



# Perturbative Reheating & Thermalization

via cascades of energetic SM particles

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w/ K.Harigaya, M.He, K.Kohri, M.Yamada

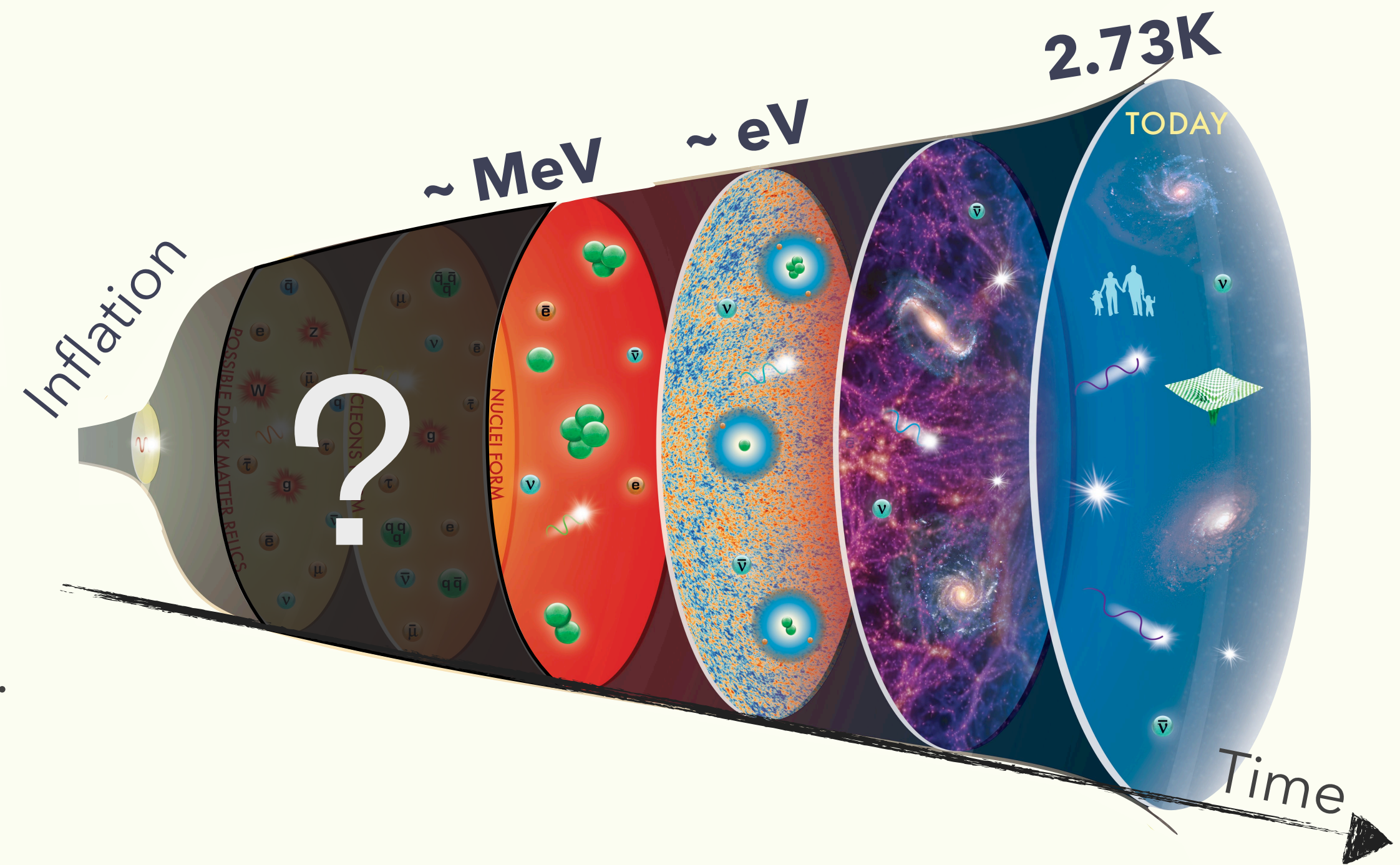
1312.3097, 1402.2846, 1901.11027,

**2208.11708, 2402.14054, 2407.15926**

# Introduction

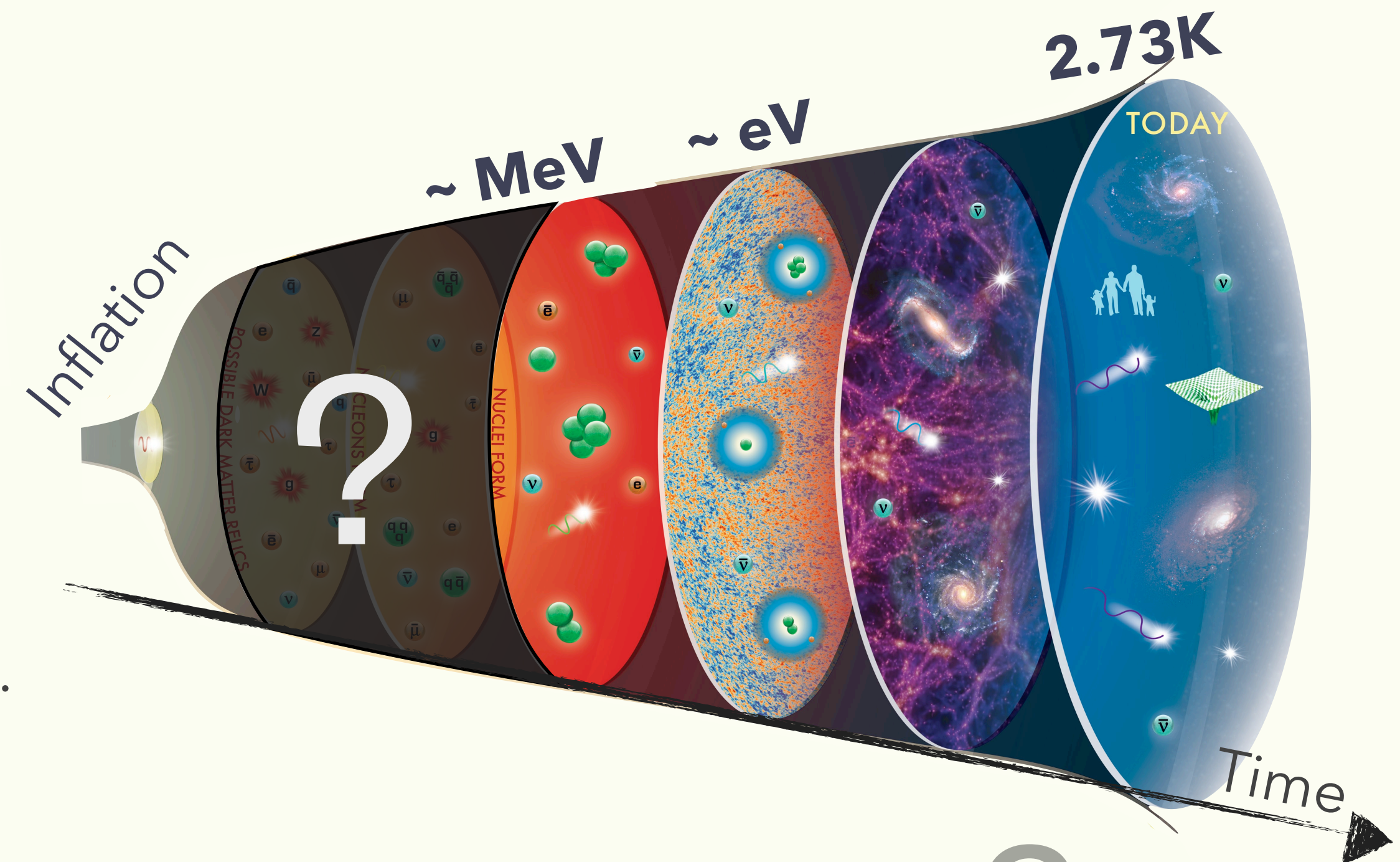
# Beginning of Hot Universe?

- Cosmic inflation (accelerated expansion)
  - Solves Horizon/Flatness problem
  - Provides the origin of density fluctuations
- © **Dilutes everything** including baryons, dark matter...



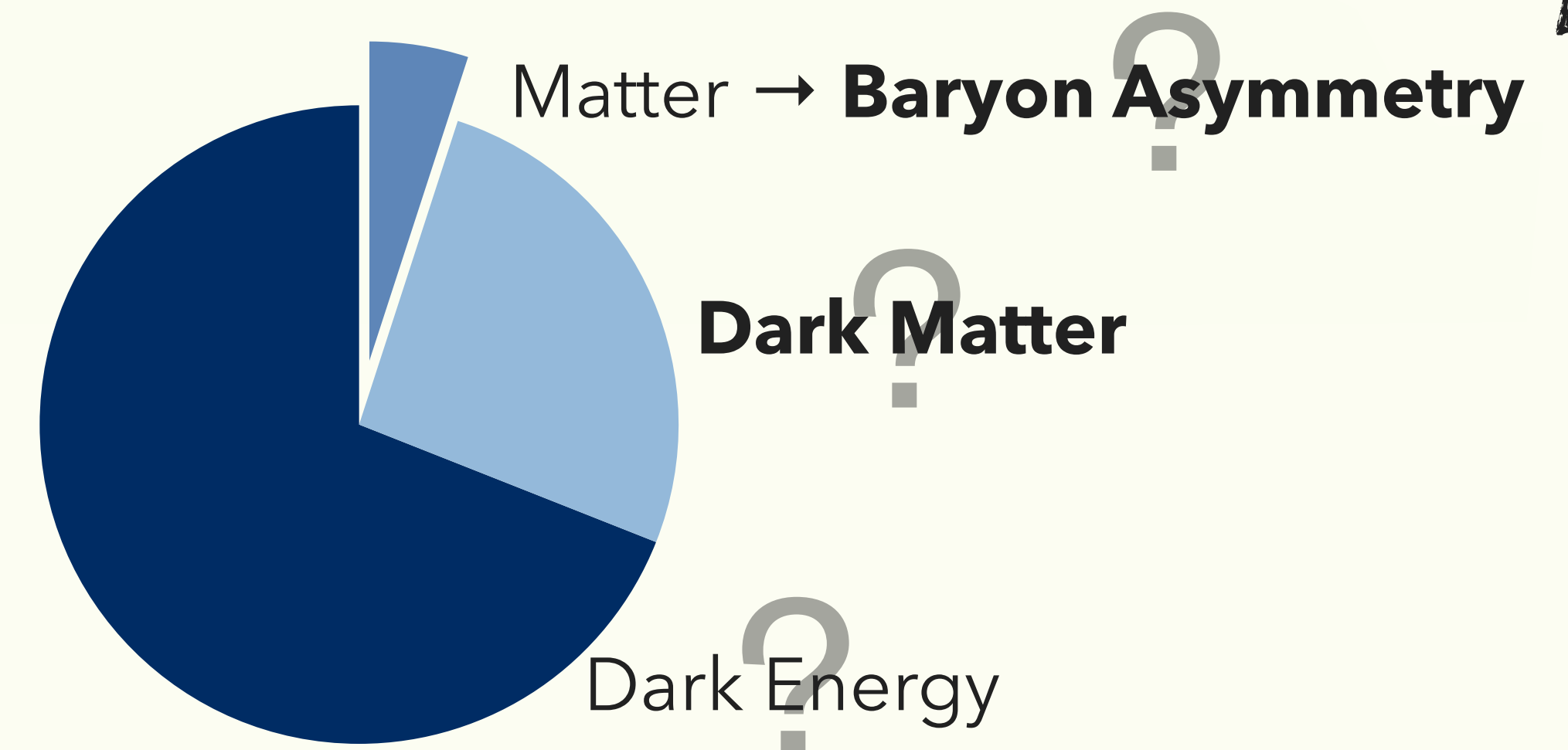
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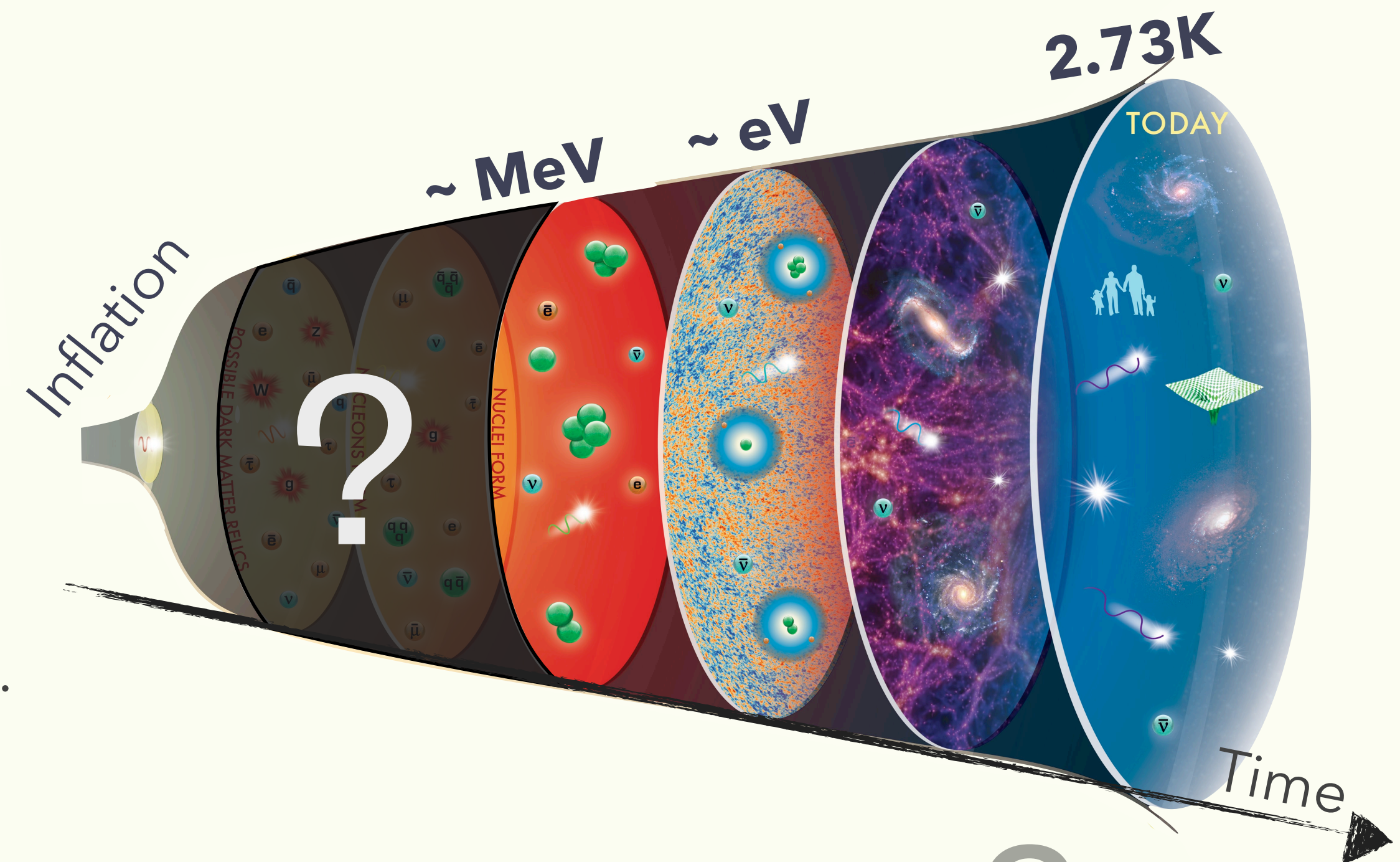
## Hot Universe

- Big Bang Nucleosynthesis
- Cosmic Microwave Background

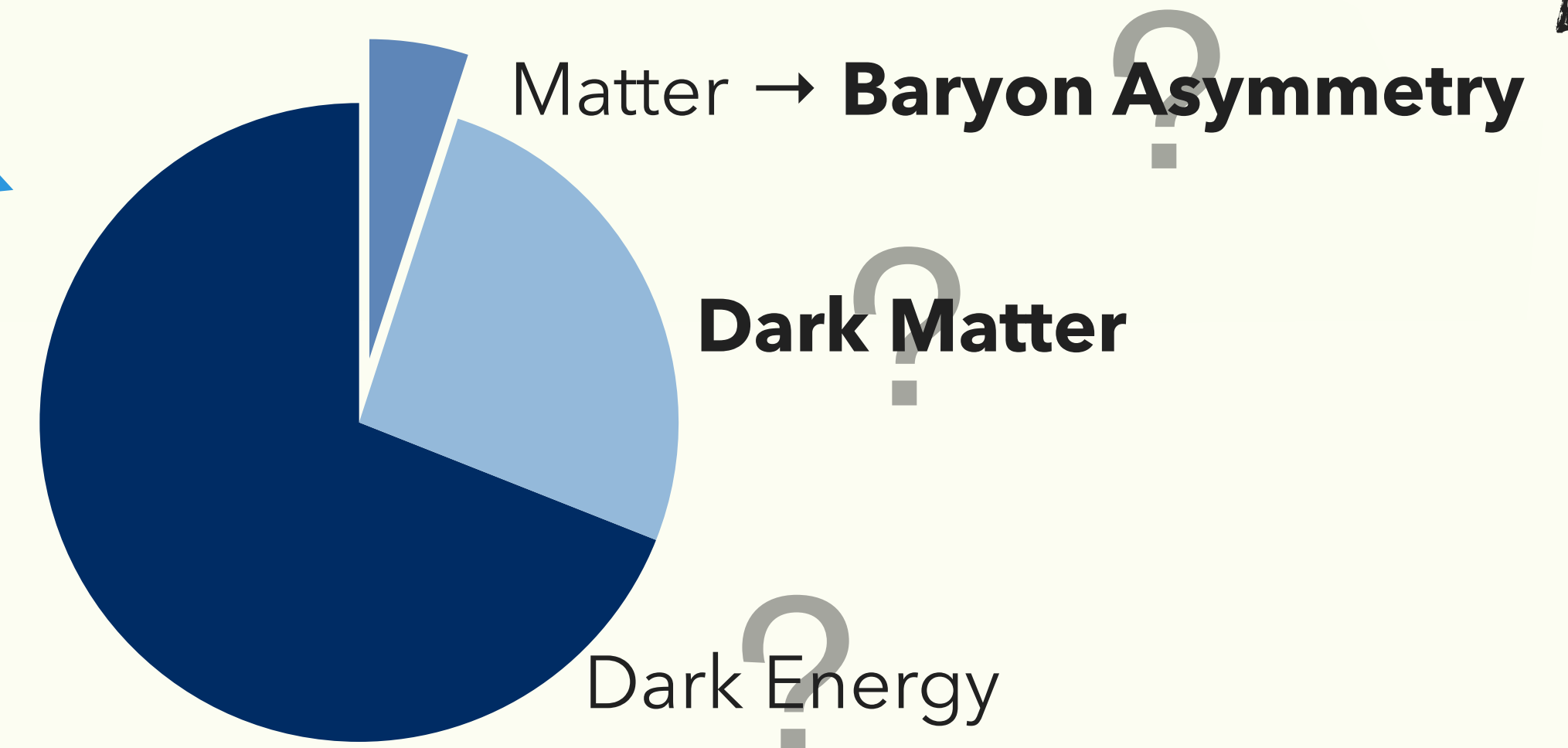


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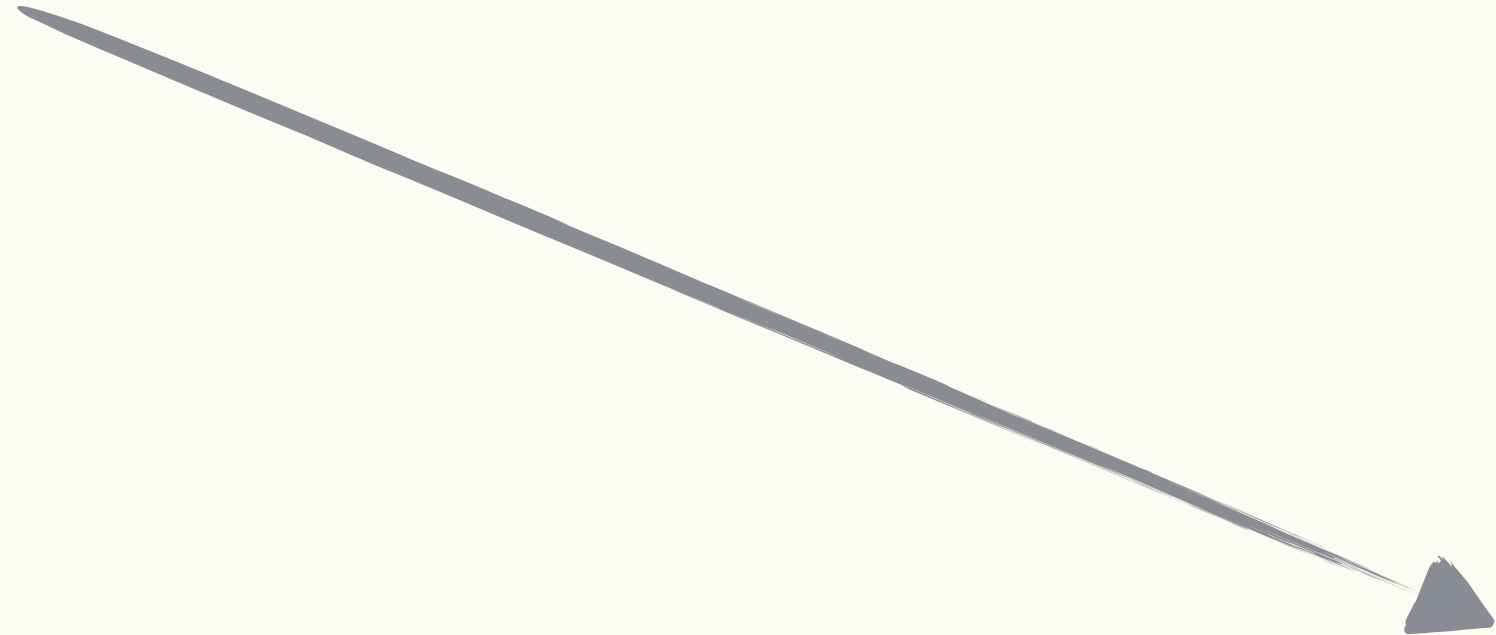
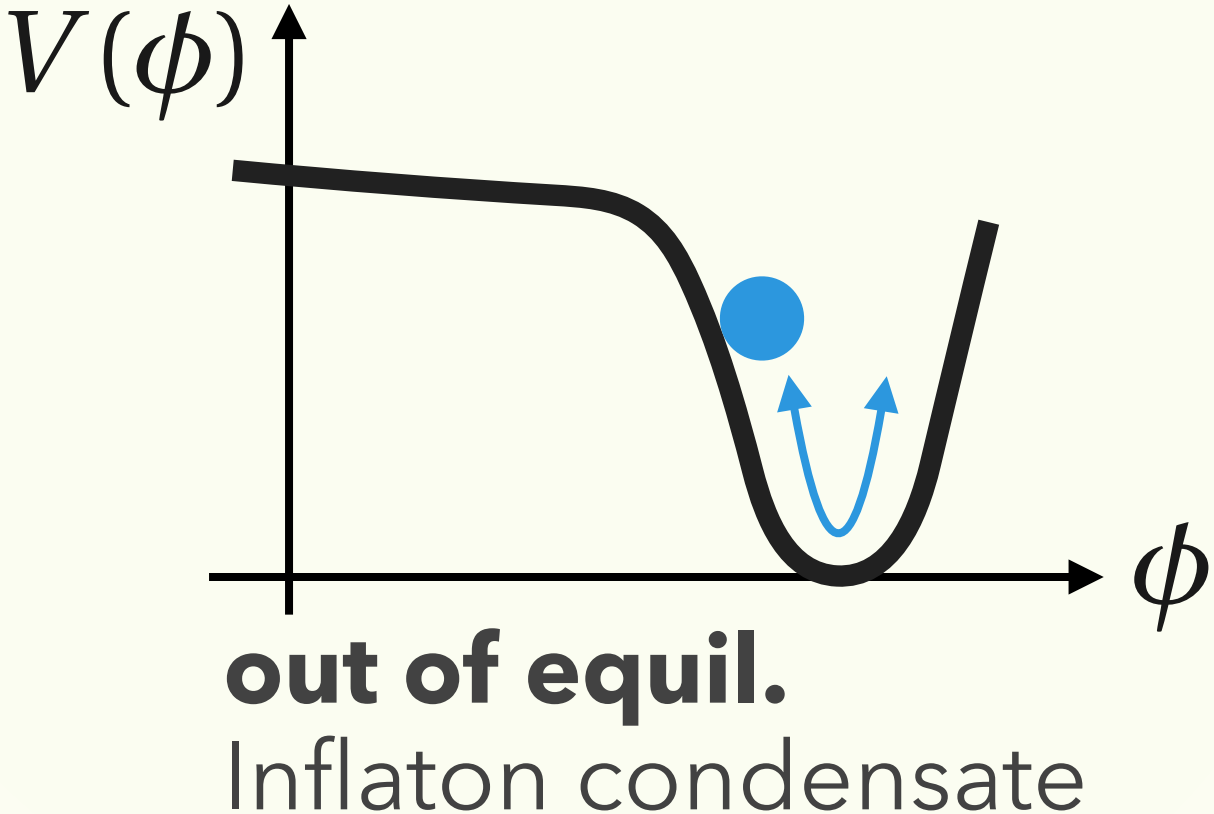
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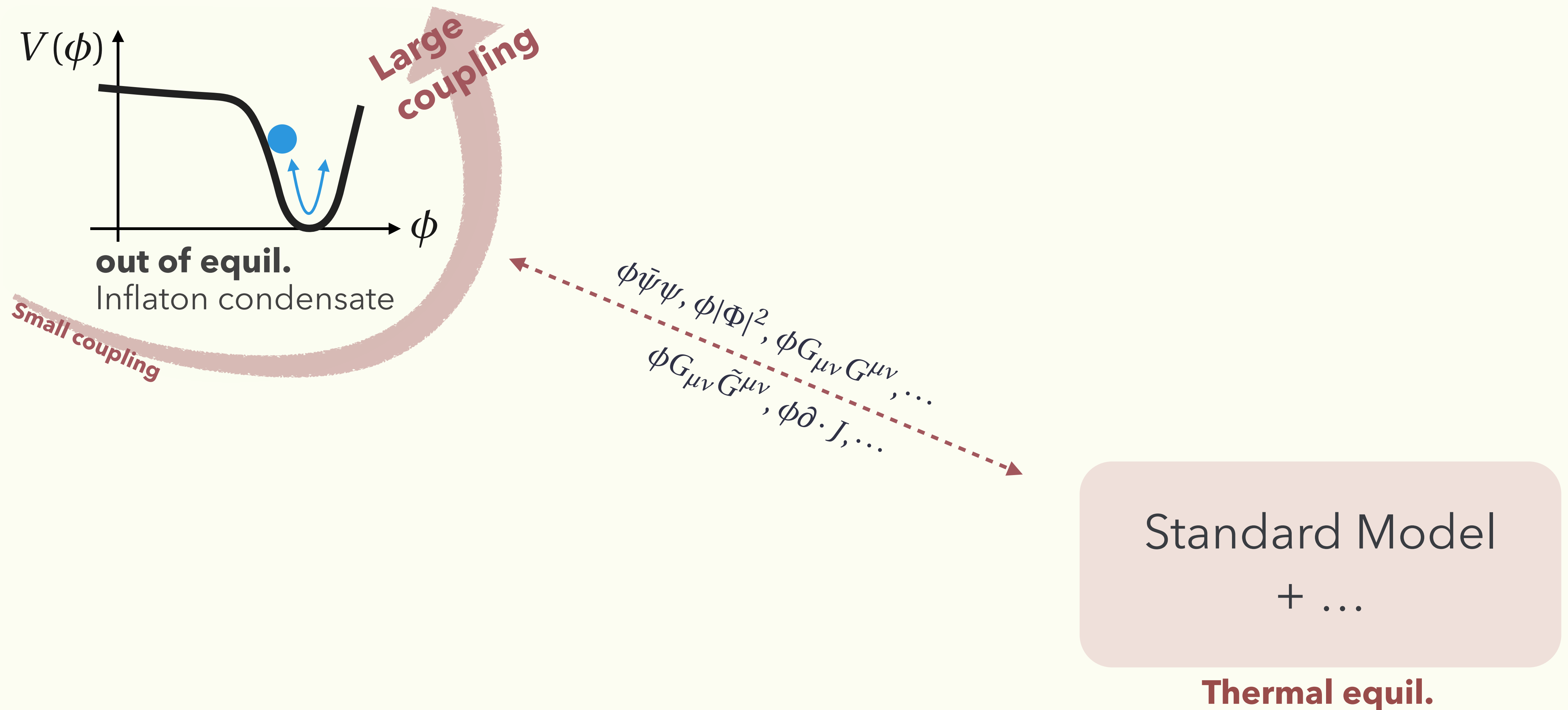
# Reheating and Thermalization



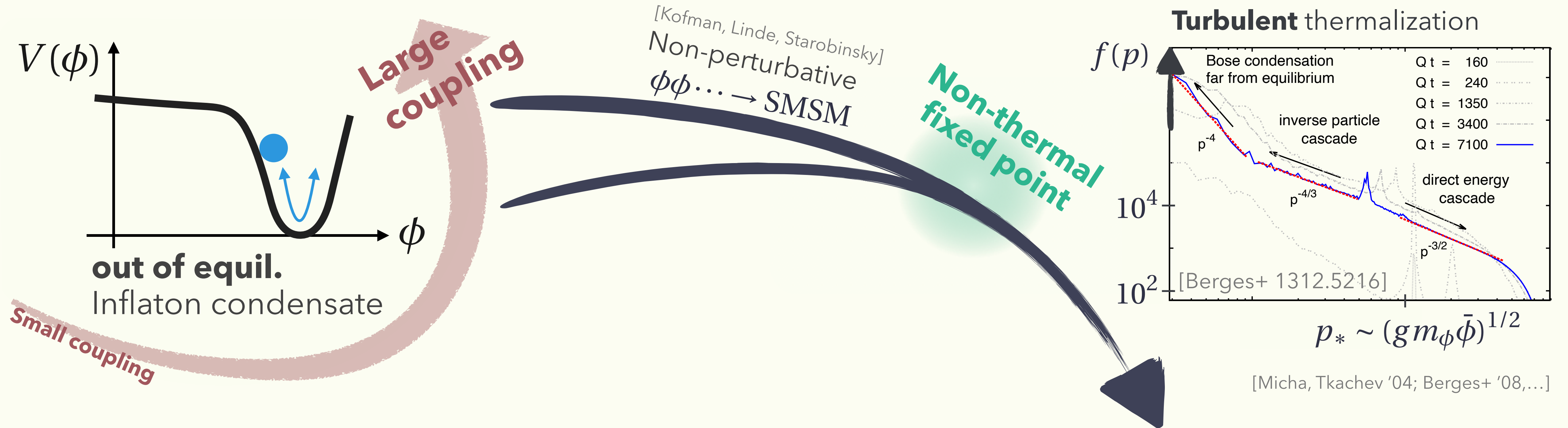
Standard Model  
+ ...

**Thermal equil.**

# Reheating and Thermalization



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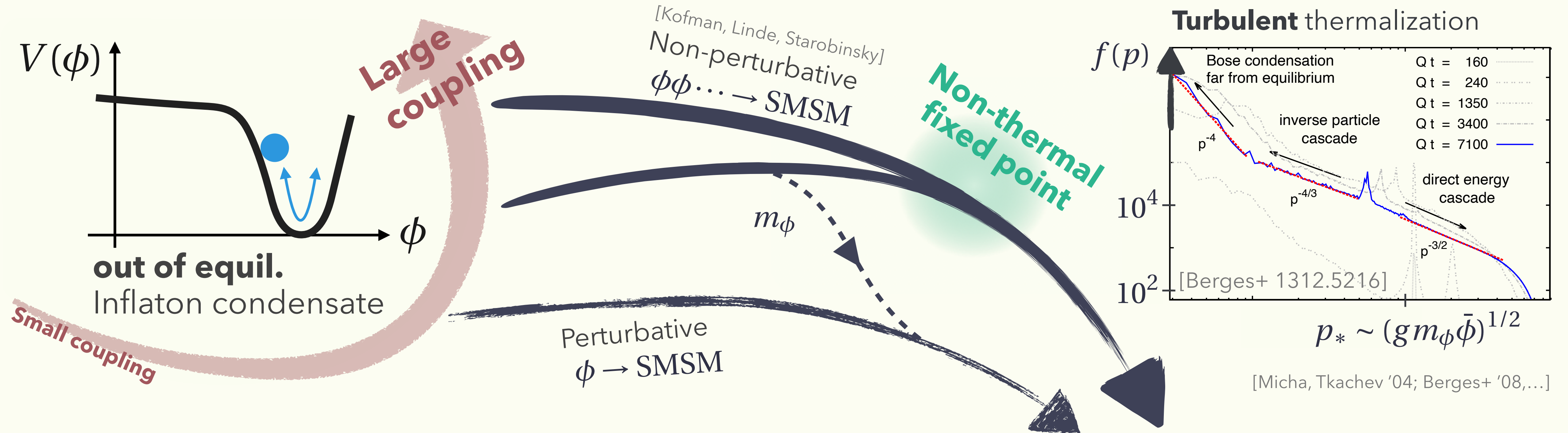


Standard Model  
+ beyond...

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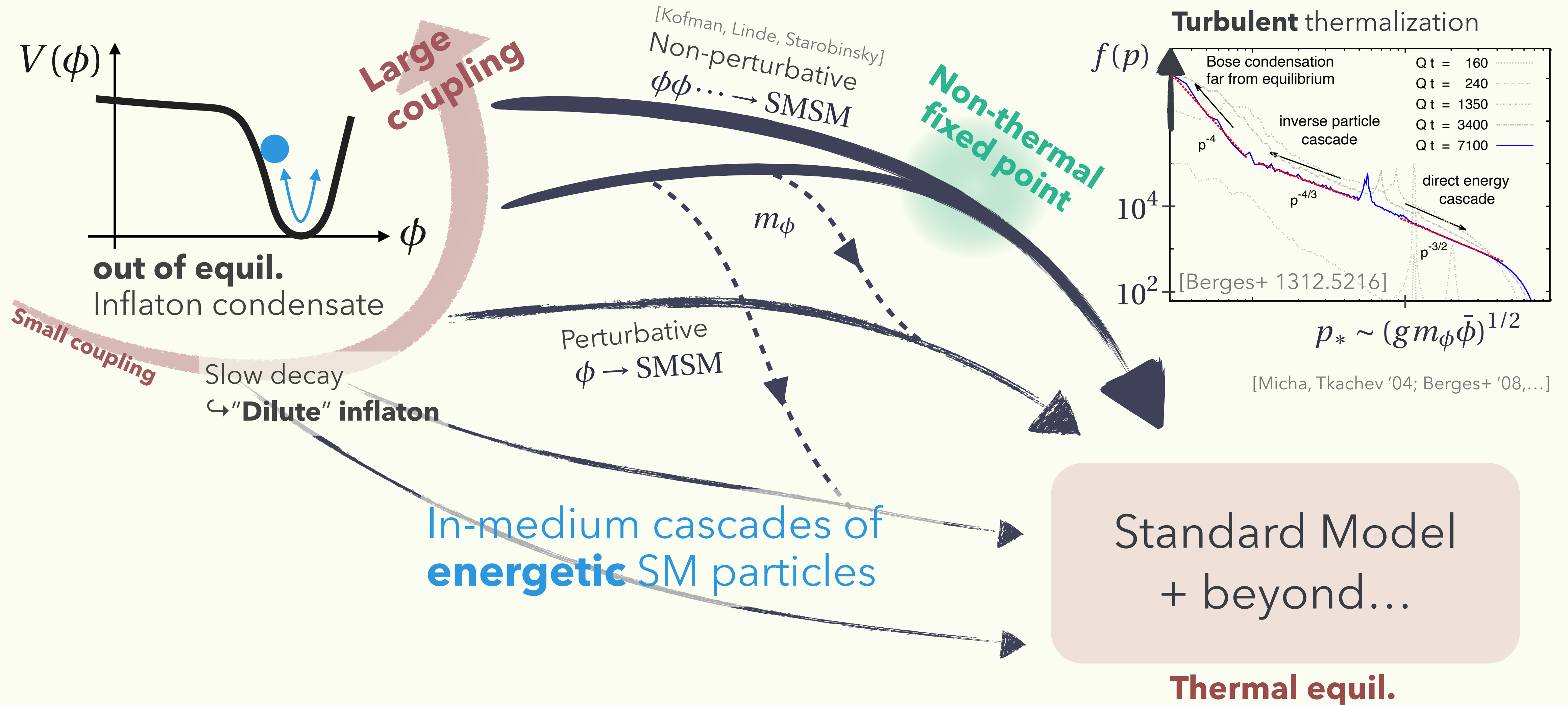
# Reheating and Thermalization



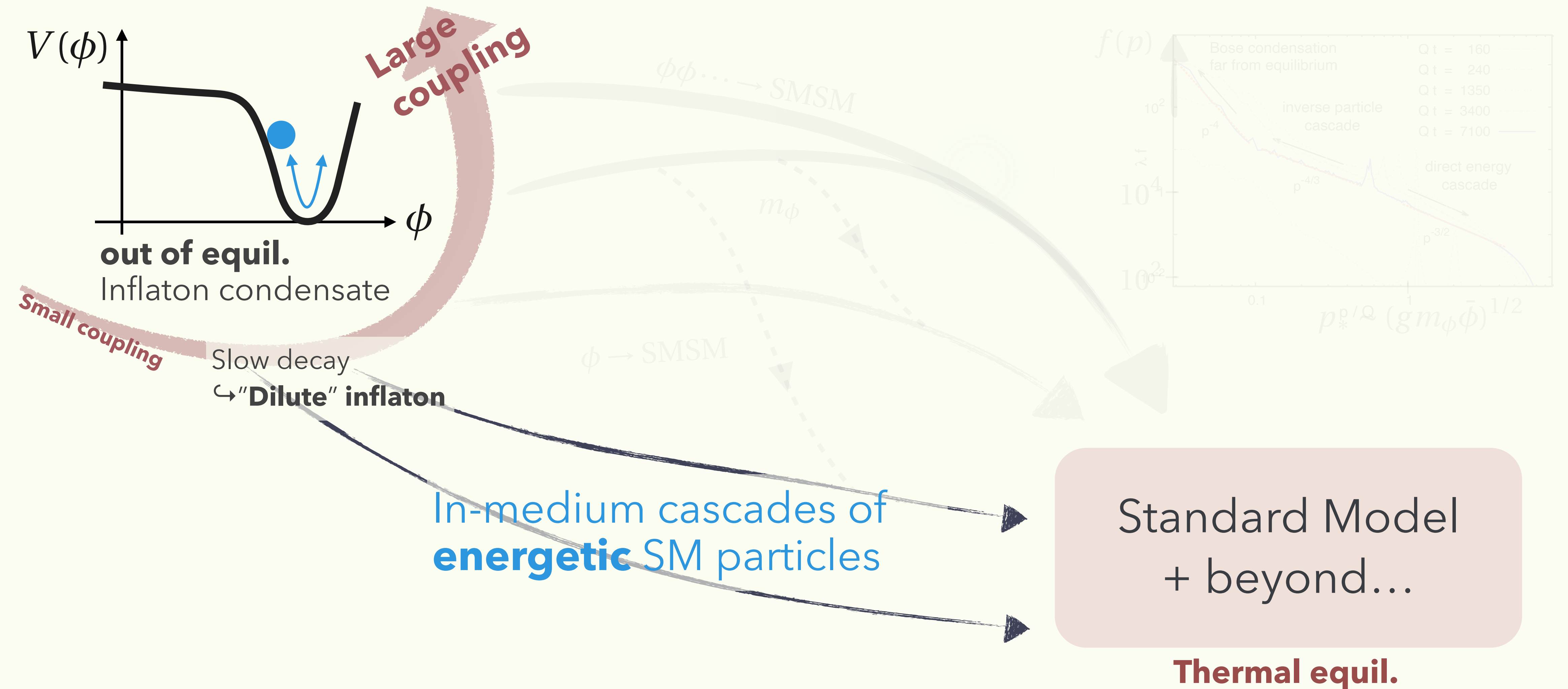
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# Reheating and Thermalization



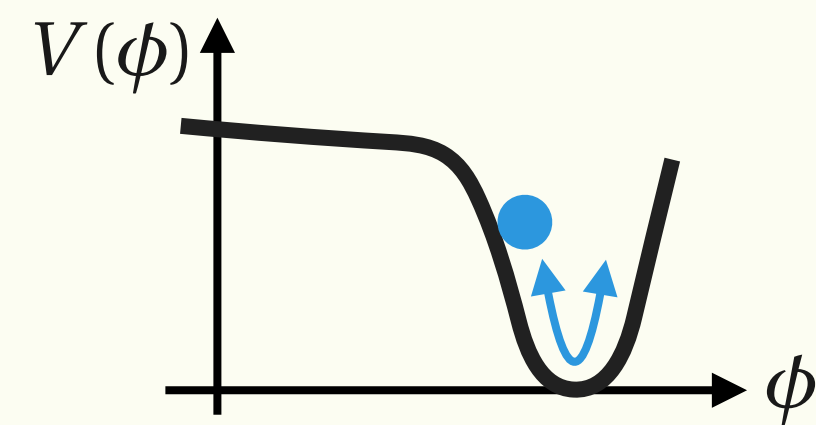
# Reheating and Thermalization



# Heavy Long-lived Matter in the early Universe

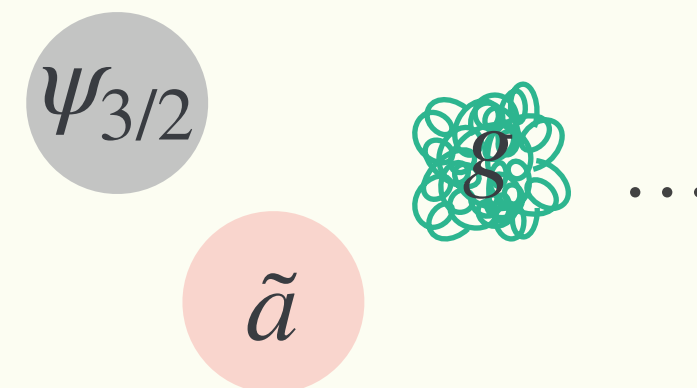
- Candidates are ubiquitous in BSMs

**Inflaton**

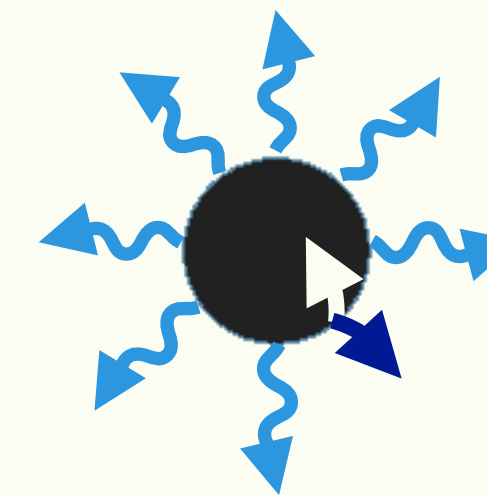


Moduli

BSM particles



Primordial Black Hole (PBH) ...



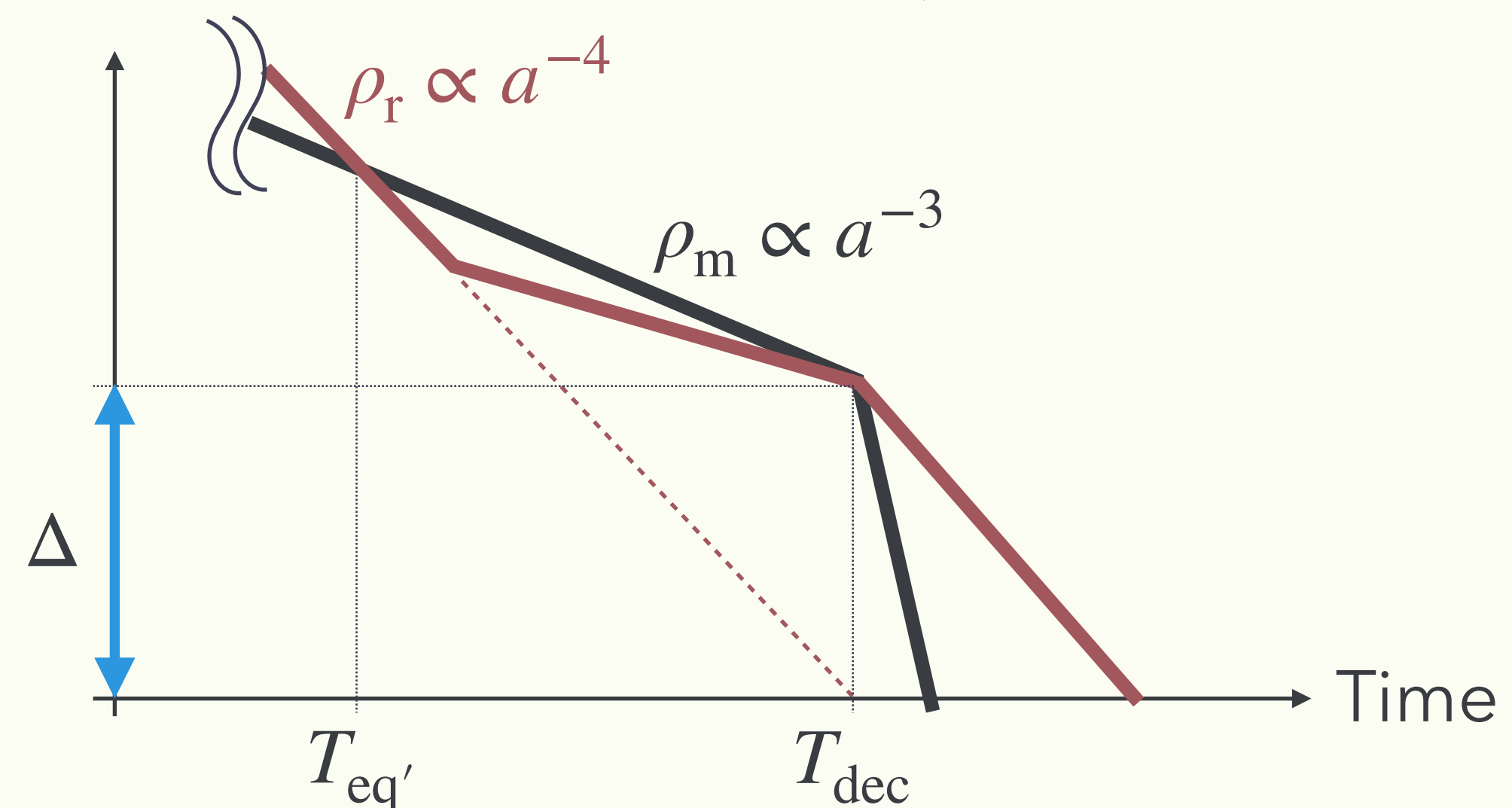
- Implications?

- (possible) matter domination

$$\rho_r \propto a^{-4} \quad \rho_m \propto a^{-3}$$

- Entropy dilution

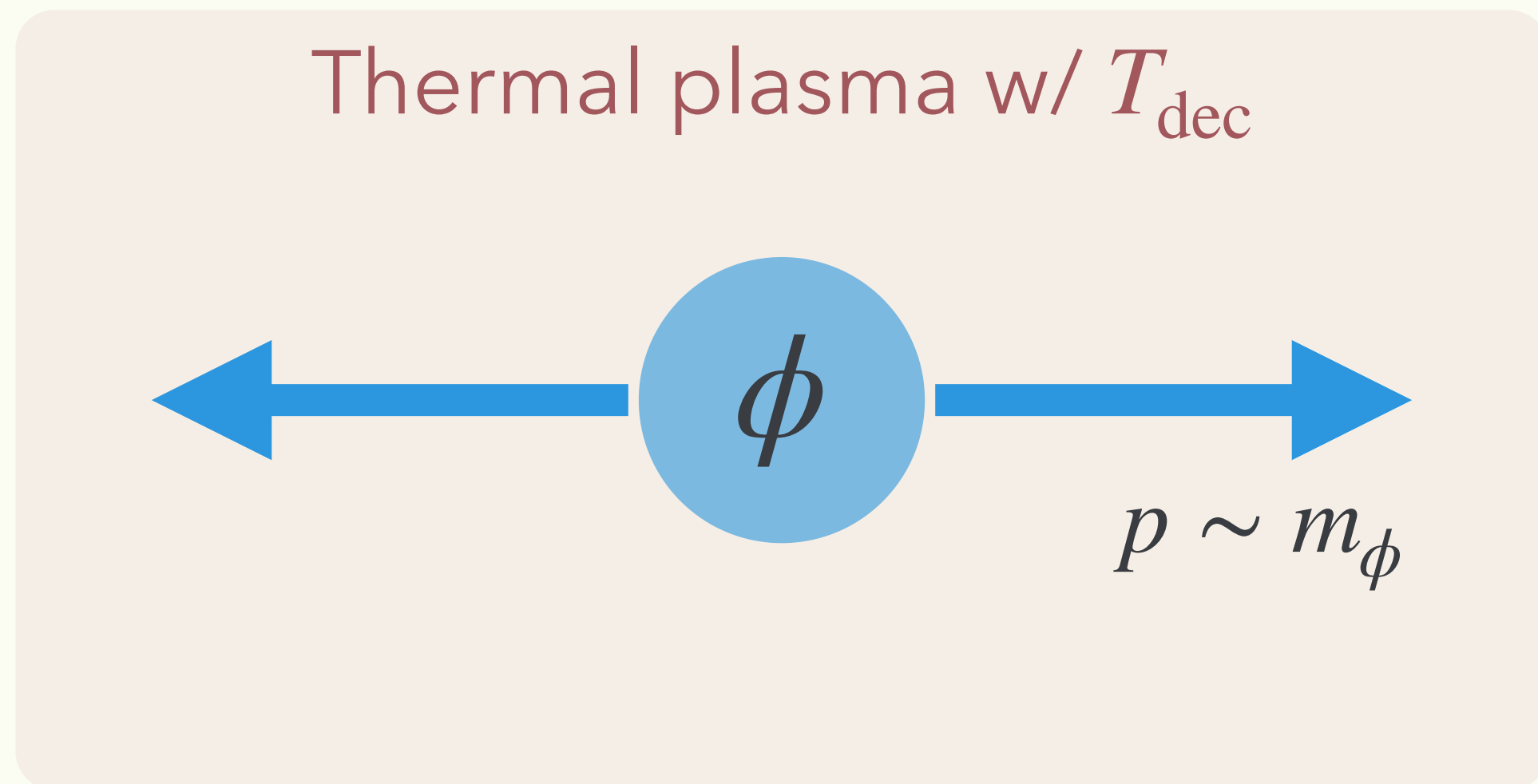
$$\Delta = T_{\text{eq}'} / T_{\text{dec}}$$



# Heavy Long-lived Matter in the early Universe

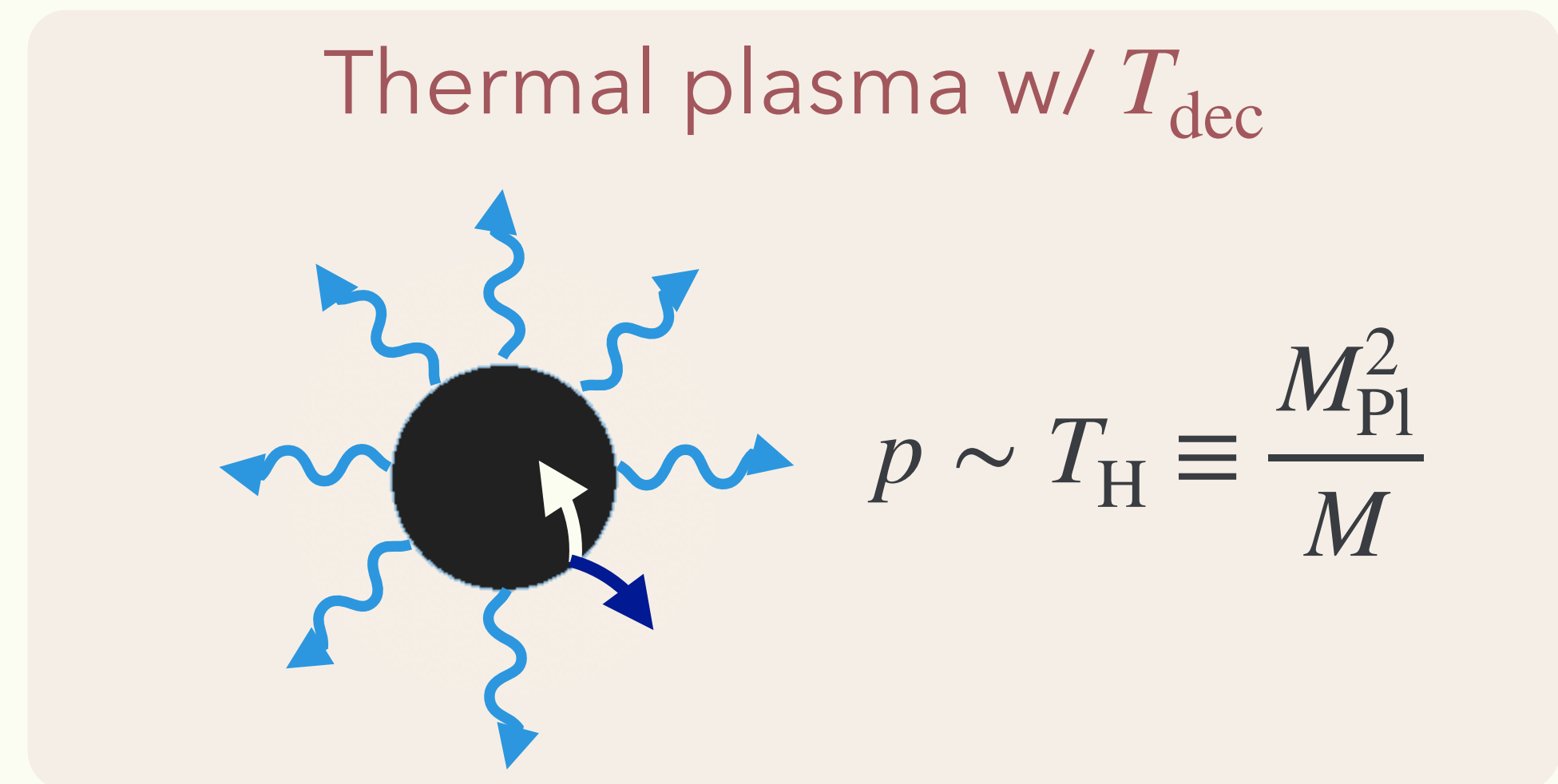
- Production of “energetic” particles

- Planck-suppressed decay of Inflaton/Moduli



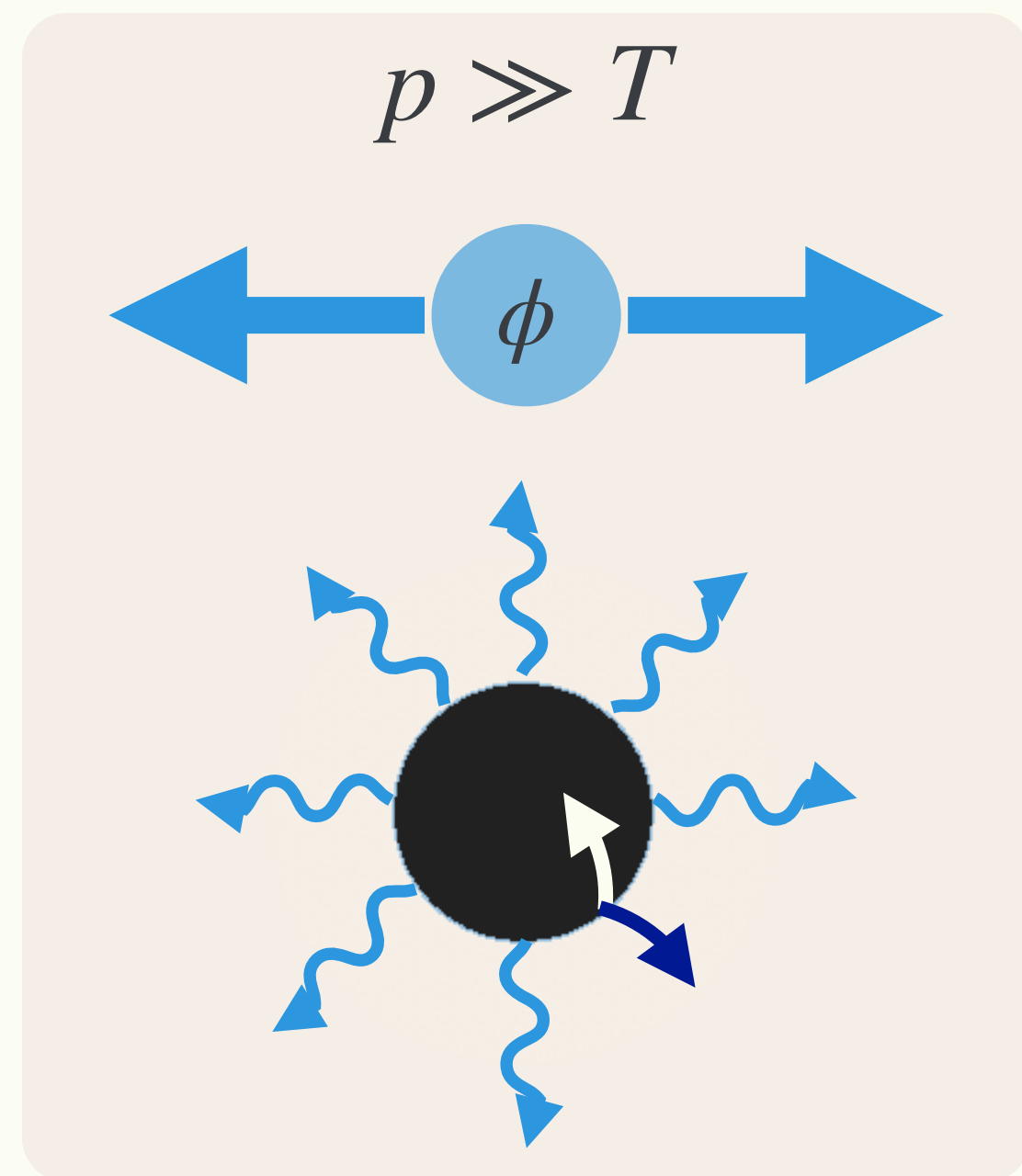
$$T_{\text{dec}} \sim \sqrt{\Gamma_\phi M_{\text{Pl}}} \sim \sqrt{\frac{m_\phi^n}{M_{\text{Pl}}^n}} m_\phi \ll m_\phi$$

- Evaporating PBH w/  $10^9 \text{ g} \gtrsim M \gg M_{\text{Pl}}$



$$T_{\text{dec}} \sim \sqrt{\Gamma_{\text{PBH}} M_{\text{Pl}}} \sim \sqrt{\frac{M_{\text{Pl}}}{M}} T_{\text{H}} \ll T_{\text{H}}$$

# Heavy Long-lived Matter in the early Universe



Decay of heavy long-lived matter

→ **energetic** particles



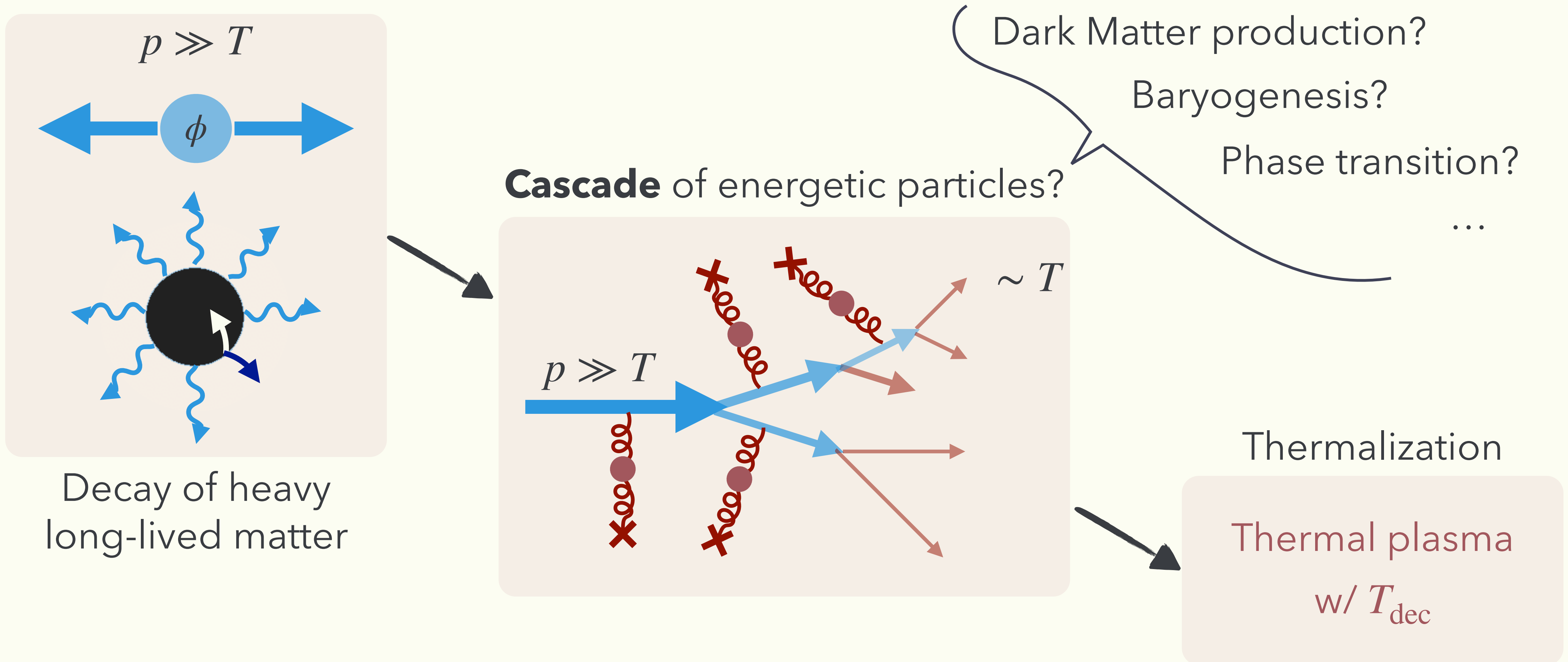
Dark Matter production?  
Baryogenesis?  
Phase transition?  
...

Thermalization

Thermal plasma

w/  $T_{\text{dec}}$

# Heavy Long-lived Matter in the early Universe

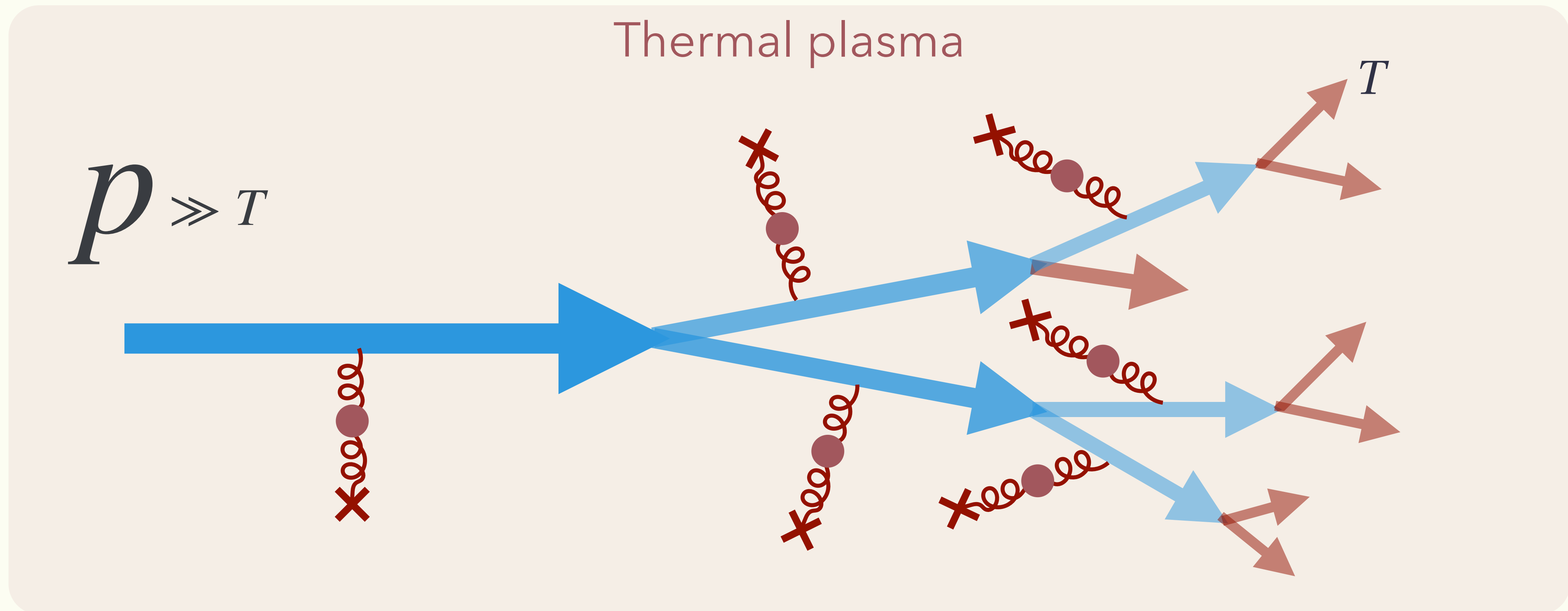


# **Cascade of energetic particles in thermal plasma**



# In-medium Cascade of Energetic Particles

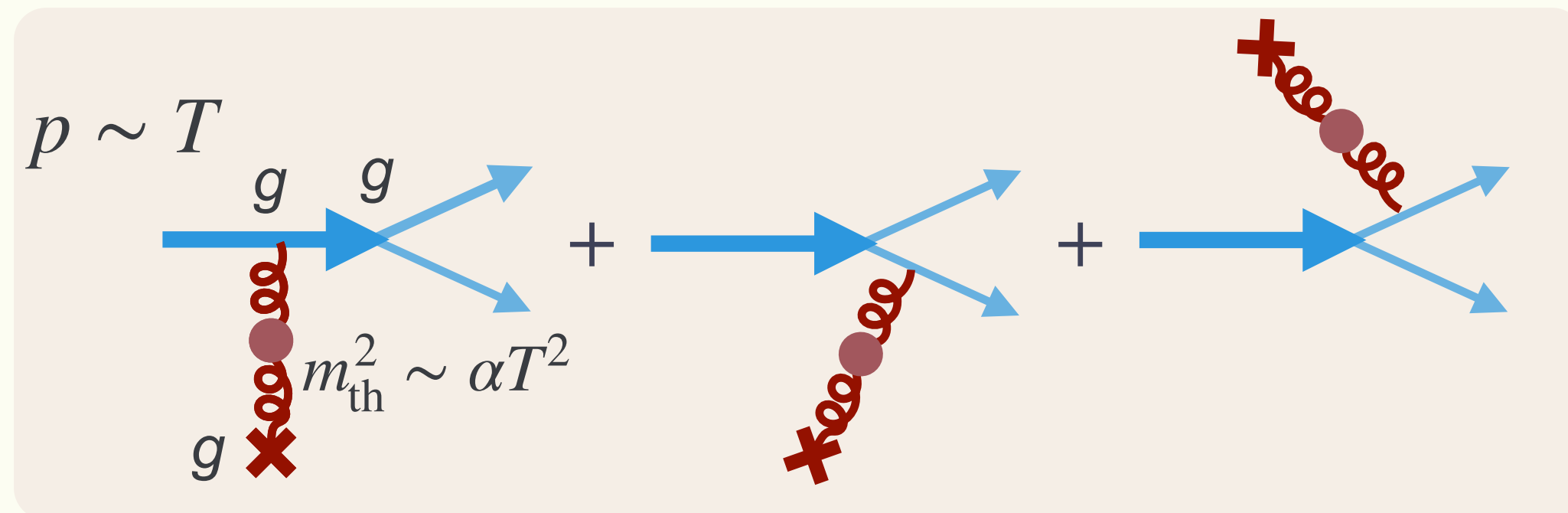
- Cascade via multiple splittings



# In-medium Cascade of Energetic Particles

- Bethe–Heitler v.s. Landau–Pomeranchuk–Migdal (LPM)

- Bethe–Heitler formula

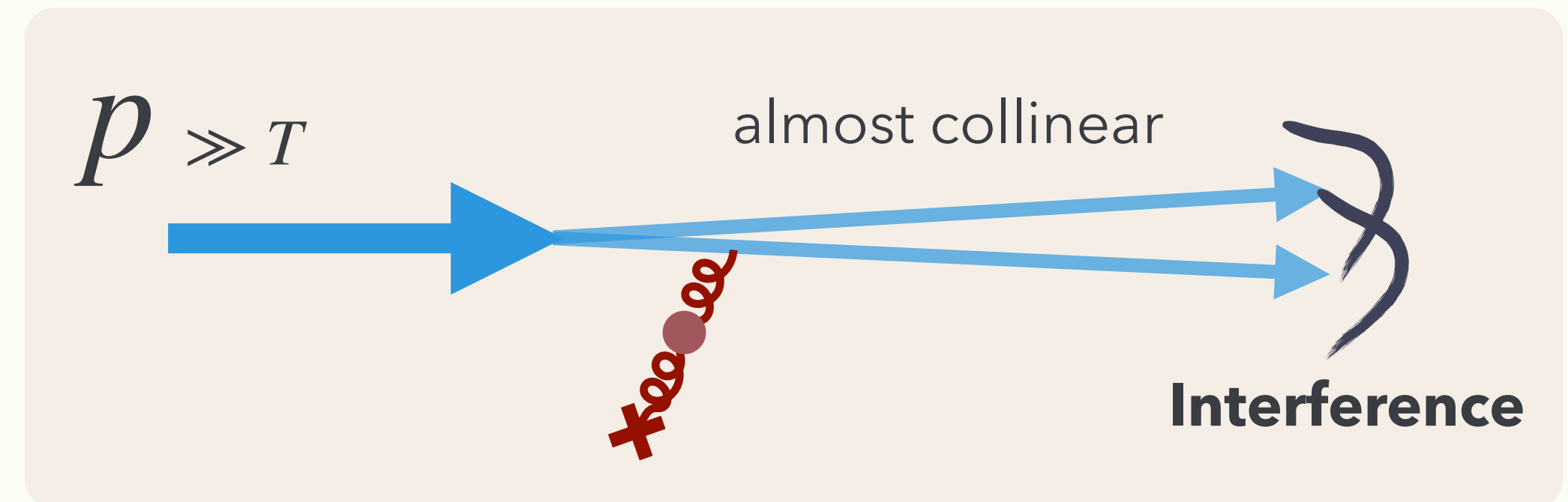


Scale-independent splitting

$$\Gamma_{\text{BH}} \sim \alpha^3 \frac{T^3}{m_{\text{th}}^2} \sim \alpha^2 T$$

- **LPM** suppression

[Landau, Pomeranchuk; Migdal]

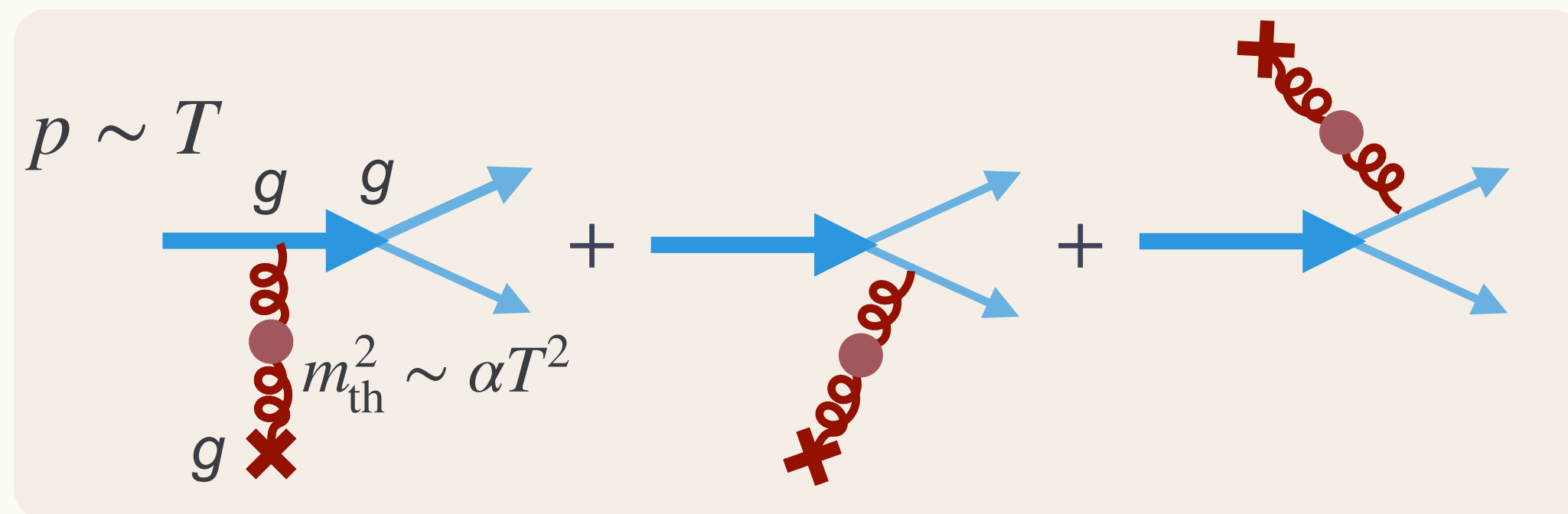


**coherent** multiple scatterings

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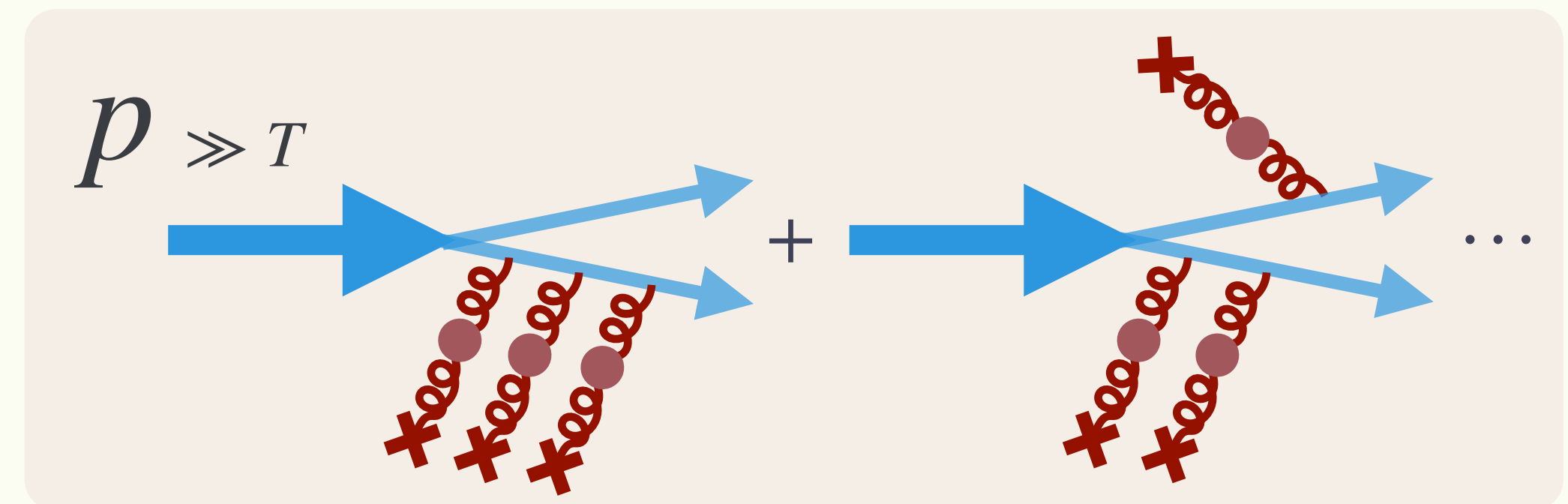


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[Landau, Pomeranchuk; Migdal]



**coherent** multiple scatterings

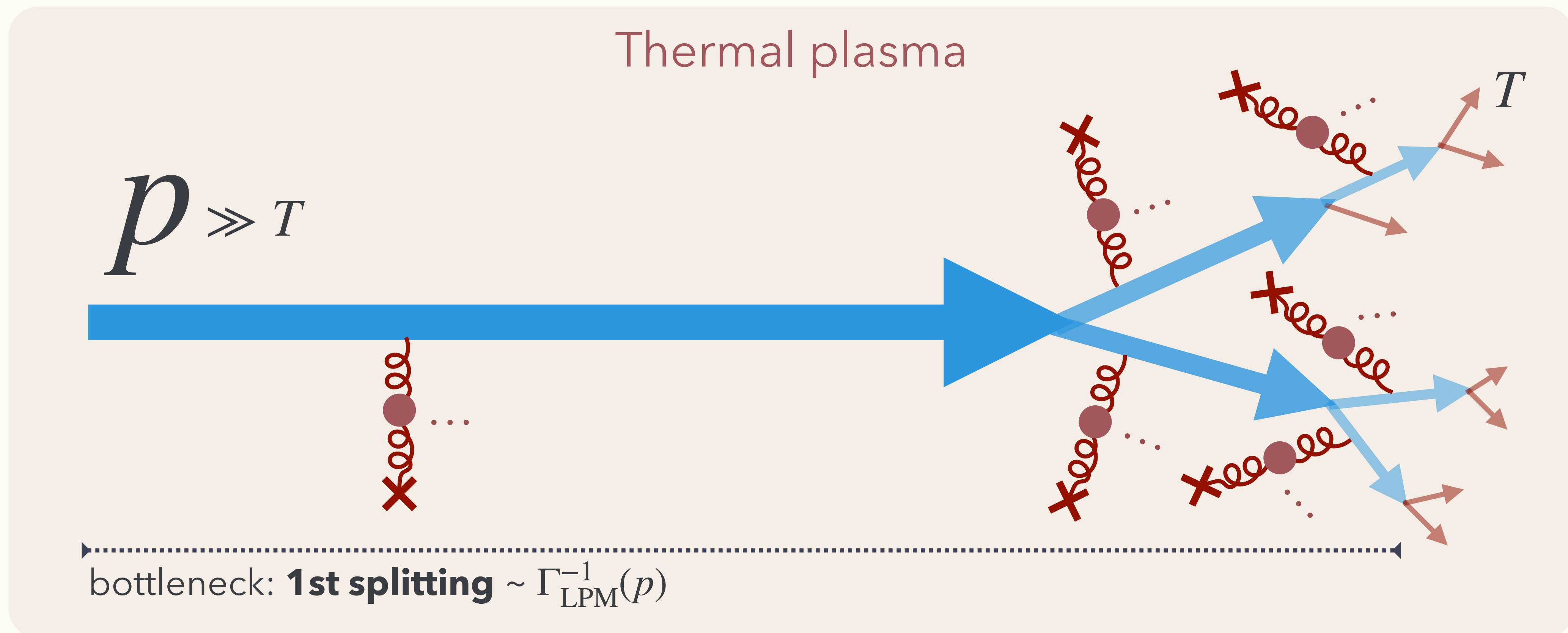
p-dependent splitting, i.e., **LPM suppression**

$$\Gamma_{\text{LPM}} \sim \alpha t_{\text{form}}^{-1}(p) \sim \alpha^2 T \times \sqrt{\frac{T}{p}}$$

[Arnold, Moore, Yaffe '01,'02,'03; Arnold, Dogan '08]

# In-medium Cascade of Energetic Particles

- Cascade via LPM-suppressed multiple splittings



# Effective Kinetic Theory of SM

- LPM-suppressed splitting function for SM

[KM, Yamada 2208.11708;  
Arnold, Morre, Yaffe '01,'02,'03; Arnold, Dogan '08]

- Kinetic equation

$$\mathcal{L} f_s(\mathbf{x}, \mathbf{p}, t) = \mathcal{S} + \mathcal{C}_{2 \leftrightarrow 2}[f_s] + \mathcal{C}_{"1 \leftrightarrow 2"}[f_s]$$

w/  $s = e_f, L_f, u_f, d_f, Q_f, \phi, B, W, g$

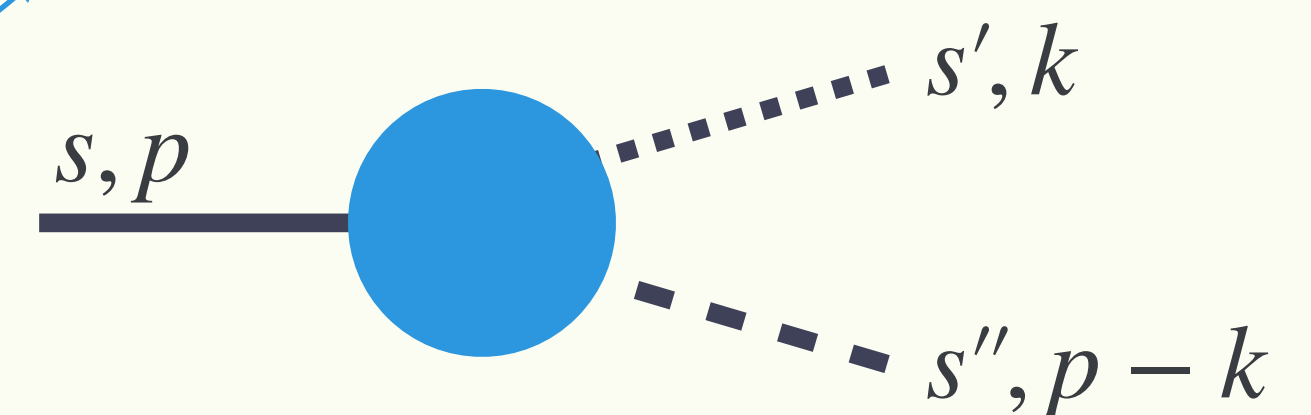
Source      Elastic scat.      **LPM-suppressed**  
e.g., inflaton, PBHs      splitting

- **Splitting function** for effective "1 to 2" processes

$$\mathcal{C}_{"1 \leftrightarrow 2"}[f_s] \supset -\frac{(2\pi)^3}{p^2 v_s} \sum_{s', s''} \int_0^p dk \gamma_{s \leftrightarrow s' s''}(p; k, p-k) f_s(p)$$

+ (inverse)

**Splitting function**



# Effective Kinetic Theory of SM (cont'd)

- LPM-suppressed splitting function for SM

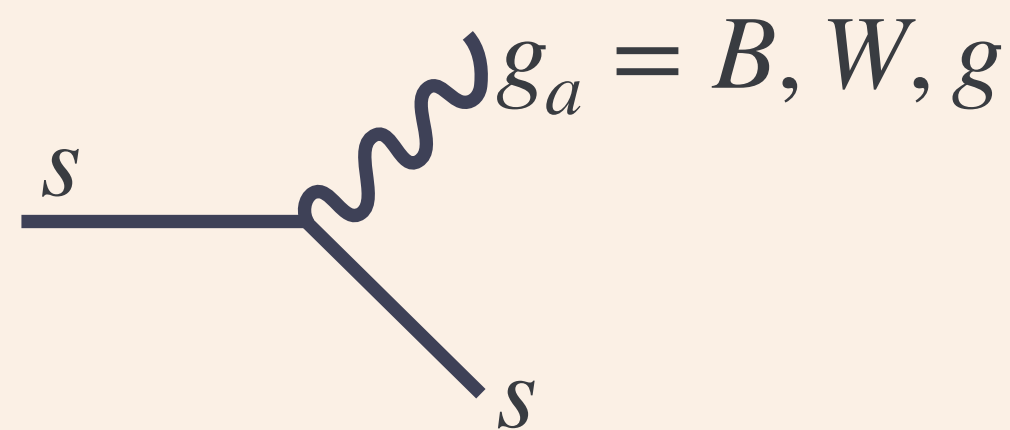
[KM, Yamada 2208.11708;  
Arnold, Morre, Yaffe '01,'02,'03; Arnold, Dogan '08]

- SM splitting function

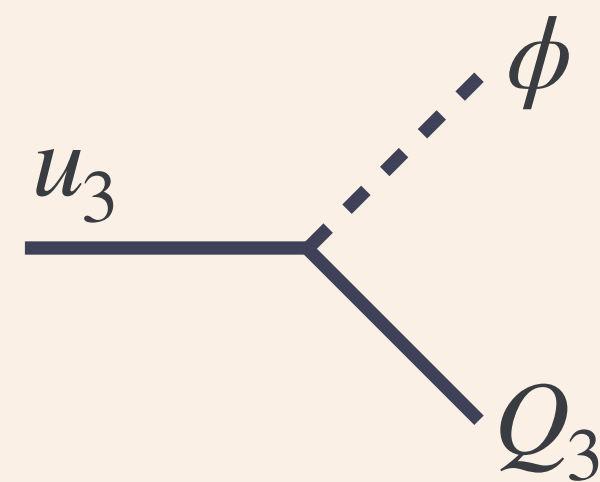
$$\gamma_{s \rightarrow s' s''}(p; xp, (1-x)p) = \frac{1}{2} \frac{\alpha_{ss's''}}{(2\pi)^4 \sqrt{2}} \times \frac{P_{s \rightarrow s' s''}^{(\text{vac})}(x)}{x(1-x)} \times \mu_{\perp}^2(1, x, 1-x; s, s', s'')$$

vacuum DGLAP  
splitting function

SM gauge + top Yukawa

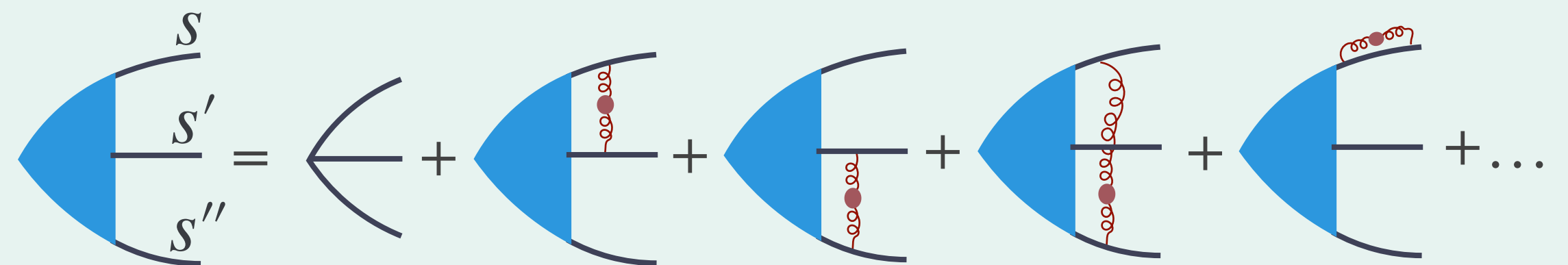


$$\alpha_{sg_a s} = d_{\mathbf{R}_s}^{(a)} C_{\mathbf{R}_s}^{(a)} \alpha_a$$



$$\alpha_{u_3 \phi Q_3} = y_t^2 / (4\pi)$$

LPM suppression



i.e., self-consistent equation for vertex func.

# Effective Kinetic Theory of SM (cont'd)

- LPM-suppressed splitting function for SM

[KM, Yamada 2208.11708;  
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- SM splitting function

$$\gamma_{s \rightarrow s' s''}(p; xp, (1-x)p) = \frac{1}{2} \frac{\alpha_{ss's''}}{(2\pi)^4 \sqrt{2}} \times \frac{P_{s \rightarrow s' s''}^{(\text{vac})}(x)}{x(1-x)} \times \mu_{\perp}^2(1, x, 1-x; s, s', s'')$$

vacuum DGLAP splitting function

SM gauge + top Yukawa

$$\alpha_{sg_a s} = d_{R_s}^{(a)} C_{R_s}^{(a)} \alpha_a \quad \alpha_{u_3 \phi Q_3} = \alpha_t$$

|       | $C_F$   | $C_A$ | $d_F$ | $d_A$ | $t_F$   | $t_A$ |
|-------|---------|-------|-------|-------|---------|-------|
| SU(3) | 4/3     | 3     | 3     | 8     | 1/2     | 3     |
| SU(2) | 3/4     | 2     | 2     | 3     | 1/2     | 2     |
| U(1)  | $q_Y^2$ | 0     | 1     | 1     | $q_Y^2$ | 0     |

**LPM suppression**

$$\mu_{\perp}^4(x_1, x_2, x_3; s_1, s_2, s_3) = \frac{2}{\pi} x_1 x_2 x_3 p \sum_a \frac{\alpha_a(m_{D,a}) - \alpha_a(Q_{\perp,a})}{-b_a / (64\pi^3)} \mathcal{N}_a$$

$$\times \sum_{\sigma \in A_3} \frac{1}{2} \left[ C_{R_{s_{\sigma(2)}}}^{(a)} + C_{R_{s_{\sigma(3)}}}^{(a)} - C_{R_{s_{\sigma(1)}}}^{(a)} \right] x_{\sigma(1)}^2$$

$$b_a = \begin{cases} -7 \\ -\frac{19}{6} \\ \frac{41}{6} \end{cases} \quad \mathcal{N}_a = \begin{cases} 15 \frac{\zeta(3)}{\pi^2} T^3 \\ 14 \frac{\zeta(3)}{\pi^2} T^3 \\ 6 \frac{\zeta(3)}{\pi^2} T^3 \end{cases} \quad m_{D,a}^2 = \begin{cases} 8\pi\alpha_3 T^2 & \text{for SU(3)} \\ \frac{22\pi}{3} \alpha_2 T^2 & \text{for SU(2)} \\ \frac{22\pi}{3} \alpha_1 T^2 & \text{for U(1)} \end{cases}$$

# Effective Kinetic Theory of SM (cont'd)

$$\begin{aligned}
\gamma_{g_a \leftrightarrow g_a g_a}(P; xP, (1-x)P) &= \frac{1}{2} \frac{d_A^{(a)} C_A^{(a)} \alpha_a}{(2\pi)^4 \sqrt{2}} \frac{1^4 + x^4 + (1-x)^4}{1^2 \cdot x^2 (1-x)^2} \mu_{\perp, a}^2(1, x, 1-x; g_a, g_a, g_a), \\
\gamma_{s \leftrightarrow g_a s}(P; xP, (1-x)P) &= \frac{1}{2} \frac{d_F^{(a)} C_{F_s}^{(a)} \alpha_a}{(2\pi)^4 \sqrt{2}} \frac{1^2 + (1-x)^2}{1 \cdot x^2 (1-x)} \mu_{\perp}^2(1, x, 1-x; s, g_a, s) \quad \text{for } s = (\text{fermion}), \\
\gamma_{g_a \leftrightarrow s \bar{s}}(P; xP, (1-x)P) &= \frac{1}{2} \frac{d_F^{(a)} C_{F_s}^{(a)} \alpha_a}{(2\pi)^4 \sqrt{2}} \frac{x^2 + (1-x)^2}{1^2 \cdot x(1-x)} \mu_{\perp}^2(1, x, 1-x; g_a, s, s) \quad \text{for } s = (\text{fermion}), \\
\gamma_{\phi \leftrightarrow g_a \phi}(P; xP, (1-x)P) &= \frac{1}{2} \frac{d_F^{(a)} C_{F_\phi}^{(a)} \alpha_a}{(2\pi)^4 \sqrt{2}} \frac{2}{x^2} \mu_{\perp}^2(1, x, 1-x; \phi, g_a, \phi), \\
\gamma_{g_a \leftrightarrow \phi \phi^*}(P; xP, (1-x)P) &= \frac{1}{2} \frac{d_F^{(a)} C_{F_\phi}^{(a)} \alpha_a}{(2\pi)^4 \sqrt{2}} \frac{2}{1^2} \mu_{\perp}^2(1, x, 1-x; g_a, \phi, \phi), \\
\gamma_{u_3 \leftrightarrow \phi Q_3}(P; xP, (1-x)P) &= \frac{1}{2} \frac{\alpha_t}{(2\pi)^4 \sqrt{2}} \frac{1}{1 \cdot (1-x)} \mu_{\perp}^2(1, x, 1-x; u_3, \phi, Q_3), \\
\gamma_{\phi \leftrightarrow u_3 \bar{Q}_3}(P; xP, (1-x)P) &= \frac{1}{2} \frac{\alpha_t}{(2\pi)^4 \sqrt{2}} \frac{1}{x(1-x)} \mu_{\perp}^2(1, x, 1-x; \phi, u_3, Q_3),
\end{aligned}$$



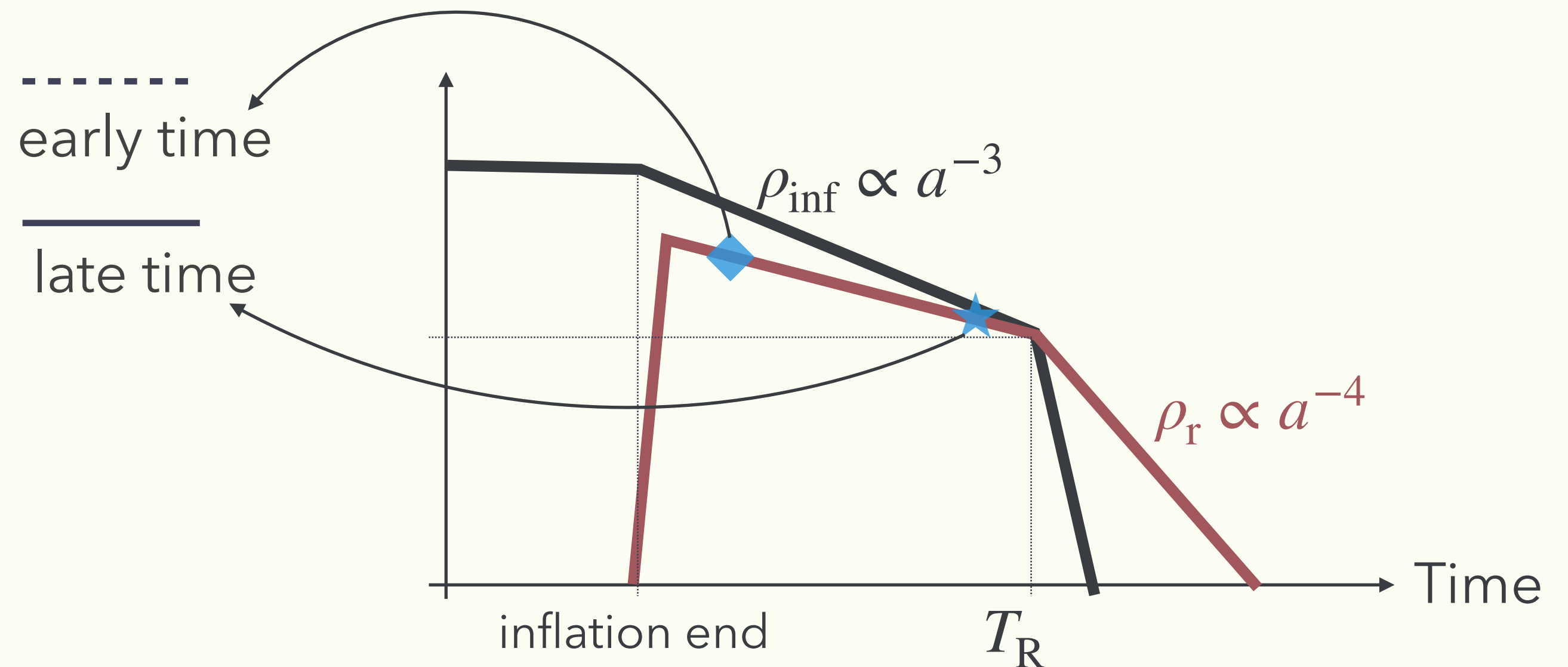
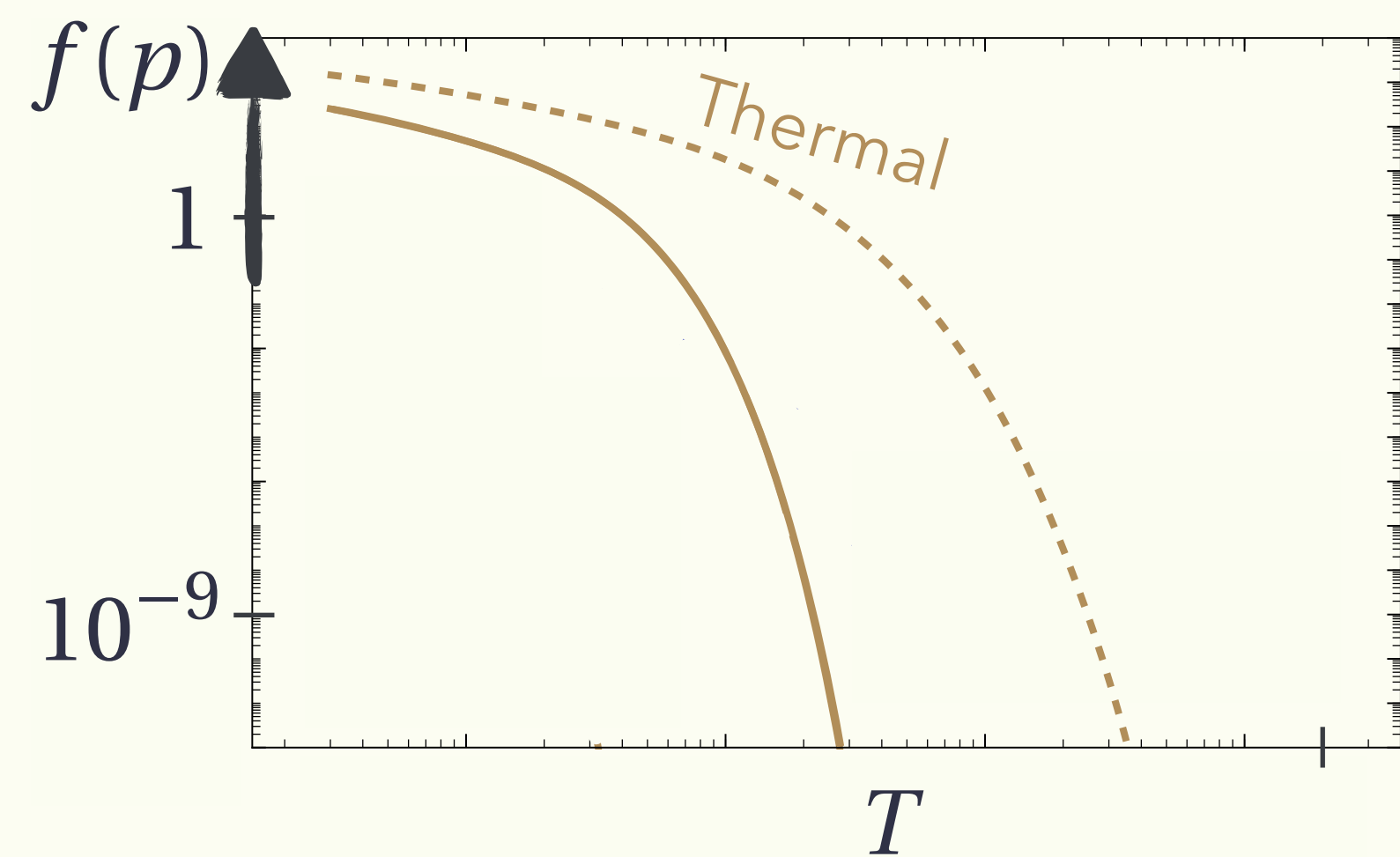
# Reheating after Inflation

(i.e., Homogeneous source)

# Suppression of Maximal Temperature

- Instantaneous v.s. Finite-time thermalization for inflaton  $\rightarrow$  gluon + gluon

- Instantaneous thermalization

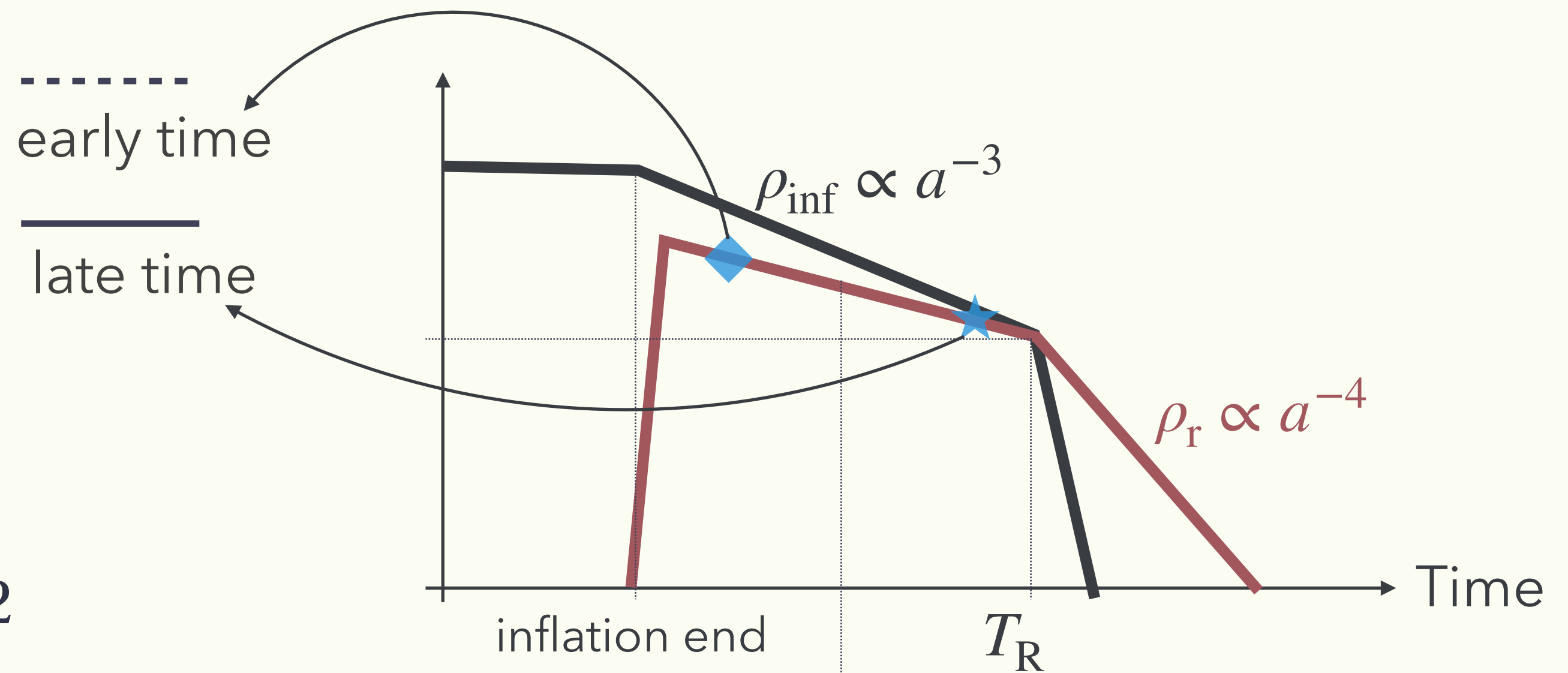
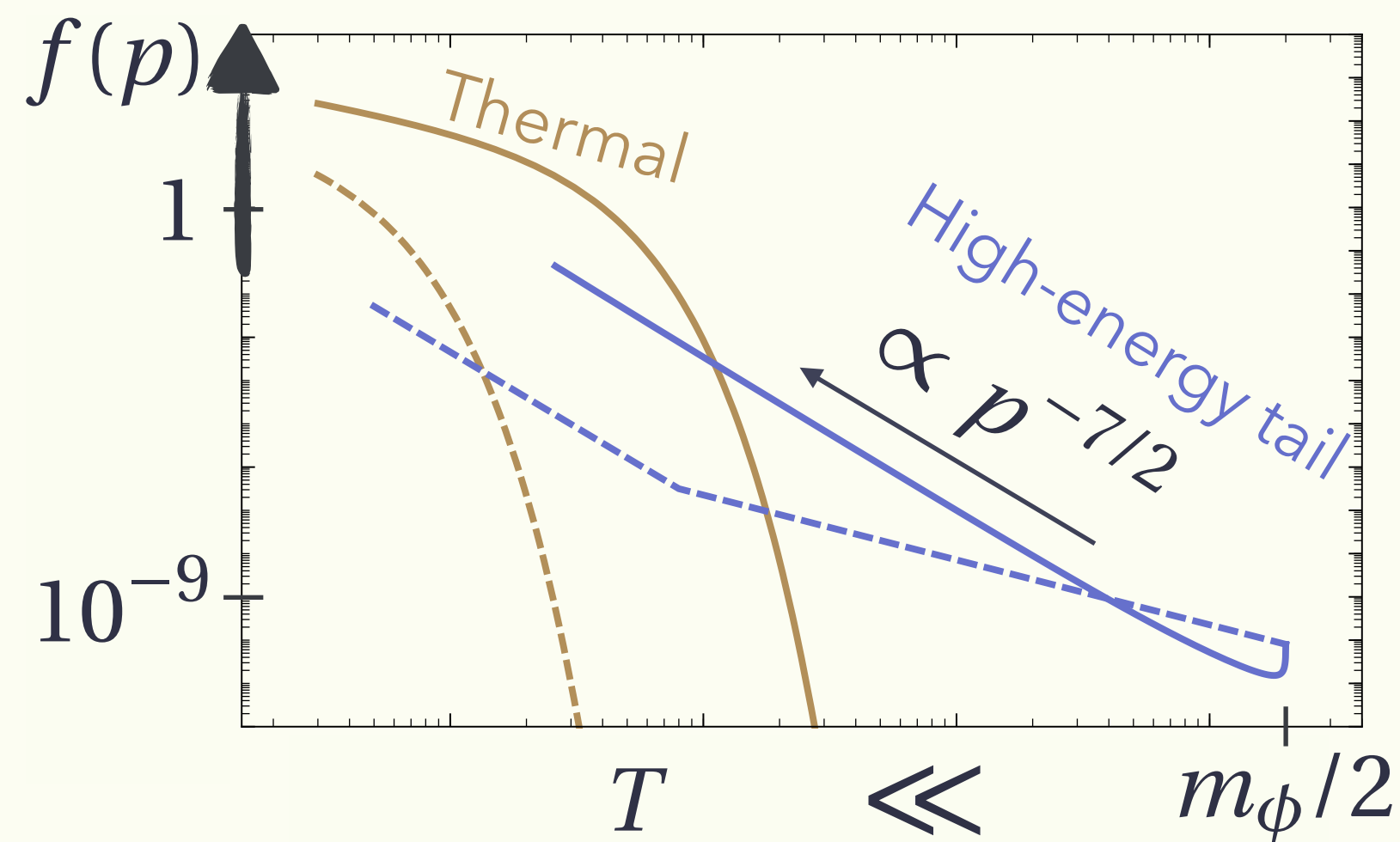


$$T_{\max}^{(\text{inst})} \sim \left( m_{\phi} T_{\text{R}}^2 M_{\text{Pl}} \right)^{1/4} \gg T_{\text{R}}$$

# Suppression of Maximal Temperature

- Instantaneous v.s. Finite-time thermalization for inflaton  $\rightarrow$  gluon + gluon

- **Finite-time** thermalization



$$\frac{T_{\max}}{T_{\max}^{(\text{inst})}} \sim 10^{-3} \left( \frac{\alpha}{0.1} \right)^{4/5} \left( \frac{T_R}{10^3 \text{ GeV}} \right)^{3/10}$$

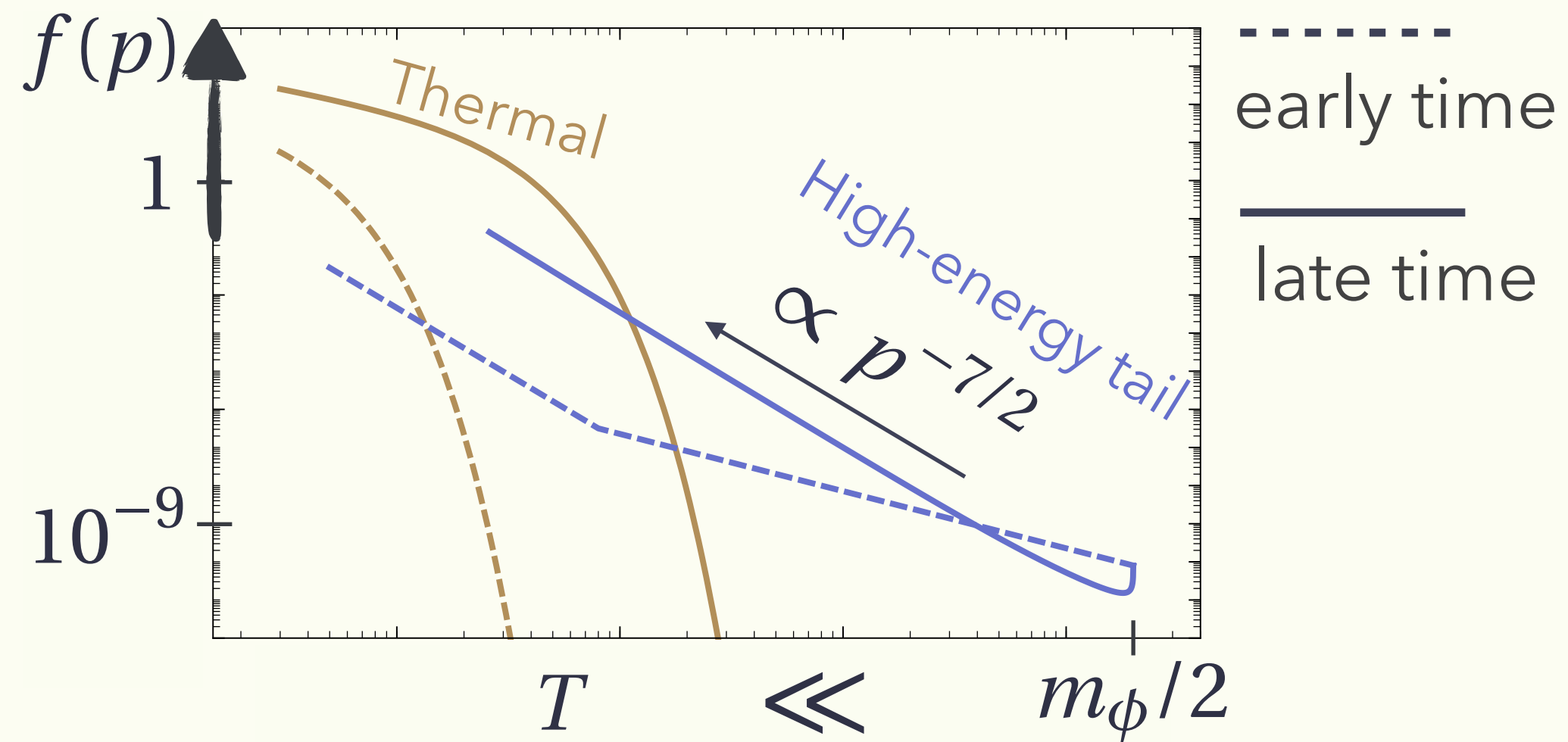
[KM, Harigaya 1312.3097]

$$\Gamma_{\text{split}}(m_\phi) < H \quad \Gamma_{\text{split}}(m_\phi) > H$$

$T_{\max}$

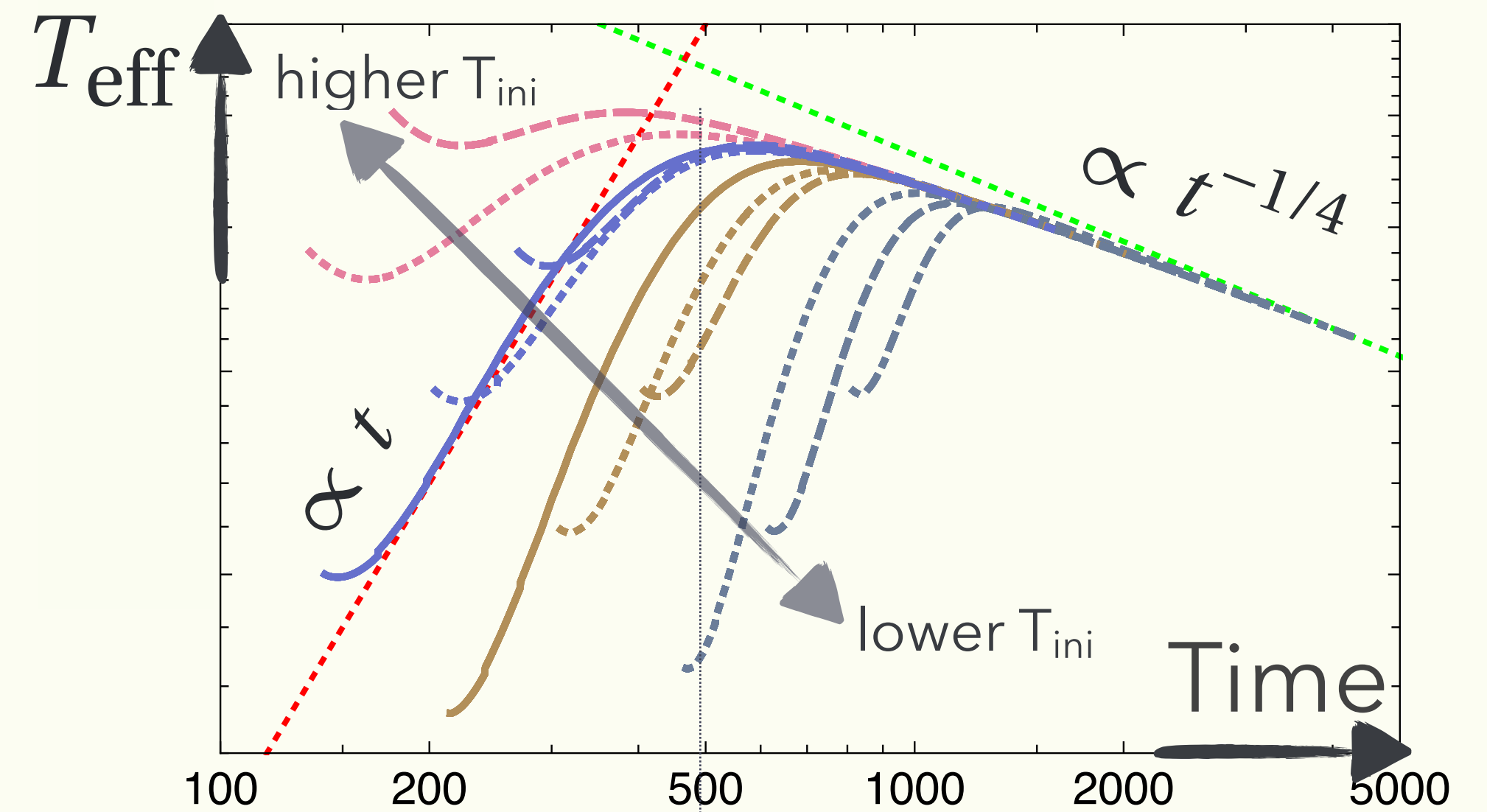
# Suppression of Maximal Temperature

- Attractor for  $\Gamma_{\text{split}}(m_\phi) \gtrsim H \gtrsim \Gamma_\phi$



$$\frac{T_{\text{max}}}{T_{\text{max}}^{(\text{inst})}} \sim 10^{-3} \left(\frac{\alpha}{0.1}\right)^{4/5} \left(\frac{T_{\text{R}}}{10^3 \text{ GeV}}\right)^{3/10}$$

[KM, Harigaya 1312.3097]



$$\Gamma_{\text{split}}(m_\phi) < H \quad \Gamma_{\text{split}}(m_\phi) > H$$

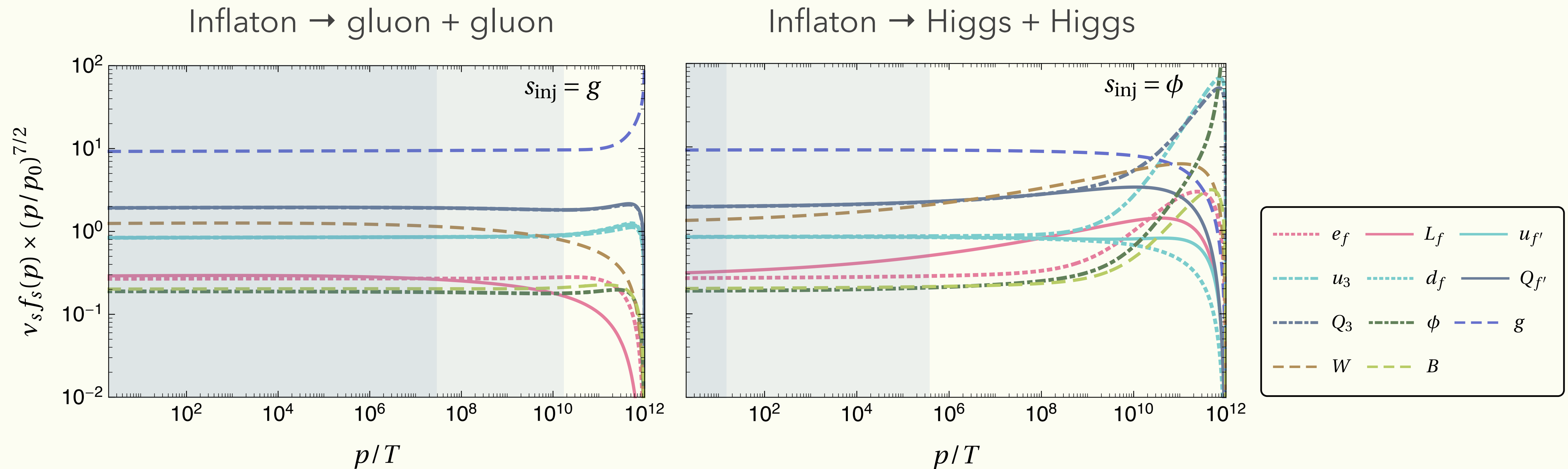
$T_{\text{max}}$

[KM, Yamada, 2402.14054]

# Universality in the Spectrum

[KM, Yamada 2208.11708]

- Hardtail composition irrespective of inflaton-SM coupling

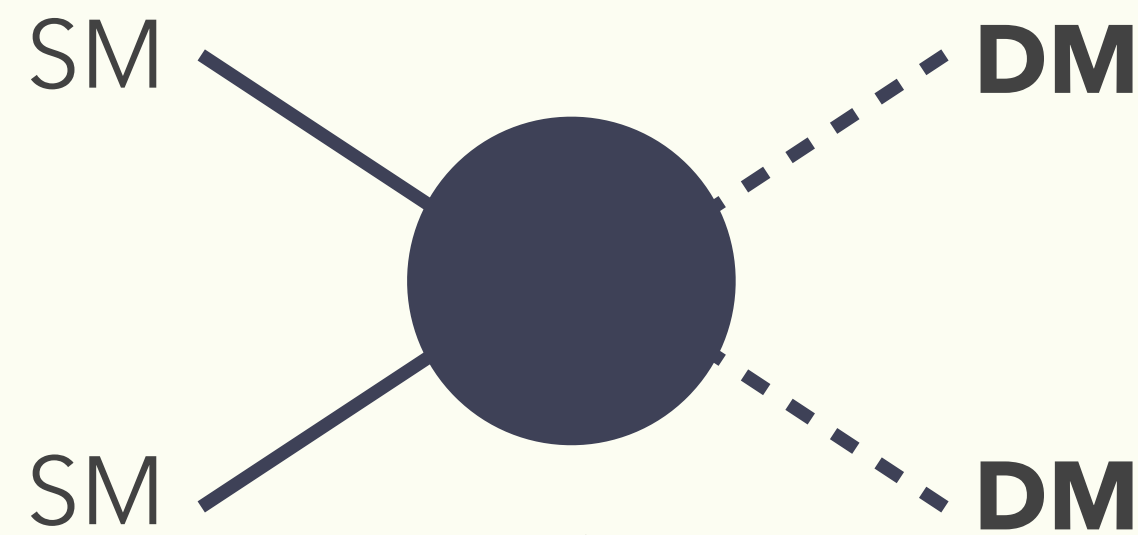
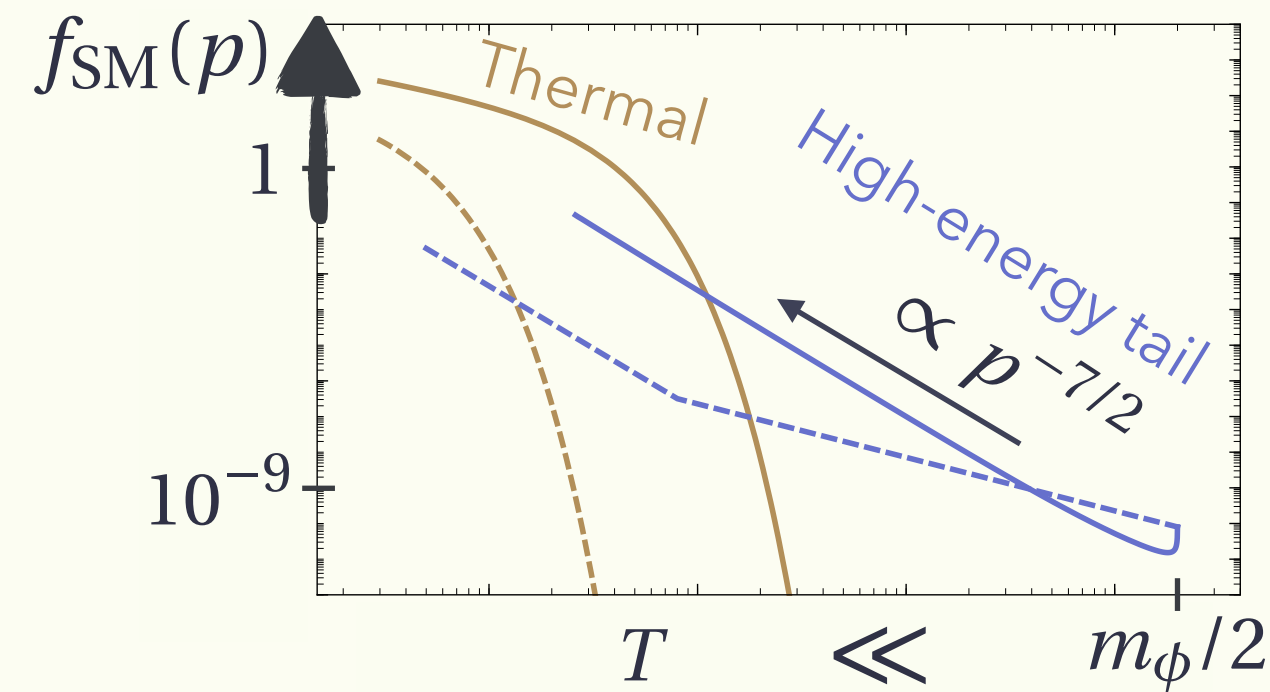




# Implications of Suppressed $T_{\max}$ & Hardtail?

- Non-thermal Dark Matter production of  $m_{\text{DM}} > T_{\text{R}}$

[KM+ 1402.2846, 1901.11027;  
Drees+; Garcia+]



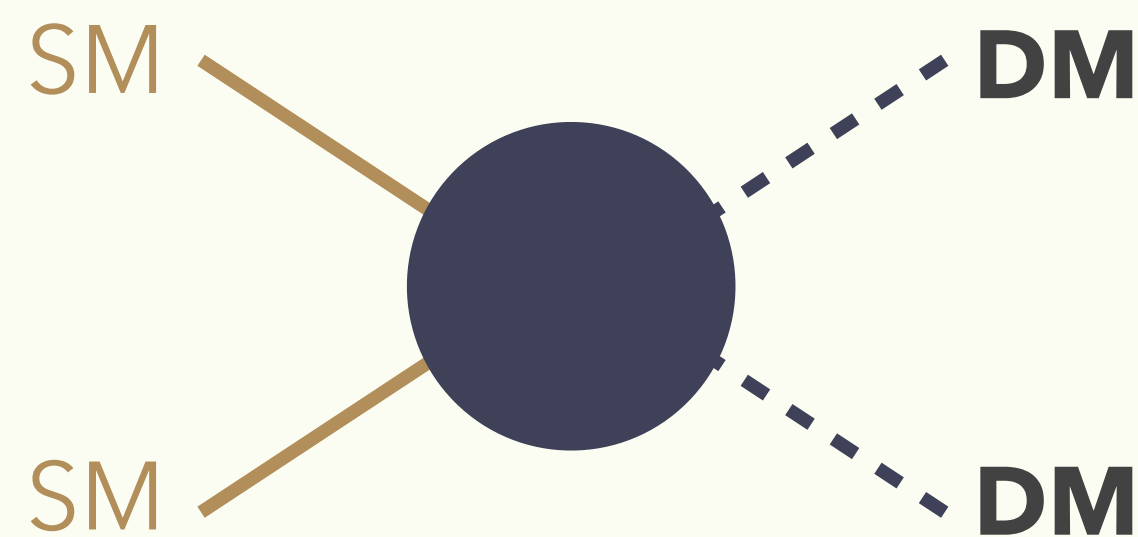
E.g.  $W W \rightarrow \text{DM DM}$

$$\langle \sigma v \rangle \simeq \frac{\alpha_{\text{DM}}^2}{m_{\text{DM}}^2} \quad \Rightarrow \quad \frac{\rho_{\text{DM}}}{s} \simeq 0.11 \alpha_{\text{DM}}^2 \frac{T_{\text{R}}^3}{m_{\text{DM}}^2}$$

“Universal” production

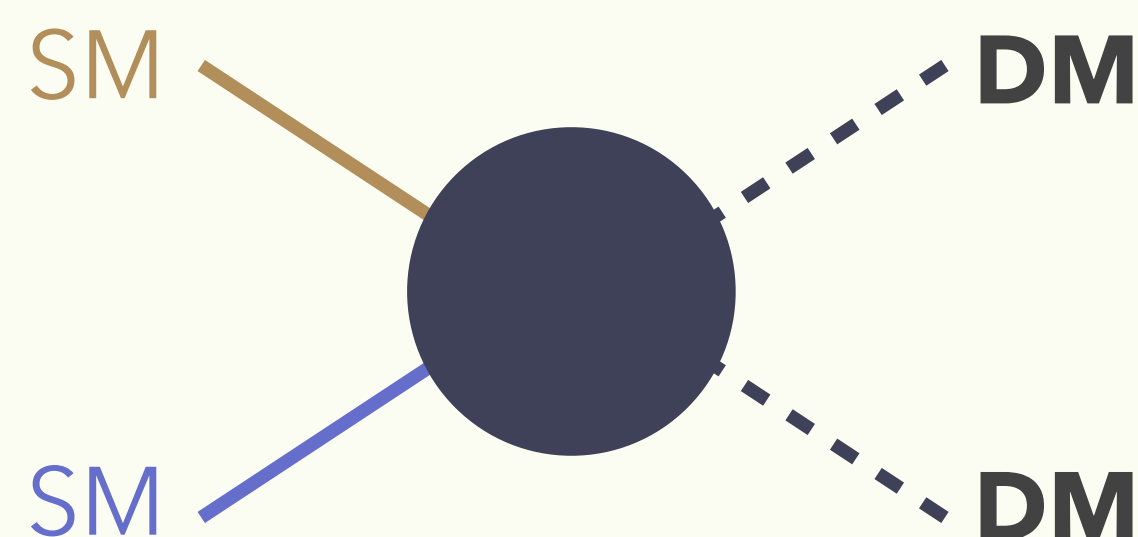
Thermal + Thermal

[Giudice, Kolb, Riotto '01]



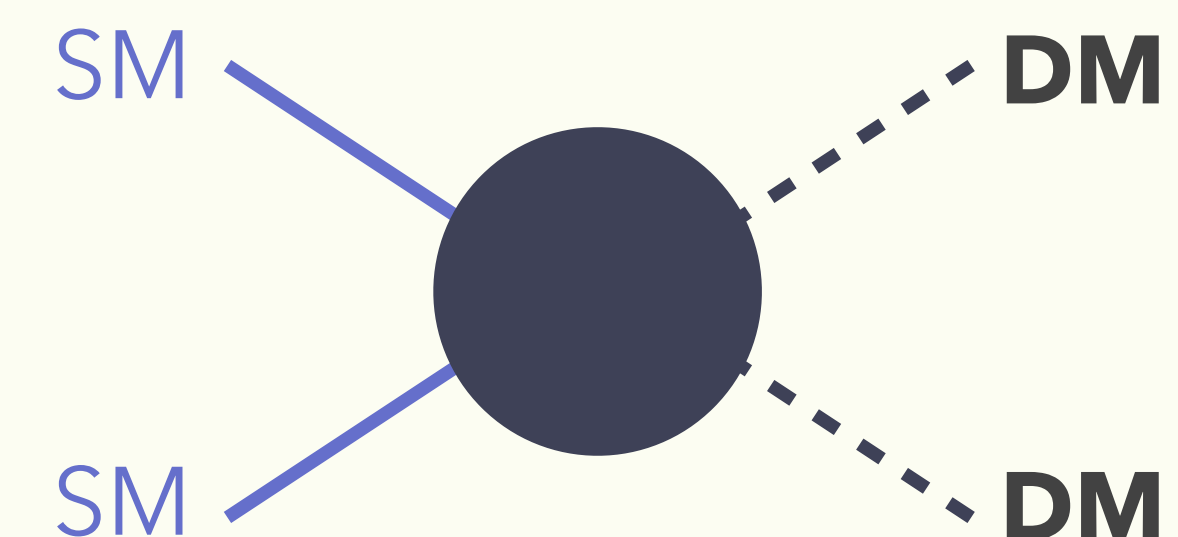
Thermal + High-E tail

[KM+ 1402.2846; Drees, Najjari '21]



High-E tail + High-E tail

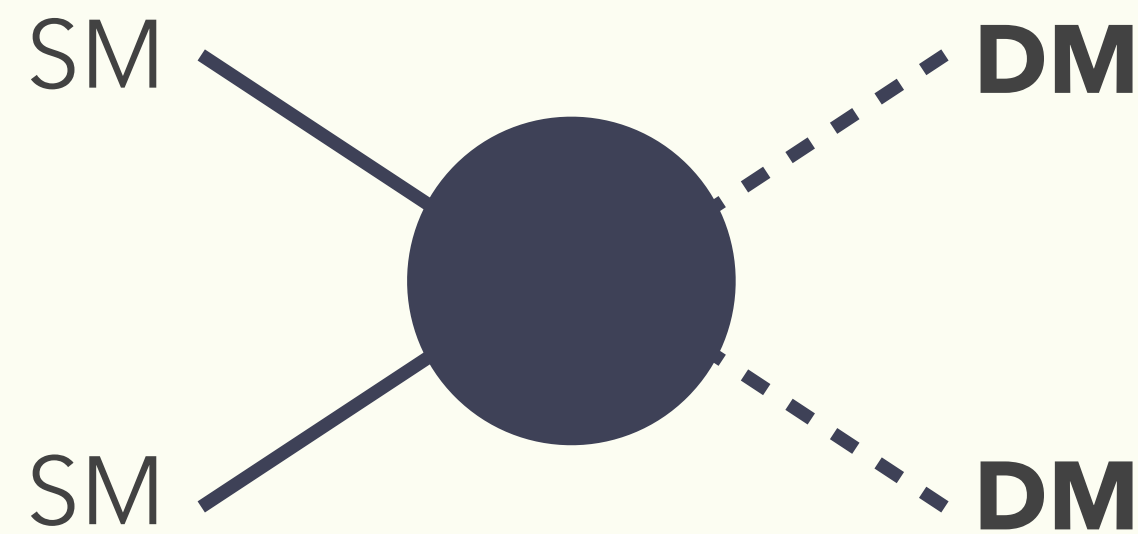
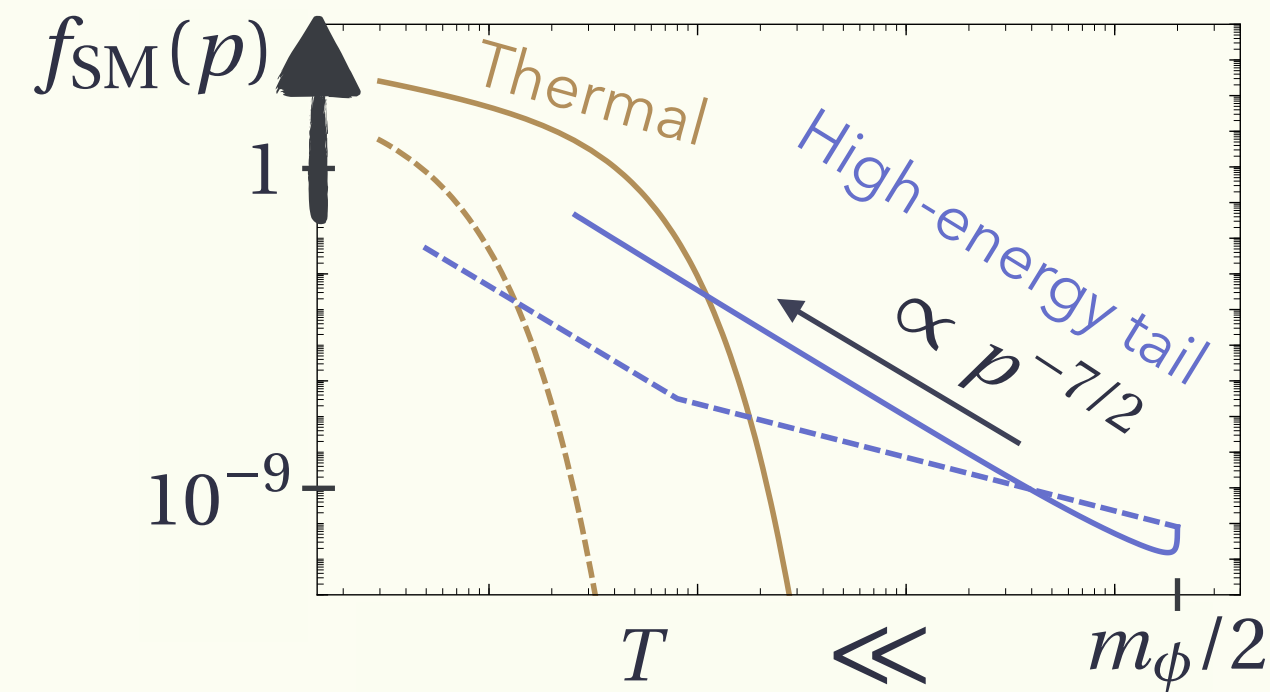
[KM+ 1901.11027; Garcia, Amin '18]



# Implications of Suppressed $T_{\max}$ & Hardtail?

- Non-thermal Dark Matter production of  $m_{\text{DM}} > T_{\text{R}}$

[KM+ 1402.2846, 1901.11027;  
Drees+; Garcia+]



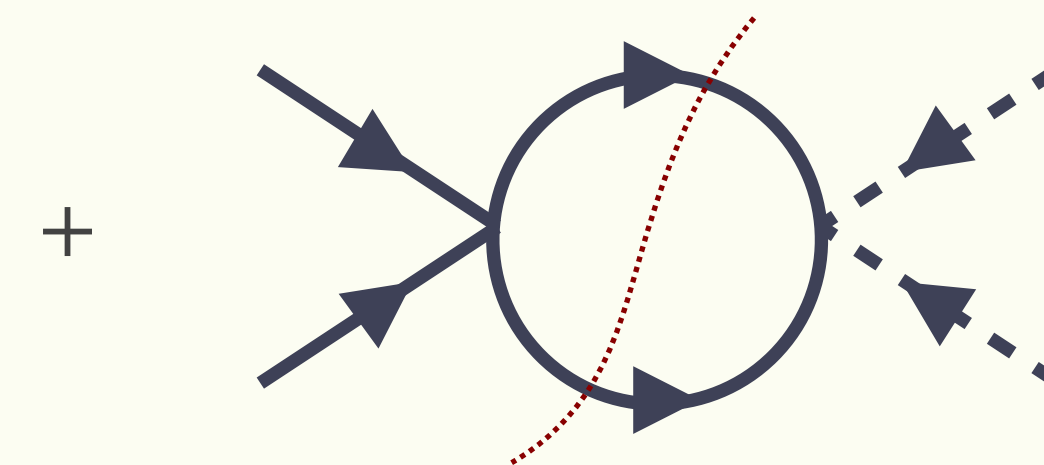
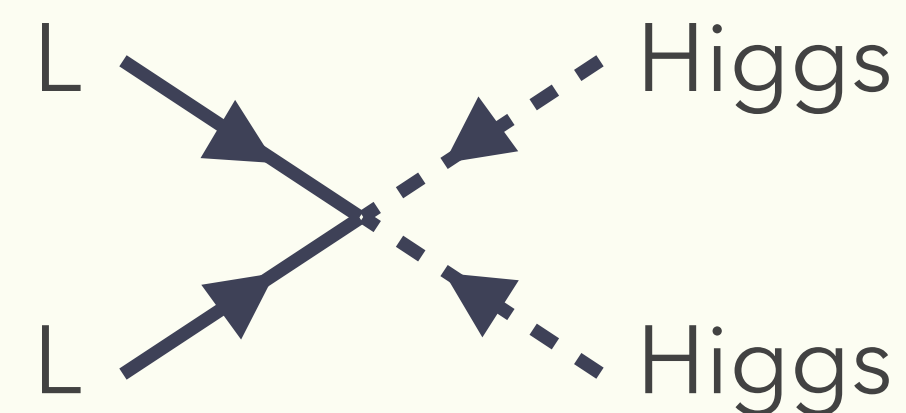
E.g.  $W W \rightarrow \text{DM DM}$

$$\langle \sigma v \rangle \simeq \frac{\alpha_{\text{DM}}^2}{m_{\text{DM}}^2} \quad \Rightarrow \quad \frac{\rho_{\text{DM}}}{s} \simeq 0.11 \alpha_{\text{DM}}^2 \frac{T_{\text{R}}^3}{m_{\text{DM}}^2}$$

"Universal" production

- Leptogenesis of  $M_N > T_{\text{R}}$

[Hamada, Kawana 1510.05186, ...]



- Phase transition ...



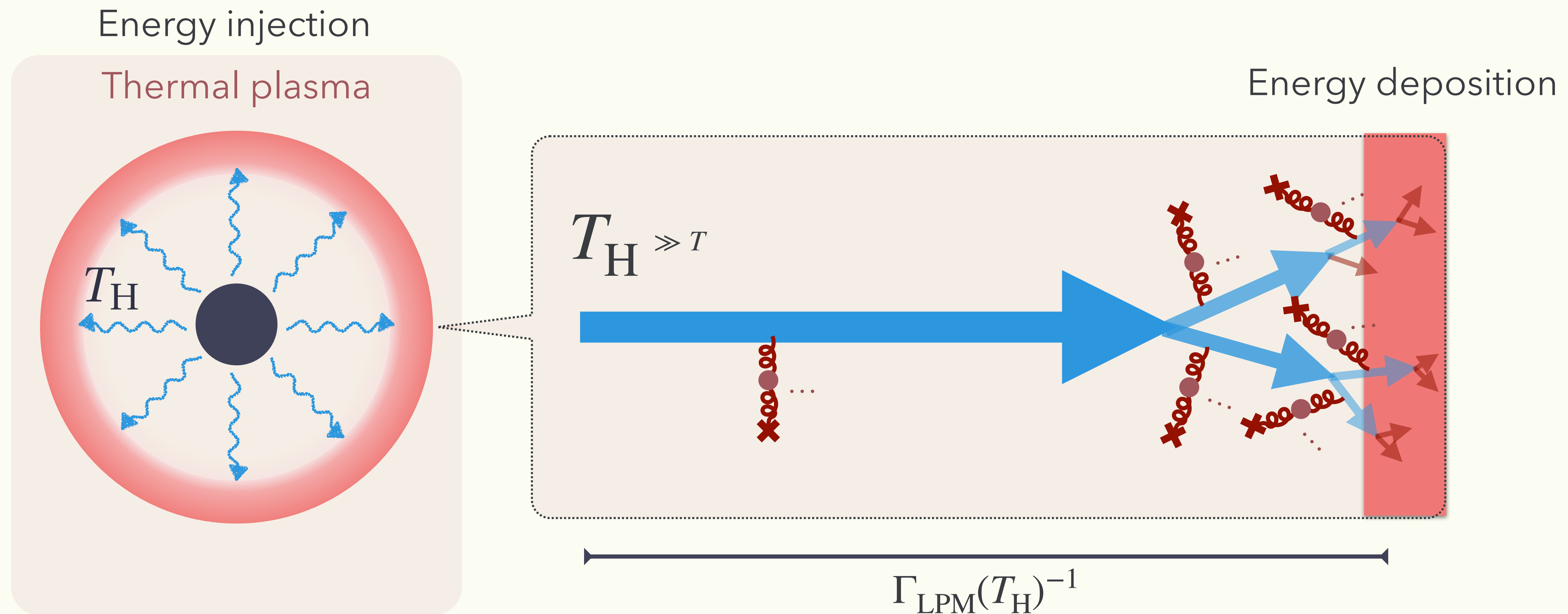
# Evaporation of PBH

(i.e., Inhomogeneous source)

# Formation of Hotspot

[He, Kohri, **KM**, Yamada 2210.06238, 2407.15926]

- Energy injection v.s. Diffusion



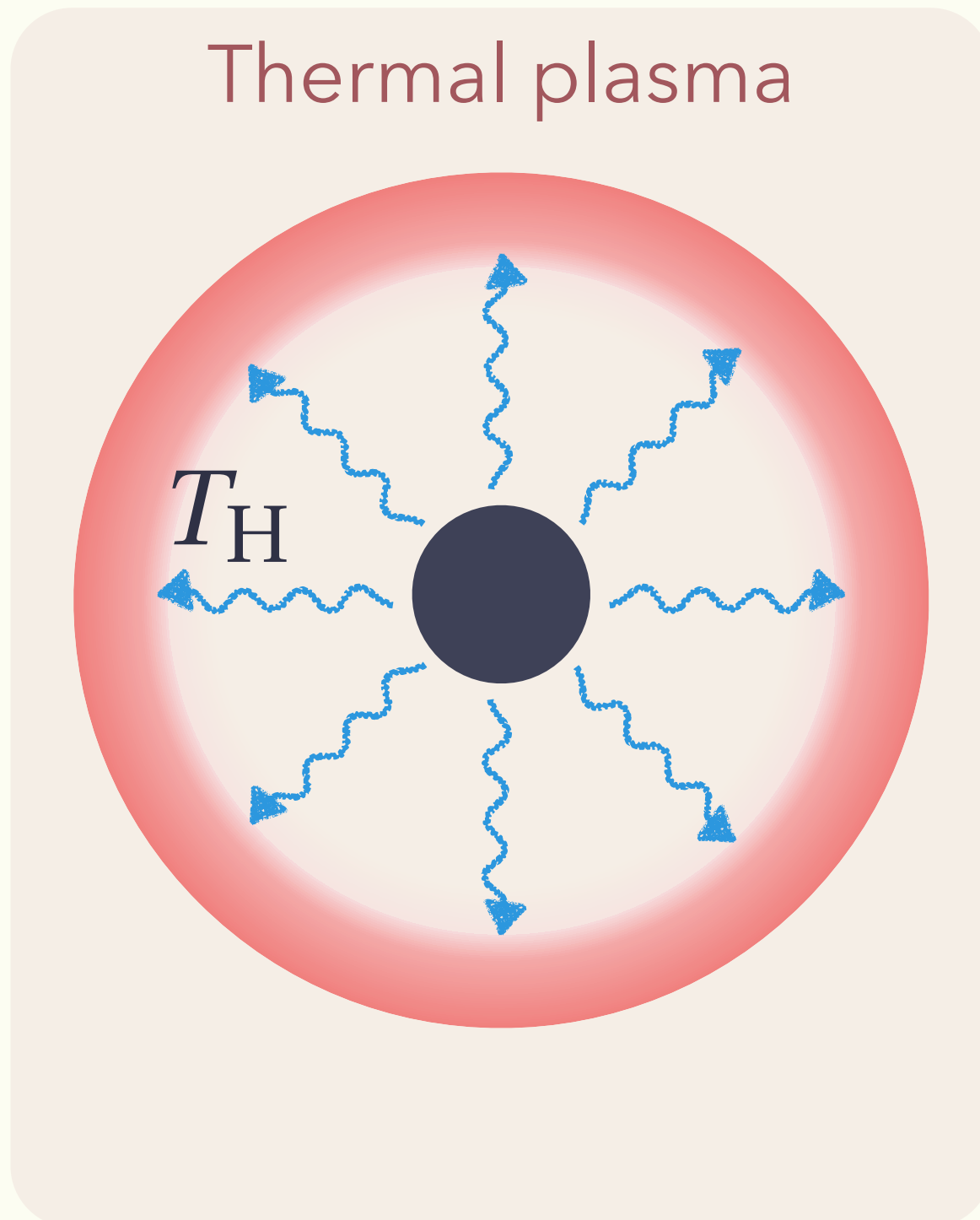
# Formation of Hotspot

[He, Kohri, **KM**, Yamada 2210.06238, 2407.15926]

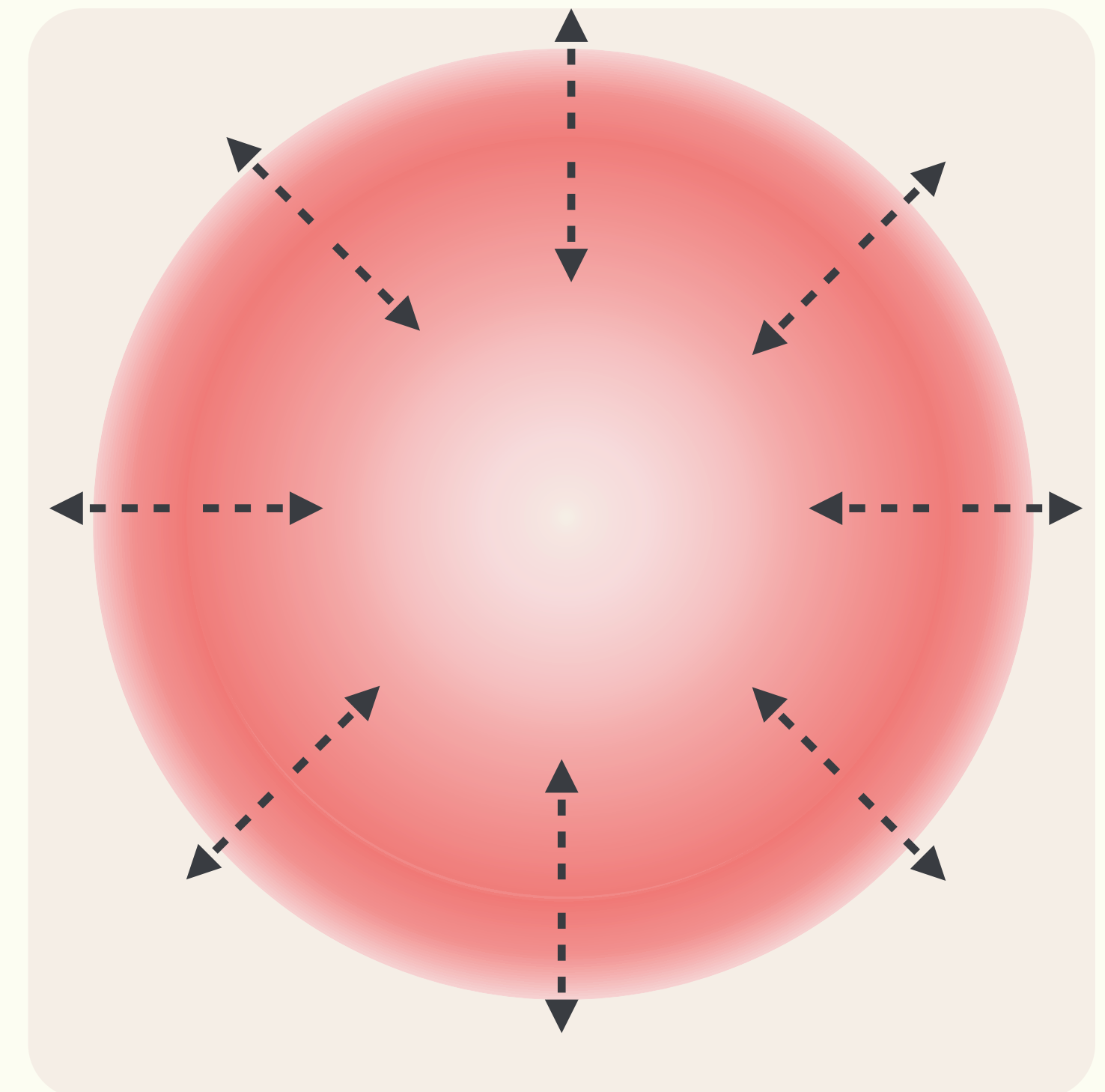
- Energy injection v.s. Diffusion

Energy injection

Thermal plasma



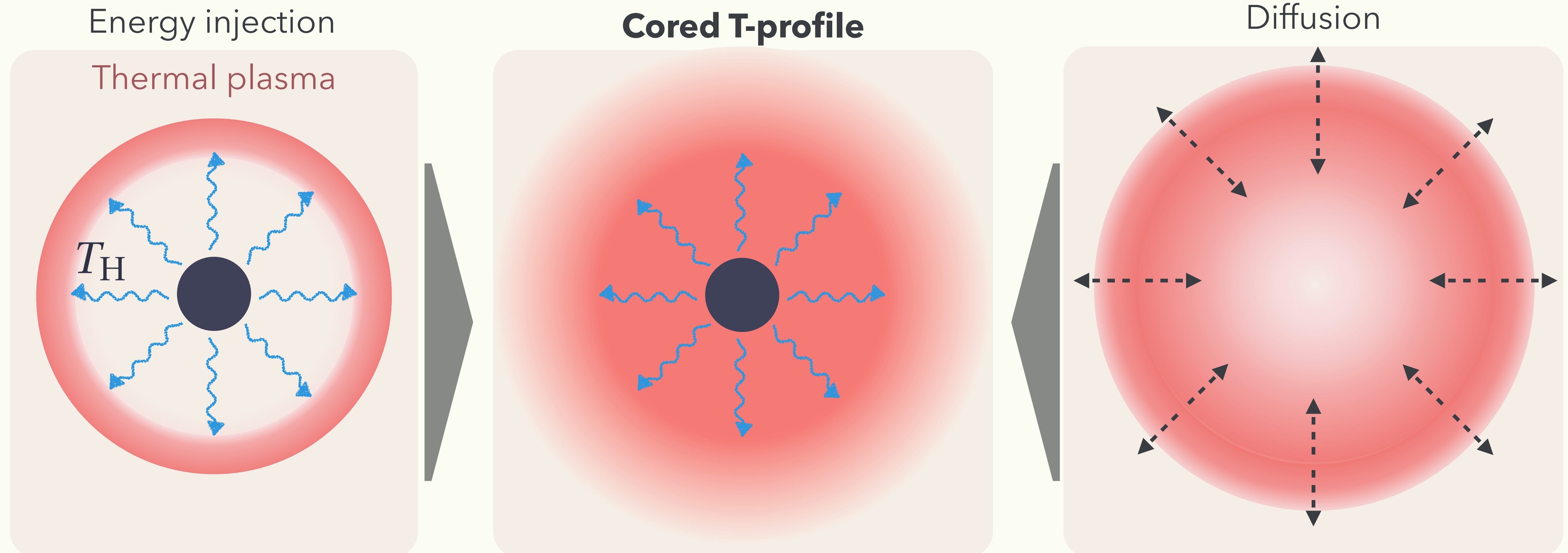
Diffusion



# Formation of Hotspot

[He, Kohri, **KM**, Yamada 2210.06238, 2407.15926]

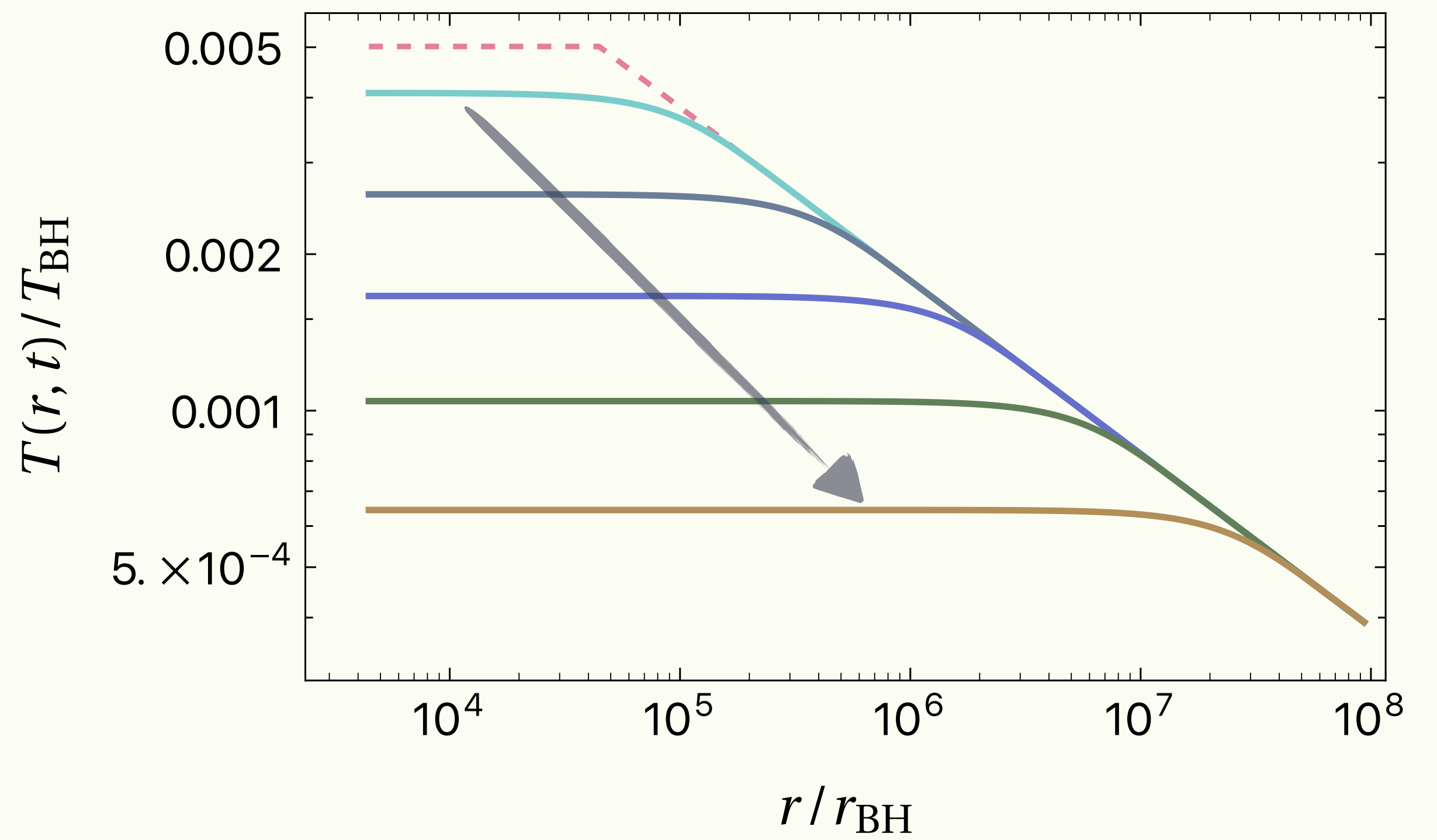
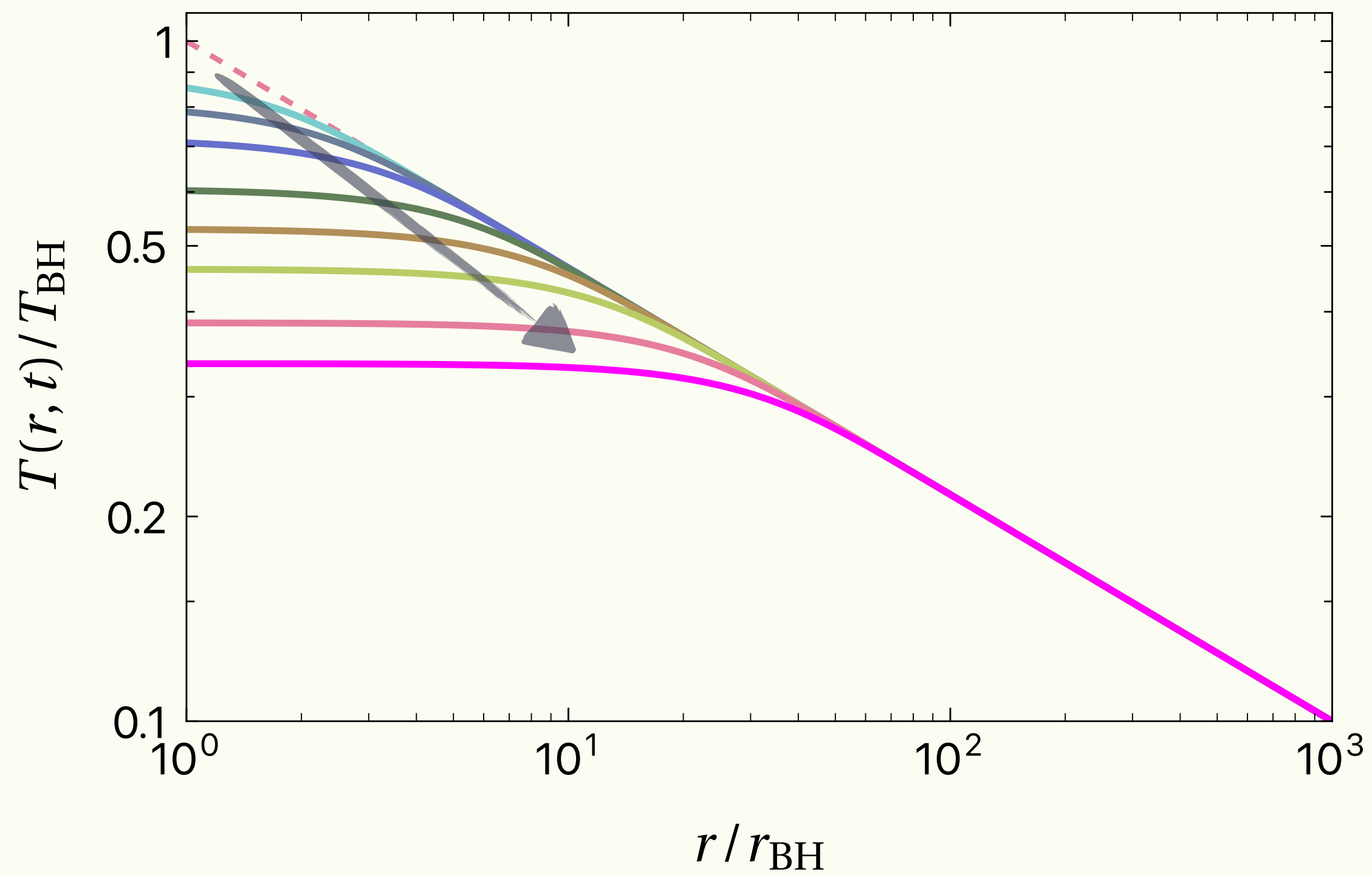
- Energy injection v.s. Diffusion



# Formation of Hotspot

[He, Kohri, **KM**, Yamada 2210.06238, 2407.15926]

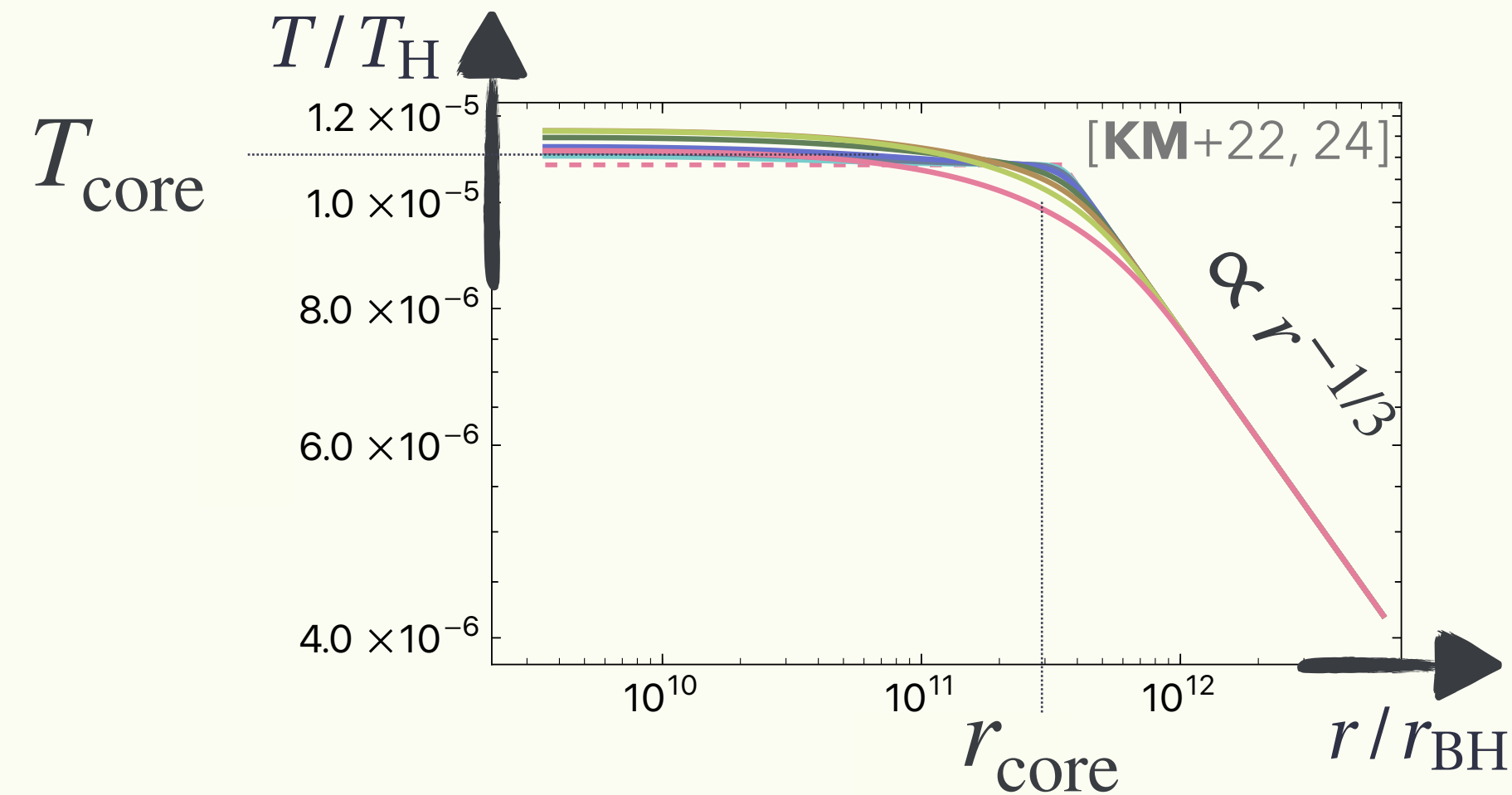
- Evolution towards the attractor



# Formation of Hotspot

[He, Kohri, **KM**, Yamada 2210.06238, 2407.15926]

- **Cored temperature profile** from the LPM suppression

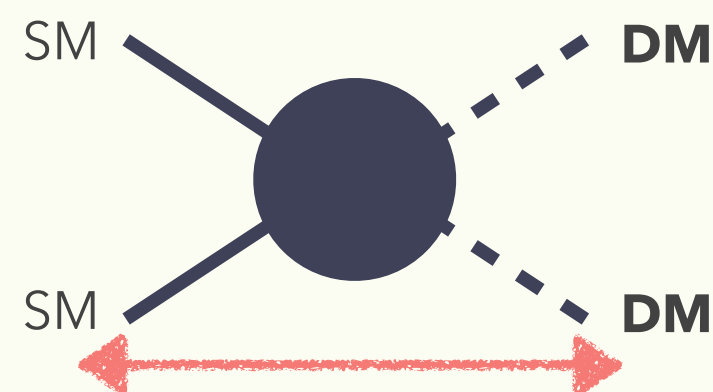


$$T_{\text{core}} \sim 7 \times 10^{-6} \left( \frac{\alpha}{0.05} \right)^{8/3} T_{\text{H}} \lesssim 10^7 \text{ GeV} \left( \frac{\alpha}{0.05} \right)^{19/3}$$

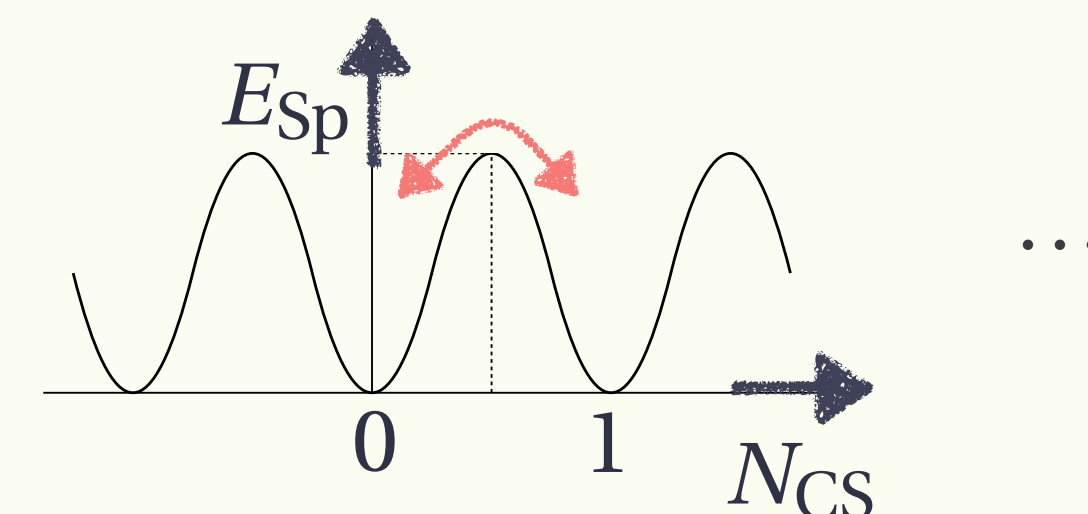
$$r_{\text{core}} \sim 3 \times 10^{11} \left( \frac{\alpha}{0.05} \right)^{-6} r_{\text{BH}}$$

- Potential impacts on physics of  $T$  if  $T_{\text{core}} > T > T_{\text{bkg}}$

Local DM **freeze-out** for  
 $T_{\text{core}} > T_{\text{FO}} > T_{\text{bkg}}$



Local **sphaleron** for  
 $T_{\text{core}} > T_{\text{Sph}} > T_{\text{bkg}}$

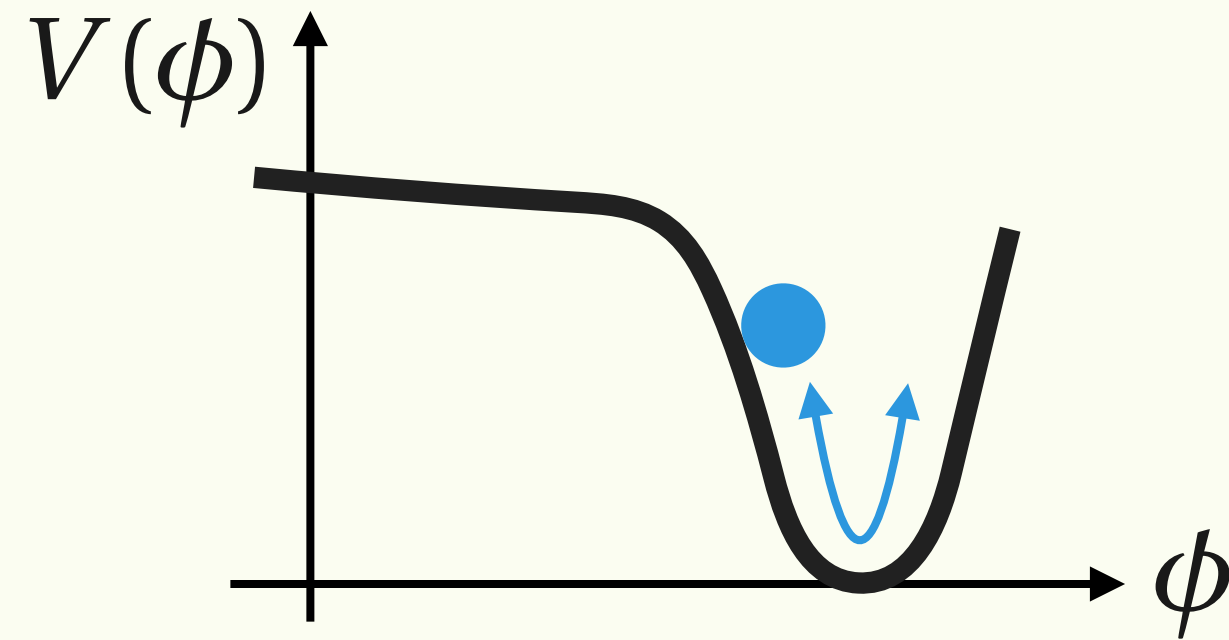
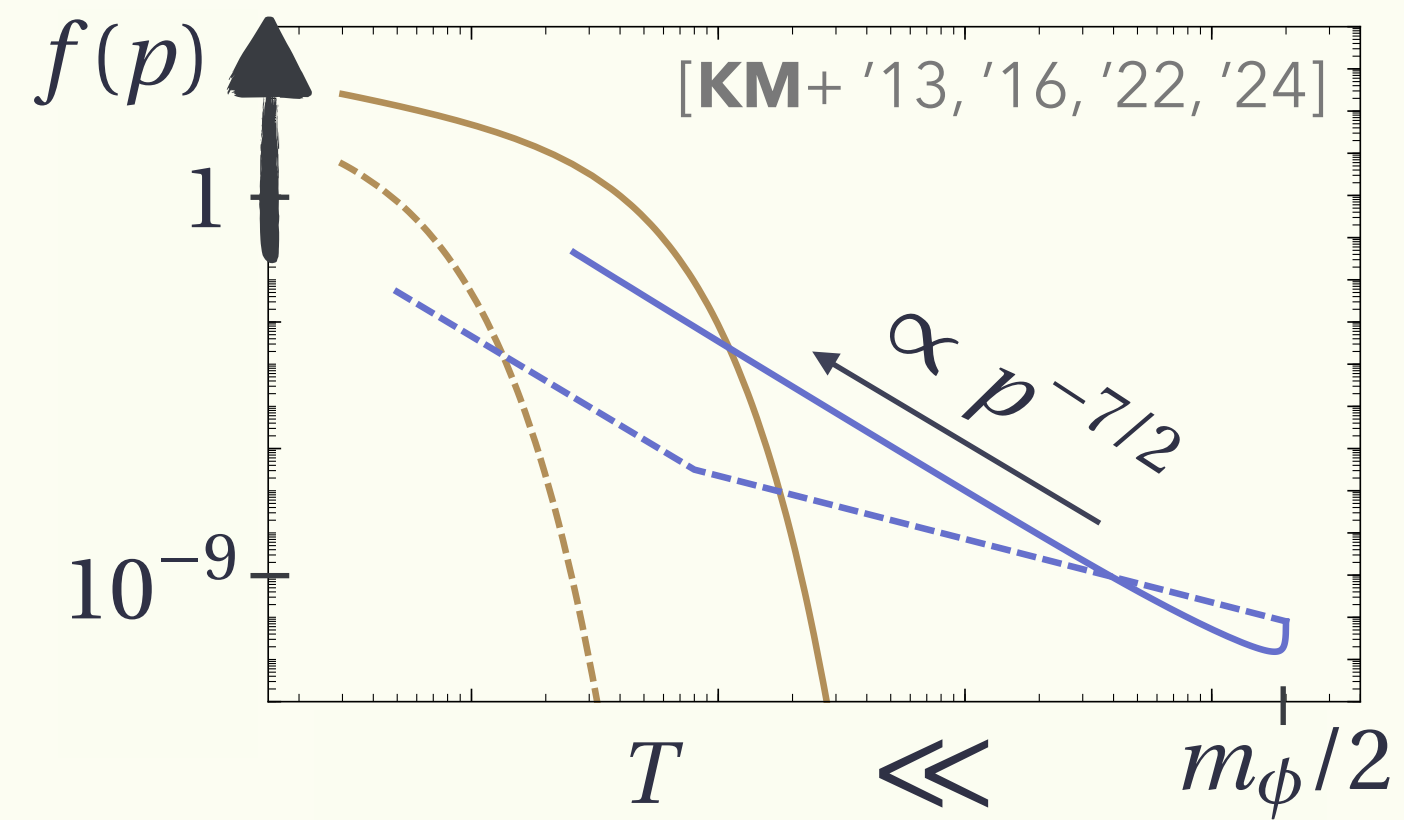


# Summary

[KM, Harigaya 1312.3097; KM, Yamada 1506.07661, 2208.11708, 2402.14054]

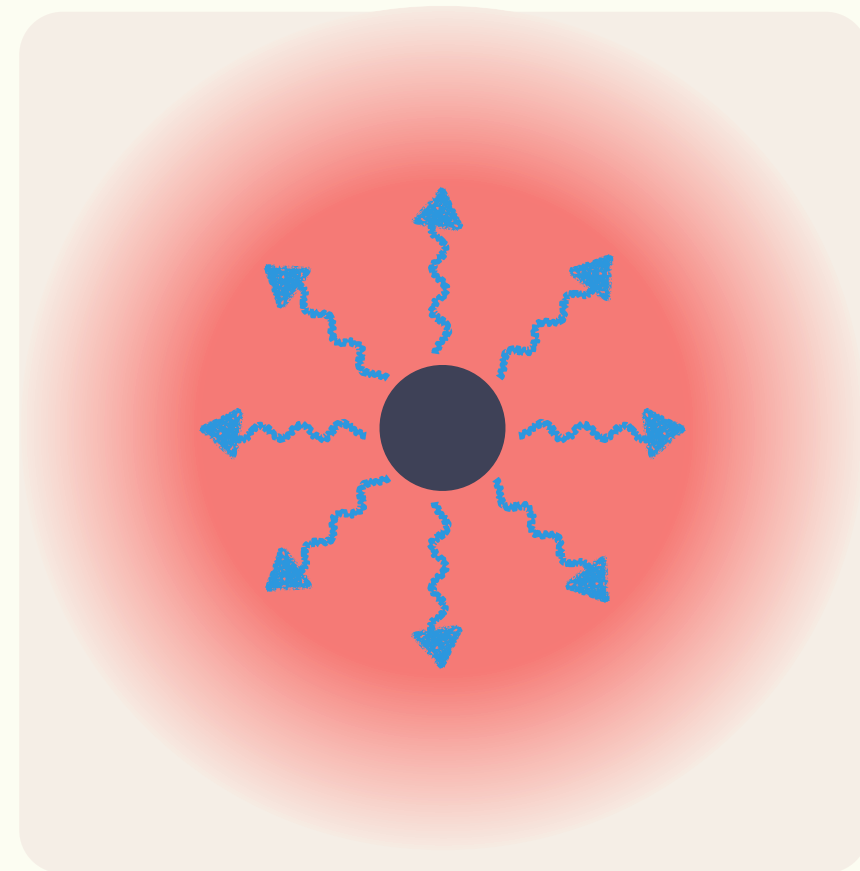
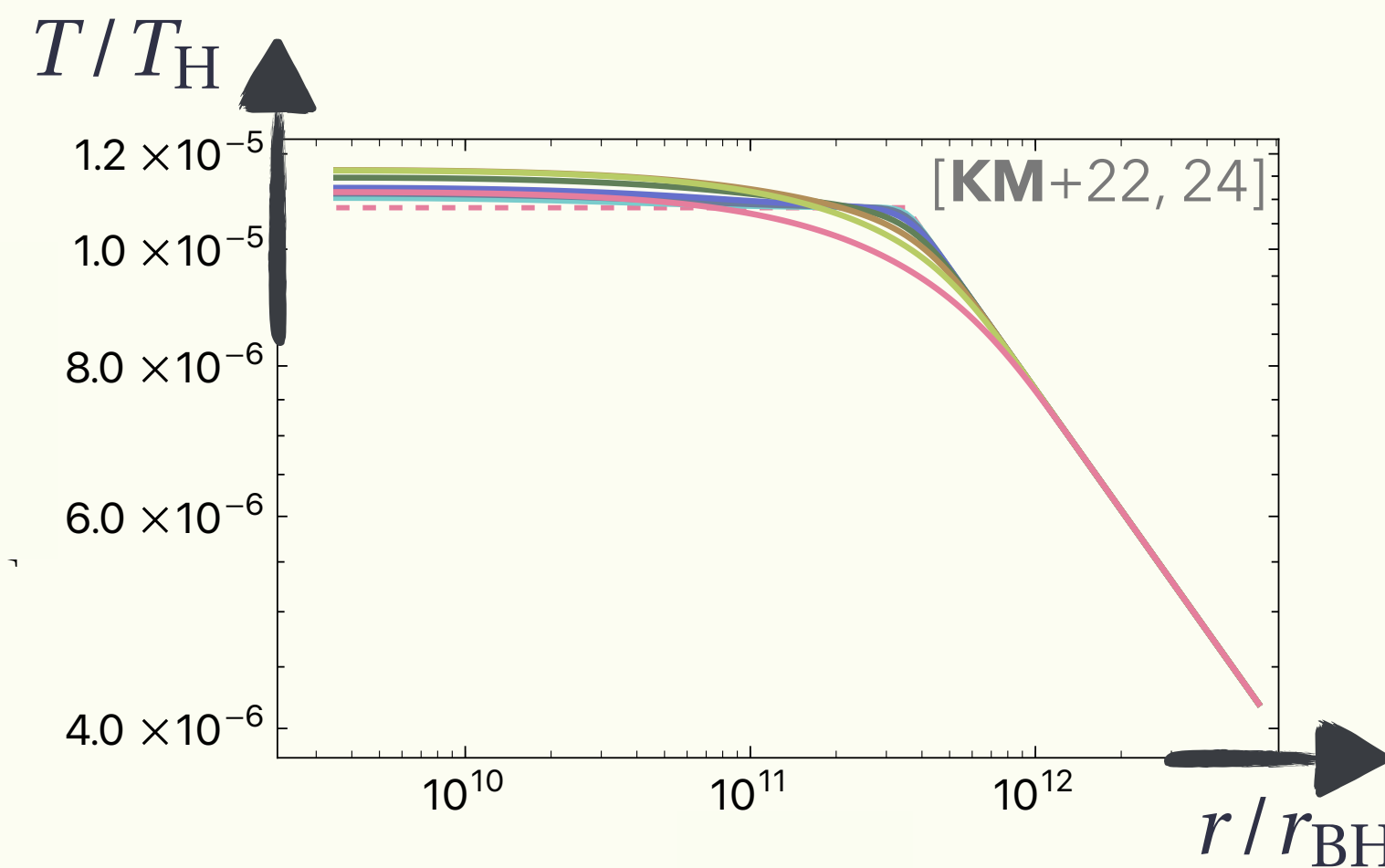
## In-medium cascades (LPM)

- Suppressed  $T_{\max}$  & Universality



w/ **small coupling** to radiation

- Cored T-profile

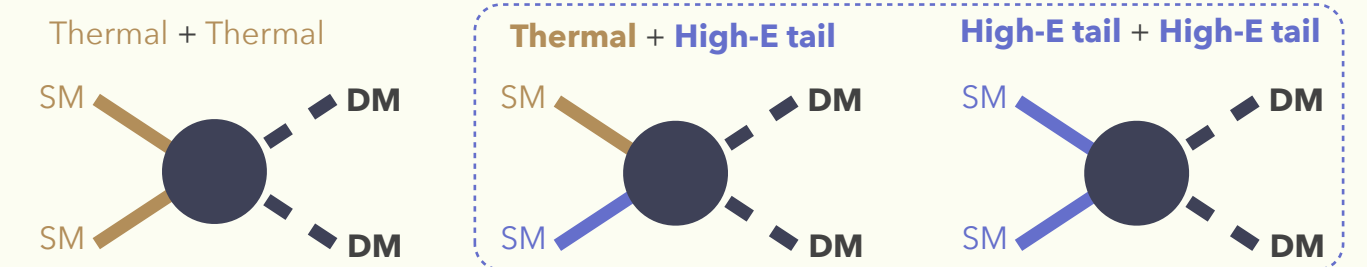


w/ life time  $\ll 1$  s

## Implications

- DM production

[KM+ 1402.2846, 1901.11027; Drees +; Garcia+]

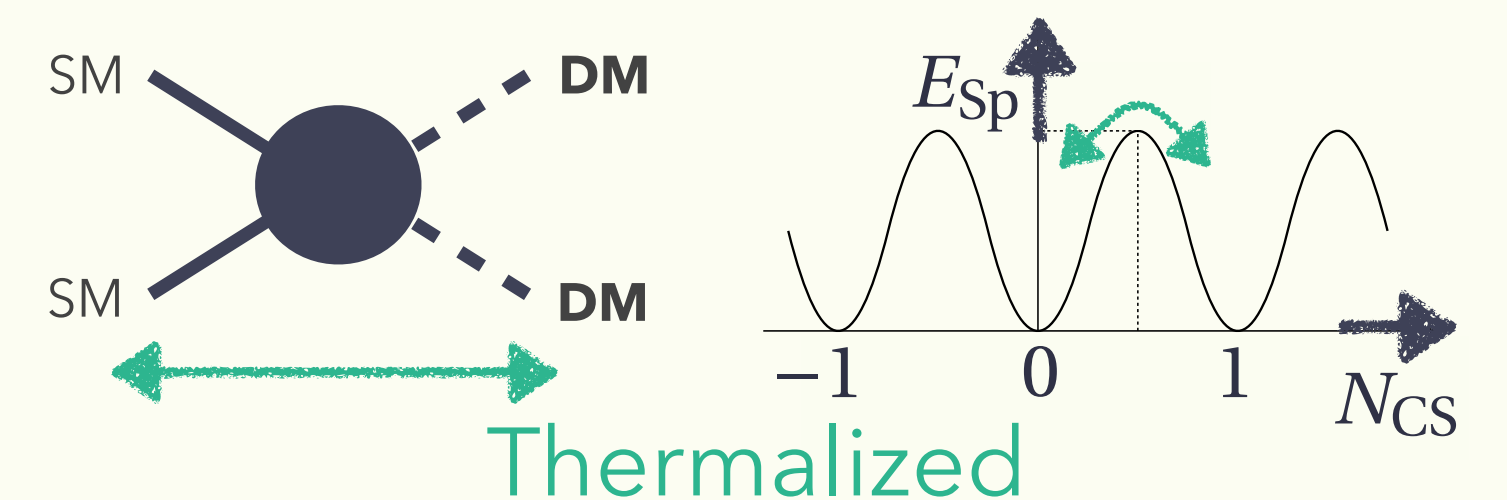


- Baryogenesis

- ...

- Local DM/baryon production

[KM+2210.06238, 2407.15926; Turner+]



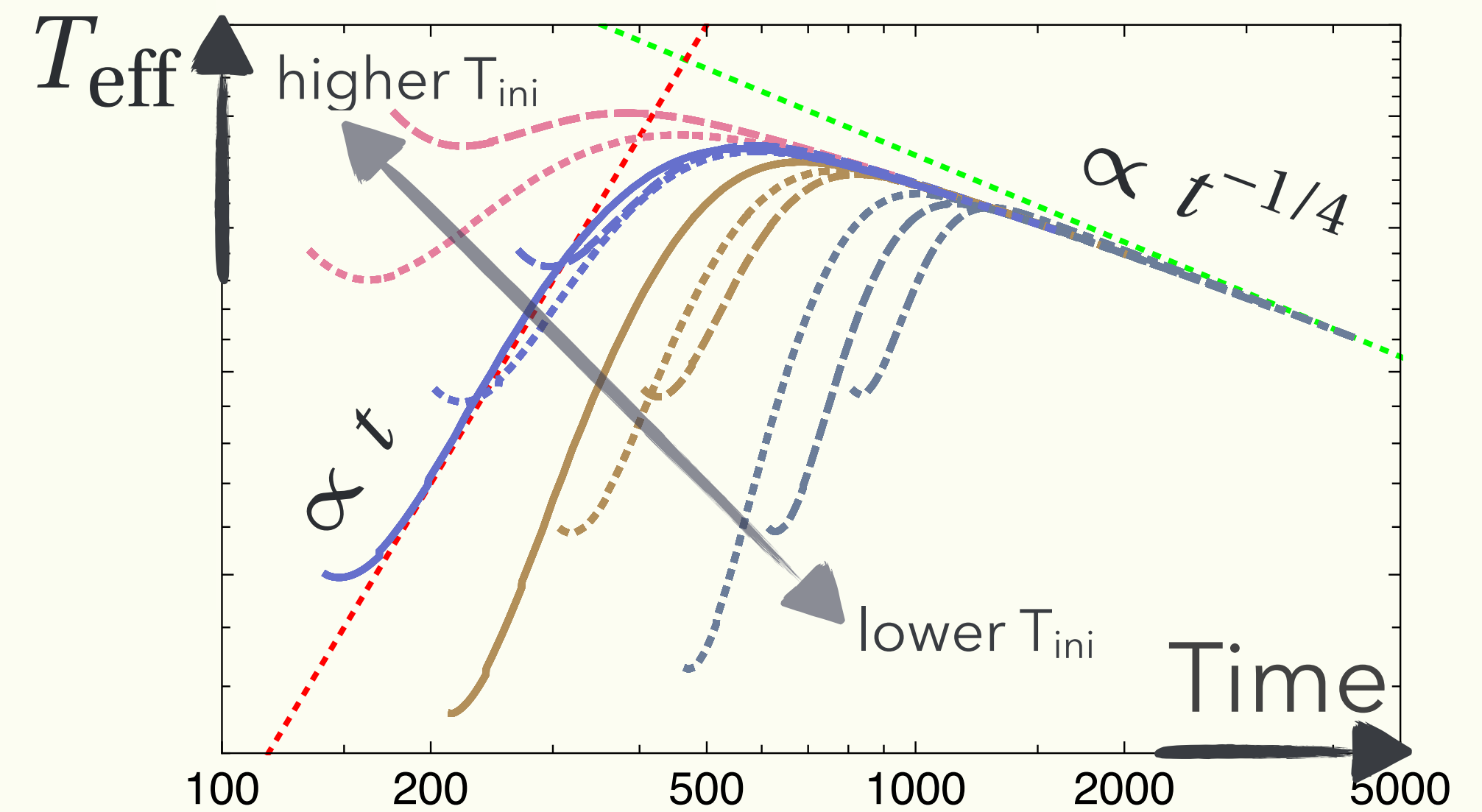
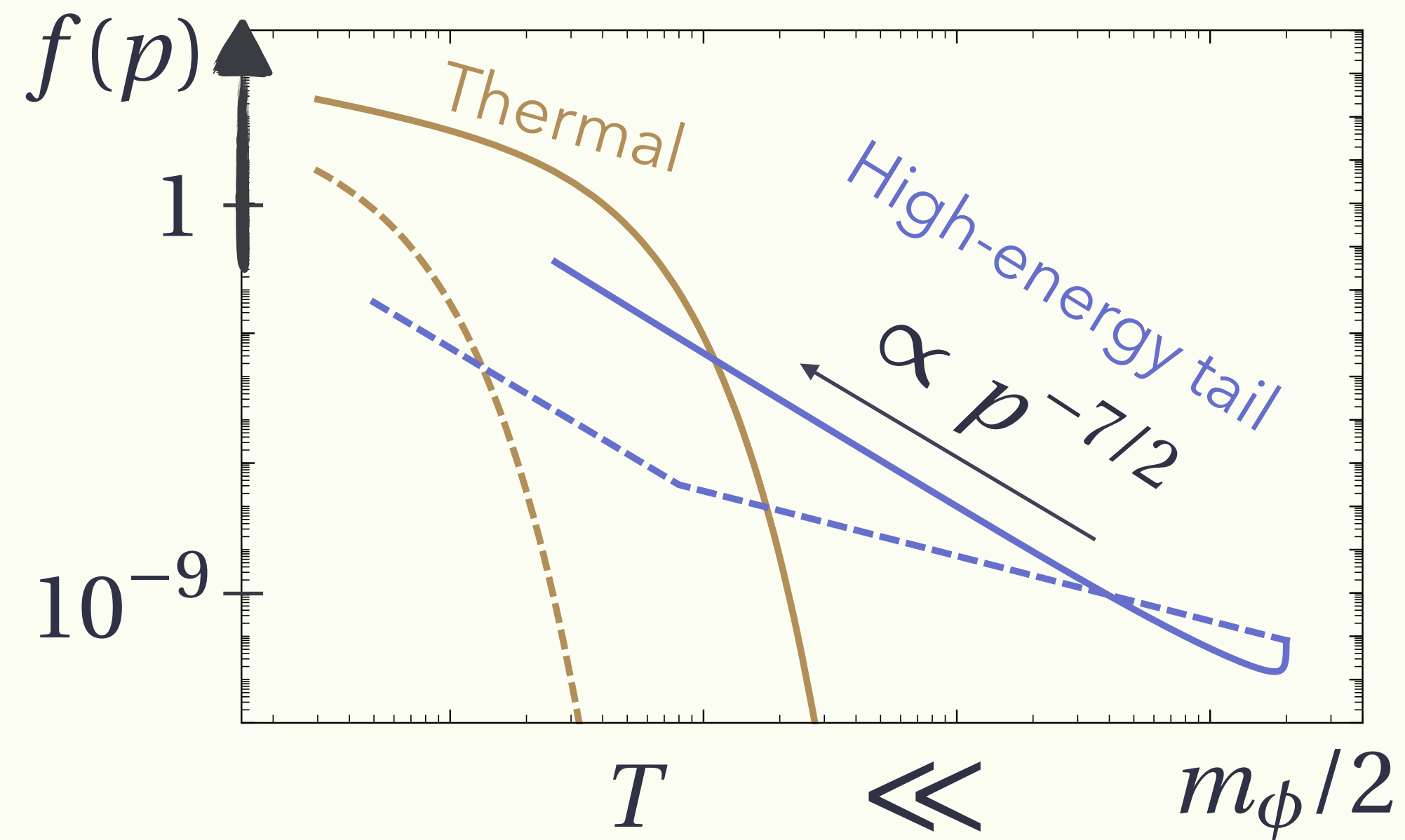
- ...

**Backup**



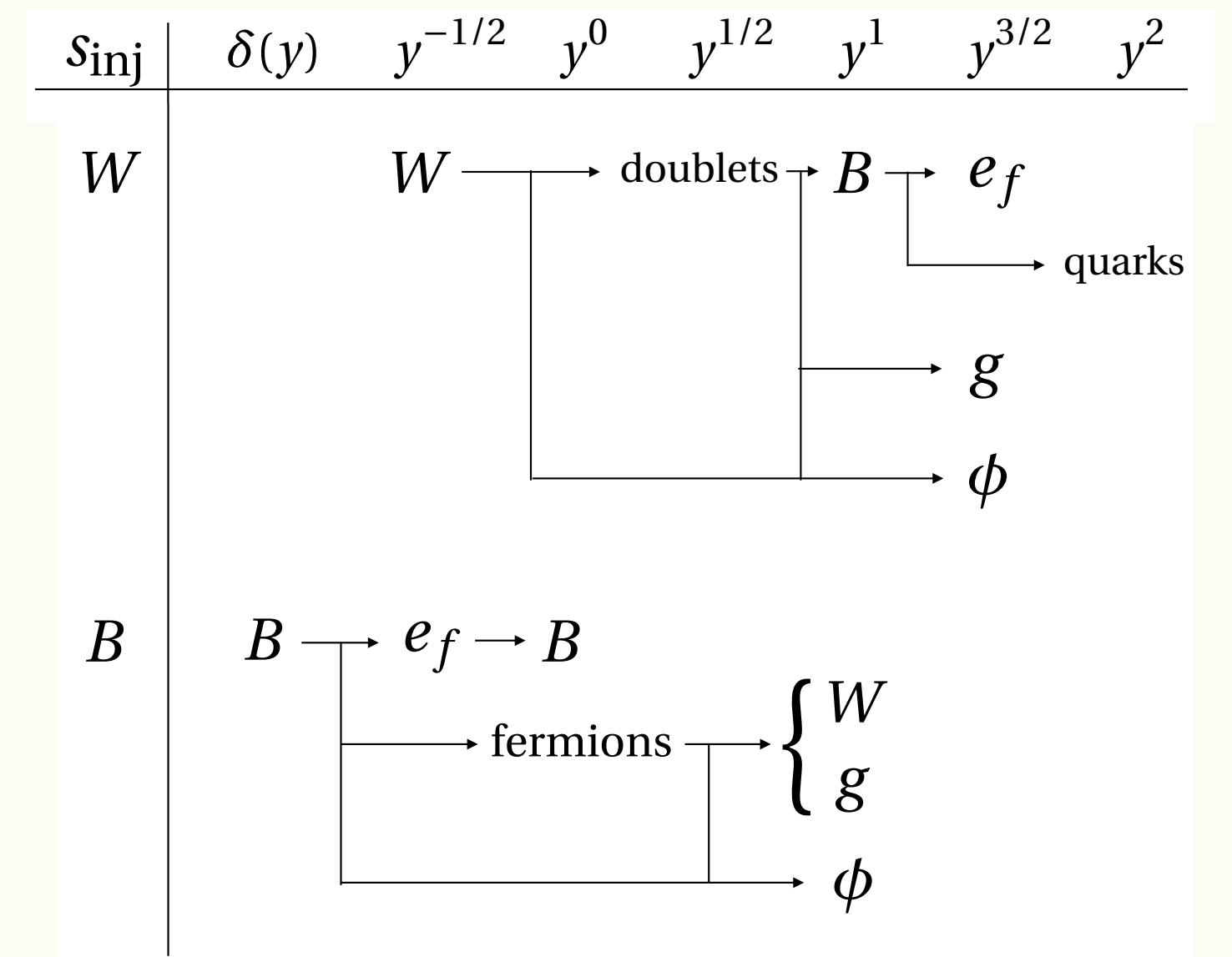
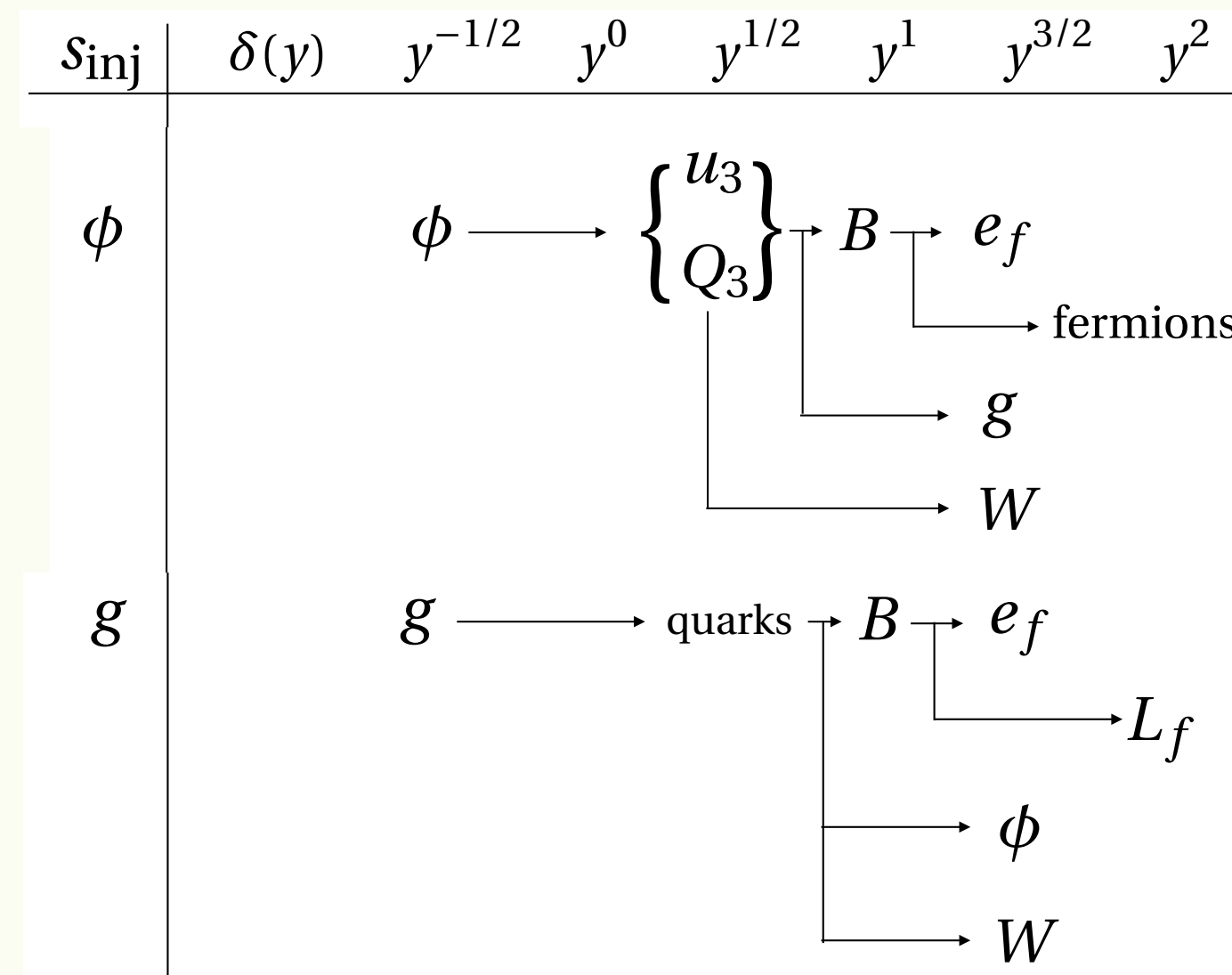
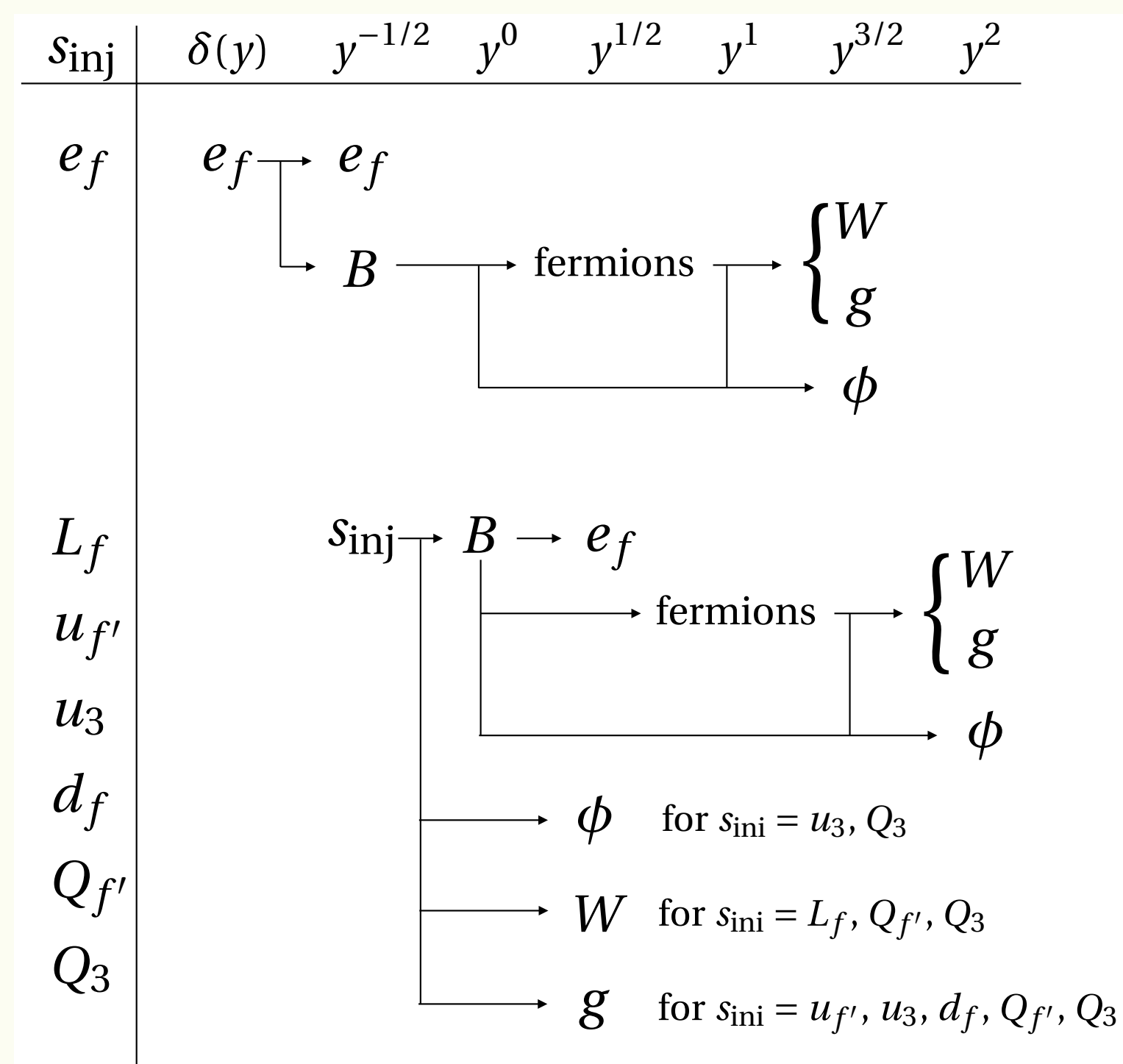
# Inflaton Decays into Pure YM

- Attractor for  $\Gamma_{\text{split}}(m_\phi) \gg H \gtrsim \Gamma_\phi$



# More on splitting functions

- **Splitting** channels in the SM



# More on splitting functions

- IR divergence in the splitting kernel?

$$\mathcal{C}_s^{“1\rightarrow 2”} = -\frac{(2\pi)^3}{p^2 v_s} \sum_{s', s''} \int_0^p dk \gamma_{s \leftrightarrow s' s''}(p; k, p-k) f_s(p) + \frac{(2\pi)^3}{p^2 v_s} \sum_{s', s''} \int_0^\infty dk \gamma_{s' \leftrightarrow s s''}(p+k; p, k) f_{s'}(p+k)$$

$$\gamma_{s \leftrightarrow s' s''}(p; k, p-k) \propto k^{-3/2} \quad \text{for } k \ll p$$

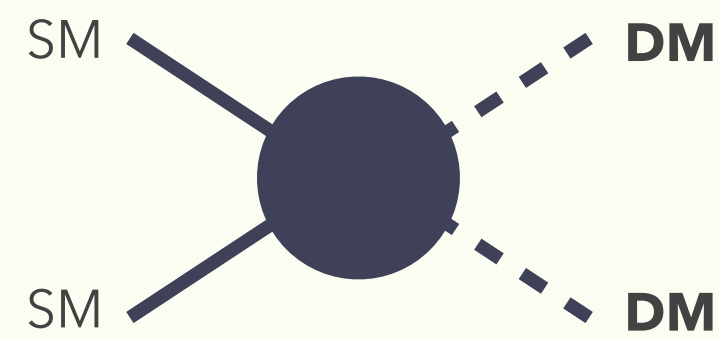
- **The collision term is IR safe!**

$$\int_0^{\epsilon p} dk \gamma_{g \leftrightarrow gg}(p; k, p-k) f_g(p) - \int_0^{\epsilon p} dk \gamma_{g \leftrightarrow gg}(p+k; p, k) f_g(p+k) \quad \text{w/ } f_g(p+k) \simeq f_g(p) + k f'_g(p)$$

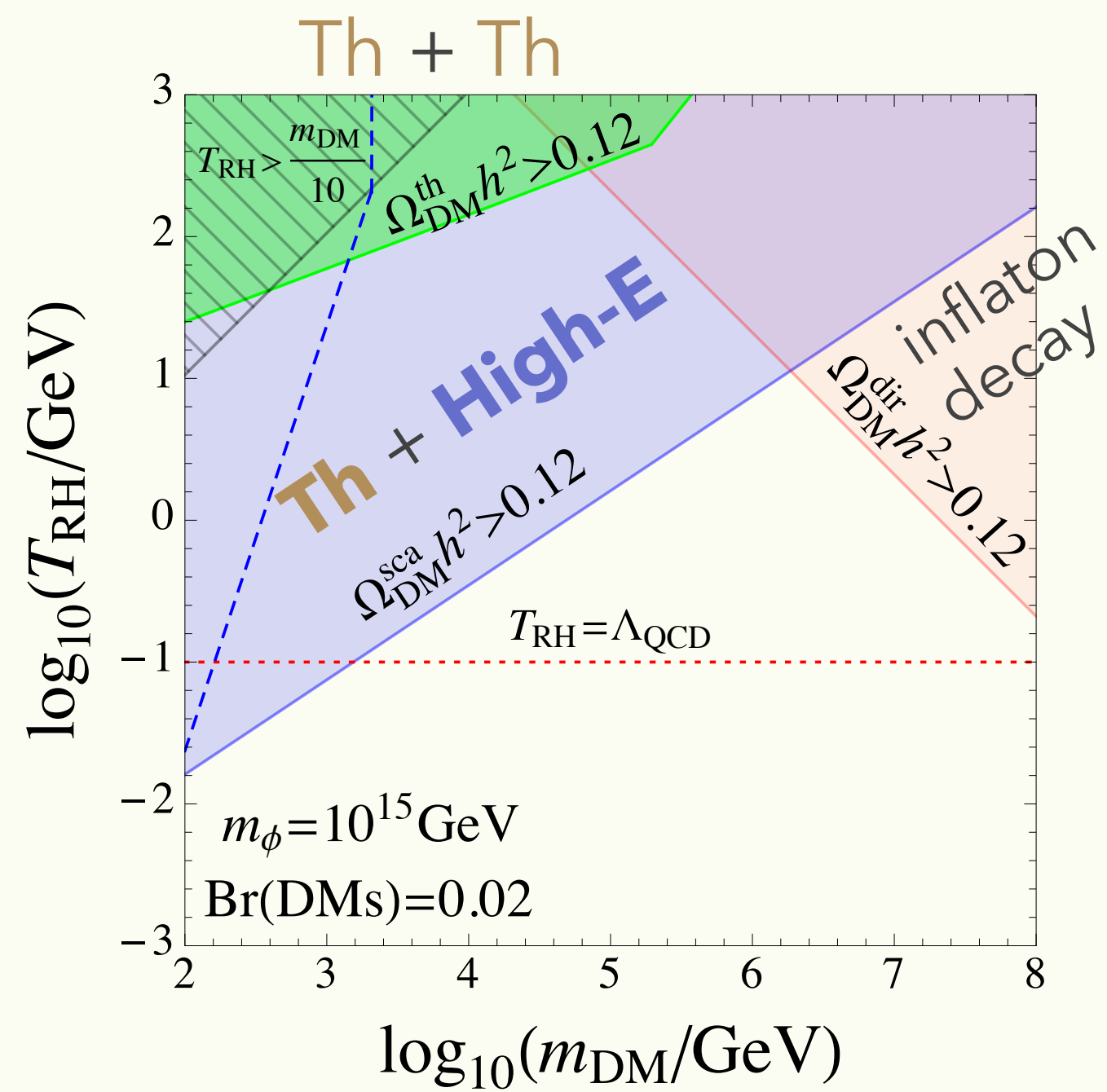
$$\simeq f_g(p) \int_0^{\epsilon p} dk [\gamma_{g \leftrightarrow gg}(p; k, p-k) - \gamma_{g \leftrightarrow gg}(p+k; p, k)] - f'_g(p) \int_0^{\epsilon p} dk k \gamma_{g \leftrightarrow gg}(p+k; p, k).$$

# Non-thermal DM Production

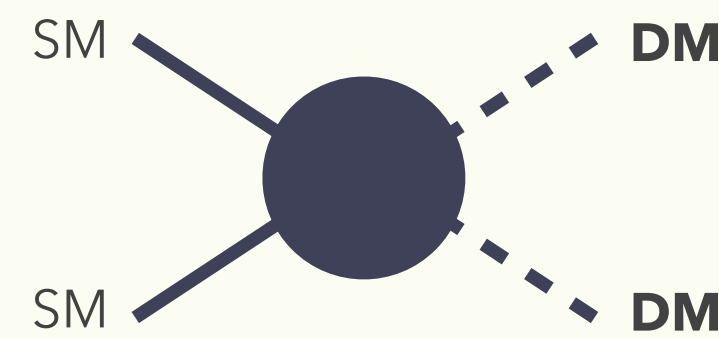
- Non-thermal DM production via SM SM to DM DM



$$\langle \sigma v \rangle \simeq \frac{\alpha_{\text{DM}}^2}{m_{\text{DM}}^2}$$

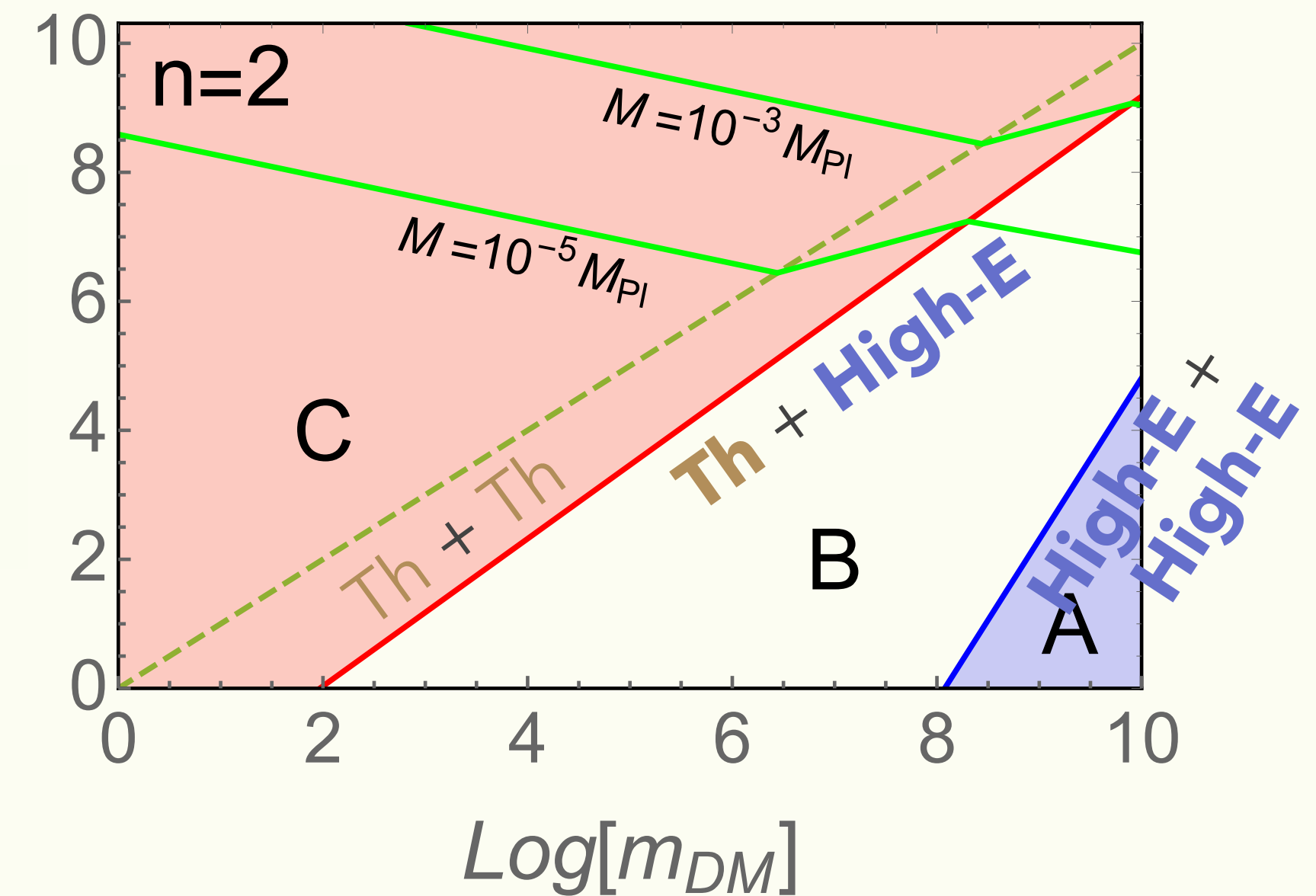


[KM+ 1402.2846]



$$\langle \sigma v \rangle = \frac{E_{\text{CM}}^n}{M^{n+2}}$$

$$w/ M \gtrsim m_{\text{inf}}$$



[KM+ 1901.11027]

# Some details after $t \gtrsim t_{\text{ev}}$

- Comparison of time scales during the hotspot formation

$$t_{\text{th}} \sim \alpha^{-2} T^{-1} \sqrt{T_{\text{H}}/T} \lesssim t_{\text{d}} \sim \alpha^{-2} T^{-1} (T_{\text{H}}/T) \lesssim t_{\text{ev}} \sim M_{\text{Pl}}^2 / T_{\text{H}}^3$$

- What is  $r_{\text{dec}}$ ? → diffusion length @  $t \sim t_{\text{ev}}$ :  $r_{\text{dec}} \sim 10 \text{ cm} \left(\frac{\alpha}{0.1}\right)^{-\frac{8}{5}} \left(\frac{T_{\text{H}}}{10^4 \text{ GeV}}\right)^{-\frac{11}{5}}$   
 → local thermal eq. w/in  $r < r_{\text{dec}}$

