

# Status report

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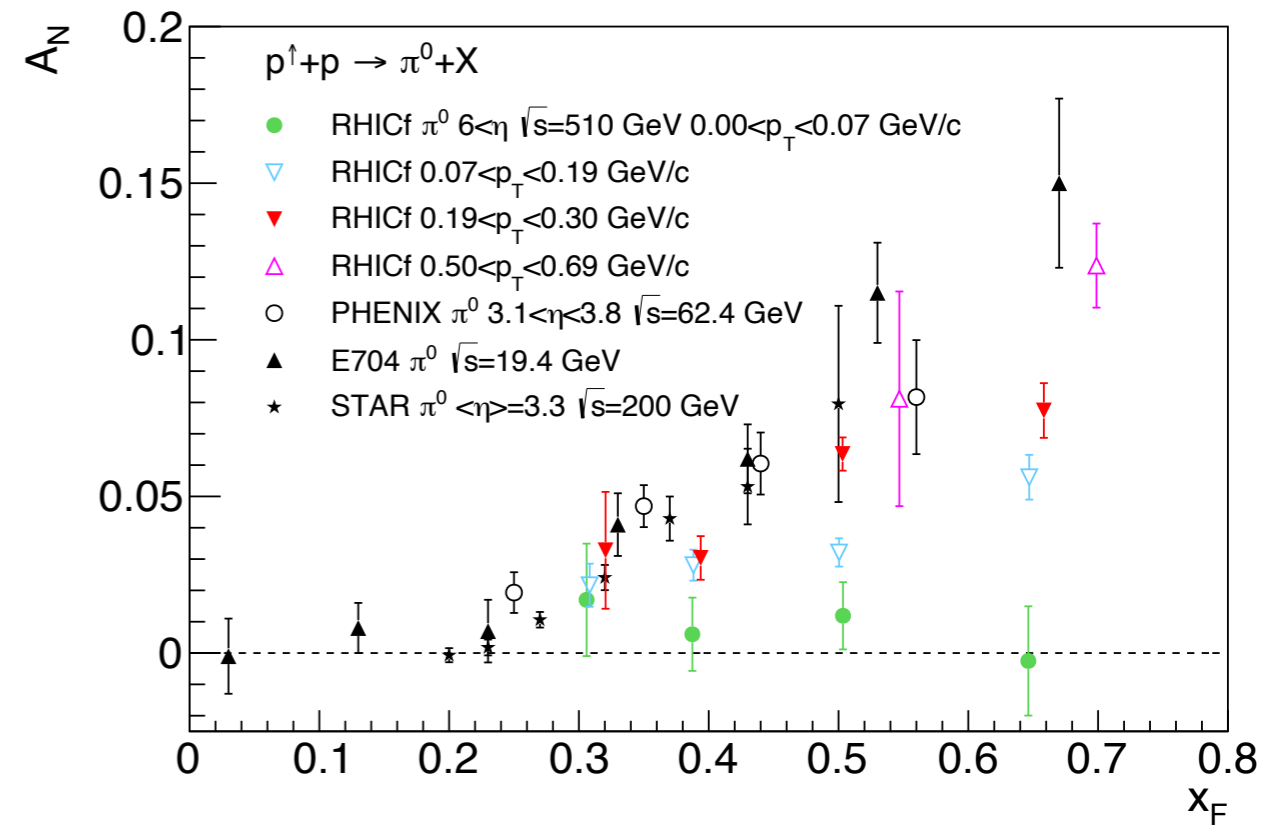
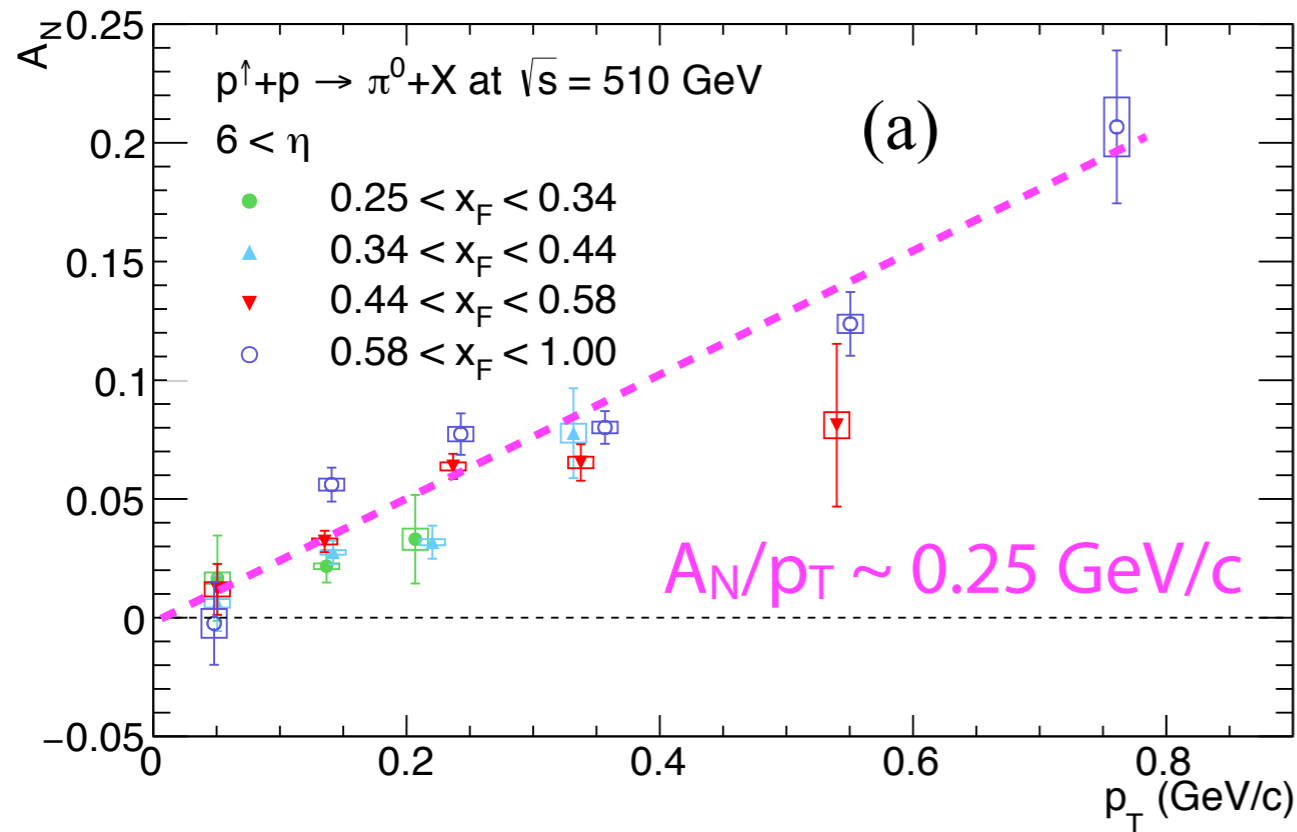
RHICf KAKEN meeting  
21 Nov. 2022

# Calculation & simulation sets for RHICf-II

	Hadronic	UPC	$\sqrt{s}$ (GeV)
$p^\uparrow$ -p	Ongoing	Negligible	510
$p^\uparrow$ -Al	Similar with p-p?		200
$p^\uparrow$ -Au	Similar with p-p?	$2\pi$ MAID?	200
etc?			

# $A_N(x_F, p_T)$ in $p^\uparrow p \rightarrow \pi^0 X$ at $\sqrt{s} = 510$ GeV

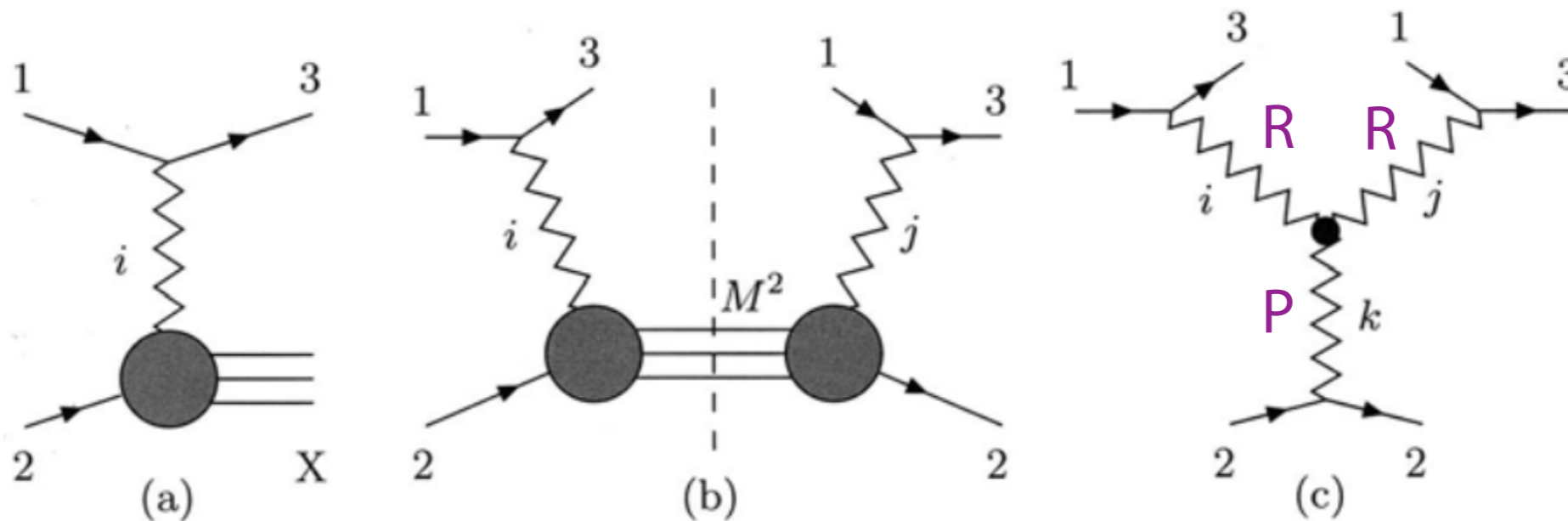
RHICf at  $\sqrt{s} = 510$  GeV



- Opposite sign compared with neutron  $A_N$
- $|A_N|/p_T$  is about half of neutron  $A_N$ .

- $A_N/x_F$  seems independent of  $\sqrt{s}$  and  $\eta$ .  
(can QCD processes make large  $A_N$  at  $p_T > 1$  GeV/c?)

# Triple-regge diagram in $p \uparrow p \rightarrow \pi X$



[Barone and Predazzi]

Triple-regge/pomeron diagram is valid in the limit of  $M^2 \rightarrow \infty$  and  $s \rightarrow \infty$  that mostly suits to the RHICf kinematics.

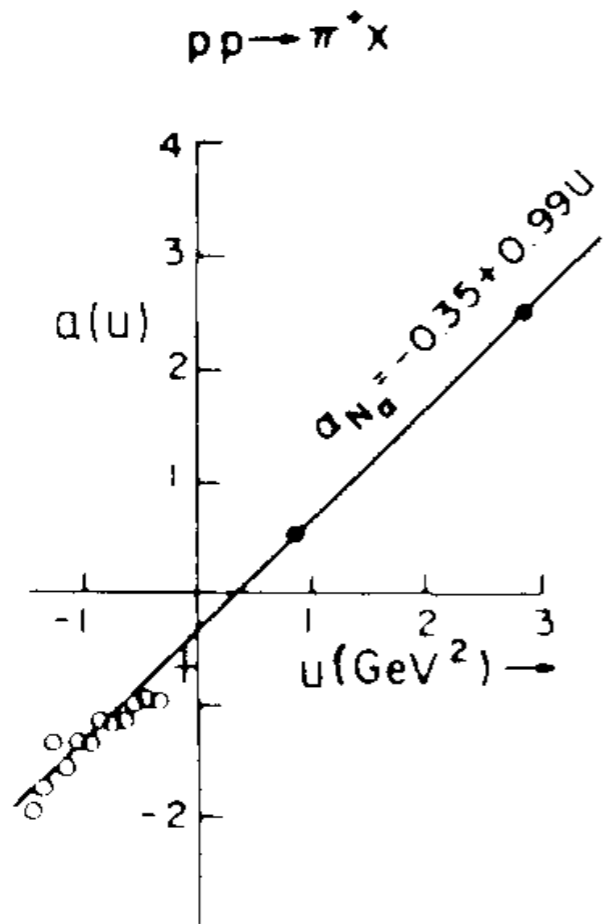
$$A(12 \rightarrow 3X) \underset{s \rightarrow \infty}{\sim} \sum_i g_{13}^i(t) g_{2X}^i(t) \eta_i(t) \left( \frac{s}{M^2} \right)^{\alpha_i(t)}$$

Sum over all trajectories

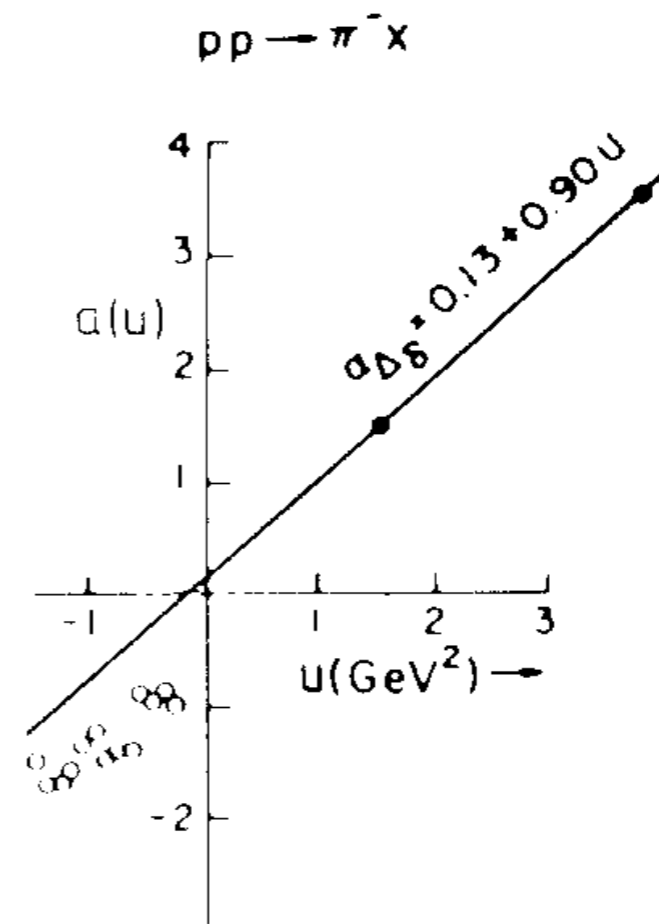
- $g_{13}$ :  $p \rightarrow \pi^0$  vertex function
- $g_{2X}$ :  $p+l(j) \rightarrow X$  cross section
- $\eta$ : trajectory's phase
- $\alpha(t)$ : regge/pomeron trajectory
- $M^2/s \sim 1 - X_F$

# Regge trajectories

[Storror, Phys. Rep. 103, 317]



$$\alpha_{N\alpha}(t) = -0.34 + 0.99t$$



$$\alpha_{\Delta\delta}(t) = 0.07 + 0.92t$$

Very old but still usable as recent papers refer

# $E d^3\sigma/dp^3$ in $p^\uparrow p \rightarrow \pi^{+/-} X$

ISR at  $\sqrt{s} = 45$  GeV

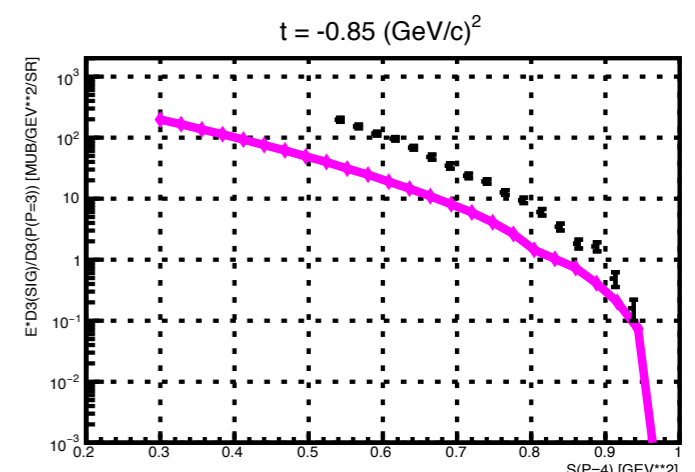
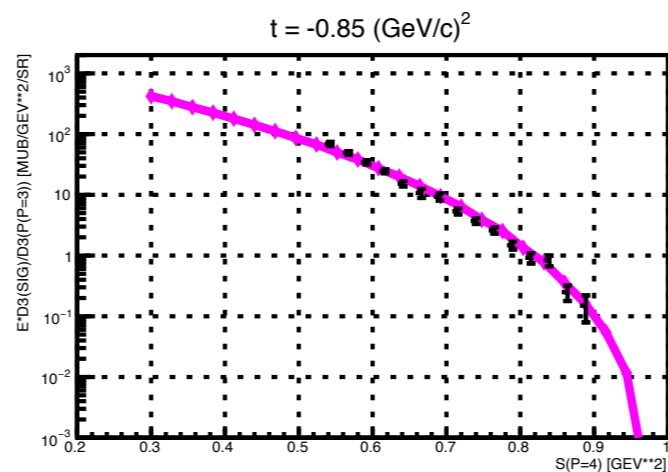
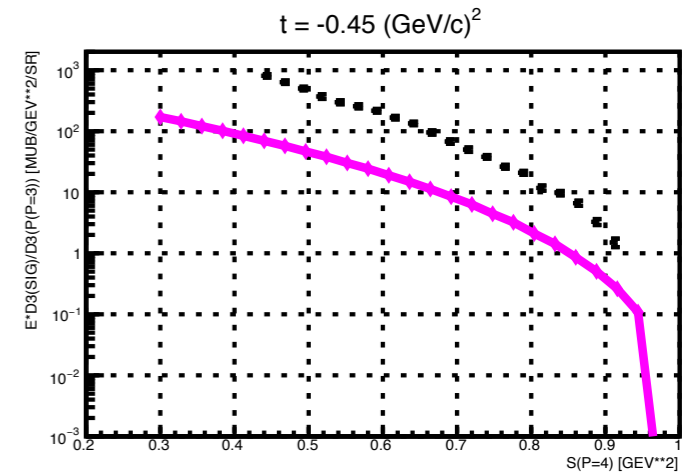
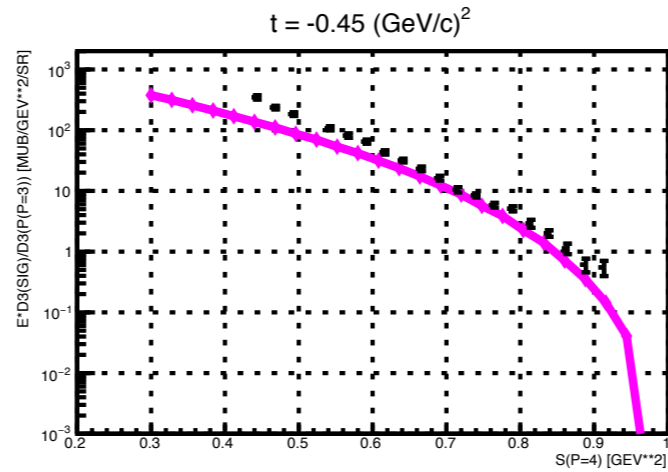
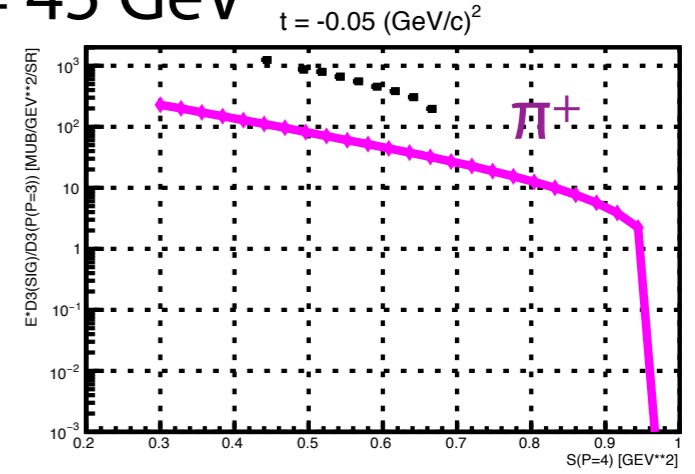
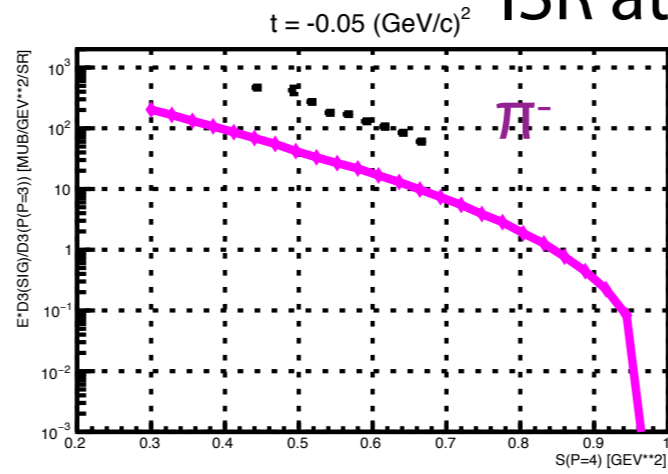
$$\pi^- \quad |\langle \Delta^{++} | \pi^+ p \rangle|^2 = 1$$

$$\pi^+ \quad |\langle \Delta^0 | \pi^- p \rangle|^2 = \frac{1}{3}$$

$$|\langle n | \pi^- p \rangle|^2 = \frac{2}{3}$$

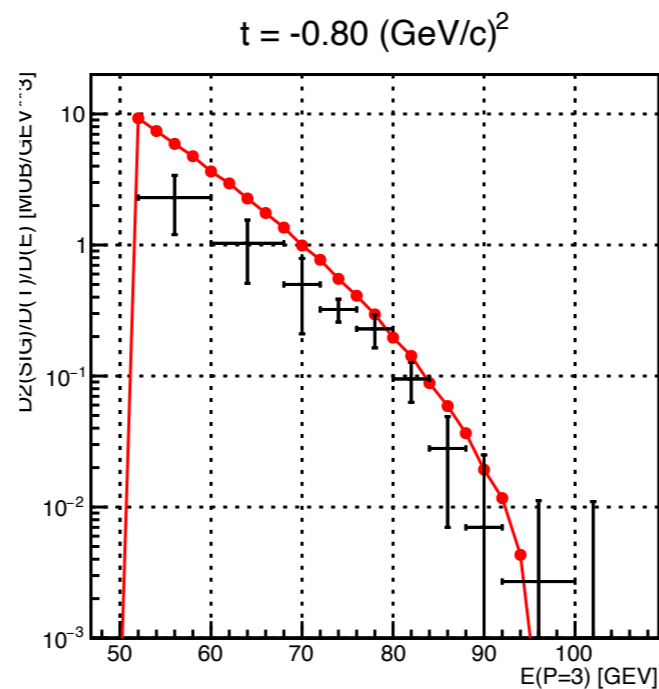
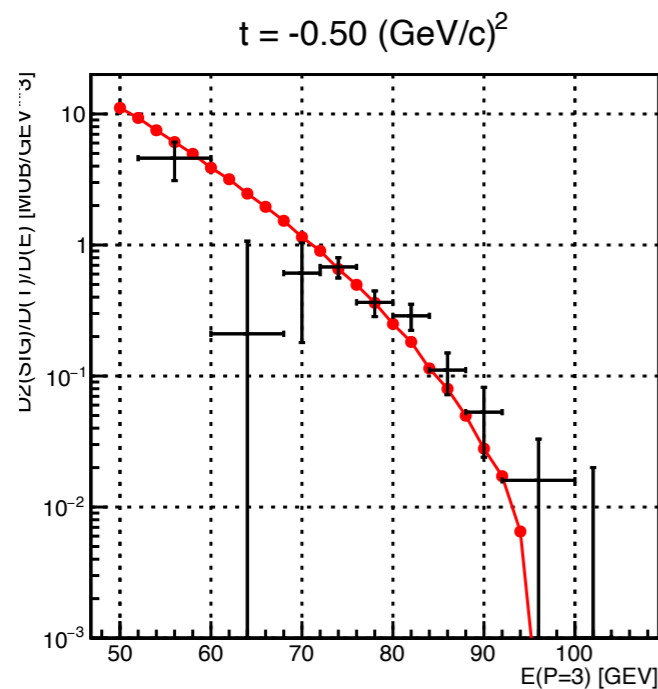
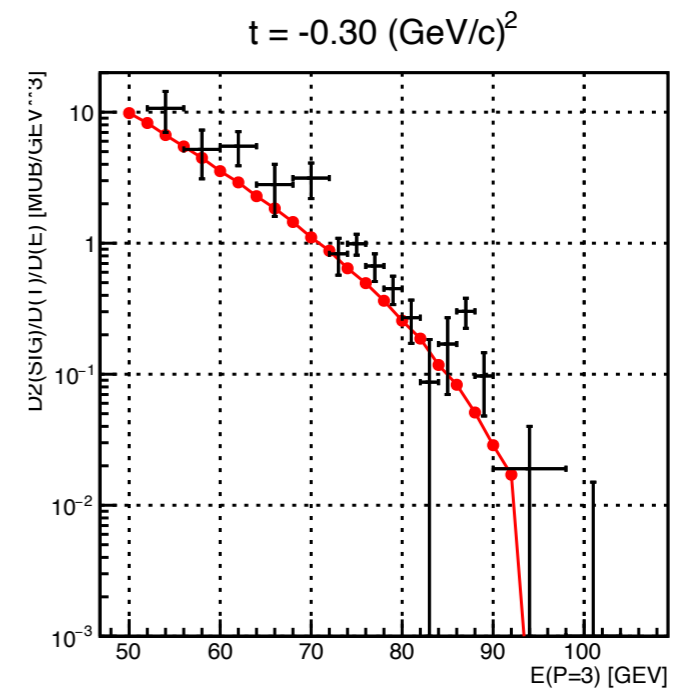
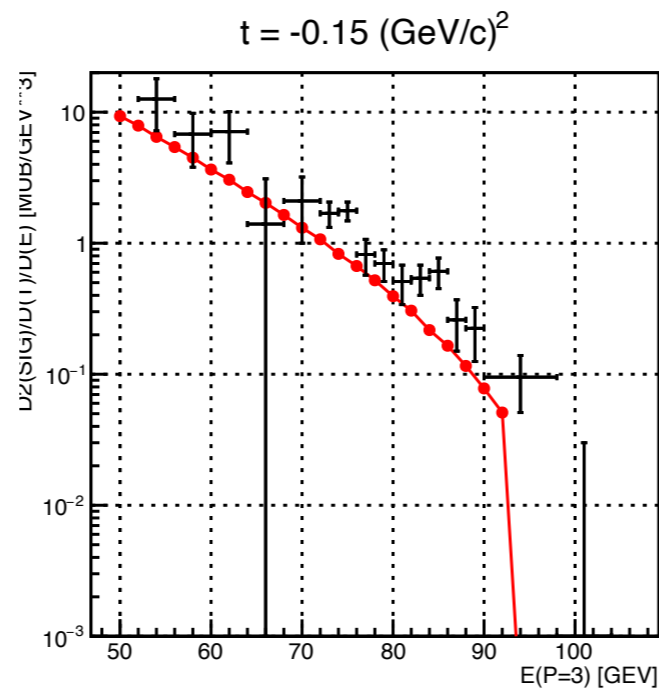
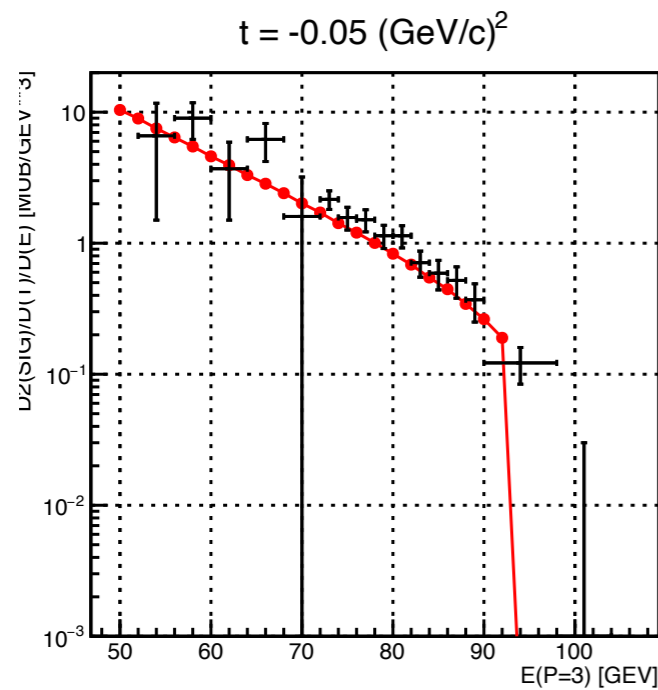
$$\pi^0 \quad |\langle p | \pi^0 p \rangle|^2 = \frac{1}{3}$$

$$|\langle \Delta^+ | \pi^0 p \rangle|^2 = \frac{2}{3}$$



# $E d^3\sigma/dp^3$ in $p^\uparrow p \rightarrow \pi^0 X$

E350 at  $\sqrt{s} = 13$  GeV

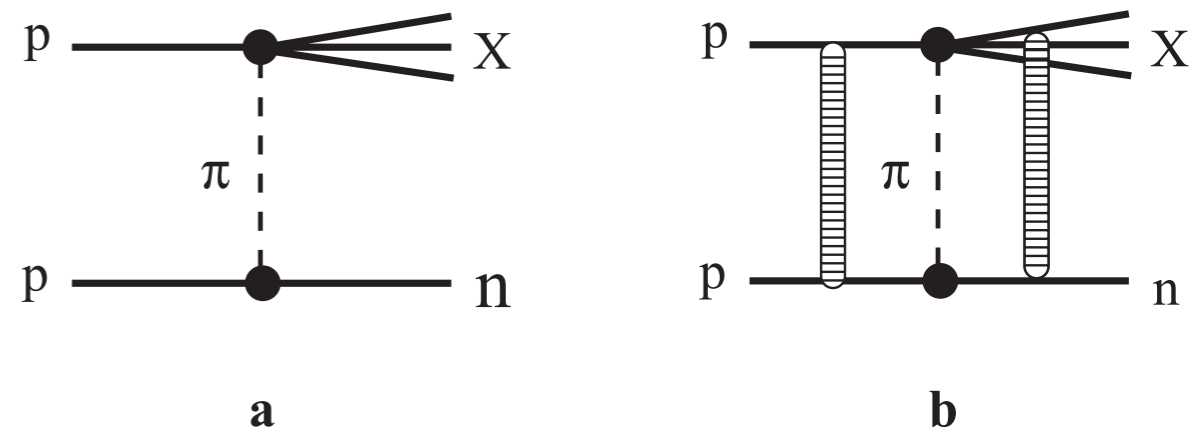


- My calculations follow the simple triple-regge diagrams driven by proton and  $\Delta(1232)$  exchanges.
- Overall not so bad

# Absorptive correction and interference

$$A_N = 2 \frac{\text{Im } M_{\text{flip}}^* M_{\text{nonflip}}}{|M_{\text{flip}}^*|^2 + |M_{\text{nonflip}}^*|^2} \propto 2\text{Im } \eta^* \eta$$

[Kopeliovich, Phys. Rev. D 78, 014031]



- Nonzero asymmetry is generated through phase interferences ( $\text{Im}[\eta_i(t)\eta_j(t)^*] \neq 0$ ); at least either A or B is needed.

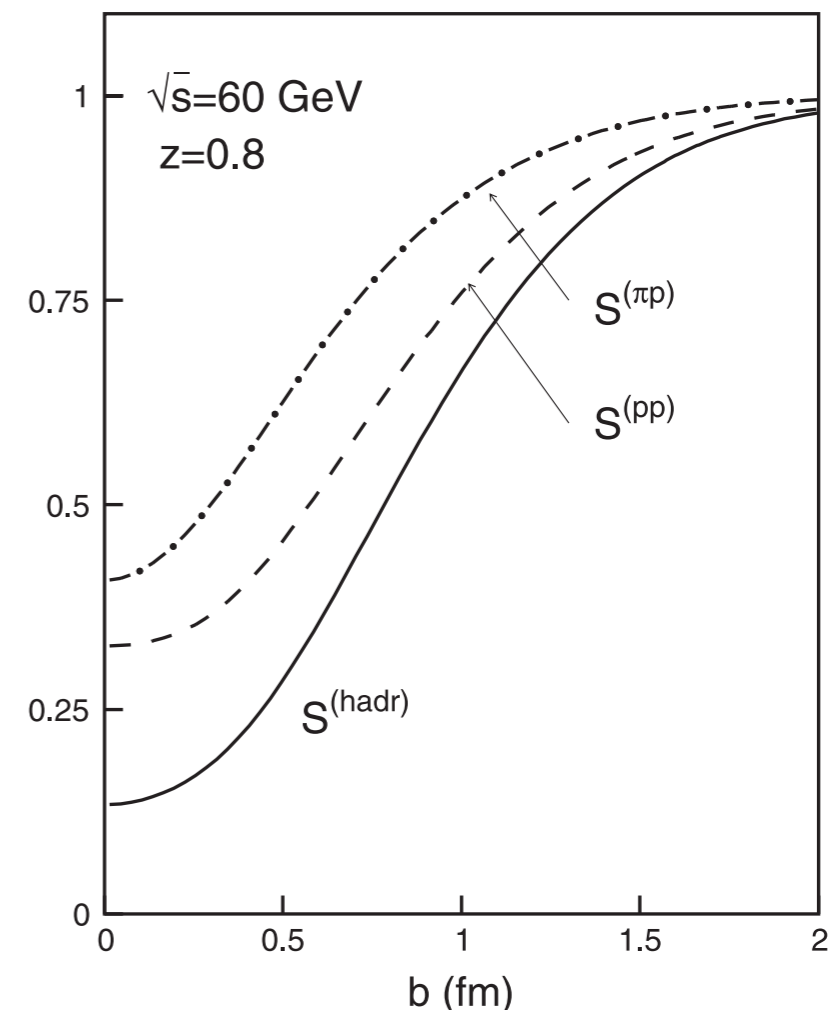
A. Interference in particle exchange

B. Interference in absorptive correction

- E.g. for forward neutrons [Kopeliovich, PRD 84]

A.  $\pi$ - $a_1$  exchange interferences  $\rightarrow$  leading

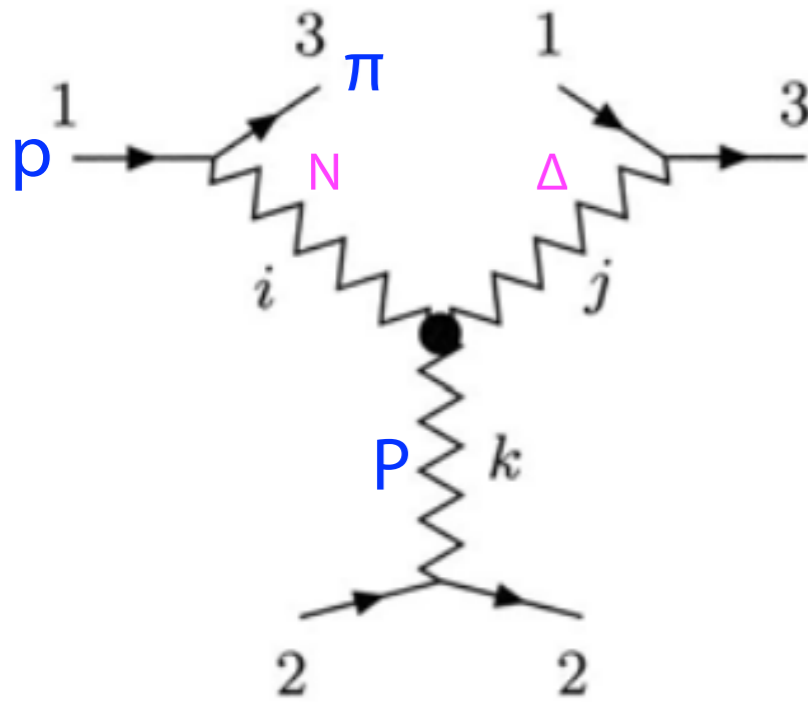
B. Absorptive correction  $\rightarrow$  sub-leading



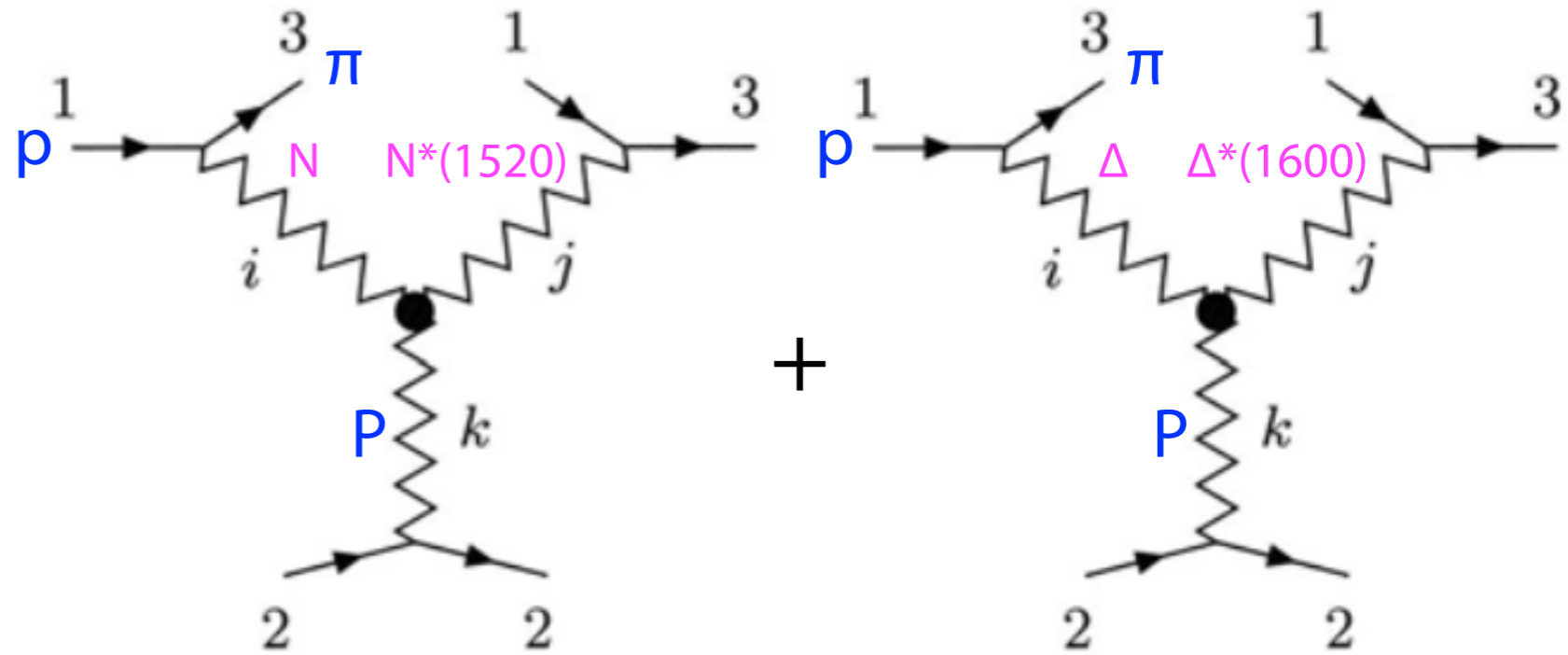


# What I did for 2+ years...

My calc. (failed)



H-J Kim et. al., PRD 106, 054001



My calculation was stuck in how to make N(1/2) and Δ(3/2) coupled. I thought this interference was necessary to generate nonzero  $A_N$ .  
→ prohibited

Each phase differences of N and Δ exchanges gives sizable  $A_N$ .

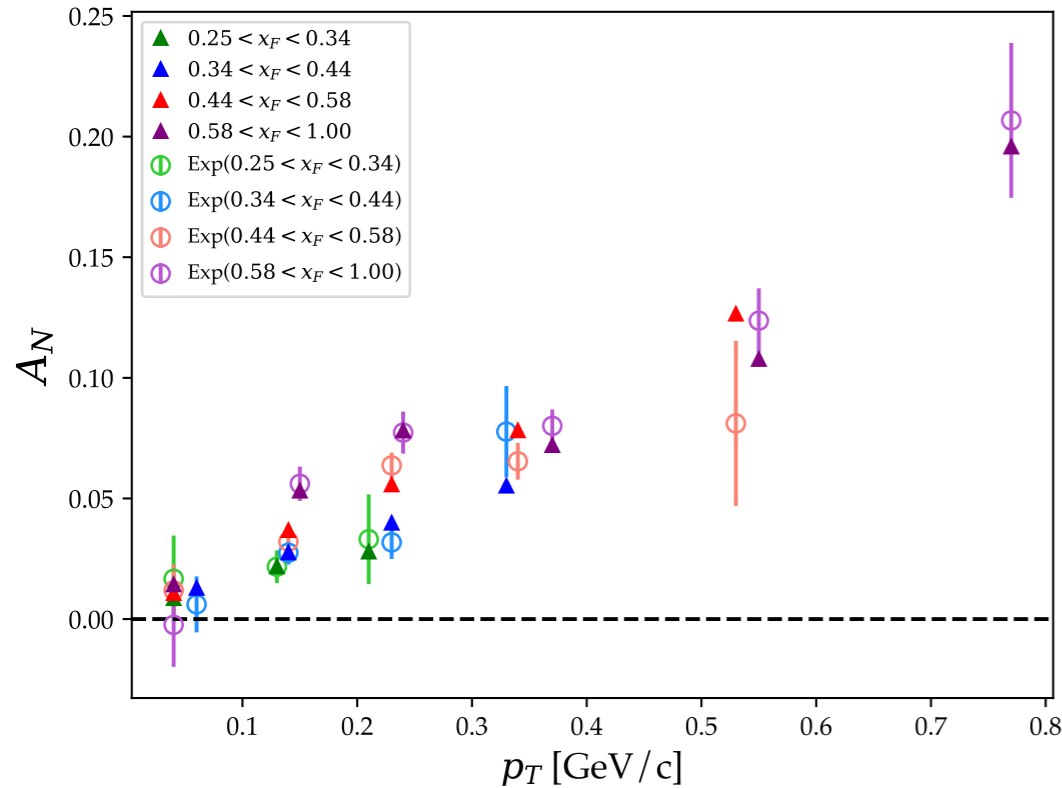
$$d\Delta\sigma_{\perp} = d\Delta\sigma_{\perp}^N + d\Delta\sigma_{\perp}^U$$

$$d\Delta\sigma_{\perp}^N = \frac{1}{s} \sum_{\lambda} \beta_{+\lambda}^N \beta_{-\lambda}^{N*} 2\text{Im} \mathcal{P}_N \mathcal{P}_N^* \times \sum_k G_k^{NN^*}(t) \gamma_k^{pp}(0) \left(\frac{M_X^2}{s_0}\right)^{\alpha_k(0)}$$

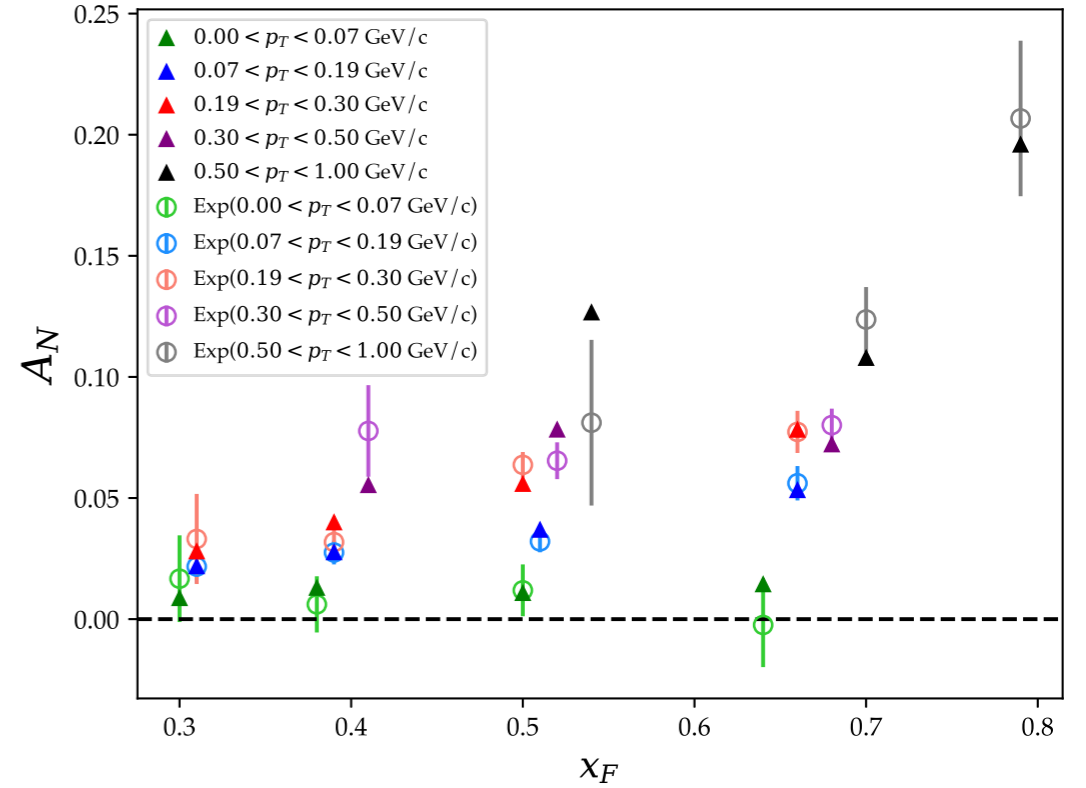
$$d\Delta\sigma_{\perp}^U = \frac{1}{s} \sum_{\lambda} (\beta_{+\lambda}^{\Delta} \beta_{-\lambda}^{\Delta*}) 2\text{Im} \mathcal{P}_{\Delta} \mathcal{P}_{\Delta}^* \times \sum_k G_k^{\Delta\Delta^*}(t) \gamma_k^{pp}(0) \left(\frac{M_X^2}{s_0}\right)^{\alpha_k(0)}$$

# H-J Kim et. al., PRD 106, 054001

momentum  $p_T$  at  $p_T < 1$  GeV/c. Employing baryonic triple Regge exchanges, we describe the complete RHICf data for the first time and show that the neutral pion production at low  $p_T$  can be interpreted as a diffractive one.



Great job!



determined. In the present work, we parametrize the form of the triple Regge couplings so that we can describe the RHICf data:  $G_{\mathbb{P}}^{ii}(t) = G_{\mathbb{P}}^{ii}(0)e^{-B_{\mathbb{P}}^{ii}|t|}$ ,  $G_{\mathbb{P}}^{ij}(t) = G_{\mathbb{P}}^{ij}(0)\sqrt{|t|}e^{-B_{\mathbb{P}}^{ij}|t|}/m_{\pi}$ . We define the following parameters:

$$\underline{g_{\mathbb{P}}^{ij} \equiv G_{\mathbb{P}}^{ij}(0)/G_{\mathbb{P}}^{NN}(0)}, \quad \underline{b_{\mathbb{P}}^{ij} \equiv B_{\mathbb{P}}^{ij} - B_{\mathbb{P}}^{NN}} \quad (17)$$

and fit them to the RHICf data. In Table I, we list the

TABLE I. Numerical values of the parameters  $g_{\mathbb{P}}^{ij}$  and  $b_{\mathbb{P}}^{ij}$ . The first column lists the values of  $g_{\mathbb{P}}^{ij}$  with  $i$  and  $j$  given whereas the second column shows the values of  $b_{\mathbb{P}}^{ij}$ .

	$g_{\mathbb{P}}^{ij}$	$b_{\mathbb{P}}^{ij}[\text{GeV}^{-2}]$
$NN^*$	0.028	0.2
$\Delta\Delta^*$	-0.018	0
$N^*N^*$	0.10	0
$\Delta\Delta$	0.022	0
$\Delta^*\Delta^*$	0.079	0

Are these numbers consistent with those from the  $\pi^0$  cross sections?  $\rightarrow$  compare RHICf or low- $\sqrt{s}$  data

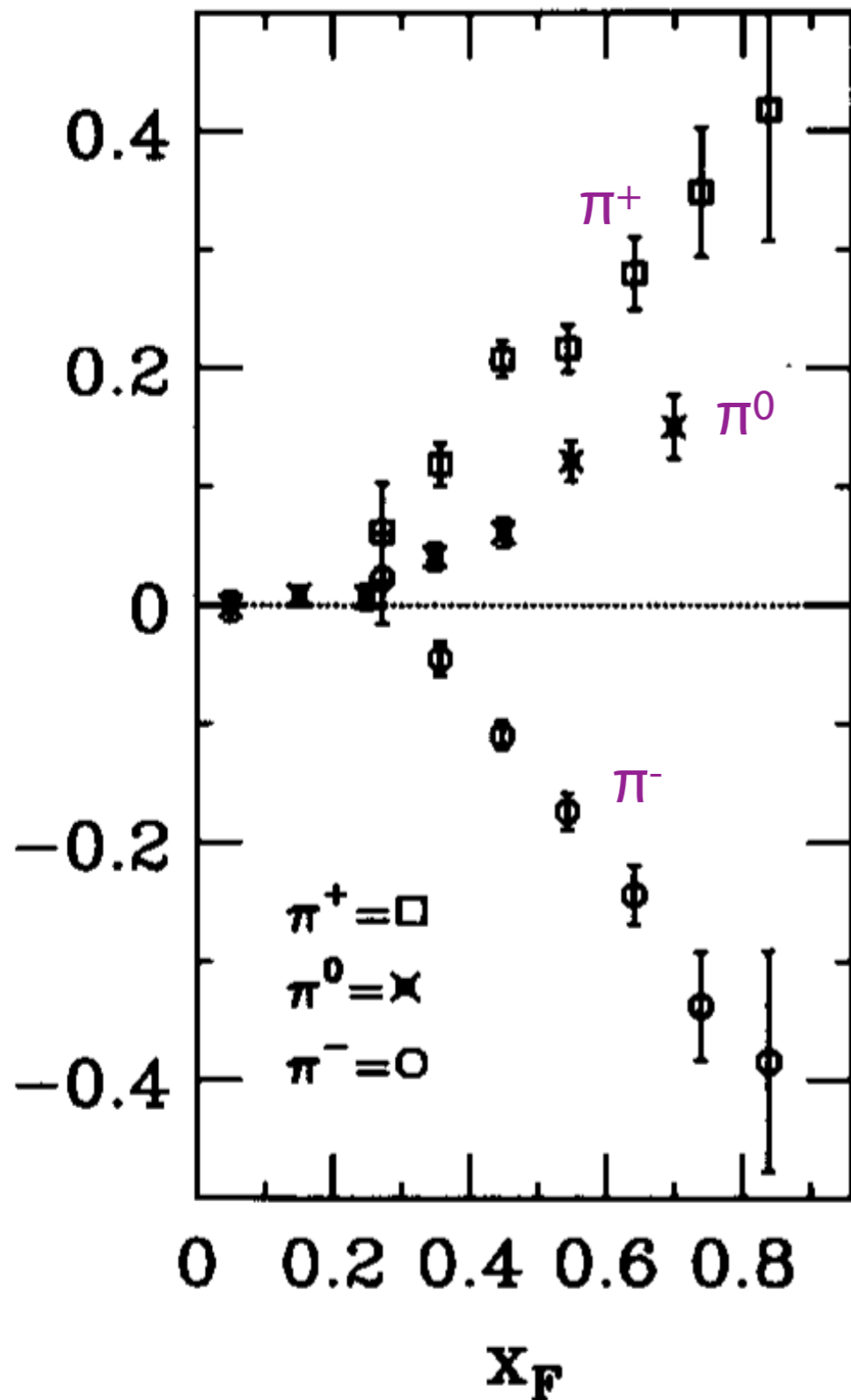
# $A_N(x_F, p_T)$ in $p^\uparrow p \rightarrow \pi X$ at $\sqrt{s} = 19.4$ GeV

E704 at  $\sqrt{s} = 19.4$  GeV

- Assuming we are in the phase space where the triple-regge diagram works reasonably,
  - $\pi^+, \pi^0$ : nucleon and  $\Delta$  exchanges
  - $\pi^-$ :  $\Delta$  exchanges
- Interesting to see how H-J Kim's model behaves for forward neutral and charged  $\pi$ s, for example in the phase space of E704
- Can estimate the BG contribution of the soft process to QCD-based models?

Inclusively measured  $A_N$  is the weighted sum of  $A_{Ni}$  for each process: 1-diff, 2-diff, non-diff, elastic, BG etc.

$$\langle A_N \rangle = \frac{\sum_i A_{Ni} \sigma_i}{\sum_i \sigma_i}$$



# Next fiscal year's plan

- An urgent need is reinforcement of the computing resources in KEK.
- Search for other processes possibly contributing to  $\pi^0$  cross section and asymmetry
- Implementation of the  $2\pi$  MAID model in the UPC simulation codes (no need to hurry up?)

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etc?			