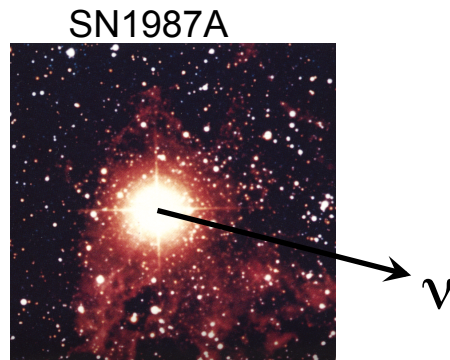
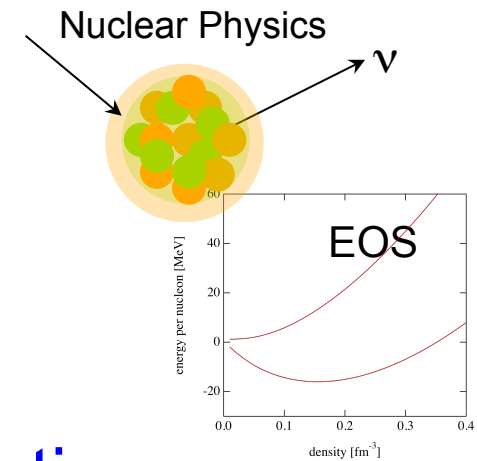


Core-collapse Supernovae: Nuclear matter and EOS



K. Sumiyoshi (Numazu)



- Status of supernova simulations
- Role of EOS: when and how?

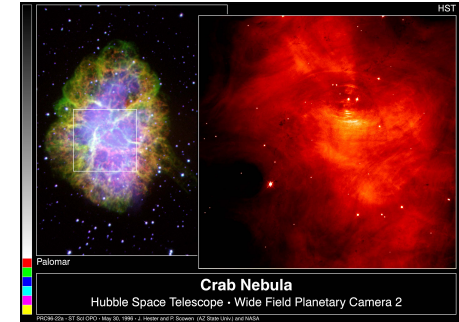
新学術「計算科学素核宇宙」そして「中性子星核物質」へ

Core-collapse supernovae are fascinating

– Birth of neutron stars and black holes

- Pulsars (1.4 solar mass in ~10km)
- Extremely dense: degenerate Fermions

Crab Nebula (SN1054)



– Bright displays and supernova neutrinos

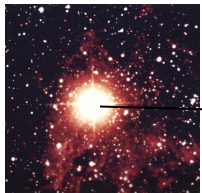
- Nobel prize in Physics in 2002
- Probe of hot & dense matter

Prof. Koshiba



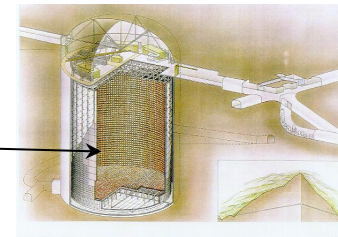
<http://nobelprize.org/>

SN1987A



supernova ν

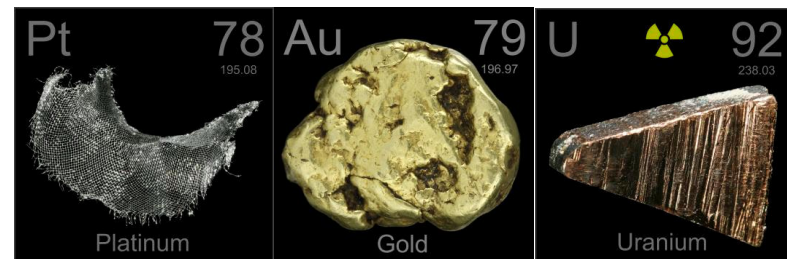
Kamiokande



<http://www-sk.icrr.u-tokyo.ac.jp/>

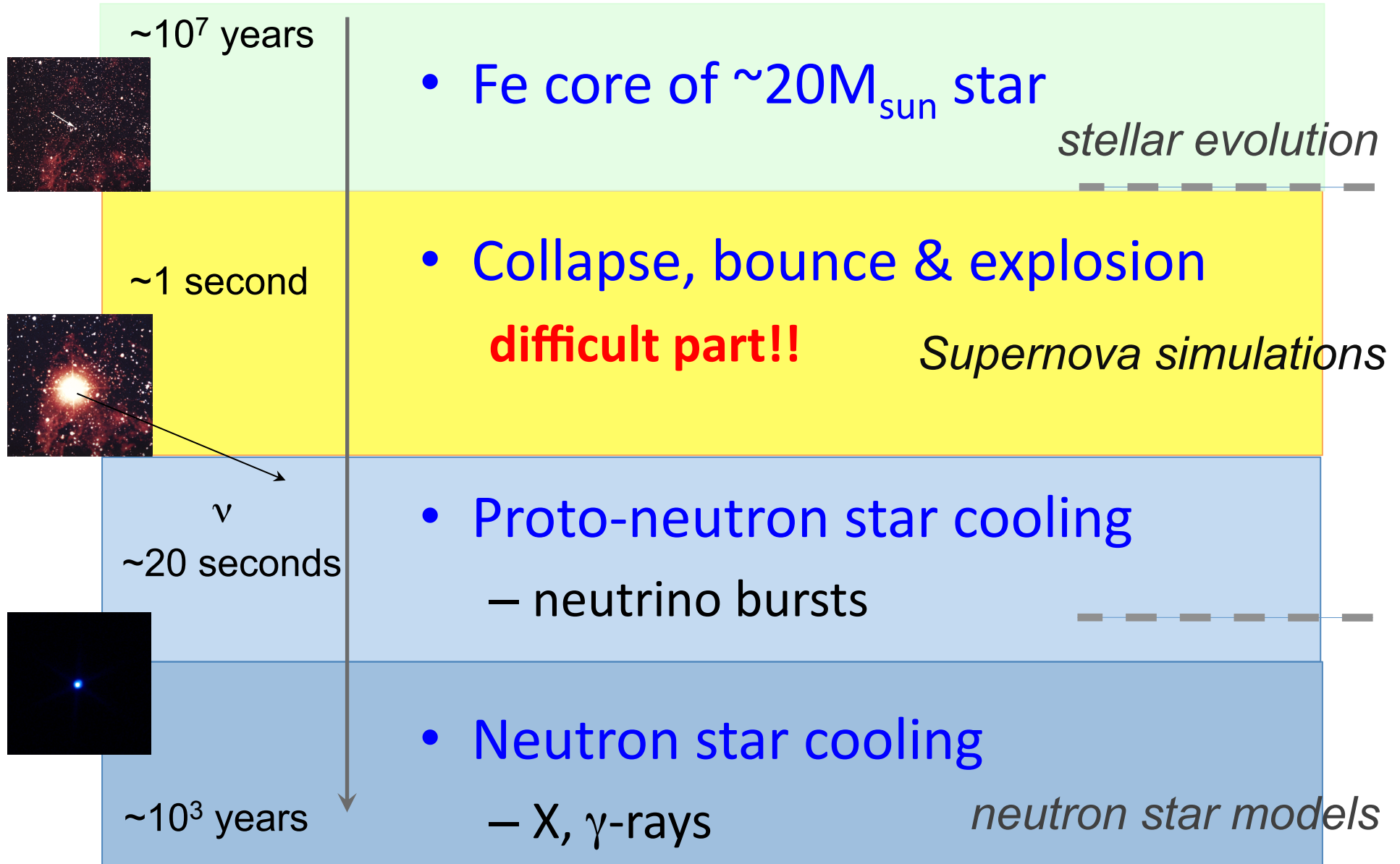
– Origin of heavy elements

- Explosive nucleosynthesis
- Half of elements beyond Fe



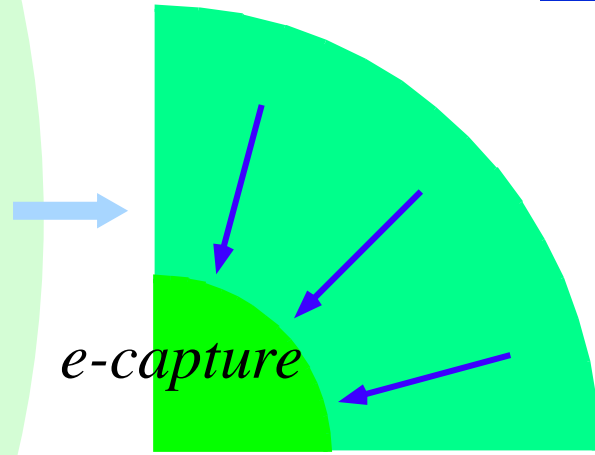
<http://periodictable.com/> 2

time **Massive stars to neutron stars**



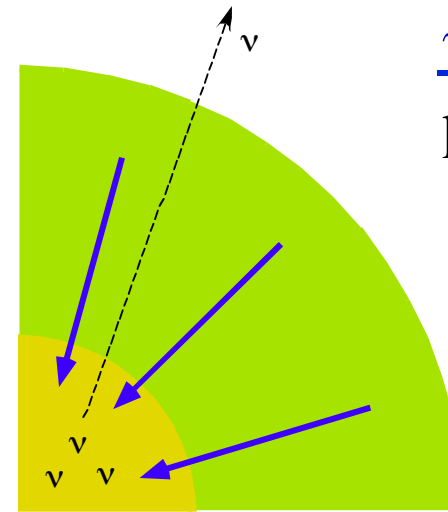
Gravitational collapse, bounce and explosion

$\sim 20M_{sun}$ star
Fe core



Collapse

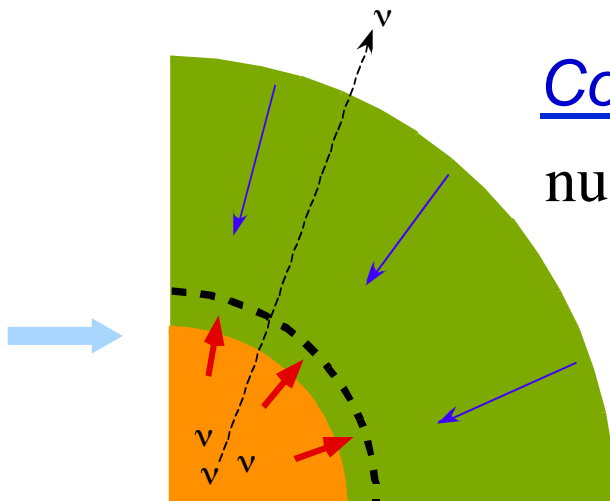
1000 km



v-trapping
high density

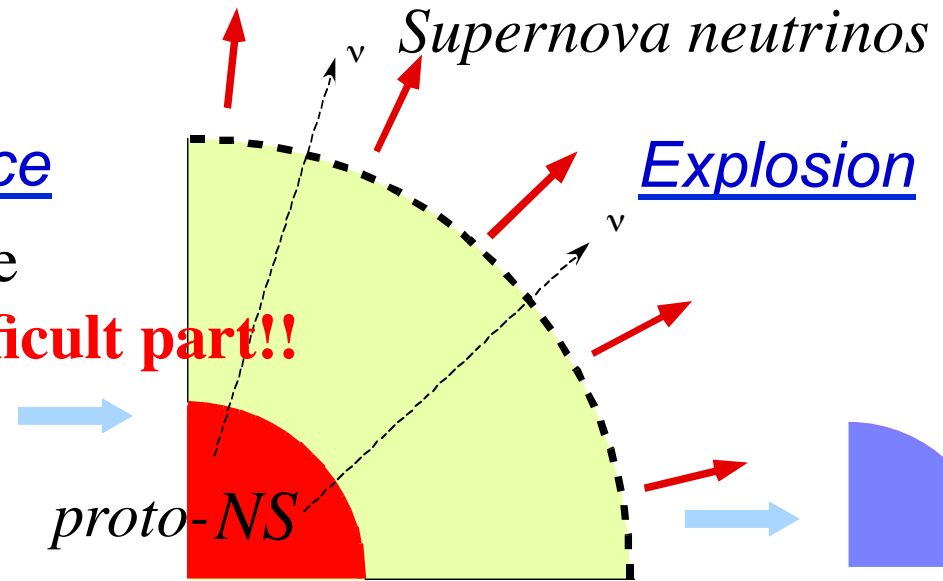
Core Bounce

nuclear force



Shockwave

difficult part!!



Explosion

proto-NS

10 km

Neutron star

Exotic conditions: challenges in nuclear physics

- **Equation of state (EOS) in supernova core**

- Dense more than nuclei: $\rho > \rho_0 = 3 \times 10^{14} \text{g/cm}^3$
- Neutron-rich: $Y_p < Z/A = 0.46$ for ^{56}Fe
- Very Hot: $T > 10^{11} \text{K}$ ($\sim 10 \text{MeV}$)

- **Neutrino reactions in hot-dense matter**

- Energy, angle dependent
 - All targets (n, p, nuclei, leptons)
 - Emission, absorption, scattering & pairs
- ex. $e^- + p \leftrightarrow \nu_e + n$
 $\nu_i + \text{Fe} \leftrightarrow \nu_i + \text{Fe}$
 $e^- + e^+ \leftrightarrow \nu_i + \bar{\nu}_i$

- **Necessary inputs for numerical simulations**

neutrino transfer (Boltzmann eqn.) + hydrodynamics

1% effects: energy budget for explosion

- Iron core to neutron star ($M_{\text{core}} \sim 1.4 M_{\text{solar}}$)
 - $R_{\text{Fe}} \sim 10^3 \text{ km} \rightarrow R_{\text{NS}} \sim 10 \text{ km}$
- Gravitational energy released

$$\Delta E_{\text{Grav}} = - \left(\frac{GM^2}{R_{\text{Fe}}} - \frac{GM^2}{R_{\text{NS}}} \right) \sim 10^{53} \text{ erg}$$

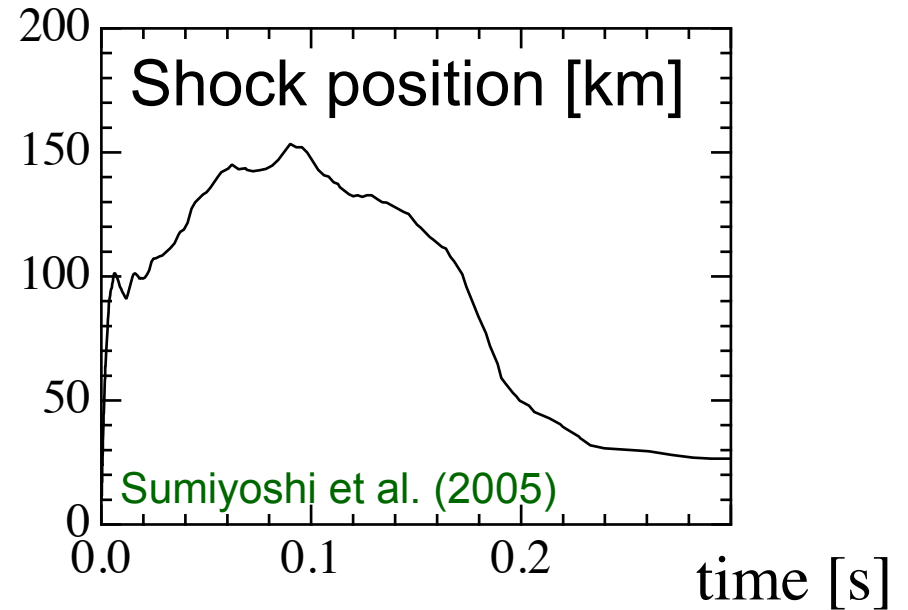
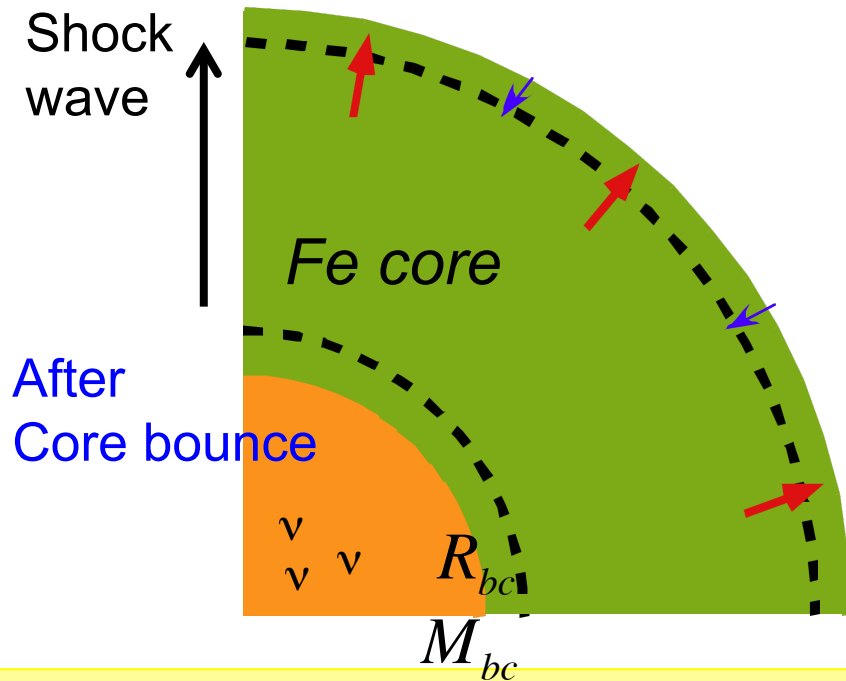
- Explosion energy: $E_{\text{exp}} \sim 10^{51} \text{ erg}$

- Neutrino carries away: $E_{\nu} \sim 10^{53} \text{ erg}$

- Only $\sim 1\%$ is used for the explosion
- Neutrino-matter interaction is essential

Initial shockwave stalls on the way

Energy is used during the propagation



Initial shock energy

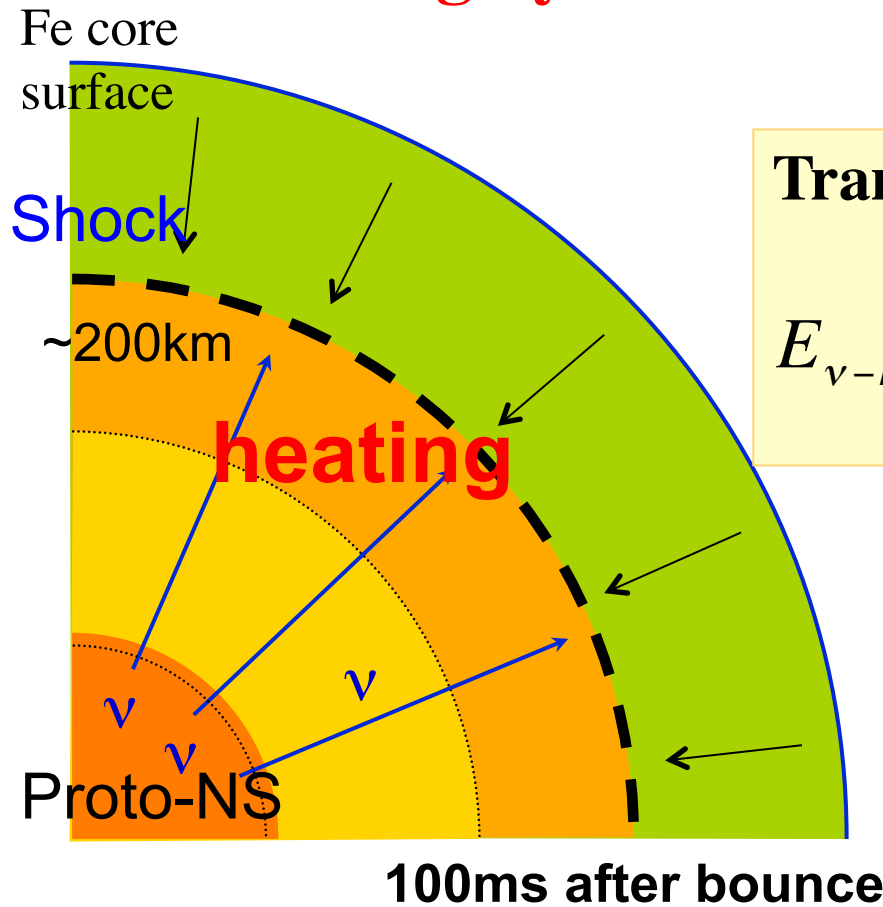
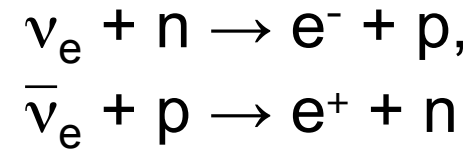
$$E_{shock} \sim \frac{GM_{bc}^2}{R_{bc}} = \text{several} \times 10^{51} \text{ erg}$$

Energy loss due to Fe dissociation

$$E_{loss} \sim -1.6 \times 10^{51} \left(\frac{M_{outer}}{0.1 M_{solar}} \right) \text{ erg}$$

Neutrino heating mechanism for revival of shock

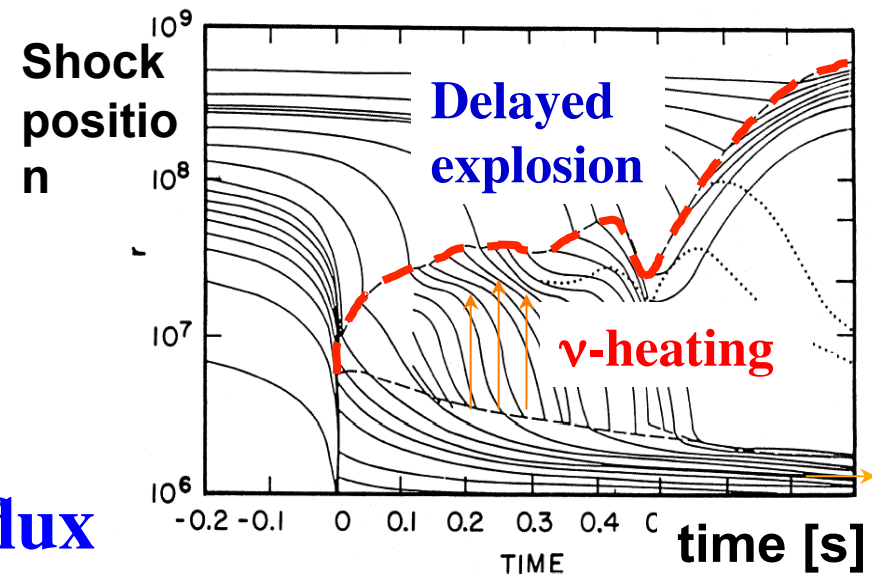
Heating by neutrino absorption



Transfer of energy from ν

$$E_{\nu\text{-heat}} \sim 2.2 \times 10^{51} \left(\frac{\Delta M}{0.1 M_{\text{solar}}} \right) \left(\frac{\Delta t}{0.1 \text{s}} \right) \text{erg}$$

Depends on neutrino energy/flux

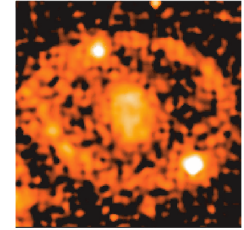


Multi-dimensions: new findings

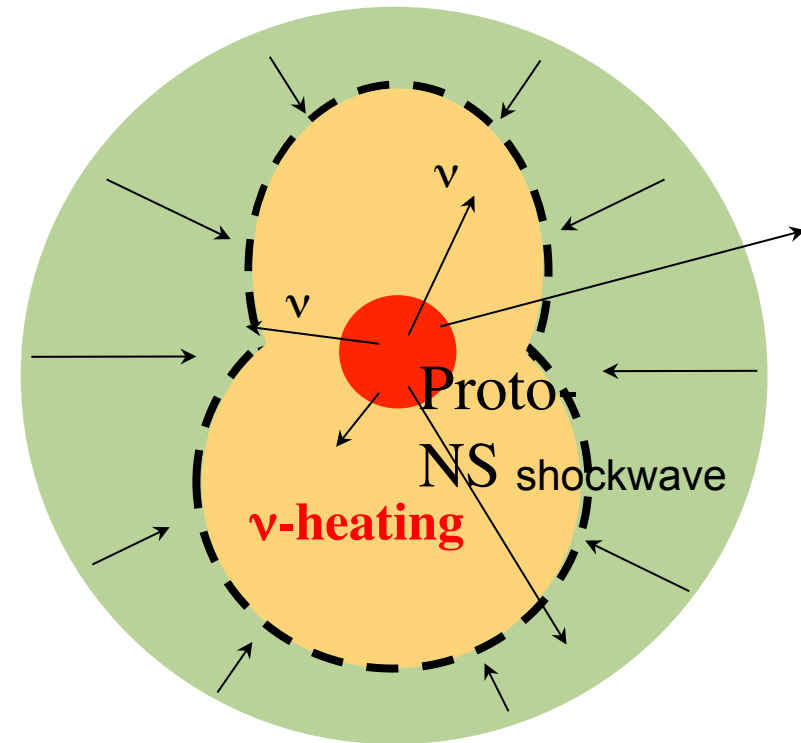
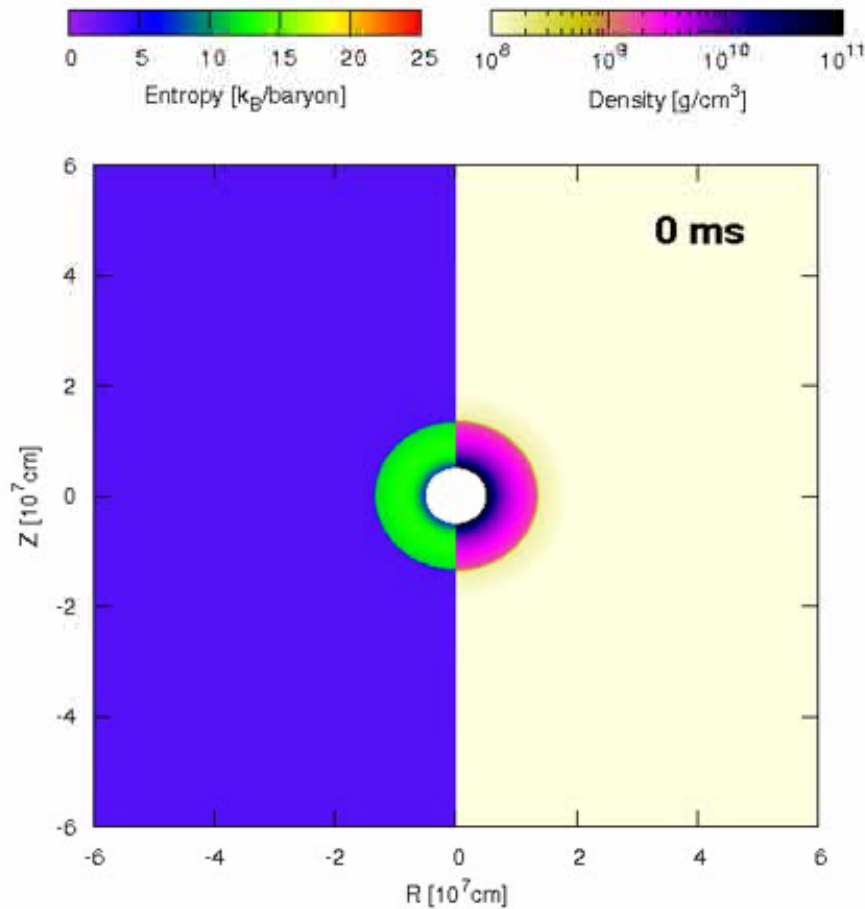
- Convection, SASI, rotation, magnetic etc - Observations

ν -heating and/or hydro instability

SN1987A



Wang (2002)



To obtain enough ν -heating

Challenges toward 3D simulations

Neutrino-transfer & hydrodynamics

- 1D: No explosion found
 - first principle calculations
- 2D: Cases of explosions
 - State-of-the-art, but approximate neutrinos

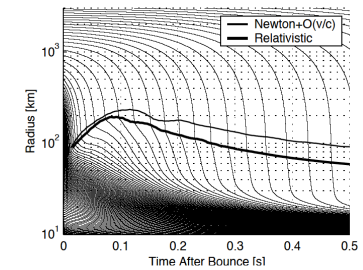
Several mechanisms, discussions not settled

- 3D: Explore new instabilities
 - Major challenges of supernova simulations

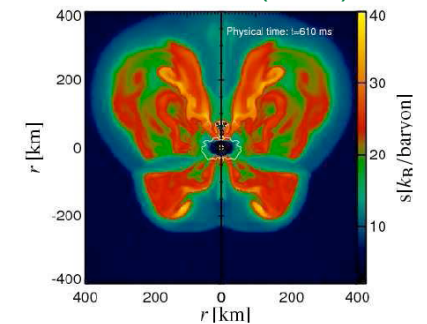
New code to solve 6D Boltzmann eqn.

(Sumiyoshi-Yamada, 2012 ApJS)

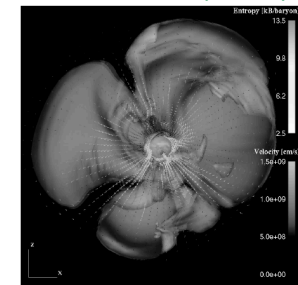
Liebendoerfer (2001)



Marek (2009)



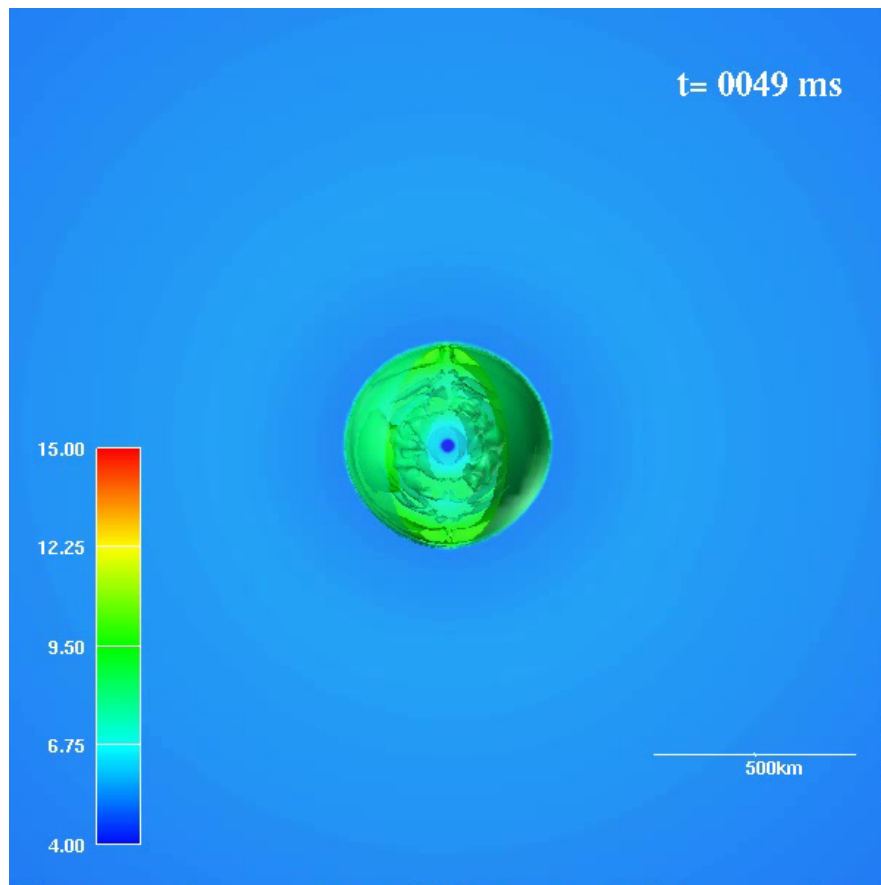
Iwakami (2008)



3D simulation of supernovae from a massive star

Explosions obtained, but still not conclusive

Need high resolutions, accurate ν -transfer



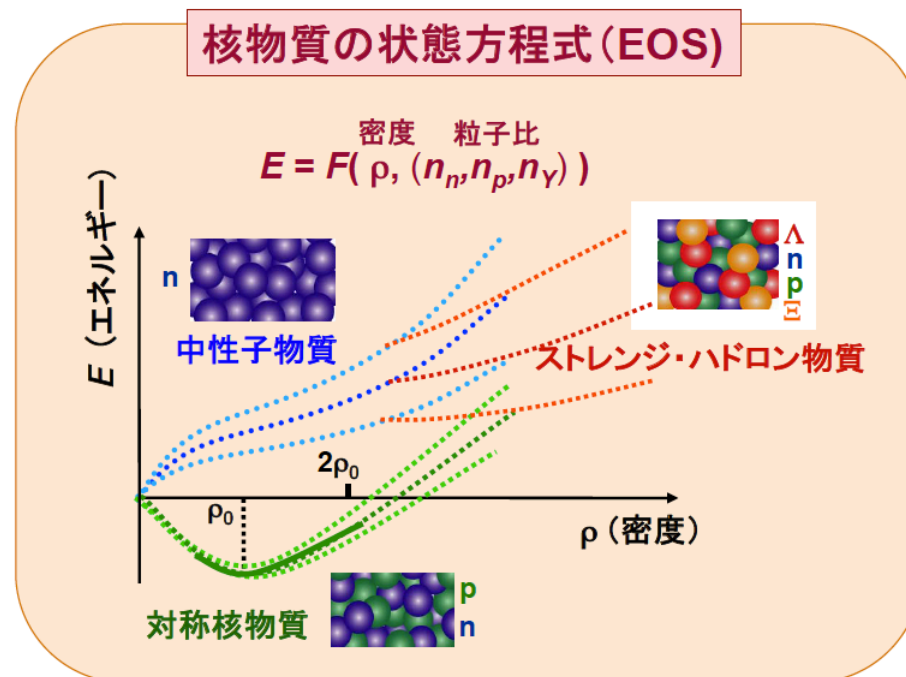
- Simulations running at K-computer, 10Peta-flops



@ Kobe, Japan

Naive questions on EOS in supernovae

- Different from NS?
- Which part of ρ , Y_p ?
- Soft EOS is better?
- Hyperons/quarks affect?



From Slides by H. Tamura @Kyoto

Shen equation of state for supernovae

H. Shen, Toki, Oyamatsu & Sumiyoshi NPA, PTP(1998), arXiv:1105.1666 (2011)

- Relativistic mean field theory+ local-density approx.
 - Based on relativistic Brueckner Hartree-Fock (RBHF) theory
 - Checked by exp. data of n-rich unstable nuclei
 - Nuclear structure: mass, charge radius, neutron skin,...

Covers wide range of

- Density: $10^{5.1} \sim 10^{16} \text{ g/cm}^3$
- Proton fraction: $0 \sim 0.65$
- Temperature: $0 \sim 400 \text{ MeV}$
- Data table $\sim 140 \text{ MB}$ (110 x 66 x 92 points)
 - Quantities: $\varepsilon, p, S, \mu_i, X_i, m^*$



Uniform and non-uniform matter

Shen-EOS

cf. Lattimer-Swesty EOS

- Extension of compressible liquid model

LS-EOS

Extensions of Shen EOS tables

- Appearance of hyperons & quarks

Ishizuka et al. JPG (2006), Nakazato et al. PRD (2008) Shen et al. ApJS (2012)

EOS table	Framework	Nucleons	Hyperons	Quarks	Max. NS
Shen EOS 1998, NPA	RMF	n, p, α , nuclei	-	-	$2.2M_{\text{sun}}$
Hyperon EOS 2008, JPG	RMF in SU(3)	n, p, α , nuclei	Λ, Σ, Ξ	-	$1.6M_{\text{sun}}$
Quark EOS 2008, PRD	RMF + MIT bag model	n, p, α , nuclei	-	u, d, s	$1.8M_{\text{sun}}$

- Mixture of nuclei in NSE

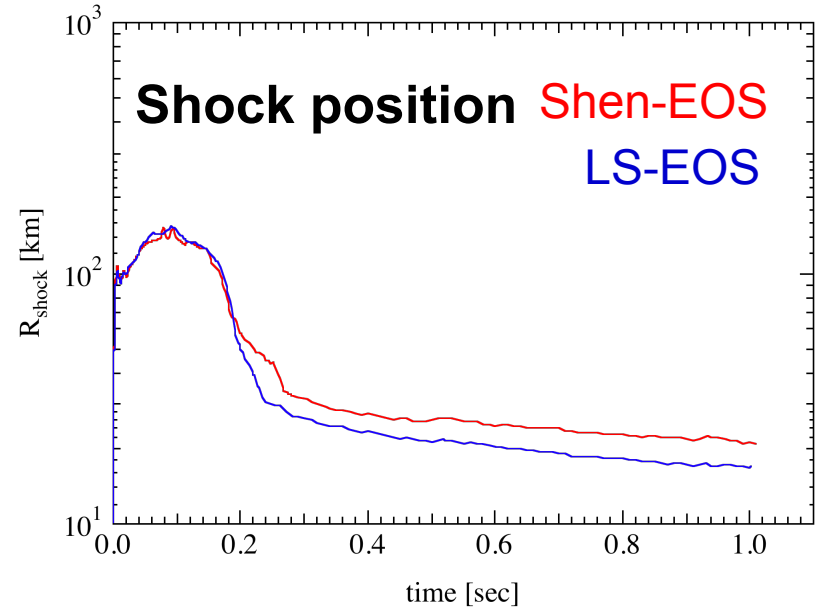
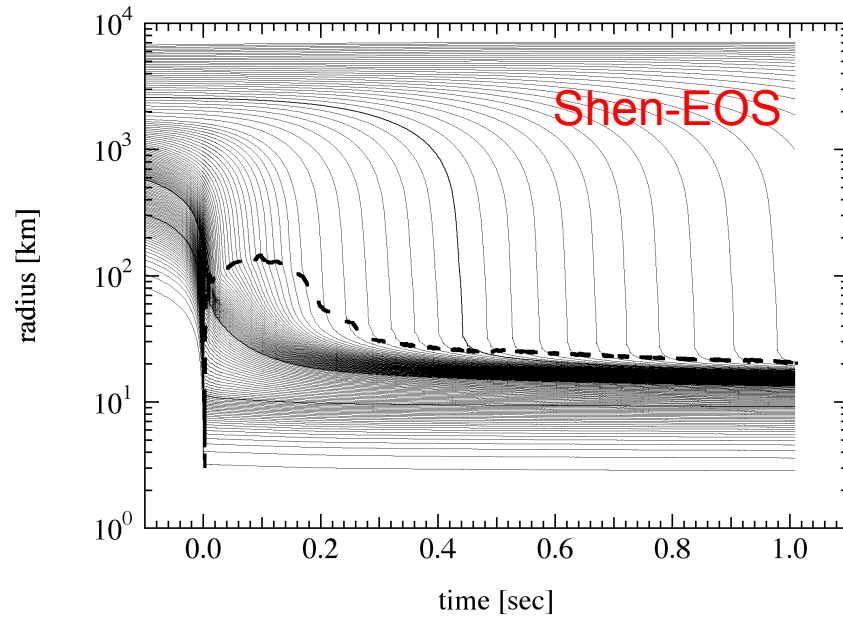
Furusawa et al. ApJ (2011)

NSE EOS 2011, (ApJ)	RMF + NSE	n, p, α , NSE of nuclei	-	-	$2.2M_{\text{sun}}$
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- Needs exp. data on nuclear mass, hyper-nuclei

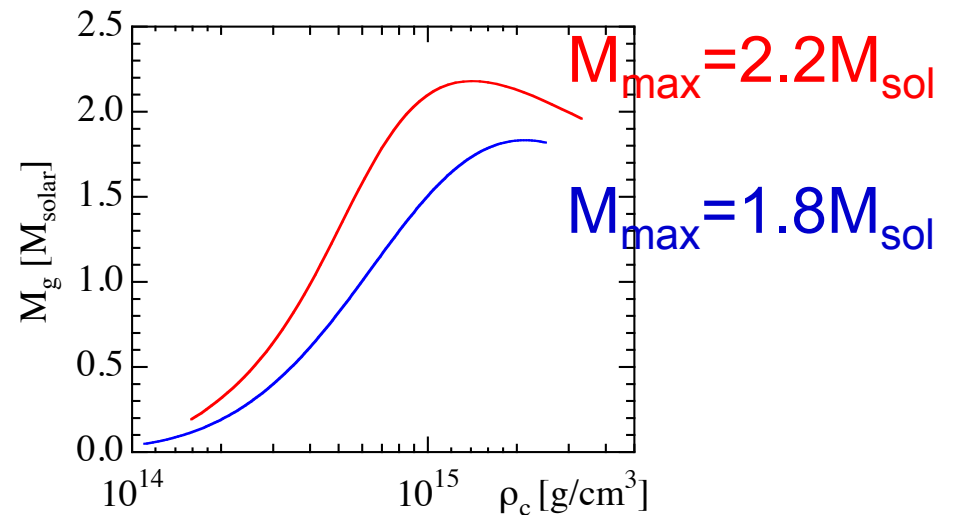
EOS dependence: no explosion in 1D

No revival of shockwave up to 1 sec. Sumiyoshi et al. ApJ (2005)



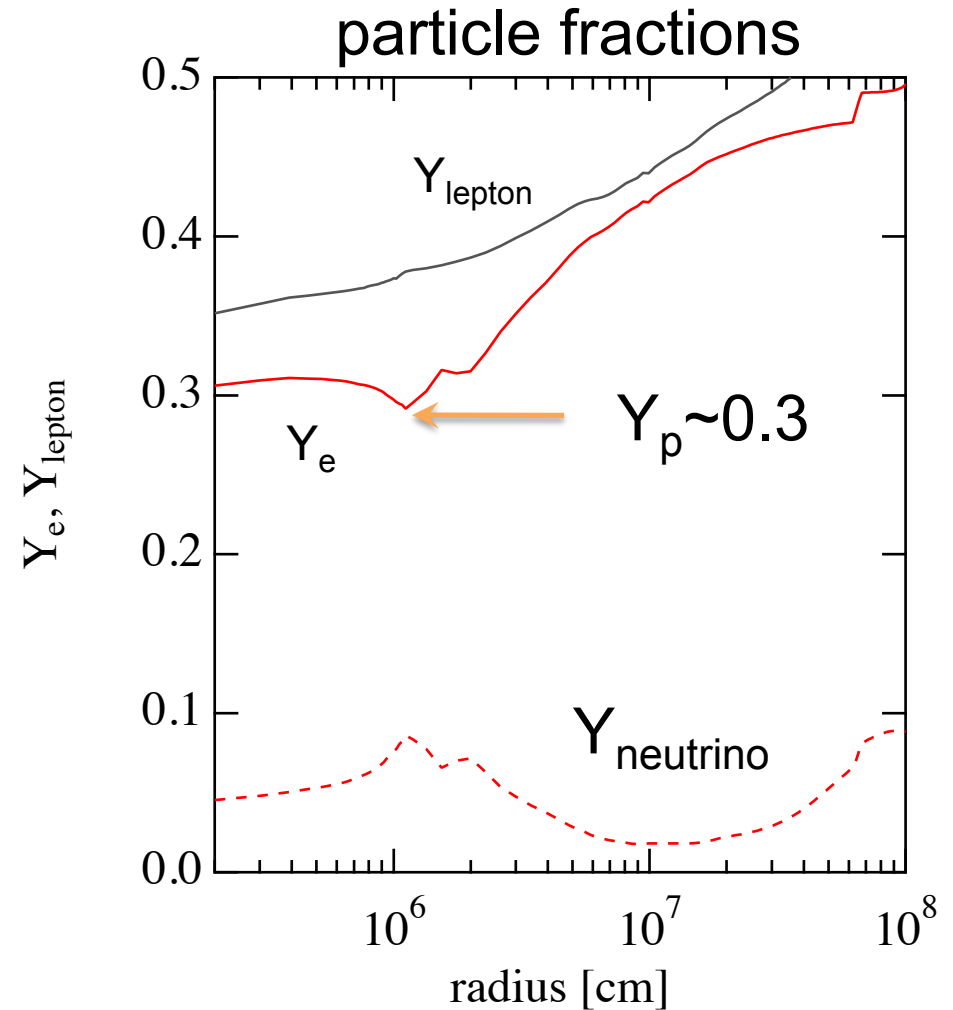
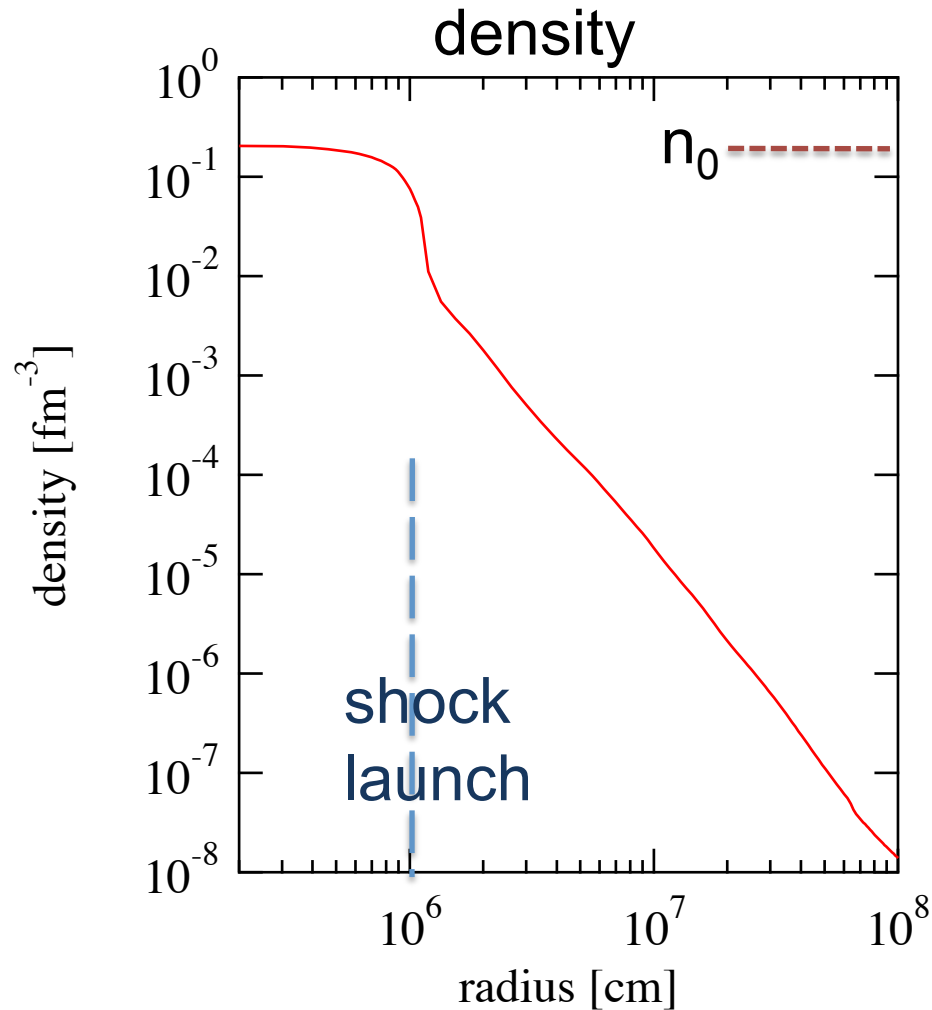
	A_{sym}	K
Shen	36.9	281
LS	29.3	180

[MeV]



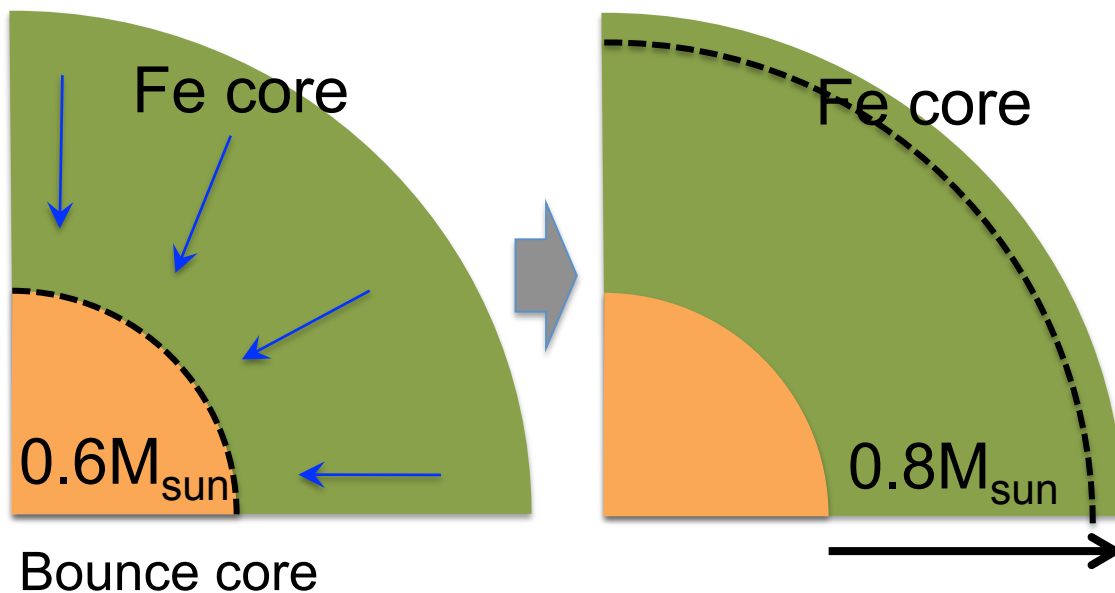
EOS condition at core bounce

- Just above n_0
- Still proton-rich with ν_e



Soft EOS is better: YES but...

- Initial energy of shock wave: $E_{\text{initial}} \sim 10^{51}$ erg
 - Size of bounce core: $R_{bc}, (M_{bc})$
 - Soft EOS \rightarrow Small R_{bc}
 - EOS around $n_0, Y_p \sim 0.3$ is important ex. L, K_{sym}
- $$E_{\text{initial}} = \frac{GM_{bc}^2}{R_{bc}}$$

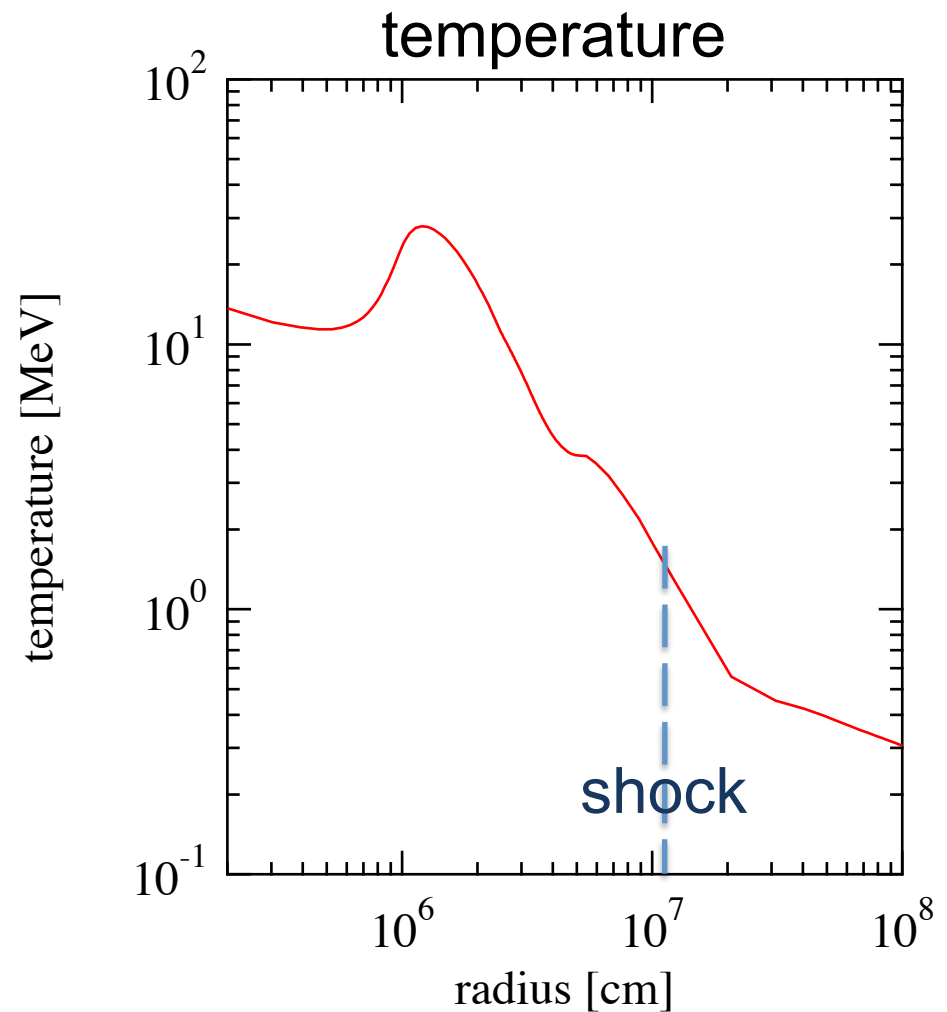
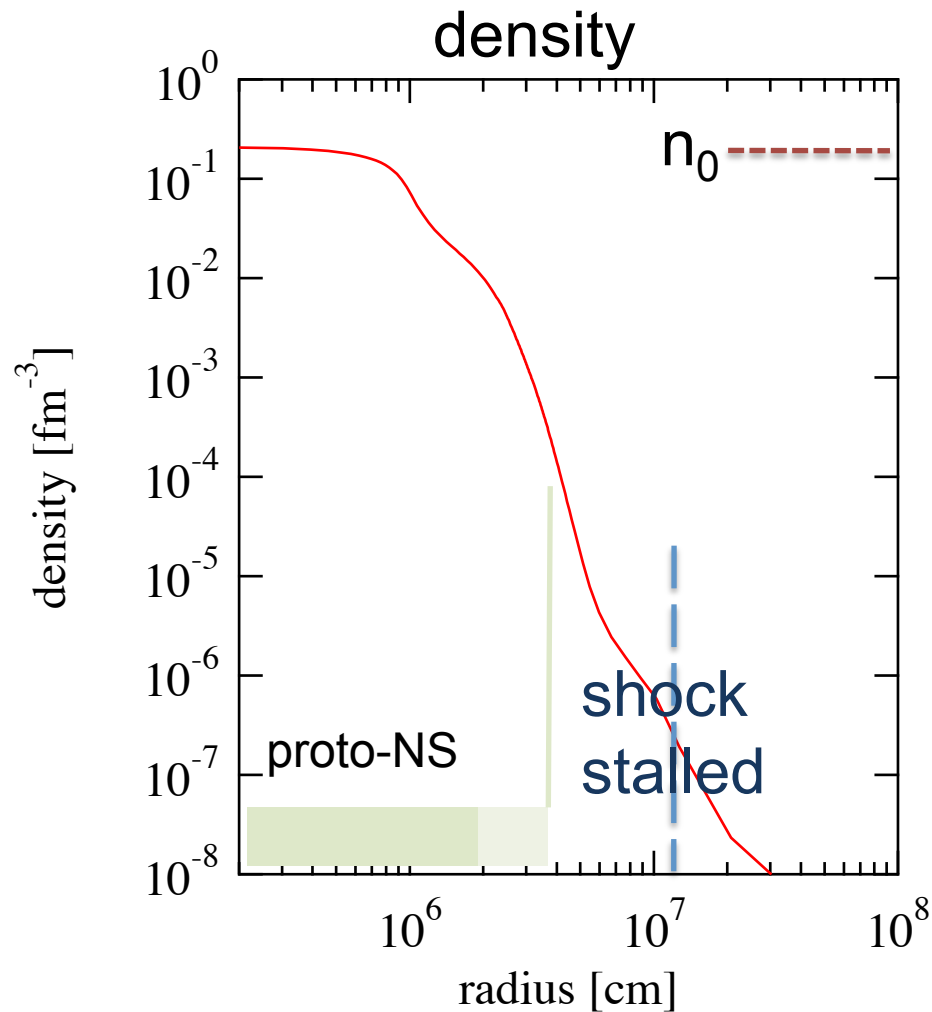


- Larger E_{initial} is better for 2D/3D
- Position of stalled shock wave
- *e-capture rates*

EOS condition at 200ms after bounce

- Proto-NS at birth

- Temperature 1~10 MeV



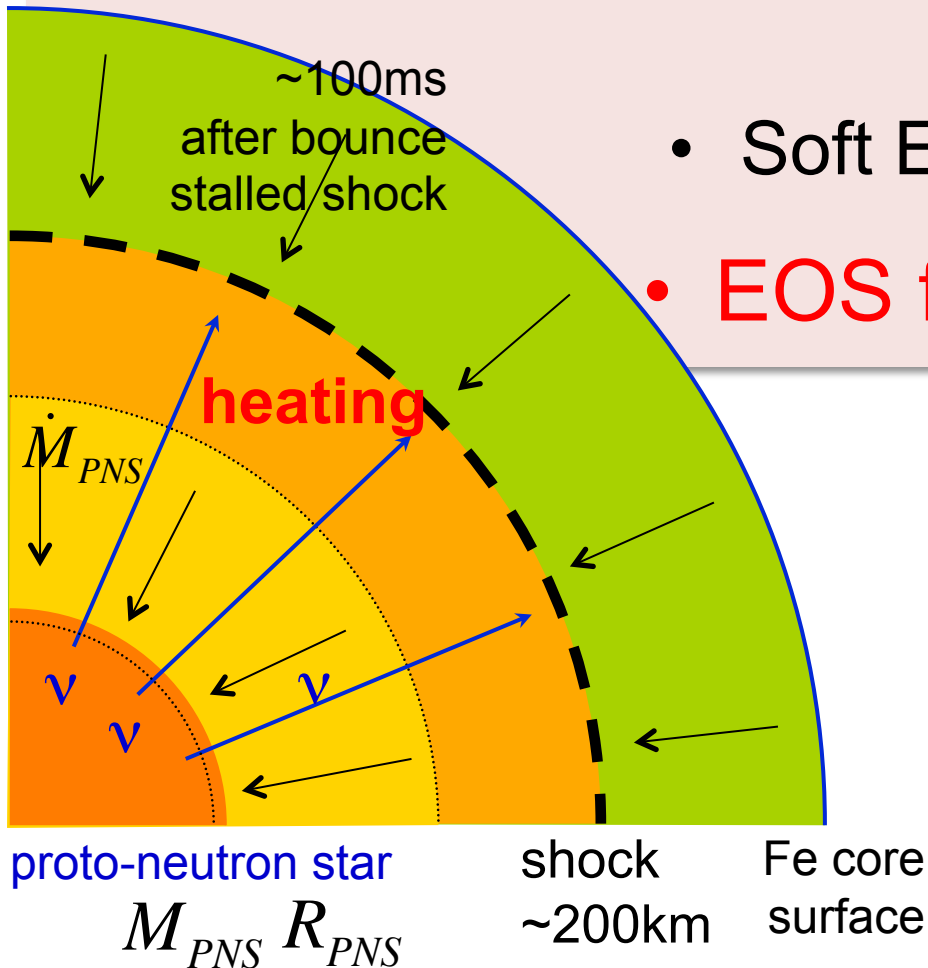
Soft EOS is better: also in 2D/3D?

- Neutrino heating:
 - absorption of neutrinos

$$E_{\text{heating}} \sim 10^{51} \text{ erg}$$

$$Q_{\text{heating}} \propto \frac{L_{\nu} E_{\nu}^2}{r^2} Y_N$$

- Soft EOS \rightarrow Large L_{ν} , E_{ν} , E_{heating}
- EOS for proto-NS is important



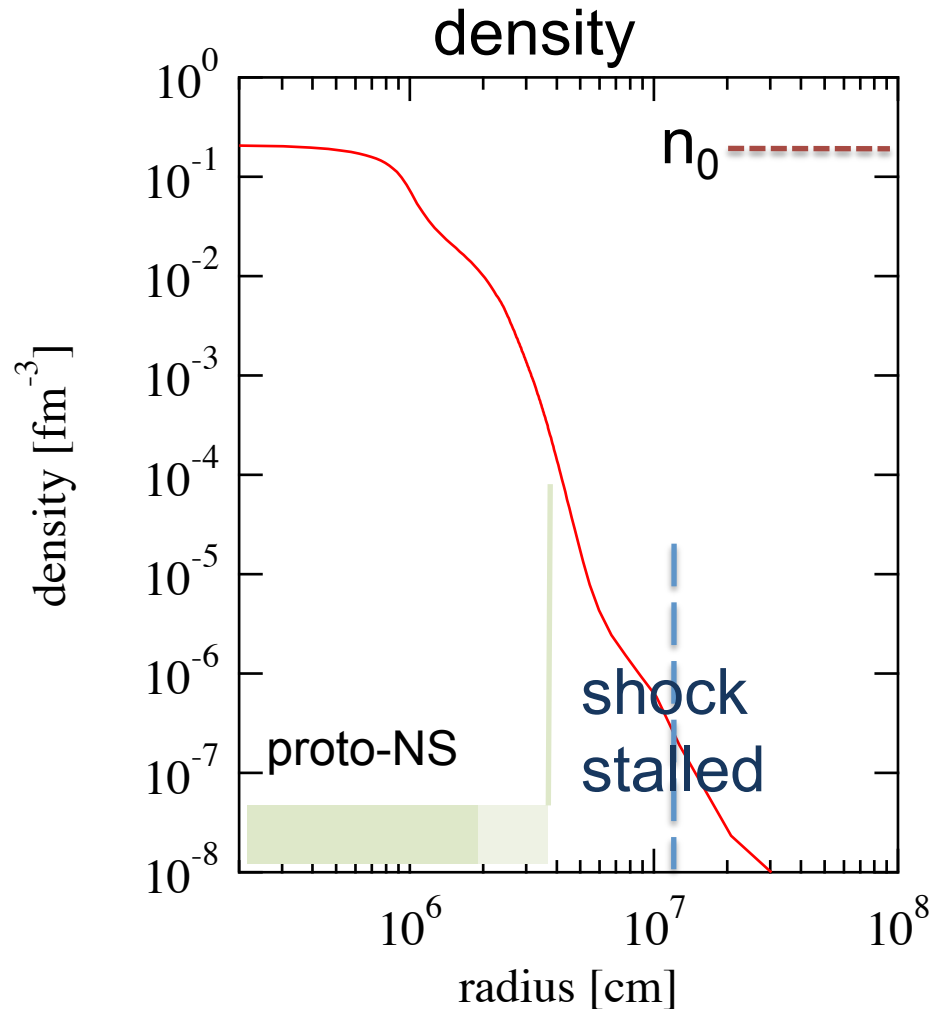
ν -energy

luminosity

$$E_{\nu} = T_{PNS} \quad L_{\nu} = \frac{GM_{PNS} \dot{M}_{PNS}}{R_{PNS}}$$

EOS condition at 200ms after bounce

- Proto-NS at birth



- Important region

- $>n_0$: proto-NS mass, radius

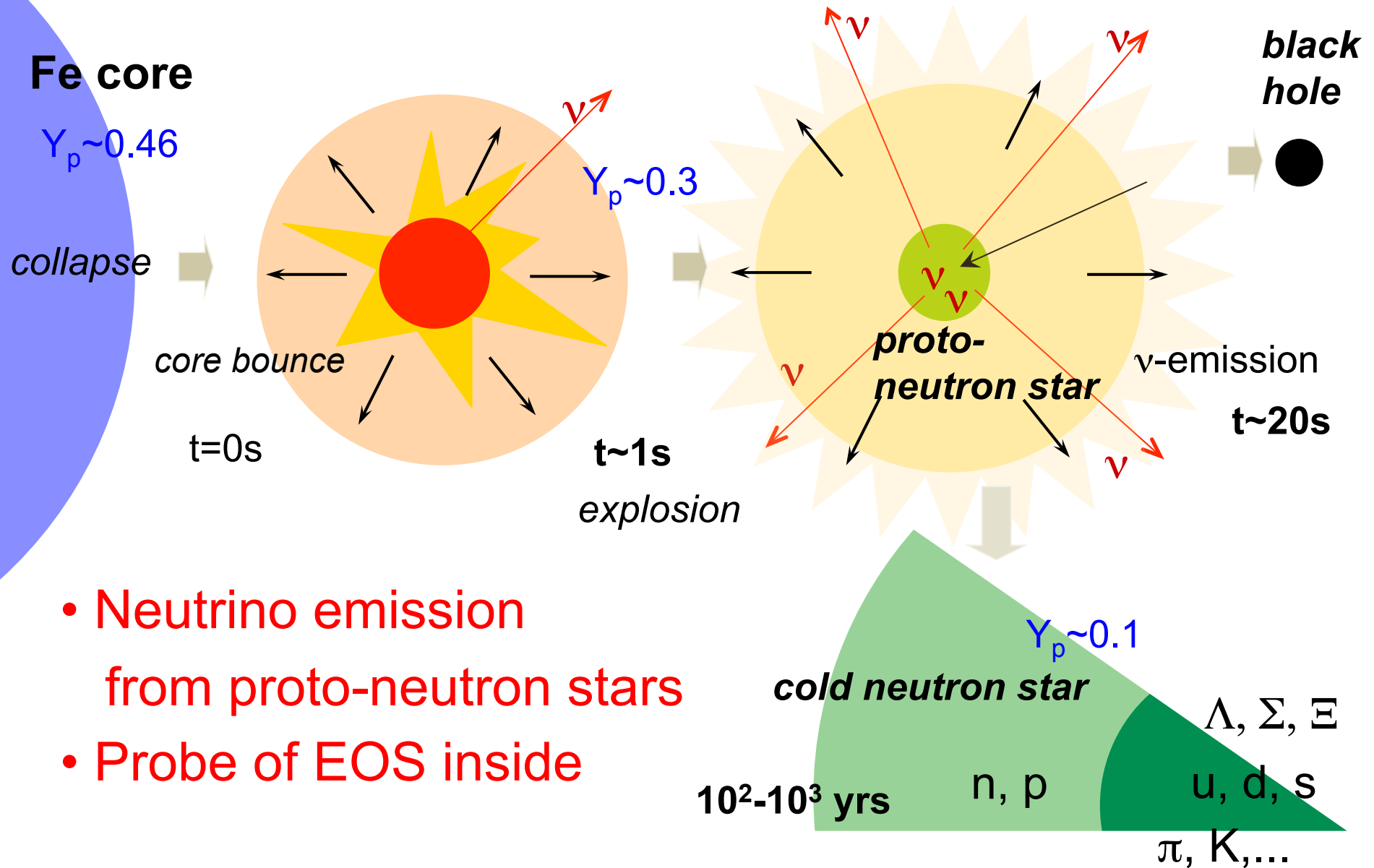
- $\sim 10^{-3}n_0$: surface

- neutrino emission, L_ν , E_ν

- $\sim 10^{-5}n_0$: heating region

- targets, composition

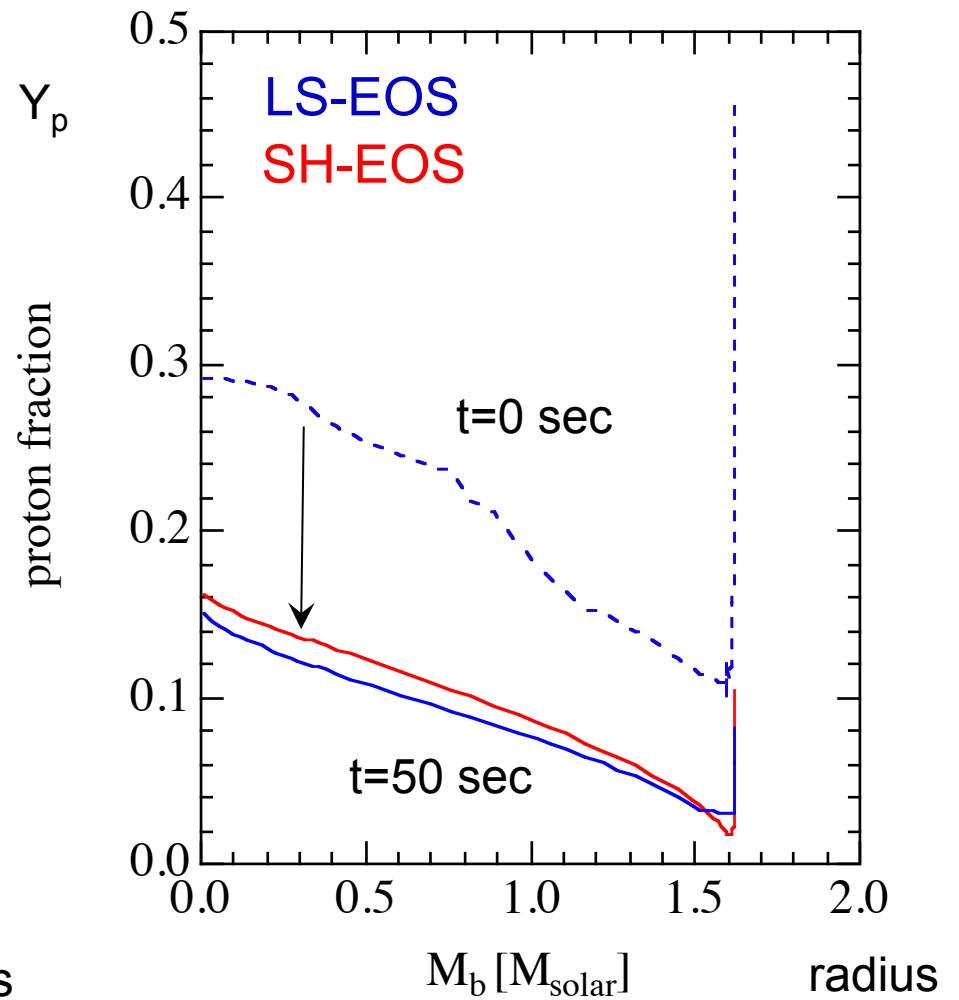
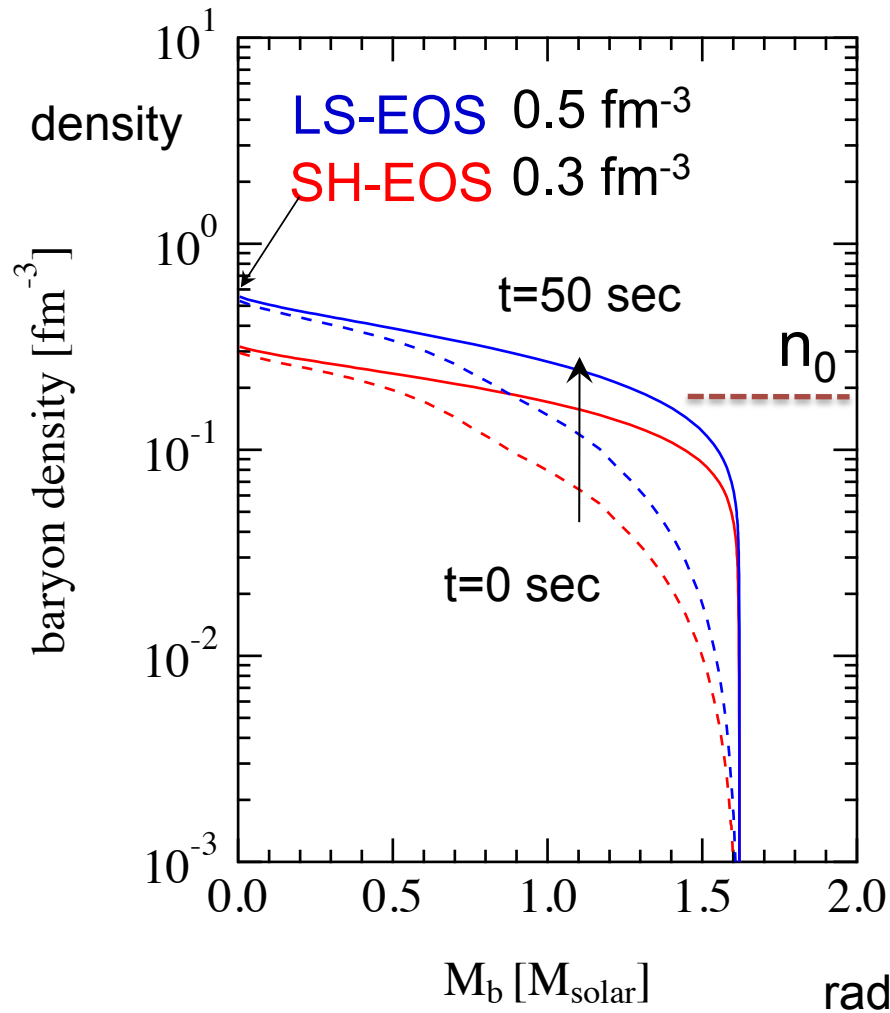
When hyperons/quarks appear?



- Neutrino emission from proto-neutron stars
- Probe of EOS inside

Proto-neutron star evolution

Neutrino emission $\Rightarrow T \downarrow$, density \uparrow , $Y_p \downarrow$,



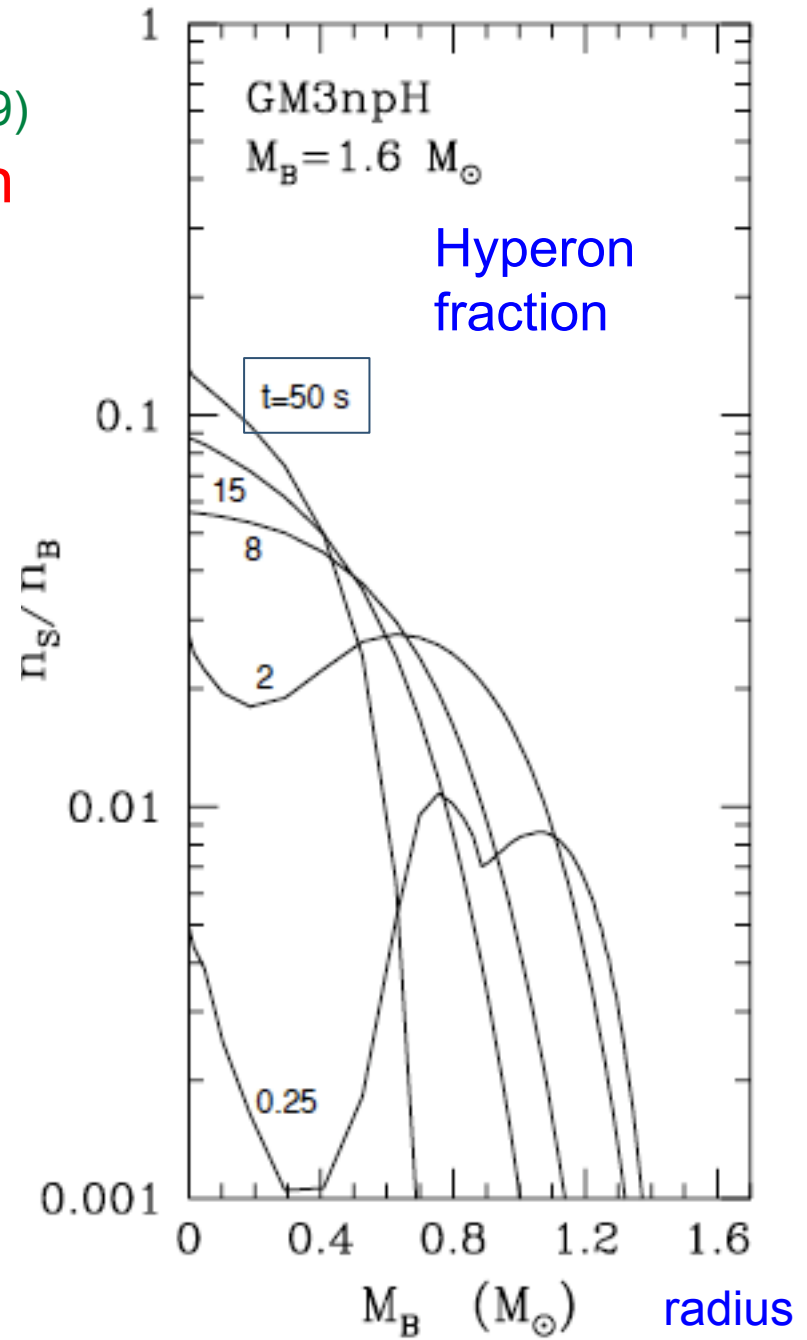
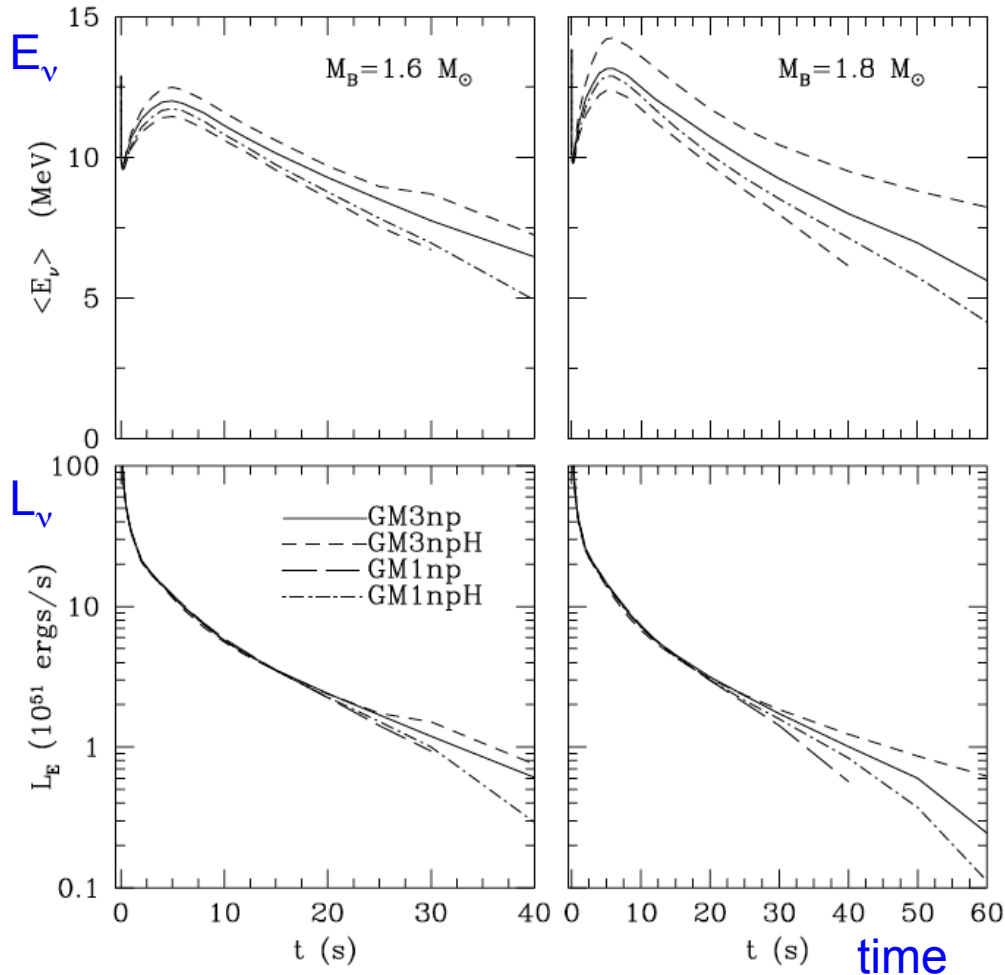
Sumiyoshi et al. (1995), H. Suzuki (2005), Nakazato (2012)

Simulation started from $t_{\text{pb}}=0.4$ sec

Hyperons in proto-NS

Pons et al. ApJ (1999)

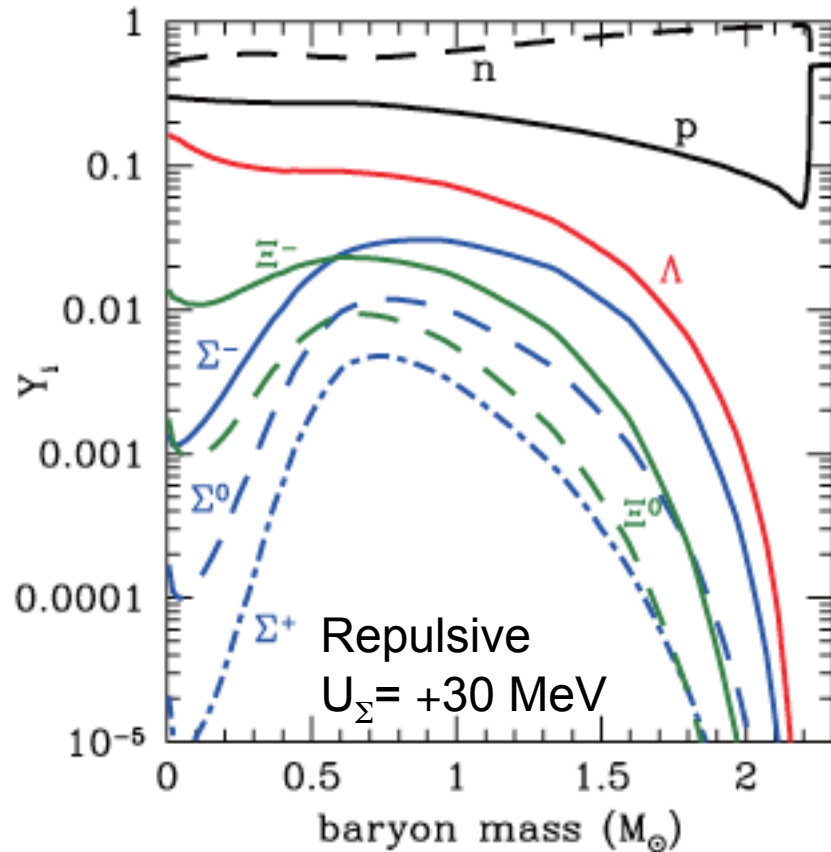
- Appear at late phase of evolution
 - Difference in neutrino emission



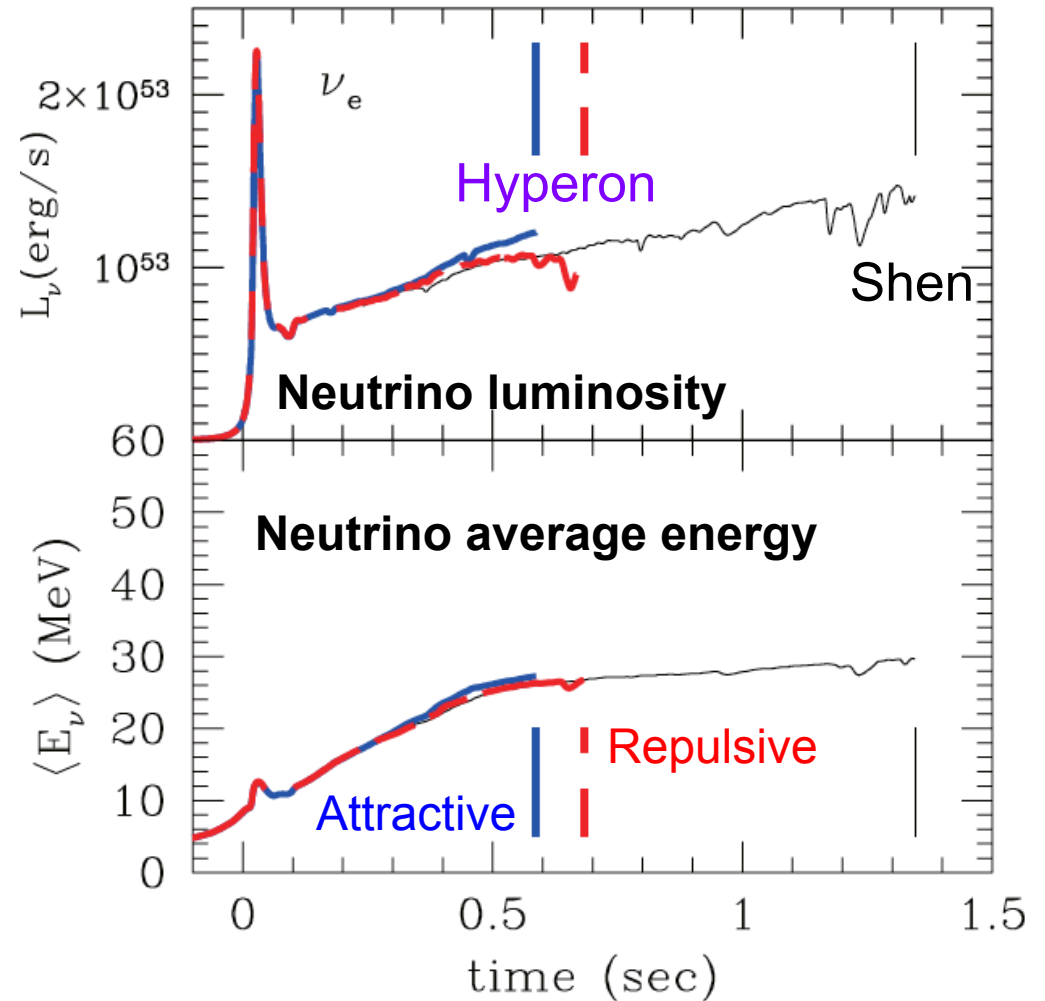
Neutrino burst from failed supernovae

- Probe EOS soft/stiff, hyperon-mixture 40M_{sun}

Nakazato et al. ApJ (2012)



Hyperon mixture
in proto-neutron star



Summary and discussions

- **Key role of EOS for successful explosion**
 - Initial shock energy (just above n_0 with $Y_p \sim 0.3$)
 - Neutrino heating (proto-neutron star EOS)
- **Supernova neutrinos from proto-neutron stars**
 - Appearance of hyperons/quarks
- **Needs systematic EOS for 2D**
 - Link to nuclear data (radii, masses, K , A_{sym})
- **Unique best EOS table for 3D**
 - Experiments & nuclear many body theories
 - Neutron star mass & radius constraint

3D supernova project in collaboration with

- Supernova research
 - S. Yamada
 - H. Suzuki
 - K. Nakazato
- EOS table
 - H. Shen
 - K. Oyamatsu
 - H. Toki
- Extension of EOS table
 - S. Furusawa
 - A. Ohnishi
 - C. Ishizuka
- Supercomputing
 - H. Matsufuru
 - A. Imakura
 - T. Sakurai
- Numerical simulations
 - H. Nagakura
 - K. Kotake
 - T. Takiwaki
- Neutrino reactions
 - T. Sato
 - S. Nasu
 - S. Nakamura

新学術領域「計算科学による素核宇融合」

Support from: HPCI Strategic Program Field 5

- Grant-in-Aid for Scientific Research on Innovative Areas (20105004, 20105005)

- Grant-in-Aid for Scientific Research (22540296, 24244036)

Supercomputing resources at KEK, RCNP, YITP, UT