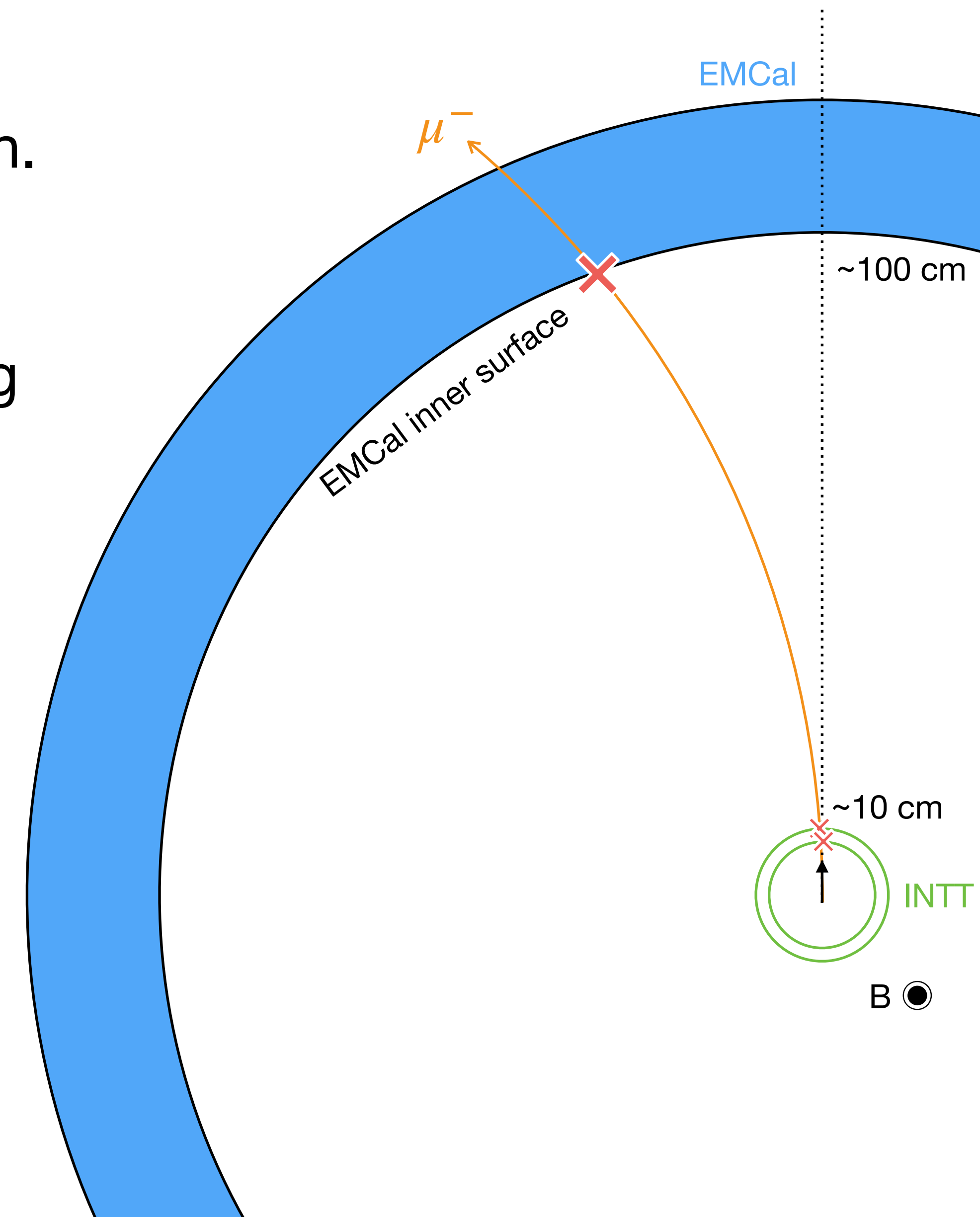


φ resolution study by MC

Genki Nukazuka (RIKEN)

Single μ^- MC for angle resolution evaluation

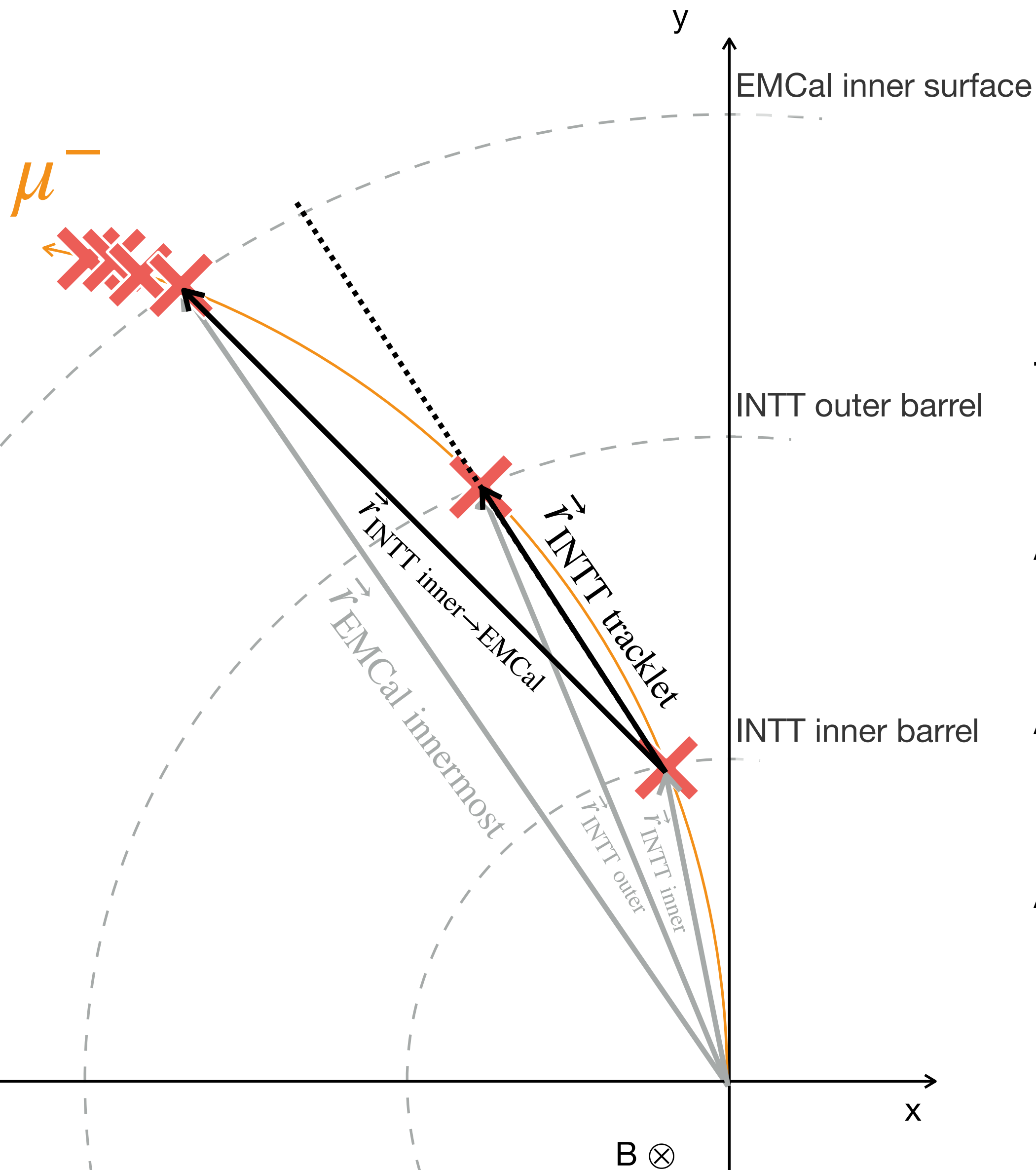
- It must be useful if we can estimate hit position on the inner surface of EMCal using INTT hit information.
- We can make such rough estimation table from single μ MC.
- The uncertainty of the estimation is a hint of tracking resolution.



Basic idea of angular resolution evaluation

Note: Currently,

$$\vec{r} = \vec{r}_{\text{mes.}} - \vec{r}_{\text{vertex}} \Big|_{\vec{r}_{\text{vertex}}=(0,0,0)} = \vec{r}_{\text{mes.}}$$



EMCal hit: the innermost (smallest ρ) G4Hit on EMCal

$$\vec{r}_{\text{EMCal innermost}}$$

INTT tracklet vector: a line from G4Hit on the inner barrel to that on the outer

$$\vec{r}_{\text{INTT tracklet}} = \vec{r}_{\text{INTT outer}} - \vec{r}_{\text{INTT inner}}$$

A vector from INTT inner barrel to EMCal hit:

$$\vec{r}_{\text{inner} \rightarrow \text{EMCal}} = \vec{r}_{\text{EMCal}} - \vec{r}_{\text{inner}}$$

Angle resolution evaluator:

$$\Delta\phi = \phi_{\text{inner} \rightarrow \text{EMCal}} - \phi_{\text{INTT tracklet}}$$

Angle resolution:

$$\frac{\sigma_{\Delta\phi}}{|\mu_{\Delta\phi}|},$$

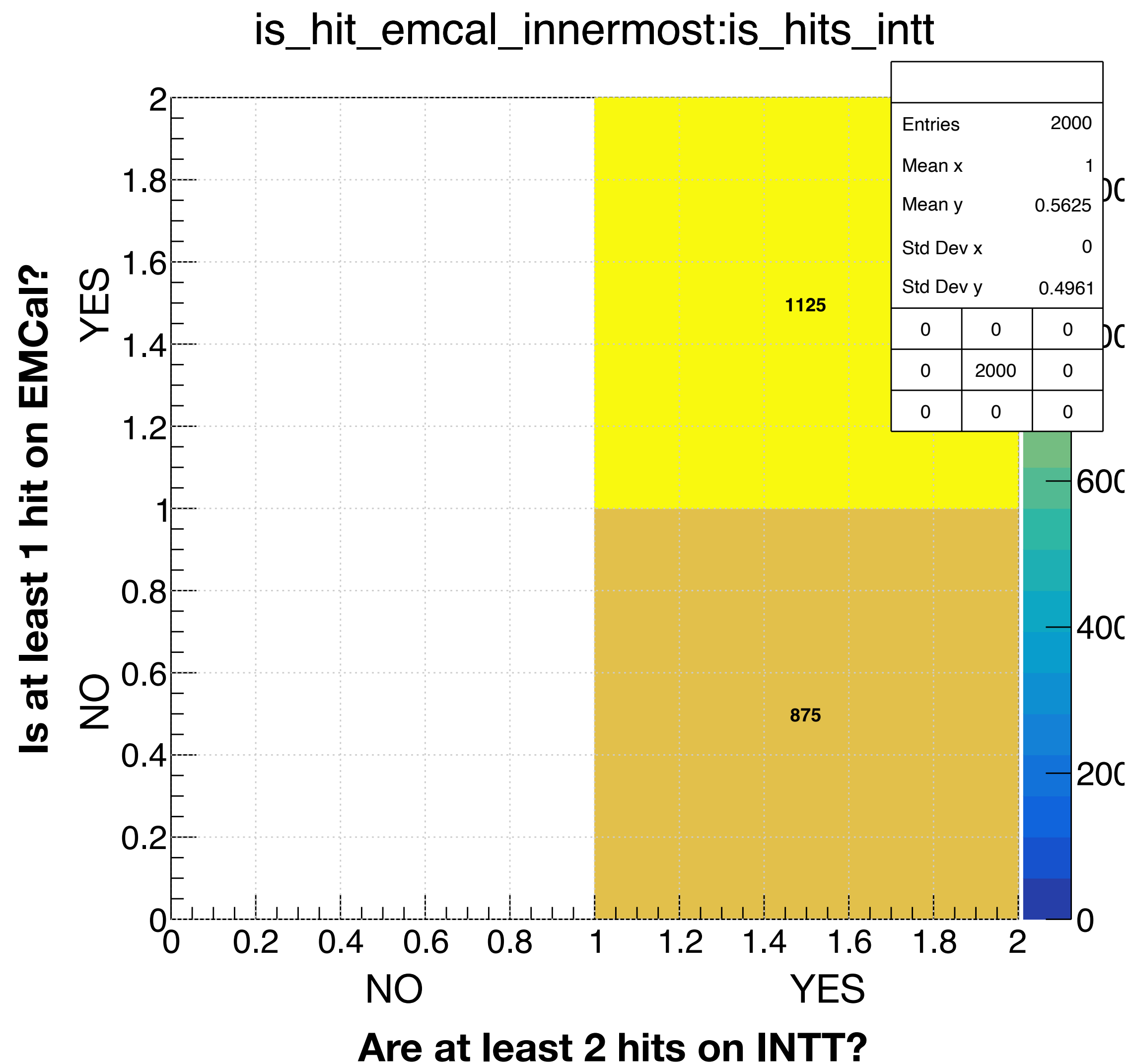
where μ and σ are determined by gaussian fit to $\Delta\phi$ distribution

Pilot run: Condition

Setup:

- Single μ^- MC with $\vec{p} = (0, 1, 0)$ GeV/c
 - i.e. no angular distribution
- $\vec{r}_{\text{vertex}} = (0,0,0)$ cm
- Beam pipe, MVTX, INTT, TPC, TPOT, and EMCal are in the simulation.
- 2000 events
 - It took long time. Is 80 min / 100k OK?

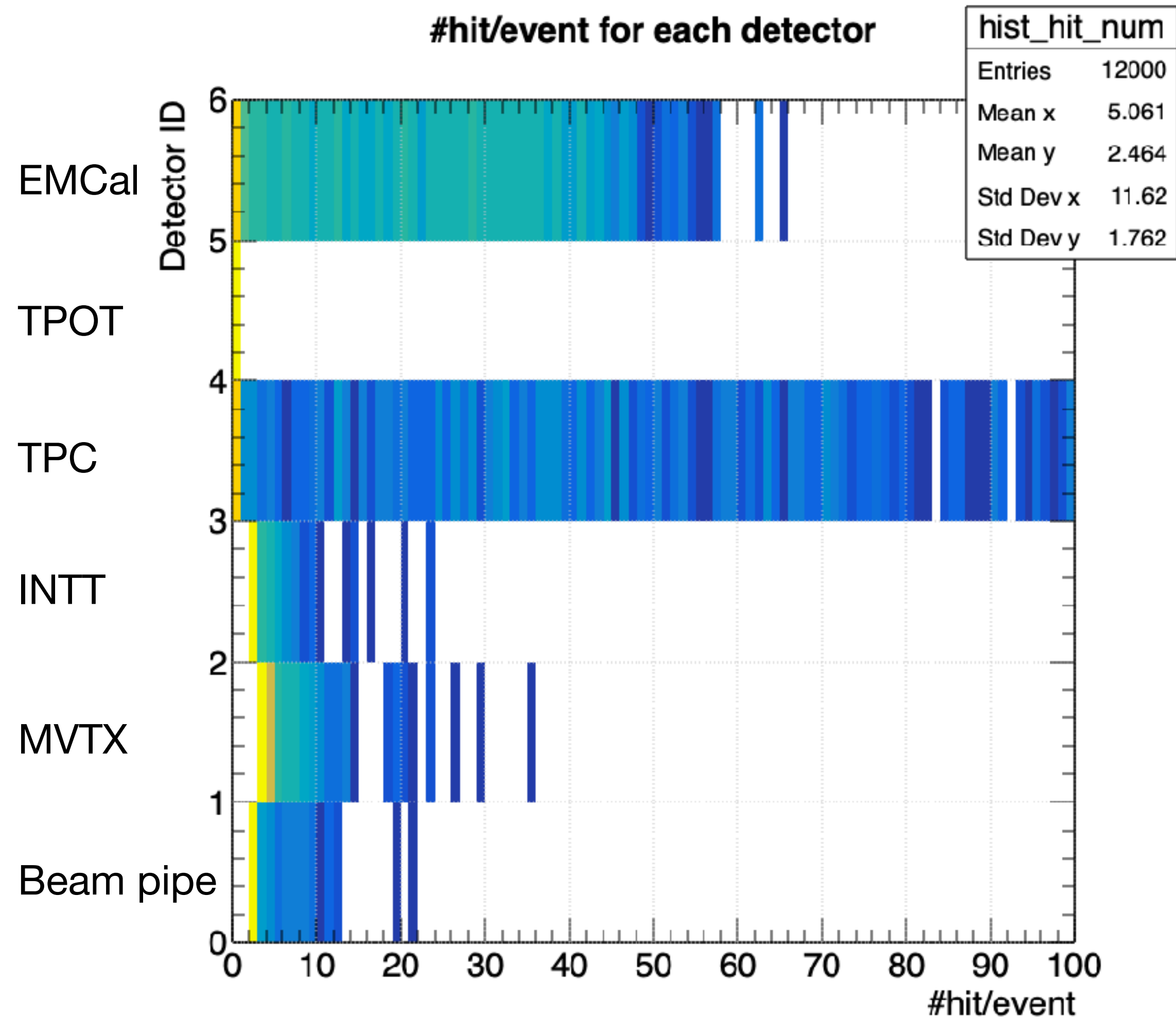
Pilot run: is a hit on INTT/EMCal?



← Events in this row: no G4hit on EMcal

Why was no hit made on EMCal for large fraction of events?

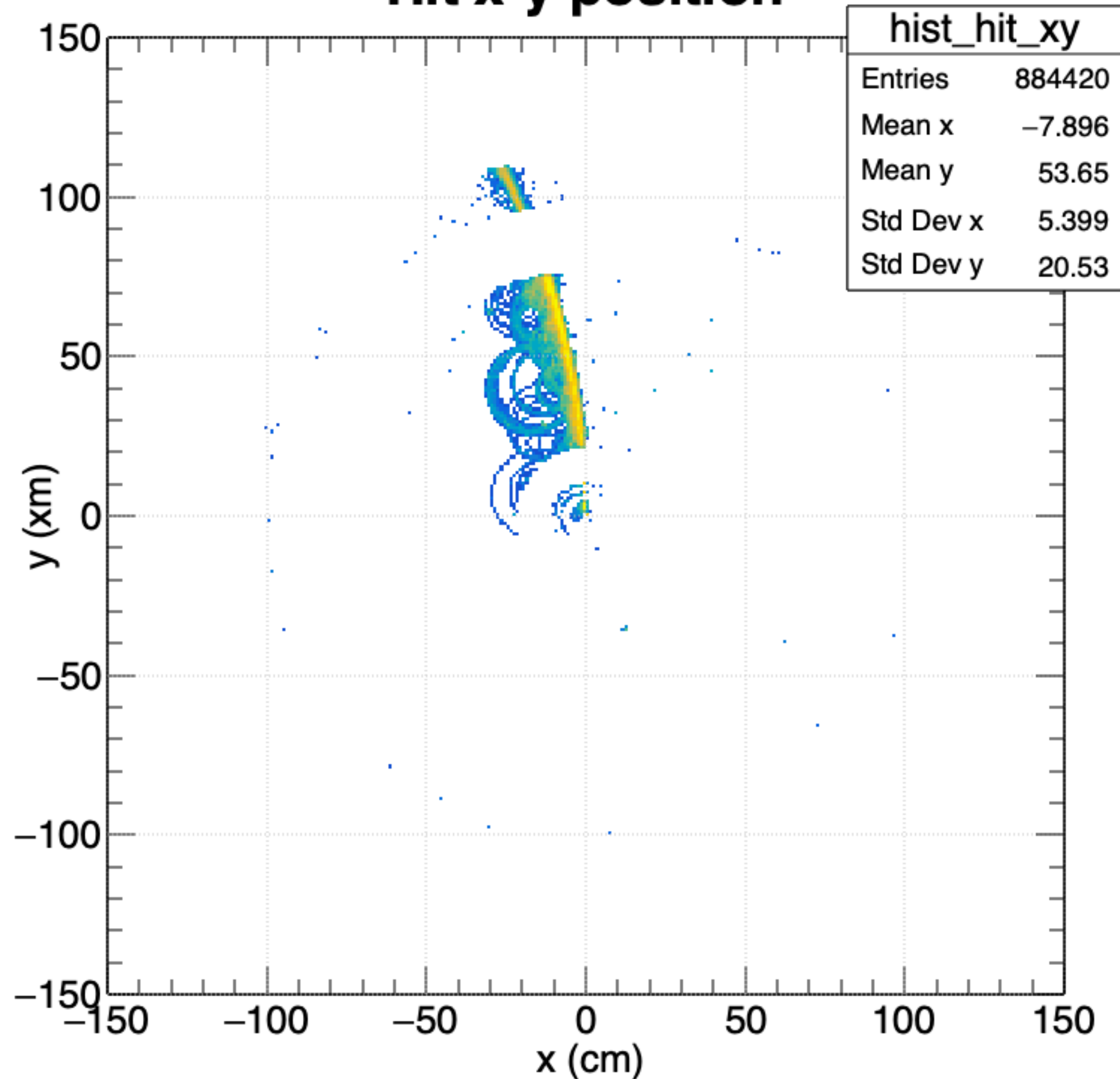
Pilot run: #G4hit for each detector



TPC also has no hit for 40% of events.

Pilot run: #G4hit position

Hit x-y position



x vs y position of G4hit. No event/hit selections were applied.

2000 events are accumulated.

Trajectory of muons are clearly seen.

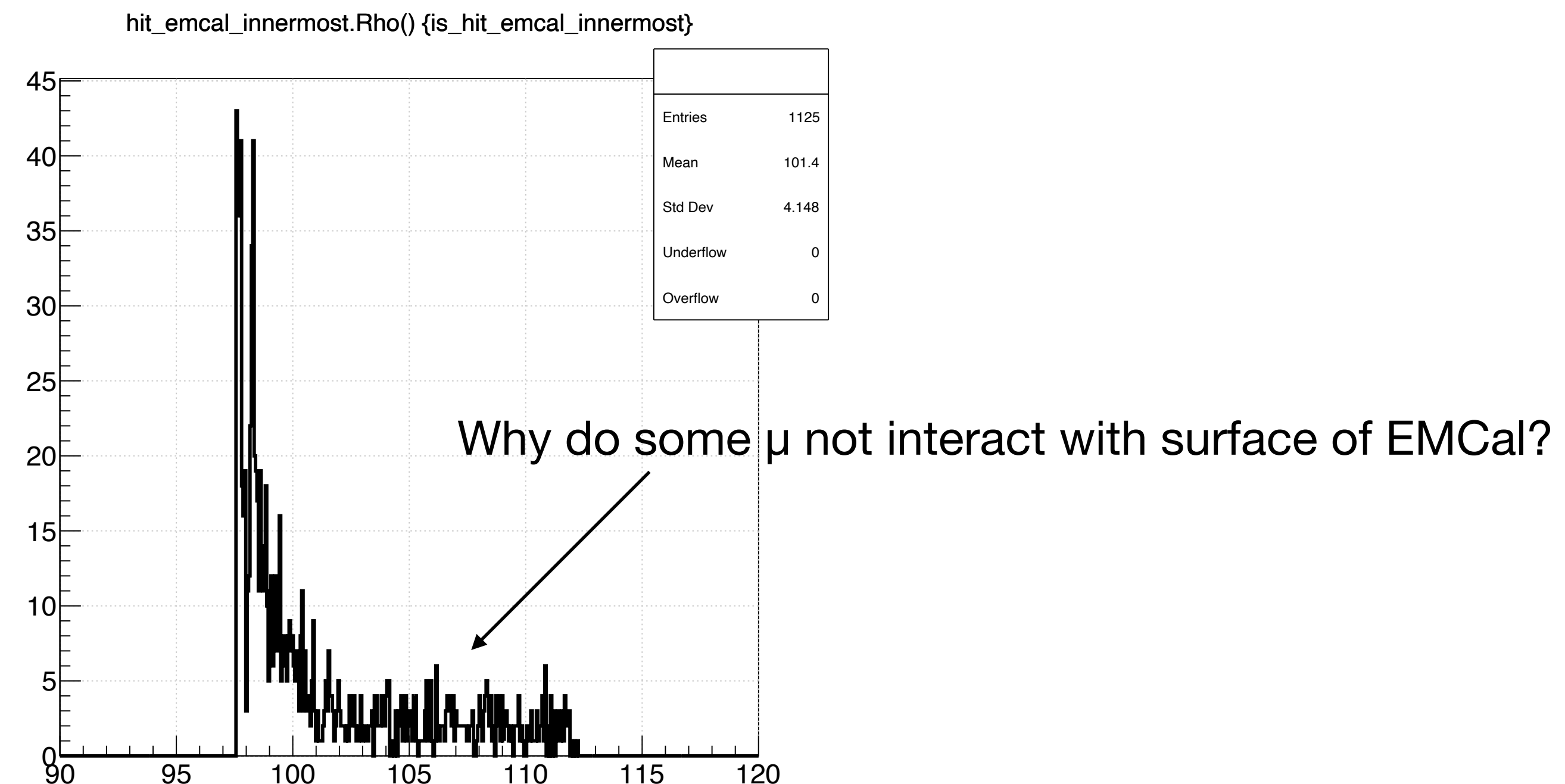
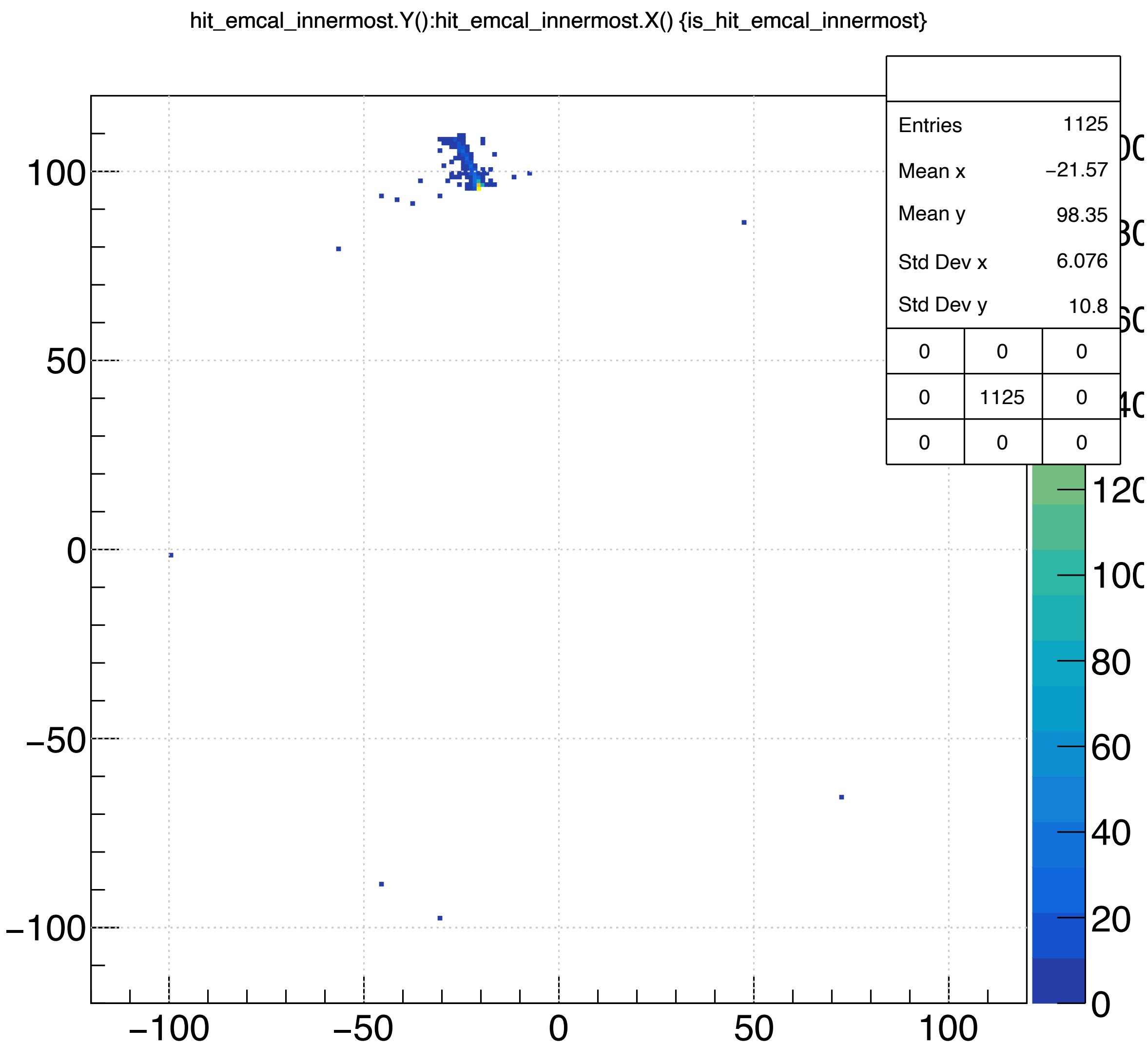
Some hits were generated in totally different directions from the beam.

Pilot run: Parameter distributions

- (Left) x_{EMCal} vs y_{EMCal} distribution

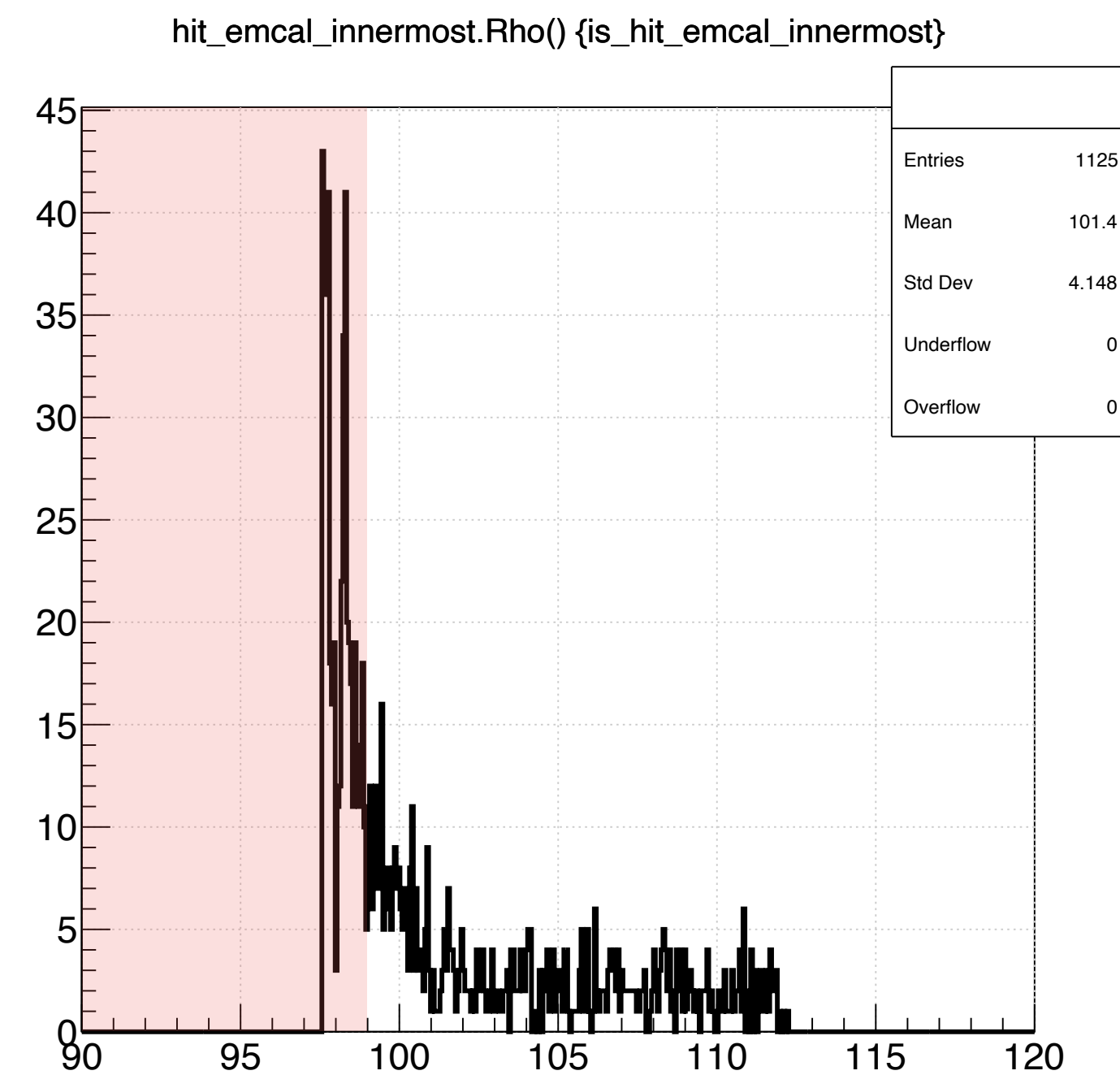
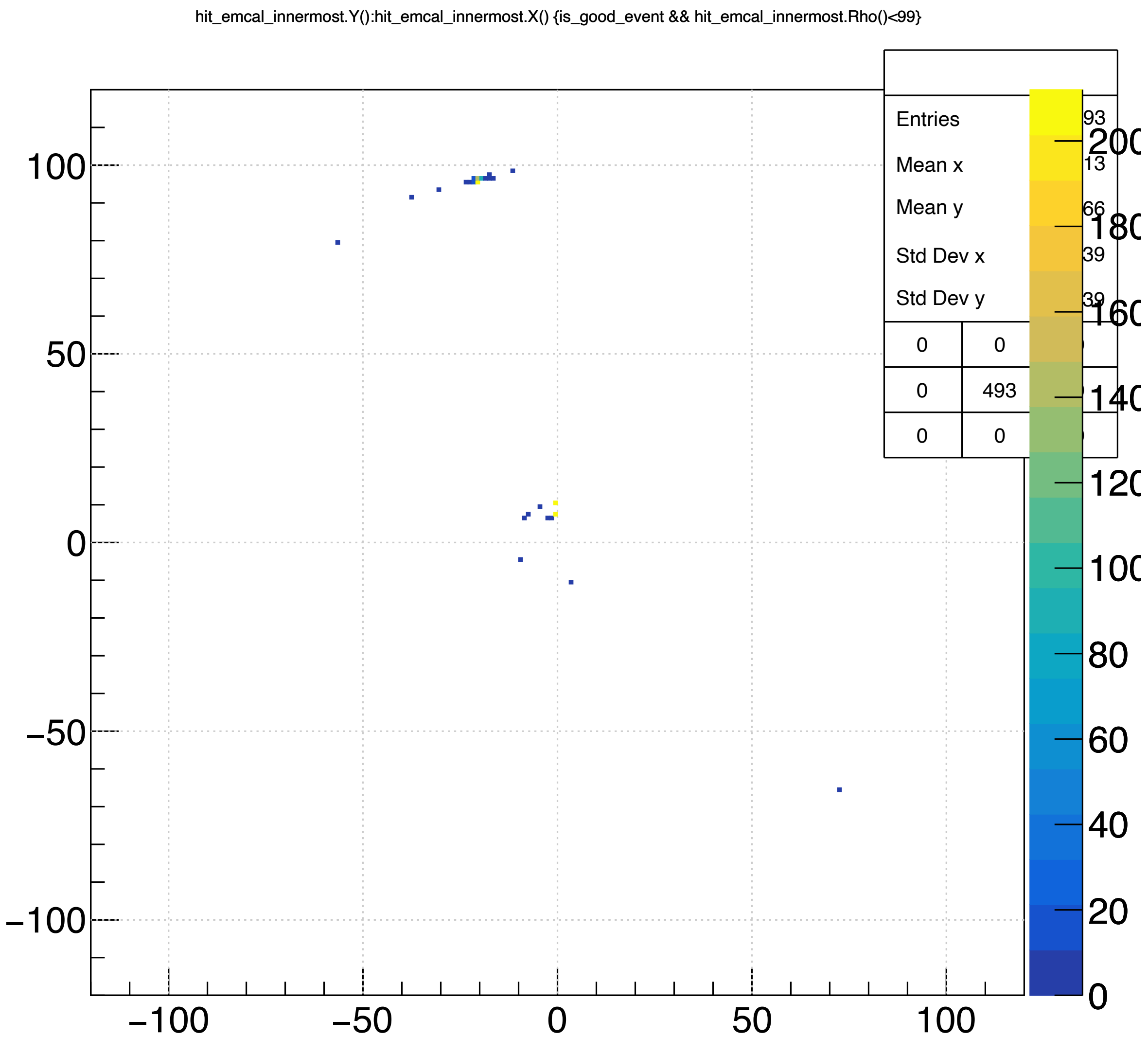
- The distribution is uniform in azimuth

- (Below) $\rho_{\text{EMCal}} = \sqrt{x_{\text{EMCal}}^2 + y_{\text{EMCal}}^2}$ distribution



Pilot run: Parameter distributions

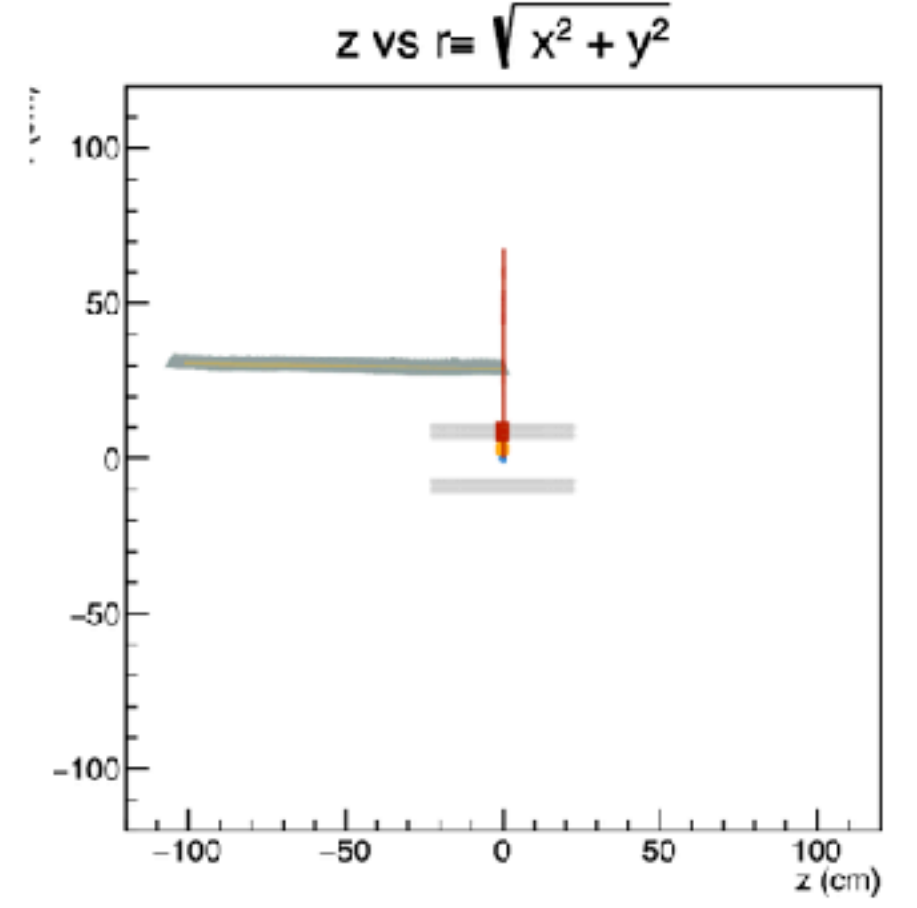
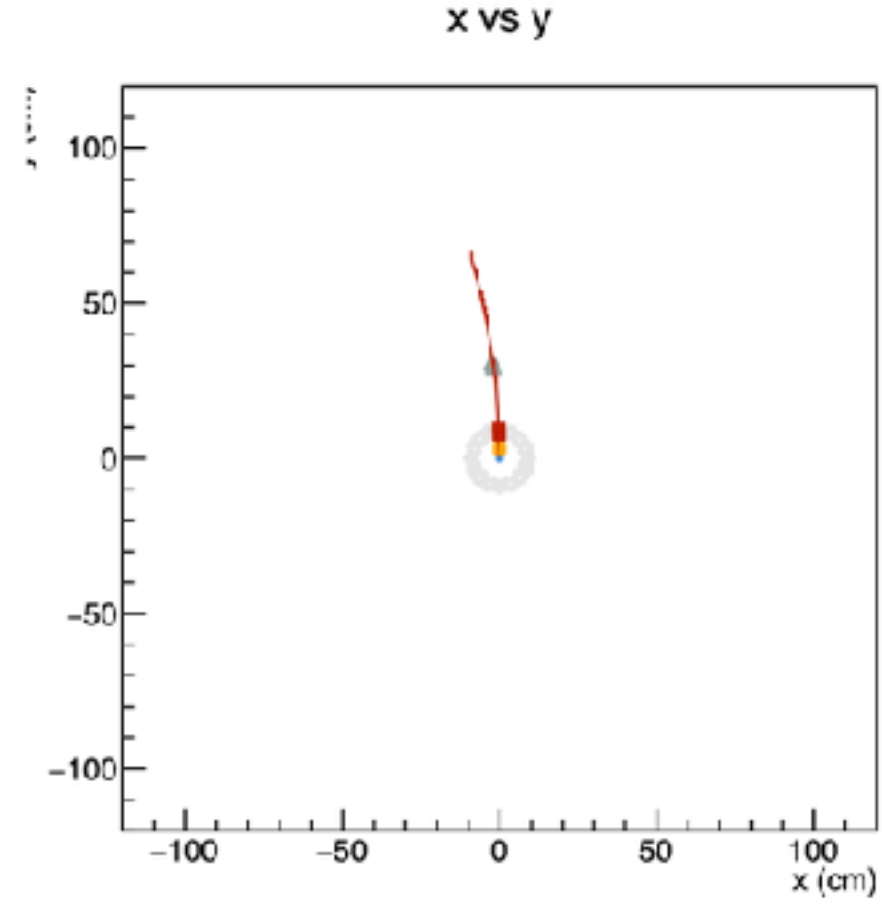
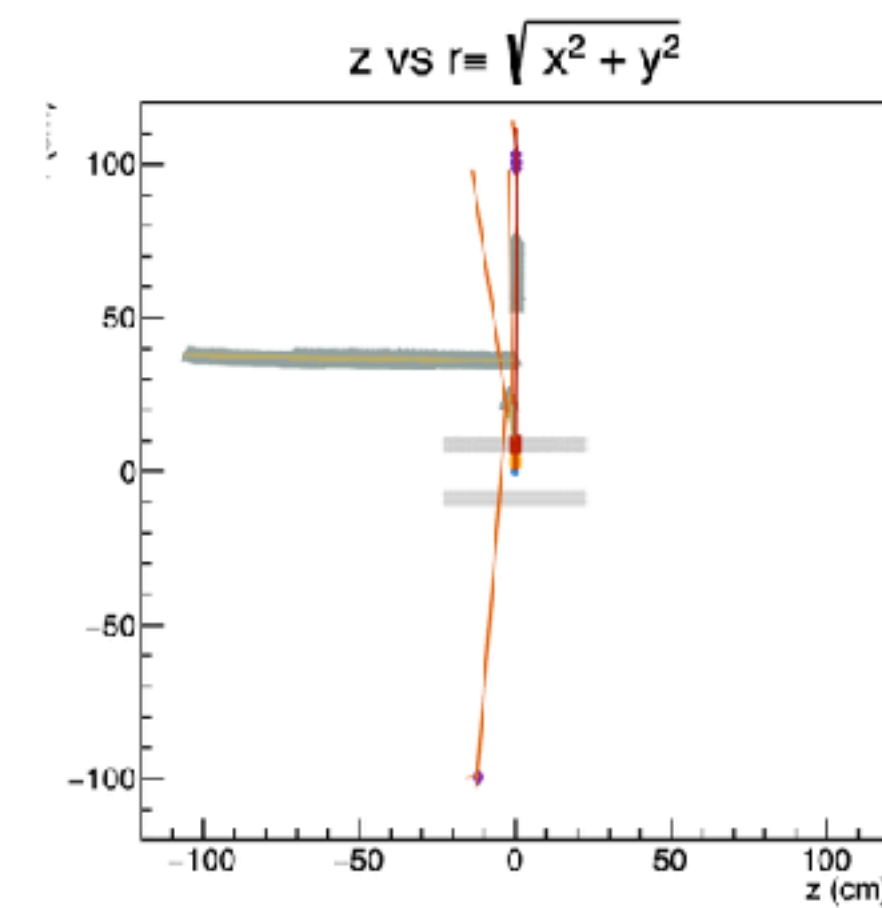
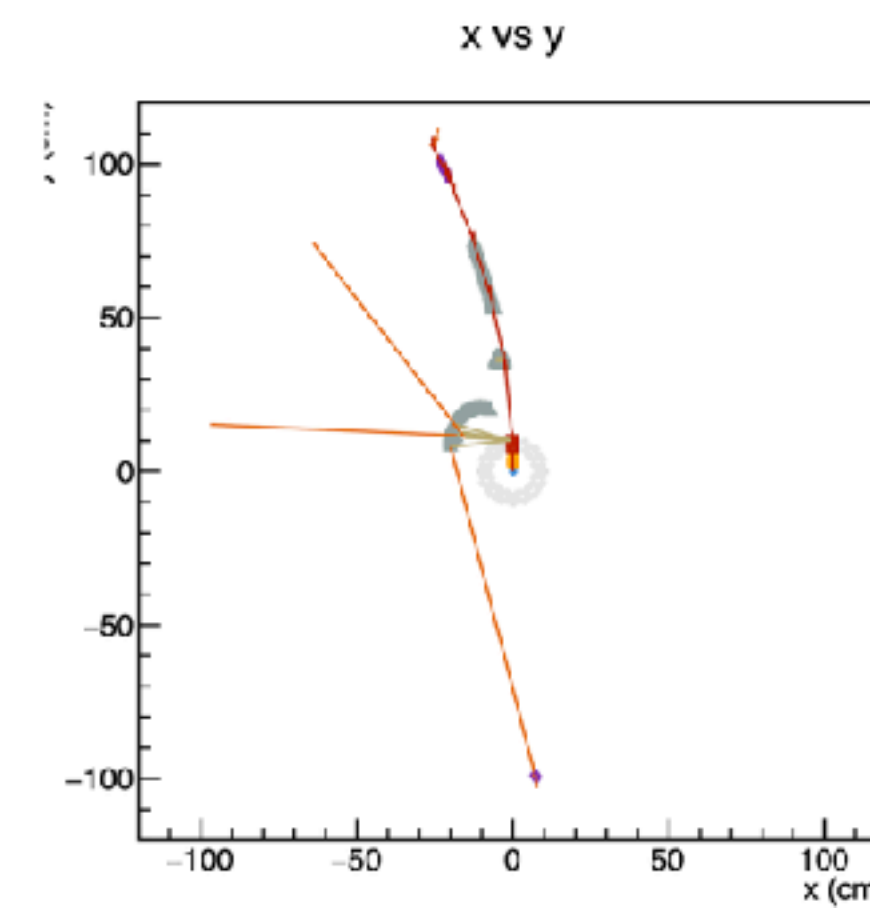
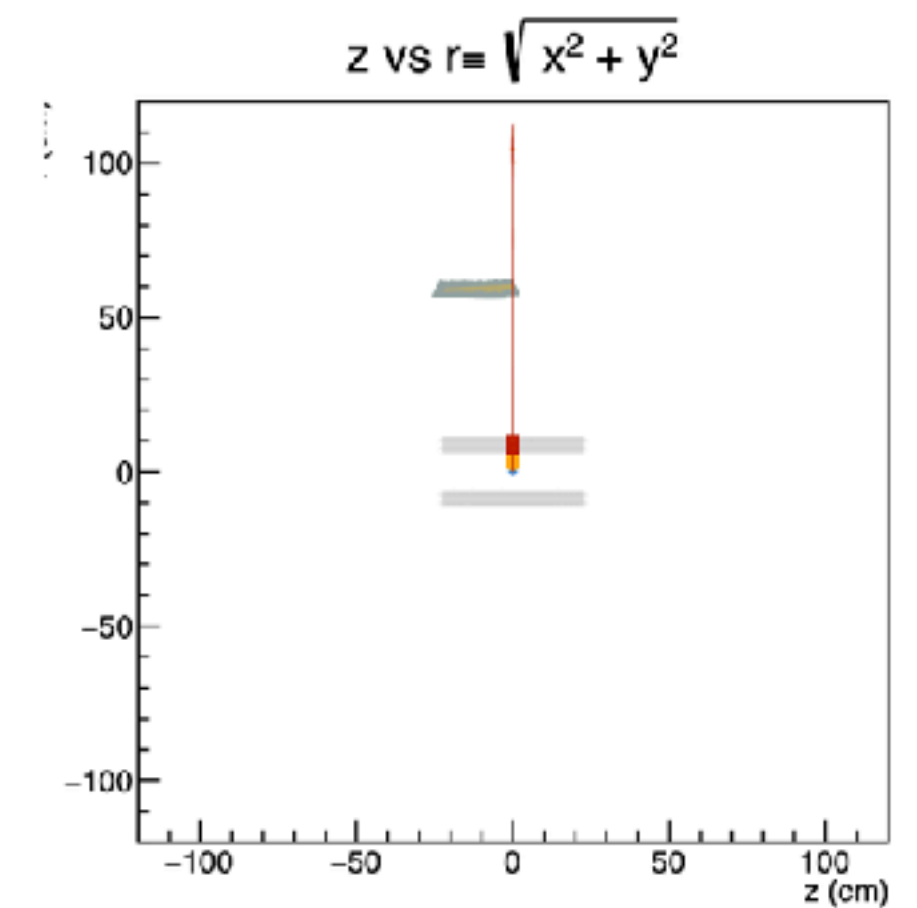
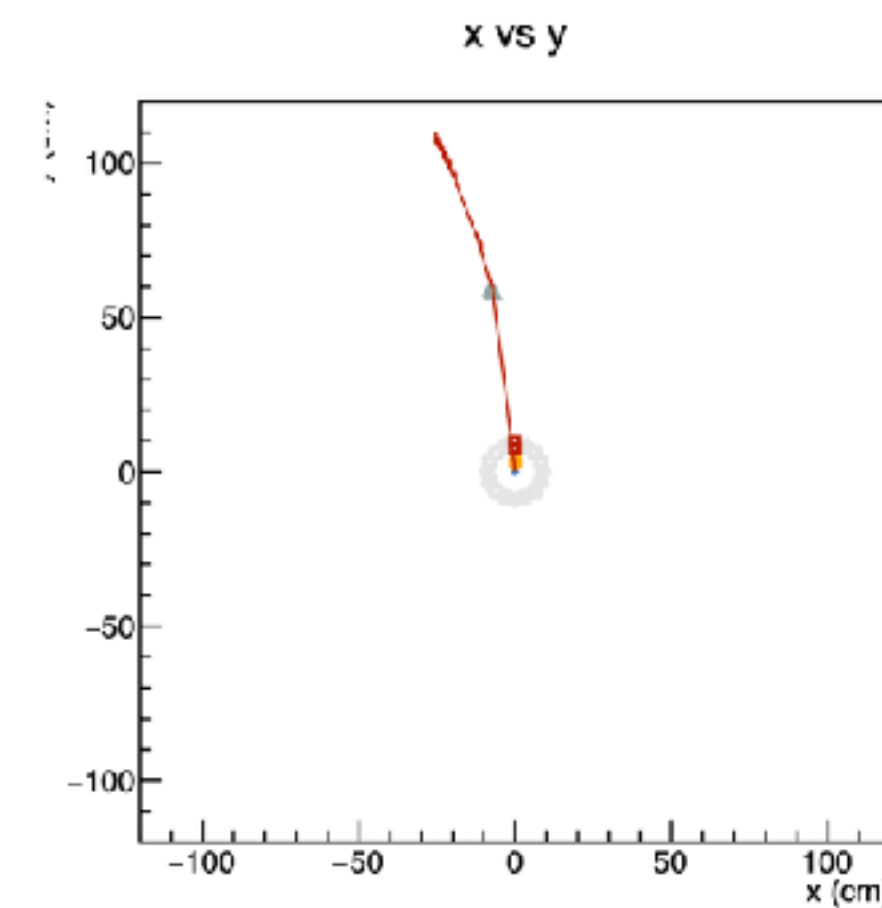
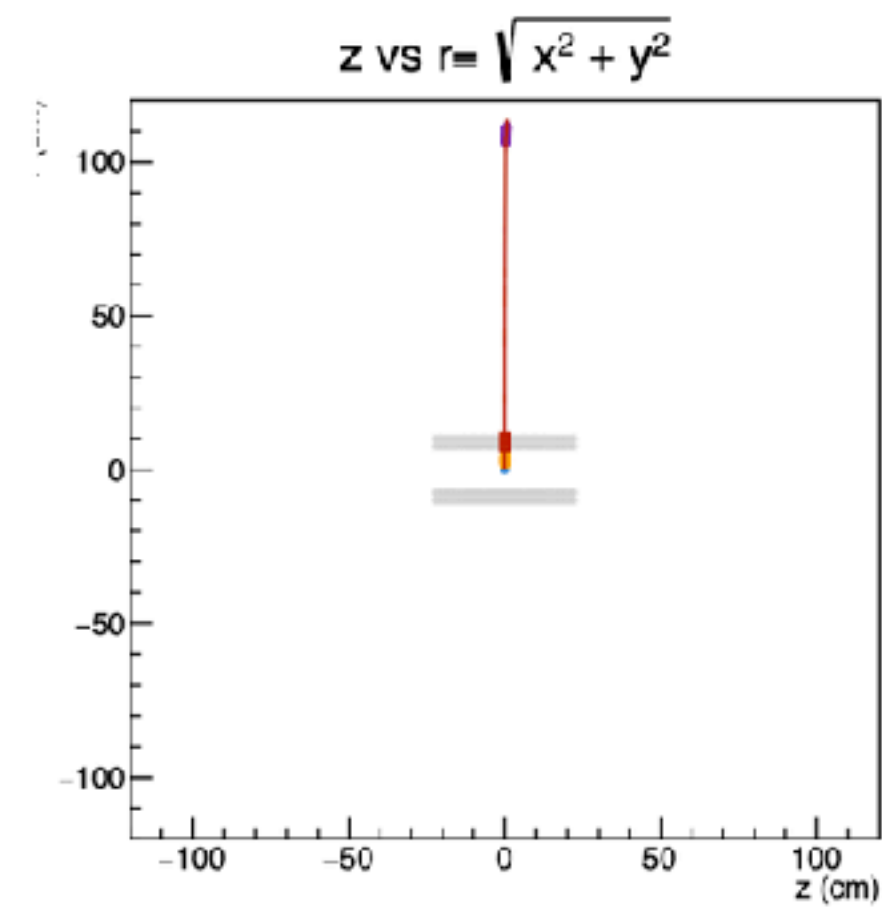
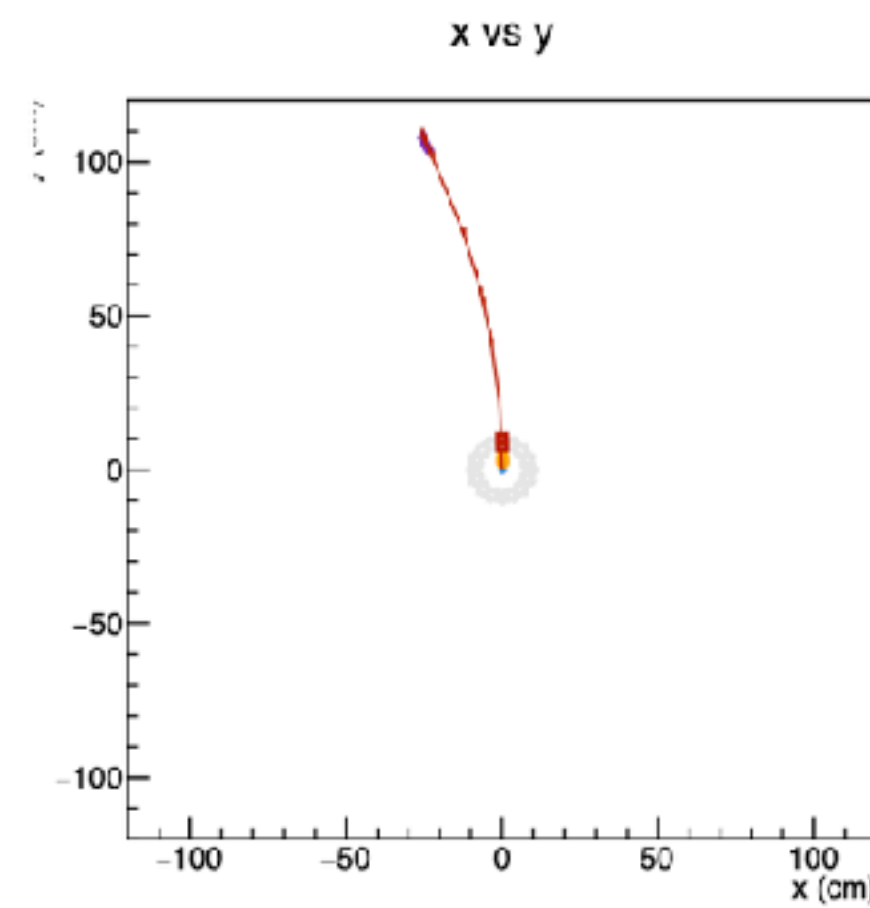
- (Left) x_{EMCal} vs y_{EMCal} distribution with a cut of $\rho_{\text{EMCal}} < 99$ cm



Pilot run: Event displays

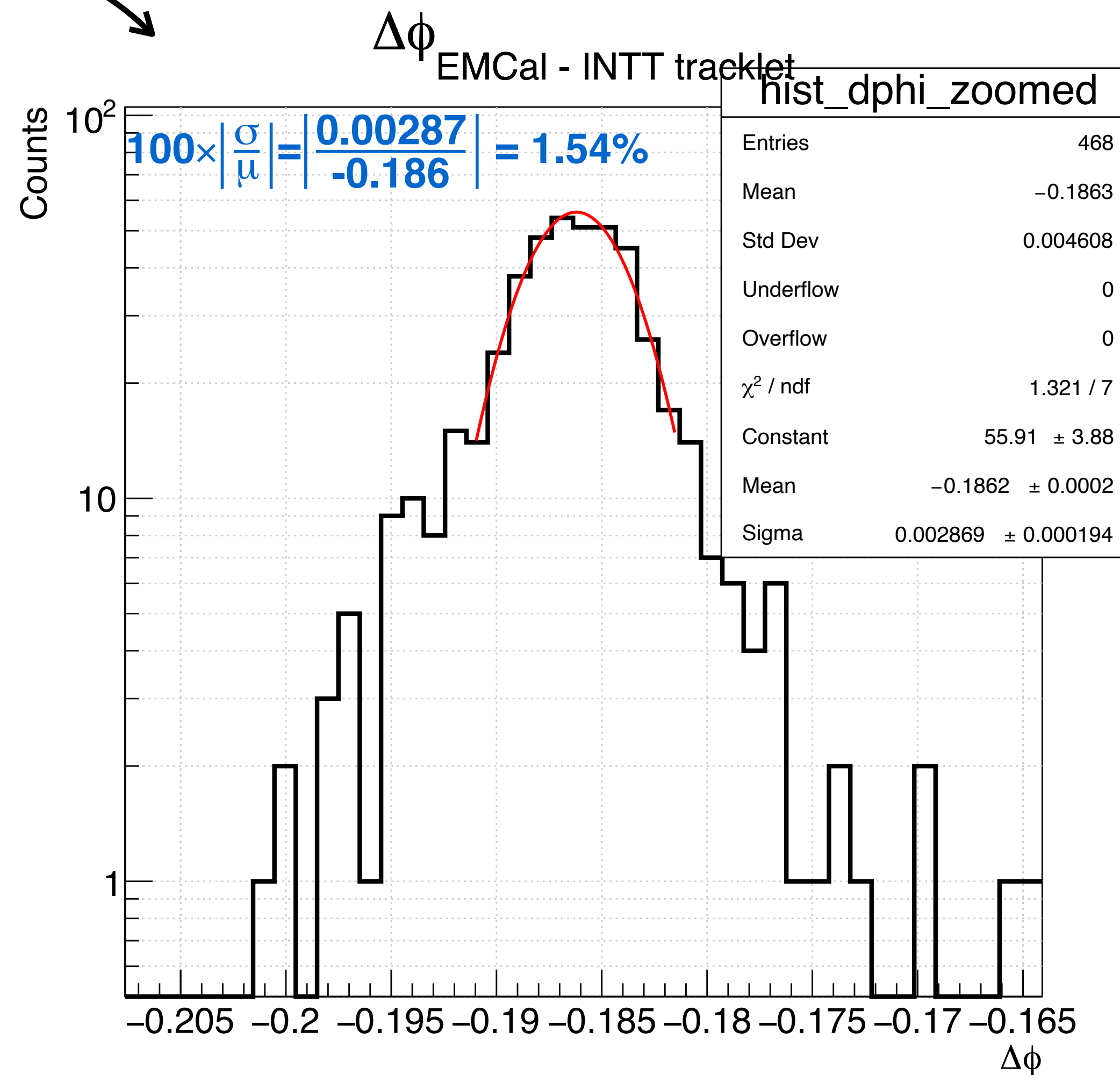
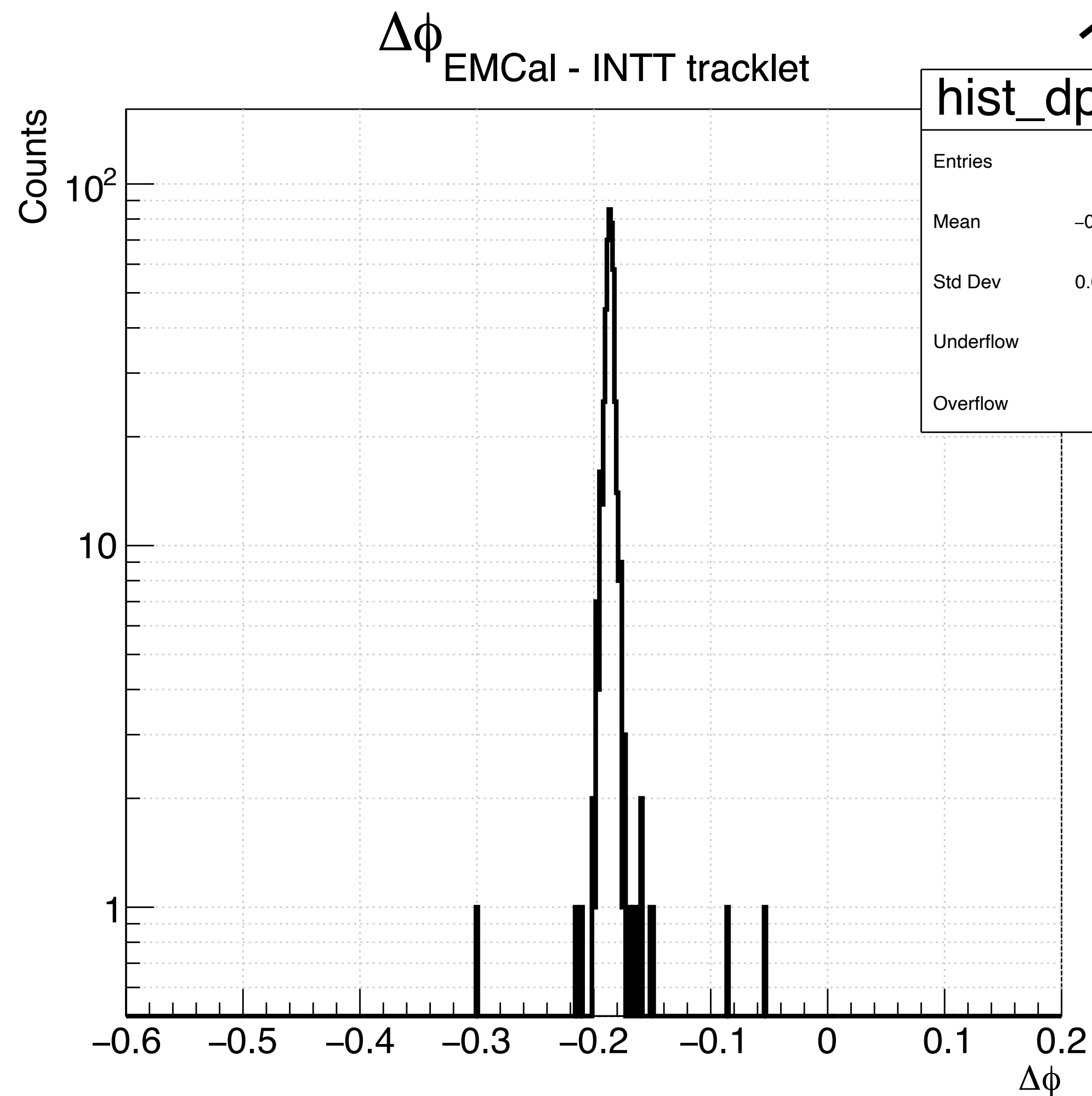
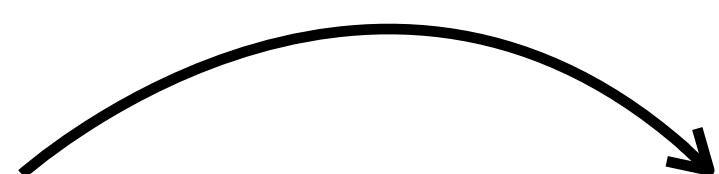
Cuts

- At least 1 EMCal hit
- At least 2 INTT hits
- $\rho_{\text{EMCal}} < 99$ cm



Pilot run: ϕ angle resolution

zoom



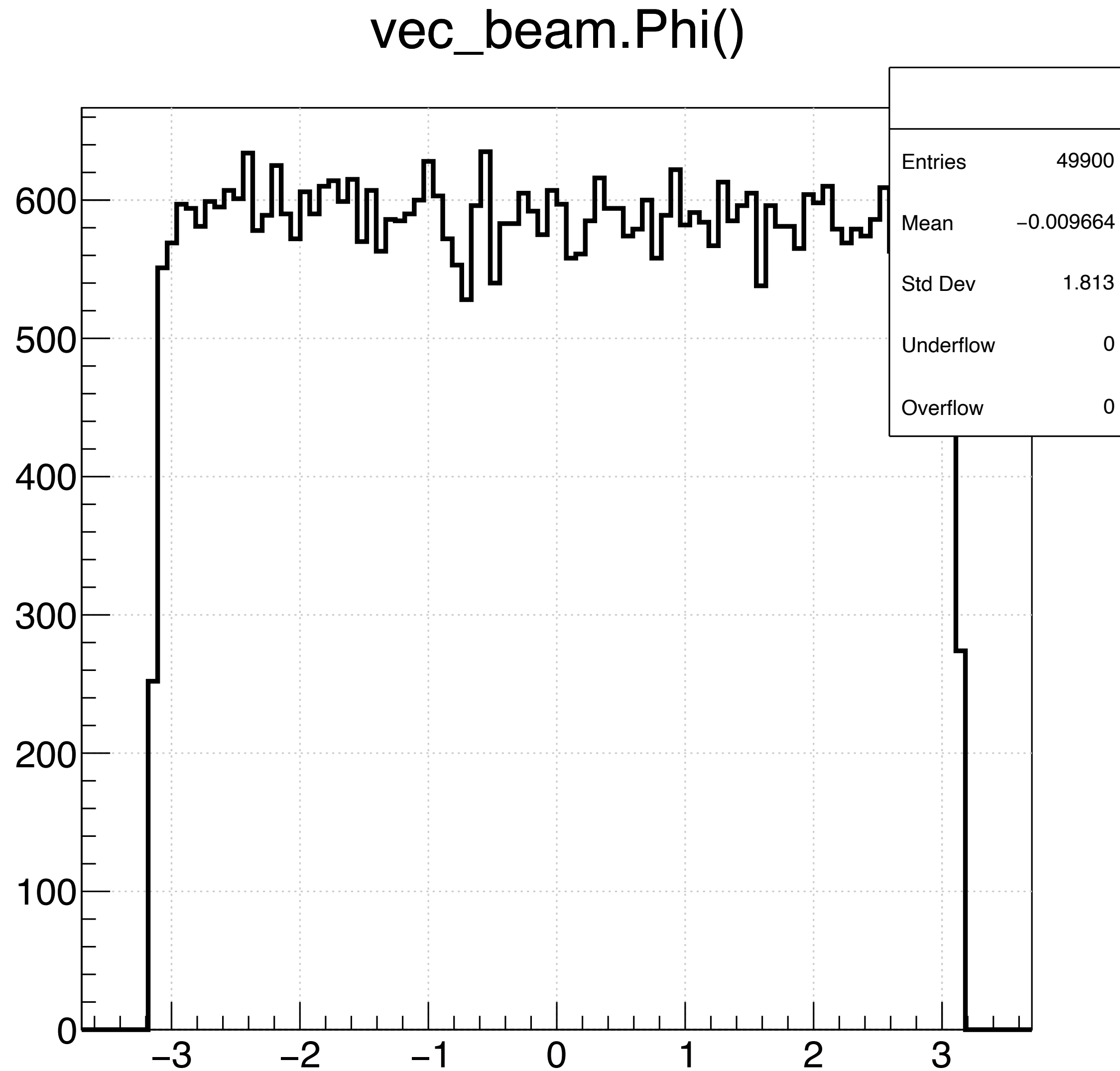
run 1: Condition

Setup:

- Single μ^- MC with $p_T = 1$ GeV/c
- $\phi = [-\pi, \pi]$
- $\eta = 0$
- $\vec{r}_{\text{vertex}} = (0,0,0)$ cm
- Beam pipe, MVTX, INTT, TPC, TPOT, and EMCal are in the simulation.
- ~50k events

Run	#event	Beam	Momentum (GeV/c)	ϕ dist (rad)	η dist	vertex (cm)	$\Delta\phi$ mean (mrad)	$\Delta\phi$ std. dev. (mrad)	$\Delta\phi$ resolution (%)
Pilot	2k	μ^-	$(p_x, p_y, p_z) =$ $(0, 1, 0)$	fixed at $\pi/2$	fixed at 0	fixed at (0, 0, 0)	186	2.87	1.54
1	50k	μ^-	$p_T = 1$ GeV	$[-\pi, \pi]$	fixed at 0	fixed at (0, 0, 0)			

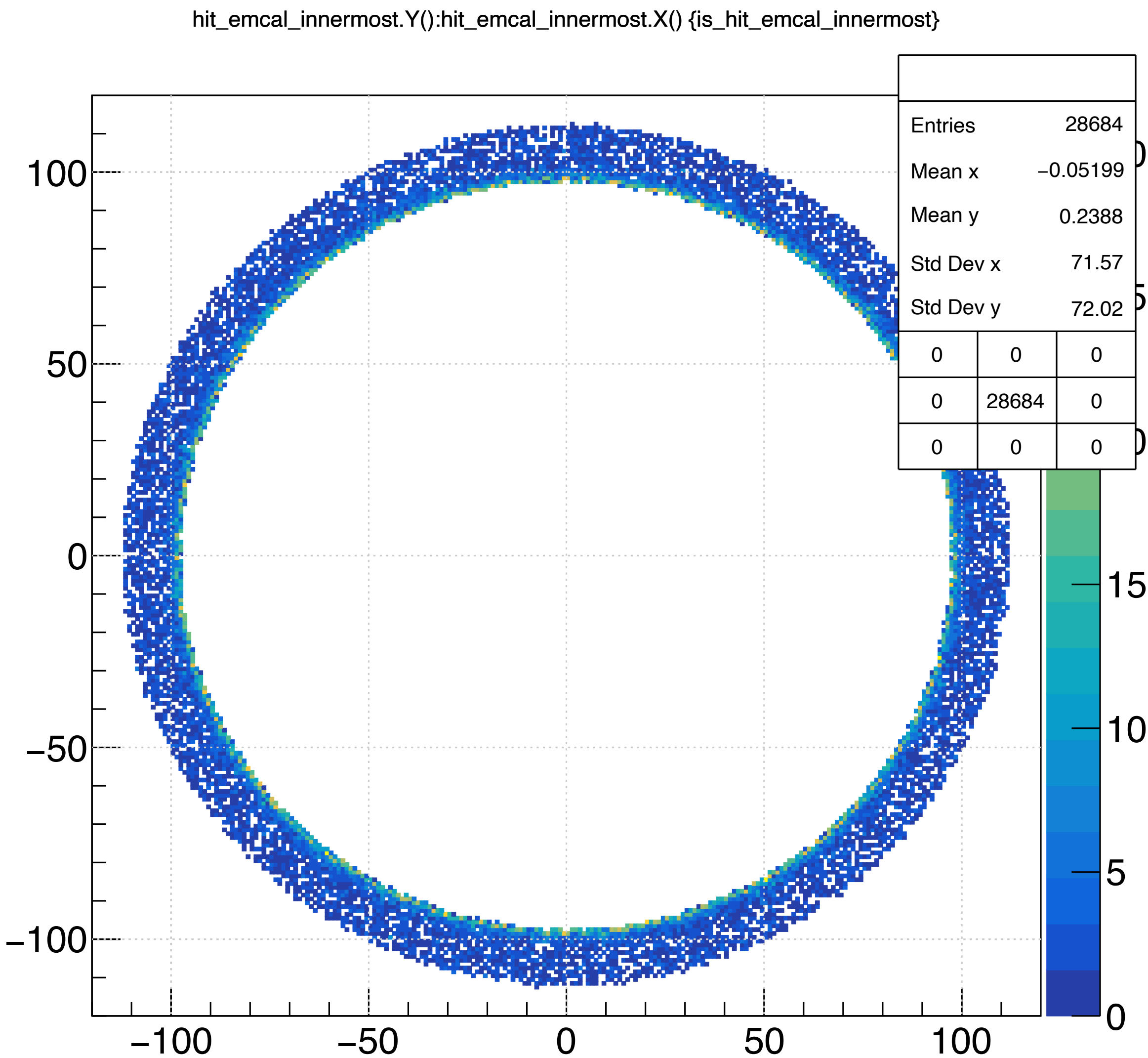
Run 1: Parameter distributions



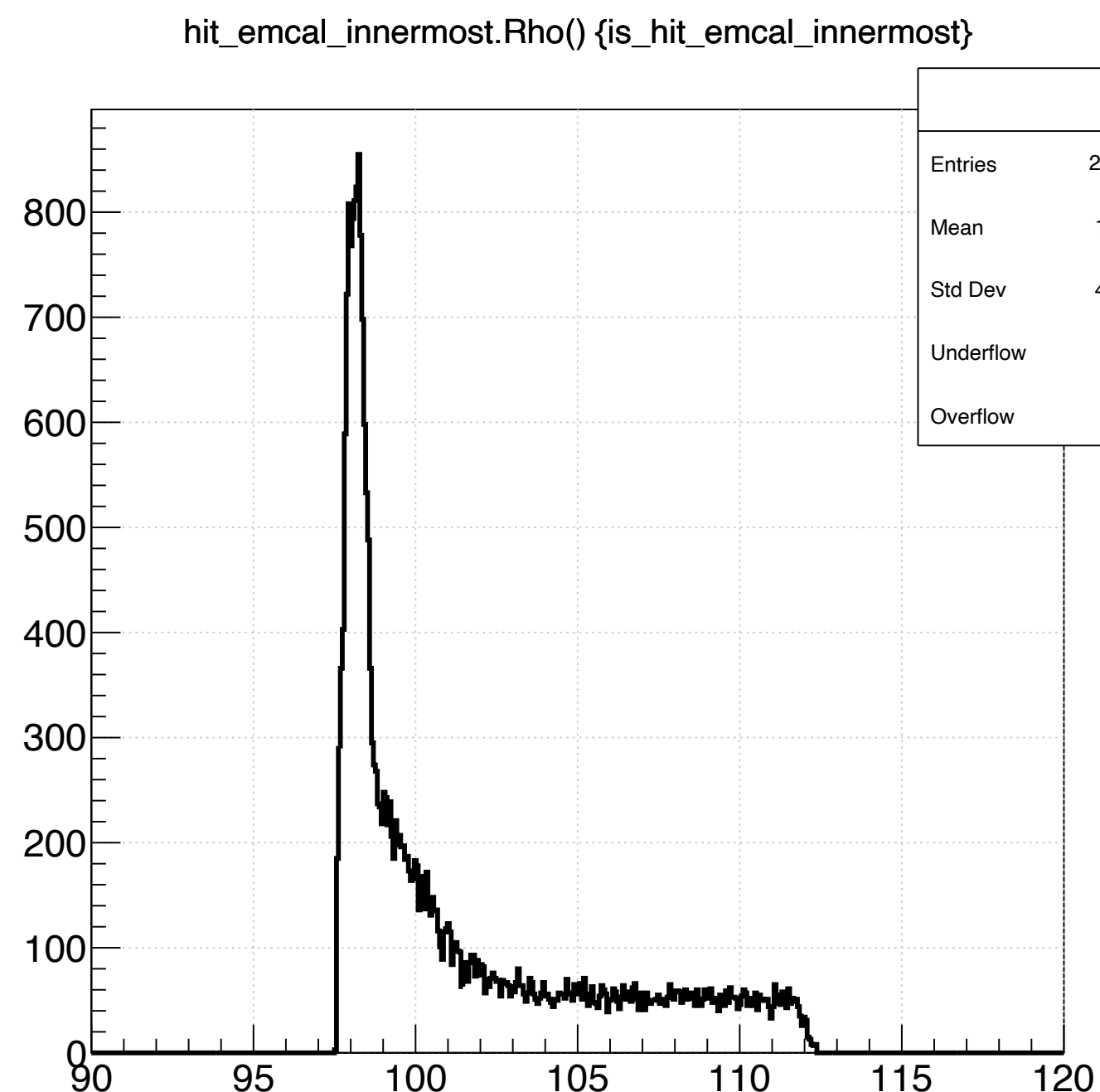
- ϕ_{beam} distribution
- Beam was generated uniformly in azimuth

Run1: Parameter distributions

- (Left) x_{EMCal} vs y_{EMCal} distribution
- The distribution is uniform in azimuth

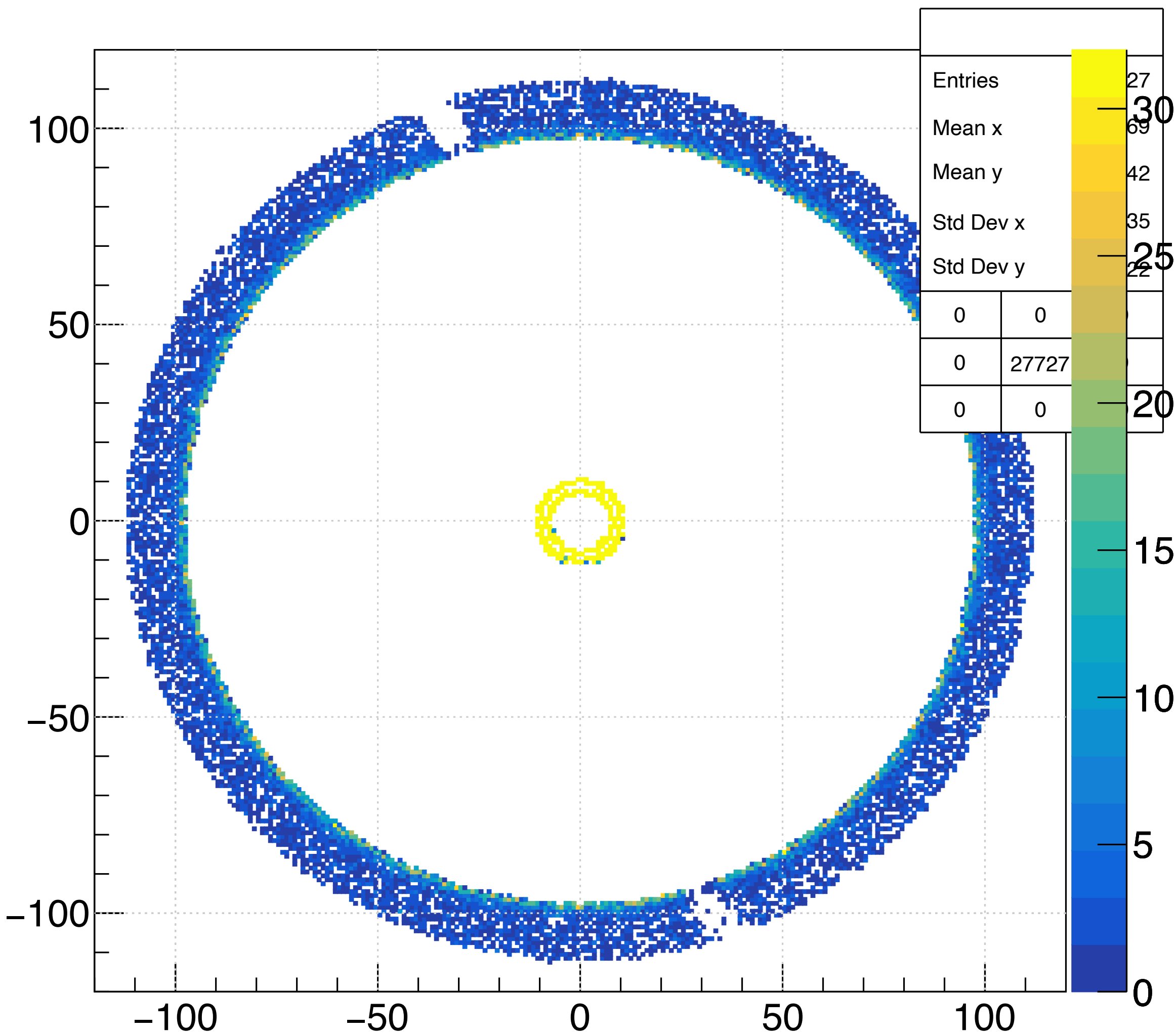


- (Below) $\rho_{\text{EMCal}} = \sqrt{x_{\text{EMCal}}^2 + y_{\text{EMCal}}^2}$ distribution



Run1: Parameter distributions

hit_emcal_innermost.Y():hit_emcal_innermost.X() {is_good_event}

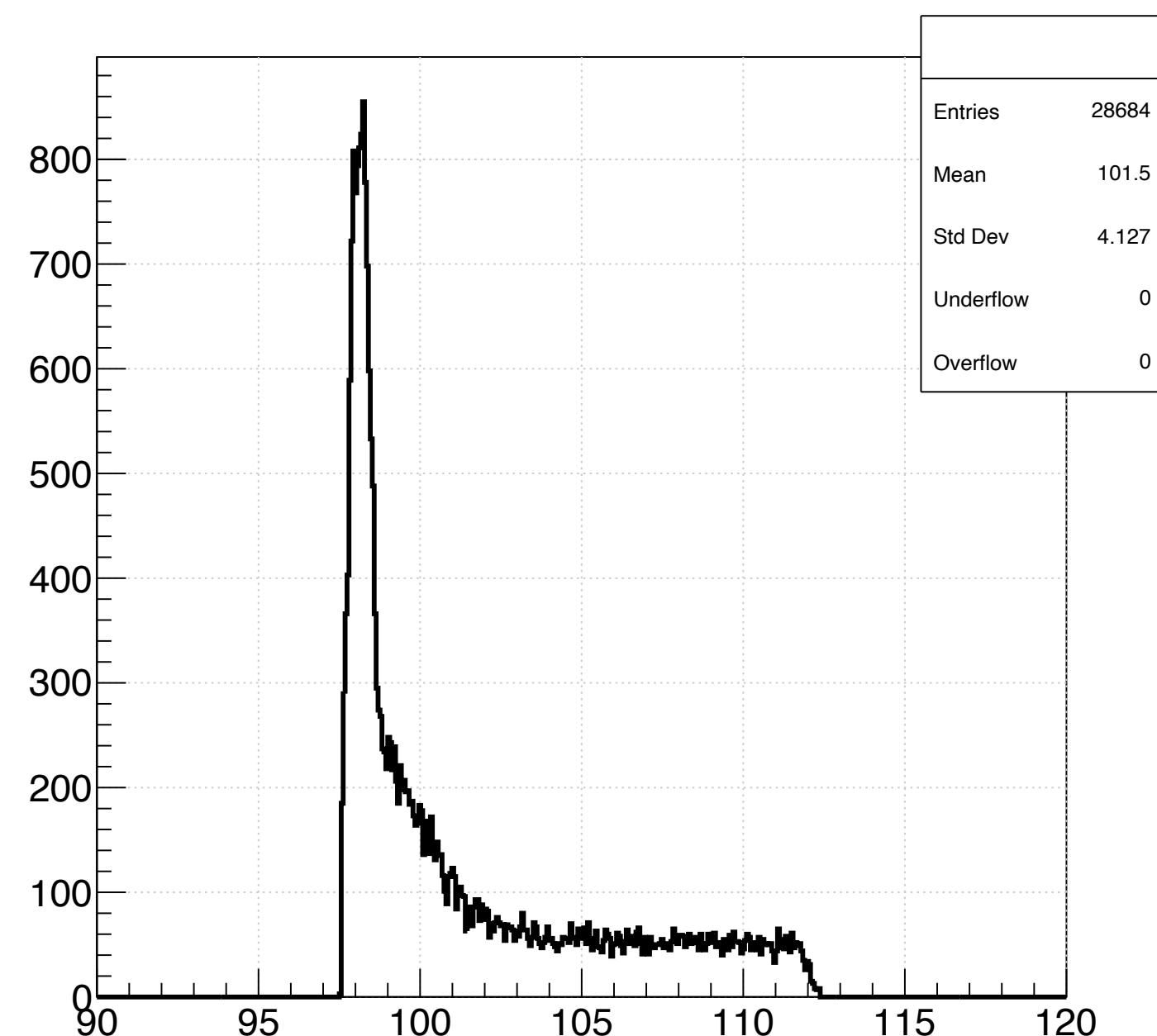


- (Left) x_{EMCal} vs y_{EMCal} distribution with cuts:

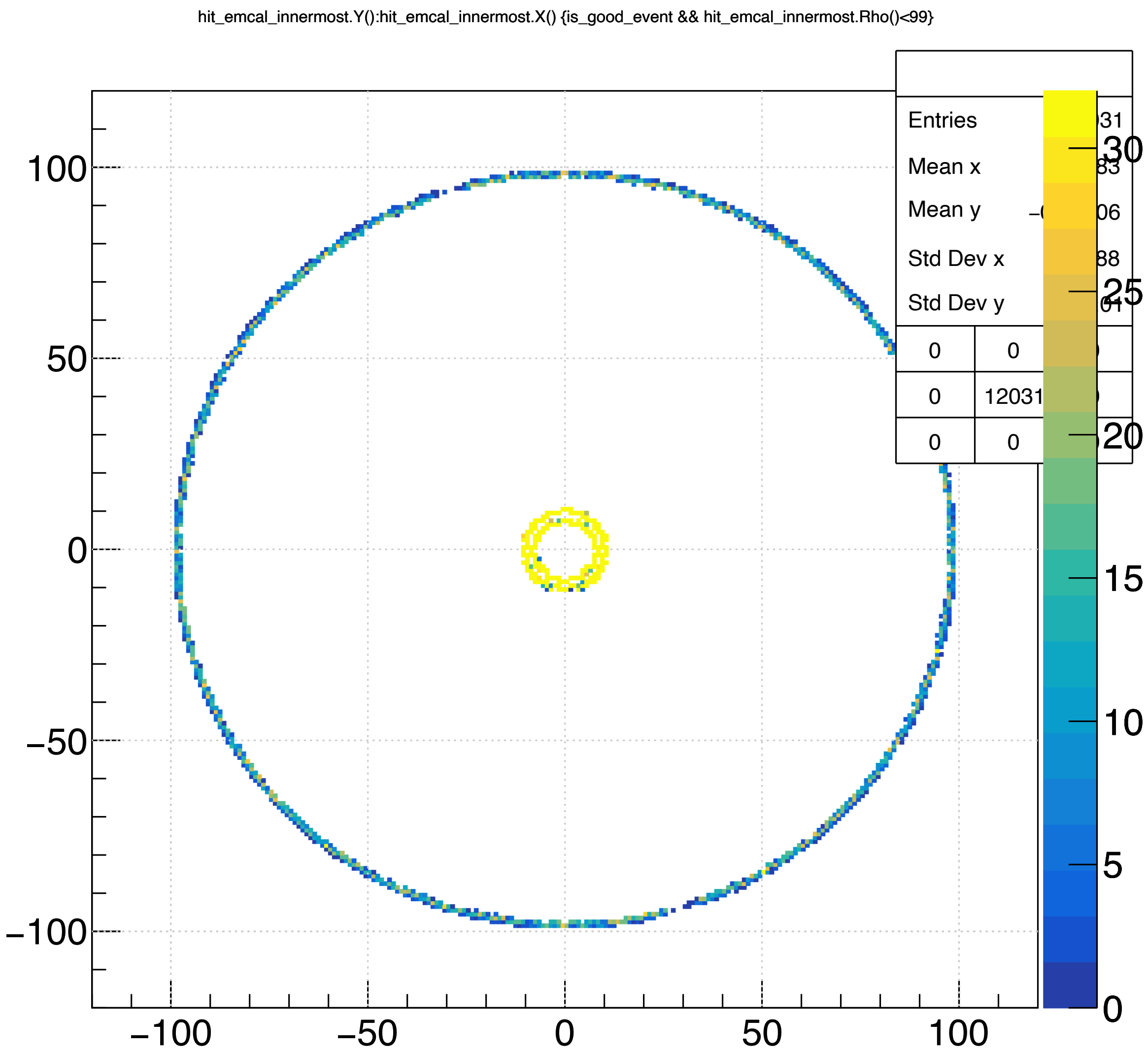
- at least 1 EMCal hit
- at least 2 INTT hits

- (Below) $\rho_{\text{EMCal}} = \sqrt{x_{\text{EMCal}}^2 + y_{\text{EMCal}}^2}$ distribution

hit_emcal_innermost.Rho() {is_hit_emcal_innermost}



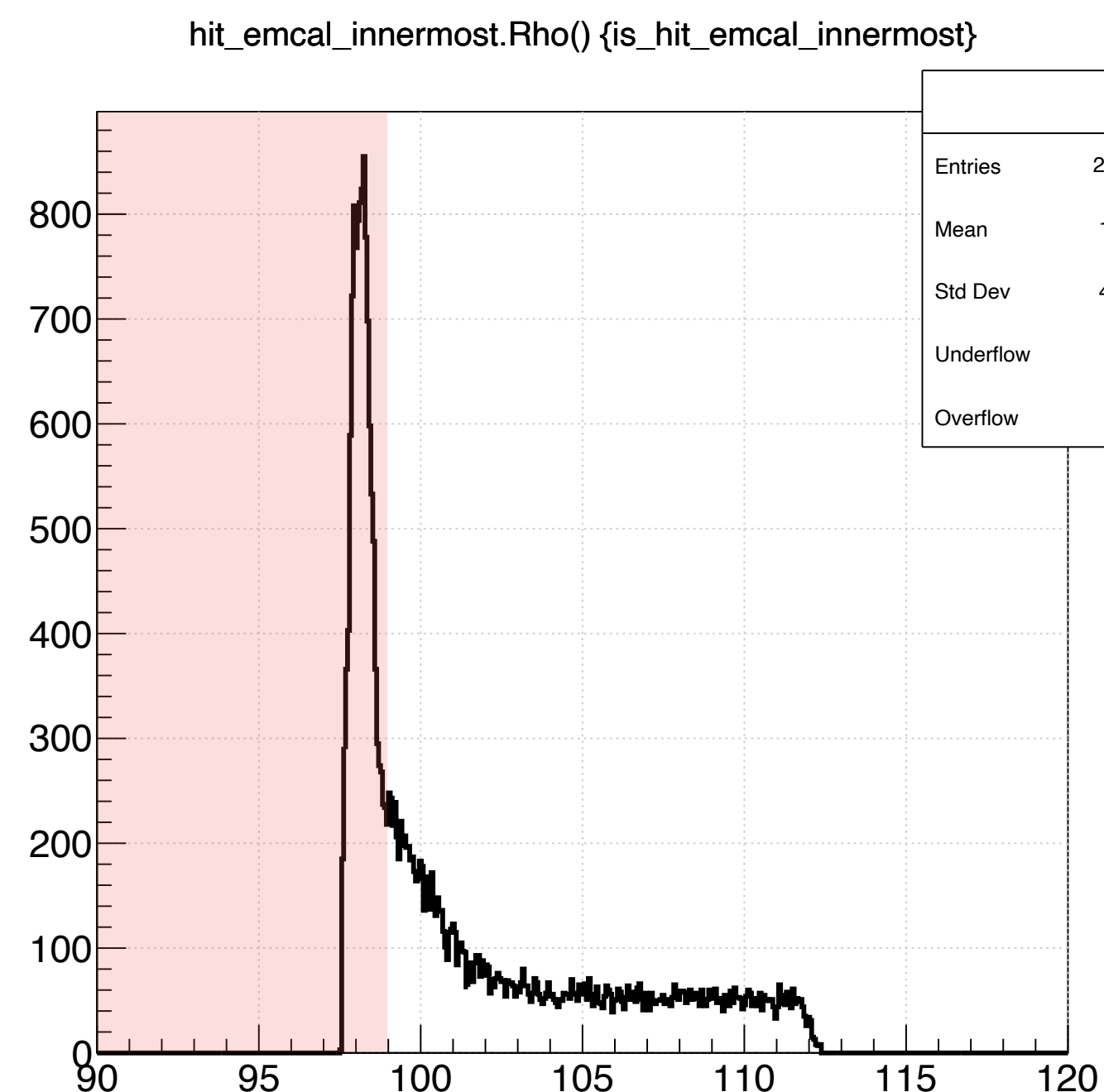
Run1: Parameter distributions



- (Left) x_{EMCal} vs y_{EMCal} distribution with cuts:

- at least 1 EMCal hit
- at least 2 INTT hits
- $\rho_{\text{EMCal}} < 99$ cm

- (Below) $\rho_{\text{EMCal}} = \sqrt{x_{\text{EMCal}}^2 + y_{\text{EMCal}}^2}$ distribution

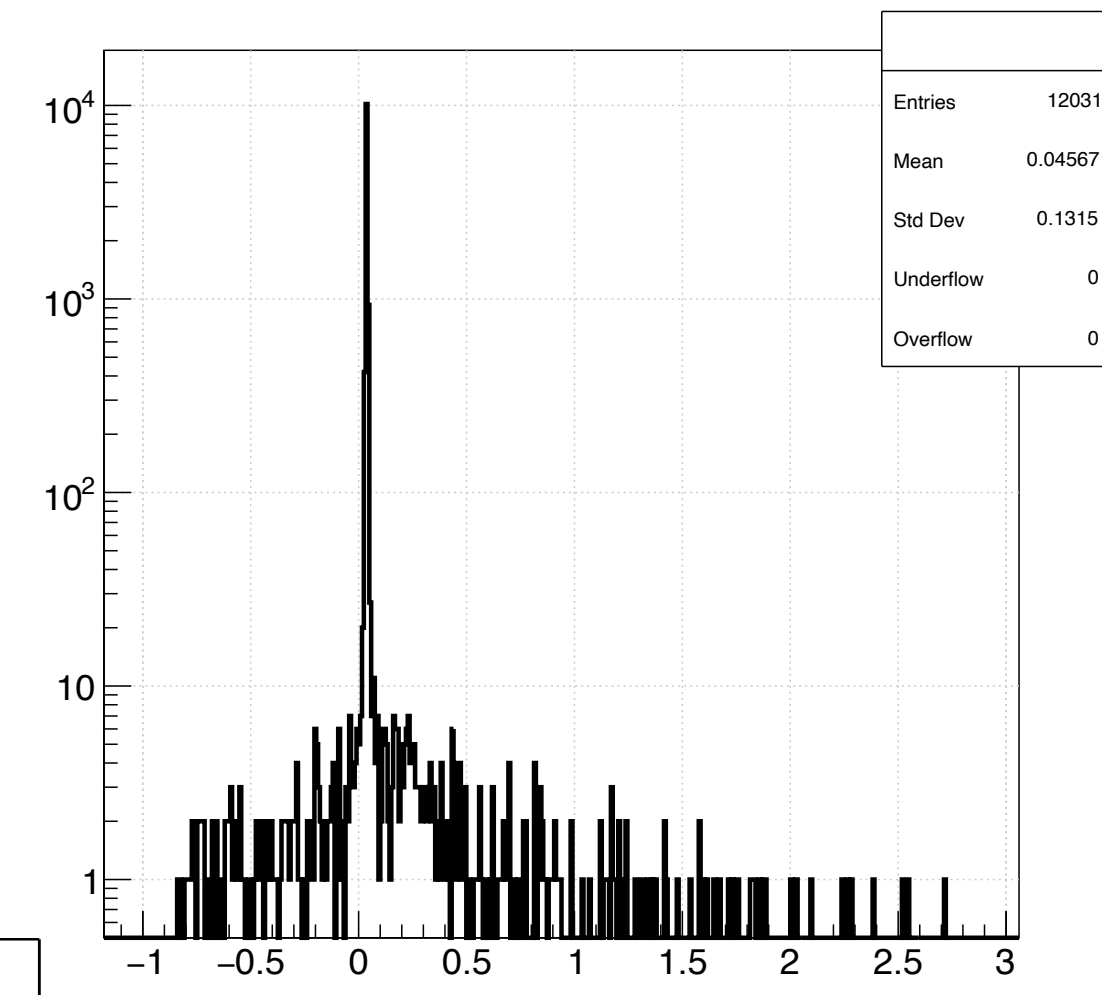
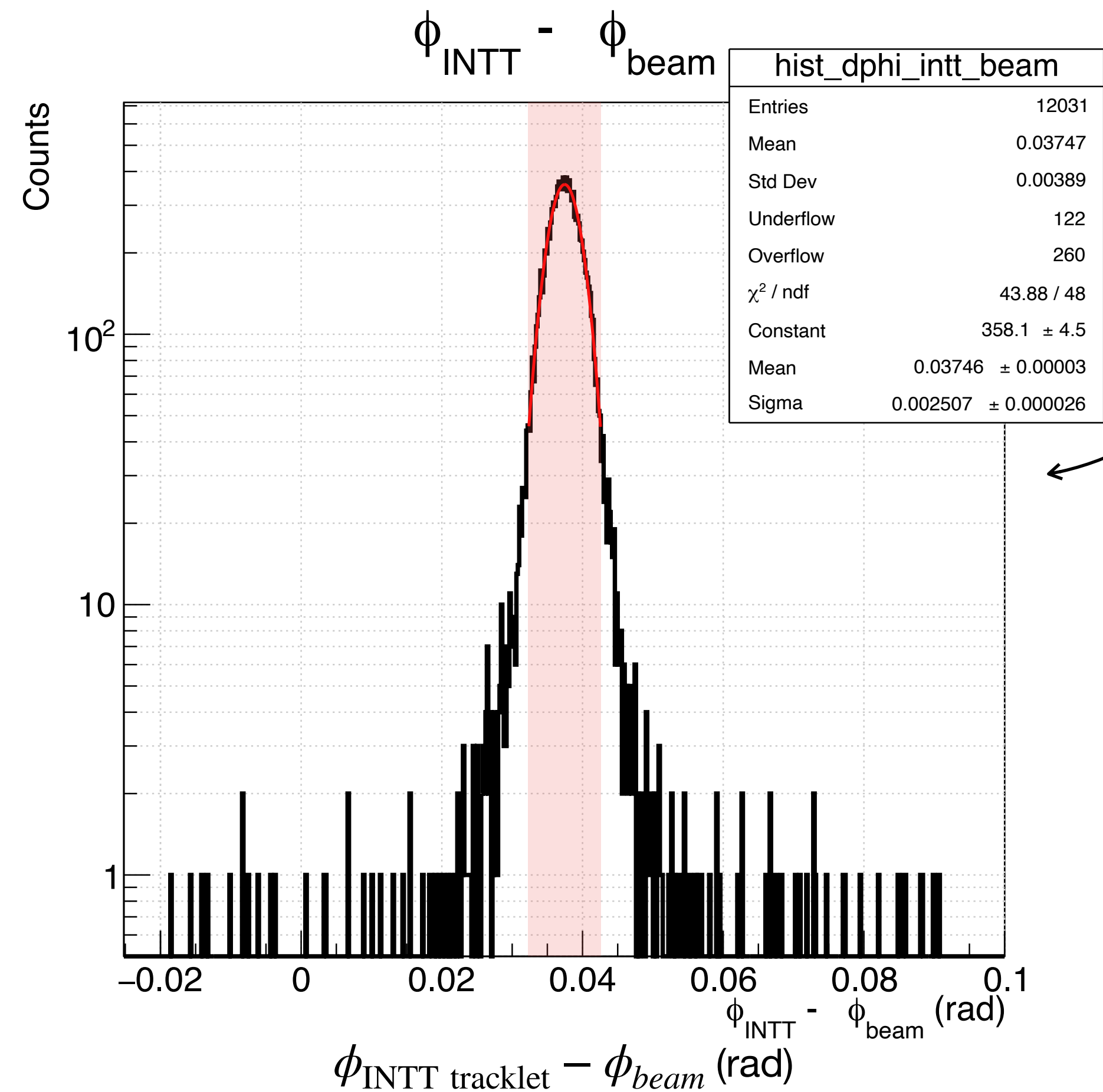
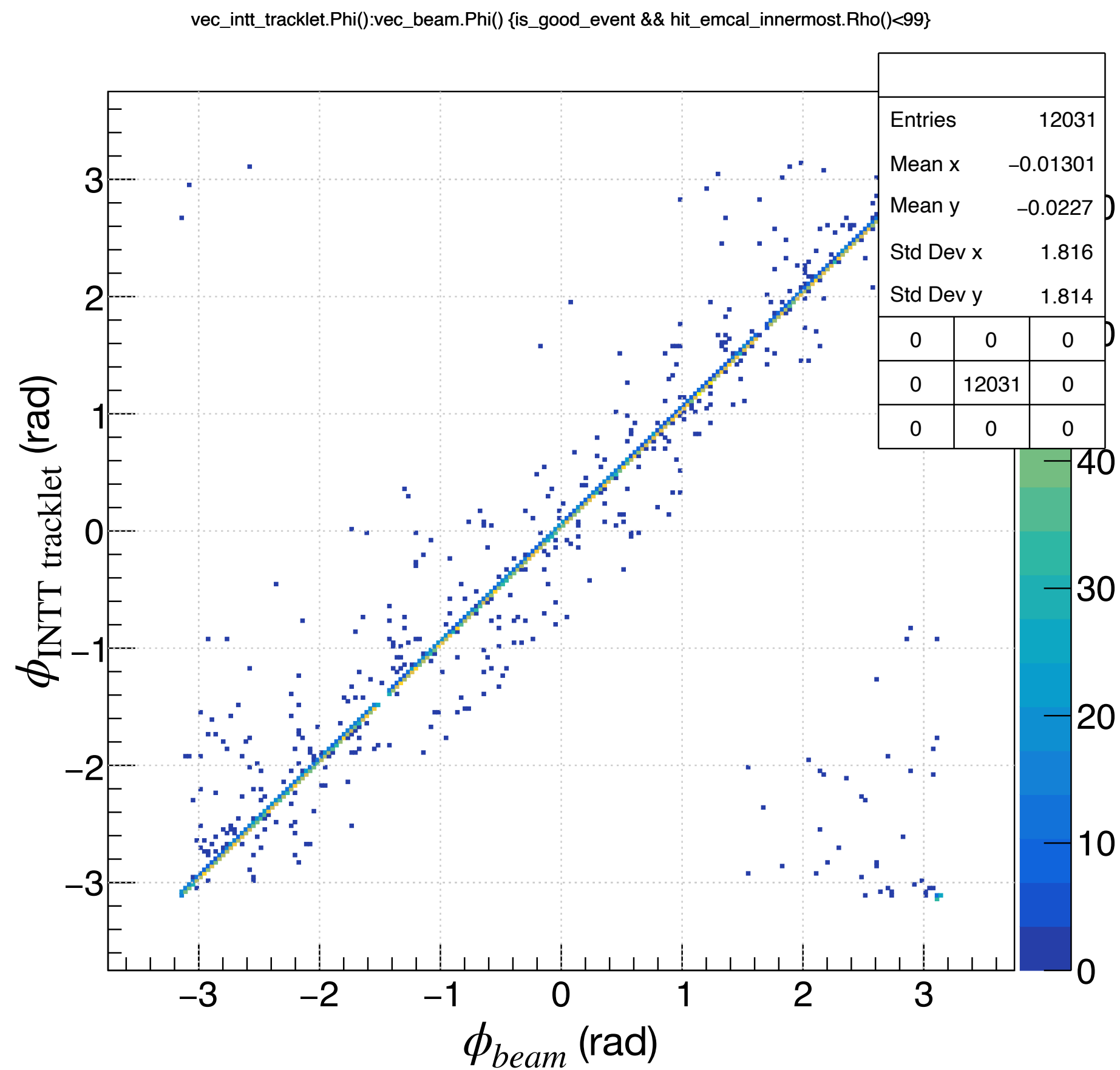


Run1: ϕ of beam and INTT tracklet

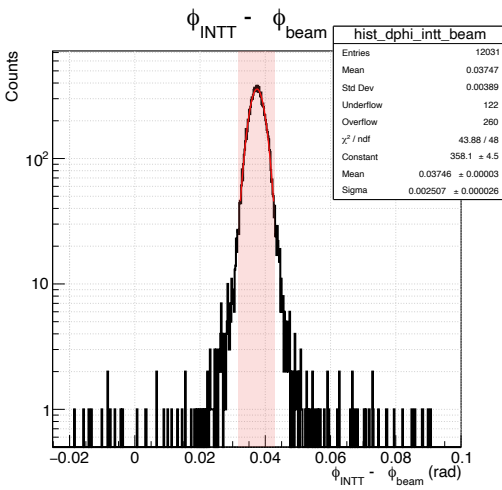
Cuts

- At least 1 EMCal hit
- At least 2 INTT hits
- $\rho_{\text{EMCal}} < 99$ cm

ROOT:Math::VectorUtil::Phi_mpi(vec_intt_tracklet.Phi()-vec_beam.Phi()) {is_good_event && hit_emcal_innermost.Rho()<99}



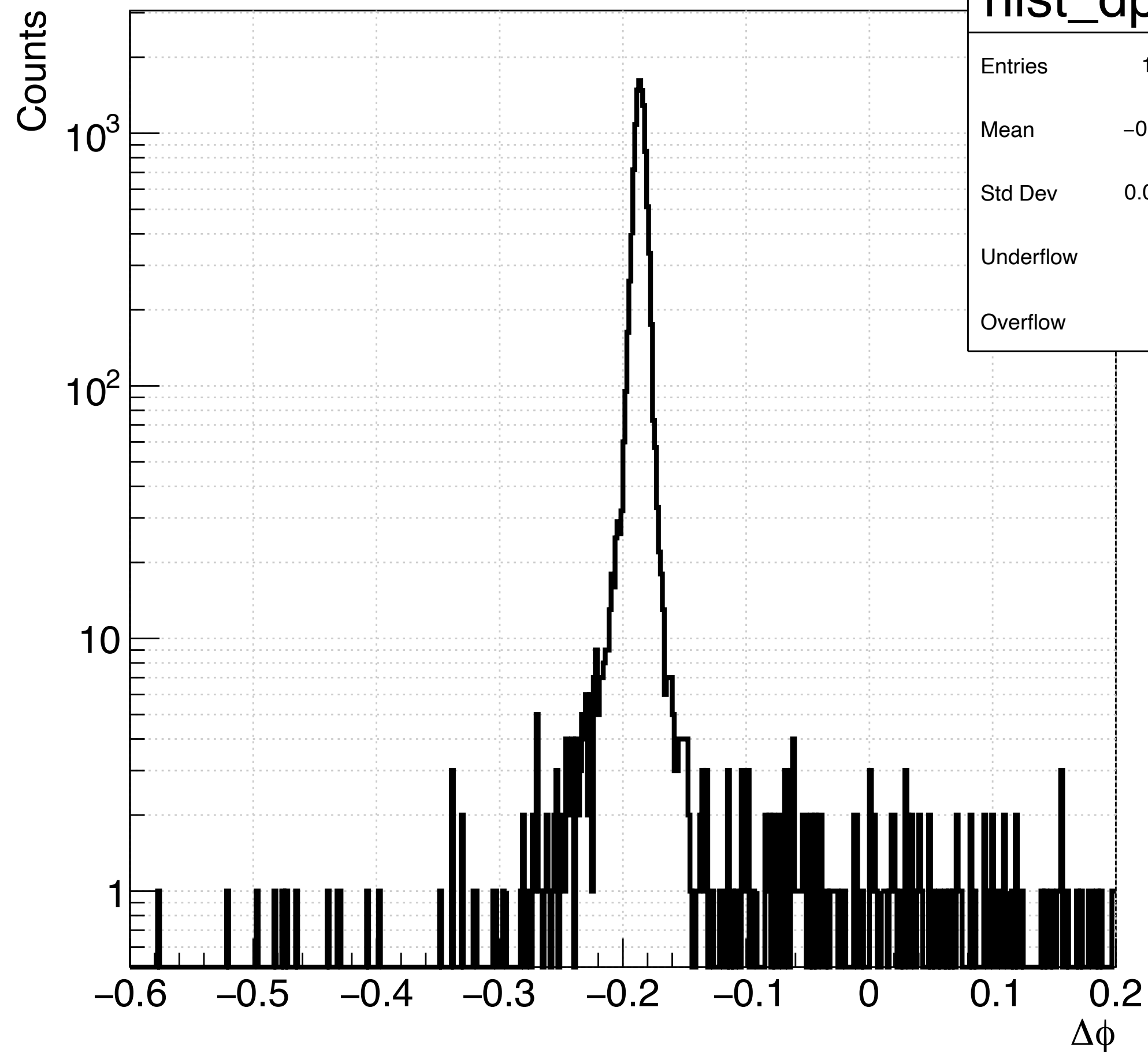
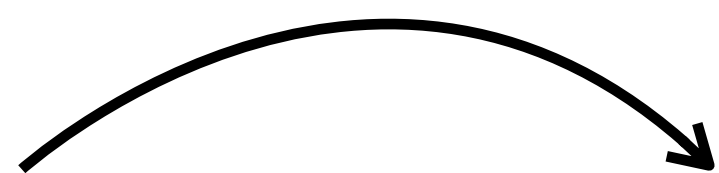
Run1 : ϕ angle resolution



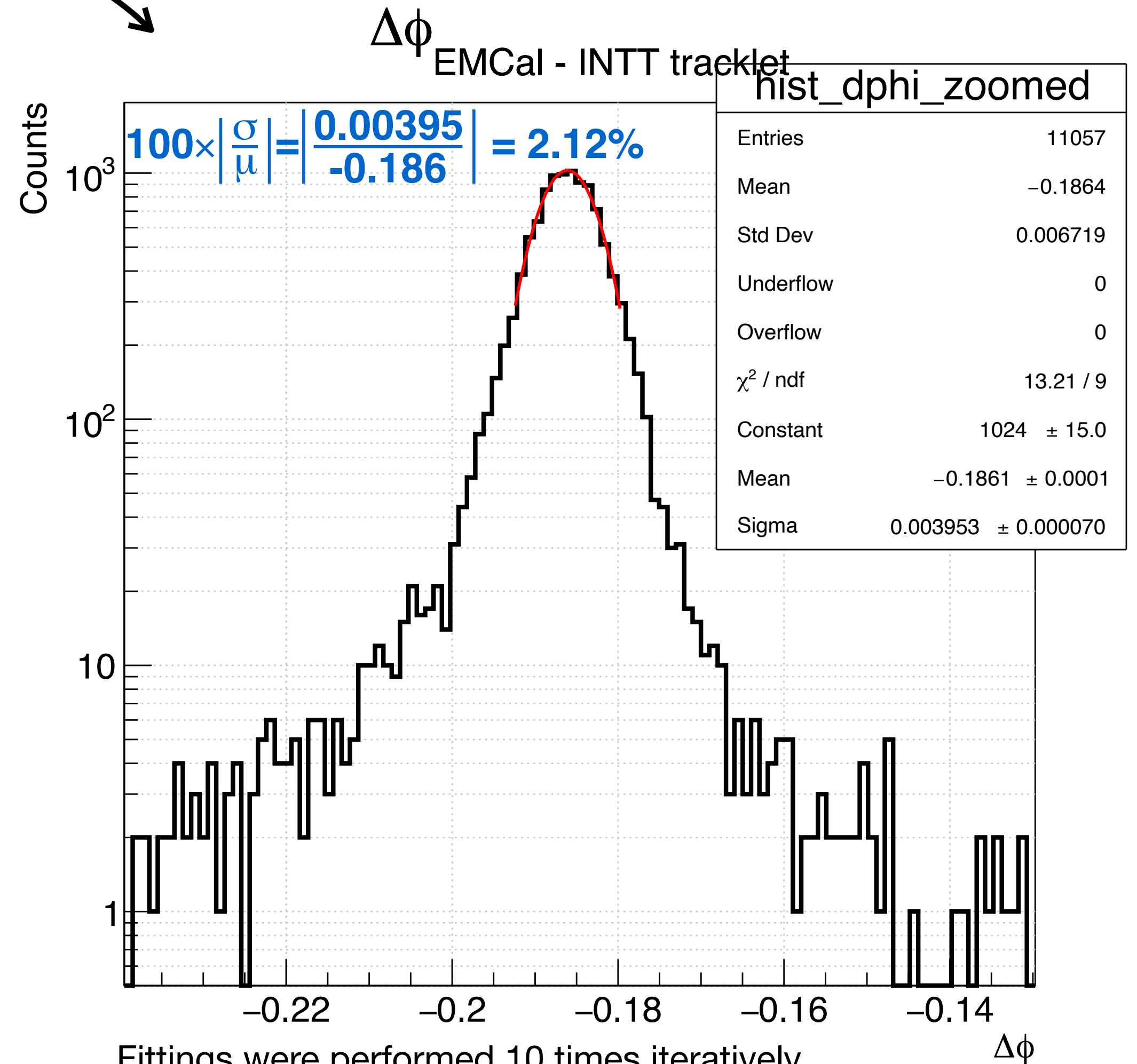
Cuts

- At least 1 EMCal hit
- At least 2 INTT hits
- $\rho_{EMCal} < 99$ cm
- $|\phi_{tracklet-beam} - \mu_{\phi_{tracklet-beam}}| < 2\sigma_{\phi_{tracklet-beam}}$

zoom



hist_dphi	
Entries	11469
Mean	-0.1846
Std Dev	0.02745
Underflow	52
Overflow	151



hist_dphi_zoomed	
Entries	11057
Mean	-0.1864
Std Dev	0.006719
Underflow	0
Overflow	0
χ^2 / ndf	13.21 / 9
Constant	1024 \pm 15.0
Mean	-0.1861 \pm 0.0001
Sigma	0.003953 \pm 0.000070

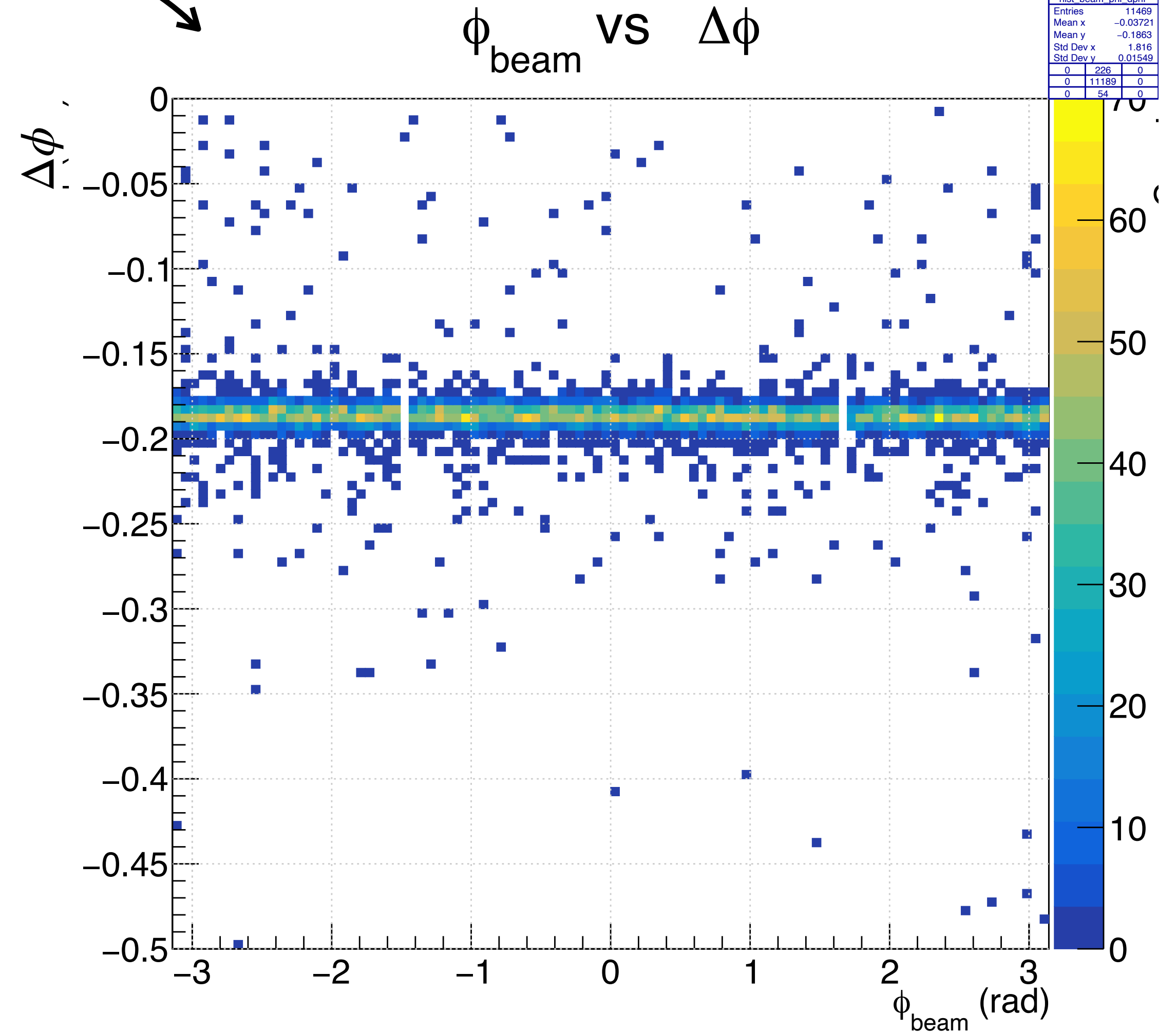
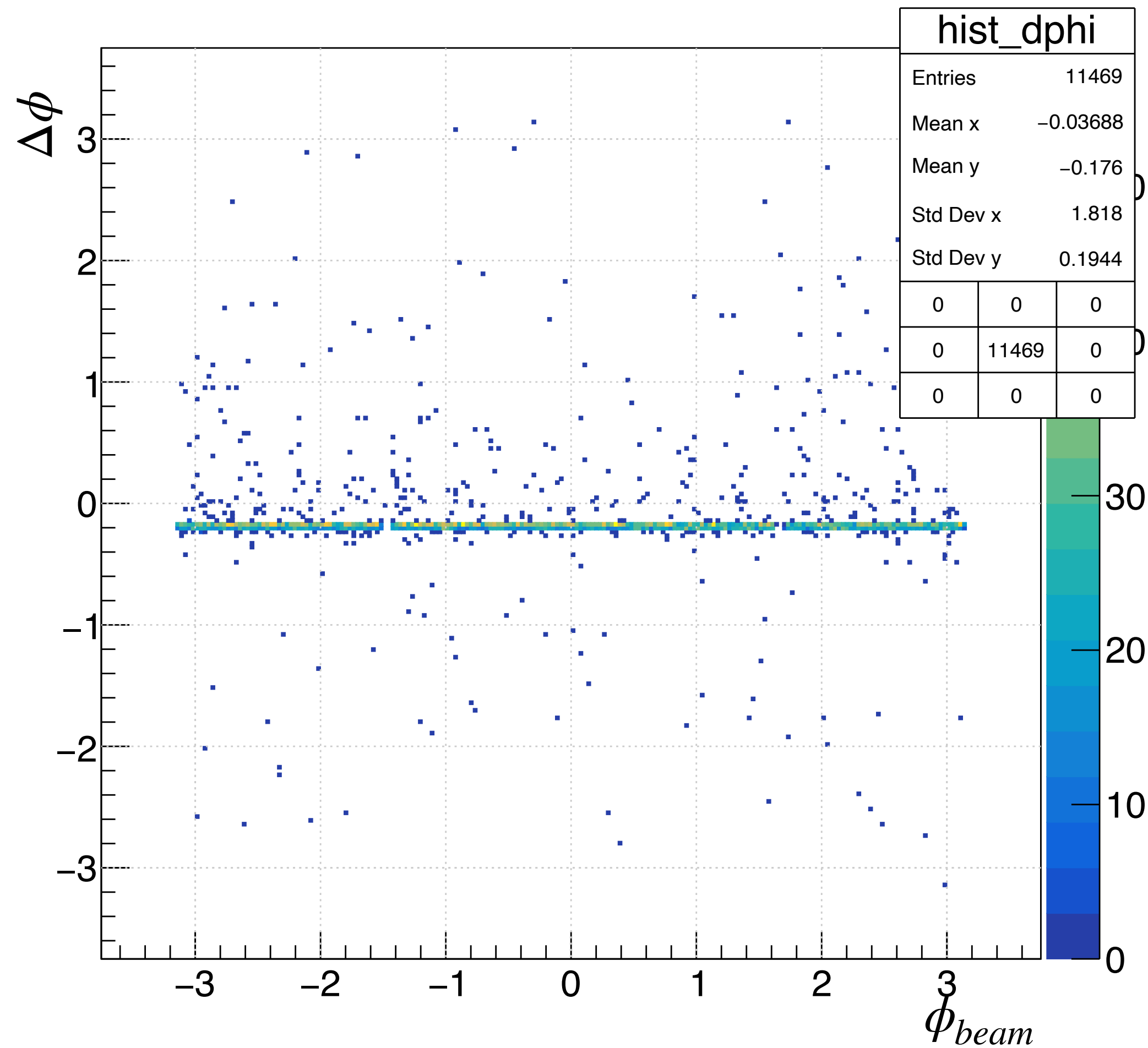
Run1 : ϕ angle resolution as a function of ϕ_{beam}

Cuts

- At least 1 EMCal hit
- At least 2 INTT hits
- $\rho_{\text{EMCal}} < 99$ cm
- $|\phi_{\text{tracklet-beam}} - \mu_{\phi_{\text{tracklet-beam}}}| < 2\sigma_{\phi_{\text{tracklet-beam}}}$

dphi_hist_emcal_vec_beam.PHI [d_good_event && ht_emcal_innermost.PHI<99 && 0.02046<-ROOT::Math::VectorBl::PHI_mpi_phi_vec_int_tracklet.PHI-vec_beam.PHI] && ROOT::Math::VectorBl::PHI_mpi_phi_vec_int_tracklet.PHI-vec_beam.PHI] && 0.042470]

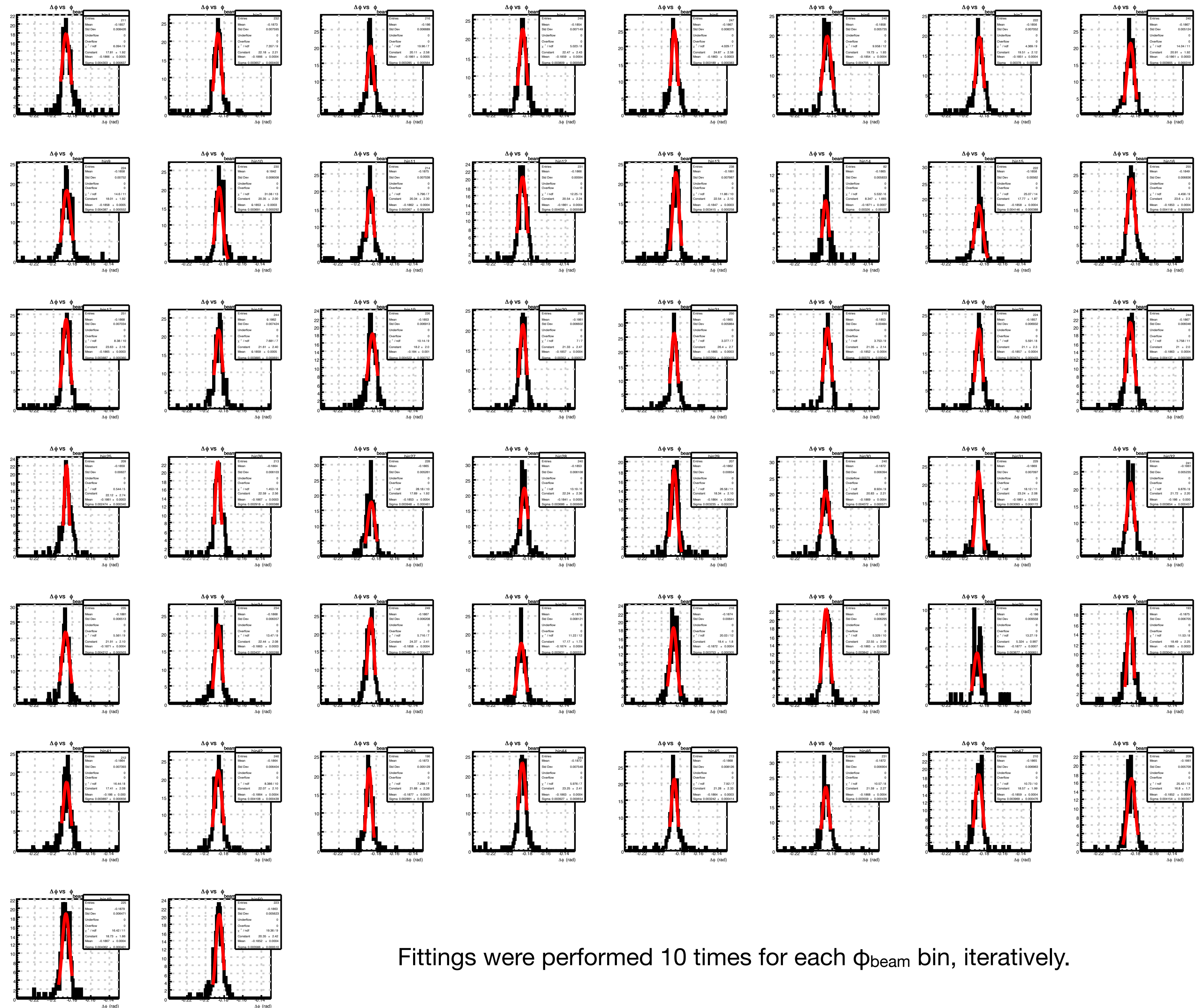
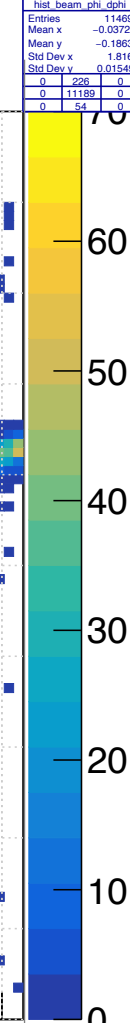
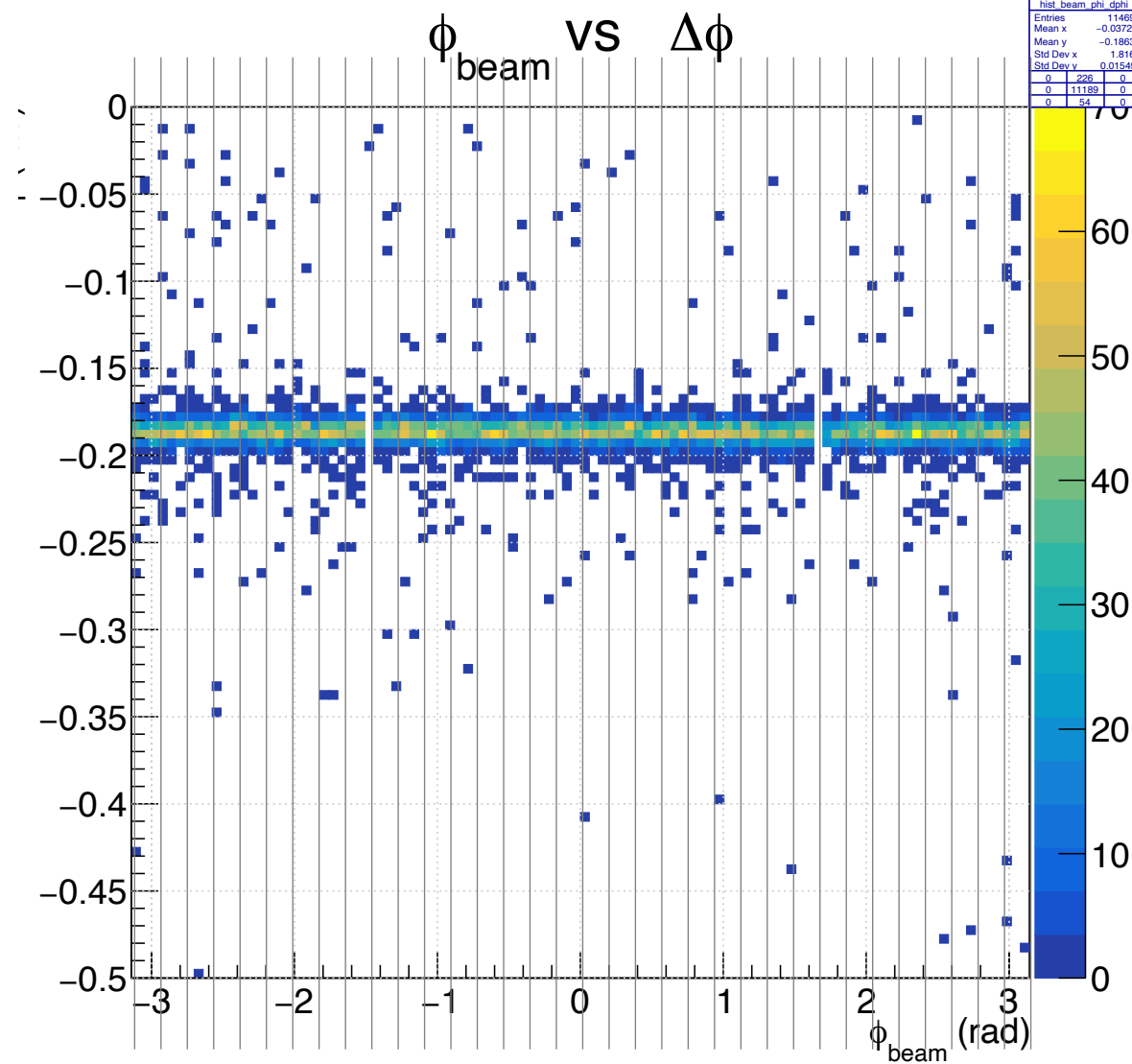
zoom



Run1 : ϕ angle

Cuts

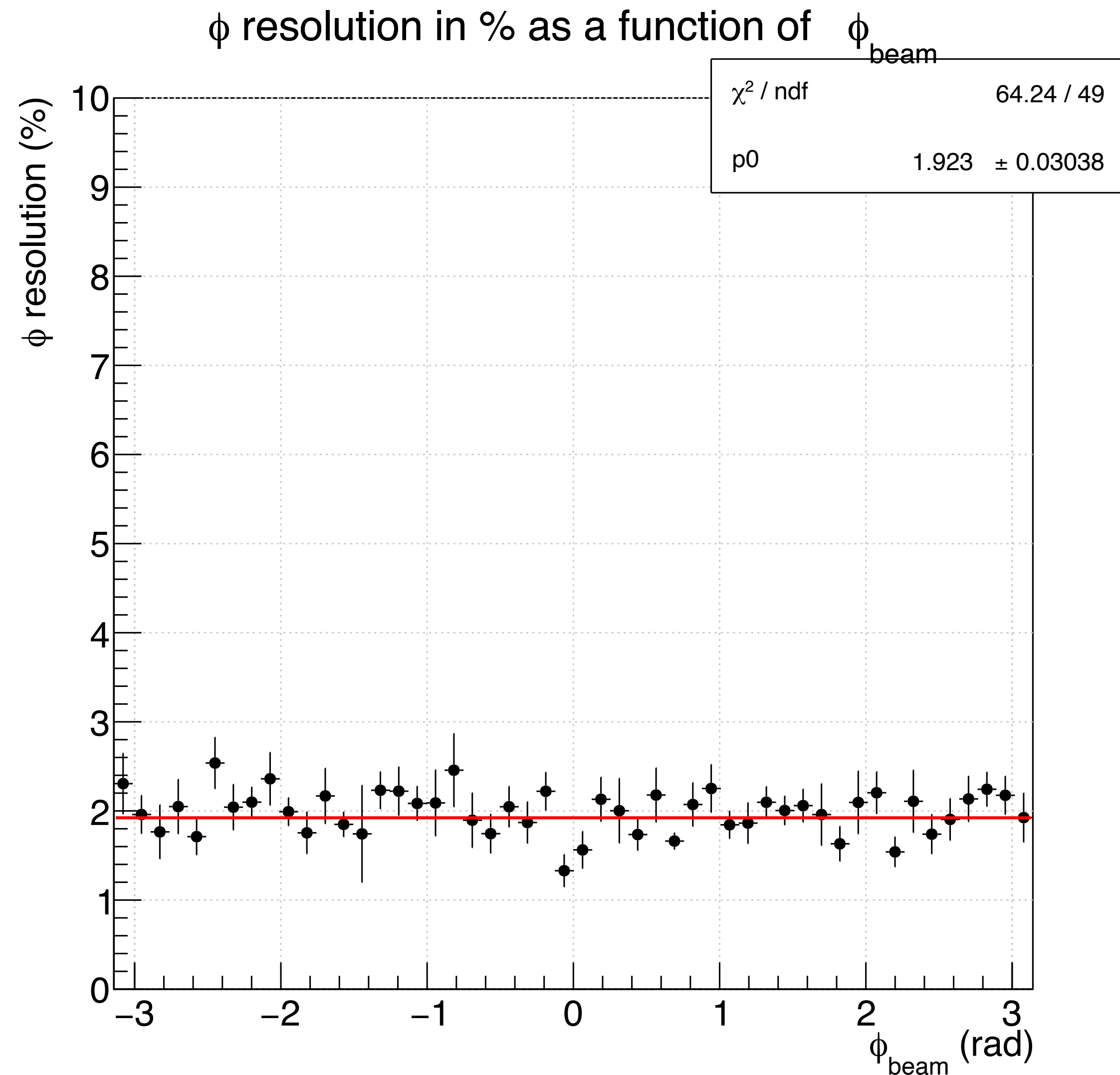
- At least 1 EMCal hit
- At least 2 INTT hits
- $\rho_{EMCal} < 99$ cm
- $|\phi_{tracklet-beam} - \mu_{\phi_{tracklet-beam}}| < 2\sigma_{\phi_{tracklet-beam}}$



Mean and std. dev. are evaluated for each ϕ_{beam} bin.
The bin width is currently $2\pi/50$.

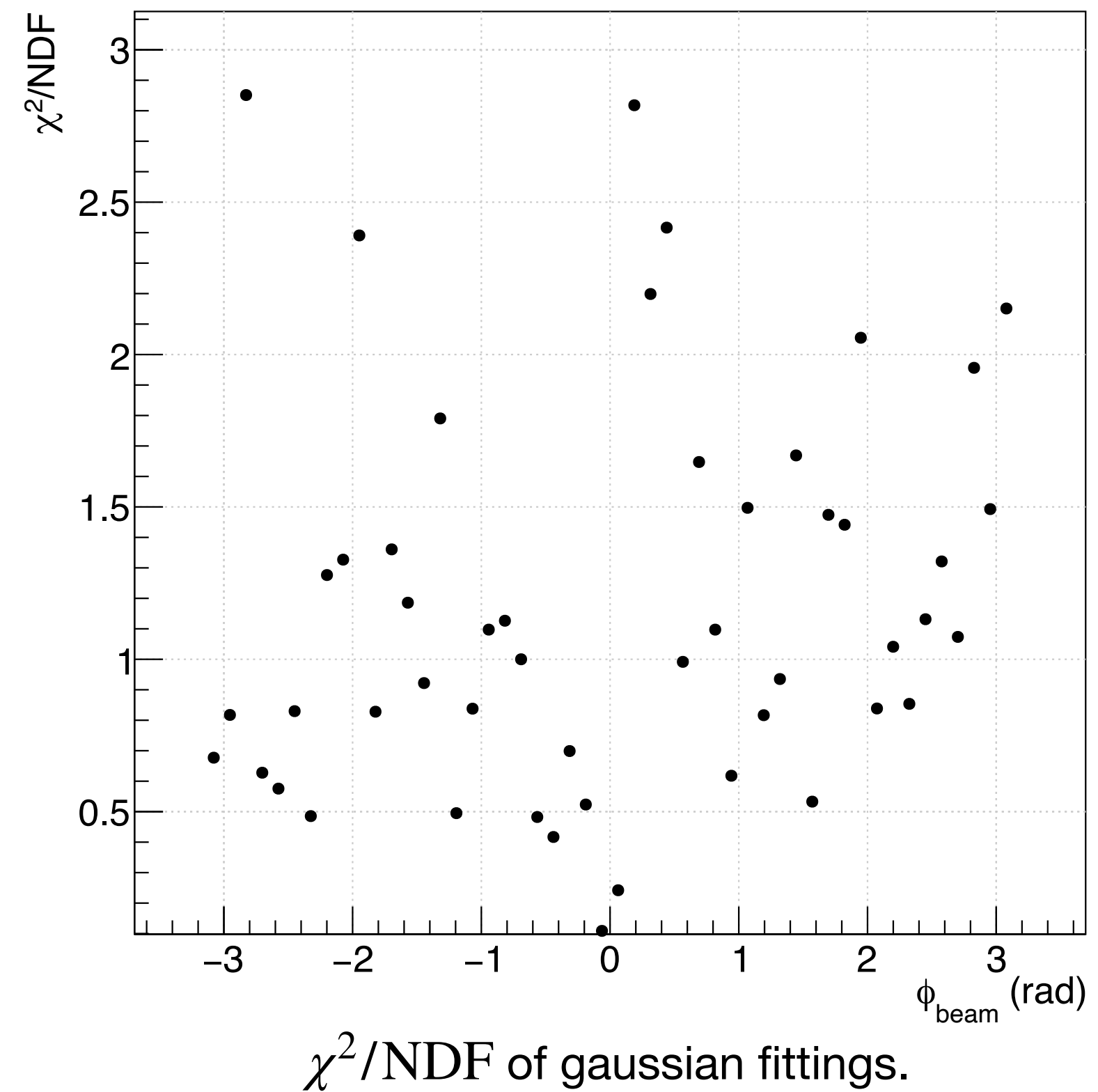
Fittings were performed 10 times for each ϕ_{beam} bin, iteratively.

Run1 : ϕ angle resolution as a function of ϕ_{beam}

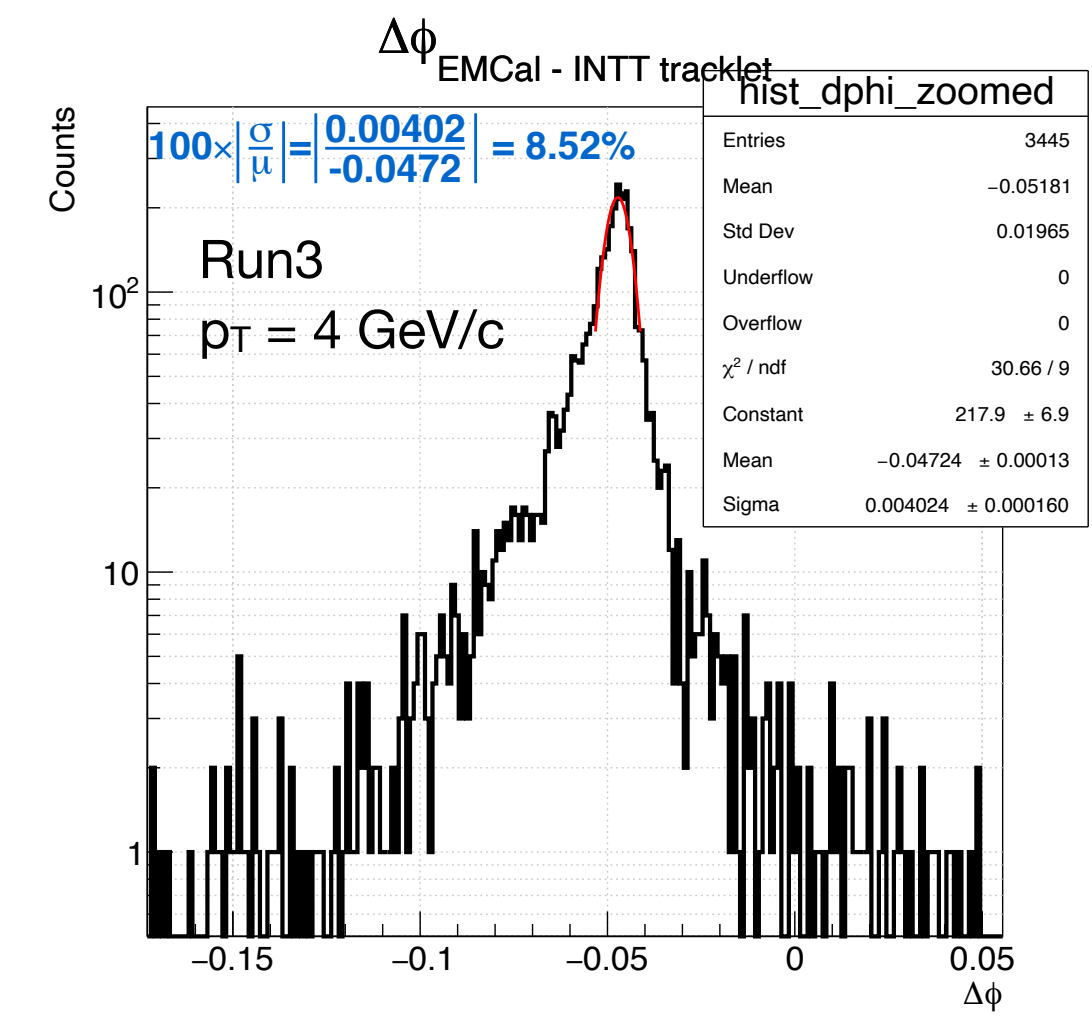
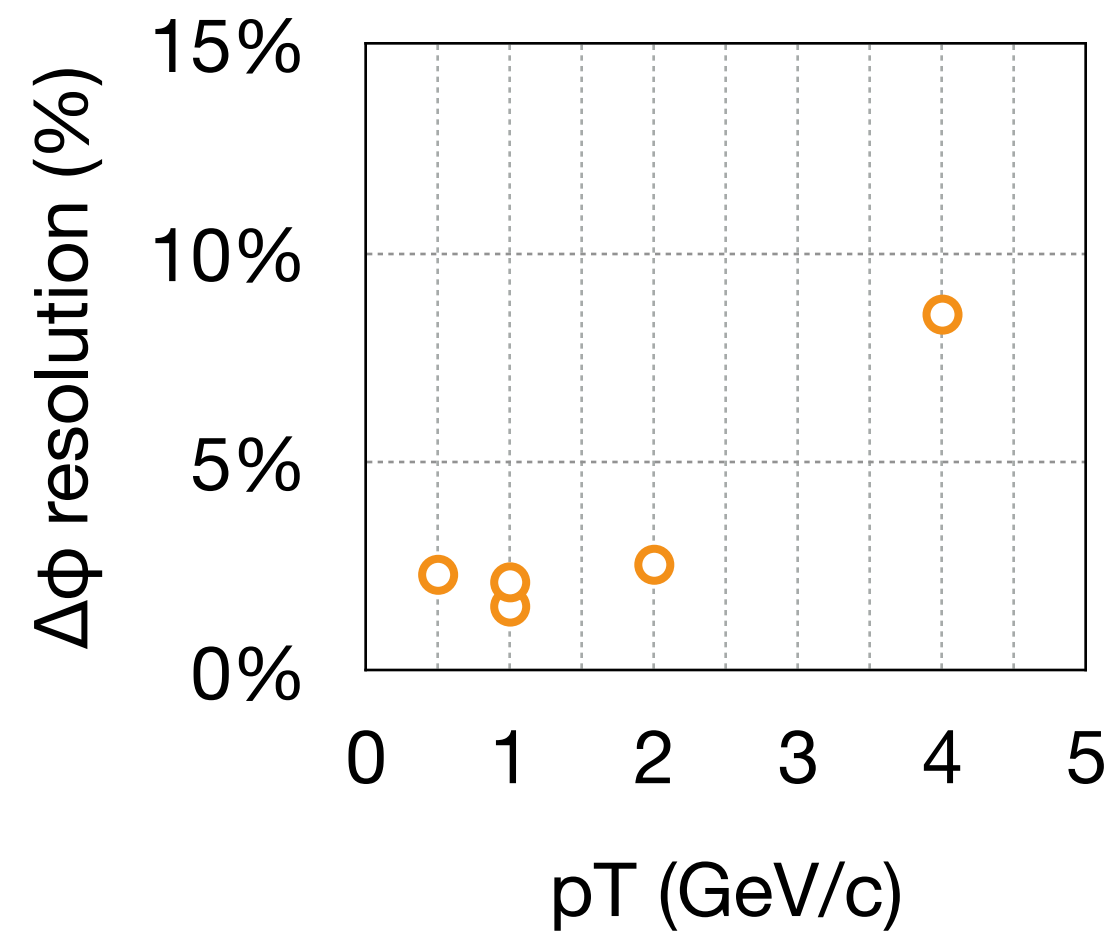
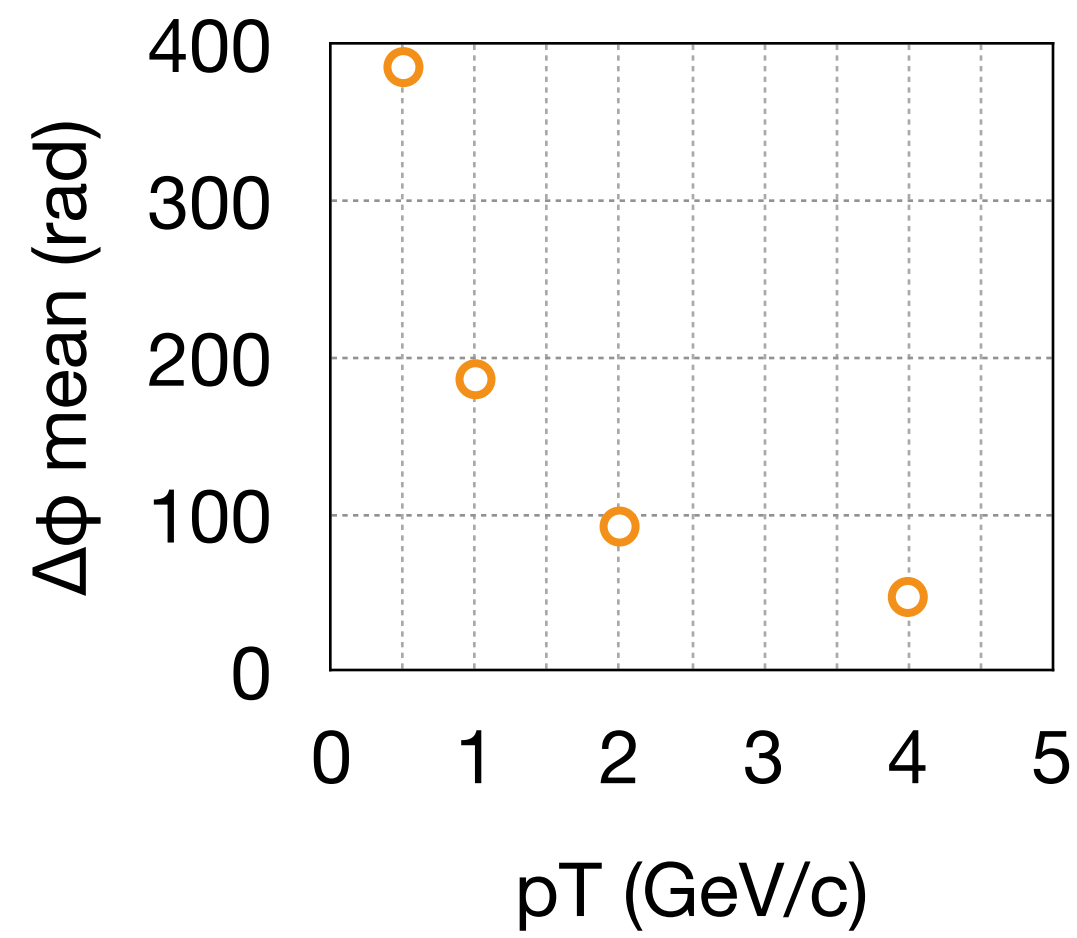


Cuts

- At least 1 EMCal hit
- At least 2 INTT hits
- $\rho_{\text{EMCal}} < 99$ cm
- $|\phi_{\text{tracklet-beam}} - \mu_{\phi_{\text{tracklet-beam}}}| < 2\sigma_{\phi_{\text{tracklet-beam}}}$



Beam Energy Scan



Run	#event	Beam	Momentum (GeV/c)	φ dist (rad)	η dist	vertex (cm)	Δφ mean (mrad)	Δφ std. dev. (mrad)	Δφ resolution (%)
Pilot	2k	μ ⁻	1	fixed at π/2	fixed at 0	fixed at (0, 0, 0)	186	2.87	1.54%
1	50k	μ ⁻	1	[-π, π]	fixed at 0	fixed at (0, 0, 0)	186	3.95	2.12%
2	50k	μ ⁻	2	[-π, π]	fixed at 0	fixed at (0, 0, 0)	92.1	2.34	2.54%
3	50k	μ ⁻	4	[-π, π]	fixed at 0	fixed at (0, 0, 0)	47.2	4.02	8.52% ←!?
4	50k	μ ⁻	0.5	[-π, π]	fixed at 0	fixed at (0, 0, 0)	385	8.85	2.30%