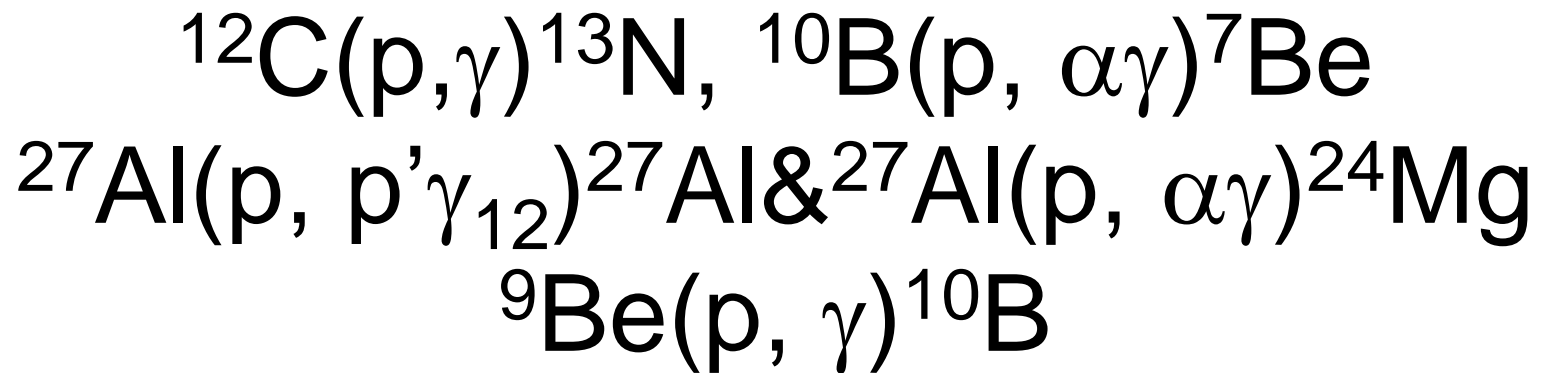


The pelletron experiment



H. Ishiyama
RNC/RIKEN

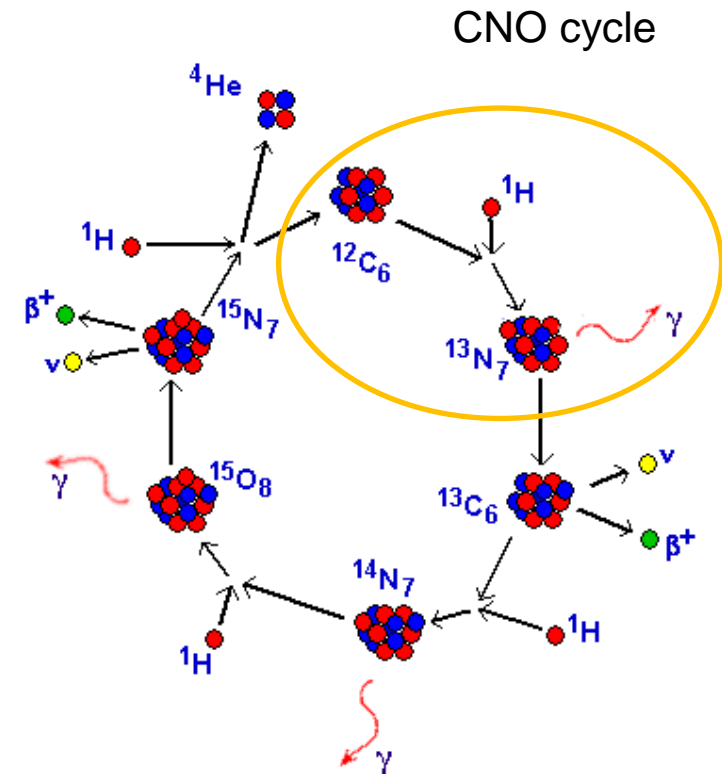
Nishina School 2023
July 27th - Aug. 4th



- A reaction involved in the CNO cycle nuclear burning in **massive*** stars, ...
- At low (astrophysical) energies, two dominant resonances are important.



* more massive than the sun



Appropriate energies of proton beams
from the accelerator (pelletron)?

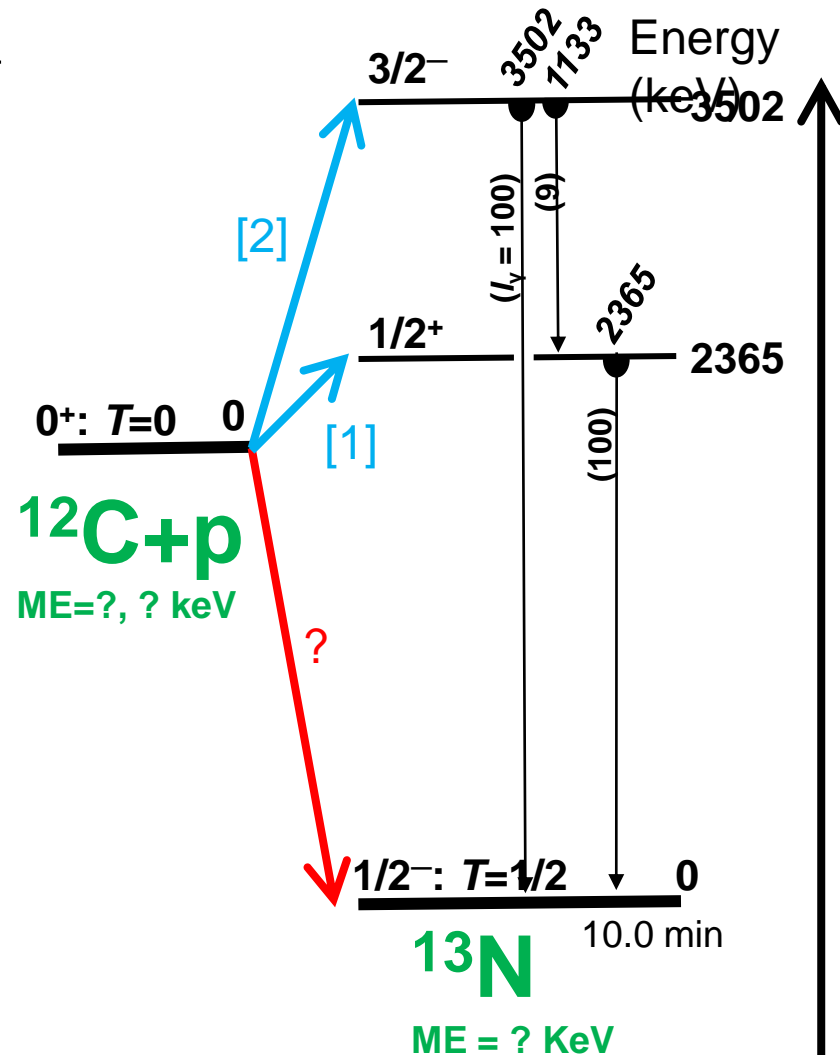
Question 1

energy (mass*) difference between $^{12}\text{C}+\text{p}$ & ^{13}N

- Energy levels of at the center-of-mass (CM) system
- mass difference between $^{12}\text{C}+\text{p}$ and ^{13}N is ? keV

Get Mass Excess (mass) from NNDC.

ME: relative mass value to ^{12}C
($\text{ME}(^{12}\text{C}) = 0$)





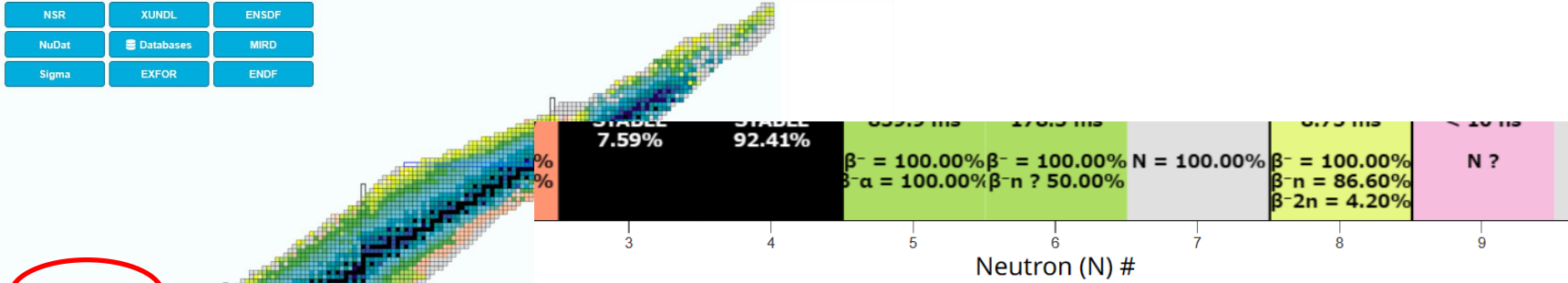
NNDC

Google 検索

I'm Feeling Lucky

National Nuclear Data Center | Databases | Structure & Decay | Reactions | Resources | Brookhaven National Laboratory

- NSR
- XUNDL
- ENSDF
- NuDat
- Databases
- MIRD
- Sigma
- EXFOR
- ENDF



Ground and isomeric state information for $^{12}_6\text{C}$

E(level) (MeV)	J $^{\pi}$	Mass Excess (keV)	T _{1/2}	Abundance	Decay Modes
0.0	0 ⁺	0	STABLE	98.93% 8	

The following are available

- List of levels
- Interactive Level Scheme (Beta)
- Level Scheme
- J vs. E* plot
- J vs. E(y) plot

N-Plot | Y-Scale | Export

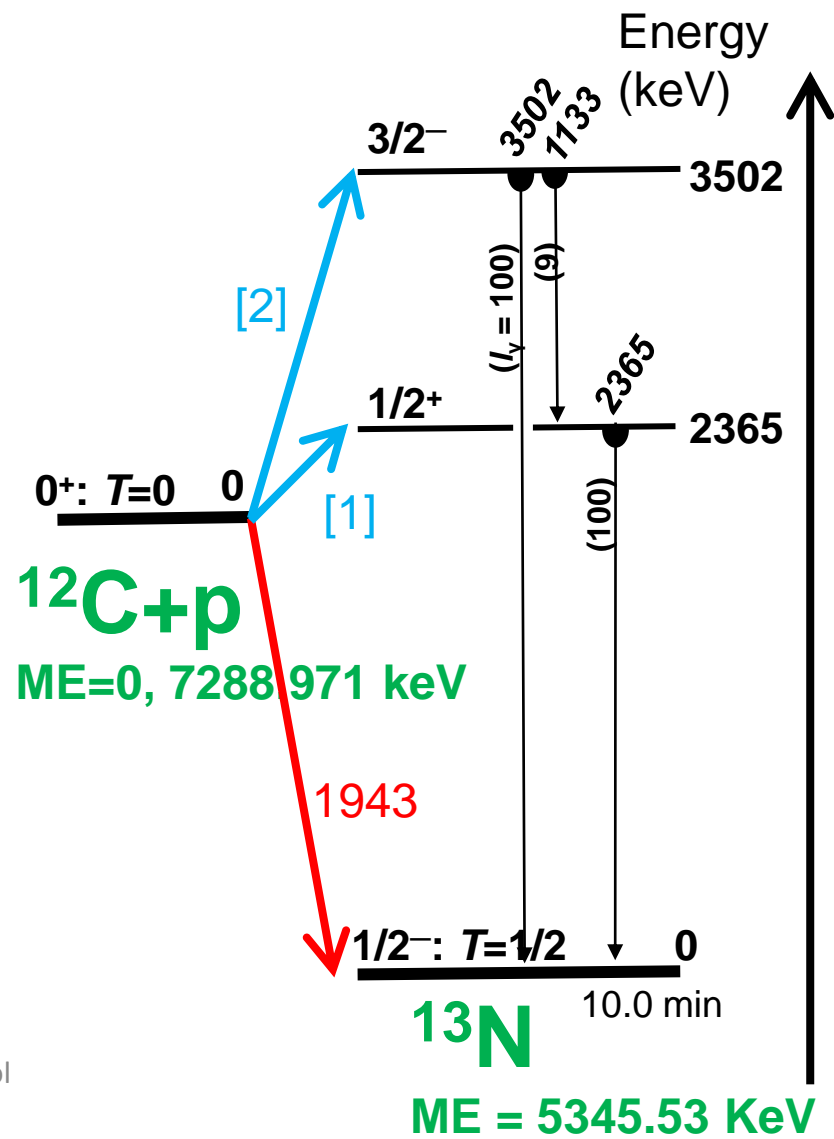
Reset | Linear | Log

N#: Even Odd | Z#: Even Odd

Question 1

energy (mass*) difference between $^{12}\text{C}+\text{p}$ & ^{13}N

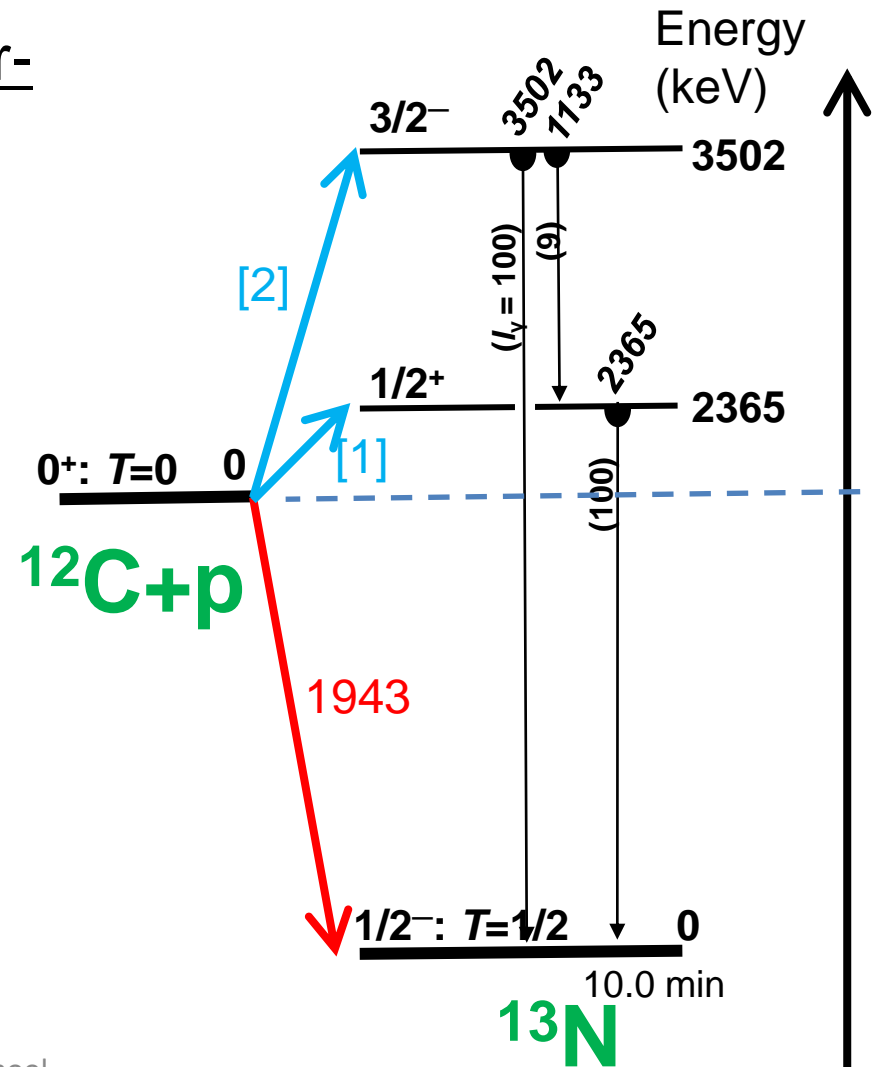
- Energy levels of at the center-of-mass (CM) system
- mass difference between $^{12}\text{C}+\text{p}$ and ^{13}N is **1943 keV**



Question 1

energy (mass) difference between $^{12}\text{C}+\text{p}$ & ^{13}N

- Energy levels of at the center-of-mass (CM) system
- mass difference between $^{12}\text{C}+\text{p}$ and ^{13}N is **1943 keV**
- Calculate the energy differences for [1] and [2]



Answers:

422 keV for [1]

1559 keV for [2]

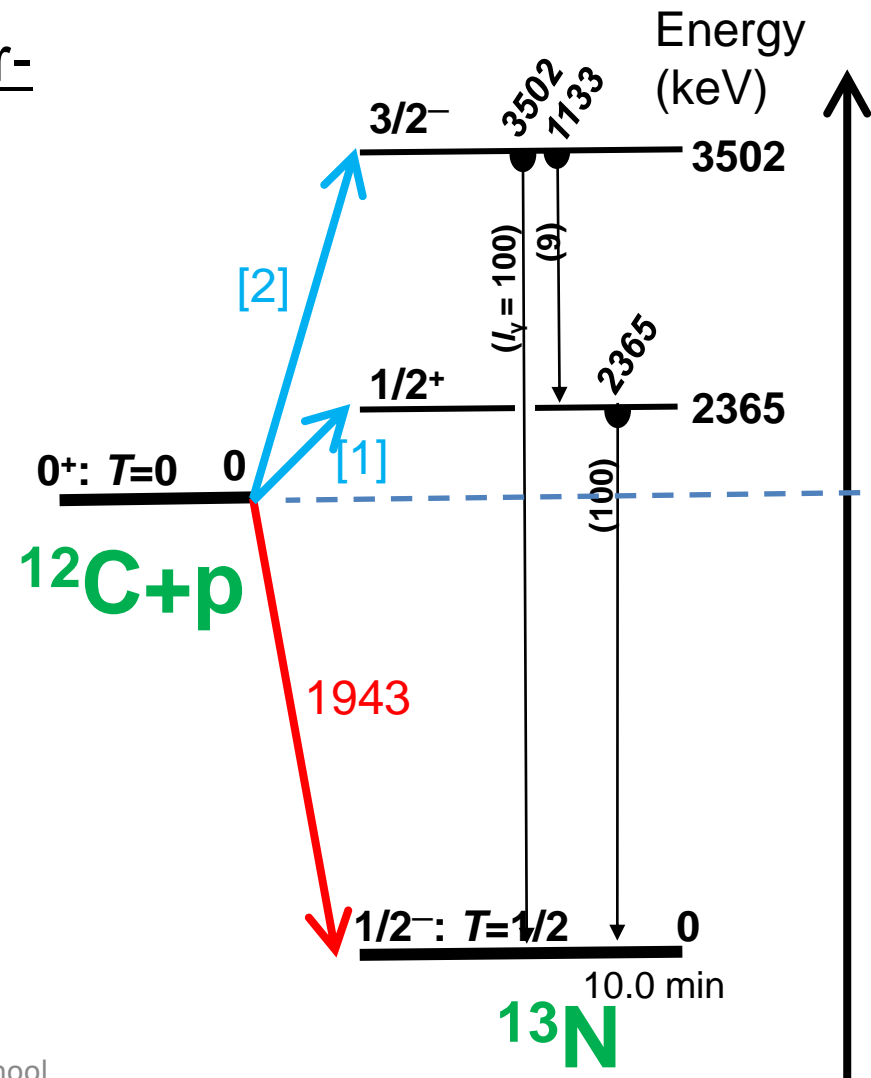
Question 1

energy (mass) difference between $^{12}\text{C}+p$ & ^{13}N

- Energy levels of at the center-of-mass (CM) system
- mass difference between $^{12}\text{C}+p$ and ^{13}N is **1943** keV
- Calculate the energy differences for [1] and [2]

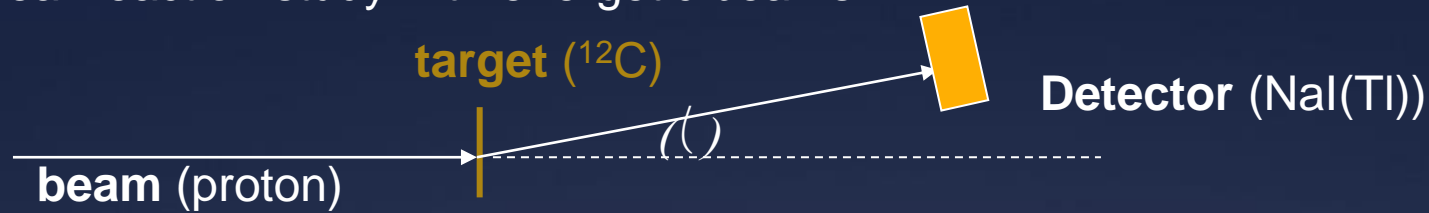
Note:

The level at 2365 keV (or 3502 keV) is a **resonance**.



In the “laboratory” frame

nuclear reaction study with energetic beams



Question 2

proton kinetic energy necessary to populate a resonance?

Is it

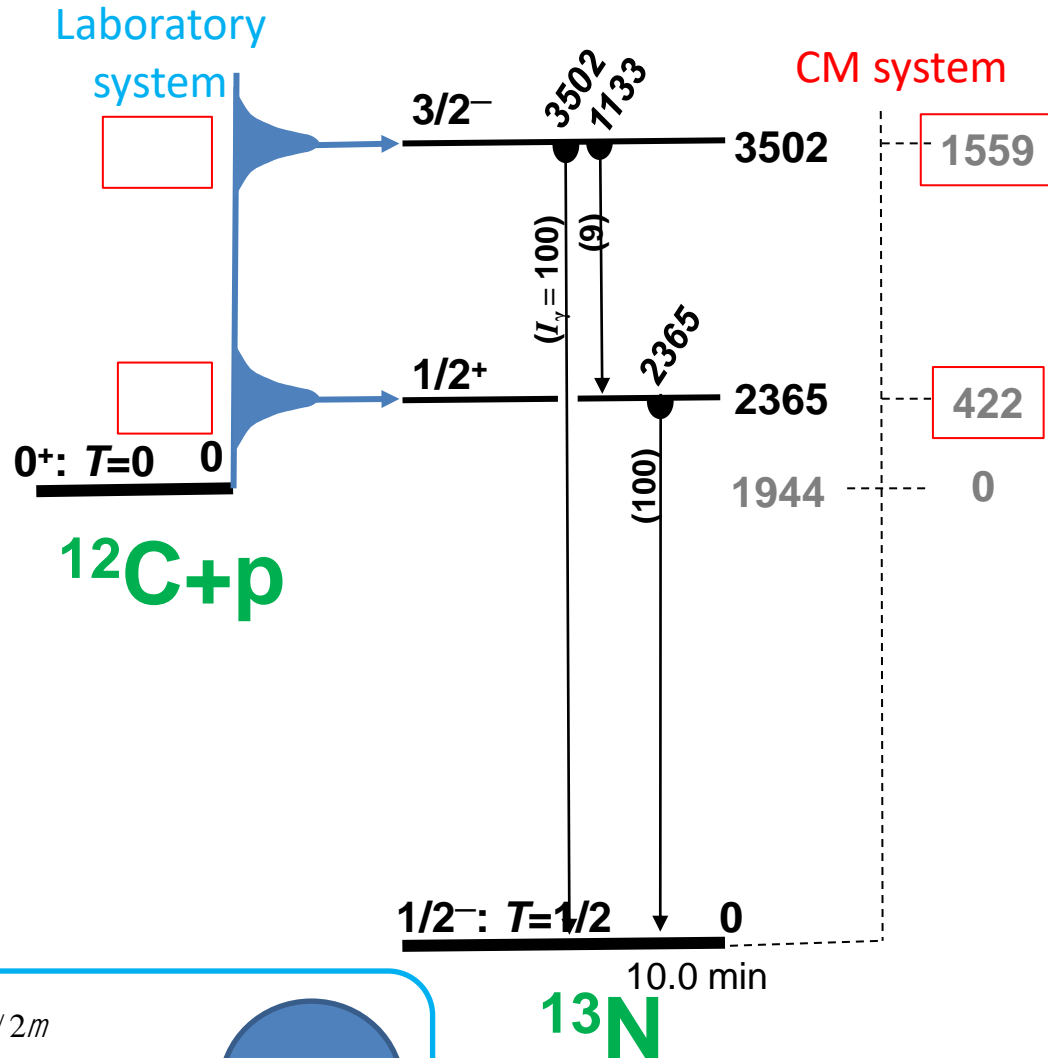
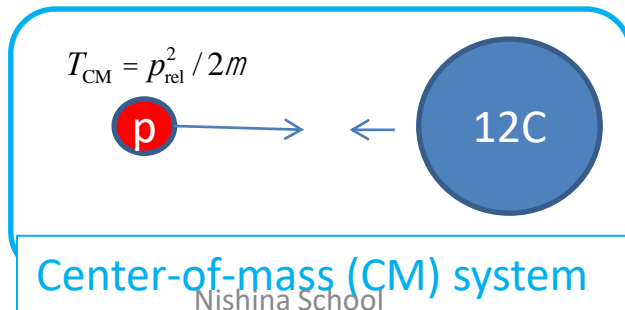
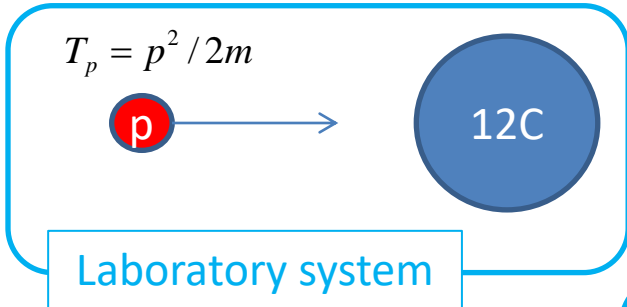
Laboratory <-> CM system :

$$T_{\text{CM}} = \frac{p_{\text{rel}}^2}{2m}, m = \frac{m_1 m_2}{m_1 + m_2}, p_{\text{rel}} = \frac{m_2 p_1 - m_1 p_2}{m_1 + m_2}$$

$$m_1 = m, m_2 @ 12m, p_1 = p, p_2 = 0$$

$$\searrow T_{\text{CM}} = \frac{p^2}{2m} \times \frac{12}{13} = T_p \times \frac{12}{13}$$

μ : reduced mass



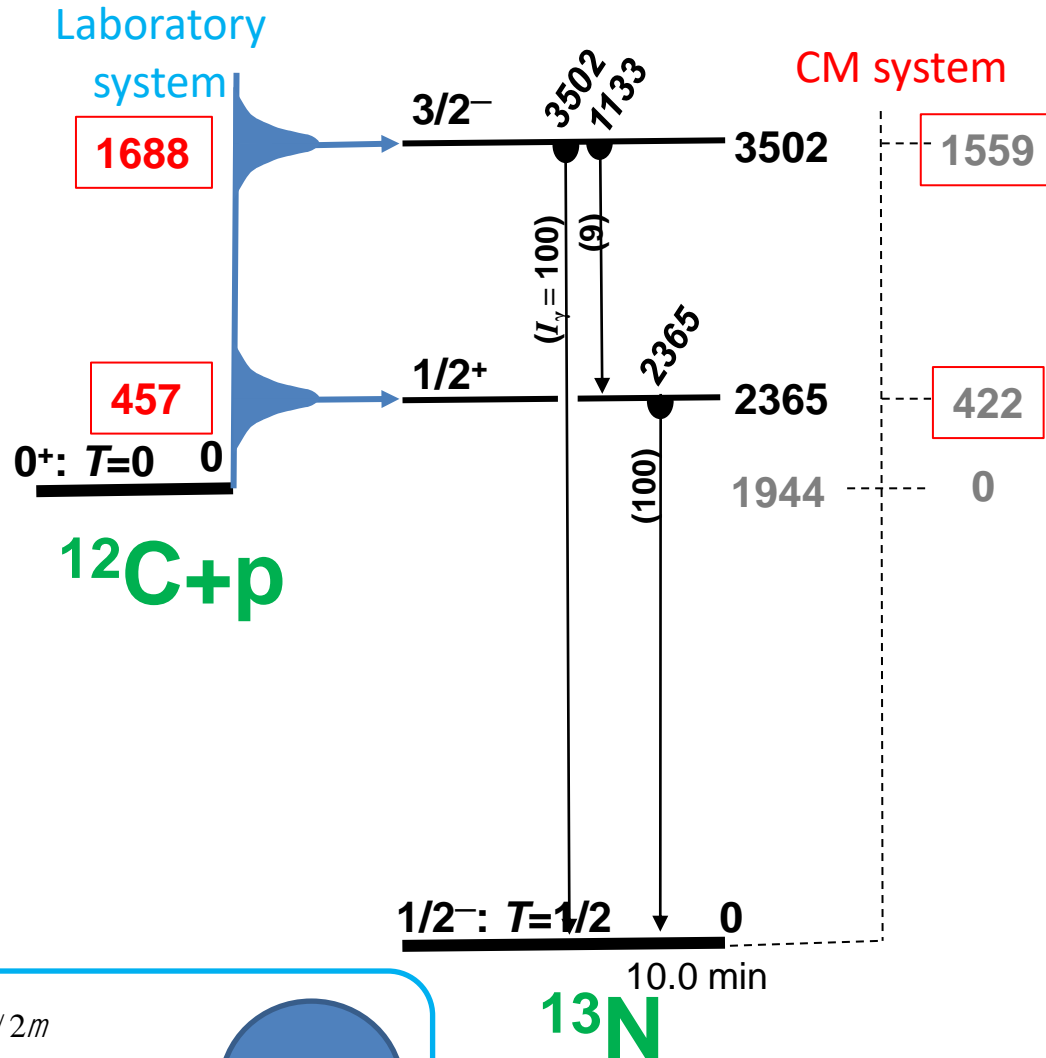
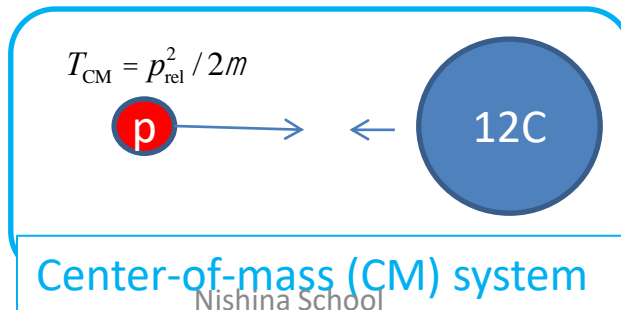
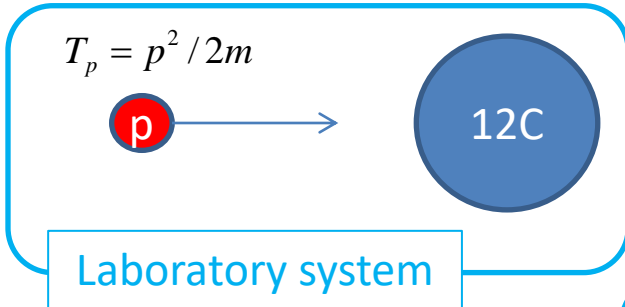
Laboratory <-> CM system :

$$T_{\text{CM}} = \frac{p_{\text{rel}}^2}{2m}, m = \frac{m_1 m_2}{m_1 + m_2}, p_{\text{rel}} = \frac{m_2 p_1 - m_1 p_2}{m_1 + m_2}$$

$$m_1 = m, m_2 @ 12m, p_1 = p, p_2 = 0$$

$$\searrow T_{\text{CM}} = \frac{p^2}{2m} \times \frac{12}{13} = T_p \times \frac{12}{13}$$

μ : reduced mass

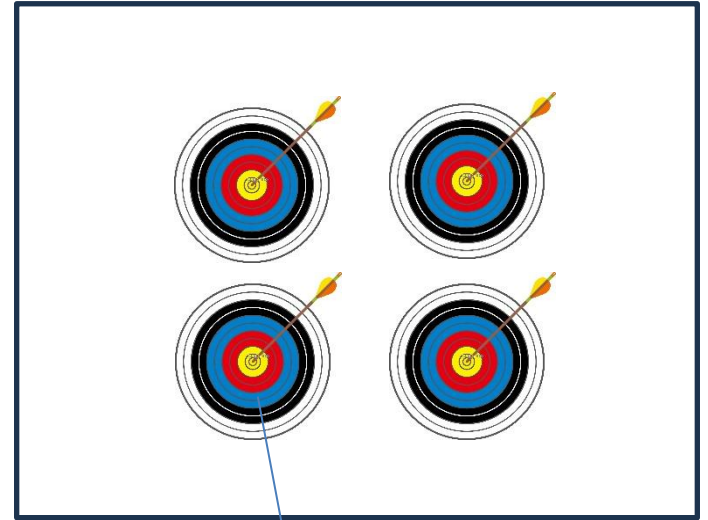


How do we measure the **cross sections**?

Cross Section?



Unit Area



Surface Area \times # of target

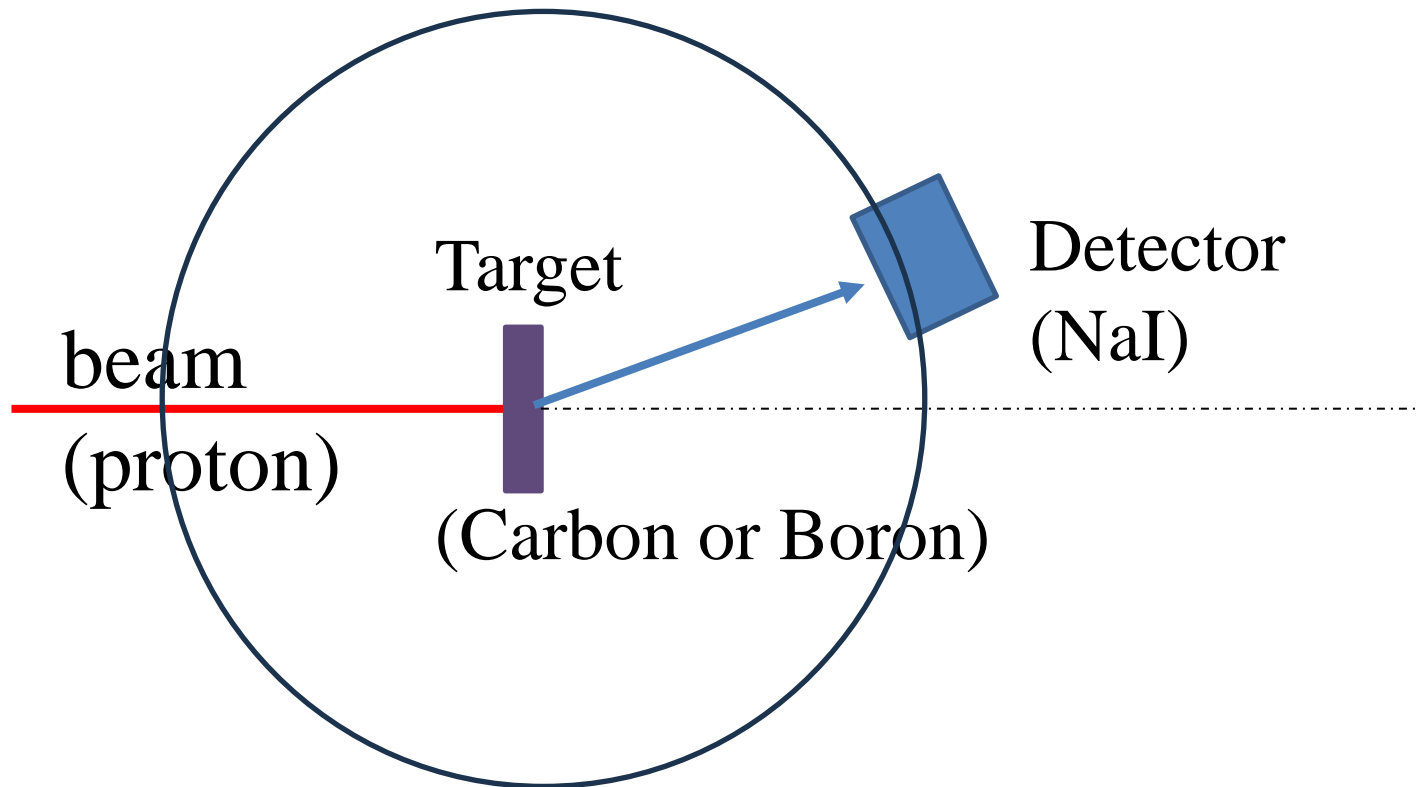
How many arrows hit targets?

= (# of arrows) \times (# of target/unit area) \times (Area of a target)

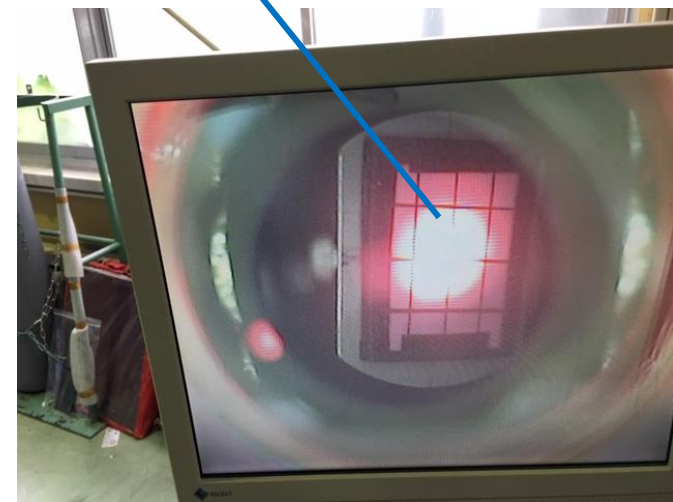
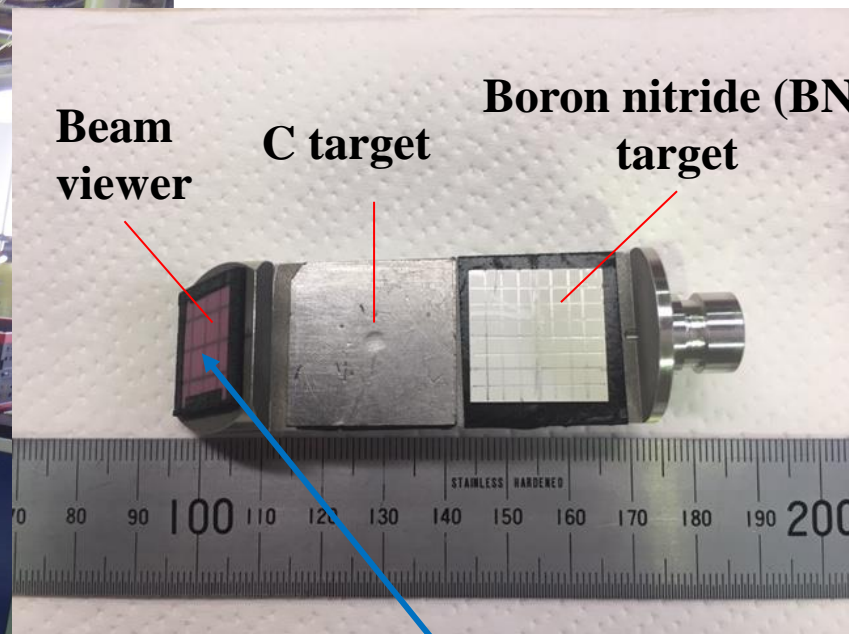
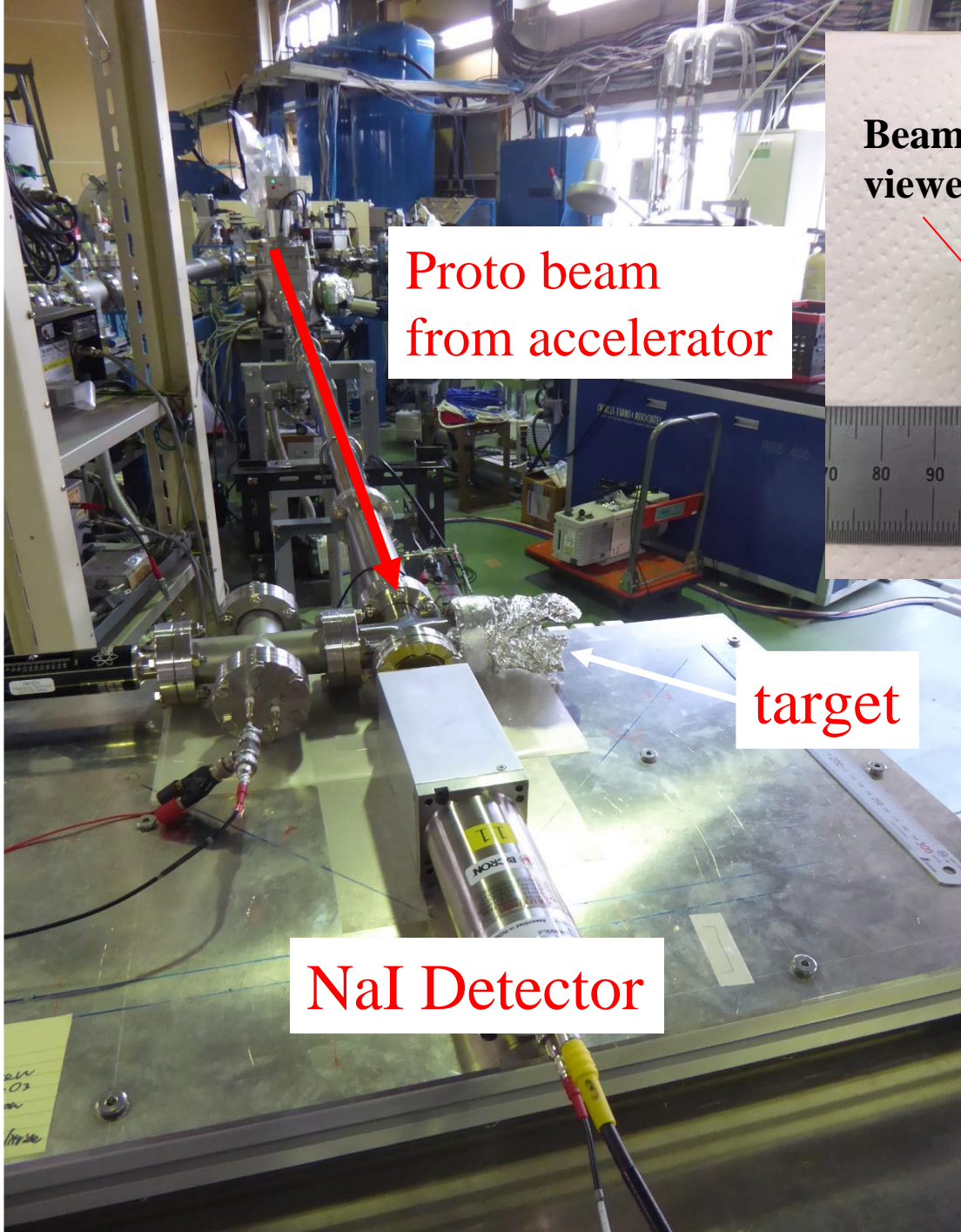
$$N_r = N_b \times N_t \times \sigma$$

How many reactions occur?

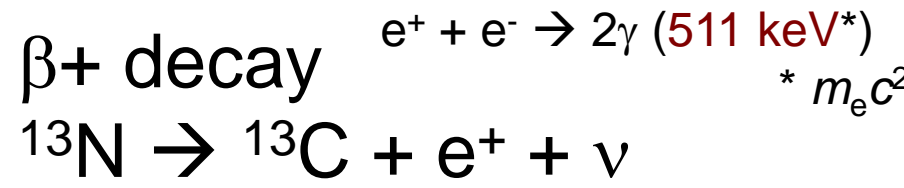
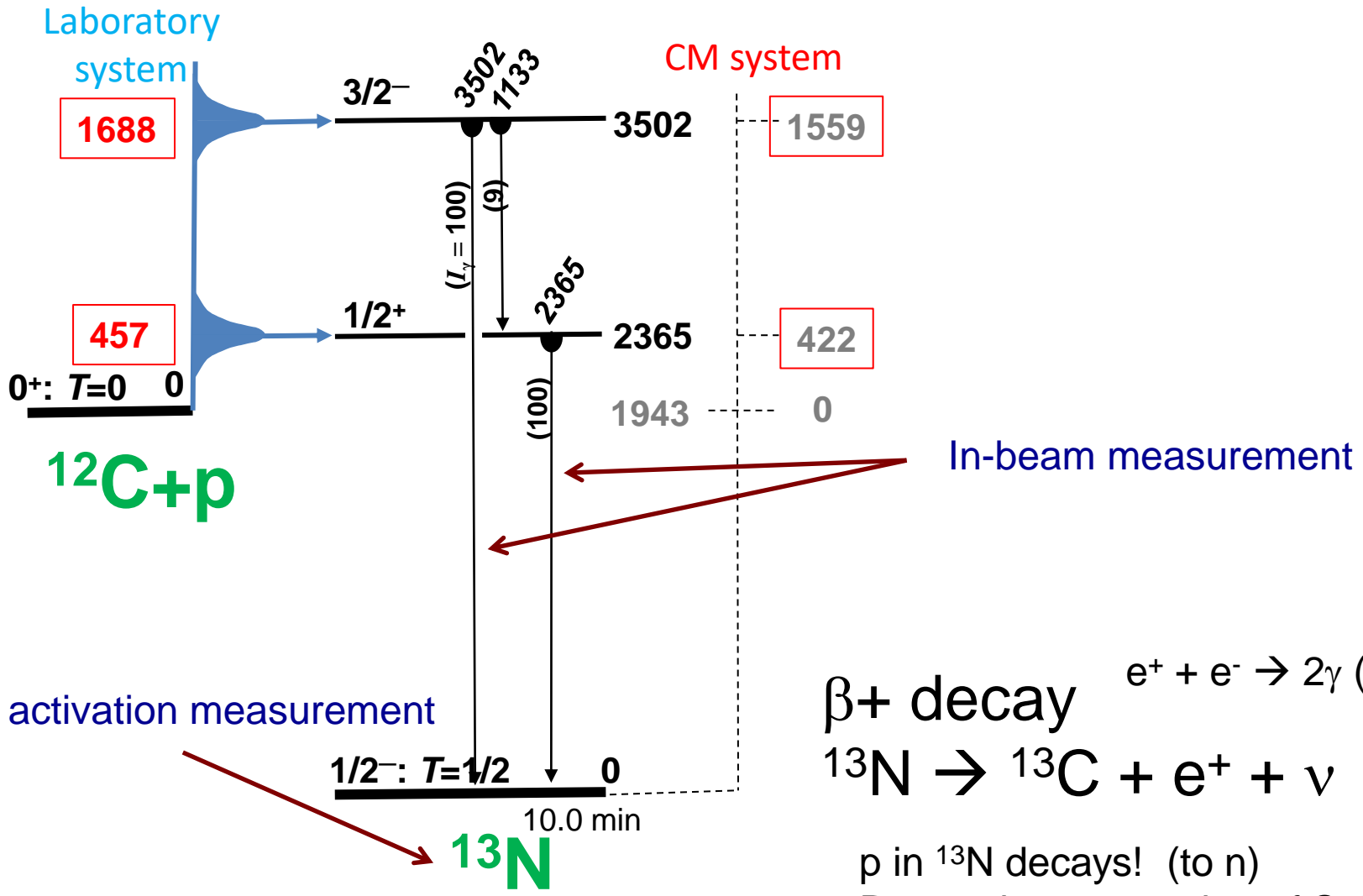
= (# of beams) \times (# of target/unit area) \times (Cross section)



$$N_{\gamma} = N_b \times N_t \times d\sigma/d\Omega \times d\Omega \times \varepsilon \times P_{\gamma}$$



“in-beam” and “activation”



p in ¹³N decays! (to n)
 Remember a question of Sakurai san

Extraction of the (resonant capture) **cross section** of $^{12}\text{C}(p,\gamma)^{13}\text{N}$

Important parameters

1. The number of protons : N_b
2. The number of ^{12}C : N_t
3. The number of the 1st or 2nd resonance populated : N_r
4. The number of emitted γ : N_γ

Extraction of the (resonant capture) cross section of $^{12}\text{C}(p,\gamma)^{13}\text{N}$

-- more in details --

I : electric current of the beam

e : electron charge

t : measurement time

σ : cross section of $p+^{12}\text{C} \rightarrow ^{13}\text{N}^*(2^{\text{nd}} : 3502 \text{ keV})$ reaction

ρ : density of target carbon foil

T : thickness of target carbon foil

N_A : Avogadro number

P_γ : decay branching ratio of the 3502 keV resonance

Ω : solid angle of NaI(Tl)

ε : photo peak efficiency of 3502 keV

$$N_b = I \cdot t / e$$

$$N_t = N_A \cdot T \cdot \rho / 12$$

$$N_r = N_b \cdot N_t \cdot \sigma$$

$$N_\gamma = N_r \cdot P_\gamma \cdot (\Omega / 4\pi) \cdot \varepsilon$$

[Parameters]

I : electric current of the beam

e : electron charge

t : measurement time

σ : cross section of p+¹²C ->
¹³N*(2nd:3502 keV) reaction

ρ : density of target carbon foil

T : thickness of target carbon foil

N_A : Avogadro number

P_γ : decay branching ration of 3502 keV

Ω : solid angle of NaI(Tl)

ε : photo peak efficiency of 3502 keV

$$\sigma = N_\gamma \cdot 12 \cdot 4\pi / (I / e \cdot t \cdot N_A \cdot T \cdot \rho \cdot P_\gamma \cdot \Omega \cdot \varepsilon)$$

$$d\sigma / d\Omega = N_\gamma \cdot 12 / (I / e \cdot t \cdot N_A \cdot T \cdot \rho \cdot P_\gamma \cdot \Omega \cdot \varepsilon)$$

\bigcirc : should be measured
 during the experiment

Design of the experiments

Yield estimation

- the yield of the measurement to check the feasibility

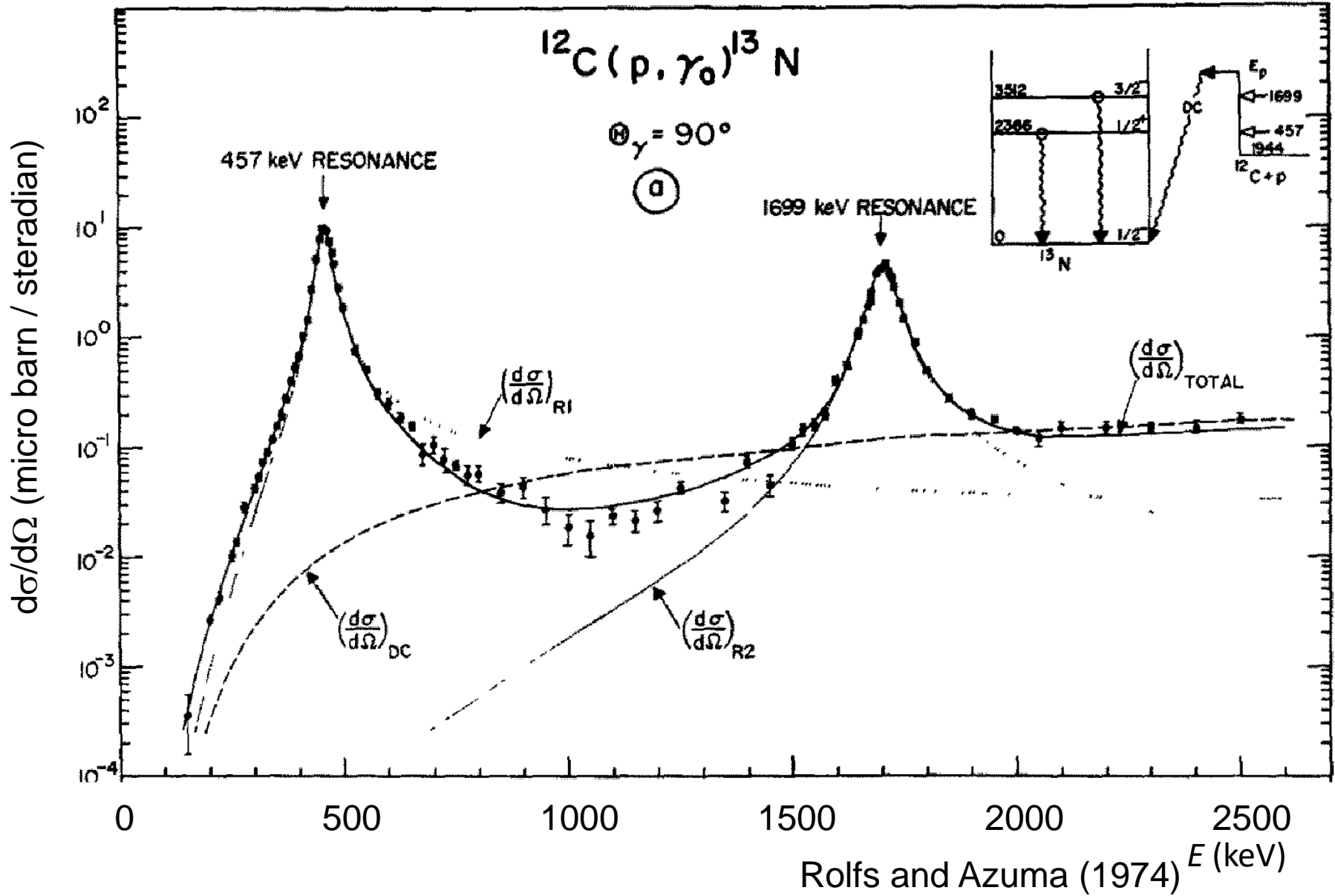
$$d\sigma / d\Omega = N_{\gamma} \cdot 12 / (I / e \cdot t \cdot N_A \cdot T \cdot \rho \cdot P_{\gamma} \cdot \Omega \cdot \varepsilon) \quad [\mu\text{barn/sr}]$$

- Let's estimate the yield of N_{γ} this afternoon!

Useful information for yield estimation

- Assumption
 - Typical beam current : **I = 200 [nA]**
 - Typical measurement time : **20 [min.]**
- Please consider and check whether **the measurement time (t)** and **the distance (L)** of NaI(Tl) to be set against the target are realistic or not.
You can select at L =10, 40, 80 cm
Be not beyond about 500 counts/sec, for γ ray counting rate.
- $1 \text{ mb} = 10^{-27} [\text{cm}^2]$
- Proton beam energy = 2 MeV
- Target thickness \gg proton range : “Thick target method”

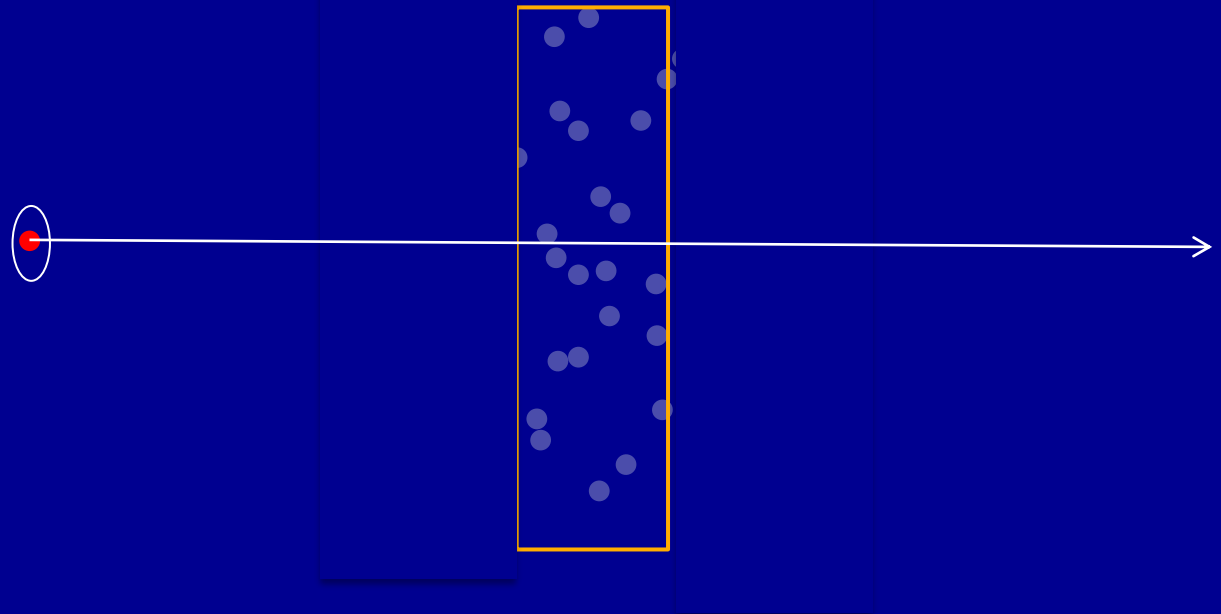
$^{12}\text{C}(p,\gamma)^{13}\text{N}$ cross section in literatures

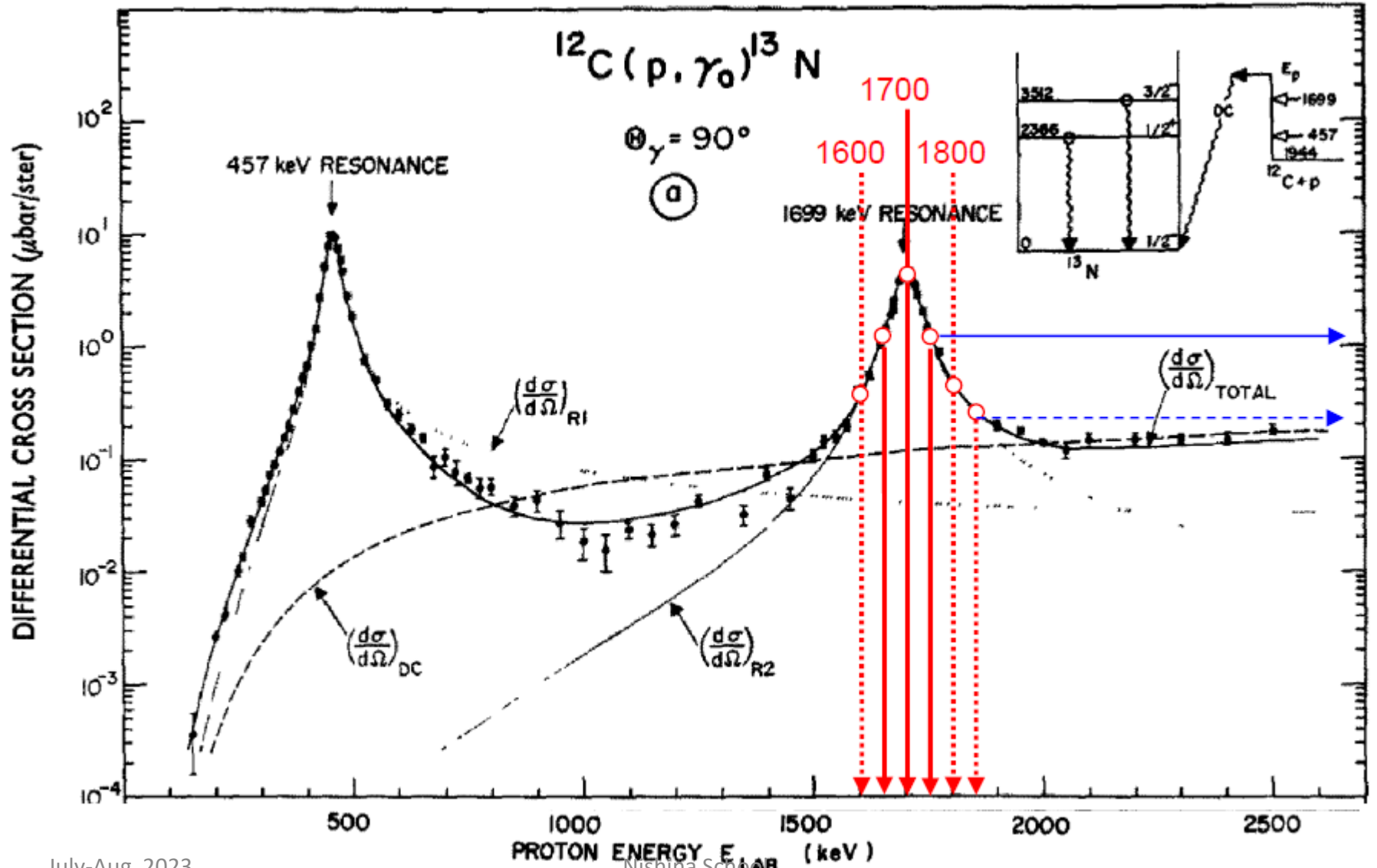


The usual method for a certain energy interval

Target: thin so that the p energy-change (loss) is small.

σ : cross section (area of the imaginary circle in the figure)

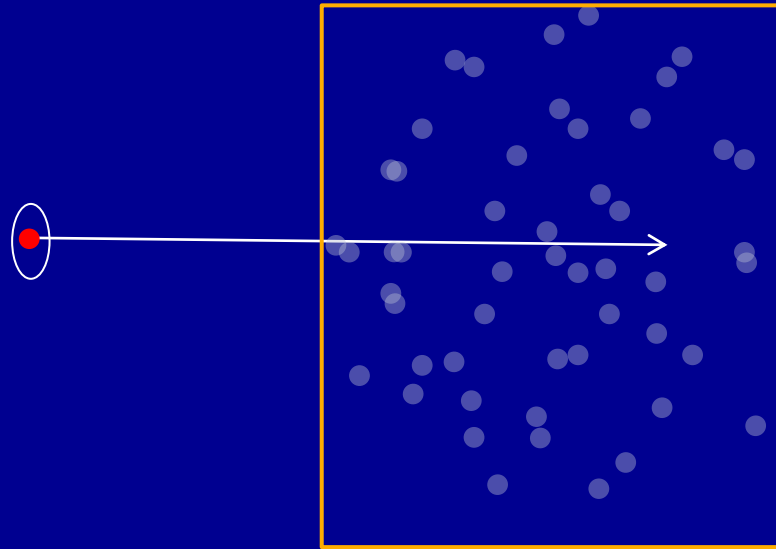




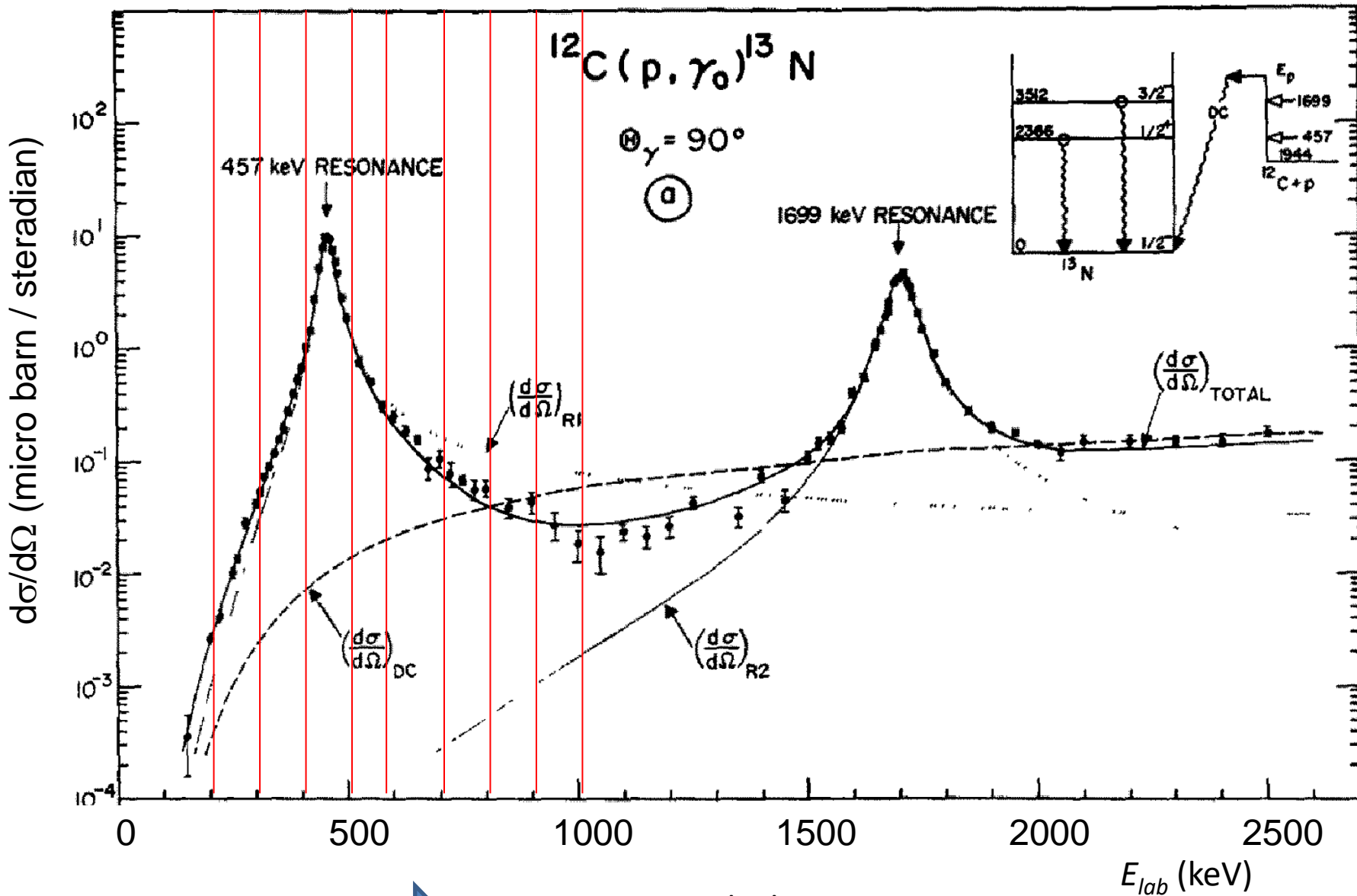
The thick target method

Target: thick enough to stop the beam

σ : cross section (area of the imaginary circle in the figure)



γ rays can be emitted in various different proton energies.
→ cross section integrated over a certain energy range.

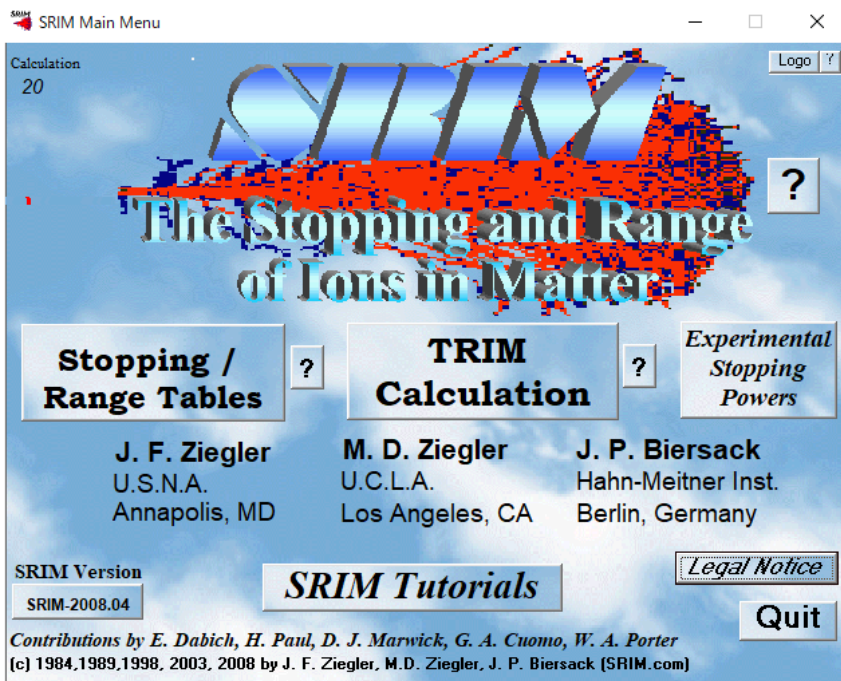


Covert to target thickness
from proton range

Rolfs and Azuma (1974)

Calculation for Range → SRIM code (free soft)

<http://www.srim.org/>



=====
Target Composition
=====

Atom Name	Atom Numb	Atomic Percent	Mass Percent
C	6	100.00	100.00

Proton beam in Carbon

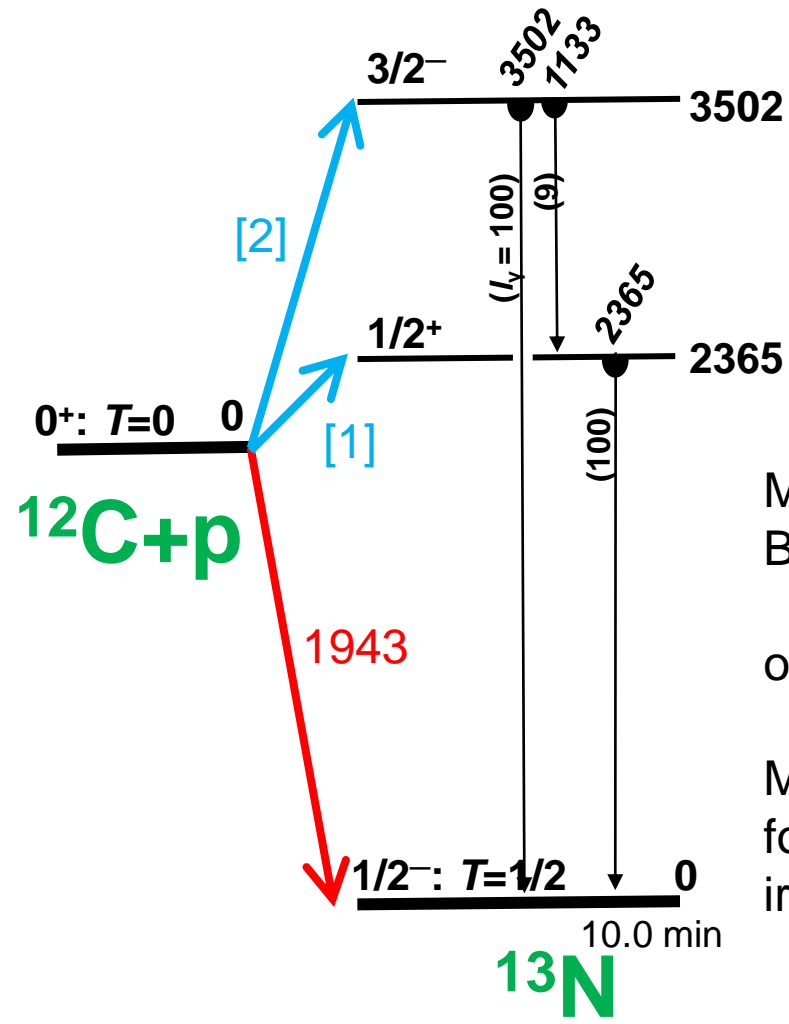
Bragg Correction = 0.00%

Stopping Units = MeV / (mg/cm2)

See bottom of Table for other Stopping units

Ion Energy	dE/dx Elec.	dE/dx Nuclear	Projected Range	Longitudinal Straggling	Lateral Straggling
500.00 keV	3.534E-01	2.738E-04	4.40 um	1837 A	1974 A
550.00 keV	3.334E-01	2.524E-04	5.04 um	2092 A	2182 A
600.00 keV	3.160E-01	2.342E-04	5.72 um	2347 A	2402 A
650.00 keV	3.007E-01	2.186E-04	6.44 um	2601 A	2632 A
700.00 keV	2.872E-01	2.051E-04	7.19 um	2856 A	2873 A
800.00 keV	2.640E-01	1.828E-04	8.80 um	3732 A	3385 A
900.00 keV	2.450E-01	1.651E-04	10.54 um	4553 A	3934 A
1.00 MeV	2.291E-01	1.507E-04	12.41 um	5350 A	4520 A
1.10 MeV	2.163E-01	1.387E-04	14.40 um	6134 A	5138 A
1.20 MeV	2.035E-01	1.286E-04	16.51 um	6915 A	5788 A
1.30 MeV	1.923E-01	1.199E-04	18.74 um	7703 A	6473 A
1.40 MeV	1.825E-01	1.124E-04	21.11 um	8501 A	7191 A
1.50 MeV	1.737E-01	1.058E-04	23.59 um	9309 A	7943 A
1.60 MeV	1.659E-01	9.998E-05	26.20 um	1.01 um	8727 A
1.70 MeV	1.588E-01	9.481E-05	28.93 um	1.10 um	9543 A
1.80 MeV	1.524E-01	9.017E-05	31.77 um	1.18 um	1.04 um
2.00 MeV	1.412E-01	8.219E-05	37.81 um	1.48 um	1.22 um

In-beam or activation



Measuring γ rays during BOT (the proton beams on the target)

or

Measuring the ^{13}N activity (511 keV photons following the β^+ decay) after the beam irradiation

Radioactive decay

$$N(t) = N_0 \exp[-t/\tau] \quad (N_0 e^{-t/\tau})$$

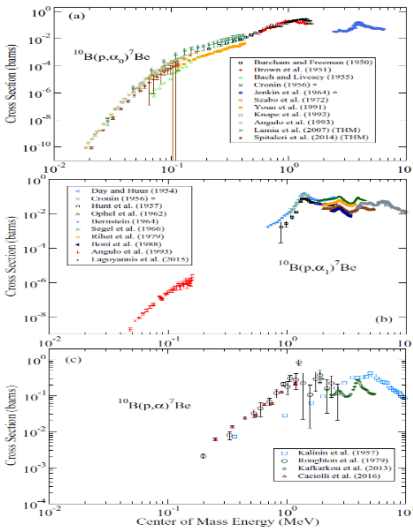
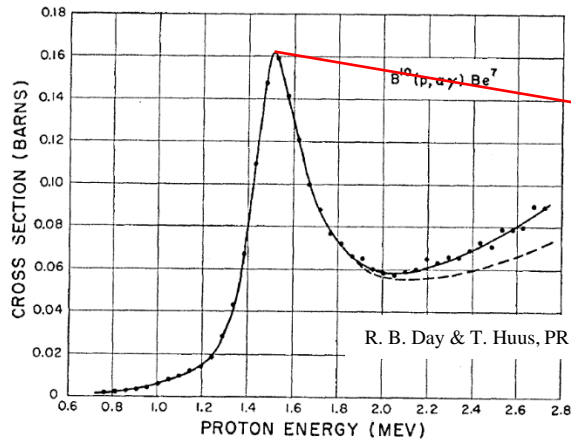
N : number of the initial nucleus (survived)
or number of decay per unit time

τ : mean life

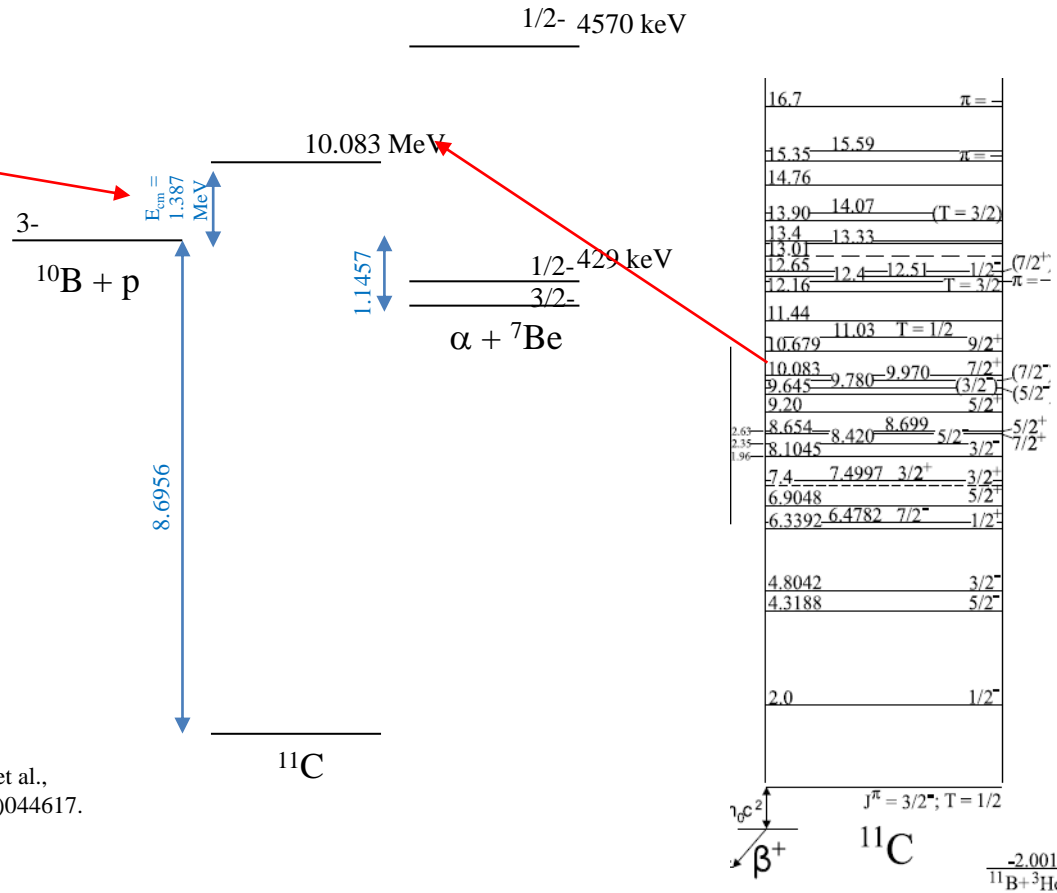
$$t_{1/2} = \text{half life} \quad \text{---} \quad N(t_{1/2}) = N_0/2$$

Q: Estimate the counts after 20 min. proton irradiation.

$^{10}\text{B}(p, \alpha\gamma)^7\text{Be}$



M. Wiescher, et al.,
PRC 95 (2017)044617.



Note)
Density of current Boron Nitride target
 $d = 2.06 \text{ g/cm}^3$

$^{27}\text{Al}(p, p_1\gamma)^{27}\text{Al}$, $^{27}\text{Al}(p, p_2\gamma)^{27}\text{Al}$ and $^{27}\text{Al}(p, \alpha\gamma)^{24}\text{Mg}$ reactions

Nuclear Instruments and Methods in Physics Research B 394 (2017) 28–32

Contents lists available at ScienceDirect

Nuclear Instruments and Methods in Physics Research B

journal homepage: www.elsevier.com/locate/nimb



Thick target yields of proton induced gamma-ray emission from Al, Si and P



A. Jokar*, O. Kakuee, M. Lamehi-Rachti, V. Fathollahi

Physics & Accelerators Research School, NSTRI, P O Box 14395-836, Tehran, Iran

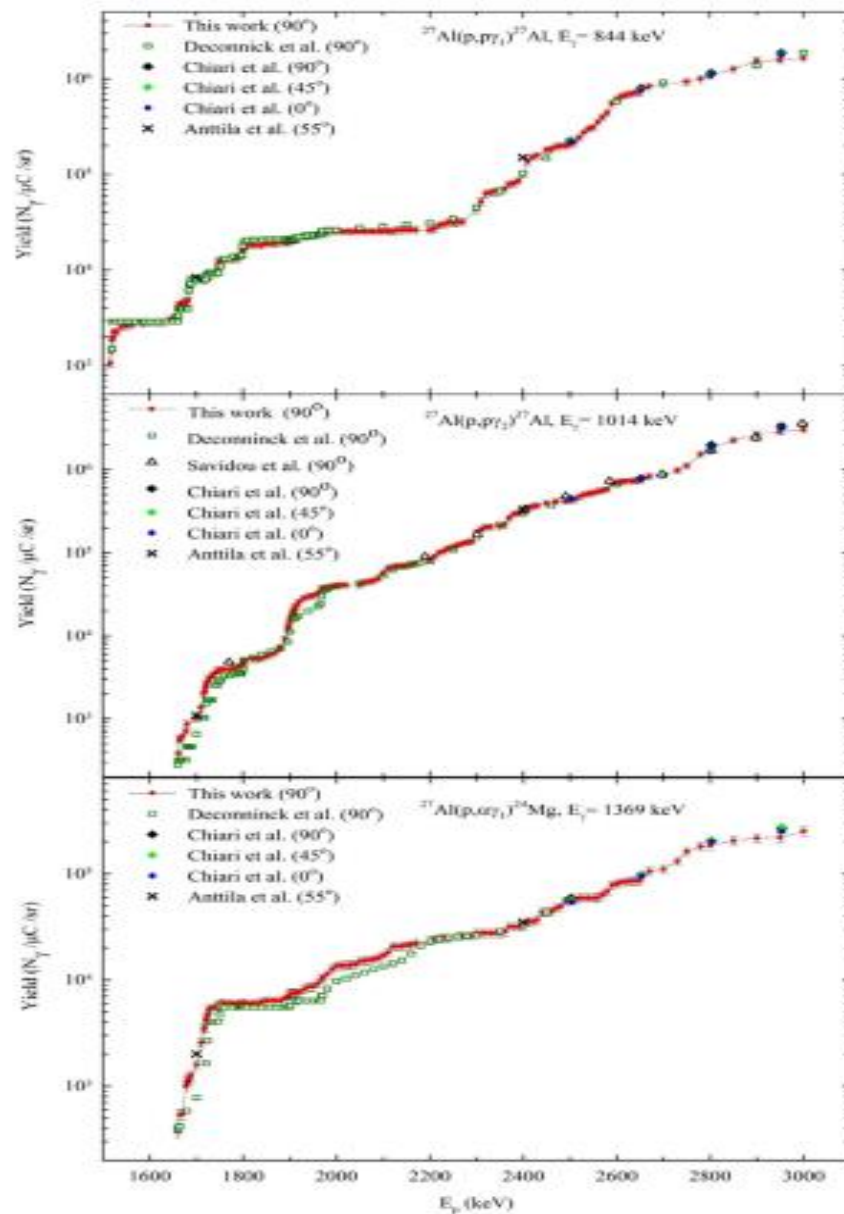
ARTICLE INFO

Article history:
Received 6 November 2016
Received in revised form 14 December 2016
Accepted 19 December 2016
Available online 30 December 2016

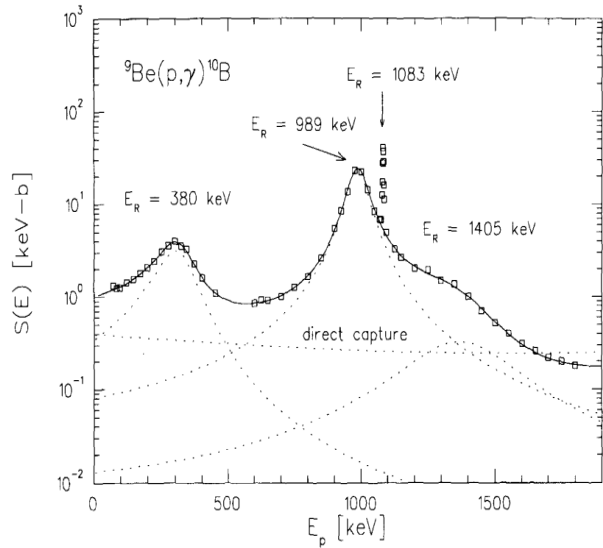
ABSTRACT

Thick target excitation yield curves of gamma-rays from the reactions $^{27}\text{Al}(p, p_1\gamma)^{27}\text{Al}$ ($E_\gamma = 844$ and 1014 keV), $^{27}\text{Al}(p, \alpha\gamma)^{24}\text{Mg}$ ($E_\gamma = 1369$ keV), $^{28}\text{Si}(p, p'\gamma)^{28}\text{Si}$ ($E_\gamma = 1779$ keV), $^{29}\text{Si}(p, p'\gamma)^{29}\text{Si}$ ($E_\gamma = 1273$ keV) and $^{31}\text{P}(p, p'\gamma)^{31}\text{P}$ ($E_\gamma = 1266$ keV) were measured by bombarding pure-element targets with protons at energies below 3 MeV. Gamma-rays were detected with a High Purity Ge detector placed at an angle of 90° with respect to the beam direction. The obtained thick target gamma-ray yields were compared with the previously published data. The overall systematic uncertainty of the thick target yield values

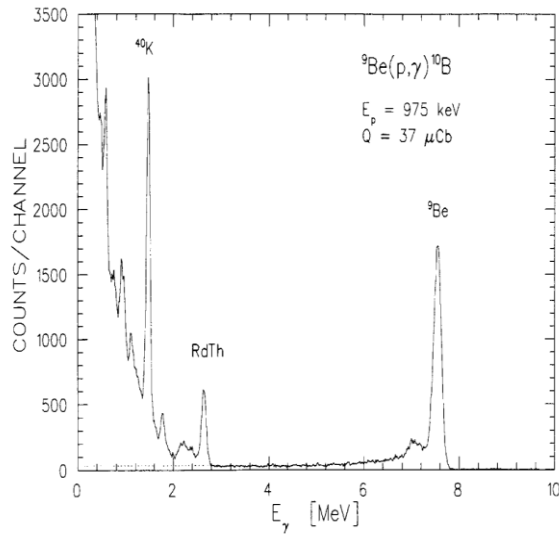
γ ray yields on thick Al target
($N_\gamma/\mu\text{C}/\text{sr}$ on literature)
 \Rightarrow Can estimate N_γ without
of target



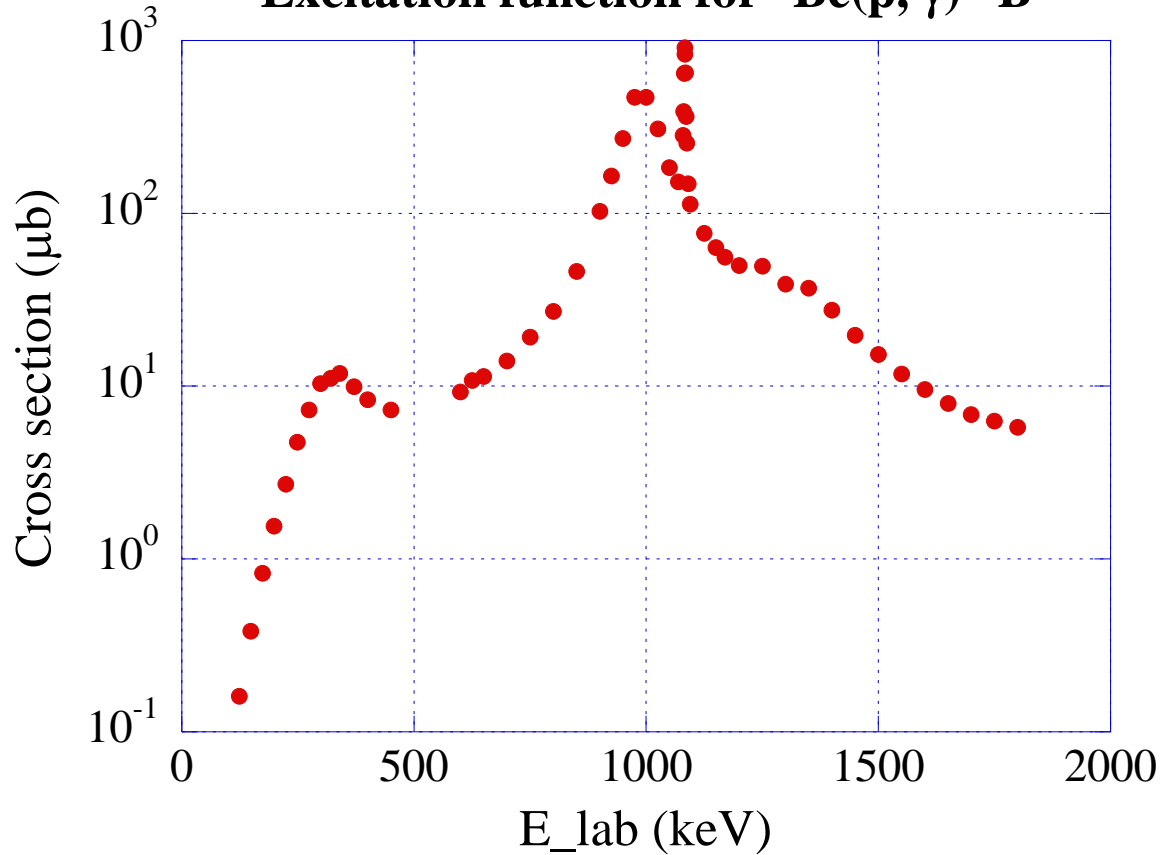
${}^9\text{Be}(p, \gamma){}^{10}\text{B}$ reaction



D. Zahnow et al. / Nuclear Physics A 589 (1995) 95-105



Excitation function for ${}^9\text{Be}(p, \gamma){}^{10}\text{B}$



Solid angle (unit: steradian)

Beam intensity: We assume 200 nA. (elementary charge: 1.6×10^{-19} C;
 $1 \text{ A} = 1 \text{ C/s}$)

Size of the NaI(Tl) crystal: $6 \times 6 \times 12 \text{ cm}^2$

“Target thickness”

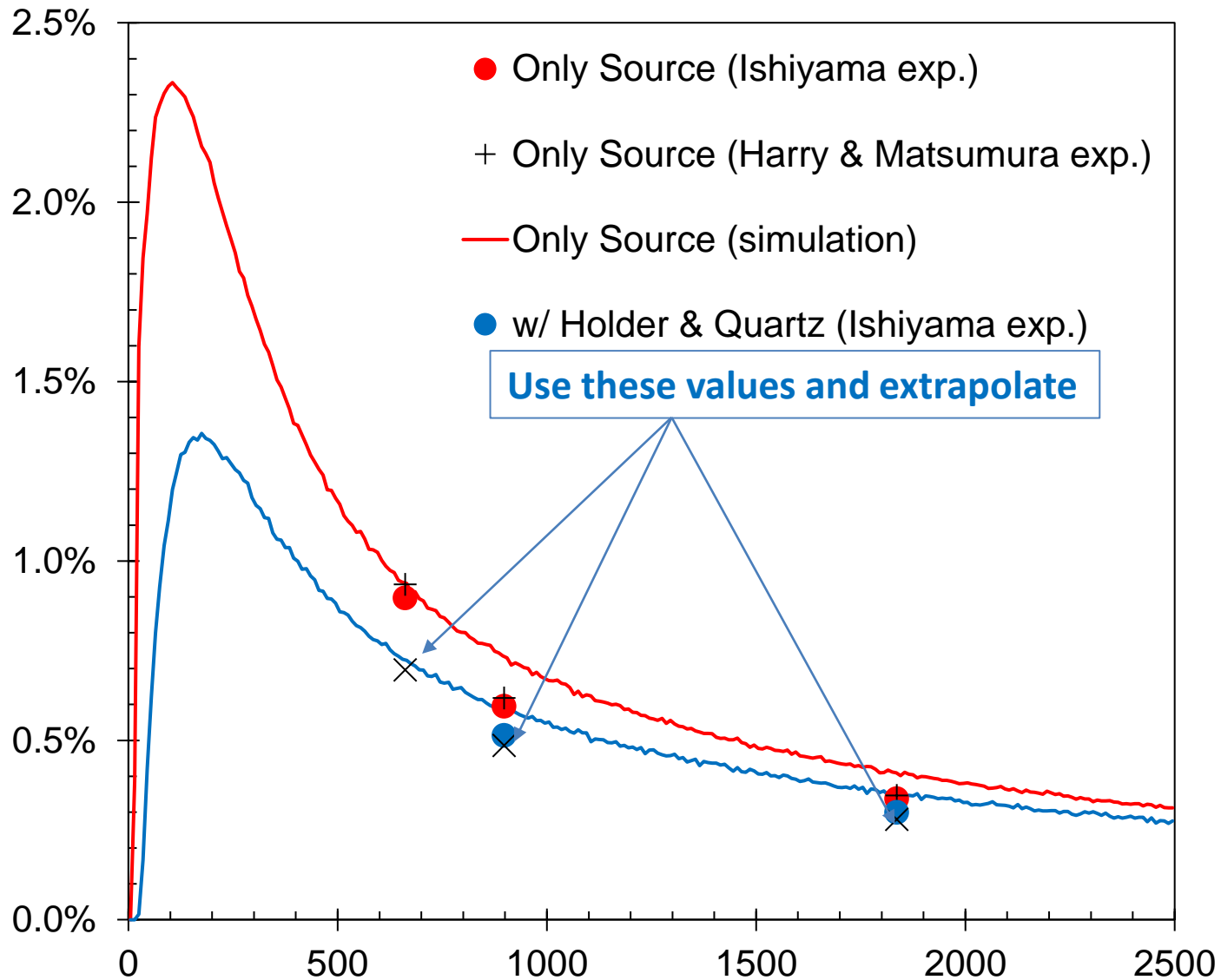
divide into 10 or 20 slices.

Photo (full-energy-peak) efficiency of the NaI(Tl) => Use following figures

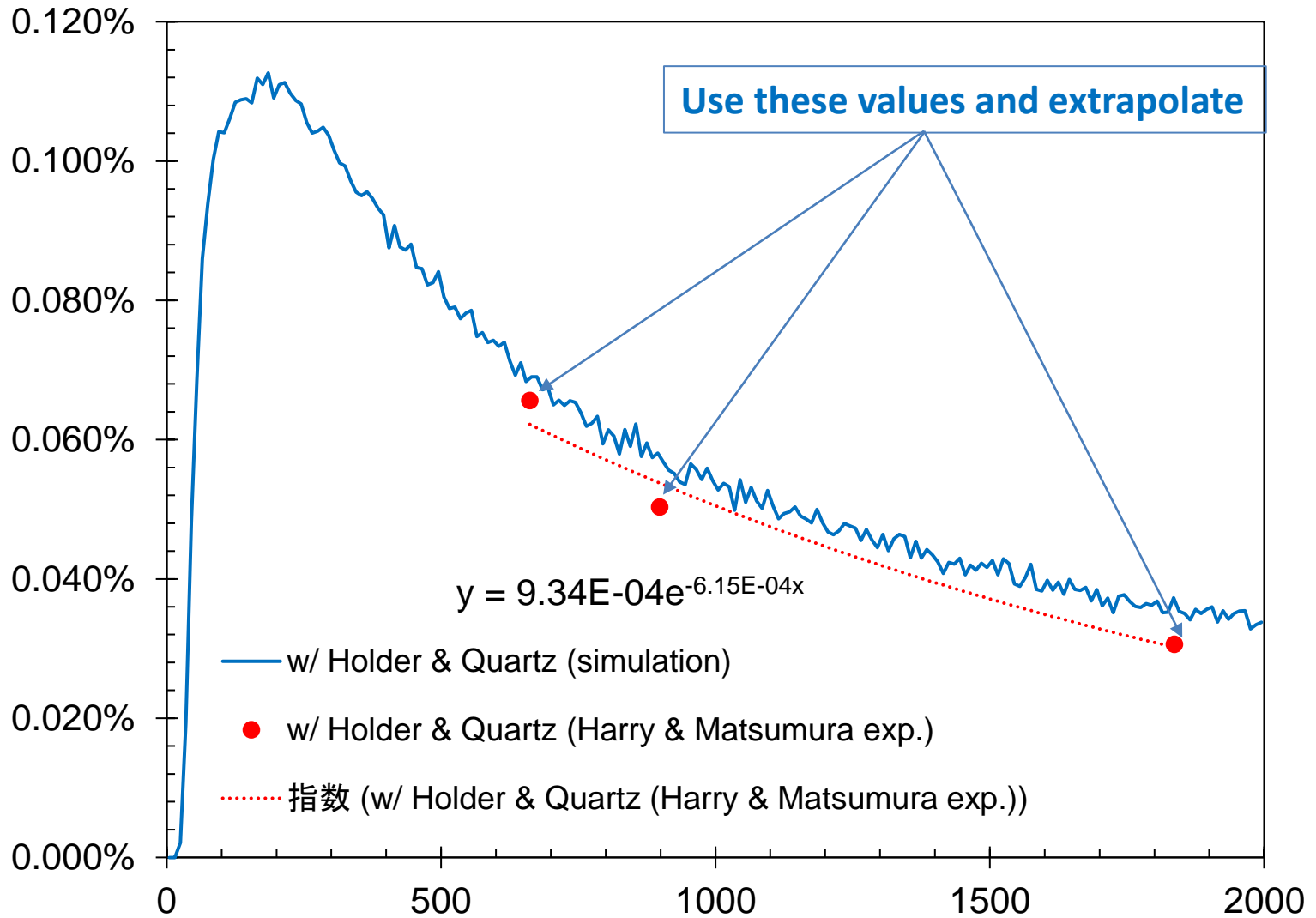
Which distance from the target to the center of NaI(Tl) scintillator should be?

NaI Detector efficiency at L = 10 cm

(For ${}^9\text{Be}$ measurement, ask Matsumura san)



NaI Detector efficiency at L = 40 cm



NaI Detector efficiency at L = 80 cm

