

Measurements of jet nuclear modification factor and azimuthal anisotropy in Pb-Pb collisions at $\sqrt{s_{NN}} = 5.02 \text{ TeV}$ with the LHC-ALICE to clarify the parton energy loss mechanism in Quark-Gluon Plasma and evaluate stopping power



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Introduction

Physics target: Parton Energy loss mechanism

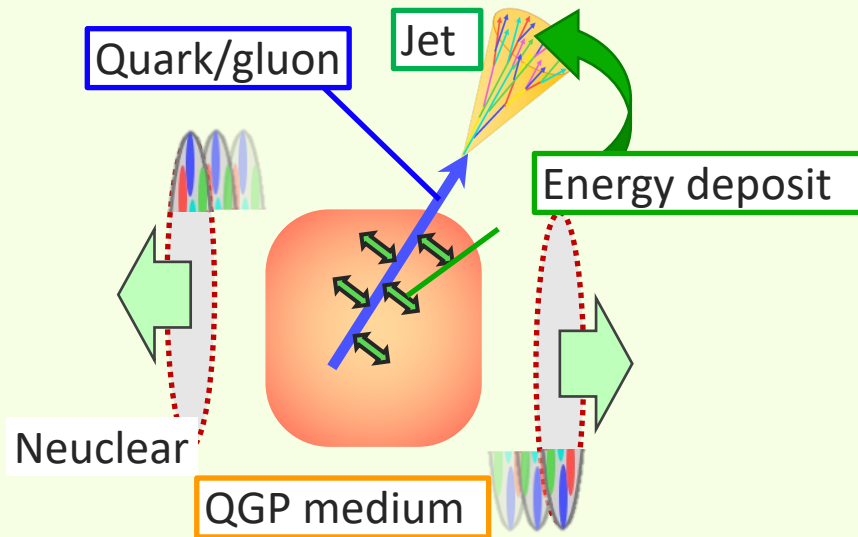
Partons deposit energy in the QGP medium.

Energy loss

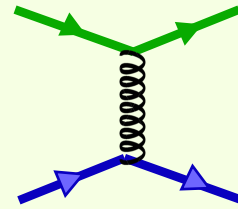
$$\Delta E \propto \hat{q} L^n$$

\hat{q} : transport coefficient

L : path length in QGP

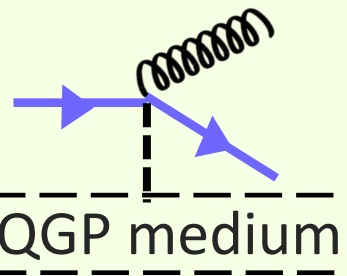


Jet suppression mechanism



Collisional

$$\Delta E \propto L$$



Radiative

$$\Delta E \propto L^2$$

AdS/CFT

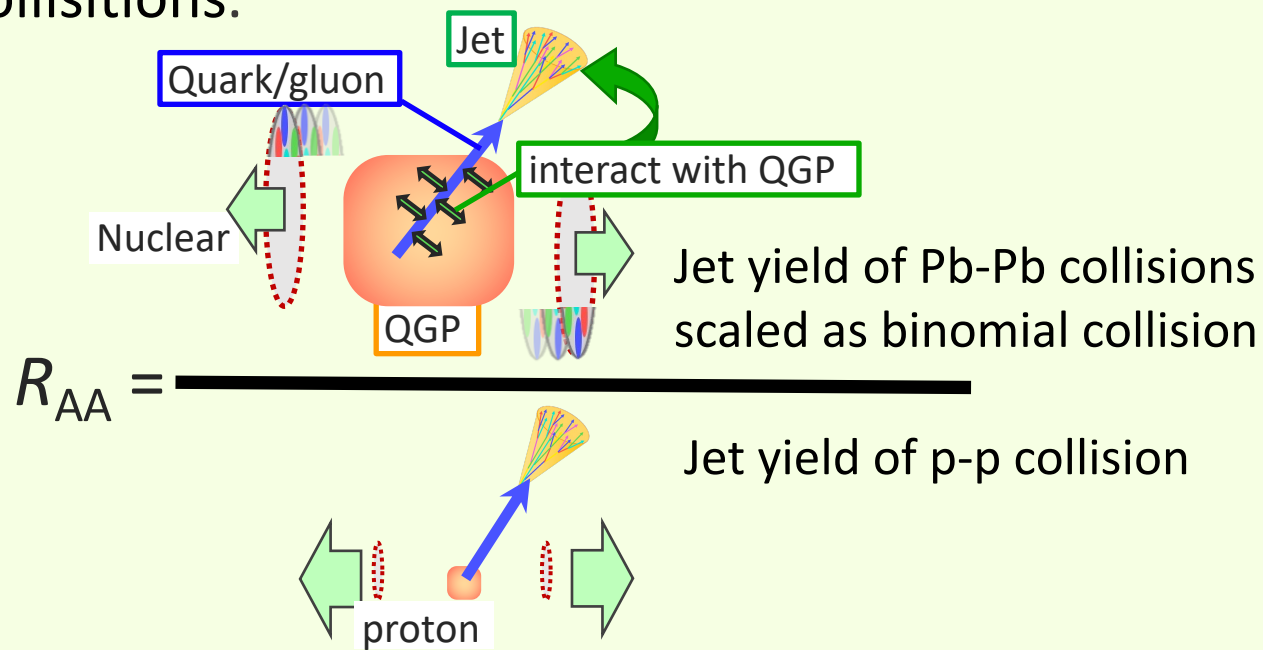
$$\Delta E \propto L^3$$

There are some jet suppression mechanisms, but the detail ratio of suppression or correct model are not clarified.

Parton Energy Loss Analysis

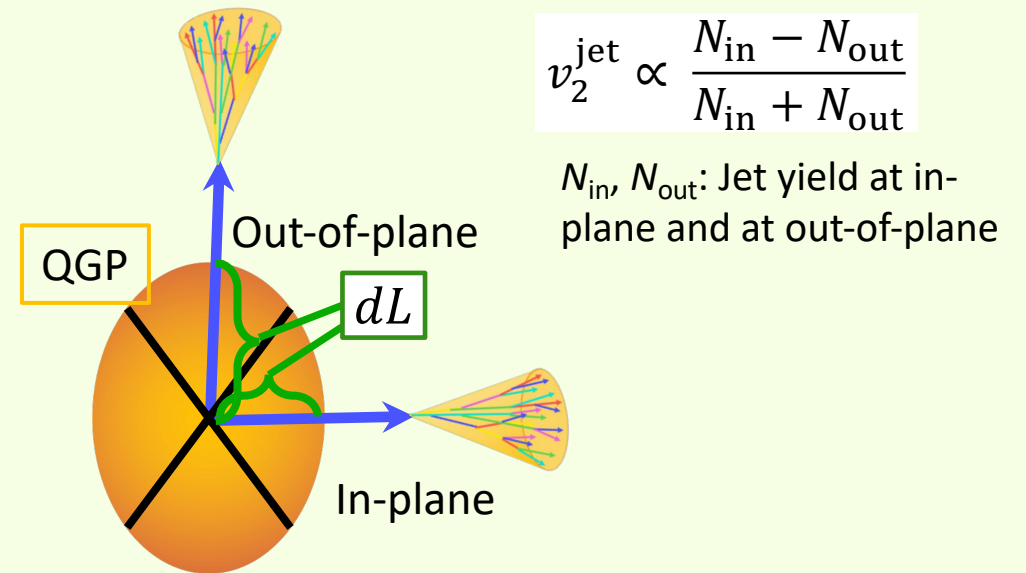
Energy loss: $\Delta E \propto \hat{q}L^n$

Nuclear modification factor (R_{AA}) is built by comparing *heavy-ion* collisions and *proton* collisions.



Using the difference between with and without suppression allow to measure the **magnitude of suppression**. \rightarrow **Quantify \hat{q}**

Jet v_2 is built by comparing in-plane jets and out-of-plane jets.



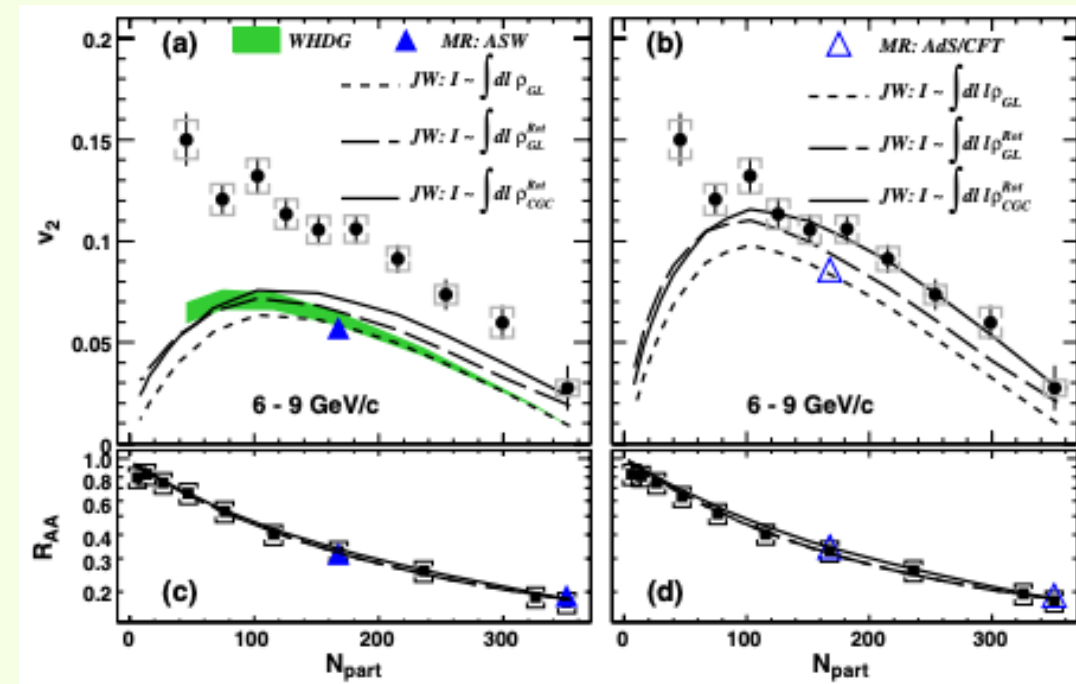
Using difference of the path length between in-plane and out-of plane allows to study **L dependency** of ΔE . \rightarrow **Quantify the power of n**

New points of my study for Energy loss ($\Delta E \propto \hat{q}L^n$)

- New jet v_2 measurement at $\sqrt{s_{NN}} = 5.02$ TeV as ALICE
- Simultaneous comparison of charged jet v_2 and R_{AA}
→ Expect strong model constraints and acquire accurate suppression parameter values.
- Use **JETSCAPE** model simulation framework

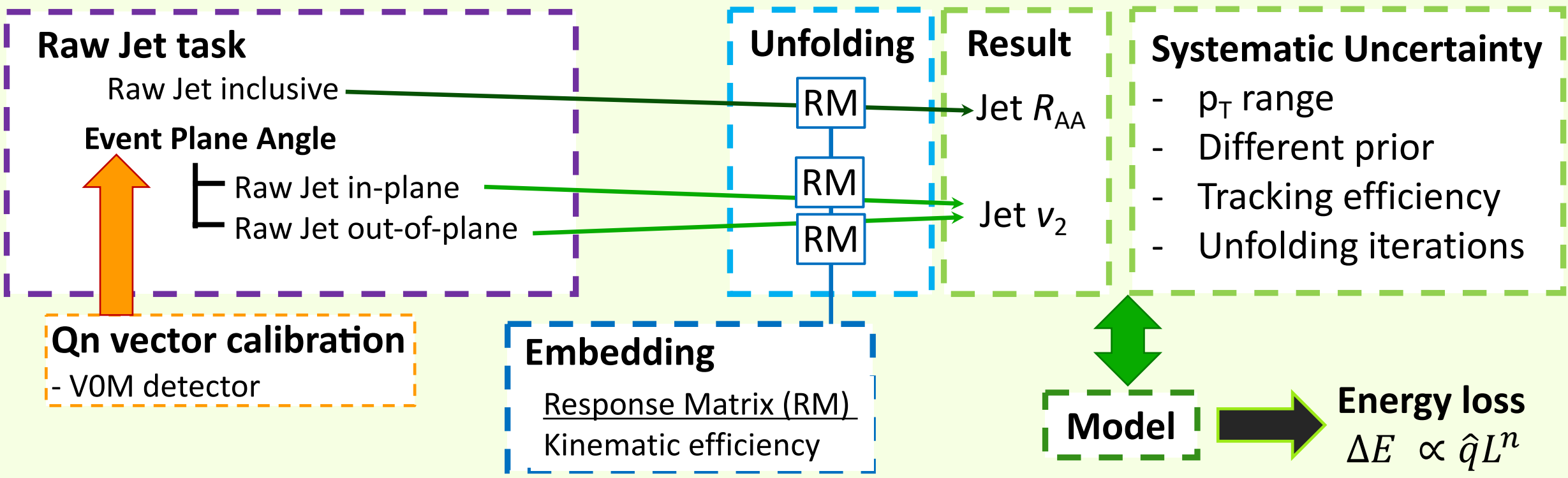
v_2 and R_{AA} of π^0 measurement using PHENIX
 $\sqrt{s_{NN}} = 200$ GeV data (2010)

<https://journals.aps.org/prl/pdf/10.1103/PhysRevLett.105.142301>



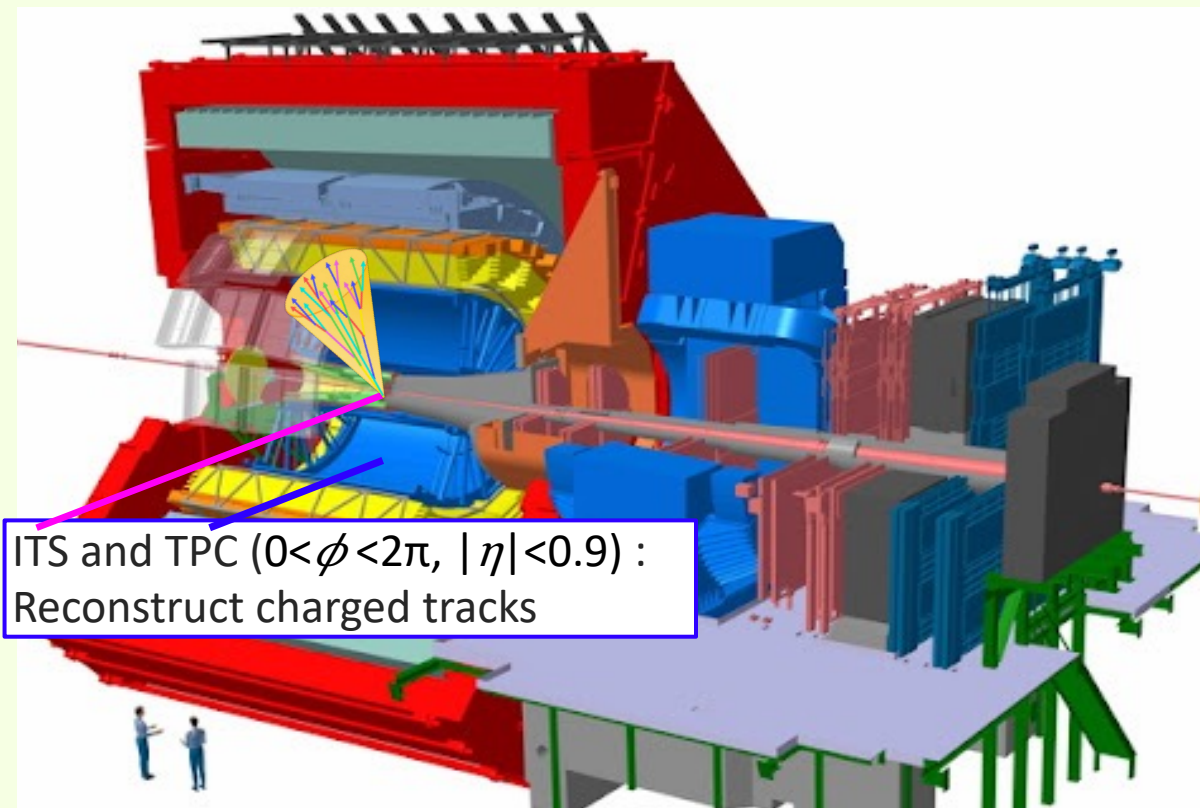
Analysis

Analysis Flow

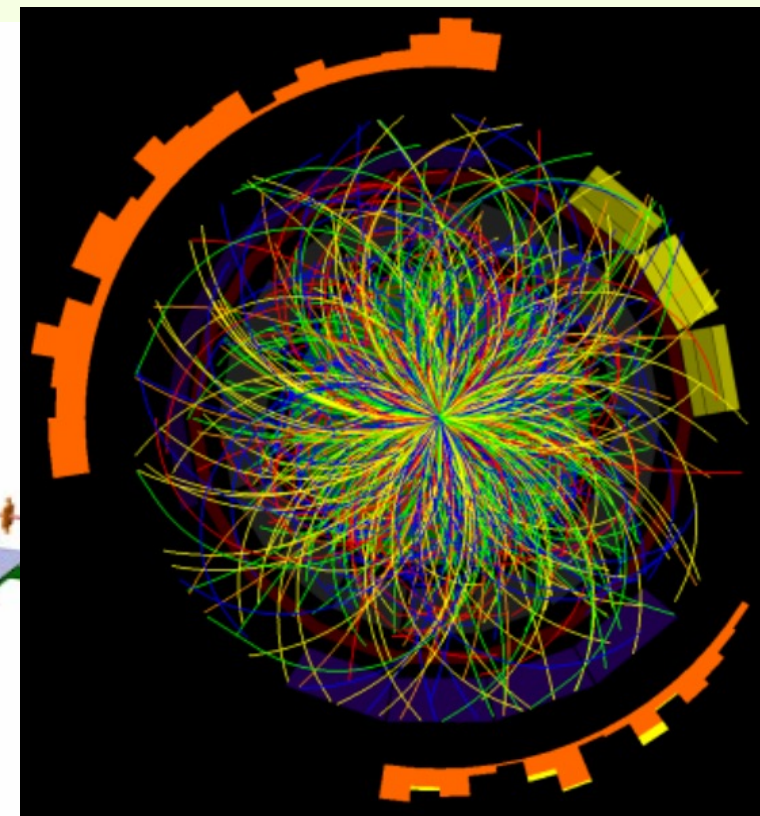


Charged Jet reconstruction in ALICE

Charged jet



ITS and TPC ($0 < \phi < 2\pi$, $|\eta| < 0.9$) :
Reconstruct charged tracks



Reconstructed tracks

Fast jet package [Phys Lett B 641 (2006) 57]

Clustering track p_T in resolution parameter (R) range.

- Signal Jet \rightarrow anti- k_T algorithm
- Background density \rightarrow k_T algorithm

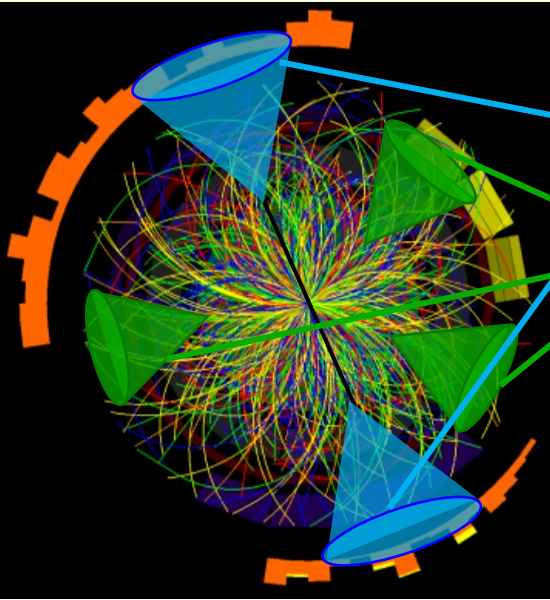
Background p_T distribution (ordinary inclusive jet way)

In HIC, a huge number of particles are produced.

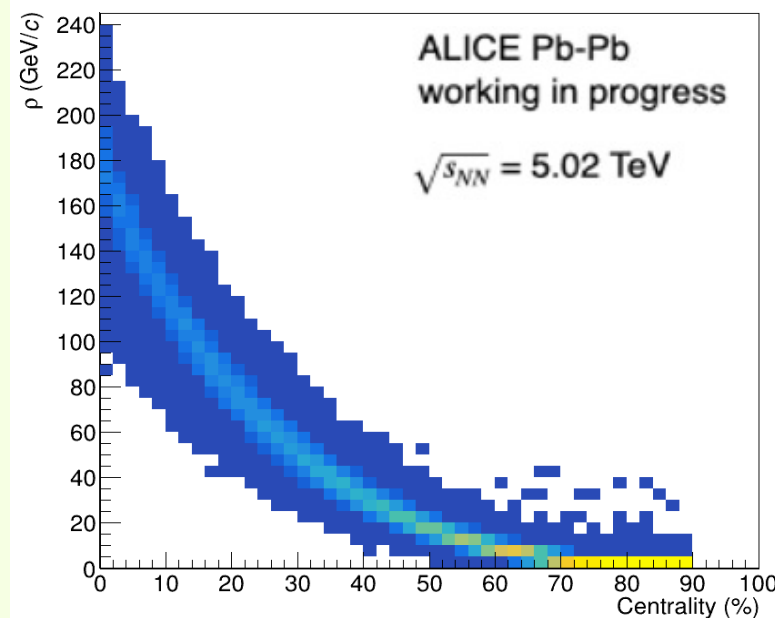
→ Signal jets are reconstructed with the background particles.

→ Estimate background p_T density (ρ) except for signal jet area

➔ $\rho = \text{median}(p_{T,i}/A_i)$ A : cluster area, i : cluster id



background p_T for centrality

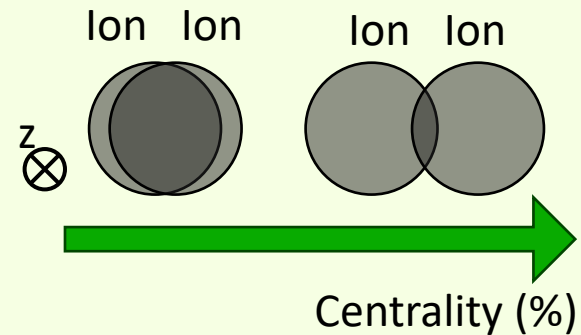


ρ is considered uniform for azimuthal angle and determined event by event
→ subtract the background from each signal jet



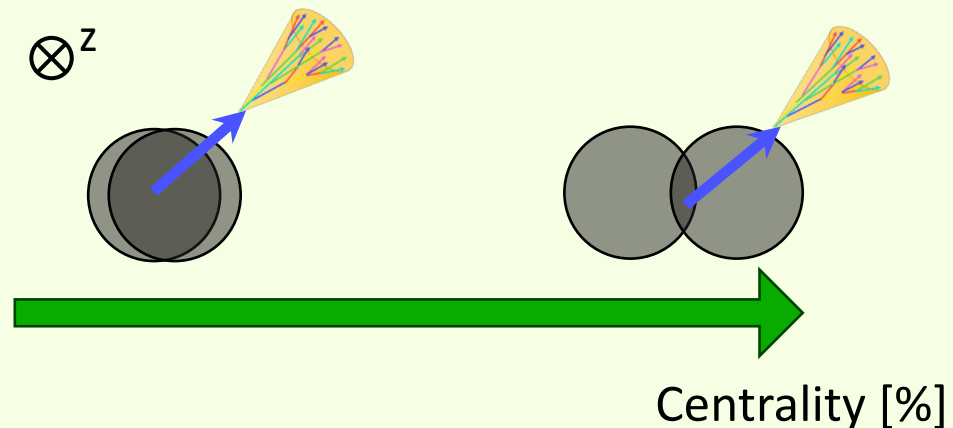
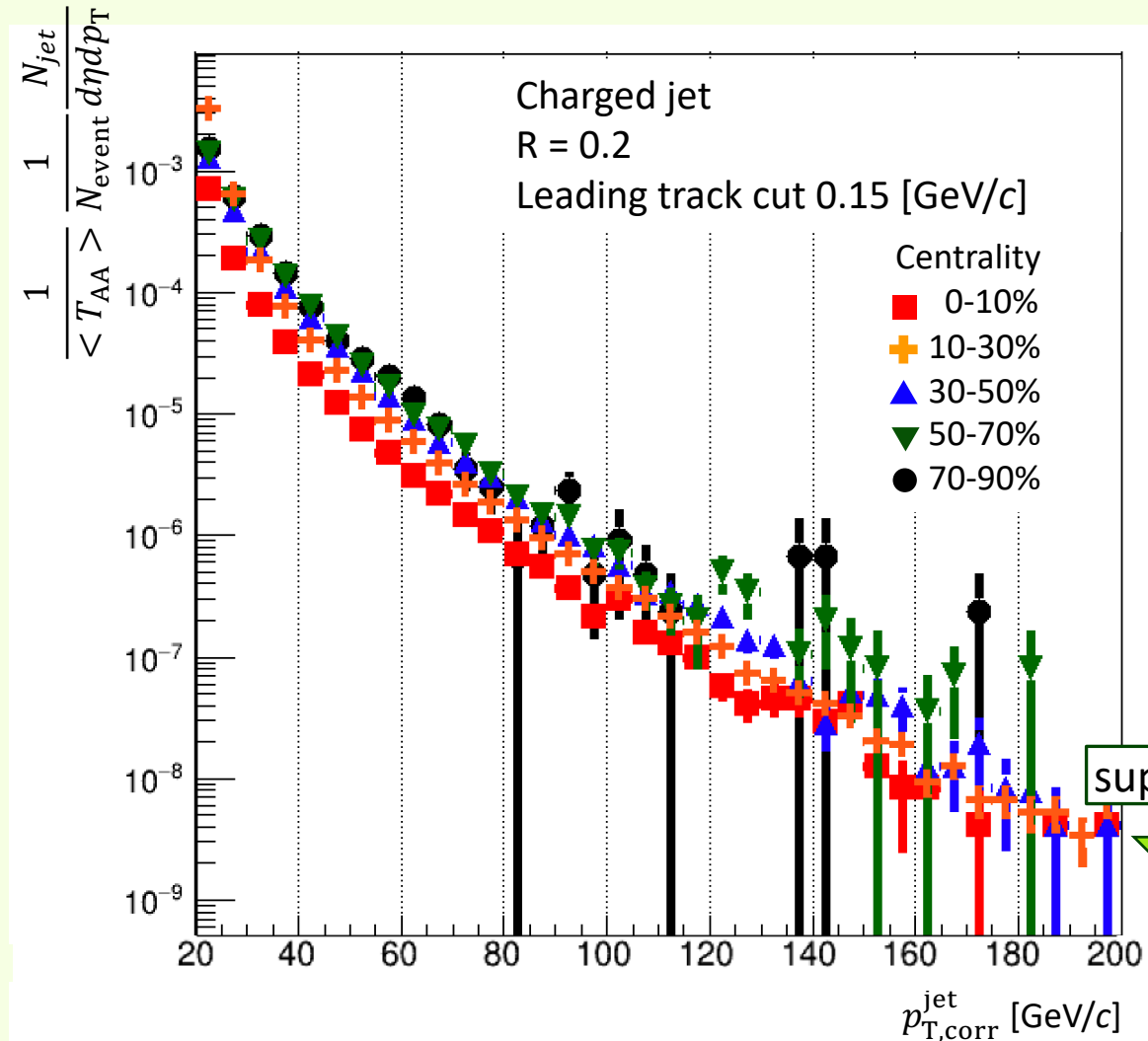
$$p_{T,\text{corr}}^{\text{jet}} = p_T^{\text{jet}} - \rho A$$

A : jet area



Inclusive Raw Charged Jet Yield

Corrected Raw jet p_T distribution (w/o unfolding): $p_{T,corr}^{jet} = p_T^{raw} - \rho A$



Determination of Event Plane Angle

Event plane angle

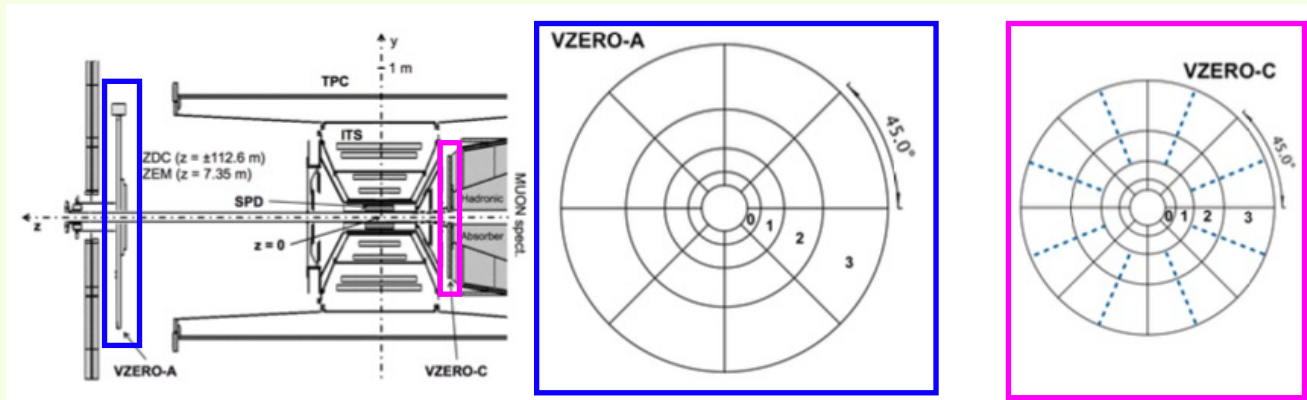
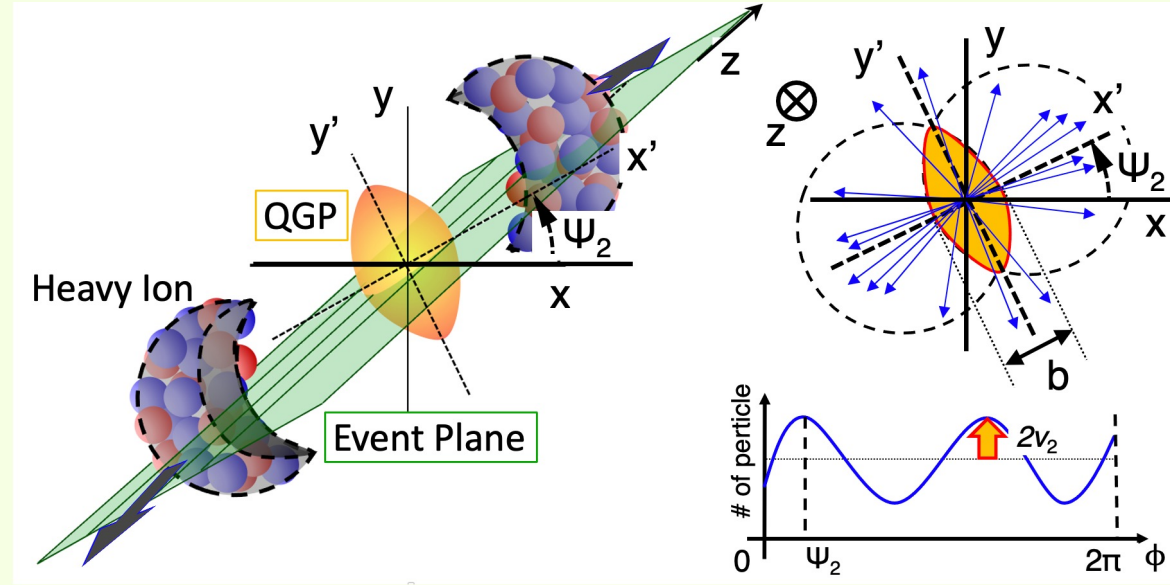
$$\Psi_{EP\ n} = \frac{1}{n} \arctan \frac{Q_{n,y}}{Q_{n,x}}$$

Flow Vector component

$$Q_{n,x} = \sum_i \omega_i \cos n\phi_i$$

$$Q_{n,y} = \sum_i \omega_i \sin n\phi_i$$

(ϕ_i : Track angle, ω_i : multiplicity weight, n: Fourier order)



Event Plane Angle Resolution

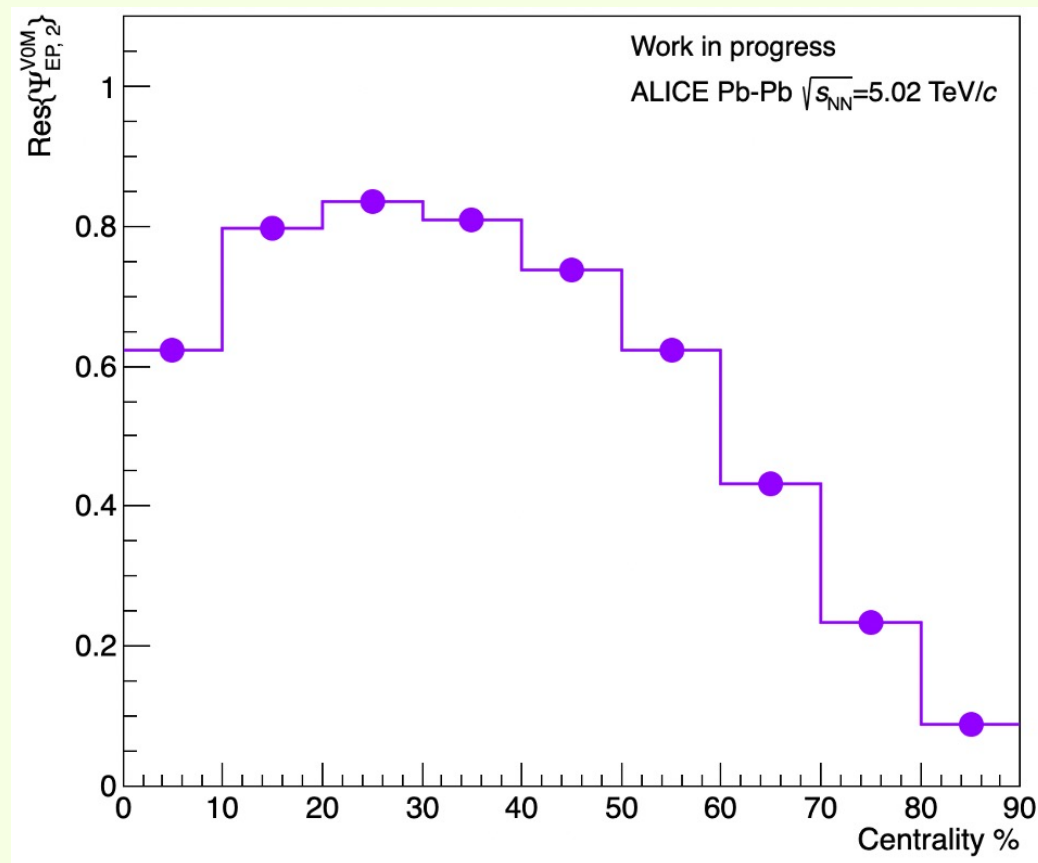
$$\text{Res}\{\Psi_{EP,2}^{\text{meas}}\} = \langle \cos(n[\Psi_{EP,n}^a - \Psi_n]) \rangle = \sqrt{\frac{\langle \cos(n[\Psi_{EP,n}^a - \Psi_{EP,n}^b]) \rangle \langle \cos(n[\Psi_{EP,n}^a - \Psi_{EP,n}^c]) \rangle}{\langle \cos(n[\Psi_{EP,n}^b - \Psi_{EP,n}^c]) \rangle}}$$

$$v_2^{\text{jet}} = \frac{1}{\text{Res}\{\Psi_{EP,2}^{\text{meas}}\}} \frac{\pi}{4} \frac{N_{in} - N_{out}}{N_{in} + N_{out}}$$

Ideally, $\Psi_{EP,n}^a - \Psi_{EP,n}^{\text{truth}}$ close to 0.
 In that case, $\text{Res}\{\Psi_{EP,2}^{\text{meas}}\}$ close to 1.

V0 sub-detector

(b: TPC $\eta < 0$, c: TPC $\eta > 0$)



V0M (V0C and V0A) event plane angle resolution for centrality

Local background p_T estimation

The soft particle background is **not uniform** for azimuthal angle (φ).

→The background calculation should take the φ dependency into account.

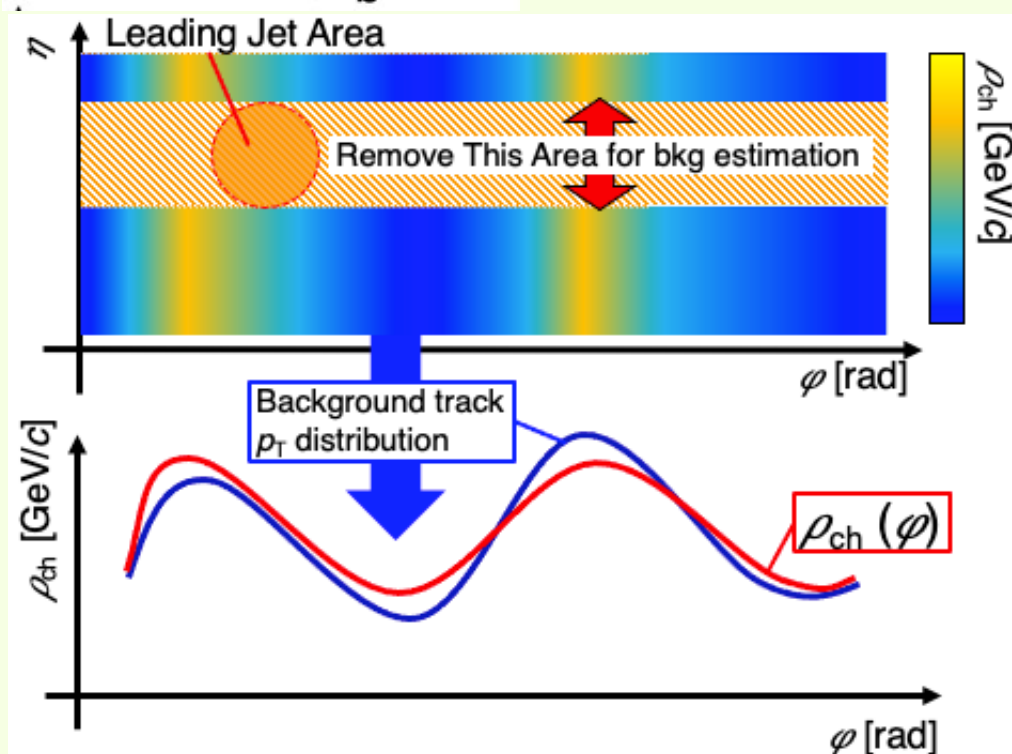
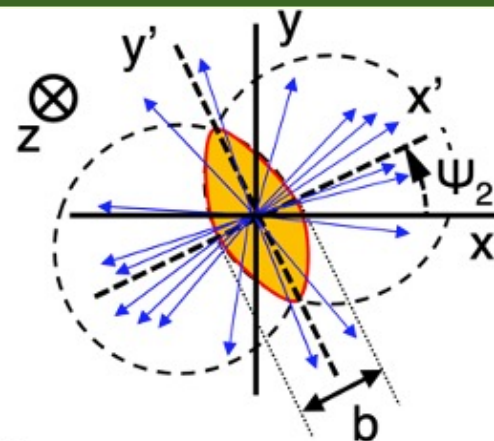
The local rho is estimated using tracks except the leading jet η region. (Because of the statistic problem, it includes the sub-leading jet region.)

In this analysis, a following equation is used.

$$\rho_{ch}(\varphi) = \rho_0 \times \left(1 + 2 \left\{ v_2^{\text{obs}} \cos(2[\varphi - \Psi_{EP,2}]) + v_3^{\text{obs}} \cos(3[\varphi - \Psi_{EP,3}]) \right\} \right)$$

$\Psi_{EP,2}$ and $\Psi_{EP,3}$ are calculated by the Qn vectors.

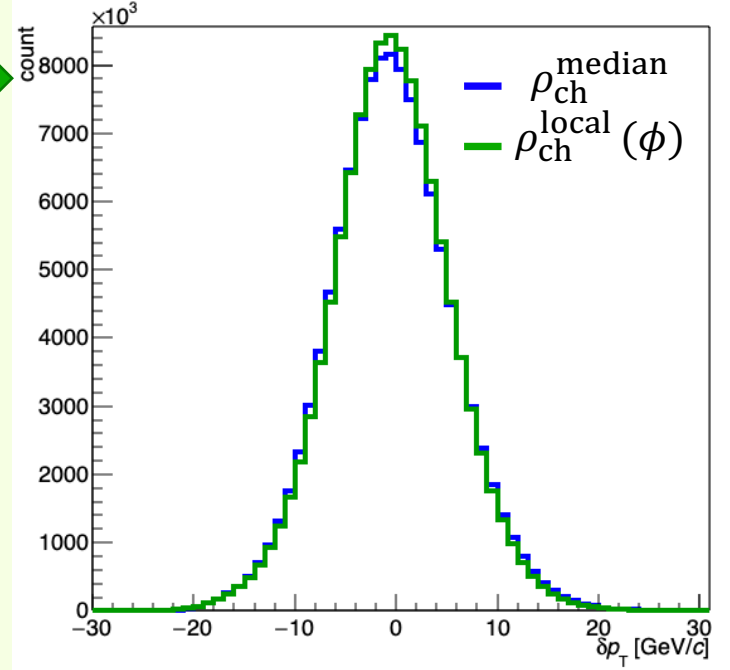
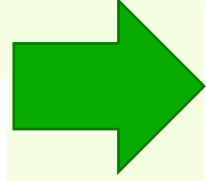
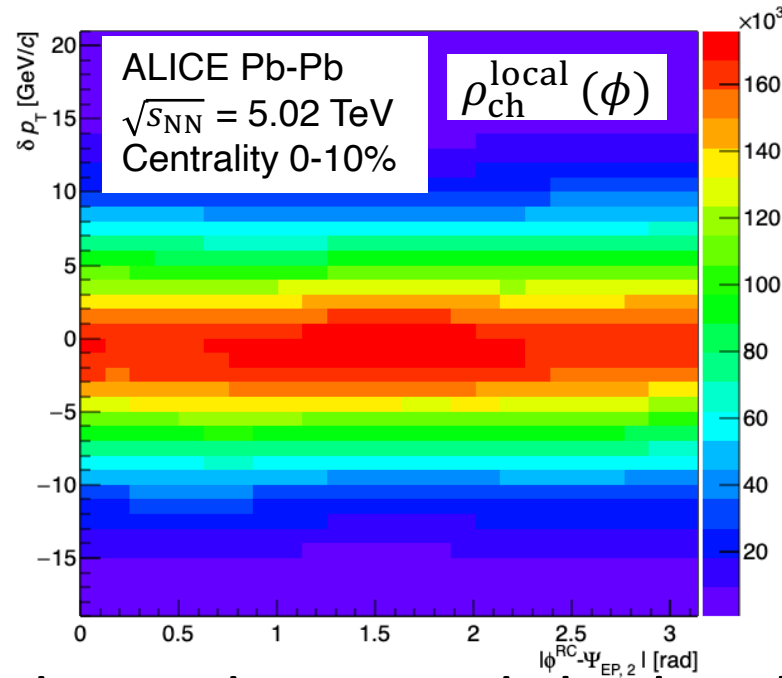
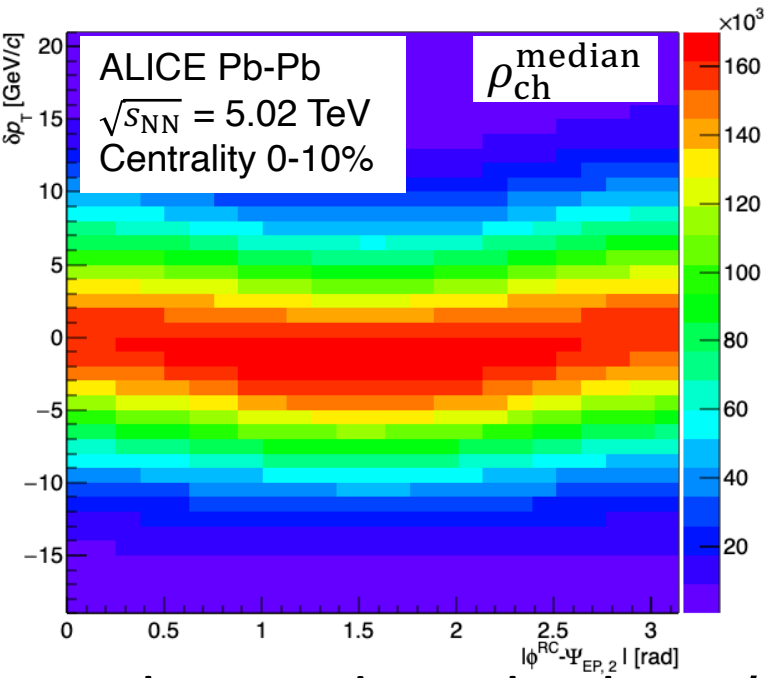
And ρ_0 , v_2^{obs} , and v_3^{obs} are fitting value.



The background δp_T distribution

$$\delta p_T = \sum_i p_{T,i}^{\text{track}} - \int_{-RC}^{RC} \rho(\phi) d\phi$$

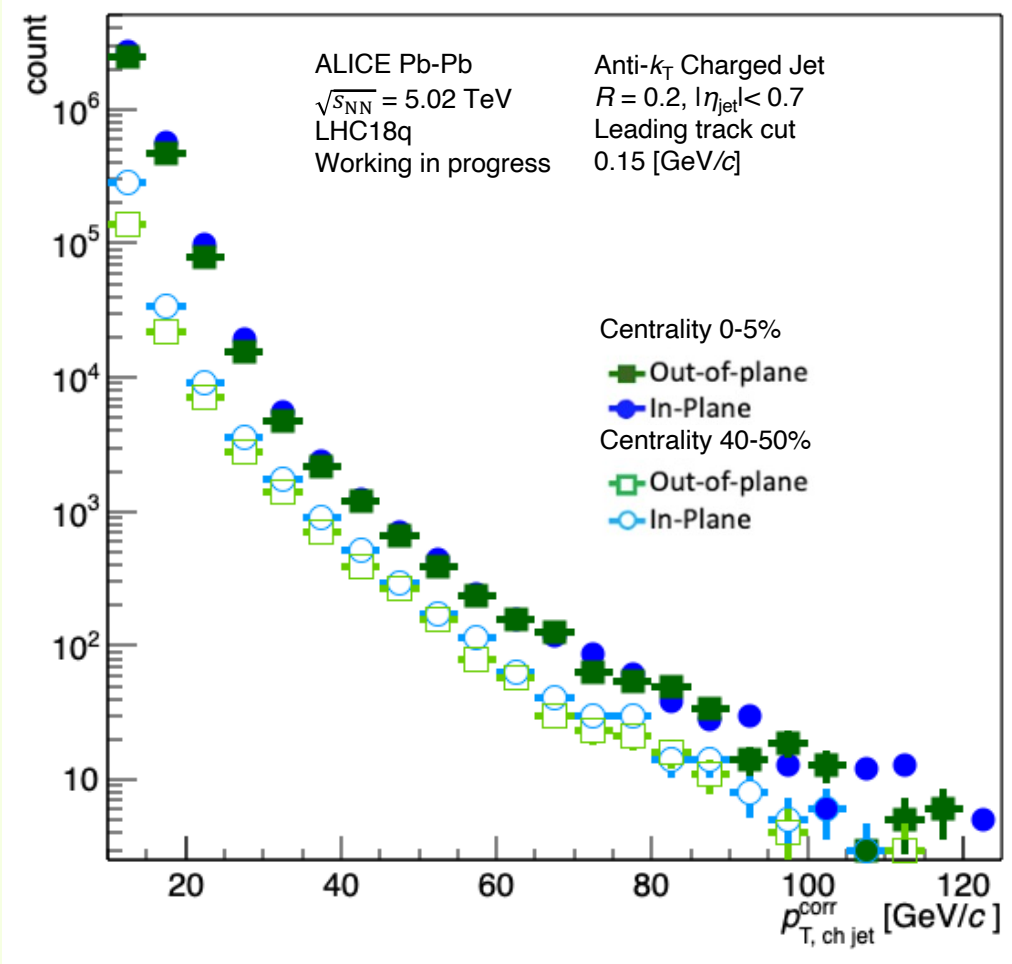
Projection on y axis



- The median rho has ϕ dependency and the local rho makes smaller the ϕ dependency.
- The dispersion of local rho background is more narrow than median rho. And these same tendency is seen in the all centrality regions.

Raw Charged Jet Spectrum for each Event Plane

Corrected Raw jet p_T distribution (w/o unfolding): $p_T^{\text{raw}} - \rho(\phi)A$

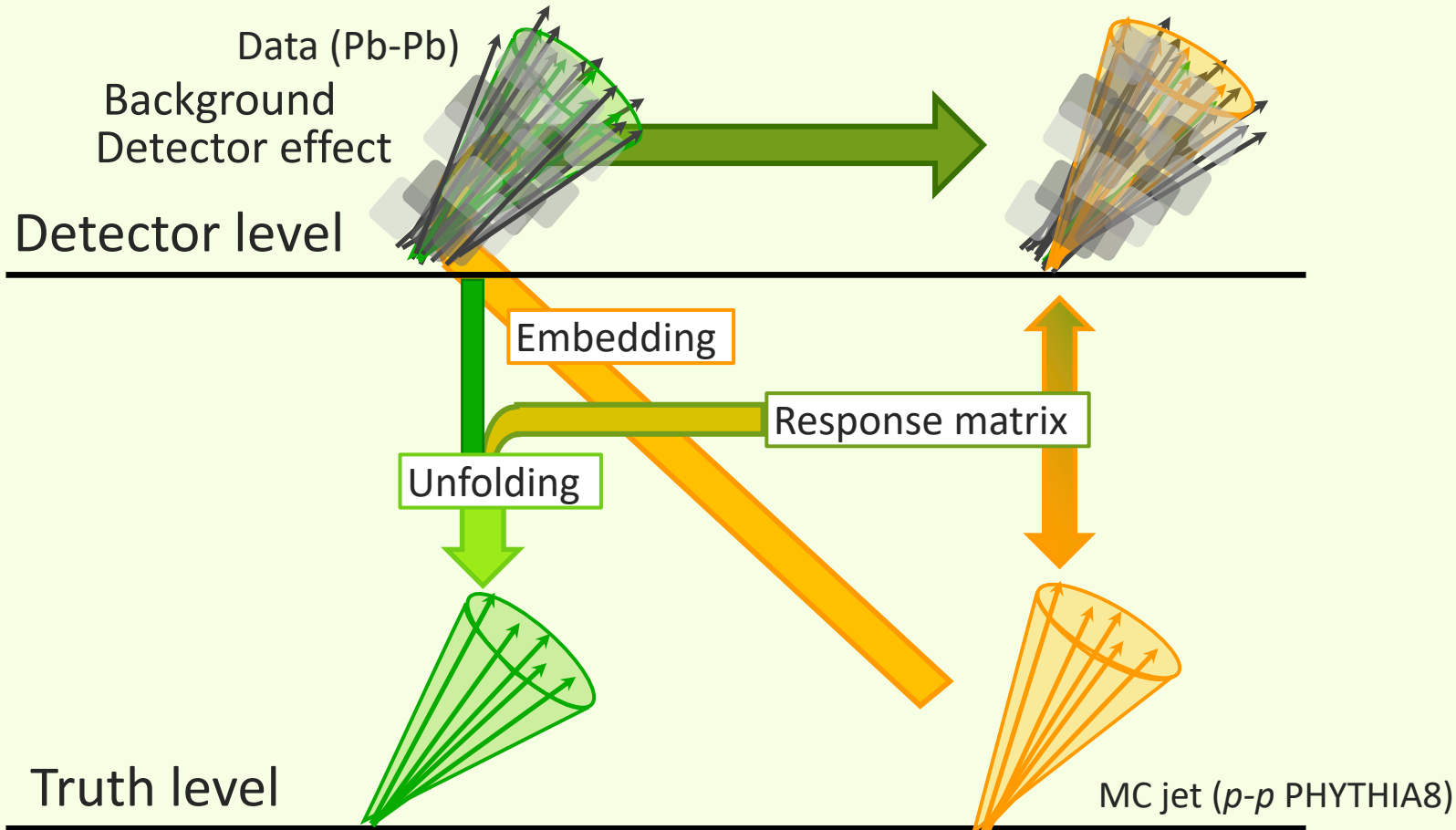


Out-Plane jets are more suppressed than In-plane ones for each centrality.

Unfolding Process

The measured jet p_T distribution is affected by the background fluctuations and the finite resolution / efficiency of the detector

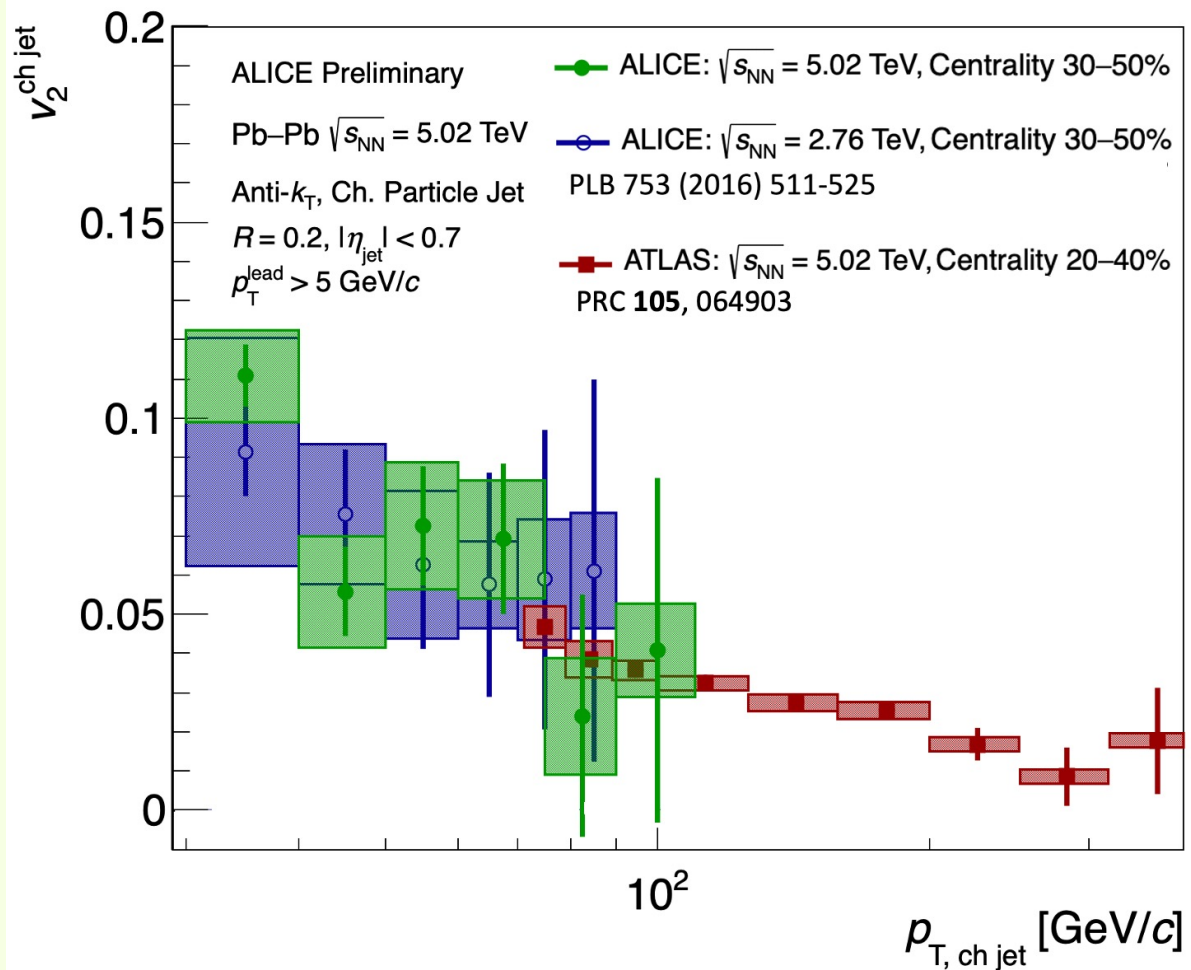
→ Correcting p_T distribution distortions by **Unfolding**.



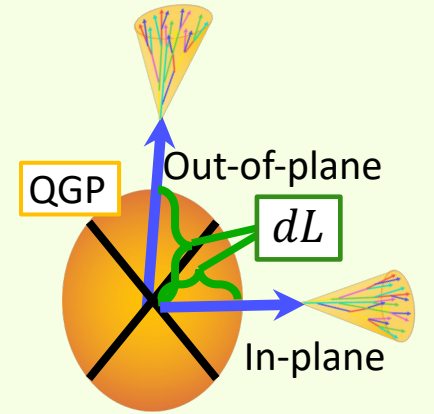
Kinds of Systematic Errors

- Detector level p_T range of response matrix
 - $\rightarrow \pm 5 \text{ GeV}/c$
- Different prior
 - \rightarrow Modify a prior distribution to unfolding by multiply a ratio of measurement distribution and MC detector level distribution.
- Tracking efficiency
 - \rightarrow Nominal (98%), Compare (94%)
- Unfolding iterations
 - $\rightarrow \pm 1$ time
- Different event plane angle determination detector
 - \rightarrow Nominal (V0M), Compare (V0C and V0A)
- Different background fitting function
 - \rightarrow Nominal (v2 and v3 combine), Compare (only v2 component)

Inclusive charged jet v_2



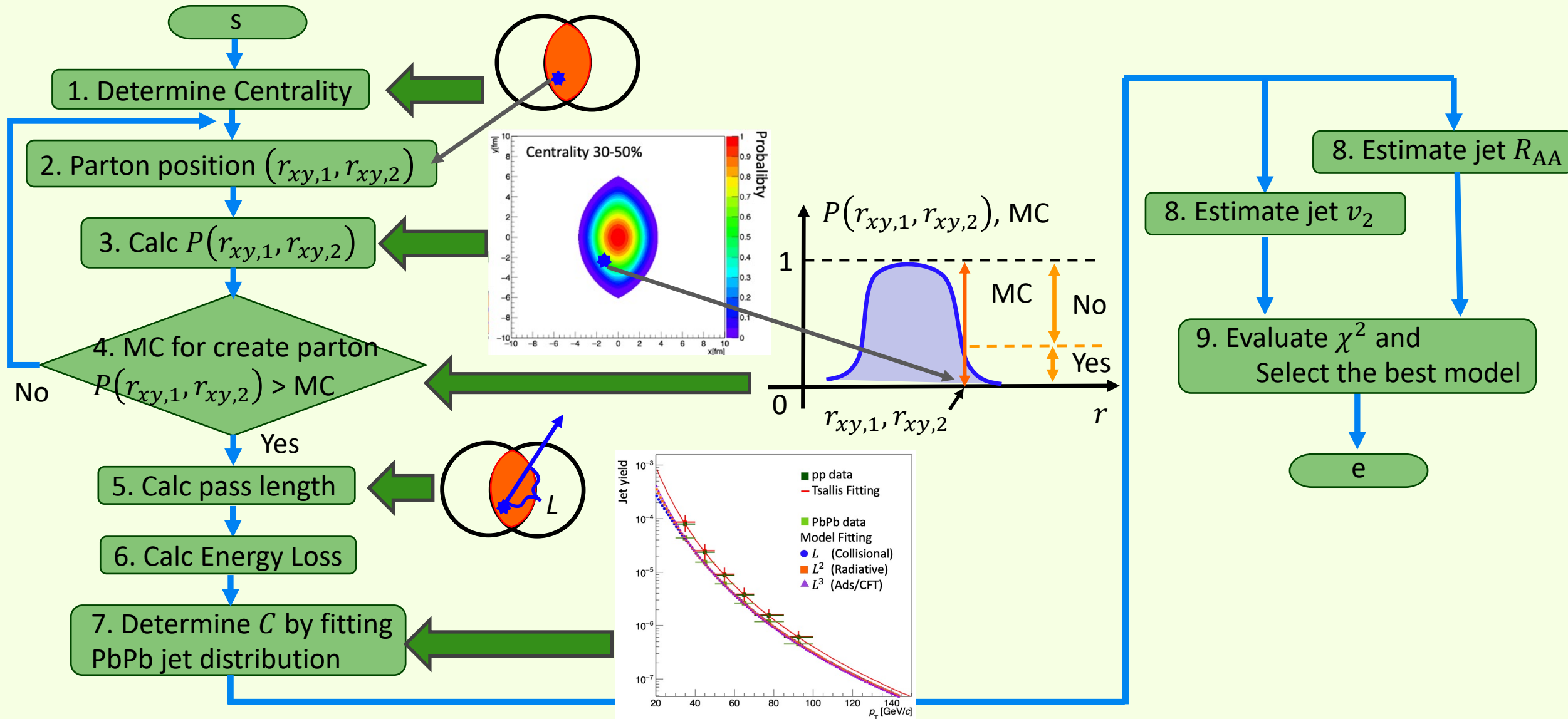
$$v_2^{ch jet}(p_T^{jet}) = \frac{\pi}{4} \frac{1}{\mathcal{R}_2} \frac{N_{in}(p_T^{jet}) - N_{out}(p_T^{jet})}{N_{in}(p_T^{jet}) + N_{out}(p_T^{jet})}$$



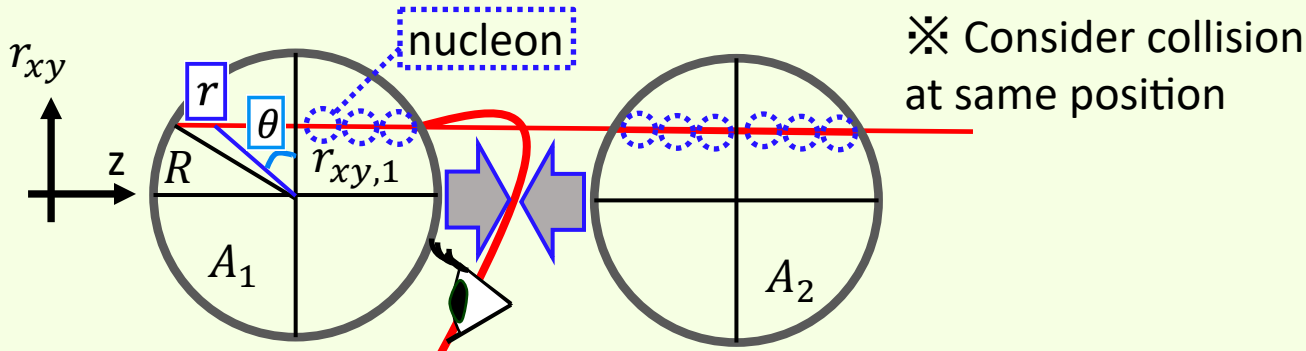
- At low p_T , the charged jet v_2 show **evidently positive value**. As it becomes high p_T , the charged jet v_2 gets **close to zero**.
- The charged jet v_2 of this measurement is **consistent with ATLAS result** within uncertainty around 70-110 GeV/c.

Model Simulation

My Simple Toy Model Algorithm

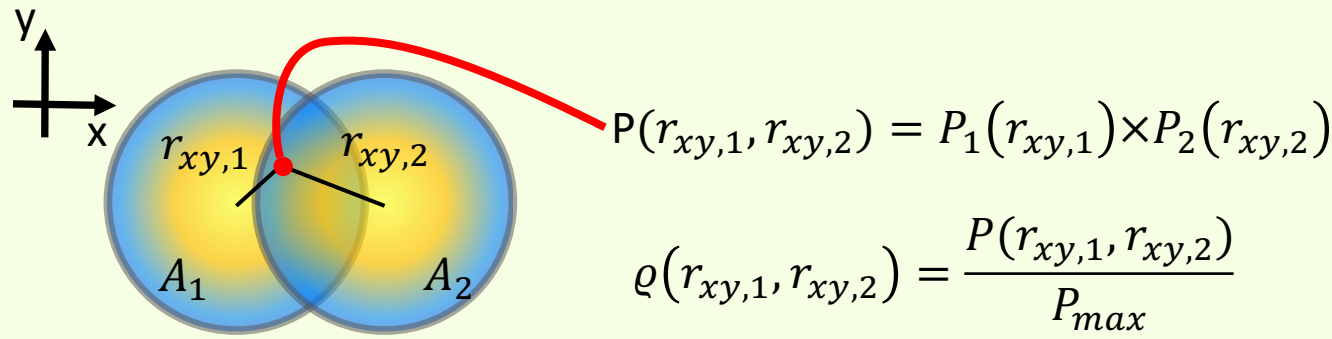
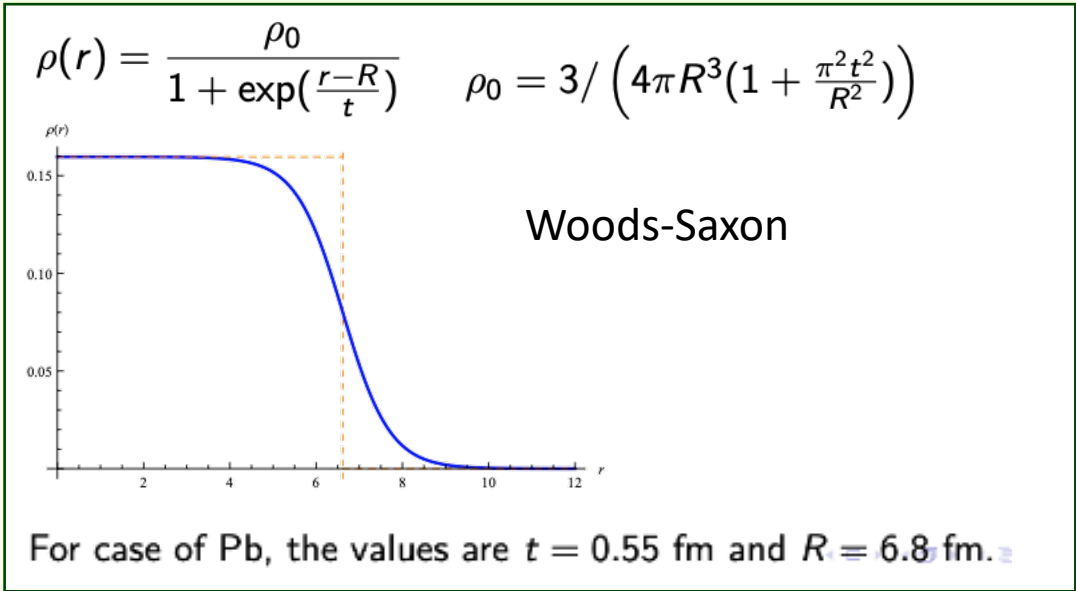


3. Calculate Hard Scattering Probability density ($P(r_{xy,1}, r_{xy,2})$)



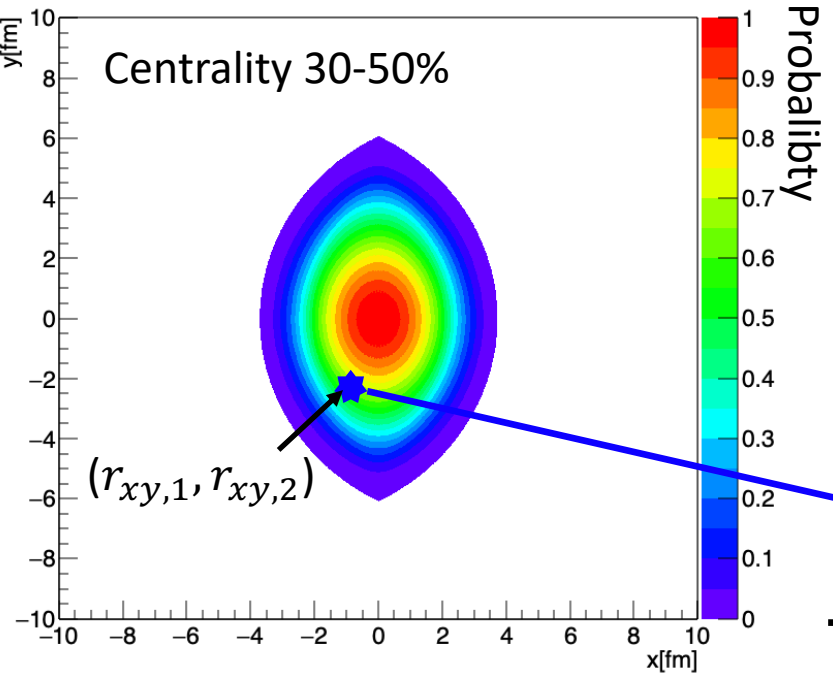
Projection (Integral) on x-y plane

$$P_1(r_{xy,1}) = 2 \int_0^{\cos^{-1} \frac{r_{xy,1}}{R}} d\theta \frac{\rho_0}{1 + \exp\left(\frac{r_{xy,1} \cos \theta - R}{t}\right)}$$

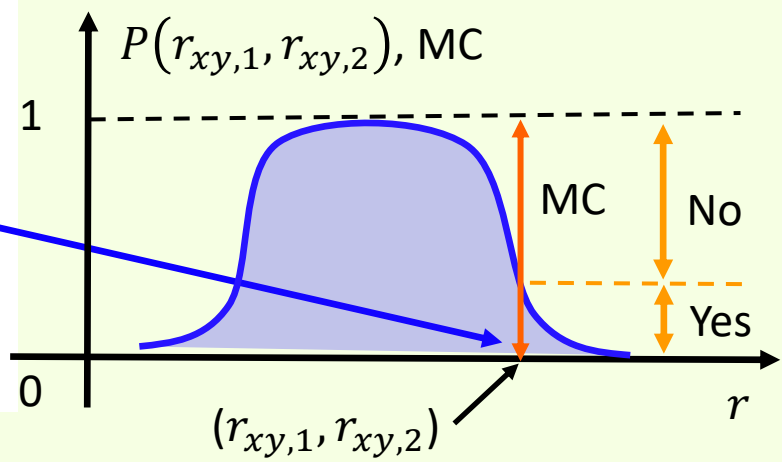


4. MC for create parton $P(r_{xy,1}, r_{xy,2}) < MC$

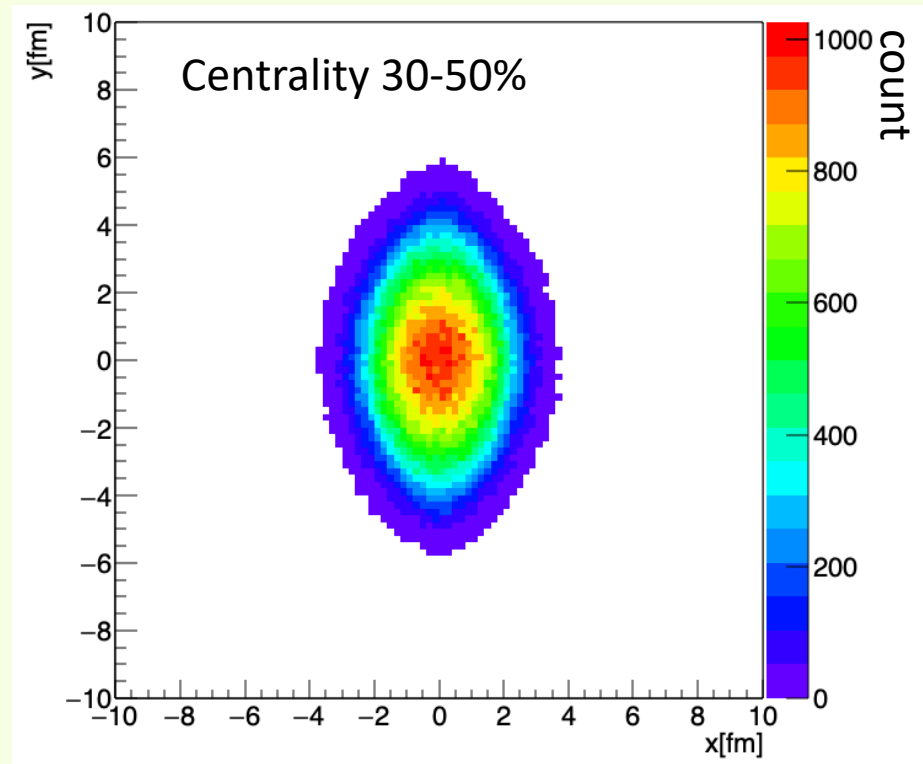
Calculate the probability density $P(r_{xy,1}, r_{xy,2})$ on the step.3



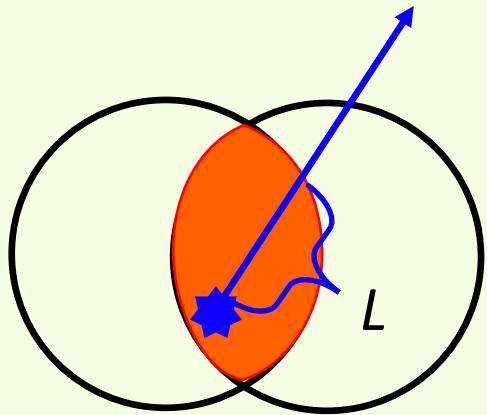
Based on the probability density, judge creation of a parton at the parton point.



Actual parton creation points (50,000 events)



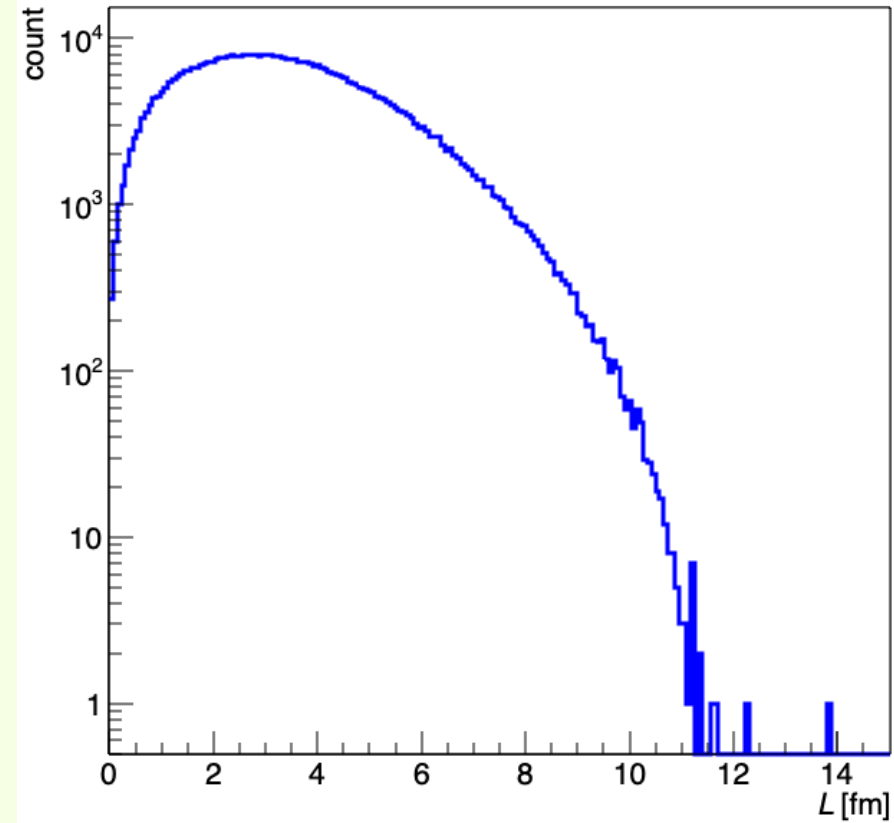
5. Calc pass length



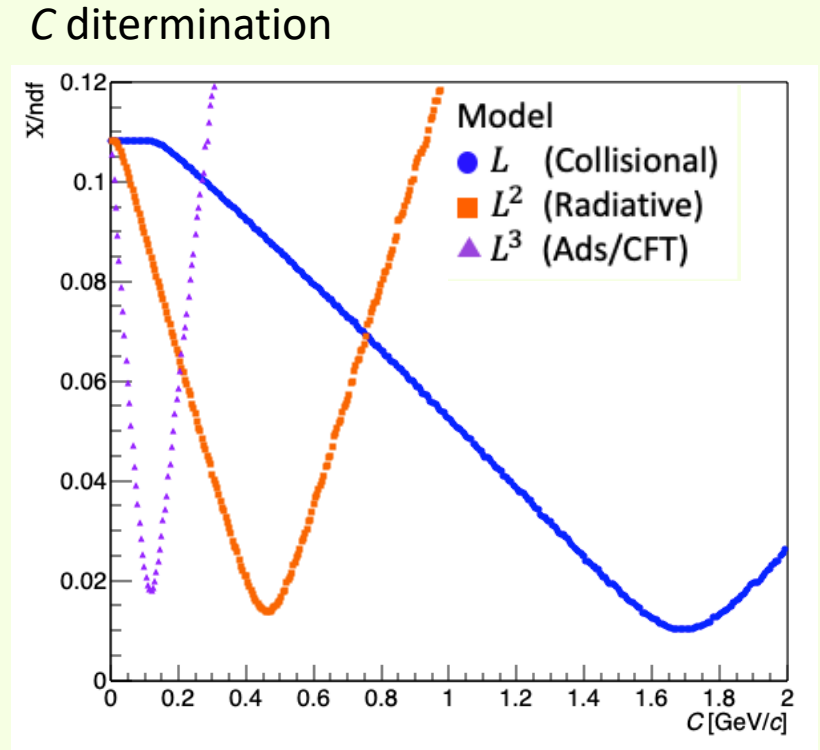
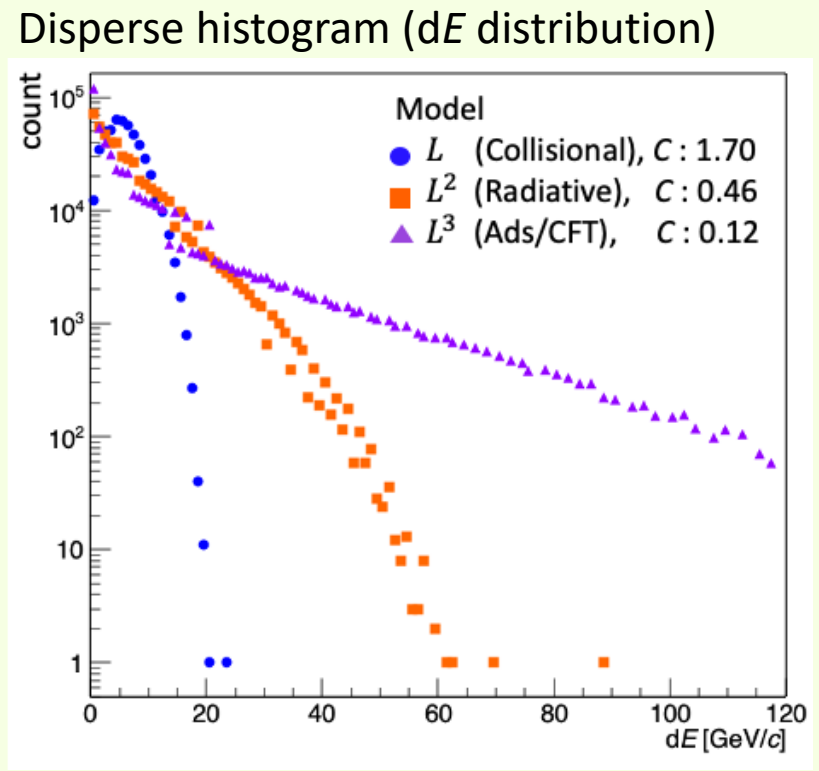
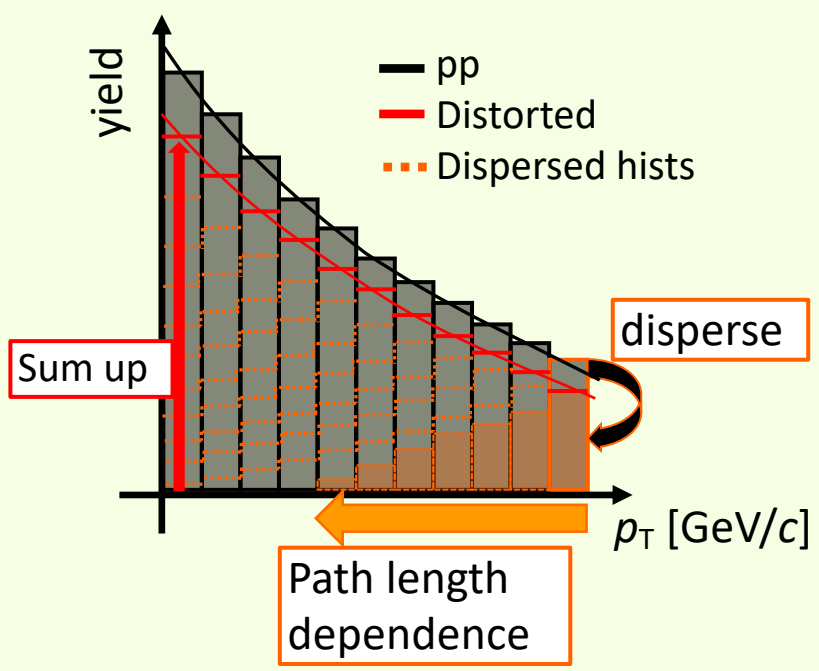
The edge is Woods-Saxon R

Regard the length from a parton creation point to a cross point of the original atom edge as the pass length.

- The original atom is supposed as a circle.
- The density of QGP is uniform on the reaction area.

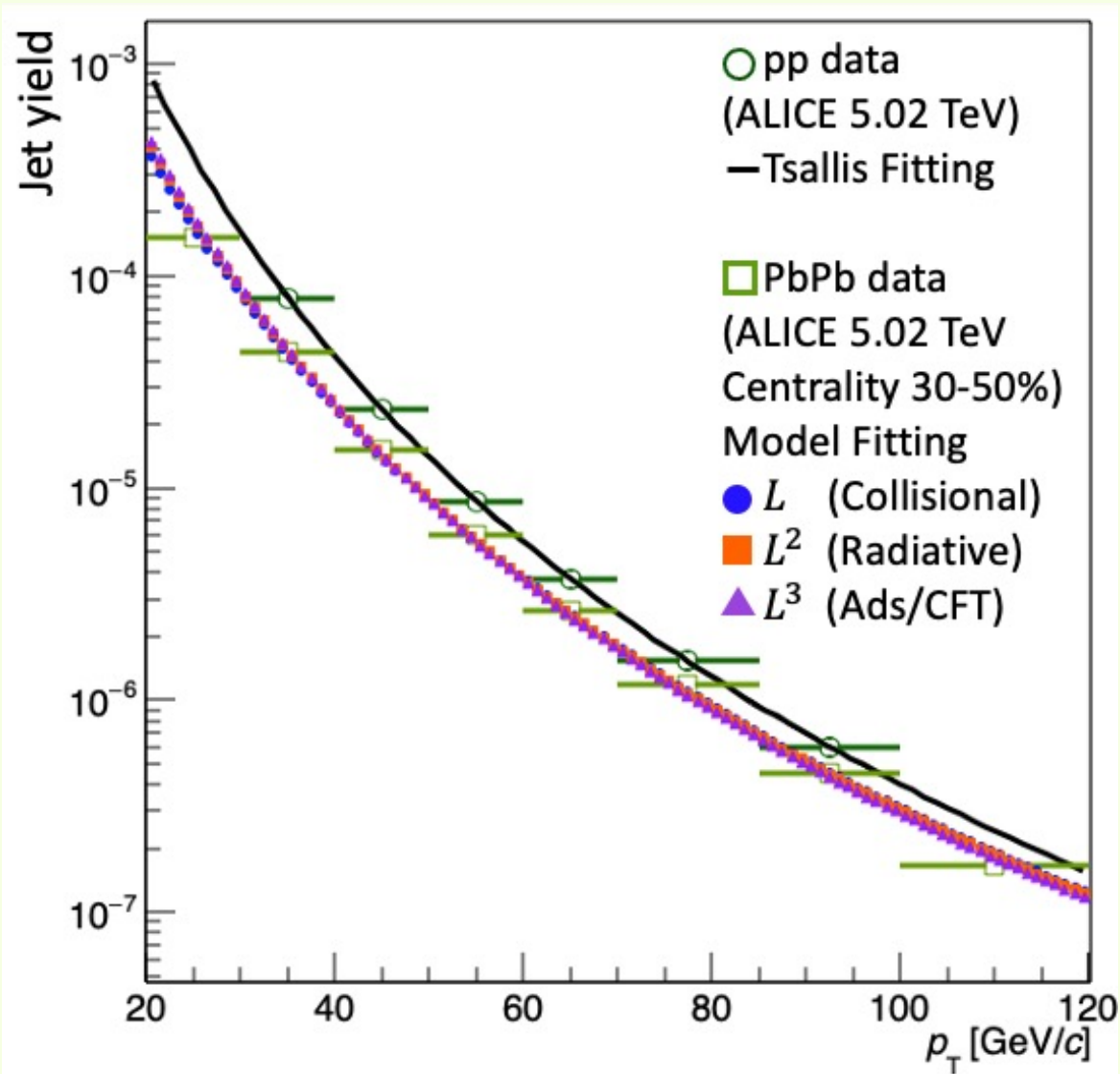


6. Calc Energy Loss ($dE = CL^n$) / 7. Determine C



1. Using the dE distribution, disperse each bin of the pp jet p_T distribution (MC/Fitting function). The dE distribution is normalized by each p_T bin counts.
2. Make a suppressed jet distribution by summing up distributions of each p_T bin.
3. Determine the best C to match the suppressed jet distribution and data PbPb jet p_T distribution.

7. Each inclusive charged jet p_T distributions



pp fitting function (Tsallis)

$$F(p_T) = p_0 \times p_T^{1+p_1} \times \left[1 + (p_2 - 1) \times \frac{p_T}{p_3} \right]^{-p_2/(p_2-1)}$$

$$p_0 : 0.524, p_1 : 2.252, p_2 : 1.127, p_3 : 0.497$$

8. Make In/Out of plane jet yield distributions

Apply suppression parameter C estimated Step.7 to In/Out of plane jets, respectively.

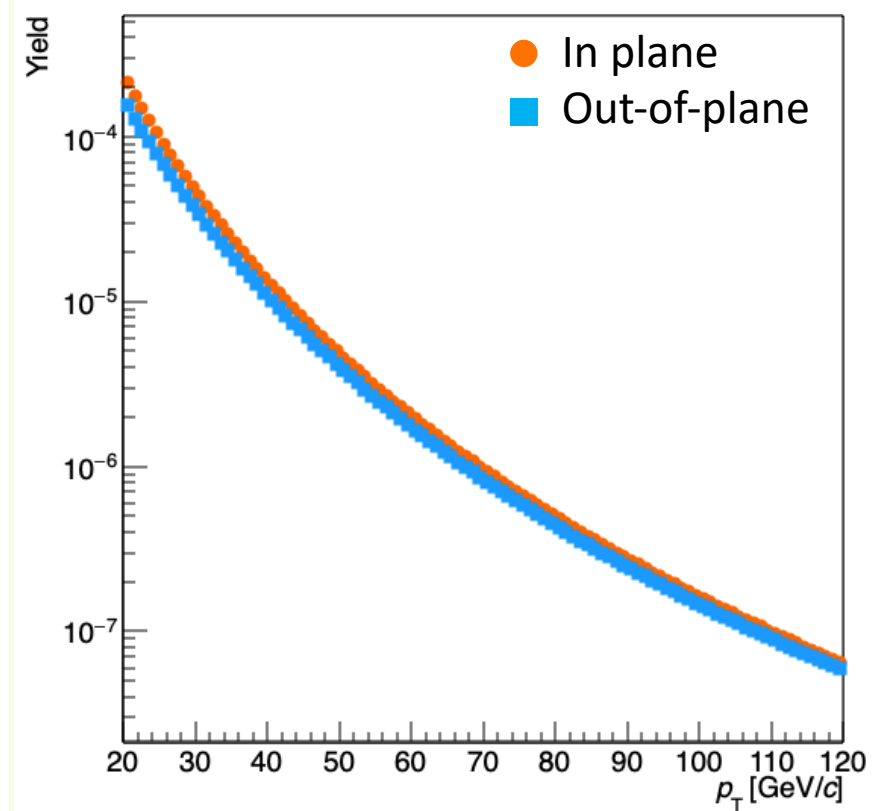
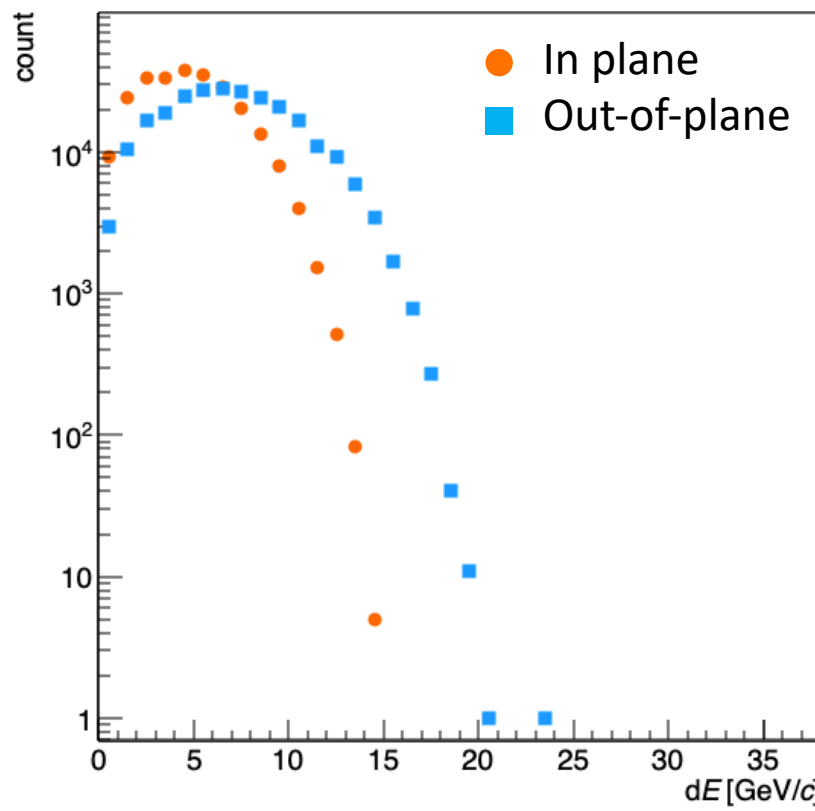
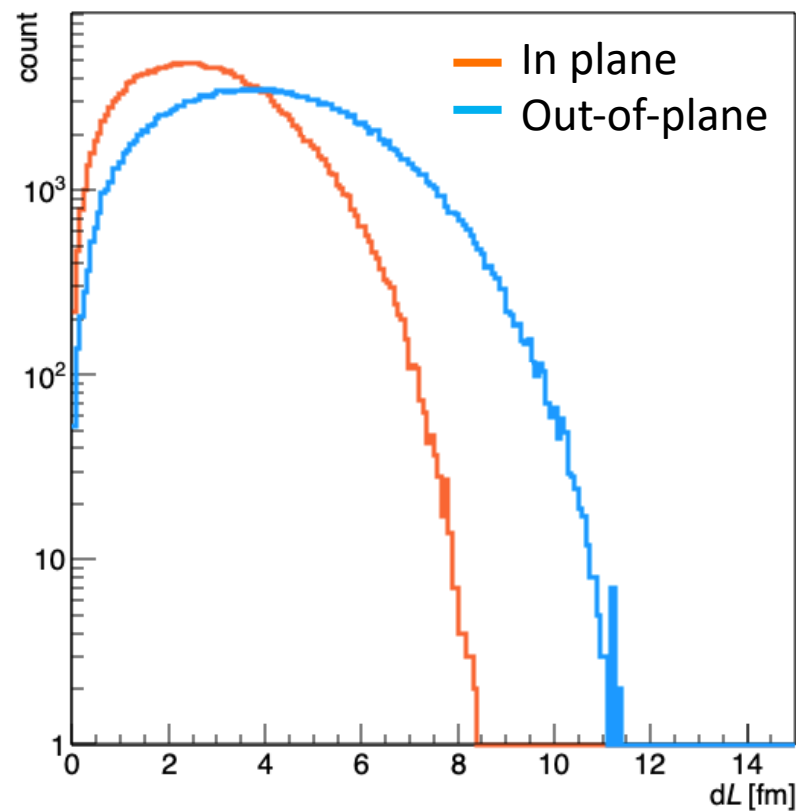
(In: parton emission angle $-\pi/4 - \pi/4$ and $3\pi/4 - 5\pi/4$,

Out: parton emission angle $\pi/4 - 3\pi/4$ and $5\pi/4 - 7\pi/4$)

Path length

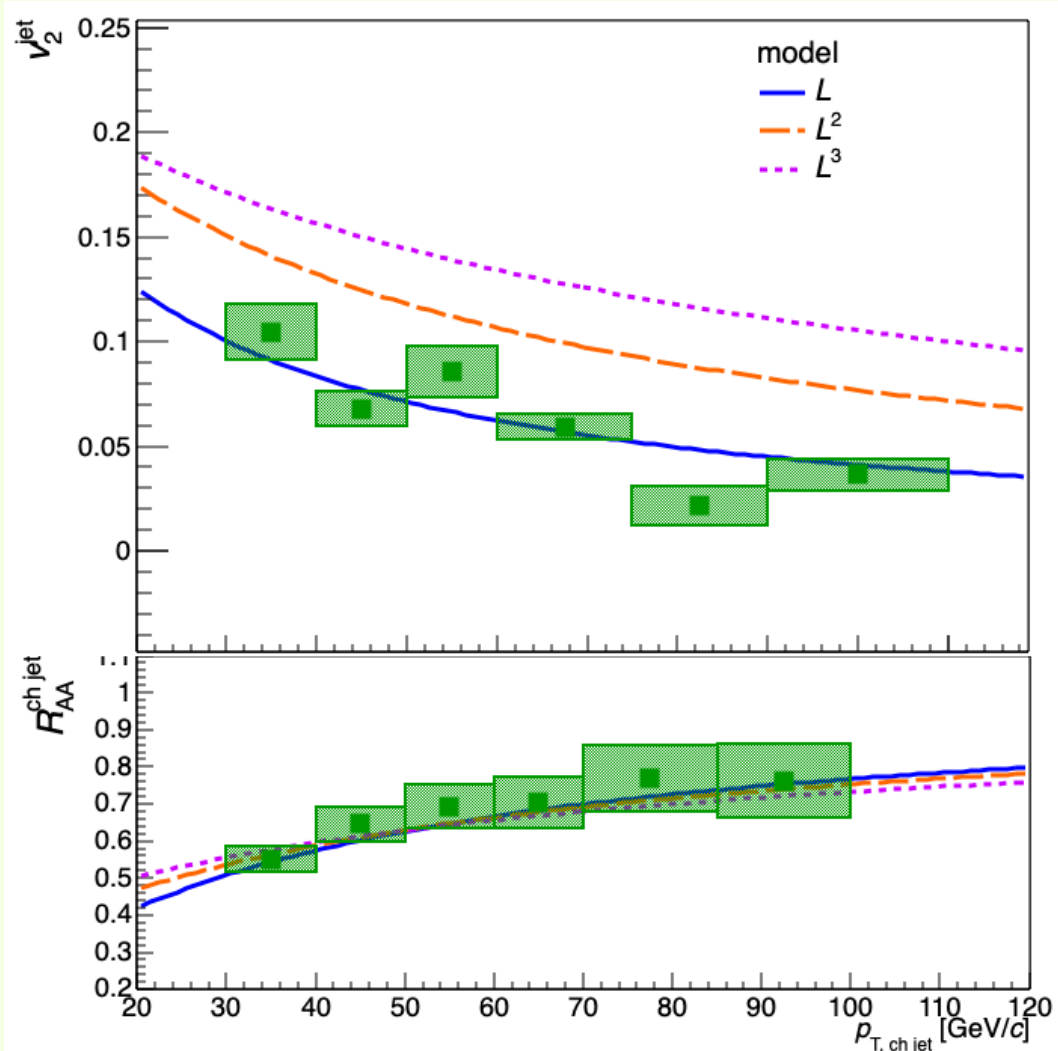
Energy Loss ($n=1$, collisional)

Jet Yield ($n=1$, collisional)



9. Use Tsallis fitting function for model R_{AA} distribution

Use Tsallis fitting function for model R_{AA} distribution



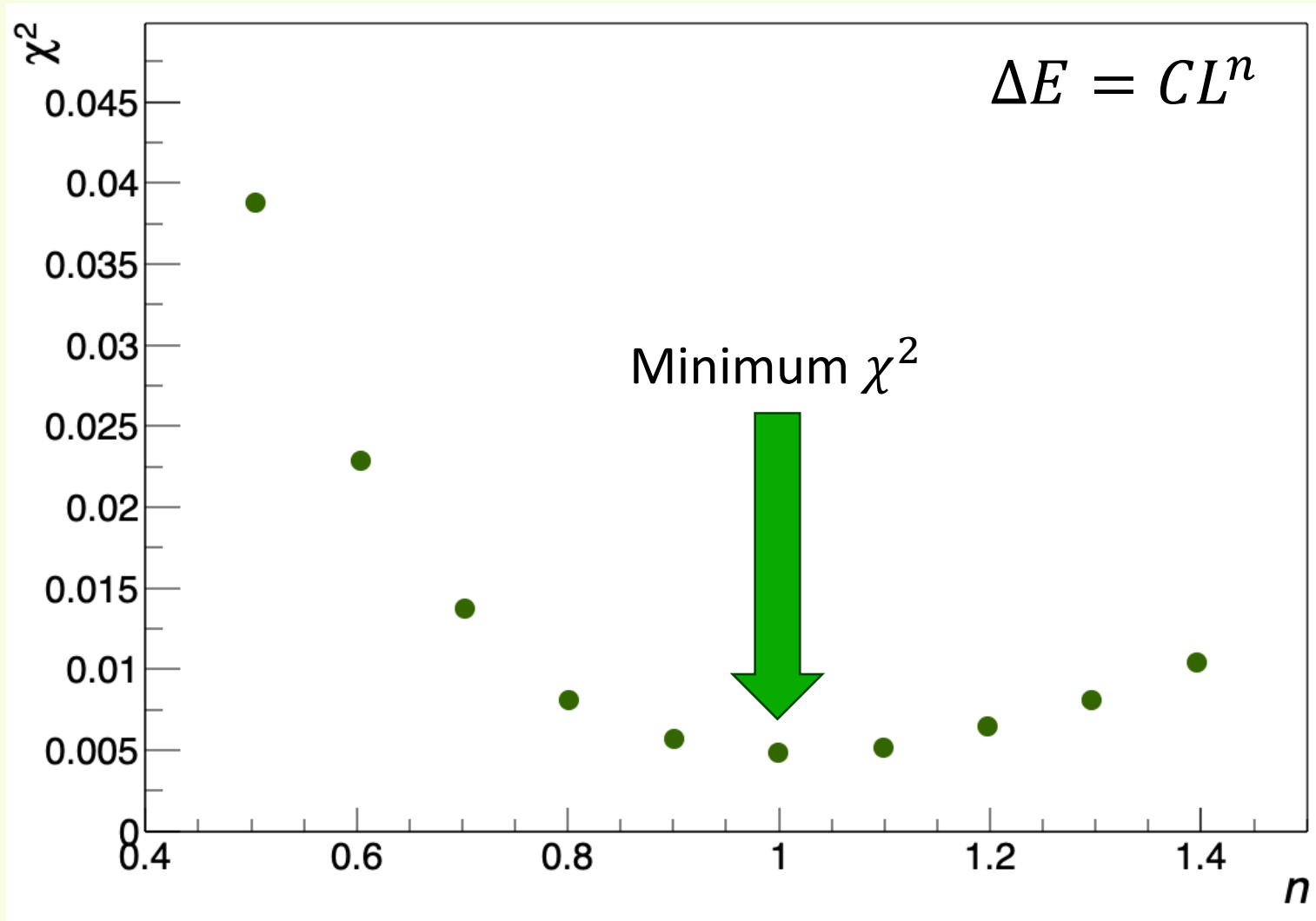
Chi²/NDF Ch-Jet R_{AA}
(L, L^2, L^3) = (**0.017**, 0.018, 0.023)

Chi²/NDF Ch-Jet v_2
(L, L^2, L^3) = (**0.0074**, 0.023, 0.036)

⊗ NDF: pT bins – 1 (Free parameter C)
(L, L^2, L^3) = (Collisional, Radiative, Ads/CFT)

→ Best model is **$dE = CL, (n = 1)$**

Best L dependence Search

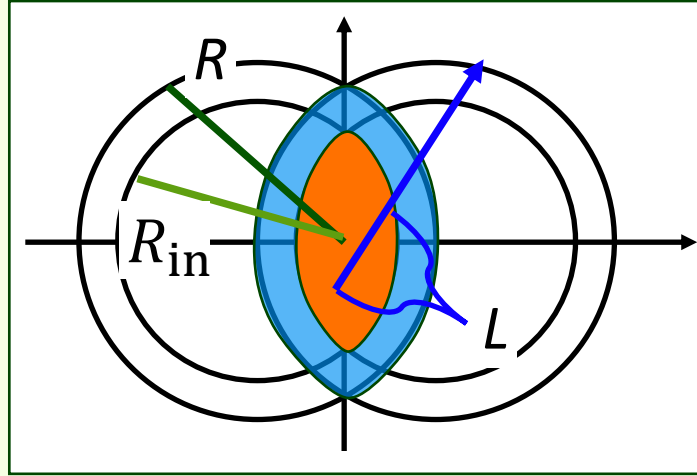
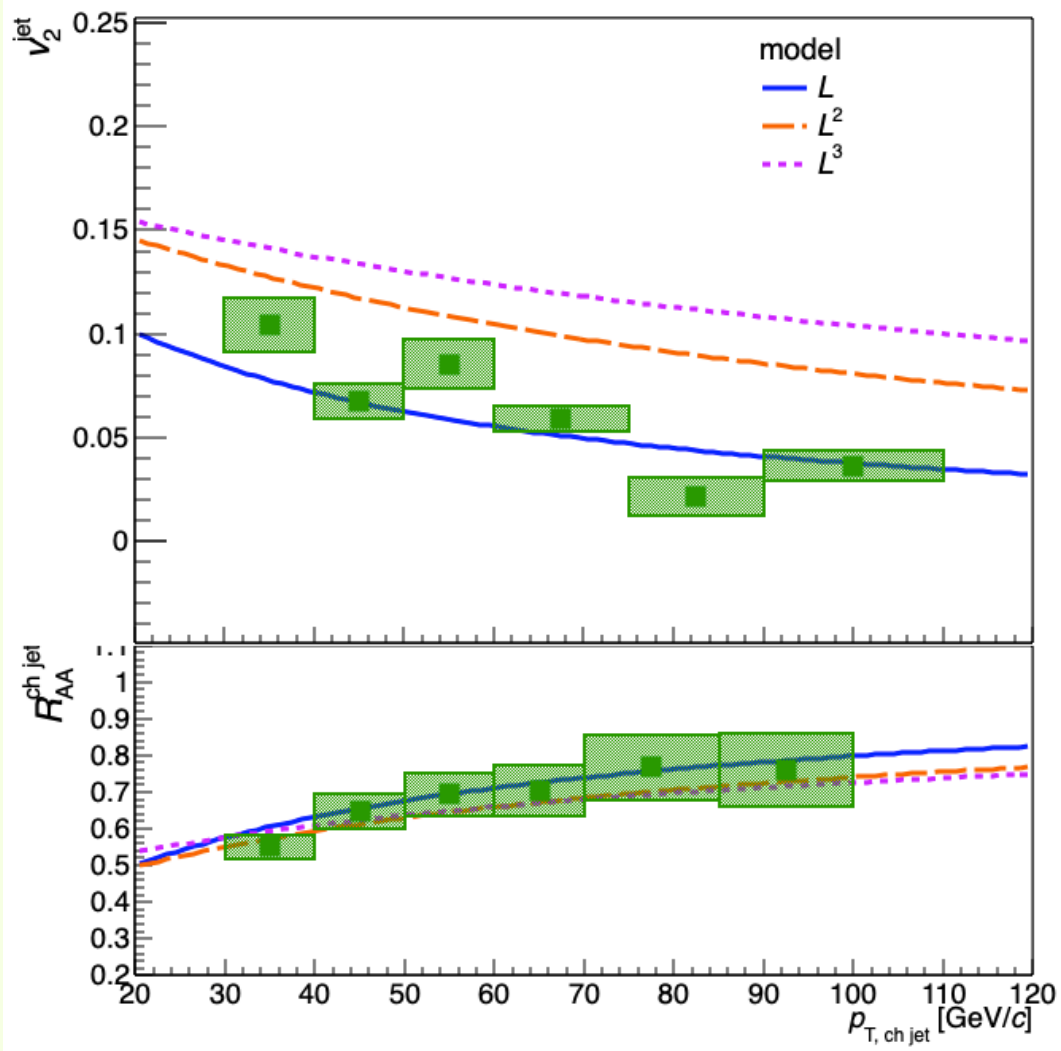


✂ Each coefficient of C is adjusted for each pass length dependency n .

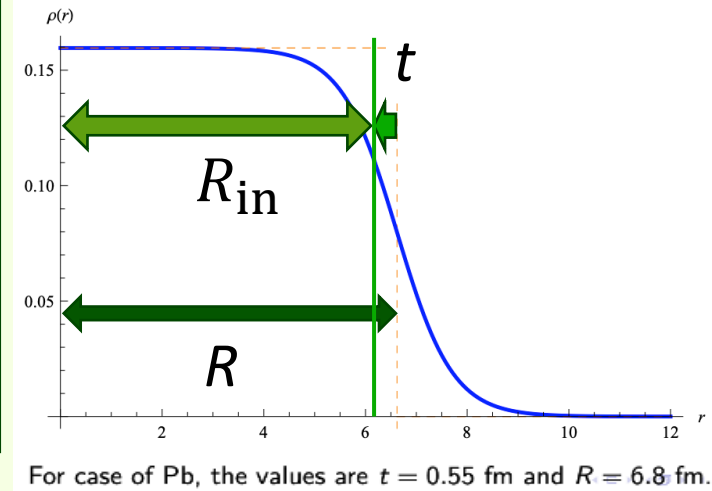
Just $n = 1$ is the best pass length dependency for parton energy loss.

Different pass length edge

Use Tsallis fitting function for model R_{AA} distribution



$$\rho(r) = \frac{\rho_0}{1 + \exp\left(\frac{r-R}{t}\right)}$$

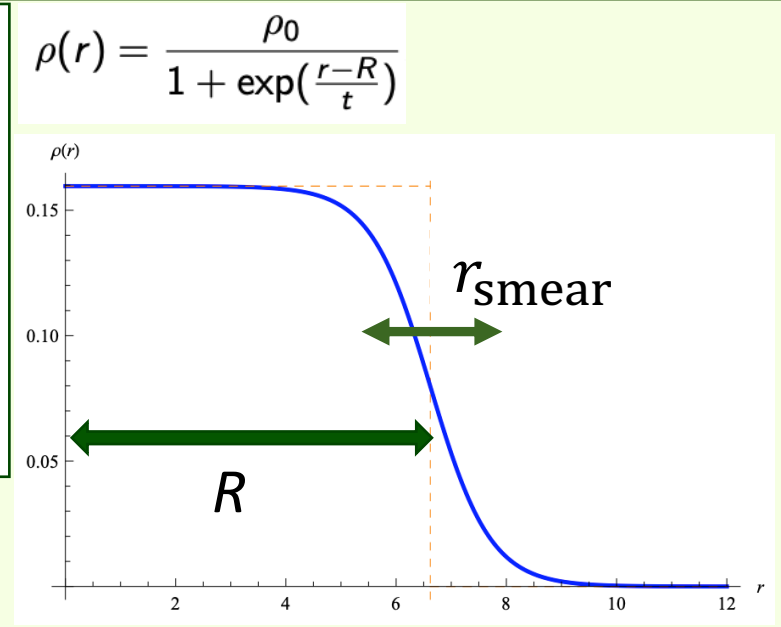
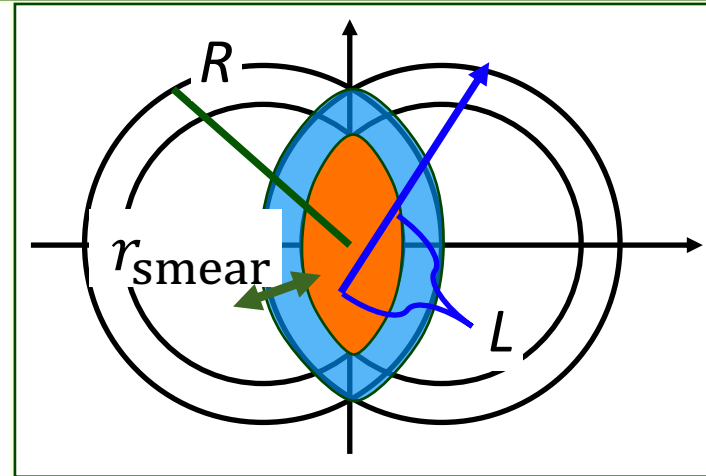
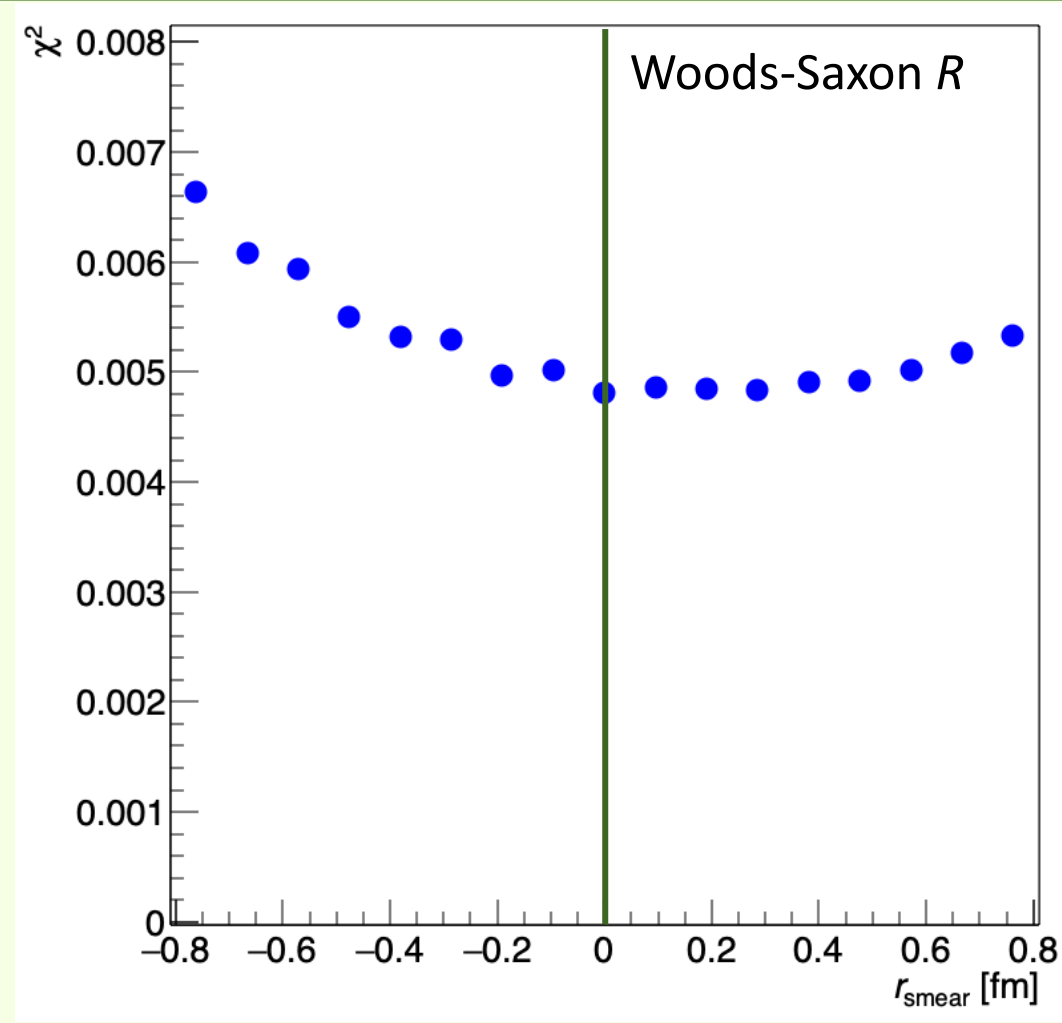


Chi²/NDF Ch-Jet R_{AA}
 $(L, L^2, L^3) = (0.013, 0.021, 0.023)$

Chi²/NDF Ch-Jet v_2
 $(L, L^2, L^3) = (0.0089, 0.022, 0.031)$

→ Best model is $dE = CL, (n = 1)$

Best QGP Edge Search



The result of QGP edge indicates the Woods-Saxon R is the best.

→ Every participants contribute the QGP creation, and the thermarization of QGP happenes immediately.
(Do not need to consider density profile and dependency of energy loss for the density.)

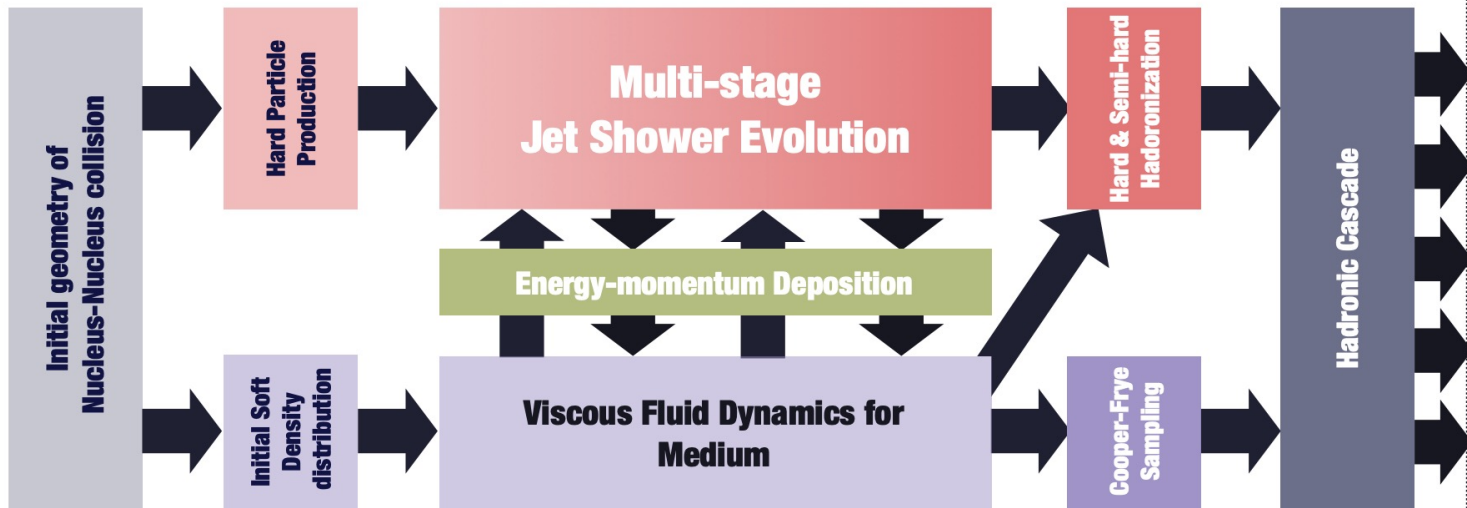
Summary and Outlook

- To clarify jet quenching mechanism and estimate its parameters, charged jet v_2 is measured using the ALICE data of Pb–Pb collision $\sqrt{s_{NN}} = 5.02$ TeV.
- The charged jet v_2 in centrality 30-50% show **positive value** and it is **consistent with other experiments**.
- Compare the data results with my very simple toy model
- The simulation indicates that the parton energy loss is proportional to path length (**$dE = CL, (n = 1)$**).
- The model with $n=1$ reproduces well the value and shape of both charged jet R_{AA} and v_2 .
- Determining the quenching parameter requires more complex models in **JETSCAPE**.
- Additional analysis: Different centrality, Different jet resolution $R(= 0.1, 0.4)$

Backup Slides

JETSCAPE Framework

JETSCAPE Event Generator

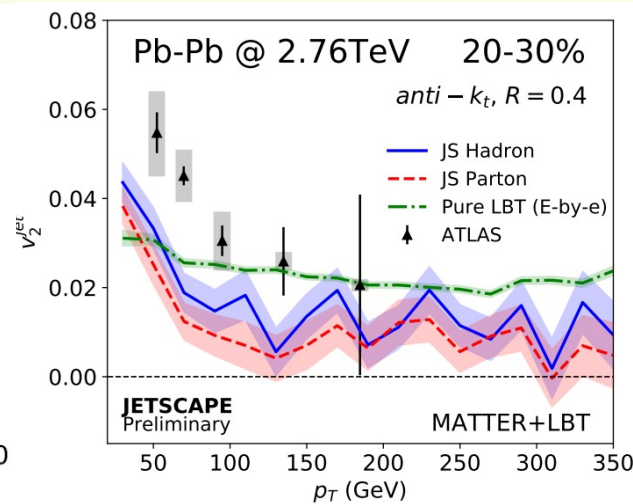
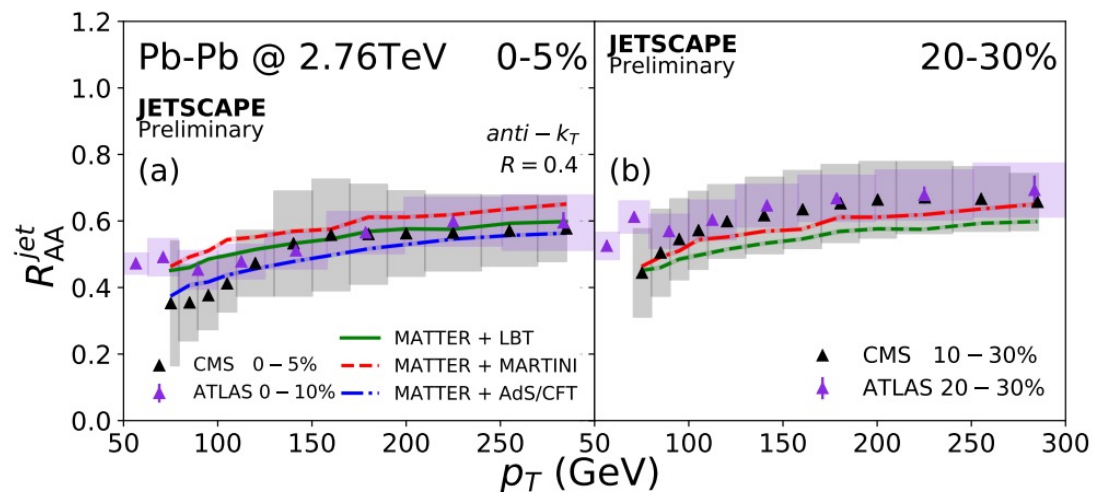


JETSCAPE <https://arxiv.org/abs/1903.07706>
 (Jet Energy-loss Tomography with a Statistically and Computationally Advanced Program Envelope)

- It has \hat{q} as a variable parameter.
- Some models having different L dependency.

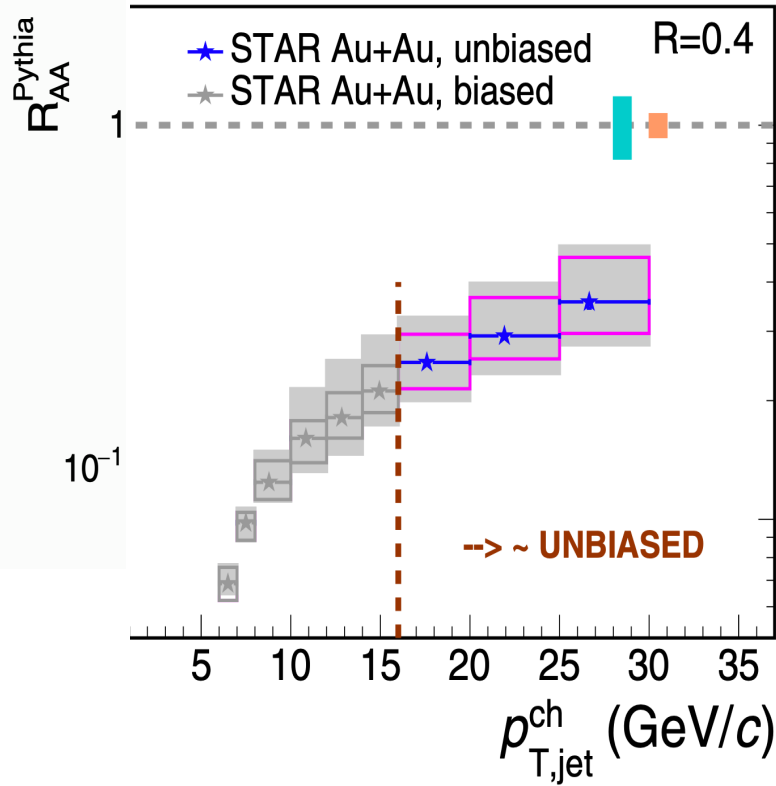
Diagram courtesy Y. Tachibana

The JETSCAPE already represents close value of the jet R_{AA} and v_2

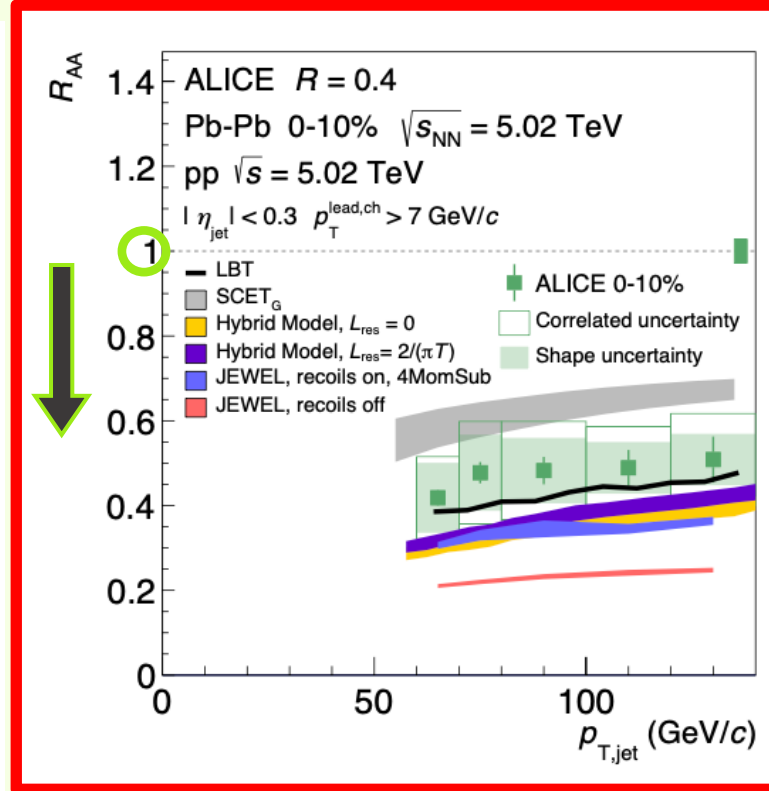


DOI: <https://doi.org/10.22323/1.345.0072>

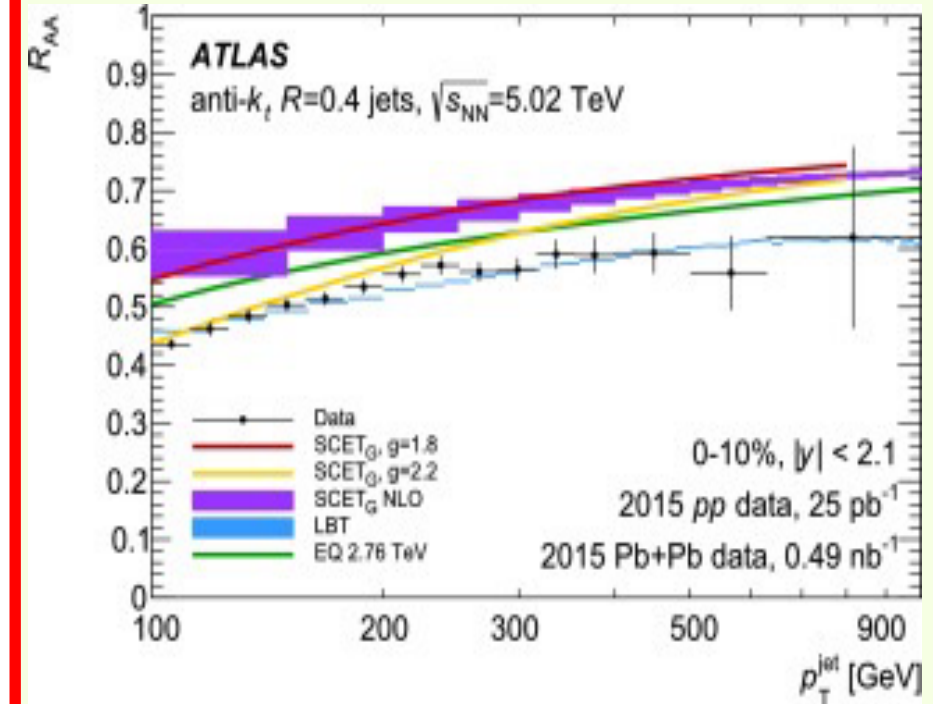
Nuclear modification factor (R_{AA})



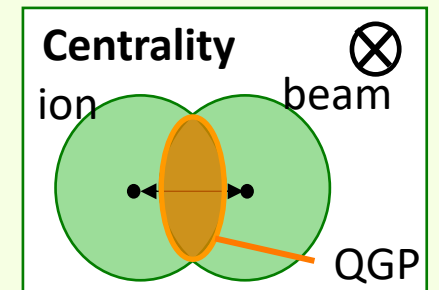
STAR Phys. Rev. C **102** (2020) 054913



ALICE Phys. Rev. C **101** (2018) 034911



ATLAS PLB 790 (2019) 108

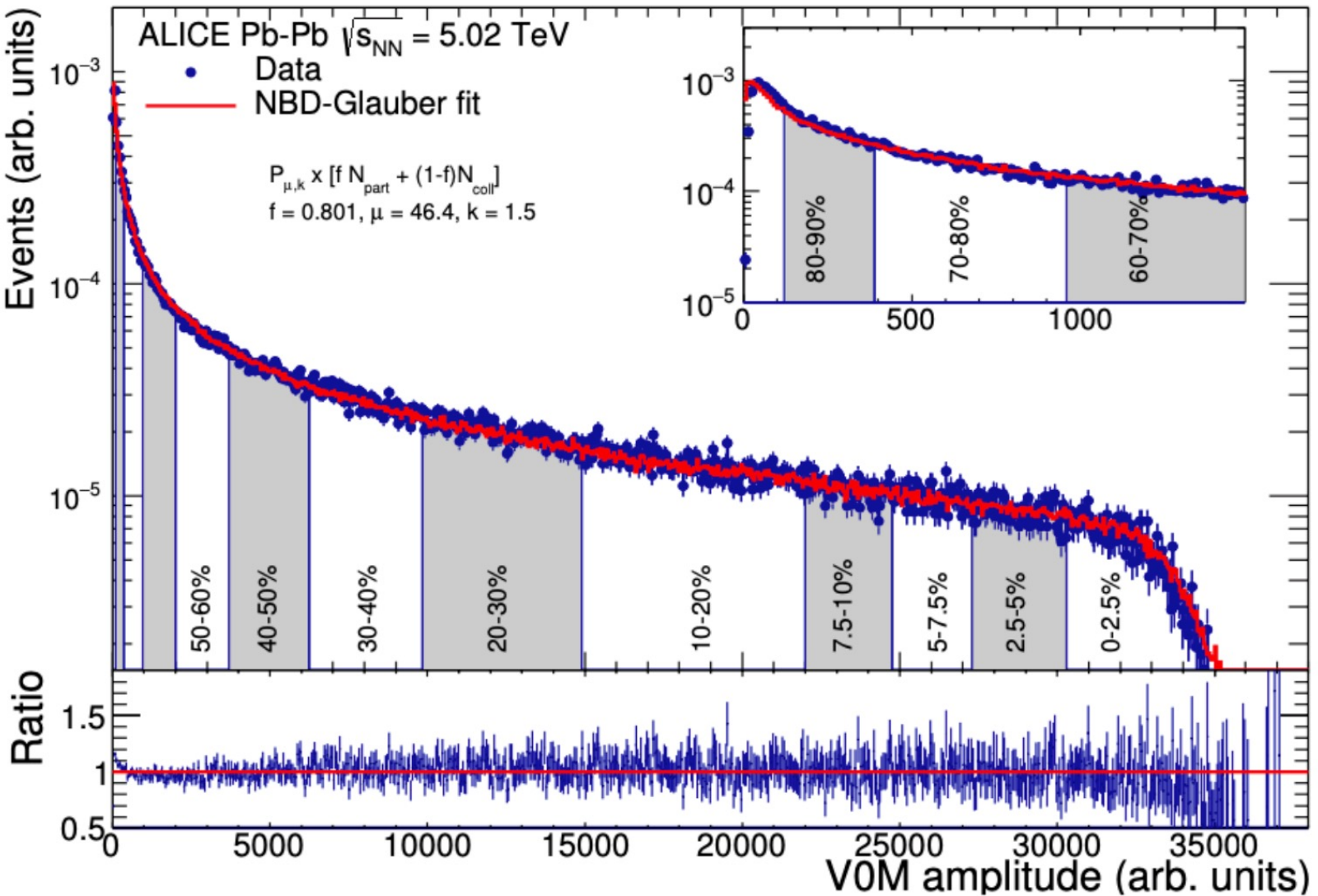


Event Selection

Number of events: 38×10^6 events

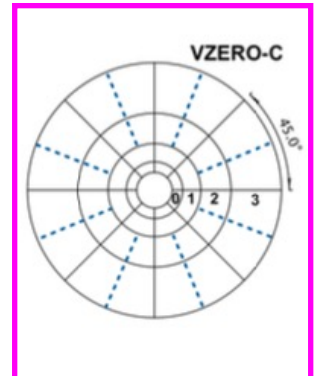
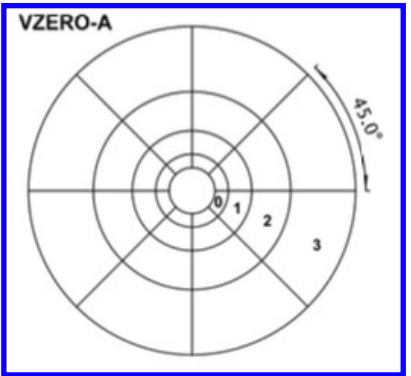
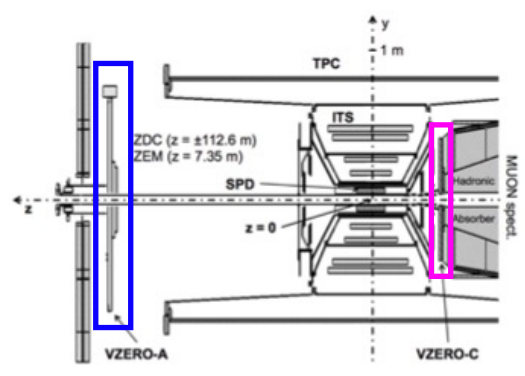
Primary vertex: $|z| < 10\text{cm}$.

Centrality determination



Using NBD-Glauber fit for V0M amplitude, the event centrality is determined

Qn vector calibration

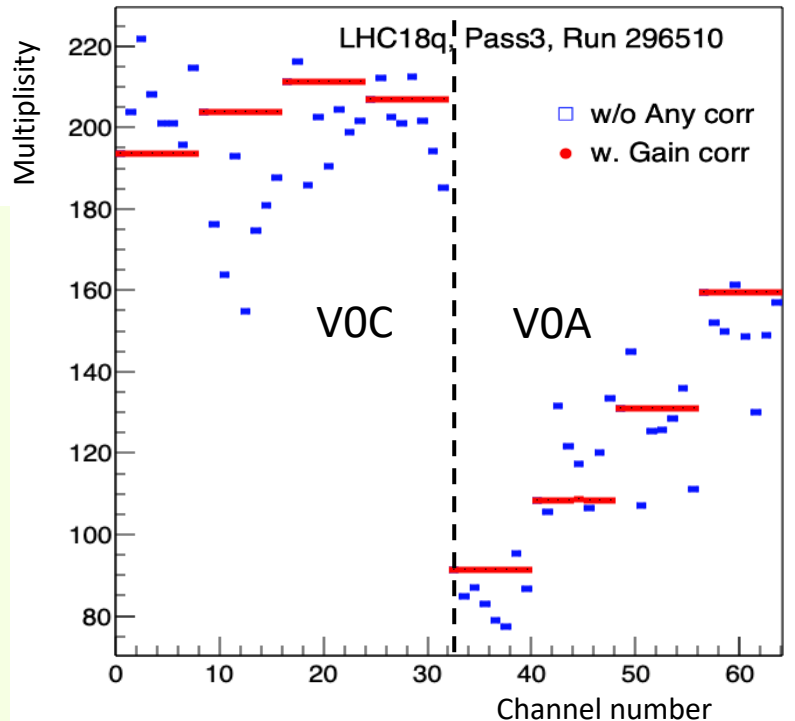


estimated for run-by-run.
Average means the run average.

Gain equalization

$$\omega_{ch} = M_i \frac{\langle M_{ref} \rangle}{\langle M_i \rangle}$$

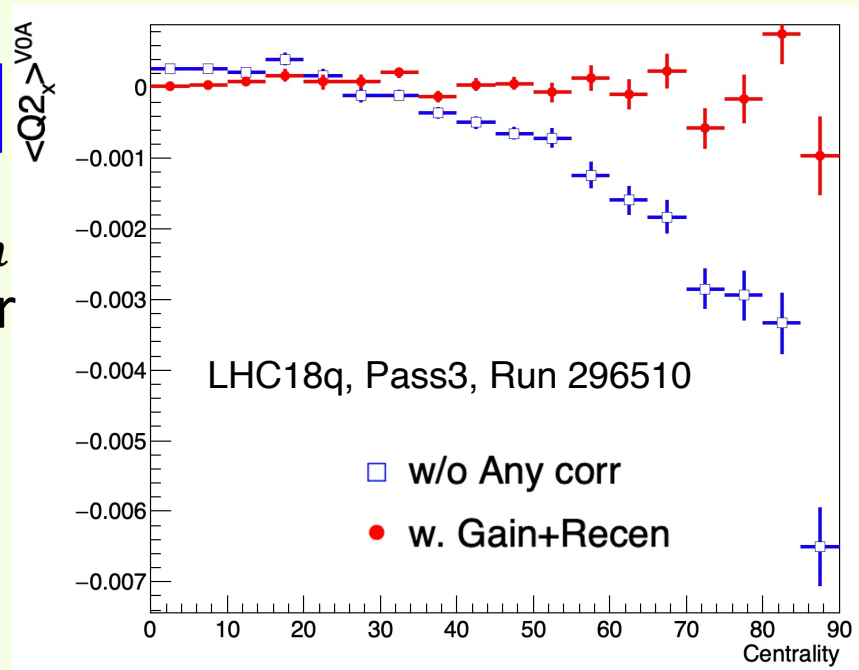
Equalize gain to uniform the each channel value on the same ring.



Recentring

$$Q'_n = Q_n - \langle Q_n \rangle$$

Equalize Q_n to uniform for centrality



Event plane angle resolution

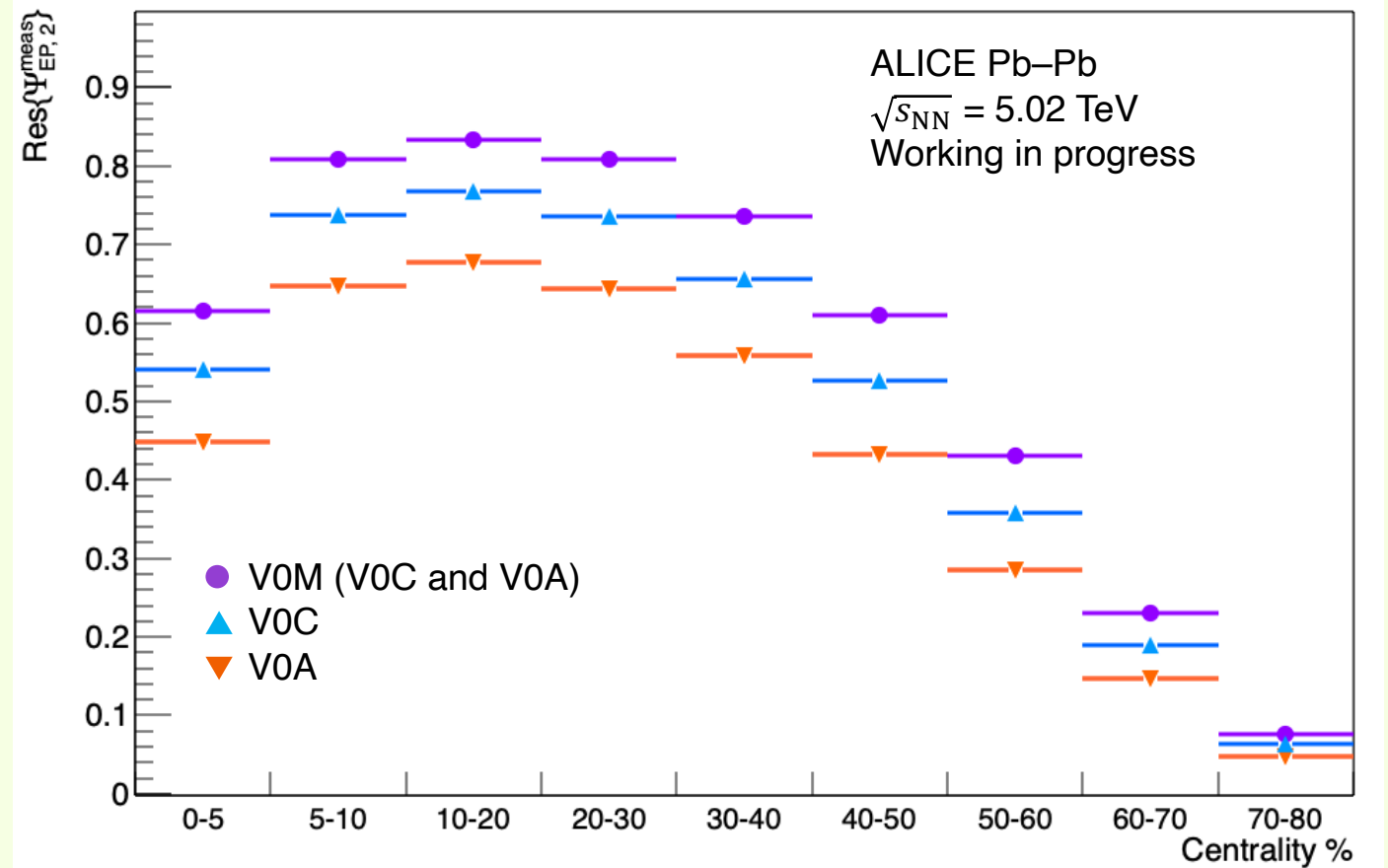
$$\text{Res}\{\Psi_{EP,2}^{\text{meas}}\} = \langle \cos(n[\Psi_{EP,n}^a - \Psi_n]) \rangle = \sqrt{\frac{\langle \cos(n[\Psi_{EP,n}^a - \Psi_{EP,n}^b]) \rangle \langle \cos(n[\Psi_{EP,n}^a - \Psi_{EP,n}^c]) \rangle}{\langle \cos(n[\Psi_{EP,n}^b - \Psi_{EP,n}^c]) \rangle}}$$

$$v_2^{\text{jet}} = \frac{1}{\text{Res}\{\Psi_{EP,2}^{\text{meas}}\}} \frac{\pi}{4} \frac{N_{in} - N_{out}}{N_{in} + N_{out}}$$

Ideally, $\Psi_{EP,n}^a - \Psi_{EP,n}^{\text{truth}}$ close to 0.
In that case, $\text{Res}\{\Psi_{EP,2}^{\text{meas}}\}$ close to 1.

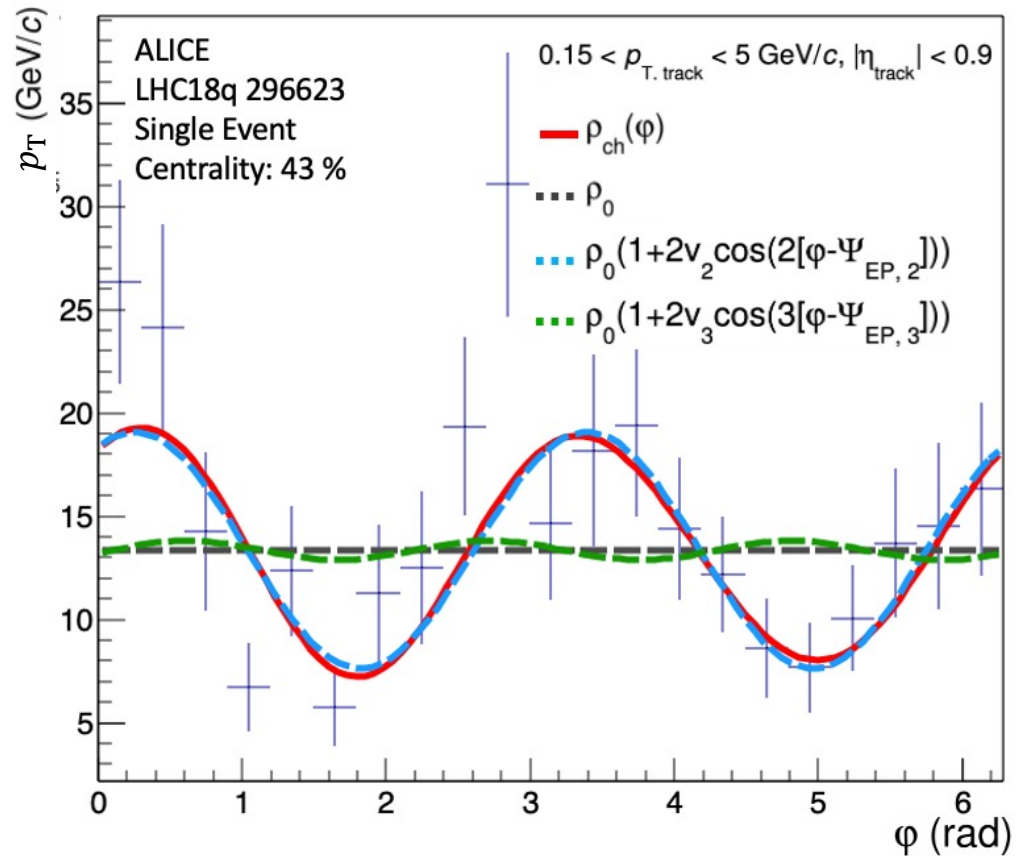
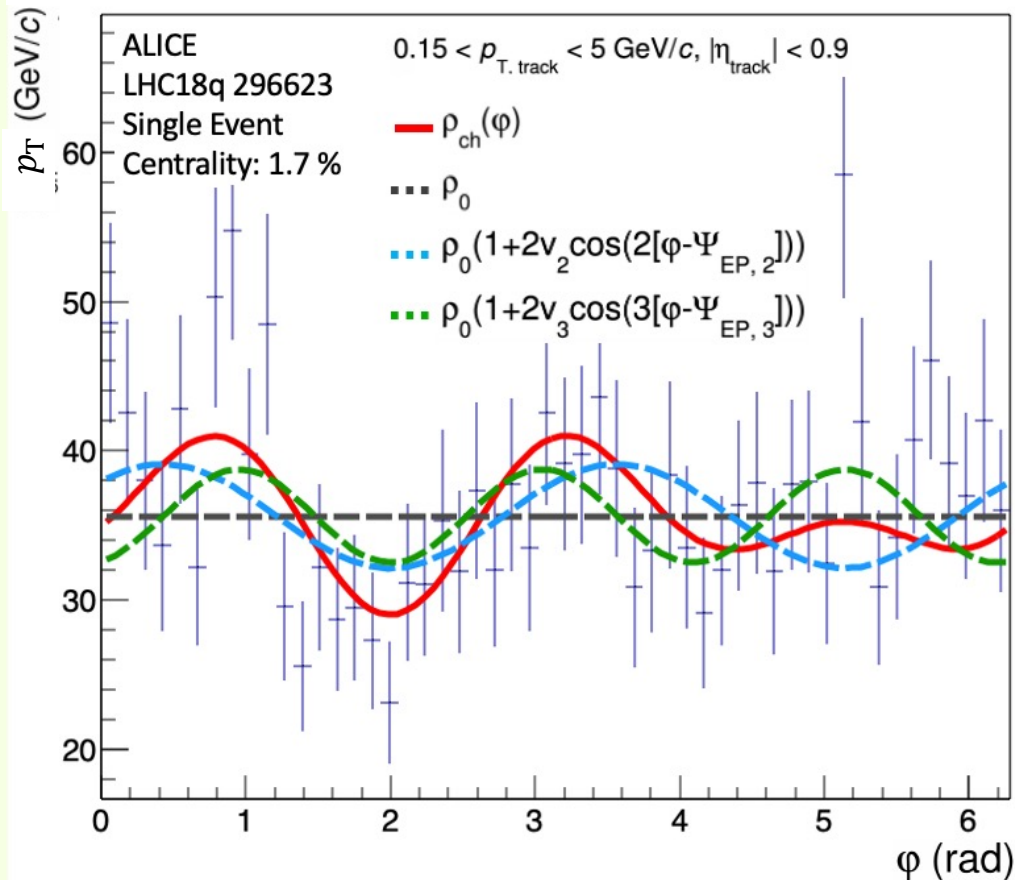
V0 sub-detector

(b: TPC $\eta < 0$, c: TPC $\eta > 0$)



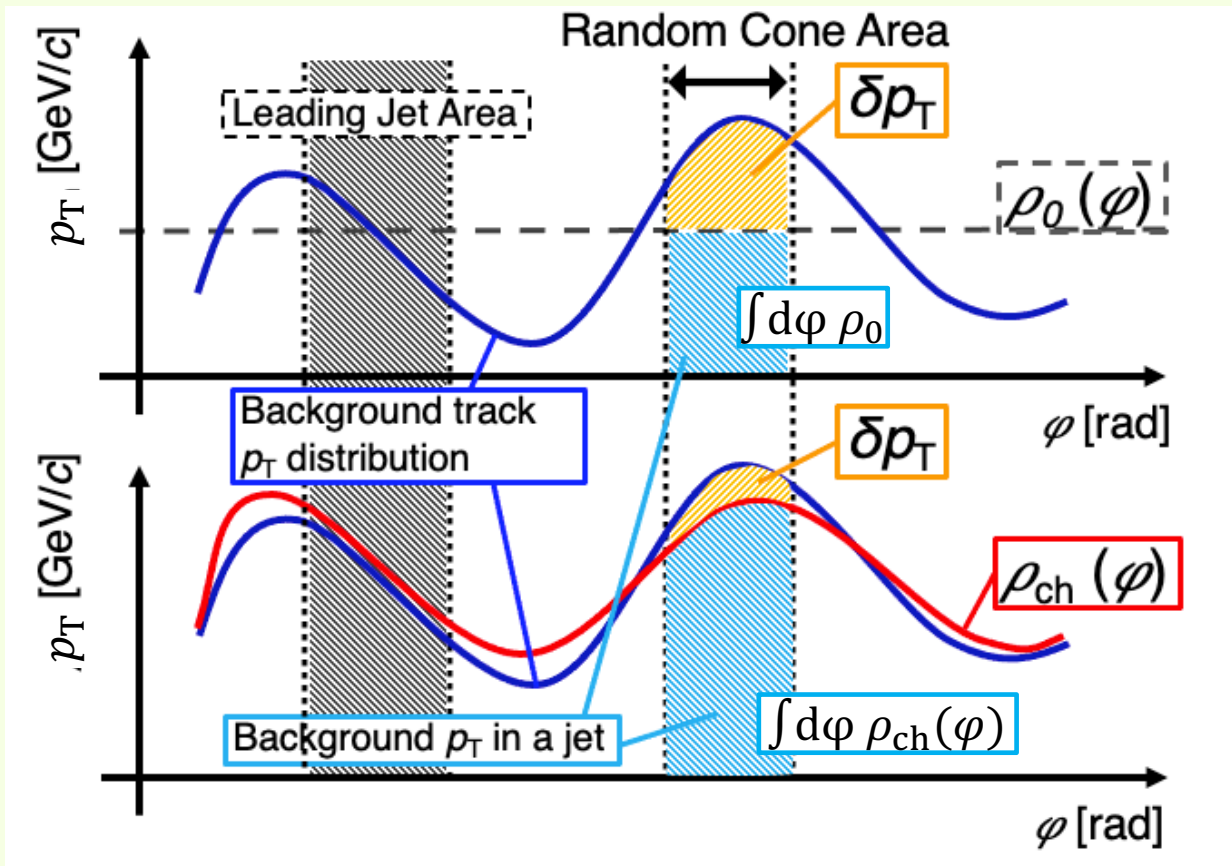
Local background p_T results

$$\rho_{\text{ch}}(\varphi) = \rho_0 \times \left(1 + 2 \left\{ v_2^{\text{obs}} \cos(2[\varphi - \Psi_{\text{EP},2}]) + v_3^{\text{obs}} \cos(3[\varphi - \Psi_{\text{EP},3}]) \right\} \right)$$



of bins = $\sqrt{N_{\text{track}}}$

Evaluation of background fit (δp_T)

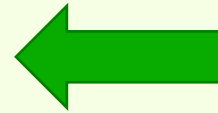
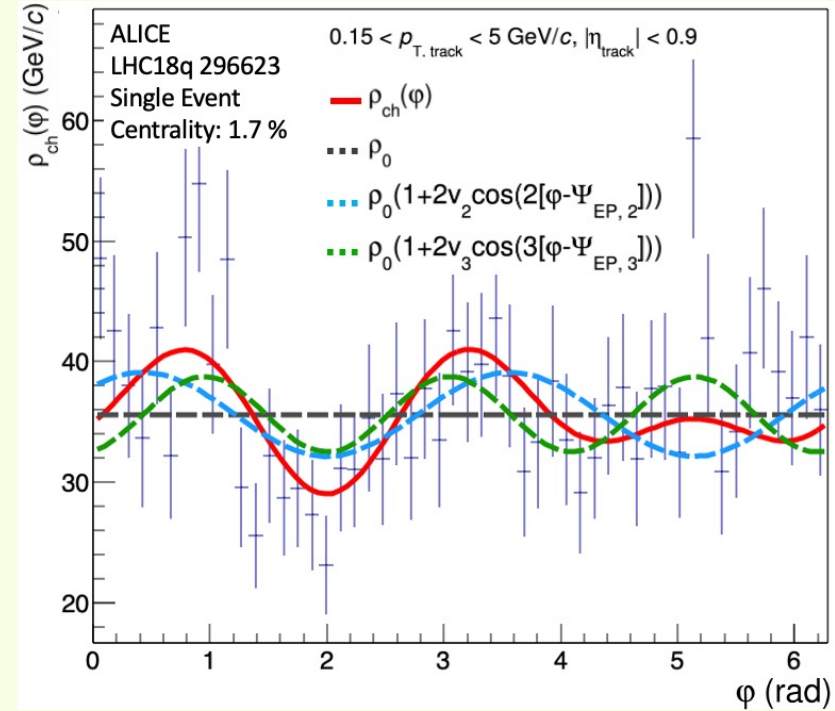
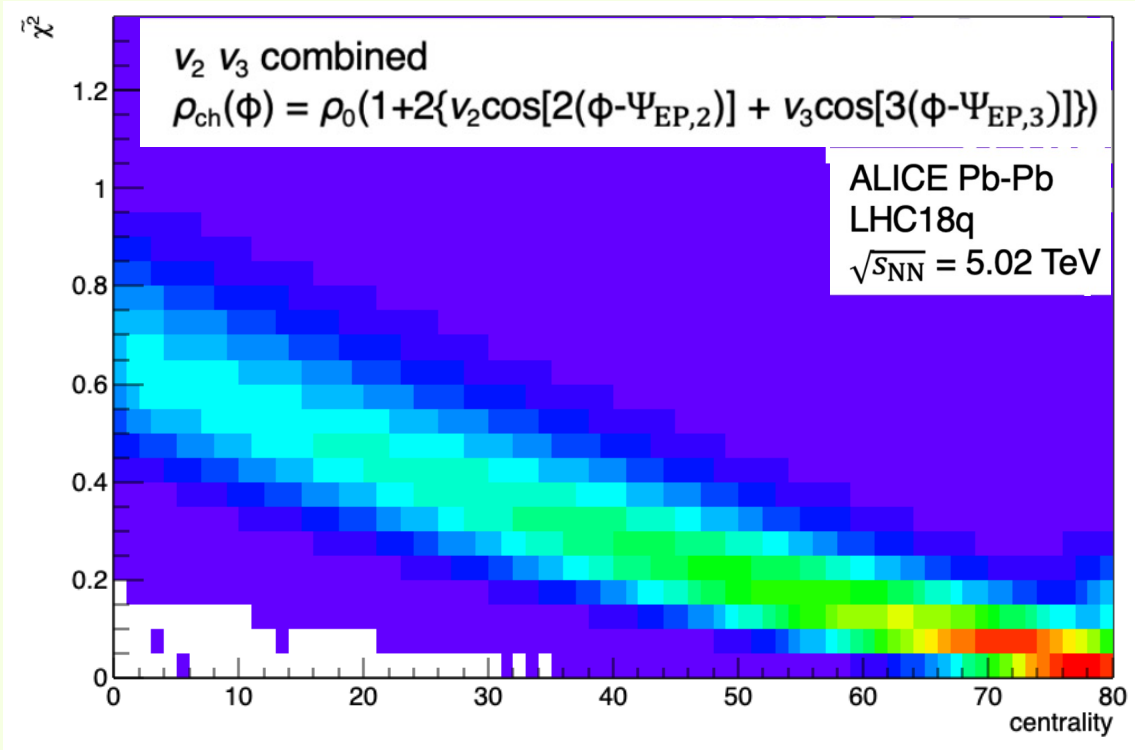


δp_T is a gap between integration of background tracks p_T and integration of background function in a random cone area.

We expect the local rho's δp_T should be smaller than the median one. And in the local rho case, δp_T phi dependency is expected to make small.

The Random cone is created once per event except the leading jet region.

Background pT function fit quality



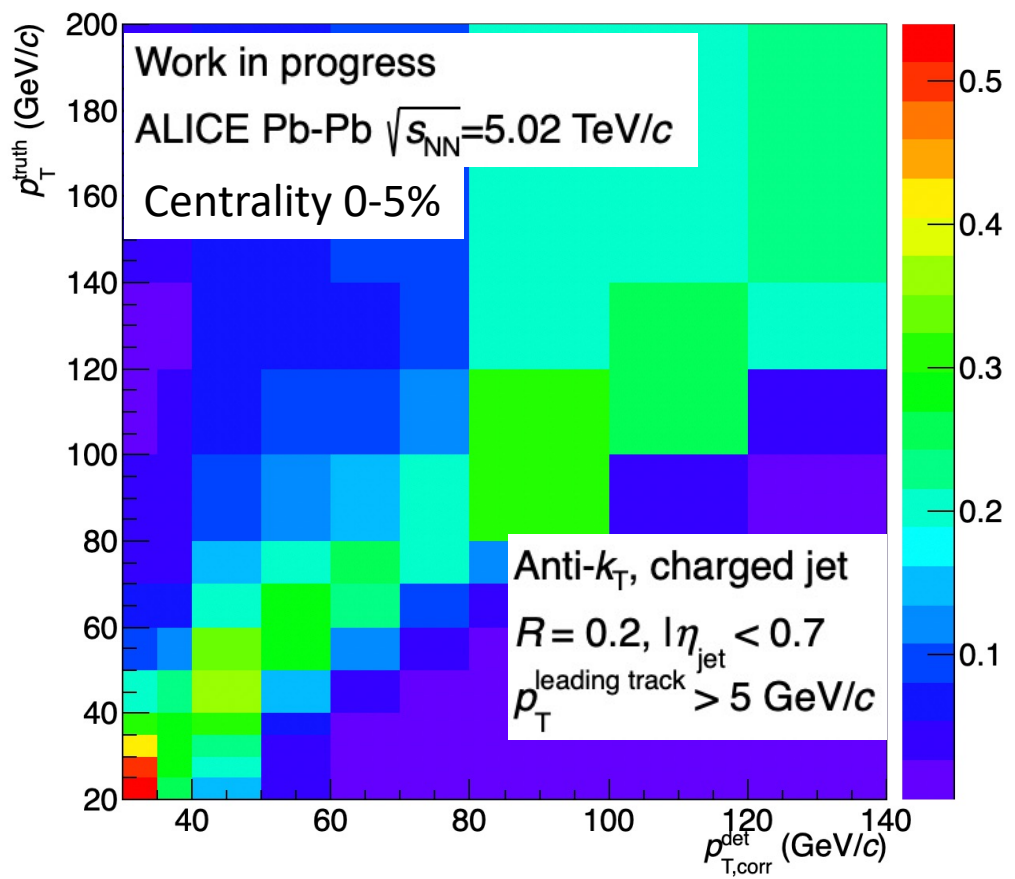
$$\tilde{\chi}^2 = \left(\sum_{n=0}^i \frac{(p_T^{\text{track}} - p_T^{\text{function}})^2}{p_T^{\text{track}}} \right) / (\# \text{ of bins} - 3)$$

of free parameters (ρ_0, v_2, v_3)

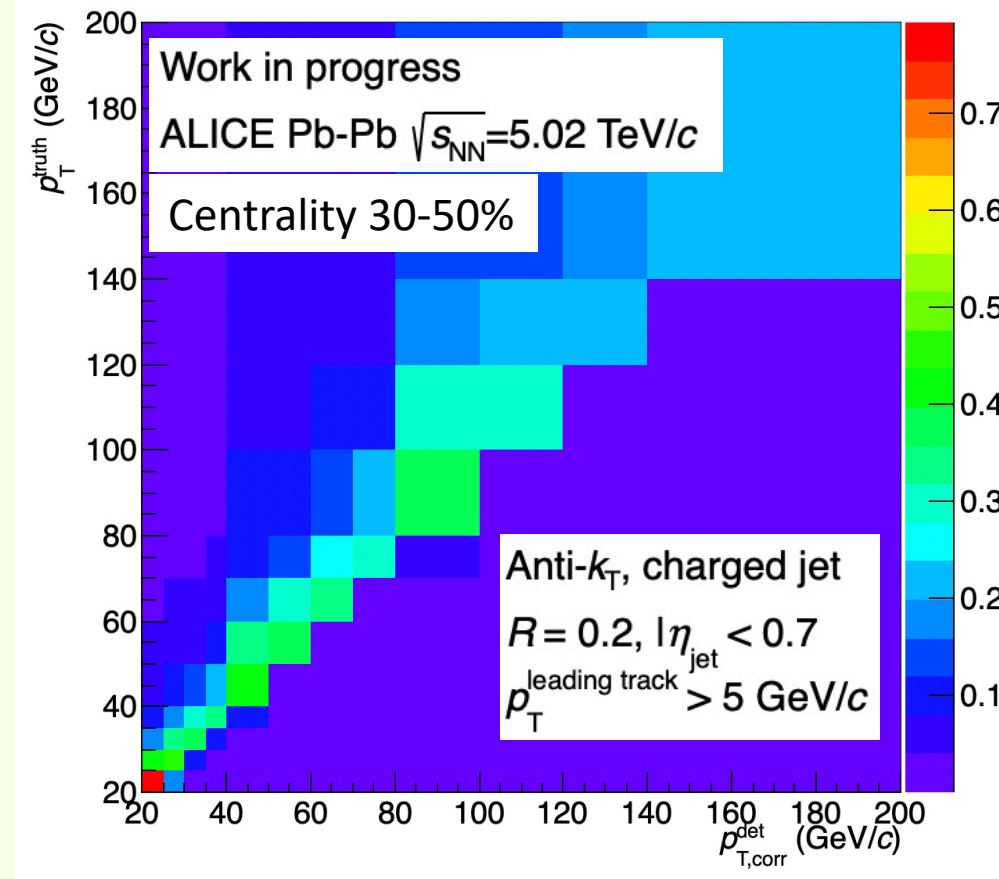
$\tilde{\chi}^2$ is smaller than 1. \rightarrow Fitting quality is good.

Response Matrix

Centrality 0-5%



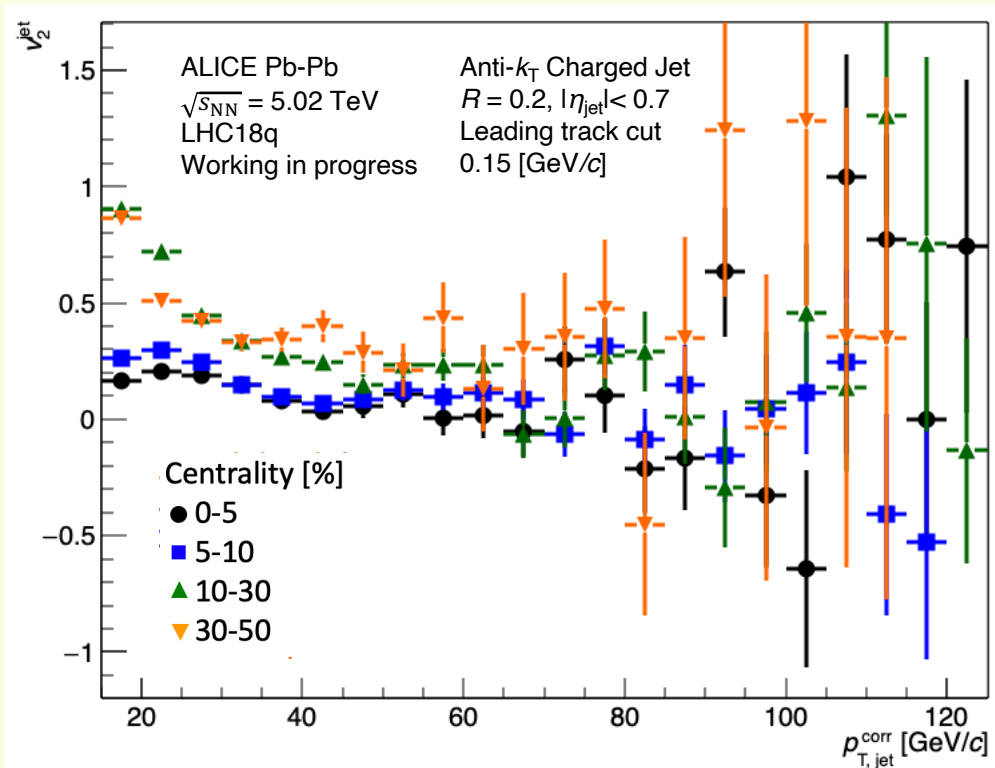
Centrality 30-50%



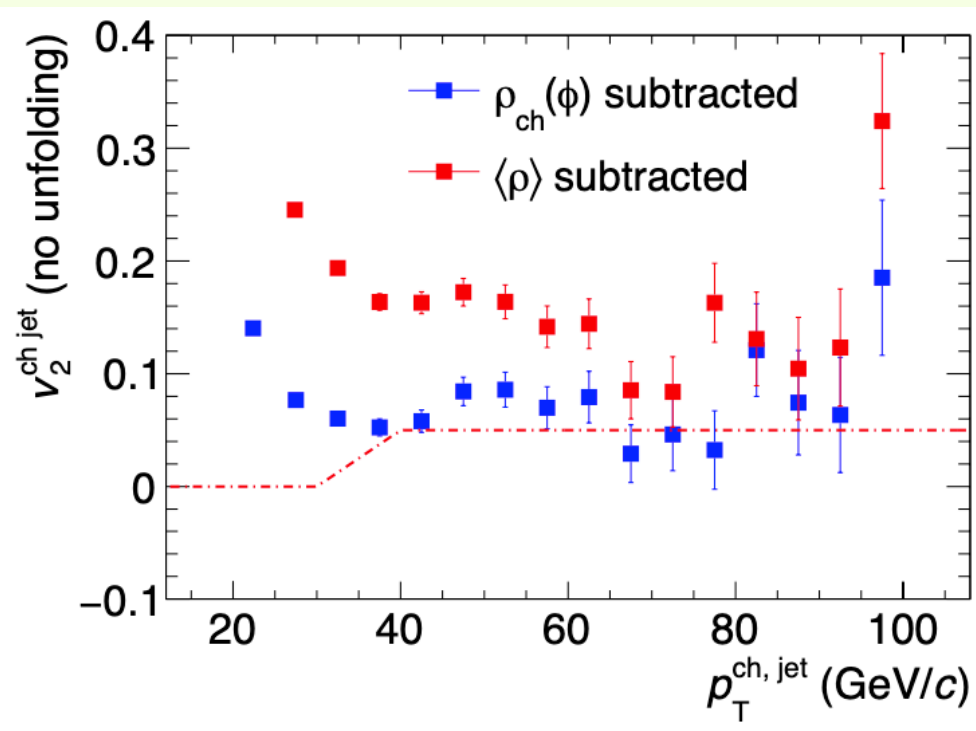
The correlation between particle level and detector level jets seems well.
→ Embedding working well.

Raw charged jet v_2 (R=0.2)

$$v_2^{\text{jet}} = \frac{1}{\text{Res}\{\psi_2^{\text{meas}}\}} \frac{\pi N_{in} - N_{out}}{4 N_{in} + N_{out}}$$



Run1 ($\sqrt{s_{NN}} = 2.76$ TeV) Result (centrality ?)



Value of jet v_2 is close to Run1 ($\sqrt{s_{NN}} = 2.76$ TeV) results.

And the shape around 20 – 60 GeV/c is also similar with Run1 results.

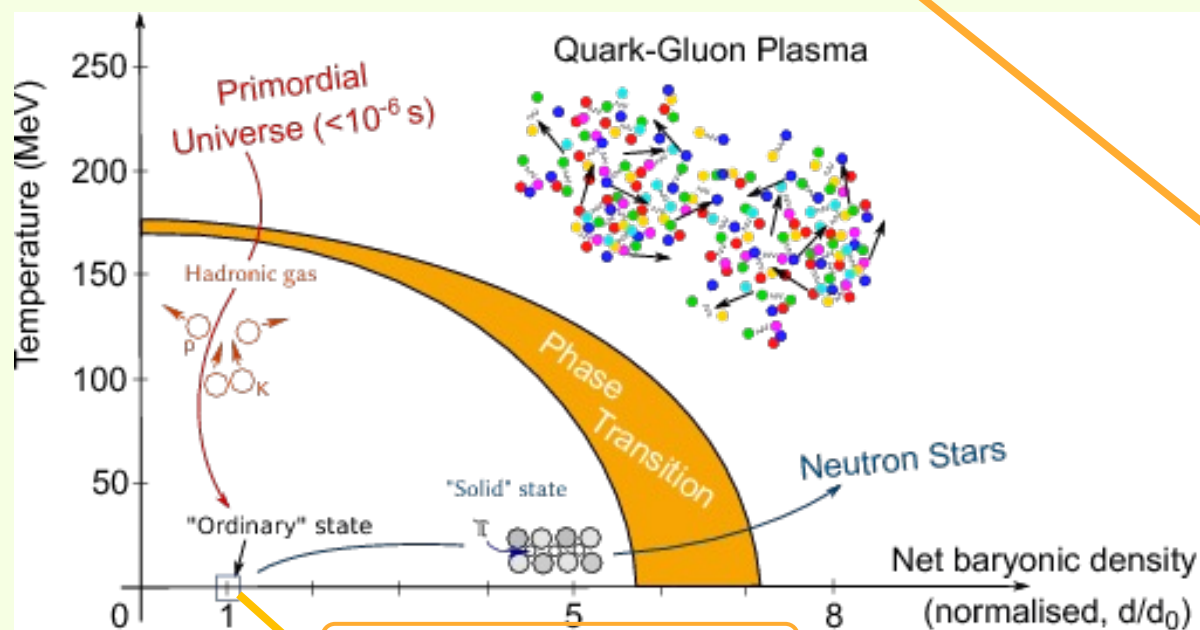
ASW model

- Medium: Gyulassy-Wang model (A center of scattering is stationary, The transfer momentum is about Debye mass(μ))
- Multiple emission: Independent random scattering \rightarrow Poisson distribution
- Emitted gluons: soft

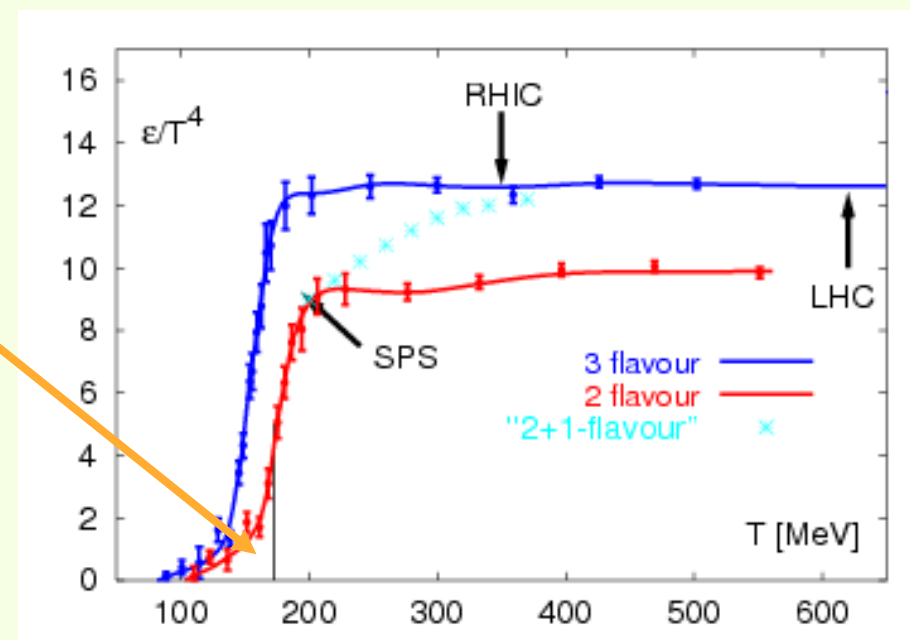
Quark-Gluon Plasma

Quark-Gluon Plasma (QGP) is a state of matter made of deconfined quarks and gluons

- Predicted by QCD theory
- Formed at high temperature and/or density
- QGP has existed in the *early Universe* ($\approx 10^{-6}$ s after the Big Bang)
- Critical temperature $T_C = 173 \pm 15$ MeV, $\epsilon_c \sim 0.7$ GeV/fm³ from Lattice QCD calculations



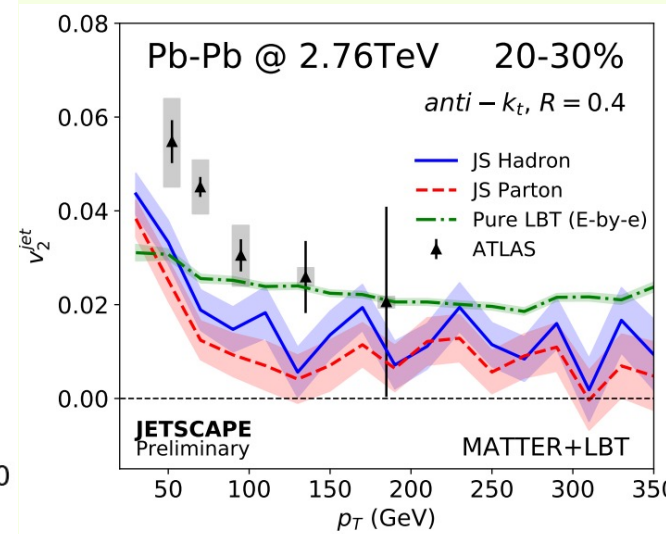
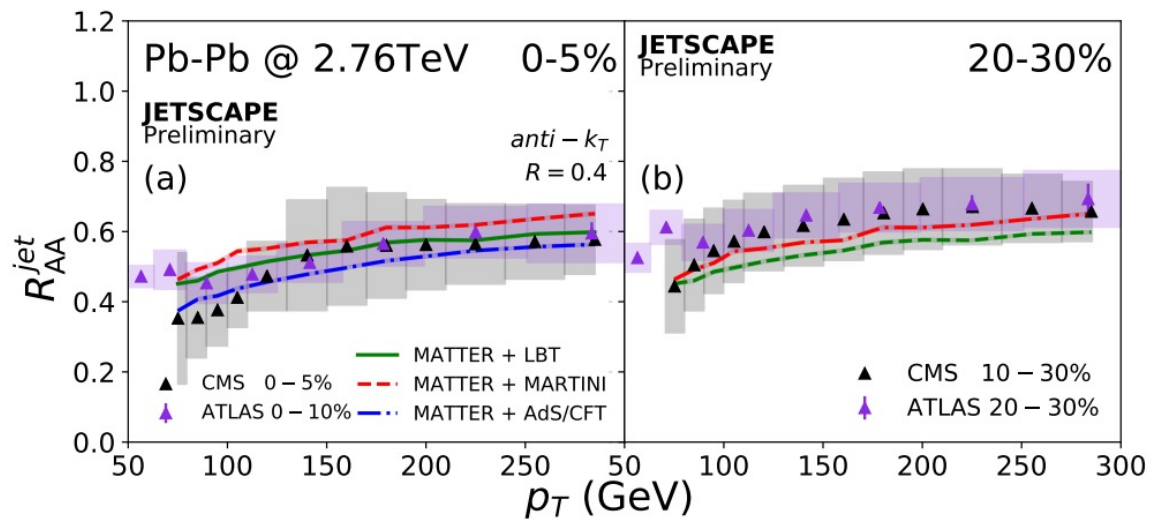
$$\rho_0 \approx 0.15 \text{ GeV}/\text{fm}^3$$



arXiv:1304.1452v1

- **JETSCAPE** (Jet Energy-loss Tomography with a Statistically and Computationally Advanced Program Envelope): <https://arxiv.org/abs/1903.07706>

1. Initial state → 2. Hydrodynamics → 3. Jet energy loss → 4. Hadronization



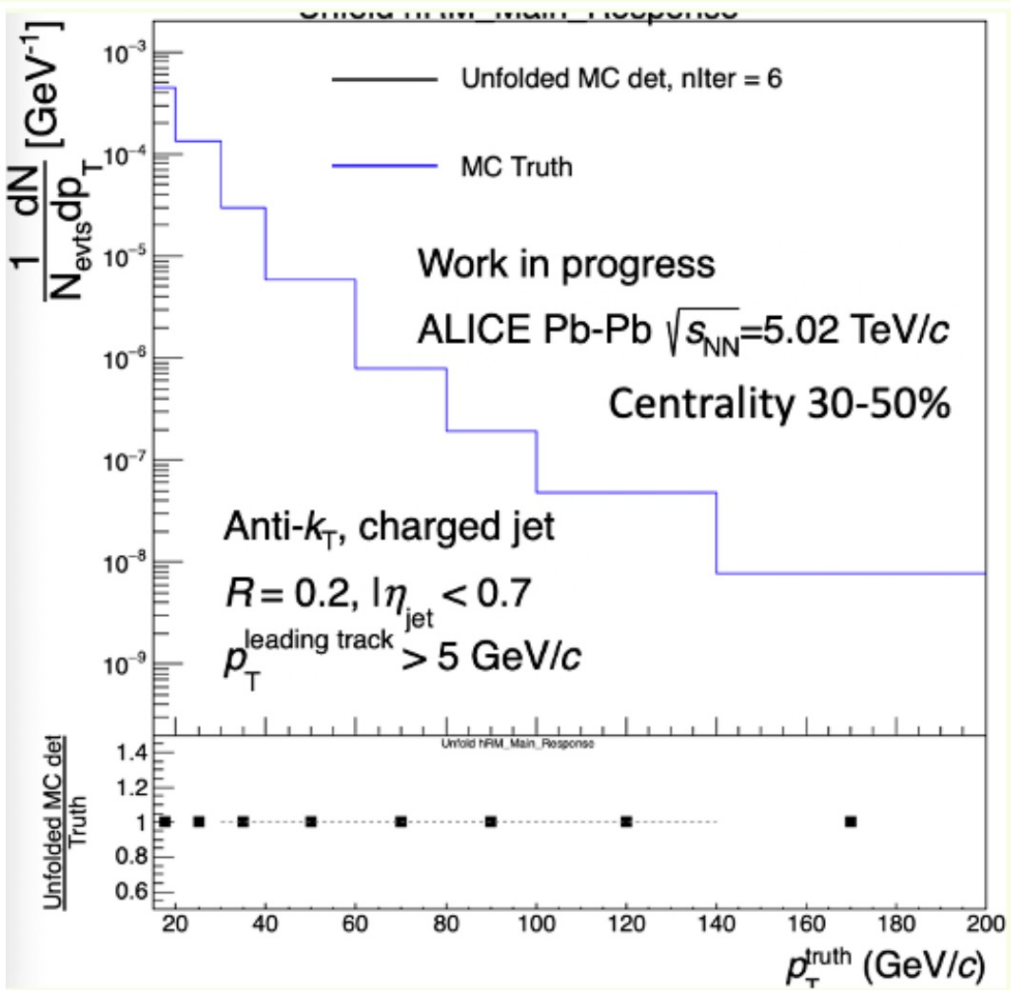
DOI: <https://doi.org/10.22323/1.345.0072>

The preceding study of JETSCAPE shows the jet transport coefficient \hat{q} by comparing the result of R_{AA} in the two centralities of CMS/ATLAS

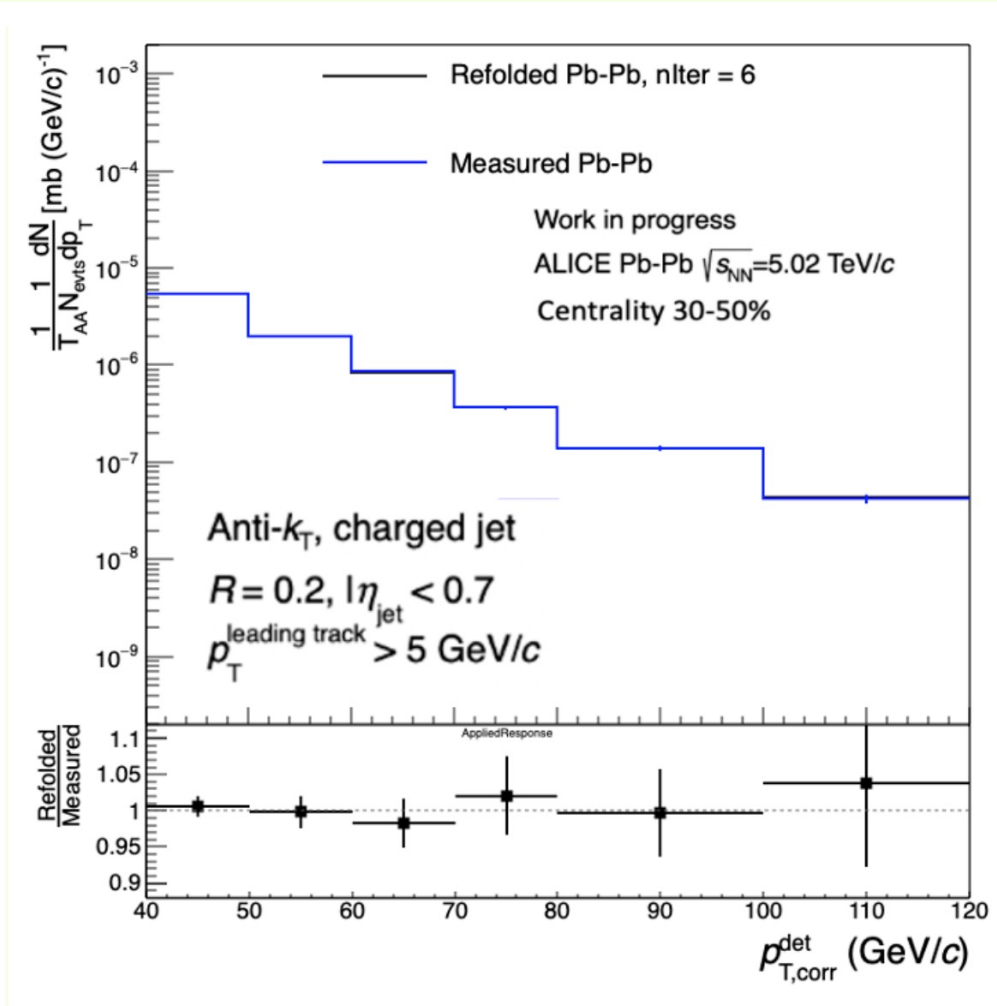
This study will constrain models and give more accurate the \hat{q} value by more various centrality information and low p_T range distribution.

Unfolding QA

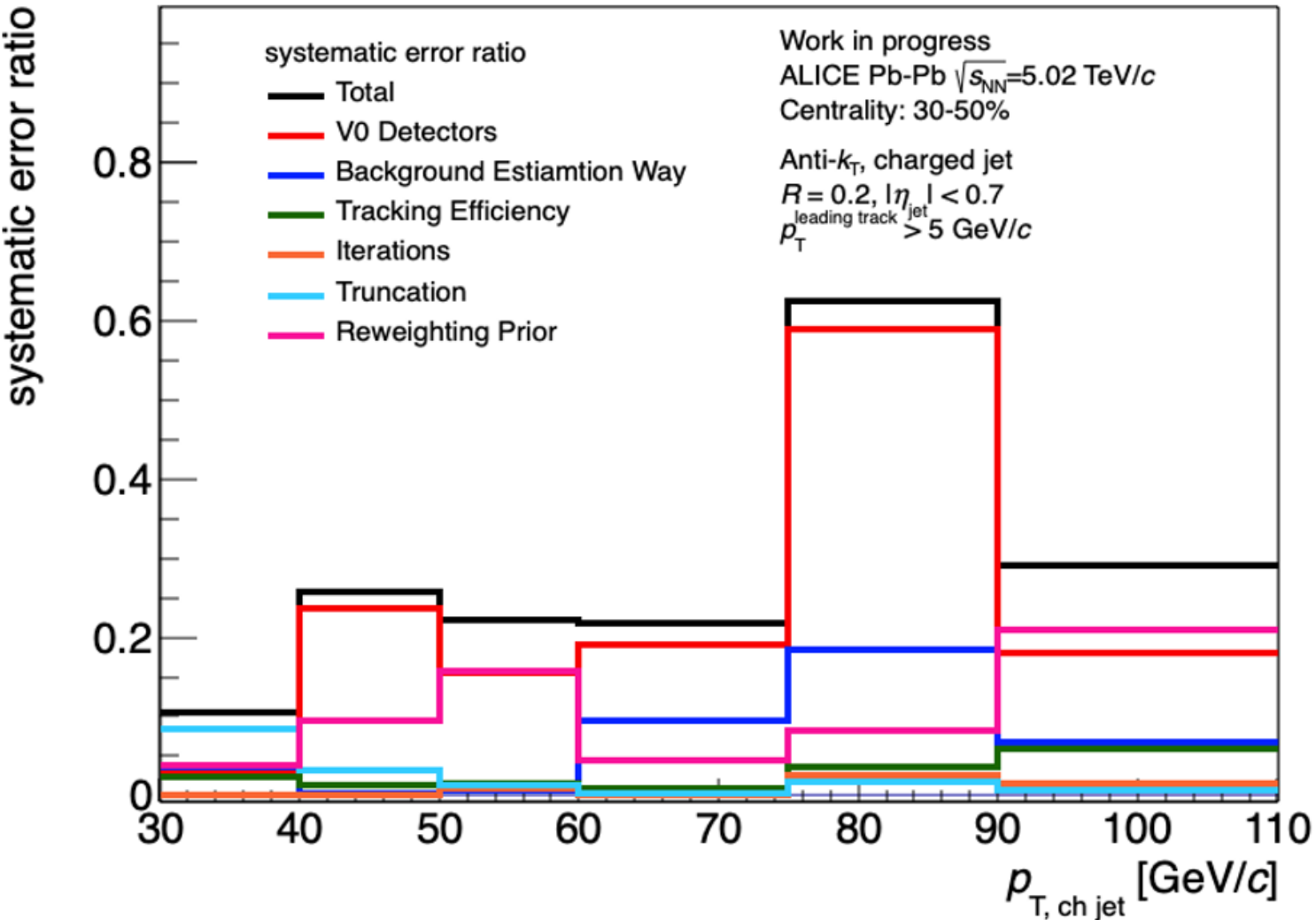
Closure test



ReFolding test



Systematic Error Ratio

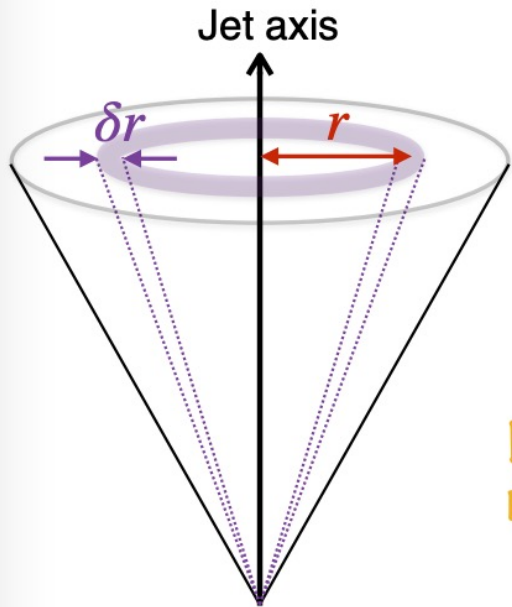


$$- \delta_{sys} = \frac{|obs^{com} - obs^{Nomi}|}{obs^{Nomi}}$$

- For all p_T range, the systematic error is lower than 1.
- The reason of the large error on 80-90 GeV/c is the observable value is very small.

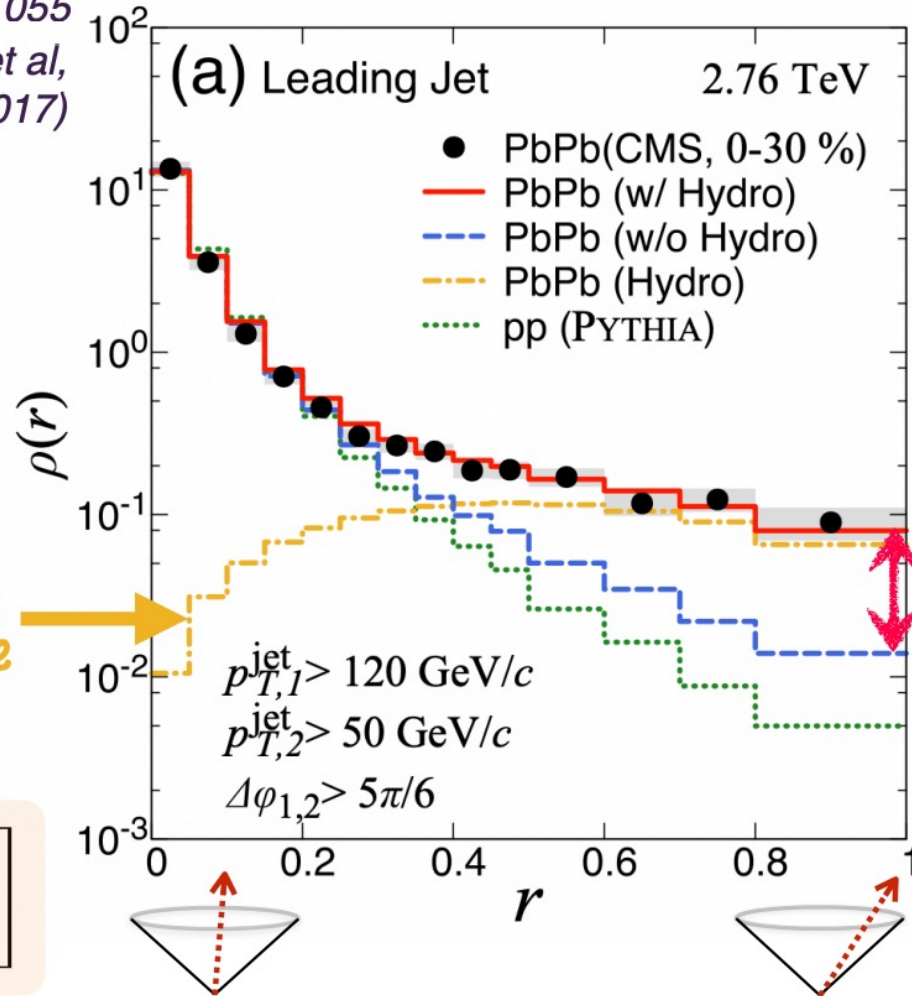
R dependency

CMS JHEP 11 (2016) 055
Y. Tachibana et al,
PRC 95, 044909 (2017)

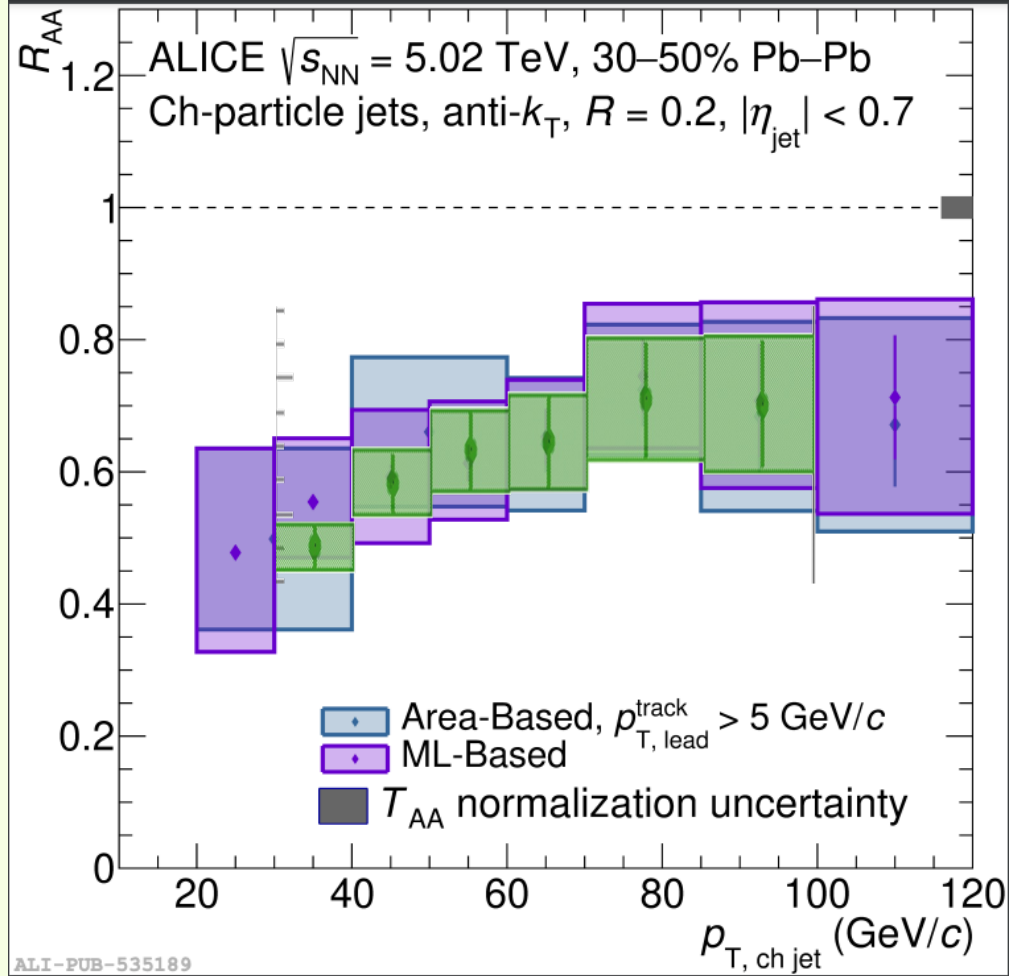


$$\rho_{\text{jet}}(r) = \frac{1}{N_{\text{jet}}} \sum_{\text{jet}} \left[\frac{1}{p_{\text{T}}^{\text{jet}}} \frac{\sum_{\text{trk} \in (r-\delta r/2, r+\delta r/2)} p_{\text{T}}^{\text{trk}}}{\delta r} \right]$$

Medium response

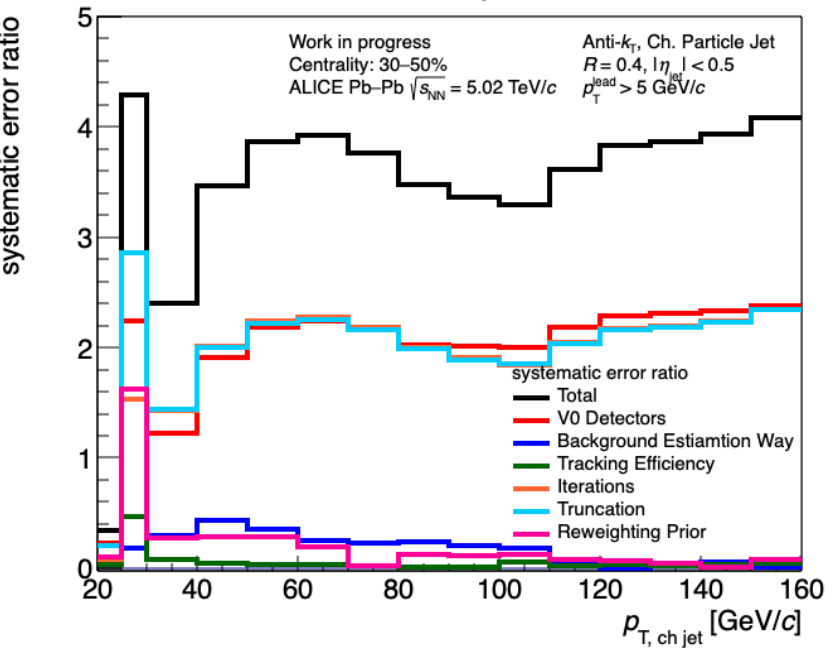
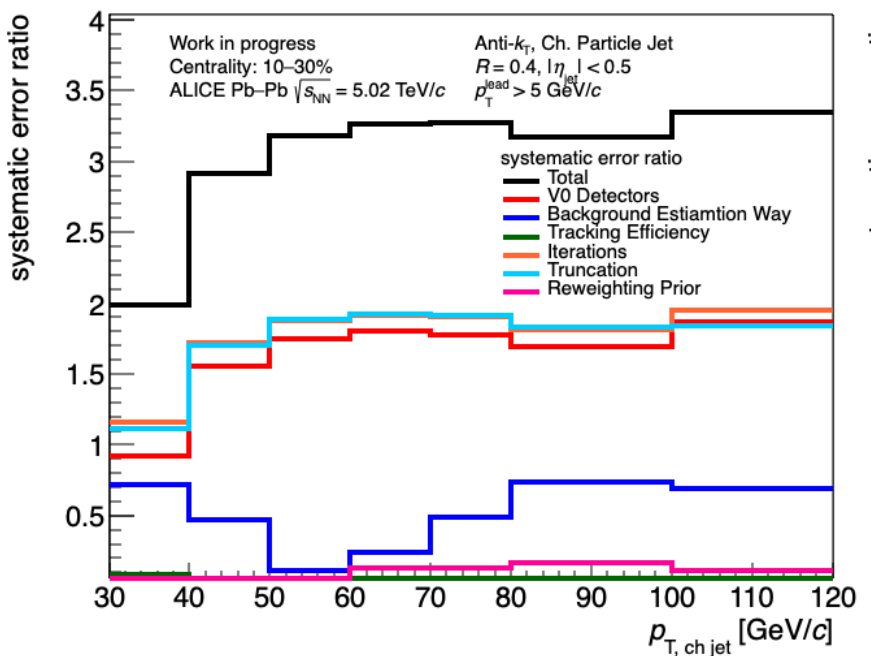
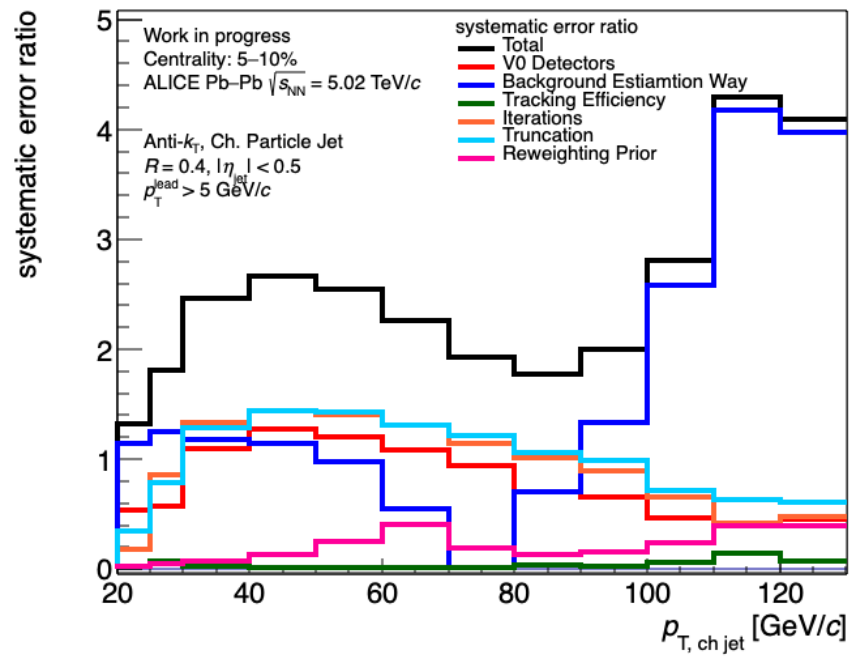


Compare my results of R_{AA} with Hannah analysis results



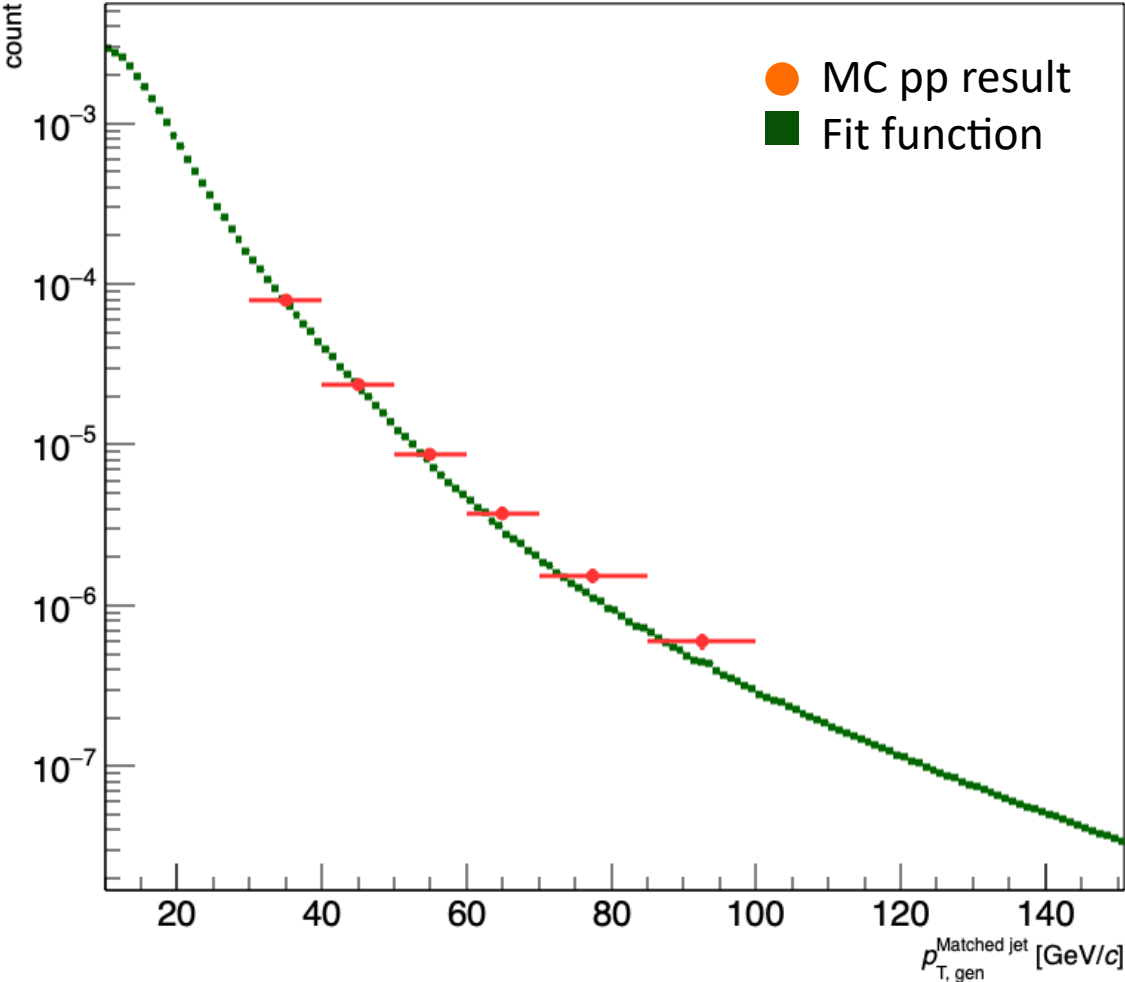
Centrality 30-50% result is consistent with Hannah's result

Systematic uncertainty of $R = 0.4$

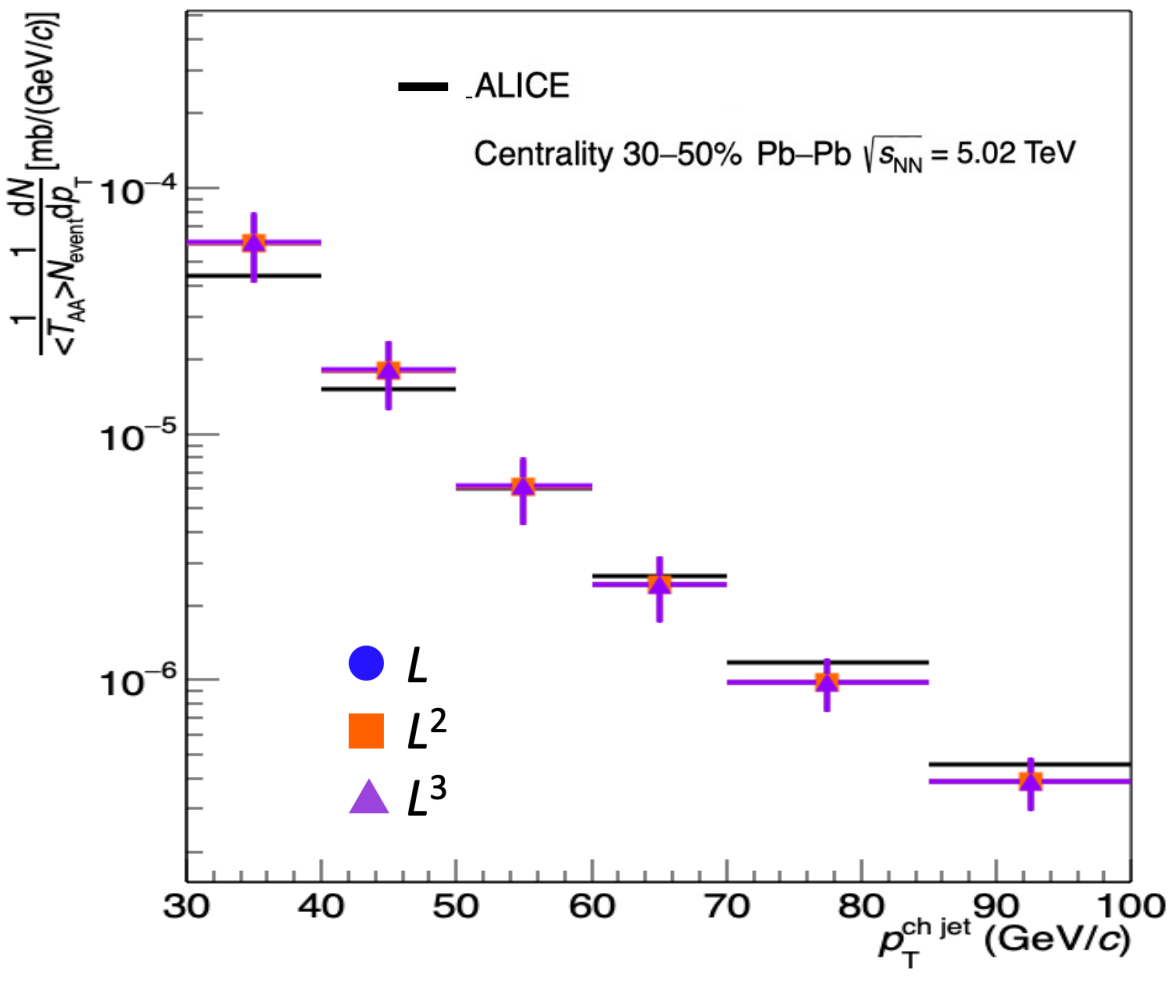


- For all centralities, itelation, V0Detector, and Turnication are very large.
- Background efficiency also too large.

Simulation fitting to data results

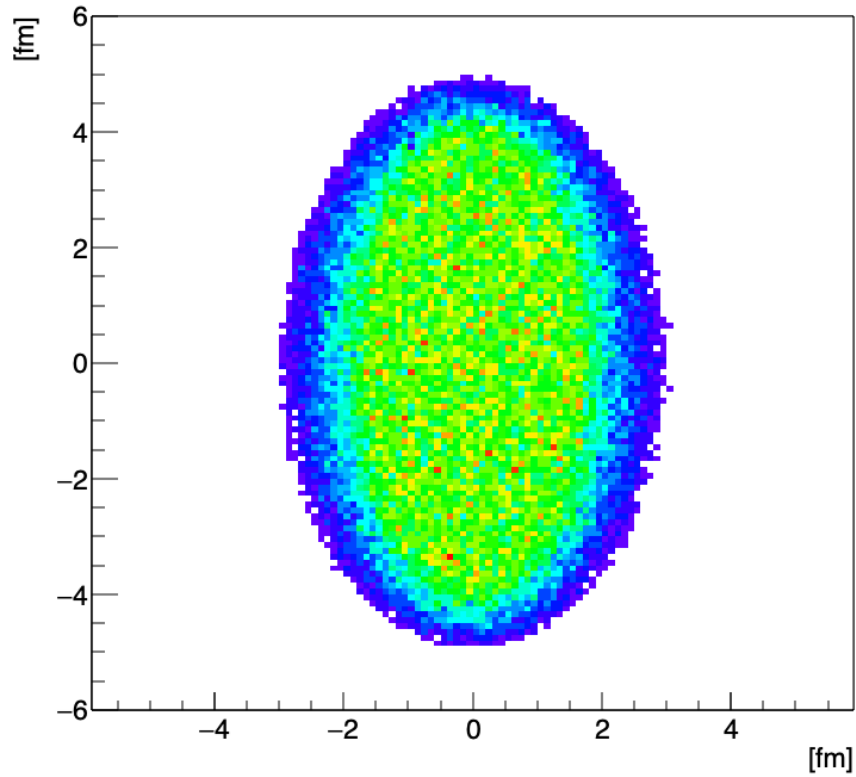


pp jet p_T distribution

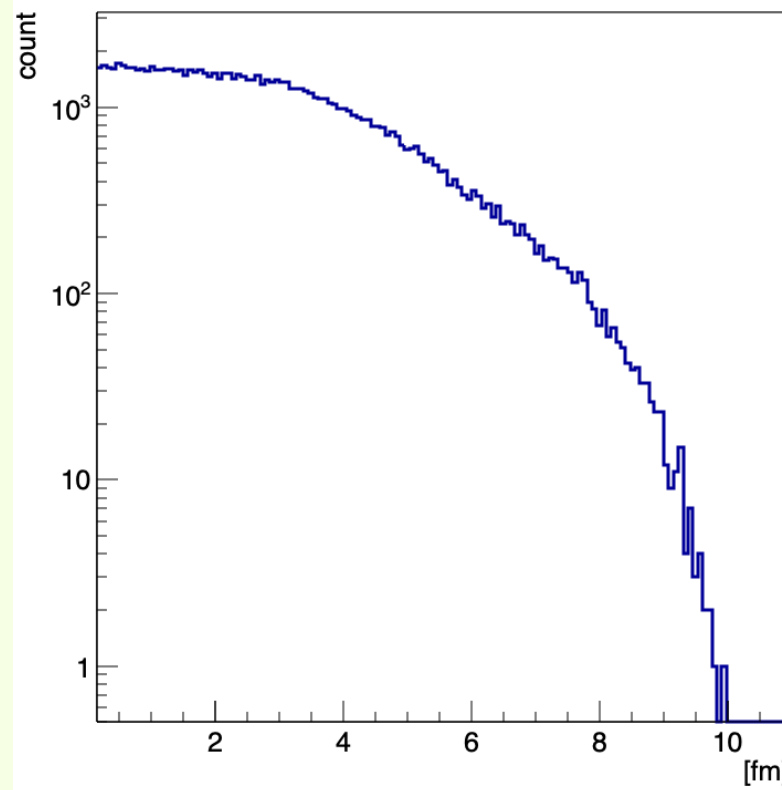


Fit dispersed model p_T distribution to data PbPb one to determine energy loss coefficient

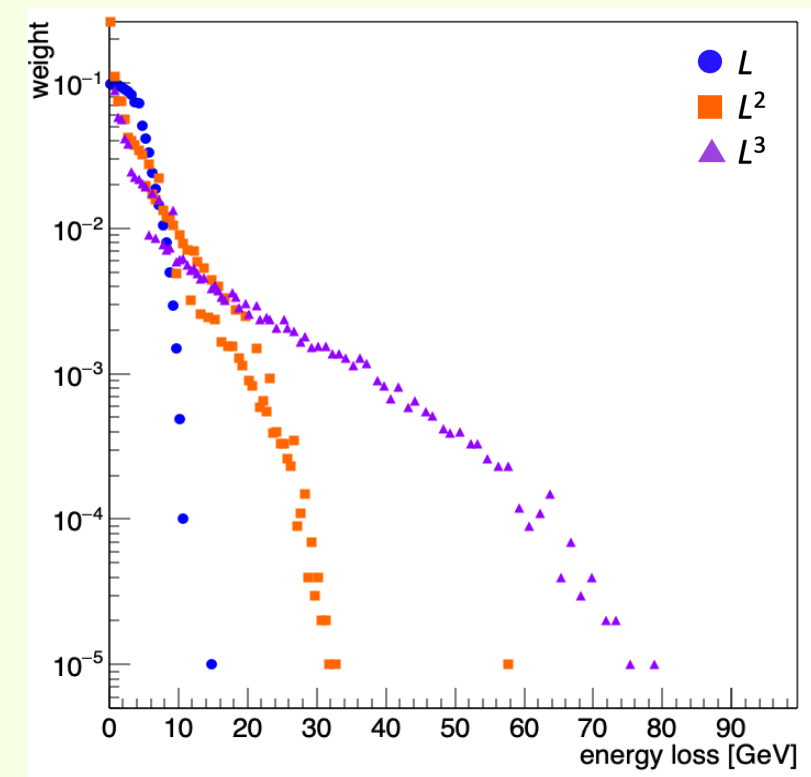
Progress figures



Parton creation points
(Centrality 30-50%)



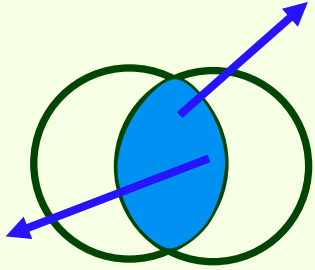
Path length distribution



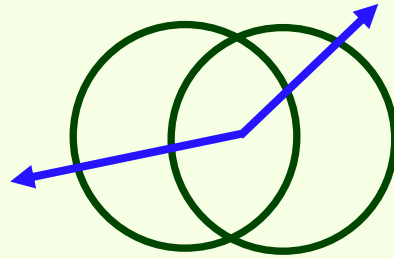
Energy loss distribution for
each toy model ($dE = CL^n$)

Results comparison of different parton emission way

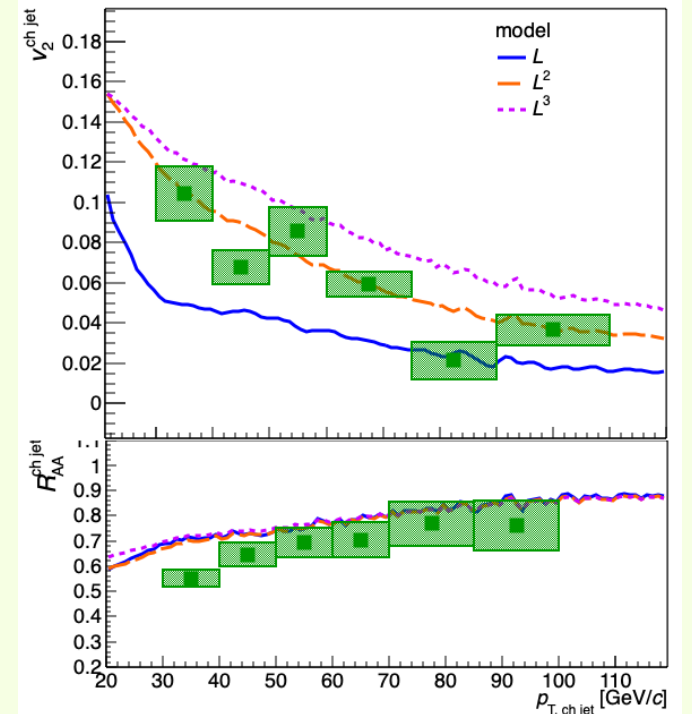
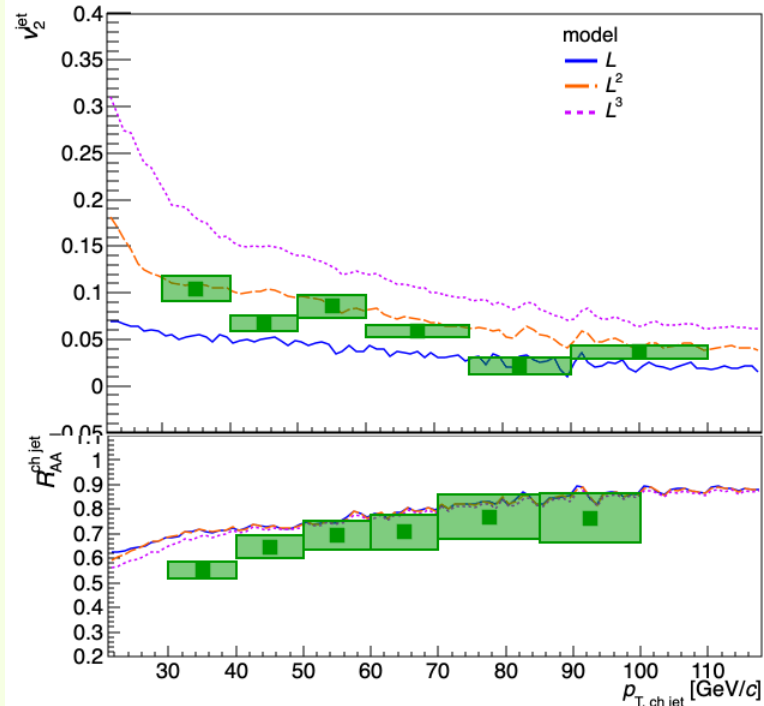
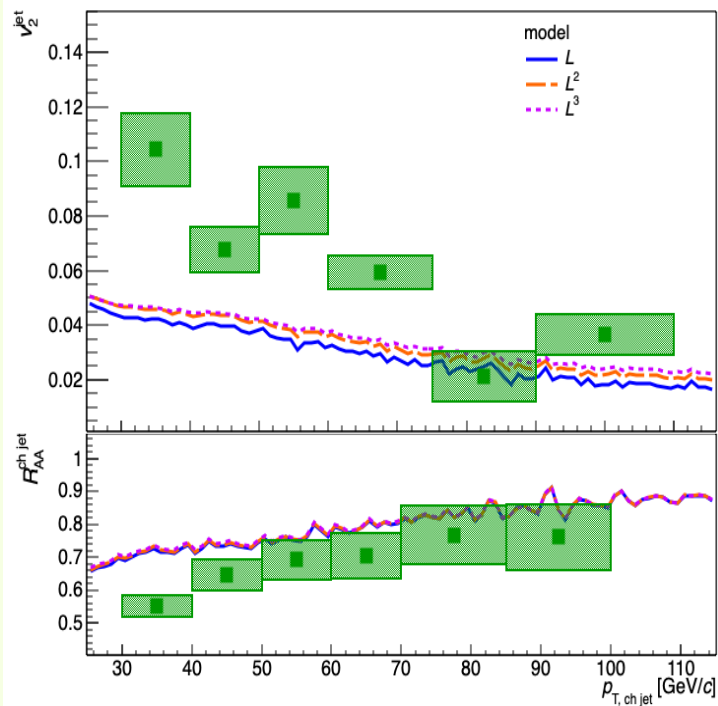
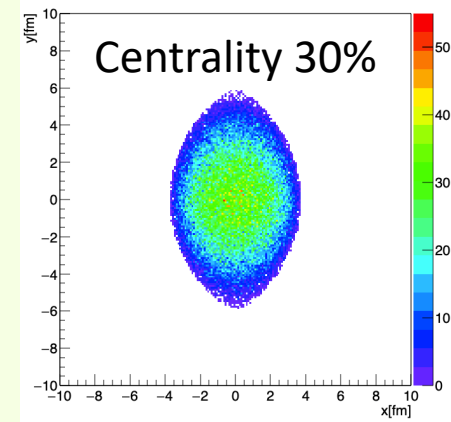
Use MC pp distribution, for model R_{AA} distribution

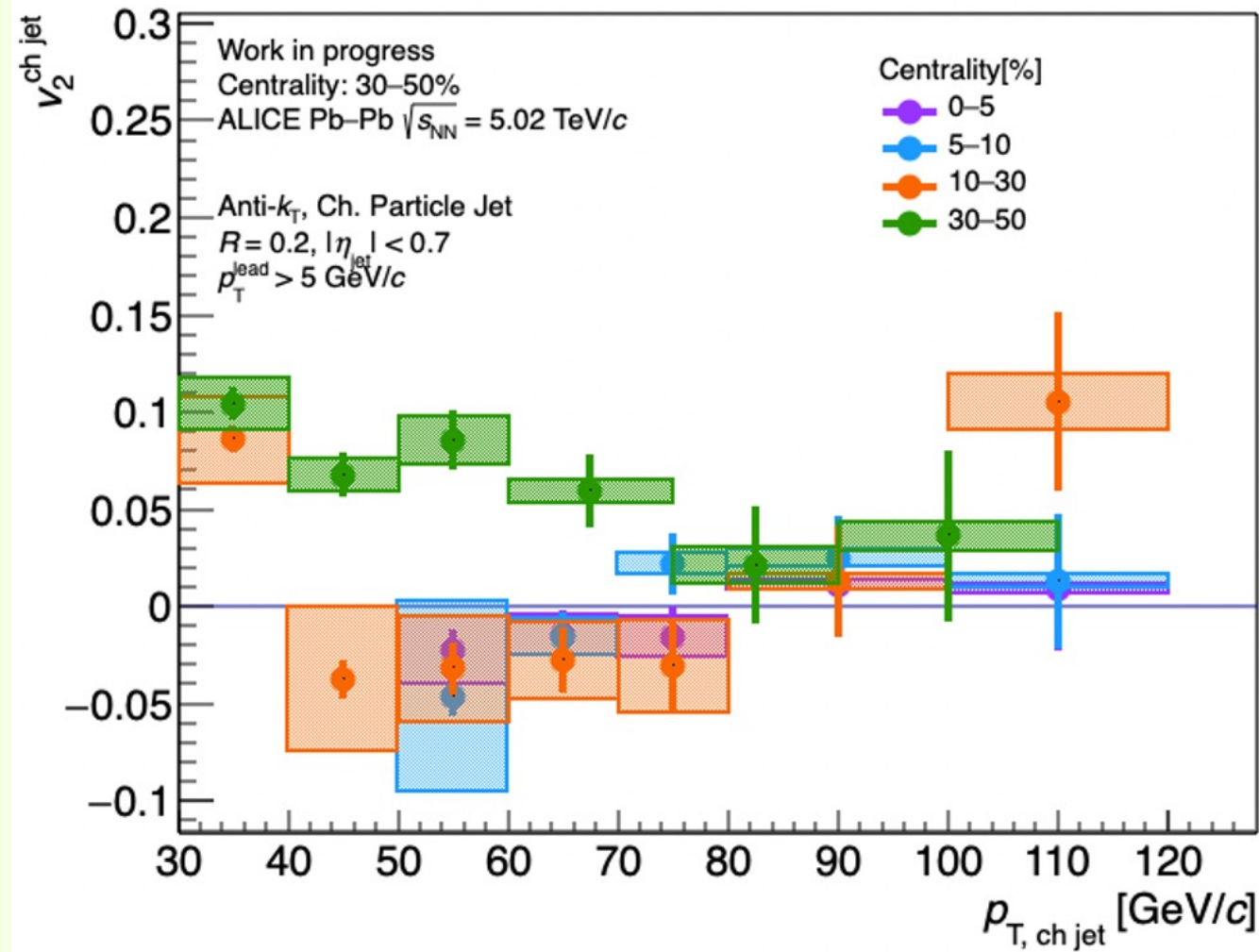


Flat parton creation



Fix center parton creation





\hat{q} Evaluation

$$\Delta E \propto \alpha_s C_R \hat{q} L^n$$

$$\Delta E = CL^n$$

$$0.3 < \alpha_s < 0.5 \rightarrow \alpha_s = 0.5$$

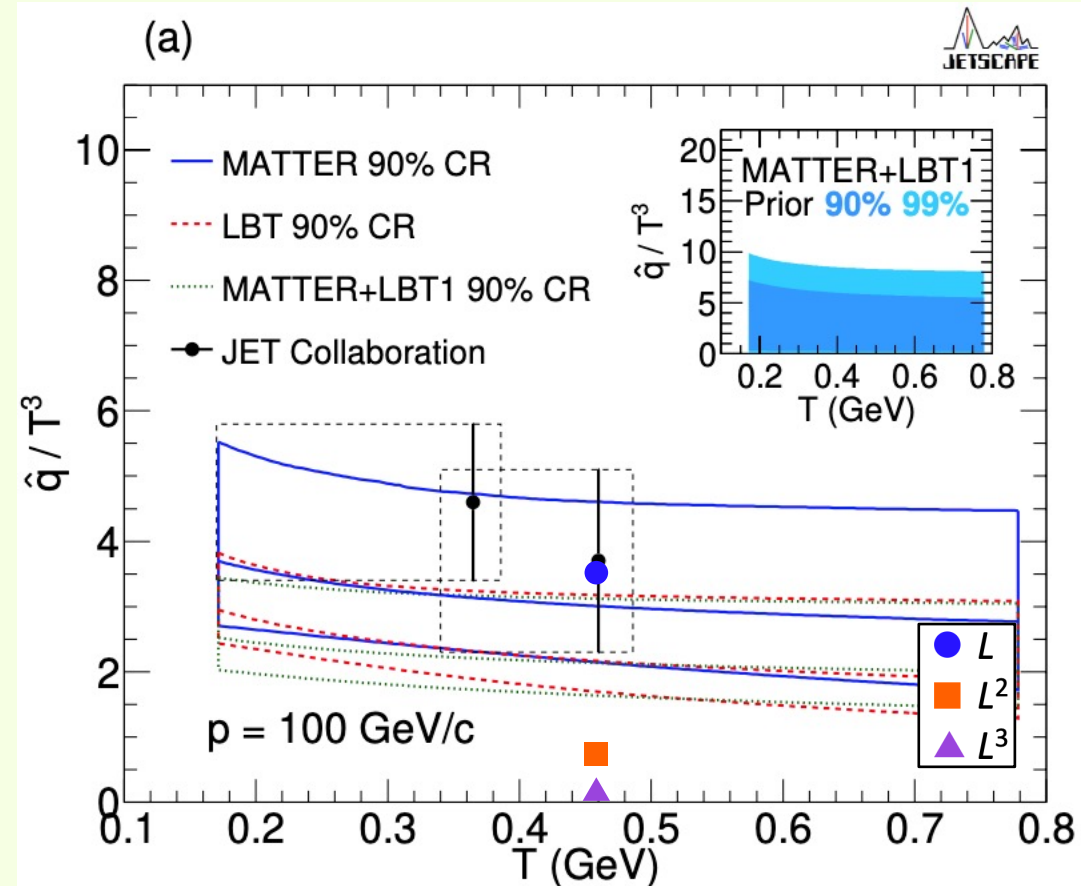
$$C_R = \begin{cases} q: 4/3 \\ g: 3 \end{cases}$$

$$\alpha_s C_R = 1.5$$

$$C = \begin{cases} 1.125 \text{ (collisional)} \\ 0.225 \text{ (radiation)} \\ 0.040 \text{ (Ads/CFT)} \end{cases}$$

$$\hat{q} = \begin{cases} 0.75 \text{ (collisional)} \\ 0.15 \text{ (radiation)} \\ 0.027 \text{ (Ads/CFT)} \end{cases}$$

$$\hat{q}/T^3 = \begin{cases} 3.47 \text{ (collisional)} \\ 0.694 \text{ (radiation)}, (T^3 = 0.216) \\ 0.125 \text{ (Ads/CFT)} \end{cases}$$



<https://doi.org/10.1103/PhysRevC.104.024905>

\hat{q} Estimation

$$\Delta E \propto \alpha_s C_R \hat{q} L^n$$

$$\Delta E = CL^n$$

$$C = \begin{cases} 1.695(\text{collisional}) \\ 0.46(\text{raiation}) \\ 0.12(\text{Ads/CFT}) \end{cases}$$

$$0.3 < \alpha_s < 0.5 \rightarrow \alpha_s = 0.5$$

$$C_R = \begin{cases} q: 4/3 \\ g: 3 \end{cases}$$

$$\alpha_s C_R = 1.5$$

$$\hat{q} = \begin{cases} 1.13 - 4.24(\text{collisional}) \\ 0.31 - 1.15(\text{raiation}) \\ 0.08 - 0.30(\text{Ads/CFT}) \end{cases}$$

$$\hat{q}/T^3 = \begin{cases} 11.6 - 43.5(\text{collisional}) \\ 3.15 - 11.8(\text{raiation}), (T = 0.46) \\ 0.82 - 3.08(\text{Ads/CFT}) \end{cases}$$

min q-hat: col, radi, AdsCft = 4.2375, 1.15, 0.3

max q-hat: col, radi, AdsCft = 1.13, 0.306667, 0.08

min q-hat/T^3: col, radi, AdsCft = 43.5348, 11.8147, 3.08211

max q-hat/T^3: col, radi, AdsCft = 11.6093, 3.1506, 0.821895

