Spin Physics at EIC

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Outline

- Deeply virtual Compton scattering (DVCS)

↪ Generalized parton distributions (GPDs)

↪ 'transverse imaging'

- Probabilistic interpretation of GPDs as Fourier transforms of impact parameter dependent PDFs
  - $H(x, 0, -\mathbf{\Delta}_\perp^2) \longrightarrow q(x, \mathbf{b}_\perp)$
  - $E(x, 0, -\mathbf{\Delta}_\perp^2) \longrightarrow \perp$ deformation of PDFs when the target is $\perp$ polarized

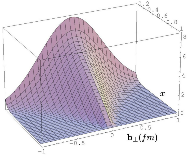
  ↪ Ji relation

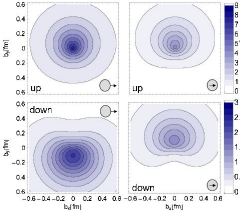
- Chromodynamik lensing and $\perp$ single-spin asymmetries (SSA)

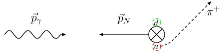
$$\left.\begin{array}{c}\text{transverse distortion of PDFs}\\ +\text{ final state interactions}\end{array}\right\} \Rightarrow$$

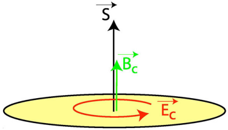
↪ SSA in $\gamma N \longrightarrow \pi + X$

- quark-gluon correlations $\rightarrow \perp$ force on q in DIS
- Summary









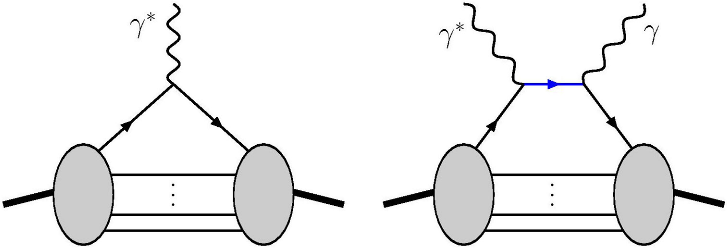
3 D imaging — join the experience!

- virtual Compton scattering: $\gamma^* p \longrightarrow \gamma p$ (actually: $e^- p \longrightarrow e^- \gamma p$)
- 'deeply': $-q_\gamma^2 \gg M_p^2, |t| \longrightarrow$ Compton amplitude dominated by (coherent superposition of) Compton scattering off single quarks

$\hookrightarrow$ only difference between form factor (a) and DVCS amplitude (b) is replacement of photon vertex by two photon vertices connected by quark (energy denominator depends on quark momentum fraction x)

$\hookrightarrow$ DVCS amplitude provides access to momentum-decomposition of form factor = Generalized Parton Distribution (GPDs).

$$\int dx H_q(x,\xi,t) = F_1^q(t) \qquad \int dx E_q(x,\xi,t) = F_2^q(t)$$



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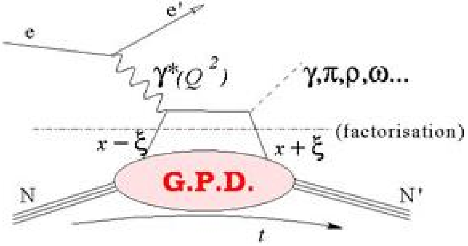


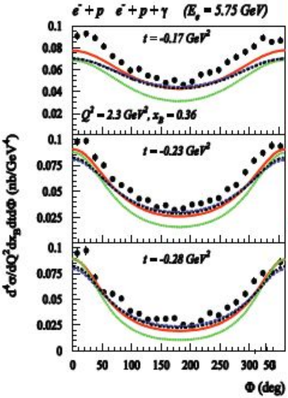
- wide Q^2 range

$\hookrightarrow$ Q^2 dependence to disentangle convolution integral in $\mathcal{A}_{DVCS}$

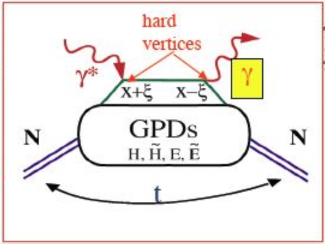
- high luminosity:
  - $\sigma_{DVCS} = \mathcal{O}(\alpha^3)$
  - study dependence on x, t, Q^2

Unprecedented set of Deeply Virtual Compton Scattering data accumulated in Hall A and with *CLAS in Hall B at JLab*

Hall A



Phys.Rev.Lett.97:262002,2006



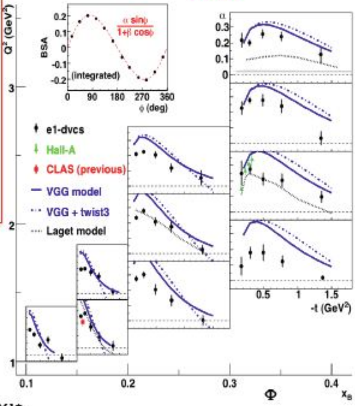
$$A = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{\Delta\sigma_{LU}}{2\sigma}$$

Polarized beam, unpolarized target:

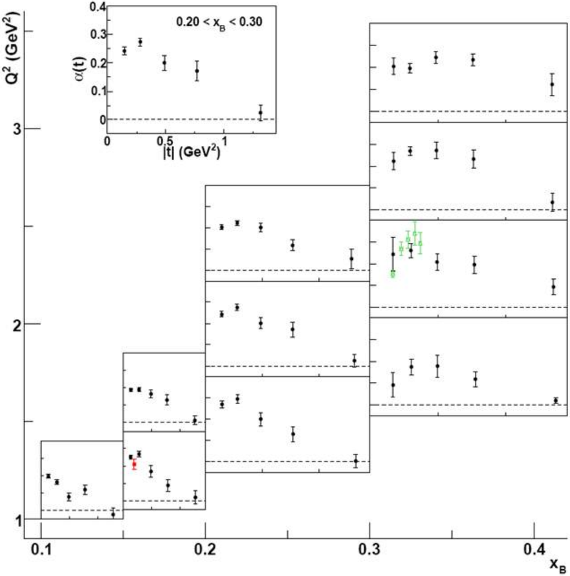
Kinematically suppressed

$$\Delta\sigma_{LU} \sim \sin\phi\{F_1 H + \xi(F_1+F_2)\tilde{H} + kF_2 E\}d\phi$$

CLAS



Phys.Rev.Lett.100:162002,2008



Q² (GeV²)
α(t)
0.20 < x_B < 0.30
|t| (GeV²)
x_B

- form factors: $\stackrel{FT}{\longleftrightarrow} \rho(\vec{r})$
- $GPDs(x, \vec{\Delta})$: form factor for quarks with momentum fraction x

$\hookrightarrow$ suitable FT of $GPDs$ should provide spatial distribution of quarks with momentum fraction x

- careful: cannot measure longitudinal momentum (x) and longitudinal position simultaneously (Heisenberg)

$\hookrightarrow$ consider purely transverse momentum transfer

Impact Parameter Dependent Quark Distributions

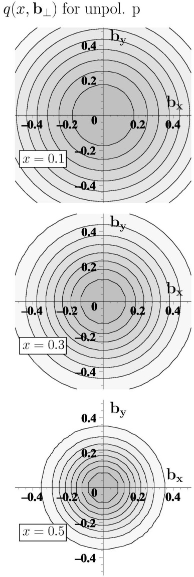
$$q(x, \mathbf{b}_\perp) = \int \frac{d^2\Delta_\perp}{(2\pi)^2} H(x, \xi = 0, -\mathbf{\Delta}_\perp^2) e^{-i\mathbf{b}_\perp \cdot \mathbf{\Delta}_\perp}$$

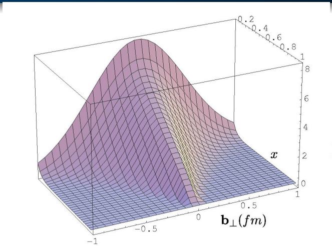
$q(x, \mathbf{b}_\perp)$ = parton distribution as a function of the separation $\mathbf{b}_\perp$ from the transverse center of momentum $\mathbf{R}_\perp \equiv \sum_{i \in q,g} \mathbf{r}_{\perp,i} x_i$
MB, Phys. Rev. D62, 071503 (2000)

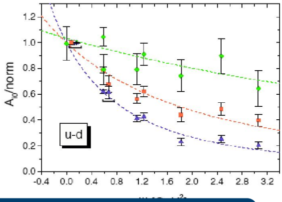
- No relativistic corrections (Galilean subgroup!)

$\hookrightarrow$ corollary: interpretation of 2d-FT of $F_1(Q^2)$ as charge density in transverse plane also free of relativistic corrections

- probabilistic interpretation





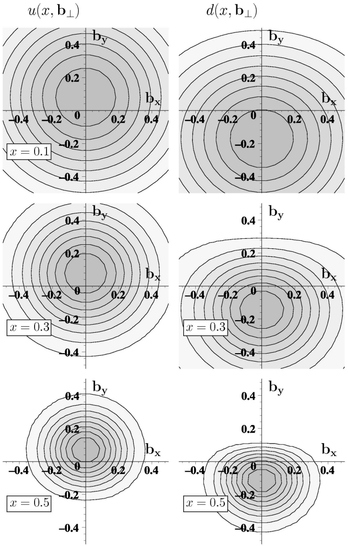


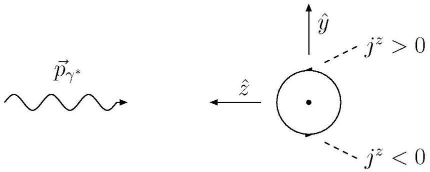
unpolarized proton

- $q(x, \mathbf{b}_\perp) = \int \frac{d^2\Delta_\perp}{(2\pi)^2} H(x, 0, -\boldsymbol{\Delta}_\perp^2) e^{-i\mathbf{b}_\perp \cdot \boldsymbol{\Delta}_\perp}$
- x = momentum fraction of the quark
- $\vec{b} = \perp$ distance of quark from $\perp$ center of momentum
- small x: large 'meson cloud'
- larger x: compact 'valence core'
- $x \to 1$: active quark becomes center of momentum

$\hookrightarrow$ $\vec{b}_\perp \to 0$ (narrow distribution) for $x \to 1$

Impact parameter dependent quark distributions





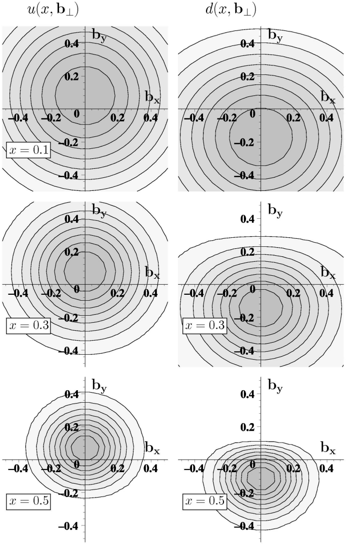
proton polarized in $+\hat{x}$ direction

no axial symmetry!

$$q(x, \mathbf{b}_\perp) = \int \frac{d^2\Delta_\perp}{(2\pi)^2} H_q(x, 0, -\Delta_\perp^2) e^{-i\mathbf{b}_\perp \cdot \Delta_\perp}$$

$$- \frac{1}{2M} \frac{\partial}{\partial b_y} \int \frac{d^2\Delta_\perp}{(2\pi)^2} E_q(x, 0, -\Delta_\perp^2) e^{-i\mathbf{b}_\perp \cdot \Delta_\perp}$$

Physics: relevant density in DIS is $j^+ \equiv j^0 + j^3$ and left-right asymmetry from j^3



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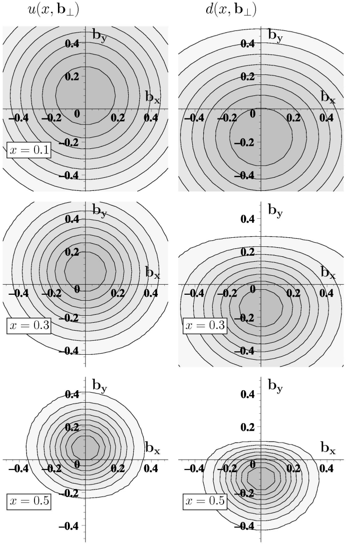
sign & magnitude of the average shift

model-independently related to p/n anomalous magnetic moments:

$$\langle b_y^q \rangle \equiv \int dx \int d^2 b_\perp q(x, \mathbf{b}_\perp) b_y = \frac{1}{2M}\int dx E_q(x, 0, 0) = \frac{\kappa_q}{2M}$$



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$$\kappa^p = 1.913 = \frac{2}{3}\kappa_u^p - \frac{1}{3}\kappa_d^p + \dots$$

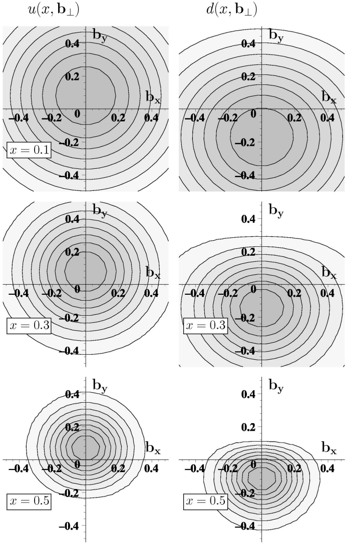
- u-quarks: $\kappa_u^p = 2\kappa_p + \kappa_n = 1.673$

↪ shift in $+\hat{y}$ direction

- d-quarks: $\kappa_d^p = 2\kappa_n + \kappa_p = -2.033$

↪ shift in $-\hat{y}$ direction

- $\langle b_y^q \rangle = \mathcal{O}\left(\pm 0.2 fm\right)$!!!!



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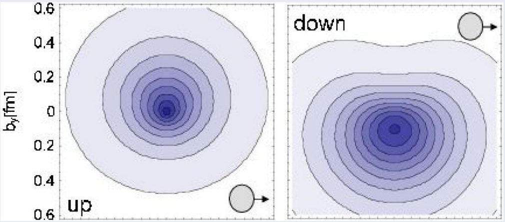
lattice QCD (QCDSF): lowest moment



transverse images ↔ Ji relation for quark angular momentum:

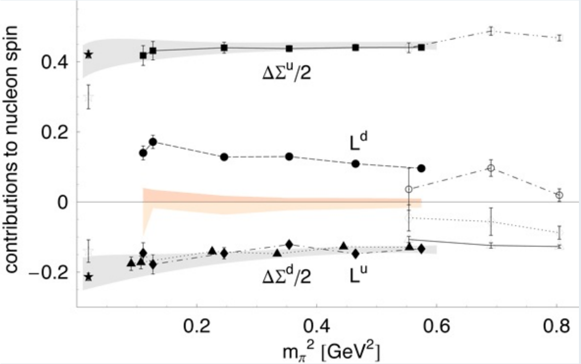
- $J_q^x = m_N \int dx\, x r^y q(x, \mathbf{r}_\perp)$ with $b^y = r^y - \frac{1}{2m_N}$, where $q(x, \mathbf{r}_\perp)$ is distribution relative to CoM of whole nucleon
- recall: $q(x, \mathbf{b}_\perp)$ for nucleon polarized in $+\hat{x}$ direction

$$q(x, \mathbf{b}_\perp) = \int \frac{d^2\Delta_\perp}{(2\pi)^2} H_q(x, 0, -\Delta_\perp^2) e^{-i\mathbf{b}_\perp \cdot \Delta_\perp} - \frac{1}{2M_N} \frac{\partial}{\partial b_y} \int \frac{d^2\Delta_\perp}{(2\pi)^2} E_q(x, 0, -\Delta_\perp^2) e^{-i\mathbf{b}_\perp \cdot \Delta_\perp}$$

$$\Rightarrow J_q^x = M_N \int dx\, x r^y q(x, \mathbf{r}_\perp) = \int dx\, x \left(m_N b^y + \frac{1}{2} \right) q(x, \mathbf{r}_\perp) = \frac{1}{2} \int dx\, x \left[H(x, 0, 0) + E(x, 0, 0) \right]$$

- X.Ji(1996): rotational invariance ⇒ apply to all components of $\vec{J}_q$
- partonic interpretation exists only for ⊥ components!

lattice: QCDSF

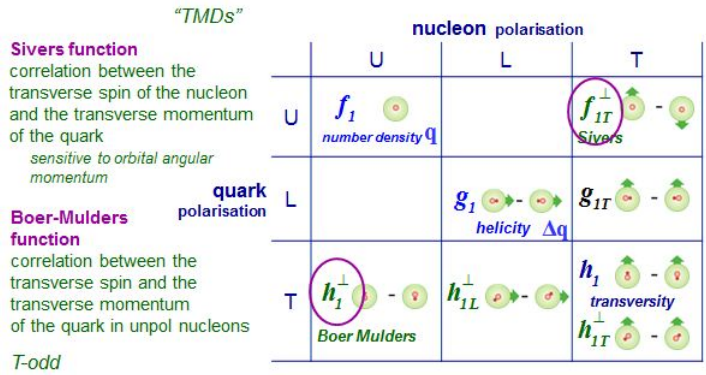


- no disconnected quark loops
- chiral extrapolation

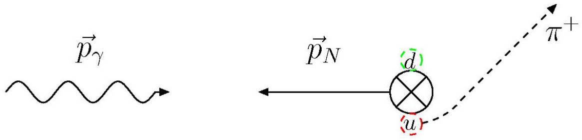
$$J^q = \frac{1}{2}\int dx\, x\,[H(x,0,0) + E(x,0,0)] \qquad L^q = J^q - \frac{1}{2}\Delta\Sigma^q$$

TMDs

- Transverse Momentum Dependent Parton Distributions
- 8 structures possible at leading twist (only 3 for PDFs)
- $f_{1T}^{\perp}$ and $h_1^{\perp}$ require both orbital angular momentum and final state interaction
- can be measured in SIDIS and DY



example: semi-inclusive deep-inelastic scattering (SIDIS) $\gamma p \rightarrow \pi X$



- u, d distributions in $\perp$ polarized proton have left-right asymmetry in $\perp$ position space (T-even!); sign 'determined' by κ_u & κ_d
- attractive FSI deflects active quark towards the CoM

$\hookrightarrow$ FSI translates position space distortion (before the quark is knocked out) in $+\hat{y}$-direction into momentum asymmetry that favors $-\hat{y}$ direction $\rightarrow$ 'chromodynamic lensing'

$\Rightarrow$ $\kappa_p\,,\kappa_n \quad \longleftrightarrow \quad$ sign of SSA!!!!!!!!

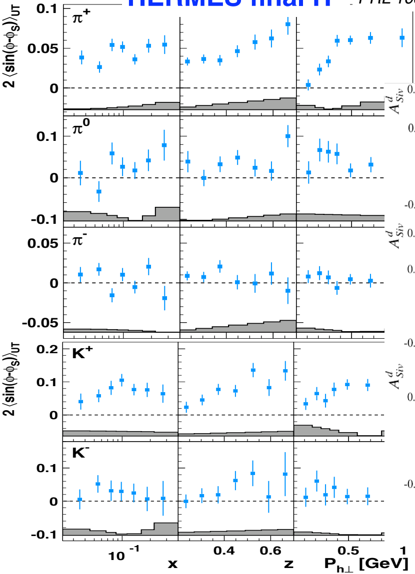
- confirmed by HERMES (and recent COMPASS) p data; consistent with vanishing isoscalar Sivers (COMPASS)

Sivers Moments for π and K from $H^{\uparrow}$ & $D^{\uparrow}$

HERMES final $H^{\uparrow}$

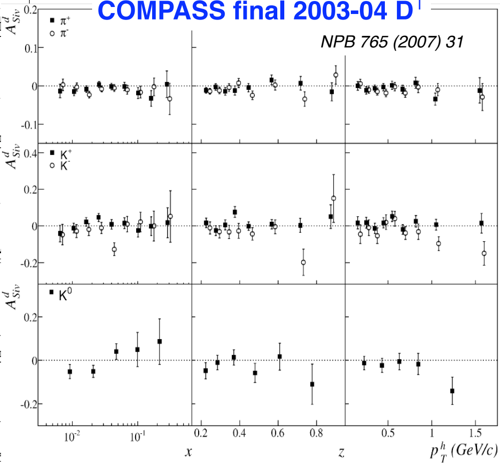
PRL 103 (2009)

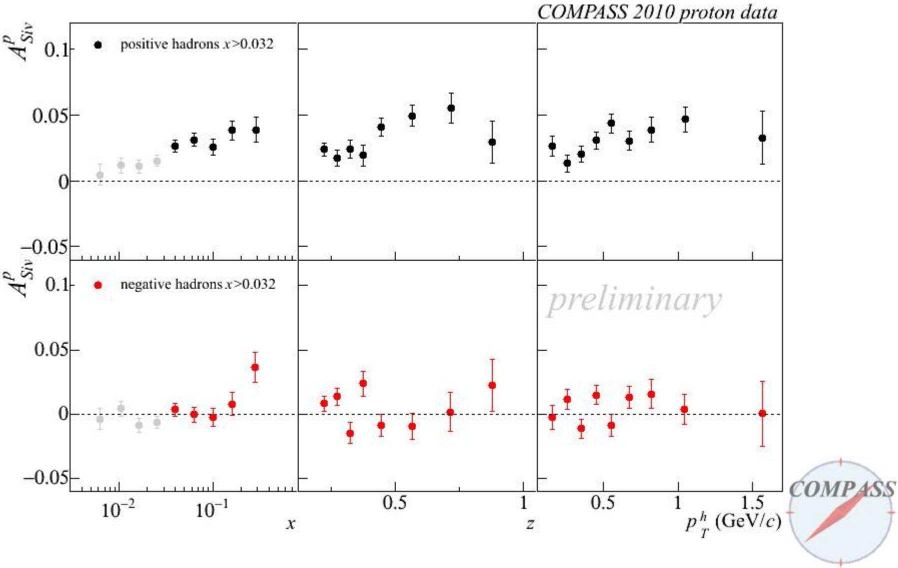
$$f_{1T}^{\perp}(x,k_T) \otimes D_1^{\perp}(z)$$



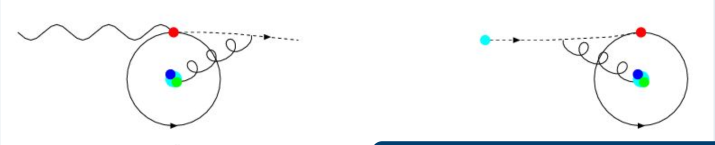
COMPASS final 2003-04 $D^{\uparrow}$

NPB 765 (2007) 31




COMPASS 2010 proton data
positive hadrons x>0.032
negative hadrons x>0.032
preliminary
A^p_{Siv}
0.1
0.05
0
−0.05
10^{-2}
10^{-1}
x
0.5
1
z
1.5
p^h_T (GeV/c)
COMPASS

compare FSI for 'red' q that is being knocked out of nucleon with ISI for 'anti-red' $\bar{q}$ that is about to annihilate with a 'red' target q



FSI in SIDIS

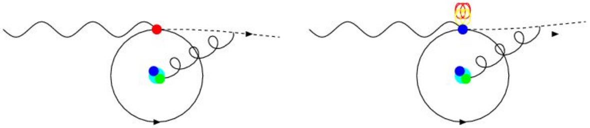
- knocked-out q 'red'
- ↪ spectators 'anti-red'
- ↪ interaction between knocked-out quark and spectators attractive

ISI in DY

- incoming $\bar{q}$ 'anti-red'
- ↪ struck target q 'red'
- ↪ spectators also 'anti-red'
- ↪ interaction between incoming $\bar{q}$ and spectators repulsive

test of $f_{1T}^{\perp}(x, \mathbf{k}_\perp)_{DY} = -f_{1T}^{\perp}(x, \mathbf{k}_\perp)_{SIDIS}$ and $h_1^{\perp}(x, \mathbf{k}_\perp)_{DY} = -h_1^{\perp}(x, \mathbf{k}_\perp)_{SIDIS}$
critical test of TMD factorization approach

'Chromodynamic lensing' mechanism for ⊥ SSA requires long range coherence of color field!



before 'dressing' active quark 'dressed' with glue

QCD-evolution: long-range color decoherence!

- after 'dressing' itself with a gluon, previously red quark more likely to be blue or green

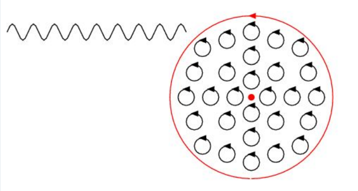
↪ attraction to far-away spectators mostly gone

- only attracted to close-by (high Q^2) g from dressing
- high Q^2: q at low x likely to have dressed itself with perturbative gluon!

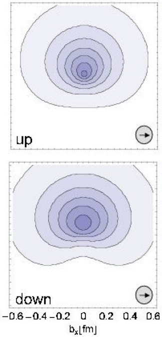
↪ 'Chromodynamic lensing' mechanism suppressed for high Q^2 & small x?

↪ interesting Q^2 dependence?

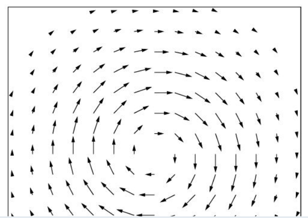
q with polarization $\odot$



lattice calculation (QCDSF)



unpolarized target



- transversity distribution in unpol. target described by chirally odd GPD $\bar{E}_T$
- $\bar{E}_T > 0$ for u & d (QCDSF)
- connection $h_1^\perp(x, \mathbf{k}_\perp) \leftrightarrow \bar{E}_T$ similar to $f_{1T}^\perp(x, \mathbf{k}_\perp) \leftrightarrow E$.

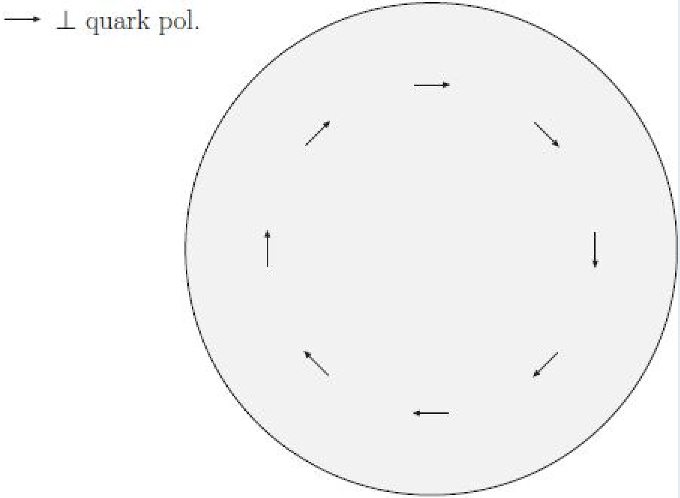
$\hookrightarrow$ $h_1^\perp(x, \mathbf{k}_\perp) < 0$ for u/p, d/p, u/π, $\bar{d}/\pi$

- $h_1^\perp{}_{SIDIS} = -h_1^\perp{}_{DY}$

experimental access

no polarization needed!

Primordial Quark Transversity Distribution



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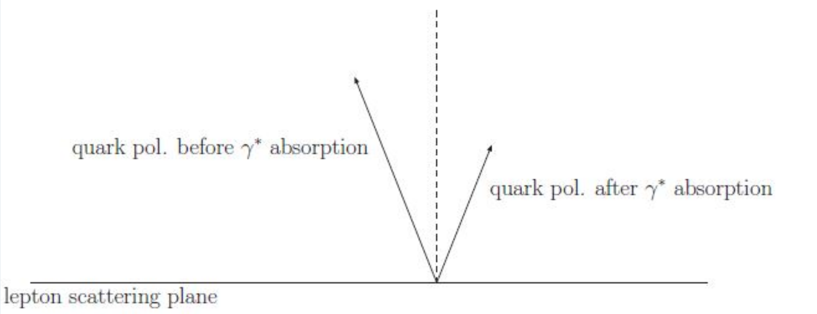
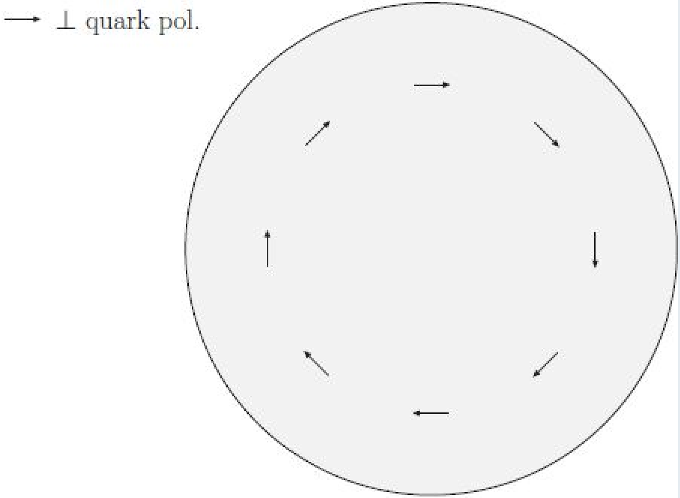


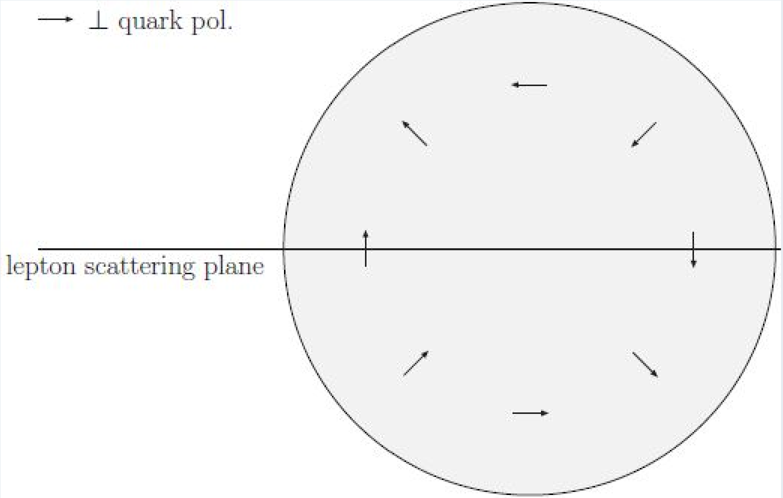
when $\perp$ pol. quark absorbs γ^*, $\perp$ polarization

- gets reduced in size
- tilted symmetrically w.r.t. normal of lepton scattering plane

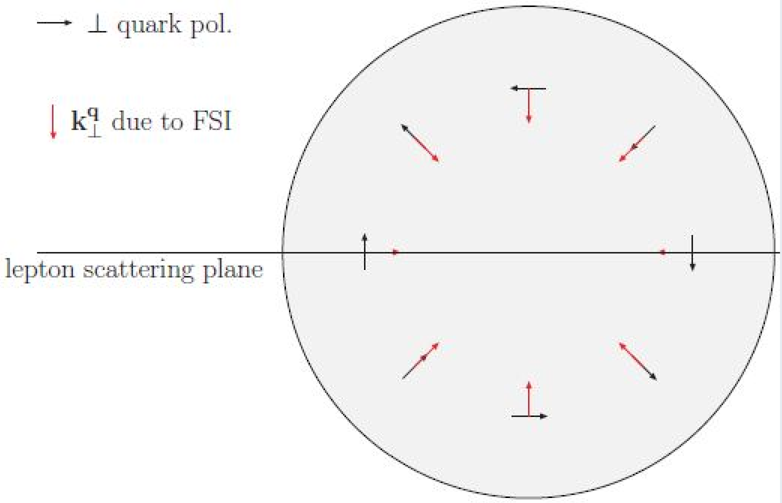
Primordial Quark Transversity Distribution



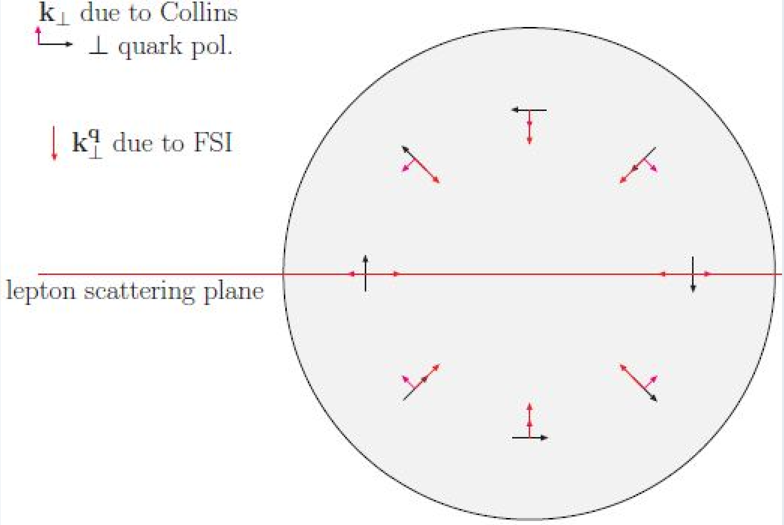
Quark Transversity Distribution after γ^* Absorption



⊥ momentum (of q) due to FSI

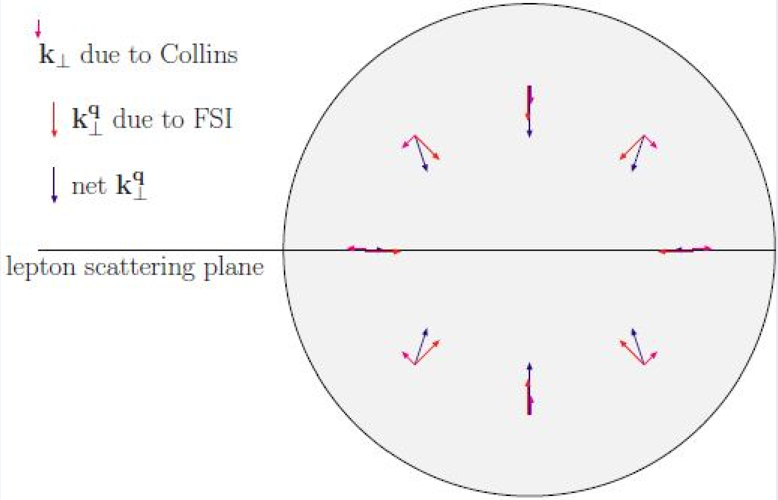


additional ⊥ momentum (of π) due to Collins effect



Collins: favored π momentum preferentially to left (quark spin up)

net $k_\perp^\pi$ (FSI + Collins)



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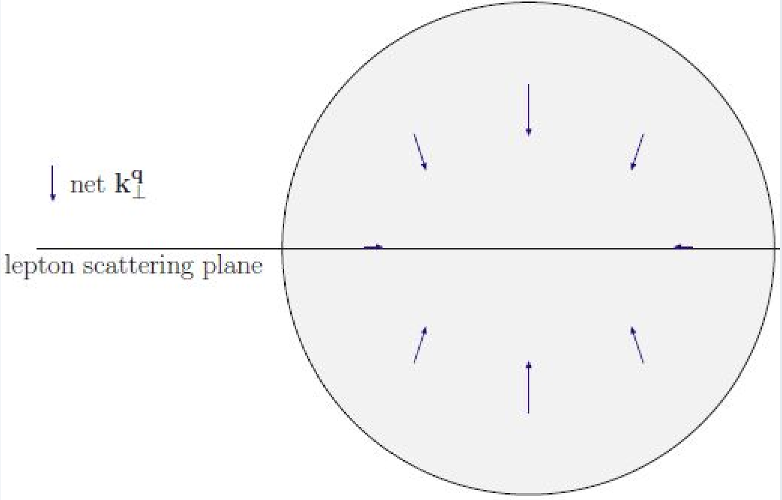

$\cos 2\pi$ modulation of $k_\perp^\pi$

higher twist in polarized DIS

- $\sigma_{LL} \propto g_1 - \frac{2Mx}{\nu} g_2$
- $g_1 = \frac{1}{2}\sum_q e_q^2 g_1^q$ with $g_1^q = q^\uparrow(x) + \bar{q}^\uparrow(x) - q^\downarrow(x) - \bar{q}^\downarrow(x)$
- g_2 involves quark-gluon correlations

$\hookrightarrow$ no parton interpret. as difference between number densities for g_2

- for $\perp$ pol. target, g_1 & g_2 contribute equally

$$\sigma_{LT} \propto g_T \equiv g_1 + g_2$$

$\hookrightarrow$ 'clean' separation between g_2 and $\frac{1}{Q^2}$ corrections to g_1

What can we learn from g_2?

- $g_2 = g_2^{WW} + \bar{g}_2$ with $g_2^{WW}(x) \equiv -g_1(x) + \int_x^1 \frac{dy}{y} g_1(y)$

$$d_2 \equiv 3\int dx\, x^2 \bar{g}_2(x) = \frac{1}{2MP^{+2}S^x}\left\langle P,S\left|\bar{q}(0)gG^{+y}(0)\gamma^+ q(0)\right|P,S\right\rangle$$

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color Lorentz force

$$\sqrt{2}G^{+y} = G^{0y} + G^{zy} = -E^y + B^x = -\left(\vec{E} + \vec{v}\times\vec{B}\right)^y \text{ for } \vec{v} = (0,0,-1)$$

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$\hookrightarrow$ $d_2 \leftrightarrow$ average **color Lorentz force** acting on quark moving with $v = c$ in $-\hat{z}$ direction in the instant after being struck by γ^*

$$\langle F^y\rangle = -2M^2 d_2 = -\frac{M}{P^{+2}S^x}\left\langle P,S\left|\bar{q}(0)gG^{+y}(0)\gamma^+q(0)\right|P,S\right\rangle$$

cf. Qiu-Sterman matrix element $\langle k_\perp^y\rangle \equiv \int_0^1 dx \int d^2k_\perp\, k_\perp^2 f_{1T}^\perp(x,k_\perp^2)$

$$\langle k_\perp^y\rangle = -\frac{1}{2p^+}\left\langle P,S\left|\bar{q}(0)\int_0^\infty dx^- gG^{+y}(x^-)\gamma^+q(0)\right|P,S\right\rangle$$

semi-classical interpretation: average $k_\perp$ in SIDIS obtained by correlating the quark density with the transverse impulse acquired from (color) Lorentz force acting on struck quark along its trajectory to (light-cone) infinity

matrix element defining d_2 $\leftrightarrow$ 1^{st} integration point in QS-integral

$$d_2 \equiv 3\int dx\, x^2 \bar{g}_2(x) = \frac{1}{2MP^{+2}S^x}\left\langle P,S\left|\bar{q}(0)gG^{+y}(0)\gamma^+q(0)\right|P,S\right\rangle$$

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sign of $d_2 \leftrightarrow\perp$ imaging

- $\kappa_q/p \longrightarrow$ sign of deformation

↪ direction of average force

↪ $d_2^u > 0$, $d_2^d < 0$

- *cf.* $f_{1T}^{\perp u} < 0$, $f_{1T}^{\perp u} < 0$

lattice (Göckeler et al., 2005)

$d_2^u \approx 0.010$, $d_2^d \approx -0.0056$

magnitude of d_2

- $\langle F^y\rangle = -2M^2 d_2 = -10\frac{GeV}{fm}d_2$
- expect partial cancellation of forces in SSA

↪ $|\langle F^y\rangle| \ll \sigma \approx 1\frac{GeV}{fm}$

↪ $d_2 = \mathcal{O}(0.01)$

color Lorentz force

$e_2 \leftrightarrow$ average **color Lorentz force** (in $\hat{y}$-direction) acting on quark (with transversity $\hat{x}$) moving with $v = c$ in $-\hat{z}$ direction in the instant after being struck by γ^*

$$\langle F^y \rangle = M^2 e_2 \equiv M^2 \int_0^1 dx \bar{e}_2(x) = \frac{M}{4P^{+2}} \sum_{i=1,2} \left\langle P \left| \bar{q}(0) g G^{+i}(0) \sigma^{+i} q(0) \right| P \right\rangle$$

chirally even

- GPD $E_q \Rightarrow \mathbf{b}_\perp$ deformation of unpol. q distr. in $\perp$ pol. target

$\hookrightarrow$ $f_{1T}^\perp$

$\hookrightarrow$ $d_2 \equiv \int dx x^2 \bar{g}_2$ force

chirally odd

- GPD $\bar{E}_T \Rightarrow \mathbf{b}_\perp$ deformation of quarks with transversity in unpol. target

$\hookrightarrow$ $h_1^\perp$

$\hookrightarrow$ $e_2 \equiv \int dx x^2 \bar{e}_2$ force

lattice (Göckeler et al., 2005)

$d_2^u \approx 0.010$, $d_2^d \approx -0.0056$

please: up to date lattice calcs.

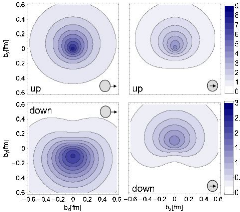
lattice

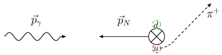
B.Musch ...

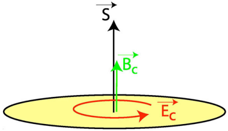
- Deeply Virtual Compton Scattering $\longrightarrow$ GPDs

$\hookrightarrow$ impact parameter dependent PDFs $q(x, \mathbf{b}_\perp)$

- $E^q(x, 0, -\boldsymbol{\Delta}_\perp^2) \leftrightarrow \kappa_{q/p}$ (contribution from quark flavor q to anomalous magnetic moment)
- $E^q(x, 0, -\boldsymbol{\Delta}_\perp^2) \longrightarrow \perp$ deformation of PDFs for $\perp$ polarized target
- $\perp$ deformation $\leftrightarrow$ (sign of) SSA (Sivers; Boer-Mulders)
- parton interpretation for Ji-relation
- higher-twist $(\int dx\, x^2 \bar{g}_2(x), \int dx\, x^2 \bar{e}(x)) \leftrightarrow \perp$ force in DIS
- $\perp$ deformation $\leftrightarrow$ (sign of) quark-gluon correlations $(\int dx\, x^2 \bar{g}_2(x), \int dx\, x^2 \bar{e}(x)\ )$







combine complementary information from deeply-virtual Compton scattering, semi-inclusive DIS & Drell-Yan to study orbital angular momentum and map the 3-d structure of hadrons