phi_7^{(0)} | \Psi_{4\text{-body}} \rangle &= \langle \phi_7^{(0)} | \frac{i\varepsilon}{E - H_{4\text{-body}} + i\varepsilon} | \phi_8^{(0)} e^{i\mathbf{P}\cdot\mathbf{R}} \rangle \\ &\approx \frac{i\varepsilon}{E - e_7 - H_{3\text{-body}} + i\varepsilon} | \mathfrak{S}_{\text{exp}}^{1/2} \psi_{17}(\mathbf{r}) e^{i\mathbf{P}\cdot\mathbf{R}} \rangle \end{aligned}$$

with

**Normalization
factor**

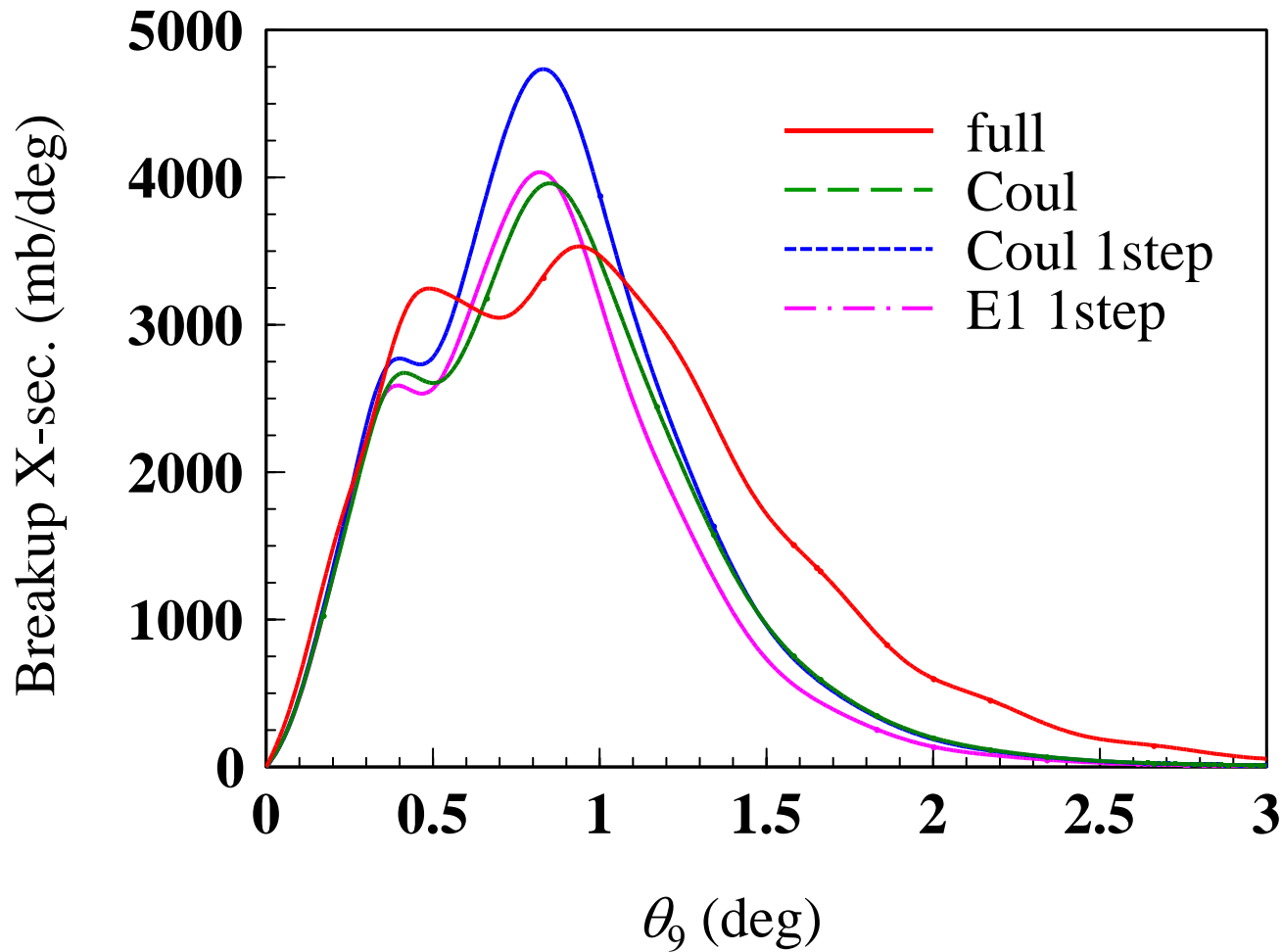
$$\mathfrak{S}_{\text{exp}}^{1/2} \psi_{17}(\mathbf{r}) \equiv \langle \phi_7^{(0)}(\mathbf{r}_{43}) | \phi_8^{(0)}(\mathbf{r}_{43}, \mathbf{r}) \rangle$$

$$H_{3\text{-body}} = T_r + T_R + V_{17}(\mathbf{r}) + U_{A7}(\mathbf{R}_{A7}) + U_{A1}(\mathbf{R}_{A1})$$

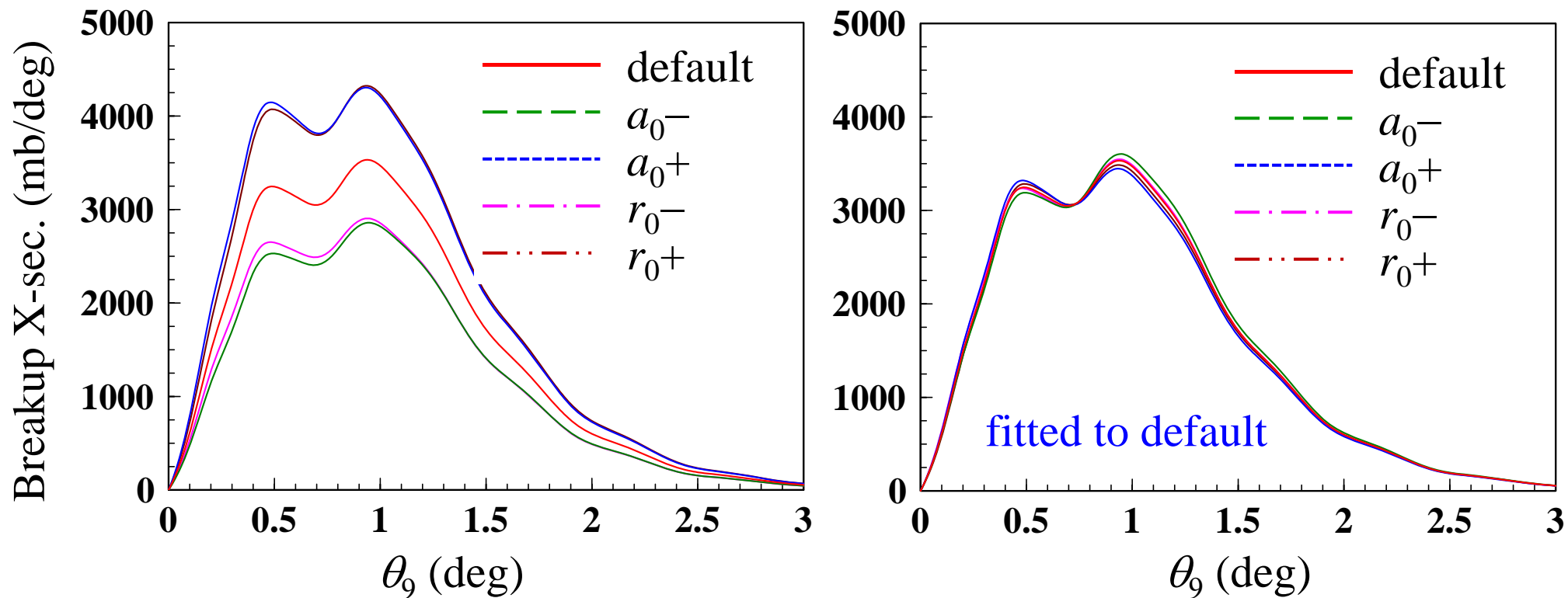
$$\mathfrak{T} \approx \mathfrak{S}_{\text{exp}}^{1/2} \mathfrak{T}_{3\text{-body}},$$

$$\mathfrak{T}_{3\text{-body}} \equiv \langle \chi_1 \chi_7 | U_{A7} + U_{A1} + V_{17} | \Psi_{3\text{-body}} \rangle,$$

${}^9\text{C}$ breakup by ${}^{208}\text{Pb}$ at 300 MeV/nucleon (nuclear and higher-order effects)



${}^9\text{C}$ breakup by ${}^{208}\text{Pb}$ at 300 A MeV (check of peripherality)



	default	a_0^-	a_0^+	r_0^-	r_0^+
S	1.00	1.26	0.80	1.22	0.81
$(C_{\text{sp}})^2$	1.63	1.30	2.05	1.28	2.10
C^2	1.63	1.64	1.64	1.57	1.69

Summary

1) **CDCC** is a powerful tool to describe projectile breakup processes non-perturbatively.

2) **Coulomb-breakup ANC method** is proposed.

- ✓ Coulomb-dominated breakup is peripheral.
- ✓ Three-body description of ${}^8\text{B}$ and ${}^9\text{C}$ breakup processes is justified.
- ✓ CDCC cross section is proportional to the ANC^2 .

3) **Some results on ${}^9\text{C}$ breakup** are discussed

- ✓ Nuclear and higher-order contributions are important.
- ✓ ${}^9\text{C}$ breakup by ${}^{208}\text{Pb}$ at (100 and) 300 MeV/nucleon is peripheral.
 - ⇒ Application to ${}^9\text{C}$ breakup at 65MeV/A (Fukui)
- ✓ Eikonal CDCC is valid.
 - ⇒ Eikonal Reaction Theory (Minomo)