

[Sakai,Sugimoto,KH (0806.3122)]

	Superstring	Experiment	
$\langle r^2 \rangle_{E,p}$	$(0.74 \text{ fm})^2$	$(0.875 \text{ fm})^2$	
$\langle r^2 \rangle_{E,n}$	0	$-0.116 \text{ fm}^2$	
$\langle r^2 \rangle_A^{1/2}$	0.54 fm	0.674 fm	
$\mu_p$	2.2	2.79	
$\mu_n$	-1.3	-1.91	
$g_A$	0.73	1.27	
$g_{\pi NN}$	7.5	13.2	
$g_{\rho NN}$	5.8	4.2 – 6.5	Lattice
$\mu_{\Delta^{++}}$	4.4	3.7 – 7.5	4.99
$\mu_{\Delta^+}$	2.3	–	2.49
$\mu_{\Delta^0}$	0.20	–	0.06
$\mu_{\Delta^-}$	-1.9	–	-2.45



# A Holographic Thermalization



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w/ N.Iizuka (CERN), T.Oka (Tokyo)

arXiv:1012.4463 (PRD84,066005(2011))

# What can the dictionary deal with?

General : Chiral condensate, Quark antiquark forces,  
Wilson / Polyakov loop, Phase diagram, Gluon scattering, ...

**Mesons** : Spectra, interactions, Skyrme term,  
Vector meson dominance, Hidden local symmetry,  
Chiral perturbations, Quark mass effects, ...

**Baryons** : Spectra, interactions, nuclear forces,  
3-body nuclear forces, Giant resonances, ...

**Exotics** : Glueball spectra, Glueball decays, ...

**Hot QCD** : Deconfinement transition, Chiral restoration,  
Quark gluon plasma, Viscosity, Jet quenching parameters,  
Quark drag force, Meson melting, Thermalization, ...

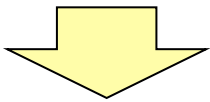
**Dense QCD** : Chiral restoration, Color superconductor,  
Meson mass in nuclear matter, ...

# Superstrings useful for...

Superstring is ...

- Bad at :
- Precision evaluation (... Large  $N_c$ )
  - Asymptotic freedom (... strong coupling)

- Good at :
- Analytic calculation
  - Finite density
  - Time dependence



Superstring, better applied to :

Robust features of strongly coupled QCD,  
time-dependent / independent

This talk : **Thermalization at Heavy ion collisions**

(1)

Problem

Derivation of the Rapid thermalization at Heavy ion collision?

(2)

Cause

QCD : strongly coupled, & confined  $\rightarrow$  deconfined

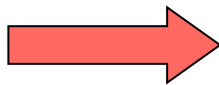
Thermalization : non-equilibrium & time-dependent process

(3)

Our solution

AdS/CFT can treat all the causes.

+ Initial condition mimicking the collision

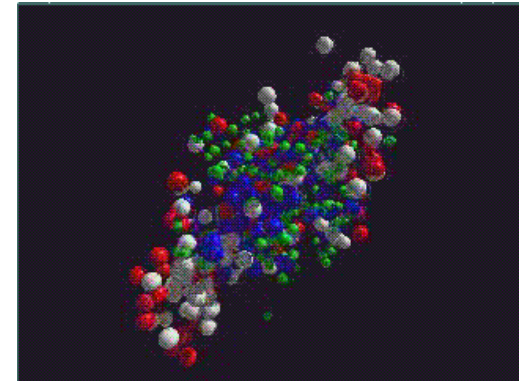
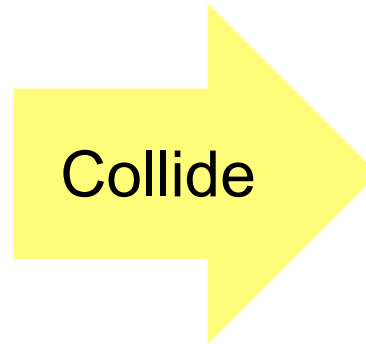
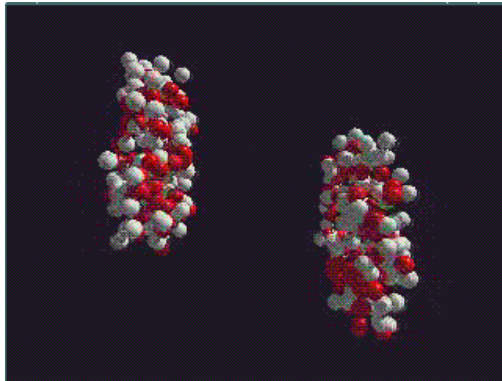


A Rapid Thermalization

(1)

Problem

Derivation of the Rapid thermalization at Heavy ion collision?



Hydrodynamic simulation suggests a rapid thermalization :

$$t_{\text{th}} < 2 \text{ [fm/c]}$$

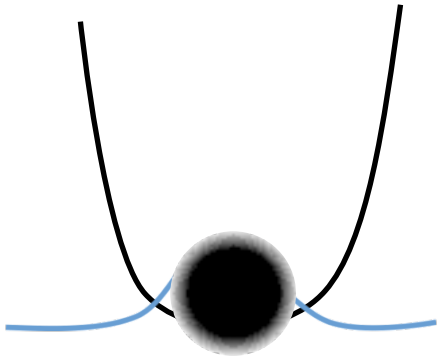
[Kolb, Huovinen, Heinz, Heiselberg ('00)],  
[Hirano ('01)], [Huovinen ('01)],  
[Teaney, Lauret, Shuryak ('01)], [Heinz, Kolb ('02)], ...

(2)

Cause

QCD : strongly coupled, & confined  $\rightarrow$  deconfined

Thermalization : non-equilibrium & time-dependent process



AdS

/

CFT

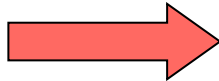
Formation of  
Black Hole Horizon = Thermalization  
+ deconfinement

(3)

Our solution

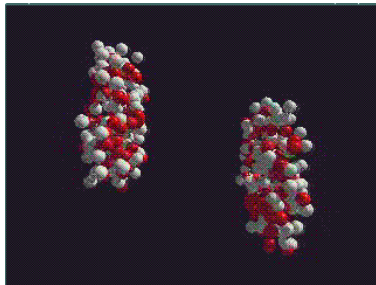
AdS/CFT can treat all the causes.

+ Initial condition mimicking the collision

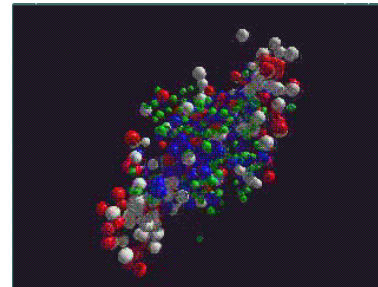


Rapid thermalization

Initial condition ?



Collide



- Bjorken expansion [Janik, Peschanski ('06)], [Chesler, Yaffe ('08)],  
[Bhattacharyya, Minwalla ('09)], ...  
[Muller, et.al ('10)]

- Sudden change of Baryon number density [Ours]

Both should give the rapid thermalization



## Plan of the remaining of this talk

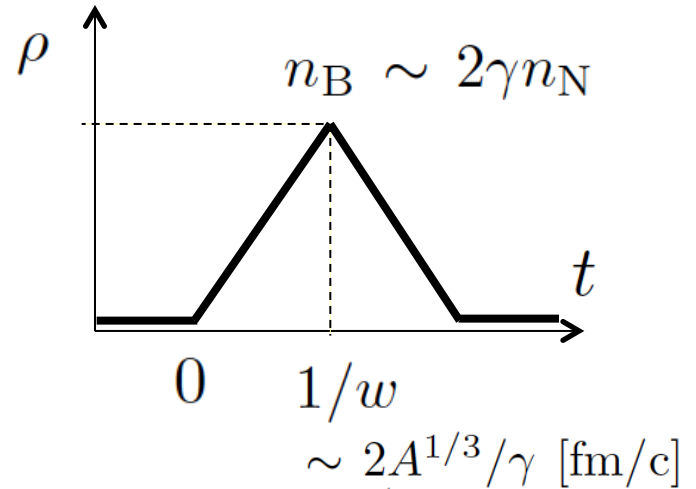
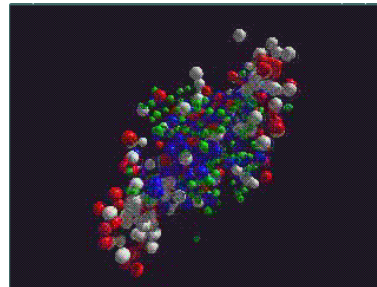
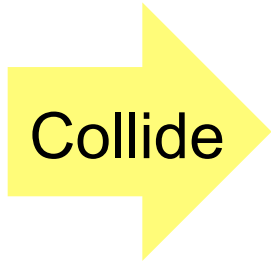
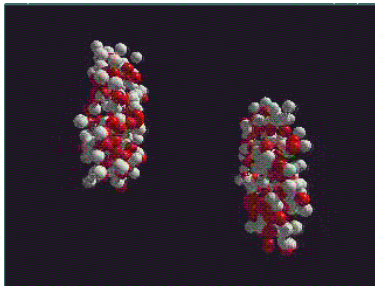
Our idea: Collision = a time dep. baryon density

Time dependence, solved

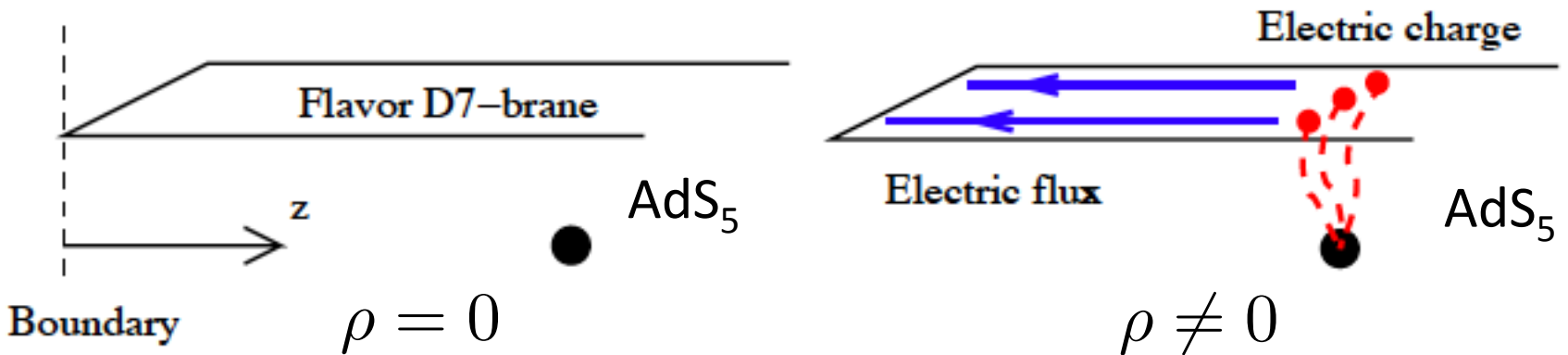
Nonlinearity  $\rightarrow$  Effective horizon

Thermalization timescale, a fun part

# Our idea : Collision = a time-dep. baryon density

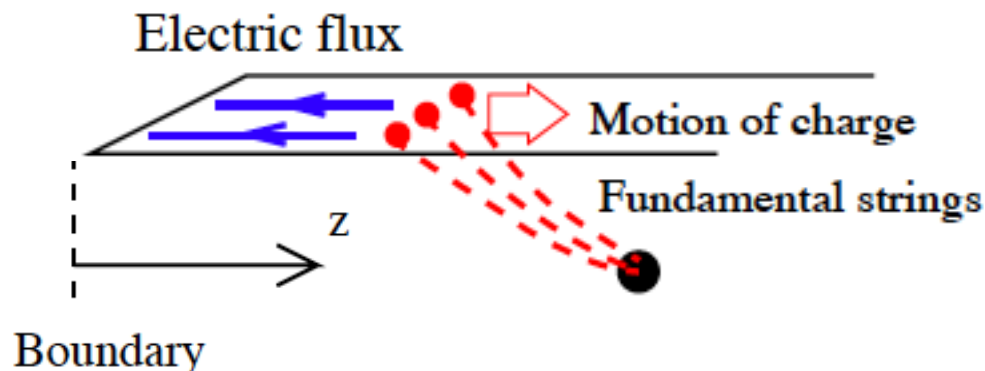


$N=2$  Supersymmetric QCD



[Aprea, Erdmenger, Evans, Fralnik ('05)], [Kim, Sin, Zahed ('06)],  
 [Horigome, Tanii ('06)], [Parnachev, Sahakyan ('06)],  
 [Kobayashi, Mateos, Matuura, Myers, Thomson ('06)], ...

## Time dependence, solved



On the Flavor D-brane in curved geometry,

**solve nonlinear Maxwell with source motion**

$$S = -\mu_7 \int d^8 \xi \sqrt{-\det (G_{ab} + 2\pi\alpha' F_{ab})}$$

$$\delta S = \mu_7 V_3 \text{Vol}(S^3) \int dt dz (A_t j^t + A_z j^z)$$

$$j^t = j^z = g'(t - z) \quad g(t) = (2/\pi)(2\pi\alpha')^4 \lambda n_B(t)$$

“Holographic Quantum Quench” [Das, Nishioka, Takayanagi ('10)]

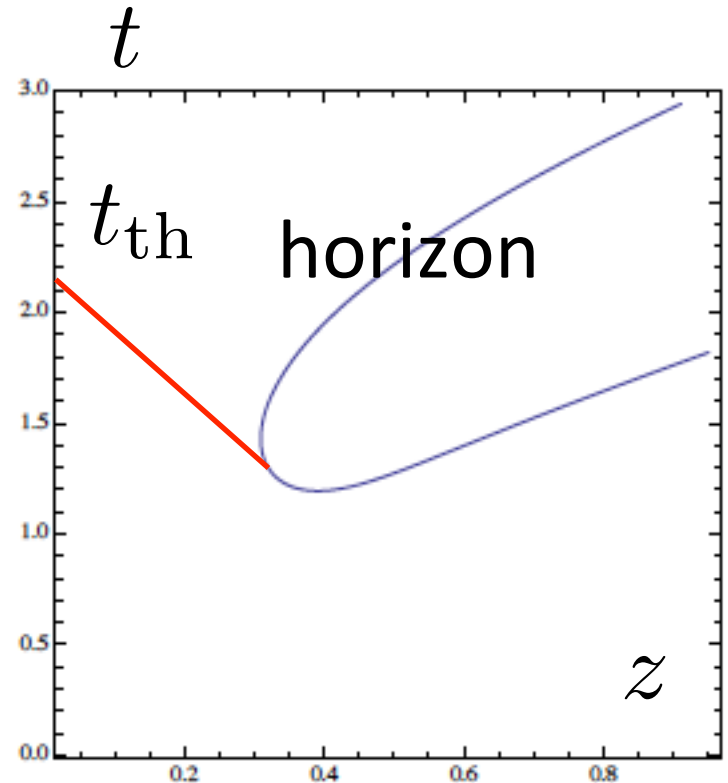
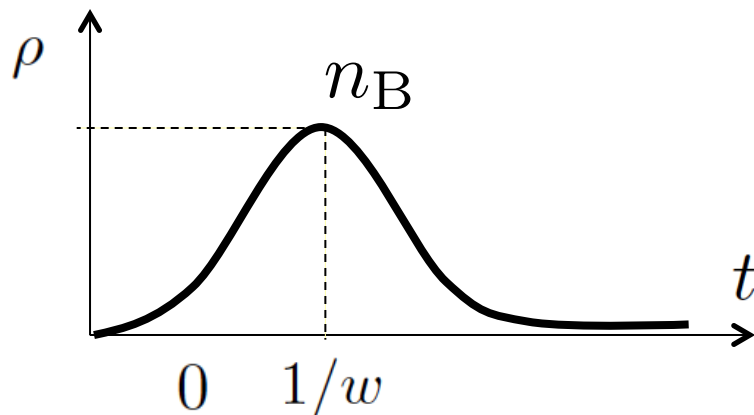
# Nonlinearity $\rightarrow$ Effective Horizon

Small fluctuation on the flavor D-brane (meson modes) feels emergence of **effective horizon**  $\rightarrow$  Thermalization

$$(\partial_z - \partial_t) [z^2(1 - z^4 R^{-4} (2\pi\alpha')^2) F_{tz}^2] = 0$$

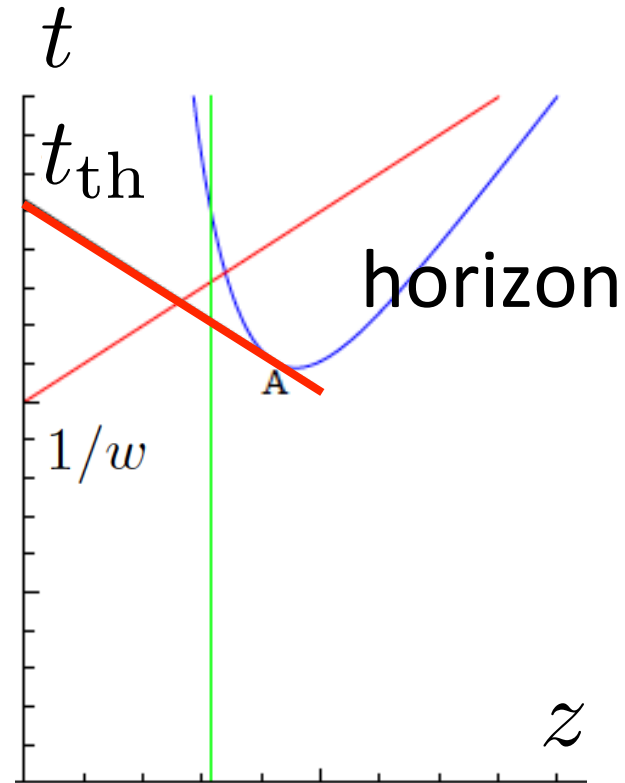
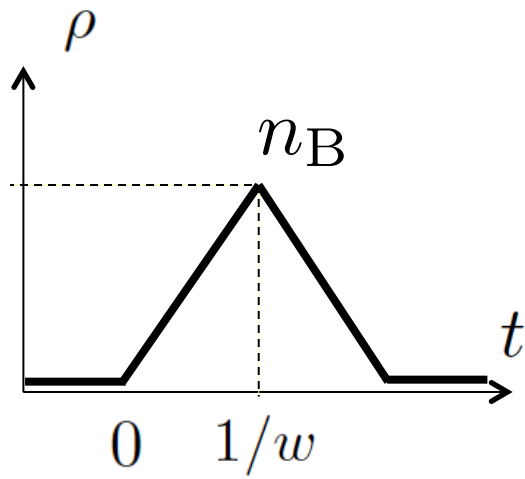
Example: gaussian change

$$\rho(t) = n_B \exp [-(2w)^2 (t - 1/w)^2]$$



# Thermalization timescale

Example: linear change



$$t_{\text{th}} \sim \min_{\{k=0,1,2\}} \left\{ \left( \frac{\lambda}{n_B^2 w^k} \right)^{1/(6+k)} \right\}$$

## Fun : physical parameters

$$t_{\text{th}} \sim \min_{\{k=0,1,2\}} \left\{ \left( \frac{\lambda}{n_{\text{B}}^2 w^k} \right)^{1/(6+k)} \right\}$$

RHIC Au Collision:

$$n_{\text{B}} \sim 2\gamma n_{\text{N}}$$
$$1/w \sim 2A^{1/3}/\gamma \text{ [fm/c]}$$
$$\gamma = E/m_{\text{Au}} \sim 100$$



$$t_{\text{th}} < 1 \text{ [fm/c]}$$

**Rapid thermalization,  
consistent with hydrodynamics**

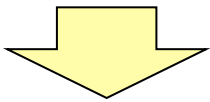
$$t_{\text{th}} \lesssim \mathcal{O}(0.1) \text{ [fm/c]} \quad \text{for LHC}$$

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