

【 中性子星の観測と理論 —研究活性化ワークショップ 2023—  
京都大学理学研究科セミナーハウス (9月6日 (水) – 8日 (金), 2023) 】

# Meson condensation in dense matter and implications for compact stars

武藤 巧(千葉工大)  
Takumi Muto (Chiba Inst. Tech.)

# 1. Introduction

## Meson condensation in dense matter

Multi-messenger

### High-density QCD

- $T$ - $Q_B$  phase diagram  
(+ strangeness, magnetic field, ...)
- various phases of hadronic matter and quark matter

### Hadron phase

Pion condensation ( $\pi^{\pm}, \pi^0$ ) (1970 ~)

Kaon condensation ( $K^{\pm}$ ) (1986 ~)

Chiral symmetry and its spontaneous breakdown



Nambu-Goldstone bosons  
(pseudo scalar)  
→ coherent states

in hyperon ( $\Lambda, \Xi, \dots$ )-mixed matter

• Softening of EOS ↔ Observations of massive  $N_{\star}$

• Rapid cooling of neutron stars → Necessity of Baryon superfluidity

# Observation of massive neutron stars (2010~)

$$M(\text{PSR J1614-2230}) = (1.97 \pm 0.04) M_{\odot}$$

[ P. Demorest et al., Nature 467 (2010) 1081.]

$$M(\text{PSR J0348+0432}) = (2.01 \pm 0.04) M_{\odot}$$

[J. Antoniadis et al.,  
Science 340, 6131 (2013).]

$$M(\text{PSR J2215+5135}) = (2.27 + 0.17-0.15) M_{\odot}$$

[M.Linares, T. Shahbaz, J.Casares, Astrophys. J. 859, 54 (2018).] **in compact binaries**

**Millisecond pulsars**

$$M(\text{PSR J0740+6620}) = (2.14 + 0.10-0.09) M_{\odot} \\ \rightarrow (2.08 \pm 0.07) M_{\odot}$$

[H.T.Cromartie et al.,  
Nat.Astron.4, 72(2020.)]

[E.Fonseca et al.,  
Astrophys. J. Lett.915,  
L12 (2021) ]

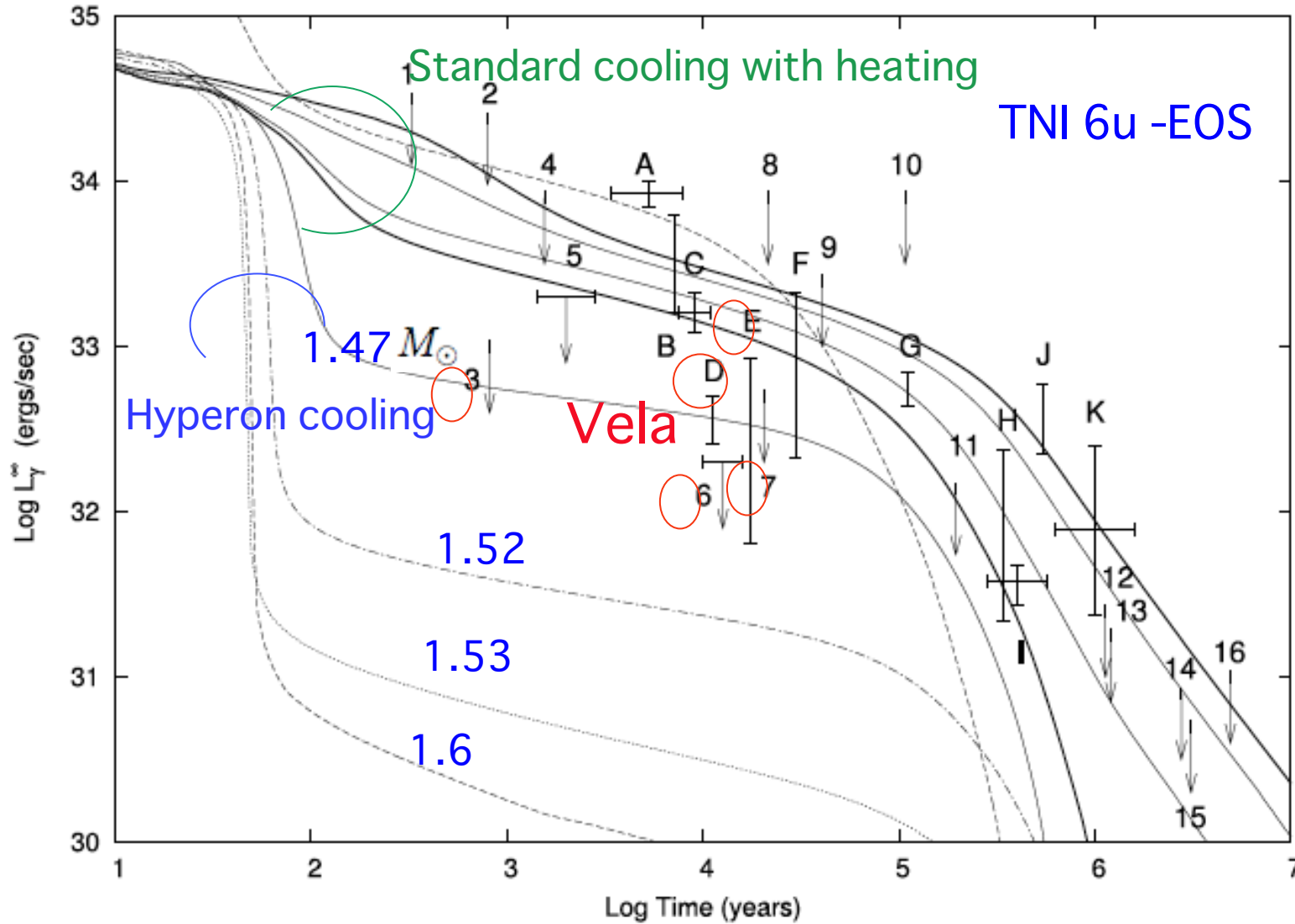
$$M(\text{PSR J1810+1744}) = (2.13 \pm 0.04) M_{\odot}$$

[R. W. Romani et al., Astrophys. J. L. 908, L46 (2021).]

$$M(\text{PSR J0952-0607}) = (2.35 \pm 0.17) M_{\odot}$$

[R. W. Romani et al., arXiv: 2207.05124[astro-ph HE]]

[S. Tsuruta et al., Astrophys. J 691, 621(2009).]



E: PSR 1705-44

3: PSR J0205+6449 (in 3C 58)    6: RX J0007.0+7302 (in CTA 1)

7: PSR 1046-58

# Present studies of meson condensation

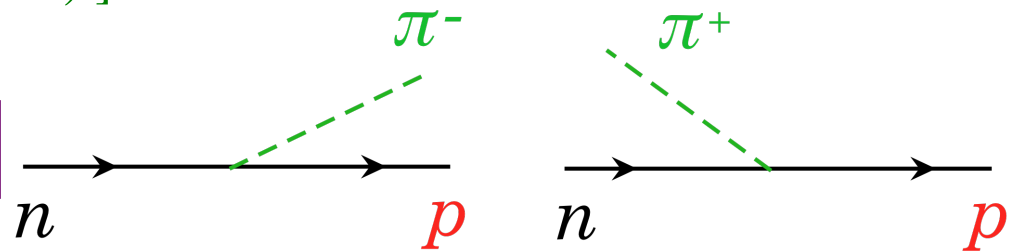
## Pion condensation ( $\pi^c$ , $\pi^0$ )

[G.Baym and D.K.Campbell,  
Mesons in Nuclei, (ed M.Rho and D.H.Wilkinson) Vol. III, p.1031 (1979).]

[A.B.Migdal, E.E.Saperstein, M.A.Troitsky, and D.N.Voskresensky,  
Phys. Rep.192 (1990), 179.]

[T. Kunihiro, T. Muto, T.Takatsuka, R.Tamagaki, and T.Tatsumi,  
Prog. Theor. Phys. Supplement 112 (1993).]

Driving force: **P-wave  $\pi$ -N int.**



$$\text{Quasi-baryons: } |\eta\rangle = \cos \phi |n\rangle - i \sin \phi |p\rangle$$

Pion properties are sensitive to medium effects.

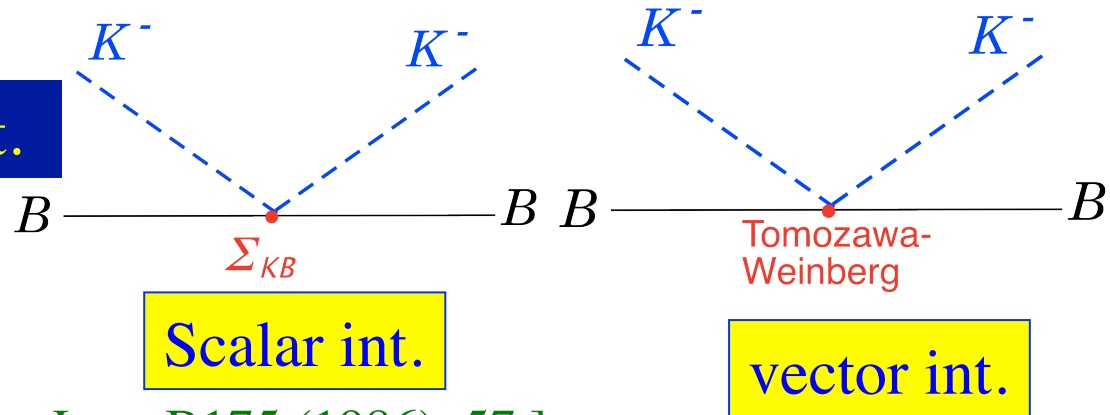
Landau-Migdal parameter in spin-isospin channel

$$g' = (0.5 - 0.6)(f_{\pi NN}/m_\pi)^2$$

# Kaon condensation ( $K^-$ )

Driving force: **S wave KB int.**

• **Softening of EOS**



[D.B. Kaplan and A. E. Nelson, Phys. Lett. B175 (1986), 57.]

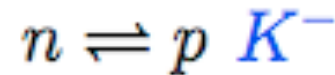
[T. Tatsumi, Prog. Theor. Phys. 80, 22(1988).]

[C.-H.Lee, G.E.Brown, D.-P.Min, and M.Rho, Nucl. Phys. A585 (1995),401.]

[T. Muto and T. Tatsumi, Phys. Lett. B283(1992), 165.]

[H. Fujii, T. Maruyama, T. Muto, and T. Tatsumi, Nucl. Phys. A597 (1996), 645.]

chemical equilibrium  
for weak processes



• **Rapid cooling of neutron stars**

[H. Fujii, T. Muto, T. Tatsumi, R. Tamagaki,  
Nucl. Phys. A578 (1994), 758; Phys. Rev. C 50 (1994), 3140.]

## 2. Overview of the present results on Kaon Condensation in hyperon (Y)-mixed matter [ (Y+K) phase ]

### 2-1 Our interaction model

[T. Muto, T. Maruyama, and T. Tatsumi, Phys. Lett. B 820 (2021), 136587.]

K-Baryon and K-K interactions : effective chiral Lagrangian

### Baryon-Baryon interaction

Minimal Relativistic Mean-Field theory  
(without nonlinear self-interactions  
by mesons( $\sigma$ ,  $\omega$ ,  $\rho$  ...))

Slope :  $L \equiv 3\rho_0 \left( \frac{\partial S}{\partial \rho_B} \right)_{\rho_B=\rho_0}$   
 $= (60 - 70) \text{ MeV}$

controls Stiffness of EOS  
from two-body B-B int.


### Three-Baryon (many-body) forces

+ Universal Three-Baryon Repulsion (**UTBR**) : String-Junction Model 2

+ Three-Nucleon attraction (**TNA**)

[R. Tamagaki,

Prog. Theor. Phys. 119 (2008), 965. ]

 The **UTBR** appropriately stiffen the EOS, consistent with recent observations of massive  $N_\star$  ( $M$  and  $R$ ...)

## 2-2 Lorentz invariant forms for UTBR

### Conditions for the EOS

(1) Saturation properties of SNM

(2) Consistency with observations of massive N☆

$M$  and  $R$

(3) Causality condition

$$v_s < c$$

$$M_{\max} \gtrsim 2.0M_{\odot}$$

for stable star with gravitational mass  $M \leq M_{\max}$

Lorentz scalar

TBR as energy density :  $\mathcal{E}(\text{TBR}) = -\mathcal{L}(\text{TBR})$

$$\mathcal{E}(\text{TBR}) = c_{m,n} (\bar{\psi}\psi)^m (\bar{\psi}\gamma^\mu\psi \cdot \bar{\psi}\gamma_\mu\psi)^n \quad (m, n = 0, 1, \dots)$$

$$\rightarrow c_3 \rho_B^s \rho_B^2 + c_4 \rho_B^2 [1 - \exp(-\eta \rho_B^2)] \quad : \text{Covariant TBR}$$

TBR3

TBR4

baryon density :  $\rho_B = \sum_{b=p,n,\Lambda,\Xi^-, \Sigma^-} \rho_b$

baryon scalar density :  $\rho_B^s = \sum_{b=p,n,\Lambda,\Xi^-, \Sigma^-} \rho_b^s$

$$\rho_b^s = \frac{2}{(2\pi)^3} \int_{|\mathbf{p}| \leq p_F(b)} d^3\mathbf{p} \frac{\widetilde{M}_b^*}{(|\mathbf{p}|^2 + \widetilde{M}_b^{*2})^{1/2}}$$

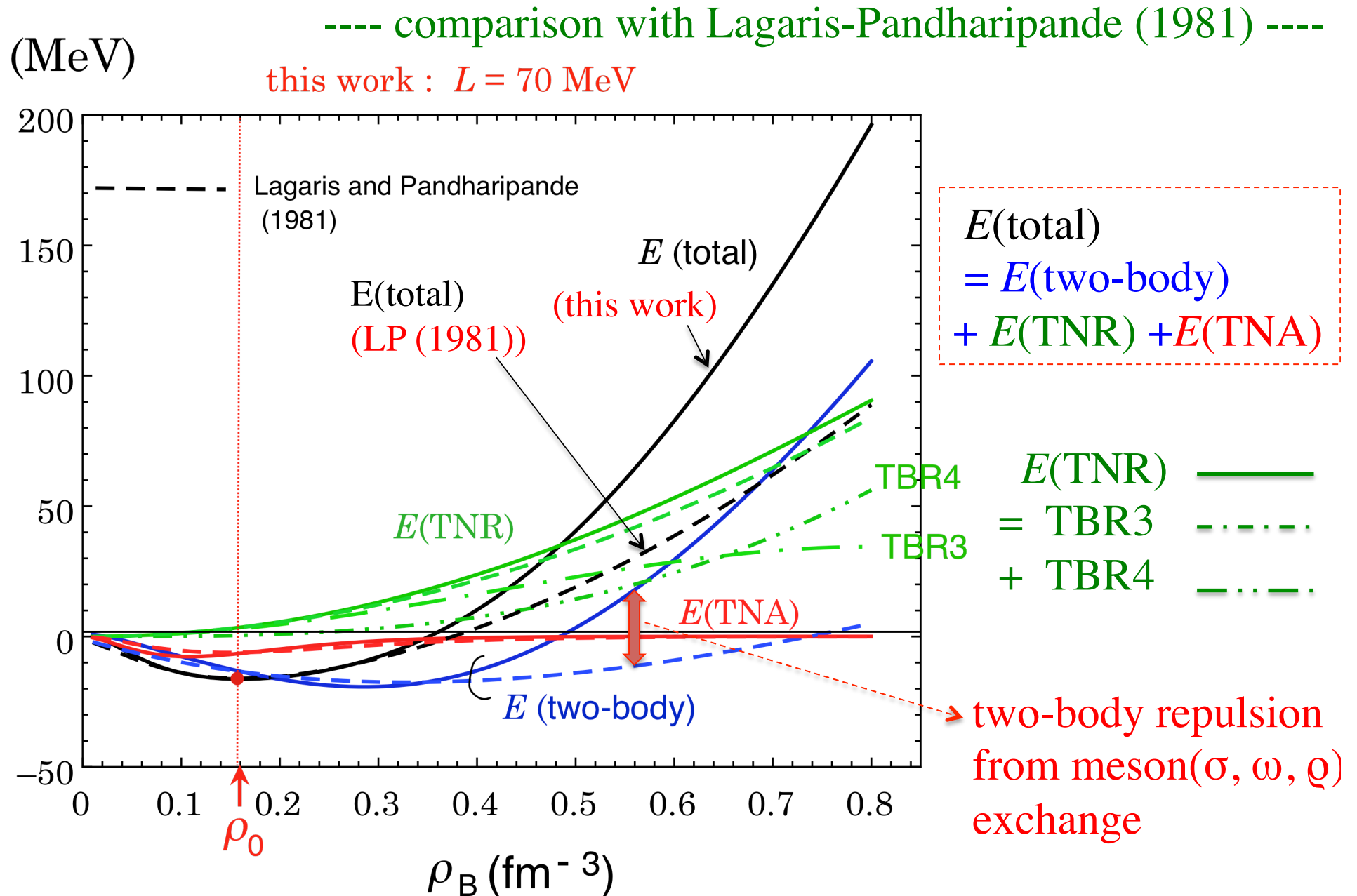
(effective baryon mass)

$$\widetilde{M}_b^* = M_b - g_{\sigma b} \sigma - g_{\sigma^* b} \sigma^* - \Sigma_{Kb} (1 - \cos \theta)$$

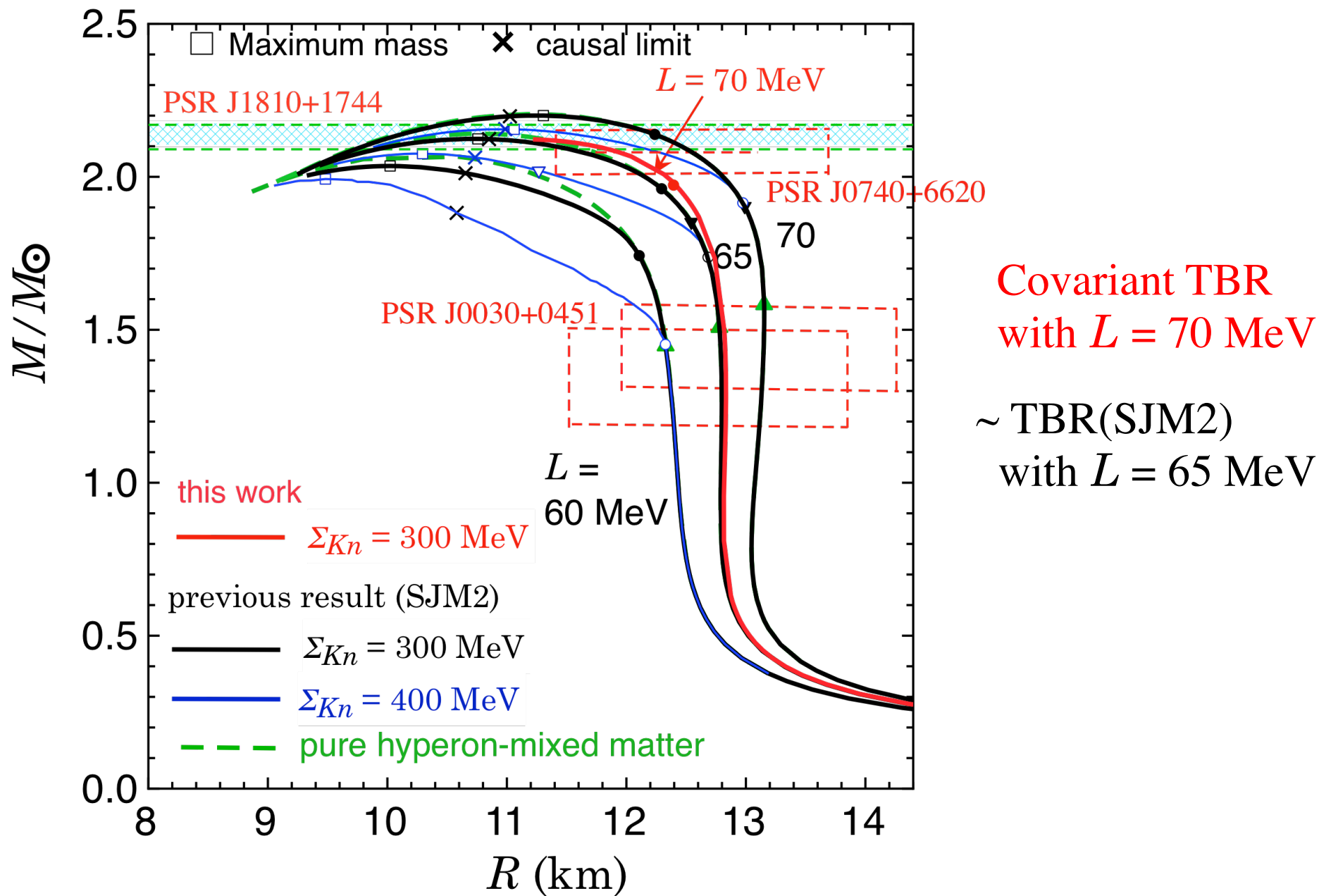


### 3. Numerical Results

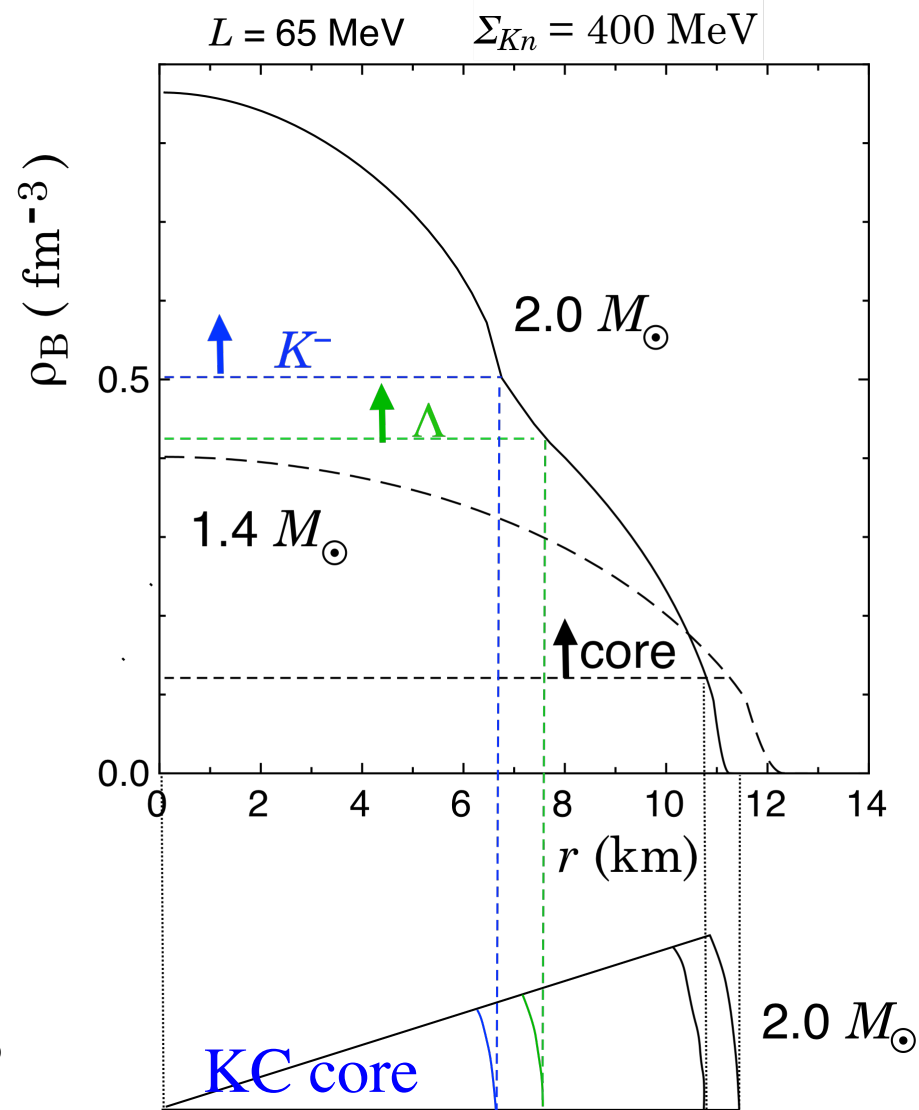
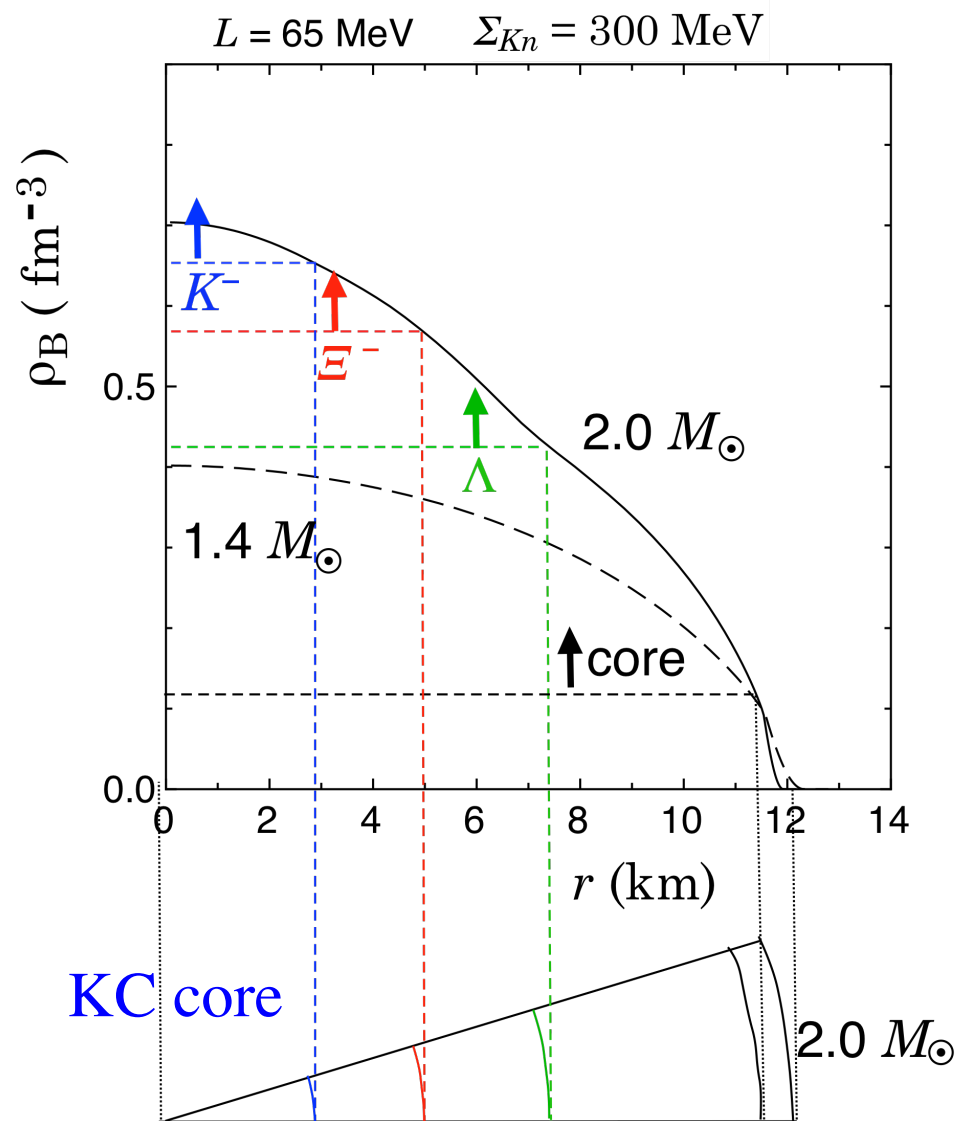
### 3-1 Energy per particle in SNM



# 3-2 Gravitational Mass – radius R relations

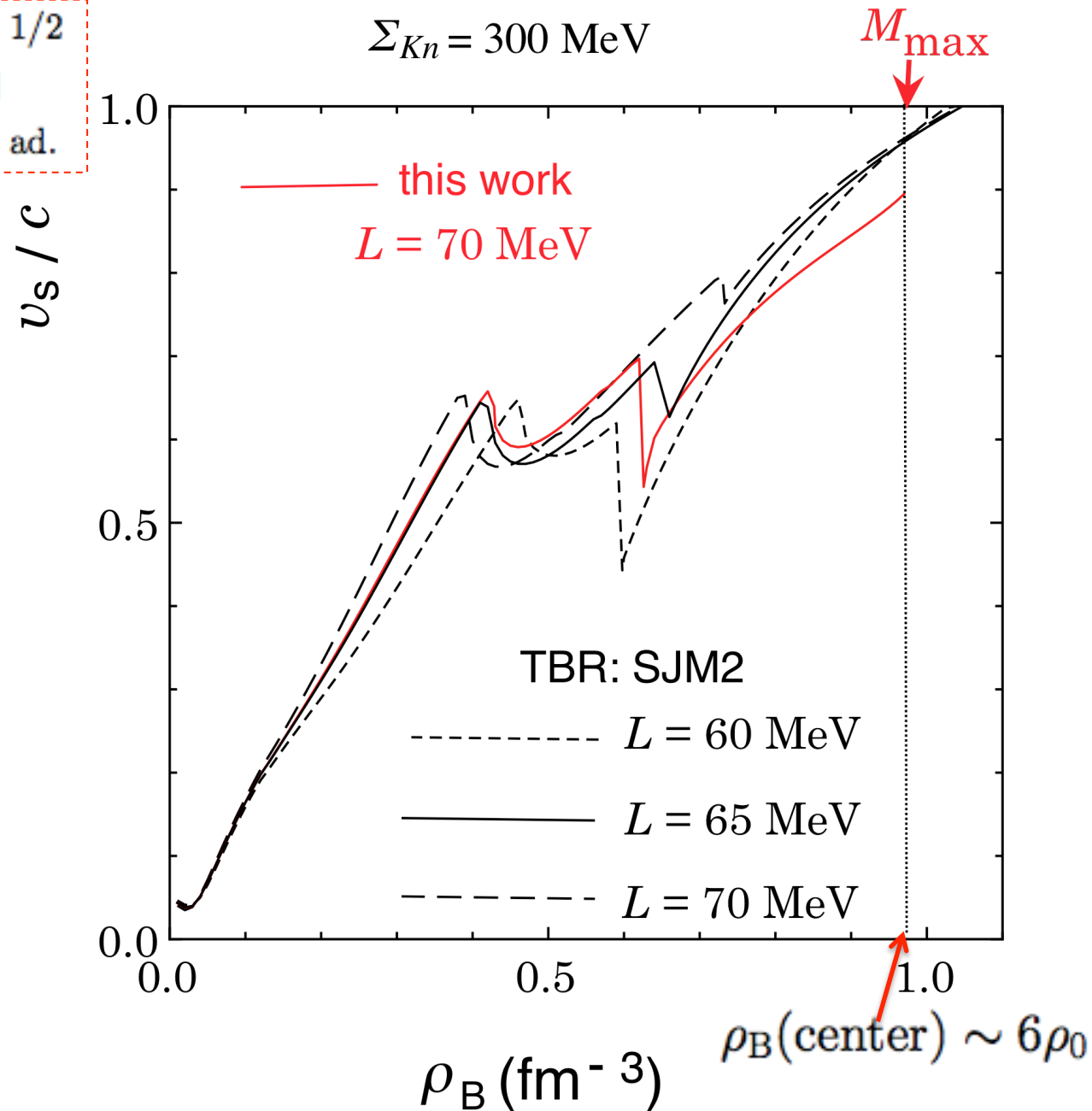


# 3-3 Density distributions --- $L = 65$ MeV ---



### 3-4 Sound velocity ( $v_s$ ) squared – baryon density $\rho_B$

$$v_s = \left( \frac{dP}{d\mathcal{E}} \right)_{\text{ad.}}^{1/2}$$



## 4. Short Summary

Lorentz-scalar form of the **TBR (Covariant TBR)**, combined with the Minimal RMF and TNA, has been obtained consistently with

- **saturation properties of SNM,**
- **causality condition**
- **observations of massive compact stars.**

In order to be consistent with causality condition,

$$E(\text{TBR}) \sim E(\text{two-body}) \text{ for SNM at high densities } \sim (0.7-0.8) \text{ fm}^{-3}$$

**Observationally,** the EOS including the (Y+K) phase with **Covariant TBR** predicts higher  $L$  ( $\sim 70$  MeV) in order to be consistent with observation of massive compact stars.

## 5. Outlook

### 5-1 Outlook Role of pion condensation

#### EOS Possible coexistence of PC and KC ( $\pi$ -K condensation)

From heavy-ion collisions, the EOS may be softer for  $\rho_B = (2 - 4.5)\rho_0$

[P. Danielewicz, R.Lacey, W.G.Lynch, Science 298, 1592 (2002).]

PC and KC couple with p-wave



Validity of Universal three-baryon repulsion (UTBR)  
and consistency with Massive  $N_\star$  observations

#### Rapid cooling mechanisms

Baryon superfluidity in the presence of KC or  $\pi$ -K condensation is needed in order to suppress too rapid neutrino emissivity.

### 5-2 Phenomena specific to meson condensation

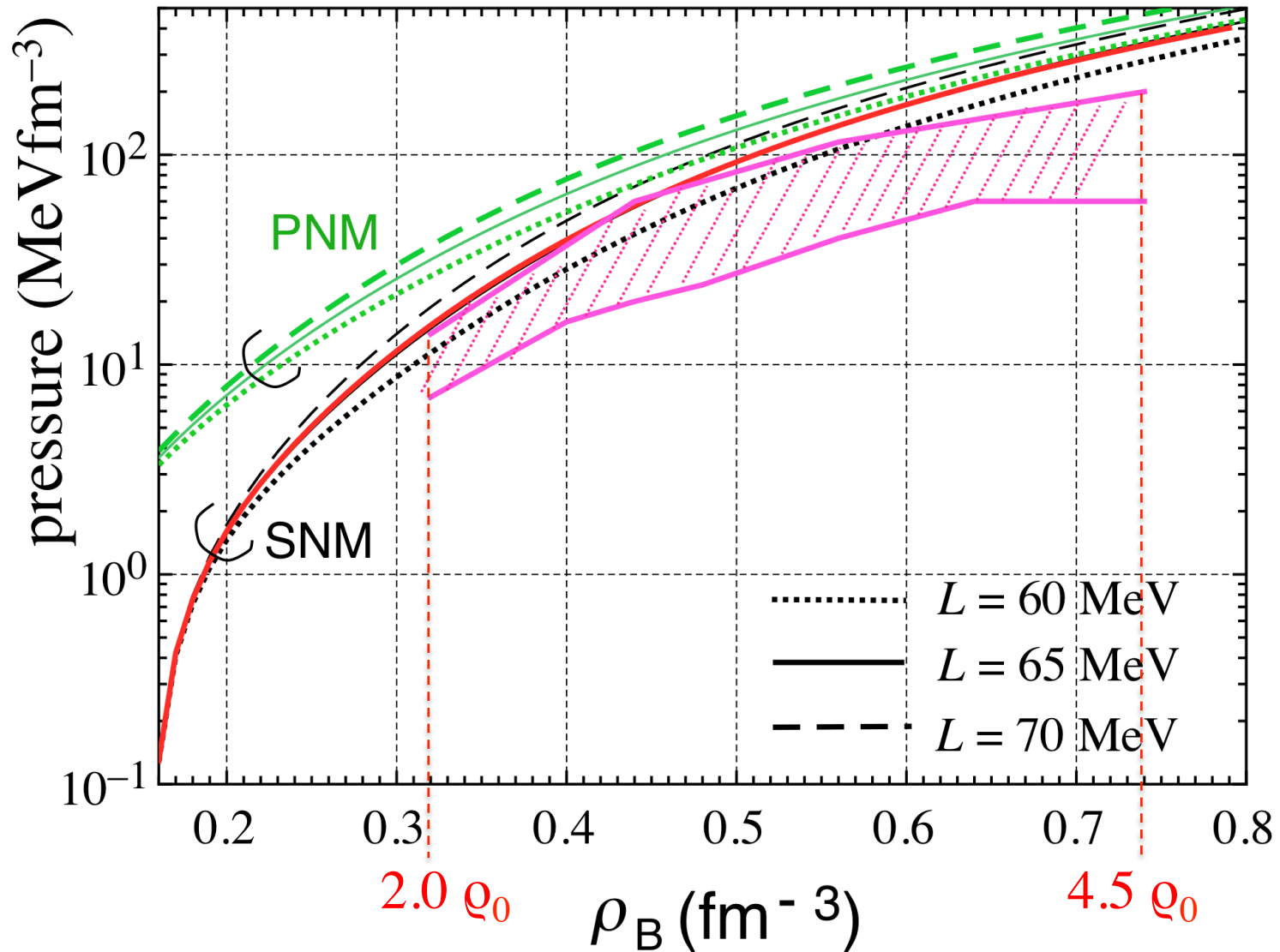
- Response to rotation and strong magnetic field as superfluidity / superconductivity
- Response to radial/nonradial oscillations

# Pressure in Symmetric Nuclear Matter



Data from [P. Danielewicz, R.Lacey, W.G.Lynch, Science 298, 1592 (2002).]

— Covariant TBR with  $L = 70$  MeV



## 5-3 Outlook Role of MC in Hadron– Quark crossover

hadron matter  $\longrightarrow$  quark matter

H-Q crossover

Meson condensation

[ K.Masuda, T. Hatsuda, T.Takatsuka,  
Astrophys. J. 764,12 (2013); PTEP 2016, 021D01(2016).]

[G. Baym, T. Hatsuda, T. Kojo, P.D.Powell, Y.Song, T.Takatsuka,  
Rept. Prog. Phys. 81, 056902 (2018).]

Nonlinear representation of NG octet bosons (elementary fields)

$$U = \exp(2i\Pi/f)$$

$$\xi \equiv U^{1/2}$$

$$\Pi = \pi_a T_a = \frac{1}{\sqrt{2}} \begin{pmatrix} \pi^0/\sqrt{2} + \eta/\sqrt{6} & & \pi^+ & & K^+ \\ & \pi^- & & -\pi^0/\sqrt{2} + \eta/\sqrt{6} & K^0 \\ & K^- & & \bar{K}^0 & \\ & & & & -\sqrt{\frac{2}{3}}\eta \end{pmatrix}$$

Meson vector current

$$V_\mu \equiv \frac{1}{2}(\xi^\dagger \partial_\mu \xi + \xi \partial_\mu \xi^\dagger)$$

Meson axial-vector current

$$A_\mu \equiv \frac{i}{2}(\xi^\dagger \partial_\mu \xi - \xi \partial_\mu \xi^\dagger)$$



## Hadron phase

$$\begin{aligned}
 \mathcal{L}_{K,B} = & \frac{1}{4}f^2 \text{Tr}(\partial^\mu U^\dagger \partial_\mu U) + \frac{1}{2}f^2 \Lambda_{\chi\text{SB}}(\text{Tr}M(U - 1) + \text{h.c.}) \\
 & + \text{Tr}\bar{\Psi}(i\gamma^\mu \partial_\mu - M_B)\Psi + \text{Tr}\bar{\Psi}i\gamma^\mu[V_\mu, \Psi] + D\text{Tr}\bar{\Psi}\gamma^\mu\gamma^5\{A_\mu, \Psi\} \\
 & + F\text{Tr}\bar{\Psi}\gamma^\mu\gamma^5[A_\mu, \Psi] + a_1\text{Tr}\bar{\Psi}(\xi M^\dagger \xi + \text{h.c.})\Psi \\
 & + a_2\text{Tr}\bar{\Psi}\Psi(\xi M^\dagger \xi + \text{h.c.}) + a_3(\text{Tr}MU + \text{h.c.})\text{Tr}\bar{\Psi}\Psi,
 \end{aligned}$$

Octet Baryons

$$\Psi = \begin{pmatrix} \Sigma^0/\sqrt{2} + \Lambda/\sqrt{6} & \Sigma^+ & p \\ \Sigma^- & -\Sigma^0/\sqrt{2} + \Lambda/\sqrt{6} & n \\ \Xi^- & \Xi^0 & -\sqrt{\frac{2}{3}}\Lambda \end{pmatrix}$$

## Quark phase

$$\mathcal{L}_{M,q} = \frac{1}{4}f^2 \text{Tr}(\partial^\mu U^\dagger \partial_\mu U) + \bar{q}(i\gamma^\mu D_\mu - g_A \gamma^\mu A_\mu \gamma_5 - M)q$$

Quark fields  $q^T = (u, d, s)$

$$D_\mu \equiv \partial_\mu + V_\mu$$