

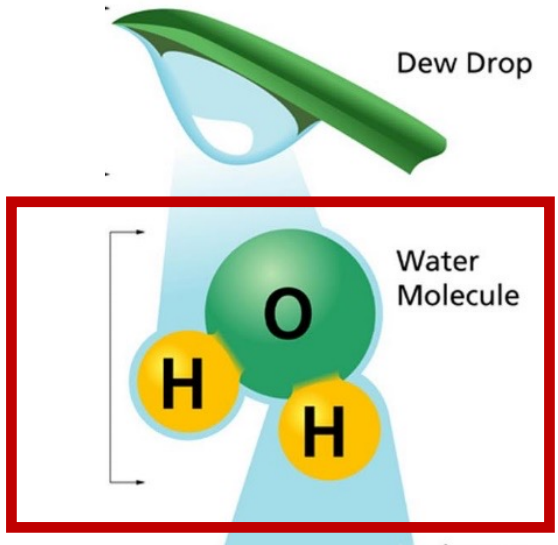
# 20 years of exotic hadrons

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Nishina Summer School, 27/July/2023  
RIKEN, Japan

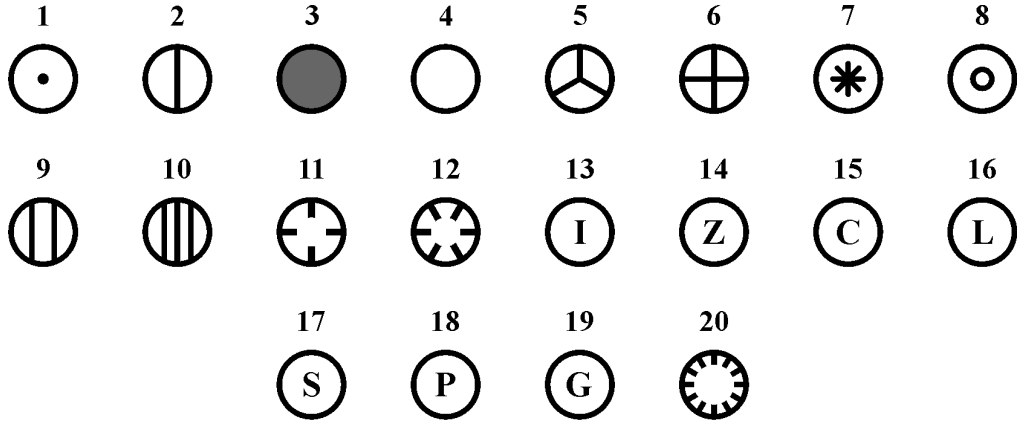
# What is matter made of



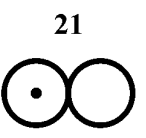
## Atomic theory of John Dalton [~1800]

All matter is made of indivisible atoms/elements

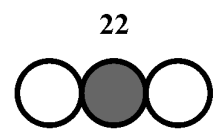
### Simple Elements



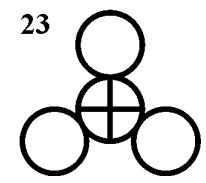
### Binary



### Ternary



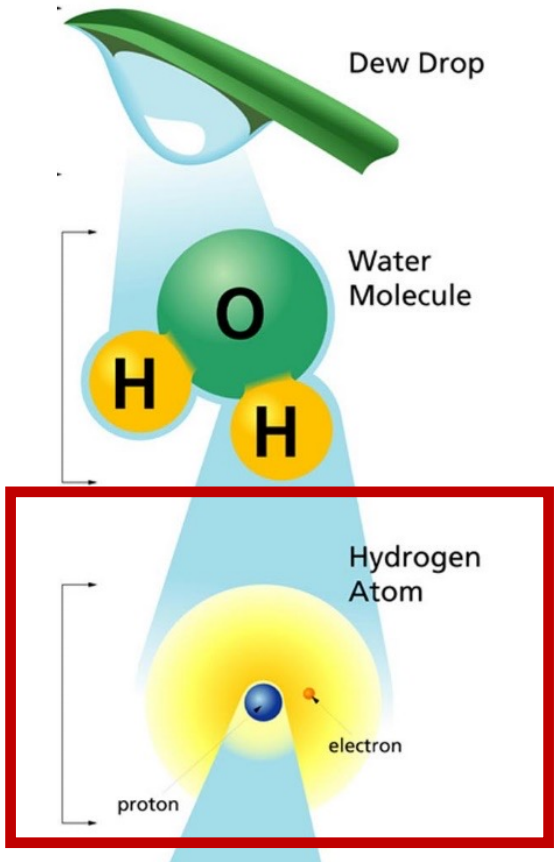
### Quaternary



discovered at

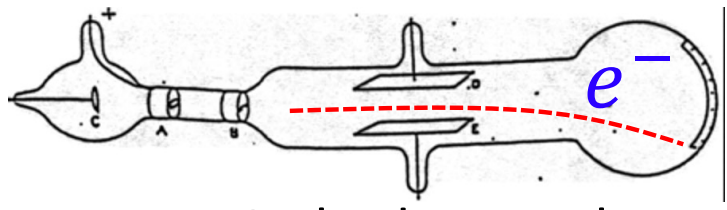


# What is matter made of



## Atomic structure [~1900 -1950]

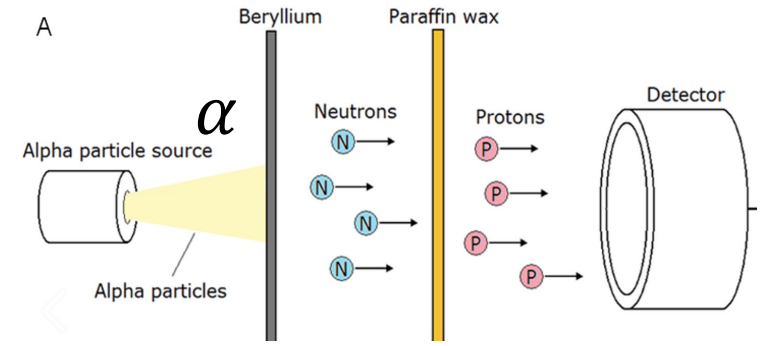
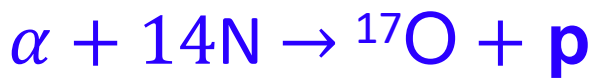
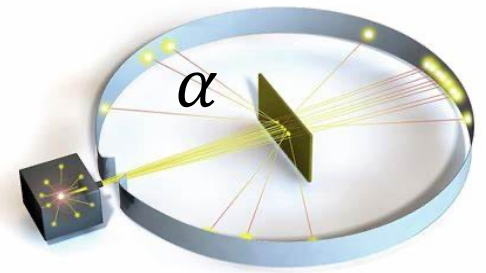
Discovery of **electrons** by Thomson, 1897



Cathode ray tubes

Discovery of **nuclei and proton** by Rutherford, 1910s

Discovery of **neutron** by Chadwick, 1932

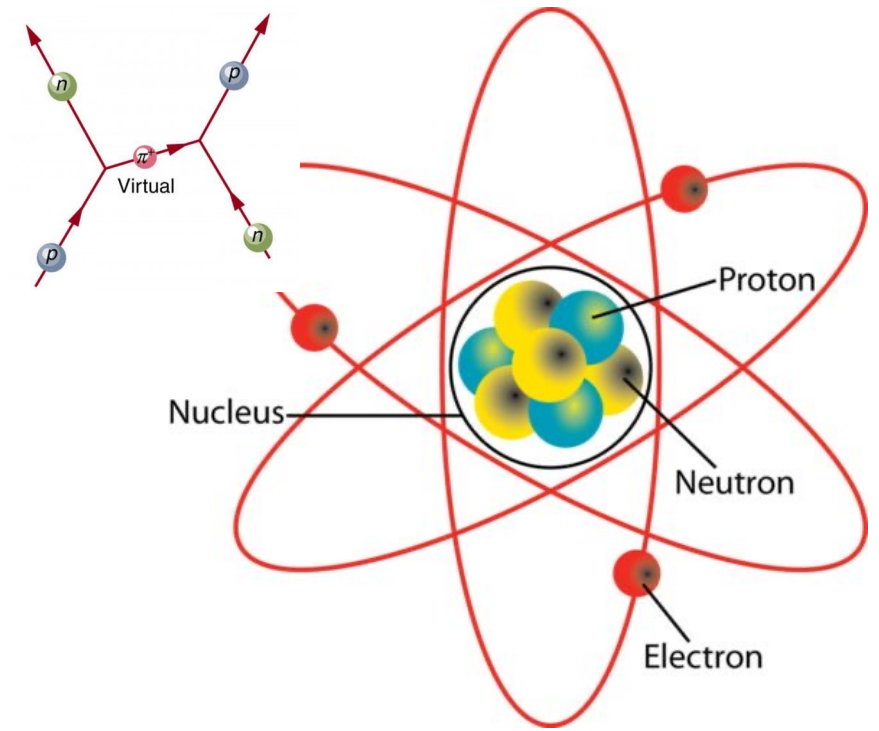
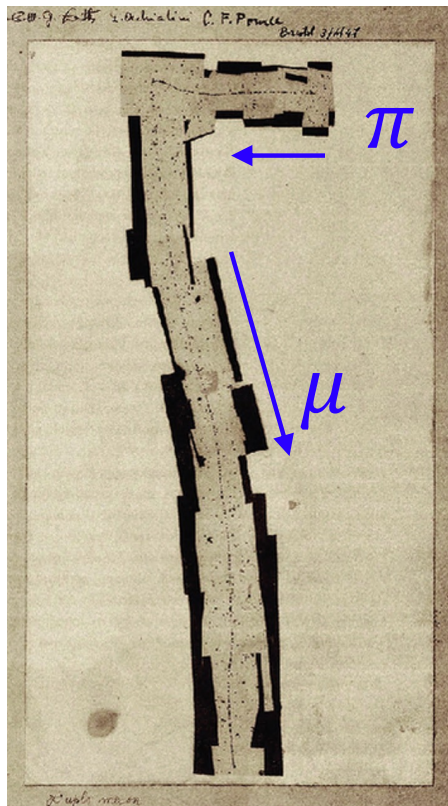


# Nuclear force

Yukawa interaction between nucleons [1935]

A strong interaction mediated by pions

Pions discovered by Powell in cosmic rays, 1947



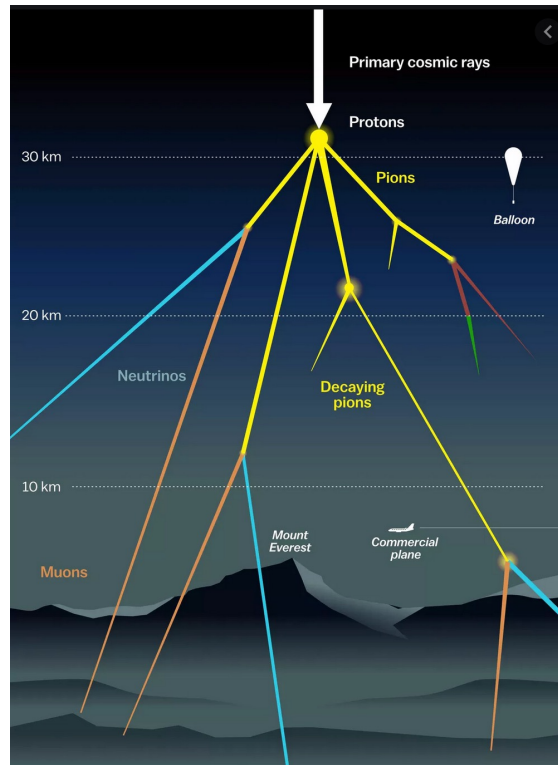
The model of matter up to 1950s

Proton }  
Neutron }  $\pi$  } Nucleus  
Electron }  $\gamma$  } Atom

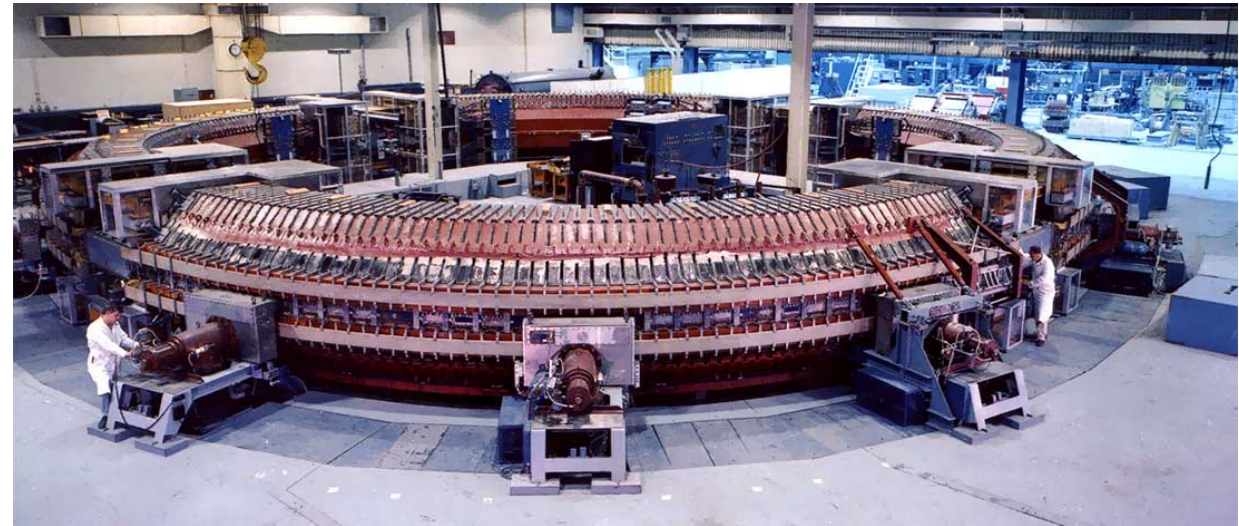
# The zoo of hadrons

- Two ways of new particle appearance

Cosmic rays



Accelerators, since 1950s



Eg: Cosmotron (1952-66) at Brookhaven

- New particles discovered

$p, n, \Sigma, \Lambda, \Xi, \Delta, \dots$  baryons

$\pi, K, \rho, \omega, \phi, \eta, \dots$  mesons

Or hadrons, strongly interacting particles



Wolfgang Pauli:

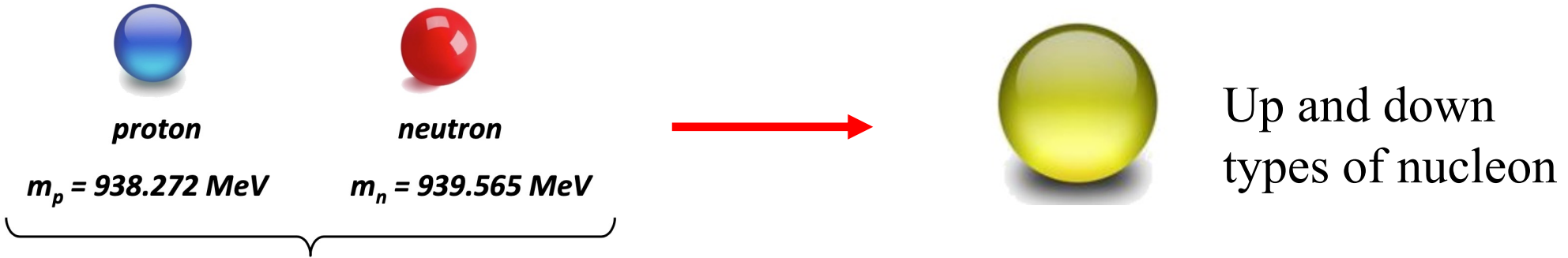
“Had I foreseen that (these particles), I would have gone into botany!” , or zoology

All elementary?

Do they exist for any reasons?

# Isospin symmetry among hadrons

- Proton and neutron **identical** under strong interaction



Introduce new quantum number: *isospin*

Proton and neutron form isospin doublet  $(I, I_3)$ :  $p = \left| \frac{1}{2}, +\frac{1}{2} \right\rangle$ ,  $n = \left| \frac{1}{2}, -\frac{1}{2} \right\rangle$

Indication of internal degree of freedom

- Other isospin multiplets

$I = 1/2$

$K^+$   $\left| \frac{1}{2}, +\frac{1}{2} \right\rangle$   
 $K^0$   $\left| \frac{1}{2}, -\frac{1}{2} \right\rangle$

$m_K \sim 500 \text{ MeV}$

$I = 1$

$\pi^+$   $|1, +1\rangle$   
 $\pi^0$   $|1, 0\rangle$   
 $\pi^-$   $|1, -1\rangle$

$m_\pi \sim 140 \text{ MeV}$

$I = 3/2$

$\Delta^{++}$   $\left| \frac{3}{2}, +\frac{3}{2} \right\rangle$   
 $\Delta^+$   $\left| \frac{3}{2}, +\frac{1}{2} \right\rangle$   
 $\Delta^0$   $\left| \frac{3}{2}, -\frac{1}{2} \right\rangle$   
 $\Delta^-$   $\left| \frac{3}{2}, -\frac{3}{2} \right\rangle$

$m_\Delta \sim 1232 \text{ MeV}$

# Extending the symmetry

- The eight-fold way by Gell-Mann (1961): **hadrons arranged in multiplets according to isospin and strangeness** (another internal quantum number)

8 lightest strange baryons: baryon octet



Particle	Mass	S
<b>n</b>	<b>938.3</b>	<b>0</b>
<b>p</b>	<b>939.6</b>	<b>0</b>
$\Sigma^+$	<b>1189.4</b>	<b>-1</b>
$\Sigma^0$	<b>1192.6</b>	<b>-1</b>
$\Sigma^-$	<b>1197.4</b>	<b>-1</b>
$\Lambda^0$	<b>1115.6</b>	<b>-1</b>
$\Xi^0$	<b>1314.9</b>	<b>-2</b>
$\Xi^-$	<b>1321.3</b>	<b>-2</b>

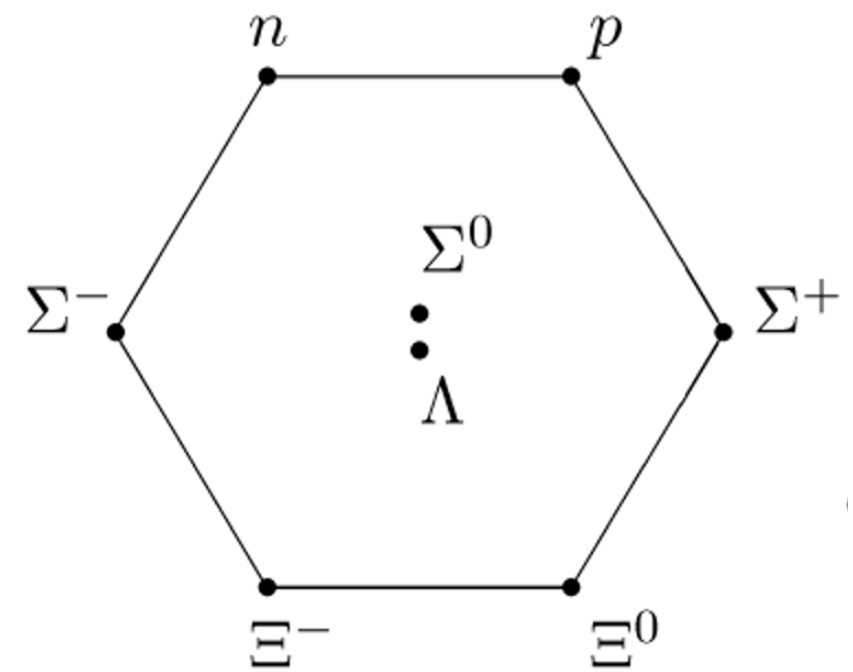
Strangeness increases



$s = 0$

$s = -1$

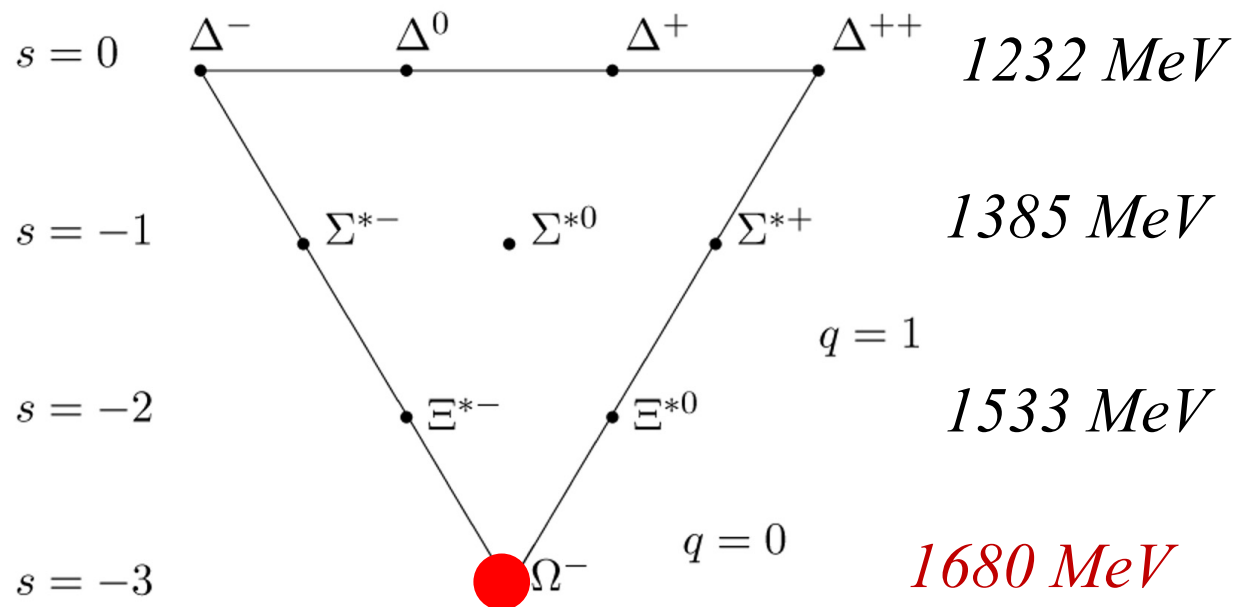
$s = -2$



$I_3$  increases

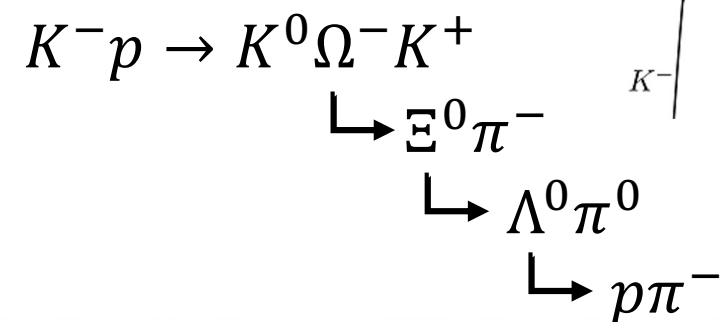
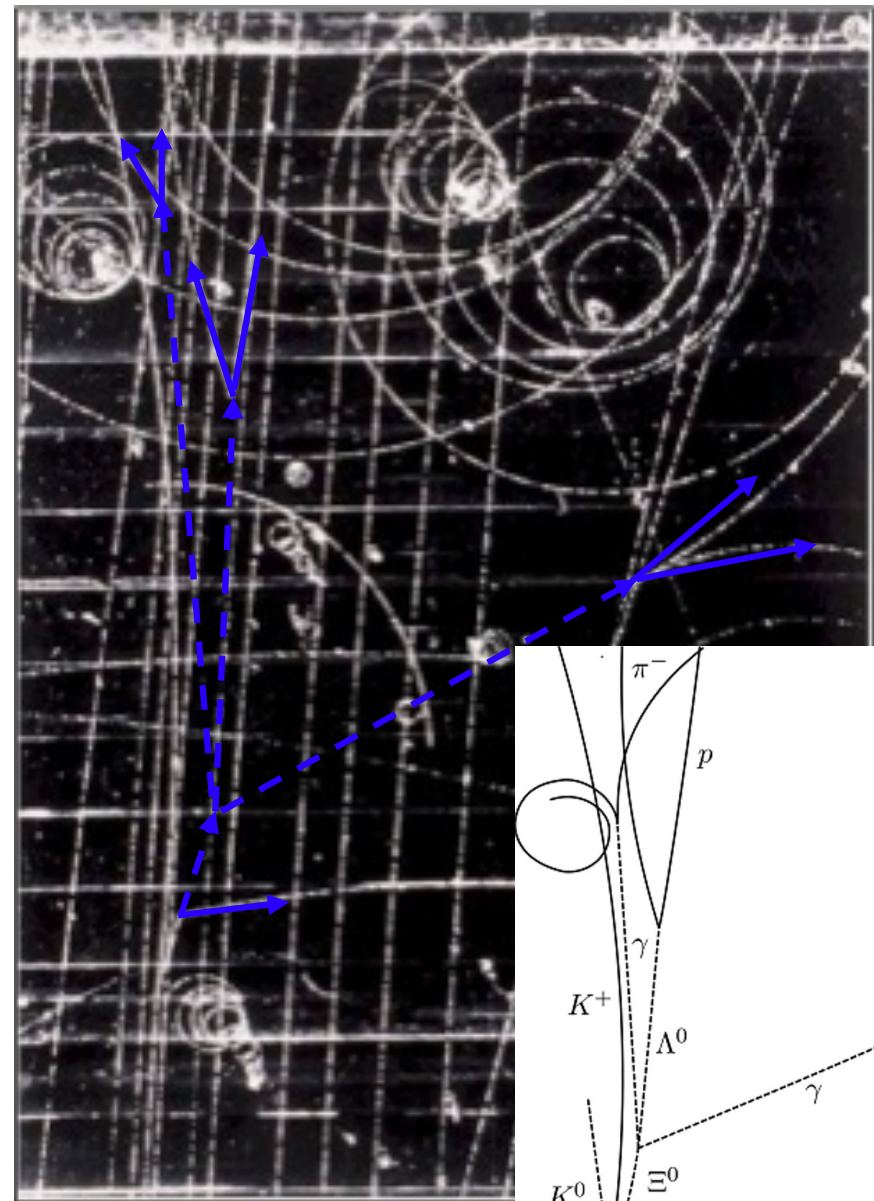


# Baryon decuplet



$\Omega^-$  baryon not known by then

Eight-fold way predicts  $\Omega^-$  and its properties. Observed in 1964.





# The quark model

- Gell-Mann and Zweig (1964):

“All multiplet patterns can be explained if you assume **hadrons are composite particles built from more elementary constituents: quarks**”

## A SCHEMATIC MODEL OF BARYONS AND MESONS \*

M. GELL-MANN

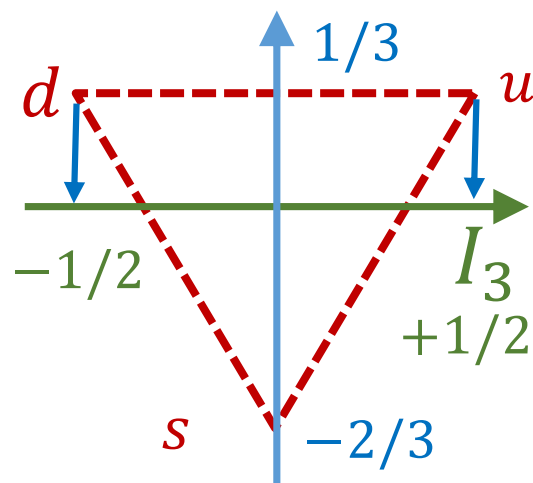
*California Institute of Technology, Pasadena, California*

Received 4 January 1964

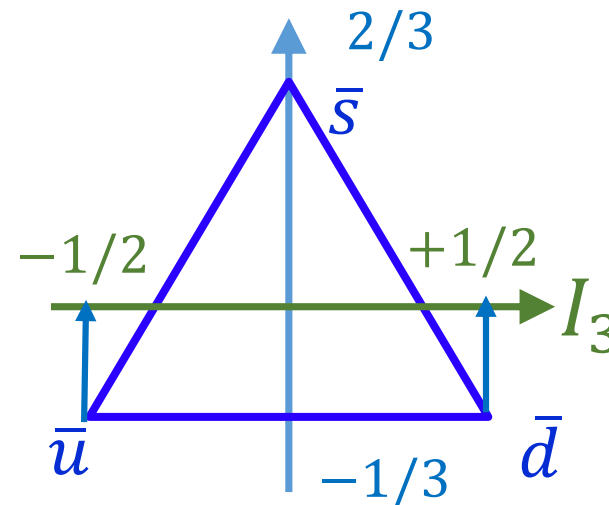
A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon  $\mathbf{b}$  if we assign to the triplet  $\mathbf{t}$  the following properties: spin  $\frac{1}{2}$ ,  $z = -\frac{1}{3}$ , and baryon number  $\frac{1}{3}$ . We then refer to the members  $u^{\frac{2}{3}}$ ,  $d^{-\frac{1}{3}}$ , and  $s^{-\frac{1}{3}}$  of the triplet as "quarks"  $\mathbf{q}$  and the members of the anti-triplet as anti-quarks  $\bar{\mathbf{q}}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqq\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(qq\bar{q}\bar{q})$ , etc. It is assuming that the lowest baryon configuration  $(qqq)$  gives just the representations **1**, **8**, and **10** that have been observed, while the lowest meson configuration  $(q\bar{q})$  similarly gives just **1** and **8**.

# Three quark flavors, SU(3)

- **Flavor** as a quantum number for quark: take three values  $u, d, s$ 
  - Strong interaction is blind to flavor, rotations among  $u, d, s$  form SU(3) symmetry
  - Isospin: symmetry between  $u - d$  flavors (quarks)
  - Symmetry breaking by non-strong interactions
    - Mass difference: large between  $u/d$  and  $s$ , smaller between  $u$  and  $d$
    - Electric charge difference:  $Q_u = +2/3, Q_{d/s} = -1/3$
- Mesons and baryons built from two basic flavor triplets



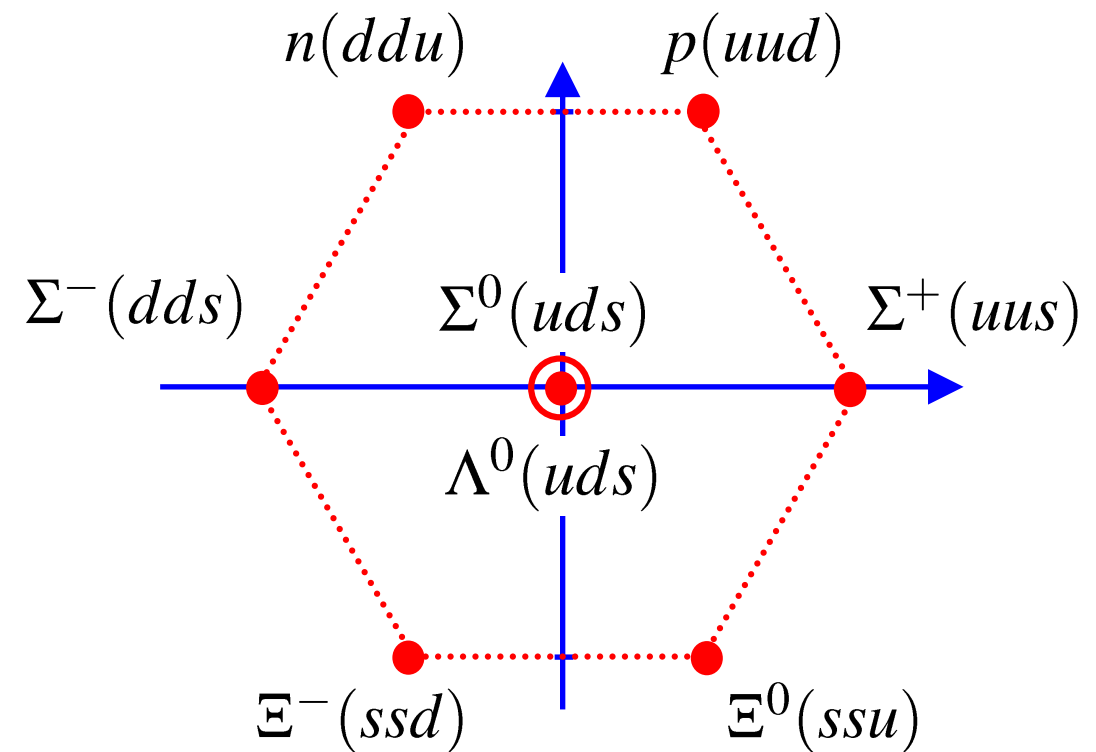
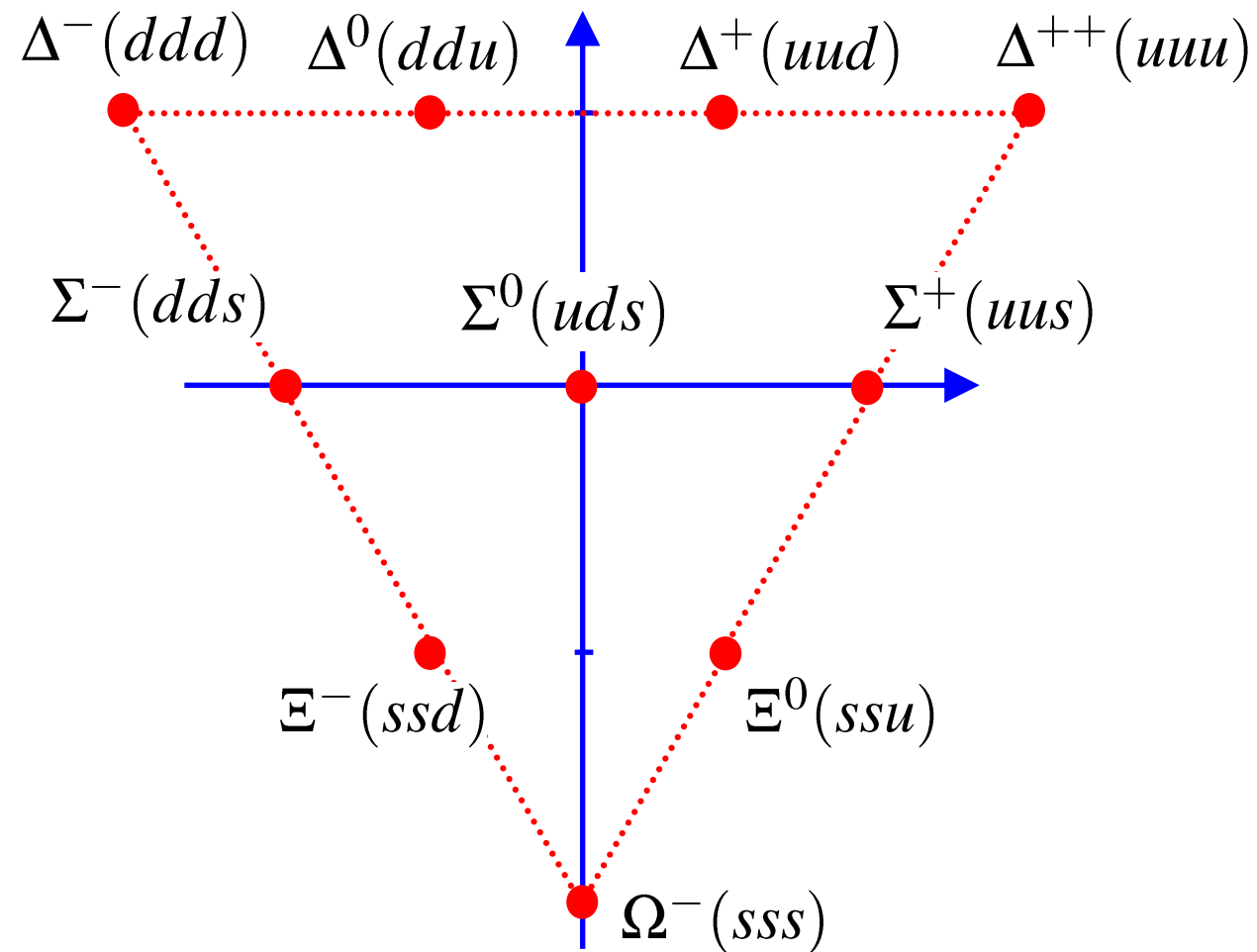
Quark



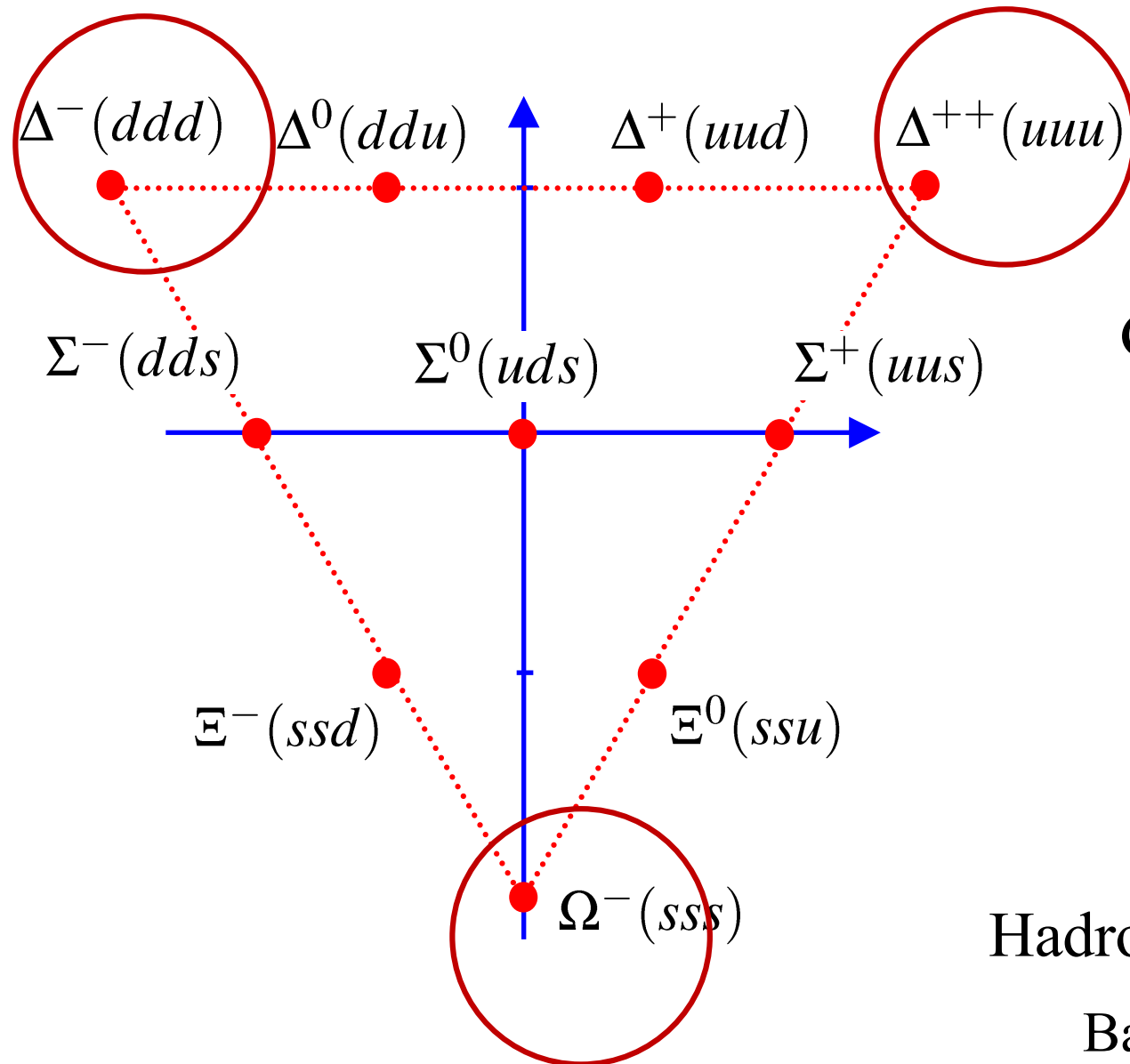
Antiquark

The genes of  
the particle zoo

# Quark configuration of known baryons



# The **color** quantum number



Pauli exclusion principle:  
can't be at the same configuration

Greenberg (1964):

Quark carries color quantum number

Red, Green, Blue

Antiquark carries anticolor

anti-Red, anti-Green, anti-Blue

Hadrons are colorless (color singlet) state

Baryons ( $qqq$ ): RGB

Mesons ( $q\bar{q}$ ):  $R\bar{R} + G\bar{G} + B\bar{B}$

# Hunting for quarks

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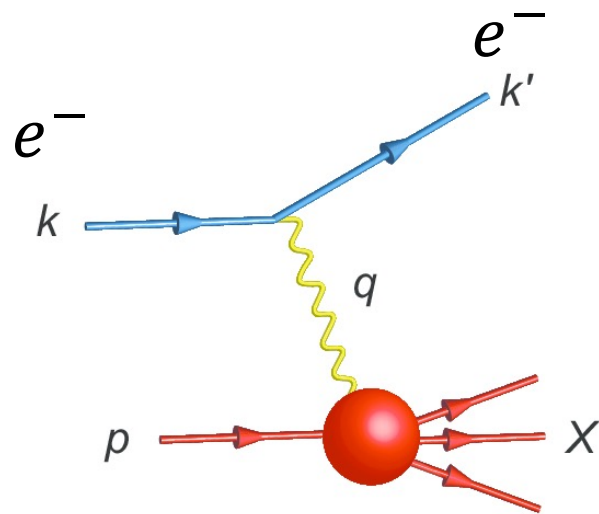
It is fun to speculate about the way quarks would behave if they were physical particles of finite mass (instead of purely mathematical entities as they would be in the limit of infinite mass). Since charge

that it would never have been detected. A search for stable quarks of charge  $-\frac{1}{3}$  or  $+\frac{2}{3}$  and/or stable di-quarks of charge  $-\frac{2}{3}$  or  $+\frac{1}{3}$  or  $+\frac{4}{3}$  at the highest energy accelerators would help to reassure us of the non-existence of real quarks.

No free quarks ever observed

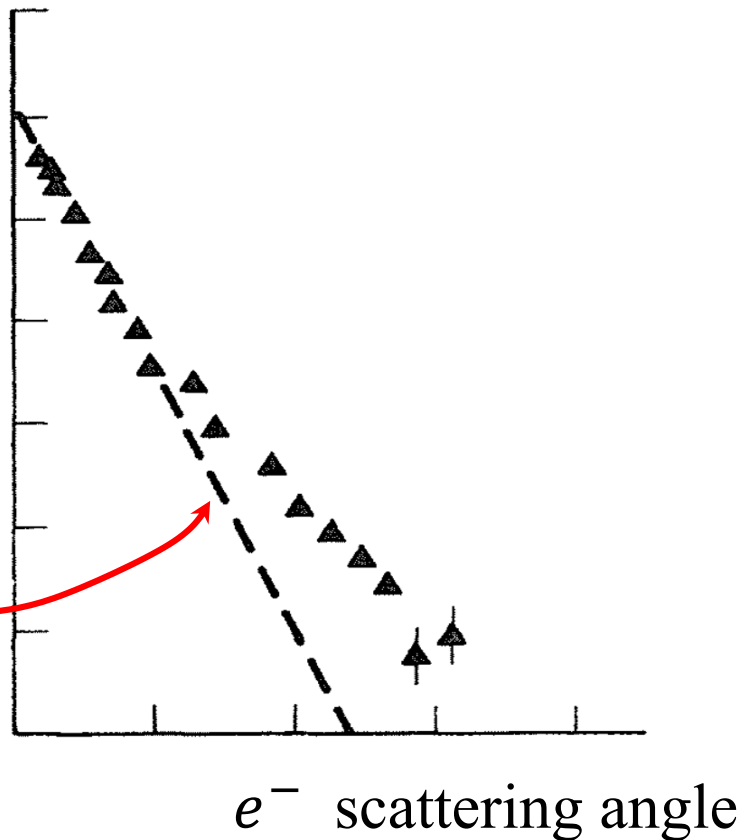
# Deep inelastic scattering

Rutherford scattering of electron on proton



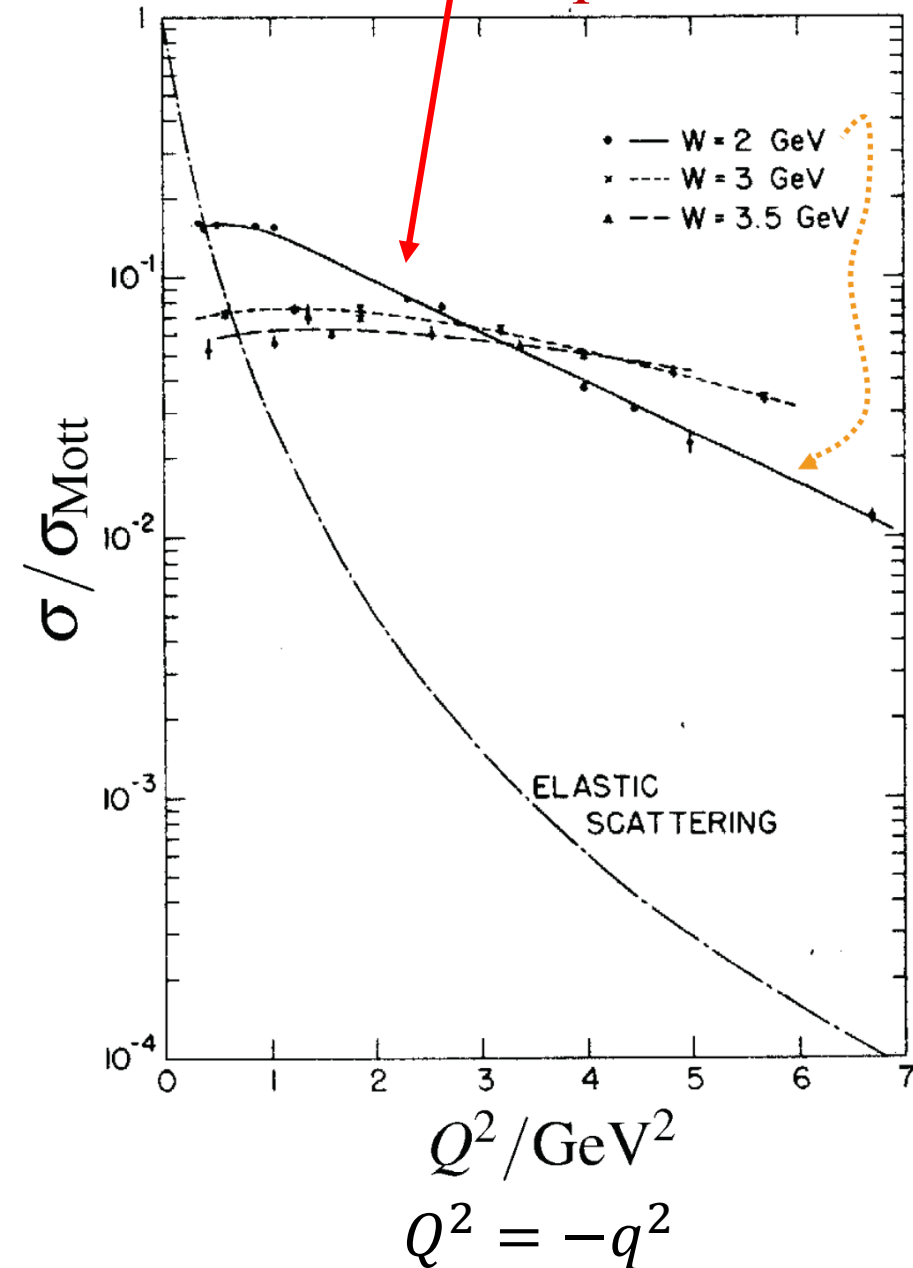
Counts

Without  
internal  
structure



$$e^- p \rightarrow e^- X$$

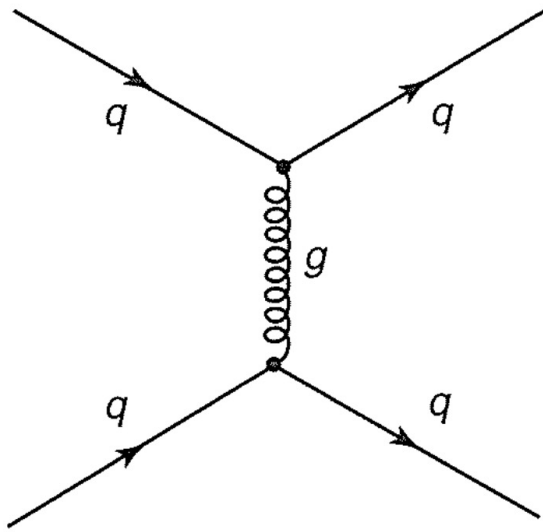
Scatter on point-like particles:  
consistent with quark model



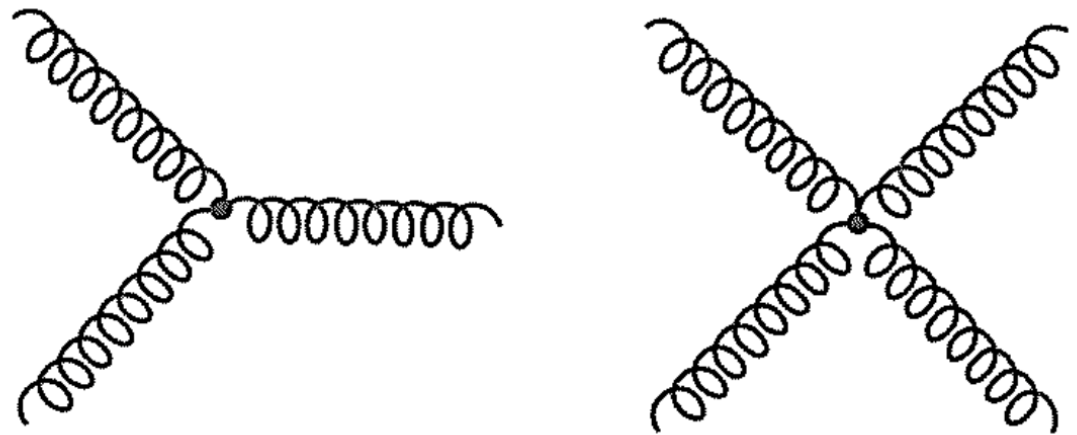
# Quantum Chromodynamics

- QCD: theory for strong interaction between colored objects. More fundamental than  $\pi$ -exchange between nucleons

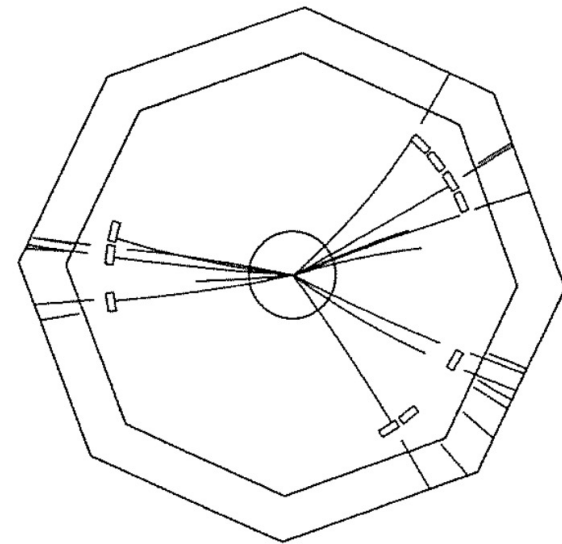
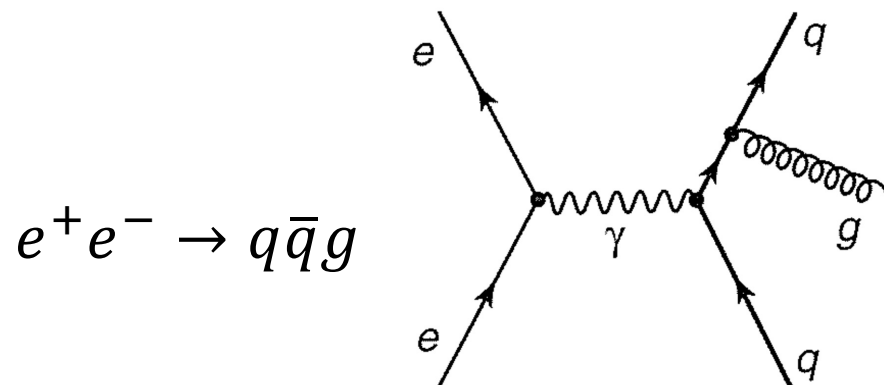
Strong interaction between quarks mediated by gluons



Direct self-interaction between gluons



- Experimental signals of gluons: three-jet events



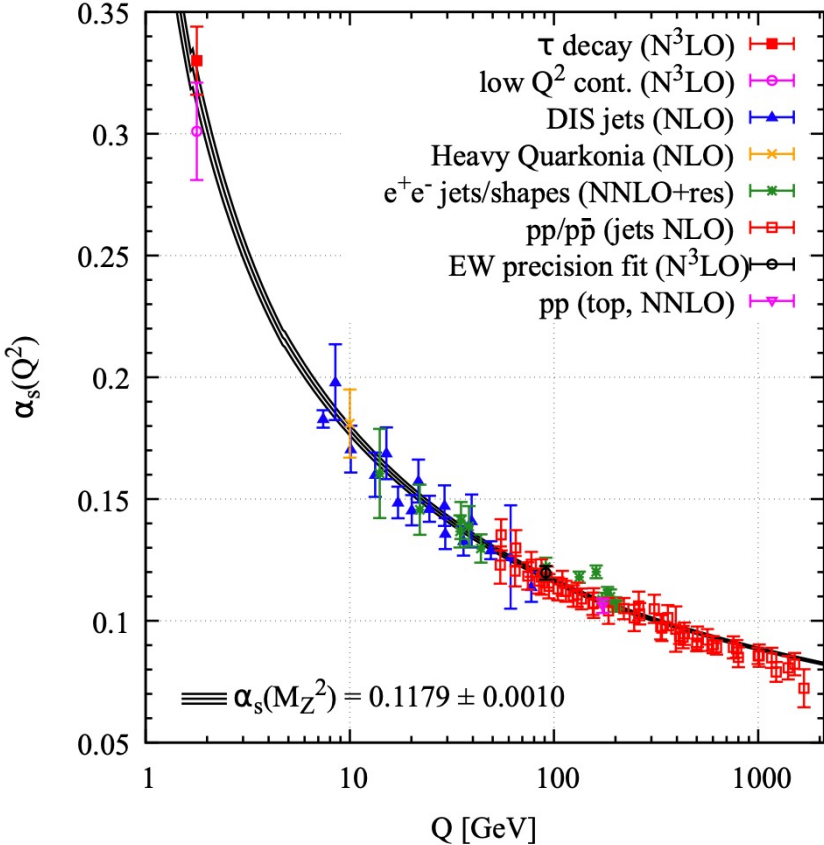
# Confinement

- Energy dependent coupling strength

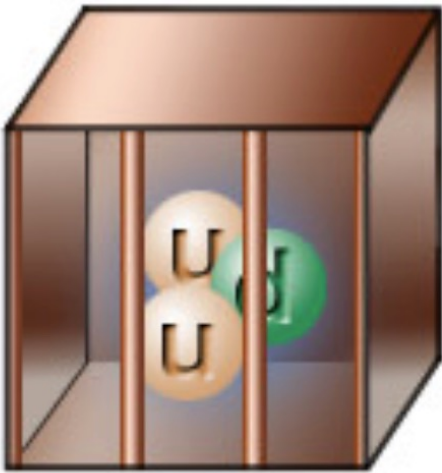
$$\alpha_s(Q^2) \approx \frac{1}{\beta_0 \ln(Q^2/\Lambda^2)}$$

$$Q^2 \rightarrow \Lambda^2, \alpha_s \rightarrow \infty$$

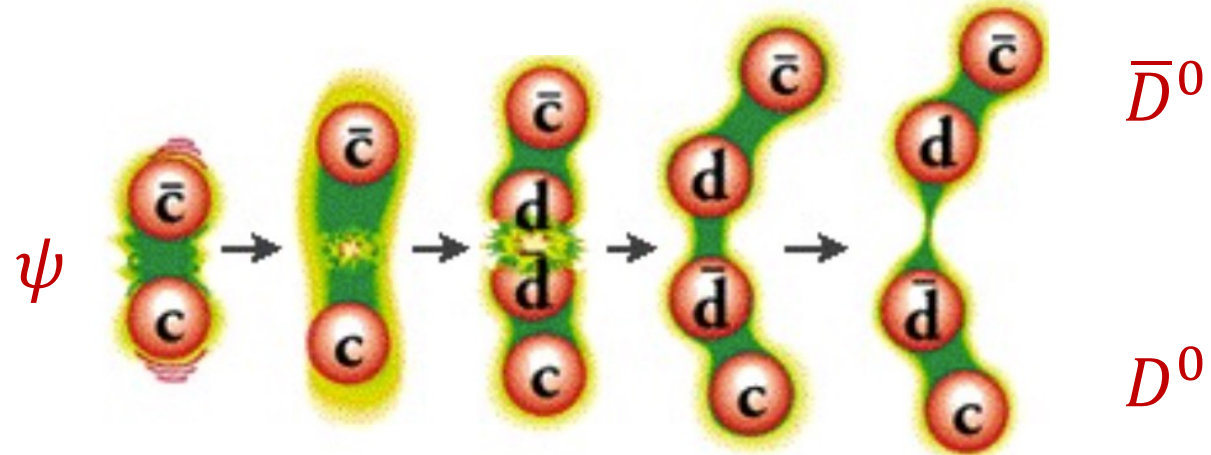
- Non perturbative in expansions of  $\alpha_s$  at low- $Q^2$
- Color confinement, no free quarks/gluons



Quarks and gluons contained in colorless hadrons



What happens if one tries to separate two quarks?





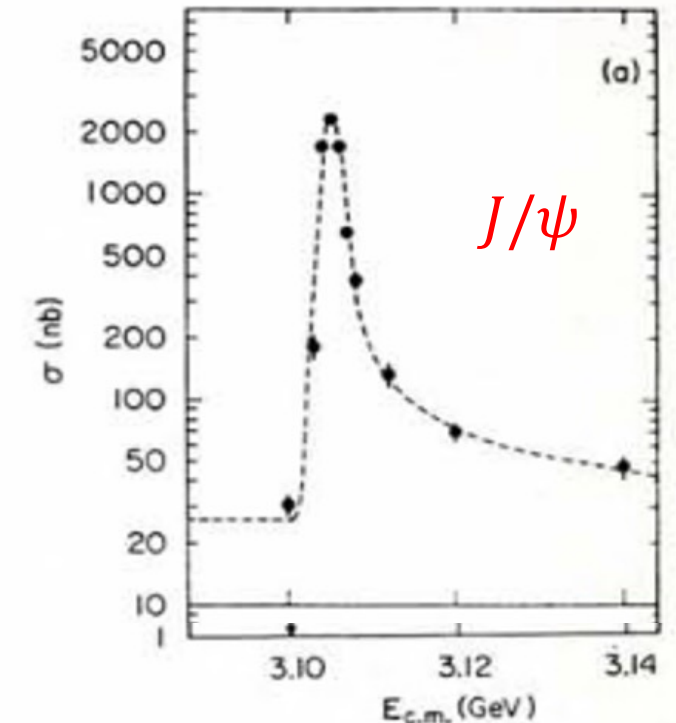
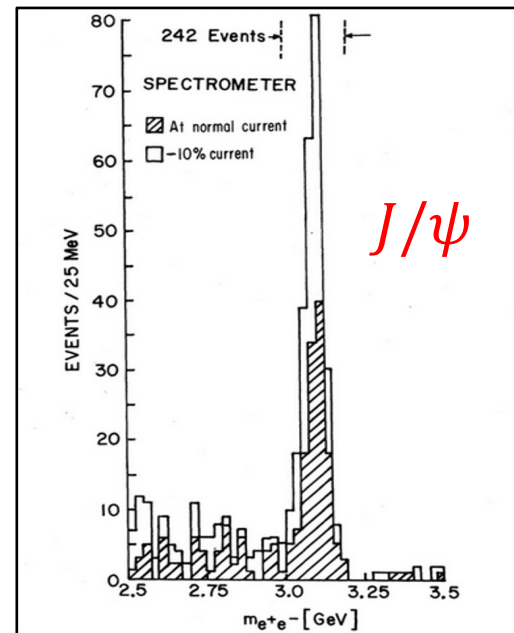
# Extensions of quark flavors

- Discovery of  $J/\psi$  in 1974, indication of a new quark flavor (**charm quark,  $c$** )

Narrow width given being much heavier than known mesons

$$m_{J/\psi} \sim 3100 \text{ MeV}, \Gamma_{J/\psi} \sim 0.1 \text{ MeV}$$

Formed by a new type of quark

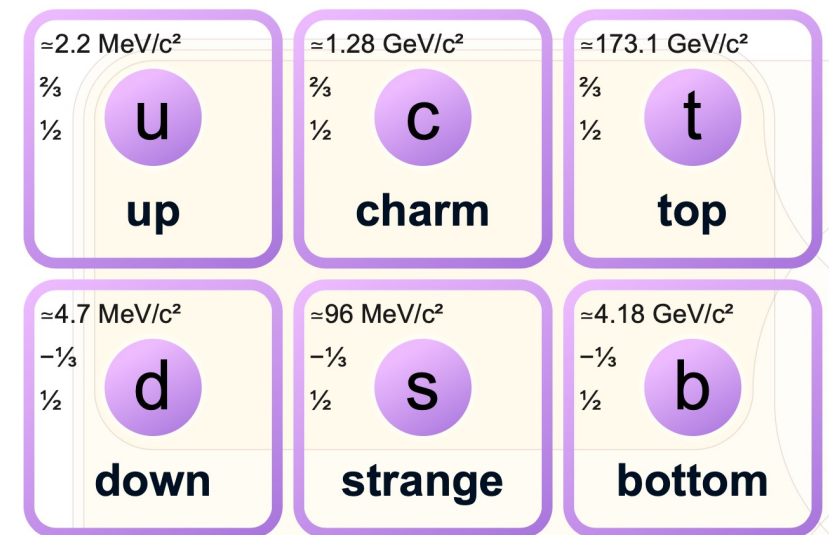


- Discovery of  $\Upsilon$  in 1977, indication of another new flavor (**bottom quark,  $b$** )

$$m_{\Upsilon} \sim 9500 \text{ MeV}, \Gamma_{\Upsilon} \sim 0.1 \text{ MeV}$$

- Top quark ( $t$ ) discovered in 1995, lifetime  $\tau \sim 10^{-25} \text{ s}$ , smaller than needed to form hadrons ( $\tau \sim 10^{-22} \text{ s}$ )

Six quark flavors observed in total



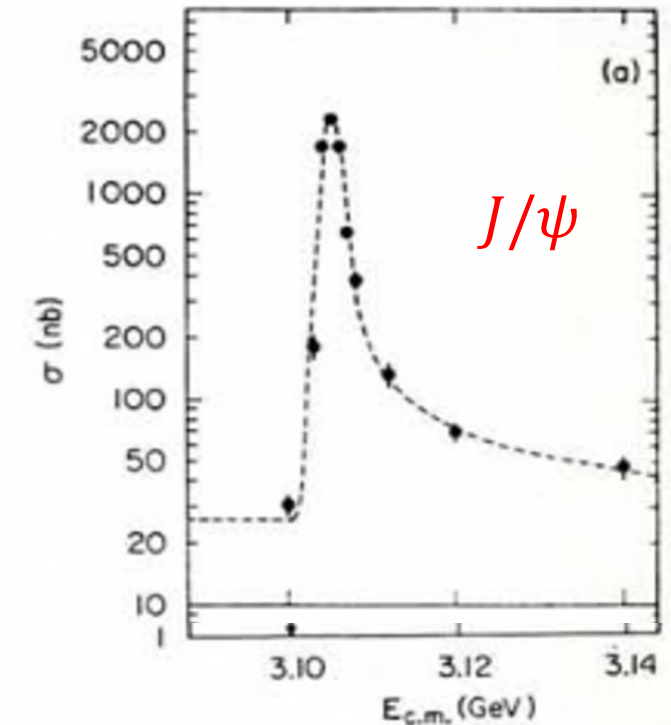
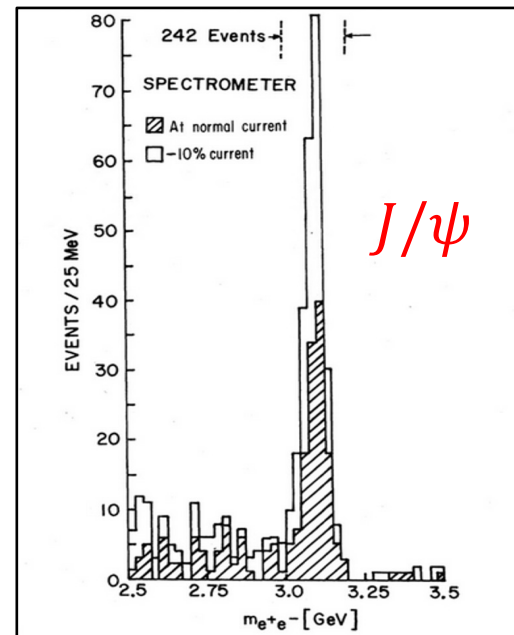
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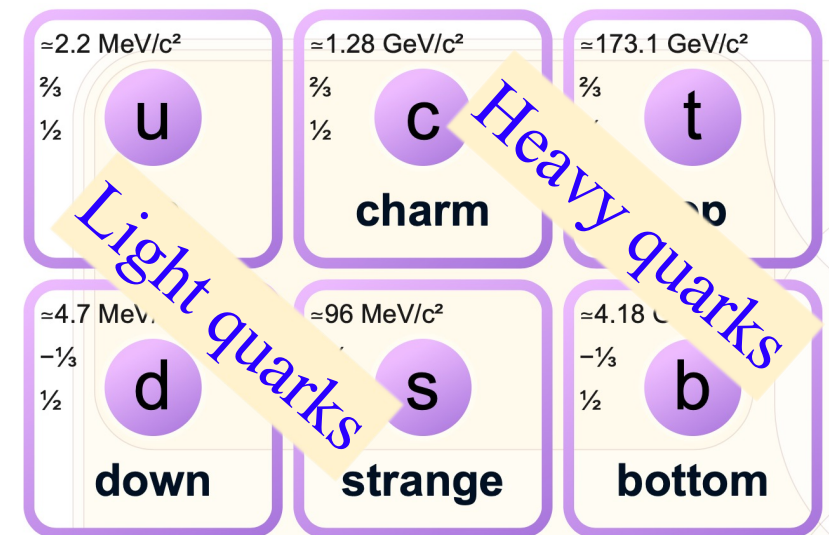


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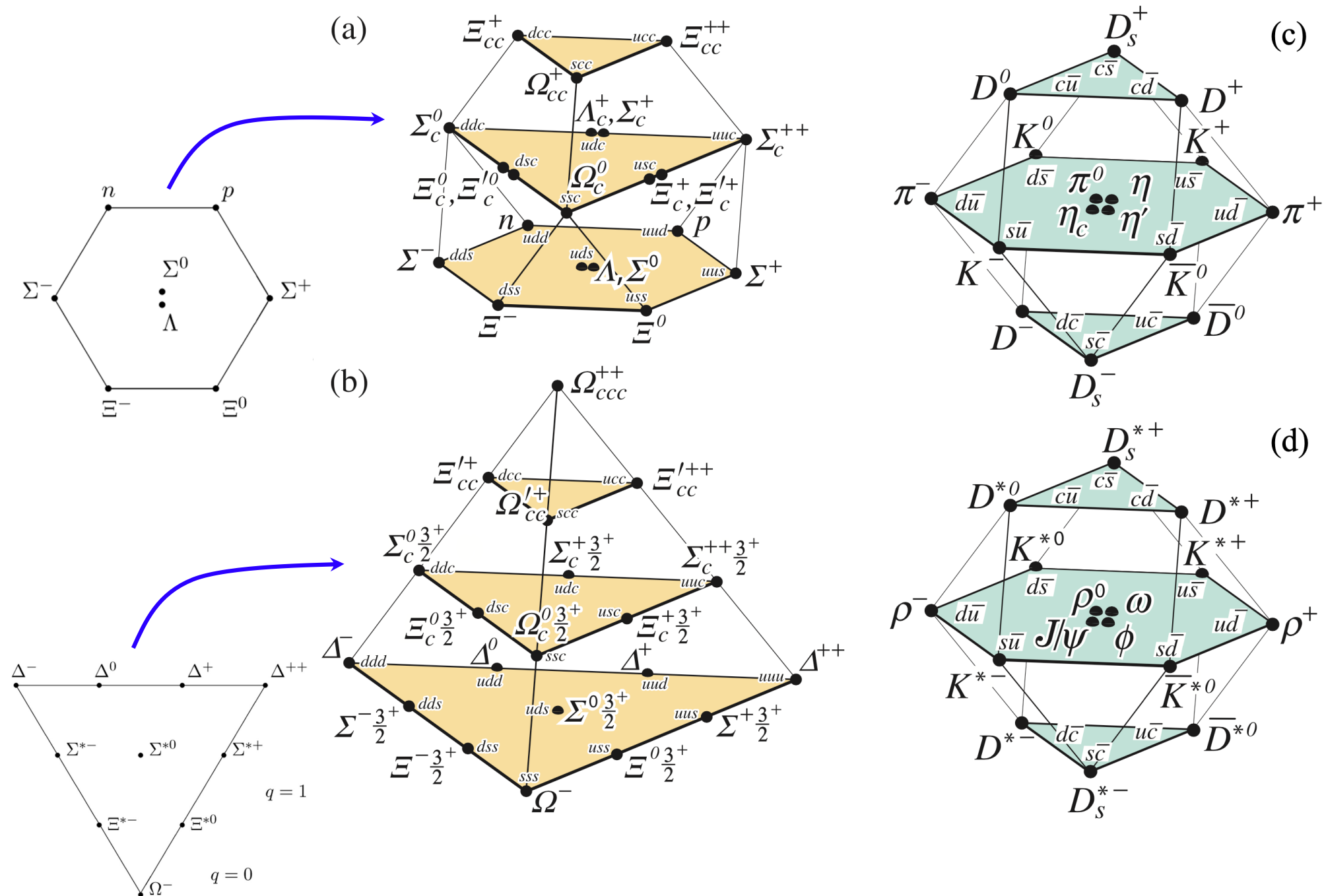


# Hadron spectroscopy

- Flavor multiplets with  $u, d, s, c$  quarks

## Baryons

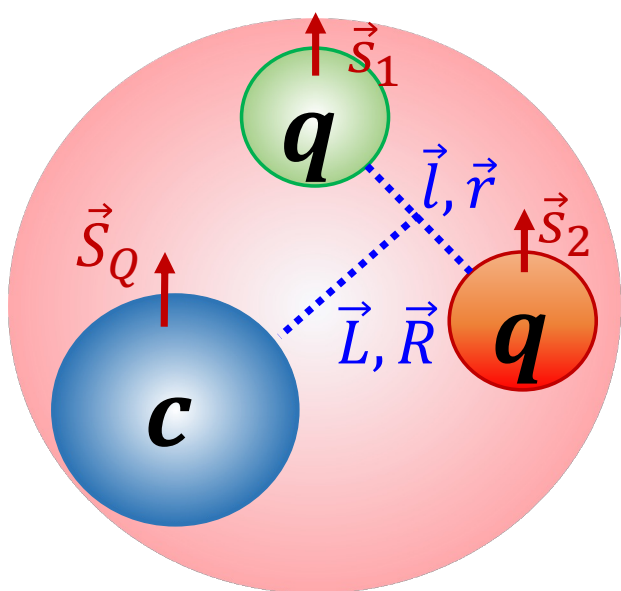
## Mesons





# Excitation spectrum (energy levels of the same flavors)

## Baryon as example



$\vec{s}_1, \vec{s}_2, \vec{s}_Q$ : spin of quarks

$\vec{l}, \vec{L}$ : orbital angular momentum

$\vec{s} = \vec{s}_1 + \vec{s}_2 + \vec{l}$ : spin of light quark system

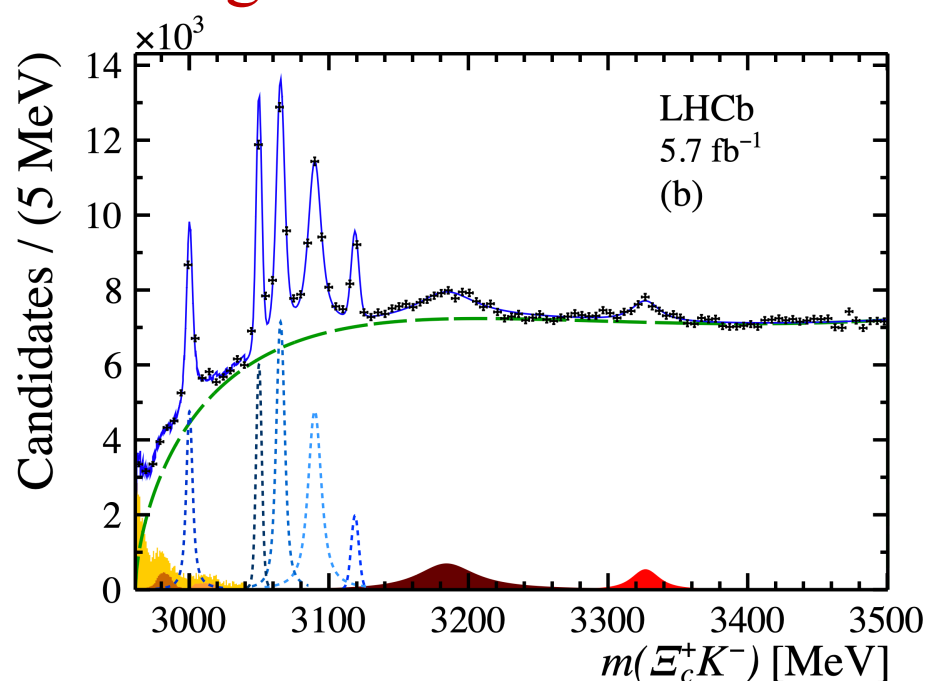
$\vec{j} = \vec{s} + \vec{L}$ : total angular momentum of light system

$\vec{J} = \vec{j} + \vec{s}_Q$ : total angular momentum of hadron

$\vec{r}, \vec{R}$ : radial excitations

Discovery of 7 narrow  $\Omega_c^0(css)$  states in  $\Xi_c^+ K^-$  invariant mass spectrum (2023)

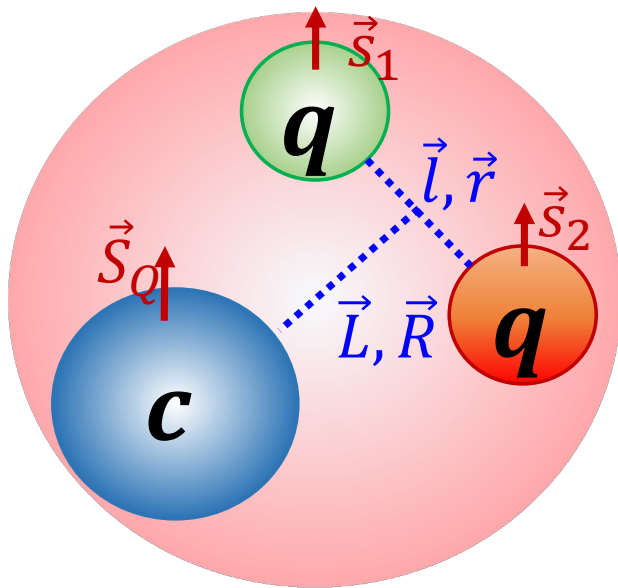
Matching to excitation modes difficult, under ongoing study



Resonance	$m$ (MeV)	$\Gamma$ (MeV)
$\Omega_c(3000)^0$	$3000.44 \pm 0.07$	$3.83 \pm 0.23$
$\Omega_c(3050)^0$	$3050.18 \pm 0.04$	$0.67 \pm 0.17$
$\Omega_c(3065)^0$	$3065.63 \pm 0.06$	$3.79 \pm 0.20$
$\Omega_c(3090)^0$	$3090.16 \pm 0.11$	$8.48 \pm 0.44$
$\Omega_c(3119)^0$	$3118.98 \pm 0.12$	$0.60 \pm 0.63$
$\Omega_c(3185)^0$	$3185.1 \pm 1.7$	$50 \pm 7$
$\Omega_c(3327)^0$	$3327.1 \pm 1.2$	$20 \pm 5$

# Excitation spectrum

## Baryon as example



$\vec{s}_1, \vec{s}_2, \vec{s}_Q$ : spin of quarks

$\vec{l}, \vec{L}$ : orbital angular momentum

$\vec{s} = \vec{s}_1 + \vec{s}_2 + \vec{l}$ : spin of light quark system

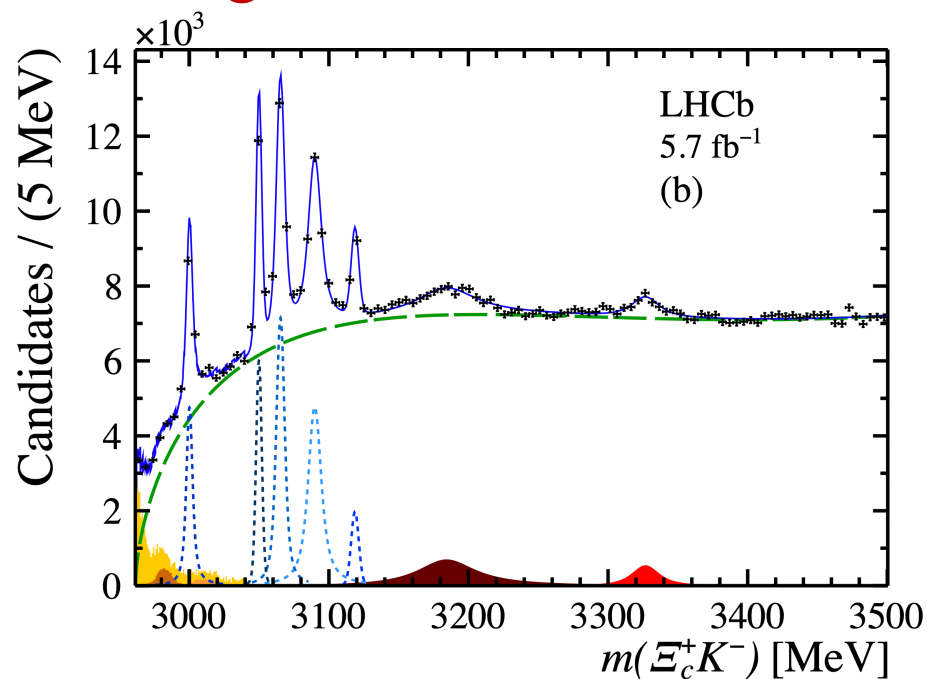
$\vec{j} = \vec{s} + \vec{L}$ : total angular momentum of light system

$\vec{J} = \vec{j} + \vec{s}_Q$ : total angular momentum of hadron

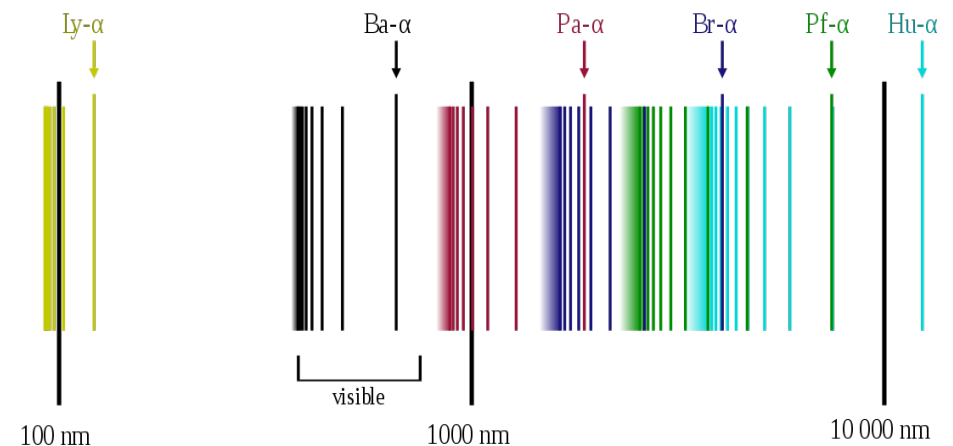
$\vec{r}, \vec{R}$ : radial excitations

Discovery of 7 narrow  $\Omega_c^0(css)$  states in  $\Xi_c^+ K^-$  invariant mass spectrum

Matching to excitation modes difficult, under ongoing study



Similarity to light spectrum!



# How to study new hadrons 1

- Most hadrons with short lifetimes,  $\tau = \text{ps, fs} \dots 10^{-22} \text{ s}$
- **First, produce them at particle colliders, with a large enough amount**

A few active large facilities in the world

Large Hadron Collider @ CERN



$pp$  collisions  
 $\sqrt{s} \sim 10 \text{ TeV}$

$\int \mathcal{L} dt \sim 10 \text{ fb}^{-1}$  (LHCb)

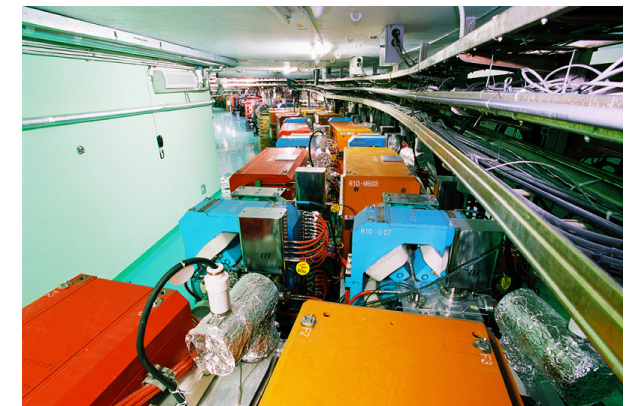
SuperKEK @ Japan



$e^+e^-$  collisions  
 $\sqrt{s} \sim 10 \text{ GeV}$

$\int \mathcal{L} dt \sim 50 \text{ ab}^{-1}$

BESIII @ China



$e^+e^-$  collisions  
 $\sqrt{s} \sim 4 \text{ GeV}$

$\int \mathcal{L} dt \sim 50 \text{ fb}^{-1}$

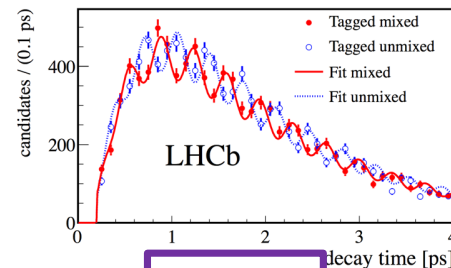
# How to study new hadrons 2

- **Second**, detect their decays into “stable” particles (those leave trajectories or produce particle showers)

eg: LHCb at LHC, dedicated for measurements of charm and bottom hadrons

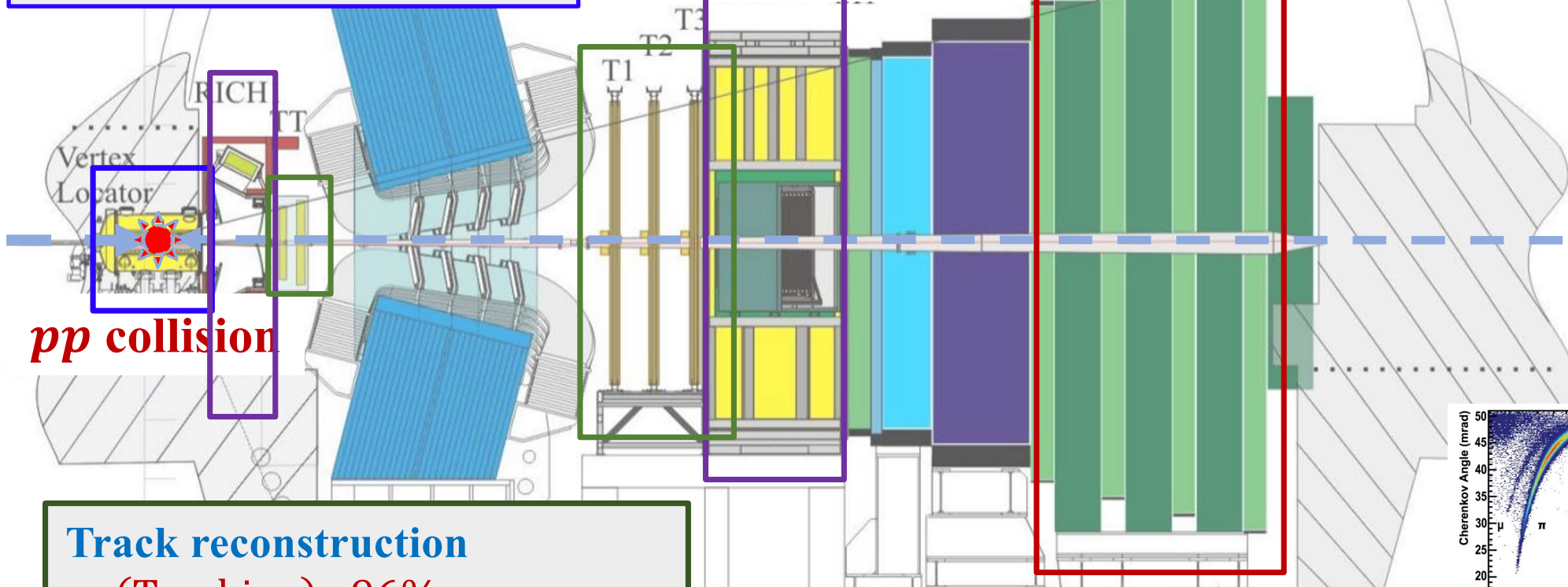
## Vertex reconstruction

- $\sigma_{IP} \sim 20 \mu\text{m}$
- $\sigma_{\tau} \sim 45 \text{ fs}$  w.r.t.  $\tau_B \approx 1.5 \text{ ps}$



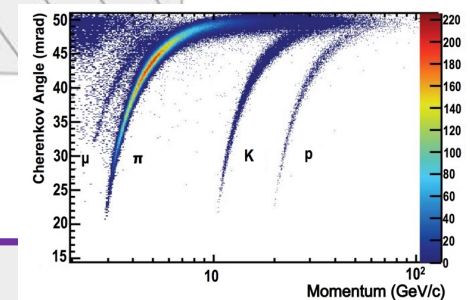
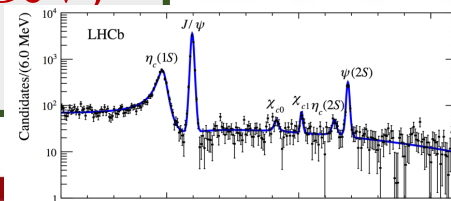
## Muon identification

- $\epsilon(\mu \rightarrow \mu) \sim 97\%$
- MisID rate ( $\pi \rightarrow \mu$ )  $\sim 1 - 3\%$



## Track reconstruction

- $\epsilon(\text{Tracking}) \sim 96\%$
- $\delta p/p \sim 0.5\% - 1\%$  (5-200 GeV)
- $\epsilon(m_{J/\psi}) \approx 15 \text{ MeV}$



## Hadron identification

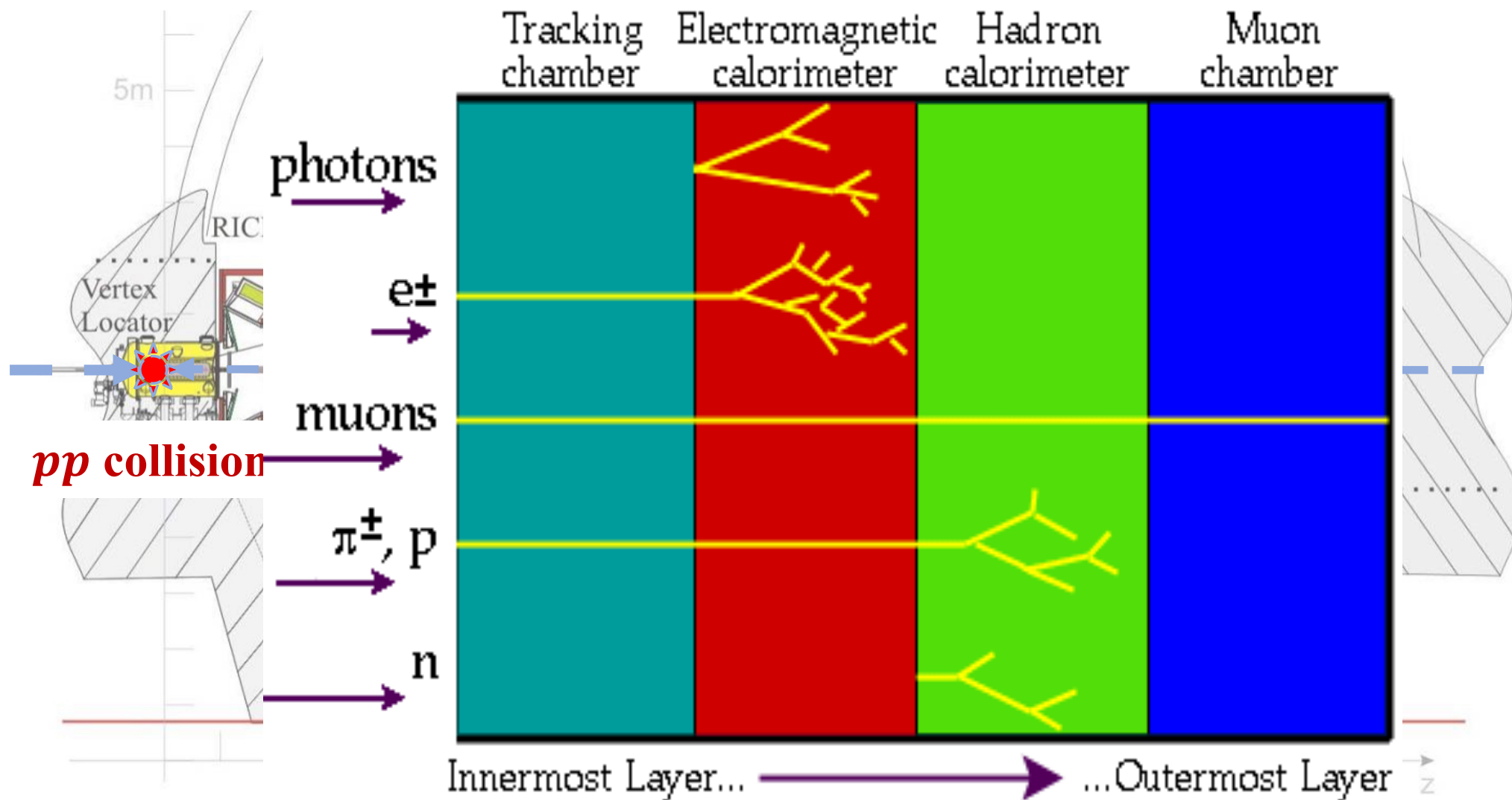
- $\epsilon(K \rightarrow K), \epsilon(p \rightarrow p) > 90\%$
- MisID rate ( $\pi \rightarrow K/p$ )  $< 5\%$



# How to study new hadrons 2

- **Second**, detect their decays into “stable” particles (those leave trajectories or produce particle showers)

eg: LHCb at LHC, dedicated for measurements of charm and bottom hadrons



# How to study new hadrons 3

- **Third**, form experimental quantities to extract signal and measure properties

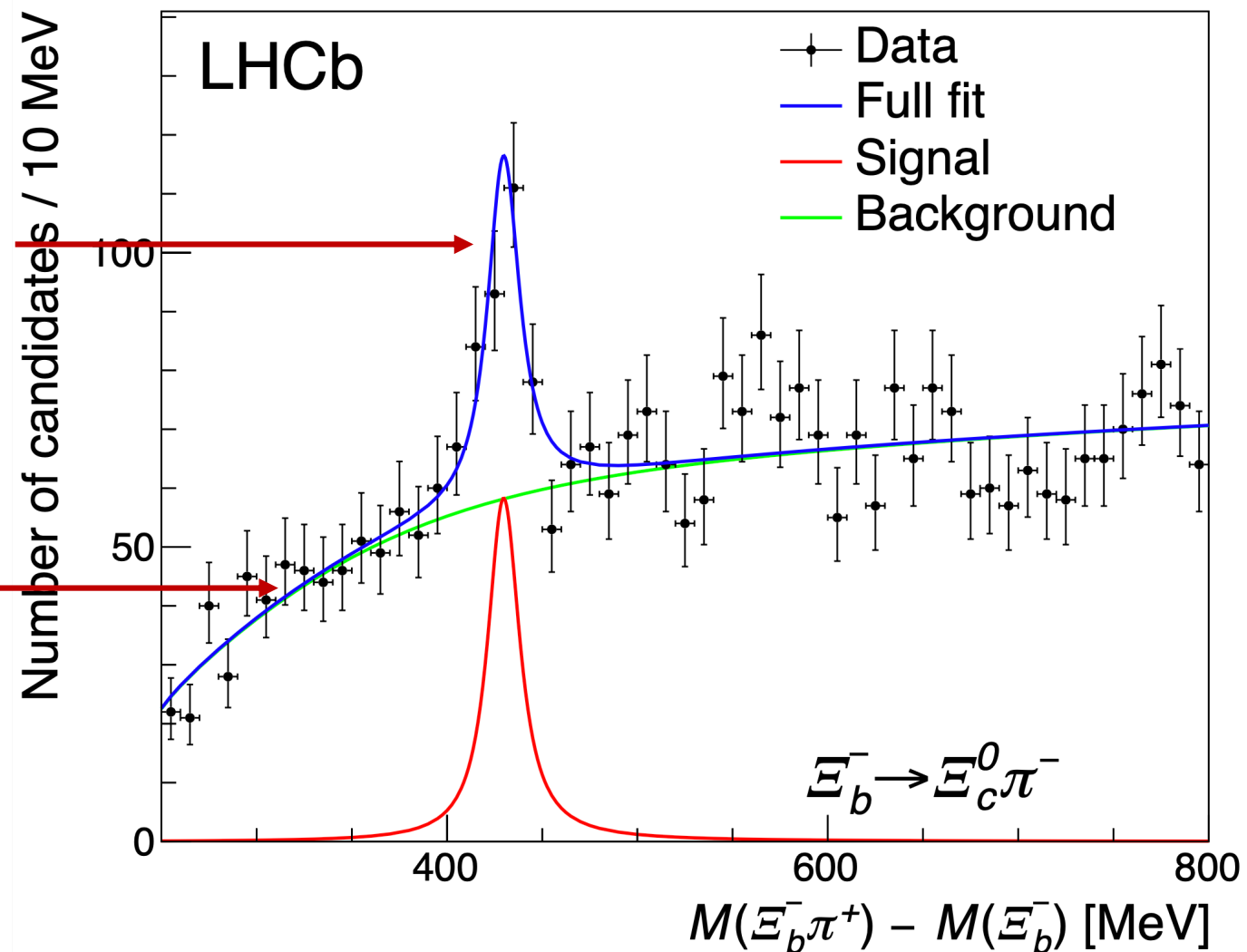
Usually invariant mass

$$X \rightarrow a + b \quad m_{X'} = \sqrt{(E_a + E_b)^2 - (\vec{p}_a + \vec{p}_b)^2}$$

Natural width  $\otimes$  resolution

Resonance

Background



Important: keep low background and high mass resolution!

# Experimental studies of “exotic” hadrons

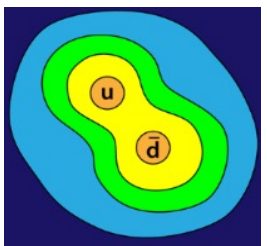
- No experimental evidence of hadrons with more than three quarks →

## Exotic hadrons

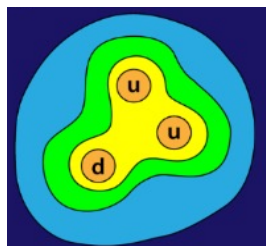
anti-triplet as anti-quarks  $\bar{q}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqqq\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(qq\bar{q}\bar{q})$ , etc. It is assuming that the lowest

Conventional:  $q\bar{q}$ ,  $qqq$

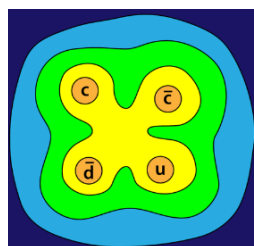
Exotic hadrons:  $qq\bar{q}\bar{q}$ ,  $qqqq\bar{q}$ , gluons...



$q\bar{q}$



$qqq$



$qq\bar{q}\bar{q}$

Tetraquark

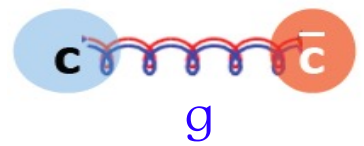


$qqqq\bar{q}$

Pentaquark



$g$

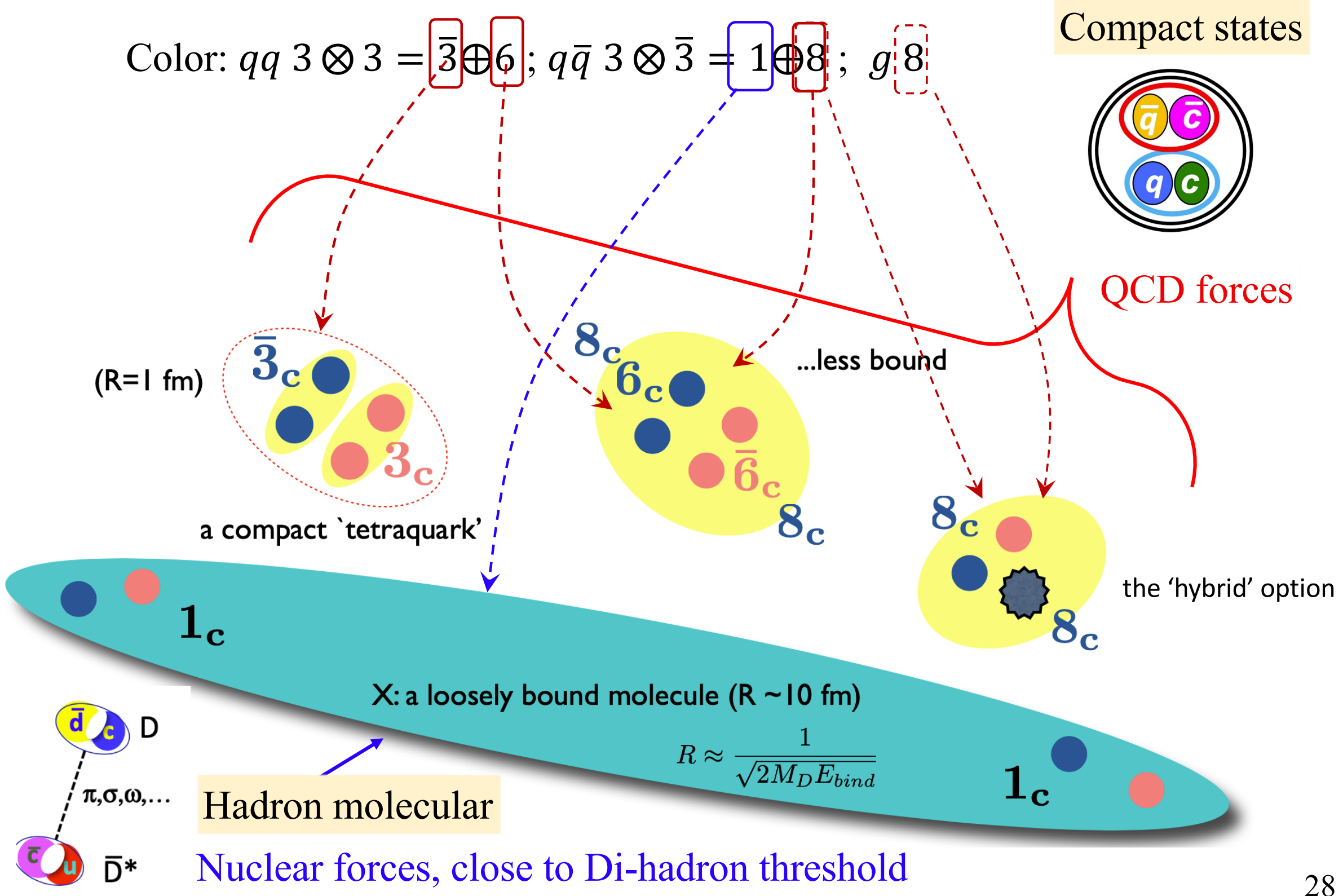


$g$

Unique color configuration

Exotics: more possibilities to form color singlet

Baryons:  $RGB$   
 Mesons:  $R\bar{R} + G\bar{G} + B\bar{B}$

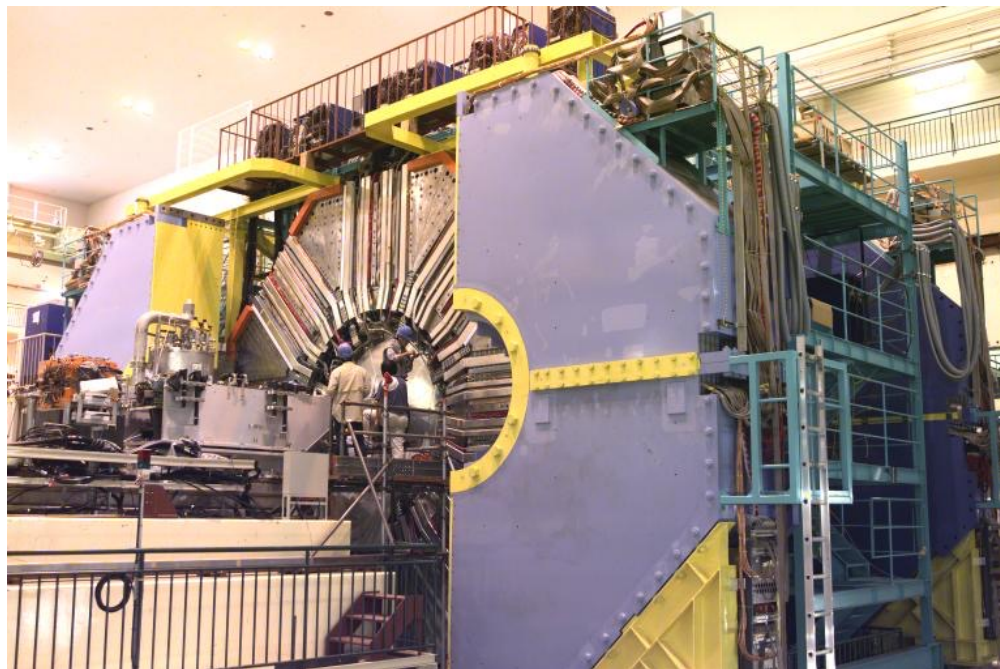


# First evidence of exotic

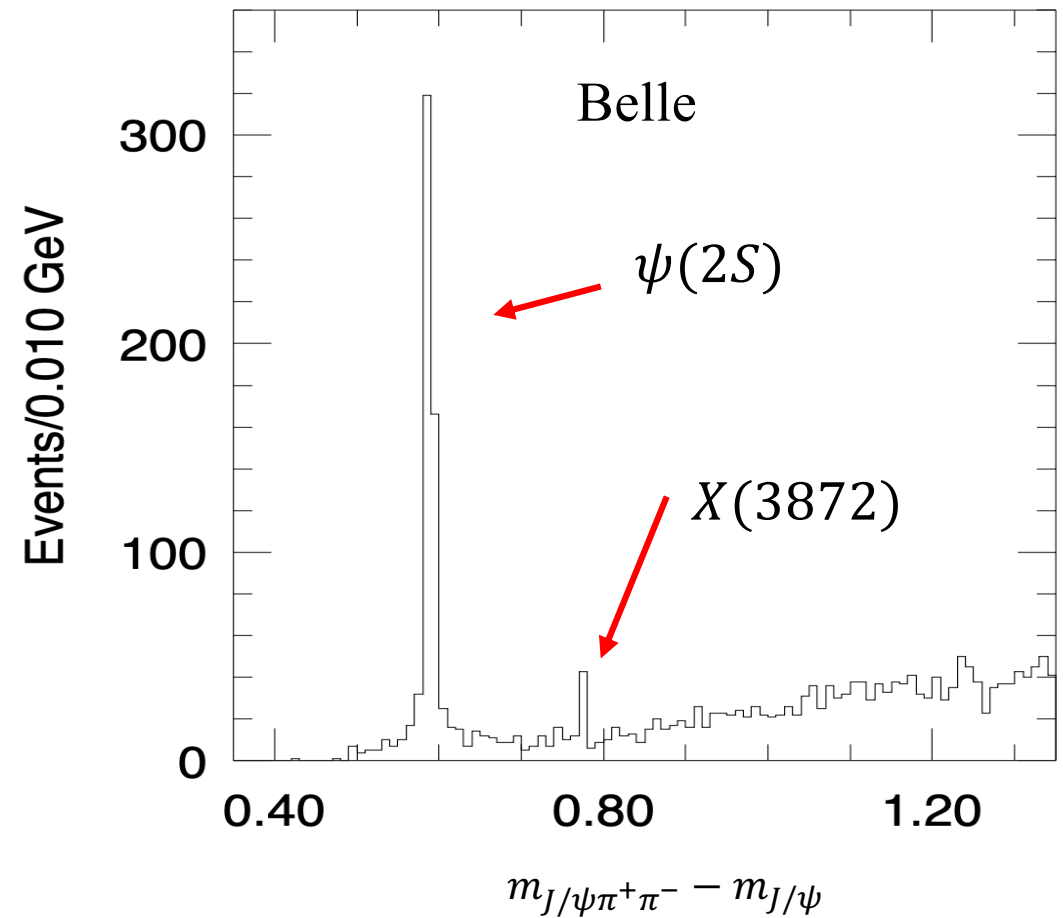
$X(3872)$  discovered at KEK in 2003

$$X(3872) \rightarrow J/\psi \pi^+ \pi^-$$

- Narrow width
- Close to  $D^{*0}D^0$  threshold
- Isospin breaking decay ...



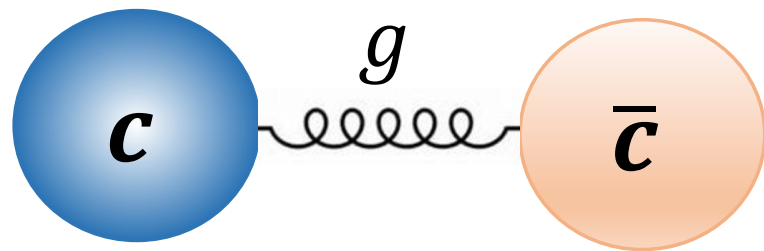
PRL91(2003)262001



# X(3872) as an exotic

$X(3872) \rightarrow J/\psi \pi^+ \pi^-$ ,  $X(3872)$  contains the  $c\bar{c}$  component, like a charmonium

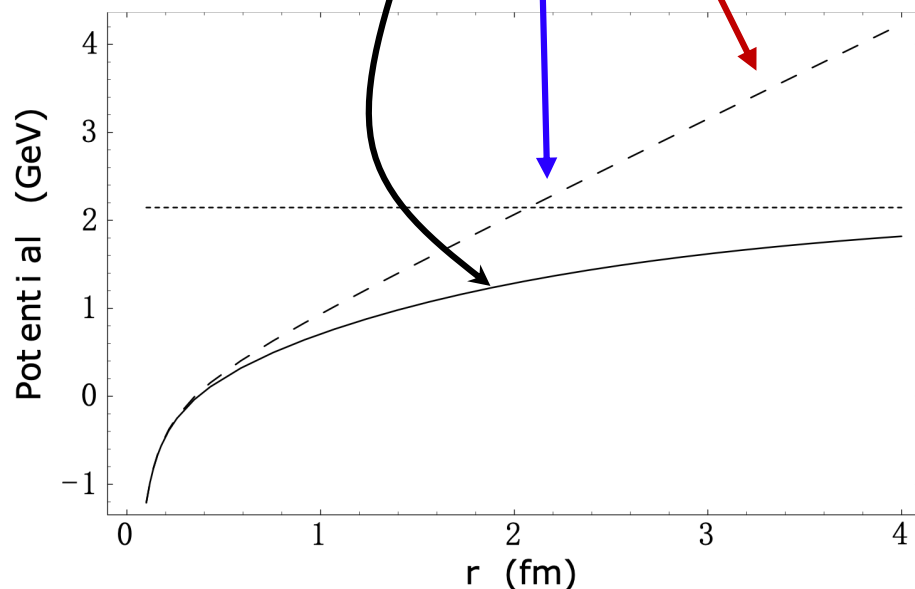
## Non-relativistic potential for $c\bar{c}$



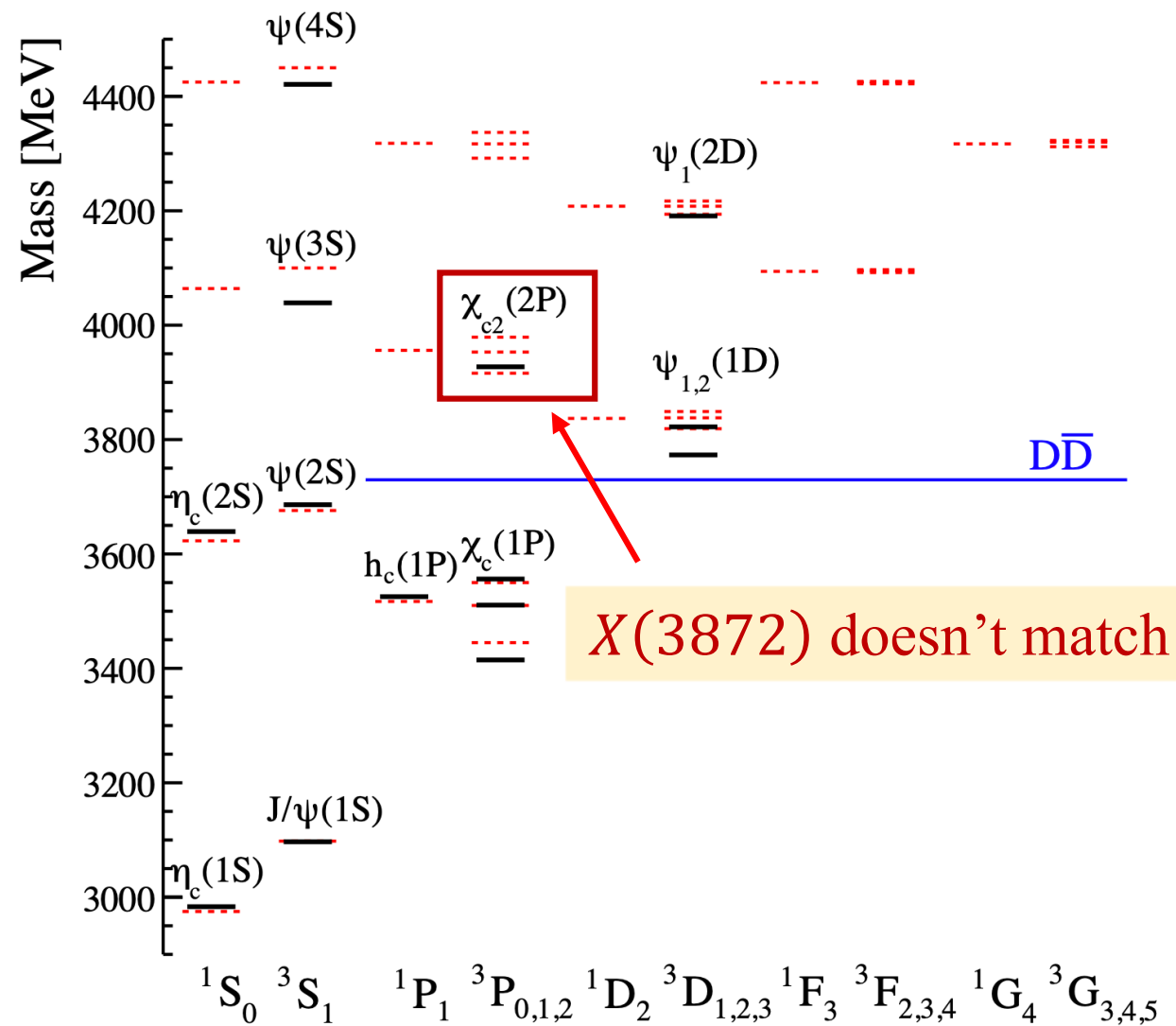
Coulomb

Confinement

$$V(r) = -\frac{4\alpha_s}{3r} + b \times r$$

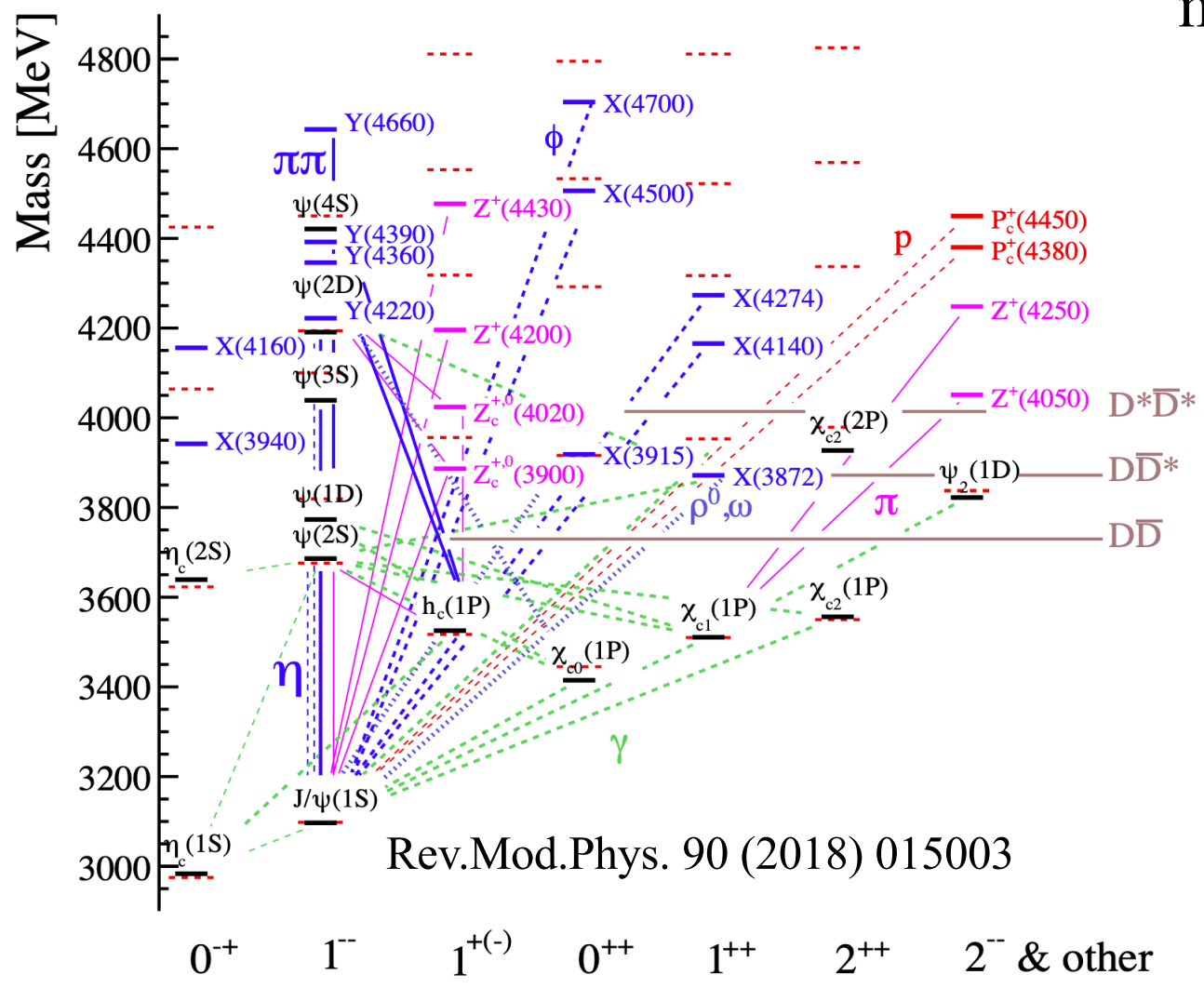


## Predicted spectrum v.s. experiment



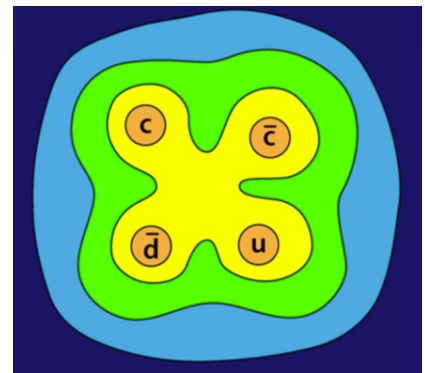
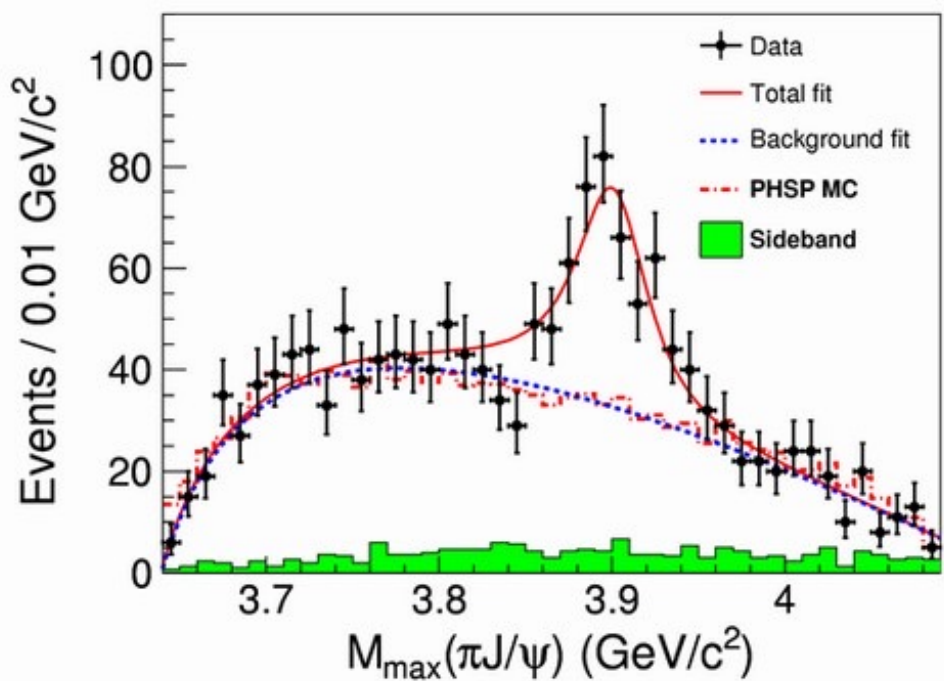
# More charmonium like exotics

## States with $c\bar{c}$ quark contents



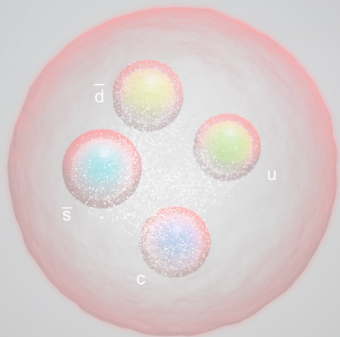
Charged  $Z_c(3900)^+$  by BESIII (2013) manifestly exotic,  $c\bar{c}u\bar{d}$

$$Z_c(3900)^+ \rightarrow J/\psi\pi^+$$

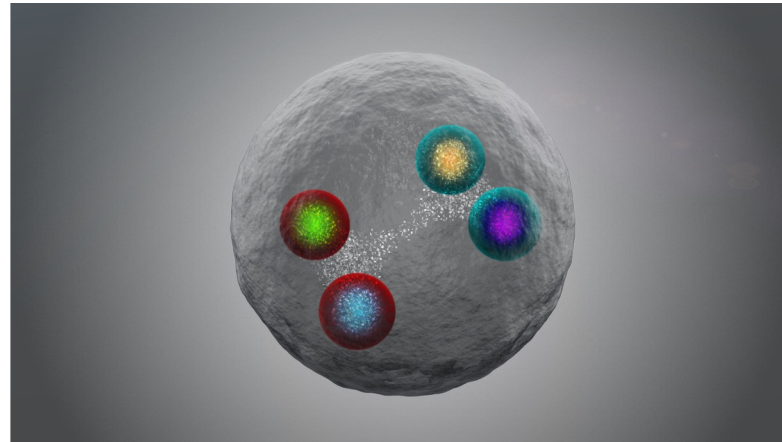


PRL 110 (2013) 252001

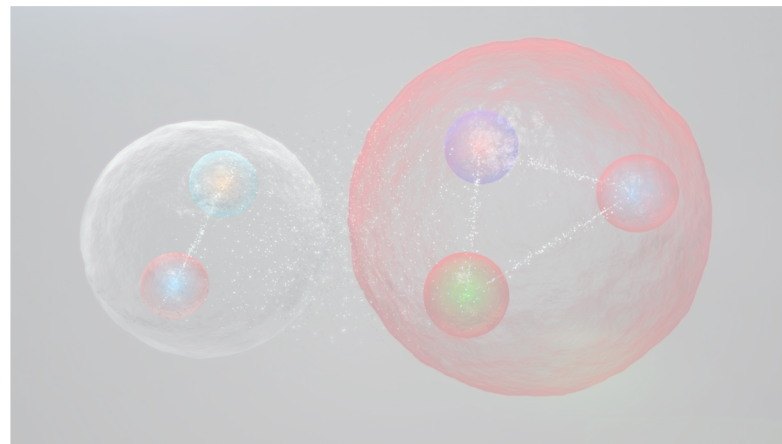
□ Single-charm tetraquark



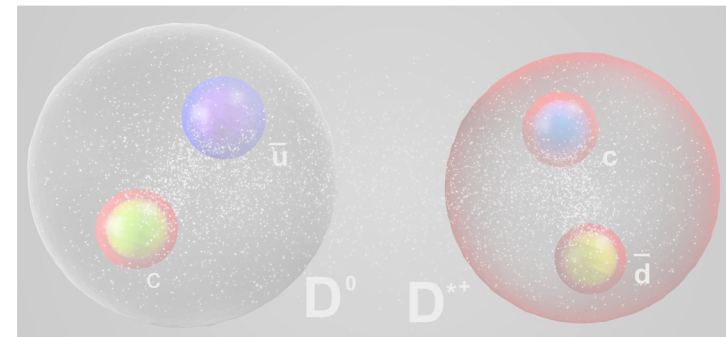
□ Hidden-charm tetraquark



□ Hidden-charm pentaquark



□ Double-charm tetraquark

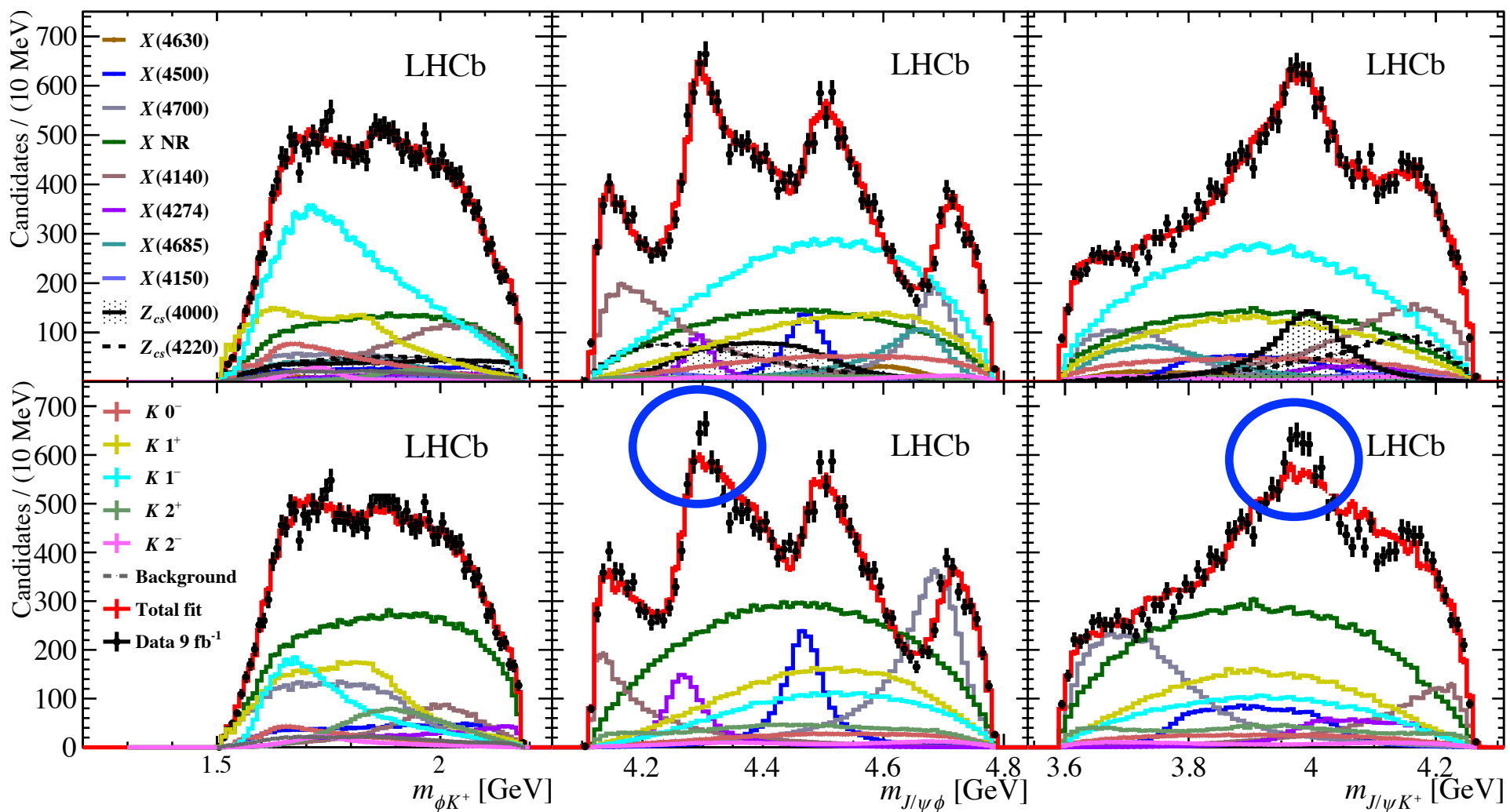




- Exotic discovered in  $B^+ \rightarrow J/\psi\phi K^+$  with amplitude analysis
  - Multiple  $X \rightarrow J/\psi\phi$  states,  $[c\bar{c}s\bar{s}]$  tetraquarks or charmonium
  - Two  $Z_{cs}^+ \rightarrow J/\psi K^+$  states:  $Z_{cs}(4000)^+$  and  $Z_{cs}(4200)^+$  with  $[c\bar{c}u\bar{s}]$ ,  $J^P = 1^+$

W/  $Z_{cs}^+$

W/o  $Z_{cs}^+$



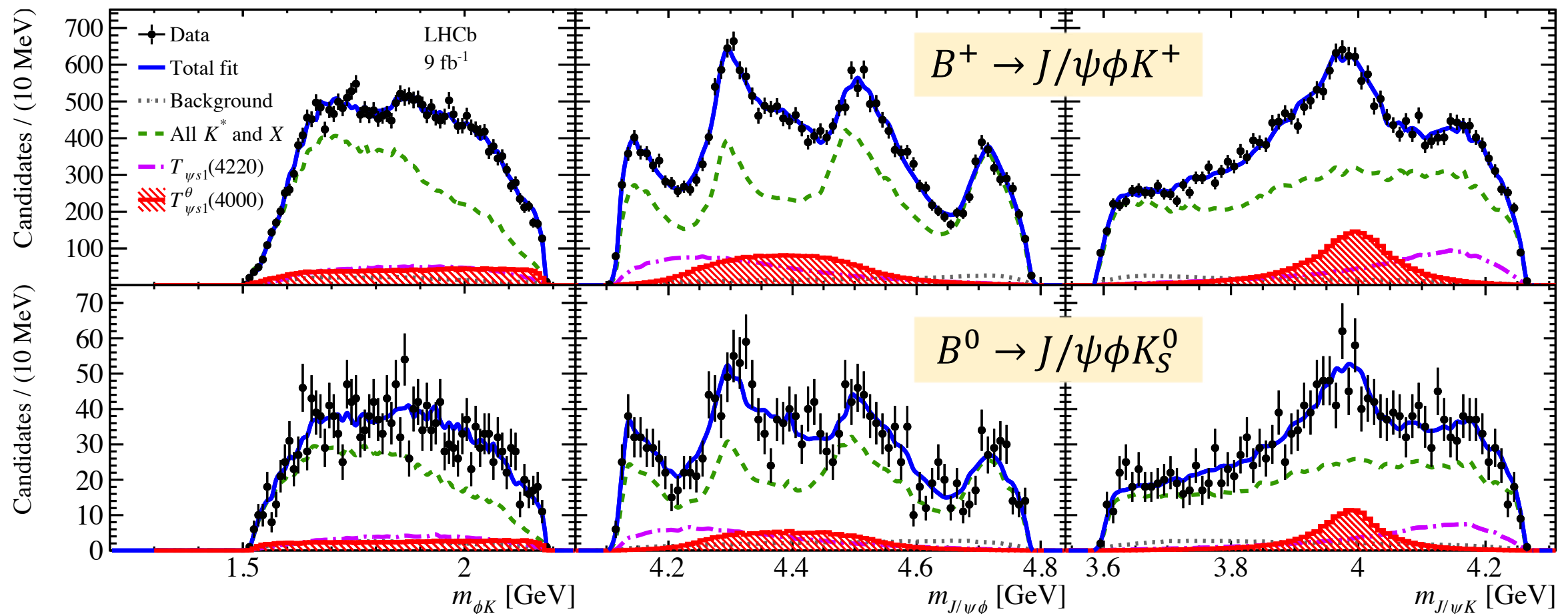
- Simultaneous amplitude analysis of  $B^+ \rightarrow J/\psi\phi K^+$  and  $B^0 \rightarrow J/\psi\phi K_S^0$  decays

Evidence of  $T_{\psi s_1}^\theta(4000)^0 [c\bar{c}d\bar{s}] \rightarrow J/\psi K_S^0$ , isospin partners of  $T_{\psi s_1}^\theta(4000)^+$

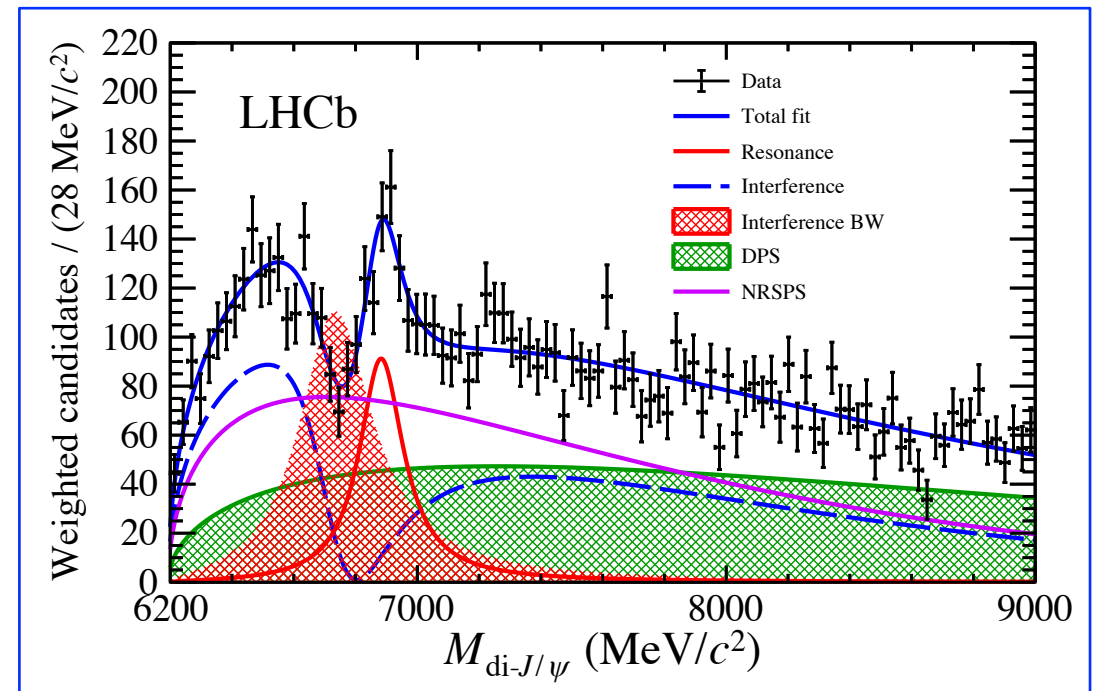
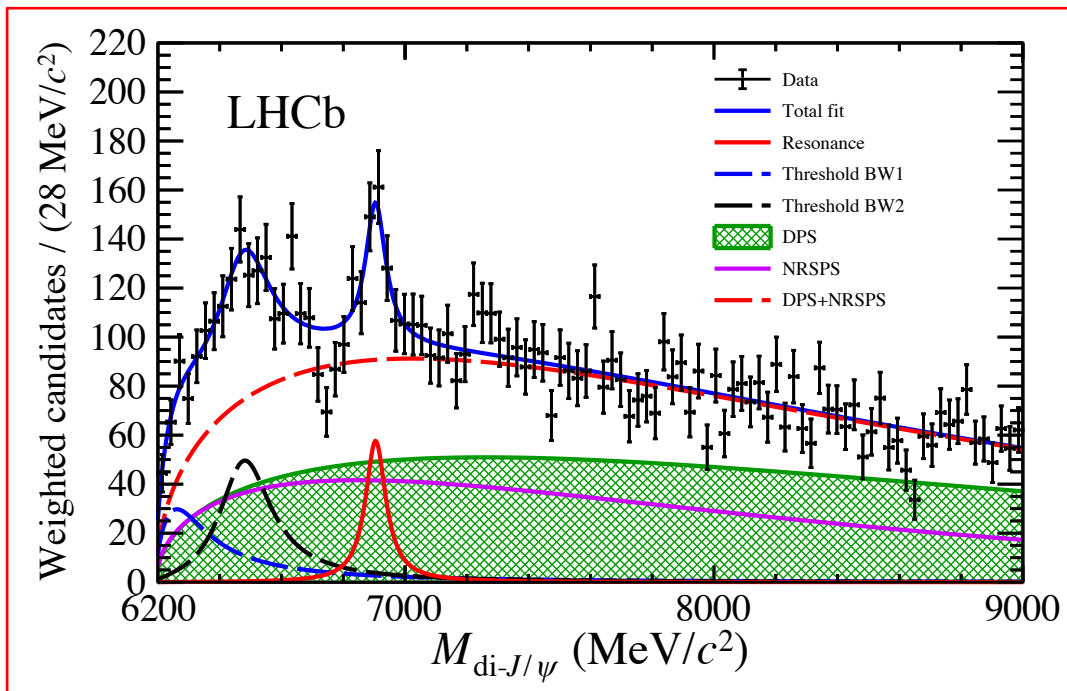
$$M(T_{\psi s_1}^\theta(4000)^0) = 3991^{+12}_{-10} + {}^{+9}_{-17} \text{ MeV}$$

$$\Gamma(T_{\psi s_1}^\theta(4000)^0) = 105^{+29}_{-25} + {}^{+17}_{-23} \text{ MeV}$$

$$\Delta M_{\text{isospin}} = -12^{+11}_{-10} + {}^{+6}_{-4} \text{ MeV}$$



- Structure in  $J/\psi$ - $J/\psi$  final state
  - $X(6900)$  consistent with fully charmed tetraquark  $T_{cc\bar{c}\bar{c}}$
  - Structure close to threshold:  $T_{cc\bar{c}\bar{c}}$  or feed-down decays
- Two alternative interpretation of data



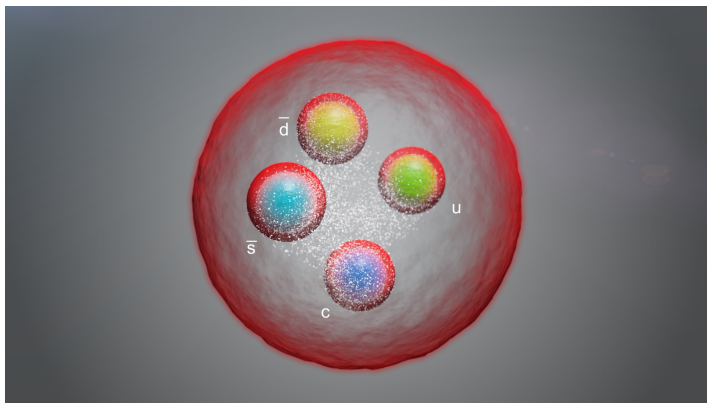
$$M(X(6900)) = 6905 \pm 11 \pm 7 \text{ MeV}/c^2$$

$$\Gamma(X(6900)) = 80 \pm 19 \pm 33 \text{ MeV}/c^2$$

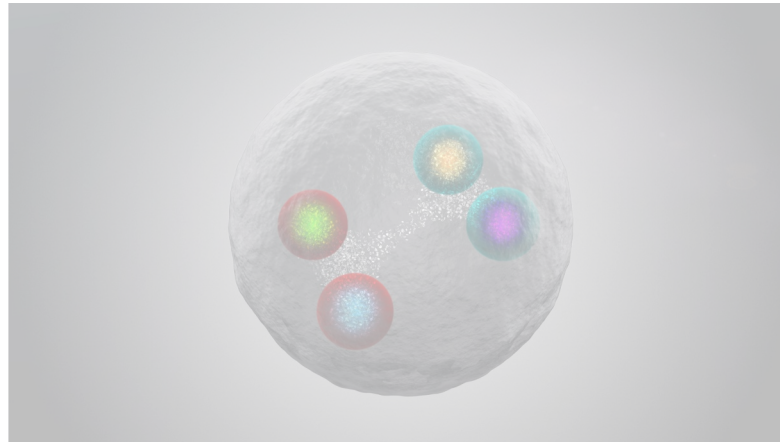
$$M(X(6900)) = 6886 \pm 11 \pm 11 \text{ MeV}/c^2$$

$$\Gamma(X(6900)) = 168 \pm 33 \pm 69 \text{ MeV}/c^2$$

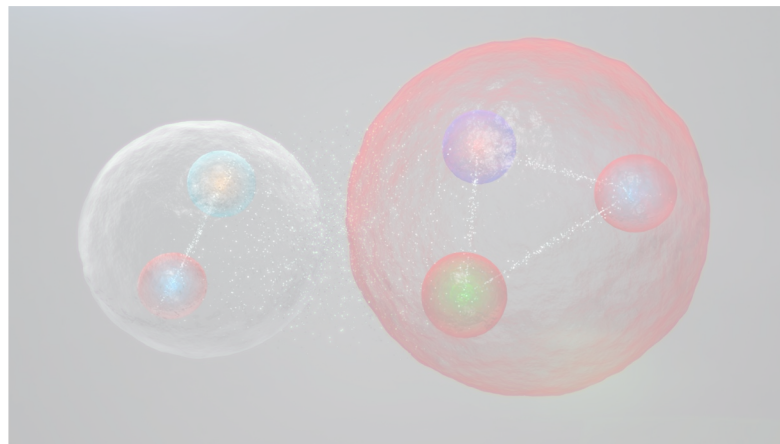
□ Single-charm tetraquark



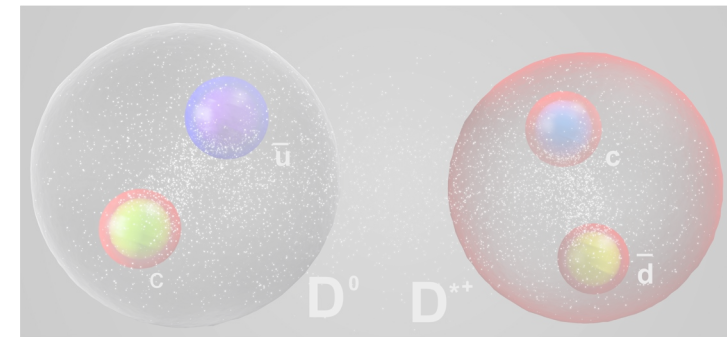
□ Hidden-charm tetraquark



□ Hidden-charm pentaquark

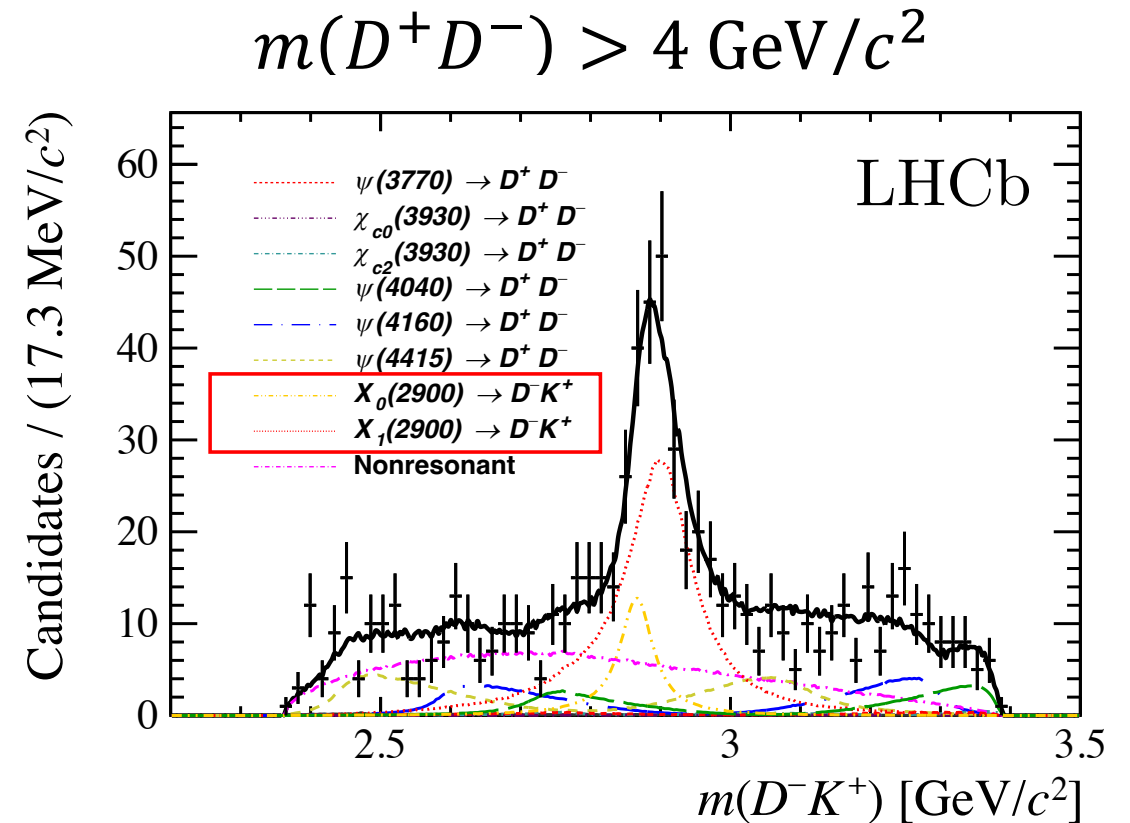
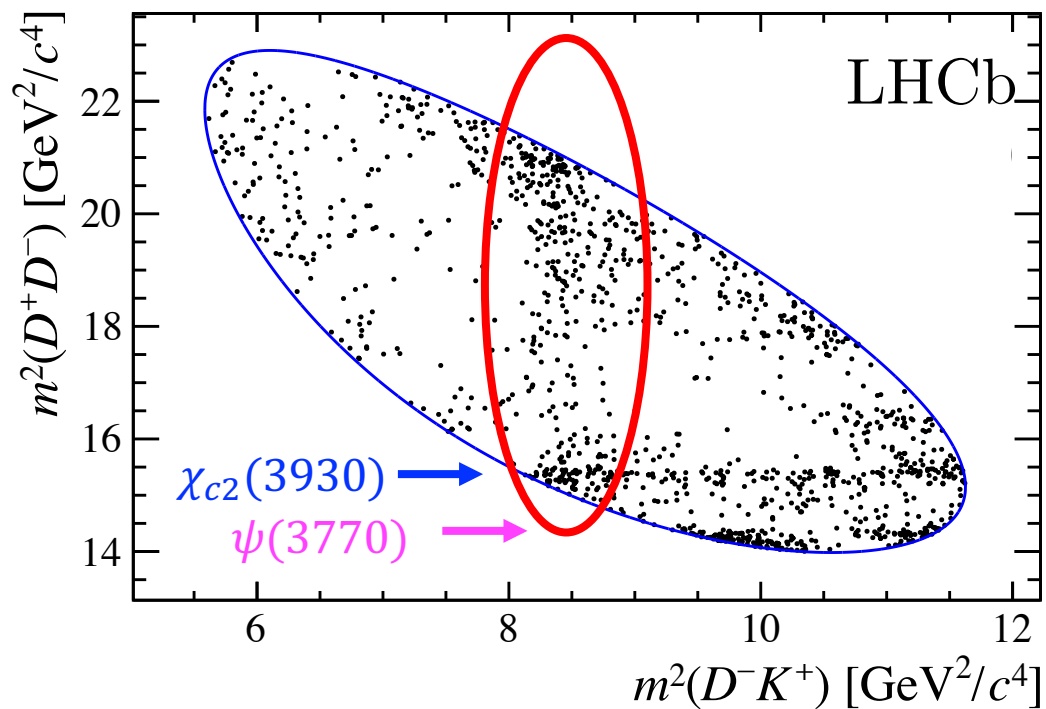


□ Double-charm tetraquark



# Tetraquarks in $B^+ \rightarrow D^+ D^- K^+$

- Structures in  $B^+ \rightarrow D^+ D^- K^+$ : amplitude analysis resolved  $X_0(2900)$  and  $X_1(2900)$  in  $D^- K^+$  final state
- Open charm tetraquarks with **four different flavors** [ $cs\bar{u}\bar{d}$ ]



$0^+$	$X_0(2900)$ :	$M = 2.866 \pm 0.007 \pm 0.002 \text{ GeV}/c^2$ ,	$\Gamma = 57 \pm 12 \pm 4 \text{ MeV}$
$1^-$	$X_1(2900)$ :	$M = 2.904 \pm 0.005 \pm 0.001 \text{ GeV}/c^2$ ,	$\Gamma = 110 \pm 11 \pm 4 \text{ MeV}$

# Tetraquarks in $B^0 \rightarrow \bar{D}^0 D_s^+ \pi^-$ and $B^+ \rightarrow \bar{D}^- D_s^+ \pi^+$

- Two isospin partners:  $T_{c\bar{s}0}^a(2900)^0 \rightarrow D_s^+ \pi^-$ ,  $T_{c\bar{s}0}^a(2900)^{++} \rightarrow D_s^+ \pi^+$

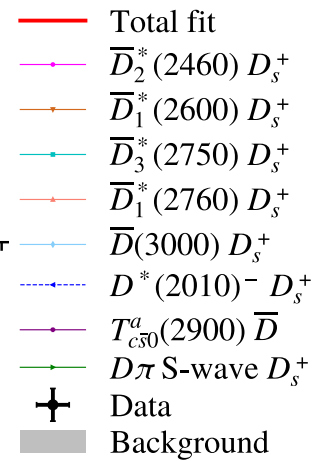
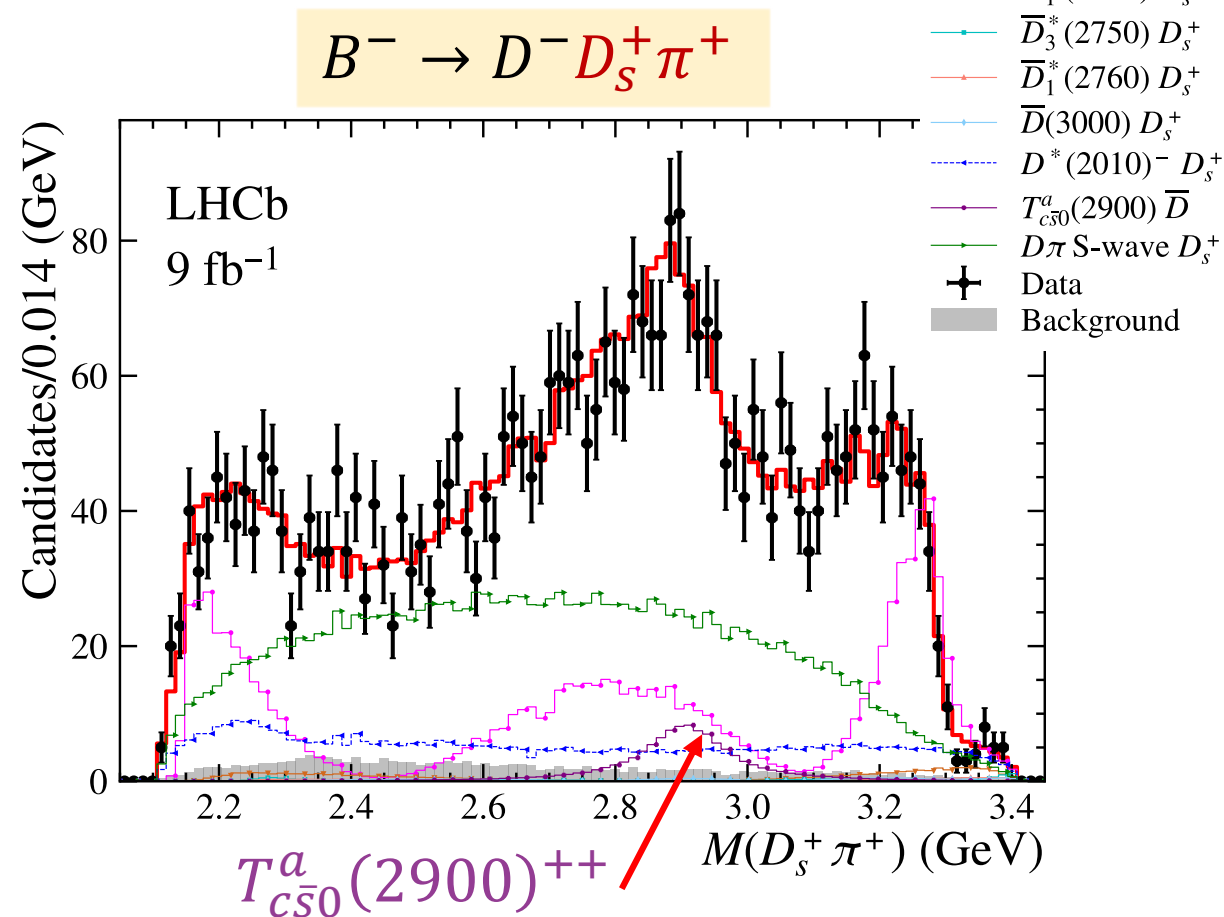
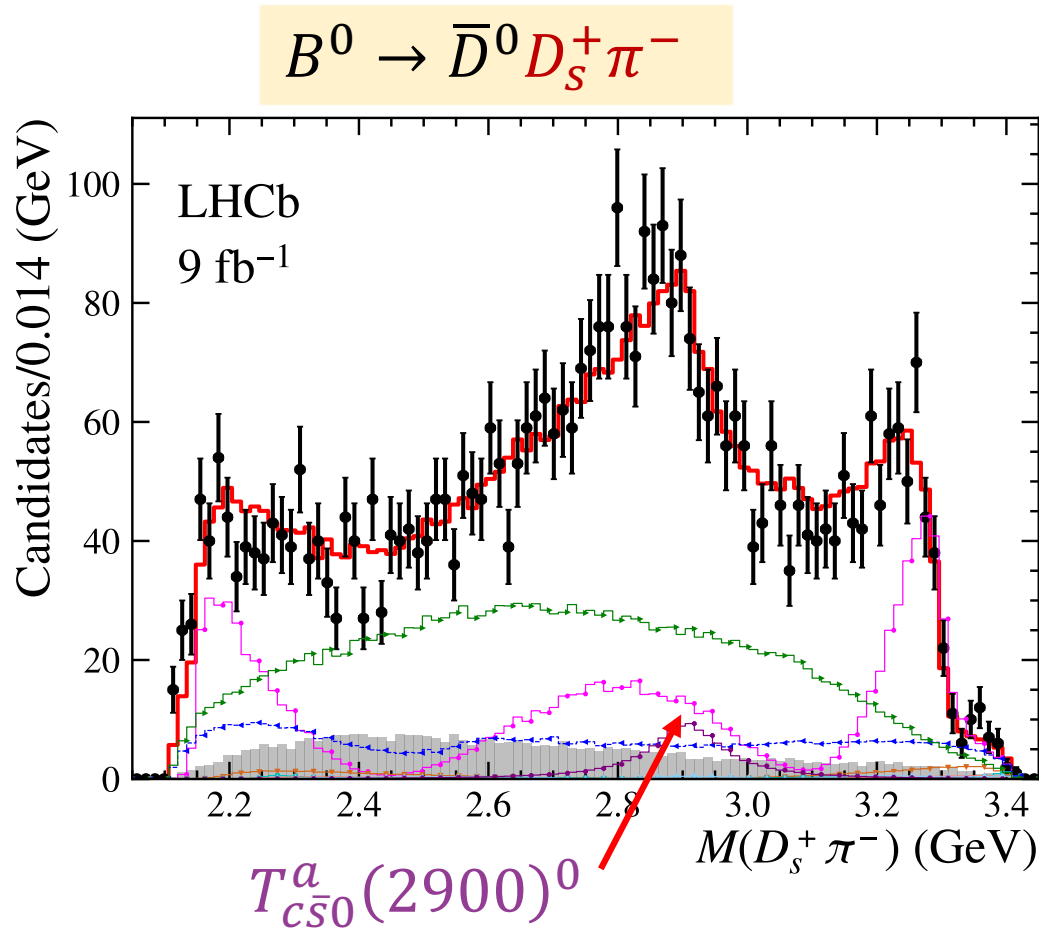
Joint amplitude analysis

$$M = 2.908 \pm 0.011 \pm 0.020 \text{ GeV}$$

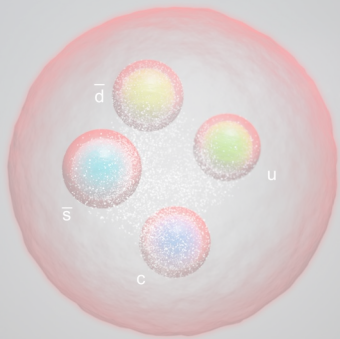
$$\Gamma = 0.136 \pm 0.023 \pm 0.011 \text{ GeV}$$

$$J^P = 0^+$$

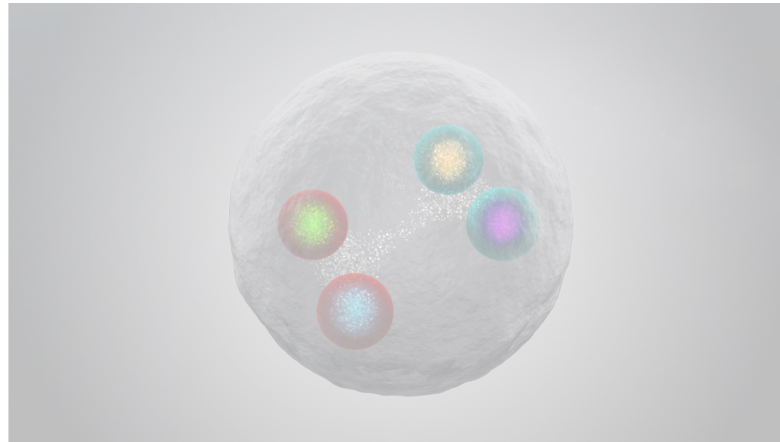
- Four different flavors  $[cd\bar{s}\bar{u}]$  and  $[cu\bar{s}\bar{d}]$



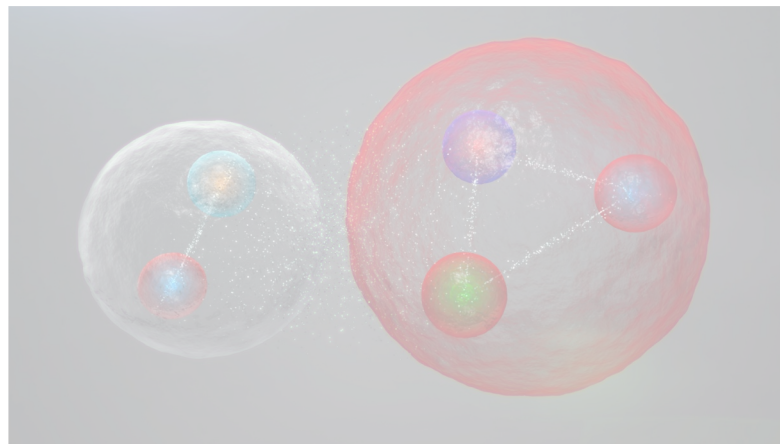
□ Single-charm tetraquark



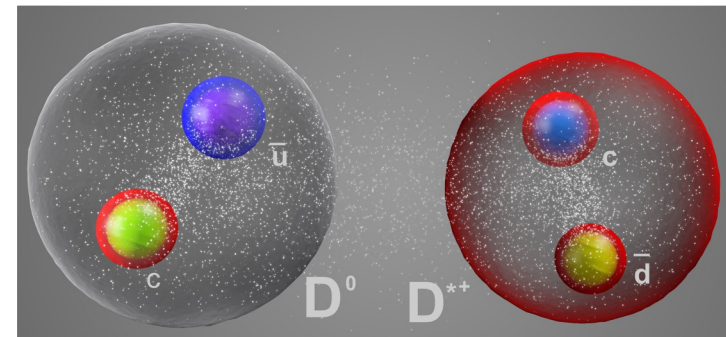
□ Hidden-charm tetraquark



□ Hidden-charm pentaquark



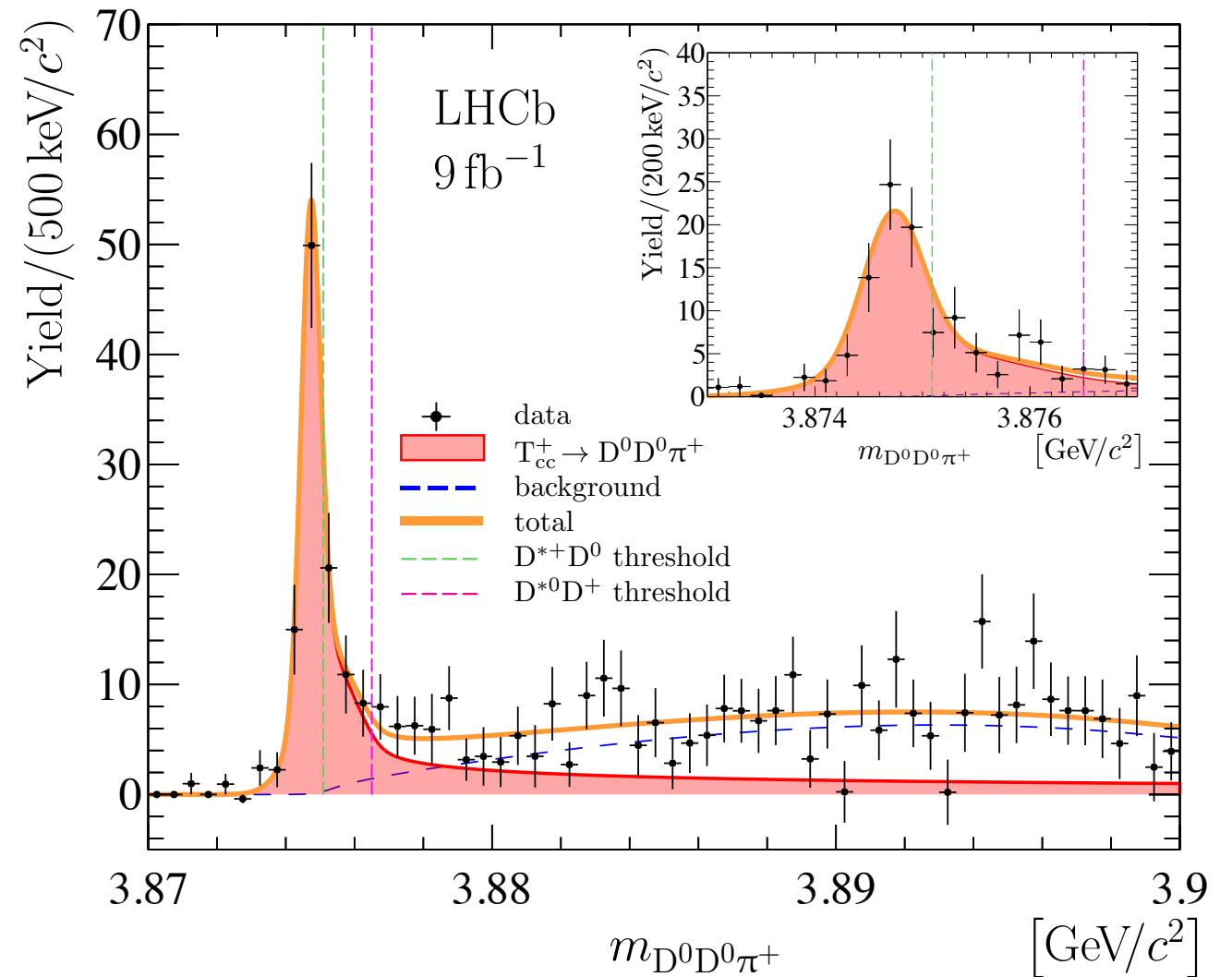
□ Double-charm tetraquark



# Observation of $T_{cc}^+$ in $D^0 D^0 \pi^+$ [arXiv: 2109.01038] ([Nature Physics](#)) [arXiv: 2109.01056] ([Nature Communications](#))

- Minimum contents  $[cc\bar{u}\bar{d}]$ , first tetraquark candidate with  $cc$
- Two fit models

Breit-Wigner resonance

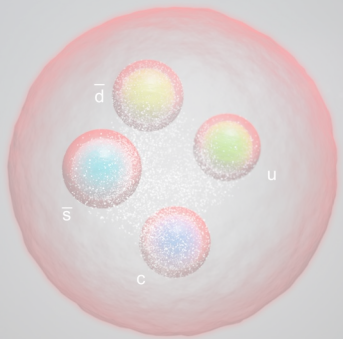


- Mass below  $D^0 D^{*+}$  threshold

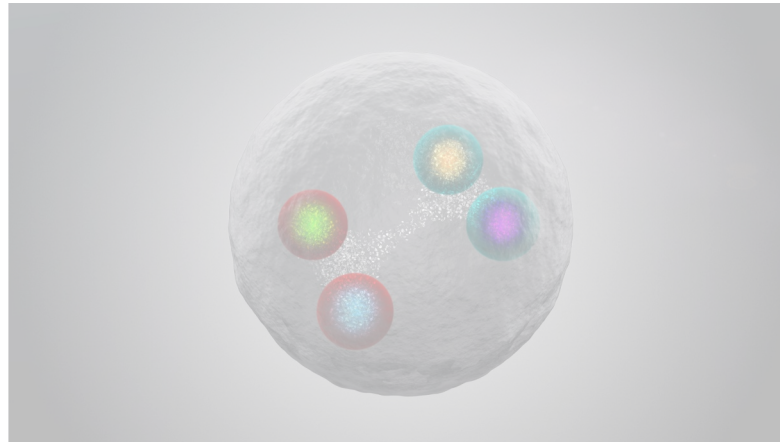
	$\delta m$ [keV/c <sup>2</sup> ]	$\Gamma$ [keV/c <sup>2</sup> ]
$\mathcal{F}^{\text{BW}}$	$-279 \pm 59$	$409 \pm 163$
$\mathcal{F}^{\text{U}}$	$-361 \pm 40$	$47.8 \pm 1.9$



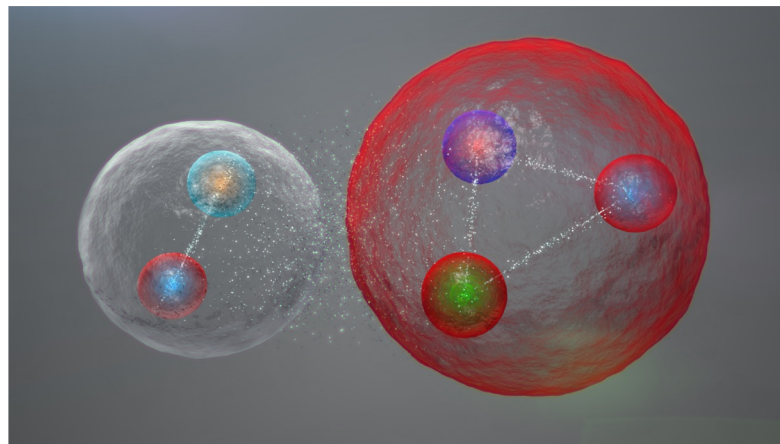
□ Single-charm tetraquark



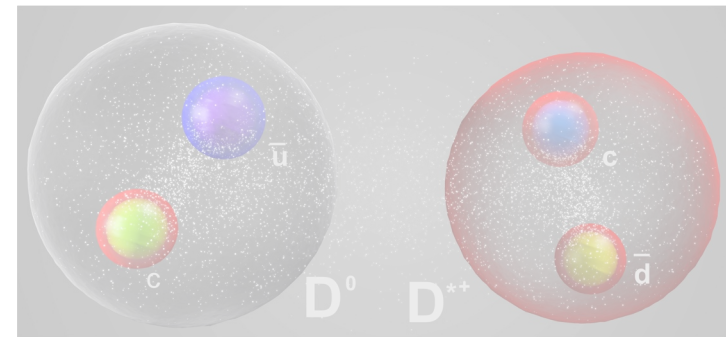
□ Hidden-charm tetraquark



□ Hidden-charm pentaquark

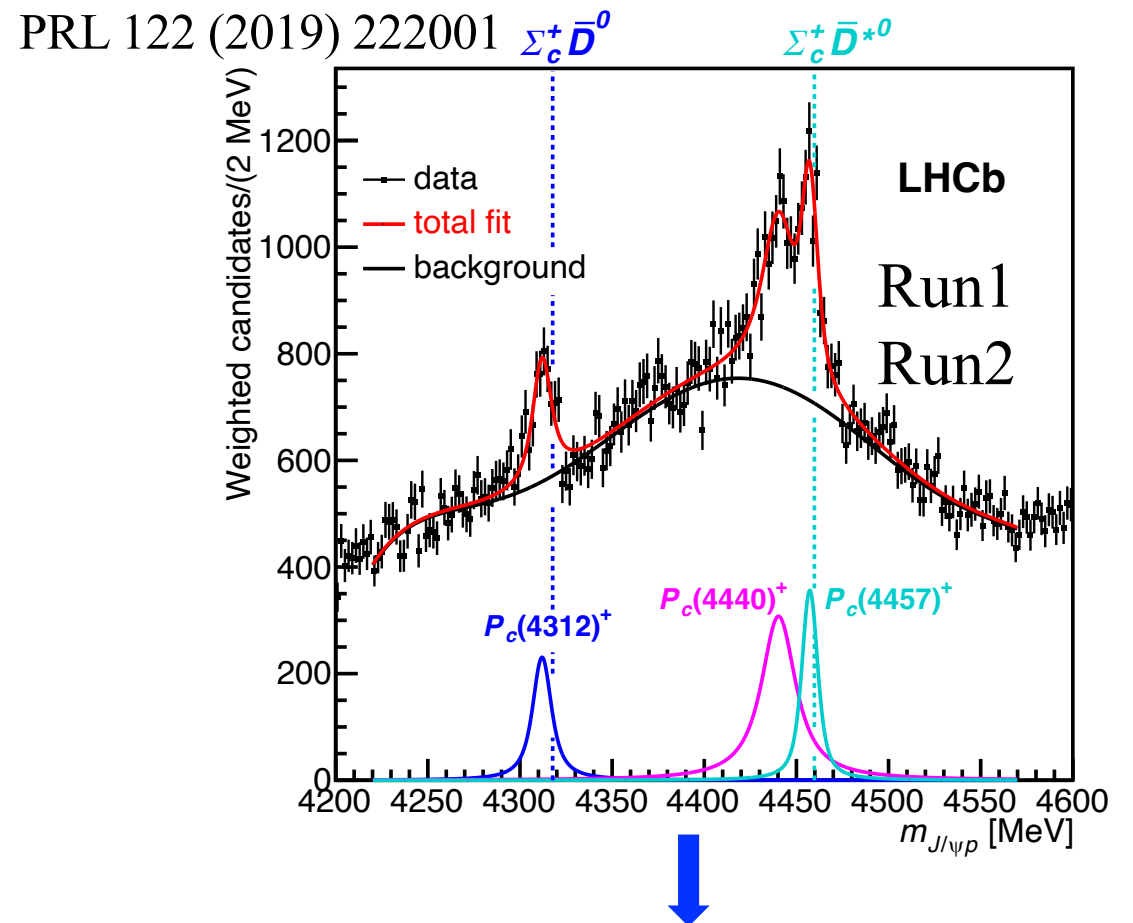
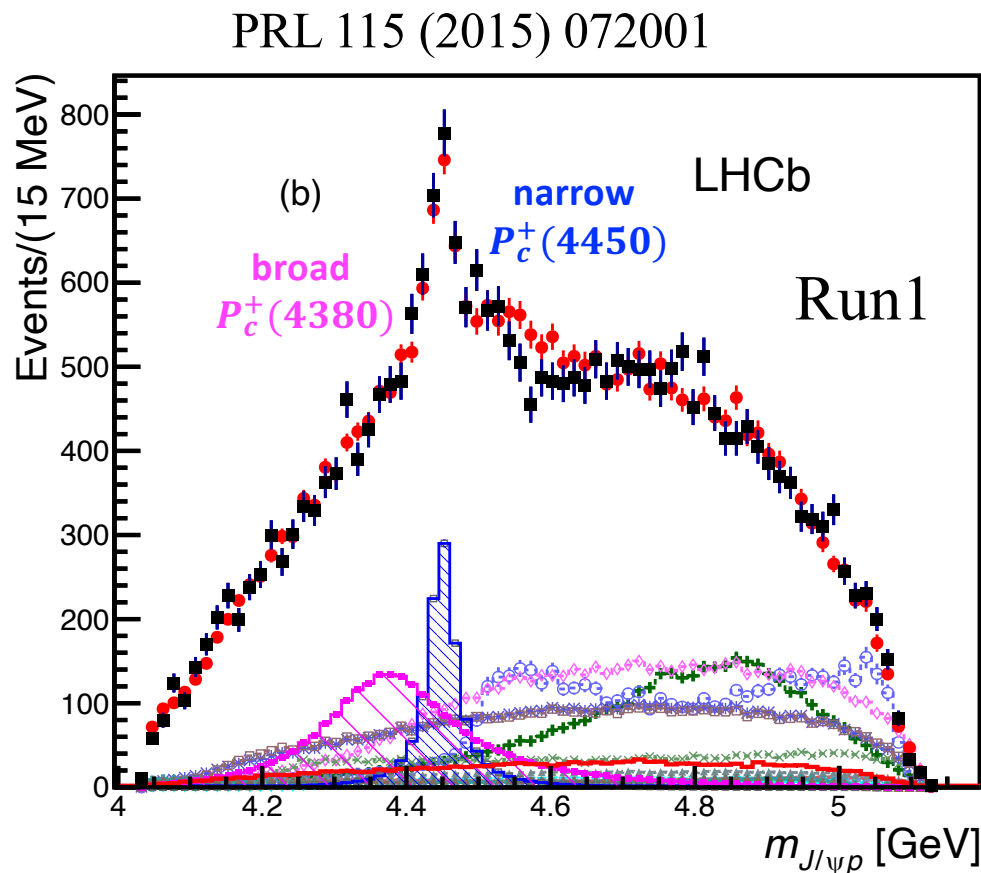


□ Double-charm tetraquark

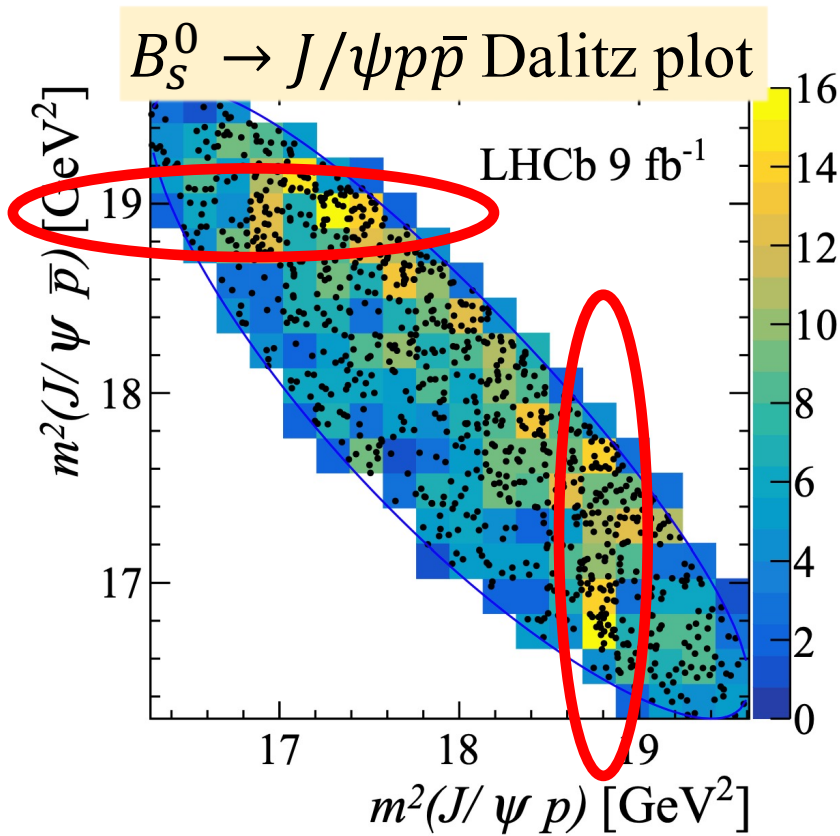


# Observation of $P_c^+$ in $\Lambda_b^0 \rightarrow J/\psi p K^-$

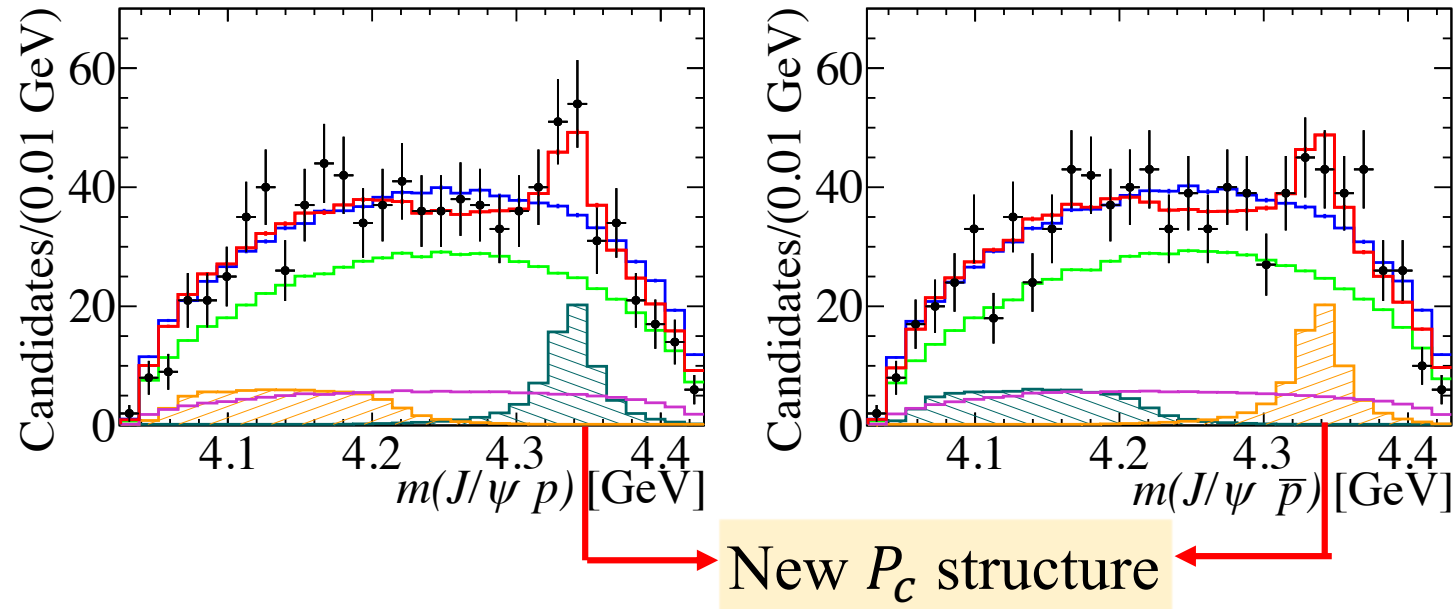
- $P_c^+$  ( $c\bar{c}uud$ ) states were first observed in  $\Lambda_b^0 \rightarrow J/\psi p K^-$  using Run1 data
- Analysis updated with  $\times 9$  more data
  - $P_c^+$  (4450) resolved into two peaks,  $P_c^+$  (4440) and  $P_c^+$  (4457), fine structure
  - A new state  $P_c^+$  (4312) observed



States close to  $\Sigma_c^+ \bar{D}^0$  and  $\Sigma_c^+ \bar{D}^{*0}$  mass thresholds consistent with molecular interpretation



## Amplitude analysis

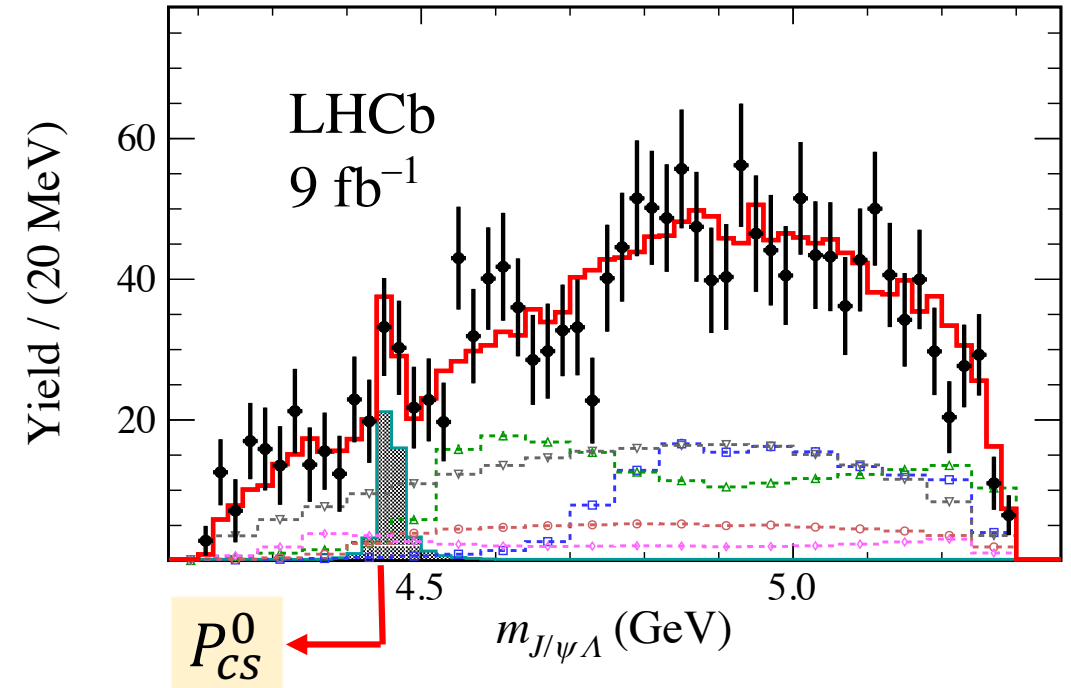
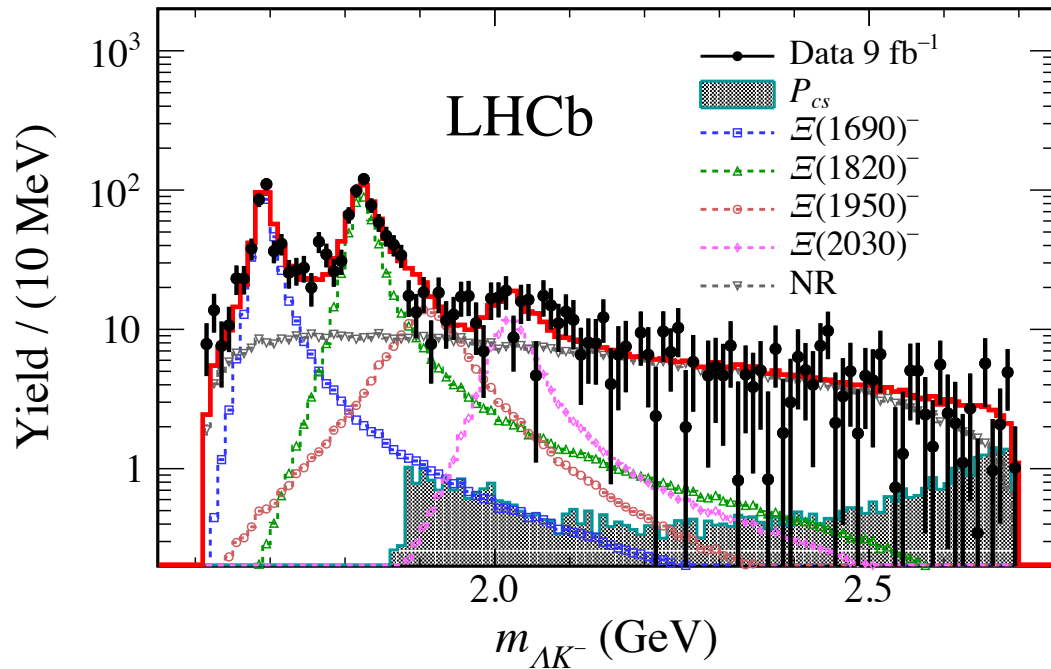


- New pentaquark candidate:  $P_c(4337)^+ \rightarrow J/\psi p > 3\sigma$  for  $J^P = 1/2^\pm, 3/2^\pm$

$$M = 4337_{-4}^{+7}(\text{stat})_{-2}^{+2}(\text{syst}) \text{ MeV}, \Gamma = 29_{-12}^{+26}(\text{stat})_{-14}^{+14}(\text{syst}) \text{ MeV}$$

- No evidence of  $P_c^+$  states observed in  $\Lambda_b^0 \rightarrow J/\psi p K^-$

- $P_{cs}^0$  ( $c\bar{c}sud$ ) observed through amplitude analysis of  $\Xi_b^- \rightarrow J/\psi \Lambda K^-$  at  $3.1\sigma$



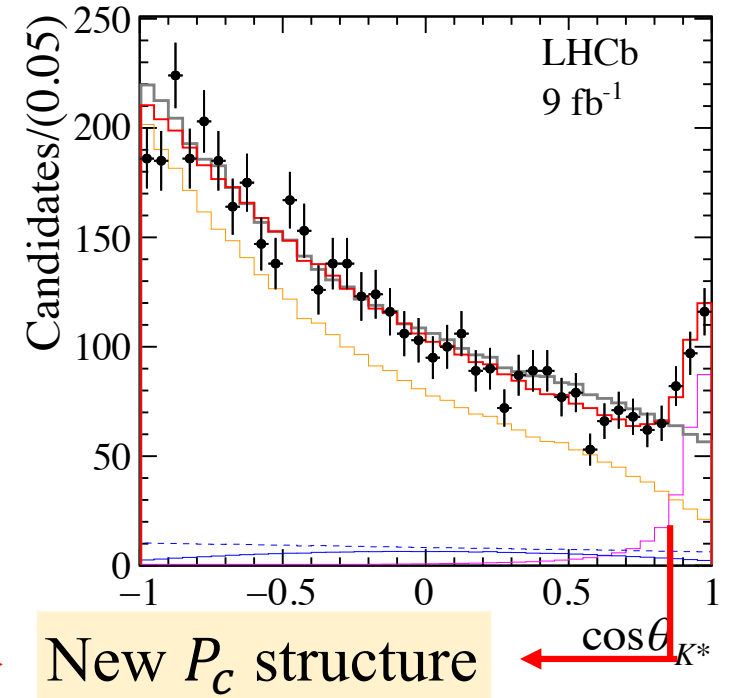
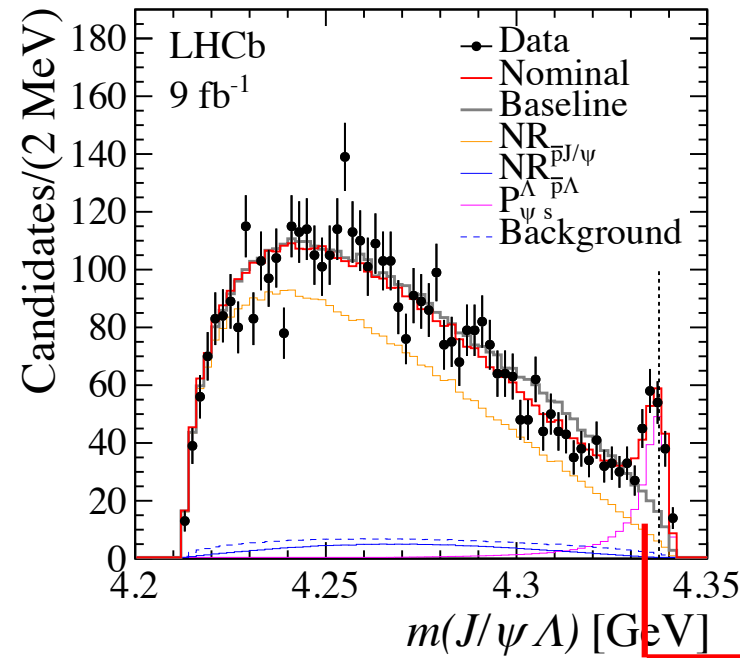
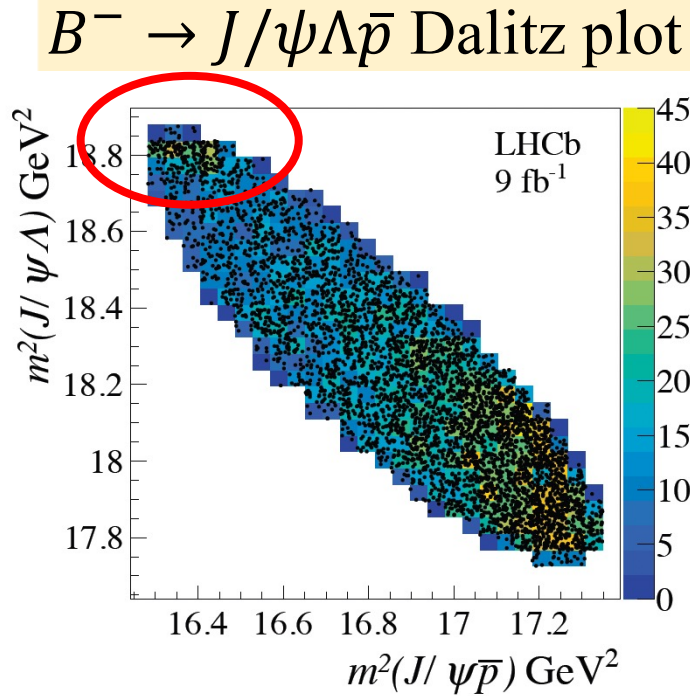
$$m(P_{cs}^0) = 4458.8 \pm 2.9_{-1.1}^{+4.7} \text{ MeV}, \quad \Gamma(P_{cs}^0) = 17.3 \pm 6.5_{-5.7}^{+8.0} \text{ MeV}$$

close to  $\Xi_c \bar{D}^*$  threshold, consistent with molecular state

More data to resolve double-peak structure and measure  $J^P$

PRD101(2020)034018

## Amplitude analysis: NR + $P_{CS}$

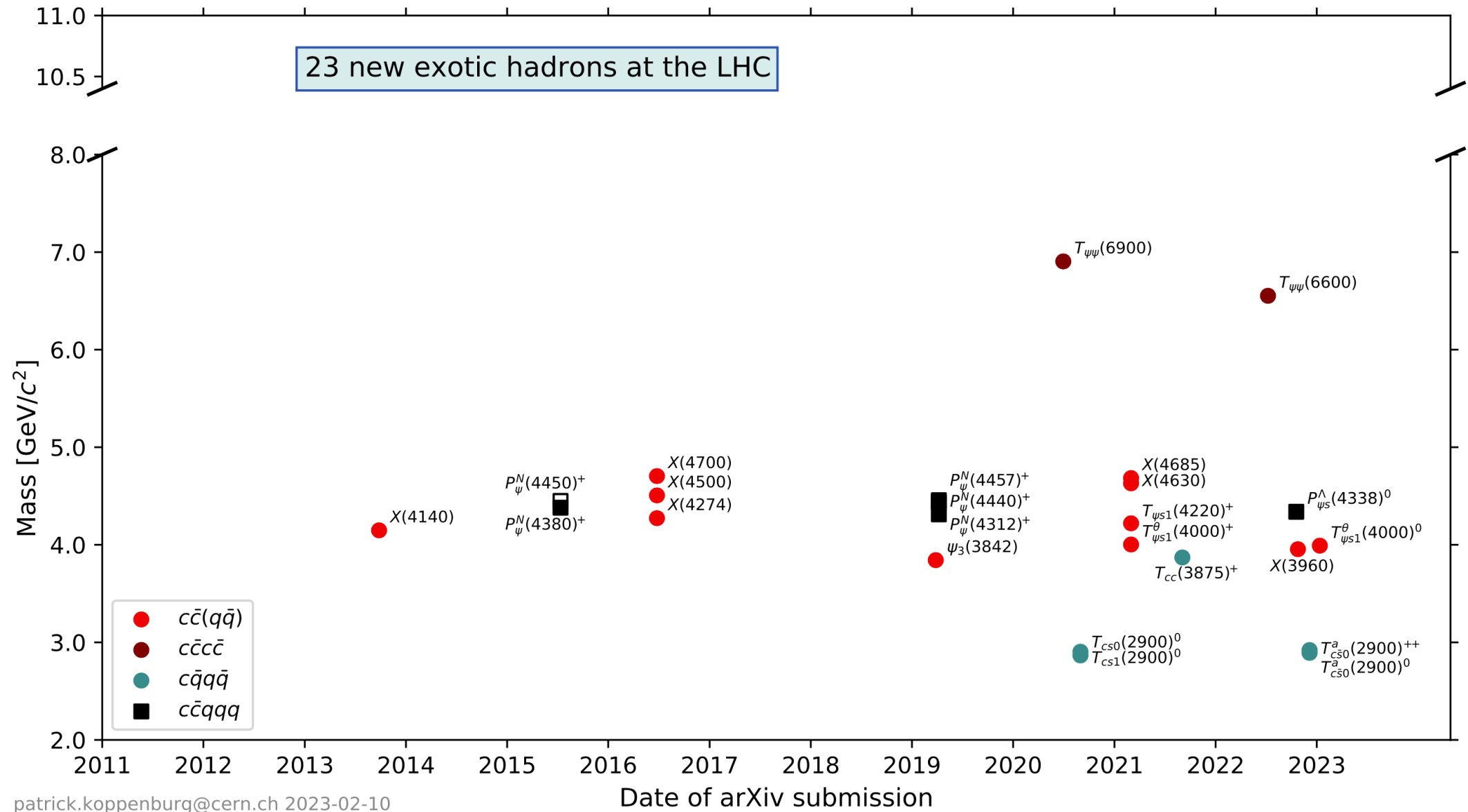


- New pentaquark candidate:  $P_{CS}(4338)^+ > 10\sigma$ ,  $J^P = 1/2^-$

$$M = 4338.2 \pm 0.7 \pm 0.4 \text{ MeV}, \Gamma = 7.0 \pm 1.2 \pm 1.3 \text{ MeV}$$

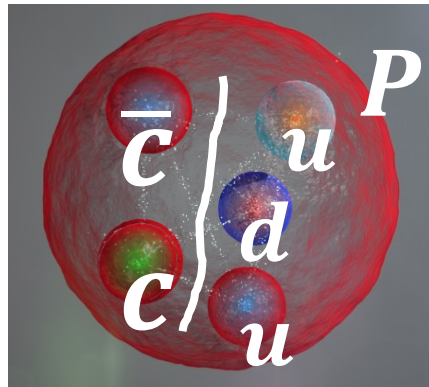
- First establishment of pentaquark with strangeness [ $c\bar{c}uds$ ]
- Close to  $E_c^+ D^-$  threshold and in  $S$ -wave

# Possible exotic states by LHC

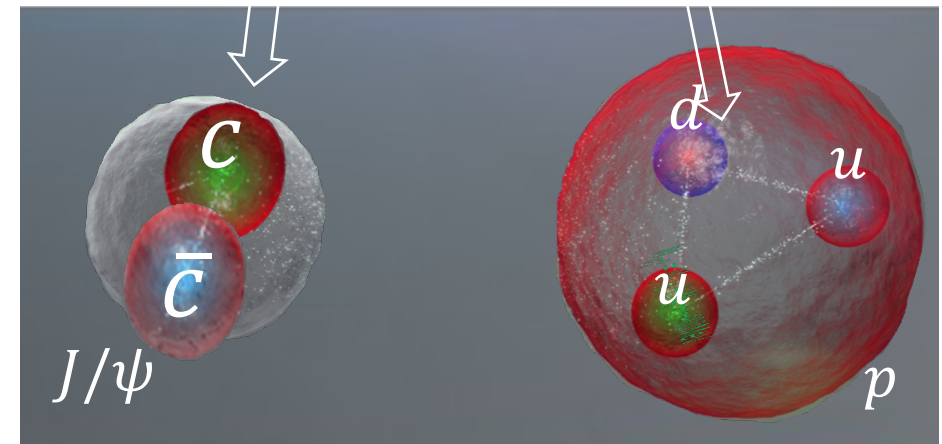
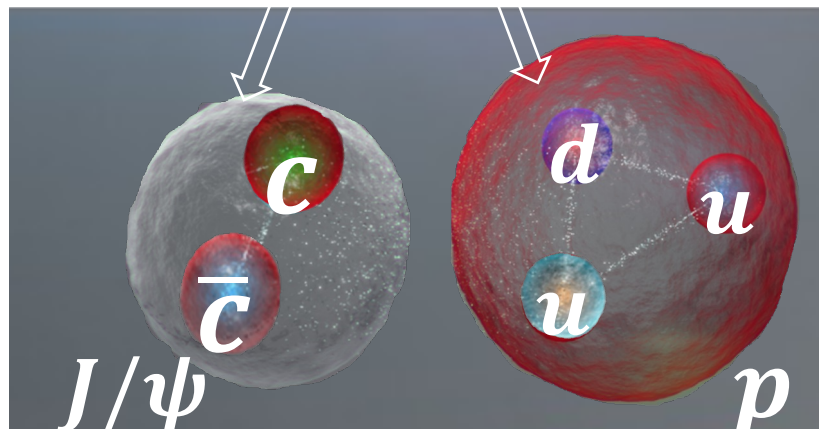
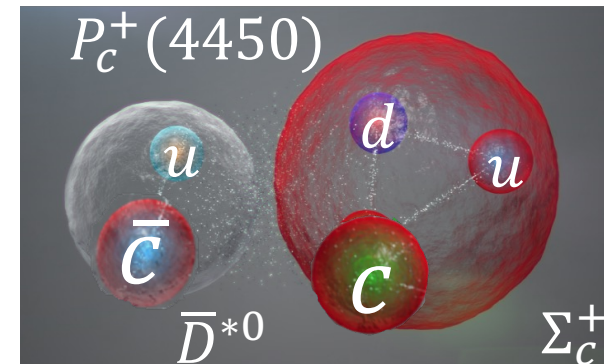


# The question: molecule or compact tetraquark

Compact



Molecule



Most exotic states compatible with molecule picture

What those compact states? Unstable?

“Build” your favourable exotic and find them in a zoo/an experiment

$\approx 2.2 \text{ MeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$ <b>u</b> up	$\approx 1.28 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$ <b>c</b> charm	$\approx 173.1 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$ <b>t</b> top
$\approx 4.7 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$ <b>d</b> down	$\approx 96 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$ <b>s</b> strange	$\approx 4.18 \text{ GeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$ <b>b</b> bottom

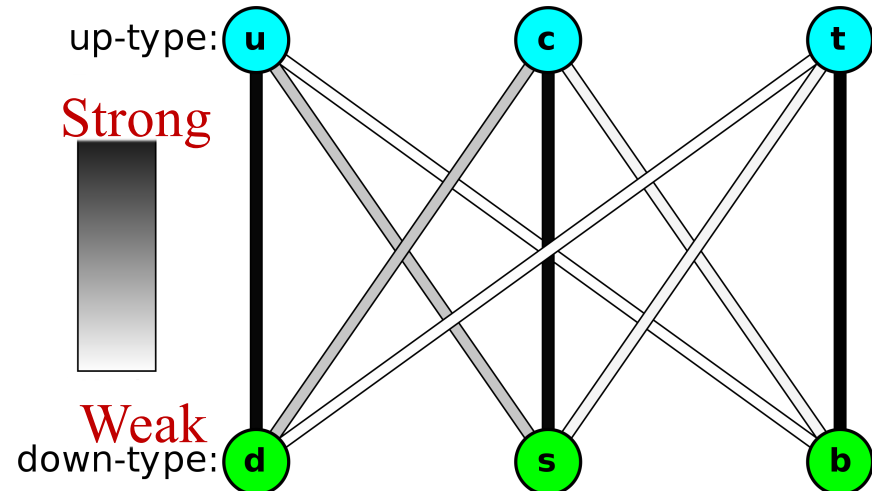
anti-triplet as anti-quarks  $\bar{q}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqqq\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(qq\bar{q}\bar{q})$ , etc. It is assuming that the lowest



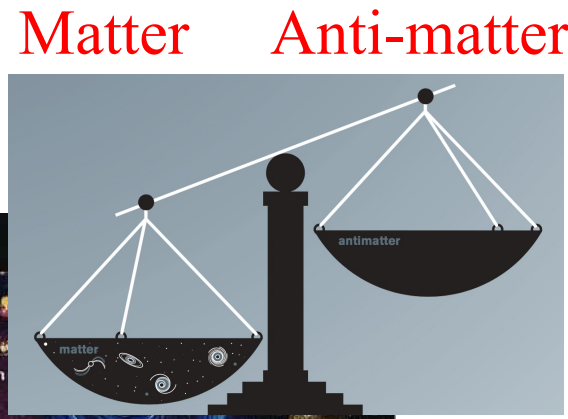
# Why six quarks

## Cabibbo-Kobayashi-Maskawa (CKM) matrix (1973)

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



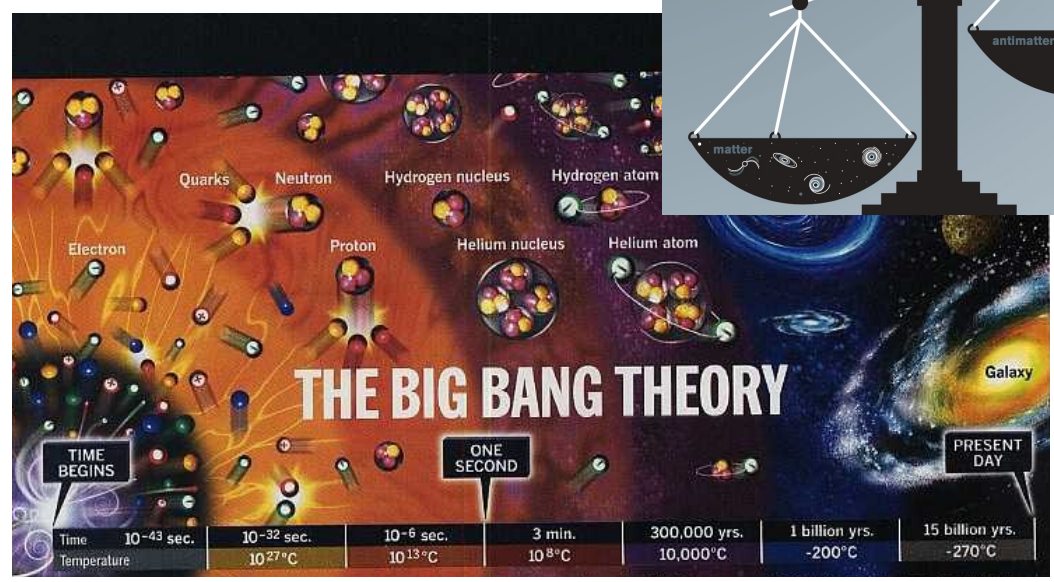
## Origins of matter and anti-matter asymmetry



Explains violations of CP symmetry

C: charge conjugation

P: parity



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ありがとうございました

감사합니다

Thank you

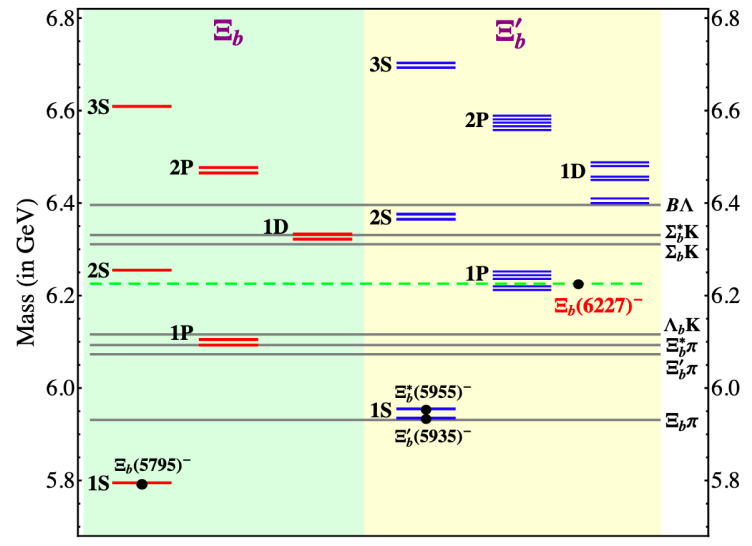
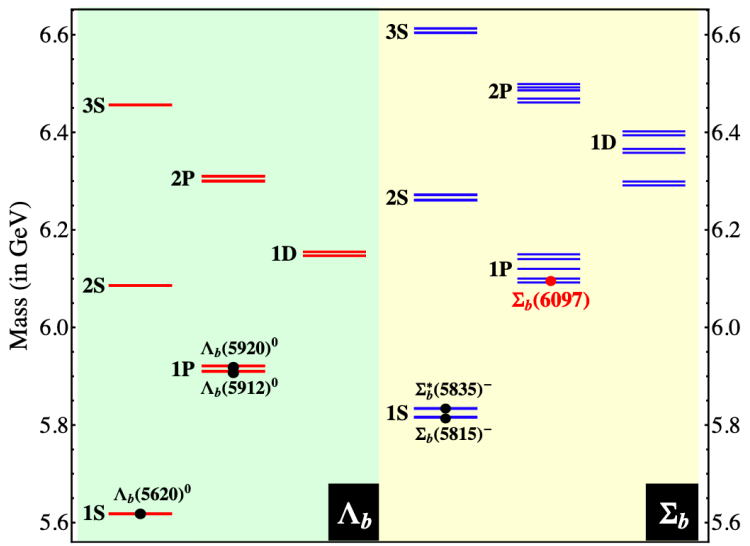
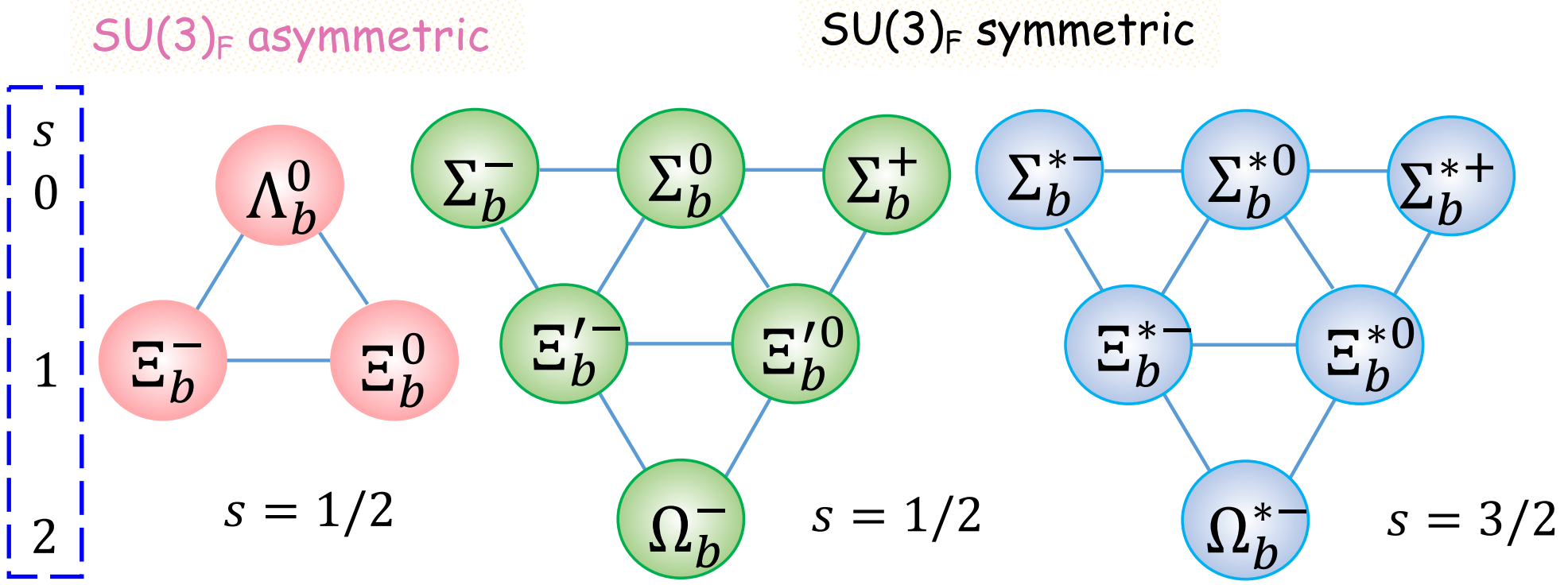
謝謝

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*Backup slides*

# Beauty baryons

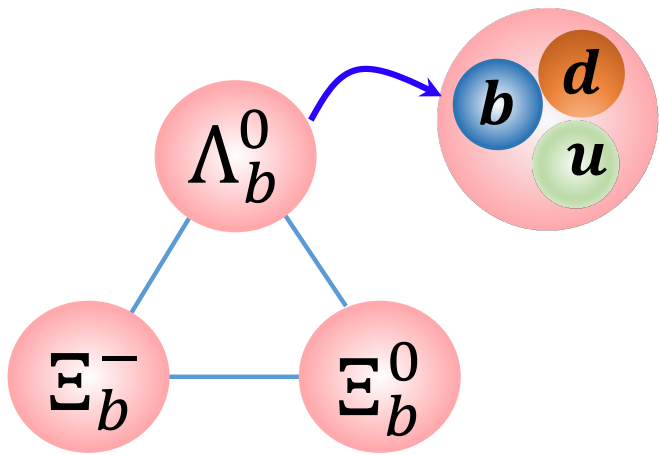
- Ground states



PRD 98 (2018) 031502  
 PRD 98 (2018) 074032  
 PRD 100 (2019) 094032

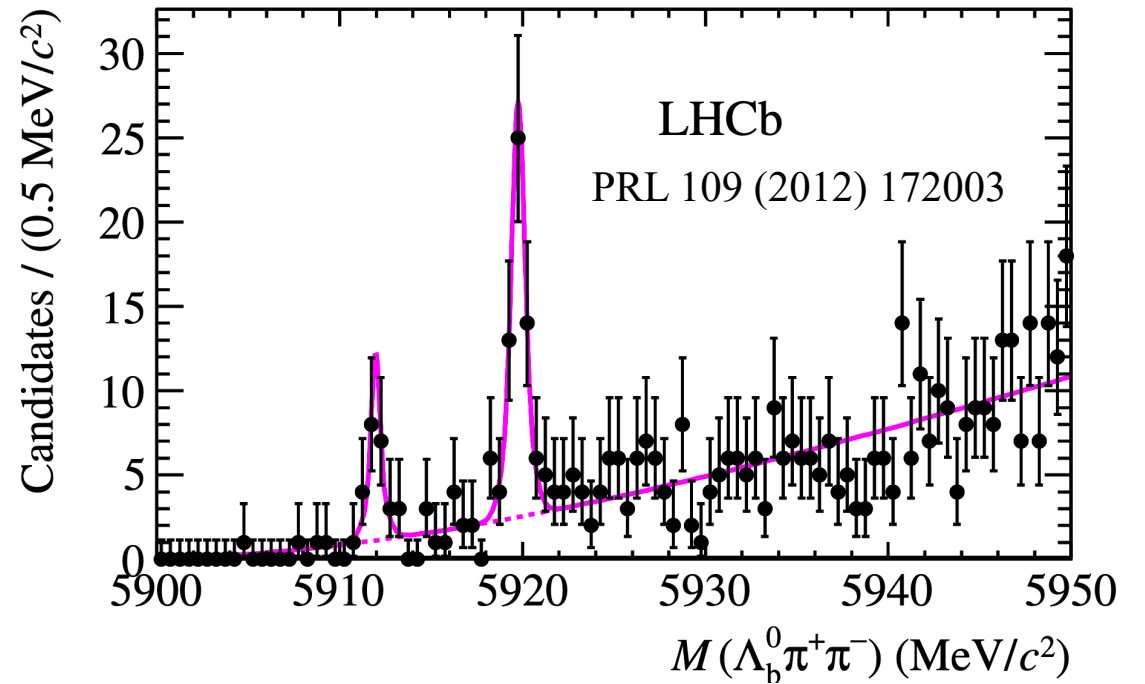
Spectrum poorly established

# Excited $\Lambda_b^0$ baryons

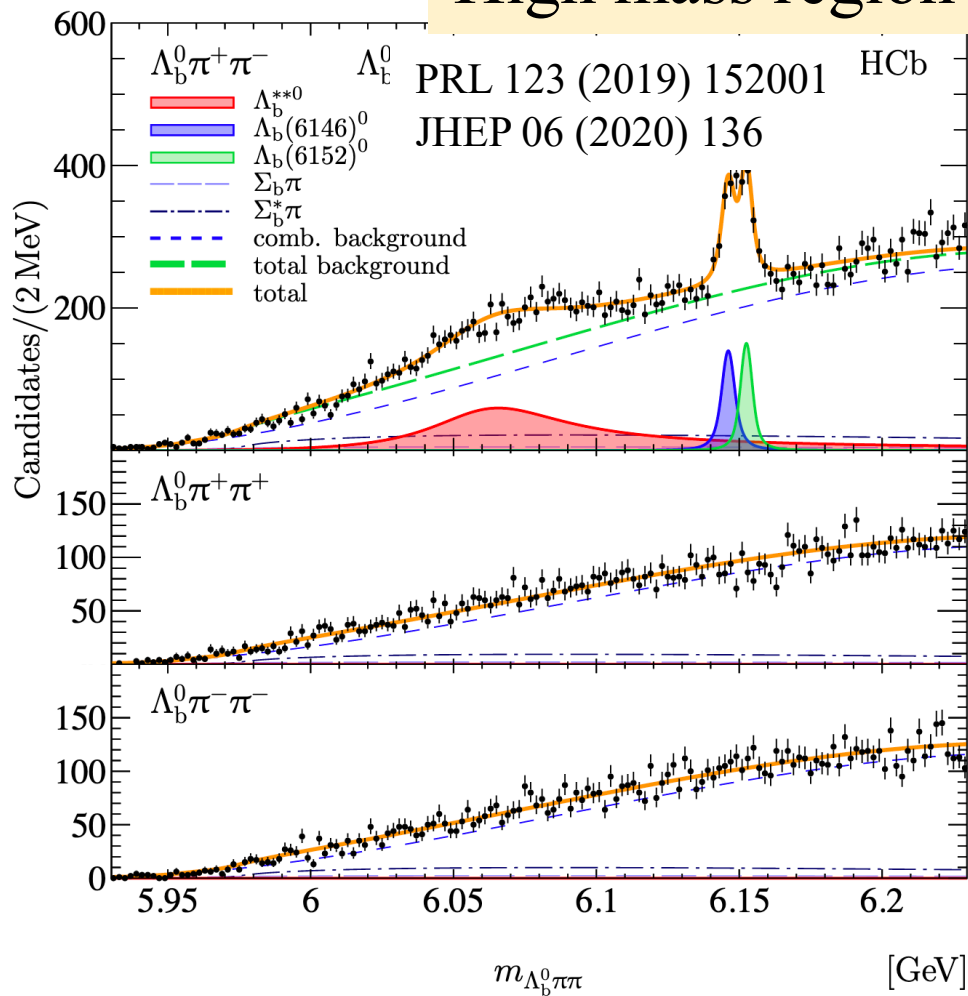


$$\Lambda_b^{**0} \rightarrow \Lambda_b^0 \pi^+ \pi^-$$

Low mass region

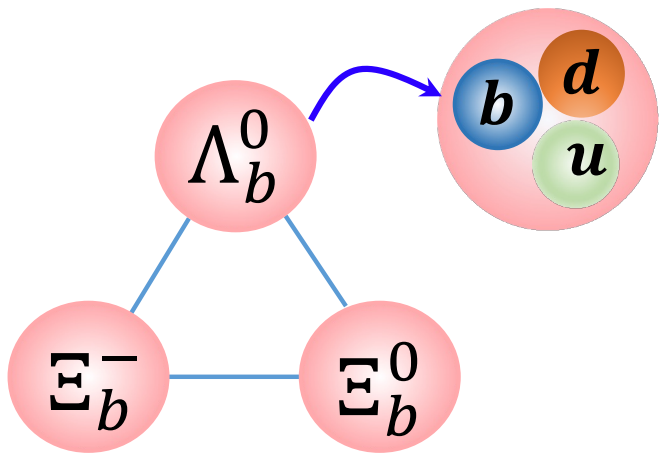


High mass region



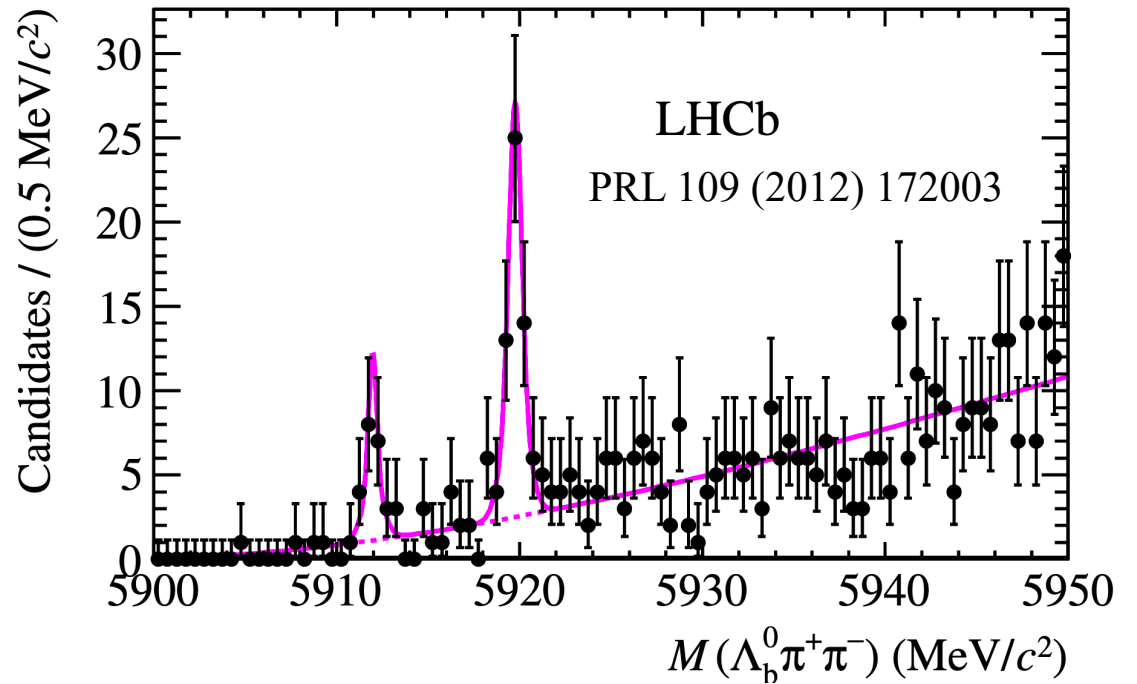
State	Mass (MeV)	Width (MeV)
$\Lambda_b^0(5620)$	$5620.60 \pm 0.17$	—
$\Lambda_b^0(5912)$	$5912.20 \pm 0.21$	$< 0.66$
$\Lambda_b^0(5920)$	$5919.92 \pm 0.19$	$< 0.83$
$\Lambda_b^0(6072)$	$6072.3 \pm 3.0$	$72 \pm 11$
$\Lambda_b^0(6146)$	$6146.2 \pm 0.4$	$2.9 \pm 1.3$
$\Lambda_b^0(6152)$	$6152.5 \pm 0.4$	$2.1 \pm 0.9$

# Excited $\Lambda_b^0$ baryons

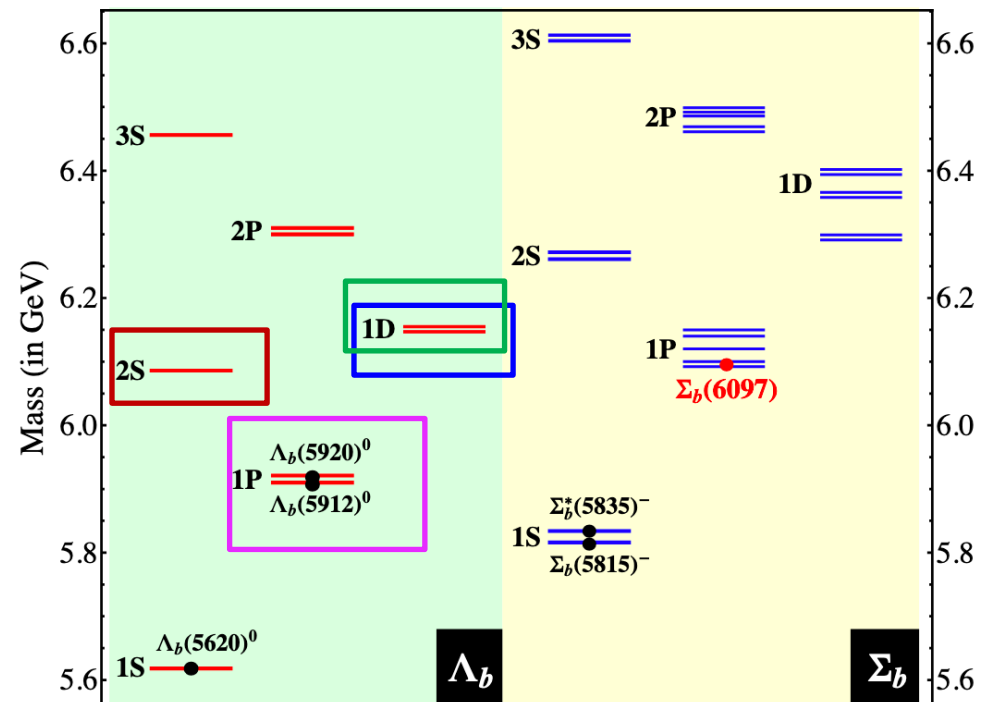
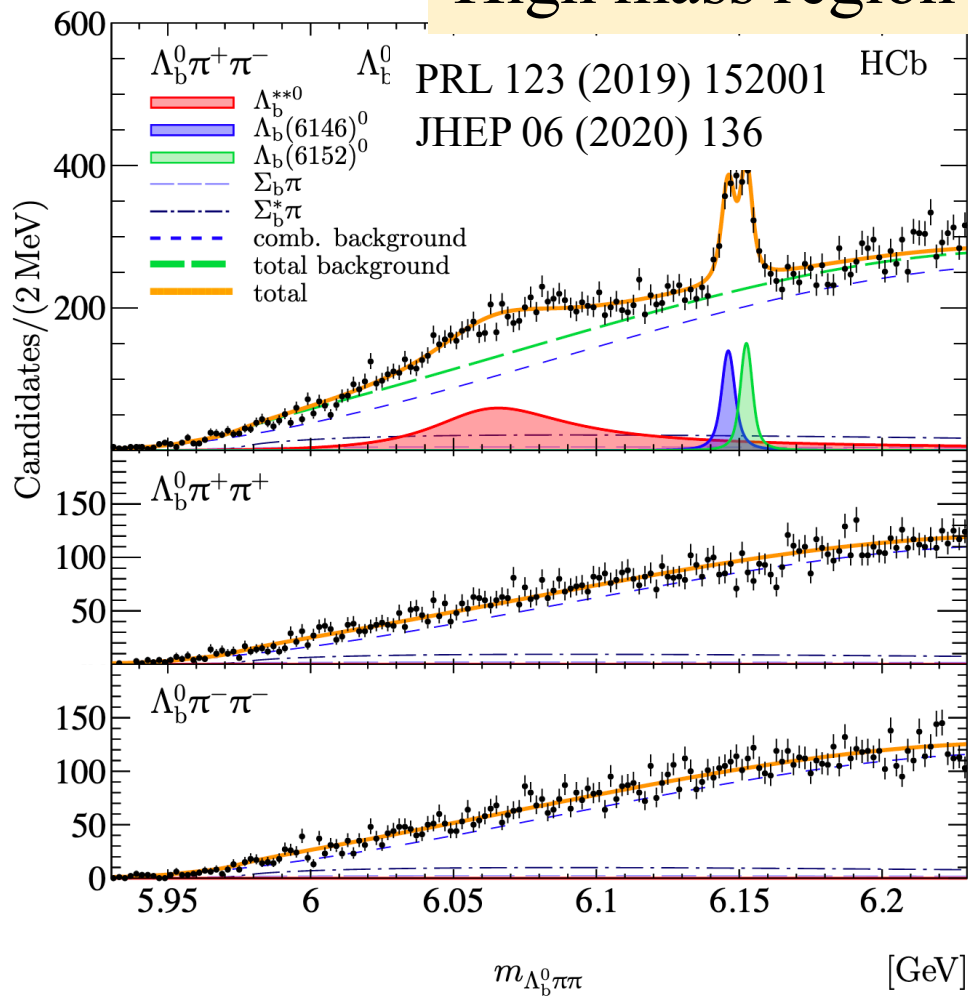


$$\Lambda_b^{**0} \rightarrow \Lambda_b^0 \pi^+ \pi^-$$

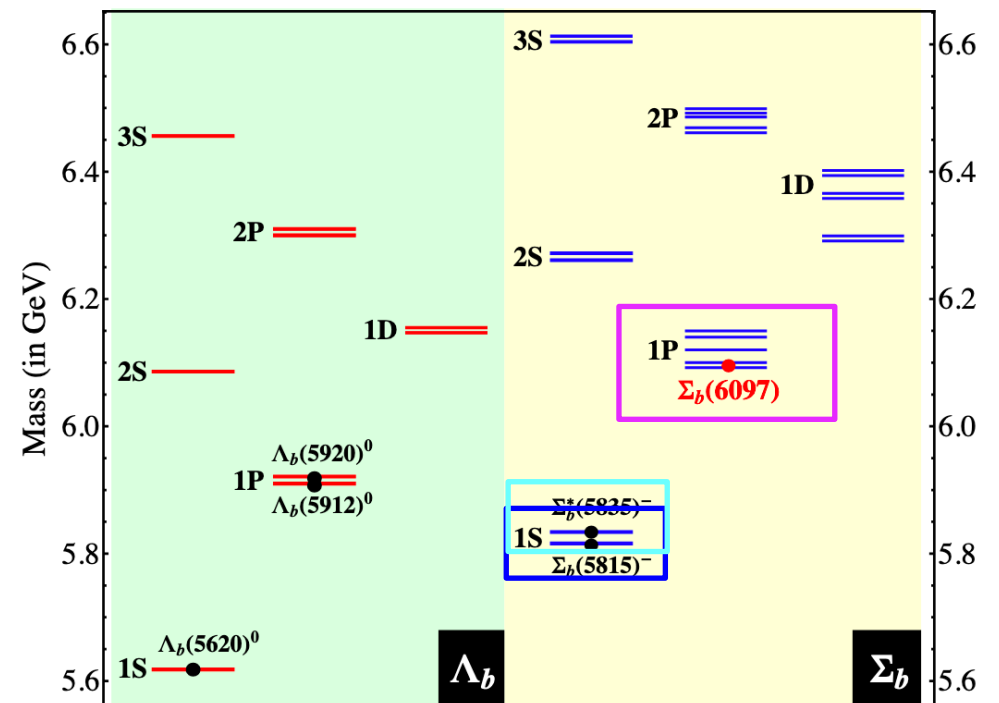
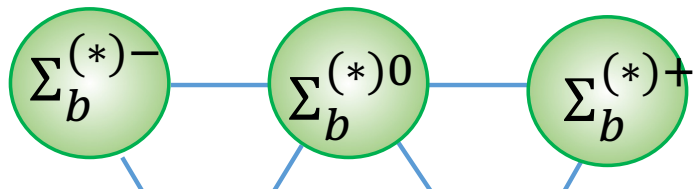
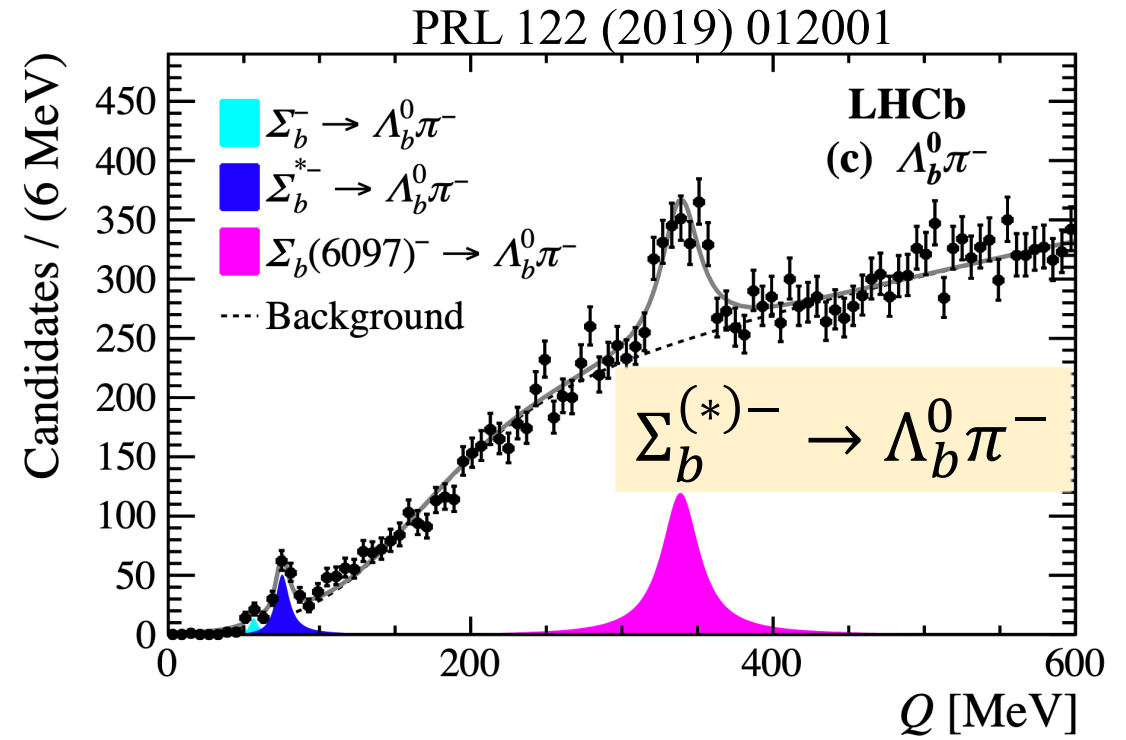
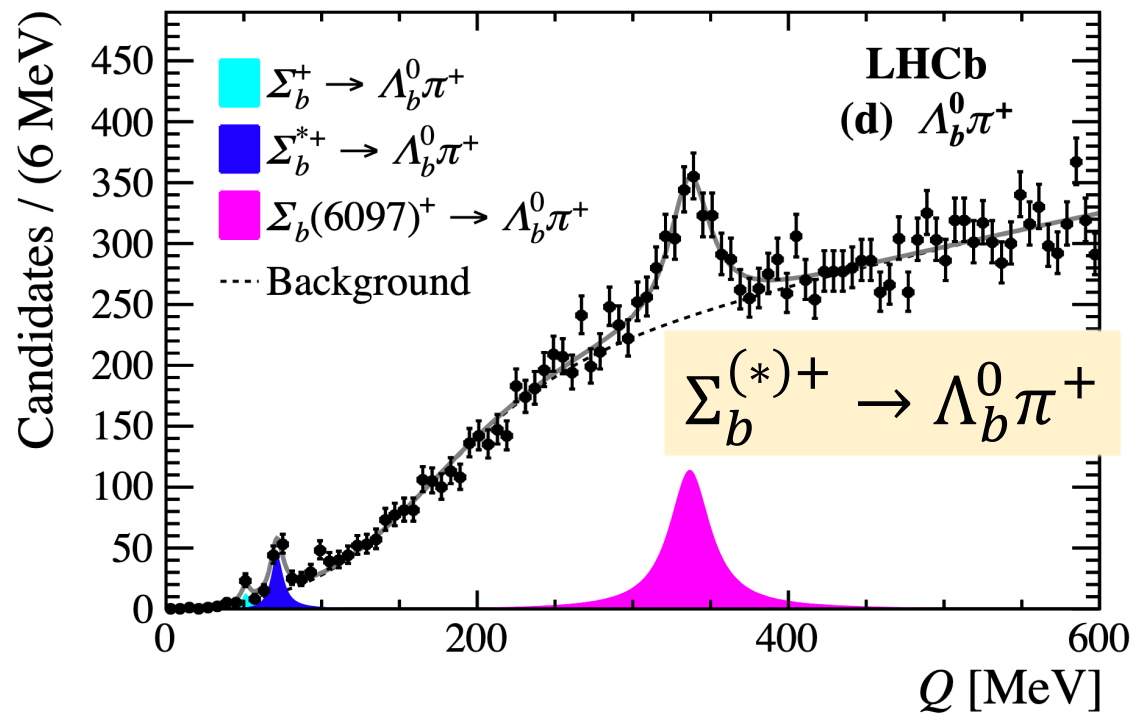
Low mass region



High mass region



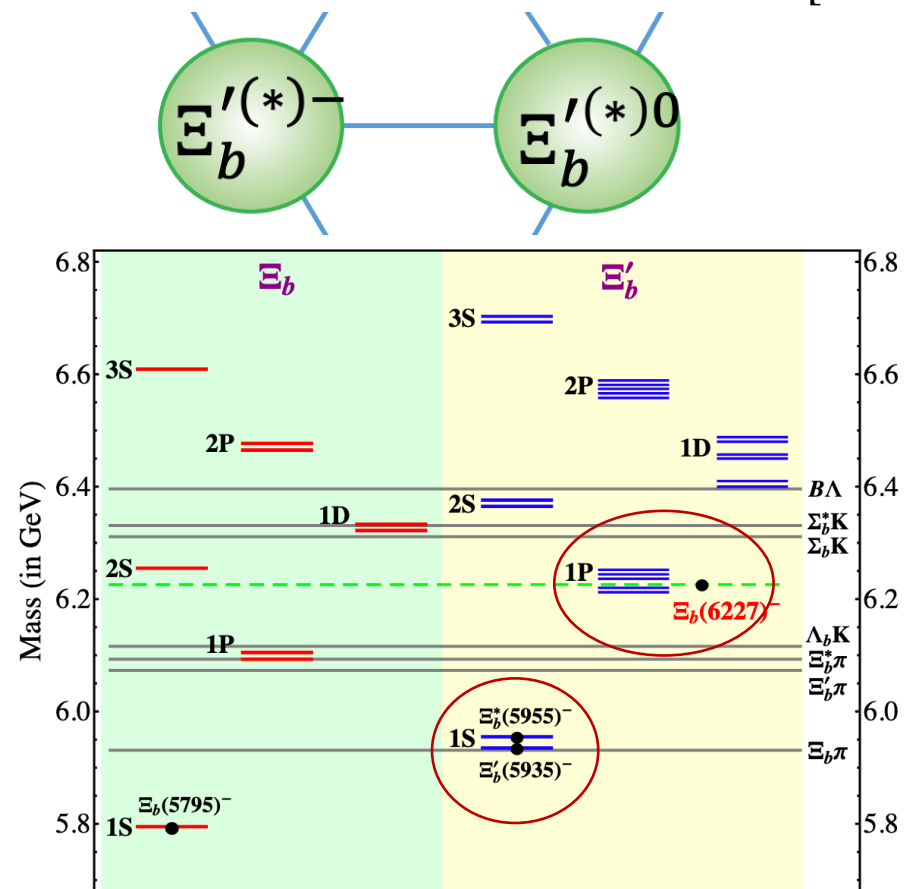
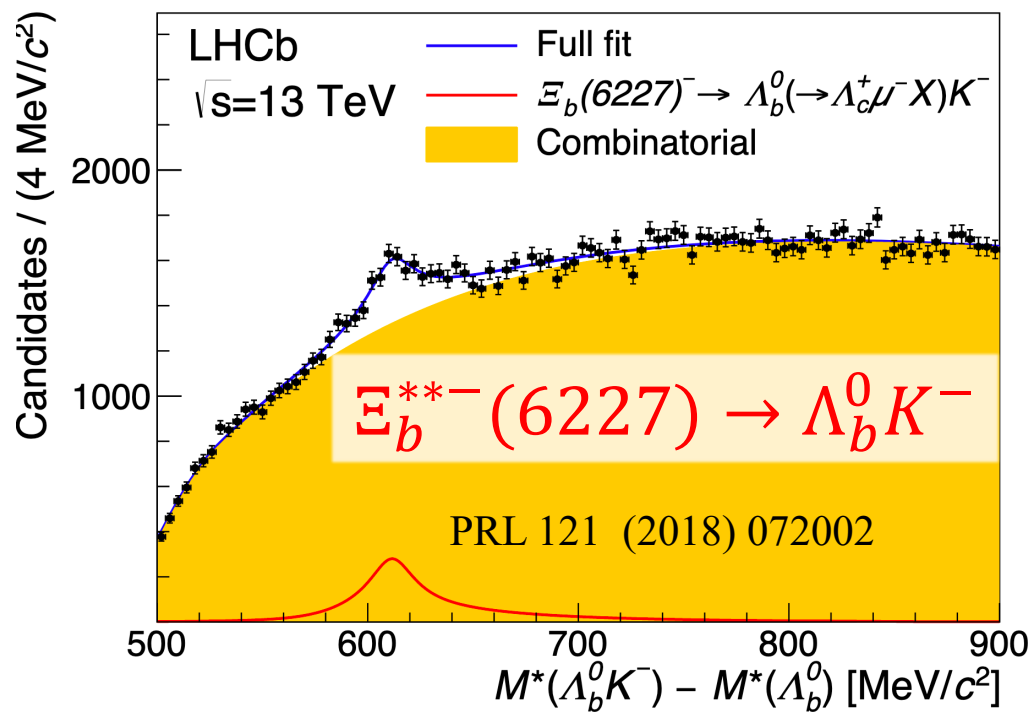
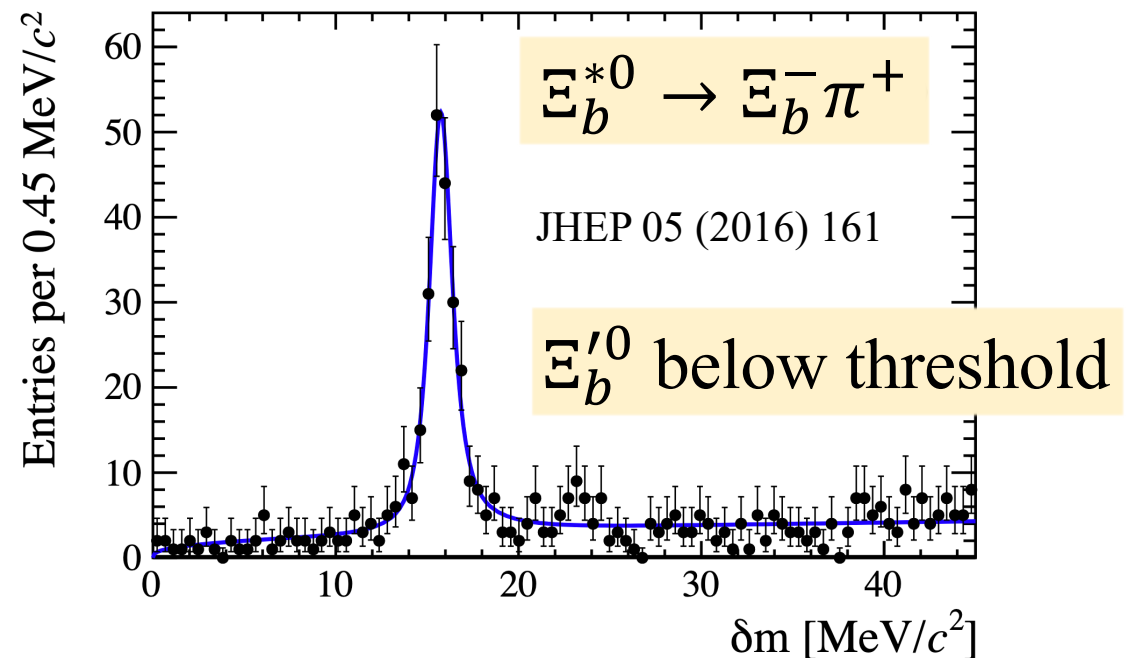
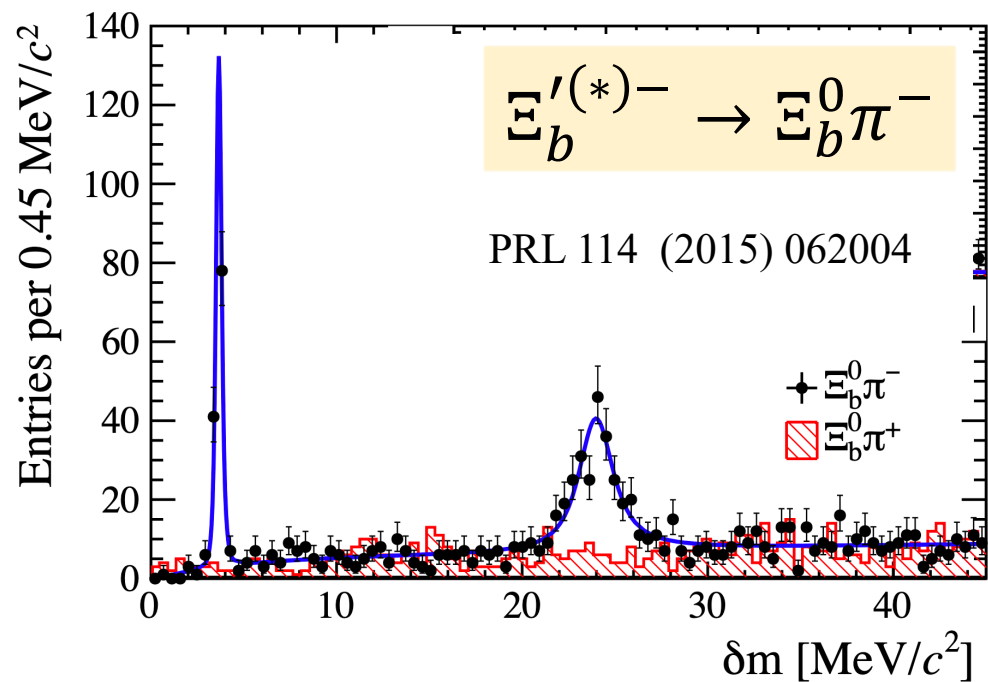
# Excited $\Sigma_b^\pm$ baryons



State	Mass (MeV)	Width (MeV)
$\Sigma_b^{+/-}$	5810/5815	5
$\Sigma_b^{*+/-}$	5830/5835	19
$\Sigma_b^{**+/-}$	6098/6096	30

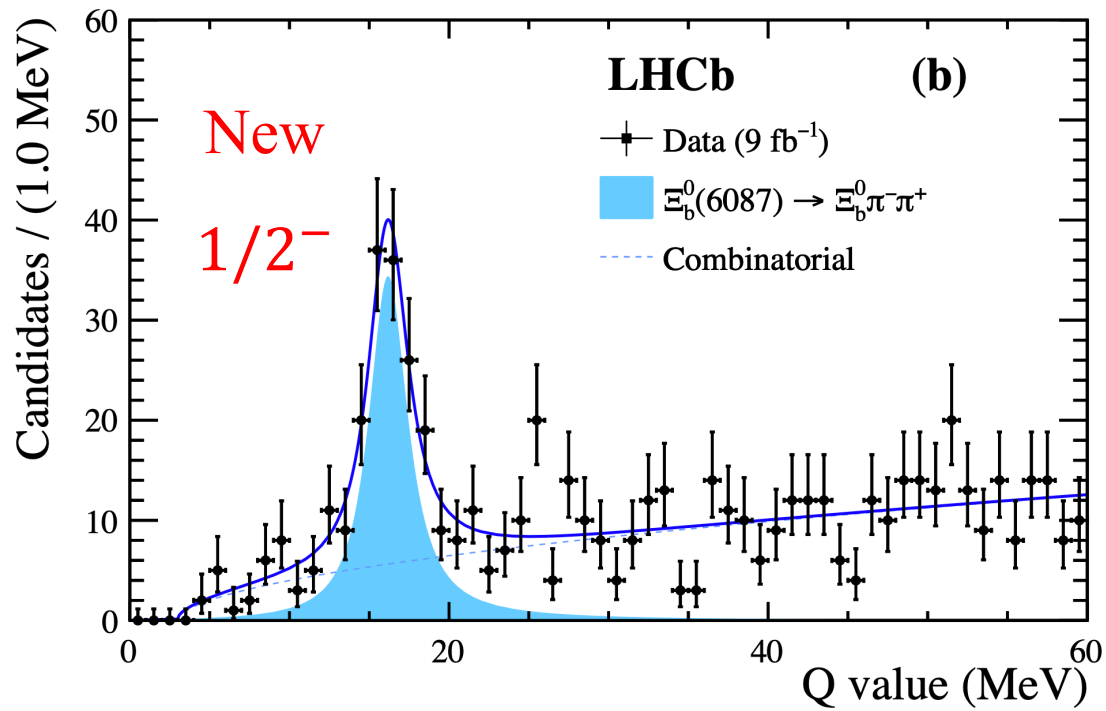
Missing other low-lying P-wave states

# Excited $\Xi_b$ baryons

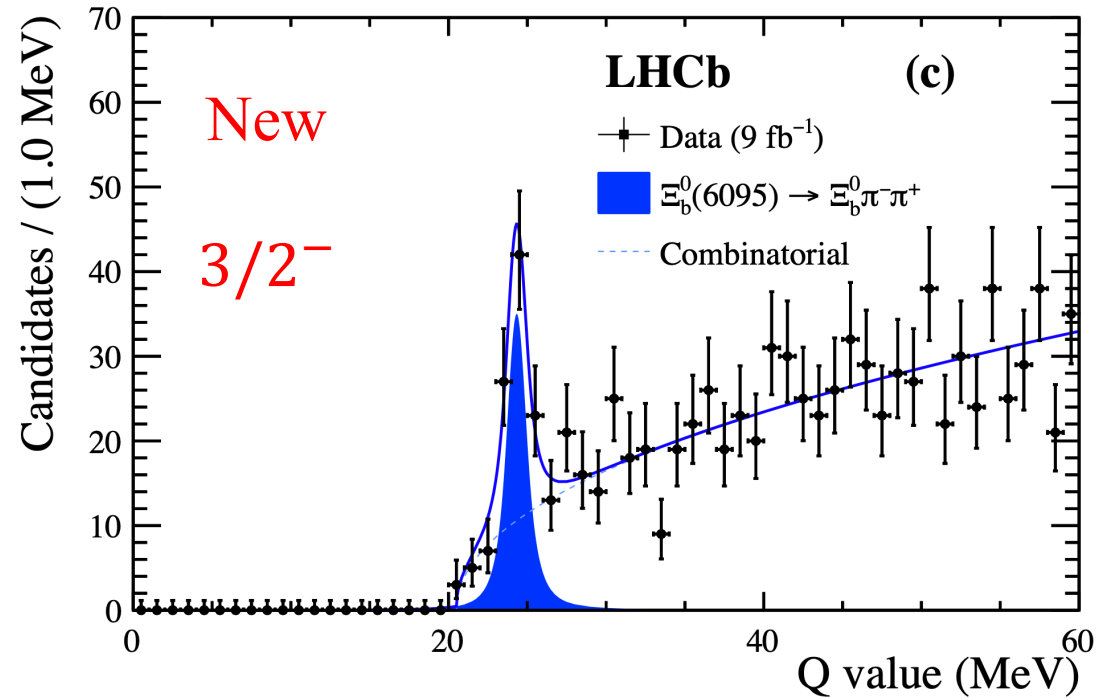




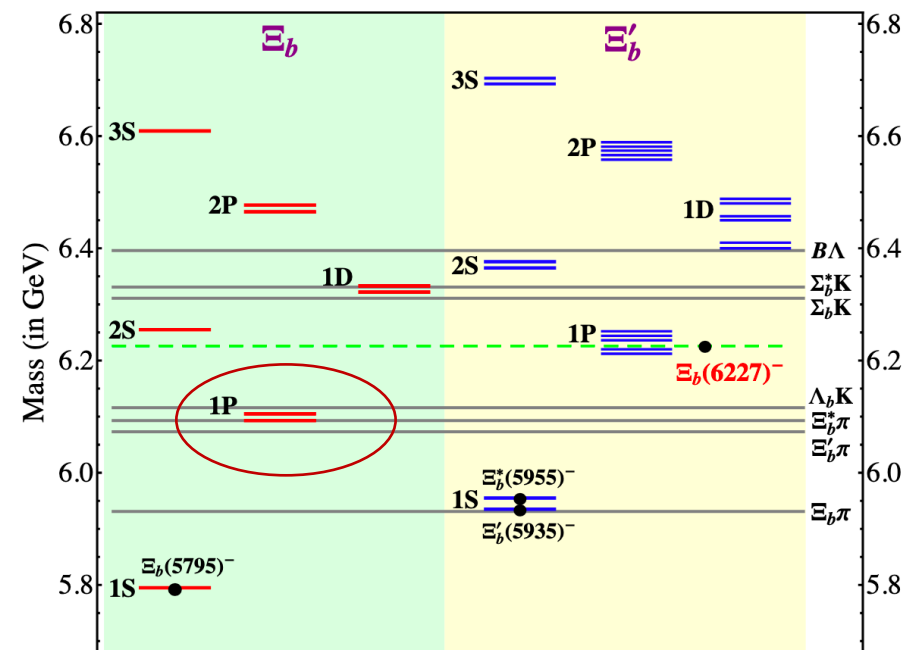
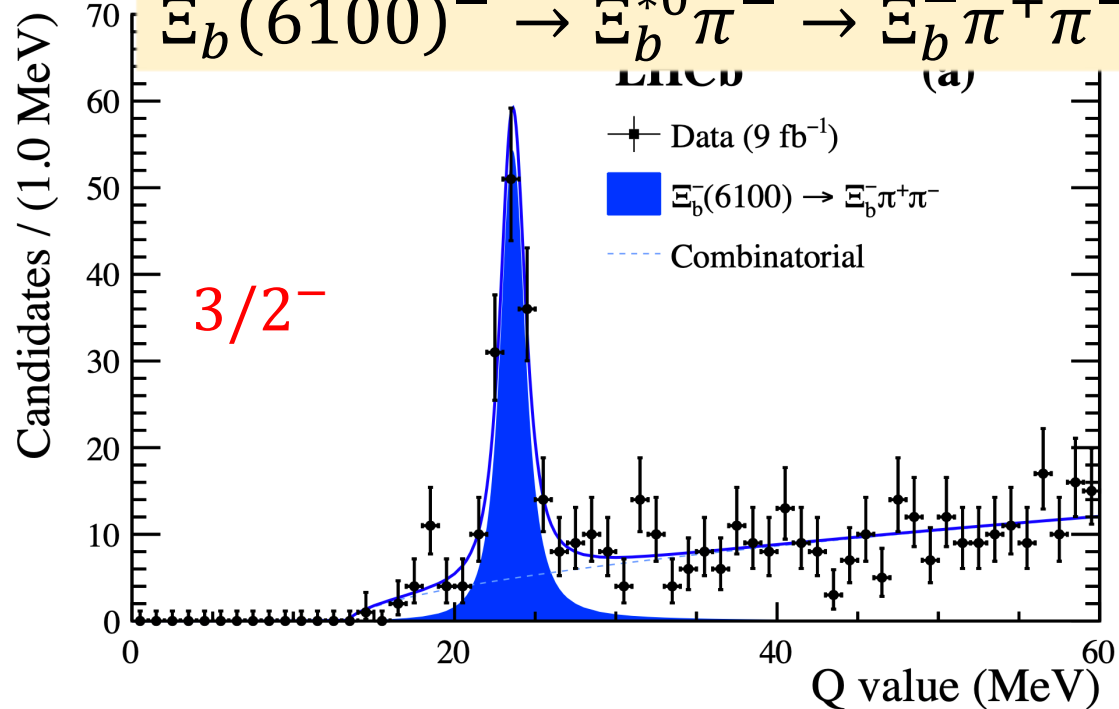
$$\Xi_b(6087)^0 \rightarrow \Xi_b'^- \pi^+ \rightarrow \Xi_b^0 \pi^+ \pi^-$$



$$\Xi_b(6095)^0 \rightarrow \Xi_b^{*-} \pi^+ \rightarrow \Xi_b^0 \pi^+ \pi^-$$

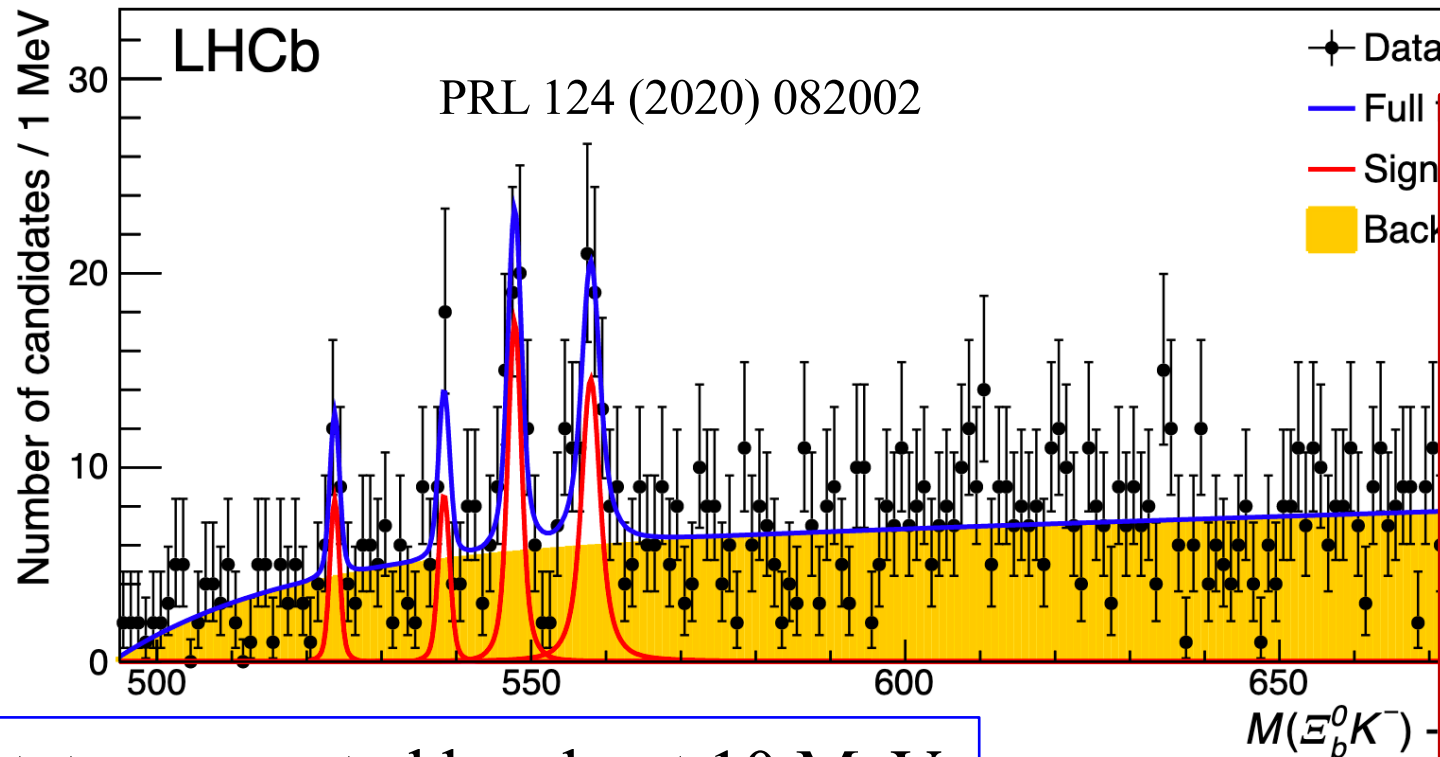


$$\Xi_b(6100)^- \rightarrow \Xi_b^{*0} \pi^- \rightarrow \Xi_b^- \pi^+ \pi^-$$



# Excited $\Omega_b^-$ baryons

- $\Omega_b^{*-} \rightarrow \Xi_b^0 K^-$  mass spectrum



Four states separated by about 10 MeV

$$m(\Omega_b(6316)^-) = 6315.64 \pm 0.31 \pm 0.07 \pm 0.50 \text{ MeV } (2.1\sigma)$$

$$\Gamma < 2.8 \text{ MeV}$$

$$m(\Omega_b(6330)^-) = 6330.30 \pm 0.28 \pm 0.07 \pm 0.50 \text{ MeV } (2.6\sigma)$$

$$\Gamma < 3.1 \text{ MeV}$$

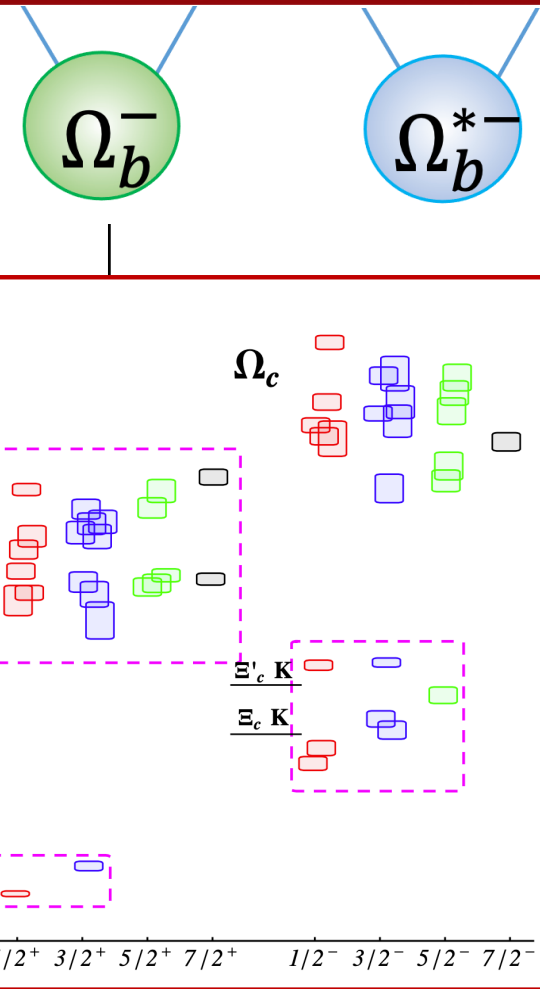
$$m(\Omega_b(6340)^-) = 6339.71 \pm 0.26 \pm 0.05 \pm 0.50 \text{ MeV } (>5\sigma)$$

$$\Gamma < 1.5 \text{ MeV}$$

$$m(\Omega_b(6350)^-) = 6349.88 \pm 0.35 \pm 0.05 \pm 0.50 \text{ MeV } (>5\sigma)$$

$$\Gamma = 1.4_{-0.8}^{+1.0} \pm 0.1 \text{ MeV}$$

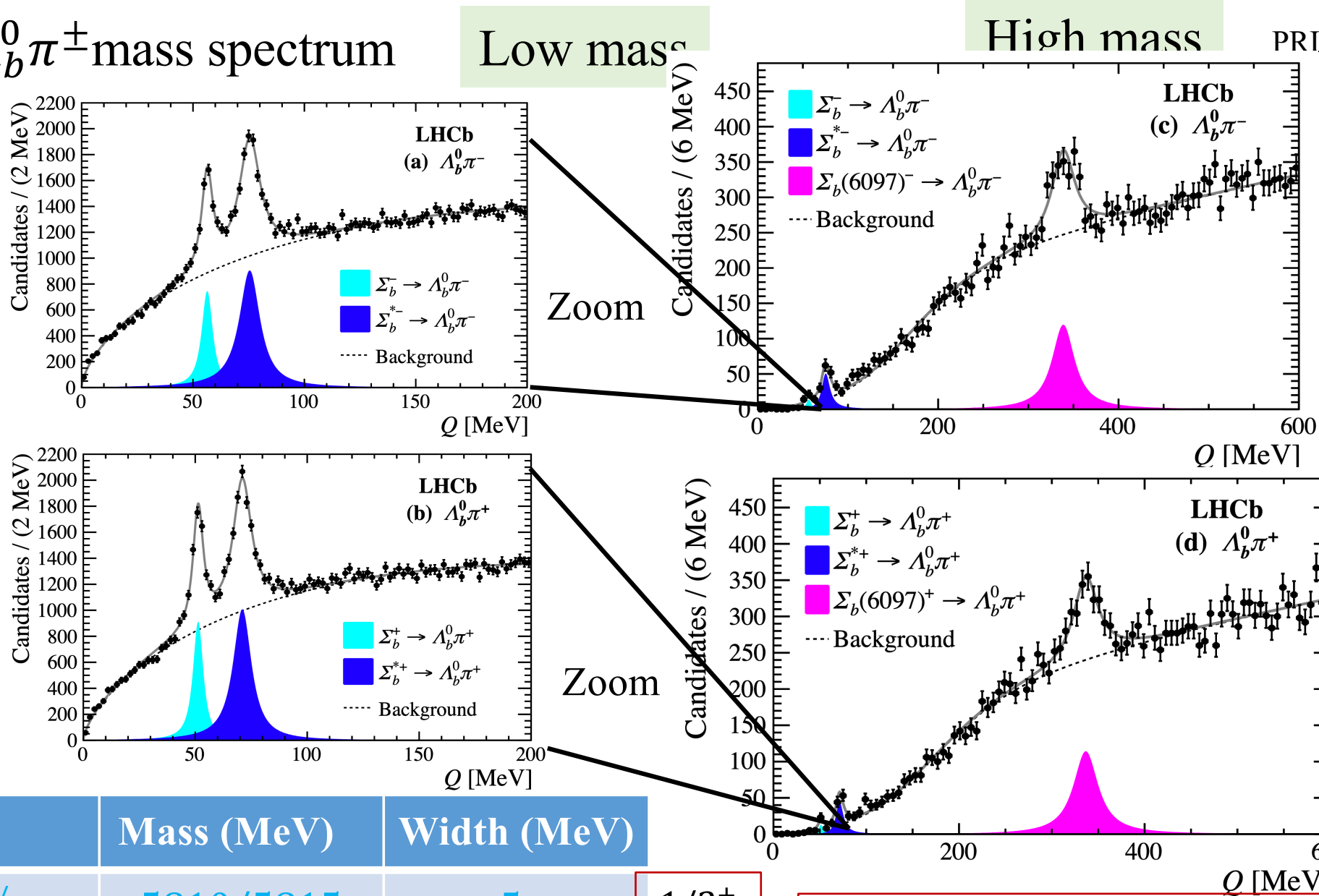
To compare  $m(\Omega_b^-) = 6046.1 \pm 1.7 \text{ MeV}$



# Excited $\Sigma_b^{+/-}$ baryons

- $\Lambda_b^0 \pi^\pm$  mass spectrum

PRL 122 (2019) 012001



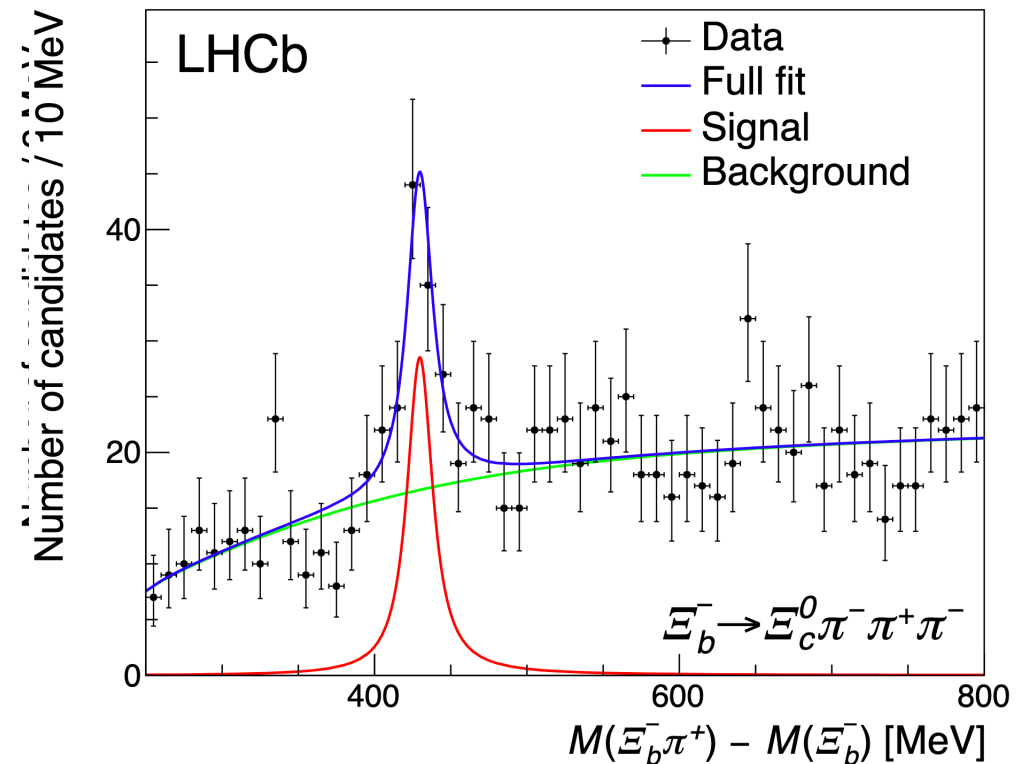
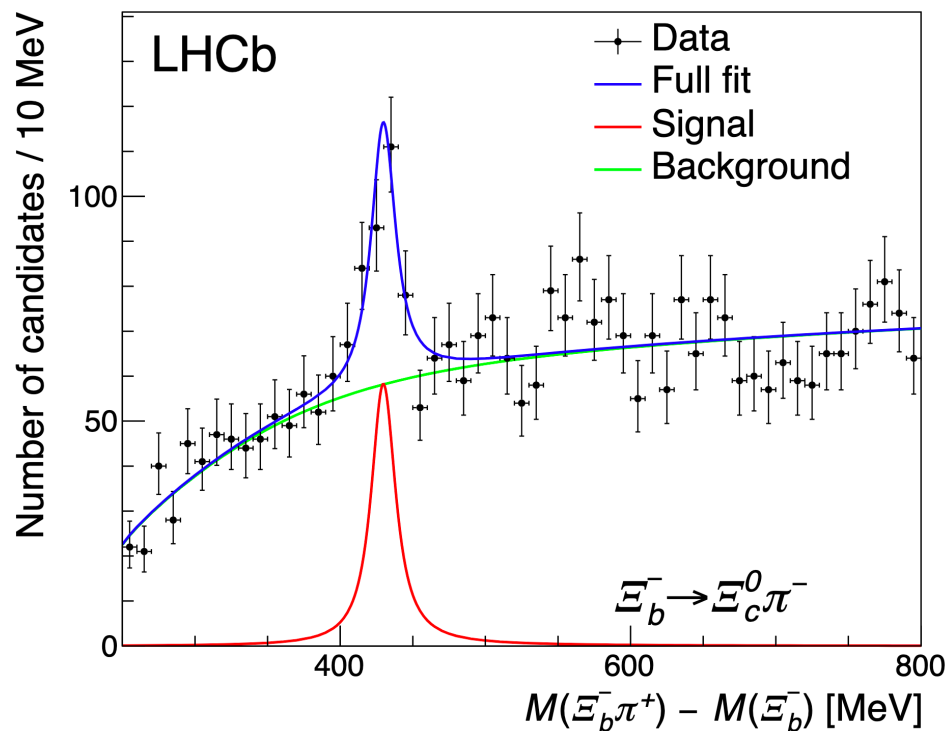
State	Mass (MeV)	Width (MeV)
$\Sigma_b^{+/-}$	5810/5815	5
$\Sigma_b^{*+/-}$	5830/5835	19
$\Sigma_b^{**+/-}$	6098/6096	30

$1/2^+$   
 $3/2^+$

$$m(\Sigma_b^{**}) - m(\Sigma_b) \approx m(\Lambda_b(5920)^0) - m(\Lambda_b^0)$$

Consistent with P-wave. Five states expected. Many states overlaid?

- $\Xi_b^- \pi^+$  mass spectrum



A new state  $\Xi_b(6227)^0$  observed

State	Mass (MeV)	Width (MeV)
$\Xi_b(6227)^0$	$6227.1 \pm 1.5$	$18.6 \pm 4.7$

$$\frac{f_{\Xi_b(6227)^0}}{f_{\Xi_b^-}} \mathcal{B}(\Xi_b(6227)^0 \rightarrow \Xi_b^- \pi^+) = 0.045 \pm 0.008 \pm 0.004$$

Mass and width consistent with  $\Xi_b(6227)^-$

# Excited $\Omega_b^-$ baryons: matching

- Five 1P states with one state not detected  $\left(\frac{1}{2}\right)^-, \left(\frac{1}{2}\right)^-, \left(\frac{3}{2}\right)^-, \left(\frac{3}{2}\right)^-, \left(\frac{5}{2}\right)^-$

States	Ref.1	Ref.2	Ref.3	Ref.4	Ref.5	Ref.6	Ref.7
$\Omega_b(6316)^-$	$\frac{1}{2}^-$	$\frac{1}{2}^-$ or $\frac{3}{2}^-$	$\frac{3}{2}^-$	$\frac{1}{2}^-$	$\frac{3}{2}^-$	$\frac{1}{2}^-$	$\frac{1}{2}^-$ or $\frac{3}{2}^-$
$\Omega_b(6330)^-$	$\frac{1}{2}^-$	$\frac{1}{2}^-$ or $\frac{3}{2}^-$	$\frac{1}{2}^-$	$\frac{3}{2}^-$	$\frac{1}{2}^-$	$\frac{3}{2}^-$	$\frac{1}{2}^-$
$\Omega_b(6340)^-$	$\frac{3}{2}^-$	$\frac{3}{2}^-$ or $\frac{5}{2}^-$	$\frac{3}{2}^-$	$\frac{1}{2}^-$	$\frac{5}{2}^-$	$\frac{3}{2}^-$	$\frac{3}{2}^-$
$\Omega_b(6350)^-$	$\frac{3}{2}^-$	$\frac{1}{2}^-$ or $\frac{5}{2}^-$	$\frac{3}{2}^-$	$\frac{3}{2}^-$	$\frac{3}{2}^-$	$\frac{5}{2}^-$	$\frac{3}{2}^-$

1. PRD 102 (2020) 014207
2. EPJC 80 (2020) 279
3. arXiv:2010.10697
4. J. Phys. Conf. Ser. 1610 (2020) 012011
5. IJMPA 35 (2020) 2050043
6. EPJC 80 (2020) 198
7. PRD 101 (2020) 114013

- Baryon-meson molecule? Thresholds far away.

Main channel	$\Xi'_b \bar{K}$	$\Xi_b^* \bar{K}$	$\Xi \bar{B}$	$\Xi \bar{B}^*$
Threshold mass	6431	6451	6598	6643

# Study of $B^0 \rightarrow \bar{D}^0 D_S^+ \pi^-$ and $B^+ \rightarrow D^- D_S^+ \pi^+$

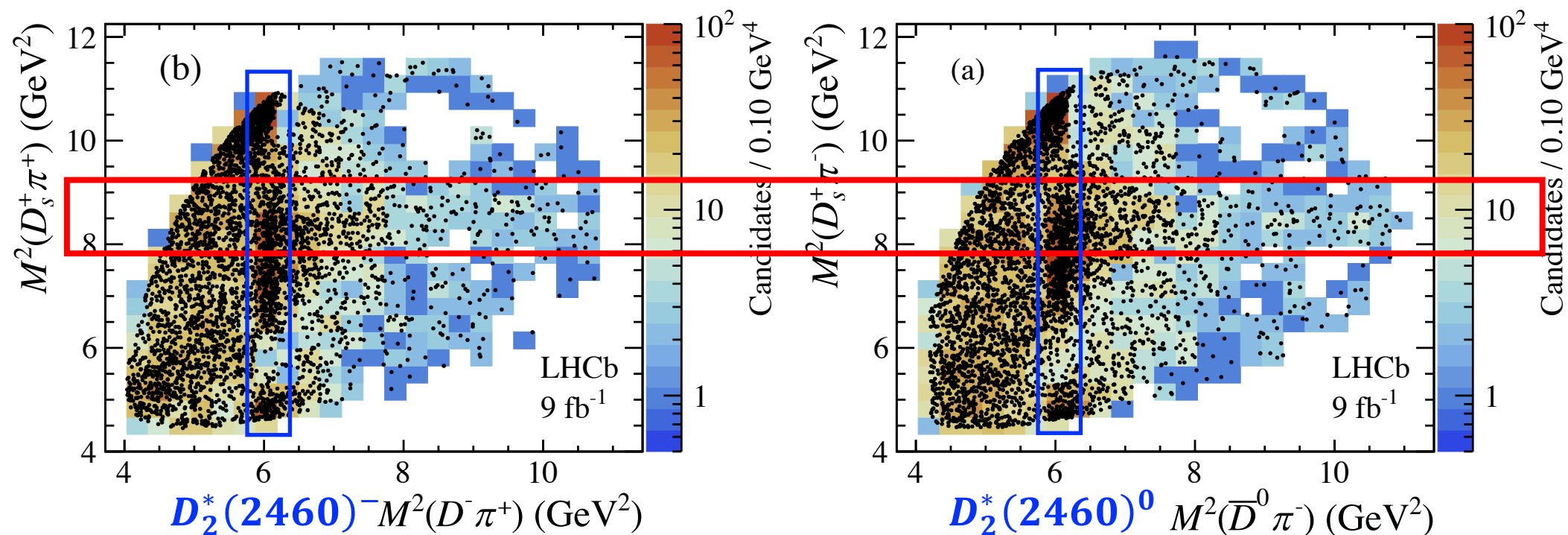
LHCb-PAPER-2022-026

LHCb-PAPER-2022-027

- Full  $9 \text{ fb}^{-1}$  Run1+Run2 LHCb data

$\Rightarrow$  **4420**  $B^0 \rightarrow \bar{D}^0 D_S^+ \pi^-$  candidates with signal purity of **90.7%**

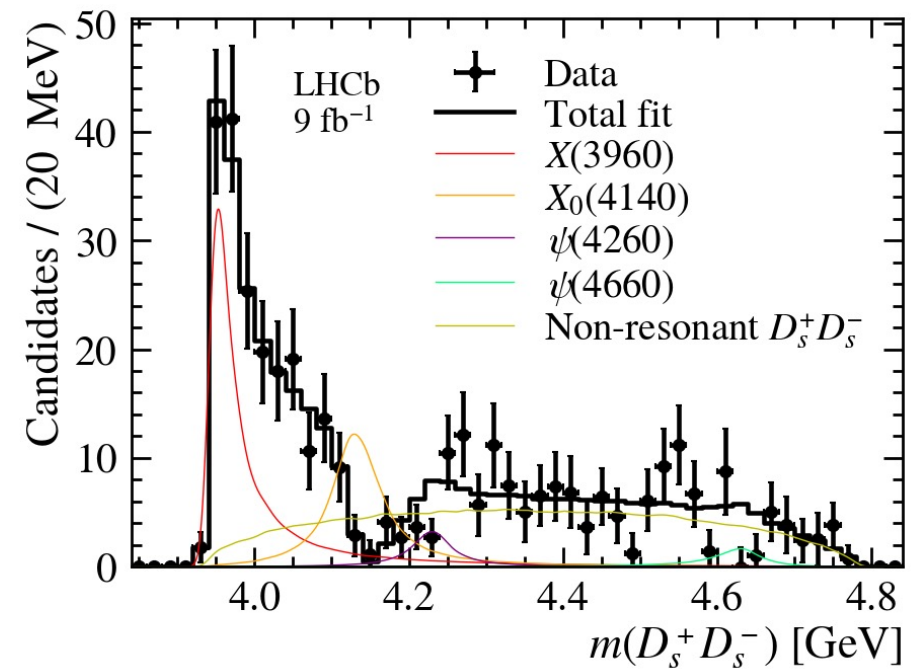
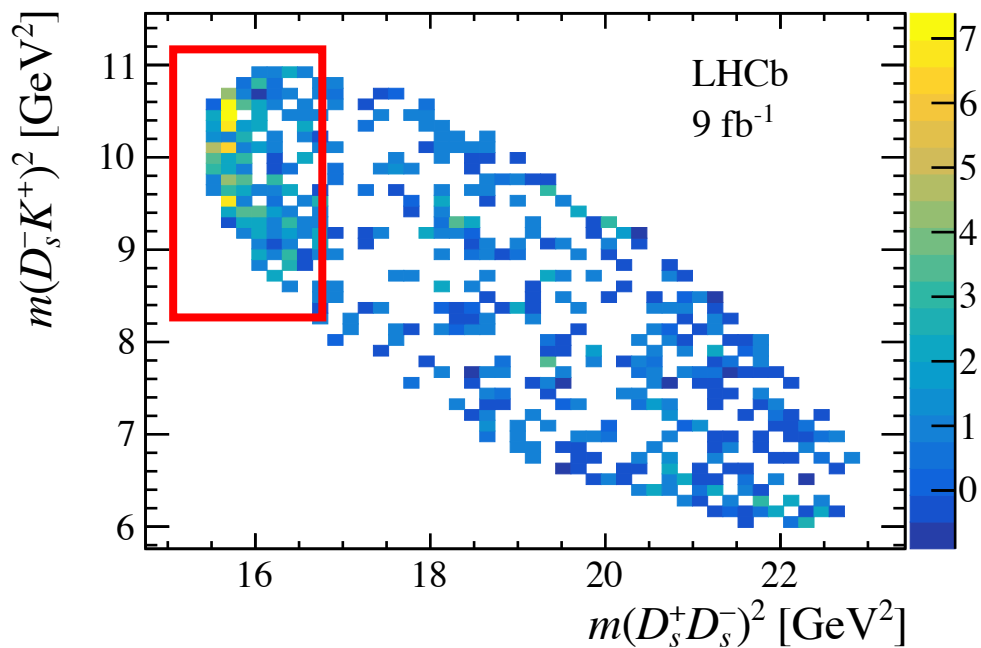
**3940**  $B^+ \rightarrow D^- D_S^+ \pi^+$  candidates with signal purity of **95.2%**



✓ Faint horizontal band at  $M^2(D_S^+ \pi) \approx 8.5 \text{ GeV}^2$  indicating  $T_{c\bar{s}}$  candidates

$\Rightarrow$  **Joint amplitude analysis** where amplitudes of the two decays are related through **isospin symmetry**

- Threshold enhancement in  $B^+ \rightarrow D_s^+ D_s^- K^+$ , described by  $X(3960) \rightarrow D_s^+ D_s^-$ 
  - $J^{PC} = 0^{++}$  preferred
- Dip at  $m(D_s^+ D_s^-) \sim 4.15$  GeV with  $X_0(4140)$  or  $J/\psi\phi \rightarrow D_s^+ D_s^-$  scattering



- $X_0(3930)$  versus  $X_0(3960)$

The same state:  $\frac{\Gamma(X \rightarrow D^+ D^-)}{\Gamma(X \rightarrow D_s^+ D_s^-)} = 0.29 \pm 0.16$  prefers **genuine  $s\bar{s}$  content inside  $X$**

# Fit parameters

- All states are relatively wide: 50 – 200 MeV

Contribution	Significance [ $\times\sigma$ ]	$M_0$ [MeV]	$\Gamma_0$ [MeV]	FF [%]
$X(2^-)$		<b>New <math>J/\psi\phi</math></b>		
$X(4150)$	4.8 (8.7)	$4146 \pm 18 \pm 33$	$135 \pm 28^{+59}_{-30}$	$2.0 \pm 0.5^{+0.8}_{-1.0}$
$X(1^-)$		<b>New <math>J/\psi\phi</math></b>		
$X(4630)$	5.5 (5.7)	$4626 \pm 16^{+18}_{-110}$	$174 \pm 27^{+134}_{-73}$	$2.6 \pm 0.5^{+2.9}_{-1.5}$
All $X(0^+)$				$20 \pm 5^{+14}_{-7}$
$X(4500)$	20 (20)	$4474 \pm 3 \pm 3$	$77 \pm 6^{+10}_{-8}$	$5.6 \pm 0.7^{+2.4}_{-0.6}$
$X(4700)$	17 (18)	$4694 \pm 4^{+16}_{-3}$	$87 \pm 8^{+16}_{-6}$	$8.9 \pm 1.2^{+4.9}_{-1.4}$
$\text{NR}_{J/\psi\phi}$	4.8 (5.7)			$28 \pm 8^{+19}_{-11}$
All $X(1^+)$		<b>Large width</b>		$26 \pm 3^{+8}_{-10}$
$X(4140)$	13 (16)	$4118 \pm 11^{+19}_{-36}$	$162 \pm 21^{+24}_{-49}$	$17 \pm 3^{+19}_{-6}$
$X(4274)$	18 (18)	$4294 \pm 4^{+3}_{-6}$	$53 \pm 5 \pm 5$	$2.8 \pm 0.5^{+0.8}_{-0.4}$
<b>New <math>J/\psi\phi</math></b> $X(4685)$	15 (15)	$4684 \pm 7^{+13}_{-16}$	$126 \pm 15^{+37}_{-41}$	$7.2 \pm 1.0^{+4.0}_{-2.0}$
All $Z_{cs}(1^+)$				$25 \pm 5^{+11}_{-12}$
$Z_{cs}(4000)$	15 (16)	$4003 \pm 6^{+4}_{-14}$	$131 \pm 15 \pm 26$	$9.4 \pm 2.1 \pm 3.4$
$Z_{cs}(4220)$	5.9 (8.4)	$4216 \pm 24^{+43}_{-30}$	$233 \pm 52^{+97}_{-73}$	$10 \pm 4^{+10}_{-7}$

**New  $Z_{cs}^+$  states: width inconsistent with  $Z_{cs}(3985)^+$  at BESIII. Different state!**



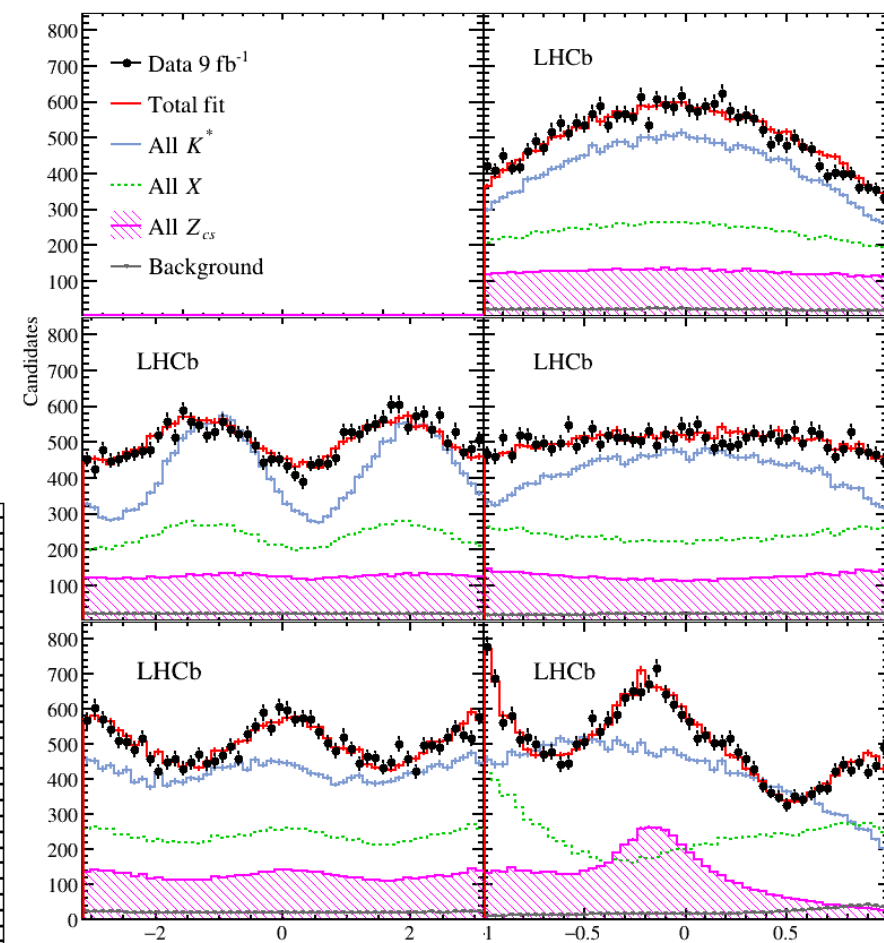
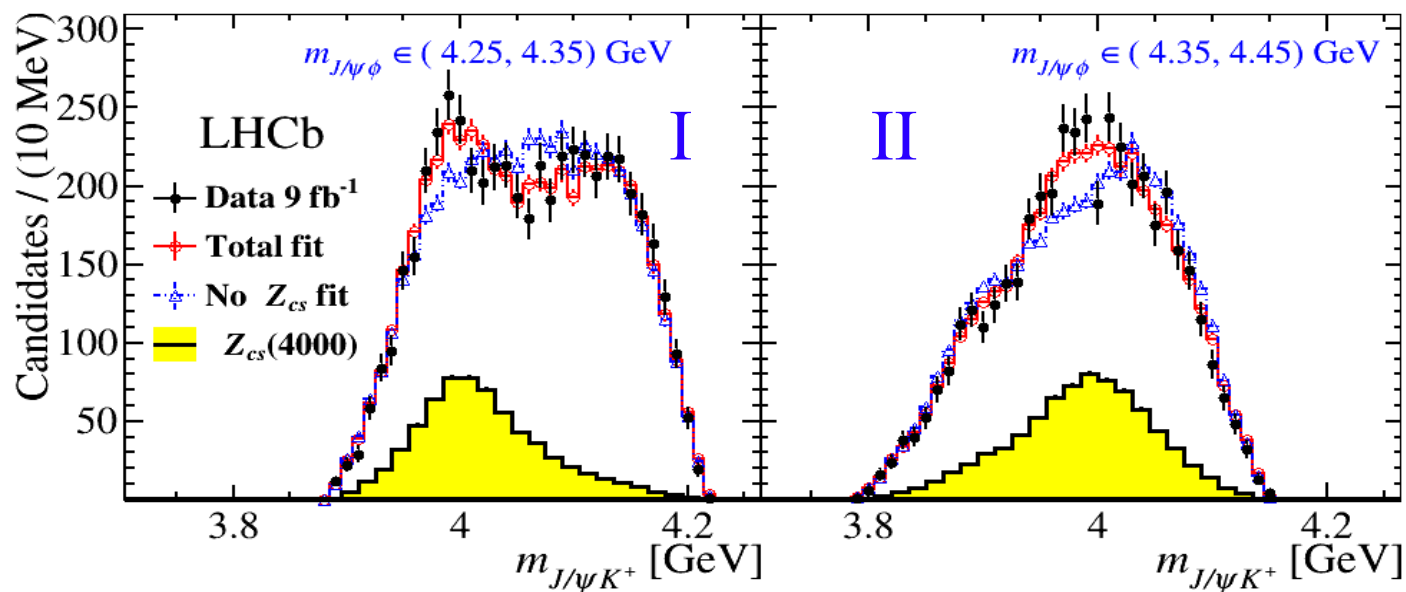
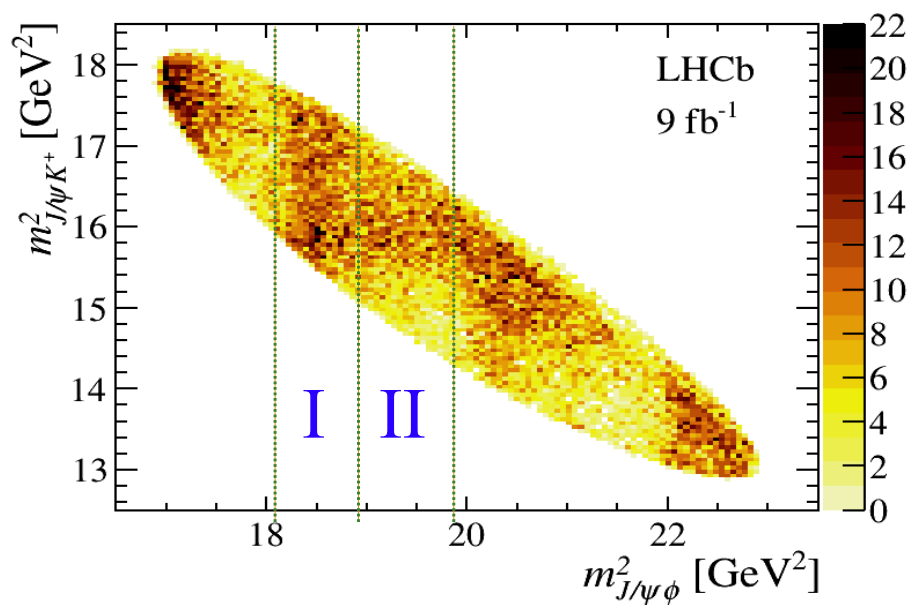
# Fit projections

- $Z_{CS}^+$  essential to describe data

arXiv:2103.01803



All angular distribution well modelled



Angles in  $B^+ \rightarrow J/\psi K^*$  chain

# $J^P$ analysis

- All  $X$  have  $C = 1$

$L = 0$  for  $J/\psi\phi$  system

$J^P$	$0^{++}$	$0^{-+}$	$1^{++}$	$1^{-+}$	Exotic $2^{++}$	$2^{-+}$
$X(4630)$	$6.7\sigma$	$5.3\sigma$	$5.8\sigma$	Prefer	$5.9\sigma$	<b><math>3.0\sigma</math></b>
$X(4500)$	Prefer	$18\sigma$	$18\sigma$	$18\sigma$	$18\sigma$	$18\sigma$
$X(4700)$	Prefer	$18\sigma$	$18\sigma$	$18\sigma$	$14\sigma$	$17\sigma$
$X(4140)$	$14\sigma$	$15\sigma$	Prefer	$14\sigma$	$13\sigma$	$14\sigma$
$X(4274)$	$18\sigma$	$18\sigma$	Prefer	$18\sigma$	$18\sigma$	$18\sigma$
$X(4685)$	$16\sigma$	$16\sigma$	Prefer	$15\sigma$	$16\sigma$	$15\sigma$
$Z_{cs}(4000)$	-	$17\sigma$	Prefer	$17\sigma$	$15\sigma$	$16\sigma$
$Z_{cs}(4220)$	-	$8.6\sigma$	Prefer	<b><math>2.4\sigma</math></b>	$4.9\sigma$	$5.7\sigma$

Same as  $Z_c(4430)^+$ ,  $Z_c(4200)^+$ ,  $Z_c(3900)^+$ ,  $L = 0$  for  $\psi\pi^+$  system

# Interpretations

- Some  $X \rightarrow J/\psi\phi$  may be  $D_s^{(*)}\bar{D}^{(*)}_s$  molecular states ?

States	$J^{PC}$	Mass	Width	Nearest thresholds/MeV	S-wave
X(4140)	$1^{++}$	4118	162	$D_s^+ D_s^{*-}$ : 4080	$J^P = 1^+$
X(4150)	$2^{-+}$	4146	135	$D_s^+ D_s^{*-}$ : 4080	$J^P = 1^+$
X(4274)	$1^{++}$	4294	53	$D_s^+ D_{s0}^{*-}(2317)^-$ : 4286	$J^P = 0^-$
X(4500)	$0^{++}$	4474	77	$D_s^+ D_{s1}^{*-}(2536)^-$ : 4503	$J^P = 1^-$
X(4630)	$1^{-+}$	4626	174	$D_s^{*-} D_{s1}^{*-}(2536)^-$ : 4636	$J^P = J^-$
X(4685)	$1^{++}$	4684	126	$D_s^{*+} D_{s2}^{*-}(2573)^-$ : 4681	$J^P = J^-$
X(4700)	$0^{++}$	4694	87	$D_s^{*+} \bar{D}_{s2}^{*-}(2573)^-$ : 4681	$J^P = J^-$

Can't rule out conventional charmonia either,  $c\bar{c} \rightarrow J/\psi\phi$  not forbidden

- $Z_{cS}(4000)^+$  and  $Z_{cS}(4220)^+$ :

May be SU(3) flavor partners of  $Z_c(3900)^+$  and  $Z_c(4020)^+$ ,  
molecular states,  $m_{D^*} + m_{D_s} \sim 4$  GeV

arXiv:2011.08725

arXiv:2103.08331

# Other models

- I. One BW for threshold structure + X(6900), w/o interference,  $P(\chi^2) = 1.2\%$
- II. Only one BW, interfering with SPS,  $P(\chi^2) = 2.8\%$
- III. Threshold structure due to feed-down decays of excited charmonia (e.g.  $\chi_{cJ}/\psi$ )
- IV. Including a component for 7.2 GeV peak

Science Bulletin 65 (2020) 1983

