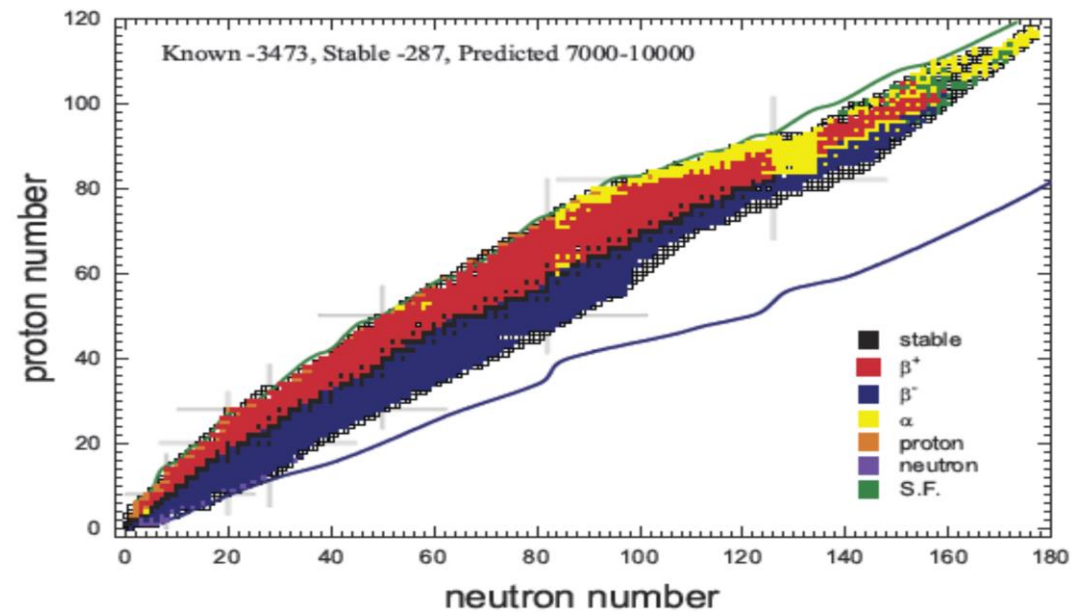


# MNT2024

RIKEN, July 2-5, 2024



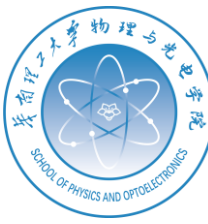
## Cluster transfer and cluster emission in multinucleon transfer reactions

**Zhao-Qing Feng**

(School of Physics and Optoelectronics, South China University of Technology)

Collaborator: Zi-Han Wang, Peng-Hui Chen

Email: [fengzhq@scut.edu.cn](mailto:fengzhq@scut.edu.cn), Tel: 020-87114086

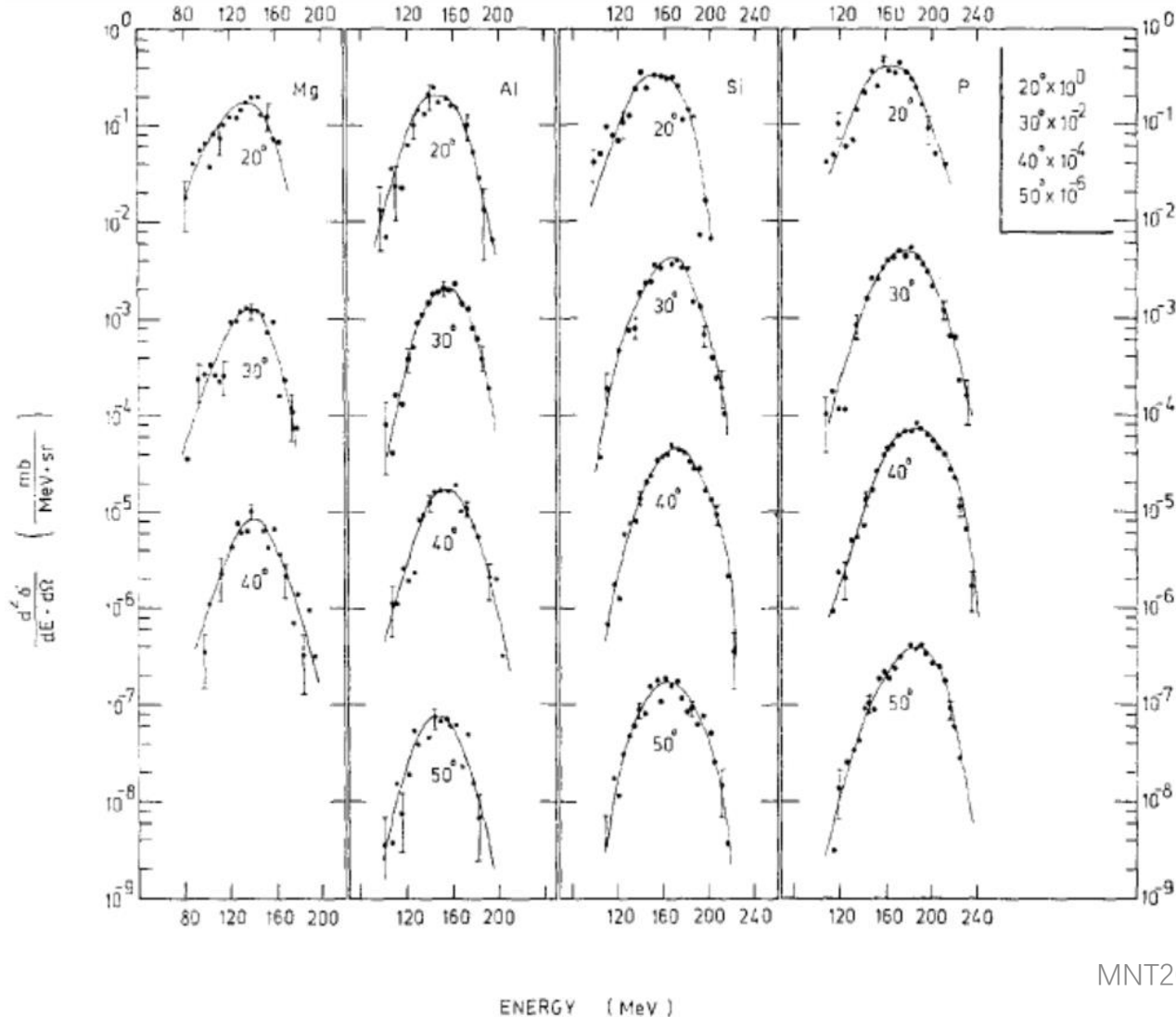


# Outline

- Brief overview of MNT reactions
- Theoretical description of MNT reactions based on the dinuclear system model
- Results and discussion
- ✓ Fusion-evaporation reactions
- ✓ Yields, total kinetic energy spectra and angular distribution in MNT reactions
- ✓ Cluster transfer and cluster emission in MNT reactions
- Summary and perspective

# Multinucleon transfer reactions-quasi-elastic scattering, quasifission, deep inelastic collisions

Dubna experiments, Nuclear Physics A 176 (1971) 284-288, A 211 (1973) 299-309, A 215 (1973) 91-108



2.N Nuclear Physics A176 (1971) 284—288; © North-Holland Publishing Co., Amsterdam  
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**NEW ISOTOPES  $^{29,30}\text{Mg}$ ,  $^{31,32,33}\text{Al}$ ,  $^{33,34,35,36}\text{Si}$ ,  $^{35,36,37,38}\text{P}$ ,  $^{39,40}\text{S}$  AND  $^{41,42}\text{Cl}$  PRODUCED IN BOMBARDMENT OF A  $^{232}\text{Th}$  TARGET WITH 290 MeV  $^{40}\text{Ar}$  IONS**

A. G. ARTUKH, V. V. AVDEICHIKOV †, G. F. GRIDNEV,  
V. L. MIKHEEV, V. V. VOLKOV and J. WILCZYŃSKI ††  
Joint Institute for Nuclear Research, Dubna, USSR

**MULTINUCLEON TRANSFER REACTIONS IN THE  $^{232}\text{Th} + ^{22}\text{Ne}$  SYSTEM**

A. G. ARTUKH, G. F. GRIDNEV, V. L. MIKHEEV, V. V. VOLKOV  
and J. WILCZYŃSKI †  
Joint Institute for Nuclear Research, Dubna, USSR

Received 18 December 1972  
(Revised 14 May 1973)

**TRANSFER REACTIONS IN THE INTERACTION OF  $^{40}\text{Ar}$  WITH  $^{232}\text{Th}$**

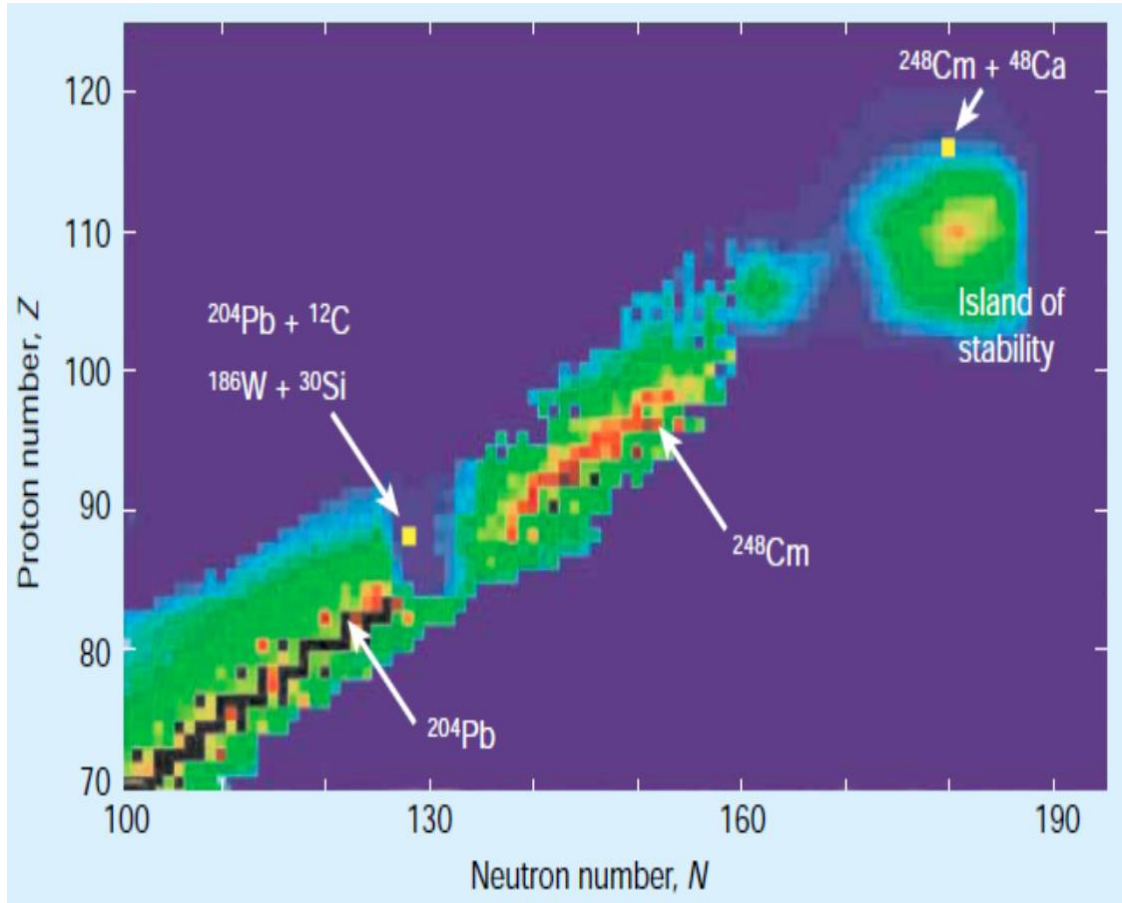
A. G. ARTUKH, G. F. GRIDNEV, V. L. MIKHEEV, V. V. VOLKOV and J. WILCZYŃSKI †  
Joint Institute for Nuclear Research, Dubna, USSR

Received 13 April 1973

## Multi-nucleon transfer reactions (MNT), experiment progress

Lab.	Reaction system	References
Dubna	$^{136}\text{Xe} + ^{208}\text{Pb}$ $^{156,160}\text{Gd} + ^{186}\text{W}$	Phys. Rev. C 86, 044611 (2012); Phys. Rev. C 96, 064621 (2017)
GSI	$^{238}\text{U} + ^{238}\text{U}$ $^{48}\text{Ca} + ^{248}\text{Cm}$ $^{48}\text{Ca} + ^{238}\text{U}$	Phys. Rev. Lett. 39, 385 (1977); Phys. Rev. Lett. 41, 469 (1978); Phys. Lett. B 748, 199 (2015); Eur. Phys. J. A 56, 224 (2020)
GANIL	$^{238}\text{U} + ^{238}\text{U}$ ; $^{136}\text{Xe} + ^{198}\text{Pt}$	IJMEP 17, 2235-2239 (2008); Phys. Rev. Lett. 115, 172503 (2015)
Argonne	$^{136}\text{Xe} + ^{208}\text{Pb}$ $^{204}\text{Hg} + ^{198}\text{Pt}$	Phys. Rev. C 91, 064615 (2015); Physics Letters B 771, 119-124 (2017)
RIKEN-KISS	$^{238}\text{U} + ^{198}\text{Pt} \rightarrow ^{241}\text{U}$	Phys. Rev. Lett. 130, 132502 (2023)

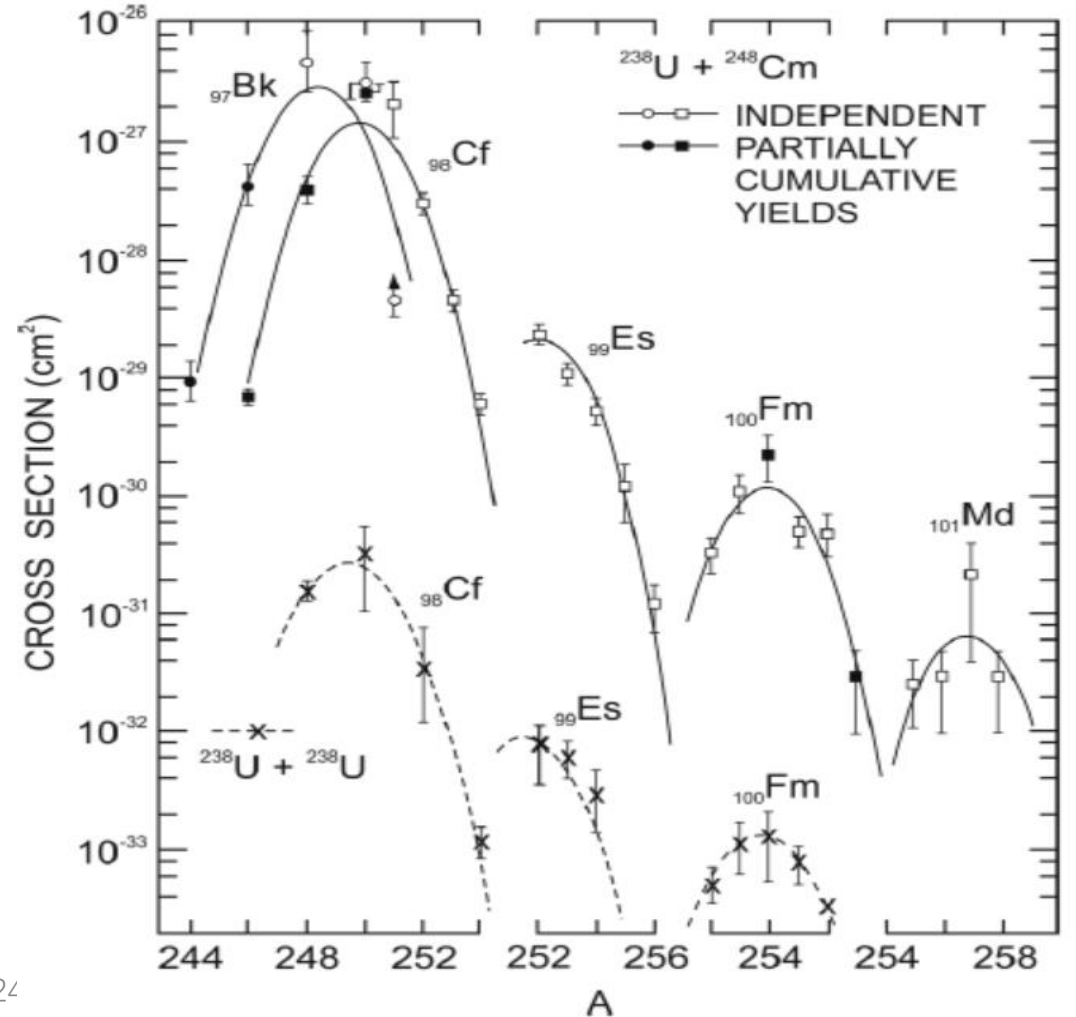
Slide from Yuri Oganessian in Lanzhou, 2005



## Damped collisions of two actinide nuclei

PRL39(1977)1065, PRL41(1978)469, ZPA292(1979)171,

PRL43(1979)1483, PRC88(2013)054615



# New isotope production around N=126

第 32 卷 第 2 期  
2015 年 6 月

原子核物理评论  
Nuclear Physics Review

Vol. 32, No. 2  
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Article ID: 1007-4627(2015)02-0137-09

## Production of Exotic Nuclei in Low-Energy Multi-Nucleon Transfer Reactions

V.I. Zagrebaev<sup>1</sup>, Walter Greiner<sup>2</sup>

(1. Flerov Laboratory of Nuclear Reactions, JINR, Dubna, Moscow Region, Russia;  
2. Frankfurt Institute for Advanced Studies, J.W. Goethe-Universität, Frankfurt, Germany)

PRL 101, 122701 (2008)

PHYSICAL REVIEW LETTERS

week ending  
19 SEPTEMBER 2008

## Production of New Heavy Isotopes in Low-Energy Multinucleon Transfer Reactions

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<sup>1</sup>Flerov Laboratory of Nuclear Reactions, JINR, Dubna, Moscow Region, Russia  
<sup>2</sup>Frankfurt Institute for Advanced Studies, J.W. Goethe-Universität, Frankfurt, Germany  
(Received 8 July 2008; published 17 September 2008)

It is shown that the multinucleon transfer reactions in low-energy collisions of heavy ions may be used for production of new neutron-rich nuclei at the “northeast” part of the nuclear map along the neutron closed shell  $N = 126$  which plays an important role in the  $r$  process of nucleosynthesis. More than 50 unknown nuclei might be produced in such reactions (in particular, in collision of  $^{136}\text{Xe}$  with  $^{208}\text{Pb}$ ) with cross sections of not less than  $1 \mu\text{b}$ .

DOI: 10.1103/PhysRevLett.101.122701

PACS numbers: 25.70.Jj, 25.70.Hi

INSTITUTE OF PHYSICS PUBLISHING

JOURNAL OF PHYSICS G: NUCLEAR AND PARTICLE PHYSICS

J. Phys. G: Nucl. Part. Phys. 34 (2007) 1–25

doi:10.1088/0954-3899/34/1/001

## The International Workshop on Nuclear Dynamics in Heavy-Ion Reactions (IWND2014) Aug 15-19, 2014, Lanzhou, China

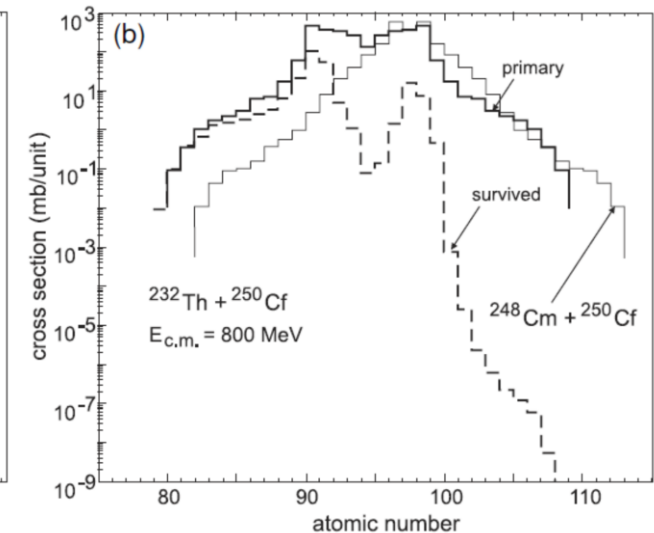
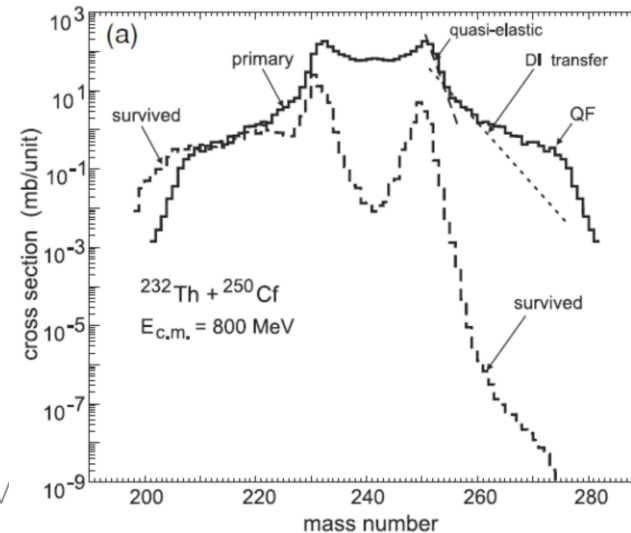


## Low-energy collisions of heavy nuclei: dynamics of sticking, mass transfer and fusion

Valery Zagrebaev<sup>1</sup> and Walter Greiner<sup>2</sup>

<sup>1</sup>Flerov Laboratory of Nuclear Reaction, JINR, Dubna, Moscow Region, Russia  
<sup>2</sup>Frankfurt Institute for Advanced Studies, JW Goethe-Universität, Frankfurt, Germany

E-mail: valeri.zagrebaev@jinr.ru



# New isotope $^{241}\text{U}$ via MNT reactions and high-precision mass measurement

PHYSICAL REVIEW LETTERS **130**, 132502 (2023)

Editors' Suggestion

Featured in Physics

## Discovery of New Isotope $^{241}\text{U}$ and Systematic High-Precision Atomic Mass Measurements of Neutron-Rich Pa-Pu Nuclei Produced via Multinucleon Transfer Reactions

T. Niwase<sup>1,\*</sup>, Y. X. Watanabe<sup>1</sup>, Y. Hirayama<sup>1</sup>, M. Mukai<sup>2</sup>, P. Schury<sup>1</sup>,  
A. N. Andreyev<sup>3</sup>, T. Hashimoto<sup>4</sup>, S. Iimura<sup>5</sup>, H. Ishiyama<sup>2</sup>, Y. Ito<sup>6</sup>, S. C. Jeong<sup>1</sup>,  
D. Kaji<sup>2</sup>, S. Kimura<sup>2</sup>, H. Miyatake<sup>1</sup>, K. Morimoto<sup>2</sup>, J.-Y. Moon<sup>4</sup>, M. Oyaizu<sup>1</sup>,  
M. Rosenbusch<sup>1</sup>, A. Taniguchi<sup>7</sup>, and M. Wada<sup>1</sup>

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<sup>2</sup>RIKEN Nishina Center for Accelerator-Based Science, Wako, Saitama 351-0198, Japan

<sup>3</sup>School of Physics, Engineering and Technology, University of York, York YO10 5DD, United Kingdom

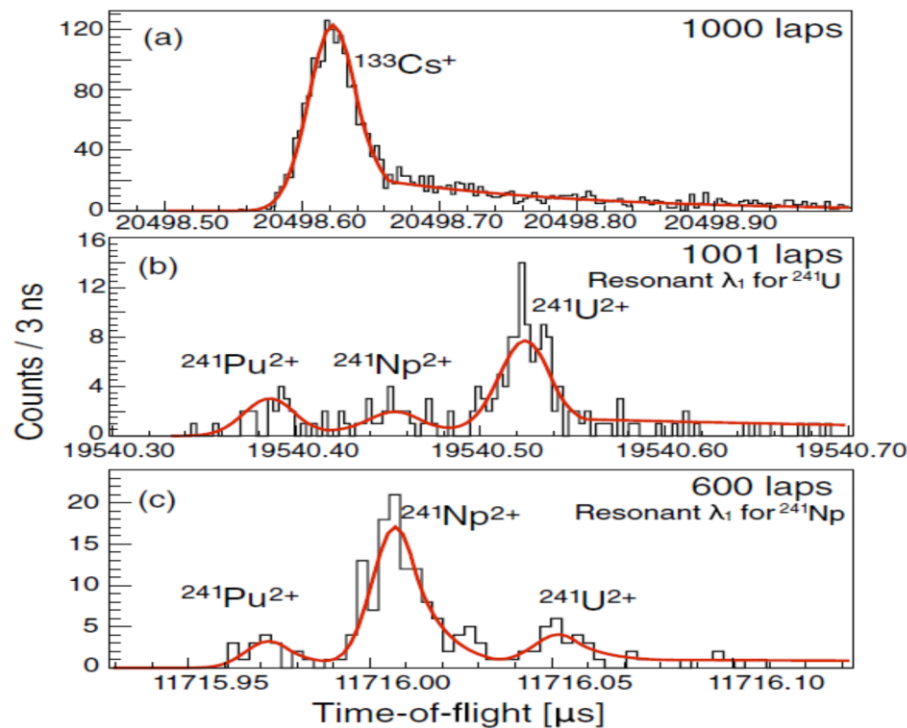
<sup>4</sup>Institute for Basic Science, 70, Yuseong-daero 1689-gil, Yuseong-gu, Daejeon 43000, Korea

<sup>5</sup>Department of Physics, Rikkyo University, Tokyo 171-8501, Japan

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(Received 21 November 2022; revised 26 January 2023; accepted 16 February 2023; published 31 March 2023)



PRL **115**, 172503 (2015)

PHYSICAL REVIEW LETTERS

week ending  
23 OCTOBER 2015

## Pathway for the Production of Neutron-Rich Isotopes around the $N = 126$ Shell Closure

Y. X. Watanabe<sup>1,\*</sup>, Y. H. Kim<sup>2,3,†</sup>, S. C. Jeong<sup>1,‡</sup>, Y. Hirayama<sup>1</sup>, N. Imai<sup>1,§</sup>, H. Ishiyama<sup>1,‡</sup>, H. S. Jung<sup>1</sup>, H. Miyatake<sup>1</sup>,  
S. Choi<sup>2,3</sup>, J. S. Song<sup>2,3,4</sup>, E. Clement<sup>5</sup>, G. de France<sup>5</sup>, A. Navin<sup>5,||</sup>, M. Rejmund<sup>5</sup>, C. Schmitt<sup>5</sup>, G. Pollarolo<sup>6</sup>, L. Corradi<sup>7</sup>,  
E. Fioretto<sup>7</sup>, D. Montanari<sup>8</sup>, M. Niikura<sup>9,¶</sup>, D. Suzuki<sup>9,\*\*</sup>, H. Nishibata<sup>10</sup>, and J. Takatsu<sup>10</sup>

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<sup>2</sup>Department of Physics and Astronomy, Seoul National University, Seoul 08826, Korea

<sup>3</sup>Institute for Nuclear and Particle Astrophysics, Seoul National University, Seoul 08826, Korea

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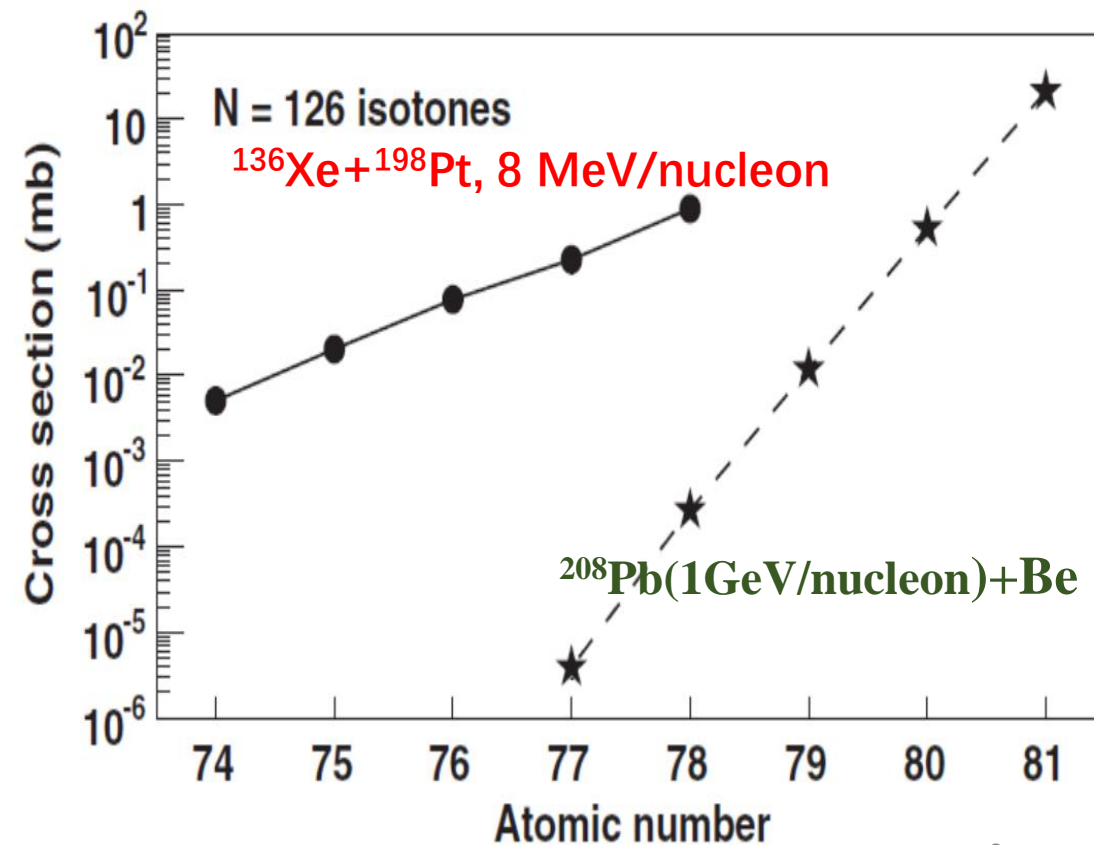
<sup>7</sup>Istituto Nazionale di Fisica Nucleare, Laboratori Nazionali di Legnaro, I-35020 Legnaro, Italy

<sup>8</sup>Dipartimento di Fisica, Università di Padova, and Istituto Nazionale di Fisica Nucleare, I-35131 Padova, Italy

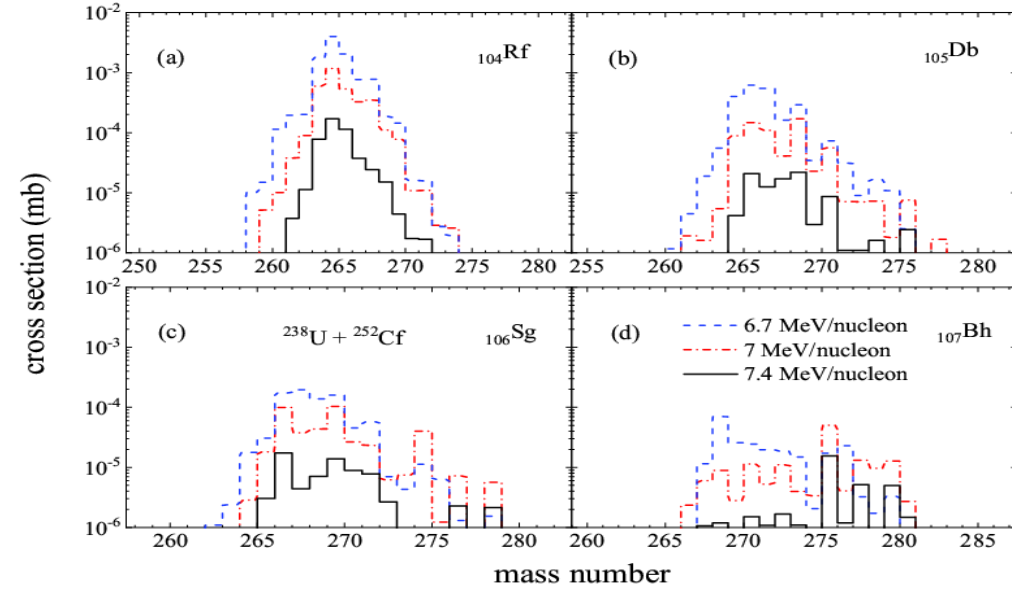
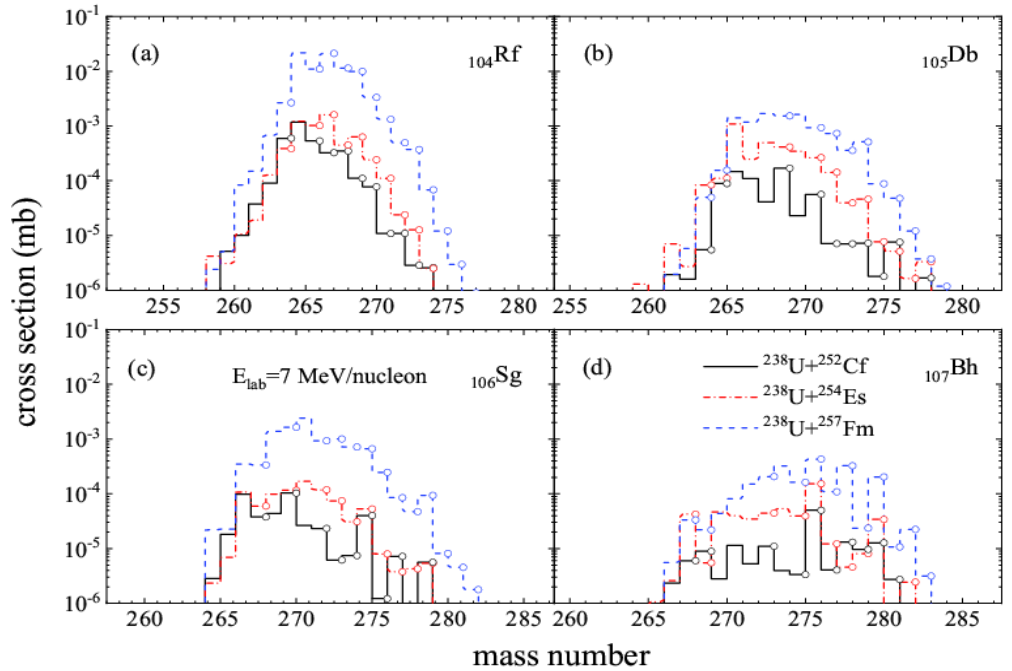
<sup>9</sup>Institut de Physique Nucléaire (IPN), IN2P3-CNRS, F-91406 Orsay Cedex, France

<sup>10</sup>Department of Physics, Osaka University, Osaka 560-0043, Japan

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# New isotope production around $N=162$ in MNT reactions



Zhao-Qing Feng,<sup>\*</sup> Gen-Ming Jin, and Jun-Qing Li  
*Institute of Modern Physics, Chinese Academy of Sciences, Lanzhou 730000, People's Republic of China*  
 (Received 3 November 2009; published 7 December 2009)

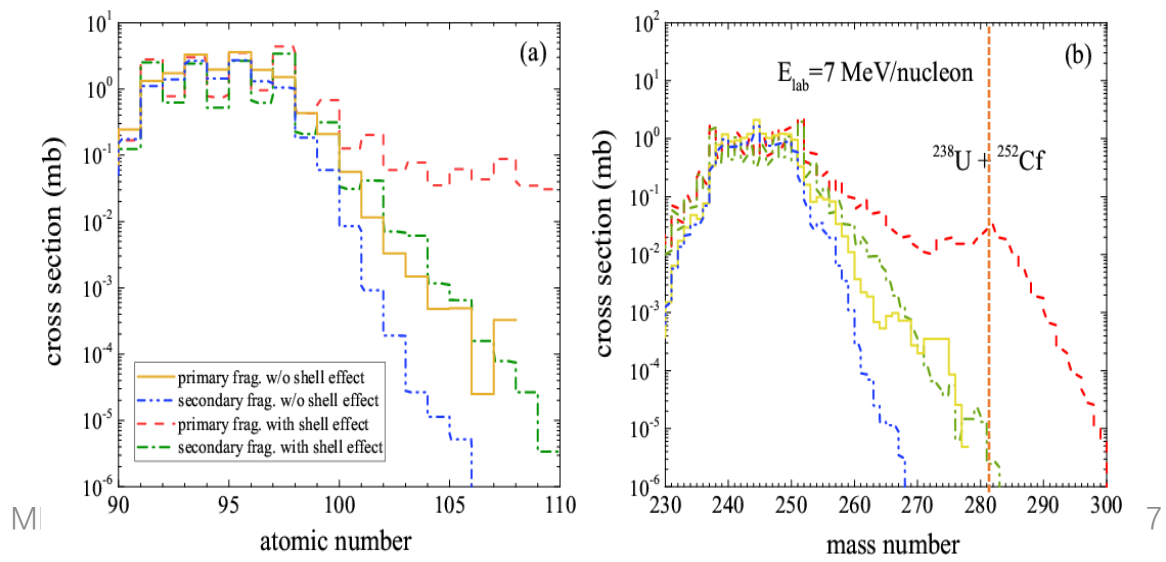
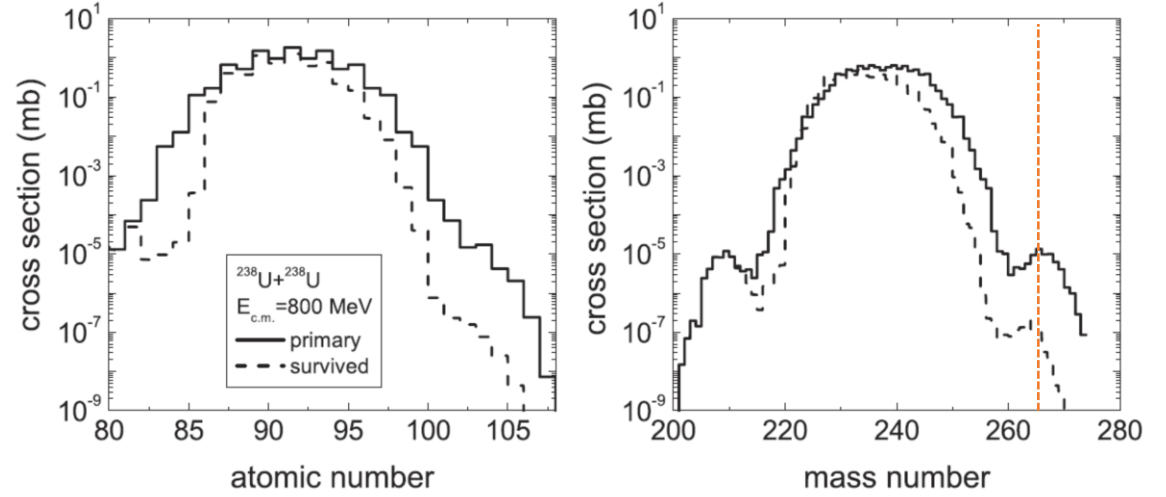
Eur. Phys. J. A (2022) 58:162  
<https://doi.org/10.1140/epja/s10050-022-00819-2>

THE EUROPEAN  
 PHYSICAL JOURNAL A

Regular Article - Theoretical Physics

## Production of neutron-rich heavy nuclei around $N = 162$ in multinucleon transfer reactions

Cheng Peng<sup>1</sup>, Zhao-Qing Feng<sup>1,\*</sup>  
<sup>1</sup> School of Physics and Optoelectronics, South China University of Technology, Guangzhou 510640, China



# Cluster emission ( $\alpha$ , ${}^8\text{Be}$ , etc) at IMP (Lanzhou) in the reaction of ${}^{12}\text{C}+{}^{209}\text{Bi}$ near barrier energy

第1卷 第1期  
1977年11月

高能物理与核物理  
PHYSICA ENERGIARUM FORTIS ET PHYSICA NUCLEARIS

Vol. 1, No. 1  
November, 1977

## ${}^{12}\text{C}$ 轰击 ${}^{209}\text{Bi}$ 时发射的 $\alpha$ 粒子

沈文庆 徐树威 王大延 谢元祥 郭中言 李祖玉  
(中国科学院近代物理研究所)



Nuclear Physics A

Volume 349, Issues 1-2, 3-10 November 1980, Pages 285-300



### Product cross sections for the reaction of ${}^{12}\text{C}$ with ${}^{209}\text{Bi}$ \*

Gen-Ming Jin<sup>1,2</sup>

<sup>1</sup> Institute of Modern Physics, Academia Sinica, Lanzhou, People's Republic of China

<sup>2</sup> The Niels Bohr Institute, Copenhagen Ø, Denmark

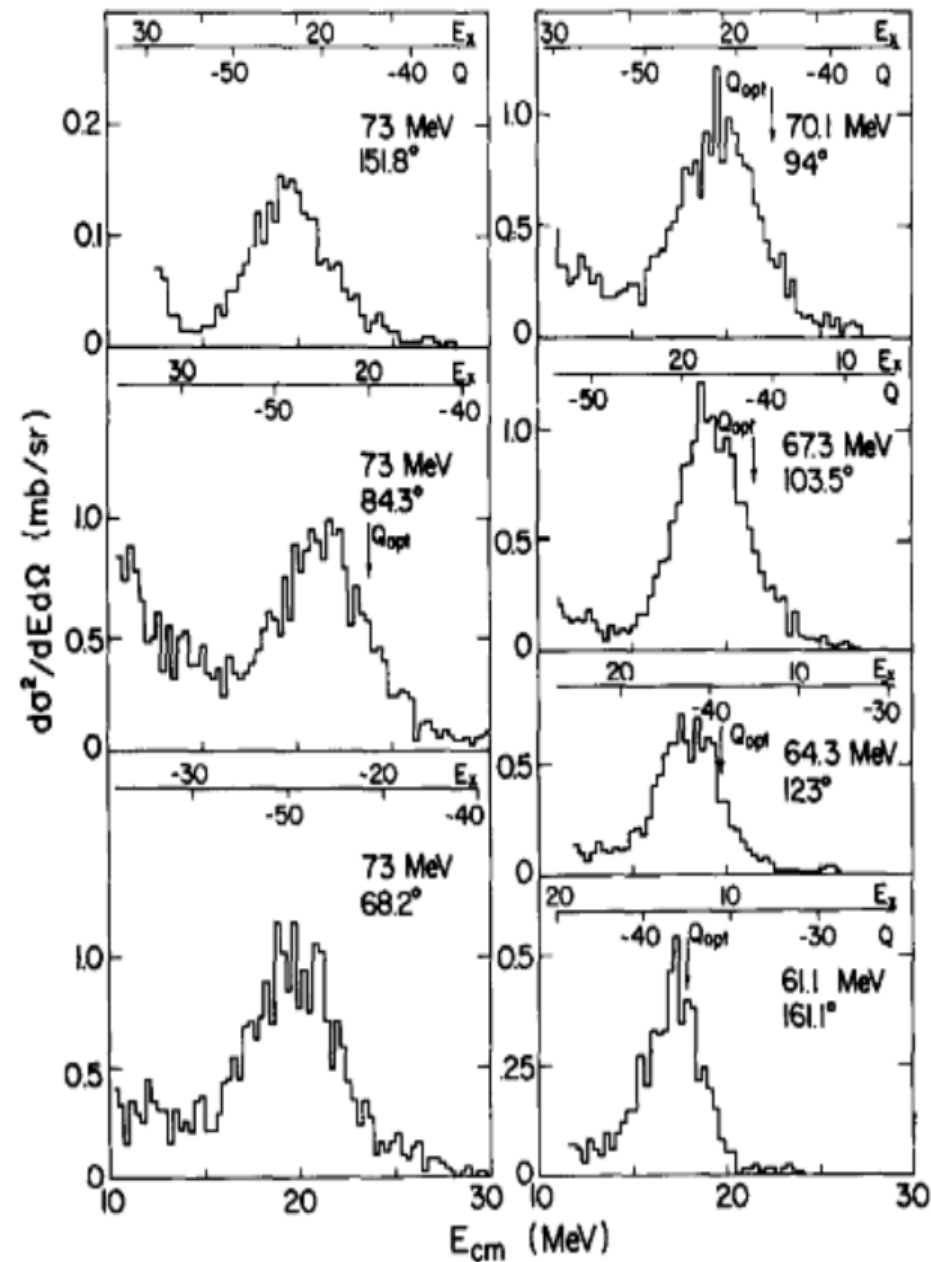
Yuan-Xiang Xie, Yong-Tai Zhu, Wen-Ging Shen, Xi-Jun Sun, Jun-Sheng Guo, Guo-Xing Liu, Ju-Sheng Yu, Chi-Chang Sun

Institute of Modern Physics, Academia Sinica, Lanzhou, People's Republic of China

J.D. Garrett

The Niels Bohr Institute, Copenhagen Ø, Denmark

轰击能量低于73MeV的 ${}^{12}\text{C}+{}^{209}\text{Bi}$ 反应研究	杨澄中, 沈文庆, 郭俊 盛, 邬恩九等	自然科学 奖	三等奖	国务院	1982-11-12
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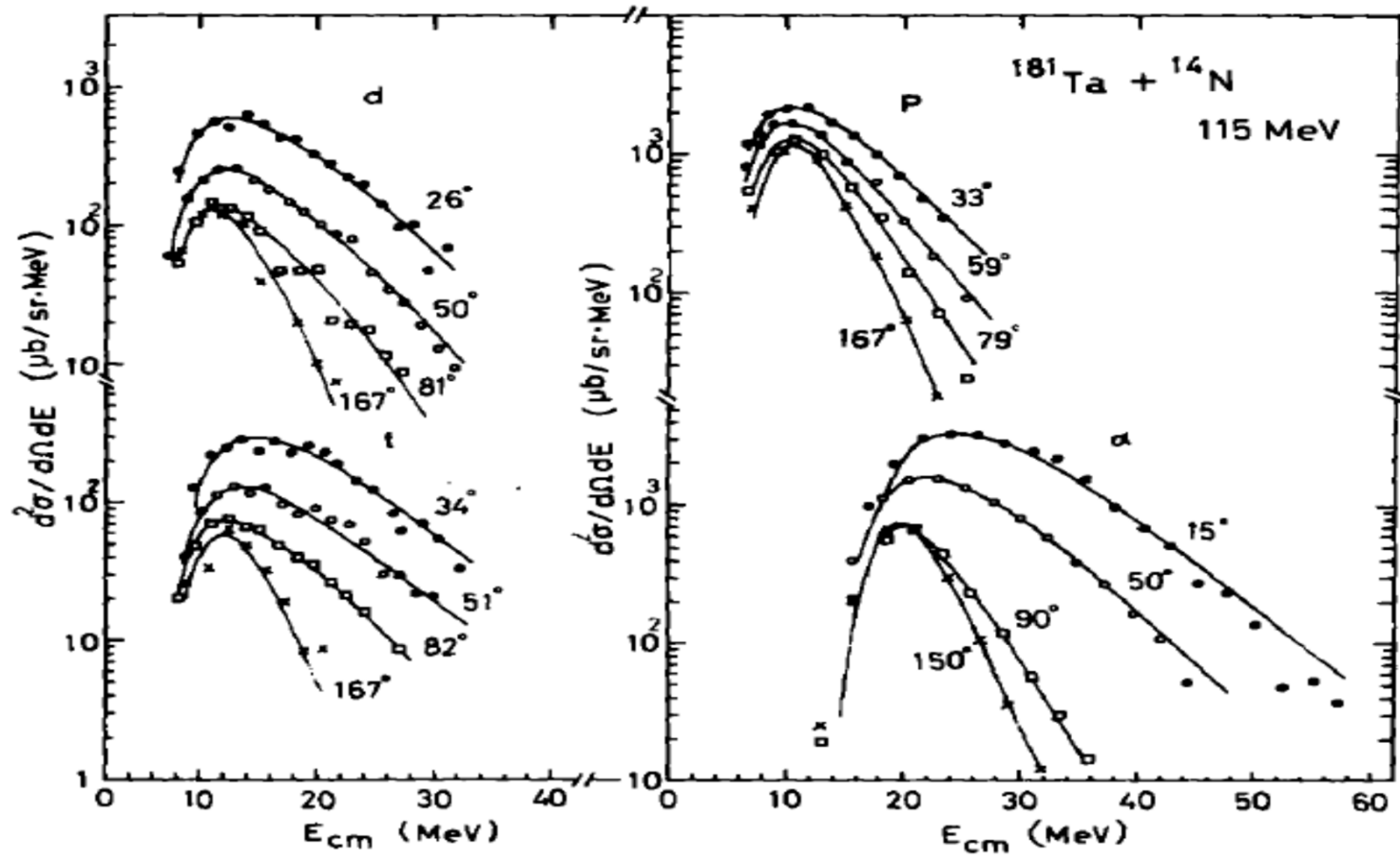
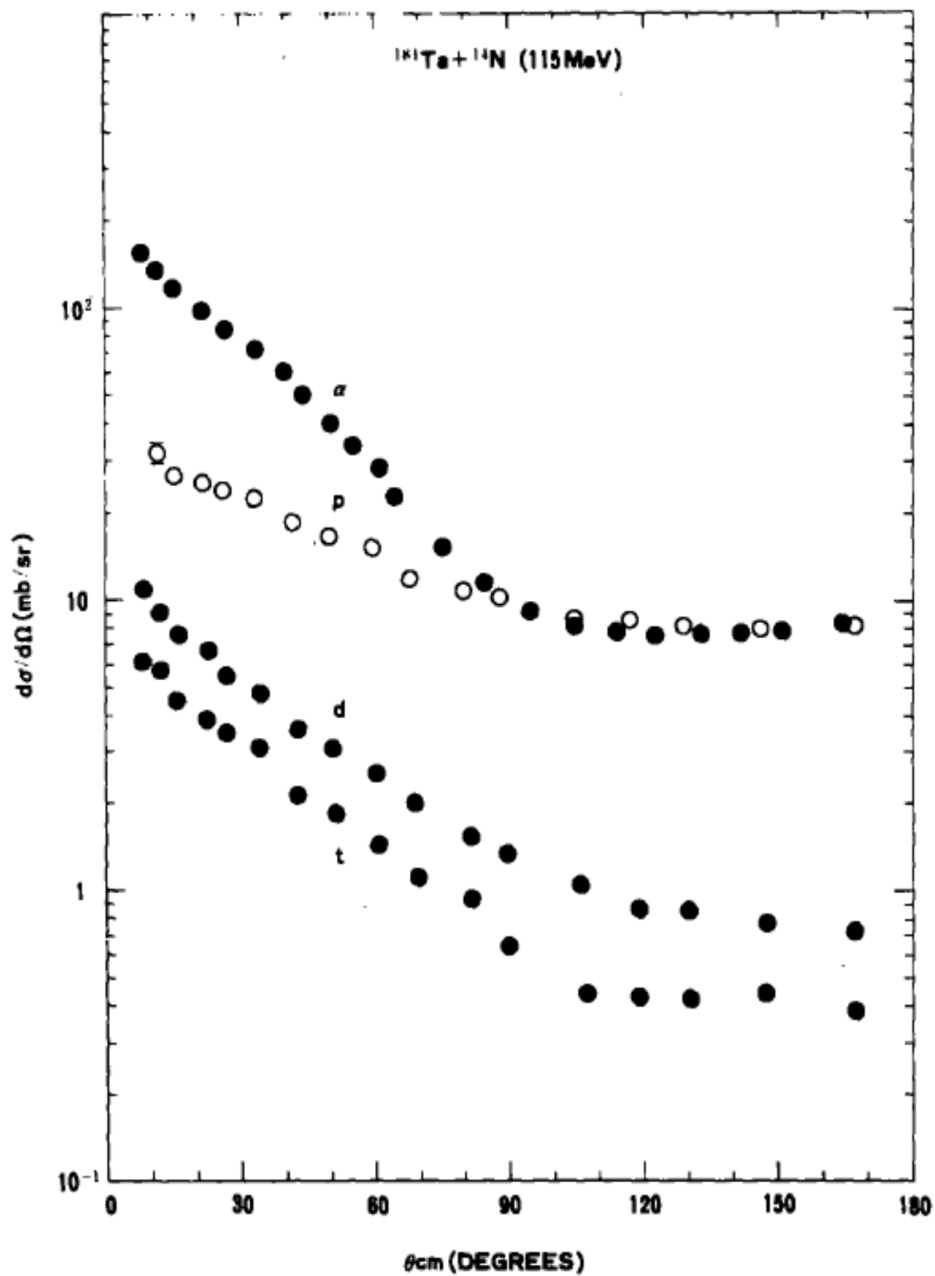




**PREEQUILIBRIUM  $\alpha$ -PARTICLE EMISSION IN HEAVY-ION REACTIONS**

H. UTSUNOMIYA †, T. NOMURA, T. INAMURA, T. SUGITATE †† and T. MOTOBAYASHI ‡  
 Cyclotron Laboratory, The Institute of Physical and Chemical Research, Wako-shi, Saitama, 351, Japan

Received 19 September 1979



# II. Dinuclear system model

## DEEP INELASTIC TRANSFER REACTIONS – THE NEW TYPE OF REACTIONS BETWEEN COMPLEX NUCLEI

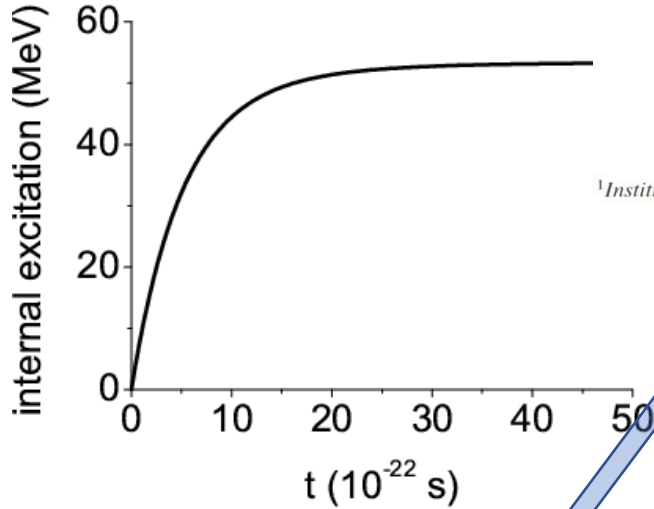
V.V. VOLKOV

Joint Institute for Nuclear Research, Dubna, USSR

Received October 1977

### Quasifission fragments:

G. G. Adamian, N. V. Antonenko, and A. S. Zubov, Phys. Rev. C 71, 034603 (2005)



PHYSICAL REVIEW C 76, 044606 (2007)

### Formation of superheavy nuclei in cold fusion reactions

Zhao-Qing Feng,<sup>1,2</sup> Gen-Ming Jin,<sup>1</sup> Jun-Qing Li,<sup>1</sup> and Werner Scheid<sup>3</sup>

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<sup>2</sup>Gesellschaft für Schwerionenforschung mbH (GSI), D-64291 Darmstadt, Germany

<sup>3</sup>Institut für Theoretische Physik der Universität, D-35392 Giessen, Germany

(Received 19 July 2007; published 16 October 2007)

PHYSICAL REVIEW C 80, 067601 (2009)

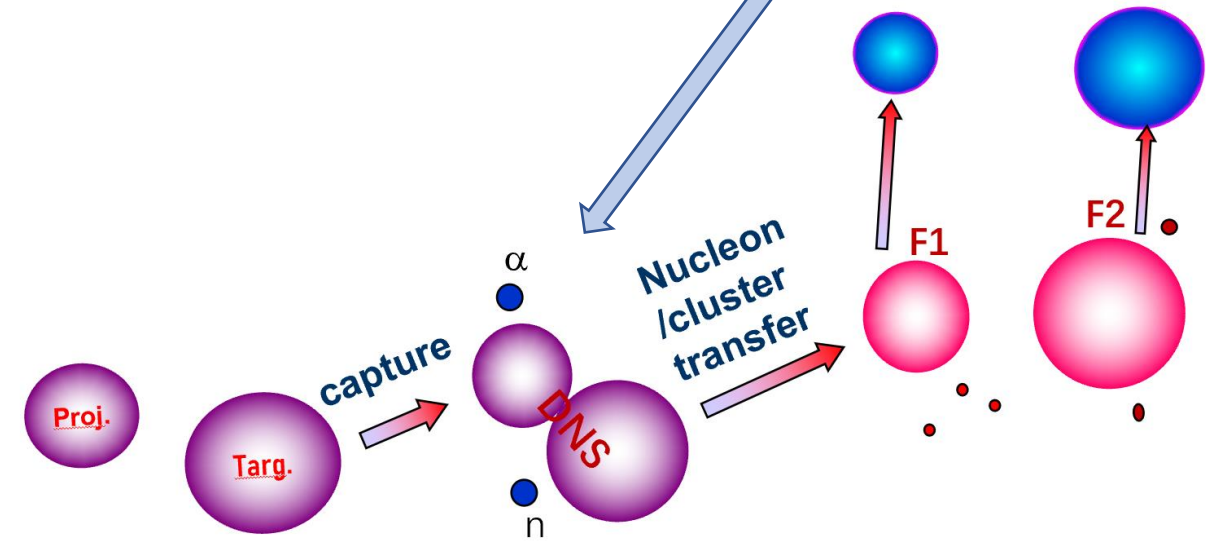
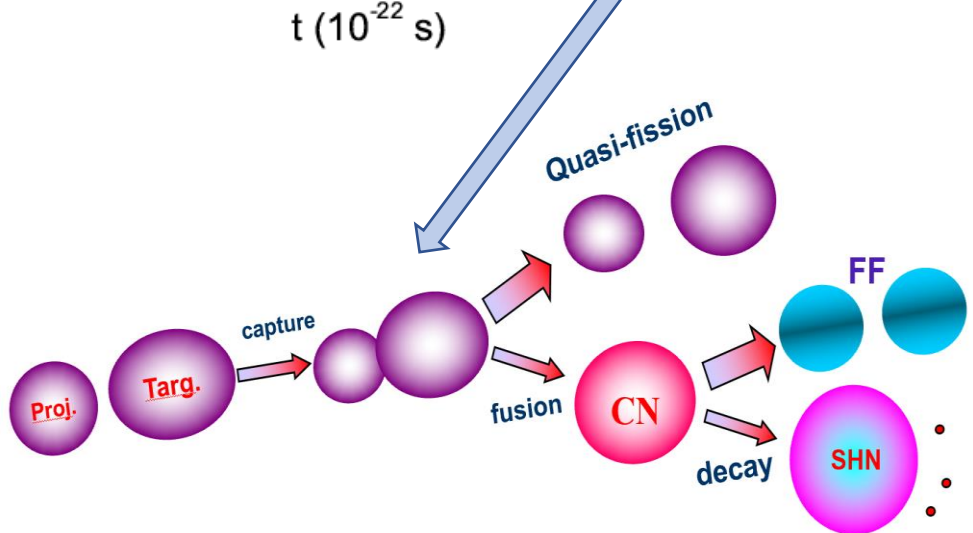
### Production of heavy isotopes in transfer reactions by collisions of <sup>238</sup>U + <sup>238</sup>U

Zhao-Qing Feng,<sup>\*</sup> Gen-Ming Jin, and Jun-Qing Li

Institute of Modern Physics, Chinese Academy of Sciences, Lanzhou 730000, People's Republic of China

(Received 3 November 2009; published 7 December 2009)

## Diffusion dynamics within the concept of dinuclear system

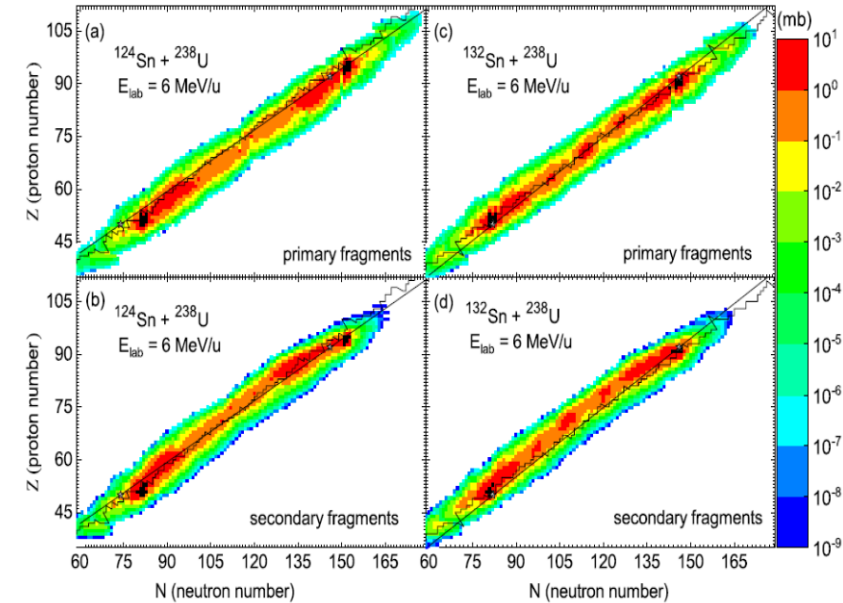
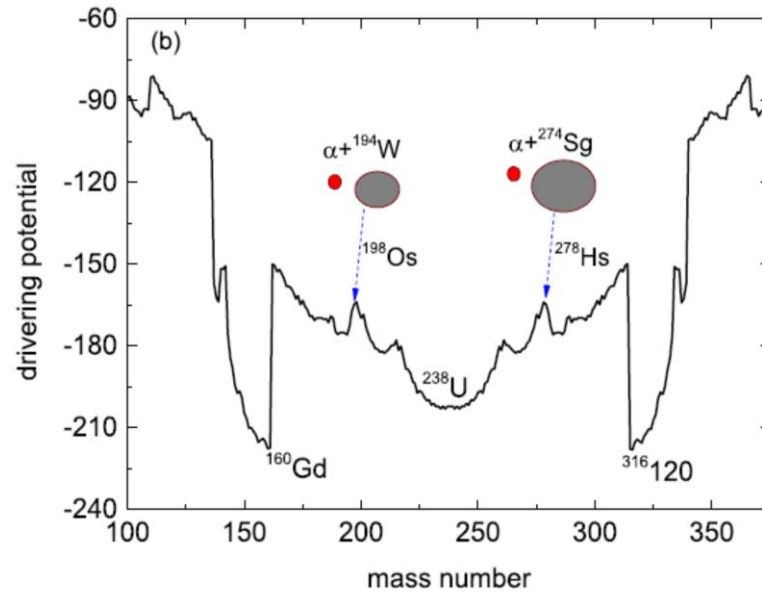
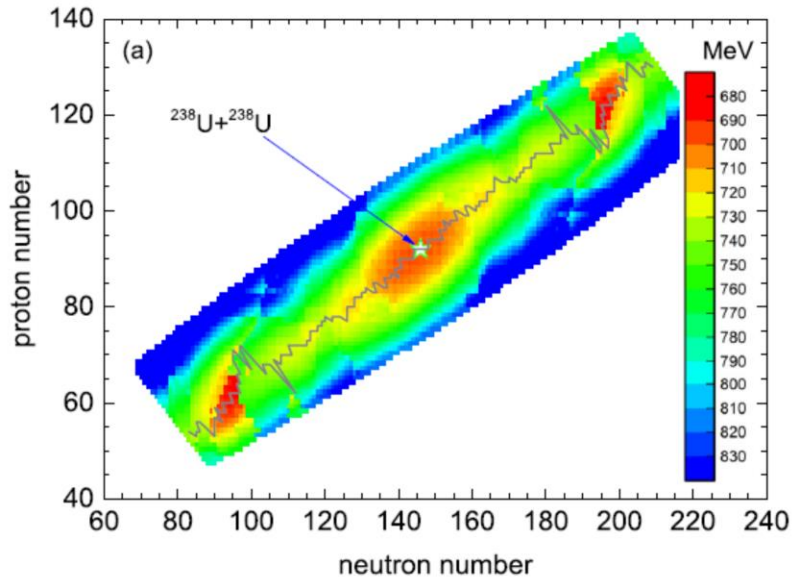
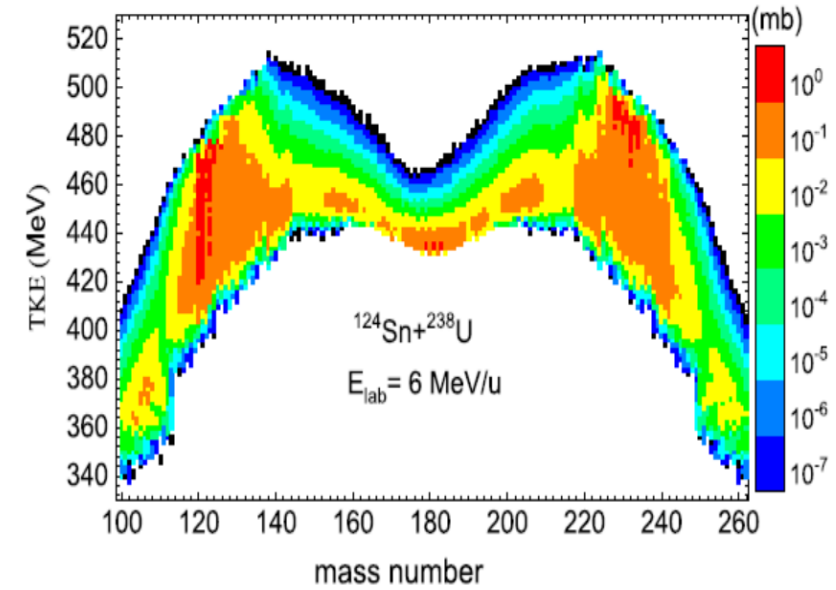
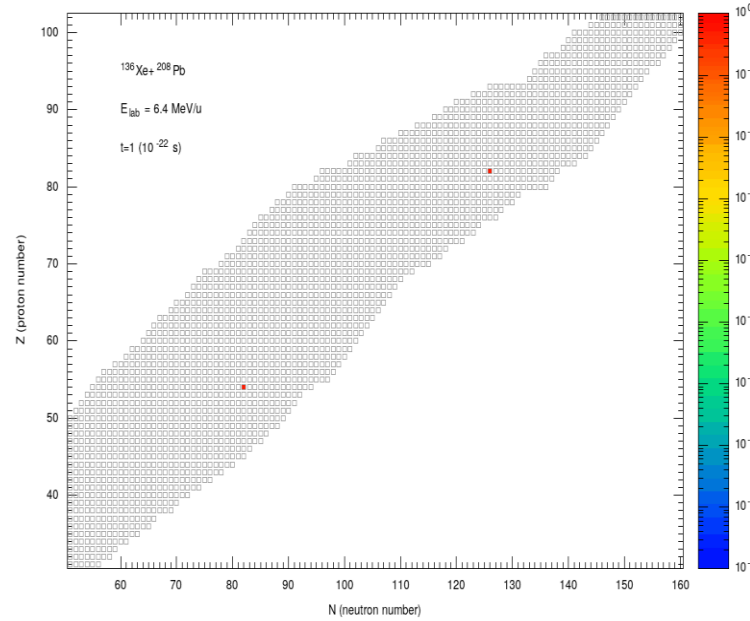


# CSs in the fusion-evaporation and MNT reactions

$$\sigma_{ER}(E_{c.m.}) = \frac{\pi\hbar^2}{2\mu E_{c.m.}} \sum_J (2J+1) T(E_{c.m.}, J) P_{CN}(E_{c.m.}, J) W_{sur}(E_{c.m.}, J)$$

$$\sigma_{pr}(Z_1, N_1, E_{c.m.}) = \sum_{J=0}^{J_{max}} \sigma_{cap}(E_{c.m.}, J) \int f(B) \times P(Z_1, N_1, E_1, J_1, B) dB.$$

$$\begin{aligned} \sigma_{sur}(Z_1, N_1, E_{c.m.}) &= \sum_{J=0}^{J_{max}} \sigma_{cap}(E_{c.m.}, J) \int f(B) \\ &\times P(Z_1, N_1, E_1, J_1, B) W_{sur}(E_1, J_1, s) dB, \end{aligned}$$



# The distribution probability with pure nucleon transfer

W. Li et al., Europhys. Lett. 64 (2003) 750; Z.-Q. Feng et al., NPA 771 (2006) 50, PRC 76 (2007) 044606, NPA 816 (2009) 33

$$\begin{aligned} & \frac{dP(Z_1, N_1, E_1, t)}{dt} \\ &= \sum_{Z'_1} W_{Z_1, N_1; Z'_1, N_1}(t) [d_{Z_1, N_1} P(Z'_1, N_1, E'_1, t) \\ & \quad - d_{Z'_1, N_1} P(Z_1, N_1, E_1, t)] + \sum_{N'_1} W_{Z_1, N_1; Z_1, N'_1}(t) \\ & \quad \times [d_{Z_1, N_1} P(Z_1, N'_1, E'_1, t) - d_{Z_1, N'_1} P(Z_1, N_1, E_1, t)] \end{aligned}$$

Transition probability

$$\begin{aligned} W_{Z_1, N_1; Z'_1, N_1} &= \frac{\tau_{\text{mem}}(Z_1, N_1, E_1; Z'_1, N_1, E'_1)}{d_{Z_1, N_1} d_{Z'_1, N_1} \hbar^2} \\ & \times \sum_{ii'} |\langle Z'_1, N_1, E'_1, i' | V | Z_1, N_1, E_1, i \rangle|^2 \end{aligned}$$

# The distribution probability with cluster transfer (neutron, proton, deuteron, triton, $^3\text{He}$ and $\alpha$ )

$$\begin{aligned} \frac{dP(Z_1, N_1, E_1, \beta_1, B, t)}{dt} &= \sum_{Z'_1=Z_1 \pm 1} W_{Z_1, N_1, \beta_1; Z'_1, N_1, \beta'_1}(t) [d_{Z_1, N_1} P(Z'_1, N_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ & + \sum_{N'_1=N_1 \pm 1} W_{Z_1, N_1, \beta_1; Z_1, N'_1, \beta'_1}(t) [d_{Z_1, N_1} P(Z_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ & + \sum_{Z'_1=\pm 1, N'_1=N_1 \pm 1} W_{Z_1, N_1, \beta_1; Z'_1, N'_1, \beta'_1}^d(t) [d_{Z_1, N_1} P(Z'_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ & + \sum_{Z'_1=\pm 1, N'_1=N_1 \pm 2} W_{Z_1, N_1, \beta_1; Z'_1, N'_1, \beta'_1}^t(t) [d_{Z_1, N_1} P(Z'_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ & + \sum_{Z'_1=\pm 2, N'_1=N_1 \pm 1} W_{Z_1, N_1, \beta_1; Z'_1, N'_1, \beta'_1}^{^3\text{He}}(t) [d_{Z_1, N_1} P(Z'_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ & + \sum_{Z'_1=\pm 2, N'_1=N_1 \pm 2} W_{Z_1, N_1, \beta_1; Z'_1, N'_1, \beta'_1}^\alpha(t) [d_{Z_1, N_1} P(Z'_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)]. \end{aligned}$$

$$W_{Z_1, N_1; Z'_1, N'_1}^\nu = G_\nu \frac{\tau_{\text{mem}}(Z_1, N_1, E_1; Z'_1, N'_1, E'_1)}{d_{Z_1, N_1} d_{Z'_1, N'_1} \hbar^2} \sum_{ii'} |\langle i' | V | i \rangle|^2$$

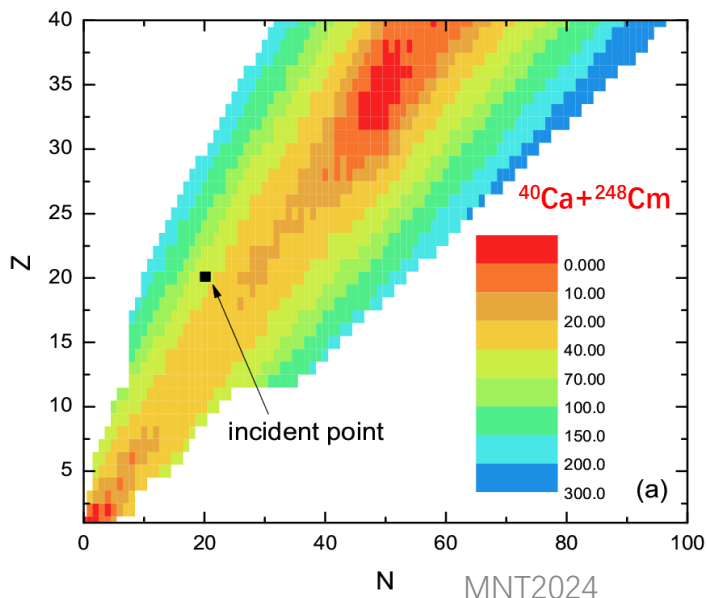
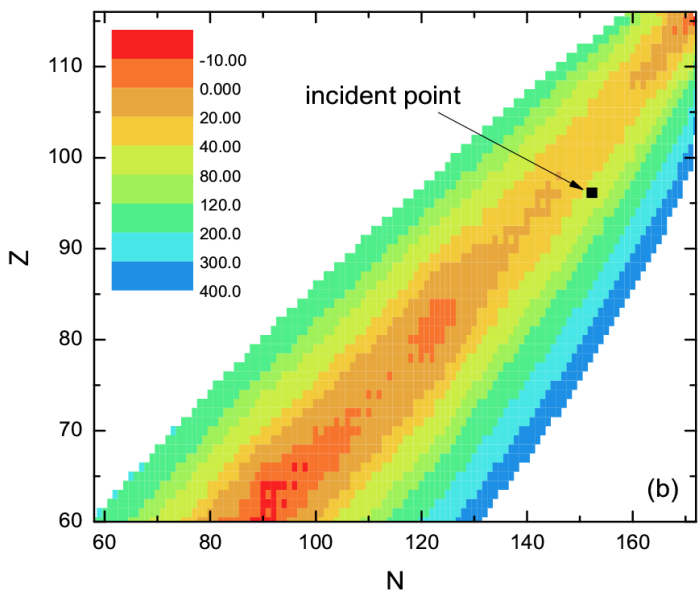
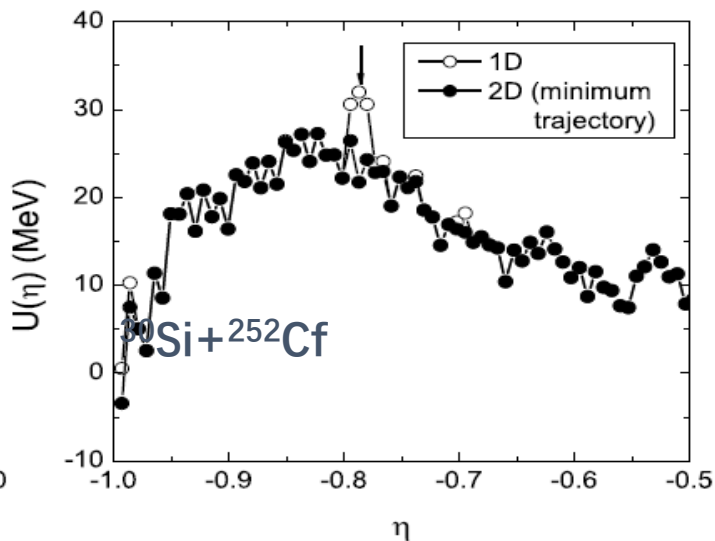
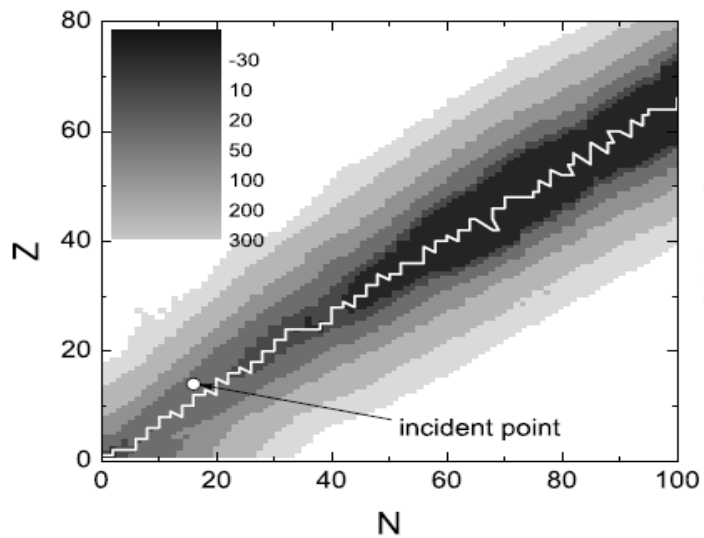
$$\begin{aligned} Z_1 &= Z_p + Z_t, \\ N_1 &= N_p + N_t \end{aligned}$$

$$\sum_{Z_1=0, N_1=0} P(Z_1, N_1, E_1, t) = 1$$

# Potential energy surface

$$U(\{\alpha\}) = B(Z_1, N_1) + B(Z_2, N_2) - [B(Z, N) + V_{\text{rot}}^{\text{CN}}(J)] + V(\{\alpha\})$$

With  $\{\alpha\}$  being  $Z_1, N_1, Z_2, N_2; J, R; \beta_1, \beta_2, \theta_1, \theta_2$



$$V(A_1, A_2, J, \mathbf{R}; \beta_1, \beta_2, \theta_1, \theta_2) = V_N(A_1, A_2, \mathbf{R}; \beta_1, \beta_2, \theta_1, \theta_2) + V_C(A_1, A_2, \mathbf{R}; \beta_1, \beta_2, \theta_1, \theta_2) + \frac{J(J+1)\hbar^2}{2\mu\mathbf{R}^2}$$

$$V_N = C_0 \left\{ \frac{F_{\text{in}} - F_{\text{ex}}}{\rho_0} \left[ \int \rho_1^2(\mathbf{r}) \rho_2(\mathbf{r} - \mathbf{R}) d\mathbf{r} + \int \rho_1(\mathbf{r}) \rho_2^2(\mathbf{r} - \mathbf{R}) d\mathbf{r} \right] + F_{\text{ex}} \int \rho_1(\mathbf{r}) \rho_2(\mathbf{r} - \mathbf{R}) d\mathbf{r} \right\}$$

with

$$F_{\text{in,ex}} = f_{\text{in,ex}} + f'_{\text{in,ex}} \frac{N_1 - Z_1}{A_1} \frac{N_2 - Z_2}{A_2}$$

$$\rho_1(\mathbf{r}) = \frac{\rho_0}{1 + \exp[(\mathbf{r} - \mathfrak{R}_1(\theta_1))/a_1]}$$

and

$$\rho_2(\mathbf{r} - \mathbf{R}) = \frac{\rho_0}{1 + \exp[(|\mathbf{r} - \mathbf{R}| - \mathfrak{R}_2(\theta_2))/a_2]}$$

# Nucleus-nucleus potential from the Skyrme energy-density functional

Commun. Theor. Phys. 74 (2022) 055302

C Peng and Z-Q Feng

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Commun. Theor. Phys. 74 (2022) 055302 (9pp)

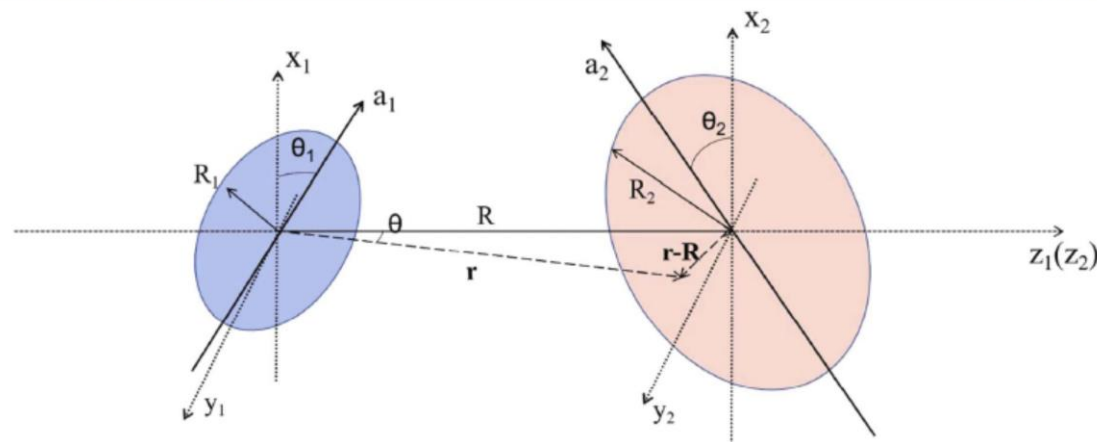
Communications in Theoretical Physics  
<https://doi.org/10.1088/1572-9494/ac6491>

## Potential energy surface and formation of superheavy nuclei with the Skyrme energy-density functional

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Bartel J and Bencheikh K 2002 Eur. Phys. J. A14 179

Denisov VY and Nörenberg W 2002 Eur. Phys. J. A15 375

$$V_{\text{nucl}}(R, \{\alpha\}_P, \{\alpha\}_T) = E_{\text{sys}}(R, \{\alpha\}_P, \{\alpha\}_T) - E_P(\{\alpha\}_P) - E_T(\{\alpha\}_T).$$

$$E_{\text{sys}}(R, \{\alpha\}_P, \{\alpha\}_T) = \int \varepsilon[\rho_{1p}(\mathbf{r}) + \rho_{2p}(\mathbf{R}-\mathbf{r}), \rho_{1n}(\mathbf{r}) + \rho_{2n}(\mathbf{R}-\mathbf{r})] d\mathbf{r},$$

$$E_P(\{\alpha\}_P) = \int \varepsilon[\rho_{1p}(\mathbf{r}), \rho_{1n}(\mathbf{r})] d\mathbf{r}$$

and

$$E_T(\{\alpha\}_T) = \int \varepsilon[\rho_{2p}(\mathbf{R}-\mathbf{r}), \rho_{2n}(\mathbf{R}-\mathbf{r})] d\mathbf{r},$$

$$\begin{aligned} \hat{V}_{\text{eff}}(\mathbf{r}_1, \mathbf{r}_2) = & t_0(1 + x_0 \hat{P}_\sigma) \delta(\mathbf{r}_1 - \mathbf{r}_2) \\ & + \frac{t_3}{6}(1 + x_3 \hat{P}_\sigma) \delta\left(\frac{1}{2}(\mathbf{r}_1 + \mathbf{r}_2)\right) \delta(\mathbf{r}_1 - \mathbf{r}_2) \\ & - \frac{t_1}{2}(1 + x_1 \hat{P}_\sigma) ((\nabla_1 - \nabla_2)^2 \delta(\mathbf{r}_1 - \mathbf{r}_2) + h.c.) \\ & - t_2(1 + x_2 \hat{P}_\sigma) ((\nabla_1 - \nabla_2) \delta(\mathbf{r}_1 - \mathbf{r}_2) (\nabla_1 - \nabla_2)) \\ & + iW_0(\hat{\sigma}_1 + \hat{\sigma}_2) \cdot \hat{\mathbf{k}}' \times \delta(\mathbf{r}_1 - \mathbf{r}_2) \hat{\mathbf{k}} \end{aligned}$$

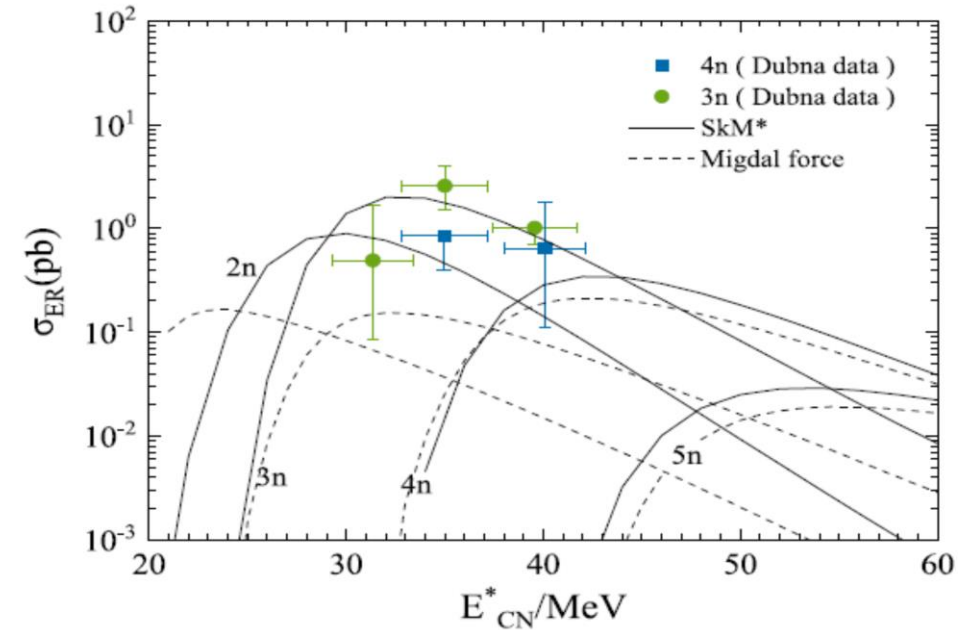
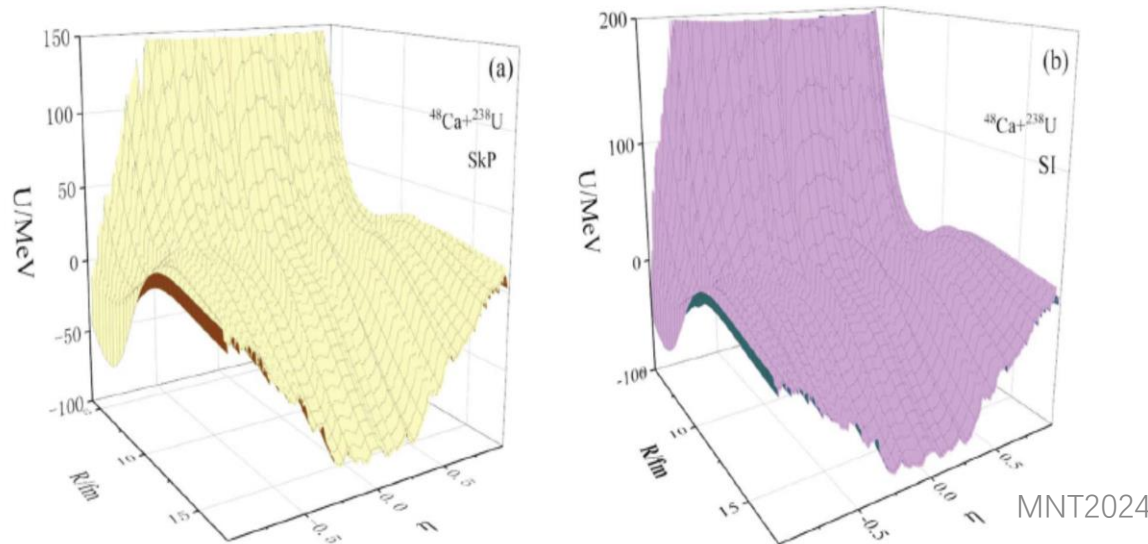
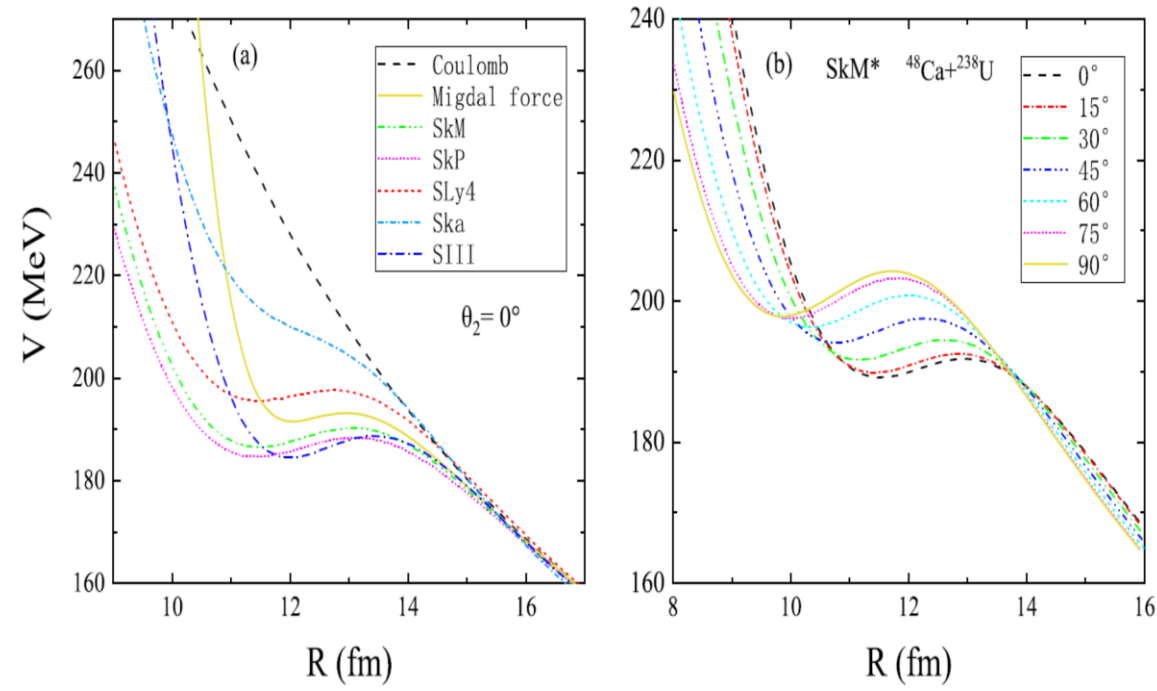
$$\begin{aligned} \nu_{sk}(\mathbf{r}) = & \frac{t_0}{2} \left[ \left(1 + \frac{1}{2}x_0\right) \rho^2 - \left(x_0 + \frac{1}{2}\right) (\rho_p^2 + \rho_n^2) \right] \\ & + \frac{1}{12} t_3 \rho^\alpha \left[ \left(1 + \frac{1}{2}x_3\right) \rho^2 - \left(x_3 + \frac{1}{2}\right) (\rho_p^2 + \rho_n^2) \right] \\ & + \frac{1}{4} \left[ t_1 \left(1 + \frac{1}{2}x_1\right) + t_2 \left(1 + \frac{1}{2}x_2\right) \right] \tau \rho \\ & + \frac{1}{4} \left[ t_2 \left(x_2 + \frac{1}{2}\right) - t_1 \left(x_1 + \frac{1}{2}\right) \right] (\tau_p \rho_p + \tau_n \rho_n) \\ & + \frac{1}{16} \left[ 3t_1 \left(1 + \frac{1}{2}x_1\right) - t_2 \left(1 + \frac{1}{2}x_2\right) \right] (\nabla \rho)^2 \\ & - \frac{1}{16} \left[ 3t_1 \left(x_1 + \frac{1}{2}\right) + t_2 \left(x_2 + \frac{1}{2}\right) \right] ((\nabla \rho_n)^2 + (\nabla \rho_p)^2) \\ & - \frac{mW_0^2}{2\hbar^2} \left[ \frac{\rho_p}{f_p} (2\nabla \rho_p + \nabla \rho_n)^2 + \frac{\rho_n}{f_n} (2\nabla \rho_n + \nabla \rho_p)^2 \right] \end{aligned}$$

MNT2024

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**Table 1.** Parameters of the Skyrme forces used in the calculation.

Parameter	SkP	SkM	SkM*	SLy4	Ska	SIII
$t_0$ (MeV fm <sup>3</sup> )	-2931.7	-2645	-2645	-2488.91	-1602.78	-1128.75
$t_1$ (MeV fm <sup>5</sup> )	320.6	385	410	486.82	570.88	395.0
$t_2$ (MeV fm <sup>5</sup> )	-337.4	-120	-135	-546.39	-67.70	-95
$t_3$ (MeV fm <sup>3+3<math>\alpha</math></sup> )	18 709	15 595	15 595	13 777	8000	14 000
$x_0$	0.292	0.09	0.09	0.834	-0.02	0.45
$x_1$	0.653	0	0	-0.344	0	0
$x_2$	-0.537	0	0	-1.0	0	0
$x_3$	0.181	0	0	1.354	-0.286	1
$W_0$ (MeV fm <sup>5</sup> )	100	130	130	123	125	120
$\alpha$	1/6	1/6	1/6	1/6	1/3	1
$K_\infty$ (MeV)	199	217	217	230	261	352

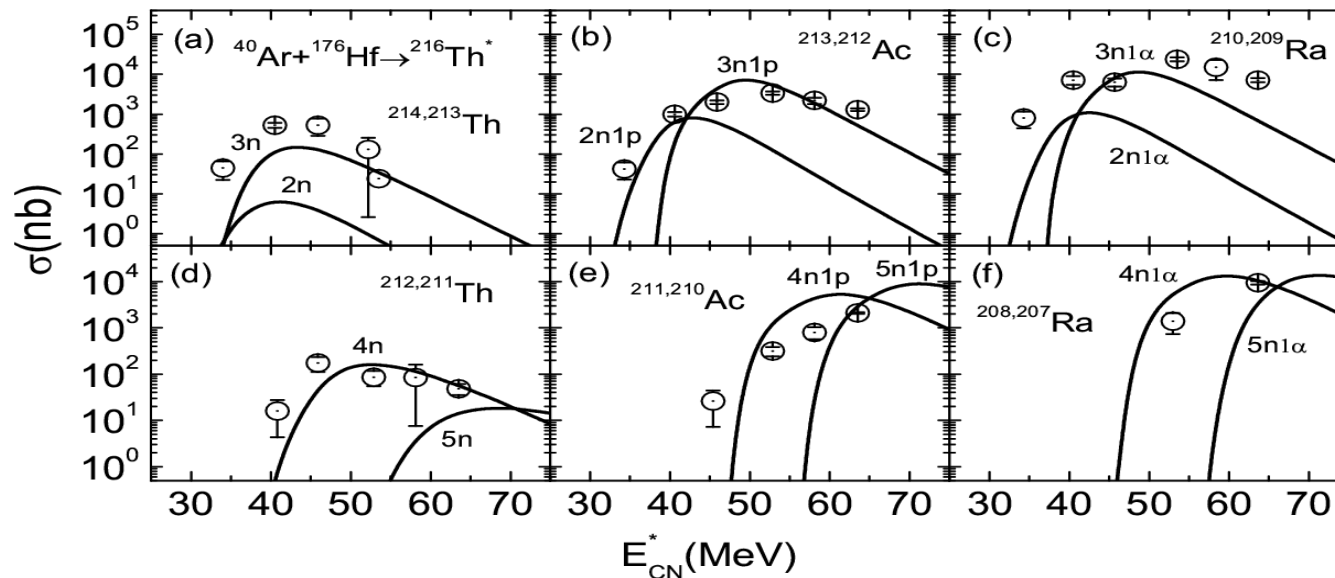
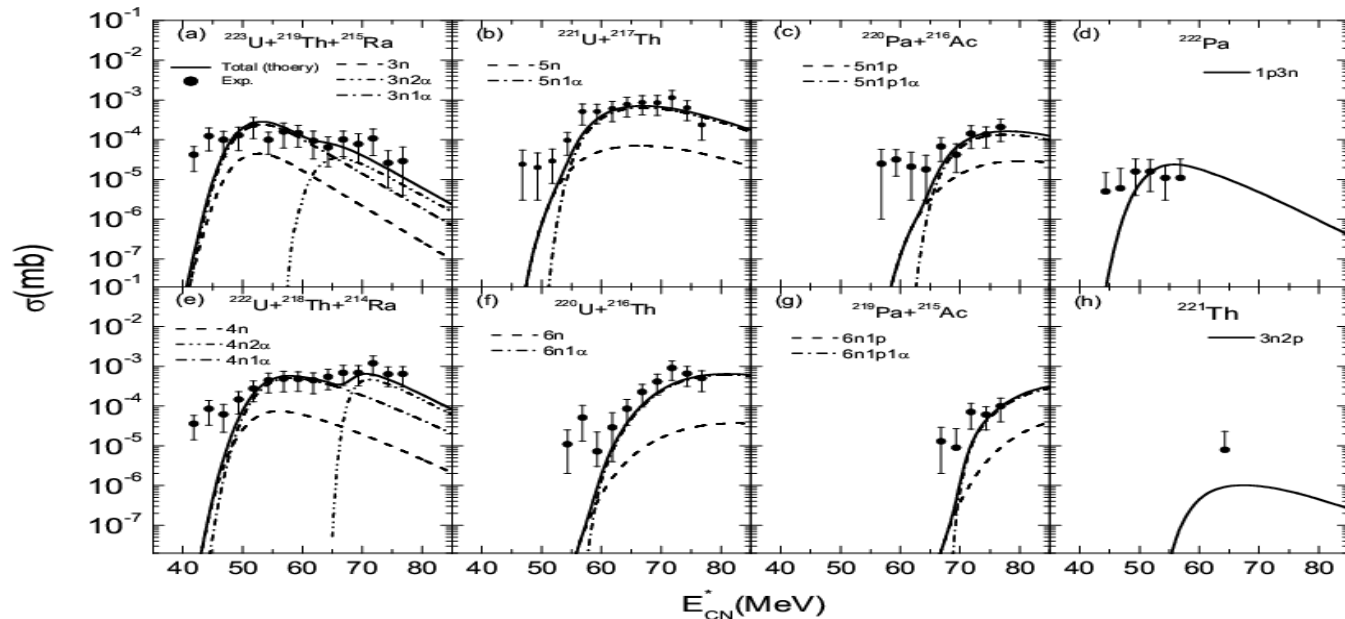
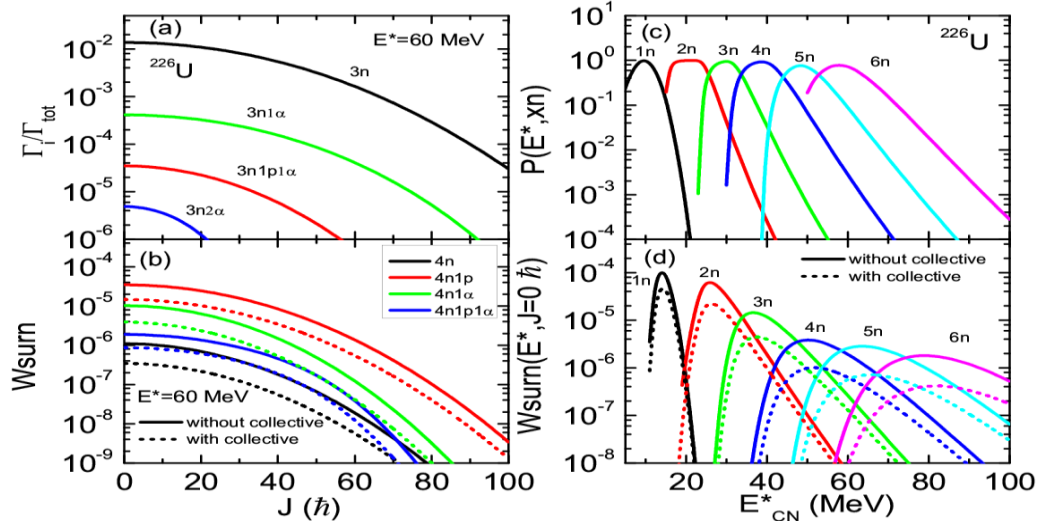
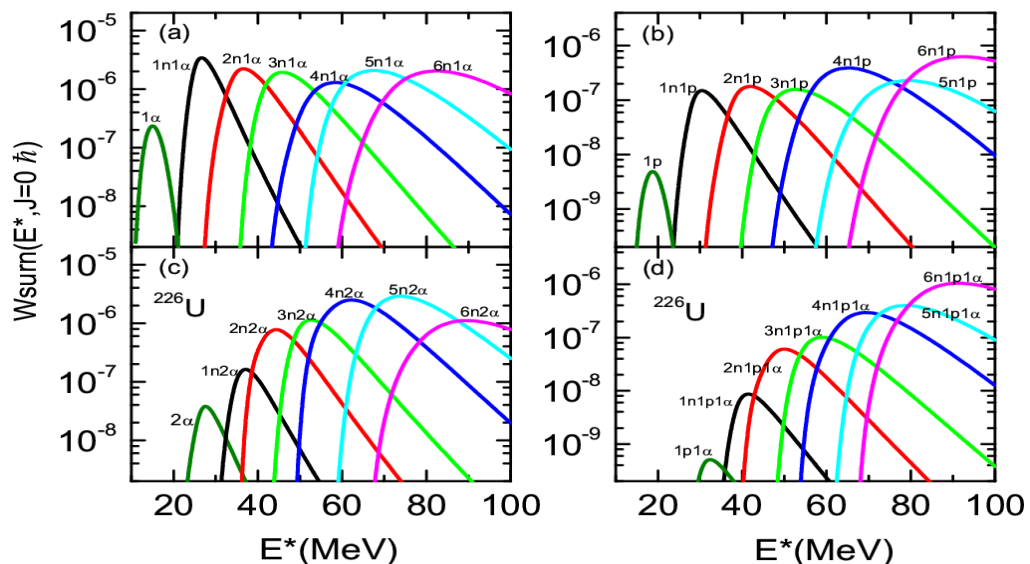


# Survival probability and fusion-evaporation CSs

Data from RIKEN (K. Nishio, H. Ikezoe, S. Mitsuoka et al, Phys. Rev. C 62, 014602 (2000))

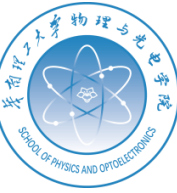
P. H. Chen, Z. Q. Feng\* et al., Chinese Physics C 40, 091002 (2016) (highlight CPC in 2016)

Peng-Hui Chen, Zhao-Qing Feng\*, et al., Eur. Phys. J. A 53, 95 (2017)





# III. Results and discussion



## 1. Fusion-evaporation reactions for synthesizing 119 and 120

Fei Niu, Peng-Hui Chen, Zhao-Qing Feng, Nuclear Science and Techniques 32 (2021) 103

第 37 卷第 3 期  
2022 年 10 月

原子核物理评论  
Nuclear Physics Review

Vol. 37, No. 3  
Oct., 2022

Article ID: 1007-4627(2022)03-0001-15

### Production cross-sections of new superheavy elements with $Z = 119-120$ in fusion-evaporation reactions

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3. College of Electrical, Power and Energy Engineering, Yangzhou University, Yangzhou 225009, China;

4. School of Physics and Optoelectronics, South China University of Technology, Guangzhou 510641, China)

Table 2 The same as in Table 1; for the production of SHE  $Z = 120$

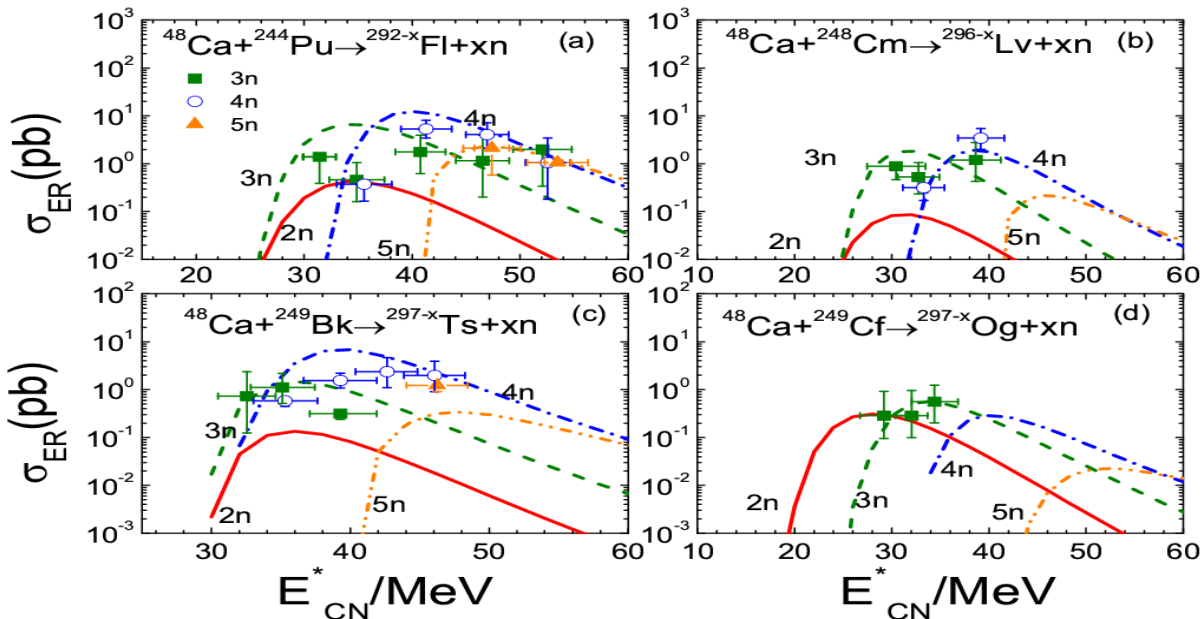
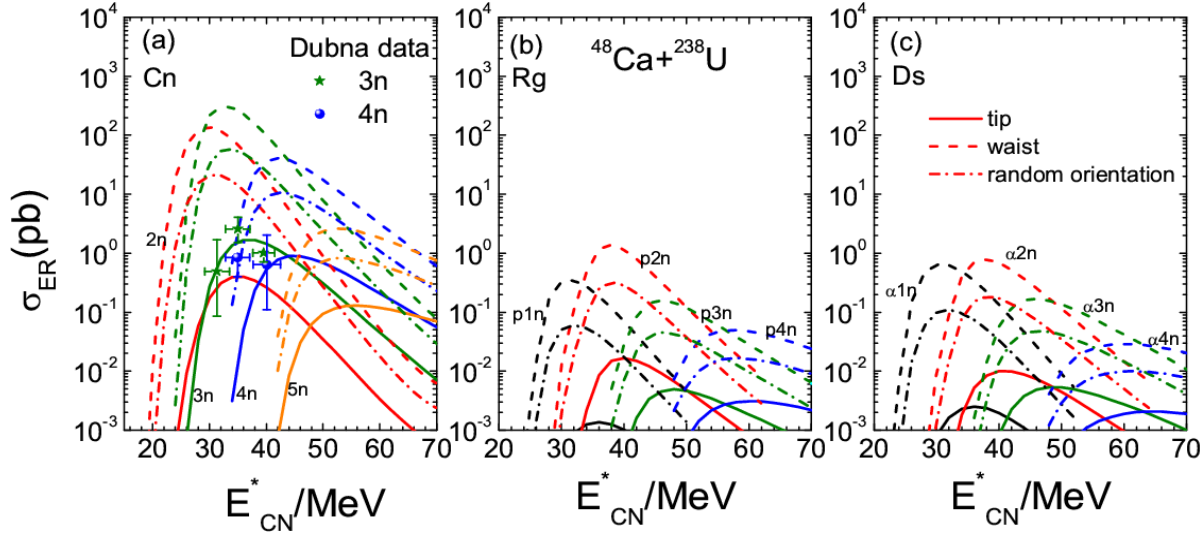
Reaction systems	$\sigma_{ER}$ (pb)	$E_{CN}^*$ (MeV)	References
$^{249}\text{Cr}(^{50}\text{Ti},4n)^{295}\text{120}$	0.006	43	[61]
$^{251}\text{Cr}(^{50}\text{Ti},4n)^{297}\text{120}$	0.003	42	
$^{248}\text{Cm}(^{54}\text{Cr},4n)^{298}\text{120}$	0.001	35	
$^{244}\text{Pu}(^{58}\text{Fe},3n)^{299}\text{120}$	0.01	36	[63]
$^{238}\text{U}(^{64}\text{Ni},3n)^{299}\text{120}$	0.007	36	
$^{248}\text{Cm}(^{54}\text{Cr},3n)^{299}\text{120}$	0.076	36	
$^{249}\text{Cr}(^{50}\text{Ti},3n)^{296}\text{120}$	0.76	33	
$^{249}\text{Cr}(^{50}\text{Ti},3n)^{296}\text{120}$	0.1	29	[64]
$^{248}\text{Cm}(^{54}\text{Cr},3n)^{299}\text{120}$	0.055	30	
$^{249}\text{Cr}(^{50}\text{Ti},4n)^{295}\text{120}$	0.046	43	[59]
$^{248}\text{Cm}(^{54}\text{Cr},4n)^{298}\text{120}$	0.028	43	
$^{249}\text{Cr}(^{50}\text{Ti},3n)^{296}\text{120}$	0.06	36	[29]
$^{248}\text{Cr}(^{46}\text{Ti},2n)^{292}\text{120}$	0.17	34	
$^{249}\text{Cr}(^{46}\text{Ti},3n)^{292}\text{120}$	0.24	39	
$^{250}\text{Cr}(^{46}\text{Ti},2n)^{294}\text{120}$	0.13	36	
$^{251}\text{Cr}(^{46}\text{Ti},3n)^{294}\text{120}$	0.37	39	
$^{251}\text{Cr}(^{50}\text{Ti},3n)^{298}\text{120}$	0.11	33	
$^{251}\text{Cr}(^{48}\text{Ti},2n)^{297}\text{120}$	0.25	25	This work
$^{244}\text{Pu}(^{58}\text{Fe},3n)^{299}\text{120}$	0.004	33	
$^{244}\text{Pu}(^{62}\text{Fe},3n)^{303}\text{120}$	0.0004	31	
$^{248}\text{Cm}(^{54}\text{Cr},3n)^{299}\text{120}$	0.004	33	
$^{248}\text{Cm}(^{52}\text{Cr},2n)^{300}\text{120}$	0.37	25	
$^{238}\text{U}(^{64}\text{Ni},3n)^{299}\text{120}$	0.001	31	
$^{238}\text{U}(^{62}\text{Ni},2n)^{300}\text{120}$	0.001	27	
$^{252}\text{Es}(^{44}\text{Sc},3n)^{293}\text{120}$	3.18	35	
$^{252}\text{Es}(^{45}\text{Sc},3n)^{293}\text{120}$	0.59	35	
$^{249}\text{Bk}(^{49}\text{V},2n)^{296}\text{120}$	0.18	27	
$^{249}\text{Bk}(^{51}\text{V},2n)^{298}\text{120}$	0.1	27	

$$Q(^{54}\text{Cr}+^{248}\text{Cm}) = -207.77 \text{ MeV}$$

$$\sigma_{3n} = 4 \text{ fb}, E_{CN}^* = 33 \text{ MeV},$$

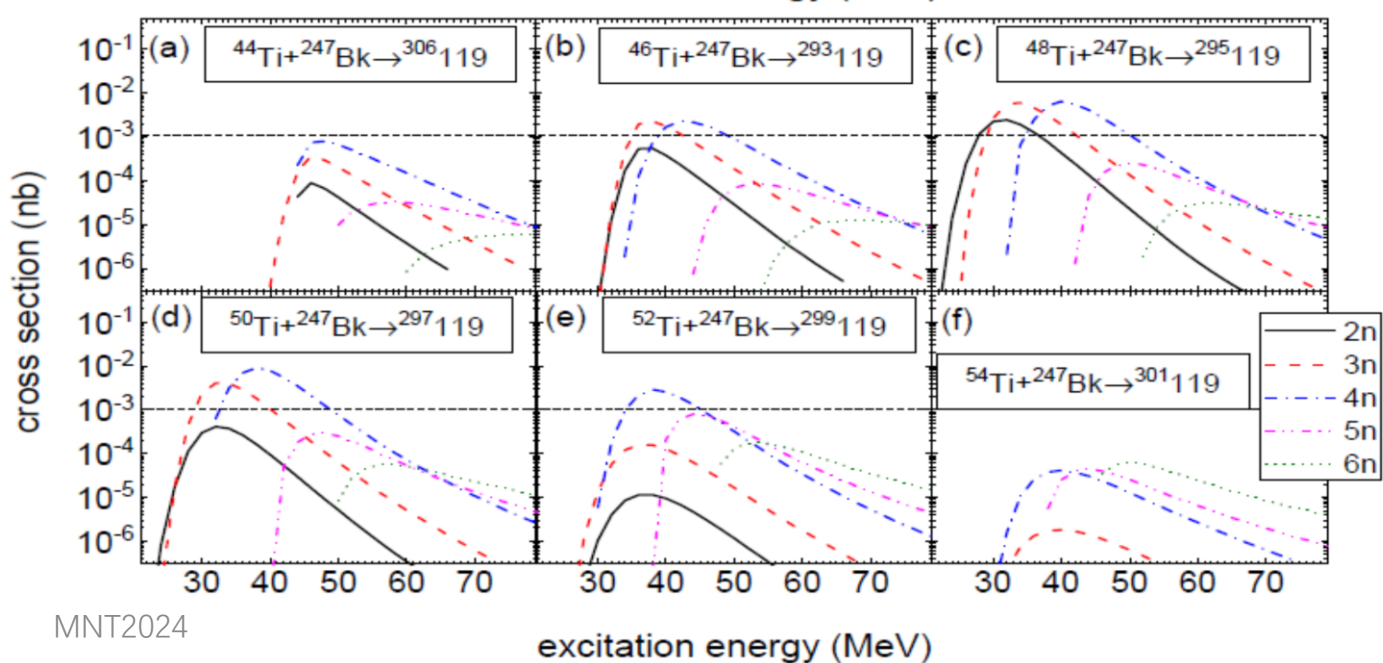
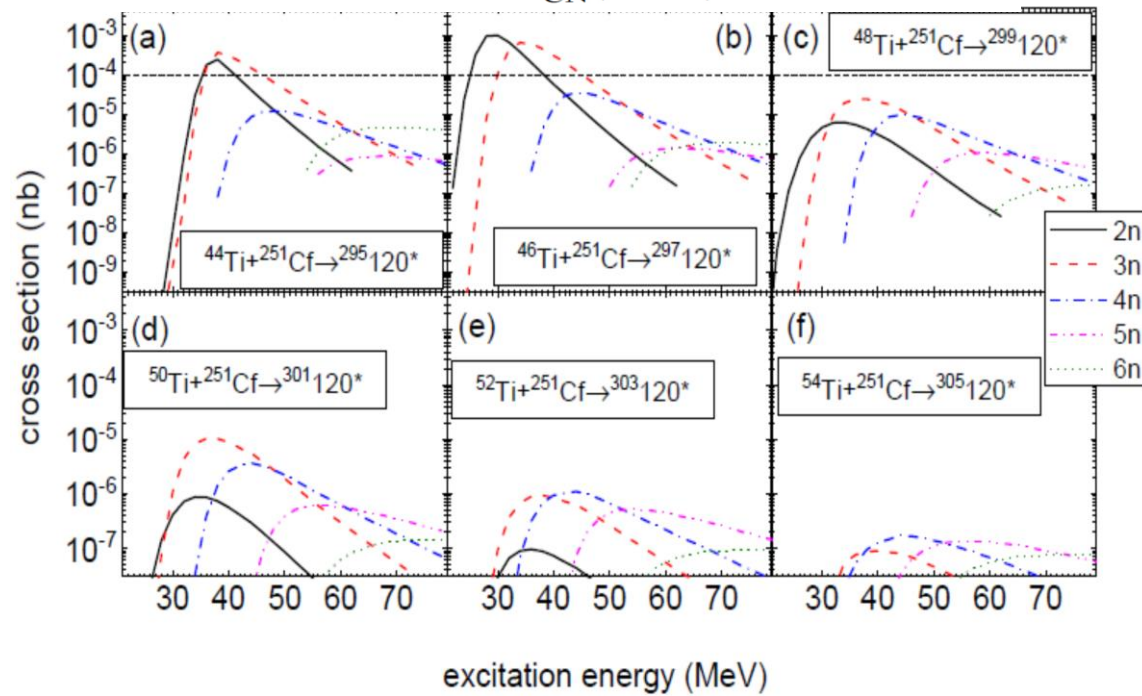
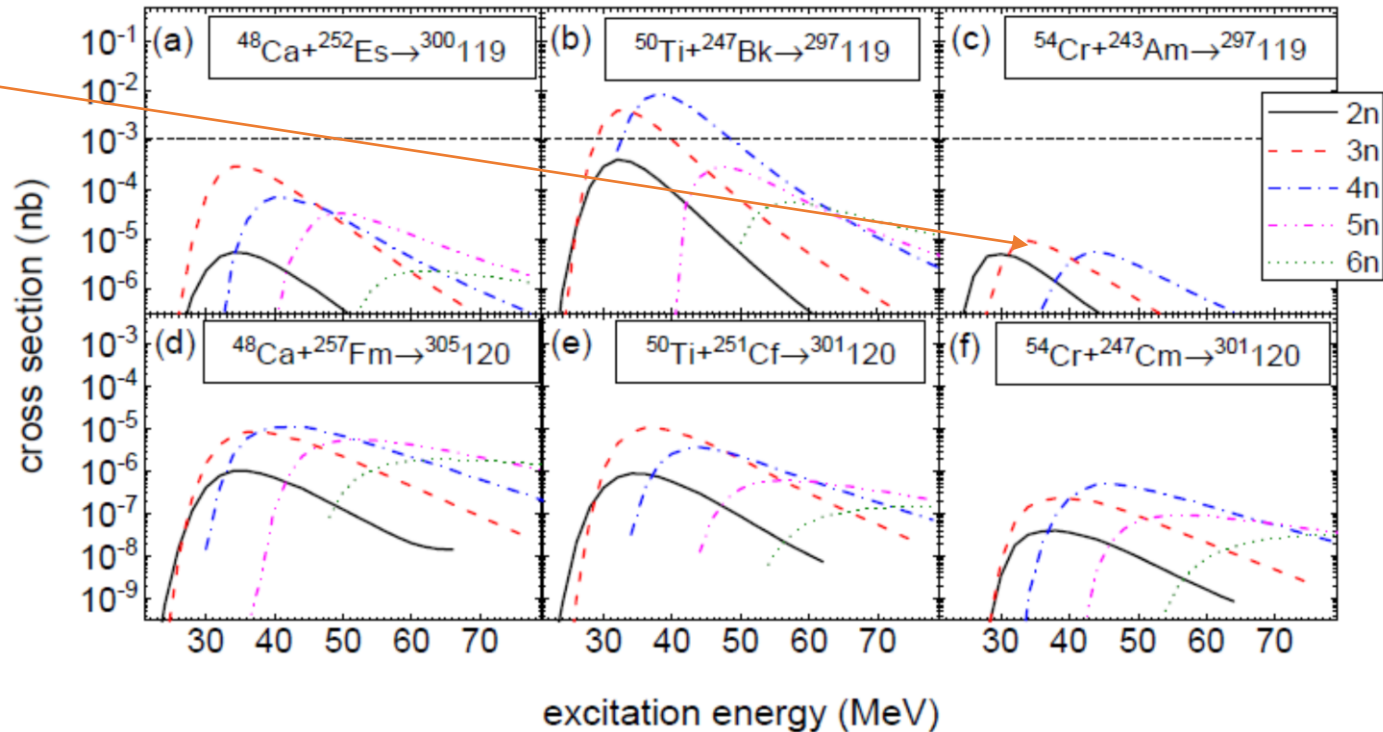
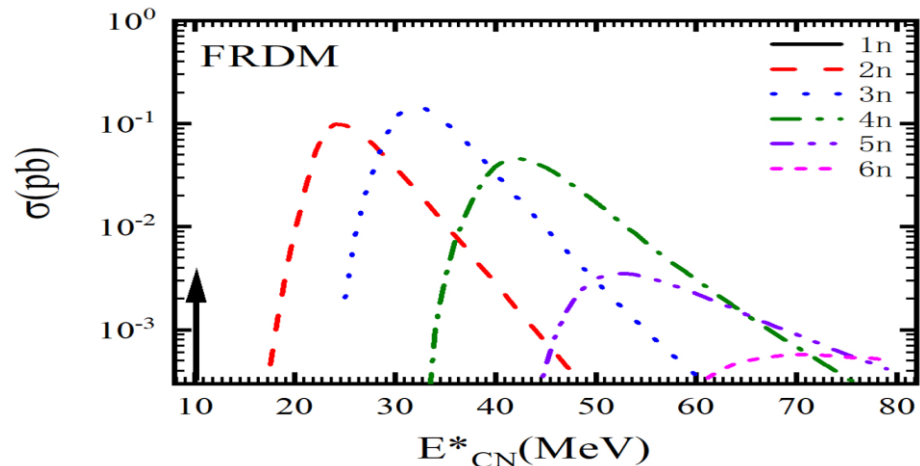
$$E_{c.m.} = 240.77 \text{ MeV},$$

$$E_{\text{lab}} = 5.43 \text{ MeV/nucleon}$$

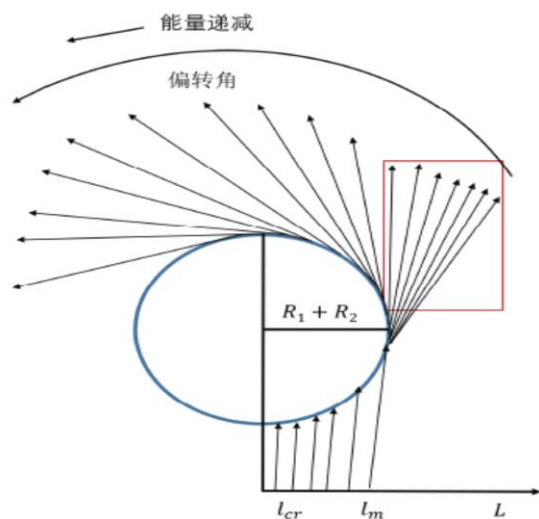
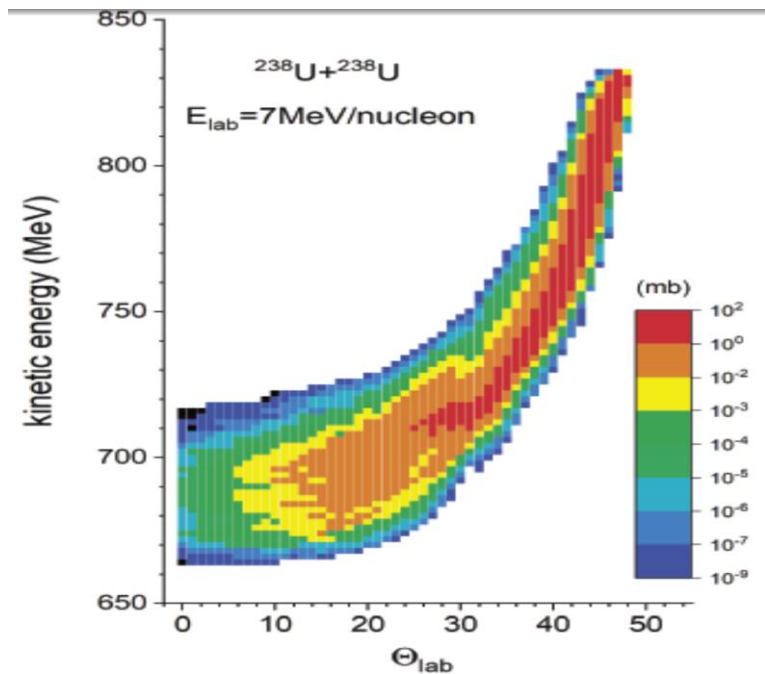


**10 fb** in the reactions  $^{54}\text{Cr}(^{243}\text{Am}, 3n)^{294}\text{119}$  at the excitation energy 34 MeV,  $Q=-205.43$  MeV,  $E_{\text{c.m.}}=239.43$  MeV,  $E_{\text{lab}}=5.42$  MeV/nucleon

mass table: [P. Möller et al., PRC 91, 024310 \(2015\)](#)



## 2. Yields, total kinetic energy spectra and angular distribution in MNT reactions

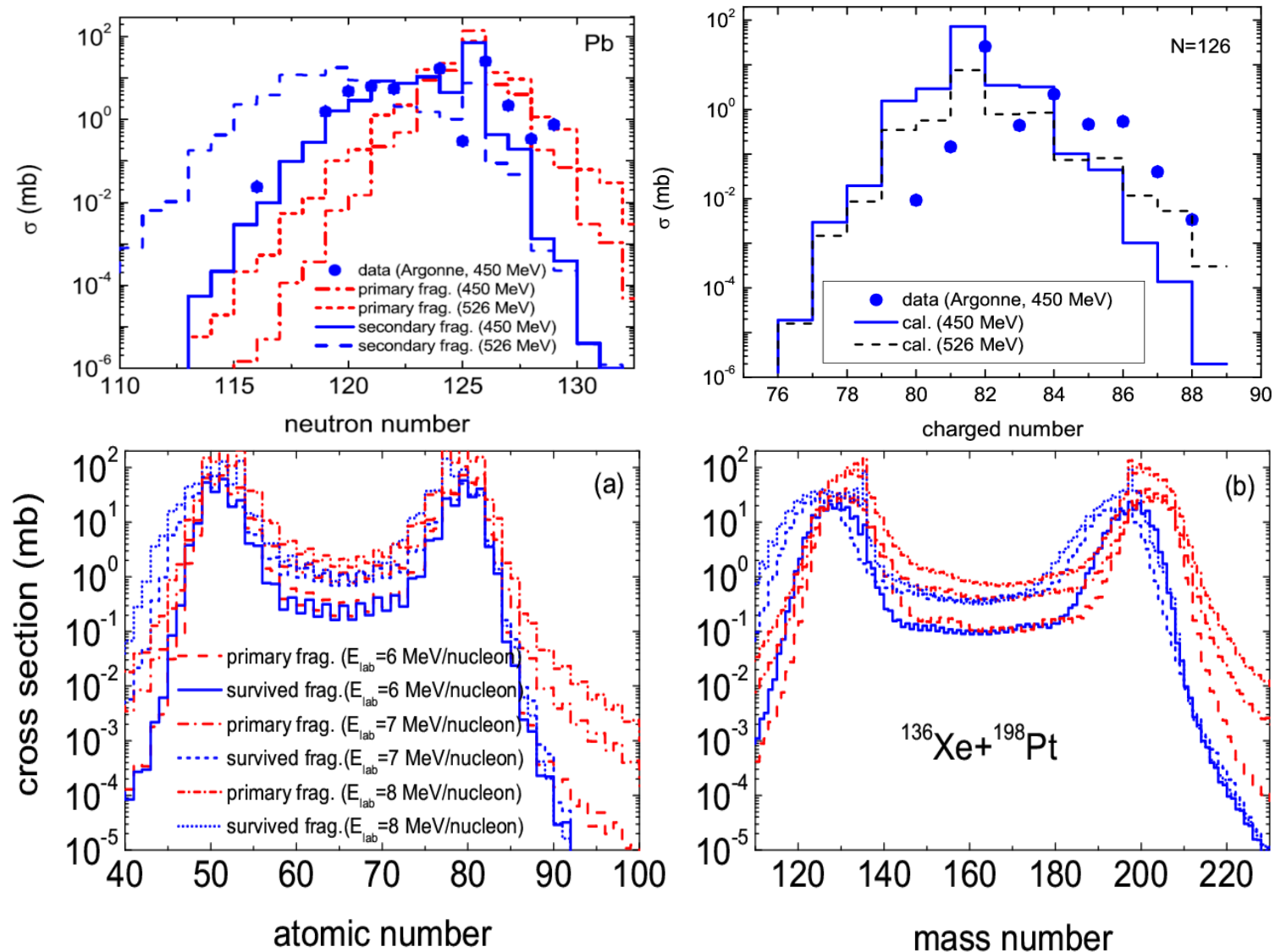


## Production of neutron-rich isotopes around $N = 126$ in multinucleon transfer reactions

Zhao-Qing Feng\*

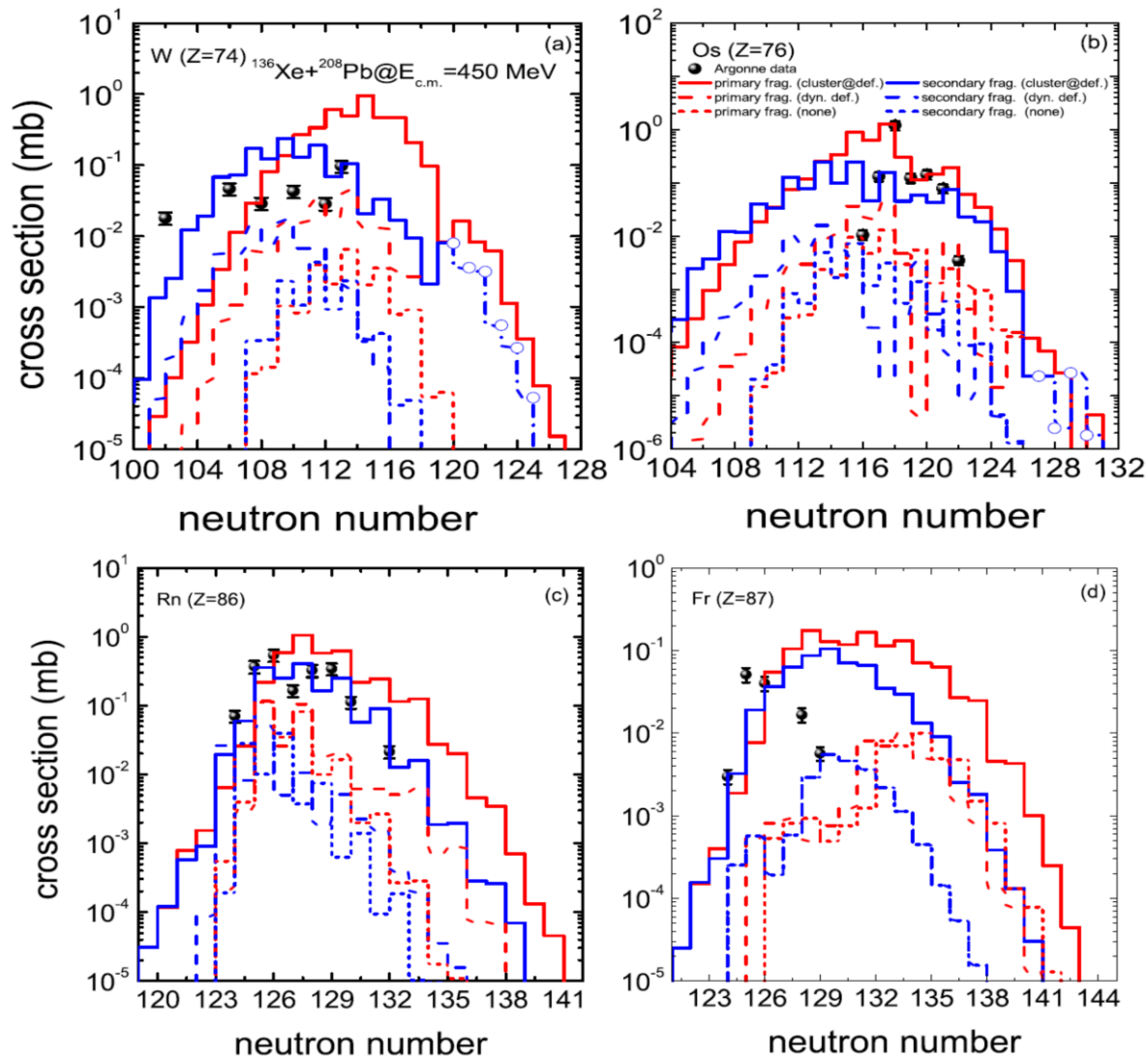
*Institute of Modern Physics, Chinese Academy of Sciences, Lanzhou 730000, People's Republic of China*

(Received 15 November 2016; published 22 February 2017)



### 3. Cluster transfer and cluster emission in massive transfer reactions

#### Cluster transfer effect on the MNT fragment production



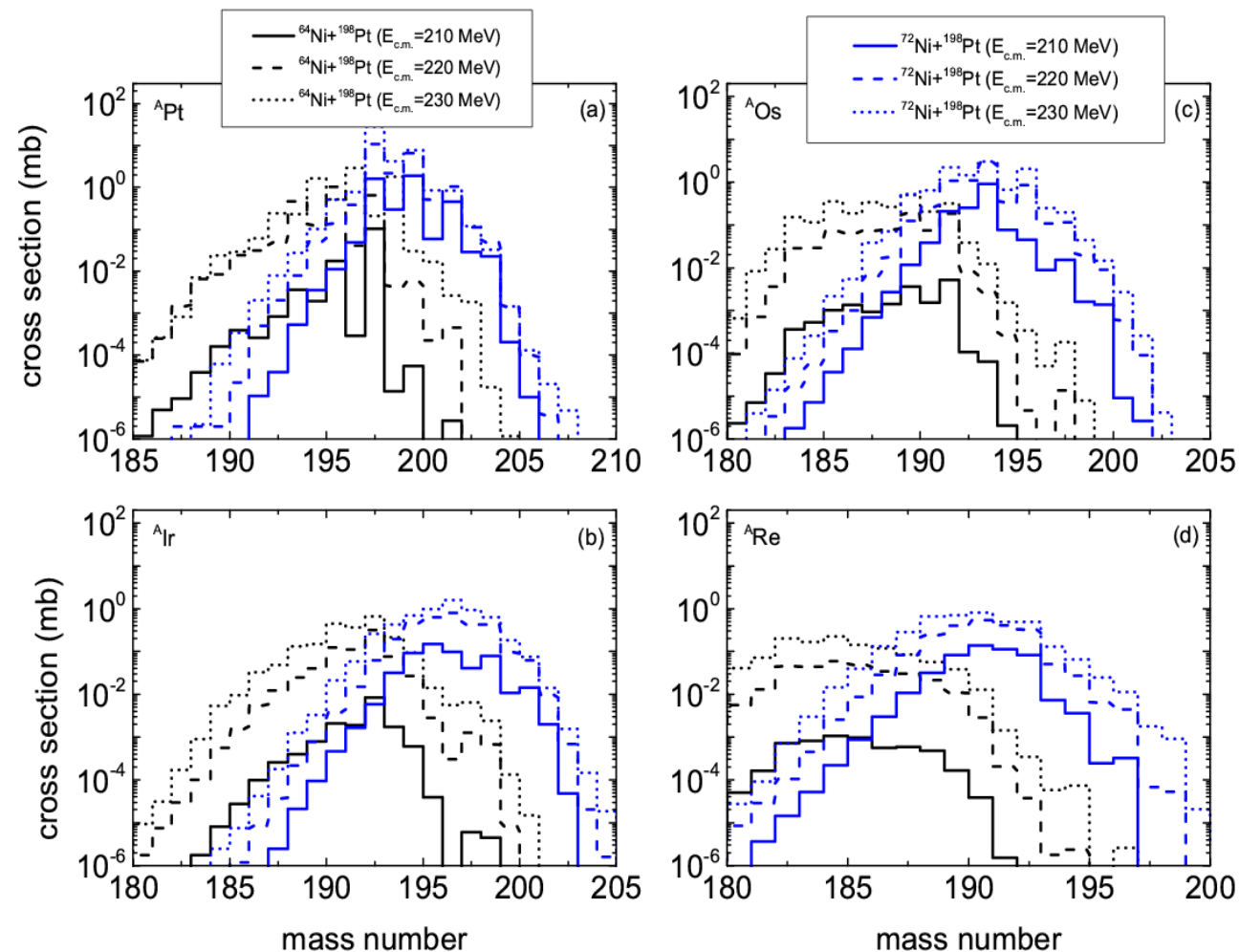
#### Effect of cluster transfer on the production of neutron-rich nuclides near $N = 126$ in multinucleon-transfer reactions

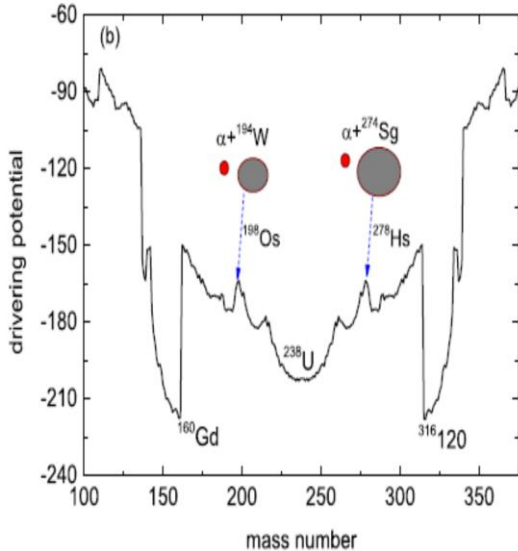
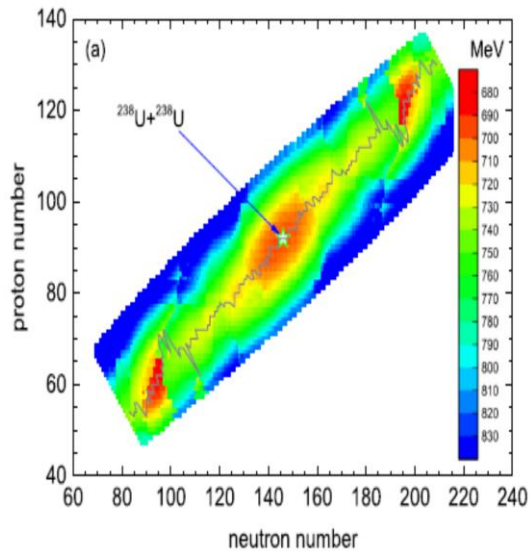
Zhao-Qing Feng\*

School of Physics and Optoelectronics, South China University of Technology, Guangzhou 510640, China

(Received 8 July 2023; revised 19 September 2023; accepted 17 October 2023; published 13 November 2023)

Phys. Rev. C **108**, L051601 (2023), arXiv:2308.03127





## Preequilibrium cluster emission in massive transfer reactions near the Coulomb barrier energy

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School of Physics and Optoelectronics, South China University of Technology, Guangzhou 510640, China

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2023 年 3 月

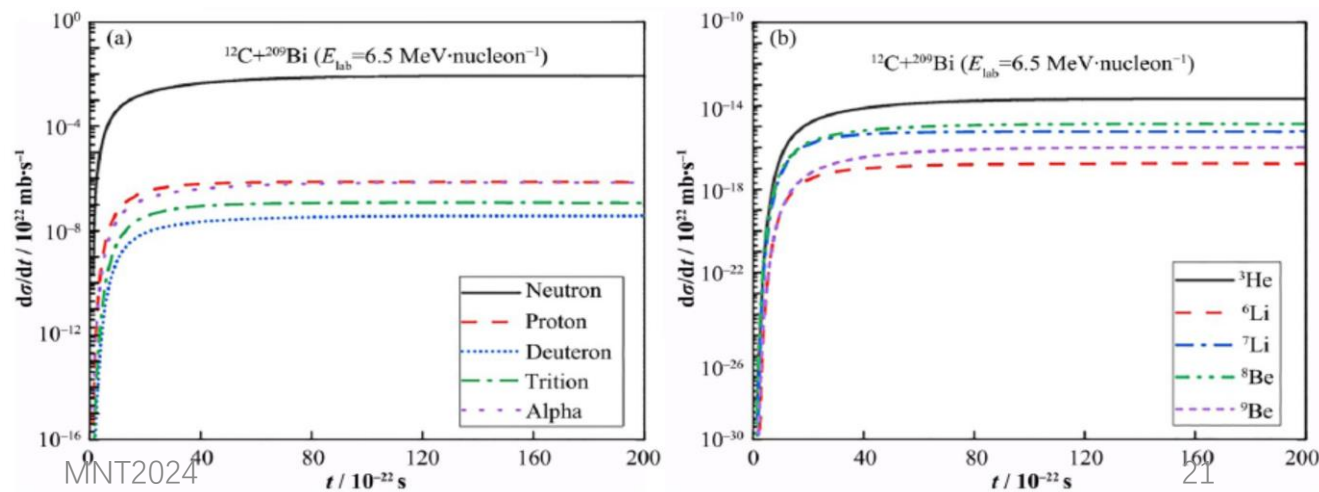
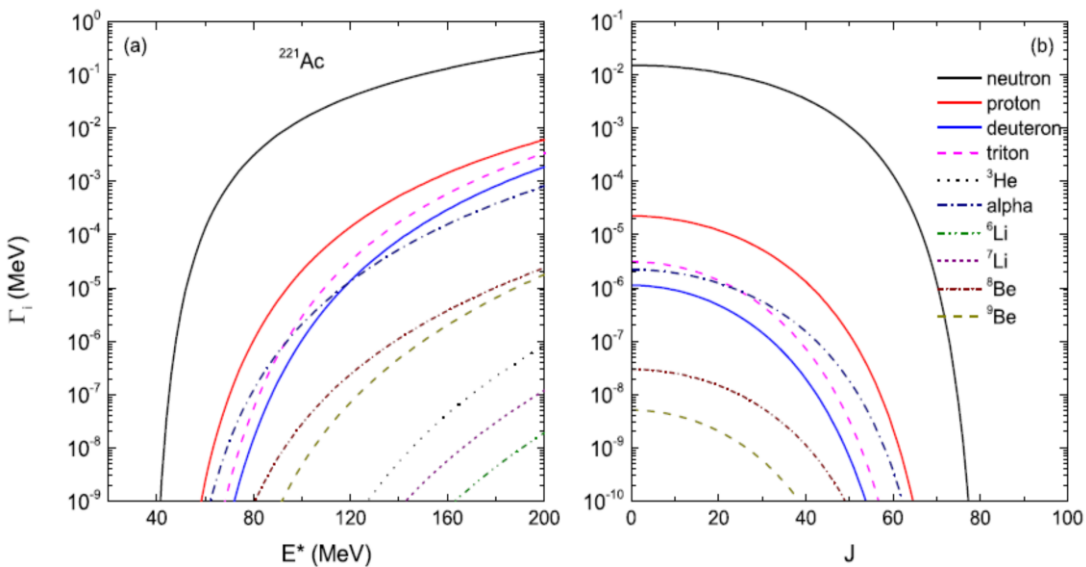
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www.hjs.sinap.ac.cn

Vol.46, No.3  
March 2023

## 基于双核模型研究大质量转移反应中 结团发射机制

徐思宇 冯兆庆

(华南理工大学 物理与光电学院 广州 510641)



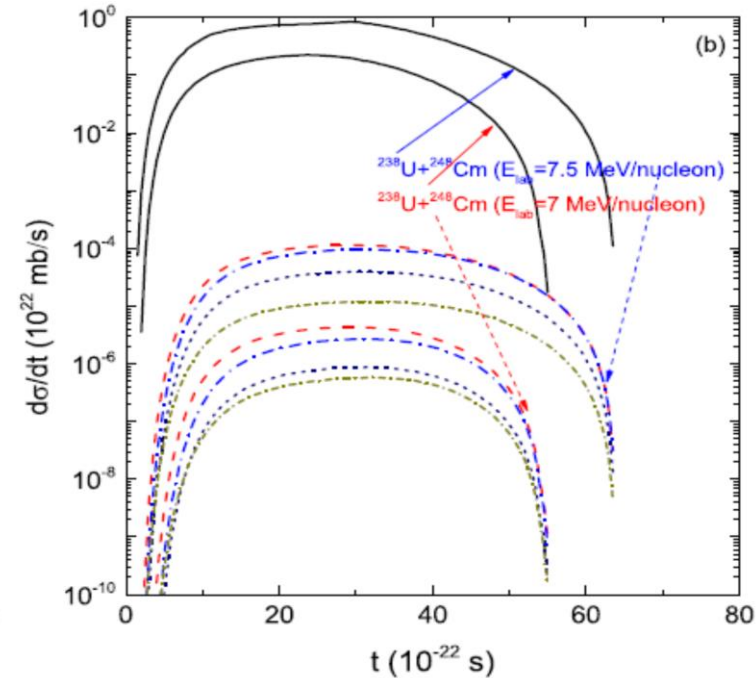
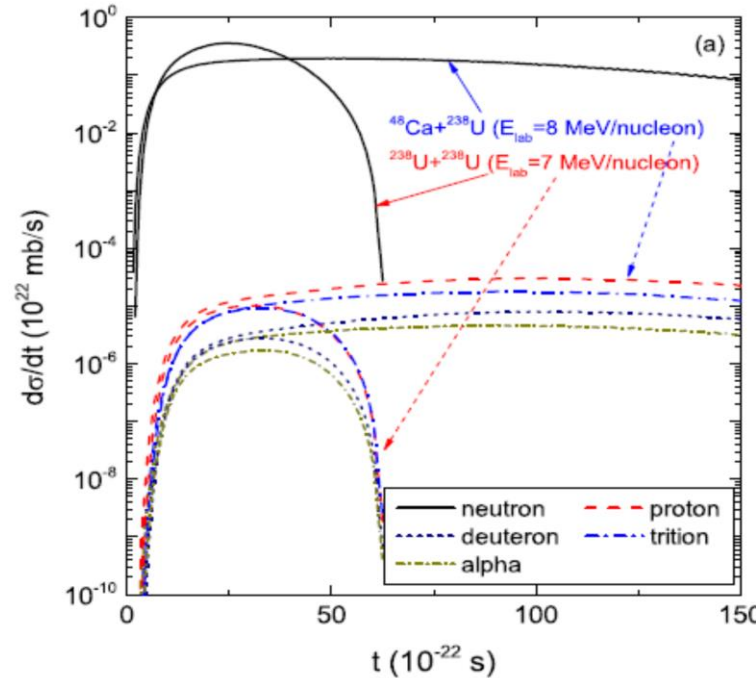
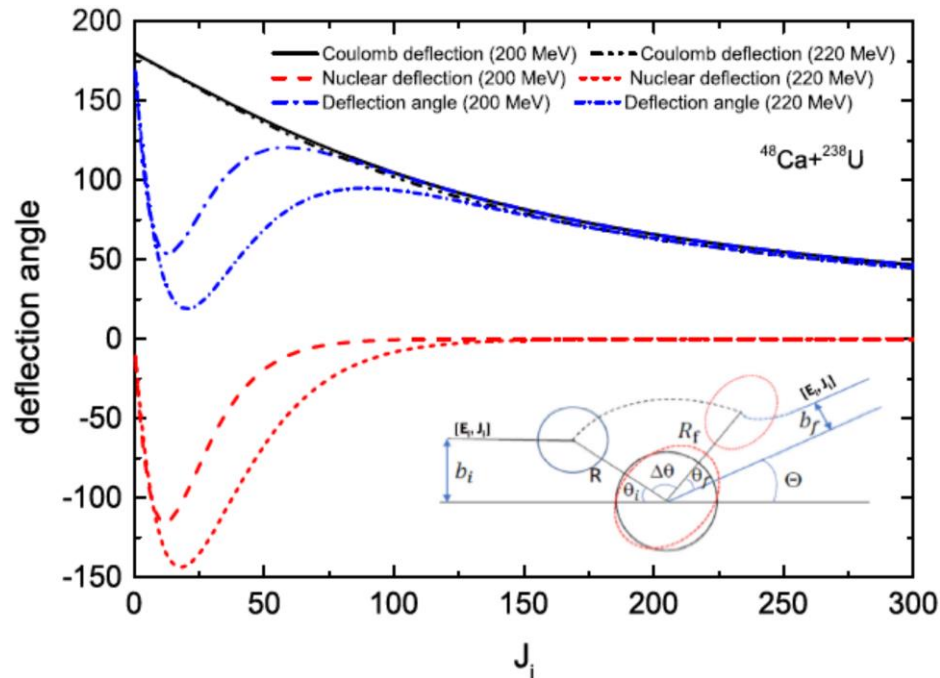
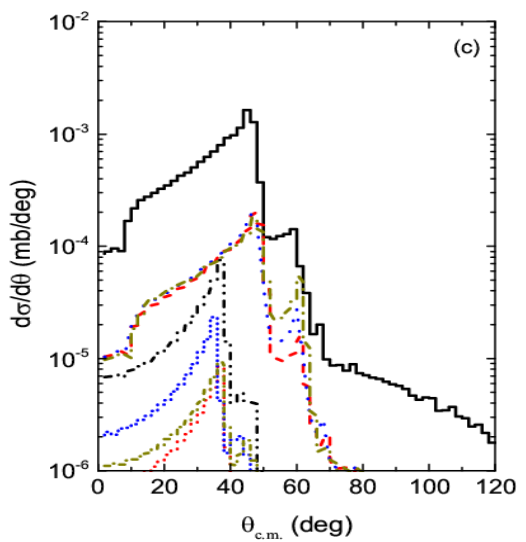
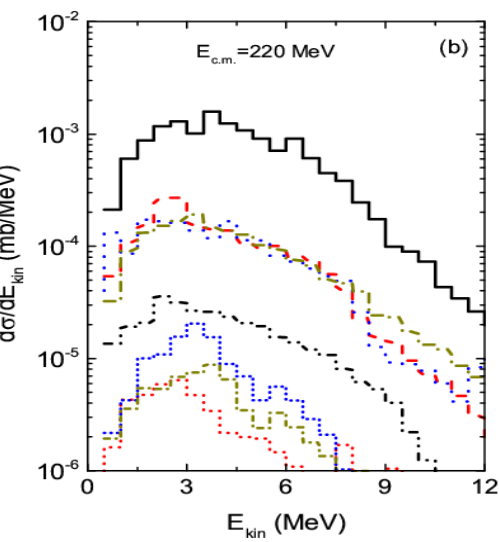
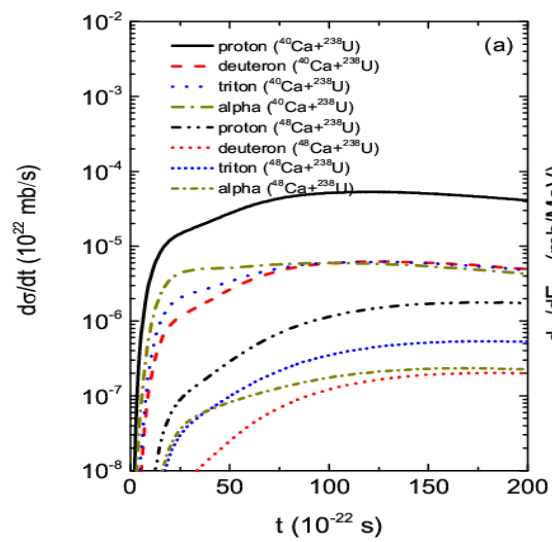


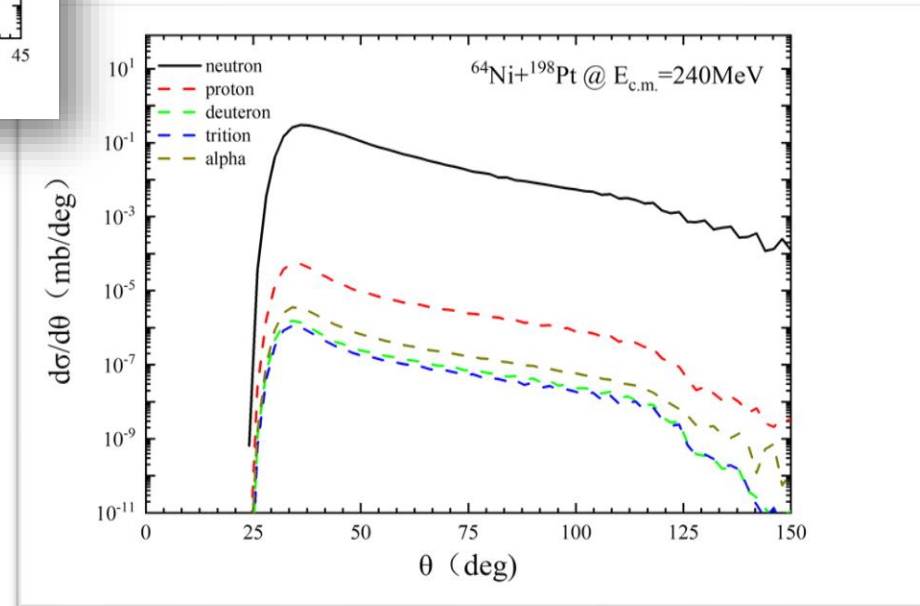
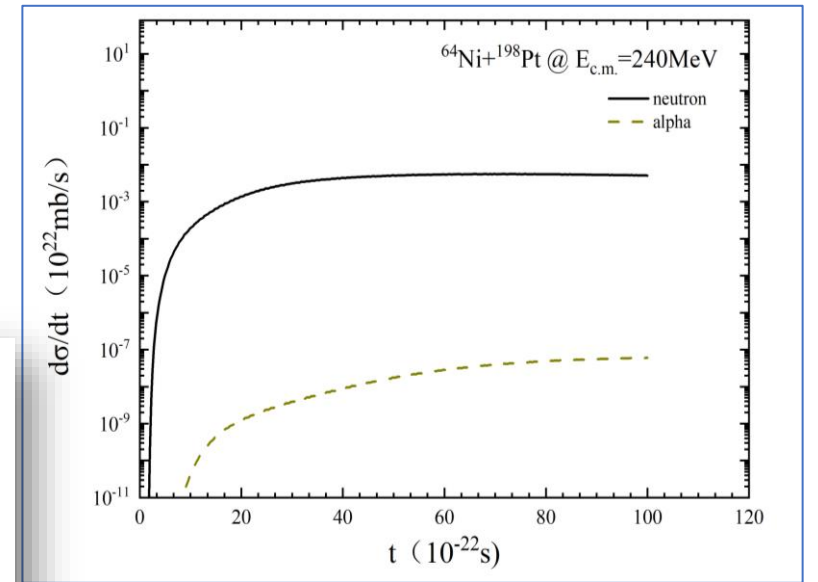
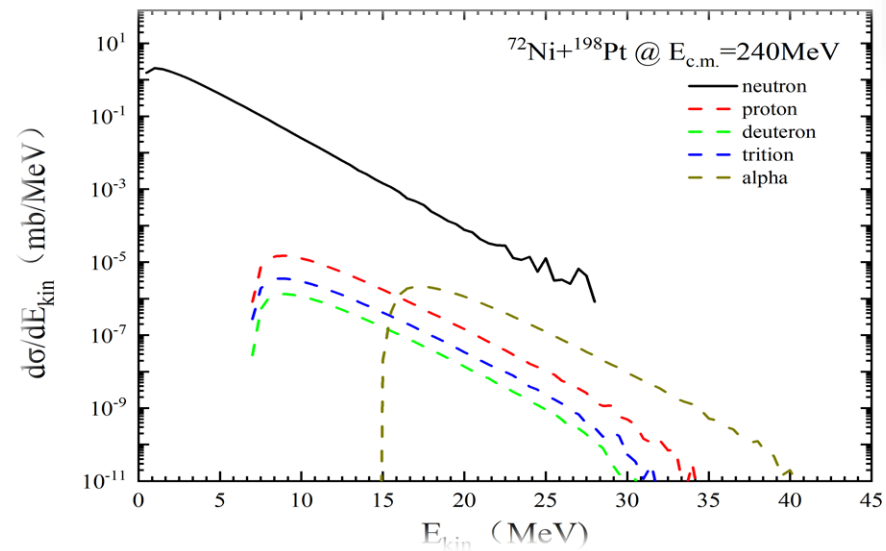
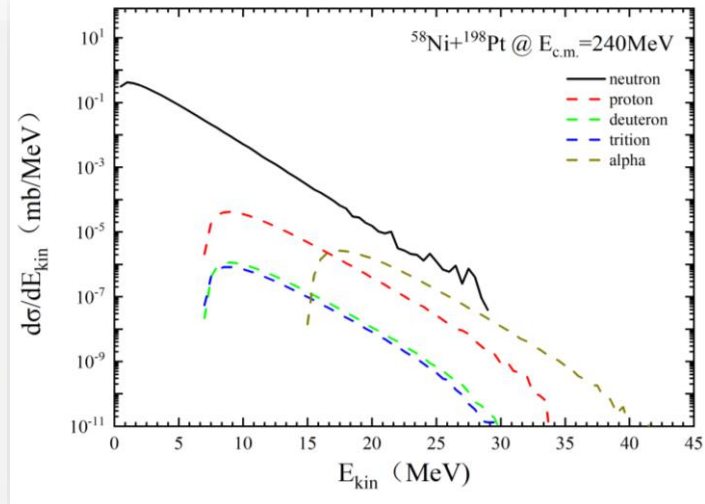
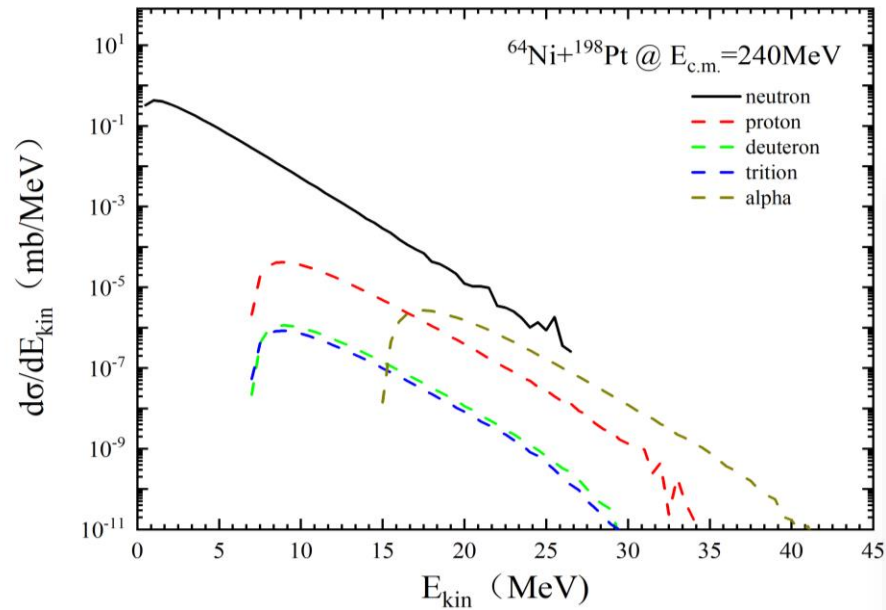
TABLE I. Production cross sections of neutron, proton, deuteron, triton,  $^3\text{He}$ ,  $\alpha$ ,  $^7\text{Li}$ , and  $^8\text{Be}$  in the preequilibrium process of massive transfer reactions.

System	$E_{c.m.}$ (MeV)	$\sigma_n$ (mb)	$\sigma_p$ (mb)	$\sigma_d$ (mb)	$\sigma_t$ (mb)	$\sigma_{^3\text{He}}$ (mb)	$\sigma_\alpha$ (mb)	$\sigma_{^7\text{Li}}$ (mb)	$\sigma_{^8\text{Be}}$ (mb)
$^{12}\text{C}+^{209}\text{Bi}$	69	2.63	$0.26 \times 10^{-3}$	$0.12 \times 10^{-4}$	$0.41 \times 10^{-4}$	$0.62 \times 10^{-11}$	$0.22 \times 10^{-3}$	$0.19 \times 10^{-12}$	$0.42 \times 10^{-12}$
$^{40}\text{Ca}+^{238}\text{U}$	220	24.65	$0.15 \times 10^{-1}$	$0.17 \times 10^{-2}$	$0.18 \times 10^{-2}$	$0.62 \times 10^{-8}$	$0.20 \times 10^{-2}$	$0.16 \times 10^{-10}$	$0.53 \times 10^{-11}$
$^{48}\text{Ca}+^{238}\text{U}$	180	$0.11 \times 10^{-1}$	$0.84 \times 10^{-12}$	$0.21 \times 10^{-14}$	$0.24 \times 10^{-13}$	$< 10^{-16}$	$0.77 \times 10^{-13}$	$< 10^{-16}$	$< 10^{-16}$
$^{48}\text{Ca}+^{238}\text{U}$	200	1.63	$0.42 \times 10^{-5}$	$0.18 \times 10^{-6}$	$0.66 \times 10^{-6}$	$< 10^{-16}$	$0.54 \times 10^{-6}$	$< 10^{-16}$	$< 10^{-16}$
$^{48}\text{Ca}+^{238}\text{U}$	220	23.16	$0.40 \times 10^{-3}$	$0.44 \times 10^{-4}$	$0.12 \times 10^{-3}$	$0.23 \times 10^{-11}$	$0.60 \times 10^{-4}$	$0.74 \times 10^{-14}$	$0.53 \times 10^{-15}$
$^{48}\text{Ca}+^{238}\text{U}$	240	96.11	$0.61 \times 10^{-2}$	$0.11 \times 10^{-2}$	$0.28 \times 10^{-2}$	$0.61 \times 10^{-9}$	$0.94 \times 10^{-3}$	$0.48 \times 10^{-11}$	$0.34 \times 10^{-12}$
$^{238}\text{U}+^{238}\text{U}$	833	20.59	$0.61 \times 10^{-3}$	$0.17 \times 10^{-3}$	$0.55 \times 10^{-3}$	$0.49 \times 10^{-10}$	$0.11 \times 10^{-3}$	$0.15 \times 10^{-11}$	$0.11 \times 10^{-12}$
$^{238}\text{U}+^{248}\text{Cm}$	850	11.53	$0.23 \times 10^{-3}$	$0.46 \times 10^{-4}$	$0.14 \times 10^{-3}$	$0.63 \times 10^{-11}$	$0.31 \times 10^{-4}$	$0.20 \times 10^{-12}$	$0.16 \times 10^{-13}$
$^{238}\text{U}+^{248}\text{Cm}$	911	56.27	$0.71 \times 10^{-2}$	$0.24 \times 10^{-2}$	$0.60 \times 10^{-2}$	$0.41 \times 10^{-8}$	$0.77 \times 10^{-3}$	$0.10 \times 10^{-9}$	$0.56 \times 10^{-11}$

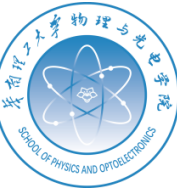


# Preequilibrium cluster emission

$58,64,72\text{Ni}+^{198}\text{Pt}$  @  $E_{c.m.}=240\text{MeV}$



# IV. Summary and perspective



- The maximal cross sections with **10 fb** for the reaction of  $^{54}\text{Cr}(^{243}\text{Am},3n)^{294}119$  corresponding to  $E_{\text{c.m.}}=239.43$  MeV and **4 fb** for  $^{54}\text{Cr}(^{248}\text{Cm},3n)^{299}120$  at 33 MeV,  $E_{\text{c.m.}}=240.77$  MeV,  $E_{\text{lab}}=5.43$  MeV/nucleon.
- Shell effect plays an important role on the MNT fragments formation. New neutron-rich isotopes around  $N=162$  is the stepstone to reach the 'island of stability'. The cluster transfer in the MNT reactions broadens the isotopic distribution and slightly enhances the fusion probability.
- **Preequilibrium clusters enable the similar reaction dynamics with the MNT reactions**

Perspective: Influence of cluster structure of projectile nuclides, such as  $^{12}\text{C}$ ,  $^{16}\text{O}$ , on the cluster emission, spectroscopic factor.

Thank you for your attention!