

# ' $^{56}\text{Ni}$ problem' in Supernova Explosions

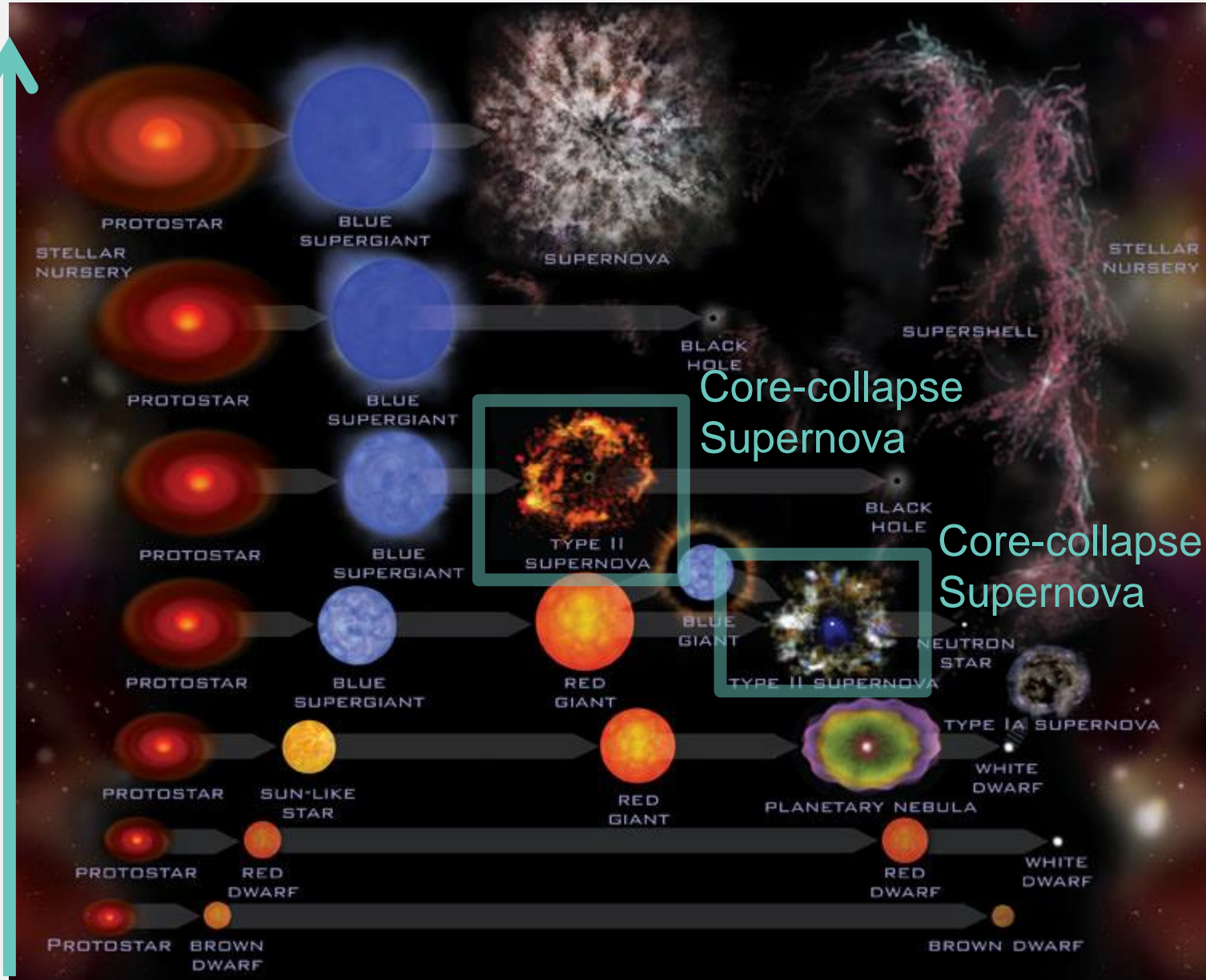
**Ryo Sawada** The University of Tokyo/ JSPS postdoctoral fellow

## Reference :

- “Nucleosynthesis Constraints on the Energy Growth Timescale of a Core-collapse Supernova Explosion”  
**Sawada & Maeda (2019), ApJ, 886, 47 (arXiv.1910.06972)**
- “A Consistent Modeling of Neutrino-driven Wind with Accretion Flow onto a Protoneutron Star and its Implications for  $^{56}\text{Ni}$  Production”  
**Sawada & Suwa (2021), ApJ, 908, 6 (arXiv.2010.05615)**
- “Constraints on the Explosion Timescale of Core-collapse Supernovae Based on Systematic Analysis of Light Curves”  
**Saito, Tanaka, Sawada, & Moriya (2022), ApJ 931, 153 (arXiv:2205.00624)**
- “Updating the  $^{56}\text{Ni}$  Problem in Core-collapse Supernova Explosion”  
**Sawada & Suwa (2023) arXiv:2301.03610**

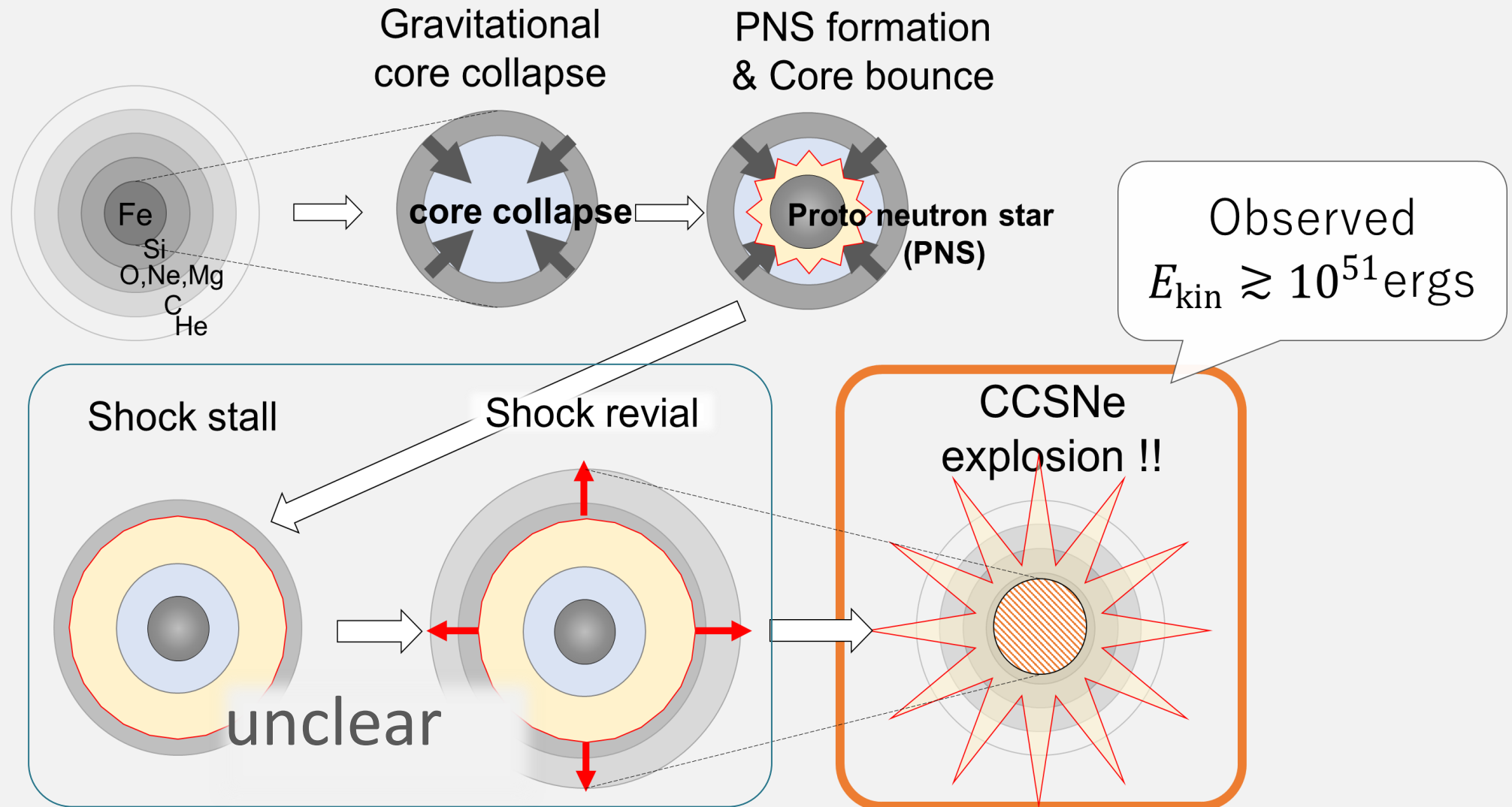
# What is the core-collapse supernova ?

Initial mass of the star ( $M_{ZAMS}$ ).



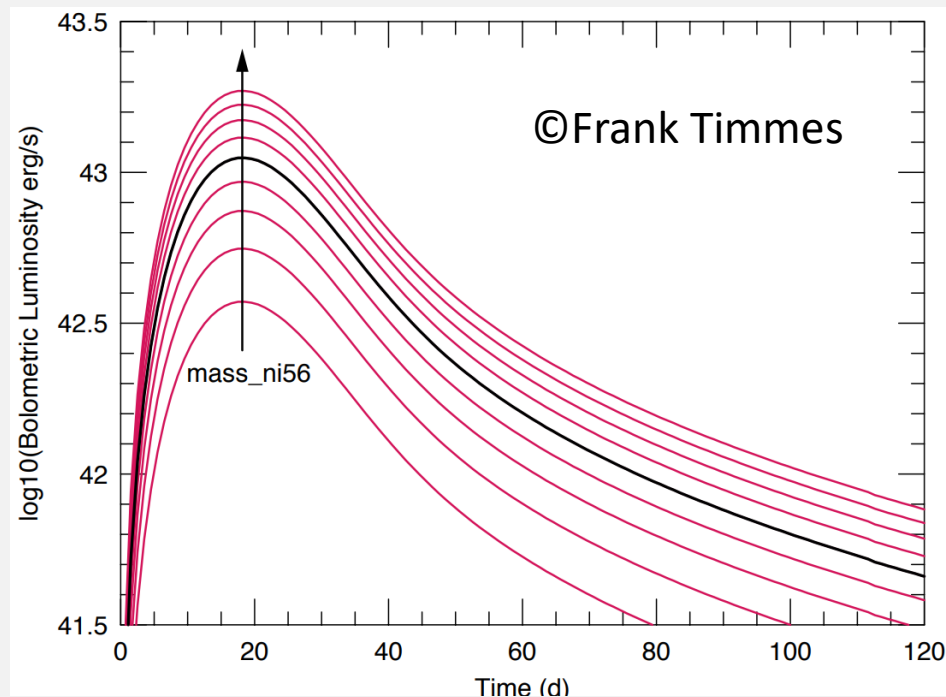
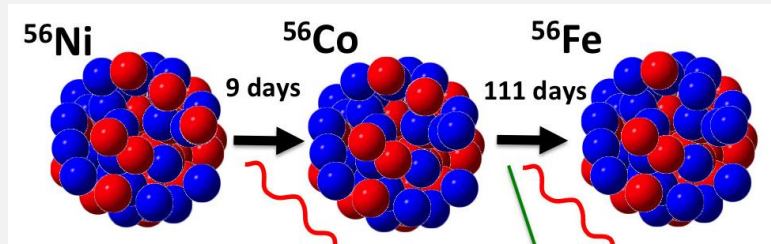
# What is the core-collapse supernova ?

- Standard scenario : Neutrino-driven model**



# Role of isotope $^{56}\text{Ni}$ in supernova explosions

- Radioactive decay heat of  $^{56}\text{Ni}$  is the energy source of supernova brightness (hereafter, refer  $^{56}\text{Ni}$  as 'nickel').



## SN1987A; Giordano(ISBN:0534424716)

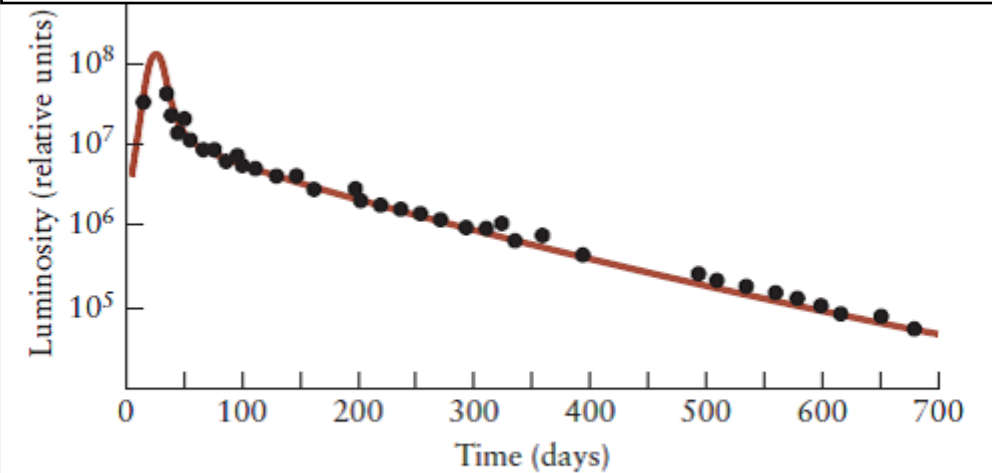
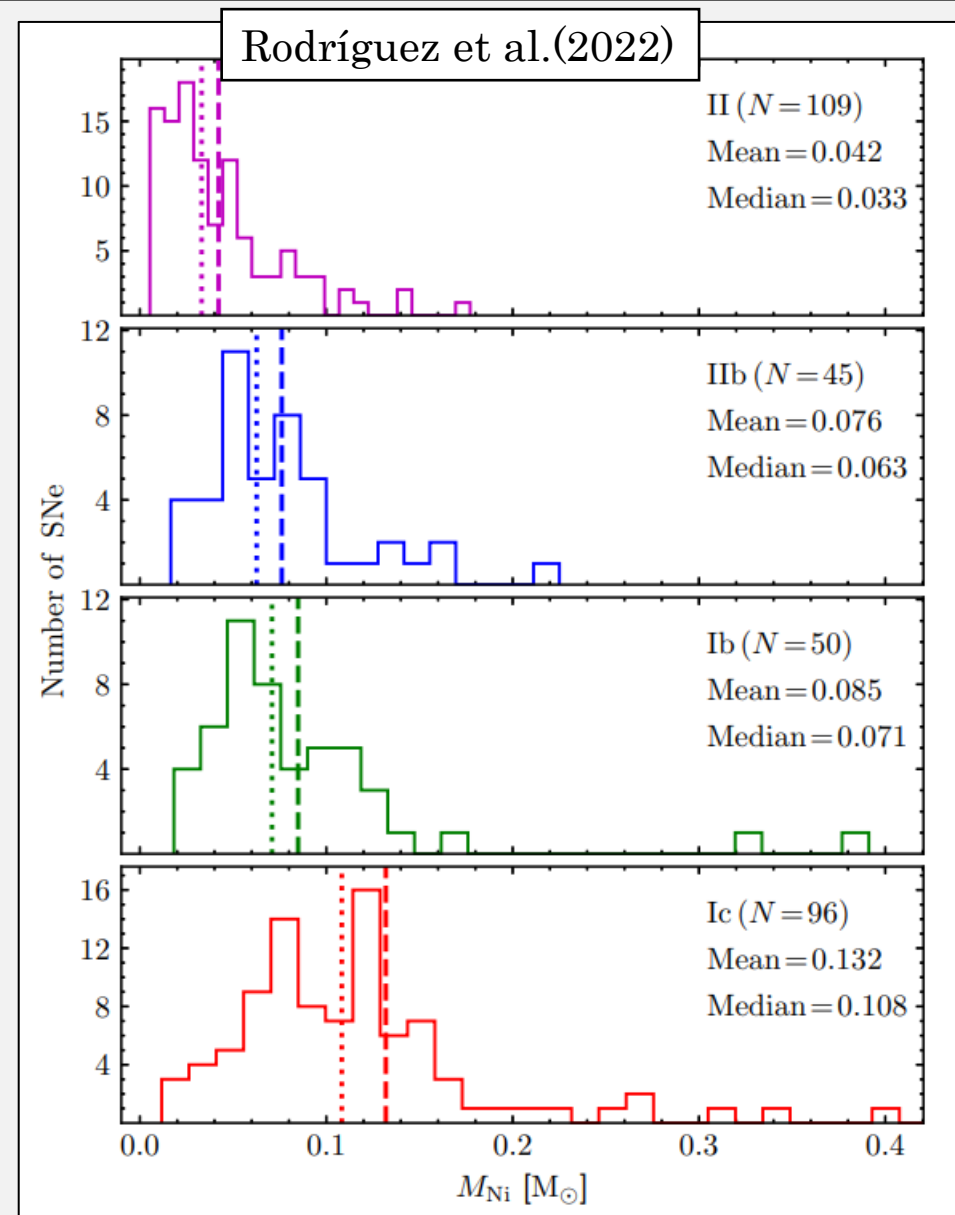
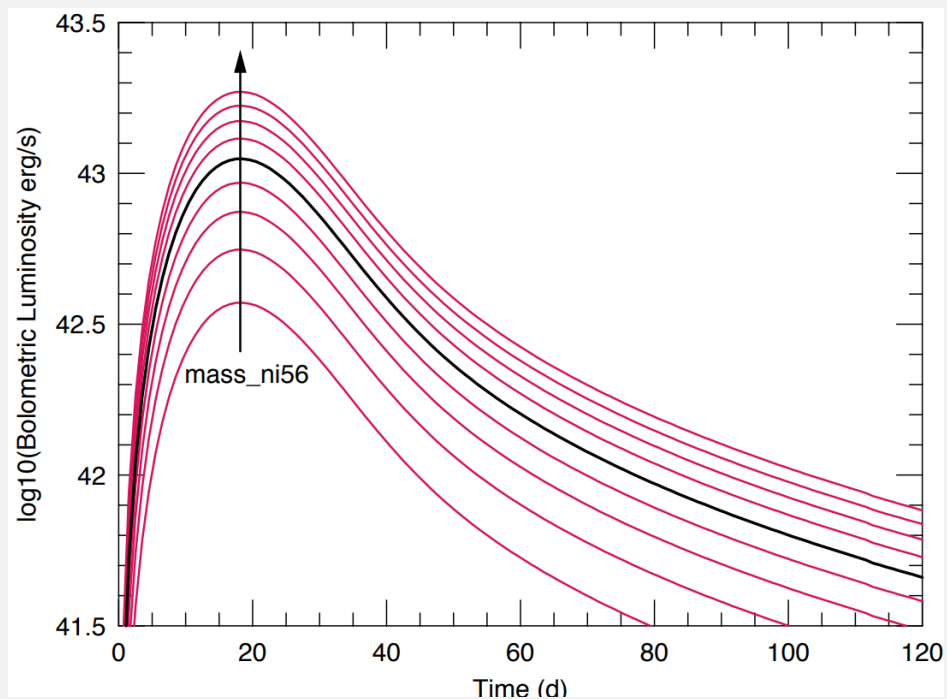


Figure P30.87 The light curve for Supernova 1987A.

- the amount of  $^{56}\text{Ni}$  synthesized can be estimated fairly accurately and easily from the SN light curve alone.

# Role of isotope $^{56}\text{Ni}$ in supernova explosions

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# Role of isotope $^{56}\text{Ni}$ in supernova explosions

- Light-curve calculation : Based on One-zone Arnett model (Arnett 1982)

$$\frac{\partial E_{\text{int}}(t)}{\partial t} = -P \frac{\partial V(t)}{\partial t} + \dot{Q}(t) - L(t).$$

$$\frac{\partial E_{\text{kin}}(t)}{\partial t} = P \frac{\partial V(t)}{\partial t}.$$

Assuming that the internal energy is dominated by radiation,

$$P \frac{\partial V(t)}{\partial t} = \frac{\epsilon}{3} \cdot 4\pi R_{\text{ej}}^2 v_{\text{ej}}(t) = \frac{E_{\text{int}}(t)}{R_{\text{ej}}} v_{\text{ej}}(t) = \frac{E_{\text{int}}(t)}{t_{\text{dyn}}}, \quad \left[ t_{\text{dyn}} = \frac{R_{\text{ej}}(t)}{v_{\text{ej}}(t)} \right]$$

When the luminosity is described by the spherical diffusion equation,

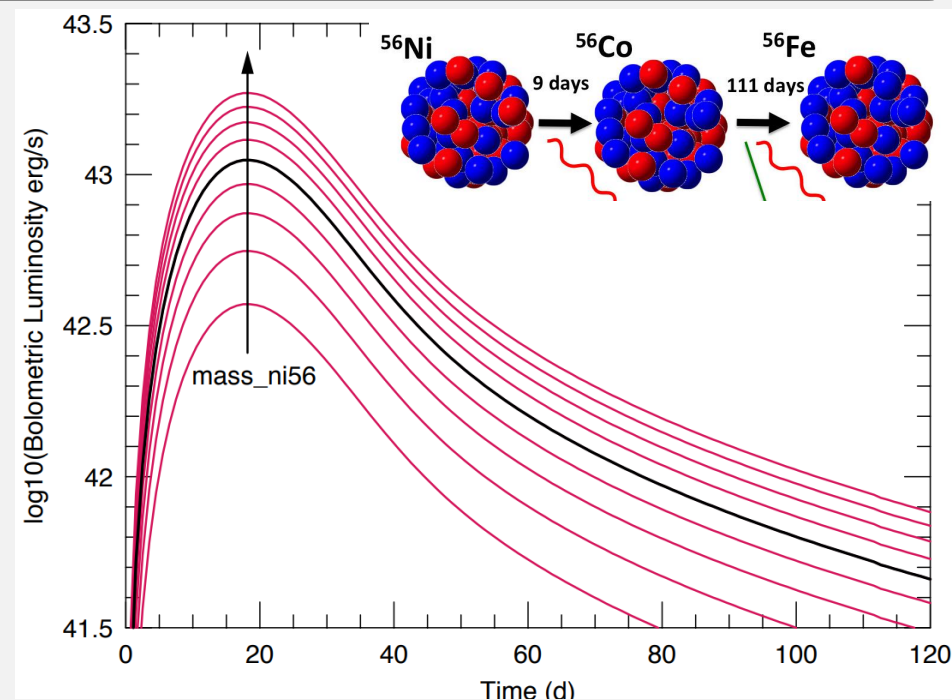
$$L(t) = -4\pi r^2 \frac{c}{3\kappa\rho} \frac{\partial e}{\partial r} = -4\pi r^2 \frac{c}{3\kappa\rho} \frac{\partial}{\partial r} \left( \frac{E_{\text{int}}(t)}{V(t)} \cdot \left( \frac{\pi \sin(\pi x)}{3x} \right) \right)$$

$$= E_{\text{int}} \cdot \frac{t_{\text{dyn}}}{t_{\text{diff}}^2}, \quad \left[ t_{\text{diff}} = \frac{3}{4\pi} \frac{\kappa M_{\text{ej}}}{c v_{\text{ej}} \xi} \right]$$

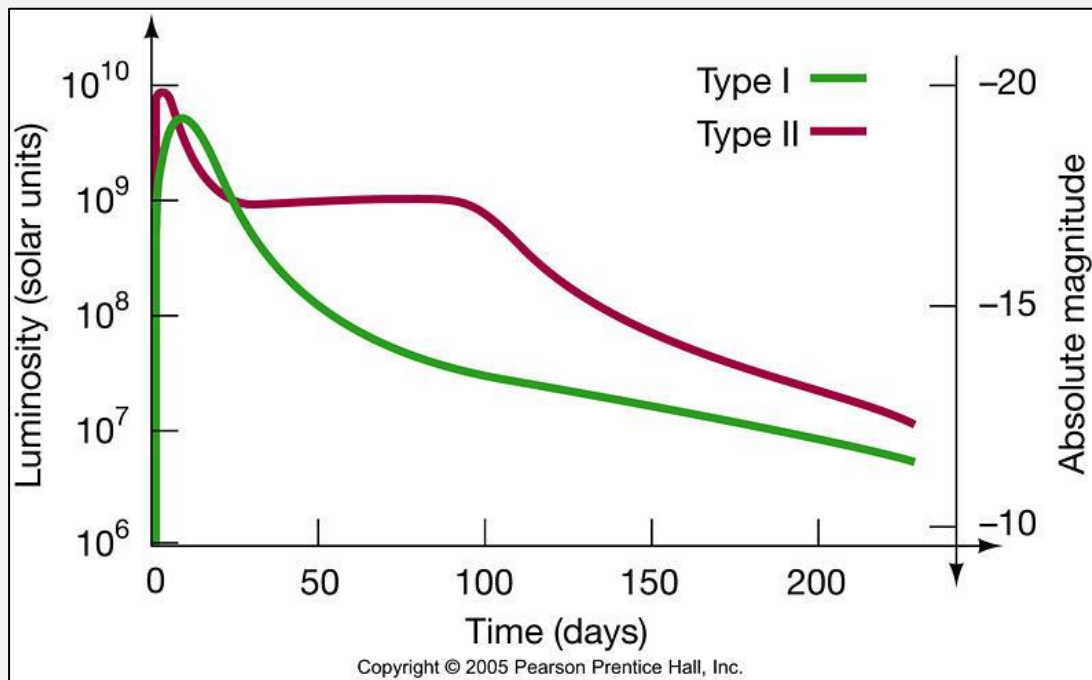
$$\frac{\partial E_{\text{int}}(t)}{\partial t} = -\frac{E_{\text{int}}(t)}{t_{\text{dyn}}} + \dot{Q}(t) - E_{\text{int}} \cdot \frac{t_{\text{dyn}}}{t_{\text{diff}}^2}$$

$$\frac{\partial E_{\text{kin}}(t)}{\partial t} = \frac{E_{\text{int}}(t)}{t_{\text{dyn}}}.$$

$$\dot{Q}(t) = f_{\text{dep}} \cdot [M(^{56}\text{Ni}) \cdot q_{\text{Ni}}(t)]$$



# Role of isotope $^{56}\text{Ni}$ in supernova explosions

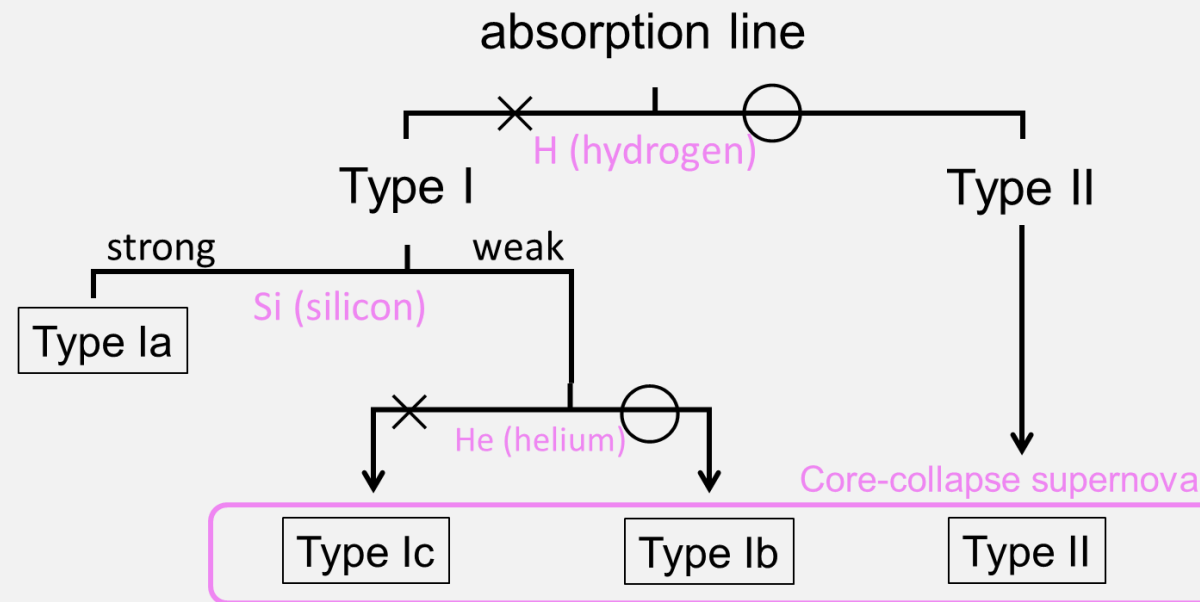


Arnett model : for Type-I Supernova

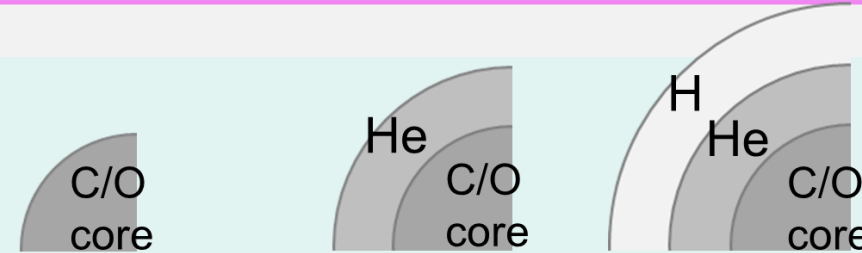
$$\frac{\partial E_{\text{int}}(t)}{\partial t} = -\frac{E_{\text{int}}(t)}{t_{\text{dyn}}} + \dot{Q}(t) - E_{\text{int}} \cdot \frac{t_{\text{dyn}}}{t_{\text{diff}}^2}$$

$$\frac{\partial E_{\text{kin}}(t)}{\partial t} = \frac{E_{\text{int}}(t)}{t_{\text{dyn}}}$$

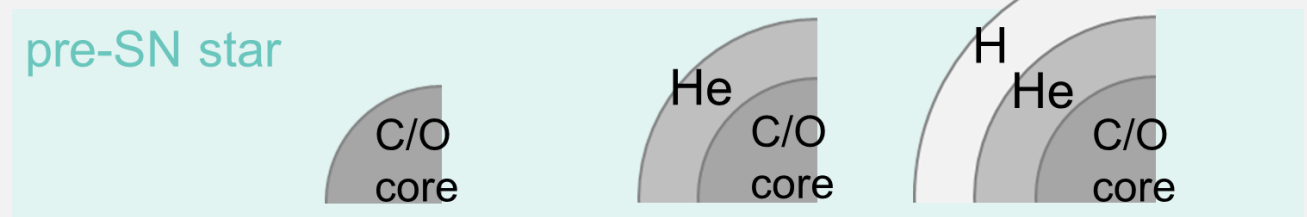
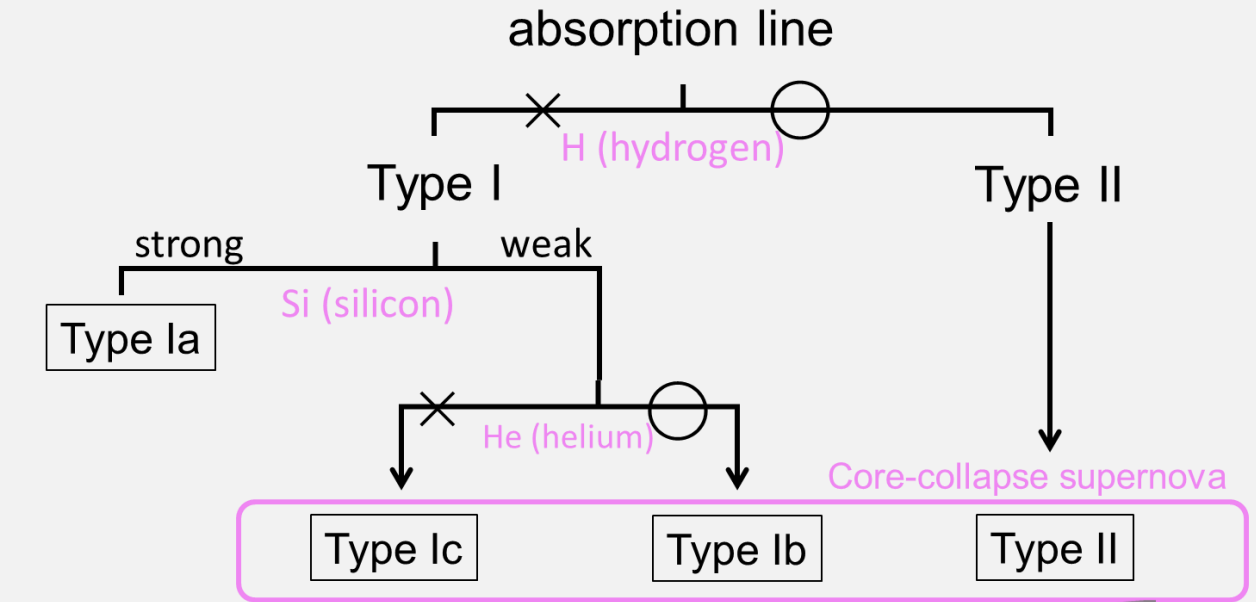
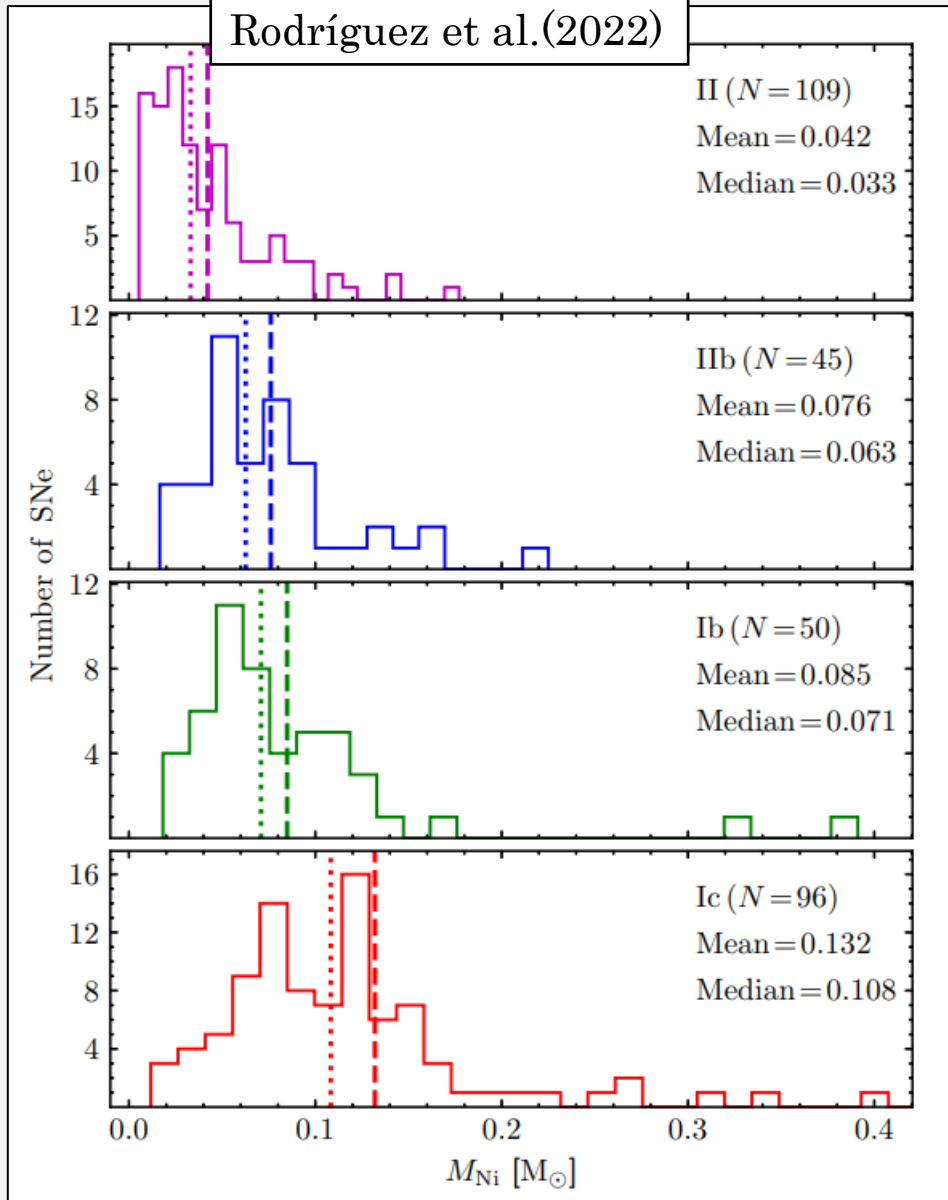
$$\dot{Q}(t) = f_{\text{dep}} \cdot [M(^{56}\text{Ni}) \cdot q_{\text{Ni}}(t)] + Q_{\text{heat}}$$



pre-SN star



# Role of isotope $^{56}\text{Ni}$ in supernova explosions





# Where is the synthesized amount of $^{56}\text{Ni}$ determined?

**[ESTIMATE]** how much explosive  $^{56}\text{Ni}$  nucleosynthesis in the CCSN

$$M(^{56}\text{Ni}) \approx [\text{Mass contained in region: } T_{\text{peak}} > 5.0 \times 10^9 \text{ [K]}] - [\text{Central compact object mass}]$$

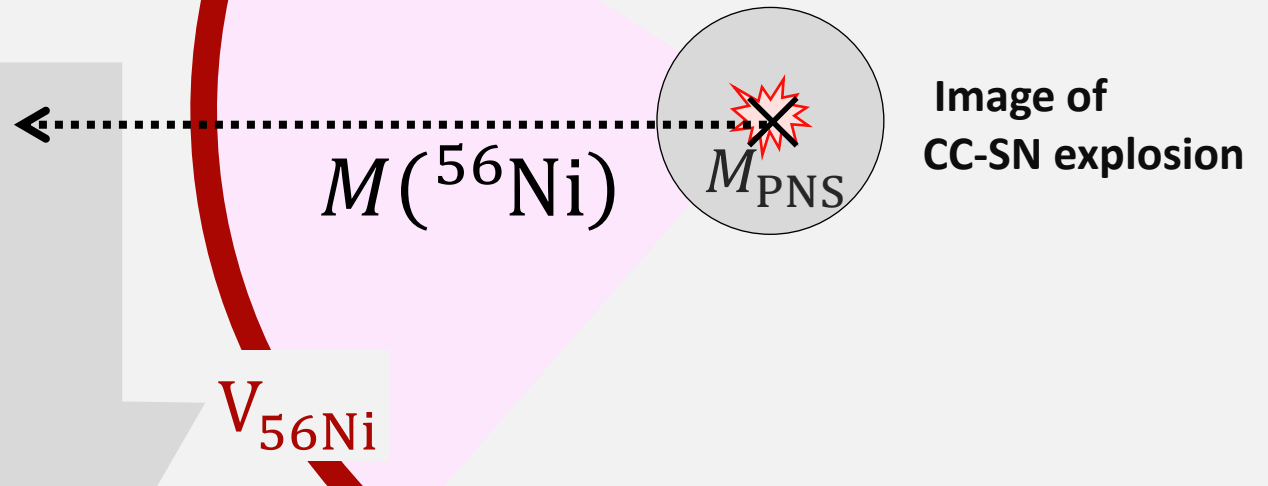
## Fire-ball model

- (1) radiation dominant,
- (2) isothermal @post-shock,
- (3) adiabatic expansion.

$$E_{\text{expl.}} = (aT^4) \times \left( \frac{4\pi}{3} r_{\text{shock}}^3 \right)$$

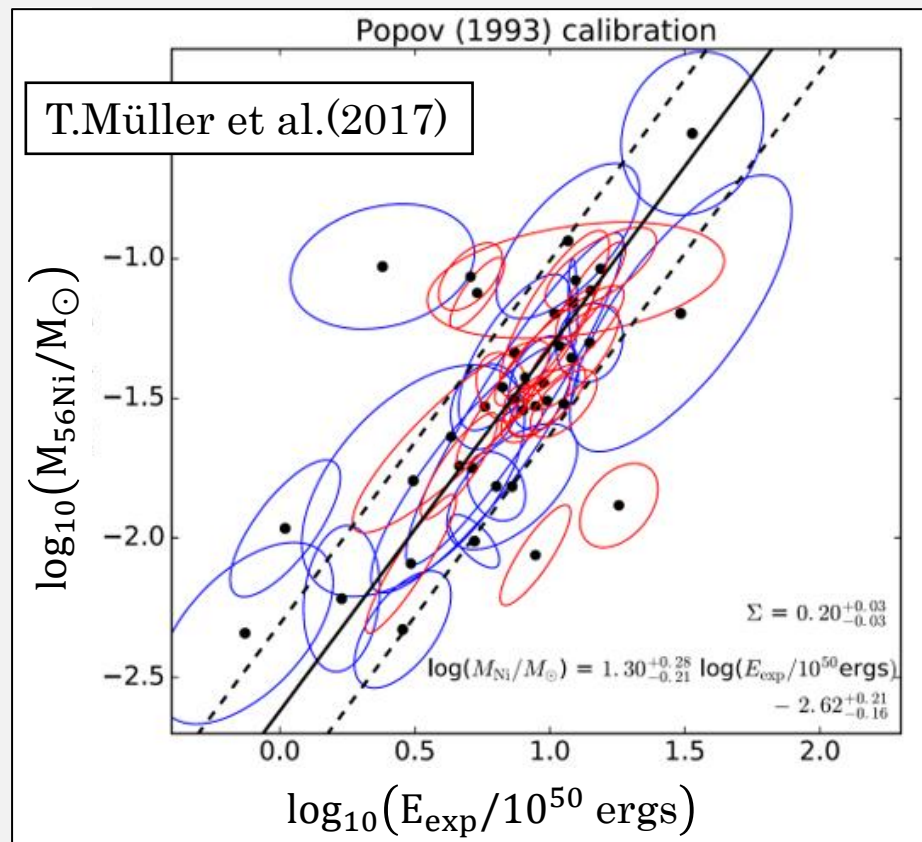
→ when  $T = 5.0 \times 10^9 \text{ [K]}$ , then  $V_{56\text{Ni}} \propto (E_{\text{expl.}} / 10^{51})$

$$\therefore M(^{56}\text{Ni}) \propto \begin{cases} 1. \text{ explosion energy. (How much extends the } ^{56}\text{Ni synthesis region? )} \\ 2. \text{ compactness. (How much mass is contained in the } ^{56}\text{Ni synthesis region? )} \end{cases}$$



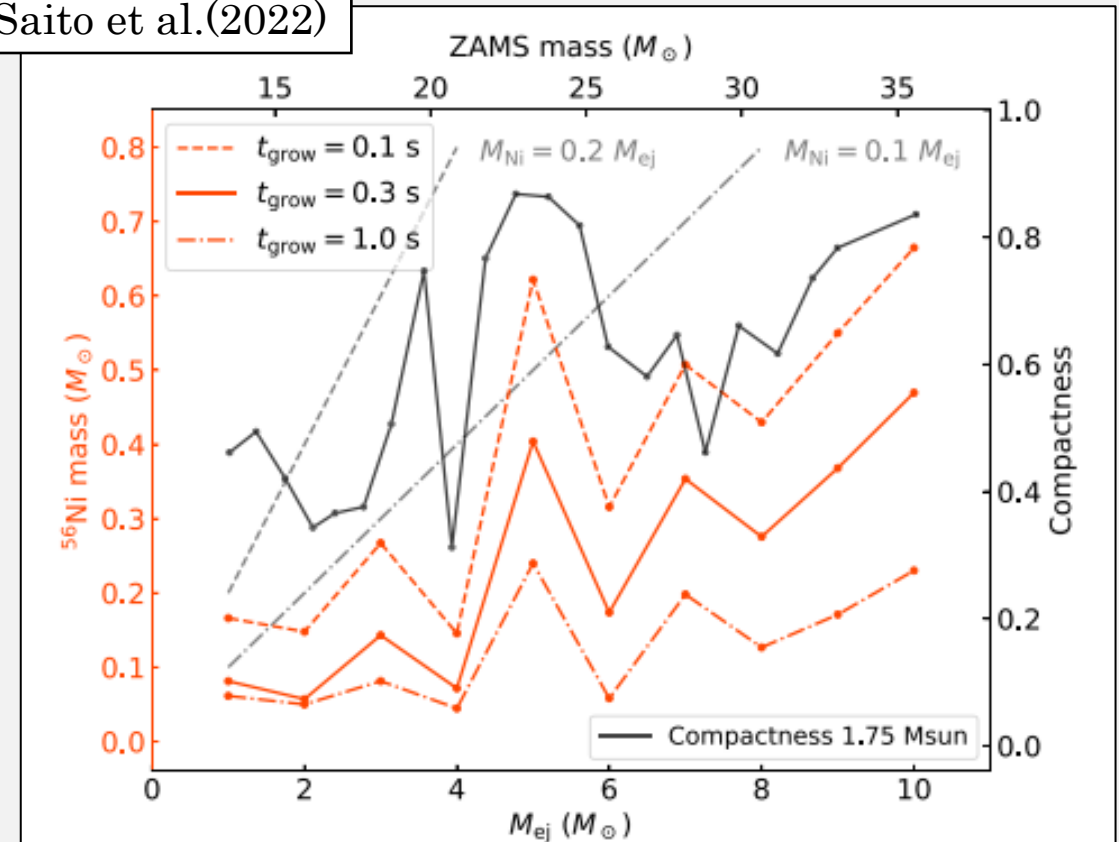
# Where is the synthesized amount of $^{56}\text{Ni}$ determined?

## • Observational



## • Theoretical

Saito et al.(2022)



$\therefore M(^{56}\text{Ni}) \propto \left\{ \begin{array}{l} \mathbf{1. explosion energy.} \text{ (How much extends the } ^{56}\text{Ni} \text{ synthesis region? )} \\ \mathbf{2. compactness.} \text{ (How much mass is contained in the } ^{56}\text{Ni} \text{ synthesis region? )} \end{array} \right.$

[topic 1 ] Can modern supernova simulations synthesize sufficient  $^{56}\text{Ni}$ ?

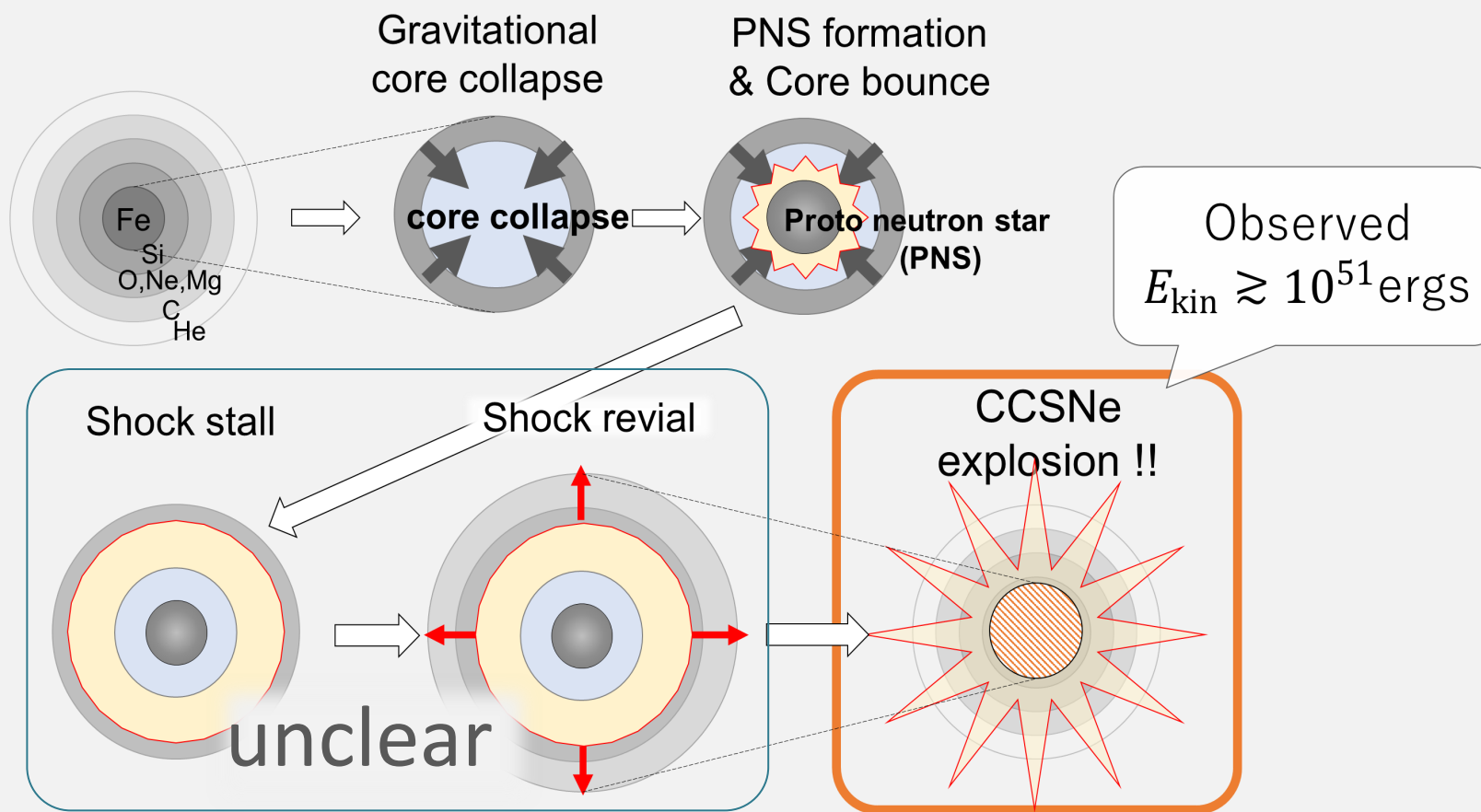
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# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

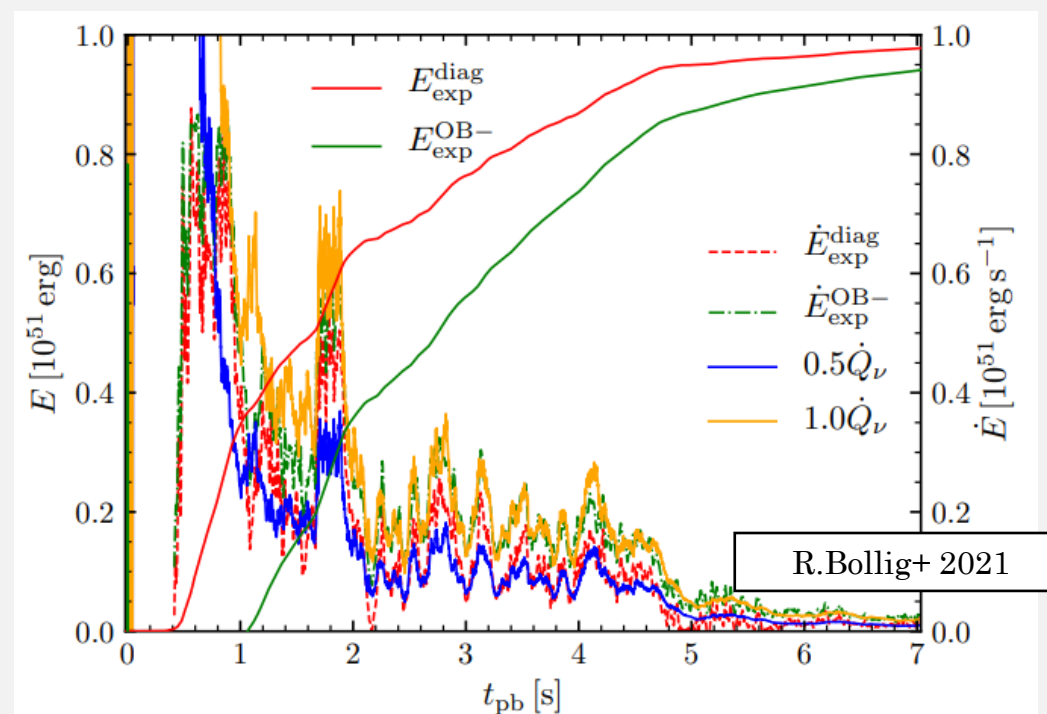
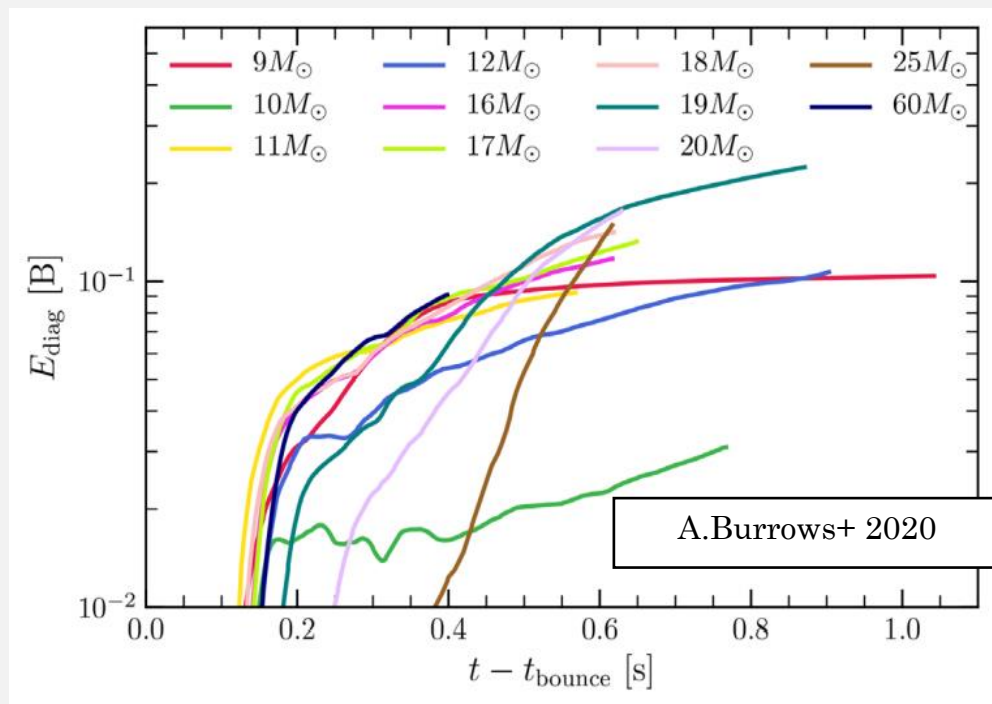
## • Standard scenario : Neutrino-driven model



\*unclear : Can reach to  $10^{51}$  [erg] ? (see, e.g., Janka 2012, and references therein)

# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

- ✓ **The state-of-the-art simulations** employ Multi-D / Full-Boltzmann  $\nu$ -transport / GR-effect etc.
- ✓ Most, if not all, of these simulations do not reach sufficient explosion energy.
- ✓ those simulations now suggest a "slower" explosion than previously thought.



Define :

$t_{\text{grow}}$  : timescale up to  $10^{51}$  [erg]

$t_{\text{grow}} \gtrsim 1$  [s]

# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

## • Our work

motivation

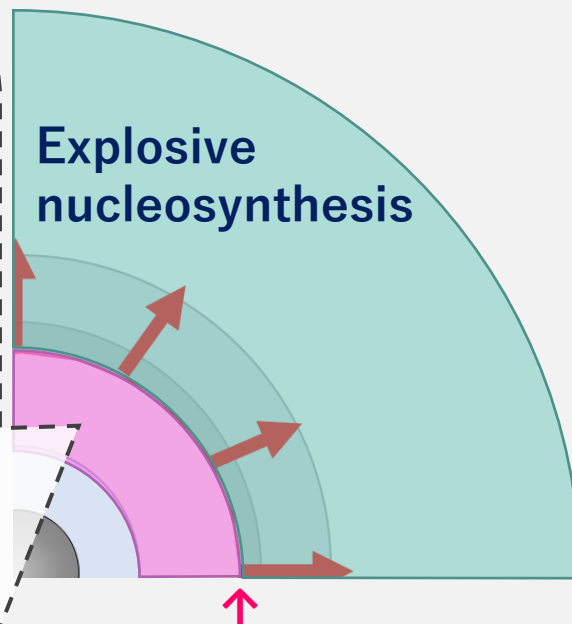
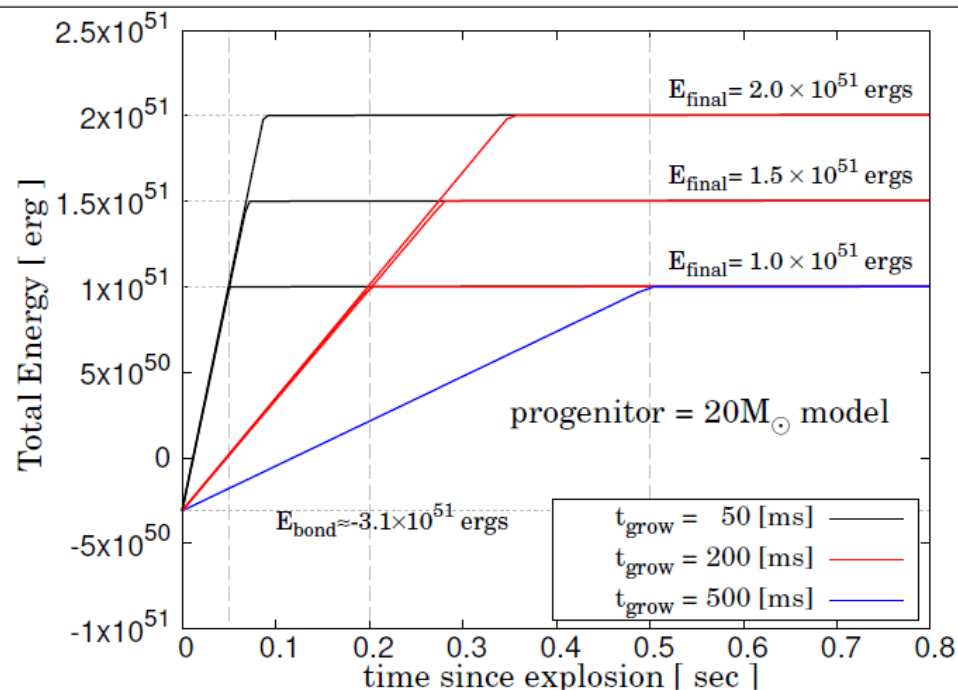
Does explosion timescale ( $t_{\text{grow}}$ ) affect nucleosynthesis?

simulation

1D hydrodynamics and nucleosynthesis  
with explosion timescale as a parameter

expl. model

Inject thermal energy  $\dot{E}_{\text{exp}}$  into pre-SN stars



Injection Boundary :  $Y_e < 0.48$

# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

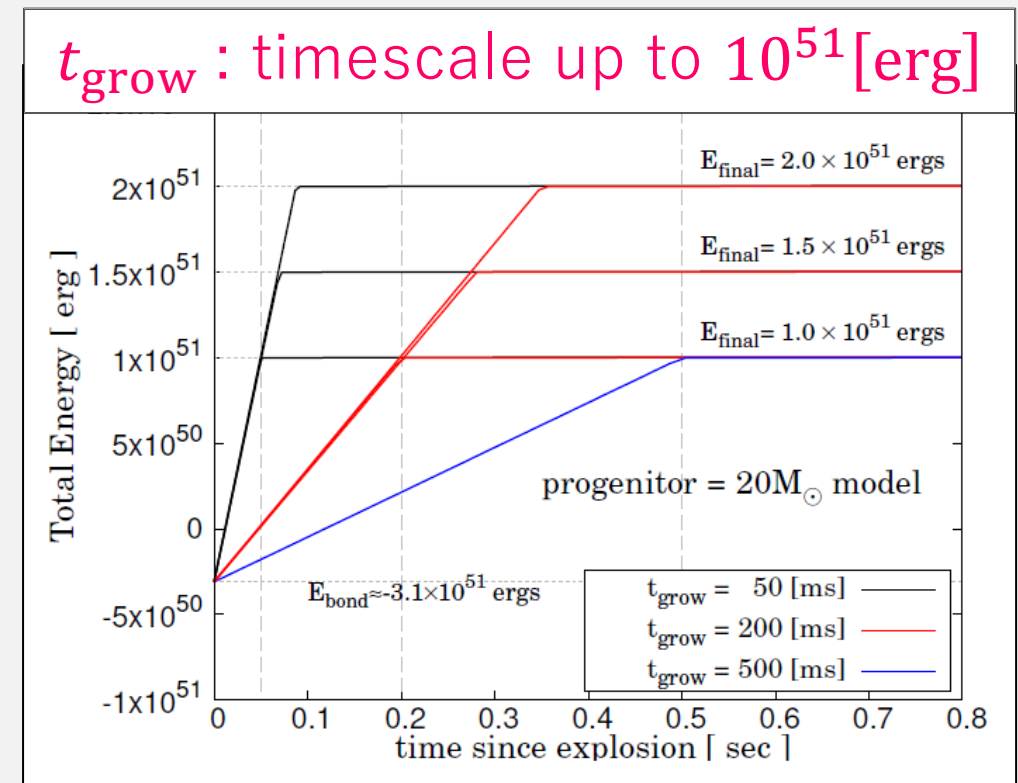
- **Our work** motivation Does explosion timescale ( $t_{\text{grow}}$ ) affect nucleosynthesis?

↓

simulation

1D hydrodynamics and nucleosynthesis  
with explosion timescale as a parameter

- ✓ model: thermal energy  $\dot{E}_{\text{expl}}$  injected into the surface of proto-neutron stars
- ✓ Progenitor :  $M_{\text{ZAMS}} = 15, 20, 25 M_{\odot}$
- ✓ hydrodynamics : based on “bl-code”.
  - Hydrodynamics : Newtonian
  - EoS : Helmholtz
  - 21-isotope  $\alpha$ -reaction
- ✓ nucleosynthesis (post-process) : 640-isotopes reaction



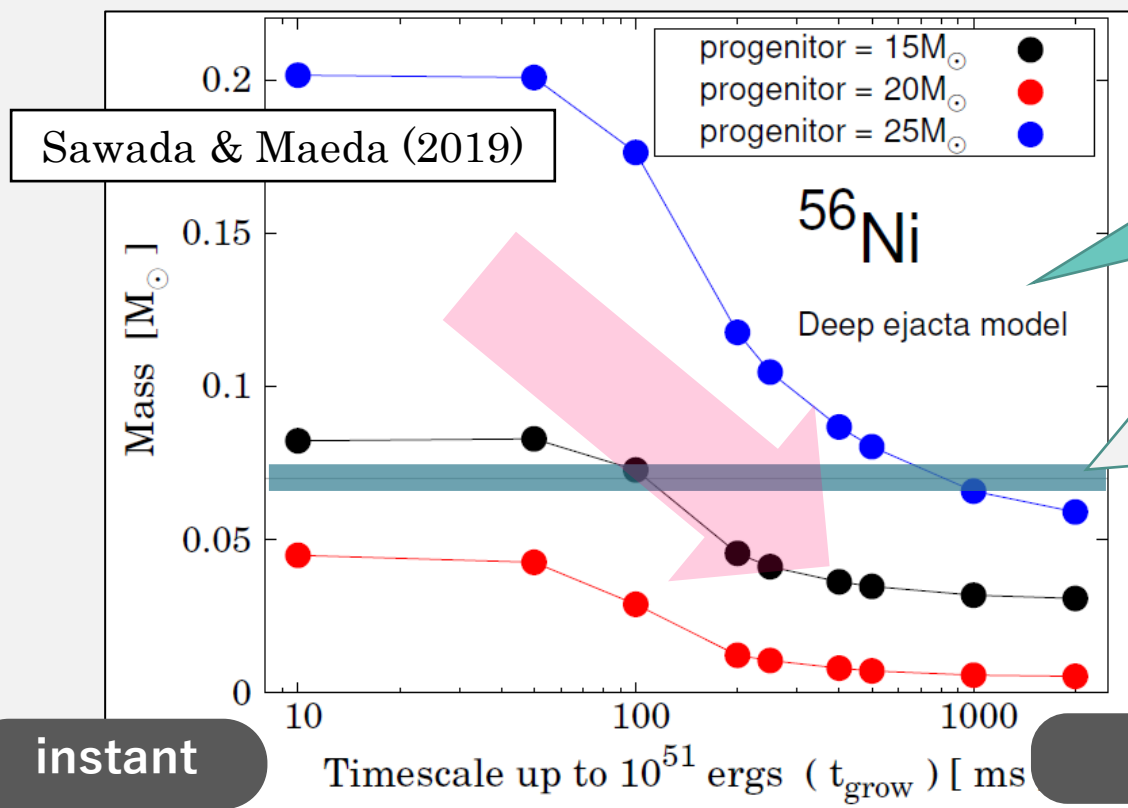
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- **Our work** motivation Does explosion timescale ( $t_{\text{grow}}$ ) affect nucleosynthesis?

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$t_{\text{grow}}$ : timescale up to  $10^{51}$  [erg]



synthesized amount =  
maximum value that can be ejected.

$0.07M_{\odot}$ ; typical value  
(eg., 1987A, 1993J, 2002ap...)

"Slow" explosions suppress  $M(^{56}\text{Ni})$   
→ unfavorable trend for observation



# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

(1) radiation dominant & isothermal @post-shock region,

Suwa, Tominaga, & Maeda (2019)

Sawada & Maeda (2019)

(2) adiabatic/constant vel. expansion ( $r_{\text{shock}} = v_{\text{shock}} \cdot t$ ),

$$E_{\text{exp}} = (aT^4) \times \left( \frac{4\pi}{3} r_{\text{shock}}^3 \right), \quad \Rightarrow T_{\text{peak}} \propto t^{-3/4}$$

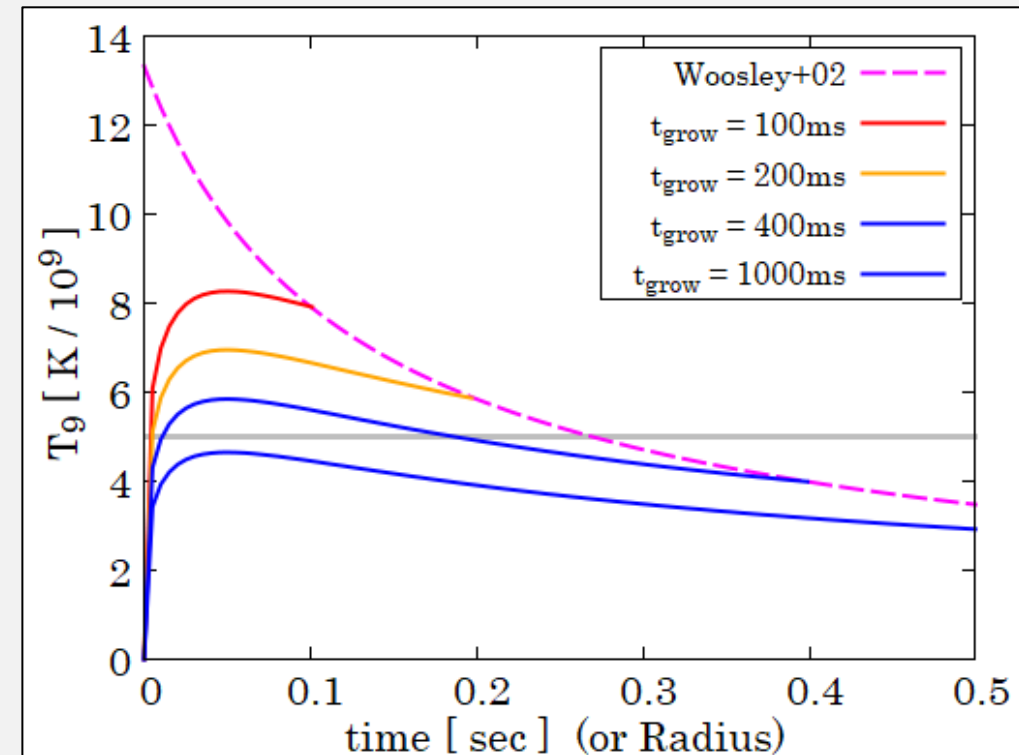
✓ When the explosion is sufficiently instantaneous, then

Deposit  $E_{\text{exp}} = 10^{51} \text{erg}$  from the initial setup.

e.g., Woosley+ 2002

✓ When taking into account the growth timescale of the explosion energy, then

$$E_{\text{exp}}(t) = \frac{10^{51} \text{erg}}{t_{\text{grow}}} \cdot t \quad \text{this work}$$



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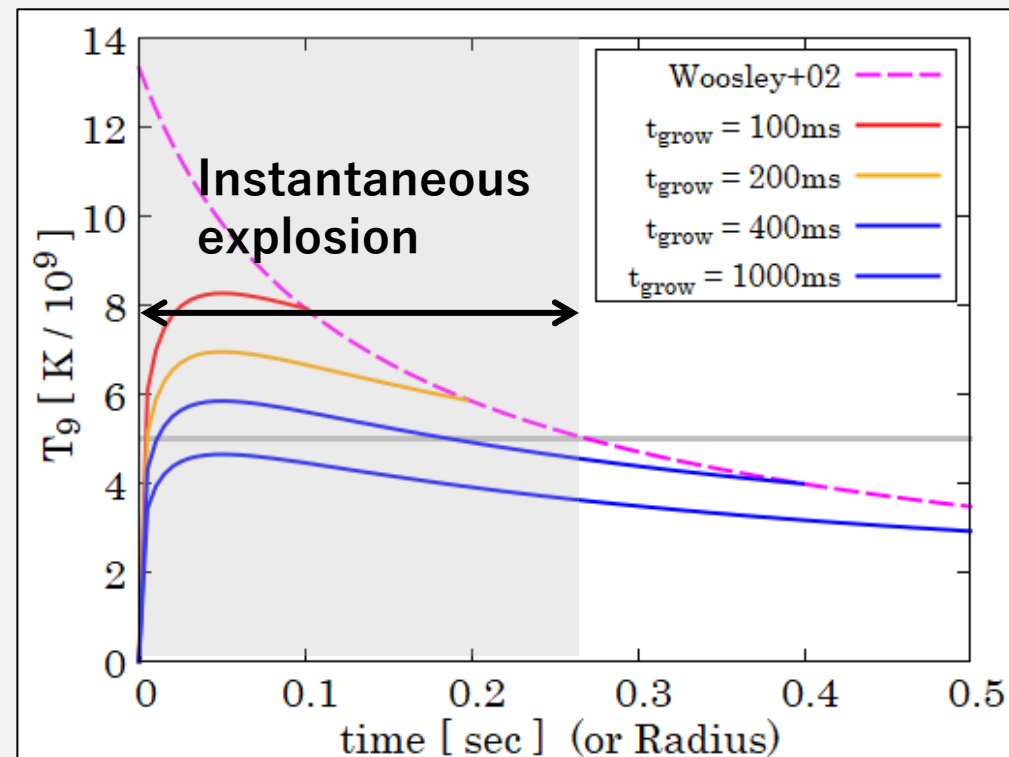
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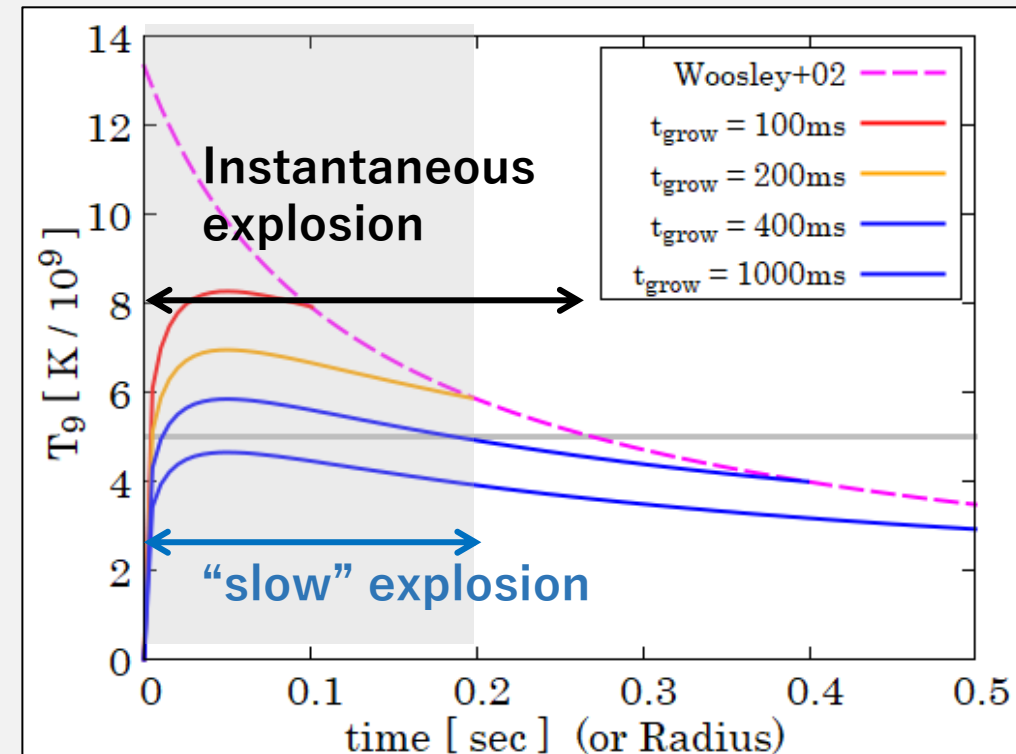
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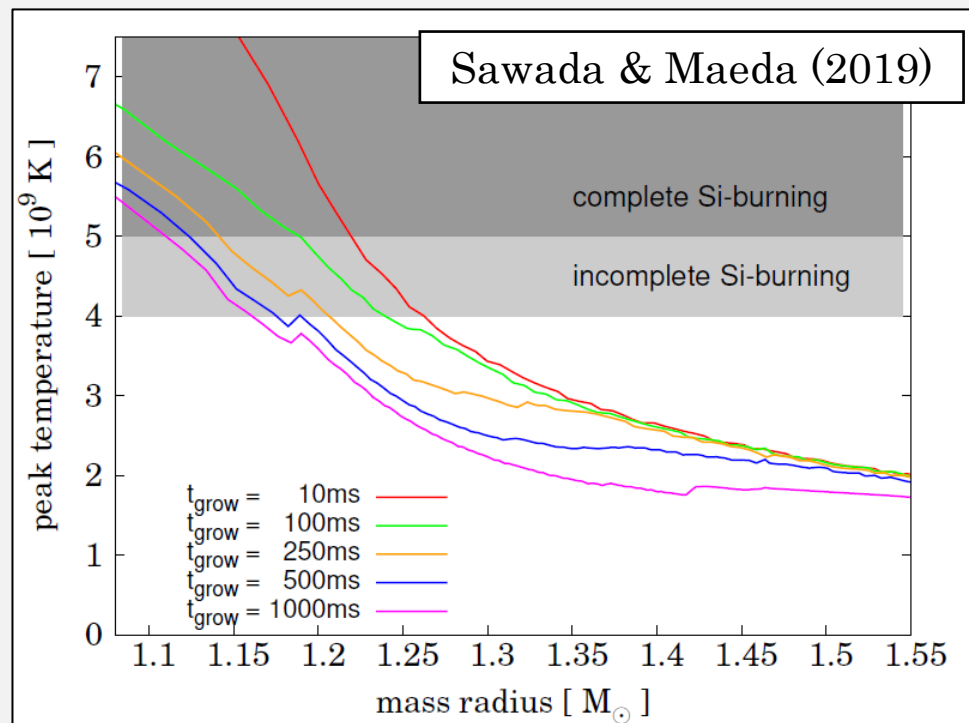
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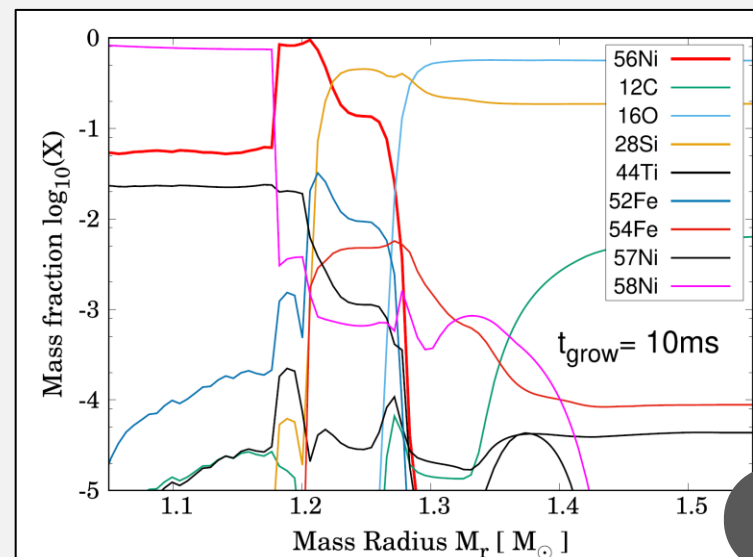
# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

## • Peak temperature

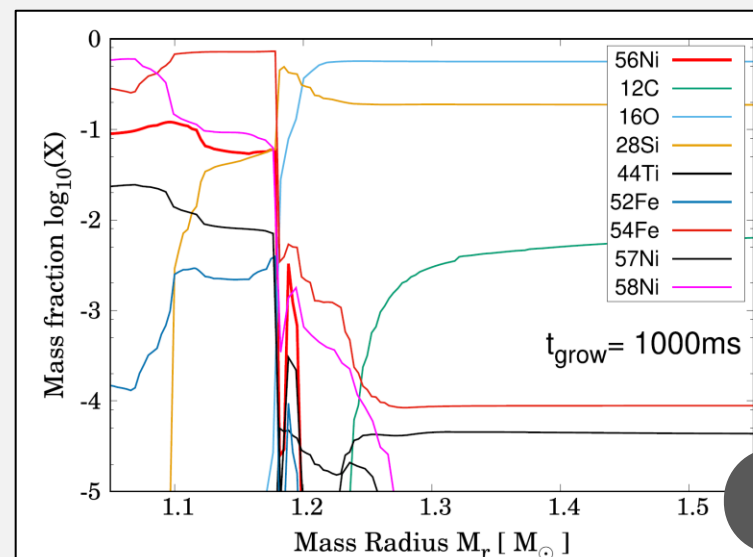
$t_{\text{grow}} = 10[\text{ms}]$



$t_{\text{grow}} = 1000[\text{ms}]$



Instant expl.



'slow' expl.

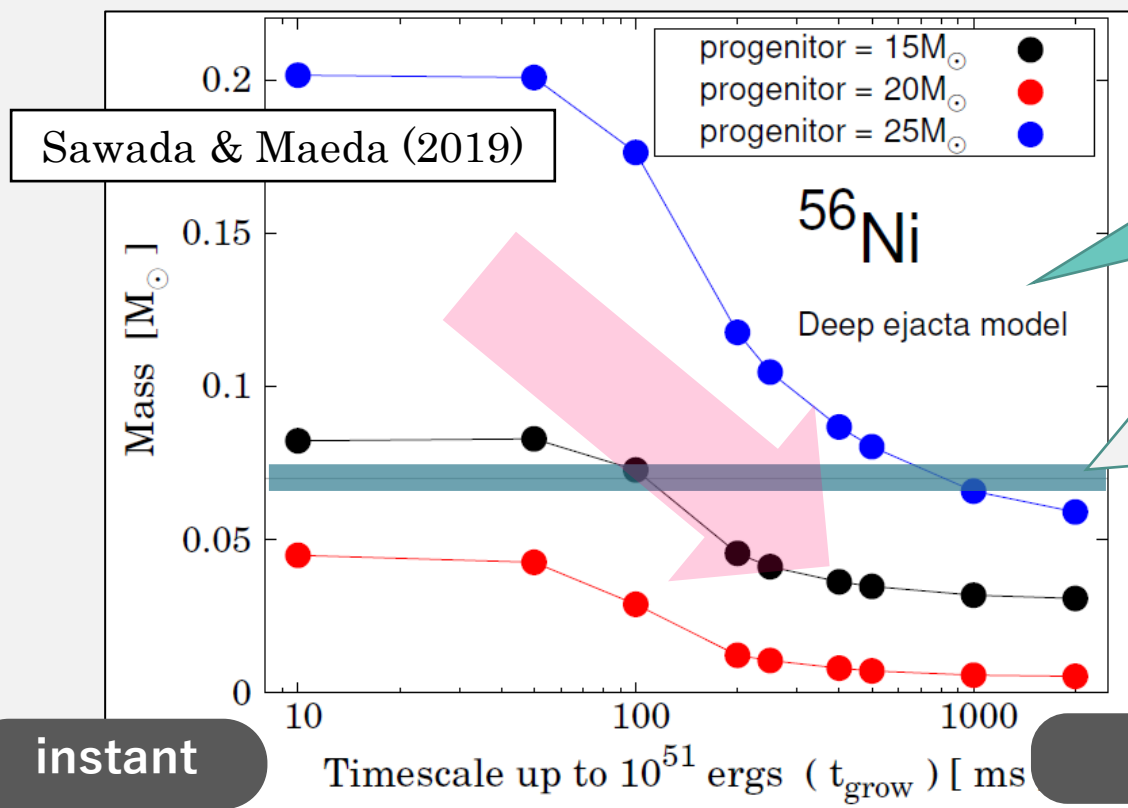
# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

- **Our work** motivation Does explosion timescale ( $t_{\text{grow}}$ ) affect nucleosynthesis?

simulation

1D hydrodynamics and nucleosynthesis  
with explosion timescale as a parameter

$t_{\text{grow}}$ : timescale up to  $10^{51}$  [erg]



synthesized amount =  
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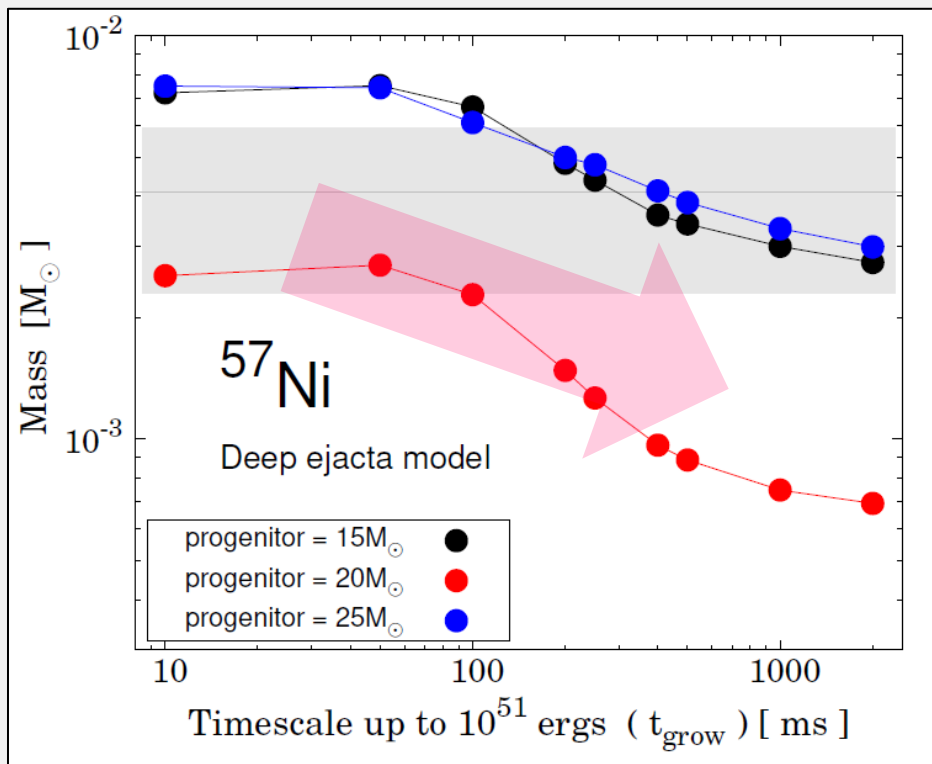
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"Slow" explosions suppress  $M(^{56}\text{Ni})$

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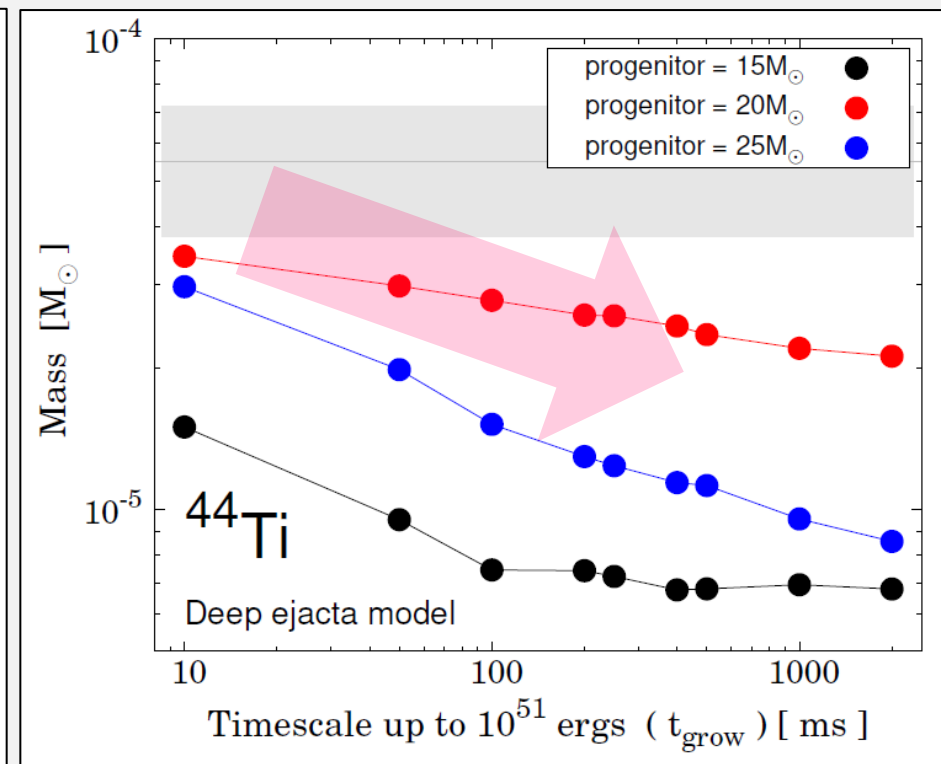
# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

✂ note : This model is not a fine-tuned model to SN1987A



Instant

Slow



Instant

Slow

Note: Multi-D effect may enhance  $M(^{44}\text{Ti})$   
(Nagataki et al. 1998; Maeda & Nomoto 2003).

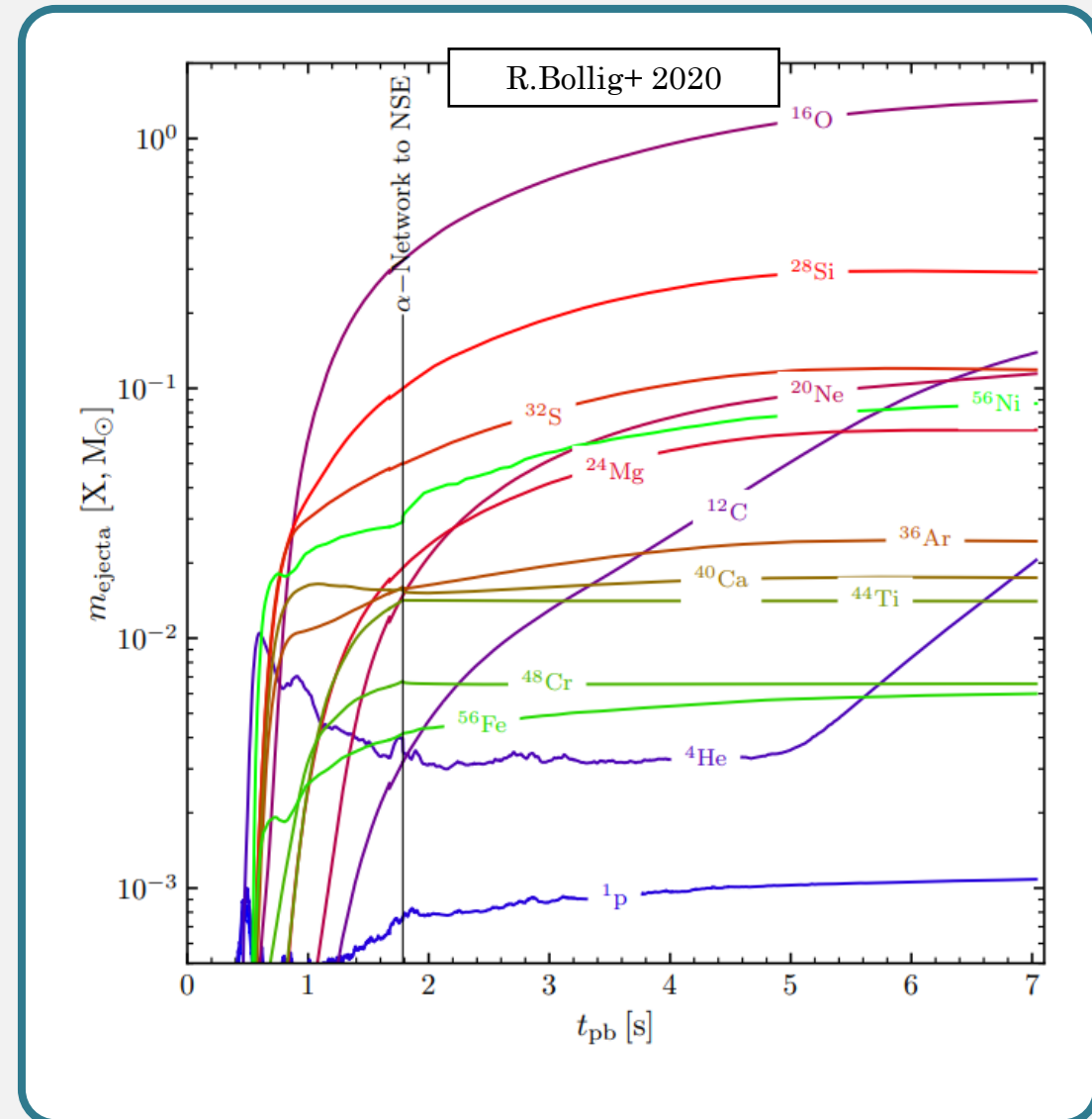
# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

- NOTE (1): all models ?**

some models in the state-of-the-art simulations have succeeded in producing the typical mass  $0.07M_{\odot}$  of  $^{56}\text{Ni}$  in CCSNe,

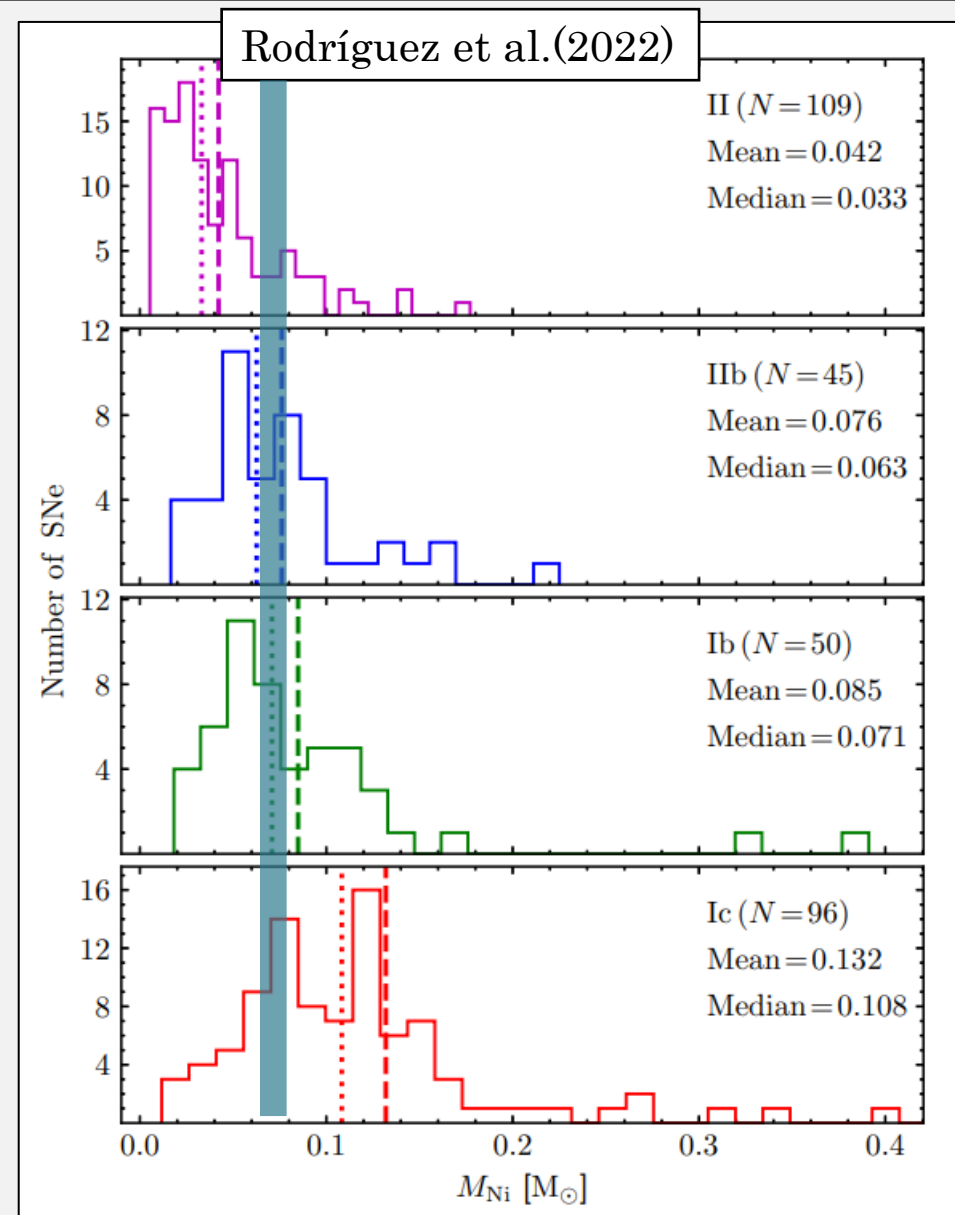
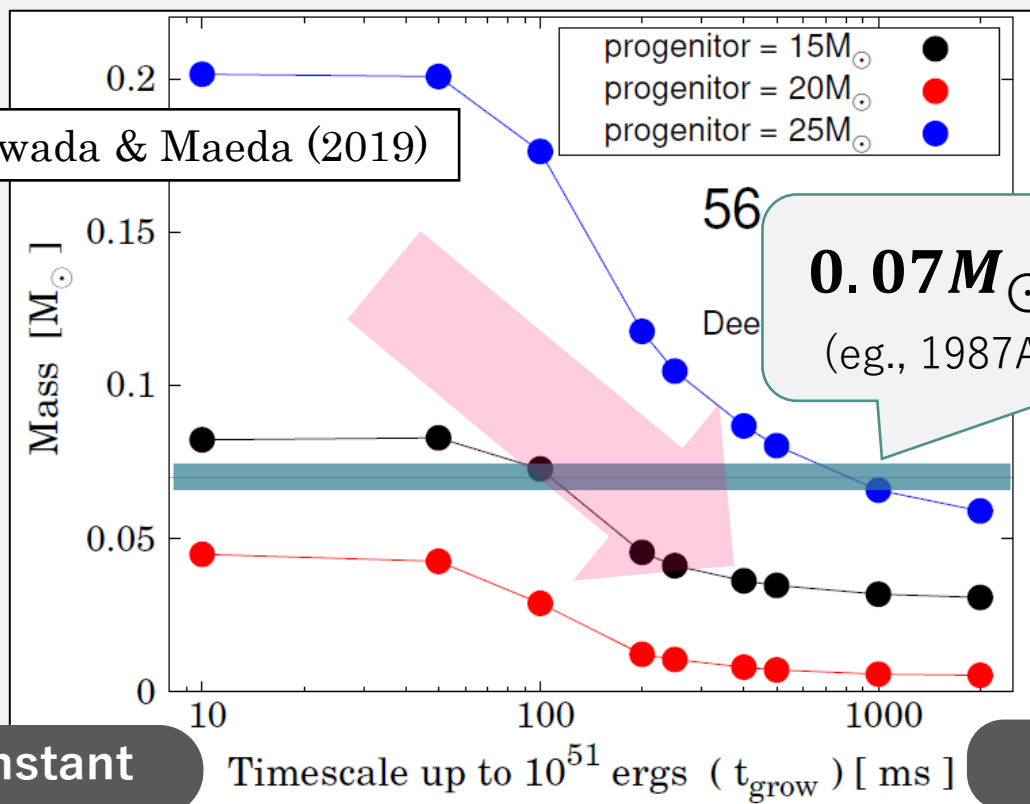
## But ‘nickel mass problem’ (Ni problem)

→ unclear whether we can reproduce sufficient  $^{56}\text{Ni}$  amount as a canonical nature.



# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

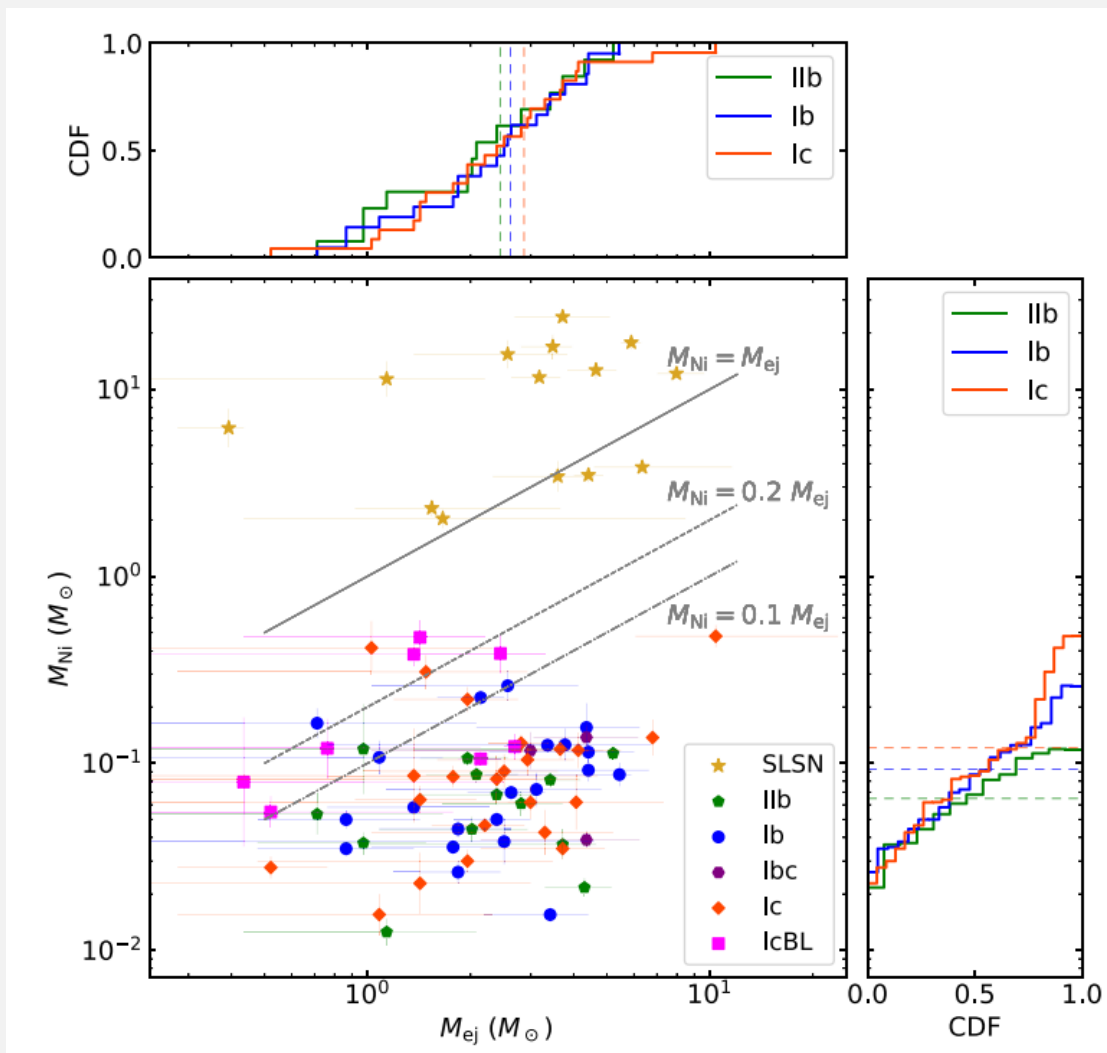
- NOTE (2): choice of typical value?**





# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

## • NOTE (2): choice of typical value?



## How to estimate the progenitor structure before the explosion

Type Ib

[ejecta mass]

+ [proto-NS mass] = He C/O core

Type Ic

[ejecta mass]

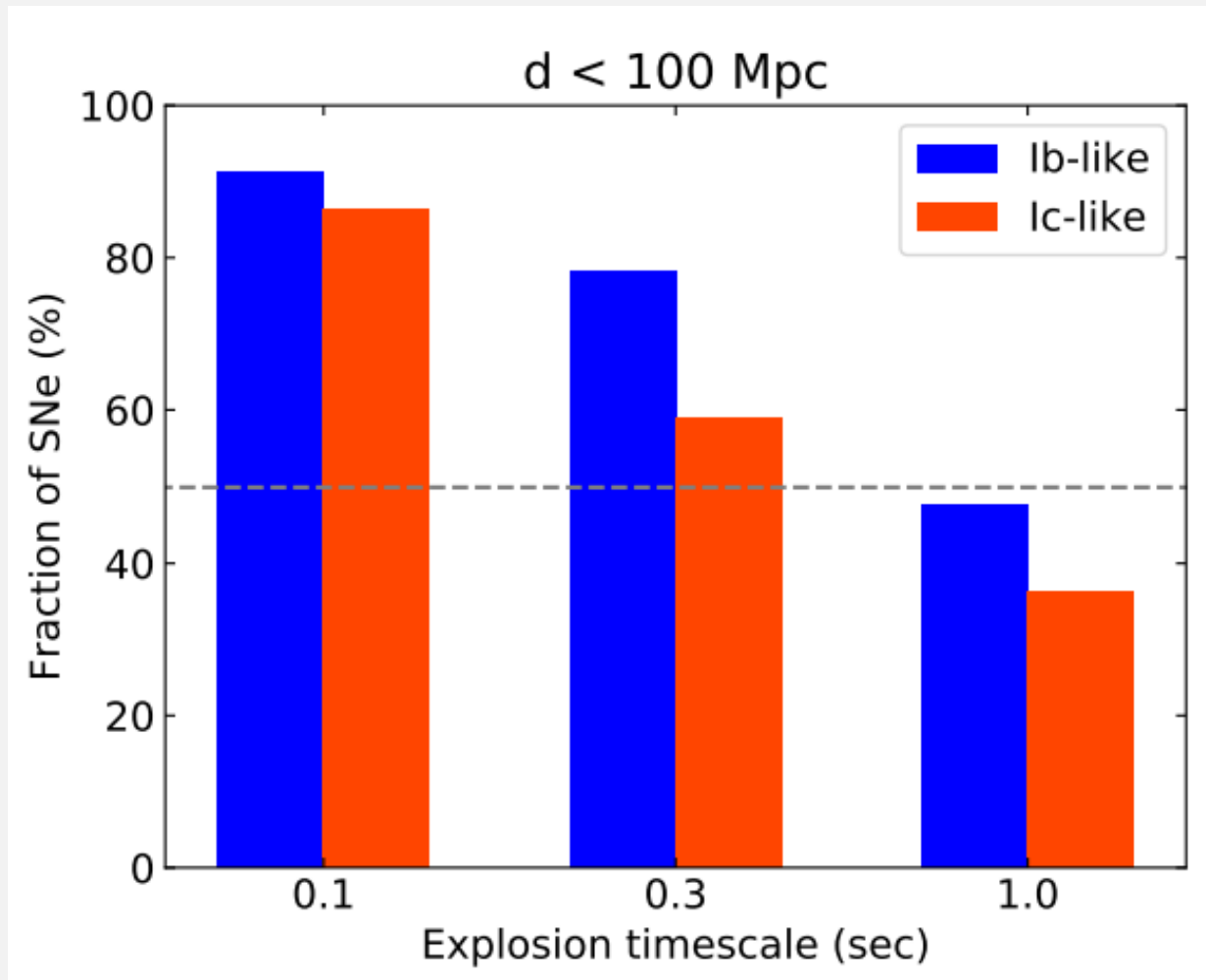
+ [proto-NS mass] = C/O core

simulation

1D hydrodynamics and nucleosynthesis  
with explosion timescale as a parameter

# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

- **NOTE (2): choice of typical value?**



A few tens of percent of observations can be explained by the *non-standard supernova explosions*,

But, the timescales that **reproduce less than 50%** are **difficult to adopt as standard explosion models**.

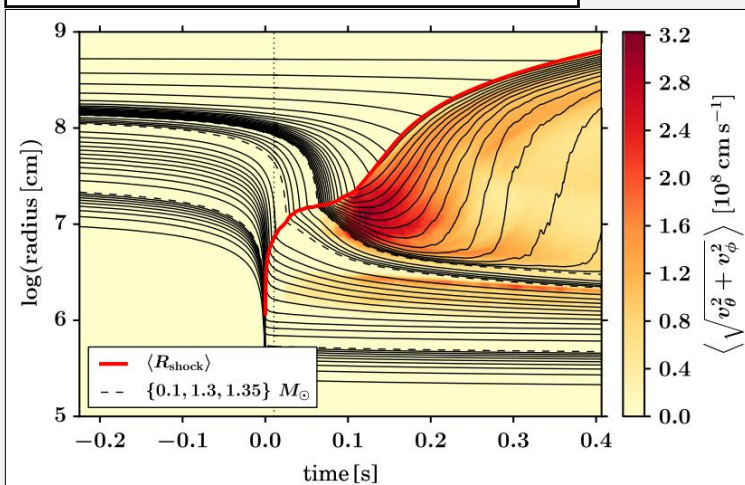
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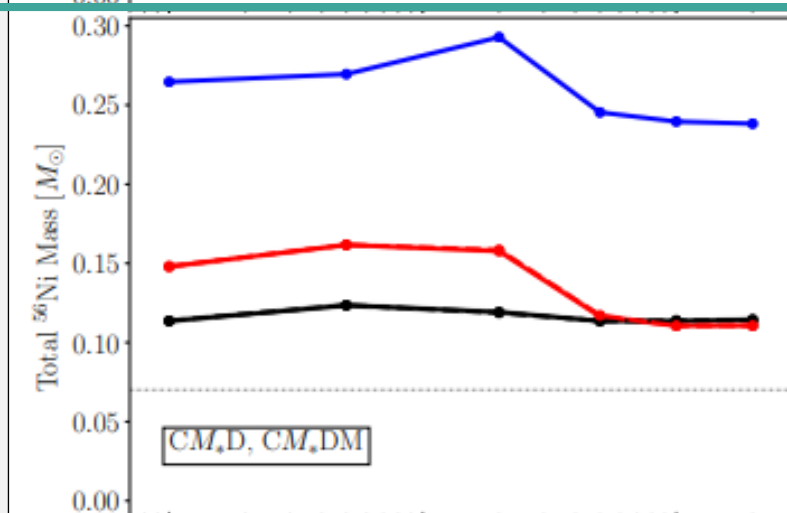
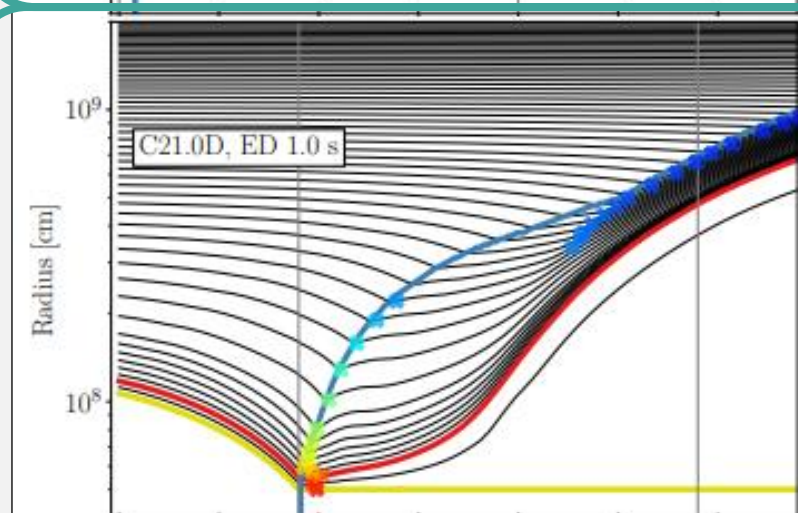
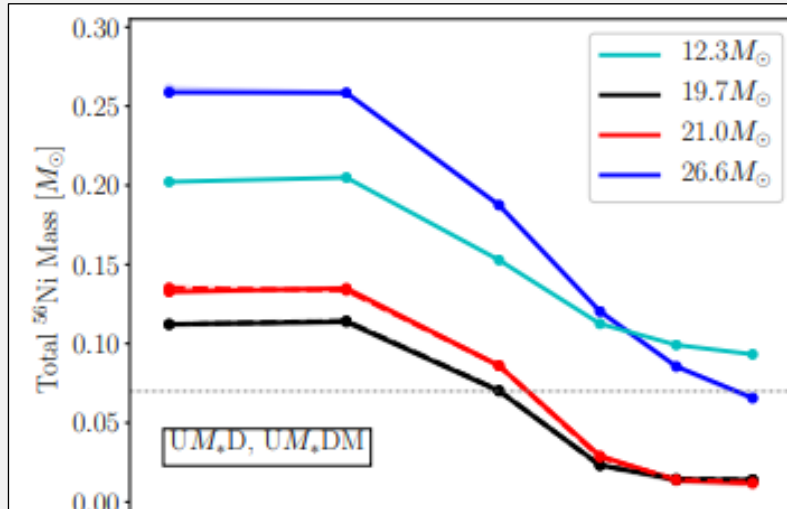
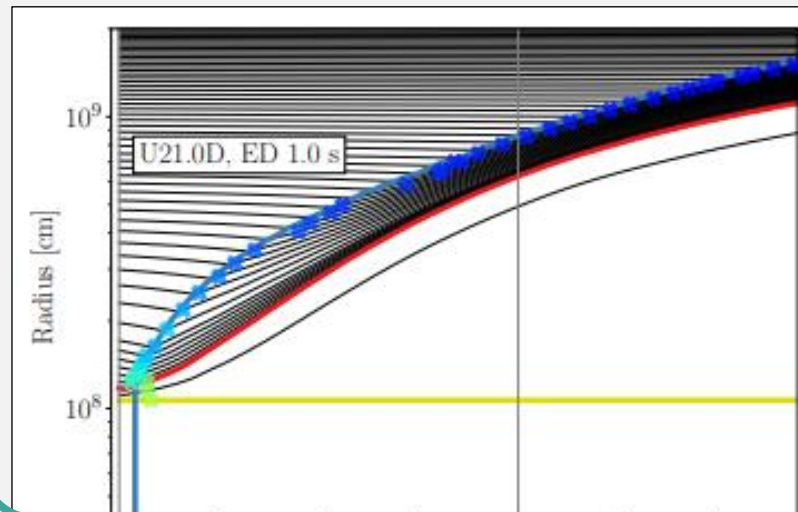
## • NOTE (3): Opposition to this study (Imasheva + 2022)

They pointed out that  
 “This results may comes from the explosion model assumed in our calculations is too simple?”

Melson, Janka & Marek 2015



Imasheva + 2022



# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

- Our work** 1D hydrodynamics and nucleosynthesis  
 simulation **with more realistic explosion calculations** /with lightbulb approximation  
 (not detailed, but mimics neutrino-driven explosions to some extent)

$$\frac{\partial r}{\partial M_r} = \frac{1}{4\pi r^2 \rho}, \quad (5)$$

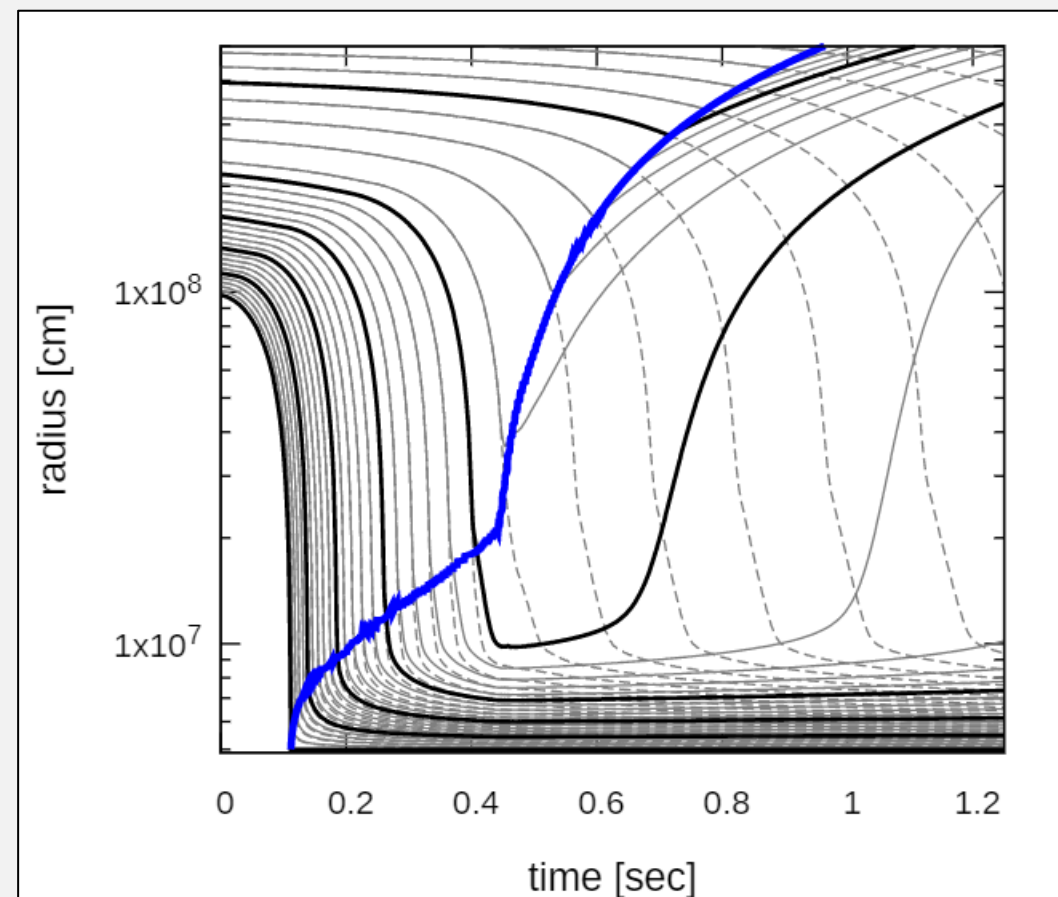
$$\frac{Dv}{Dt} = -\frac{GM_r}{r^2} - 4\pi r^2 \frac{\partial P}{\partial M_r}, \quad (6)$$

$$\frac{D\epsilon}{Dt} = -P \frac{D}{Dt} \left( \frac{1}{\rho} \right) + \mathcal{H} - \mathcal{C}, \quad (7)$$

$$\mathcal{H} = 1.544 \times 10^{20} \text{ erg g}^{-1} \text{ s}^{-1}$$

$$\times \left( \frac{L_{\nu_e}}{10^{52} \text{ MeV}} \right) \left( \frac{r_{\nu_e}}{100 \text{ km}} \right)^{-2} \left( \frac{T_{\nu_e}}{4.0 \text{ MeV}} \right)^2,$$

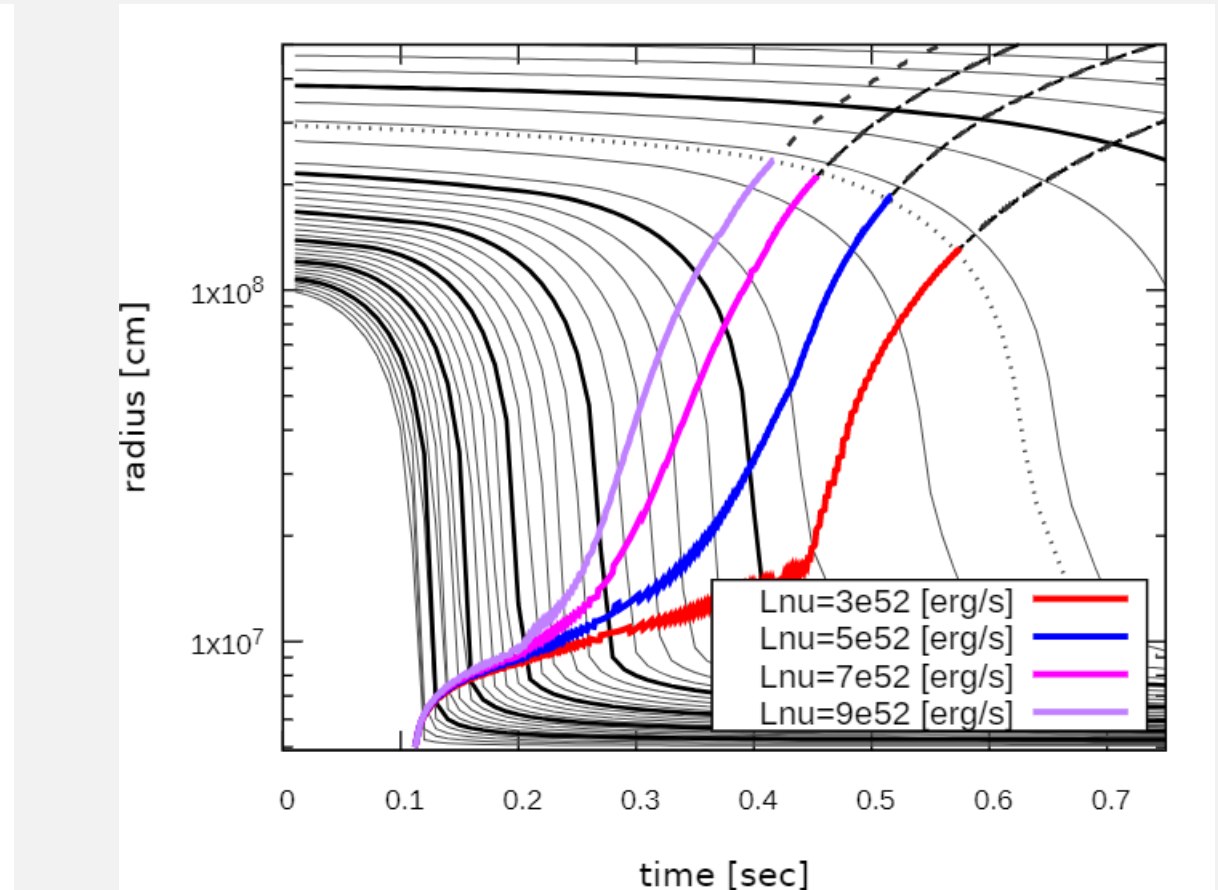
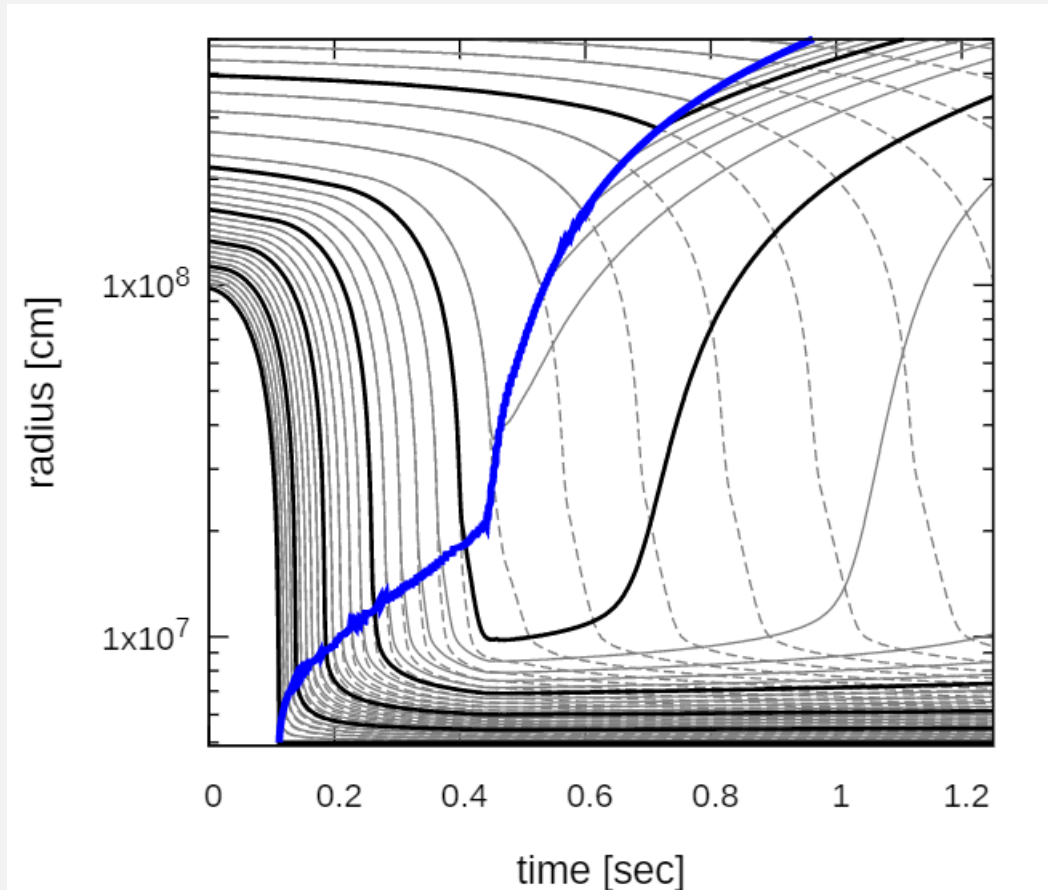
$$\mathcal{C} = 1.399 \times 10^{20} \text{ erg g}^{-1} \text{ s}^{-1} \times \left( \frac{T}{2.0 \text{ MeV}} \right)^6.$$



# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

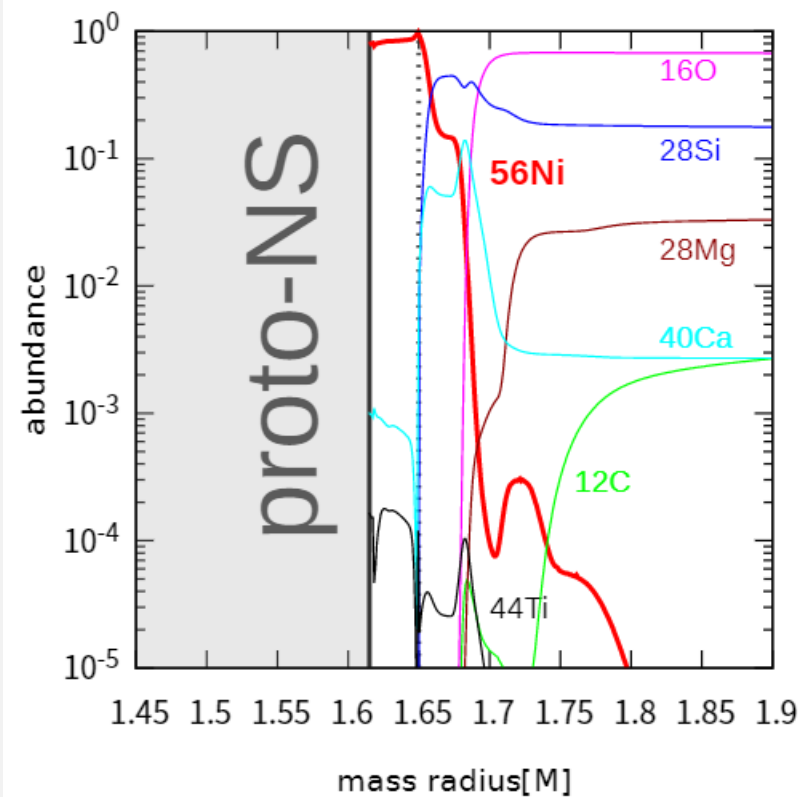
- Our work** 1D hydrodynamics and nucleosynthesis  
 with more **realistic explosion calculations** /with lightbulb approximation  
 (not detailed, but mimics neutrino-driven explosions to some extent)

simulation

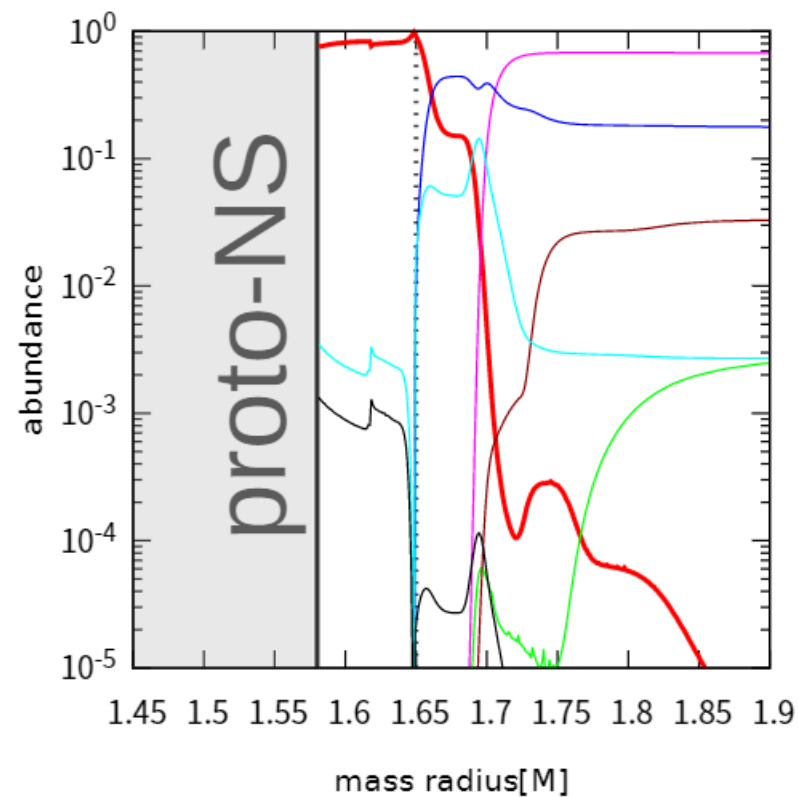


# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

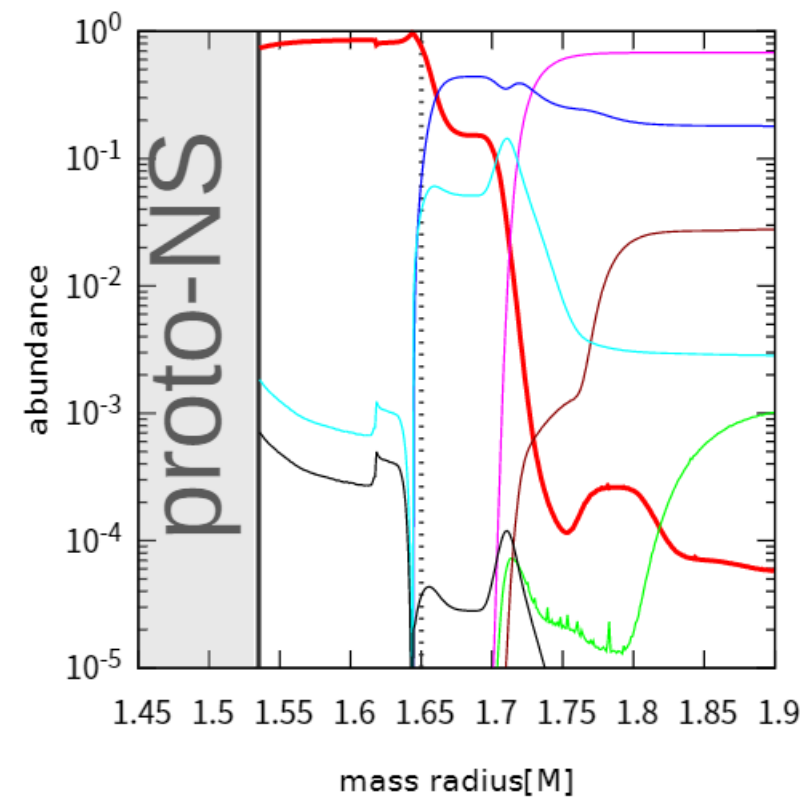
- Our work** 1D hydrodynamics and nucleosynthesis  
 simulation with more realistic explosion calculations /with lightbulb approximation  
 (not detailed, but mimics neutrino-driven explosions to some extent)



(a)



(b)

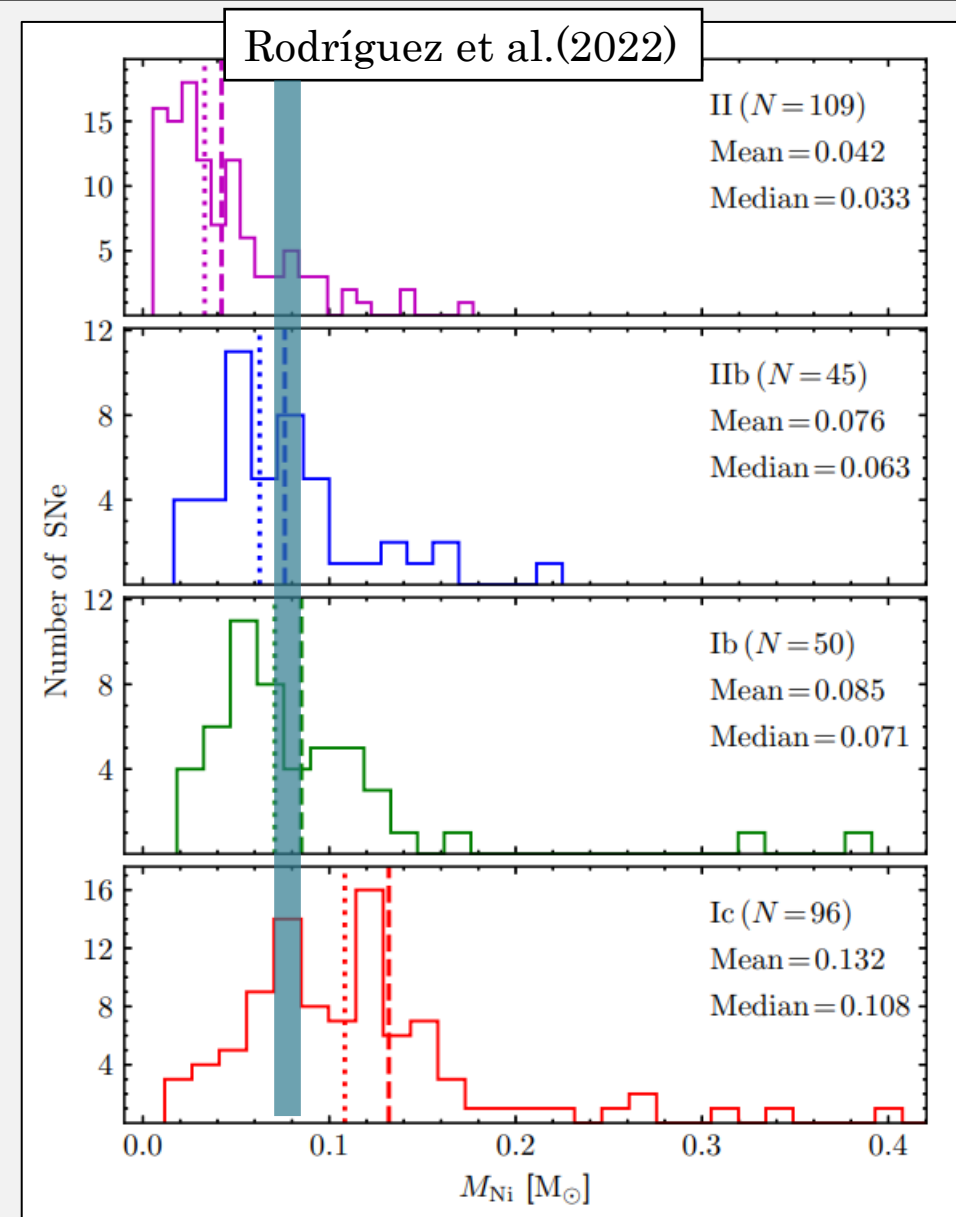
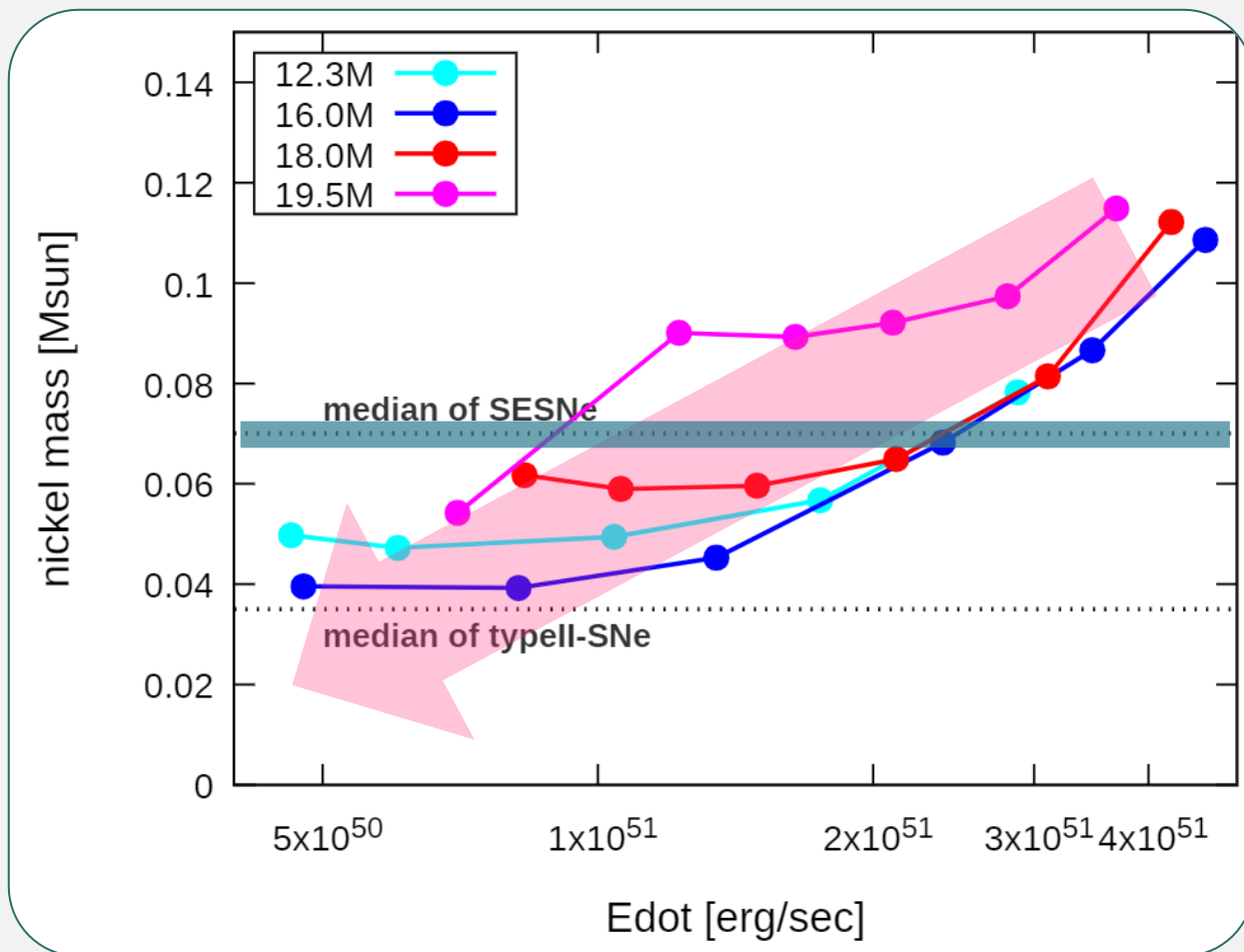


(c)

# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

- NOTE (3): Opposition to this study** (Imasheva + 2022)

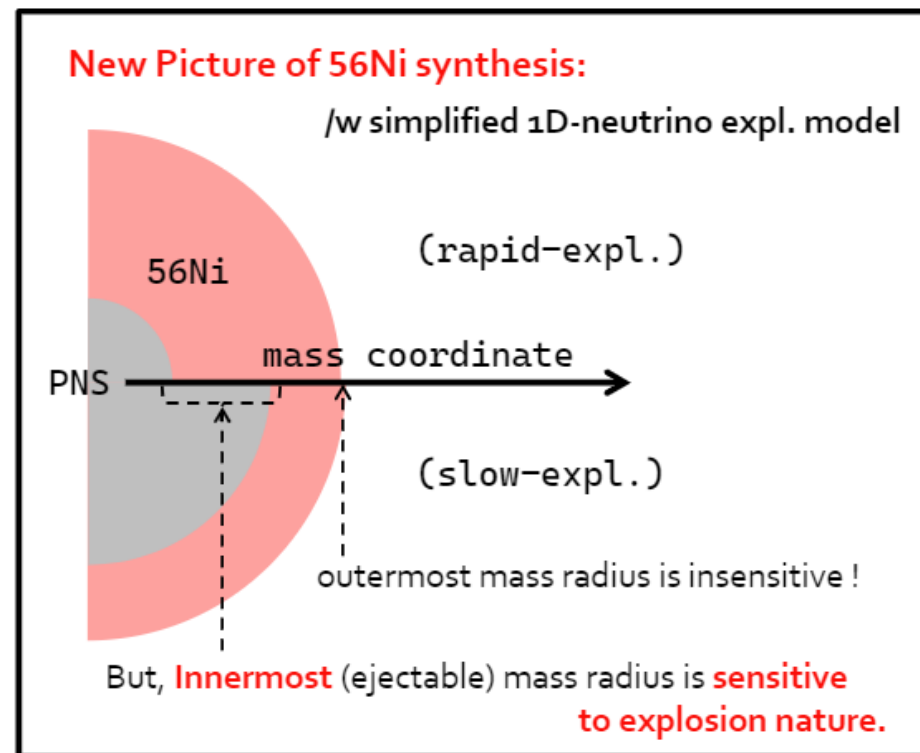
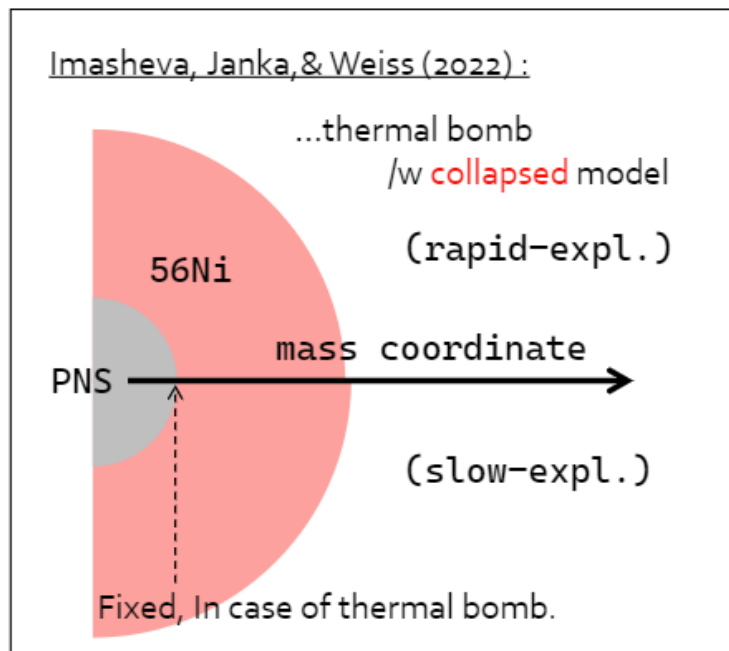
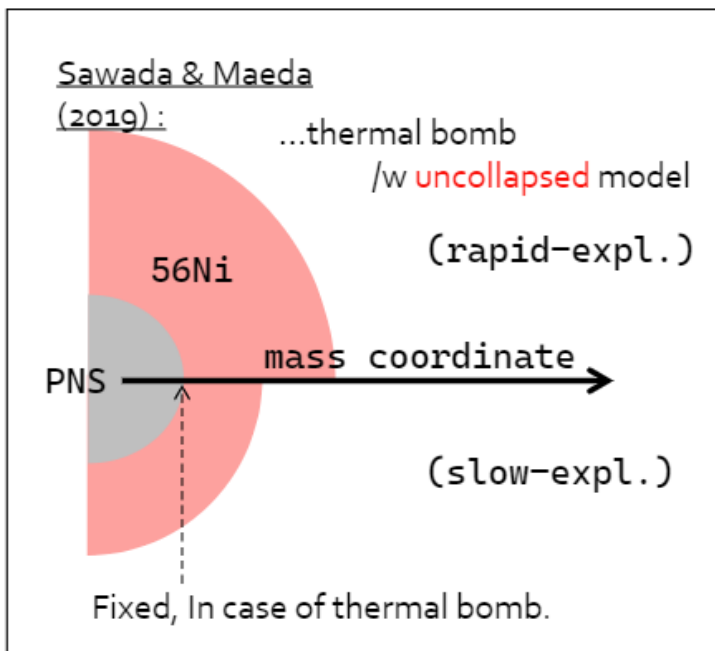
->Using more **realistic explosion calculations** /with lightbulb approximation (not detailed, but mimics neutrino-driven explosions to some extent)



# [topic 1] Can modern supernova simulations synthesize sufficient $^{56}\text{Ni}$ ?

- NOTE (3): Opposition to this study** (Imasheva + 2022)

->Using more **realistic explosion calculations** /with lightbulb approximation  
(not detailed, but mimics neutrino-driven explosions to some extent)



\*slow-expl:  $\dot{E}_{\text{expl.}} \leq 1.0 \times 10^{51} [\text{erg s}^{-1}]$ , rapid-expl:  $\dot{E}_{\text{expl.}} > 1.0 \times 10^{51} [\text{erg s}^{-1}]$

Figure 11. Schematic picture of core-collapse supernova.