



# **$B\rho$ -defined Isochronous Mass Spectrometry and Mass Measurements of Short-lived Nuclides at CSRe-Lanzhou**

- 1. Principle of  $B\rho$ -defined IMS**
- 2. Velocity determination with two TOF detectors**
- 3. Realization of  $B\rho$ -defined IMS**
- 4. New masses from the  $B\rho$ -defined IMS**
- 5. Summary**

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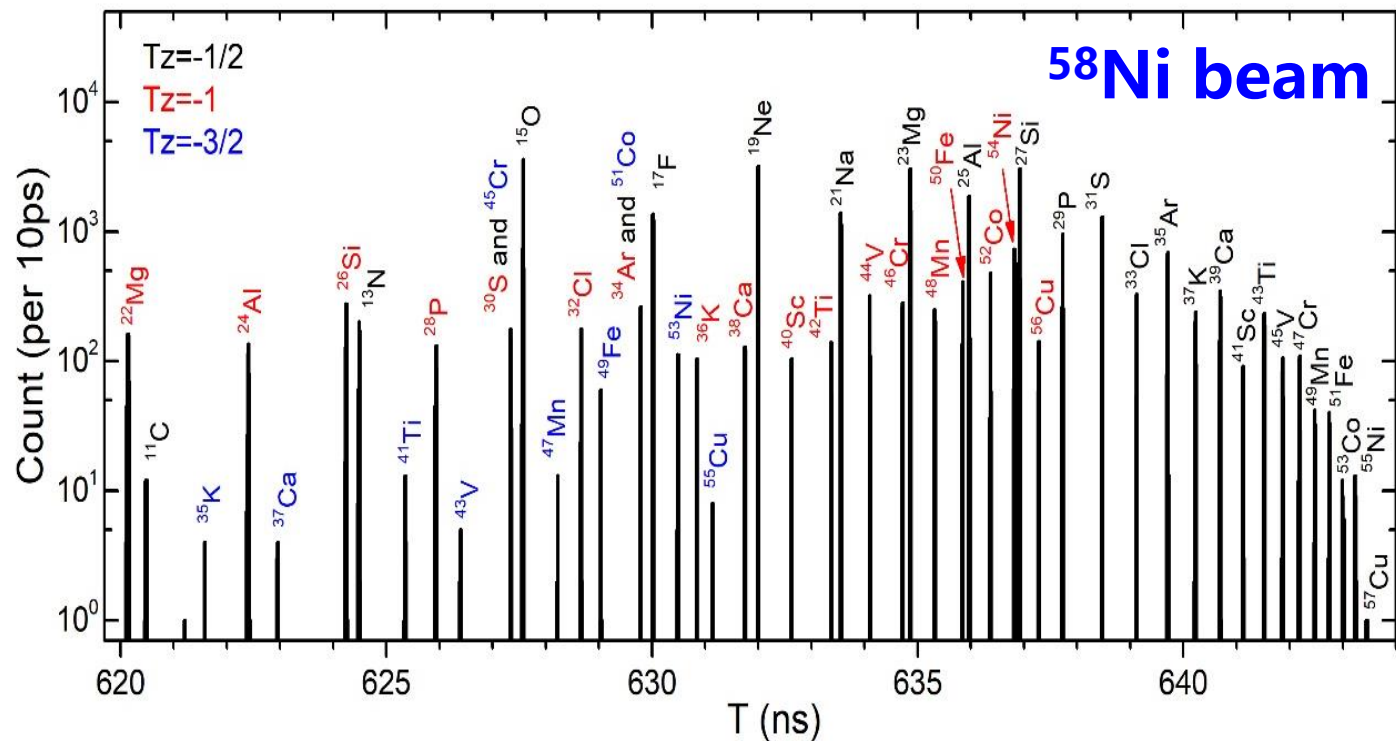
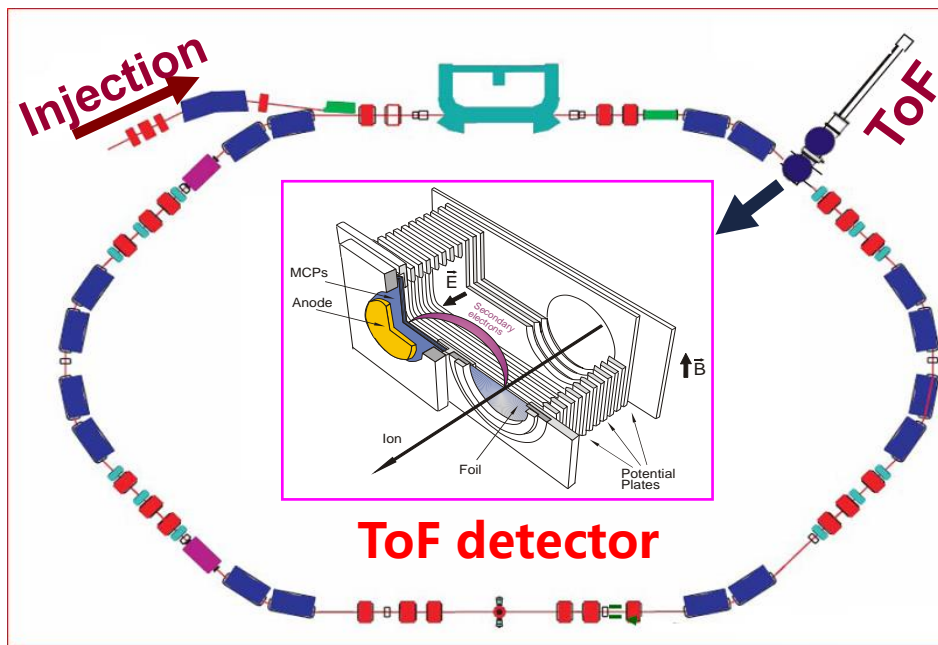
# 1. Principle of $B\rho$ -defined IMS

## Conventional IMS ( $\gamma = \gamma_t$ )

$$\frac{\Delta T}{T} = \frac{1}{\gamma^2} \frac{\Delta(m/q)}{m/q} + \left( \frac{1}{\gamma_t^2} - \frac{1}{\gamma^2} \right) \frac{\Delta(B\rho)}{B\rho}$$

$$\gamma_t^{-2} = \frac{dC/C}{d(B\rho)/(B\rho)}$$

$\gamma_t$ : machine parameter determined by beam optics

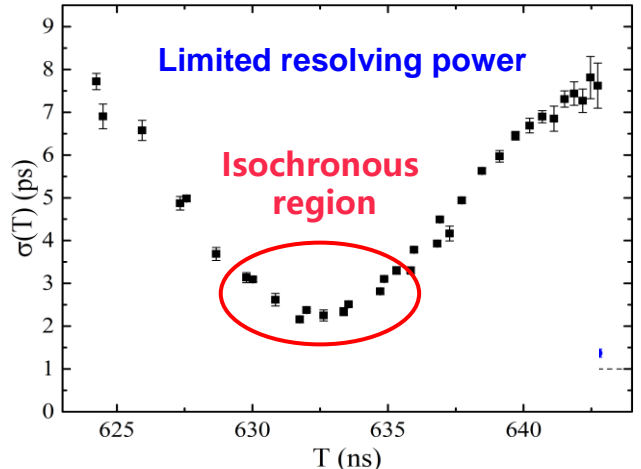


# 1. Principle of $B\rho$ -defined IMS

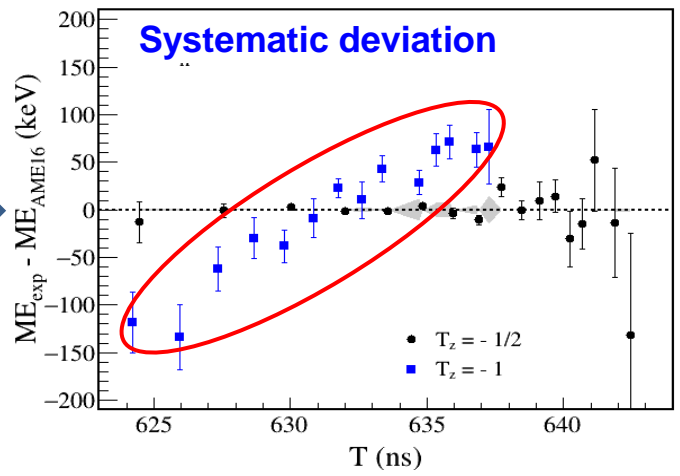
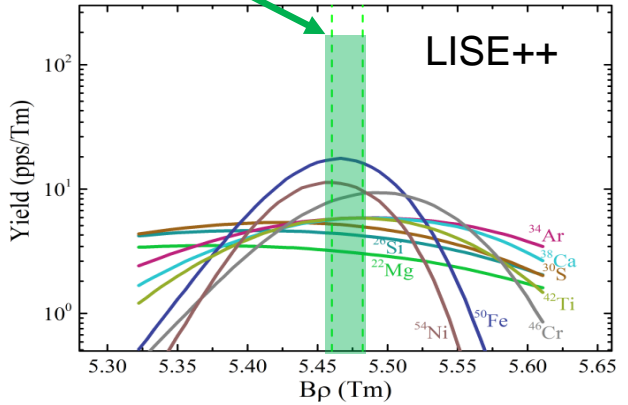
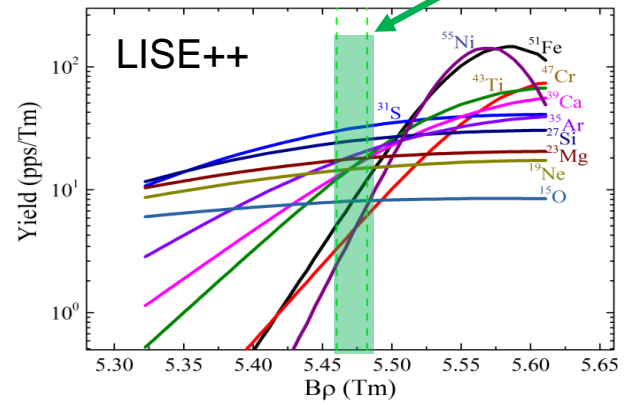
## Limitation of conventional IMS

- 1) Phase slip factor:  $\frac{\delta T}{T} = \left( \frac{1}{\gamma_t^2} - \frac{1}{\gamma^2} \right) \cdot \frac{\delta(B\rho)}{B\rho}$
- 2) Orbit-dependent  $\gamma_t$
- 3) Asymmetric momentum distribution of stored ions
- 4) Energy losses of stored ions

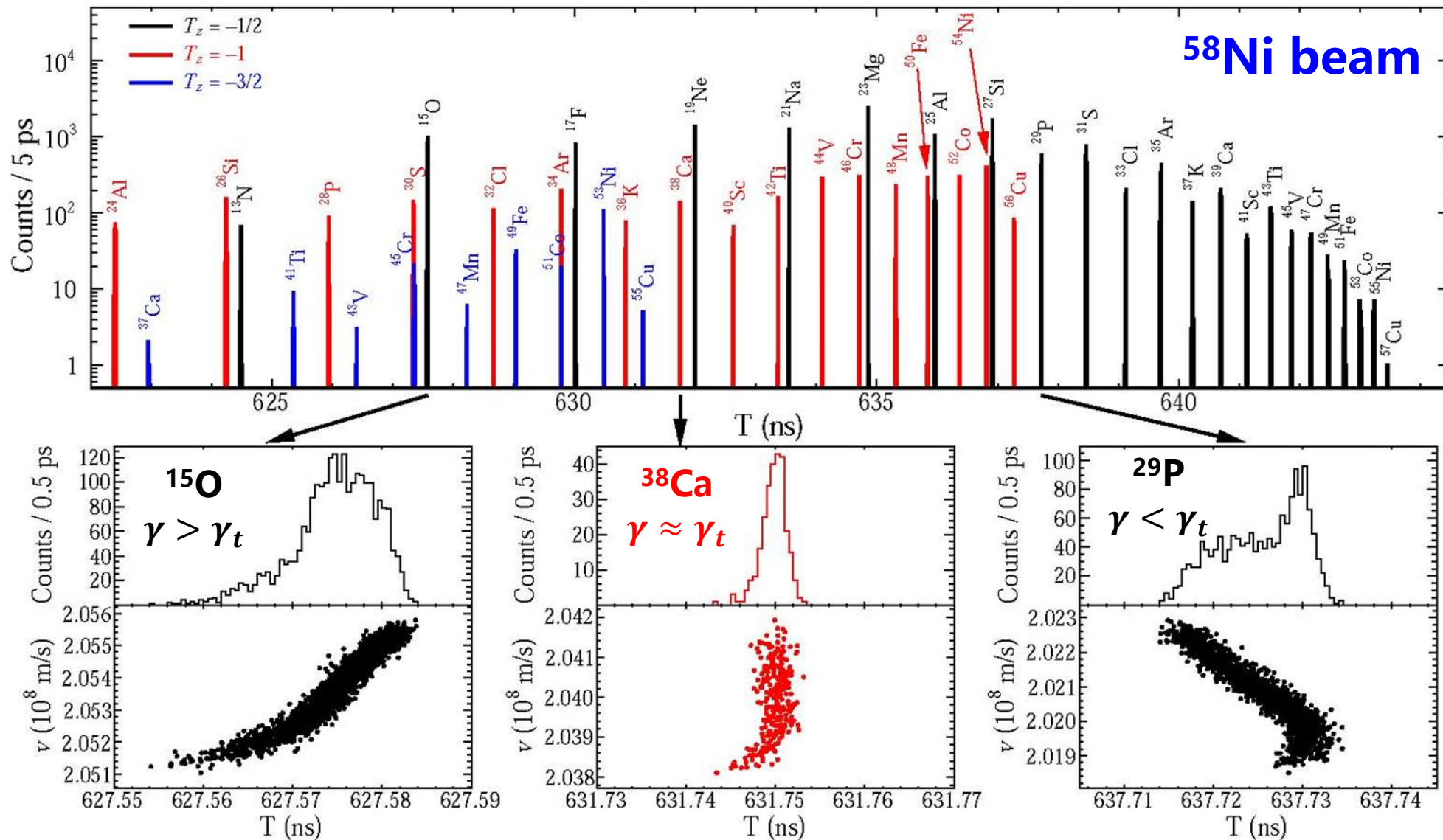
**$^{58}\text{Ni}$  beam**



**$B\rho$  acceptance**

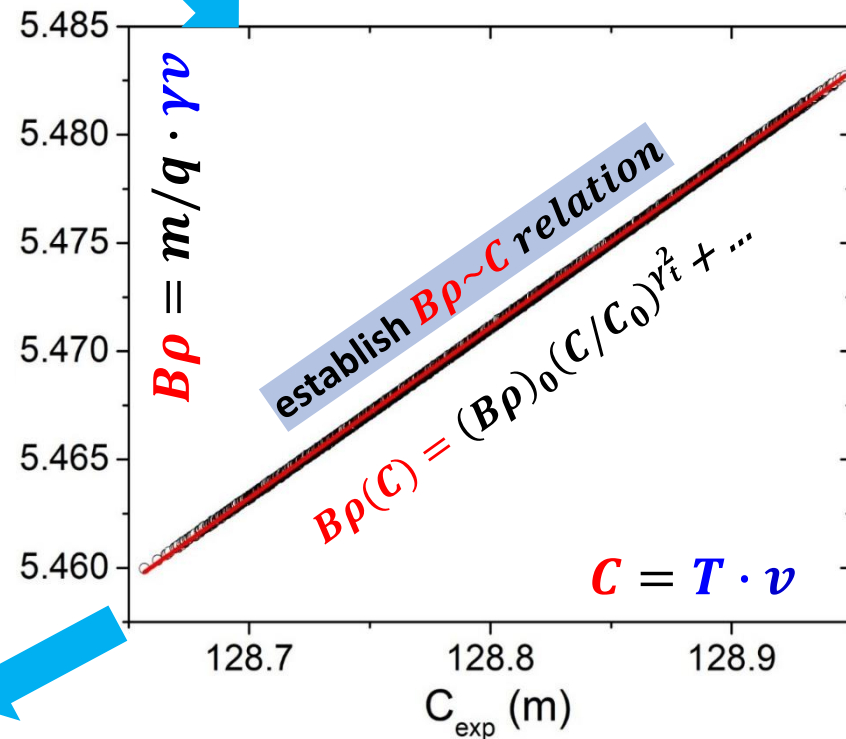
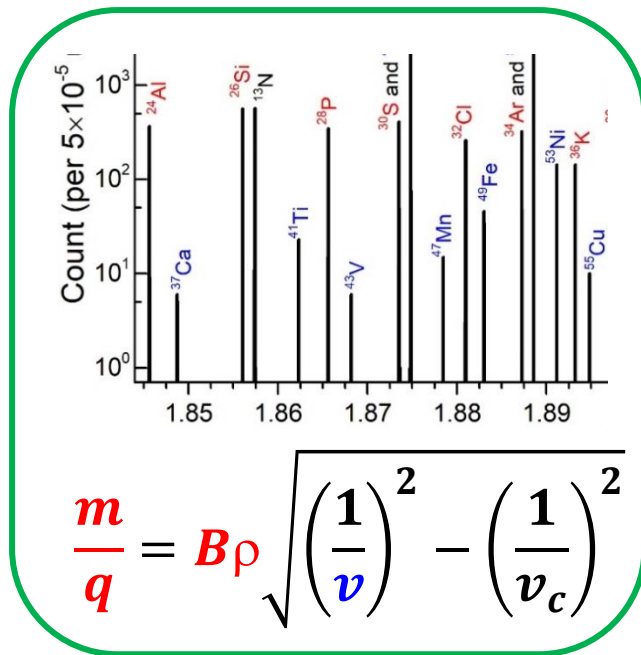
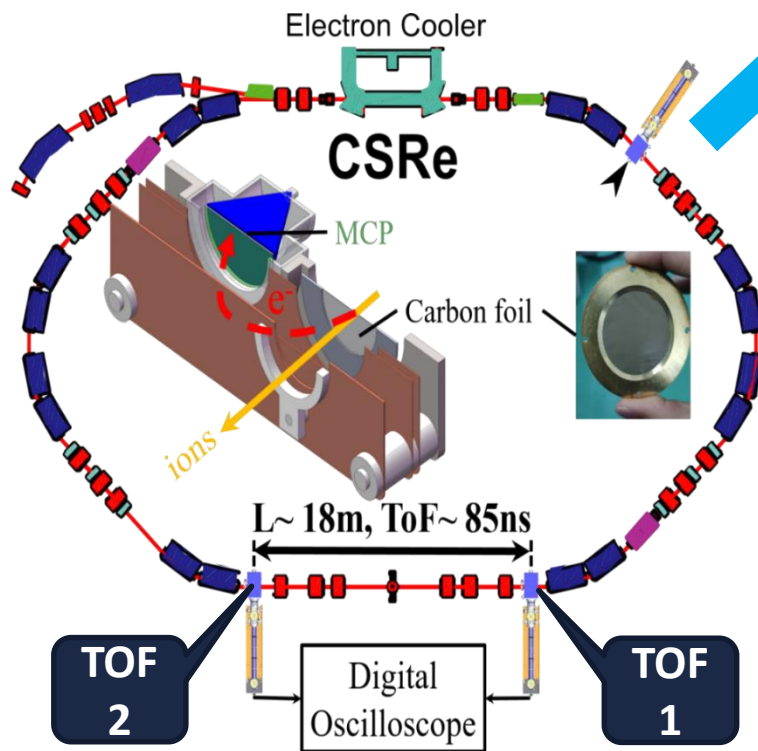


# 1. Principle of $B_{\rho}$ -defined IMS



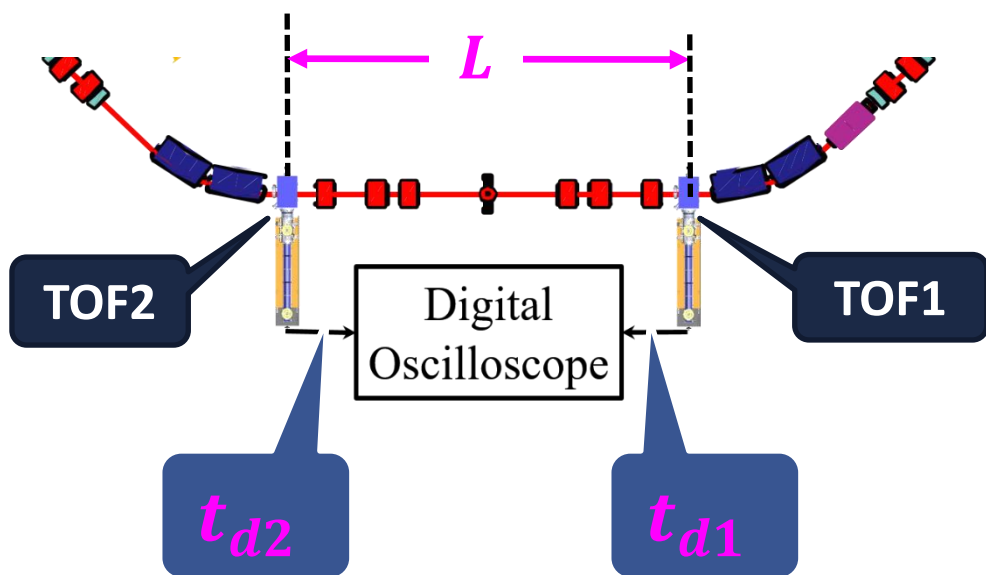
# 1. Principle of $B\rho$ -defined IMS

From  $\left\{ T, v, \frac{m}{q} \right\}$ ,  $\rightarrow B\rho, C$



# 1. Principle of $B\rho$ -defined IMS

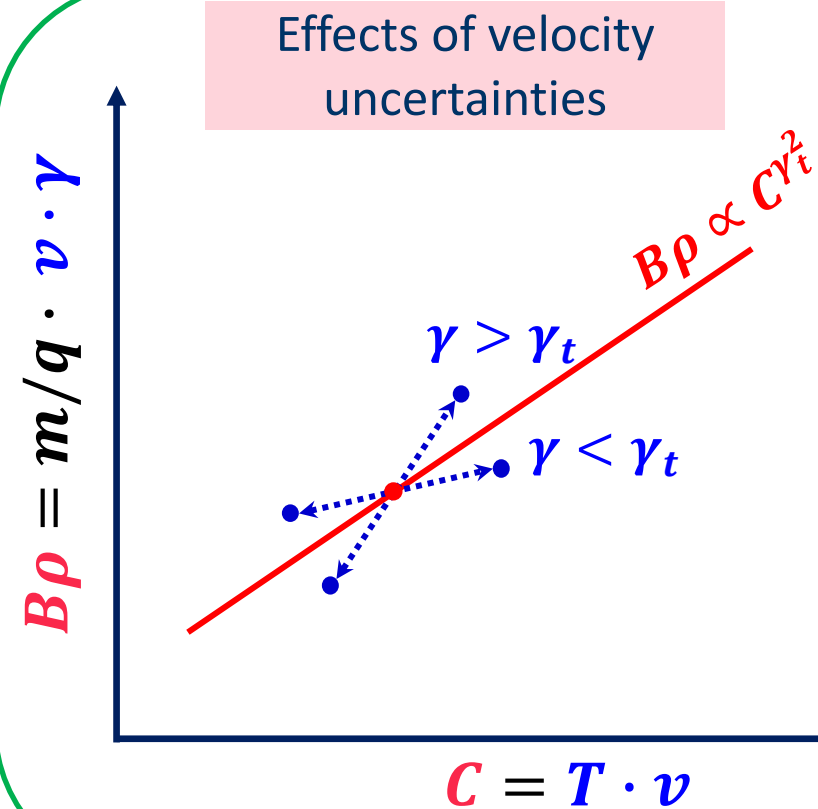
Accuracy of velocity determination is of top importance



$$v = \frac{L}{\Delta t_{ion}} = \frac{L}{\Delta t_{exp} - \Delta t_d}$$

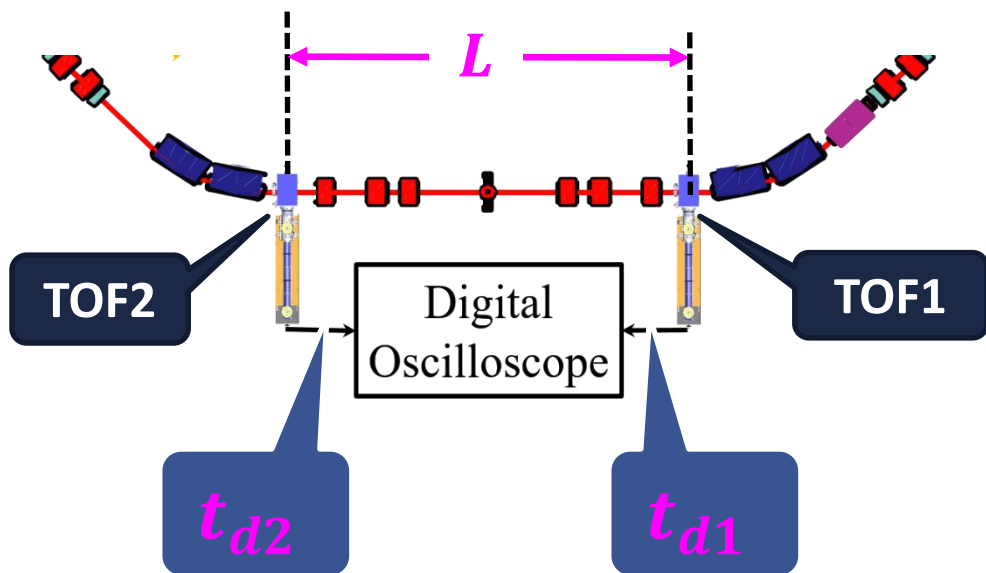
$$L = 18034(1.3) \text{ mm}$$

$$\Delta t_d = 99(4) \text{ ps}$$



# 1. Principle of $B\rho$ -defined IMS

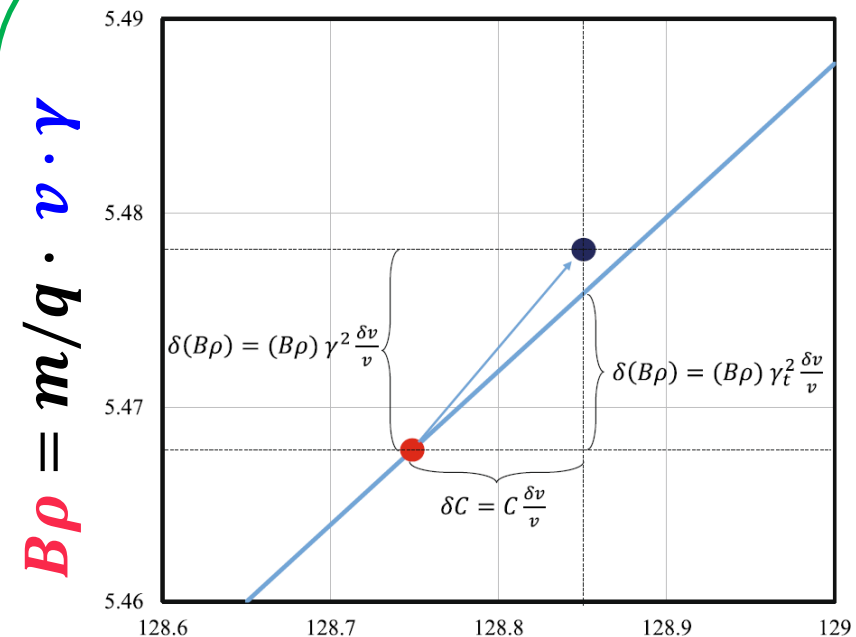
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$$C = T \cdot v$$



# 1. Principle of $B\rho$ -defined IMS

Accuracy of velocity determination is of top importance

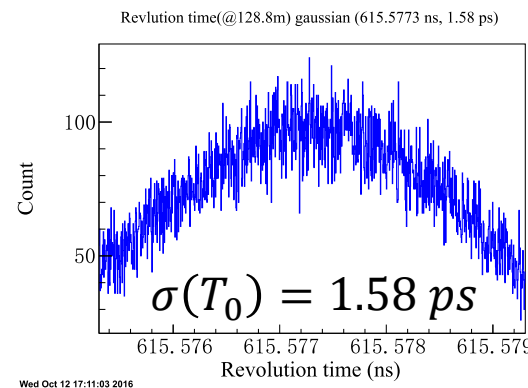
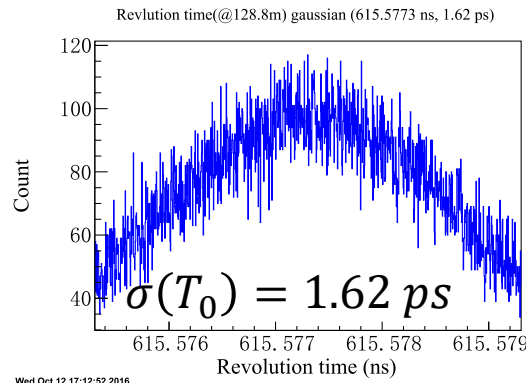
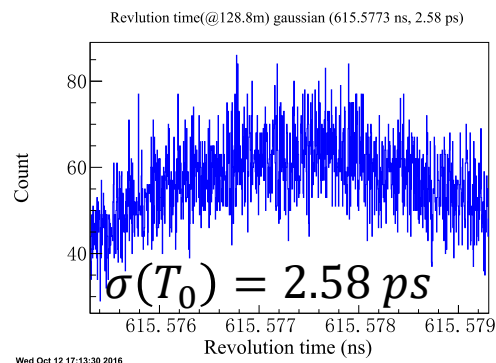
$$\sigma(T_i) = 0 \text{ ps}$$

$$\frac{\sigma(\gamma_t)}{\gamma_t} = 1.0 \times 10^{-3}$$

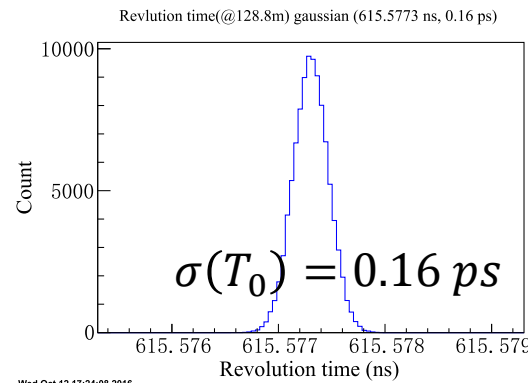
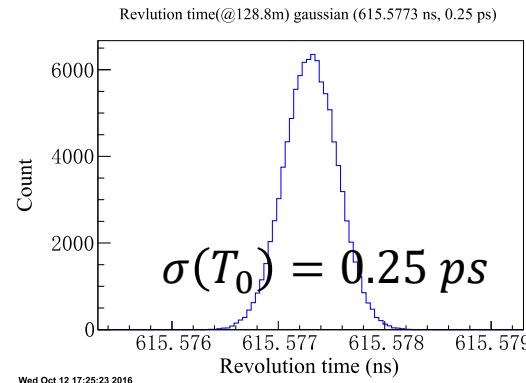
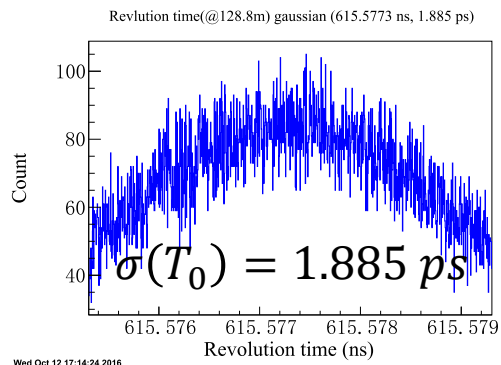
$$\frac{\sigma(v_i)}{v_i} = 1.0 \times 10^{-4}$$

$$1.0 \times 10^{-5}$$

$$1.0 \times 10^{-6}$$



$$1.0 \times 10^{-4}$$

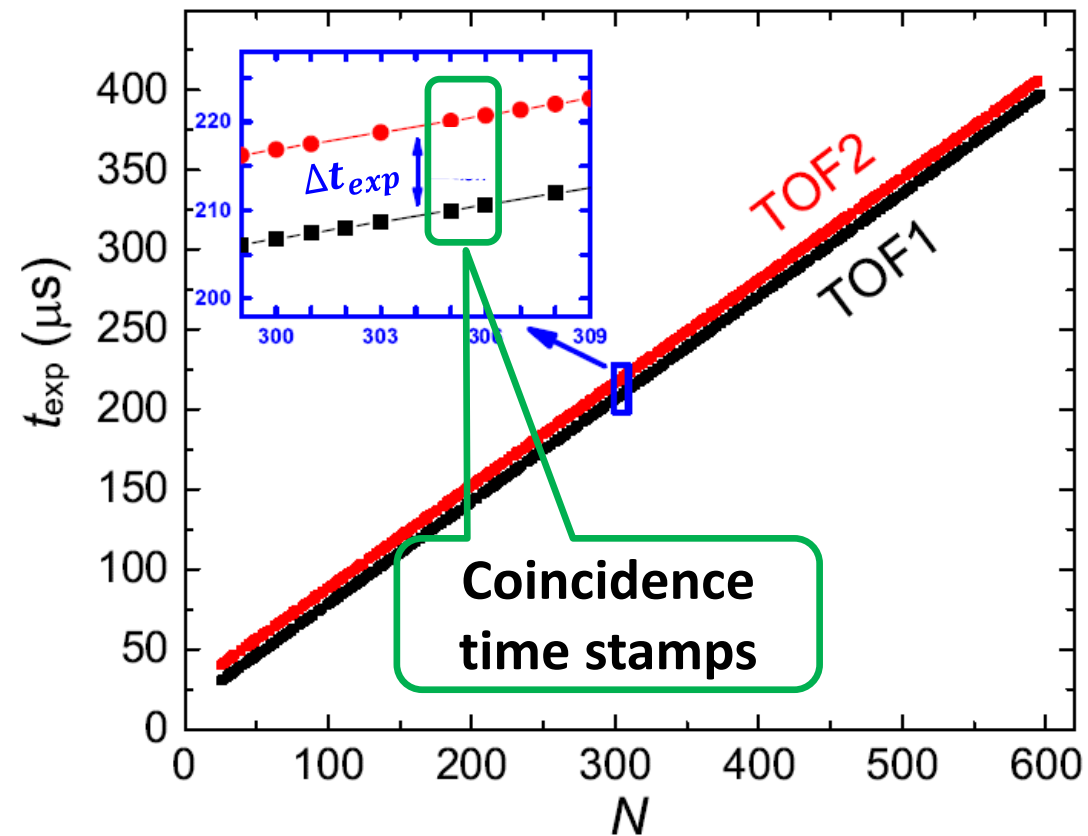
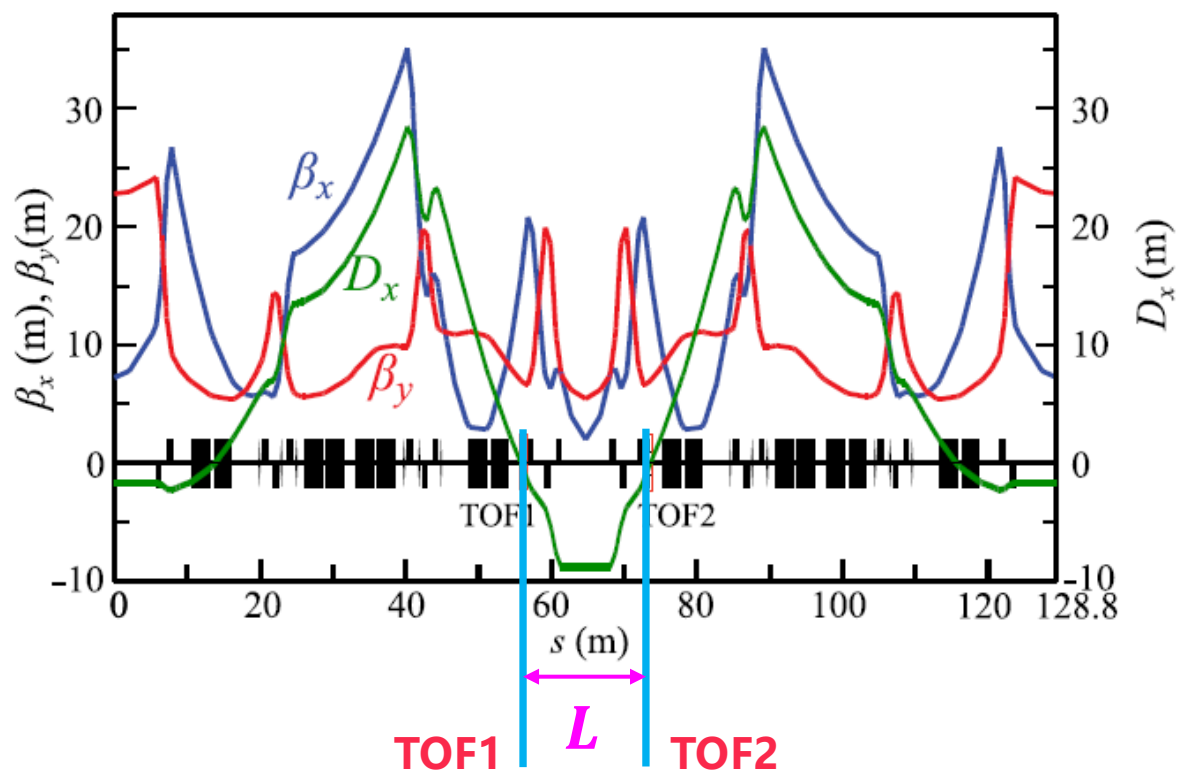




## 2. Velocity determination with two TOF detectors

$\Delta t_{exp}$  determinations  
using coincidence time stamps

$$v = \frac{L}{\Delta t_{exp} - \Delta t_d}$$

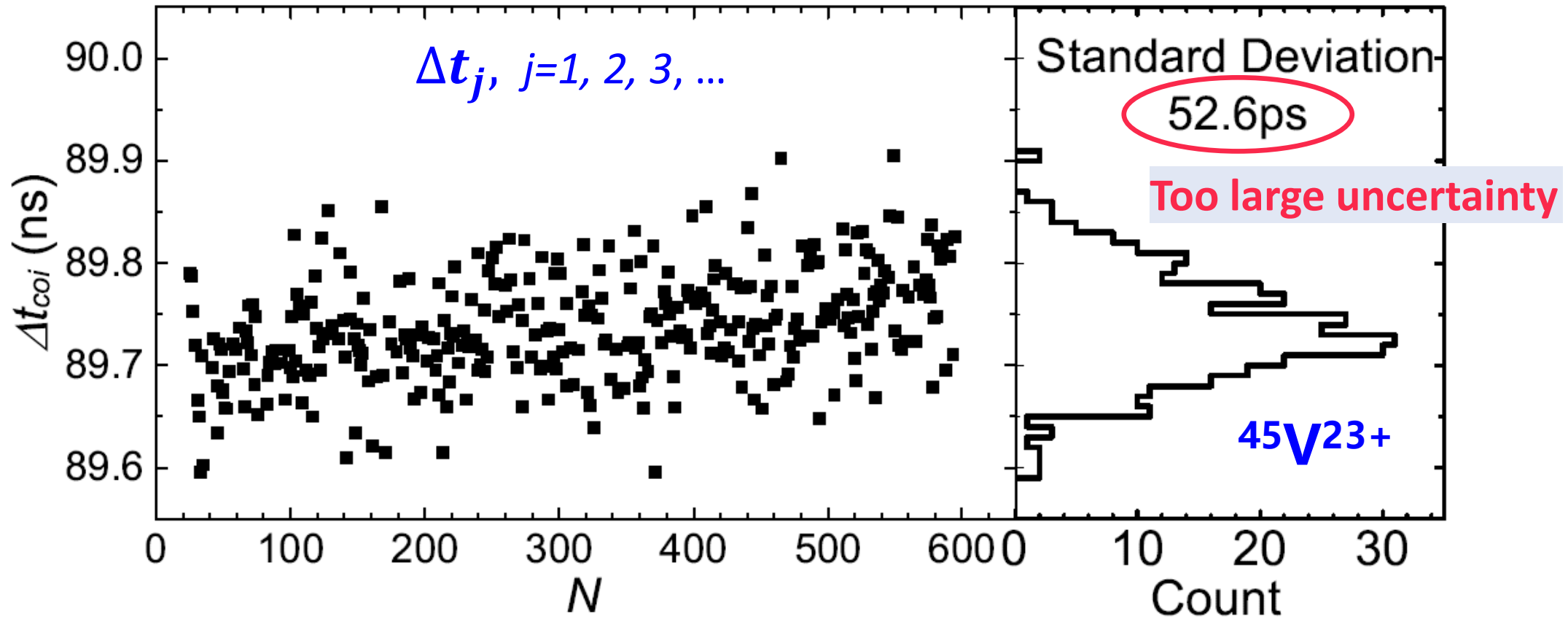




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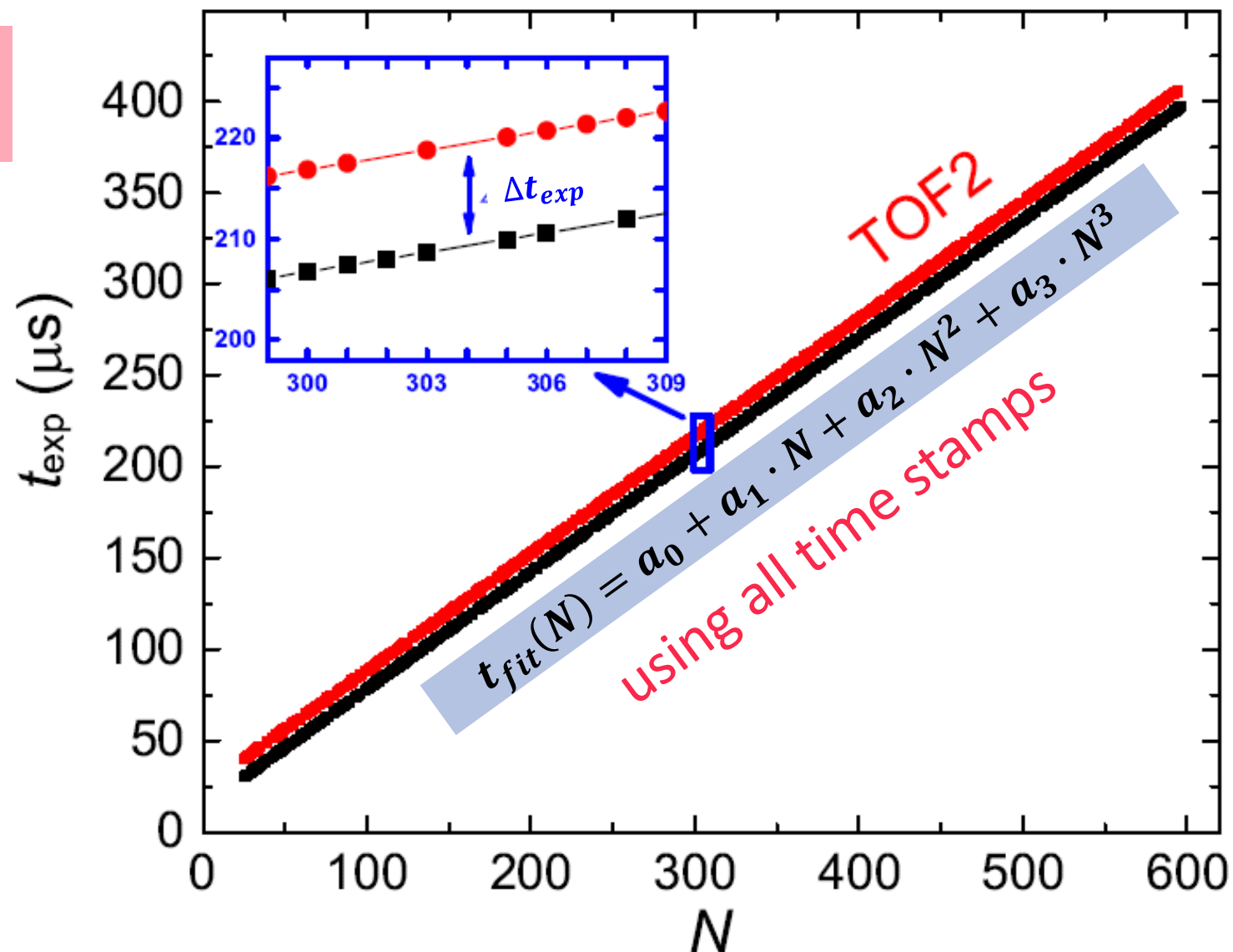
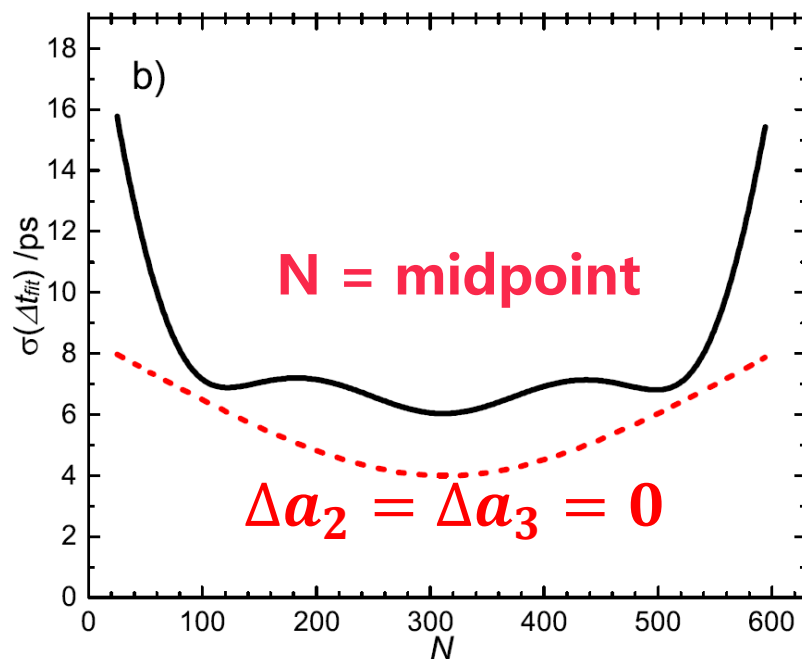




## 2. Velocity determination with two TOF detectors

$\Delta t_{exp}$  determinations using polynomial fit to all time stamps

$$\begin{aligned}\Delta t_{exp}(N) &= \Delta t_{fit}(N) \\ &= t_{fit}^{TOF2}(N) - t_{fit}^{TOF1}(N)\end{aligned}$$



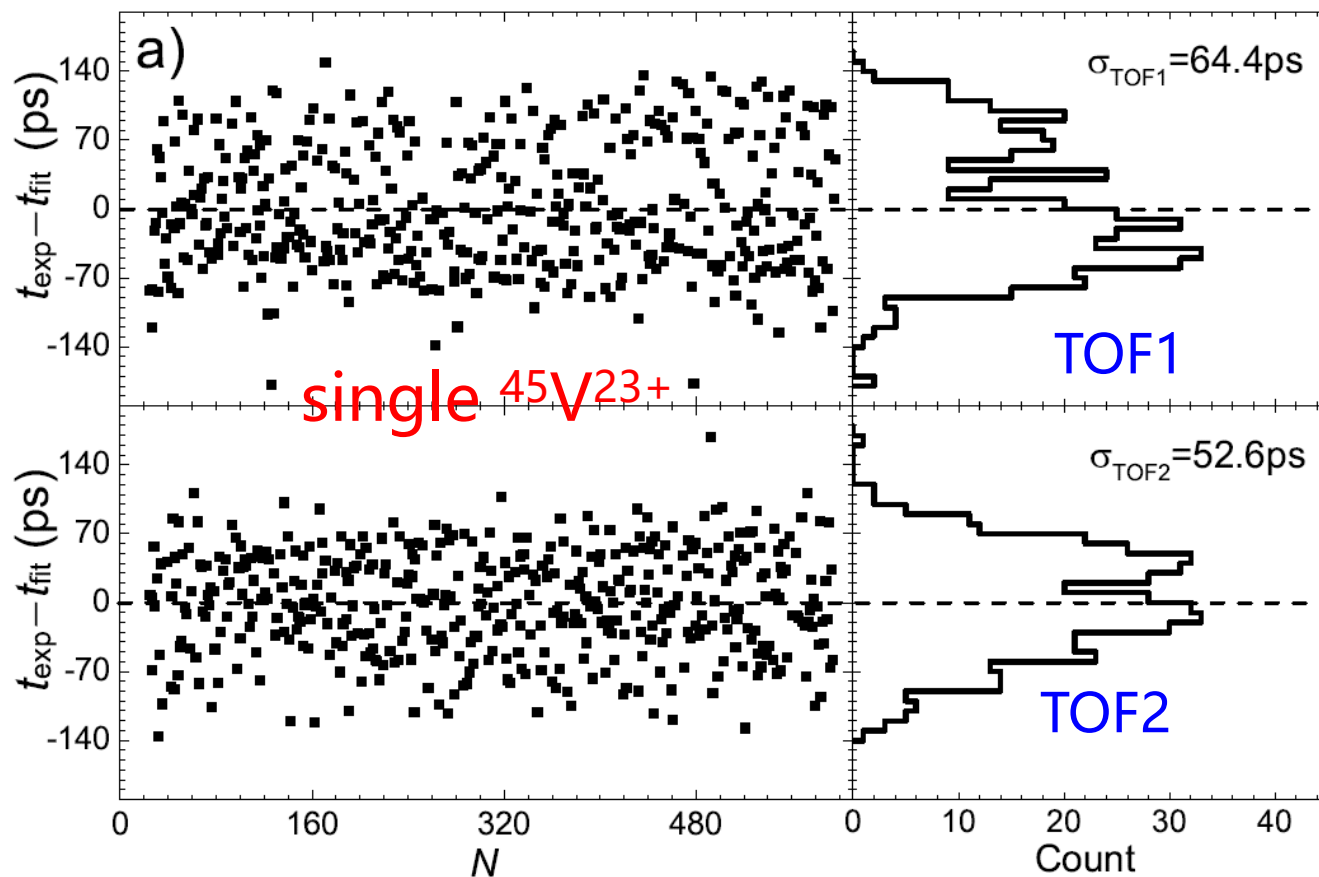


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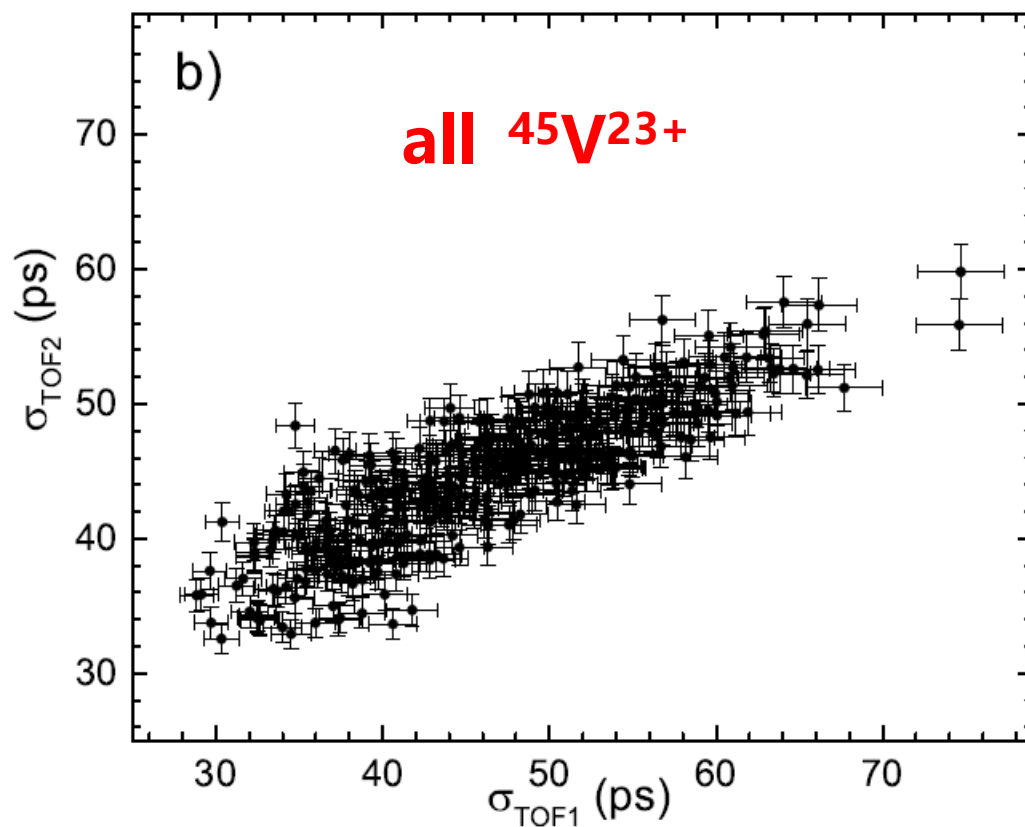


$\sigma_{TOF}$  are too large and asymmetric

Fit residuals



$\sigma_{TOF1}$  is correlated with  $\sigma_{TOF2}$



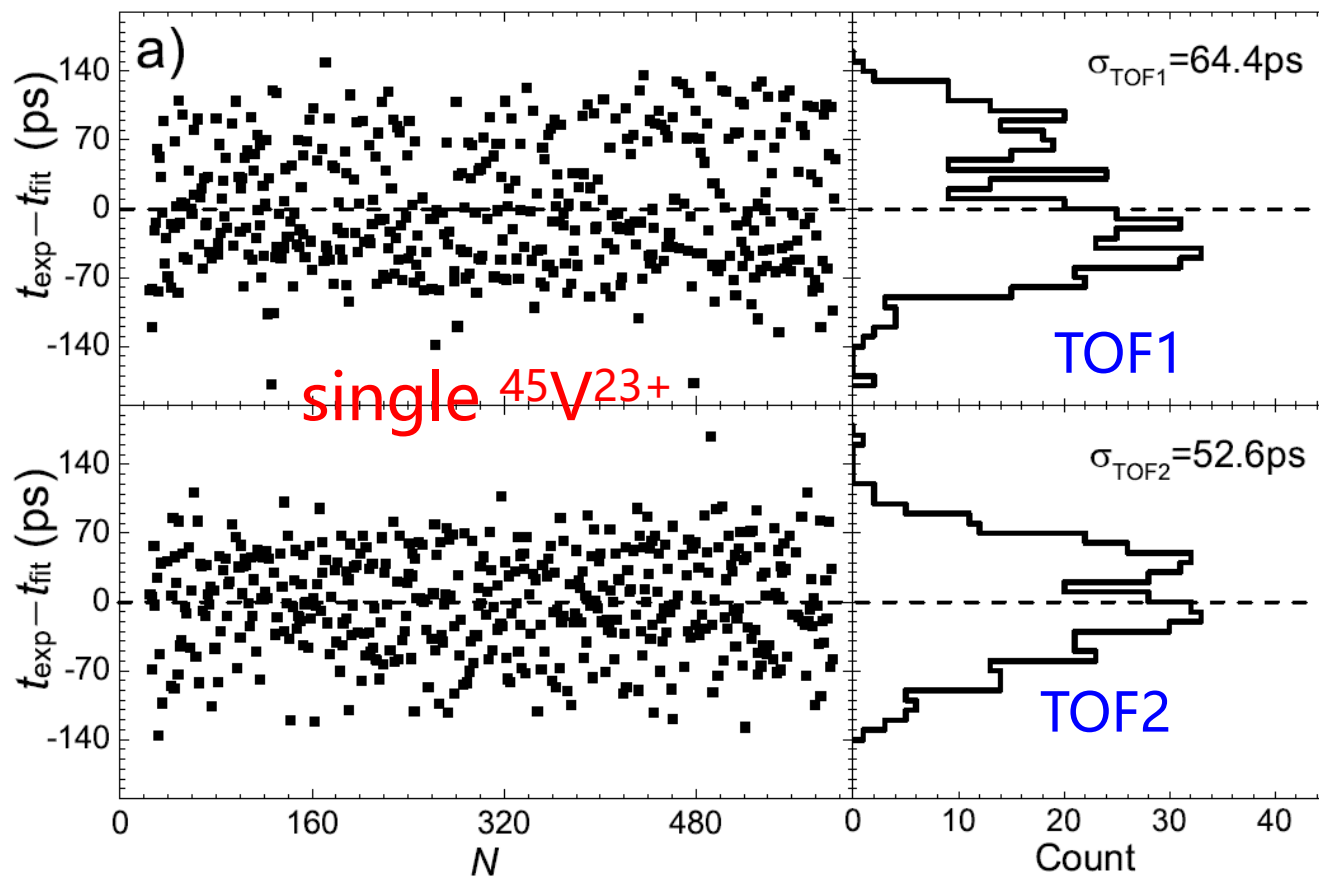


## 2. Velocity determination with two TOF detectors

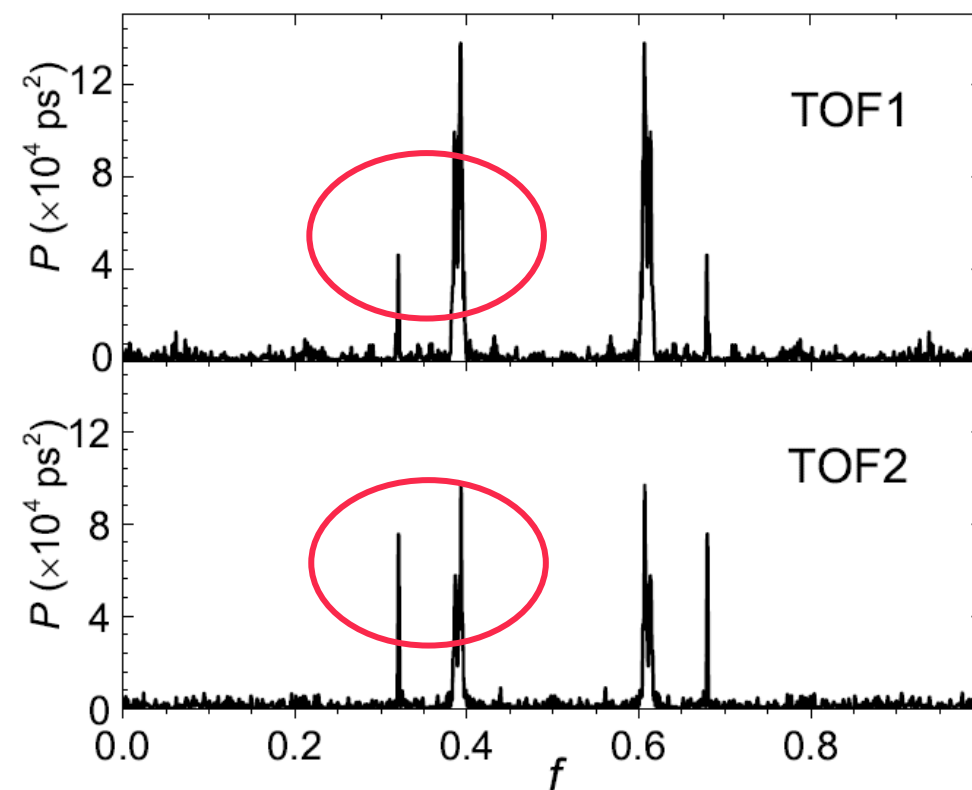


$$P(f) = \frac{1}{n_s} \left\{ \left[ \sum_j^{n_s} X_{N_j} \cdot \cos(2\pi f \cdot N_j) \right]^2 + \left[ \sum_j^{n_s} X_{N_j} \cdot \sin(2\pi f \cdot N_j) \right]^2 \right\}$$

Fit residuals



Discrete Fourier Transform

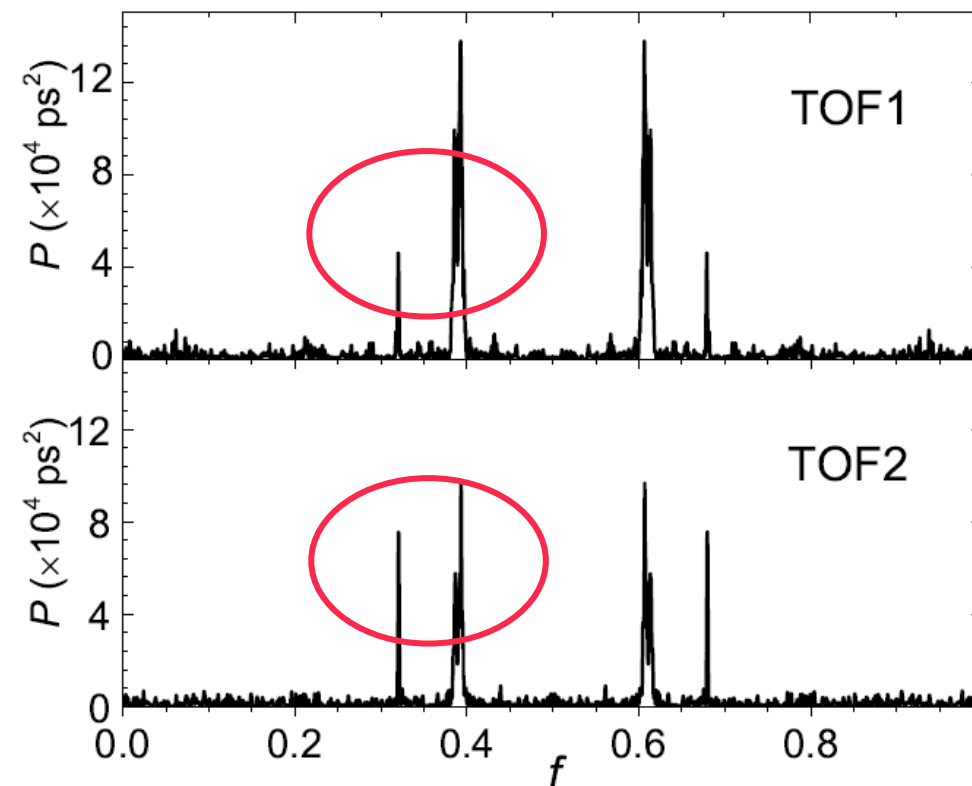
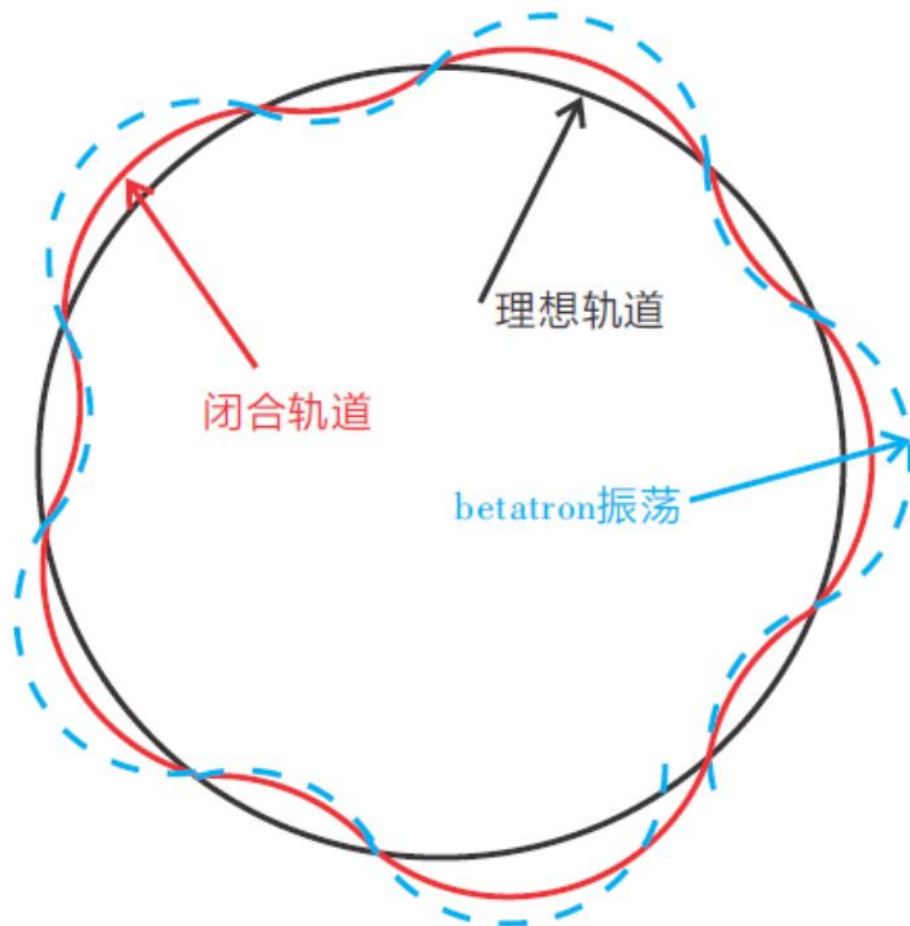


Two peaks at same  $f$

## 2. Velocity determination with two TOF detectors

$$P(f) = \frac{1}{n_s} \left\{ \left[ \sum_j^{n_s} X_{N_j} \cdot \cos(2\pi f \cdot N_j) \right]^2 + \left[ \sum_j^{n_s} X_{N_j} \cdot \sin(2\pi f \cdot N_j) \right]^2 \right\}$$

Discrete Fourier Transform



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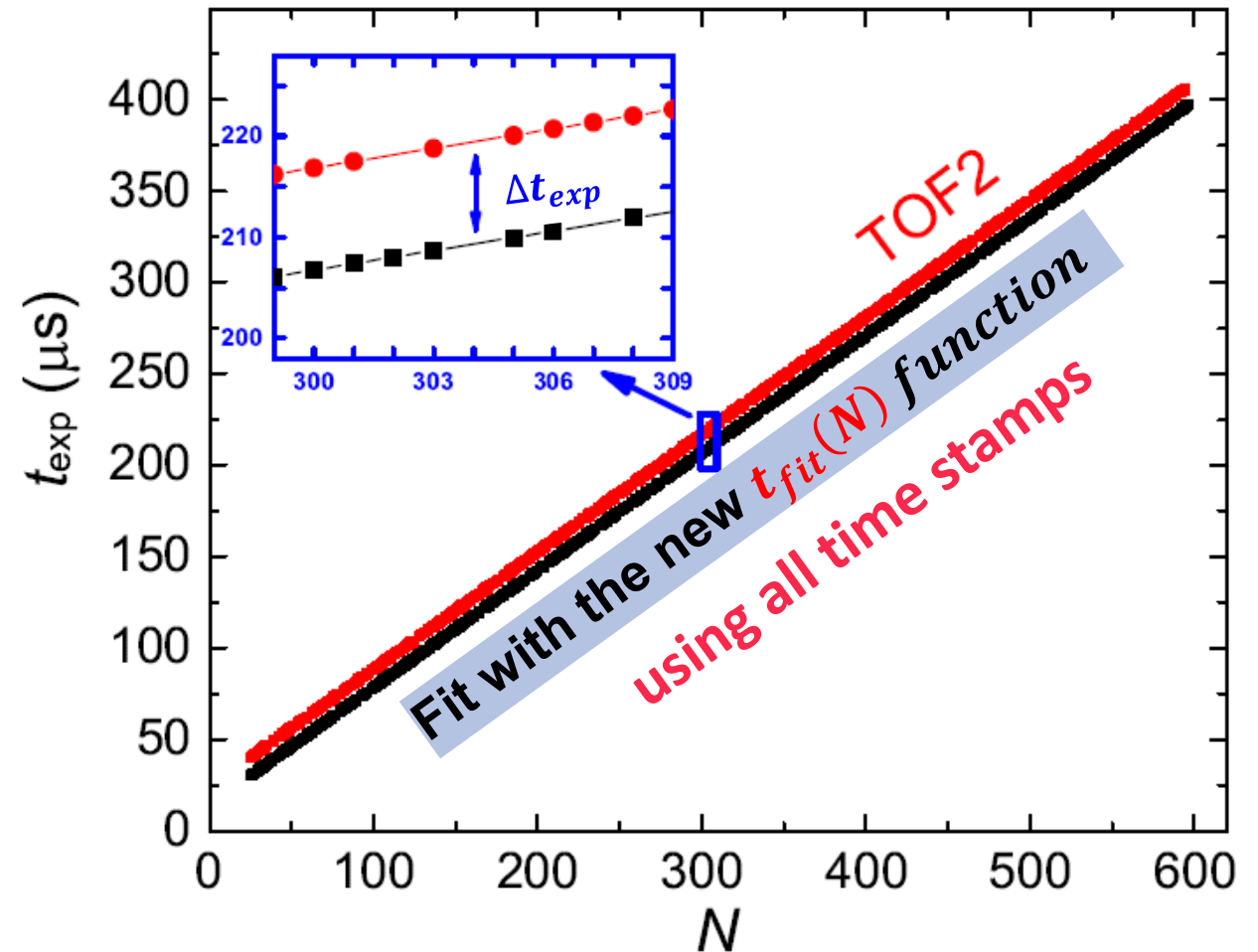
## 2. Velocity determination with two TOF detectors



$\Delta t_{exp}$  determinations considering betatron oscillation of stored ions

$$t_{fit}(N) = \sum_{i=0}^{i=3} a_i \cdot N^i + A_x \cdot \sin[2\pi(Q_{x0}N + Q_{x1}N^2) + \varphi_x] + A_y \cdot \sin[2\pi(Q_{y0}N + Q_{y1}N^2) + \varphi_y]$$

- ➔ The polynomial function describes ion motion with a mean orbital length
- ➔ The sine-like terms describe the periodic time fluctuations due to betatron oscillations.





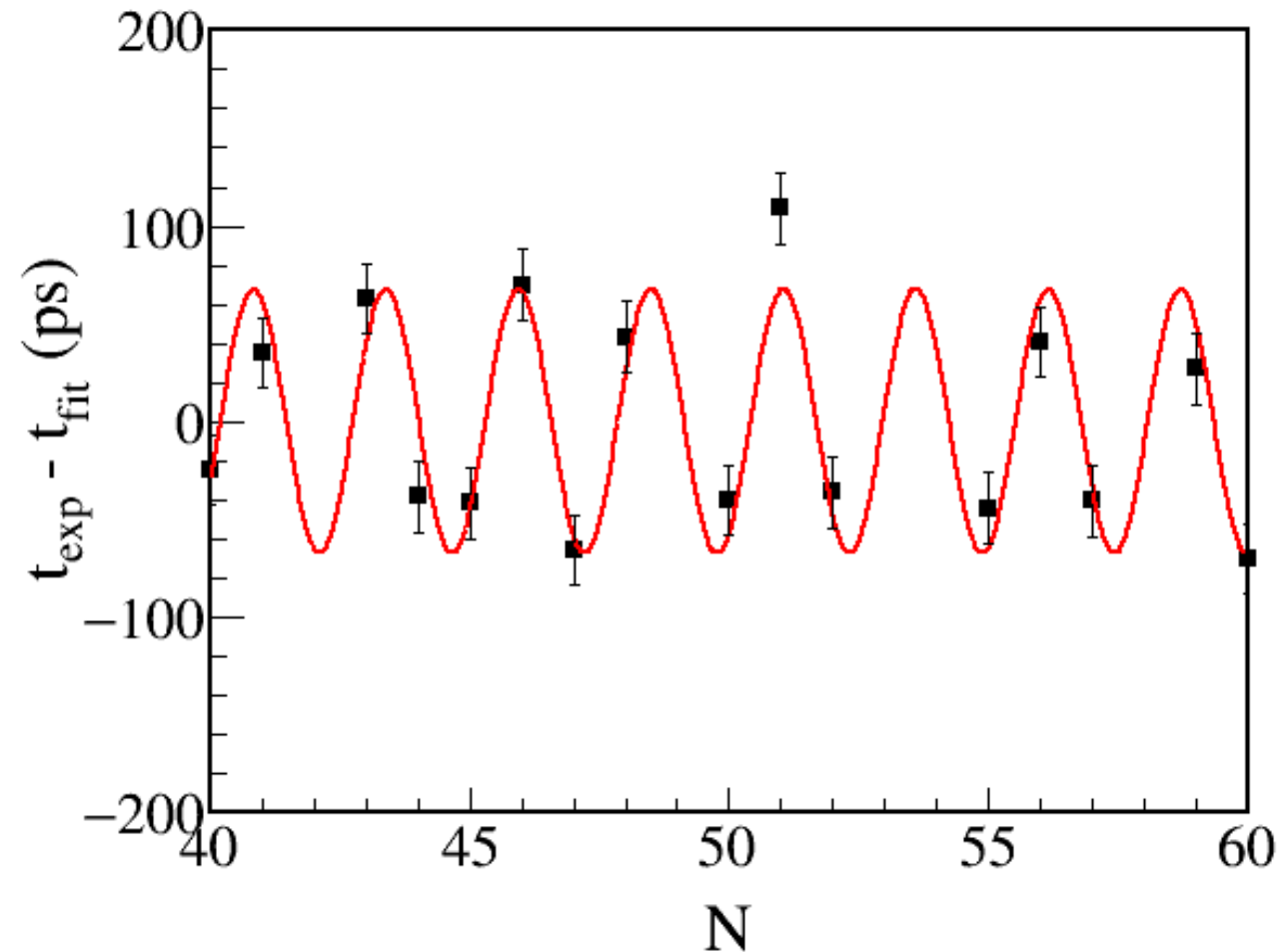
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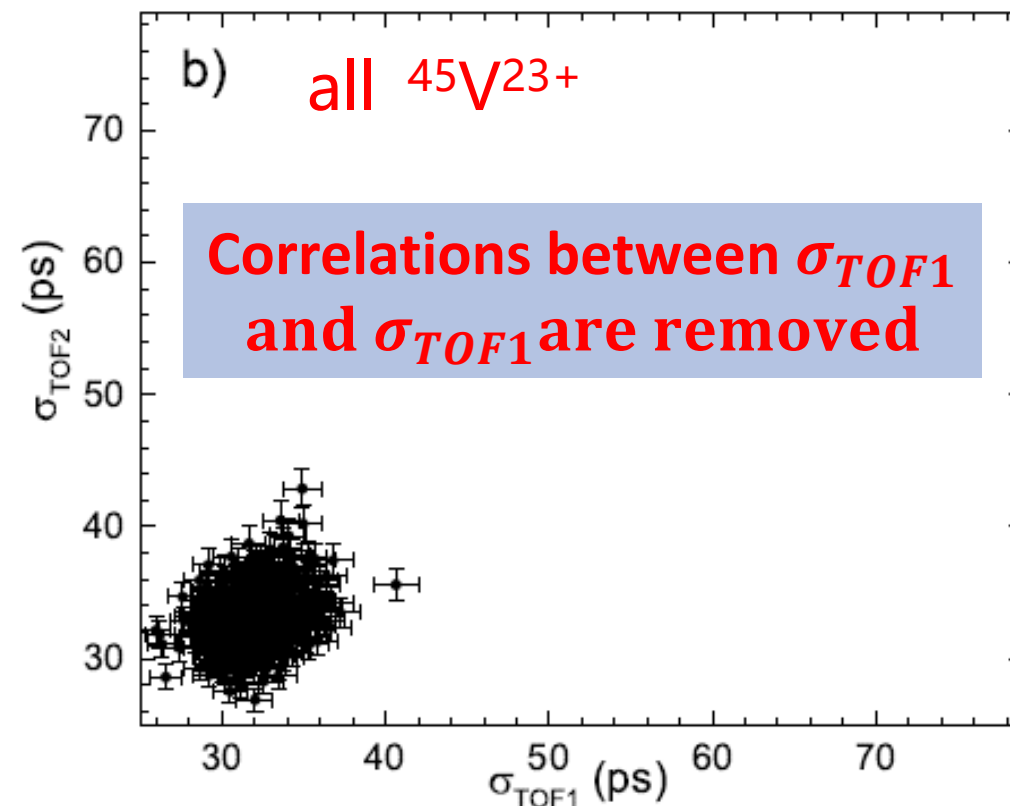
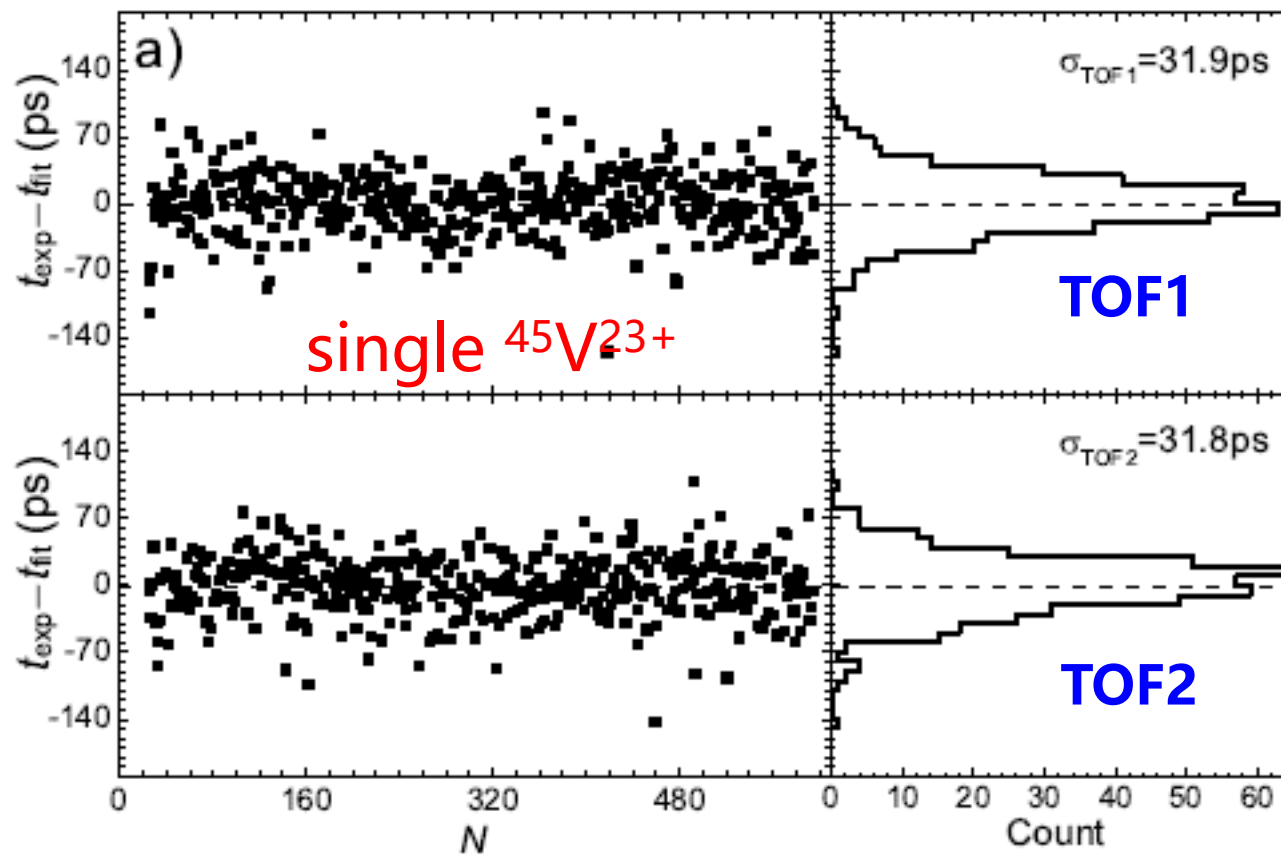




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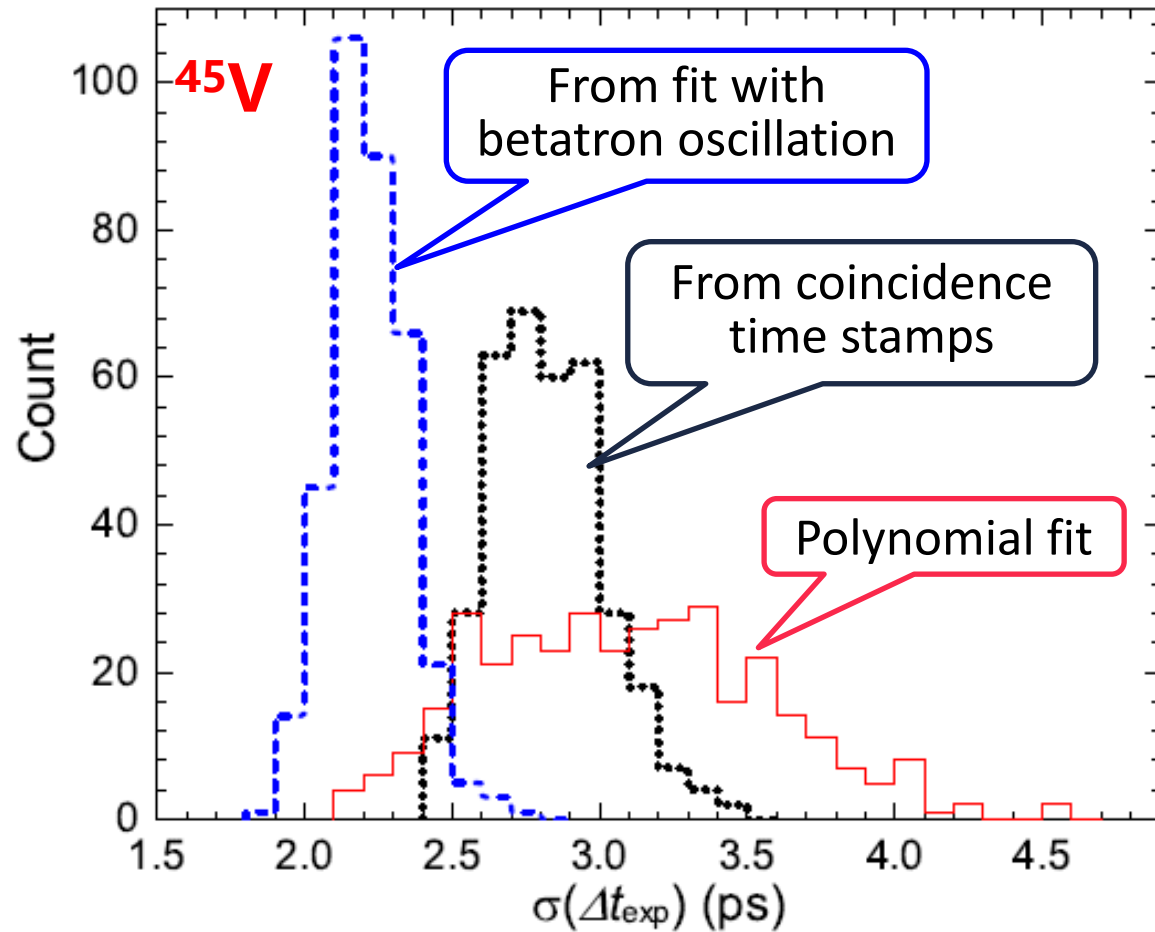
$$t_{fit}(N) = \sum_{i=0}^3 a_i \cdot N^i + A_x \sin[2\pi(Q_{x0}N + Q_{x1}N^2) + \varphi_x] + A_y \sin[2\pi(Q_{y0}N + Q_{y1}N^2) + \varphi_y]$$

Fit residuals



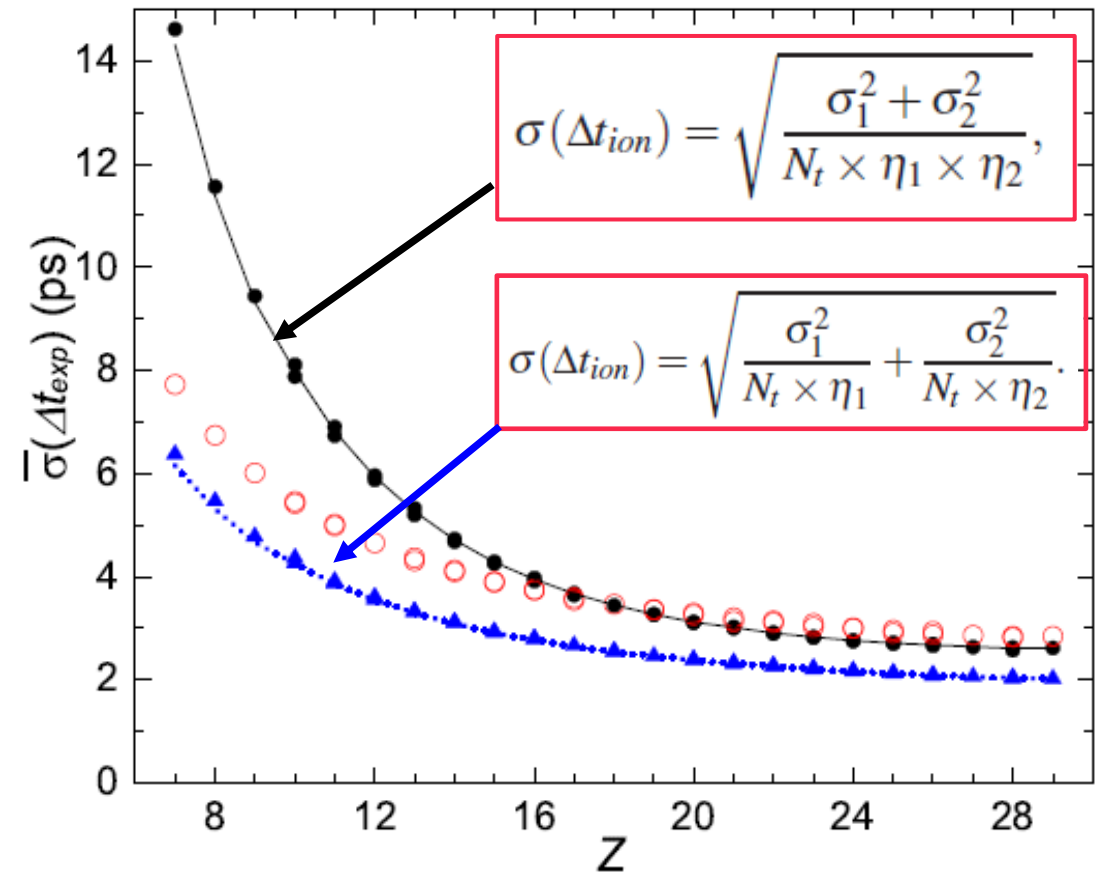
## 2. Velocity determination with two TOF detectors

$$\Delta t_{exp}(N) = \sum_{i=0}^{i=3} \Delta a_i \cdot N^i$$



$$\overline{\sigma(\Delta t_{exp})} = (2.0 \sim 6.4) \text{ ps},$$

$$\text{relative: } (2.2 \sim 7.2) \times 10^{-5}$$





## 2. Velocity determination with two TOF detectors

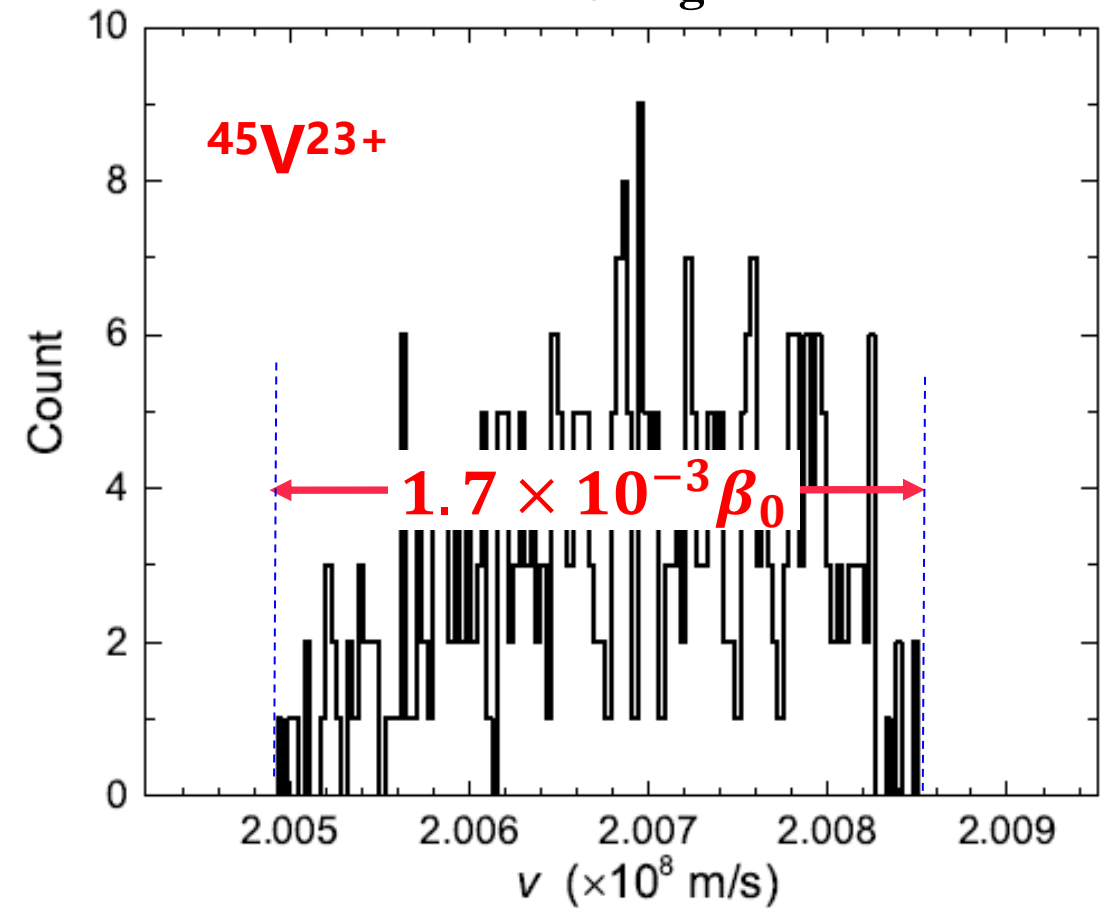
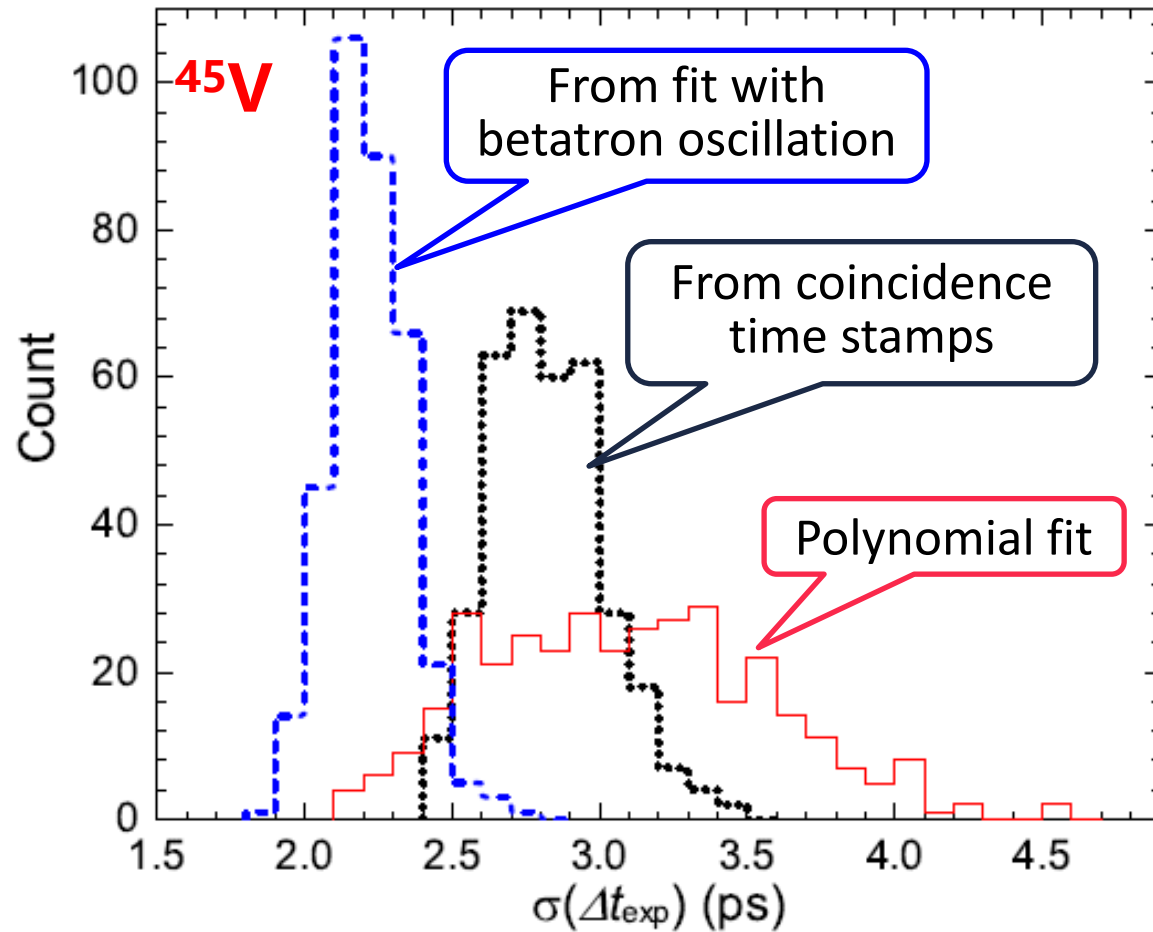
$$\Delta t_{exp}(N) = \sum_{i=0}^{i=3} \Delta a_i \cdot N^i$$

$$v = \frac{L}{\Delta t_{exp} - \Delta t_d}$$

$$L = 18034(1.3) \text{ mm}$$

$$\Delta t_d = 99(4) \text{ ps}$$

Using FL-266nm-Pico laser





## 2. Velocity determination with two TOF detectors



PHYSICAL REVIEW ACCELERATORS AND BEAMS **24**, 042802 (2021)

Editors' Suggestion

### In-ring velocity measurement for isochronous mass spectrometry

X. Zhou<sup>1,2</sup>, M. Zhang<sup>1,2</sup>, M. Wang<sup>1,2,\*</sup>, Y. H. Zhang<sup>1,2,†</sup>, Y. J. Yuan<sup>1,2,‡</sup>, X. L. Yan<sup>1,§</sup>,  
X. H. Zhou<sup>1,2</sup>, H. S. Xu<sup>1,2</sup>, X. C. Chen<sup>1</sup>, Y. M. Xing<sup>1</sup>, R. J. Chen<sup>1,3</sup>, X. Xu<sup>4,1</sup>, P. Shuai<sup>1</sup>,  
C. Y. Fu<sup>1</sup>, Q. Zeng<sup>1,5</sup>, M. Z. Sun<sup>1</sup>, H. F. Li<sup>1,2</sup>, Q. Wang<sup>1,2</sup>, T. Bao<sup>1</sup>, M. Si<sup>1,2,6</sup>, H. Y. Deng<sup>1,2</sup>,  
M. Z. Liu<sup>1,2</sup>, T. Liao<sup>1,2</sup>, J. Y. Shi<sup>1,2</sup>, Y. N. Song<sup>1,2</sup>, J. C. Yang<sup>1</sup>, W. W. Ge<sup>1</sup>, Yu. A. Litvinov<sup>1,3</sup>,  
S. A. Litvinov<sup>1,3</sup>, R. S. Sidhu<sup>3</sup>, T. Yamaguchi<sup>7</sup>, S. Omika<sup>7</sup>, K. Wakayama<sup>7</sup>,  
S. Suzuki<sup>1,8</sup> and T. Moriguchi<sup>8</sup>

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<sup>6</sup>*Université Paris-Saclay, CNRS/IN2P3, IJCLab, F-91405 Orsay, France*

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# 3. Realization of $B\rho$ -defined IMS



## Logic of mass determinations

Measurements

$T_i, v_i$   
( $i = 1, 2, \dots, N$ )



Construct

$$(B\rho)^i = \frac{m}{q} \cdot (\gamma v)_i$$

$$C_i = v_i \cdot T_i$$

$B\rho \sim C$   
line using  
known  $m/q$



Outputs

$$\frac{m}{q} = B\rho \sqrt{\left(\frac{1}{v}\right)^2 - \left(\frac{1}{v_c}\right)^2}$$

new  $(m/q)^i$   
using  $(B\rho)_{fit}^i$



T spectrum  
 $T_{fix}^i @ C_{fix}$

$$T_{fix}^i = C_{fix} \sqrt{\frac{1}{(B\rho)_{fix}^2} \left[ \left(\frac{m}{q}\right)_{exp}^i \right]^2 + \left(\frac{1}{v_c}\right)^2}$$

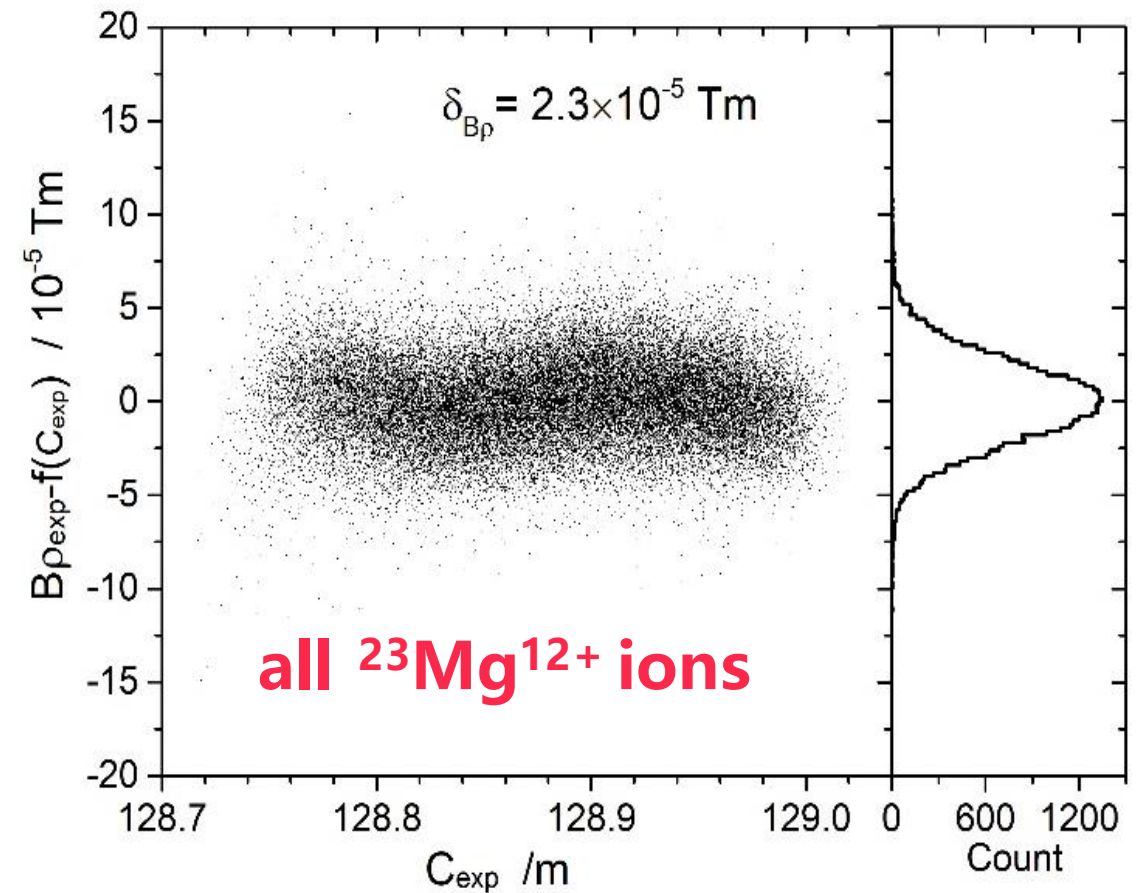
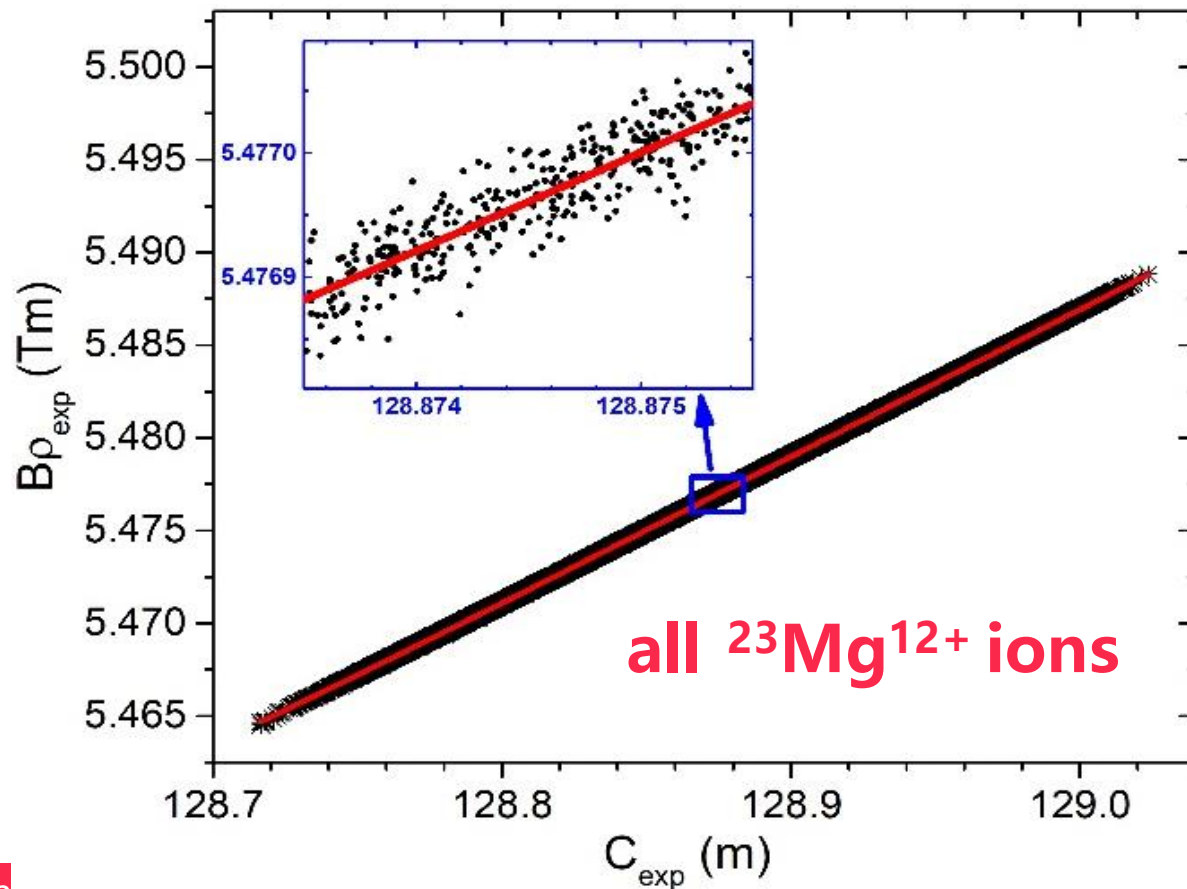


### 3. Realization of $B\rho$ -defined IMS



$$B\rho = f(C) = (B\rho)_0 \cdot \left(\frac{C}{C_0}\right)^K + a_1 \cdot e^{-a_2 \cdot (C - C_0)}$$

$^{58}\text{Ni}$  beam





# 3. Realization of $B\rho$ -defined IMS



$$\left(\frac{m}{q}\right)_{exp}^i = \frac{f(C_{exp}^i)}{(\gamma v)^i_{exp}}, \quad i = 1, 2, 3 \dots$$

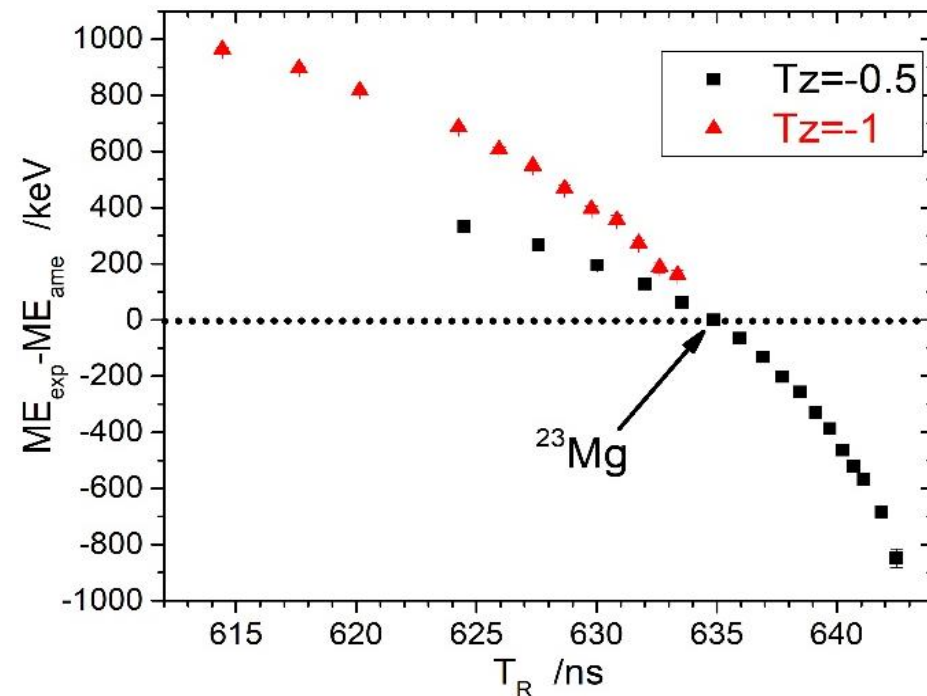
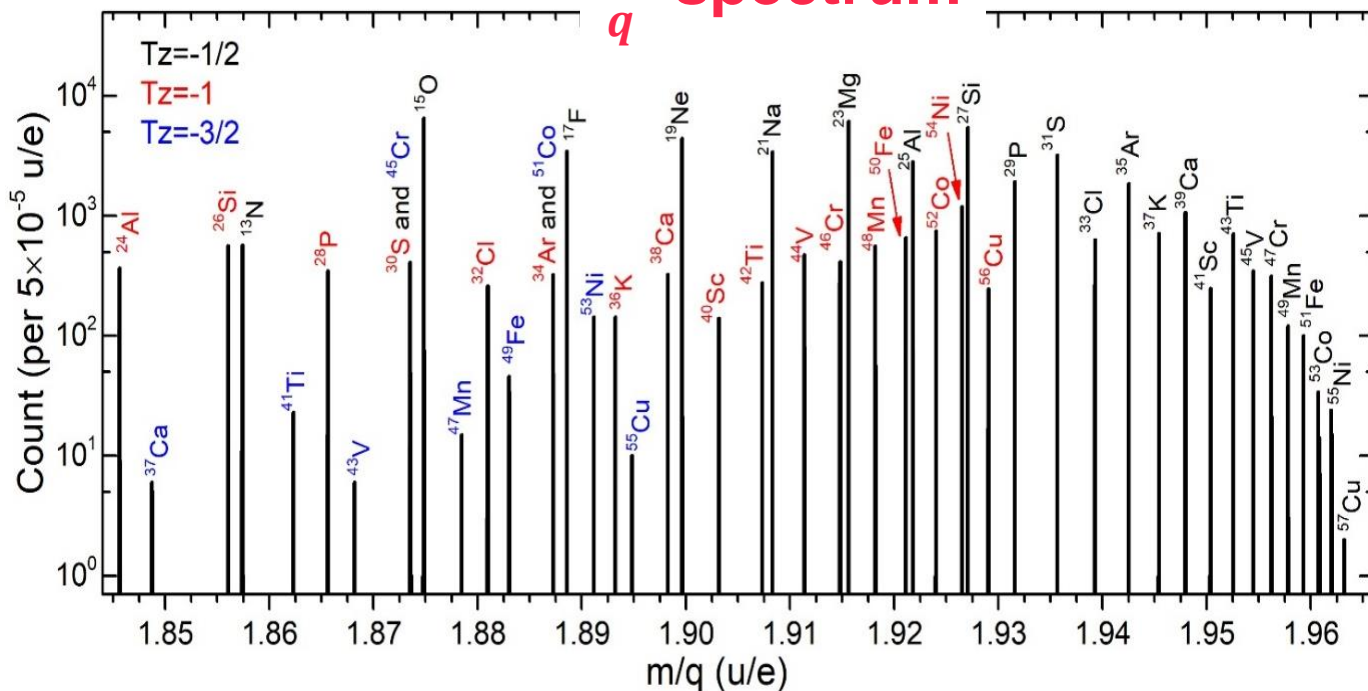
$$v = \frac{L}{\Delta t_{exp} - \Delta t_d}$$

$L = 18034(1.3) \text{ mm}$

$\Delta t_d = 99(4) \text{ ps}$

Using FL-266nm-Pico laser

$\frac{m}{q}$  spectrum



Systematic errors are due to biased  $L$  and  $\Delta t_d$  in the velocity determination



# 3. Realization of $B\rho$ -defined IMS

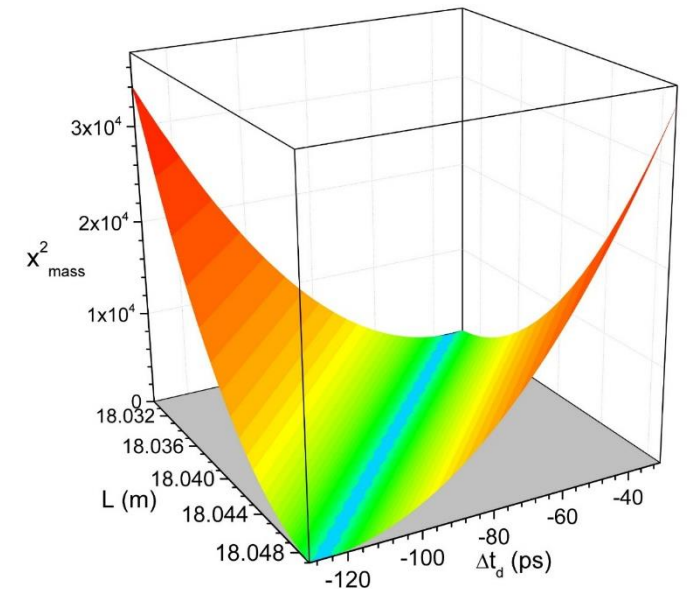
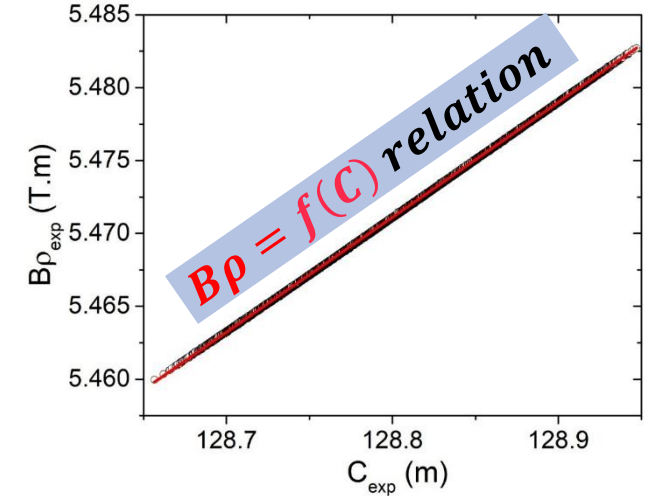


$L$  and  $\Delta t_d$  determinations

$$v = \frac{L}{\Delta t_{exp} - \Delta t_d}$$

- ➔ Calibration with known-mass nuclei in order to find the correct  $L$  and  $\Delta t_d$
- ➔ Procedure: Minimize the  $\chi^2$  by varying  $L$  and  $\Delta t_d$

$$\chi^2 = \frac{1}{N_c} \cdot \sum_i \frac{(ME_{exp}^i - ME_{AME}^i)^2}{\sigma(ME_{exp}^i)^2}$$







### 3. Realization of $B\rho$ -defined IMS

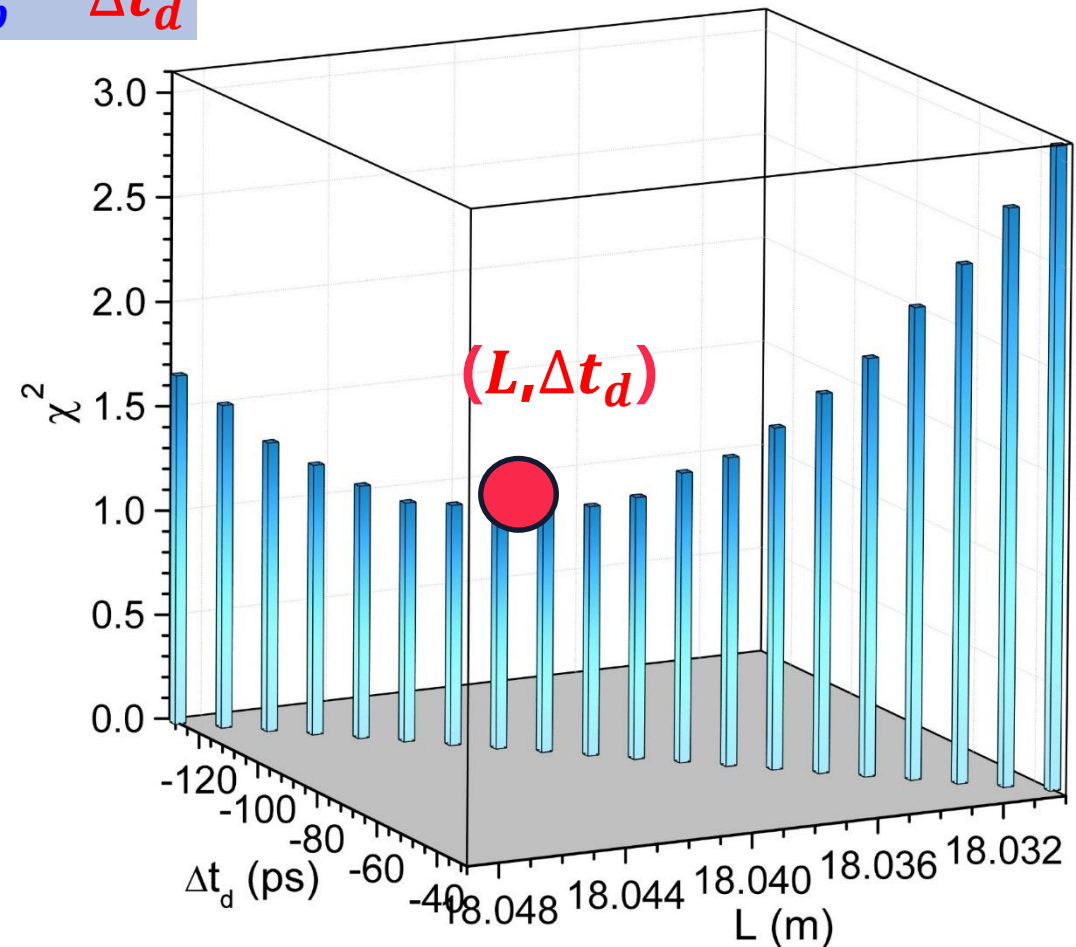


$L$  and  $\Delta t_d$  determinations

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$$\chi^2 = \frac{1}{N_c} \cdot \sum_i \frac{(ME_{exp}^i - ME_{AME}^i)^2}{\sigma(ME_{exp}^i)^2}$$





### 3. Realization of $B\rho$ -defined IMS



Using the new  $L$  and  $\Delta t_d$  values:

$$L = 18037 \text{ mm}$$

$$\Delta t_d = 101.6 \text{ ps}$$

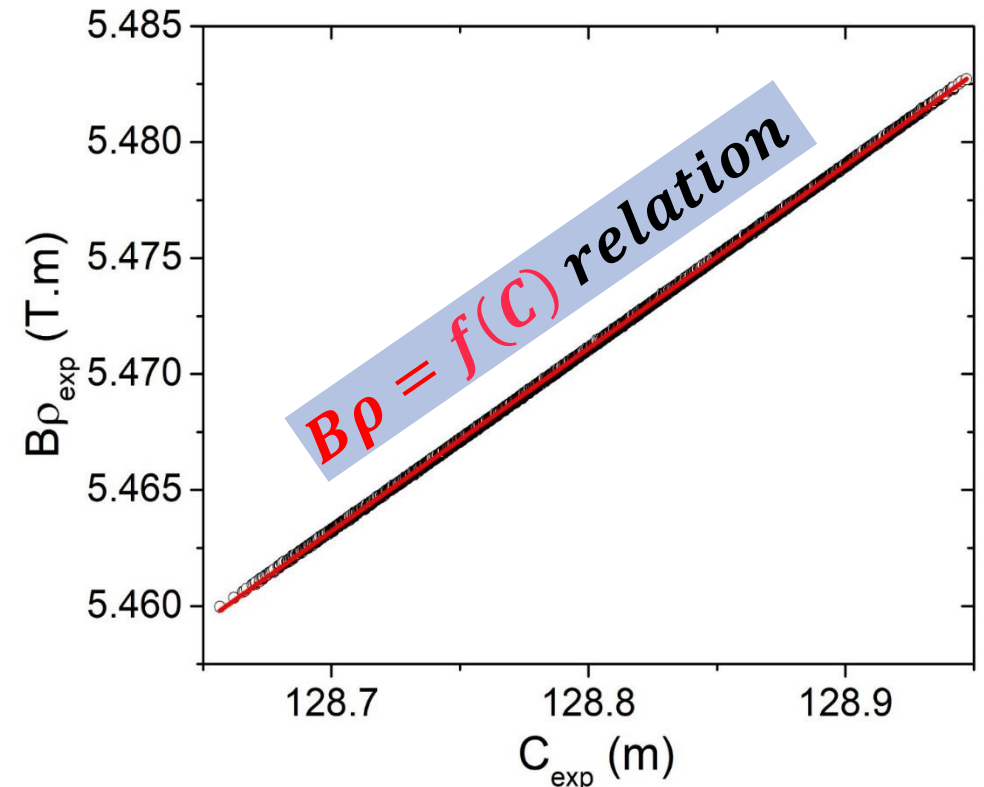
➔ Re-recalculate the  $\{(B\rho)_{exp}^i, C_{exp}^i\}$  data using known-mass nuclei.

➔ Fit the  $\{(B\rho)_{exp}^i, C_{exp}^i\}$  data using

$$f(C) = (B\rho)_0 \cdot \left(\frac{C}{C_0}\right)^K + a_1 \cdot \exp[-a_2 \cdot (C - C_0)]$$

➔ Individual  $m/q$  determinations via

$$(m/q)_{exp}^i = \frac{f(C_{exp}^i)}{(\gamma v)_{exp}^i}, \quad i = 1, 2, 3, \dots N_t$$





# 3. Realization of $B\rho$ -defined IMS

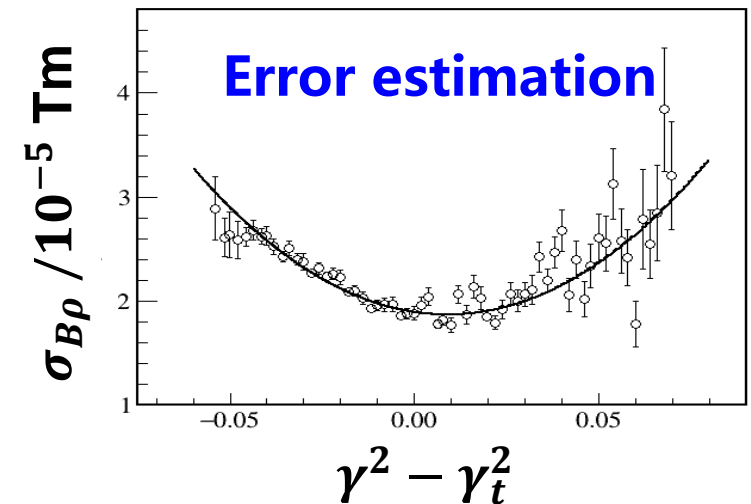
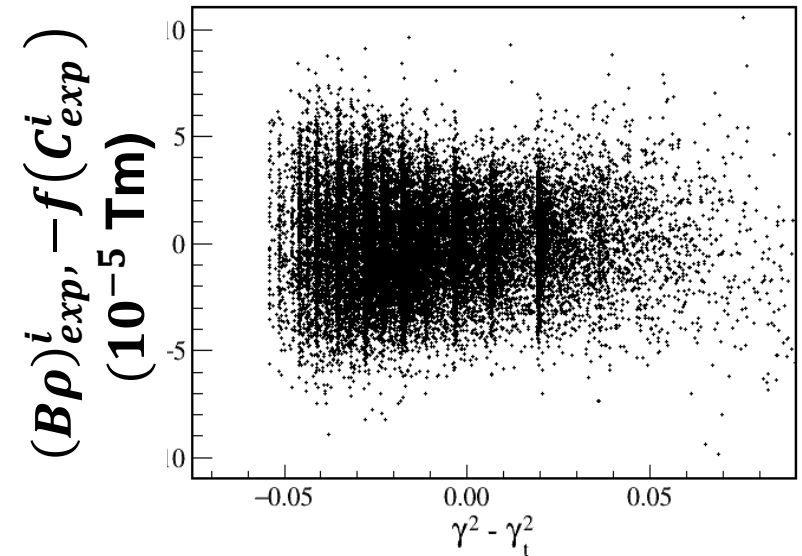


## ➔ Error estimation

$$\gamma_t^2 = \frac{d(B\rho)/(B\rho)}{dC/C} = \frac{C}{f(C)} \cdot \frac{df(C)}{dC}$$

$$\sigma_{B\rho}(\gamma, \gamma_t) = b_0 + b_1 \cdot (\gamma^2 - \gamma_t^2) + b_2 \cdot (\gamma^2 - \gamma_t^2)^2$$

$$\frac{\sigma[(m/q)^i_{exp}]}{(m/q)^i_{exp}} = \frac{\sigma_{B\rho}(\gamma_{exp}^i, \gamma_t^i)}{f(C_{exp}^i)}, i = 1, 2, 3 \dots N_t.$$





# 3. Realization of $B\rho$ -defined IMS

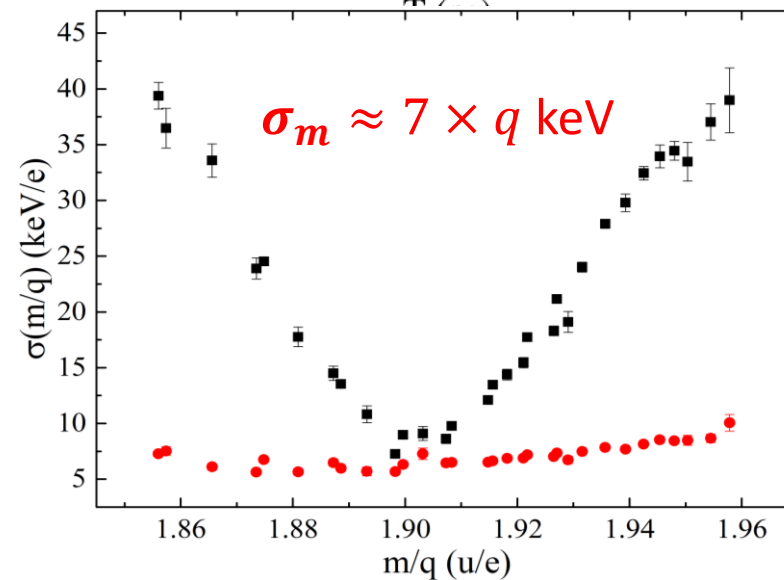
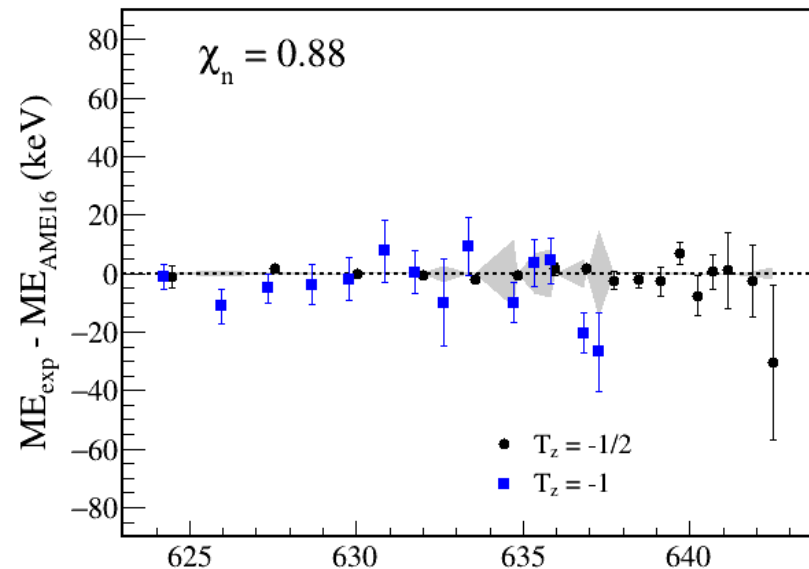
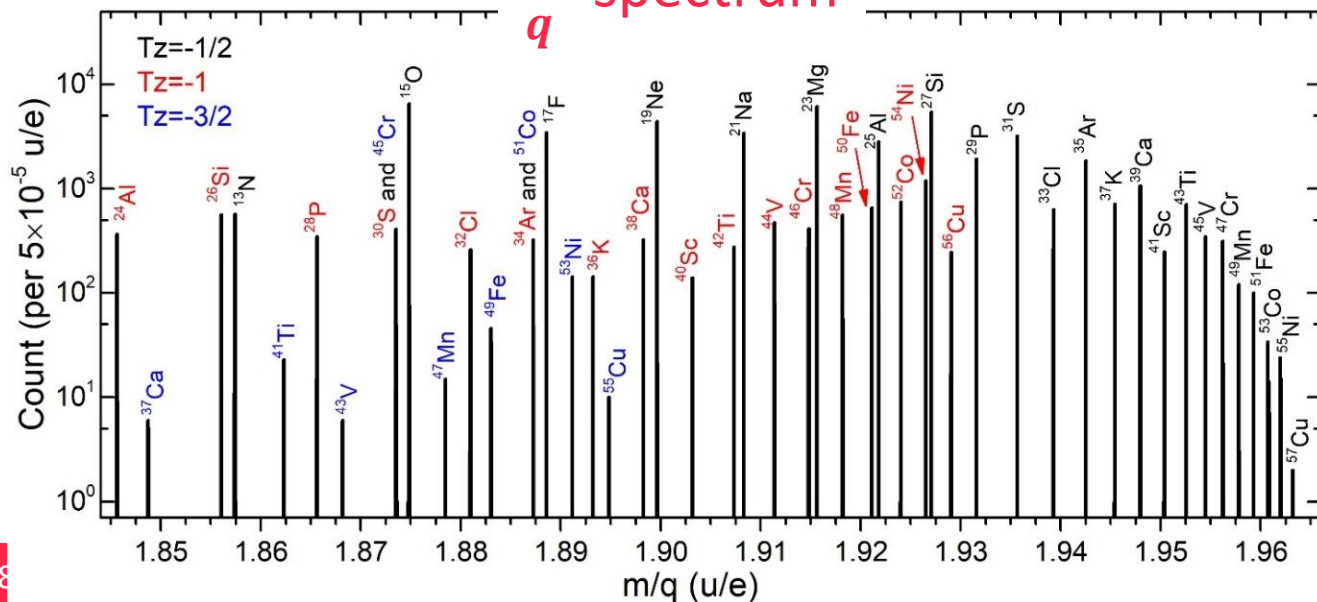


## Masses and uncertainties

$$(m/q)^i_{exp} = \frac{f(C^i_{exp})}{(\gamma\nu)^i_{exp}}, \quad i = 1, 2, 3, \dots N_t$$

$$\frac{\sigma[(m/q)^i_{exp}]}{(m/q)^i_{exp}} = \frac{\sigma_{B\rho}(\gamma^i_{exp}, \gamma^i_t)}{f(C^i_{exp})}, \quad i = 1, 2, 3 \dots N_t.$$

$\frac{m}{q}$  spectrum





# 3. Realization of $B\rho$ -defined IMS

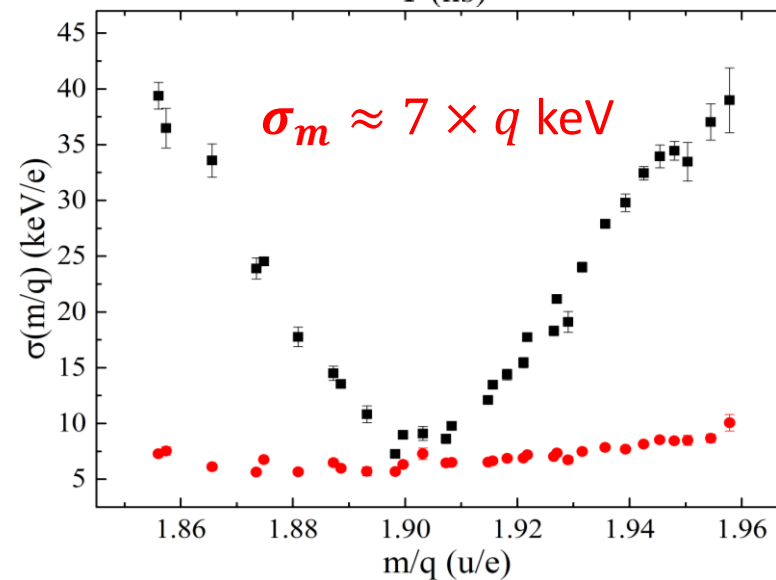
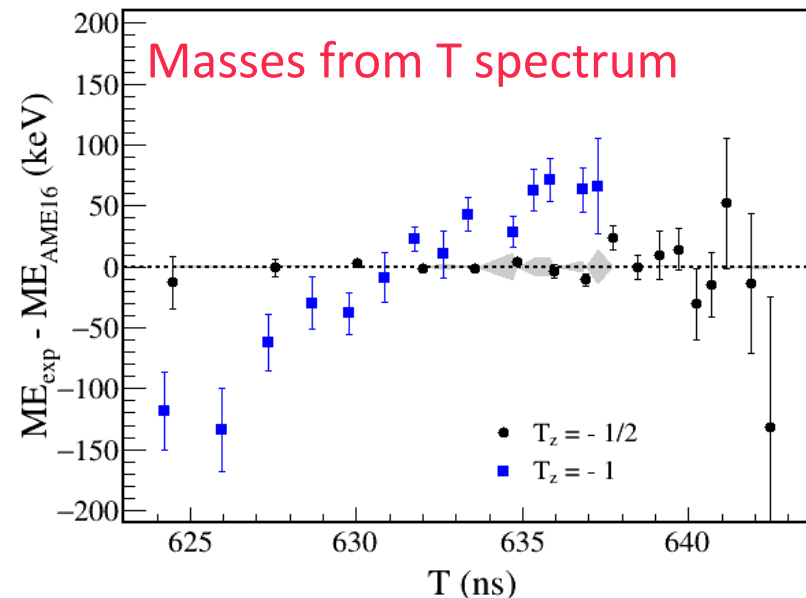
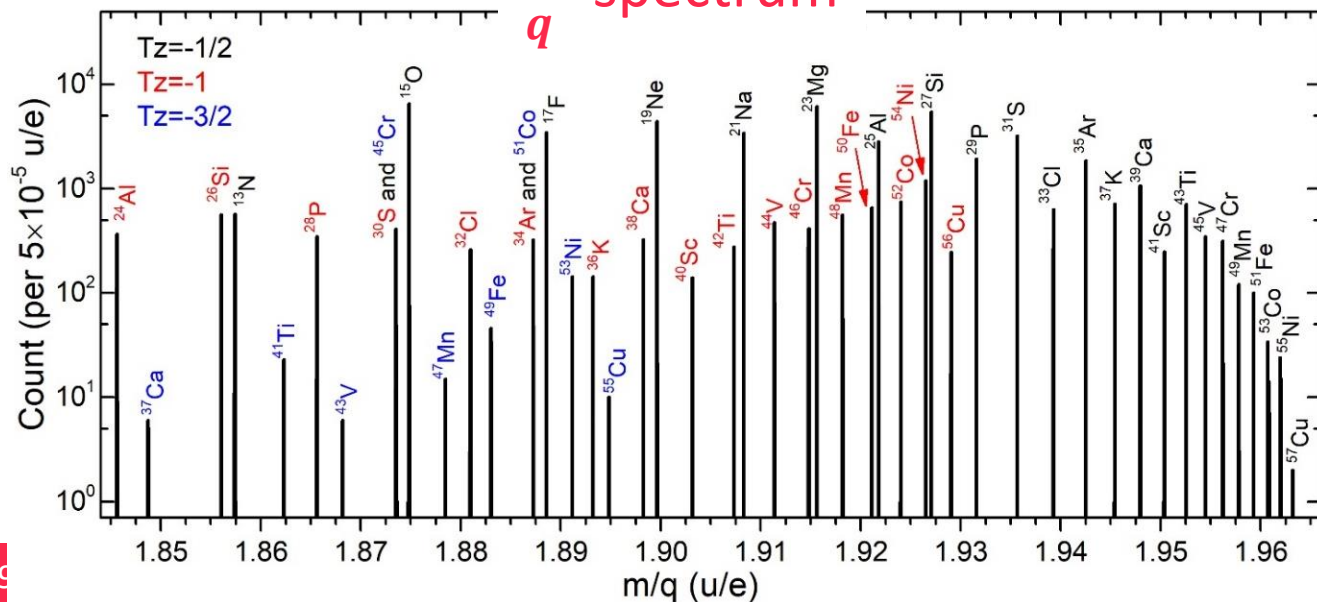


## Masses and uncertainties

$$(m/q)^i_{exp} = \frac{f(C^i_{exp})}{(\gamma\nu)^i_{exp}}, \quad i = 1, 2, 3, \dots N_t$$

$$\frac{\sigma[(m/q)^i_{exp}]}{(m/q)^i_{exp}} = \frac{\sigma_{B\rho}(\gamma^i_{exp}, \gamma^i_t)}{f(C^i_{exp})}, \quad i = 1, 2, 3 \dots N_t.$$

$\frac{m}{q}$  spectrum





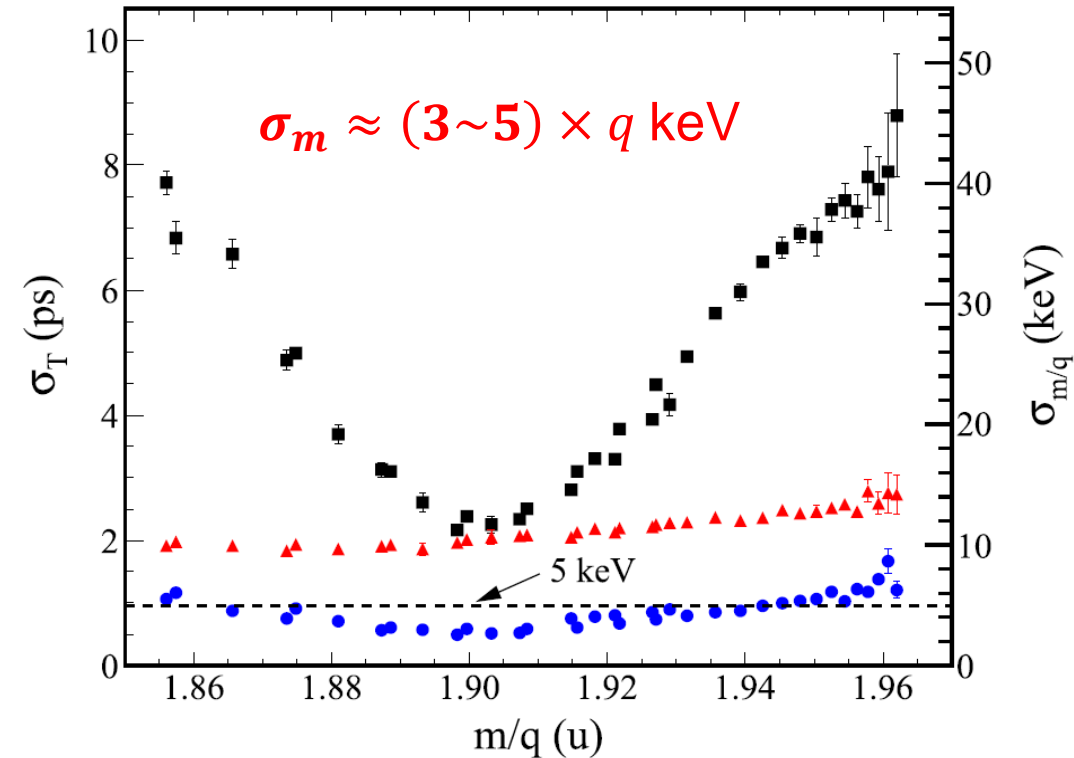
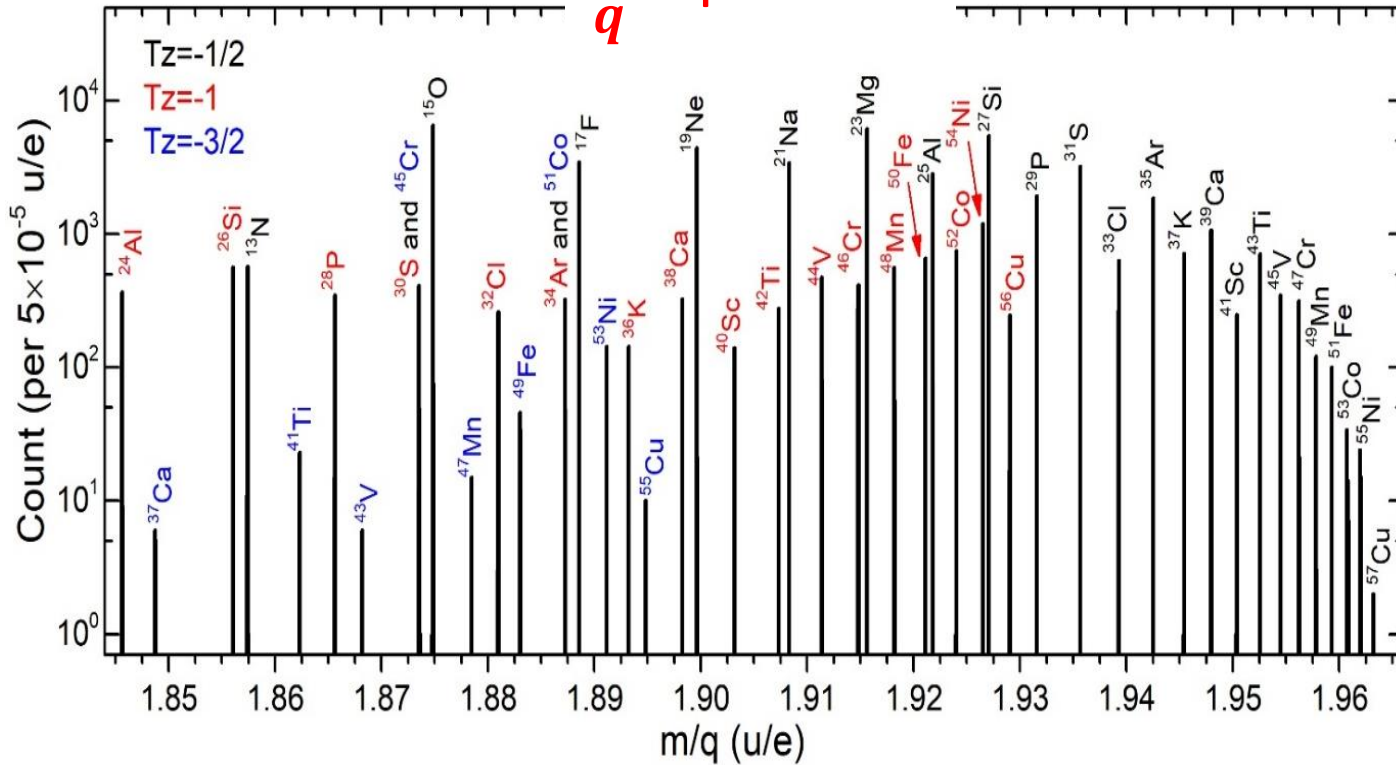
# 3. Realization of $B\rho$ -defined IMS



Mass resolving powers are significantly improved after field drift correction for all nuclides in the large  $m/q$ -range of  $\Delta(m/q) \approx 0.10 \text{ u e}^{-1}$

$\frac{m}{q}$  spectrum

$^{58}\text{Ni}$  beam

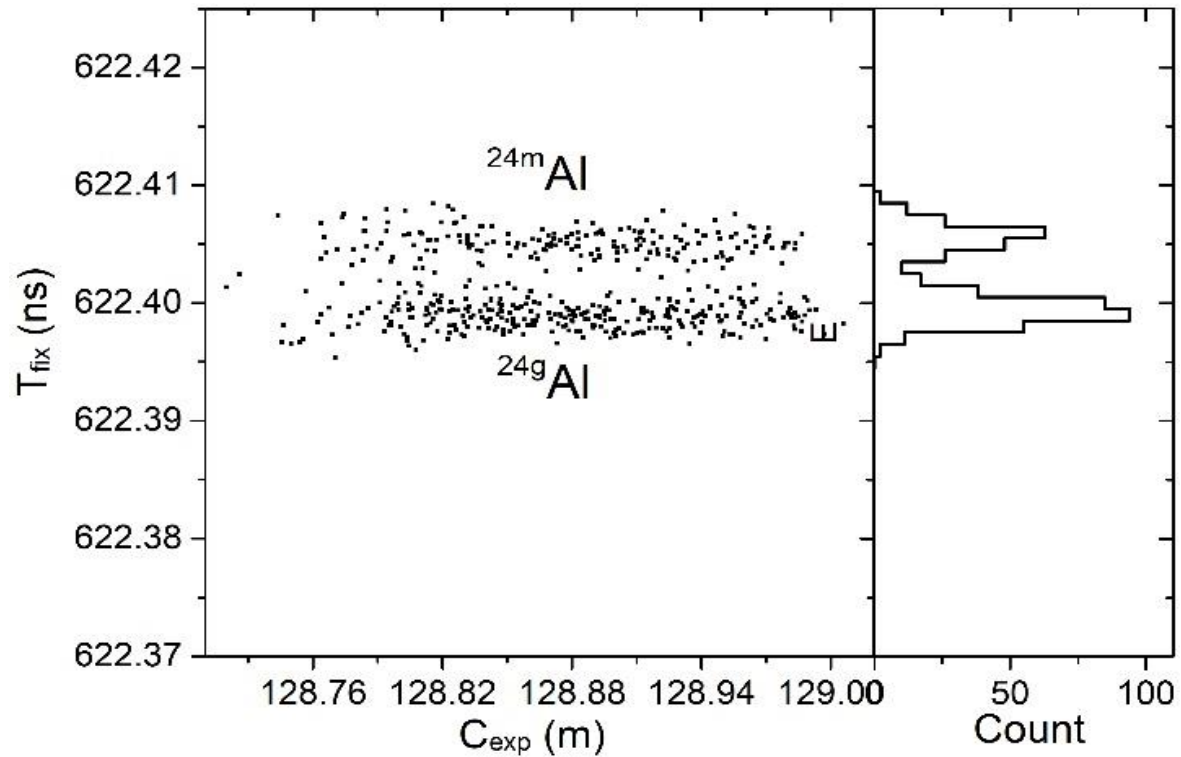
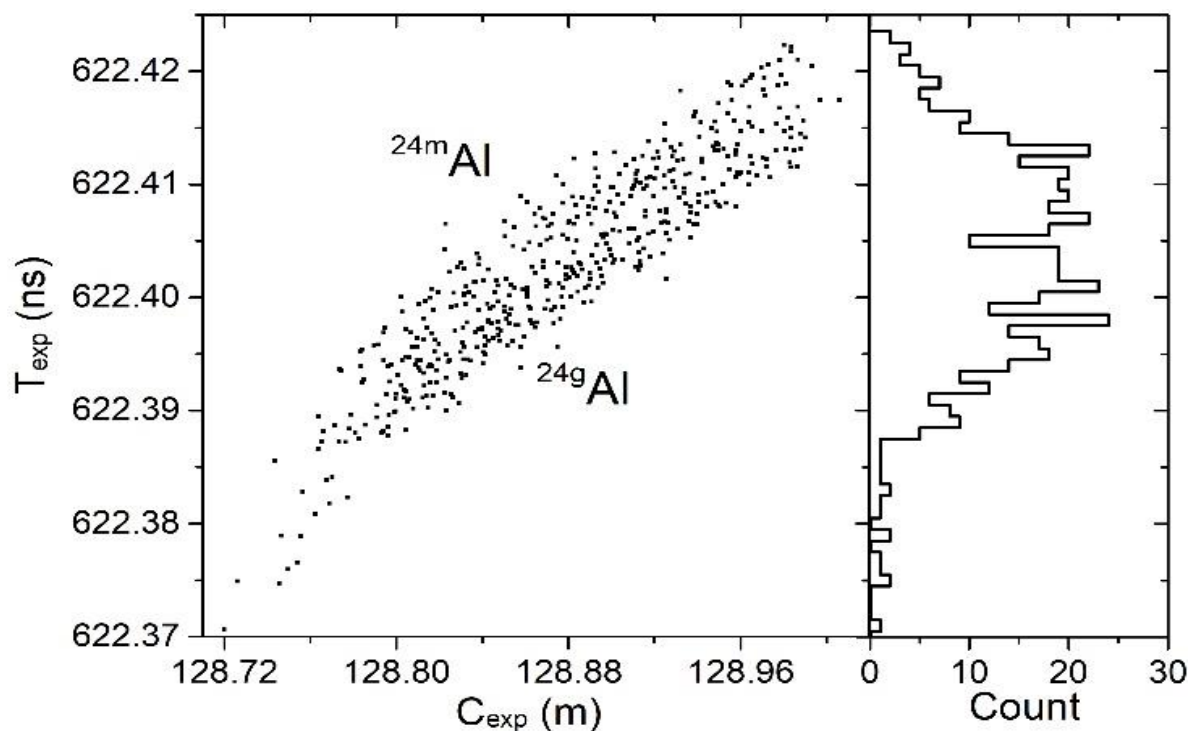




### 3. Realization of $B\rho$ -defined IMS



$$T_{fix}^i = C_{fix} \cdot \sqrt{\frac{1}{(B\rho)_{fix}^2} \cdot \left[ \left( \frac{m}{q} \right)_{exp}^i \right]^2 + \left( \frac{1}{v_c} \right)^2}, \quad i = 1, 2, 3 \dots$$

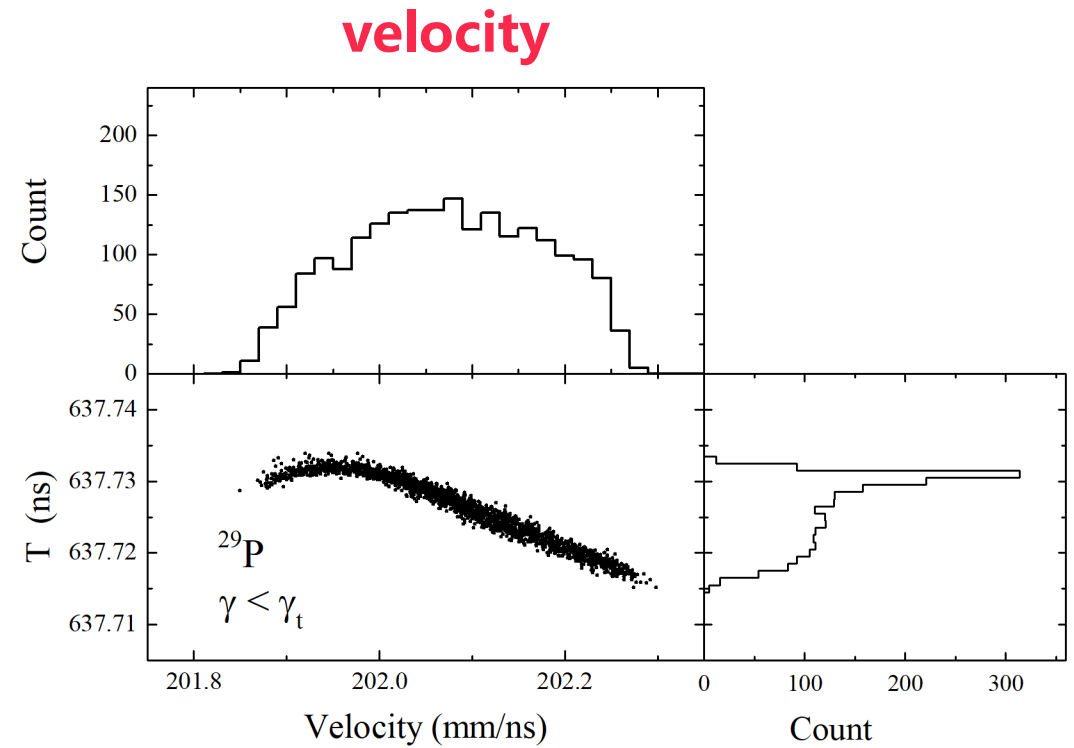
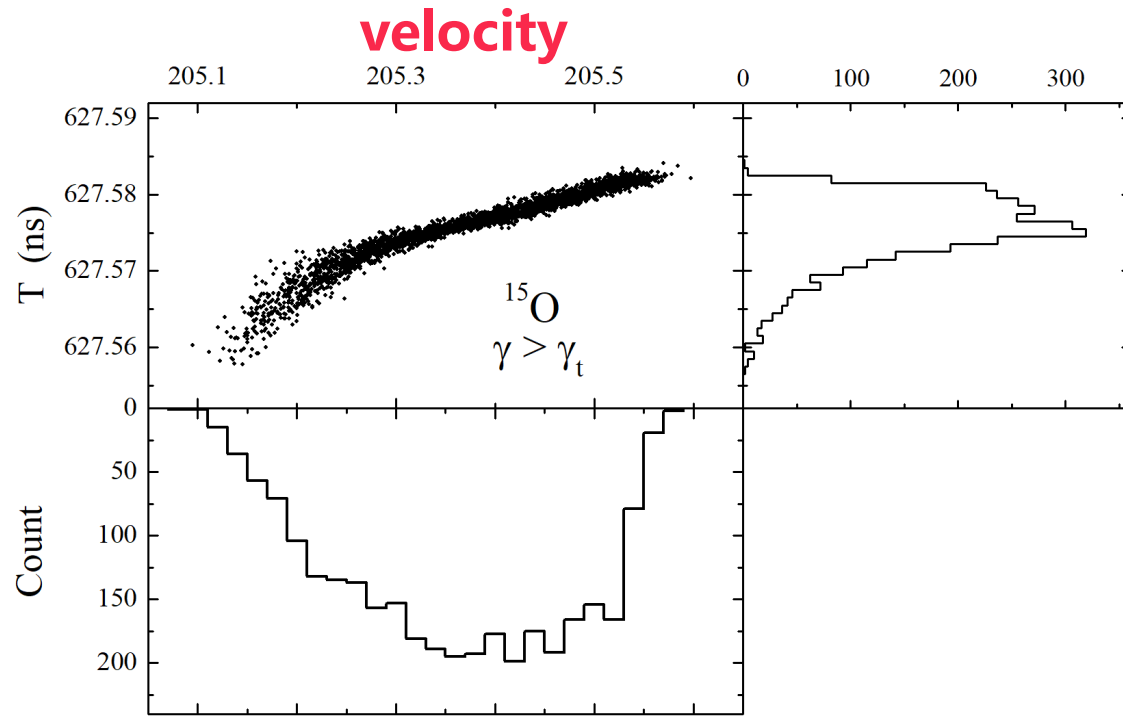




# 3. Realization of $B\rho$ -defined IMS



## Asymmetric $T$ and $v$ distributions



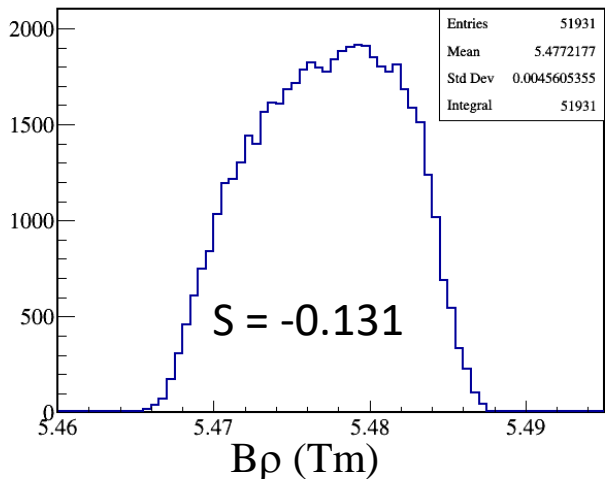




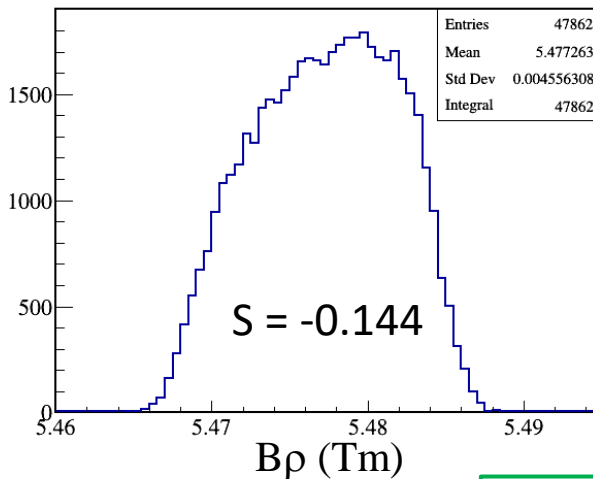
# 3. Realization of $B\rho$ -defined IMS



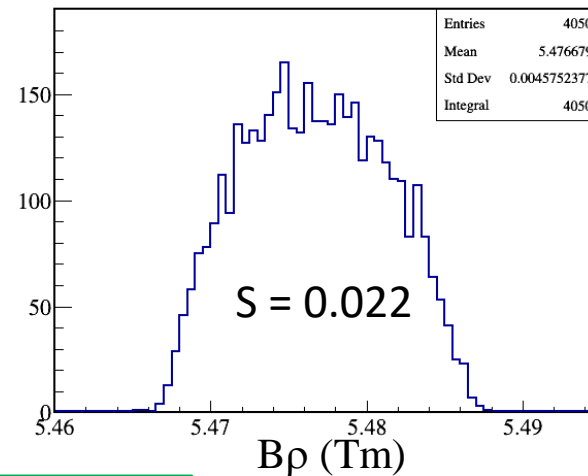
All ions



$T_z = -1/2$



$T_z = -1$

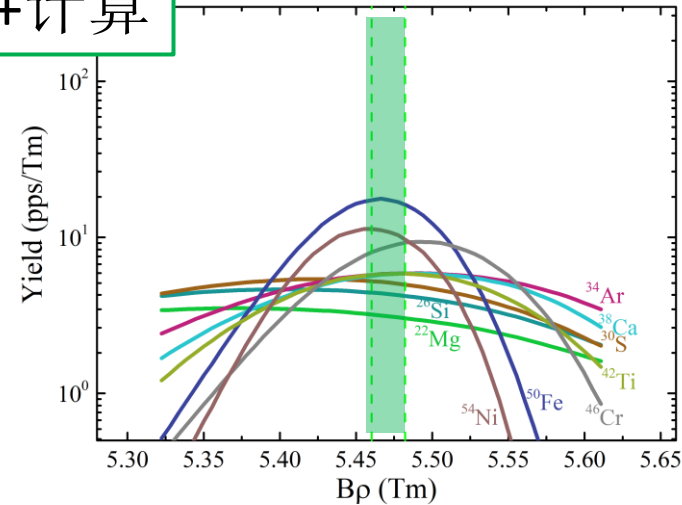
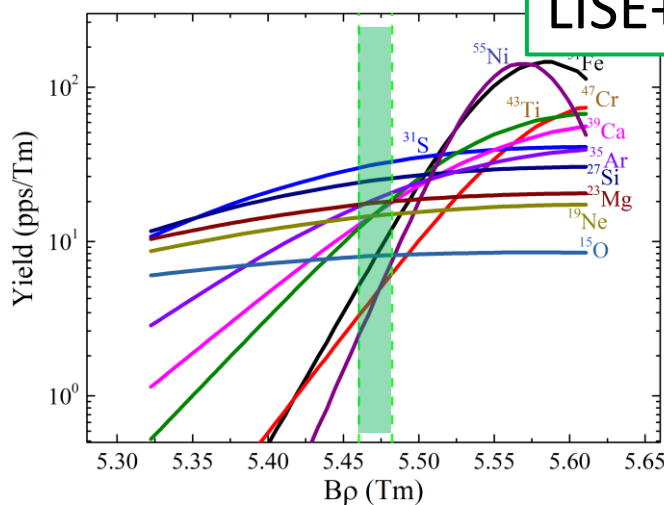


偏度 (Skewness)

$$S = \left( \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^3 \right) / \sigma^3$$

$\bar{x}$ 是平均值,  $\sigma$ 是标准差

LISE++计算





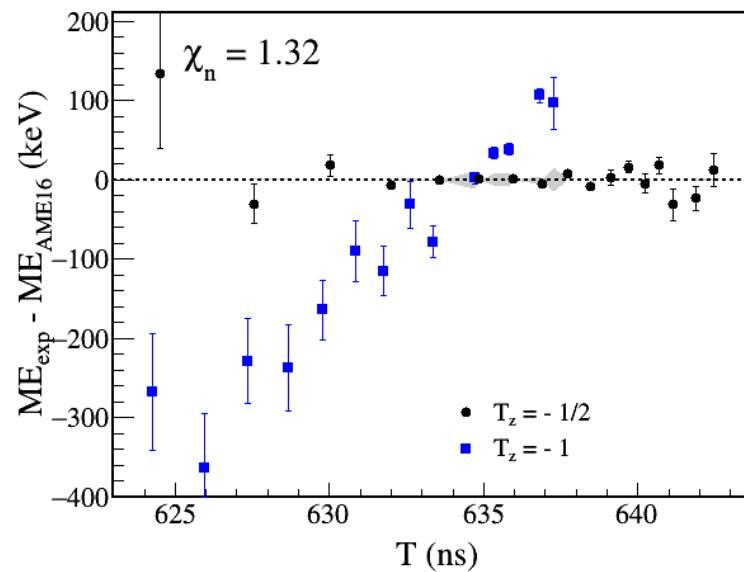
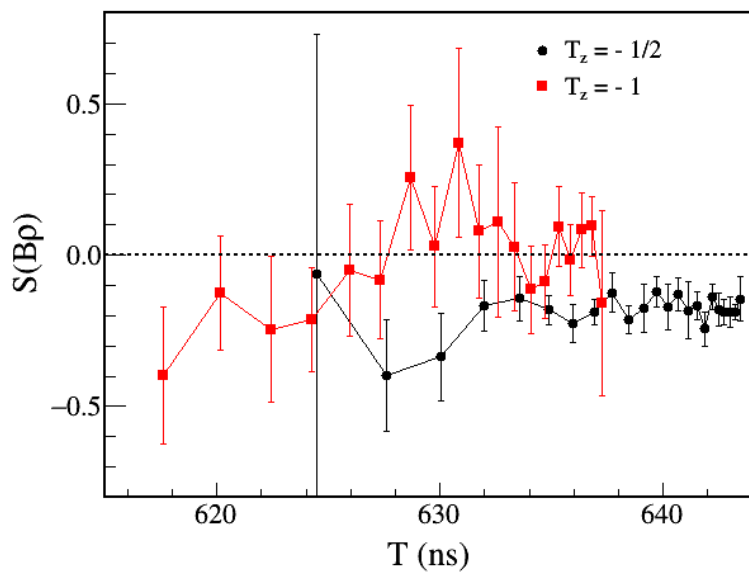
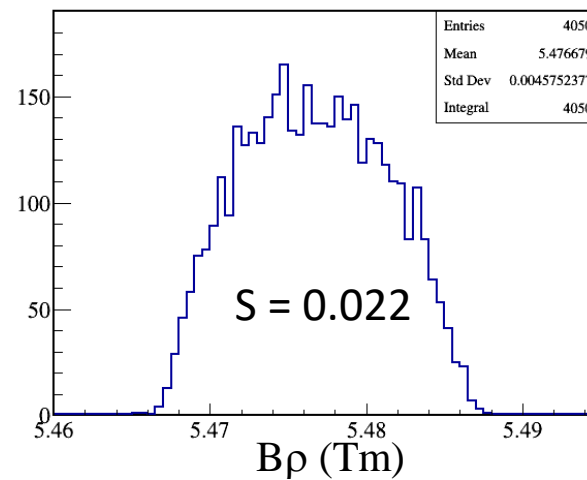
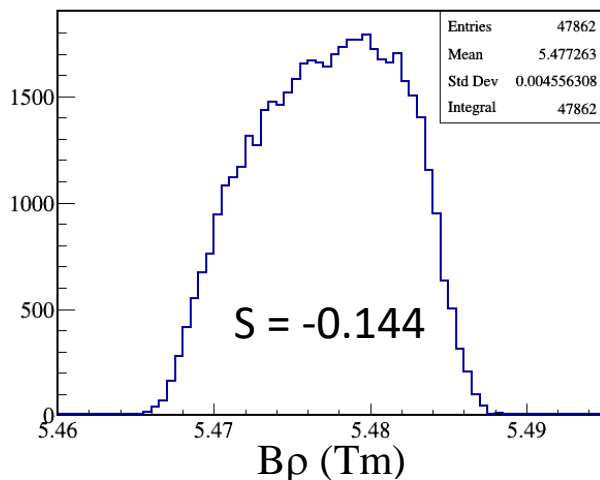
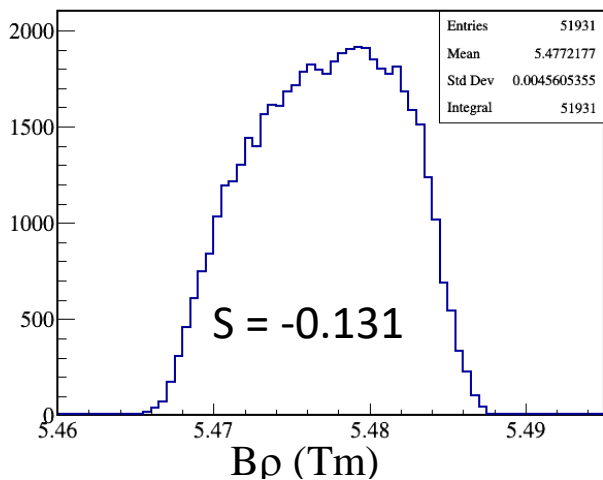
# 3. Realization of $B\rho$ -defined IMS



All ions

$T_z = -1/2$

$T_z = -1$



Obtained from T spectrum



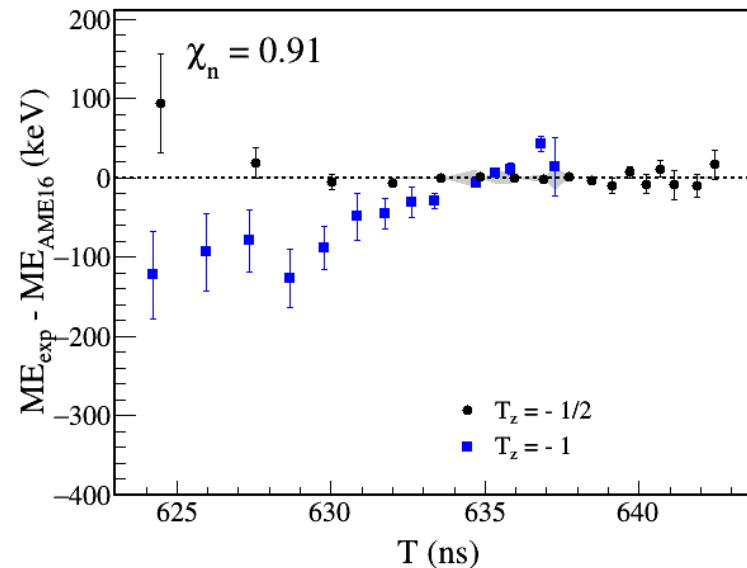
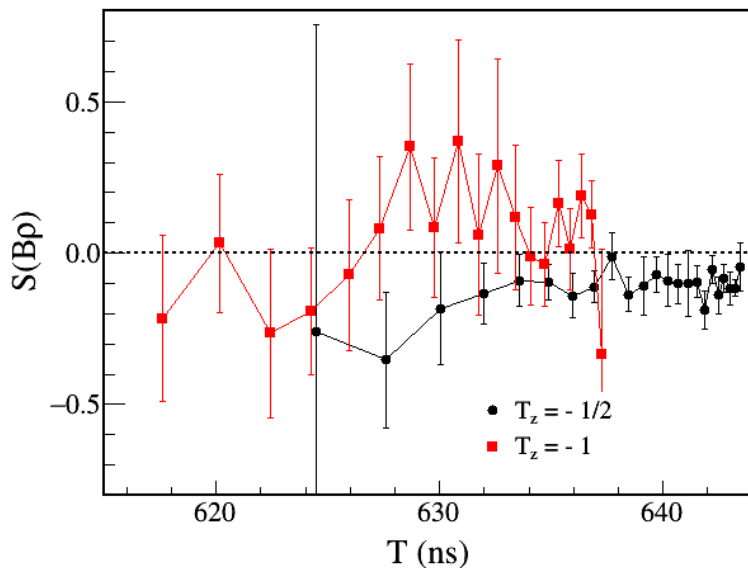
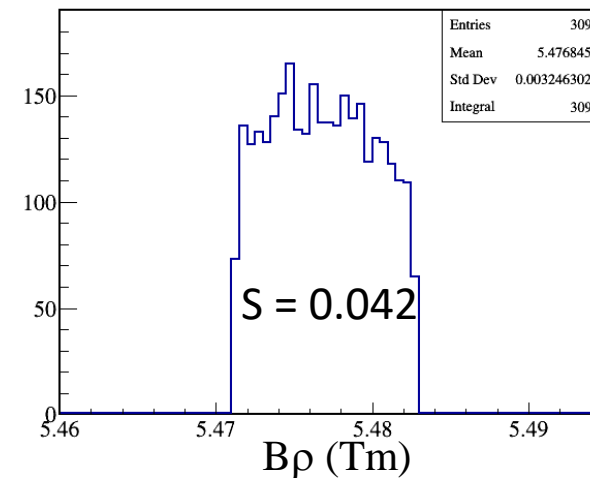
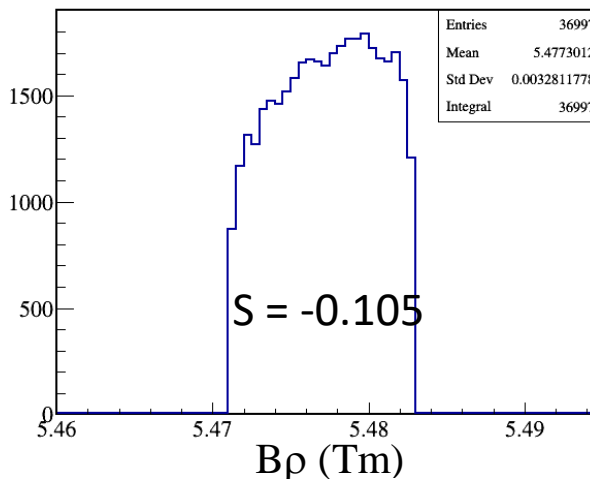
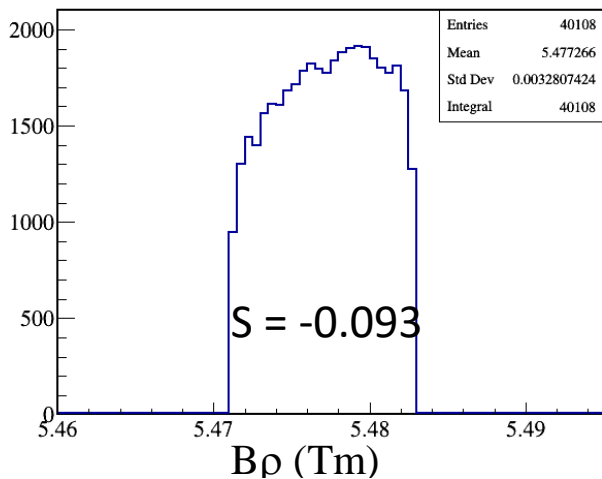
# 3. Realization of $B\rho$ -defined IMS



All ions

$T_z = -1/2$

$T_z = -1$



Obtained from T spectrum



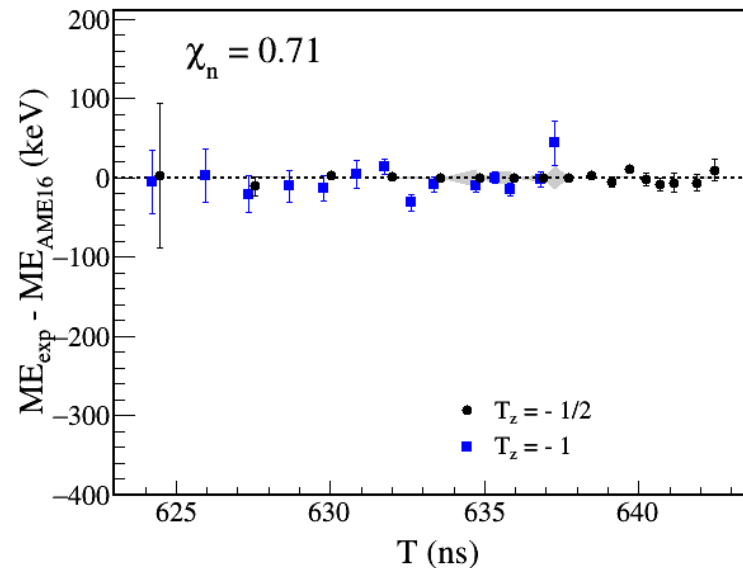
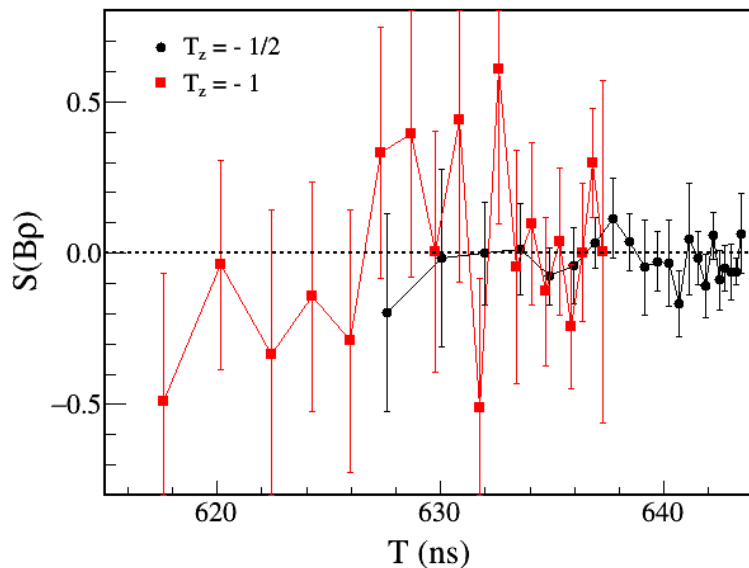
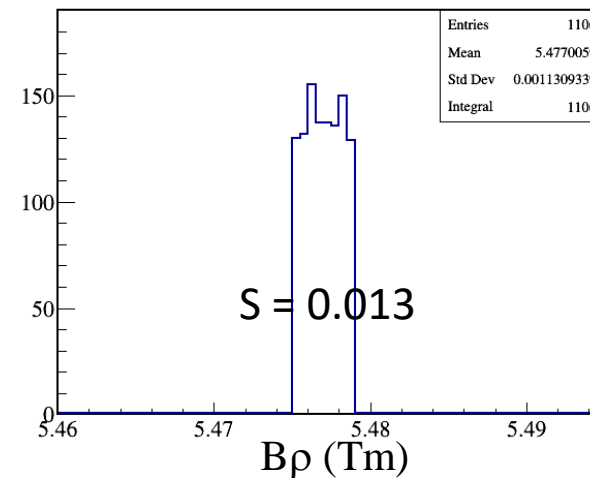
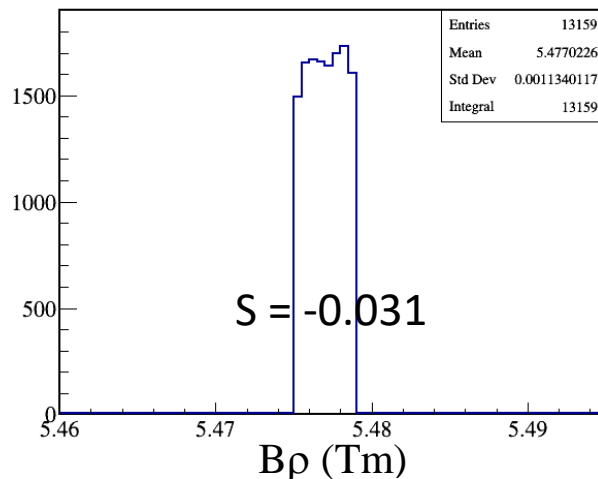
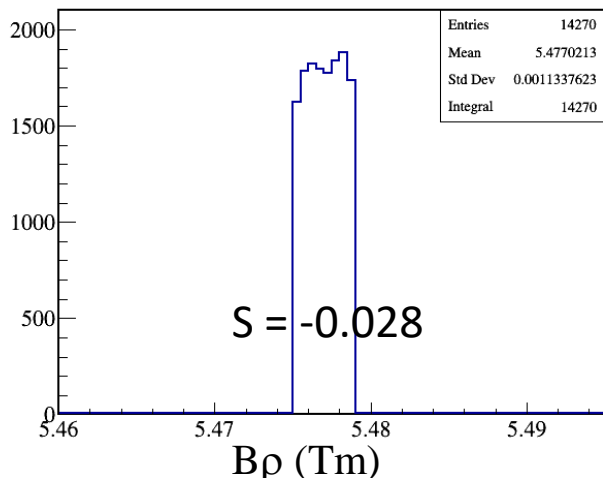
# 3. Realization of $B\rho$ -defined IMS



所有离子

$T_z = -1/2$

$T_z = -1$



Obtained from T spectrum



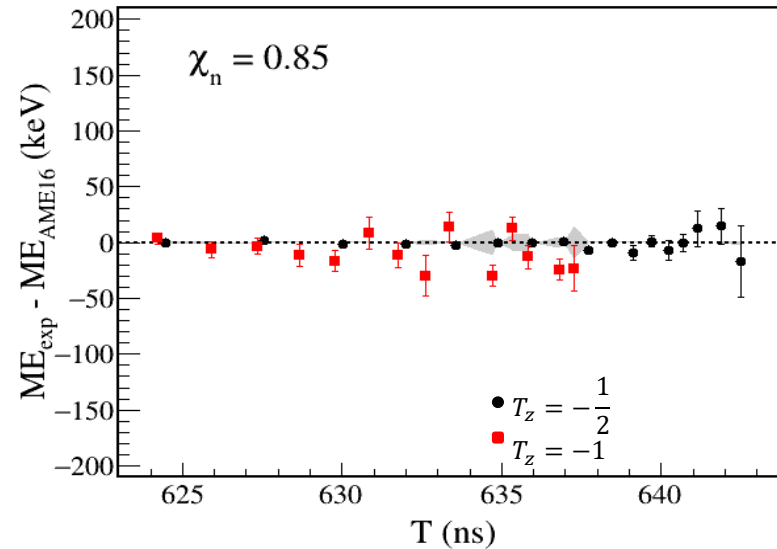
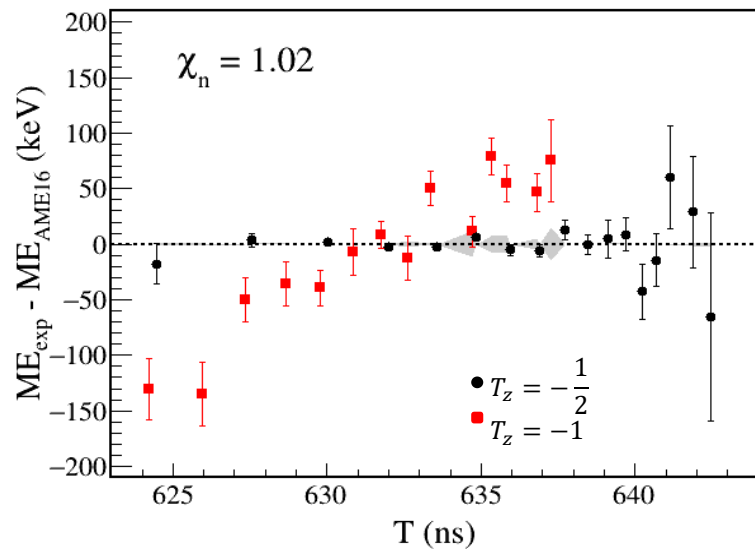
# 3. Realization of $B\rho$ -defined IMS



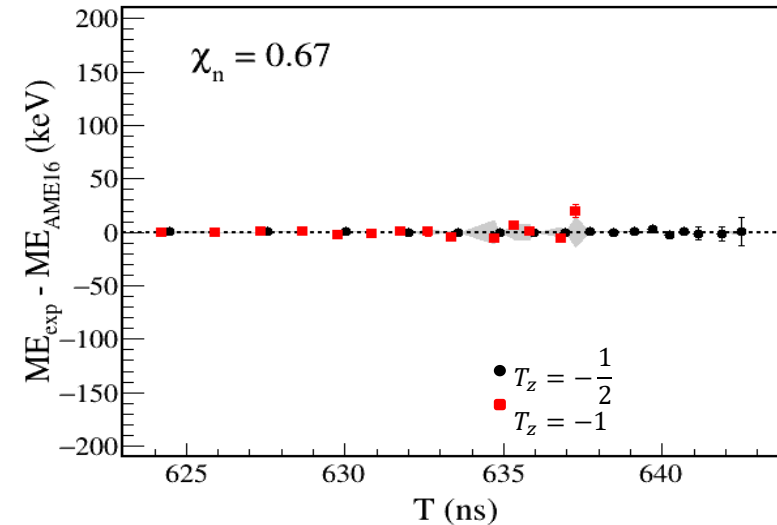
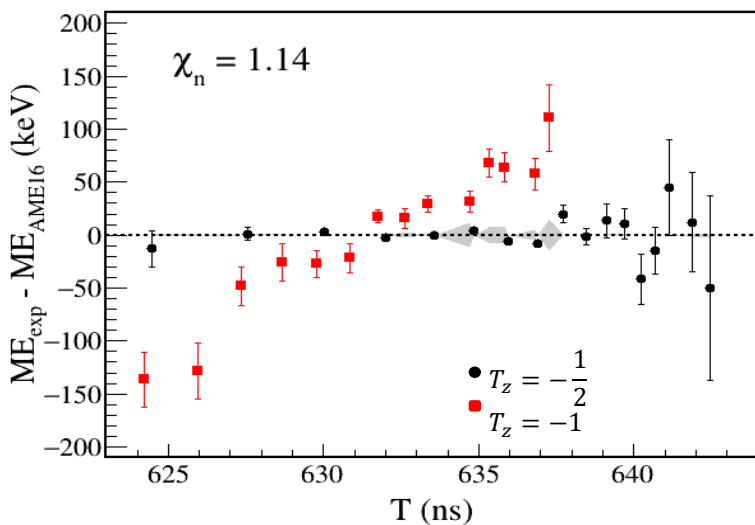
## Single TOF

## Double TOF

Without  
Field correction



With  
Field correction



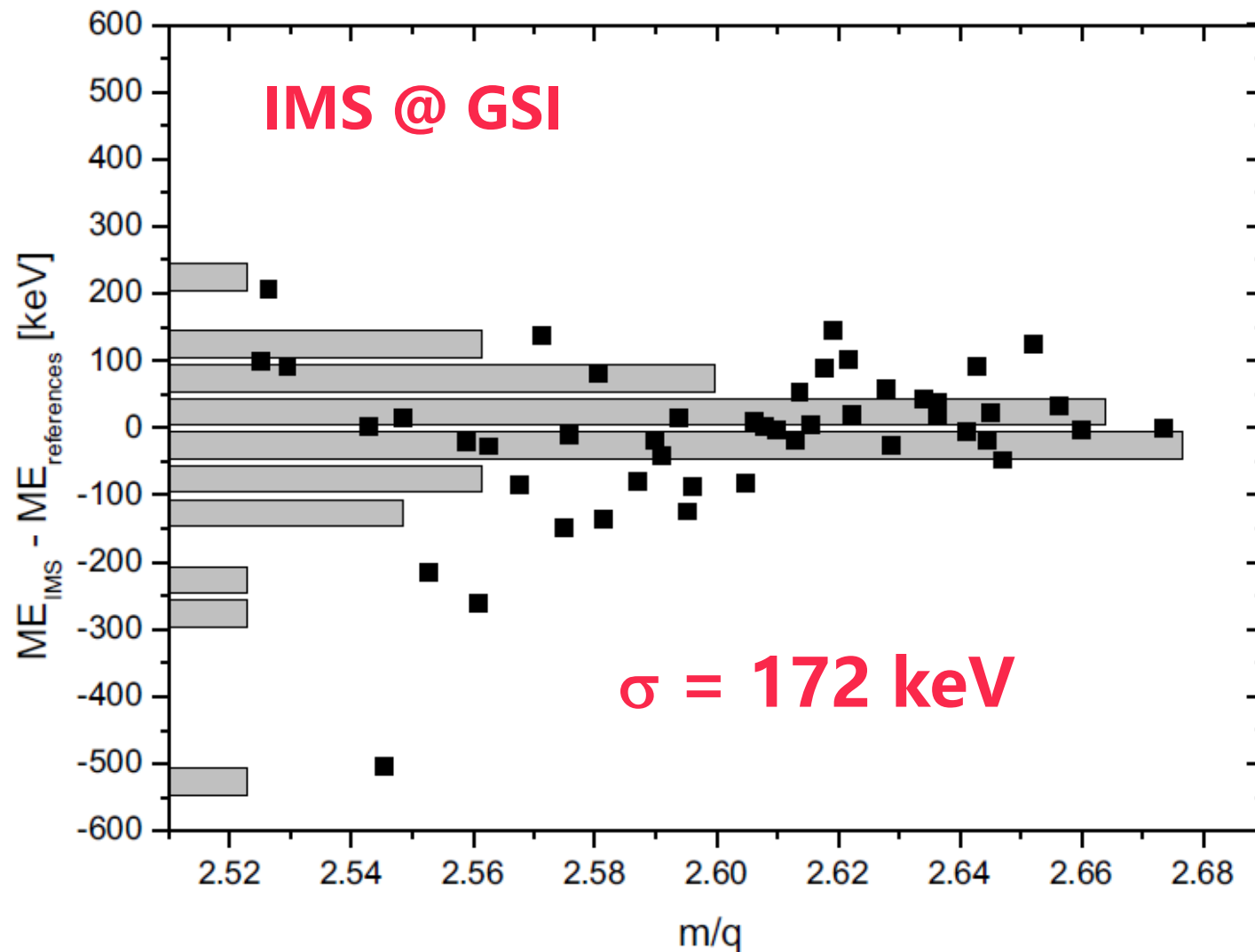
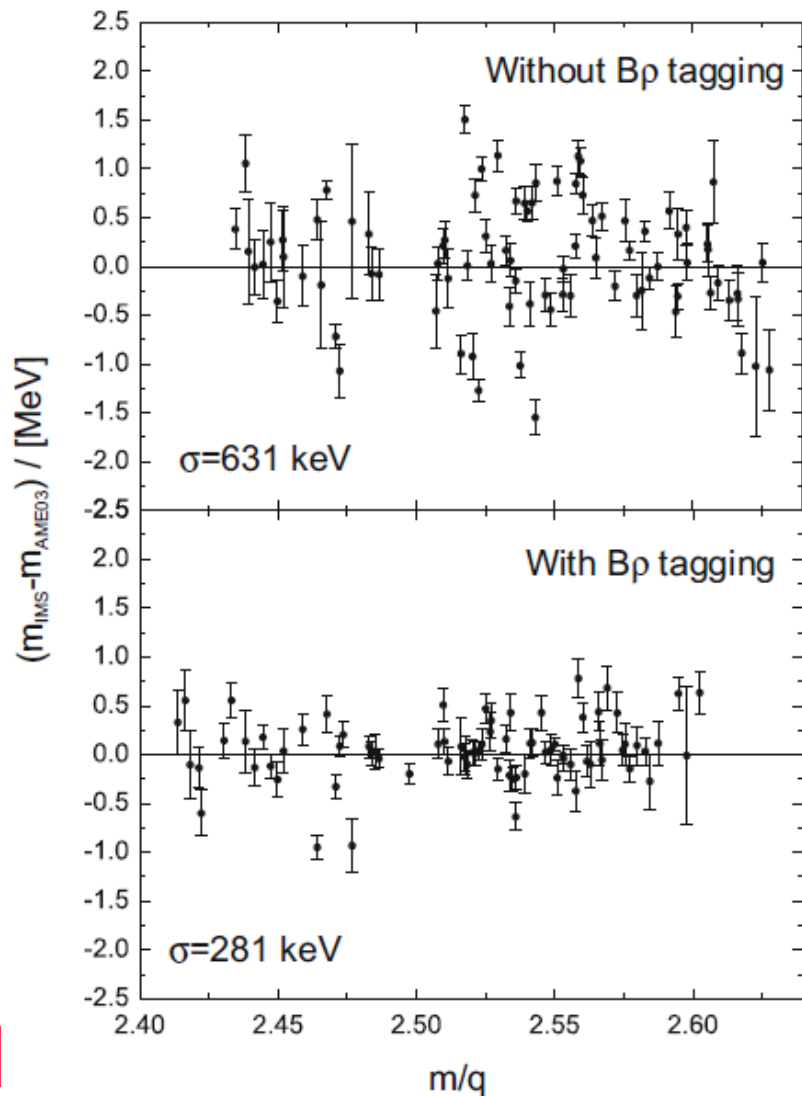


# 3. Realization of $B\beta$ -defined IMS



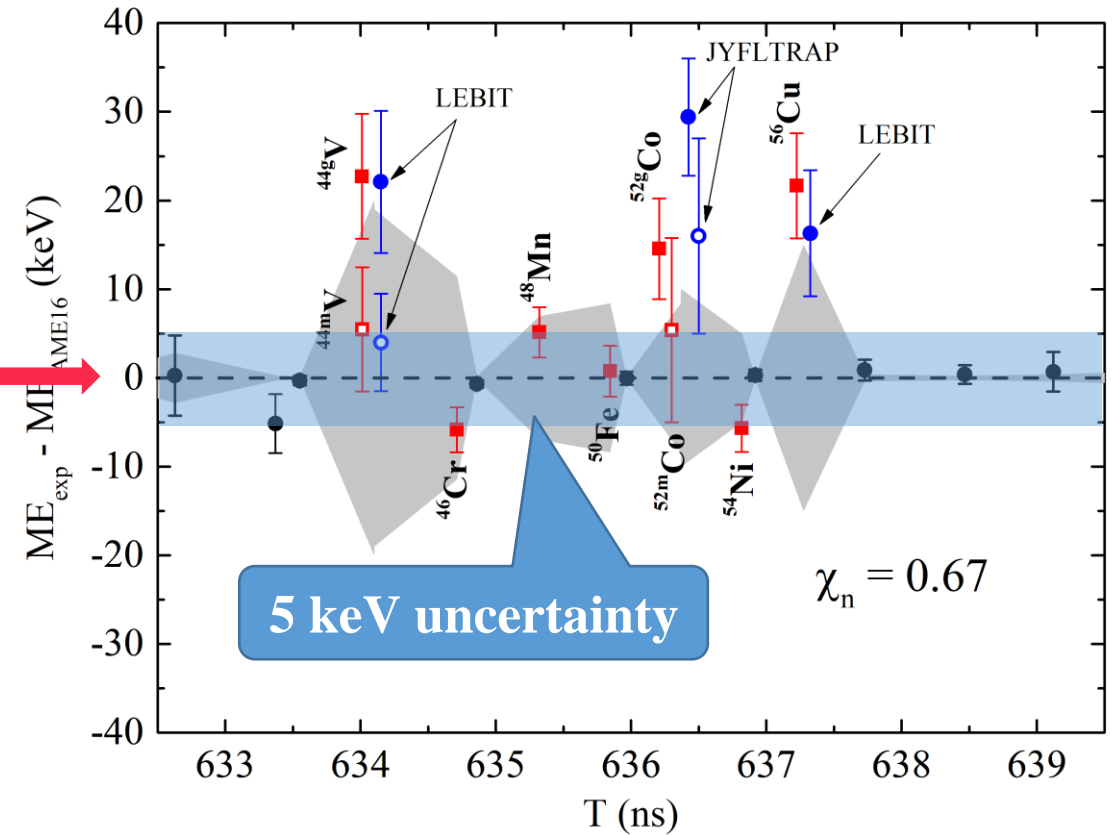
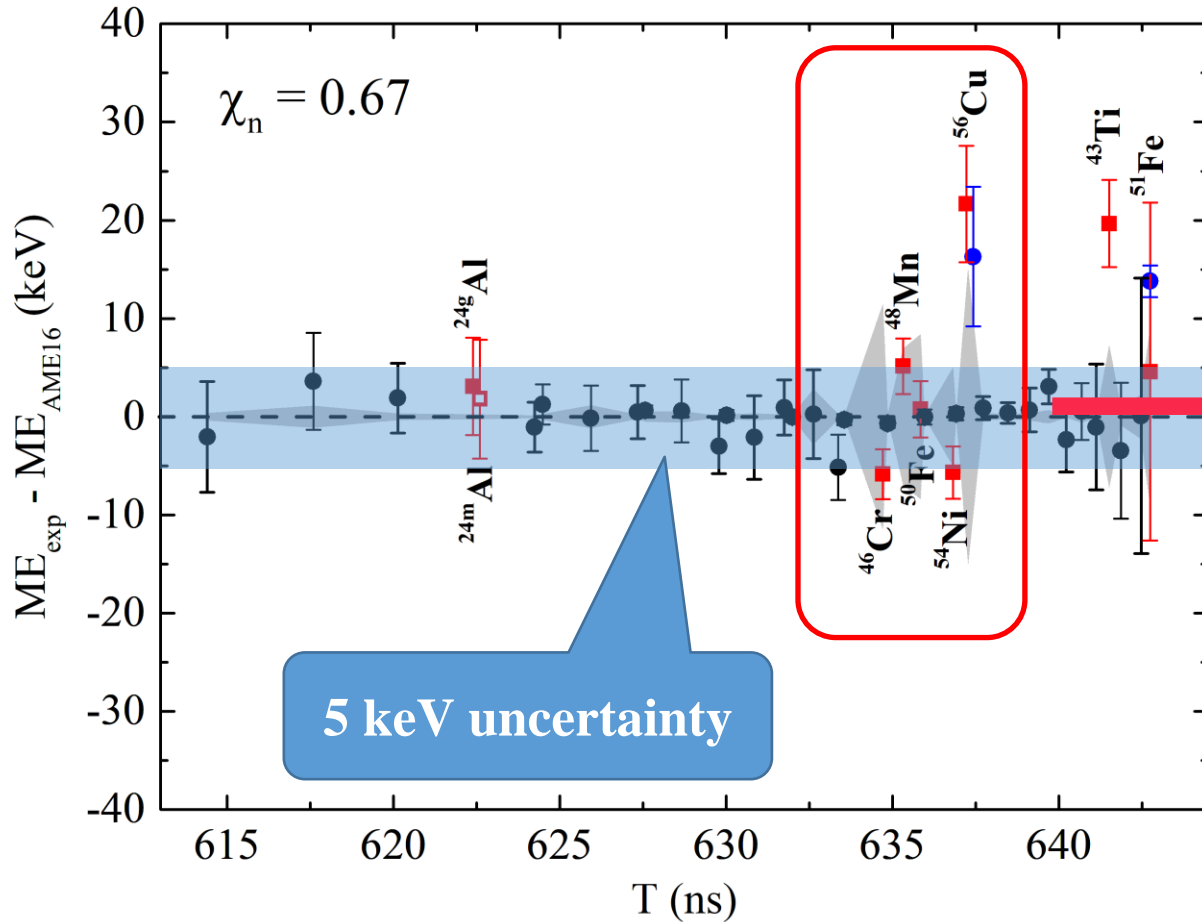
Hyperfine Interact 173: 49-54 (2006)

Eur. Phys. J. A52, 138 (2016)



# 3. Realization of $B_{\rho}$ -defined IMS

## Re-determined masses of $T_Z = -1$ nuclei

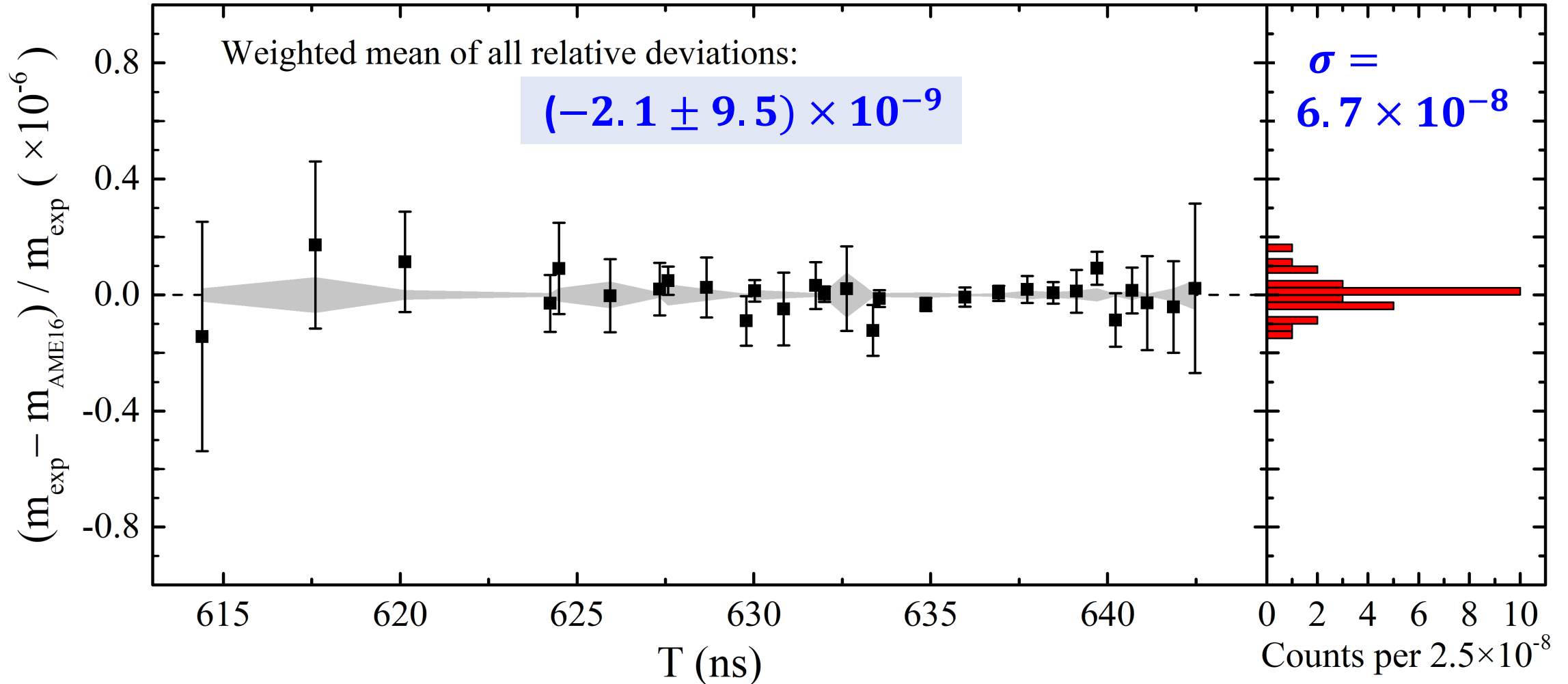




### 3. Realization of $B\rho$ -defined IMS



Check the mass accuracy of the  $B\rho$ -defined IMS





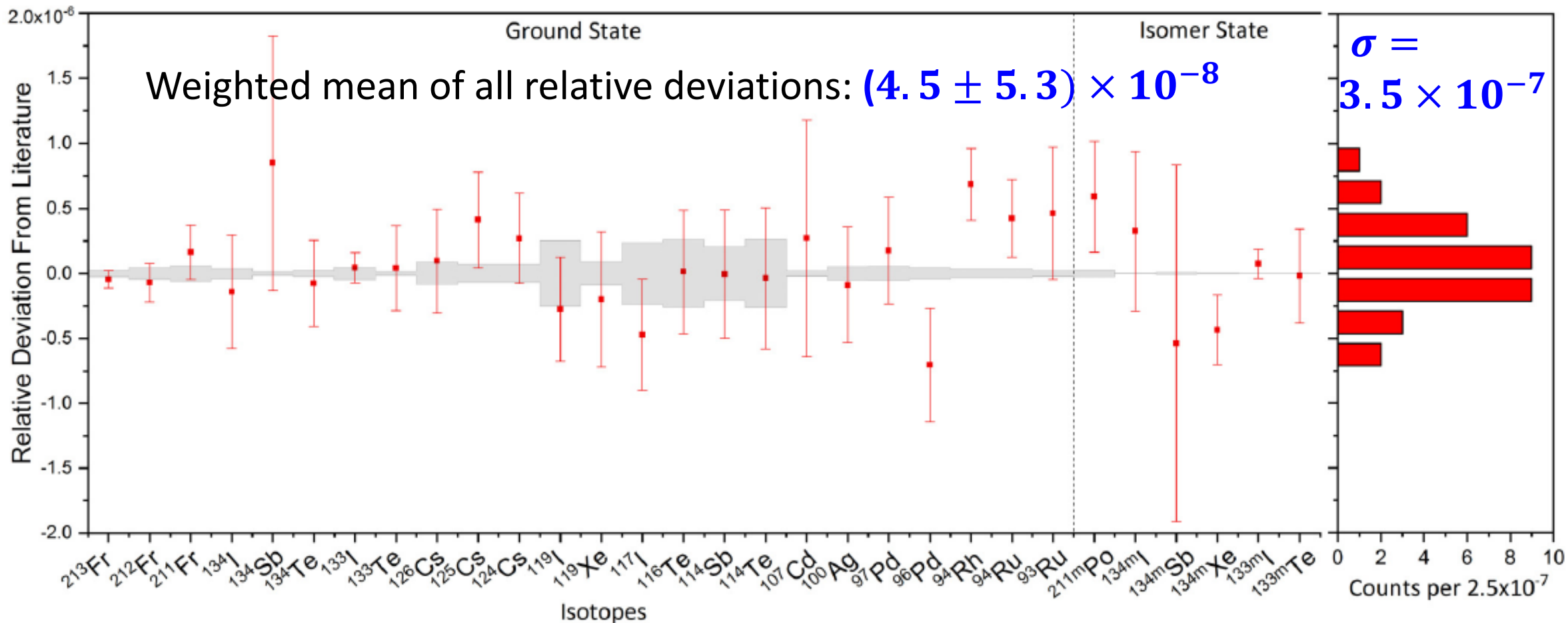


# 3. Realization of $B\rho$ -defined IMS



## Mass accuracy of the MR-TOF-MS at GSI

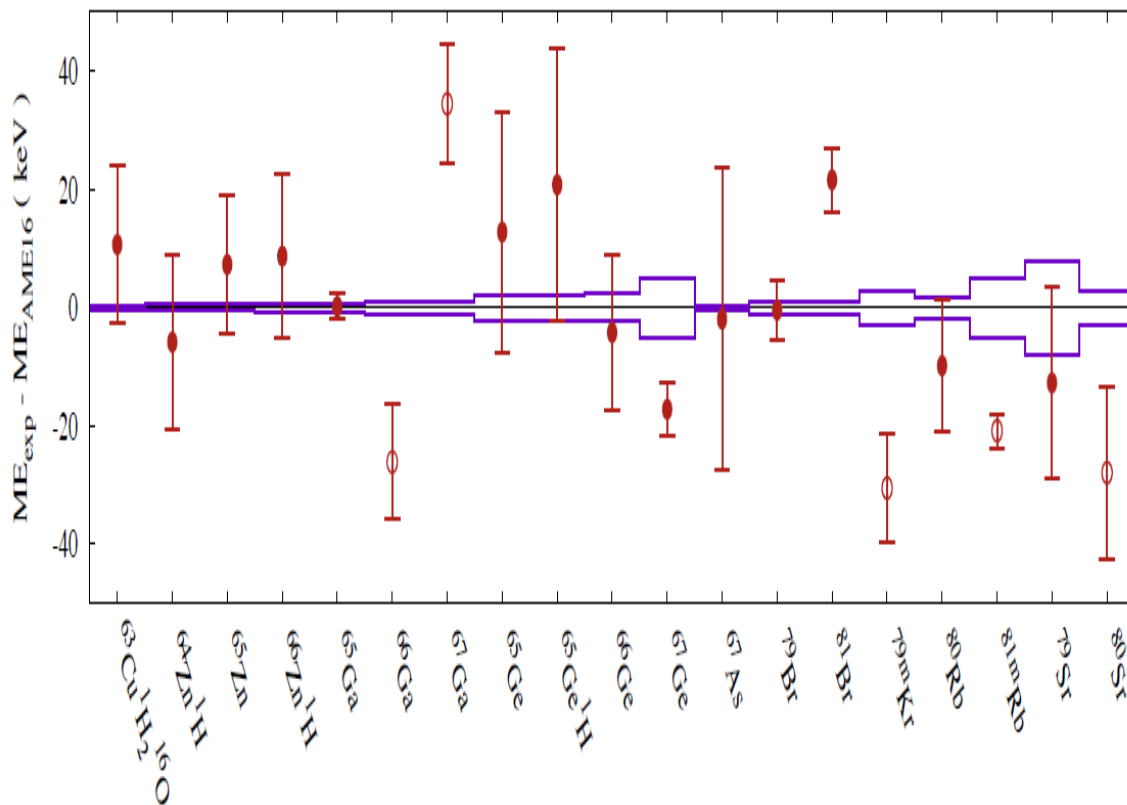
PHYSICAL REVIEW C 99, 064313 (2019)



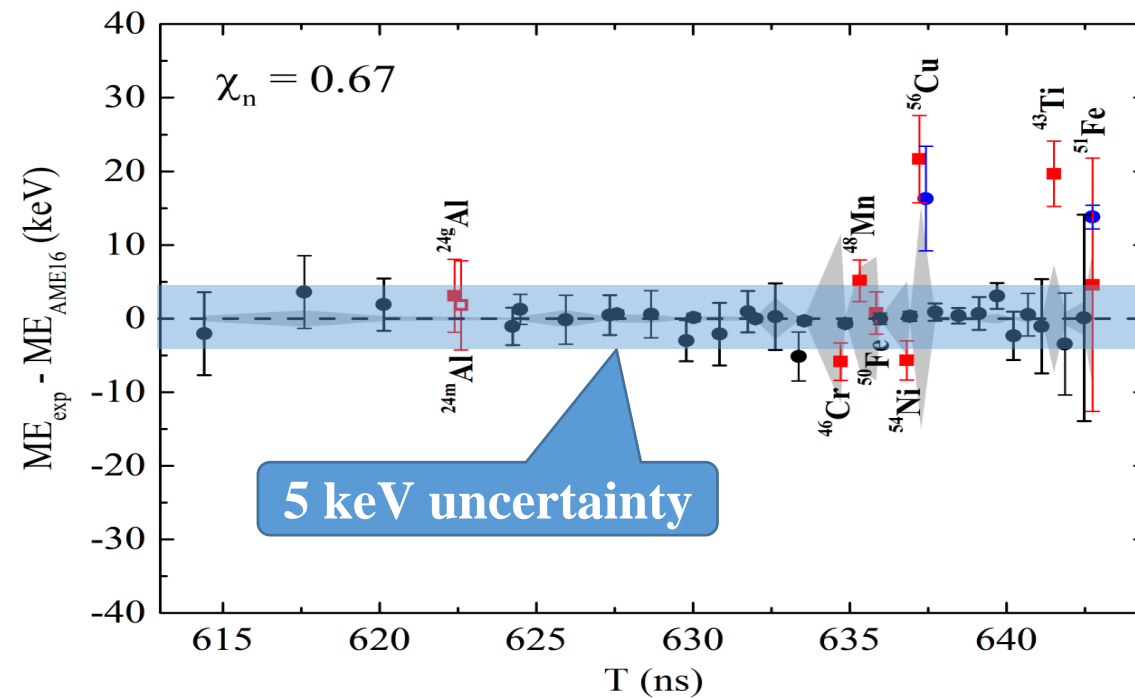
## Comparison with MR-TOF-MS@RIKEN

Mass accuracy using MR-TOF-MS at RIKEN

S. Kimura et al., IJMS 430, 134(2018)



Mass accuracy using  $B\rho$ -IMS at IMP





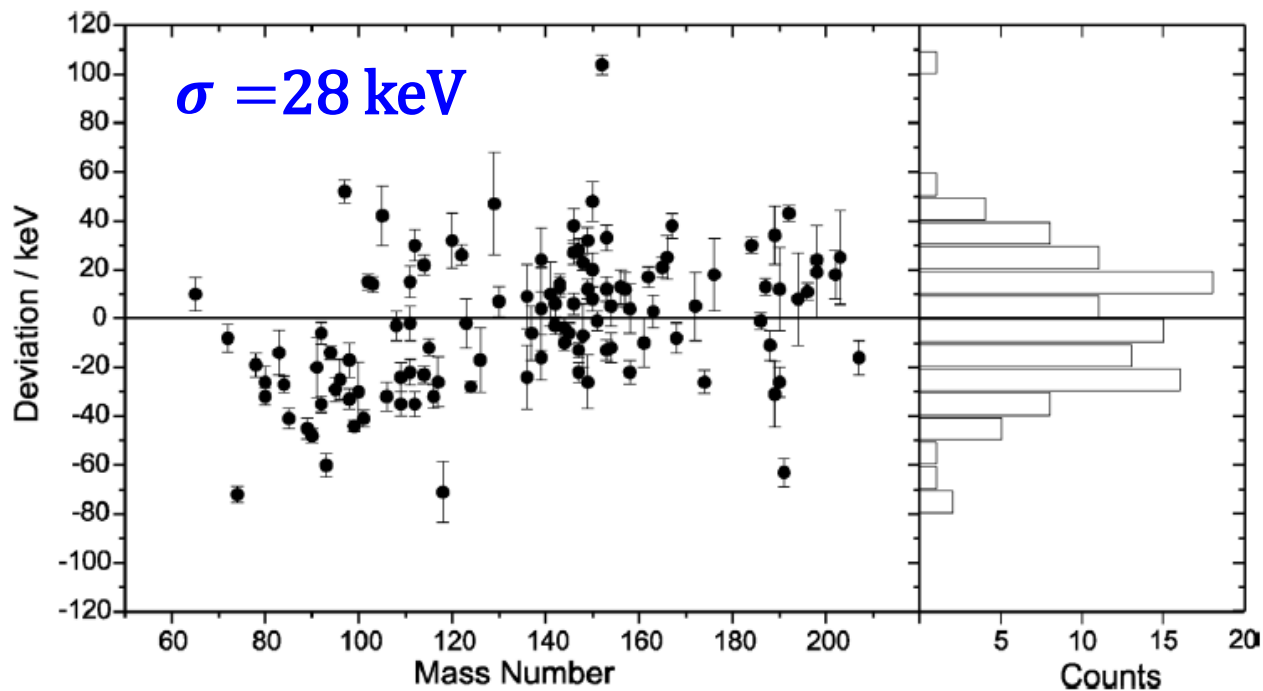
# 3. Realization of $B\rho$ -defined IMS



## Comparison with SMS @ GSI

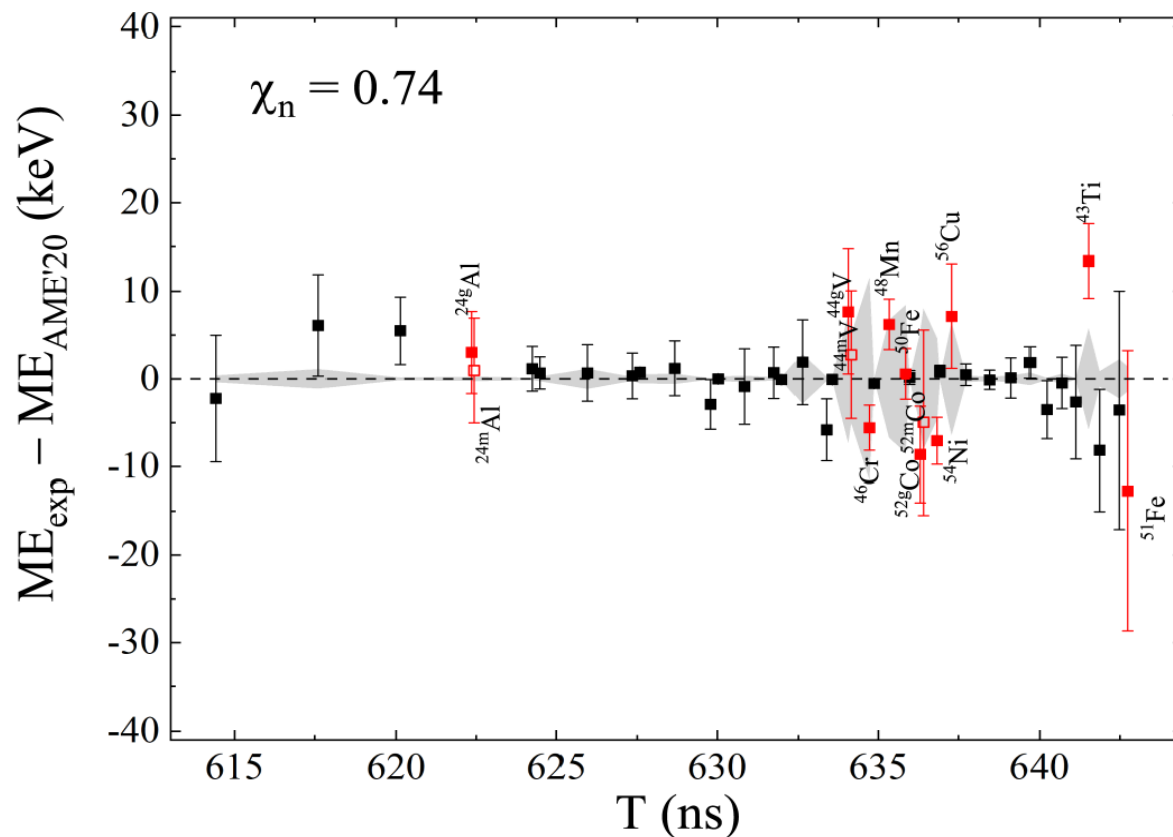
SMS at GSI

Nucl. Phys. A 756, 3 (2005)



$B\rho$ -IMS at IMP

PHYSICAL REVIEW C 106, L051301 (2022)





### 3. Realization of $B\rho$ -defined IMS



#### Advantages of $B\rho$ -defined IMS

- 1) Fast measurement:  $t_{exp} \approx 0.1 \text{ ms}$
- 2) High sensitivity: *a single ion,  $\sigma_m \approx (3\sim 5) \times q \text{ (keV)}$*
- 3) High efficiency: *tens of ions in a single run*
- 4) High precision: *on par with PTMS for short-lived nuclei*
- 5) Zero background: *background-free measurements*



# 3. Realization of $B\rho$ -defined IMS



PHYSICAL REVIEW C **106**, L051301 (2022)

Letter

## **$B\rho$ -defined isochronous mass spectrometry:** An approach for high-precision mass measurements of short-lived nuclei

M. Wang<sup>1,2,\*</sup>, M. Zhang<sup>1,2</sup>, X. Zhou<sup>1,2</sup>, Y. H. Zhang<sup>1,2,†</sup>, Yu. A. Litvinov<sup>1,3,‡</sup>, H. S. Xu<sup>1,2</sup>, R. J. Chen<sup>1,3</sup>, H. Y. Deng<sup>1,2</sup>, C. Y. Fu<sup>1</sup>, W. W. Ge<sup>1</sup>, H. F. Li<sup>1,2</sup>, T. Liao<sup>1,2</sup>, S. A. Litvinov<sup>1,3</sup>, P. Shuai<sup>1</sup>, J. Y. Shi<sup>1,2</sup>, M. Si<sup>1,2</sup>, R. S. Sidhu<sup>3</sup>, Y. N. Song<sup>1,2</sup>, M. Z. Sun<sup>1</sup>, S. Suzuki<sup>1</sup>, Q. Wang<sup>1,2</sup>, Y. M. Xing<sup>1</sup>, X. Xu<sup>1</sup>, T. Yamaguchi<sup>4</sup>, X. L. Yan<sup>1</sup>, J. C. Yang<sup>1,2</sup>, Y. J. Yuan<sup>1,2</sup>, Q. Zeng<sup>5</sup> and X. H. Zhou<sup>1,2</sup>

Eur. Phys. J. A (2023) 59:27  
<https://doi.org/10.1140/epja/s10050-023-00928-6>

THE EUROPEAN  
PHYSICAL JOURNAL A



Regular Article - Experimental Physics

## **$B\rho$ -defined isochronous mass spectrometry** and mass measurements of $^{58}\text{Ni}$ fragments

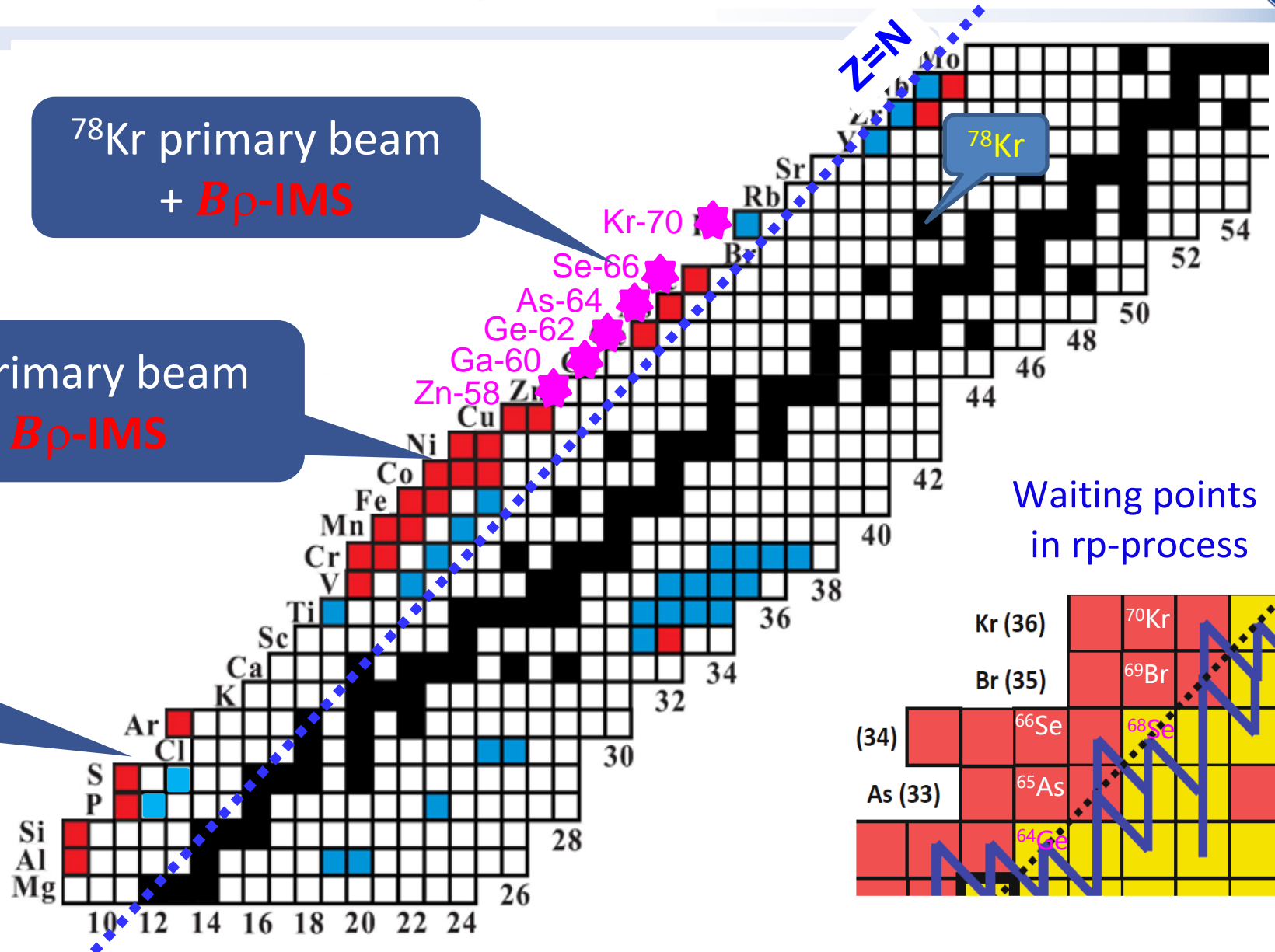
M. Zhang<sup>1,2</sup>, X. Zhou<sup>1,2</sup>, M. Wang<sup>1,2,a</sup>, Y. H. Zhang<sup>1,2,b</sup>, Yu. A. Litvinov<sup>1,3,c</sup>, H. S. Xu<sup>1,2</sup>, R. J. Chen<sup>1,3</sup>, H. Y. Deng<sup>1,2</sup>, C. Y. Fu<sup>1</sup>, W. W. Ge<sup>1</sup>, H. F. Li<sup>1,2</sup>, T. Liao<sup>1,2</sup>, S. A. Litvinov<sup>3,1</sup>, P. Shuai<sup>1</sup>, J. Y. Shi<sup>1,2</sup>, R. S. Sidhu<sup>3</sup>, Y. N. Song<sup>1,2</sup>, M. Z. Sun<sup>1</sup>, S. Suzuki<sup>1</sup>, Q. Wang<sup>1,2</sup>, Y. M. Xing<sup>1</sup>, X. Xu<sup>1</sup>, T. Yamaguchi<sup>4</sup>, X. L. Yan<sup>1</sup>, J. C. Yang<sup>1,2</sup>, Y. J. Yuan<sup>1,2</sup>, Q. Zeng<sup>5</sup>, X. H. Zhou<sup>1,2</sup>

# 4. New masses from the $B_{\rho}$ -defined IMS

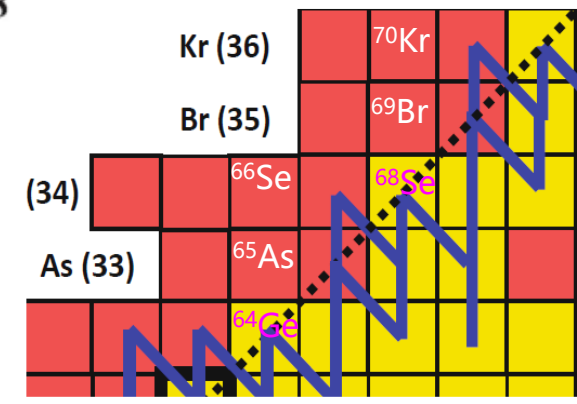
$^{78}\text{Kr}$  primary beam  
+  $B_{\rho}$ -IMS

$^{58}\text{Ni}$  primary beam  
+  $B_{\rho}$ -IMS

$^{36}\text{Ar}$  primary beam  
+  $B_{\rho}$ -IMS



Waiting points  
in rp-process





# 4. New masses from the $B_{\rho}$ -defined IMS



M. Zhang et al., Eur. Phys. J. A 59: 27(2023)

$^{58}\text{Ni}$  beam

**Table 1** Experimental mass excesses (MEs) obtained from this work (third column), from an earlier CSRe measurement (fourth column) [19,39–41] and from the literatures (sixth column). Also the

recent Penning-trap measurements for  $^{44g,44m}\text{V}$  [42],  $^{52g,52m}\text{Co}$  [43],  $^{56}\text{Cu}$  [44],  $^{51}\text{Fe}$  [45] and AME2016 for  $^{43}\text{Ti}$  [46] are included. All ME units are in keV

Atom	Number of events	ME This work	ME Earlier CSRe	$\Delta\text{ME}_{\text{CSRe}}$	ME Literature	$\text{ME}_{\text{CSRe}} - \text{ME}_{\text{Lit}}$
$^{44g}\text{V}$	334	-23800.4(71)	-23827(20)	-26(21)	-23804.9(80) [42]	-4.5(110)
$^{44m}\text{V}$	267	-23534.3(73)	-23541(19)	-6(20)	-23537.0(55) [42]	-2.7(91)
$^{46}\text{Cr}$	745	-29477.2(26)	-29471(11)	6(11)		
$^{48}\text{Mn}$	685	-29290.4(29)	-29299(7)	-9(8)		
$^{50}\text{Fe}$	782	-34475.8(29)	-34477(6)	-1(7)		
$^{52g}\text{Co}$	609	-34352.6(55)	-34361(8)	-8(10)	-34331.6(66) [43]	21(9)
$^{52m}\text{Co}$	236	-33973.0(106)	-33974(10)	-2(15)	-33958(11) [43]	15(15)
$^{54}\text{Ni}$	1254	-39285.4(27)	-39278.3(40)	7(5)		
$^{56}\text{Cu}$	294	-38622.6(60)	-38643(15)	-21(16)	-38626.7(71) [44]	-3.9(93)
$^{41}\text{Ti}$	25	-15724.3(187)	-15697.5(279)	27(37)		
$^{43}\text{V}$	9	-17899.3(316)	-17916.4(428)	-17(53)		
$^{45}\text{Cr}$	57	-19474.6(110)	-19514.8(354)	-40(37)		
$^{47}\text{Mn}$	18	-22560.8(192)	-22566.4(317)	-5.6(370)		
$^{49}\text{Fe}$	86	-24671.6(84)	-24750.7(242)	-79(27)		
$^{51}\text{Co}$	48	-27386.0(115)	-27342.1(484)	44(50)		
$^{53}\text{Ni}$	168	-29613.7(58)	-29630.8(252)	-17(26)		
$^{55}\text{Cu}$	11	-31807.0(248)	-31635(156)	172(158)		
$^{43}\text{Ti}$	757	-29302.2(42)	-29306(9)	-4(10)	-29321(7) [46]	19(8)
$^{51}\text{Fe}$	108	-40201.9(159)	-40198(14)	4(21)	-40189.2(14) [45]	13(16)



# 4. New masses from the $B_{\rho}$ -defined IMS



$^{78}\text{Kr}$  beam

M. Wang et al., Phys. Rev. Lett. 130, 192501 (2023)

Atom	Counts	$\text{ME}_{\text{IMS}}$ (keV)	$\text{ME}_{\text{AME}'20}$ (keV)	$\Delta\text{ME}$ (keV)
$^{58}\text{Zn}$	51	-42 248(36)	-42 300(50)	51(62)
$^{60}\text{Ga}$	32	-40 034(46)	-39 590(200) <sup>b</sup>	-440(210) <sup>b</sup>
$^{62}\text{Ge}$	47	-42 289(37)	-42 140(140) <sup>b</sup>	-150(140) <sup>b</sup>
$^{64}\text{As}^{\text{a}}$	6	-39 710(110)	-39 530(200) <sup>b</sup>	-170(230) <sup>b</sup>
$^{66}\text{Se}^{\text{a}}$	20	-41 982(61)	-41 660(200) <sup>b</sup>	-320(210) <sup>b</sup>
$^{70}\text{Kr}$	4	-41 320(140)	-41 100(200) <sup>b</sup>	-220(250) <sup>b</sup>
$^{61}\text{Ga}$	124	-47 168(21)	-47 135(38)	-33(43)
$^{63}\text{Gs}^{\text{a}}$	279	-46 978(15)	-46 921(37)	-57(40)
$^{65}\text{As}^{\text{a}}$	33	-46 806(42)	-46 937(85)	131(95)
$^{67}\text{Se}^{\text{a}}$	174	-46 549(20)	-46 580(67)	32(70)
$^{71}\text{Kr}$	148	-46 056(24)	-46 327(129)	270(130)
$^{75}\text{Sr}$	4	-46 200(150)	-46 620(220)	420(260)



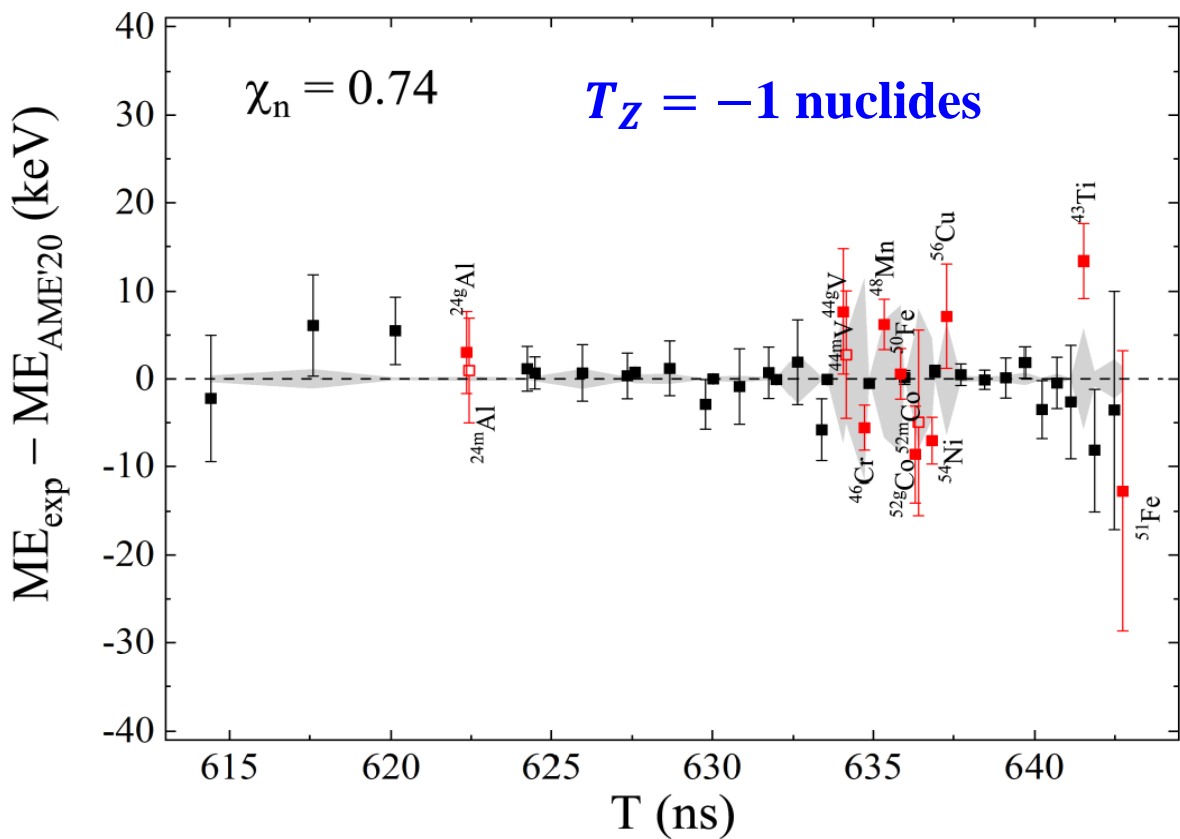


# 4. New masses from the $B_{\rho}$ -defined IMS

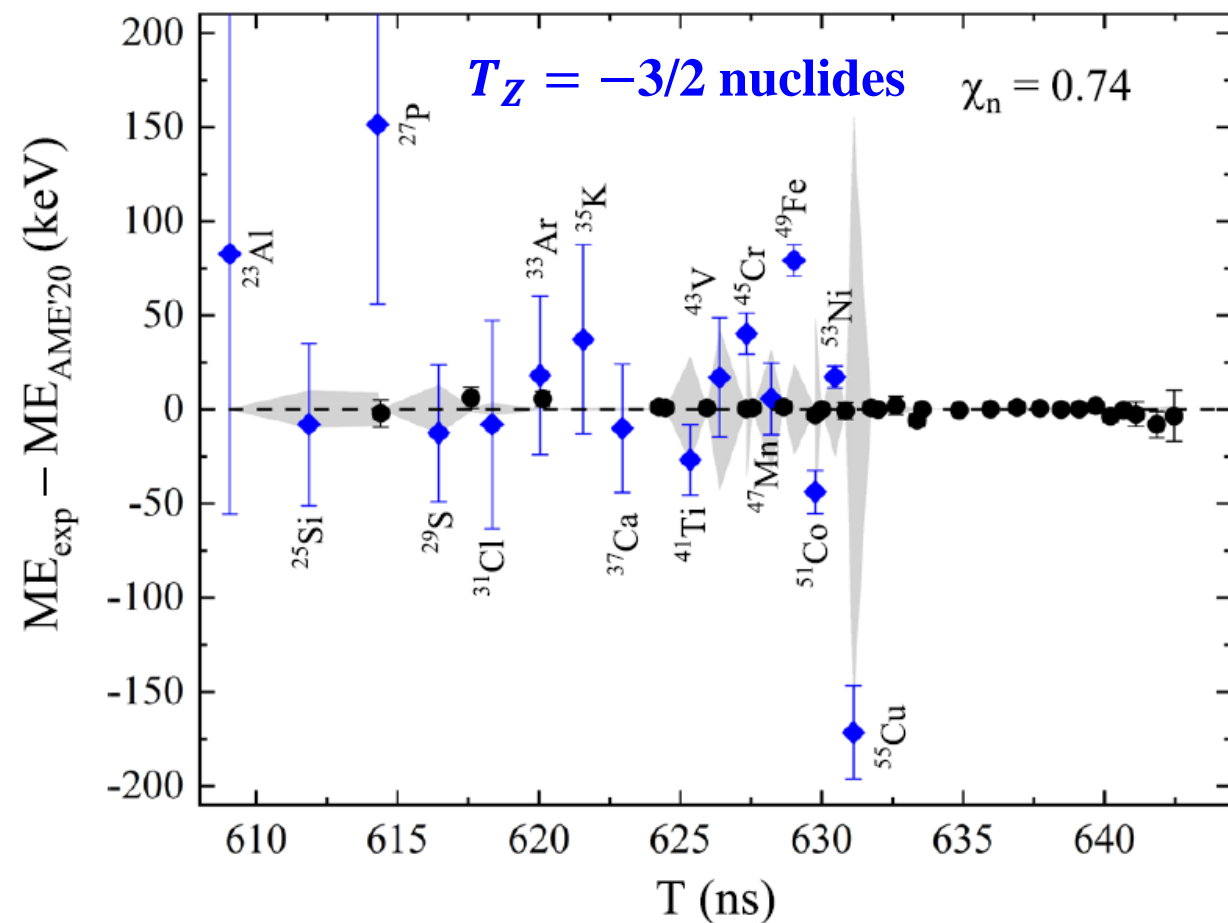


## $^{58}\text{Ni}$ beam

M. Wang et al., PRC 106, L051301(2022)



M. Zhang et al., Eur. Phys. J. A 59: 27(2023)

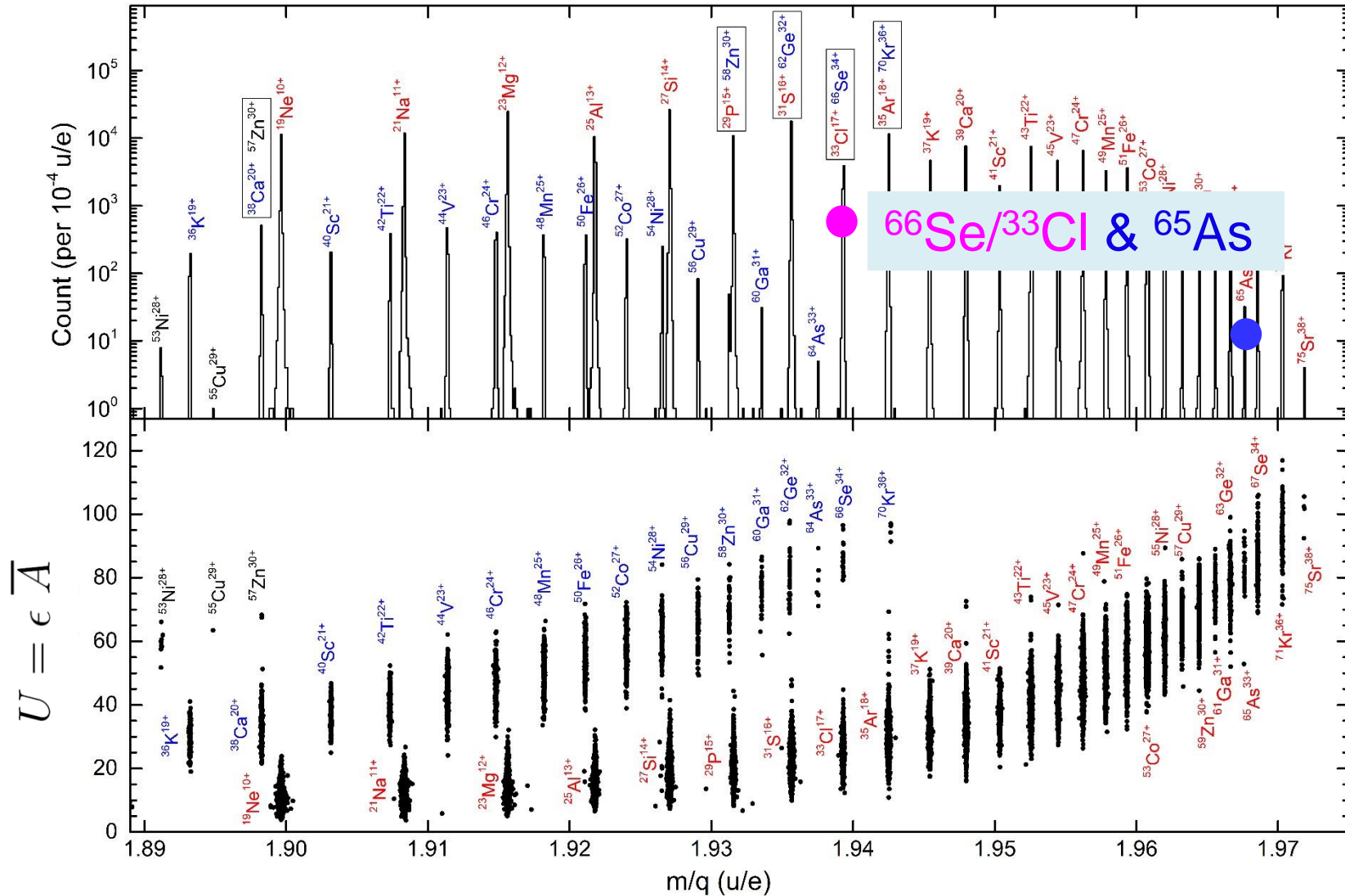




# 4. New masses from the $B_{\rho}$ -defined IMS

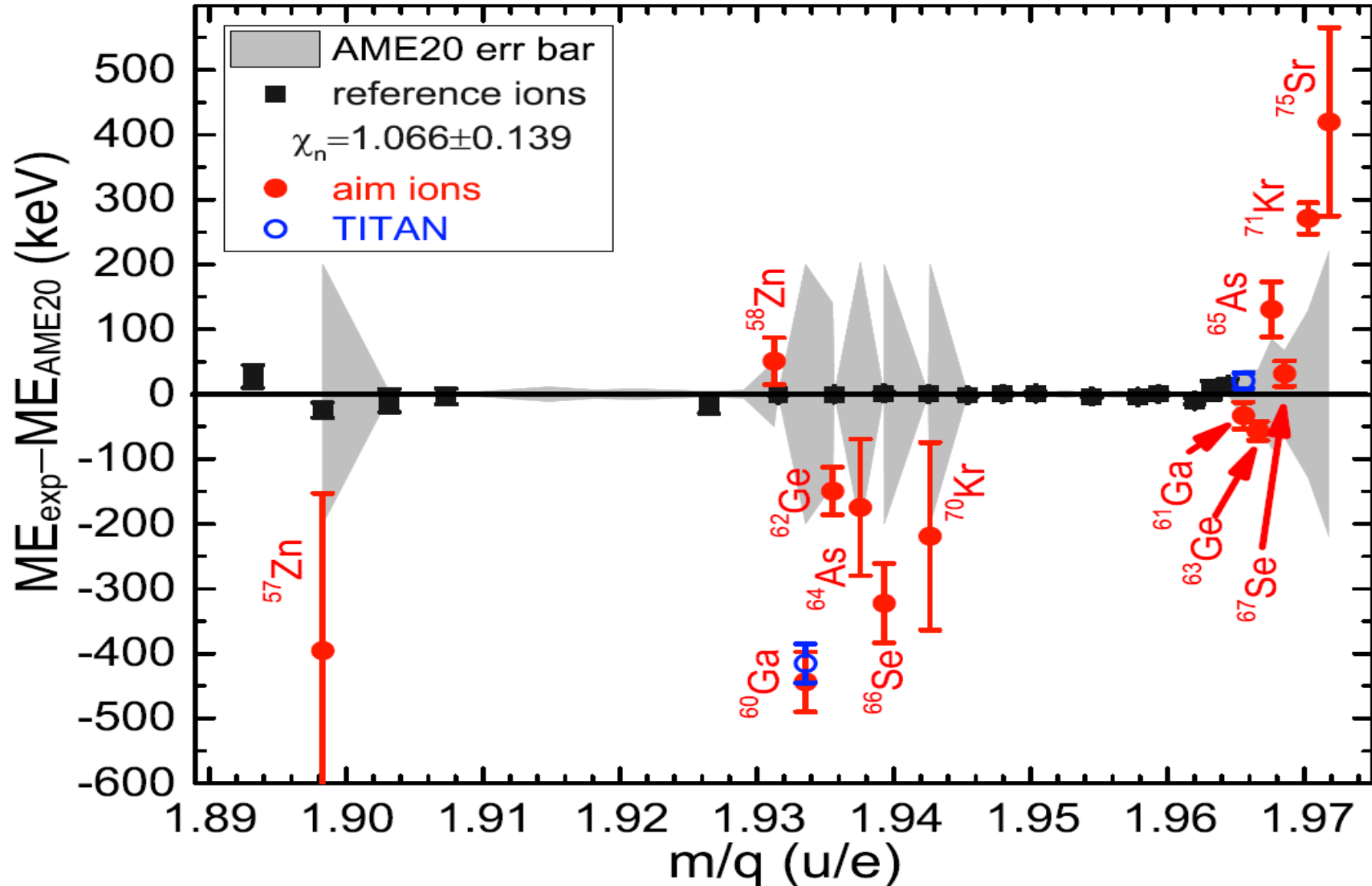


$^{78}\text{Kr}$  beam



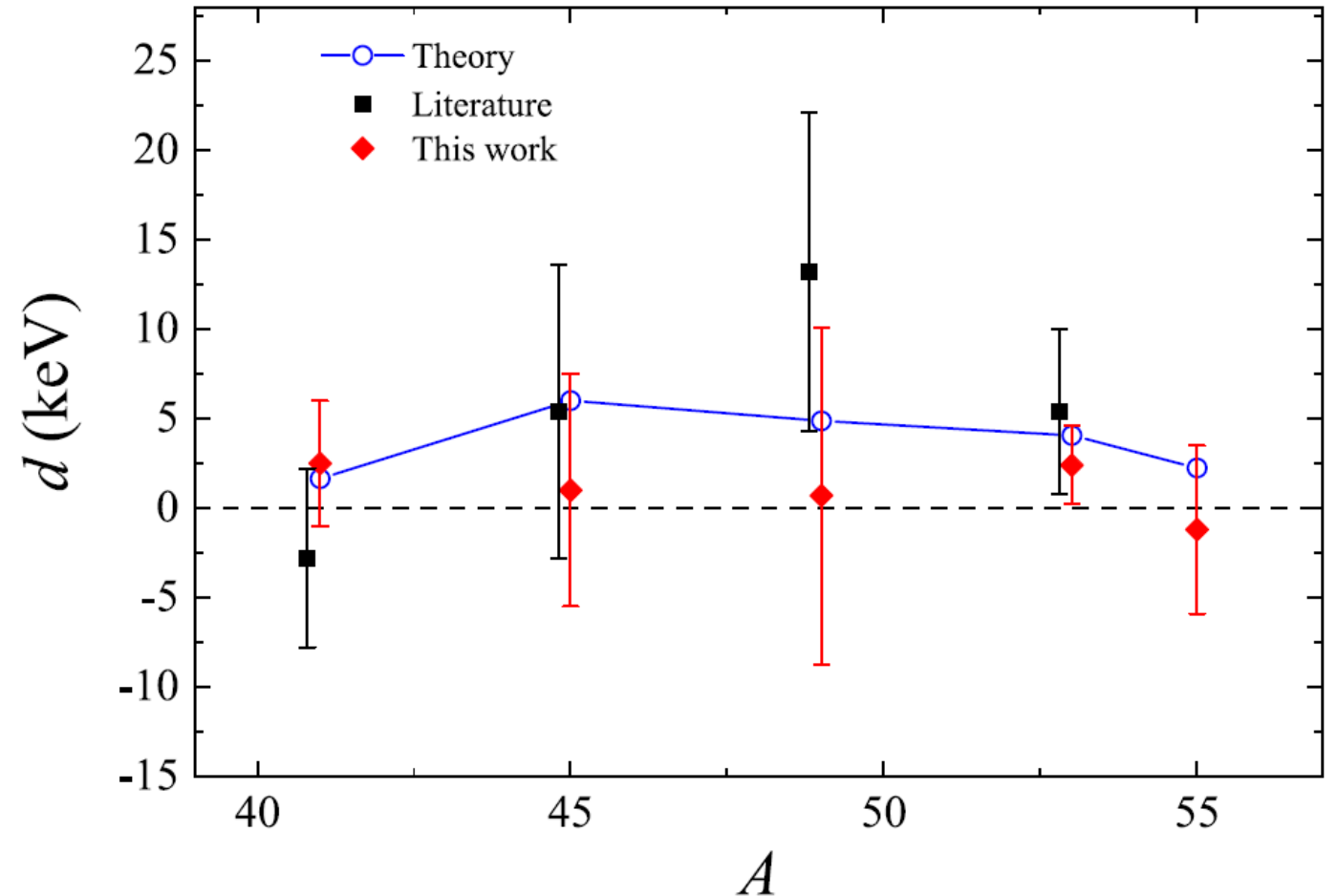
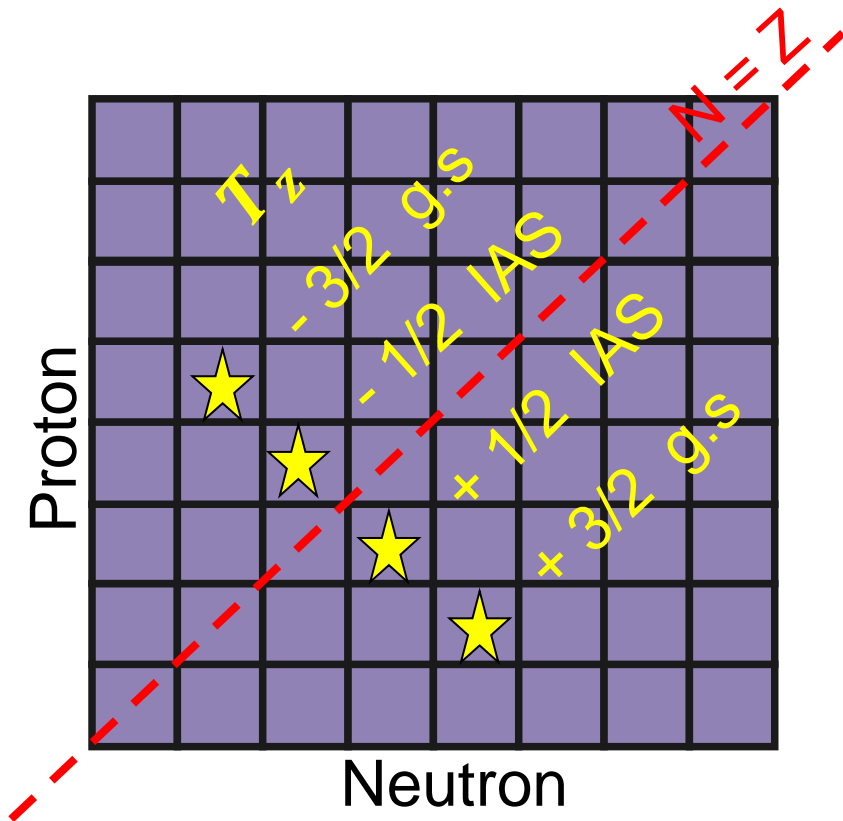
# 4. New masses from the $B\rho$ -defined IMS

$^{78}\text{Kr}$  beam



$$M(A, T, T_z) = a(A, T) + b(A, T)T_z + c(A, T)T_z^2 + d(A, T)T_z^3$$

M. Zhang et al., Eur. Phys. J. A 59: 27(2023)



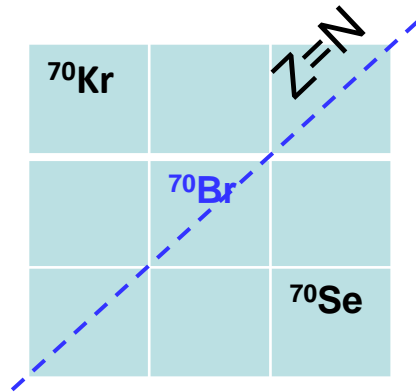


# The ground state mass of $^{70}\text{Br}$ (W.J. Huang et al., PRC submitted)



IMME:

$$M(A, T, T_z) = a(A, T) + b(A, T)T_z + c(A, T)T_z^2$$



Isovector component of NN interaction

Isotensor component of NN interaction

Coulomb interaction is the main contributor

$$b = (M_1 - M_{-1})/2$$

Charge symmetry

$$c = \frac{M_1 + M_{-1}}{2} - M_0$$

Charge independence

Average properties like Coulomb radius or pairing

Sensitive to the WF of valence particles which contains particular nuclear structure information

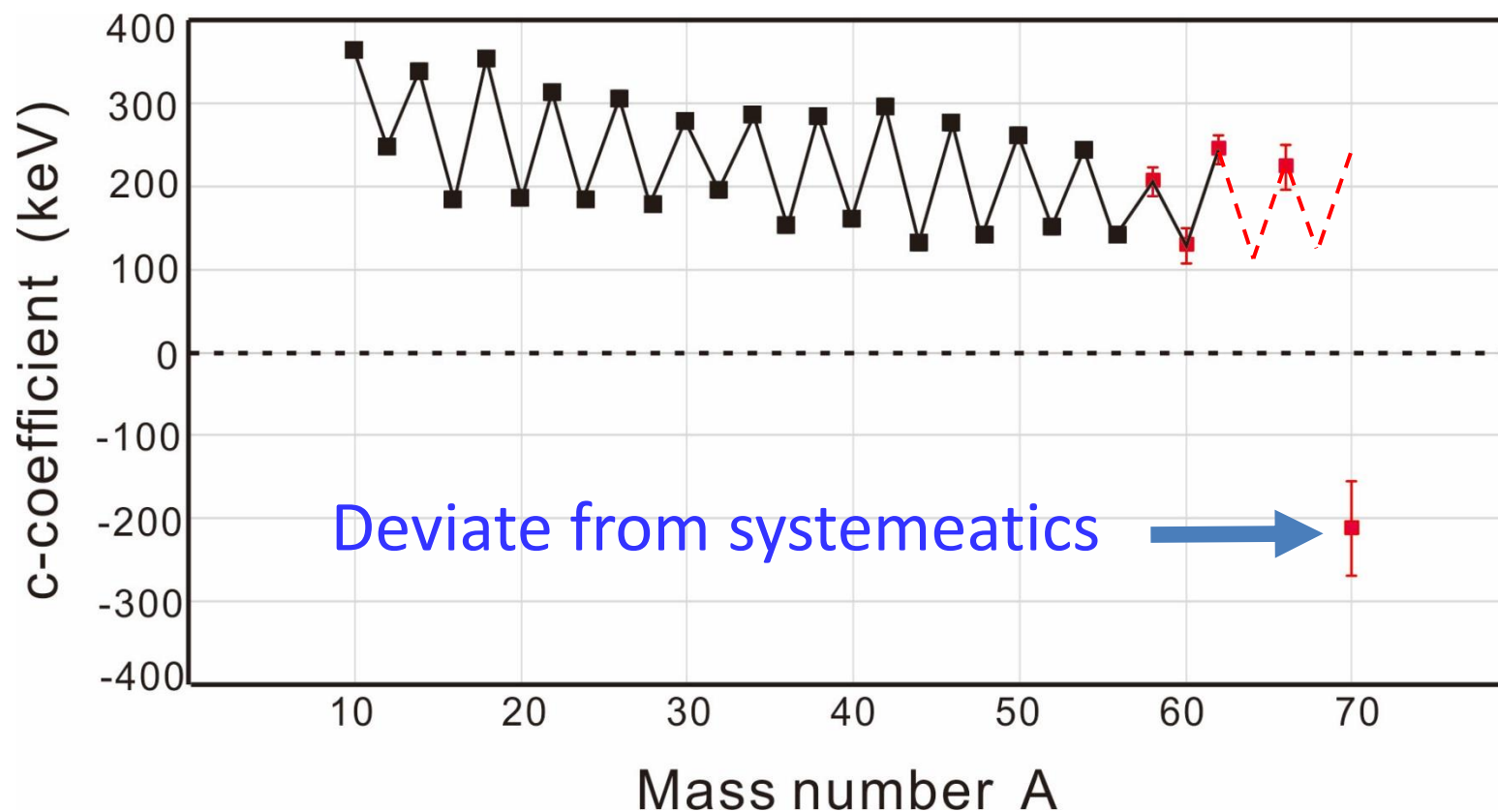


# The ground state mass of $^{70}\text{Br}$ (W.J. Huang et al., PRC submitted)



For T=1 multiplets

$$c = \frac{M_1 + M_{-1}}{2} - M_0$$



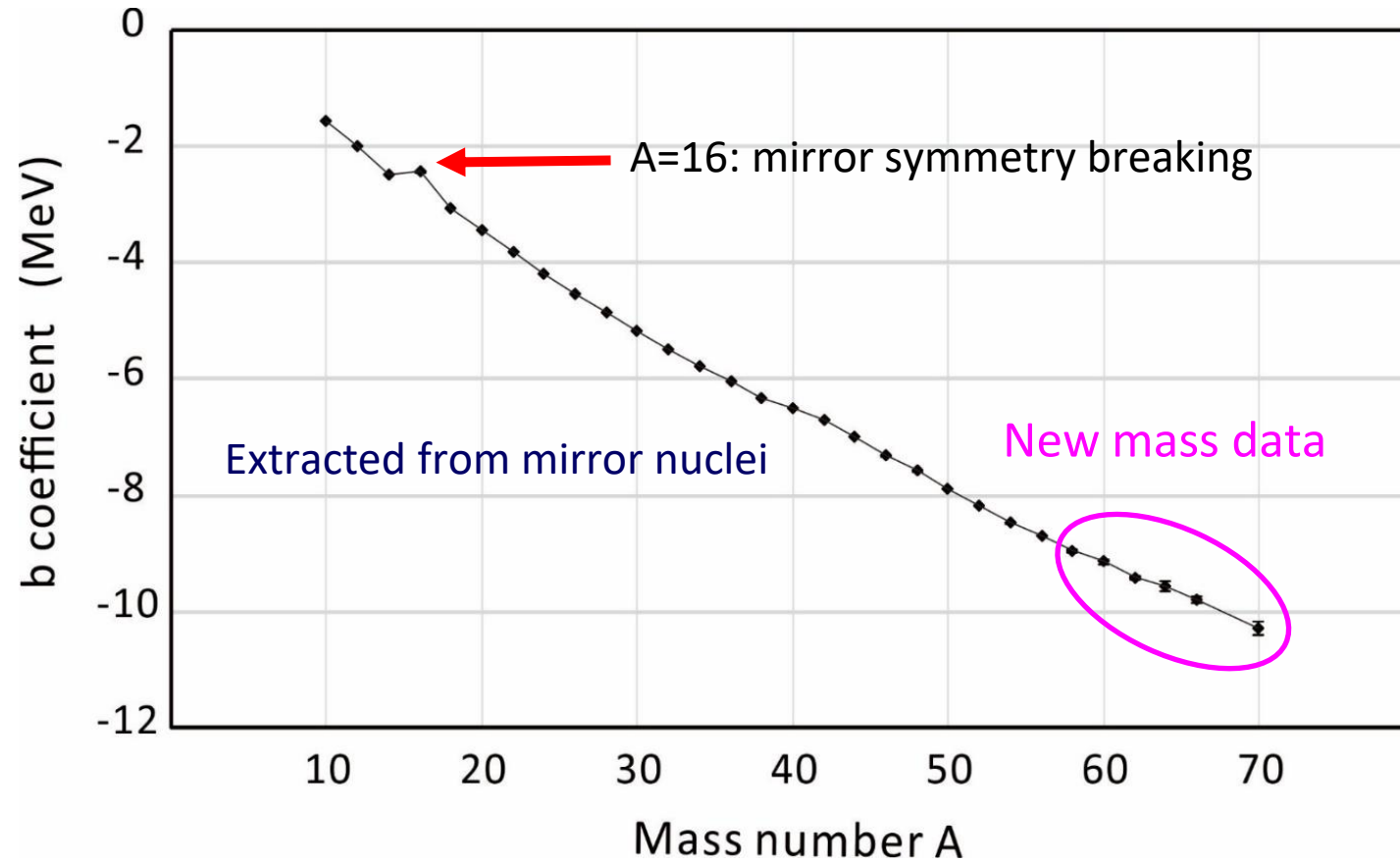


# The ground state mass of $^{70}\text{Br}$ (W.J. Huang et al., PRC submitted)



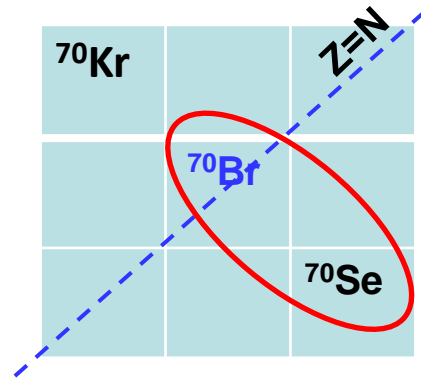
For T=1 multiplets

$$b = (M_1 - M_{-1})/2$$





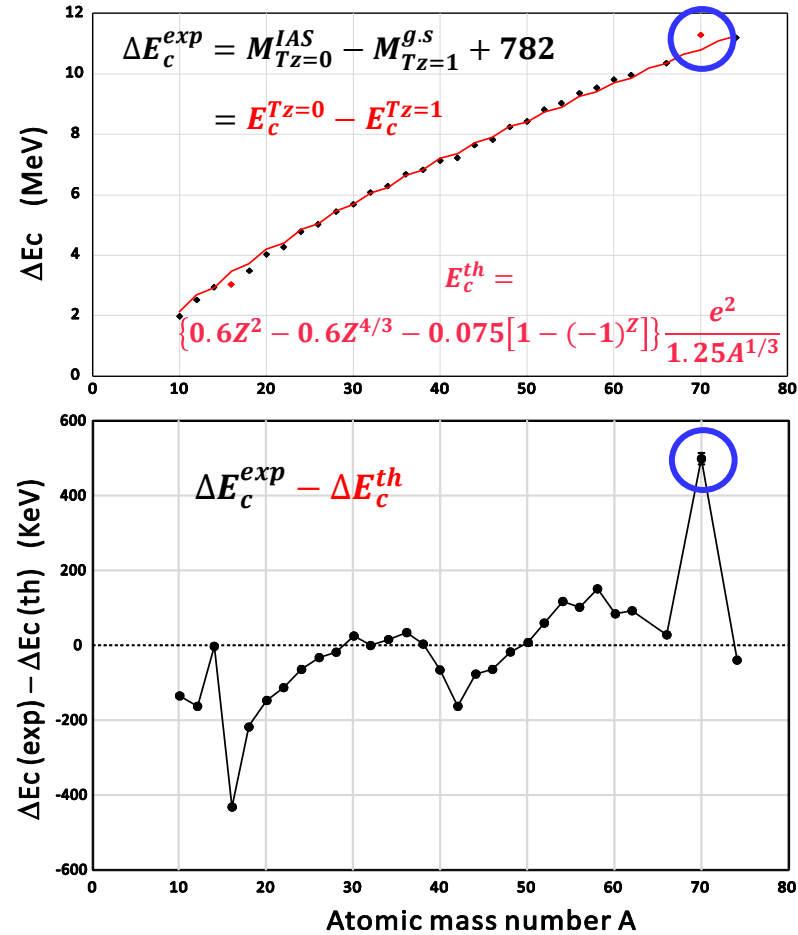
# The ground state mass of $^{70}\text{Br}$ (W.J. Huang et al., PRC submitted)



$^{70}\text{Br}$  (T=1, IAS)

$$\Delta E_c^{exp} = M_{TZ=0}^{IAS} - M_{TZ=1}^{g.s} + 782$$

$^{70}\text{Se}$  (g.s)







# The ground state mass of $^{70}\text{Br}$ (W.J. Huang et al., PRC submitted)



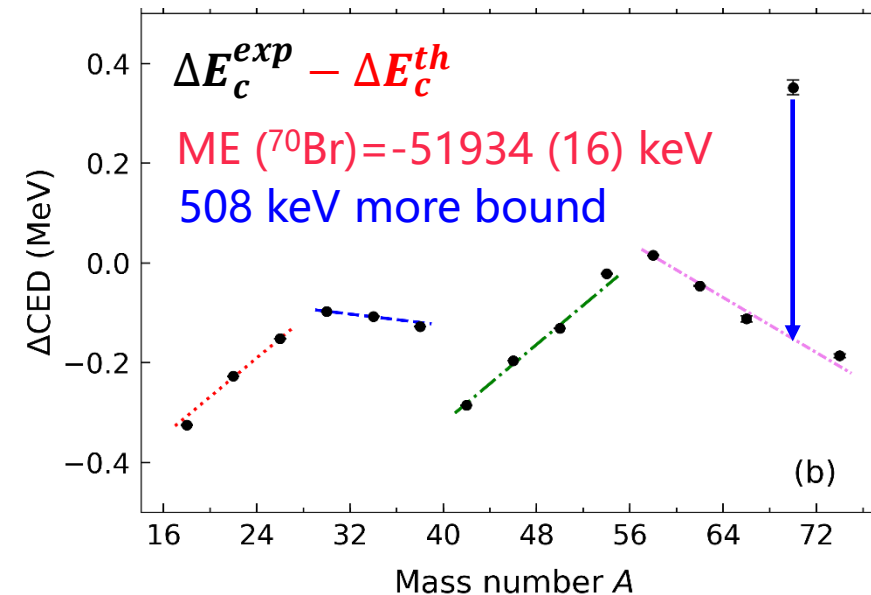
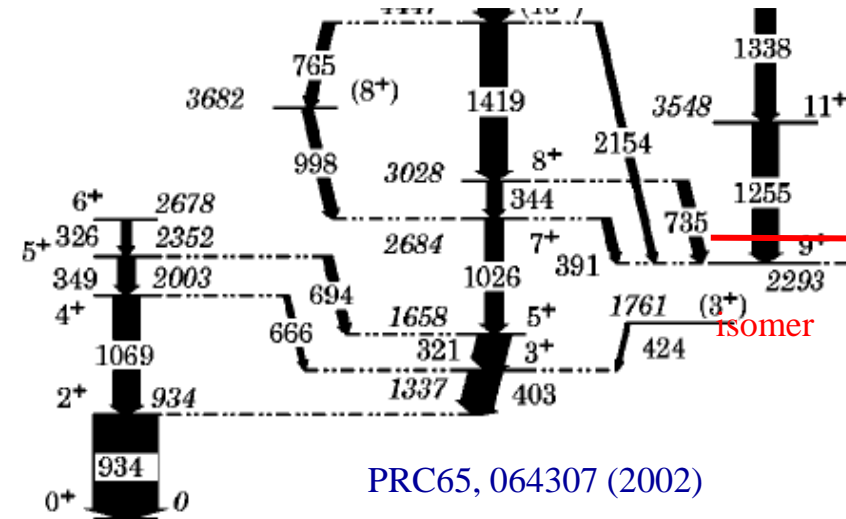
J. Savory et al., PRL 102, 132501 (2009)

rp Process and Masses of  $N \approx Z \approx 34$  Nuclides

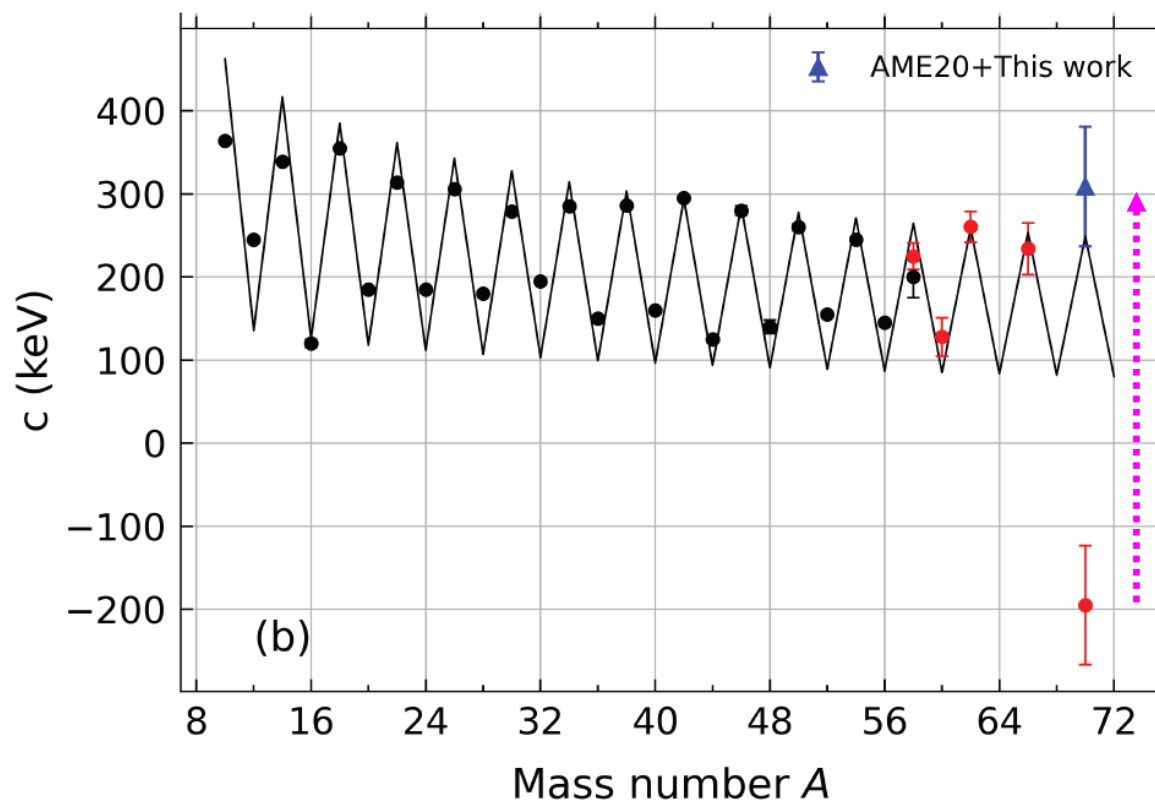
TABLE II. Mass excess values (ME) in keV obtained with LEBIT, from AME'03 [28] and the difference  $\Delta\text{ME} = \text{ME}_{\text{AME}'03} - \text{ME}_{\text{LEBIT}}$ . Also given are new mass predictions for  $^{70}\text{Kr}$  and  $^{71}\text{Kr}$ .

Species	$\text{ME}_{\text{LEBIT}}$	$\text{ME}_{\text{AME}'03}$	$\Delta\text{ME}$
$^{68}\text{Se}$	-54 189.3(5)	-54 210(30)	-21(30)
$^{70}\text{Se}$	-61 929.7(1.6)	-62 050(60)	-120(60)
$^{70}\text{Br}$	<u>-51 425(15)</u>	-51 430(310)	-5(310)
$^{71}\text{Br}$	-56 502.4(5.4)	-57 060(570)	-558(570)
	$\text{ME}_{\text{LEBIT+CDE}}$	$\text{ME}_{\text{AME}'03}$	$\Delta\text{ME}$
$^{70}\text{Kr}$	-41 304(100)	-41 680(390)	-376(403)
$^{71}\text{Kr}$	-46 025(100)	-46 920(650)	895(658)

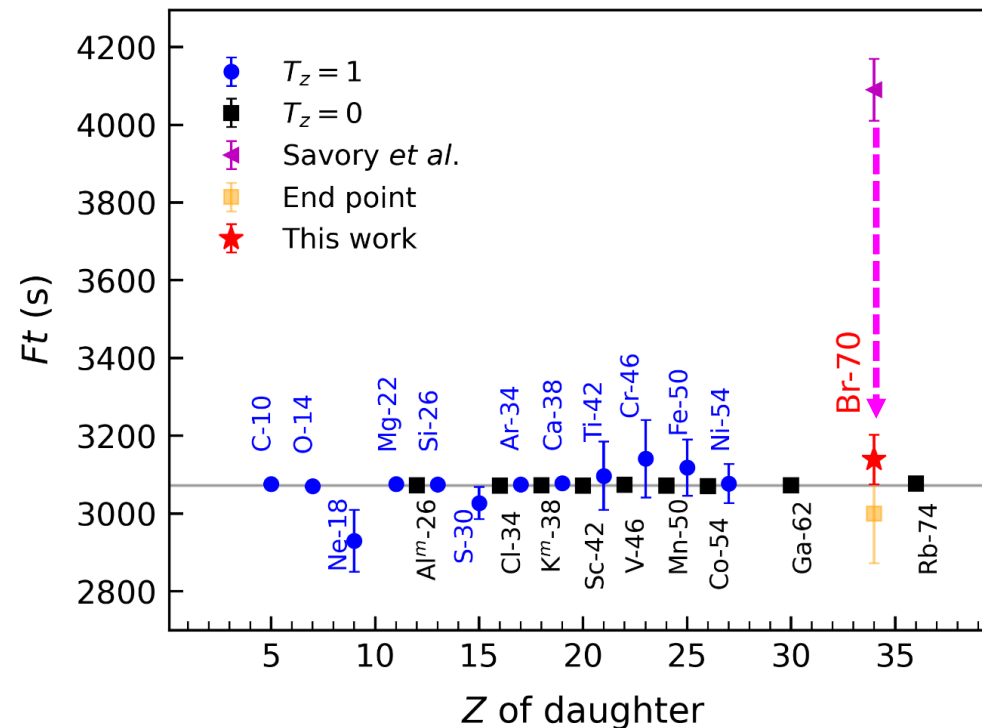
PRC 70, 014310 (2004)  
 $Q_{\text{EC}}(9+) = 12.19 (\pm 7 \pm 4) \text{ MeV}$   
 $Q_{\text{EC}}(\text{g.s.}) = 9.90 (\pm 7 \pm 4) \text{ MeV}$   
 $\text{ME}(\text{gs}) = -52.03 (\pm 7 \pm 4) \text{ MeV}$



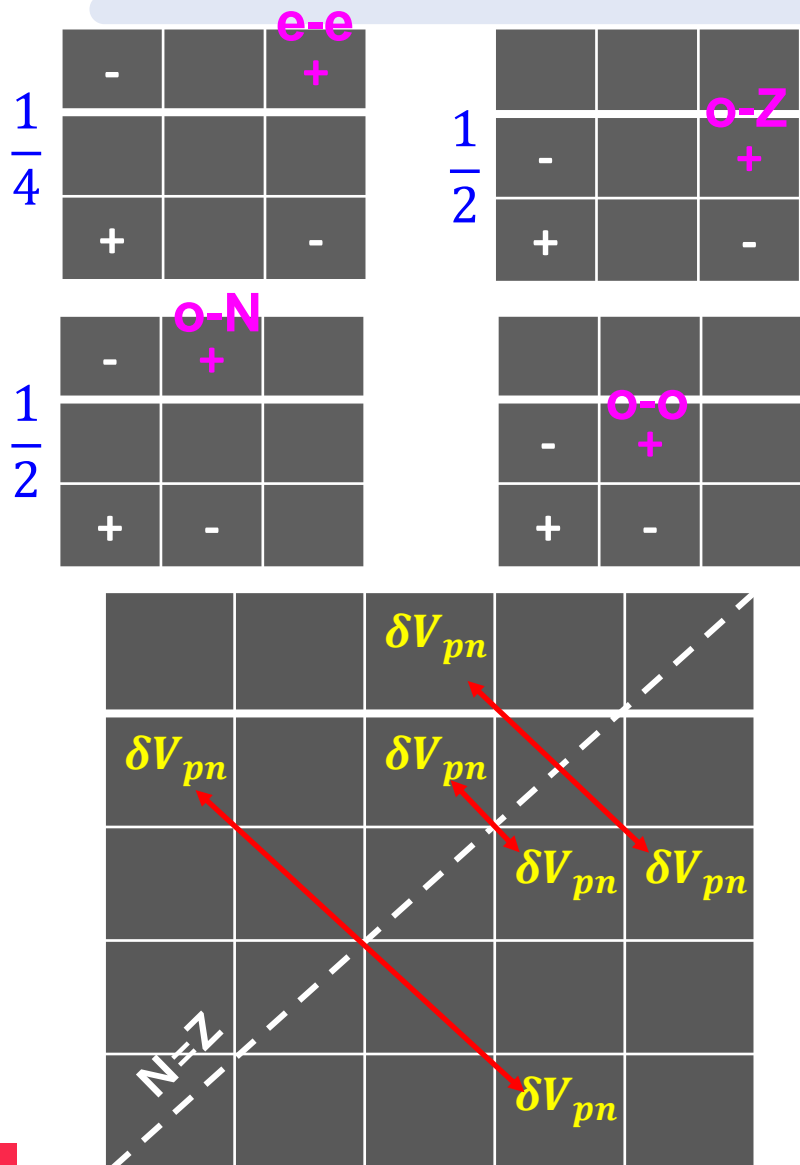
$$M(A, T, T_z) = a(A, T) + b(A, T)T_z + c(A, T)T_z^2$$



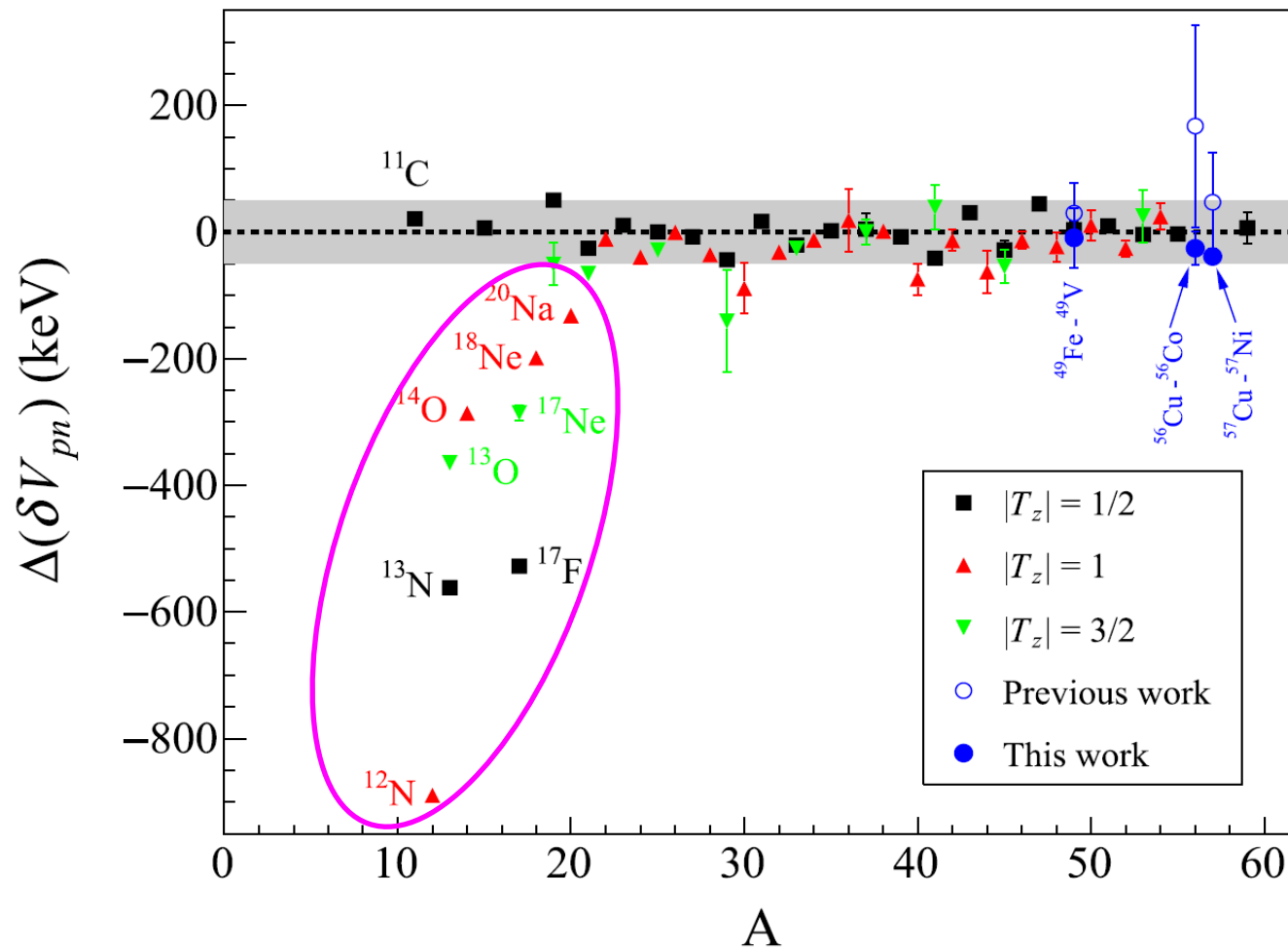
$$Ft \equiv ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C)$$



If CVC hypothesis is correct, the corrected Ft values should be same



M. Zhang et al., Eur. Phys. J. A 59: 27(2023)

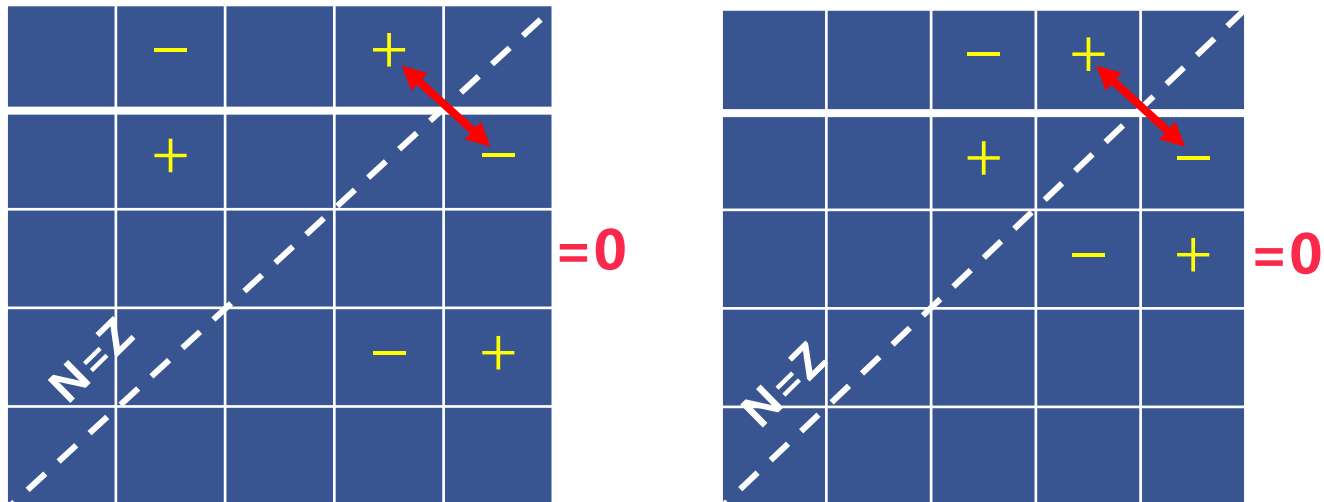
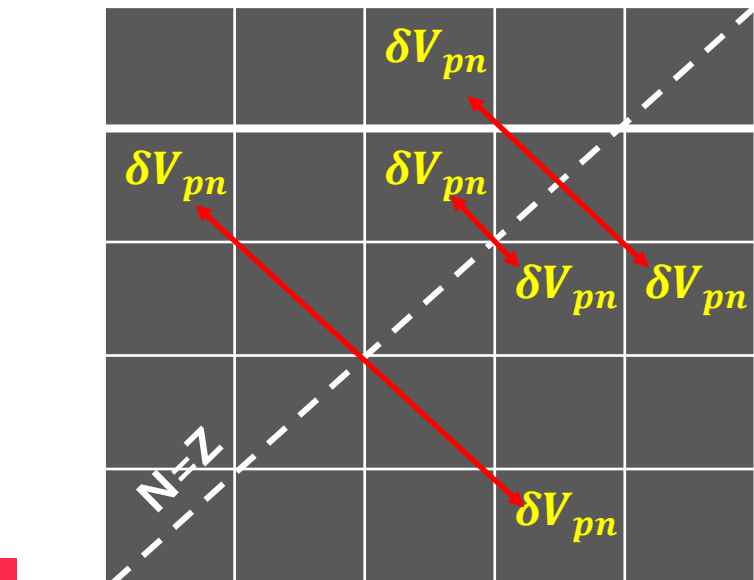
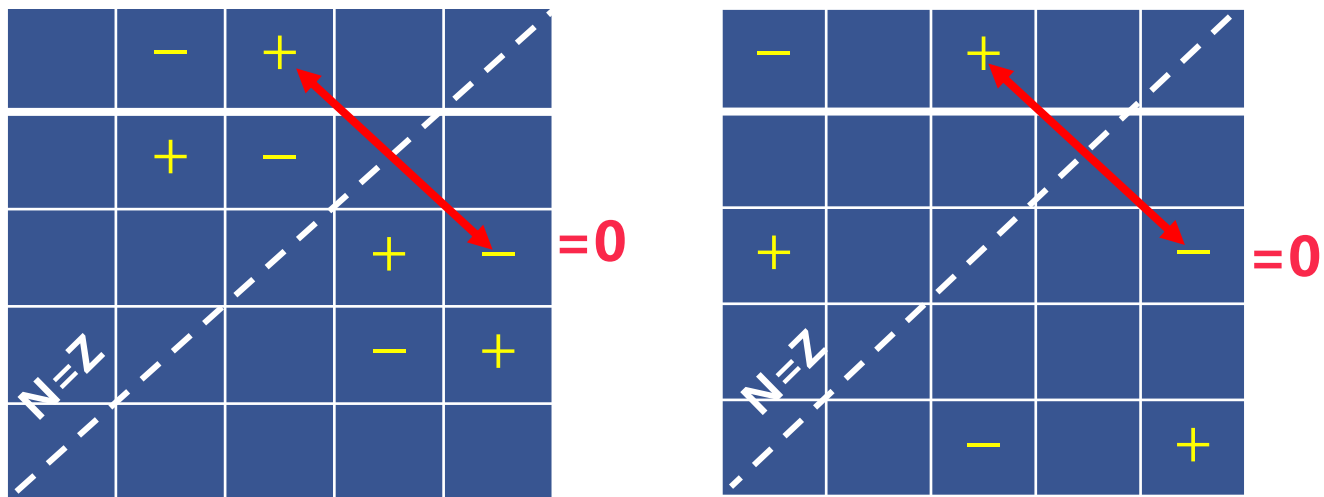
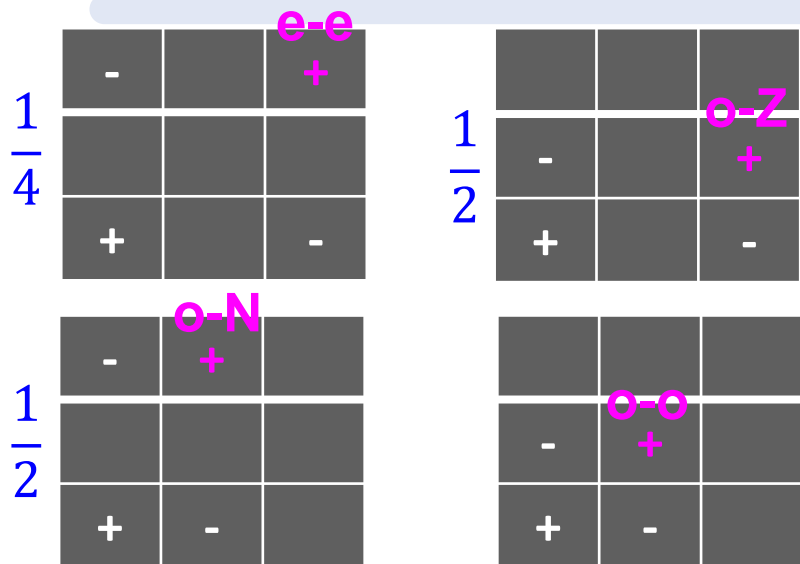




# Mirror symmetry of residual pn interaction



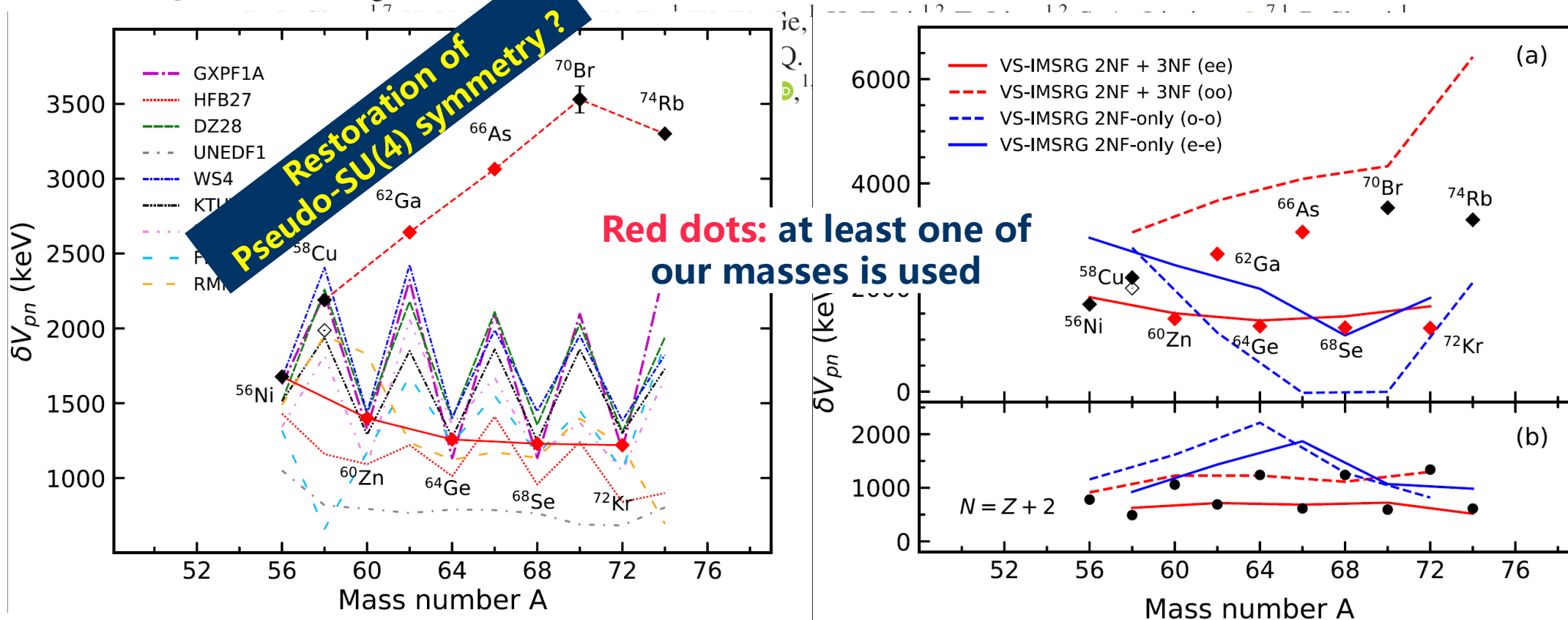
## Local mass relationship



M. Wang et al., PRL 130, 192501 (2023)

## Mass Measurement of Upper $fp$ -Shell $N=Z-2$ and $N=Z-1$ Nuclei and the Importance of Three-Nucleon Force along the $N=Z$ Line

M. Wang<sup>1,2</sup>, Y. H. Zhang<sup>1,2,\*</sup>, X. Zhou<sup>1,2</sup>, X. H. Zhou<sup>1,2,†</sup>, H. S. Xu<sup>1,2</sup>, M. L. Liu<sup>1</sup>, J. G. Li<sup>1</sup>, Y. F. Niu<sup>3,4</sup>, W. J. Huang<sup>1,5</sup>, Q. Yuan<sup>6</sup>, S. Zhang<sup>1,7</sup>, F. R. Xue<sup>6,‡</sup>, Yu. A. Litvinov<sup>1,7</sup>, K. Blaum<sup>8</sup>, Z. Meisel<sup>9</sup>, R. F. Casten<sup>10</sup>, R. B. Cakirli<sup>11</sup>



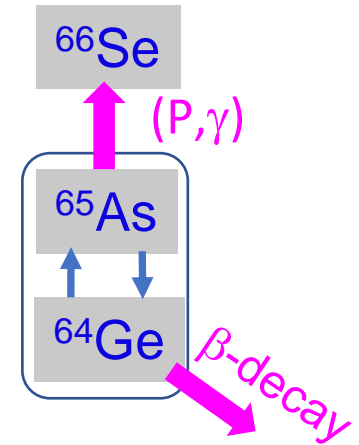


# Waiting point $^{64}\text{Ge}$ in the rp-process of Type I X-ray bursts

## Effective lifetimes of $^{64}\text{Ge}$

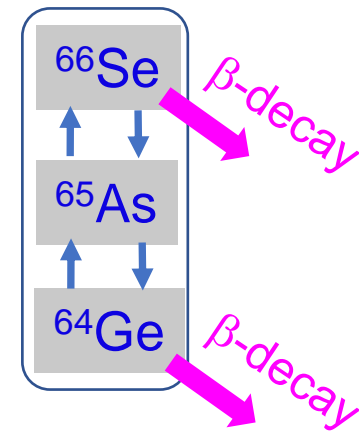
$T < 1.5\text{-}2\text{ GK}$ ,  $^{68}\text{Se} - ^{69}\text{Br}$  equilibrium

$$\lambda_{\text{total}} = \lambda_{\beta(Z,N)} + Y_p^2 \rho^2 N_A^2 \left( \frac{2\pi\hbar^2}{kT} \right)^{3/2} \frac{G_{(Z+1,N)}(T)}{2G_{(Z,N)}(T)} \exp\left( \frac{Q_{(Z,N)(p,\gamma)}}{kT} \right) \langle p\gamma \rangle_{(Z+1,N)}$$



$T > 1.5\text{-}2\text{ GK}$ ,  $^{68}\text{Se} - ^{70}\text{Kr}$  equilibrium

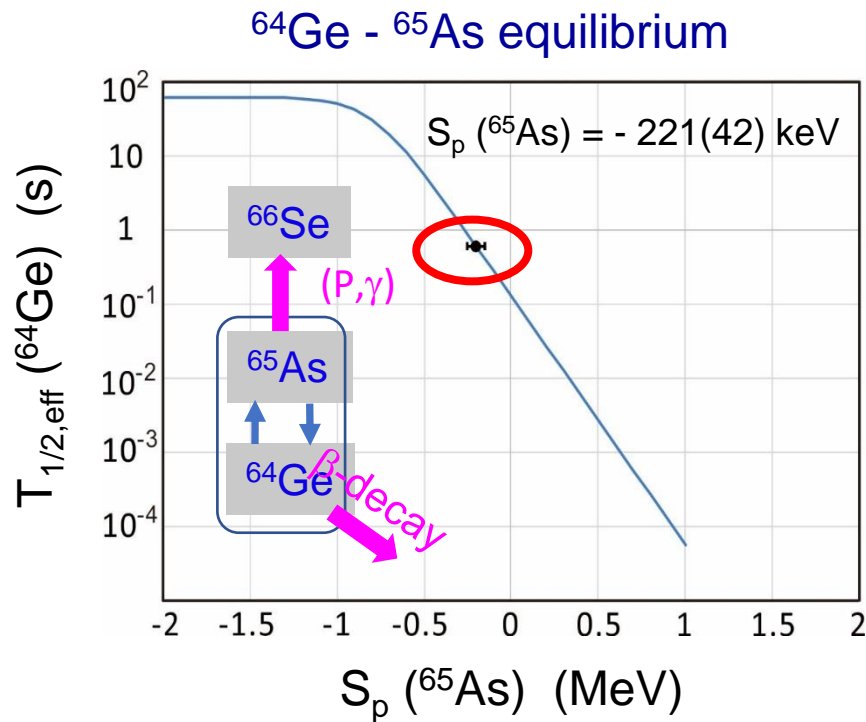
$$\lambda_{\text{total}} = \lambda_{\beta(Z,N)} + \left[ Y_p \rho N_A \left( \frac{2\pi\hbar^2}{kT} \right)^{3/2} \right]^2 \left( \frac{1}{\mu_{(Z,N)} \mu_{(Z+1,N)}} \right)^{3/2} \frac{G_{(Z+2,N)}(T)}{4G_{(Z,N)}(T)} \times \exp\left( \frac{Q_{(Z,N)(p,\gamma)} + Q_{(Z+1,N)(p,\gamma)}}{kT} \right) \lambda_{\beta(Z+2,N)}$$



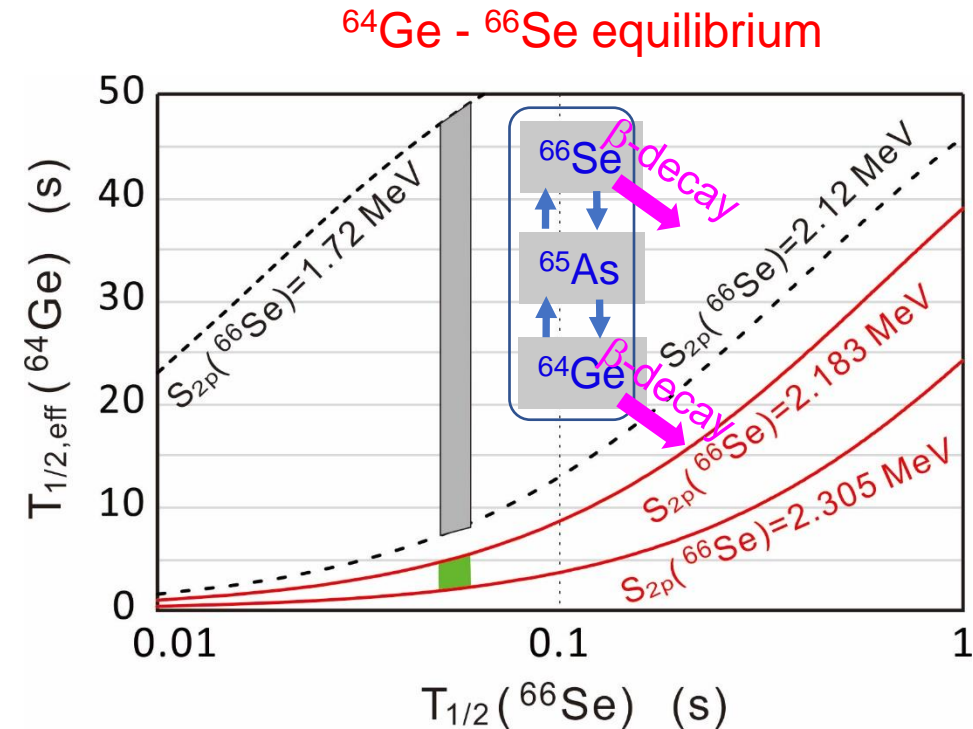
# Waiting point $^{64}\text{Ge}$ in the rp-process of Type I X-ray bursts

## Effective lifetimes of $^{64}\text{Ge}$

$$T_{1/2} (^{64}\text{Ge}) = 63.7(2.5) \text{ (s)}$$



$$S_p(^{65}\text{As}) = -221(42) \text{ keV}$$



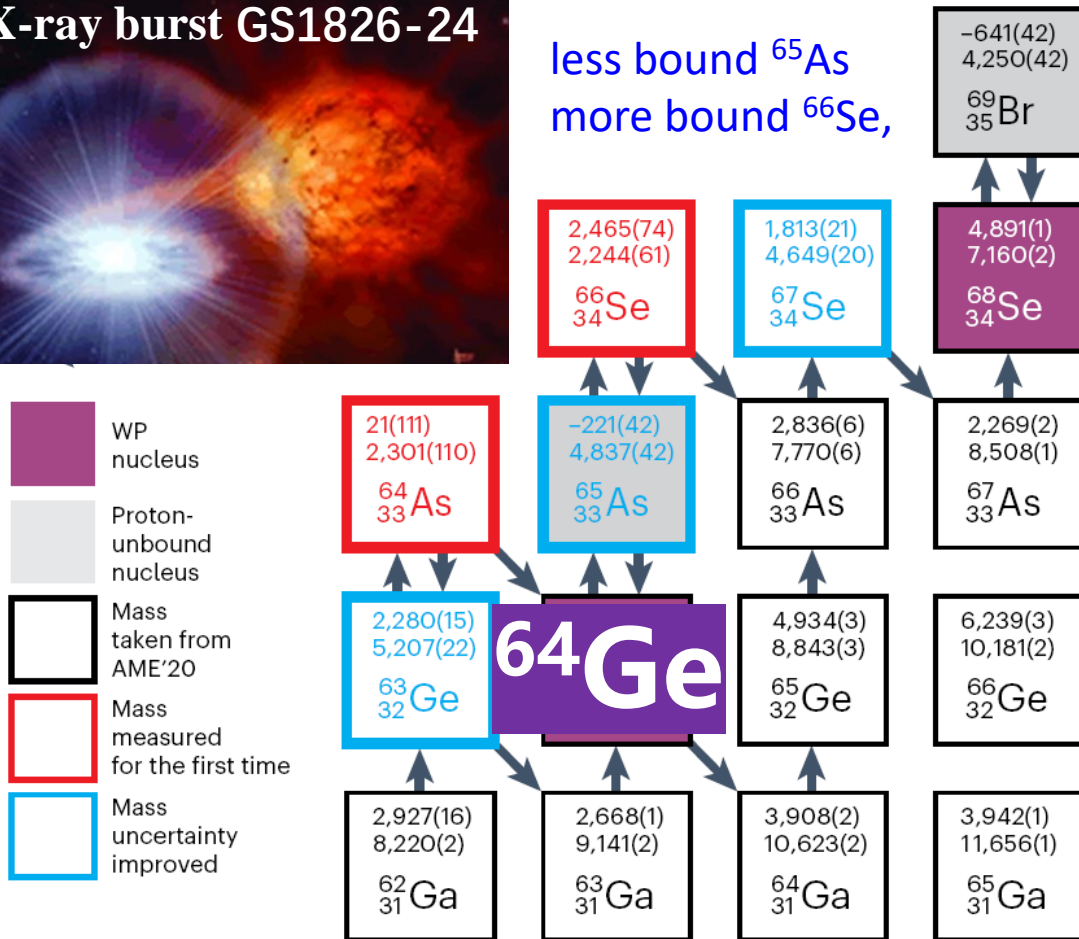
$$T_{1/2} (^{66}\text{Se}) = 54(4) \text{ (ms)}$$

$$S_{2p} (^{66}\text{Se}) = 2.244(61) \text{ MeV}$$

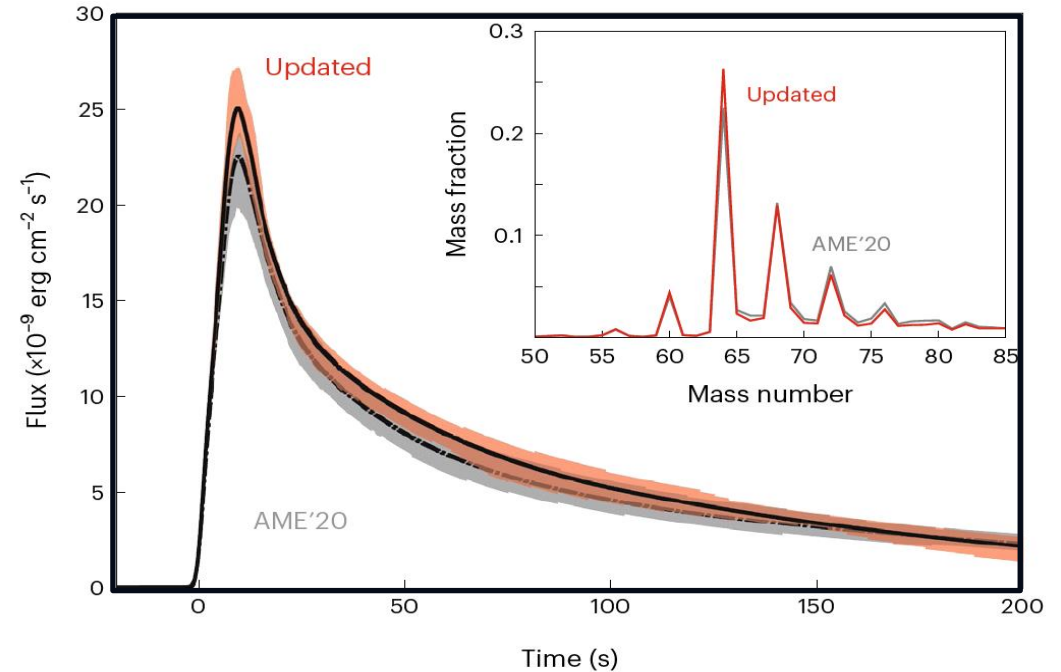
All Q-values of (p, $\gamma$ ) reaction around  $^{64}\text{Ge}$  obtained



less bound  $^{65}\text{As}$   
more bound  $^{66}\text{Se}$ ,



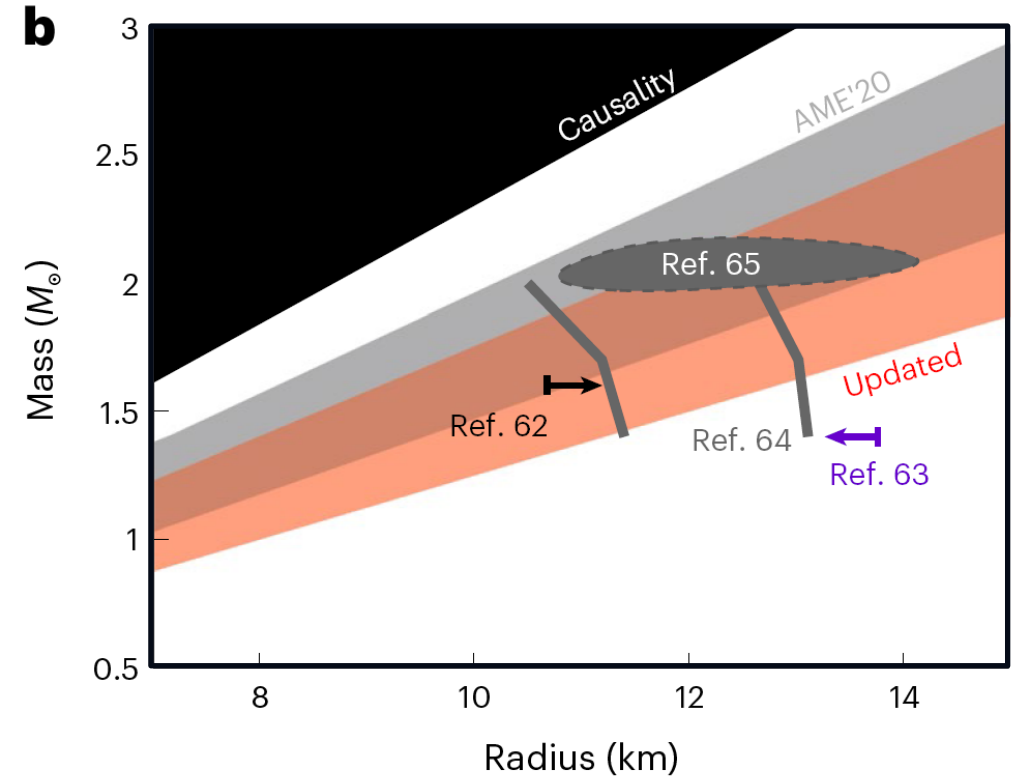
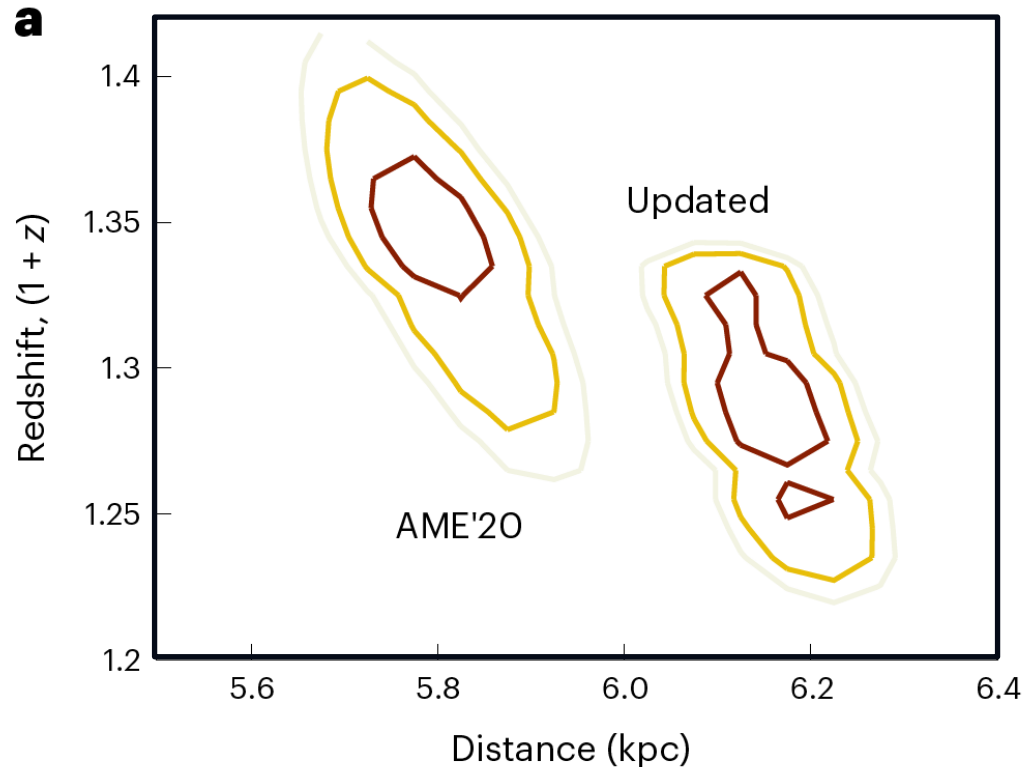
Multizone X-ray burst simulations



- peak luminosity (flux) increased
- A=64 mass fraction increased by 17%
- A=65 mass fraction decreased by 14%



New light curve enables us to set new constraints on the optimal  $d$  and  $(1+z)$  parameters



- the neutron star in GS1826-24 is 6.5% farther away (0.4 kpc=1300 ly) from us !
- reduced  $1+z$  value indicates weaker gravitation than believed !

- Mass and Radius are constrained



nature physics



Article

<https://doi.org/10.1038/s41567-023-02034-2>

## Mass measurements show slowdown of rapid proton capture process at waiting-point nucleus $^{64}\text{Ge}$

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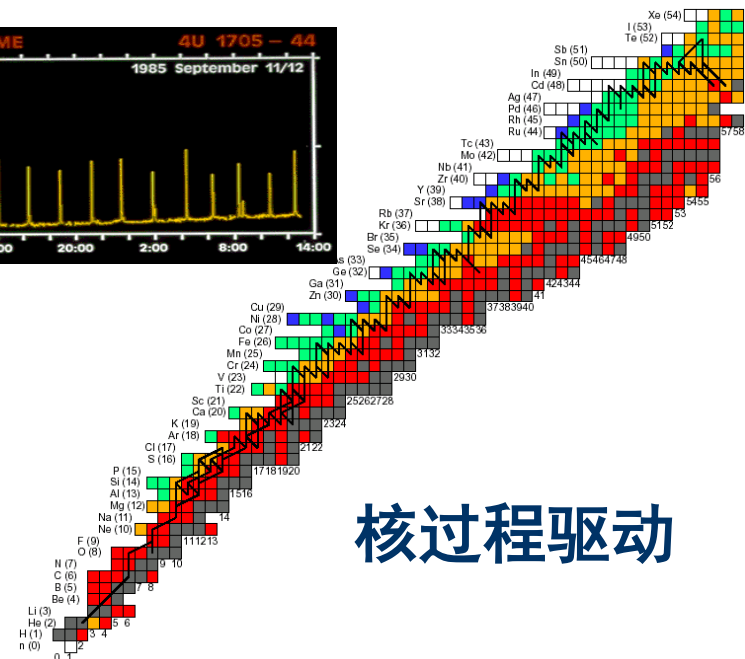
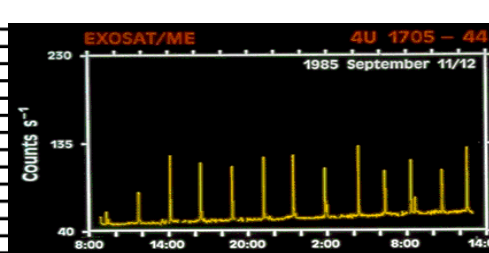
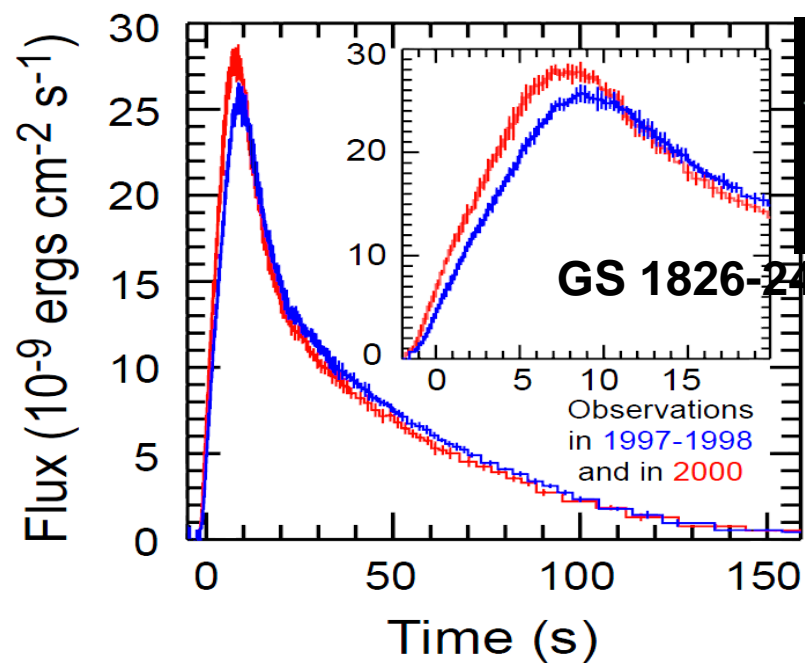
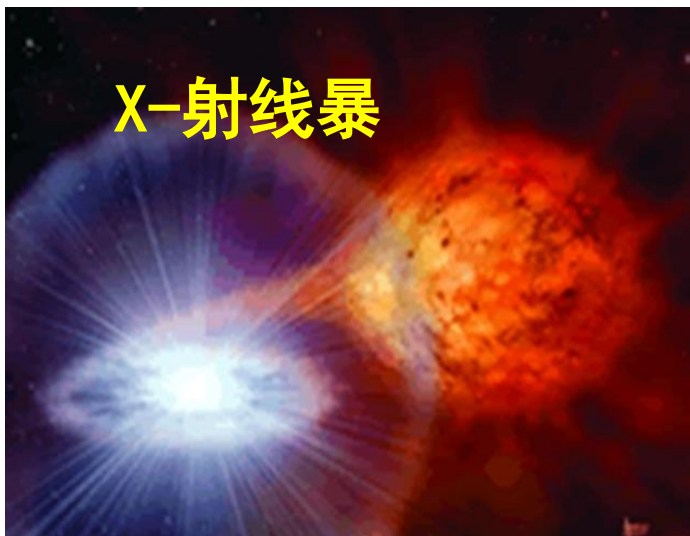
## 5. Summary



1. *B $\rho$* -defined IMS has been established in CSRe which shows several advantages in mass measurement of short-lived nuclei
2. Masses of  $^{78}\text{Kr}$ ,  $^{58}\text{Ni}$ ,  $^{36}\text{Ar}$  fragments have been measured, enabling to address several issues in nuclear structure and nuclear astrophysics
3. *B $\rho$* -defined IMS will be installed in the SRing of HIAF facility and the masses of heavy and n-rich exotic nuclei will be touched in the future
4. We need close collaborations both in experiment and in theory

Thanks for your attention

# 原子核质量与核天体物理



X-射线暴模型  
+核物理输入

灵敏度研究



光度曲线  
元素丰度

模型预言与  
天文观测比较



中子星性质