

中性子星物質の状態方程式と冷却現象 EOS of NS-Matter and NS-cooling

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- Hyperons surely participate in NS cores
- NS Observations
 - Two serious problems:
 - (1) Strong softening of EOS
 - (2) Too-rapid Cooling
 - feedback to the physics of hadrons and quarks
- Summary

In collaboration with R. Tamagaki, S. Nishizaki, Y. Yamamoto,
T. Hatsuda and M. Masuda

1. Hyperons surely participate in
neutron star cores

Hyperon-mixing

$$\Delta m$$

$$= m_\Lambda - m_n$$

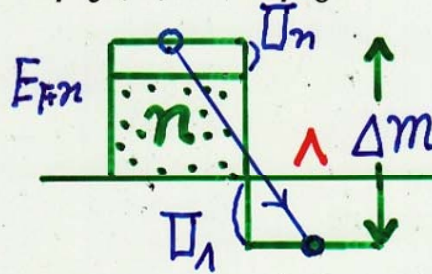
$$\simeq 175 \text{ MeV}$$

$$\Delta m = m_\Lambda - m_n$$

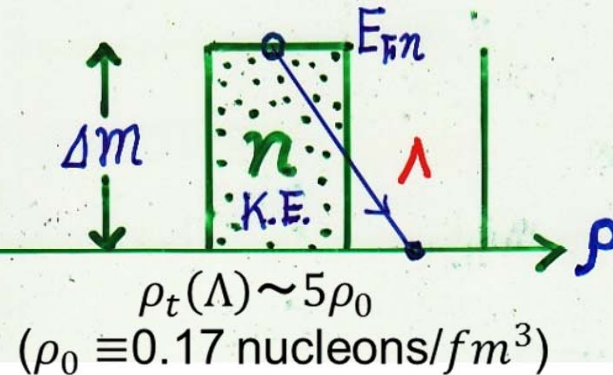
$$\simeq 175 \text{ MeV}$$

$\langle \text{K.E.} + \text{Int. E} \rangle$

$$\rho_t(\Lambda) < 5\rho_0$$



$\langle \text{K.E. only} \rangle$

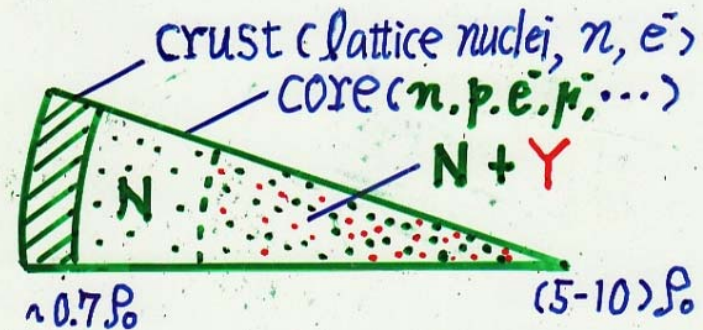


(1) K.E. only : $\text{K.E.} + m_n = \mu_n = \mu_\Lambda = m_\Lambda$

$$61(\rho/\rho_0)^{2/3} \text{ MeV} \rightarrow \rho_t(\Lambda) \sim 5\rho_0$$

(2) K.E. + Int. E: $\text{K.E.} + U_n + m_n = \mu_n = \mu_\Lambda = m_\Lambda + U_\Lambda$

$U_\Lambda < 0$ (assured by the existence of Λ -hypernuclei),
and $U_n > 0 \rightarrow \rho_t(\Lambda) \ll 5\rho_0$ is expected



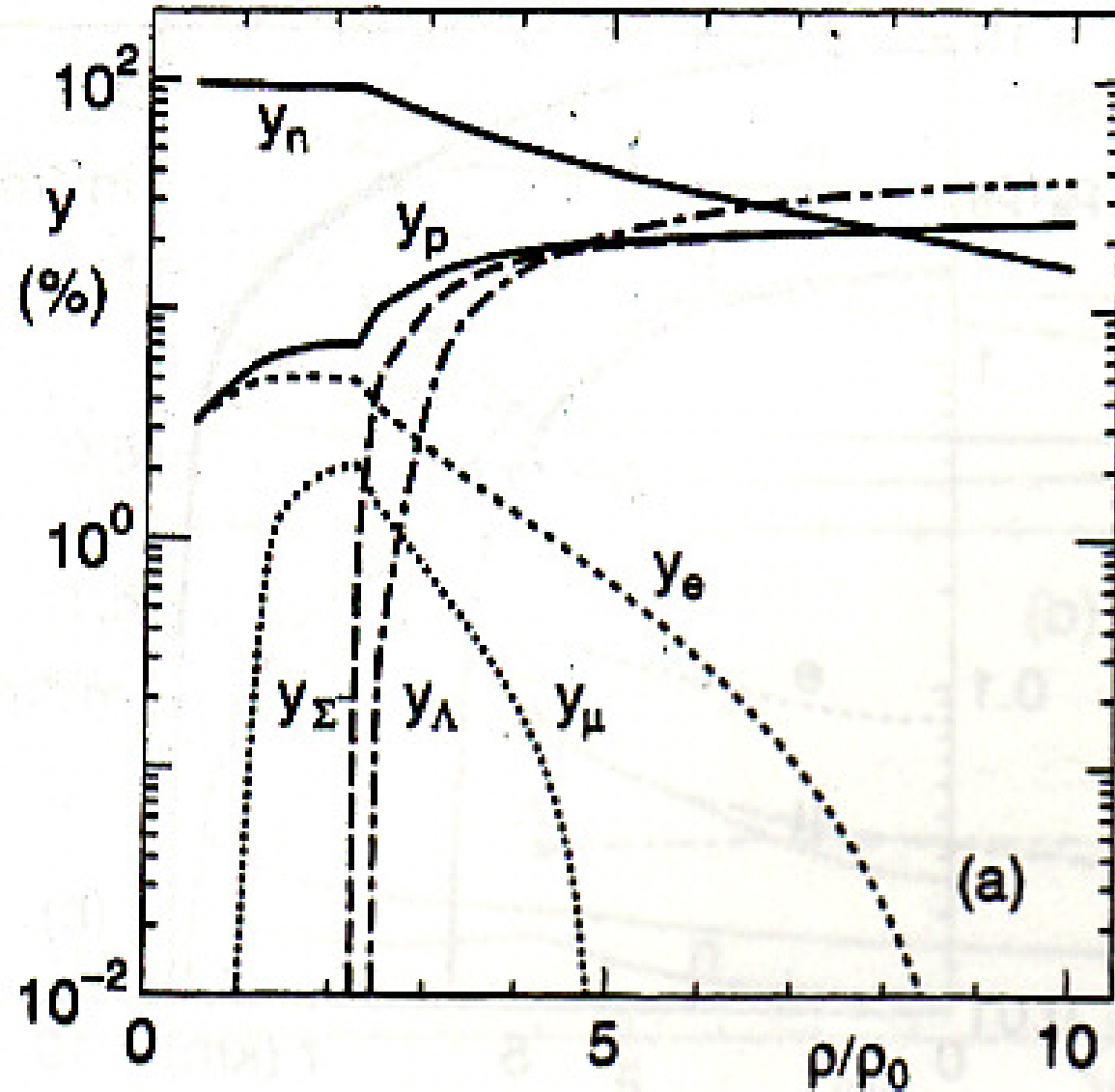
□ Our approach to NS-matter with Λ -mixing

- Matter composed of N (n, p), Λ (Σ^-) and Leptons (e^- , μ^-)
- effective interaction approach based on G-matrix calculations, (effective int. V for NN, N Λ , $\Lambda\Lambda$)
Introduction of 3-body force U (TNI, phenomenological Illinois-type, expressed as effective 2-body force)
- V+U satisfy the saturation property and symmetry energy at nuclear density
- (hard, soft) is classified by the incompressibility κ ;
 $\kappa=300, 280, 250$ MeV for TNI3,TNI6,TNI2

[1] S. Nishizaki, Y. Yamamoto and T. Takatsuka, Prog.Theor. Phys.105 (2001) 607; 108 (2002) 703

[2] T. Takatsuka, Prog. Theor. Phys. Suppl. No. 156 (2004) 84

- Hyperons appear at $\rho_t \sim (2-2.5)\rho_0$



○ So many works including ours have been devoted to the Λ -mixing in neutron stars (NSs) (e.g. [3][4])

→ **Hyperon surely participate in NS Cores**

($\rho_t(\Lambda) \sim 2\rho_0$, increasing population with ρ)

→ Standard picture for NS constituents;

Old (n, p, e^- , μ^-) → Now (n, p, **Λ** , e^- , μ^-)

→ NS properties should be discussed by taking account of Λ degrees of freedom

[3] M. Baldo, G.F. Burgio and H.-J. Schulze, Phys. Rev. C61 (2000) 055801

[4] I. Vidaña, A. Polls, A. Ramos, L. Engvik and M. Hjorth-Jensen, Phys. Rev. C62 (2000) 035801

2. What happens ?

Two Serious Problems

(1) Dramatic Softening of NS EOS

→ Contradicts observed mass (M_{obs}) of NSs:

$$\begin{aligned} M_{max} < M_{obs} &= (1.44 \pm 0.002)M_{\odot} \text{ for PSR1913+16} \\ &= (1.97 \pm 0.04)M_{\odot} \text{ for PSRJ1614-2230} \end{aligned}$$

→ Problem 1

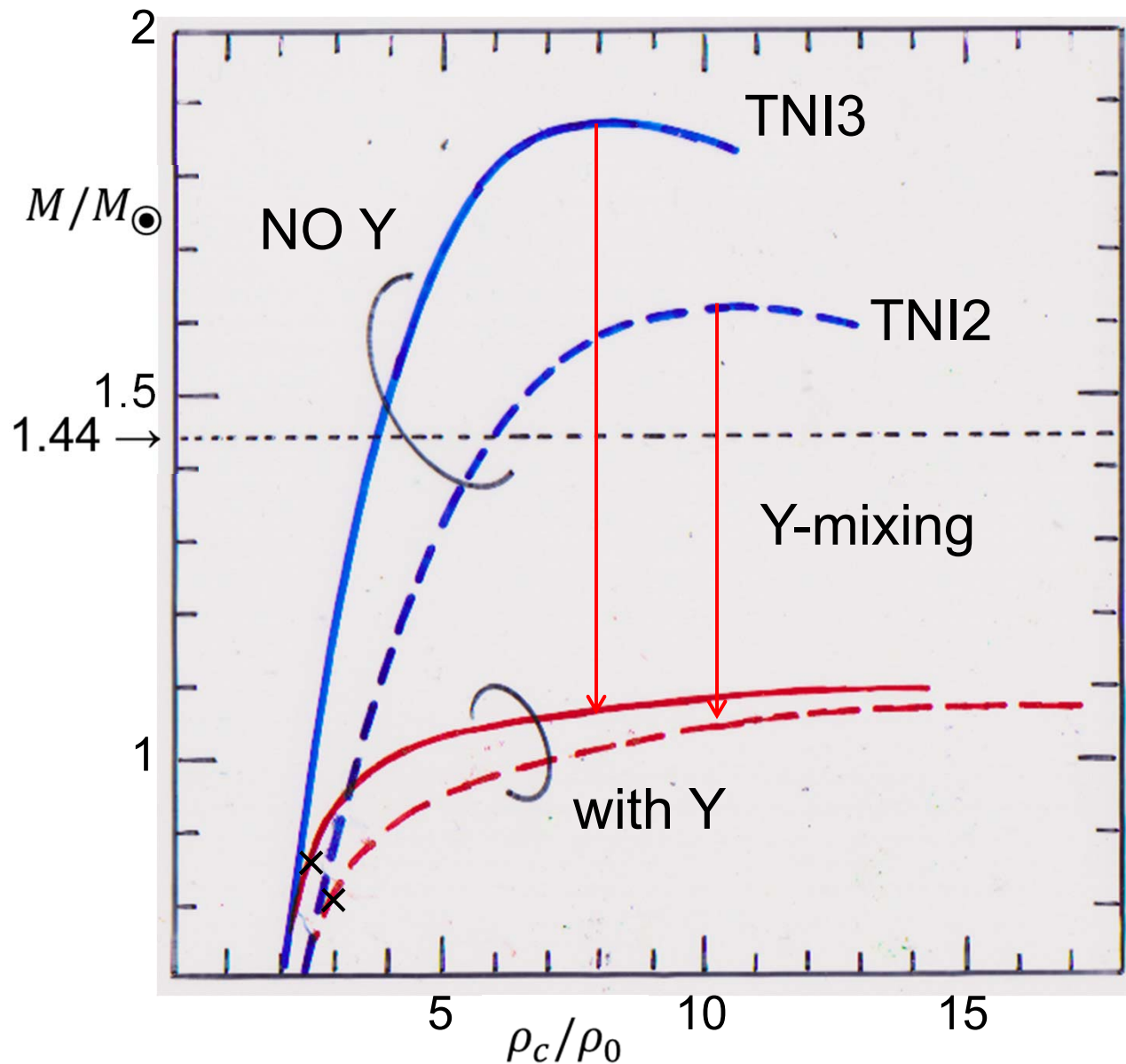
(2) Too rapid cooling

→ contradicts observed surface-temperature (T_s) of NSs:

- All of the NSs whose T_s are observed by thermal X-ray should have $M < M_{\odot}$ ----unlikely
- Thermal evolution of colder class NSs (Vela X-1, 3C58, Geminga, etc.) is very difficult to be explained

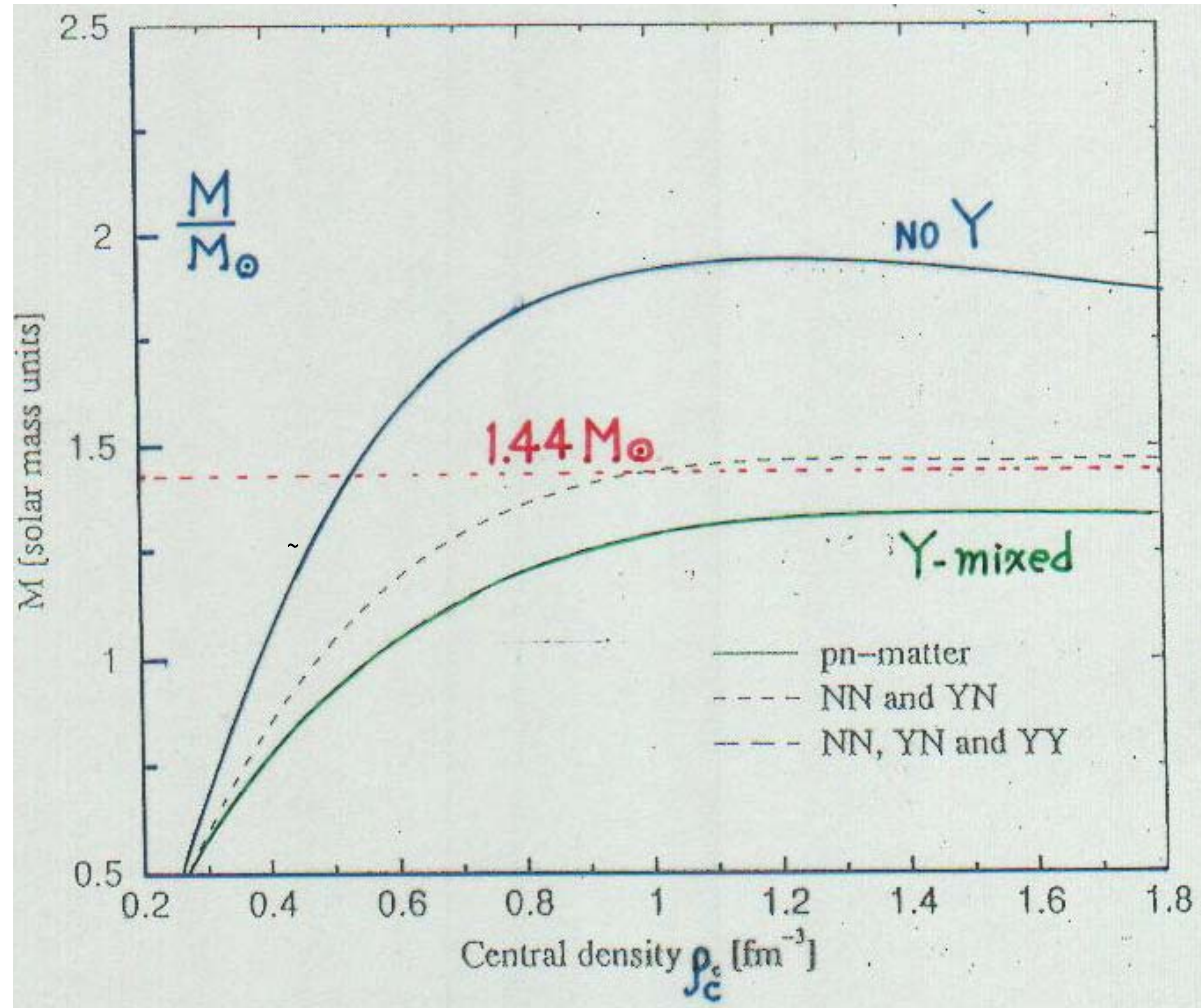
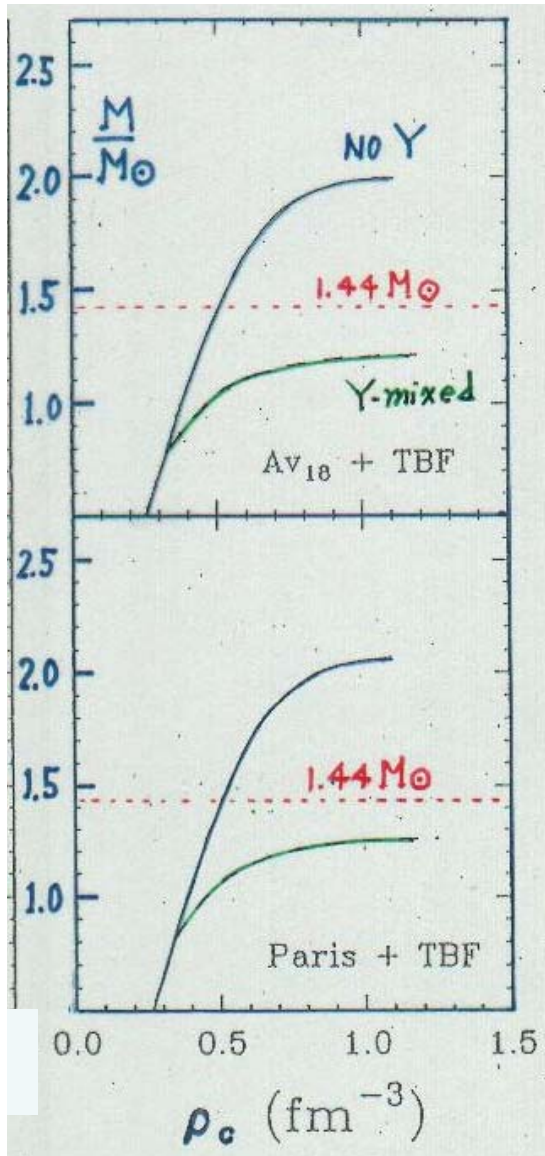
→ Problem 2

$M_{max} < M_{obs}$ (Softened EOS by Y)



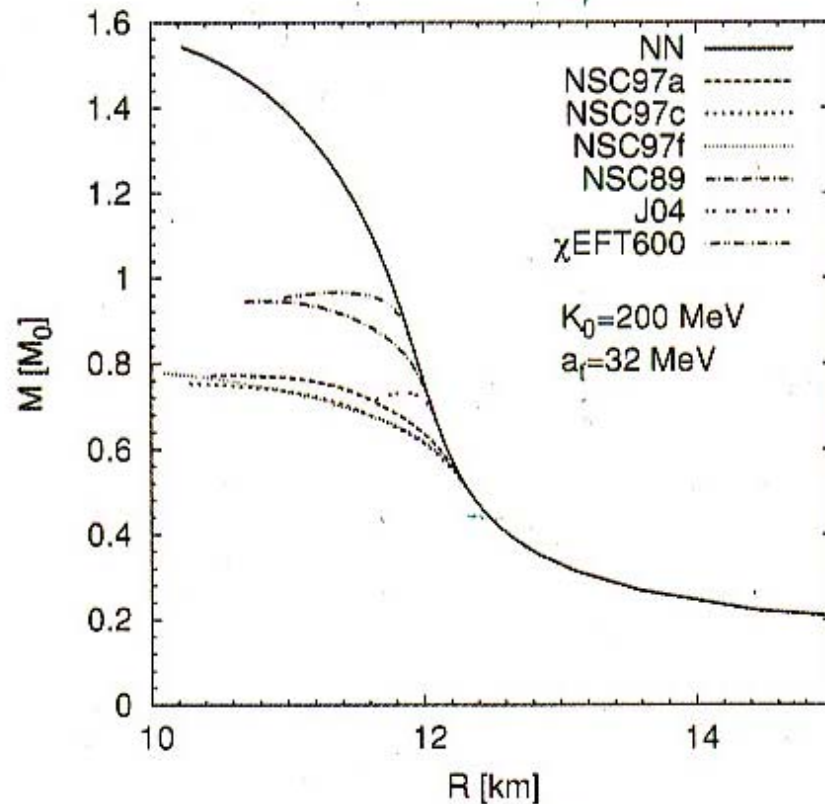
(1)

Strong Softening
of the EOS

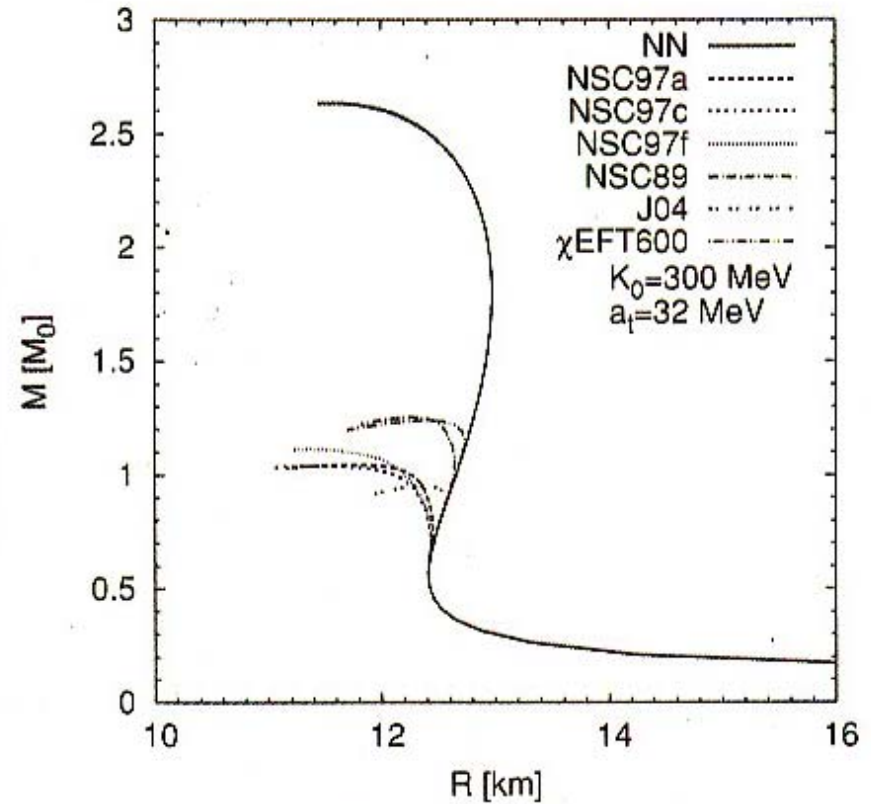


↑ L-Vidana et al, P.R. C62 (2000) 035801
 ← M. Baldo et al, P.R. C61 (2000) 055801

- Hyperons are always present
 → profound consequence for NS-mass



(a) $K_0 = 200$ MeV



(b) $K_0 = 300$ MeV

(2) Too rapid cooling

NS cooling due to ν -emission

(J. M. Lattimer et al. , PRL66(1991)2701)

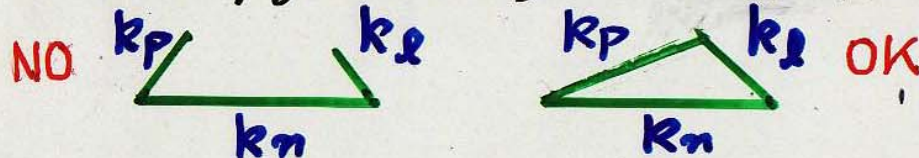
o Modified URCA (Murca) --- Standard (slow)

$$\bullet n+n \rightarrow p+n+l+\bar{\nu}_l ; (l \equiv e^-, \mu^-)$$

o Direct URCA (usual β -decay type) --- Non-standard (fast)

$$\bullet n \rightarrow p+l+\bar{\nu}_l, p+l \rightarrow n+\nu_l \text{ (N-Durca)}$$

* usually forbidden, but made possible for $Y_p \geq 15\%$



$$\bullet \Lambda \rightarrow p+l+\bar{\nu}_l, p+l \rightarrow \Lambda+\nu_l \text{ (Y-Durca)}$$
$$\bullet \Sigma^- \rightarrow \Lambda+l+\bar{\nu}_l, \Lambda+l \rightarrow \Sigma^-+\nu_l \text{ (")}$$

Y-cooling

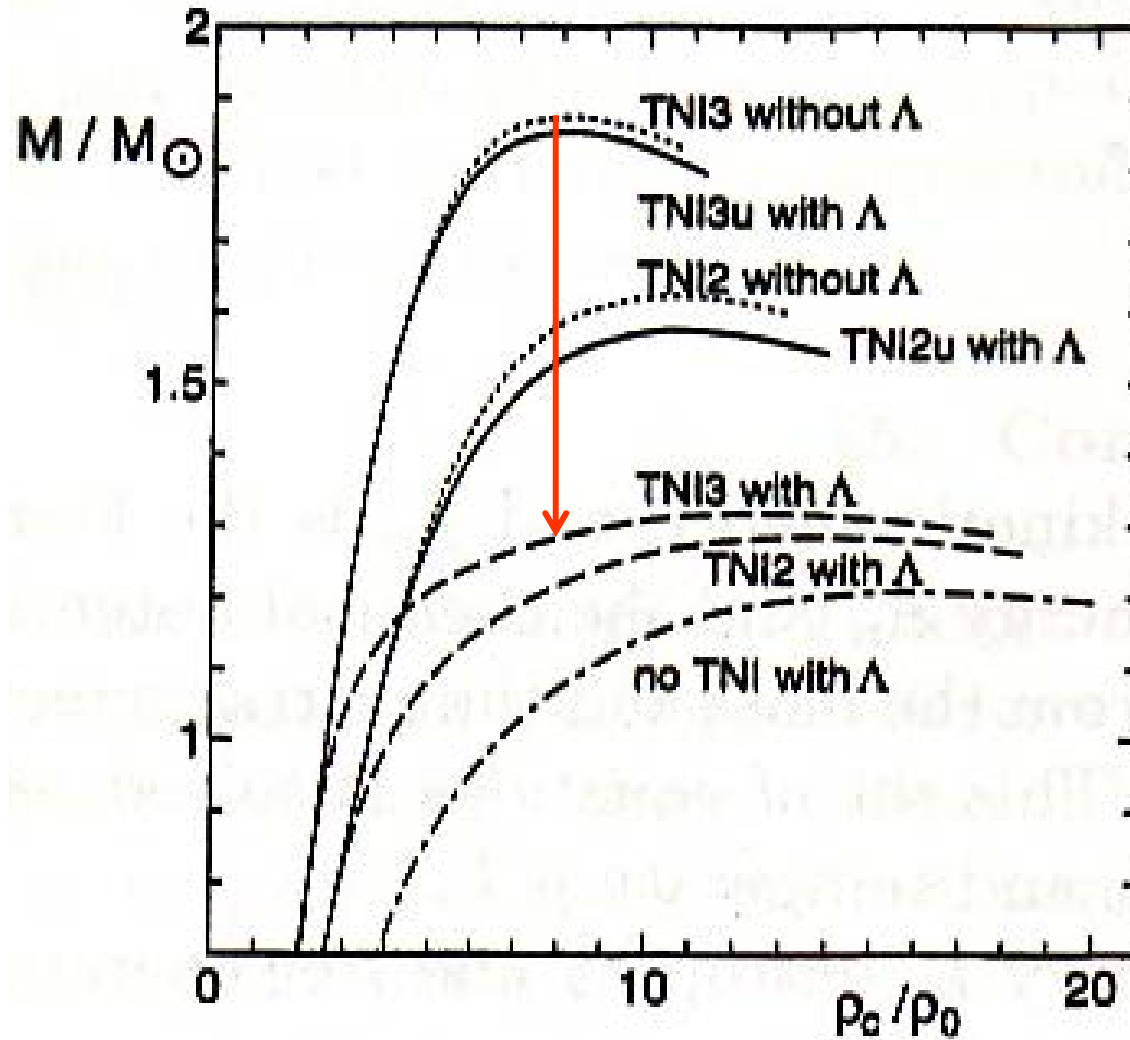
o ϵ_ν (Durca) $\sim 10^6 \epsilon_\nu$ (Murca)

- But, if directly applied, it causes a serious problem of “too rapid cooling” incompatible with NS surface-temperature observations.
- Since NSs with $M \geq M_0$ have a Y-mixed core, most NSs (with $M < M_{\odot}$) are too cold to be observed by thermal X-rays----- unlikely?
- How to explain the existence of colder class NSs (such as Velax-1, 3C58, Geminga, etc.)

○ These problems are **serious** because of the points,

- ① Y surely participate in NSs → cannot be ignored
- ② Dilemma: Enhancement of NN repulsion → more developed Y-mixing → stronger softening effect → a good-for-nothing
- ③ Without Σ^- -mixing (i.e. only Λ), the situation is unchanged

Even Λ -only mixing, situation is the same!



3. Possible solution for the problem

Problem 1:

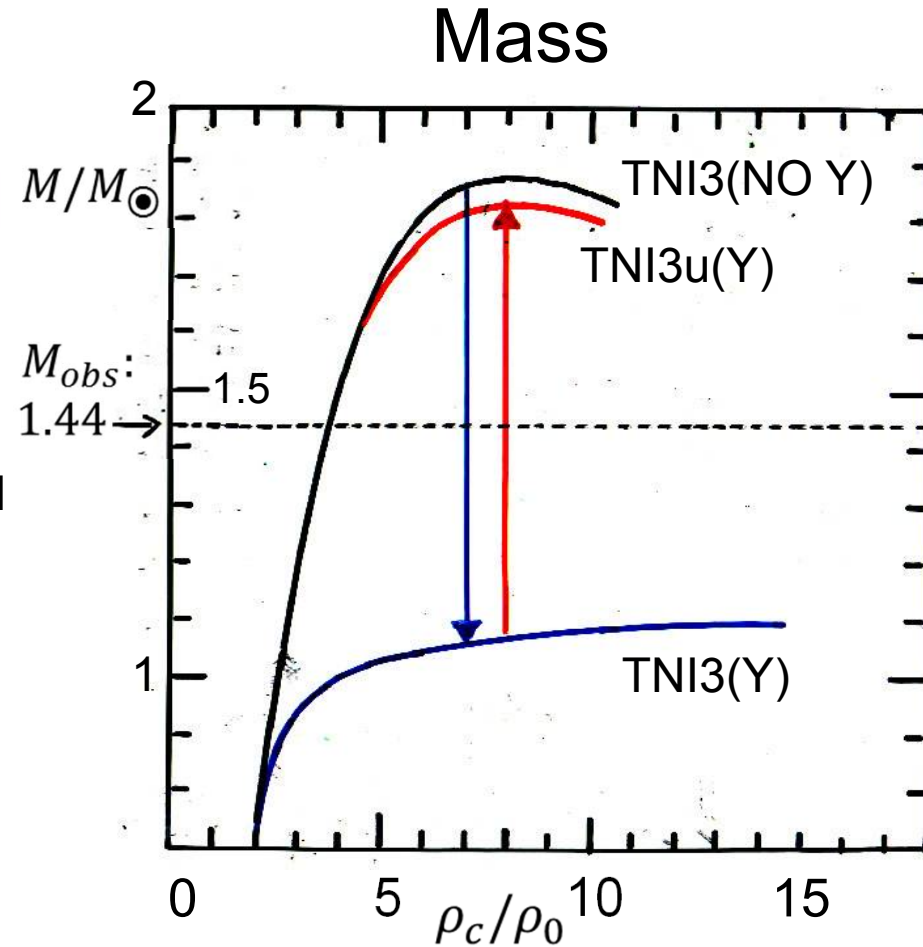
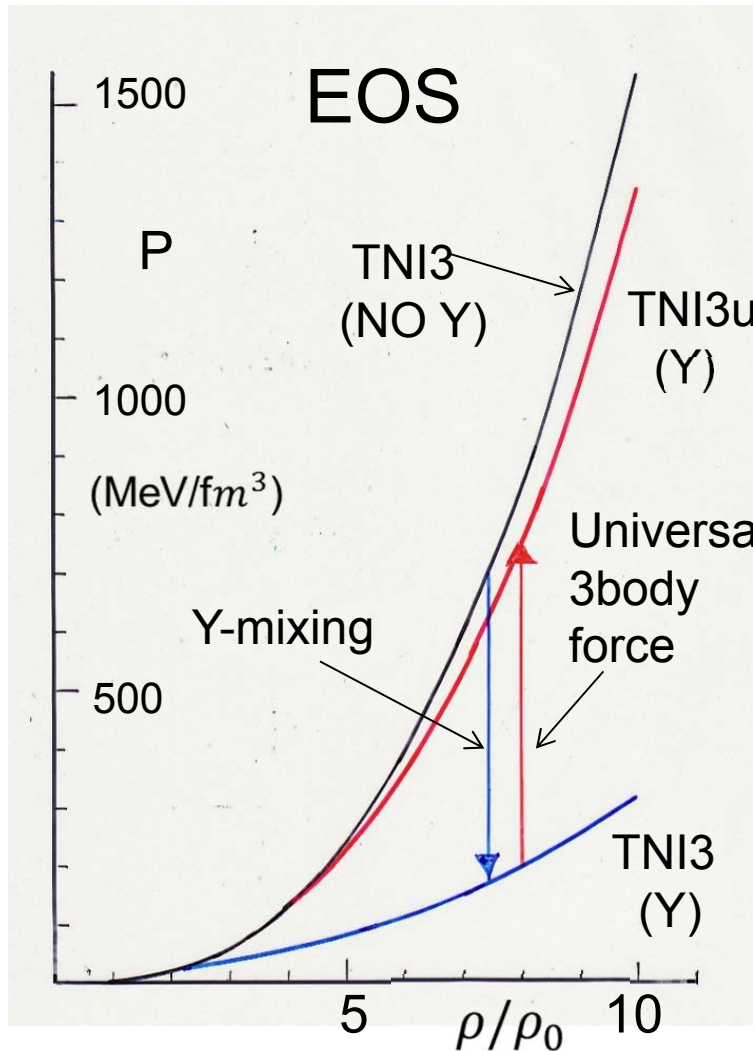
Dramatic softening of EOS →

Universal 3-body force

The contradiction between theory and observation ($M_{\text{max}} < M_{\text{obs}}$) strongly suggests the necessity of some extra repulsion in dense hypernuclear systems

→ 3-body force repulsion acting “universally” on NN, YN and YY parts (**universal 3-body force**) is a promising candidate [1][2]

Dramatic softening of EOS \longrightarrow Necessity of “Extra Repulsion”



TNI3 \longrightarrow TNI3u: Universal inclusion of TNI3 repulsion

Comment 1 :an **origin** of “universal 3-body force”

- “3-body force of extended $2\pi\Delta$ -type”(at long and intermediate ranges) + “3-body force based on the string-junction quark model(SJM;at short distance) has been studied [5]

[5] T.Takatsuka,S.Nishizaki and R.Tamagaki,
Proc.Int.Symp.”FM50”(AIP Conference proceedings,
2008)209

Extended $2\pi\Delta$ -Type 3-body Force

; not universal

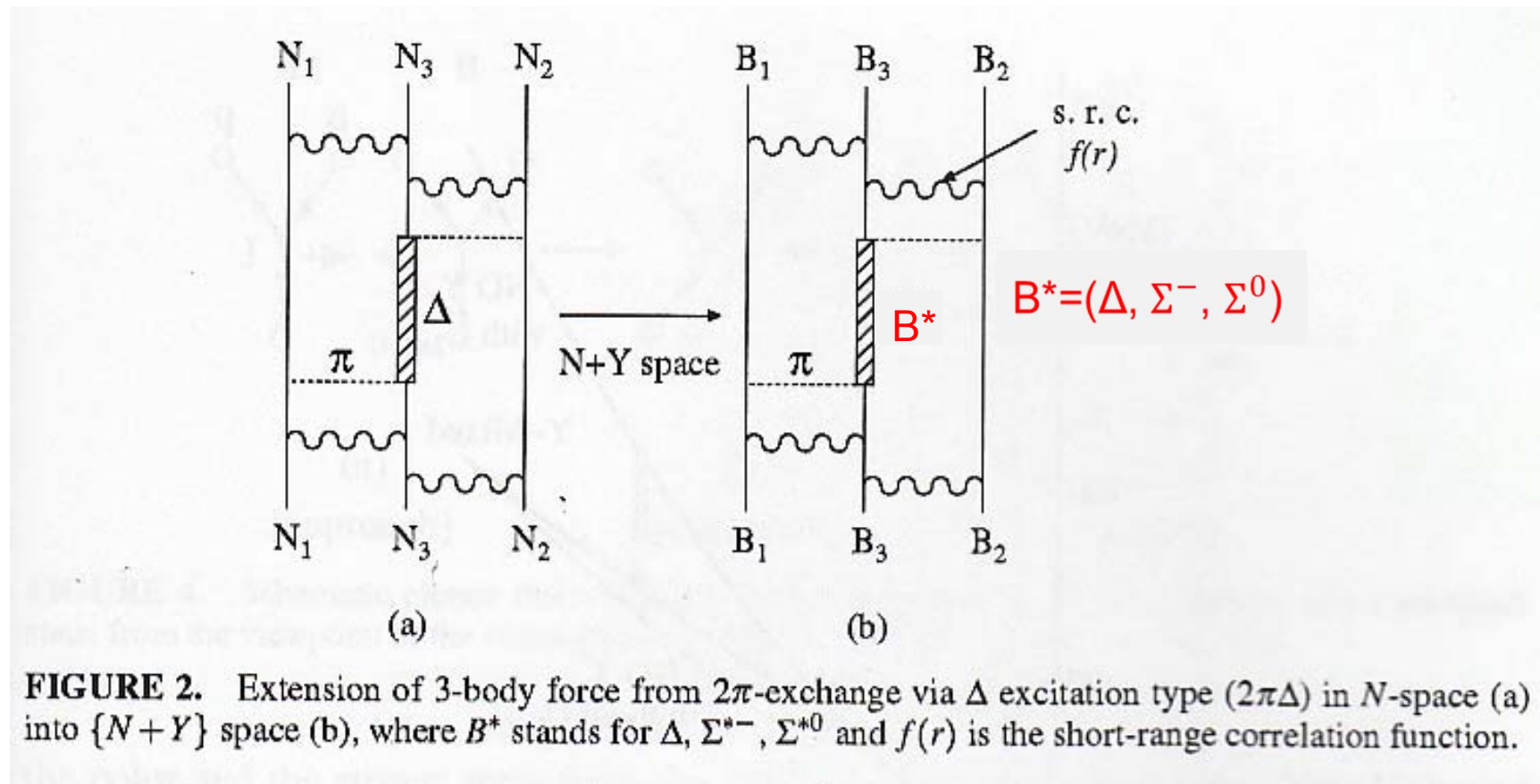
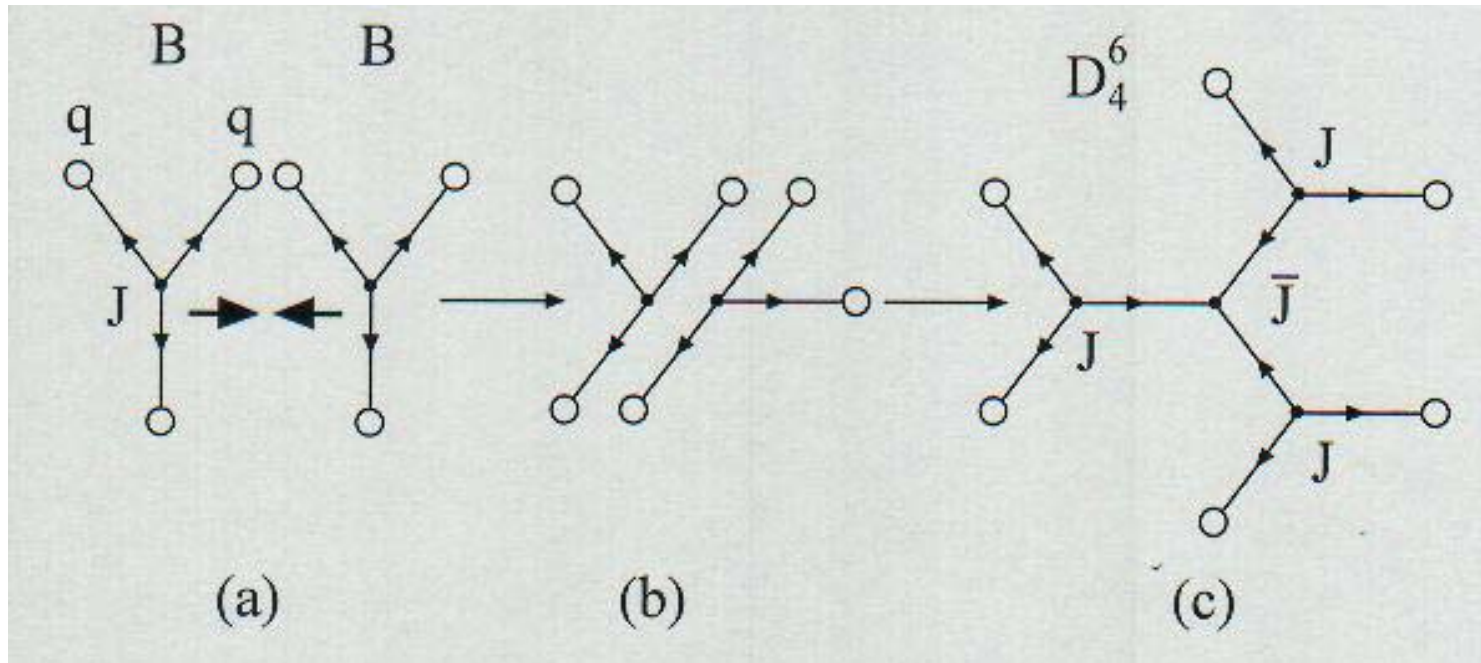


FIGURE 2. Extension of 3-body force from 2π -exchange via Δ excitation type ($2\pi\Delta$) in N -space (a) into $\{N+Y\}$ space (b), where B^* stands for $\Delta, \Sigma^{*-}, \Sigma^{*0}$ and $f(r)$ is the short-range correlation function.

○ Short-range correlations among N_1, N_2 and N_3 are duly taken into account ; T.Kasahara, Y.Akaishi and H.Tanaka, PTP Suppl.No.56(1974)96

Repulsion from SJM-----**flavor independent**



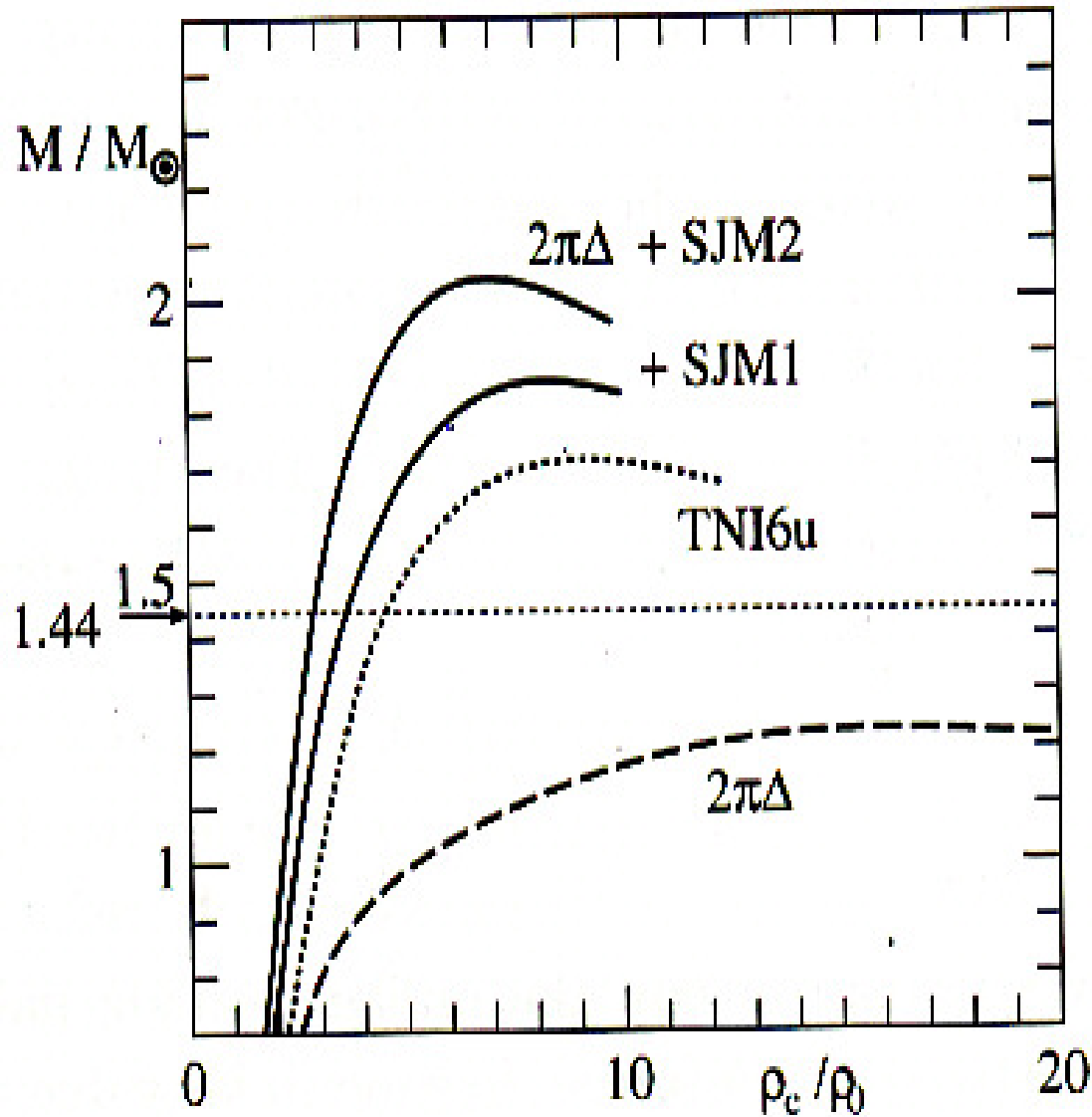
- (a) 2B come in short distance
- (b) Deformation (resistance)
- (c) Fusion into 6-quark state

(by R. Tamagaki)

Prog. Theor. Phys. 119
(2008) 965.

- **Energy barrier ($\sim 2\text{GeV}$) corresponds to repulsive core of BB interactions**

Mass v.s. Central Density



NS-mass from 2-body force + "universal" 3-body force ($2\pi\Delta$ -type + SJM).

$M_{max} > 2M_{\odot}$
is possible.

Comment 2: Quark degrees of freedom

$2M_{\text{sun}}$ NS \rightarrow high central density

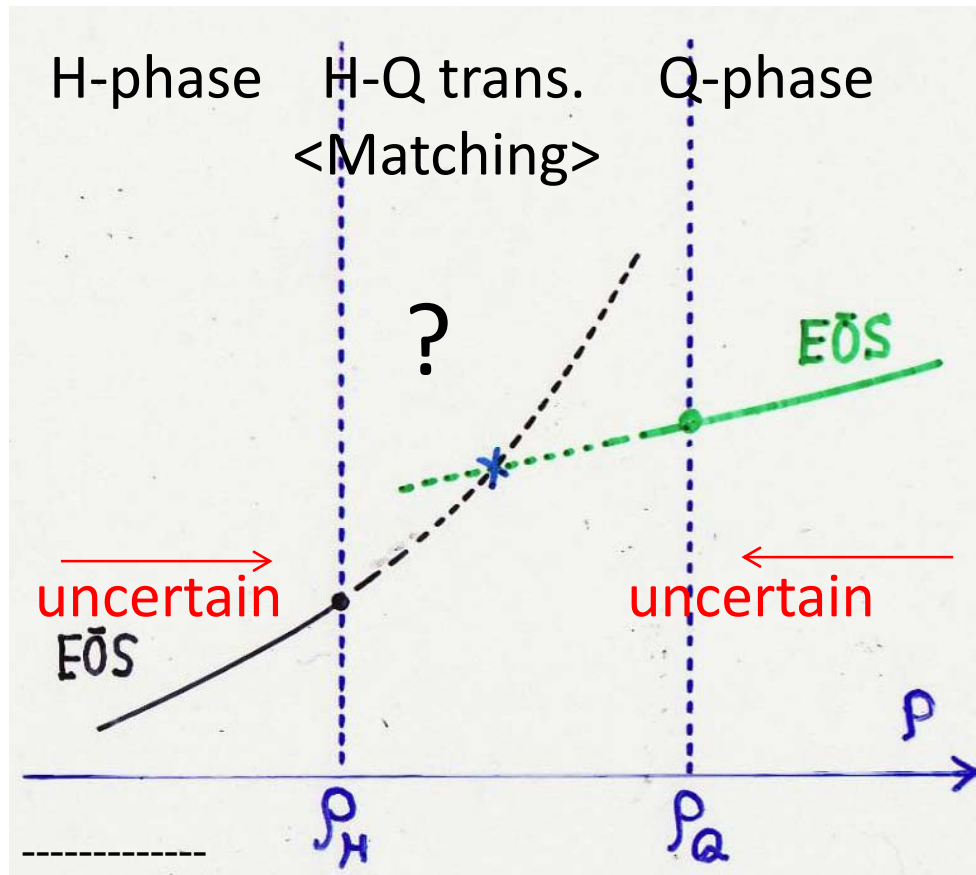
\rightarrow possibility of a hybrid star

From a view of “smooth crossover” in the hadron - quark phase transition, a possibility of hybrid stars (NSs with quark matt. core)

Is discussed \rightarrow $2M_{\text{sun}}$ is possible under the conditions ;1) crossover proceeds in rather low densities,2) strongly correlated quark matter.

□ Possibility of quark matter in NSs ^{*)}

A way of approach



- H: point particle + interaction
→ G-Matrix, Variational
- Q: q-matter + asymptotic freedom
- HQ Phase transition
Cross point (Maxwell, Gibbs) → not necessarily reliable
- Need new strategy

*) [6] T. Takatsuka, T. Hatsuda and K. Masuda, Proc. of "OMEGA11"
(Nov.14-17, 2001, RIKAEEN)

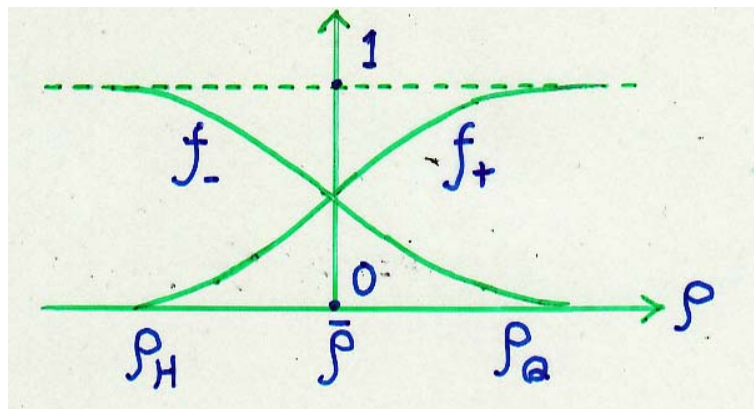
[7] K. Masuda, T. Hatsuda and T. Takatsuka, arxiv:1205.362 [nucl-th.]

□ Interpolation between H- and Q-phases

○ From a view of “H-Q Crossover”

$$P(\rho) = P_H(\rho)f_-(\rho) + P_Q(\rho)f_+(\rho),$$

$$f_{\pm}(\rho) = \frac{1}{2} \left\{ 1 \pm \tanh \left(\frac{\rho - \bar{\rho}}{\Gamma} \right) \right\}$$



*) Asakawa-Hatsuda
P.R. D55(1997)
4488

○ energy density $\varepsilon(\rho)$ is derived from

$$P(\rho) = \rho^2 \partial \left(\frac{\varepsilon(\rho)}{\rho} \right) / \partial \rho$$

□ Quark Matter phase

- (2 + 1) -flavor NJL model with vector interaction

$$L_{NJL} = \bar{q}(i\not{\partial} - m)q + \frac{1}{2}G_S \sum_{\alpha=0}^8 \{(\bar{q}\lambda^\alpha q)^2 + (\bar{q}\lambda^\alpha i\gamma_5 q)^2\} \\ + G_D \{ \det \bar{q}(1 + \gamma_5)q + h.c. \} - \frac{1}{2}g_V (\bar{q}\gamma^\mu q)^2$$

with $q \equiv \{q_i; i = u, d, s\}$ $m \equiv \{m_i\}$

- Hatsuda-Kunihiro parameter set (Phys. Rep - 247 (1994) 221)

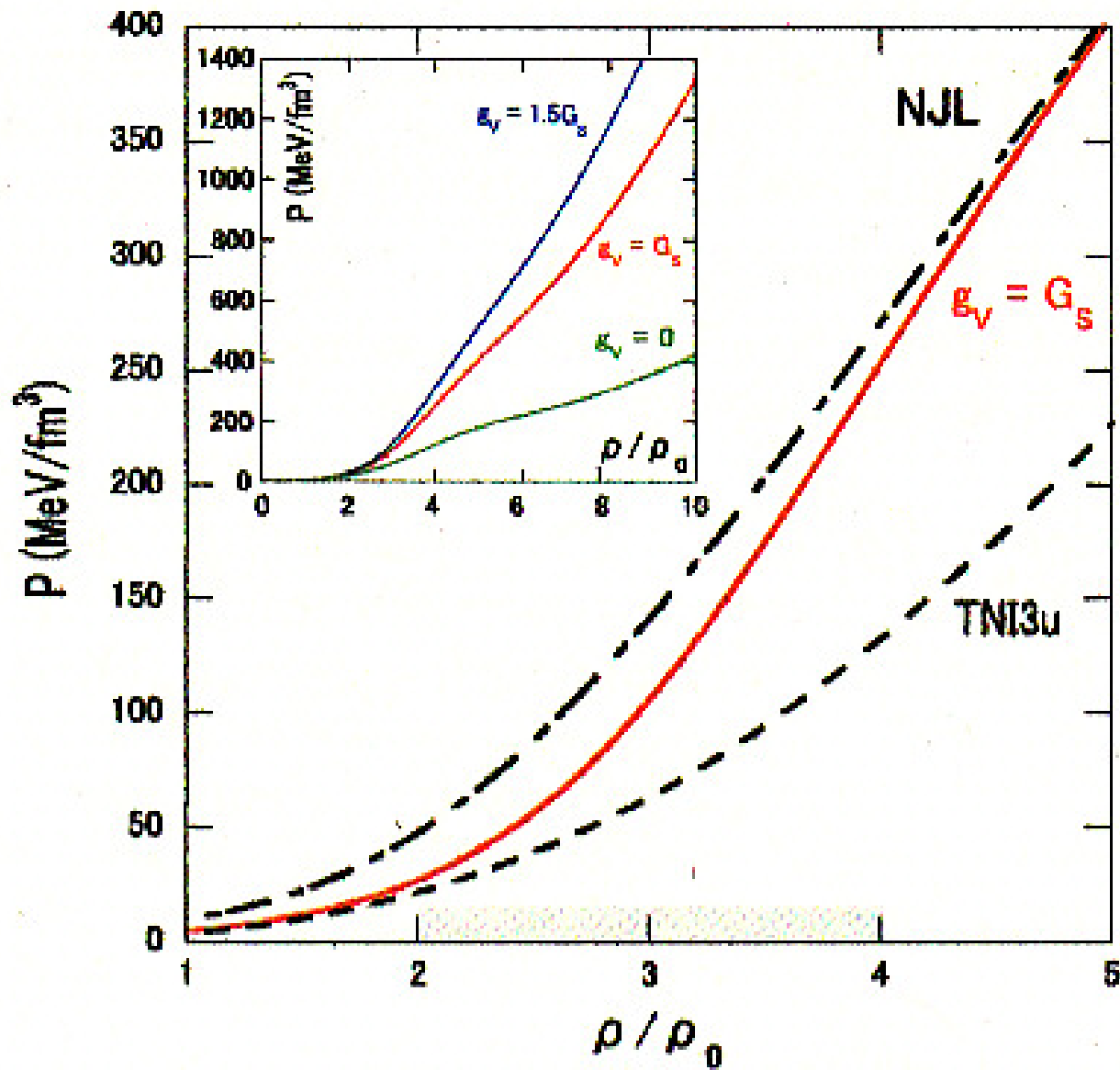
$$\Lambda = 631.4 \text{ MeV}, G_S \Lambda^2 = 1835, G_D \Lambda^2 = 9.29$$

$$m_u = m_d = 5.5 \text{ MeV}, m_s = 135.7 \text{ MeV}$$

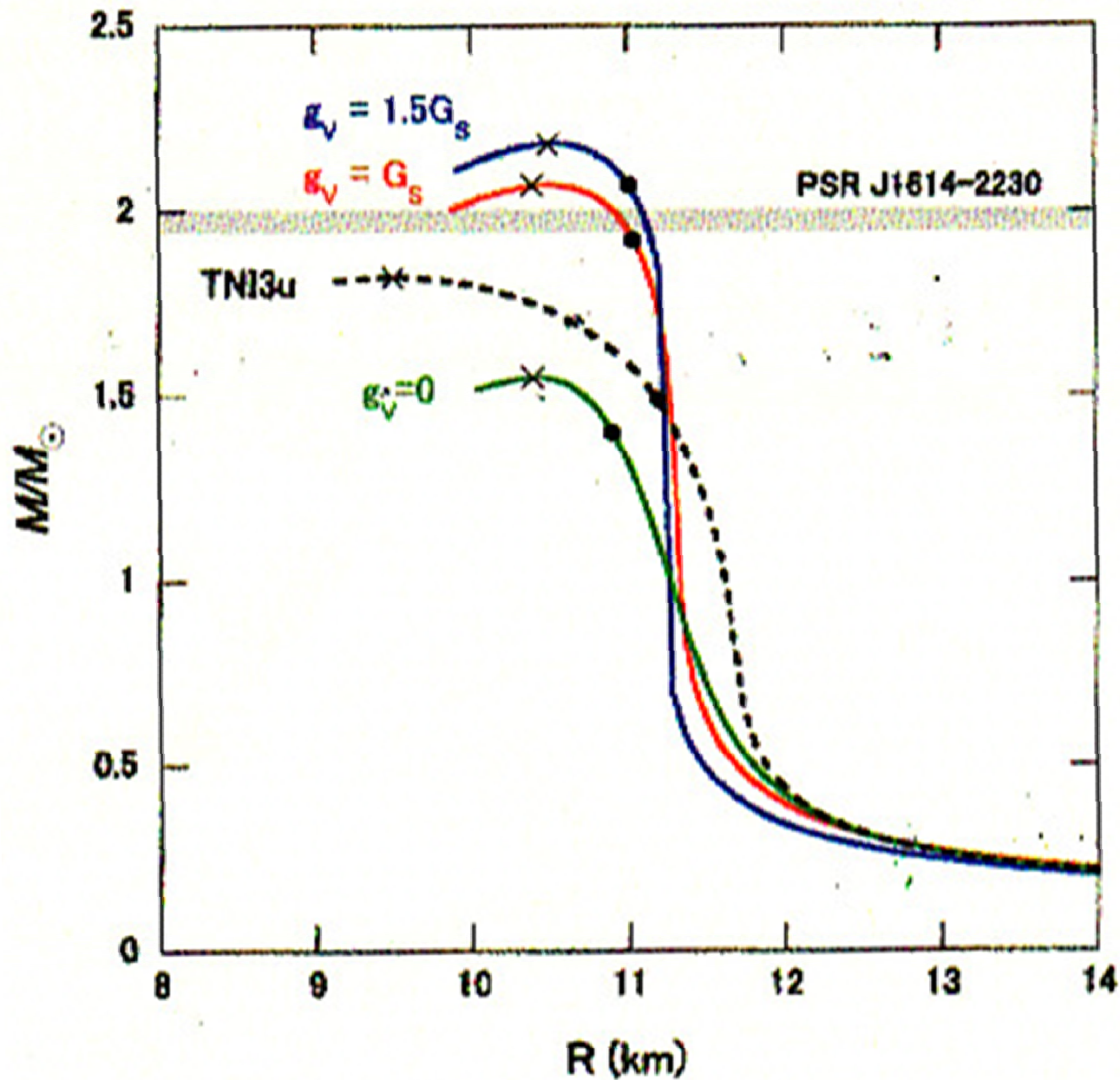
- g_V is not well determined, but it is suggested that g_V can be comparable or even larger than g_S

→ we take

$$\frac{g_V}{g_S} \sim (0 - 1.5)$$



Pressure v.s.
density



Mass v.s.
Radius

$M_{max} > 2M_\odot$

Is possible

Problem 2 :

Too -rapid cooling \rightarrow **Hyperon superfluidity**

NSs with $M > 1.35 M_{\text{sun}}$ have a Y-mixed core. If Y-superfluidity is realized, it suppresses the efficient ν -emission by Y-Durca ($\exp(-\Delta/T)$)

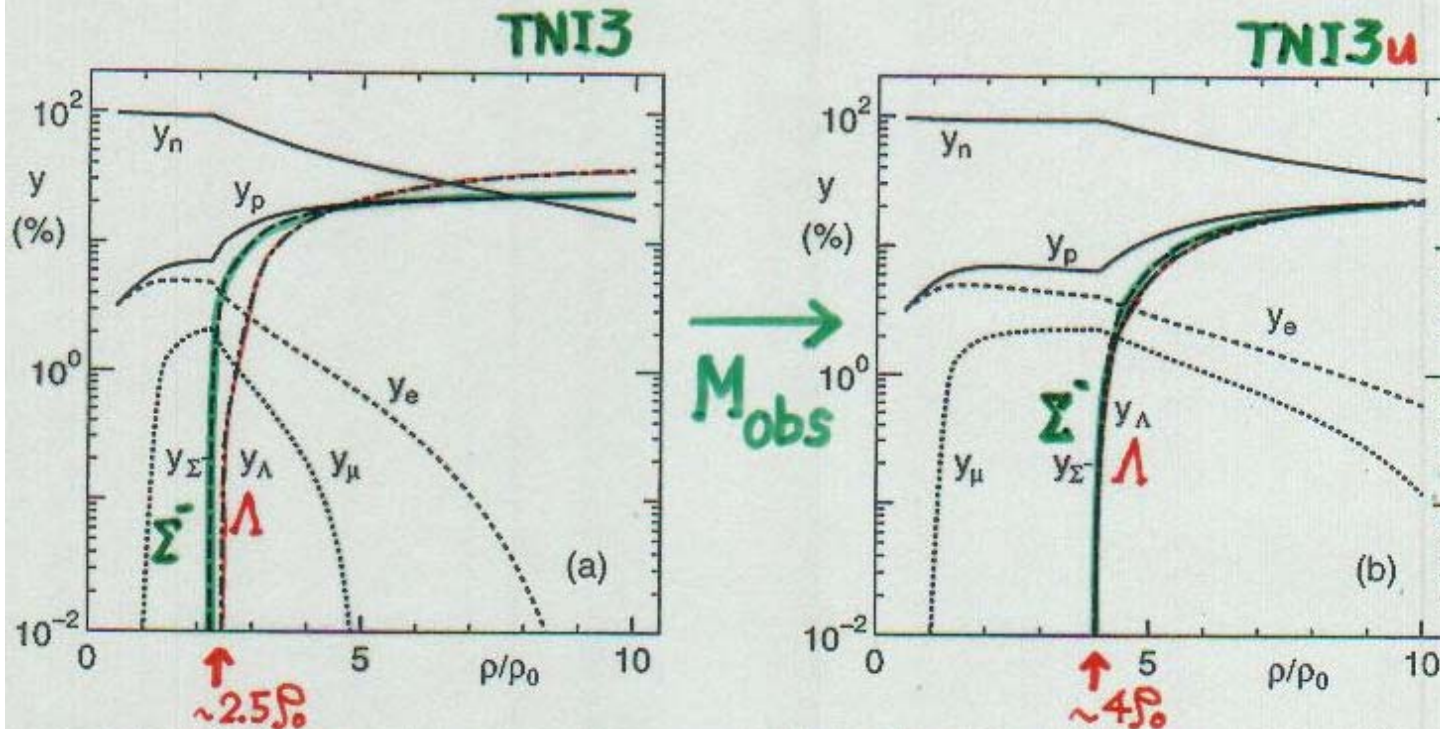
\rightarrow moderate cooling consistent with colder class NSs

That is, a new scenario is

Lighter NSs \rightarrow standard slow cooling of MUrca

Heavier NSs \rightarrow nonstandard fast cooling of YDurca
("hyperon cooling")

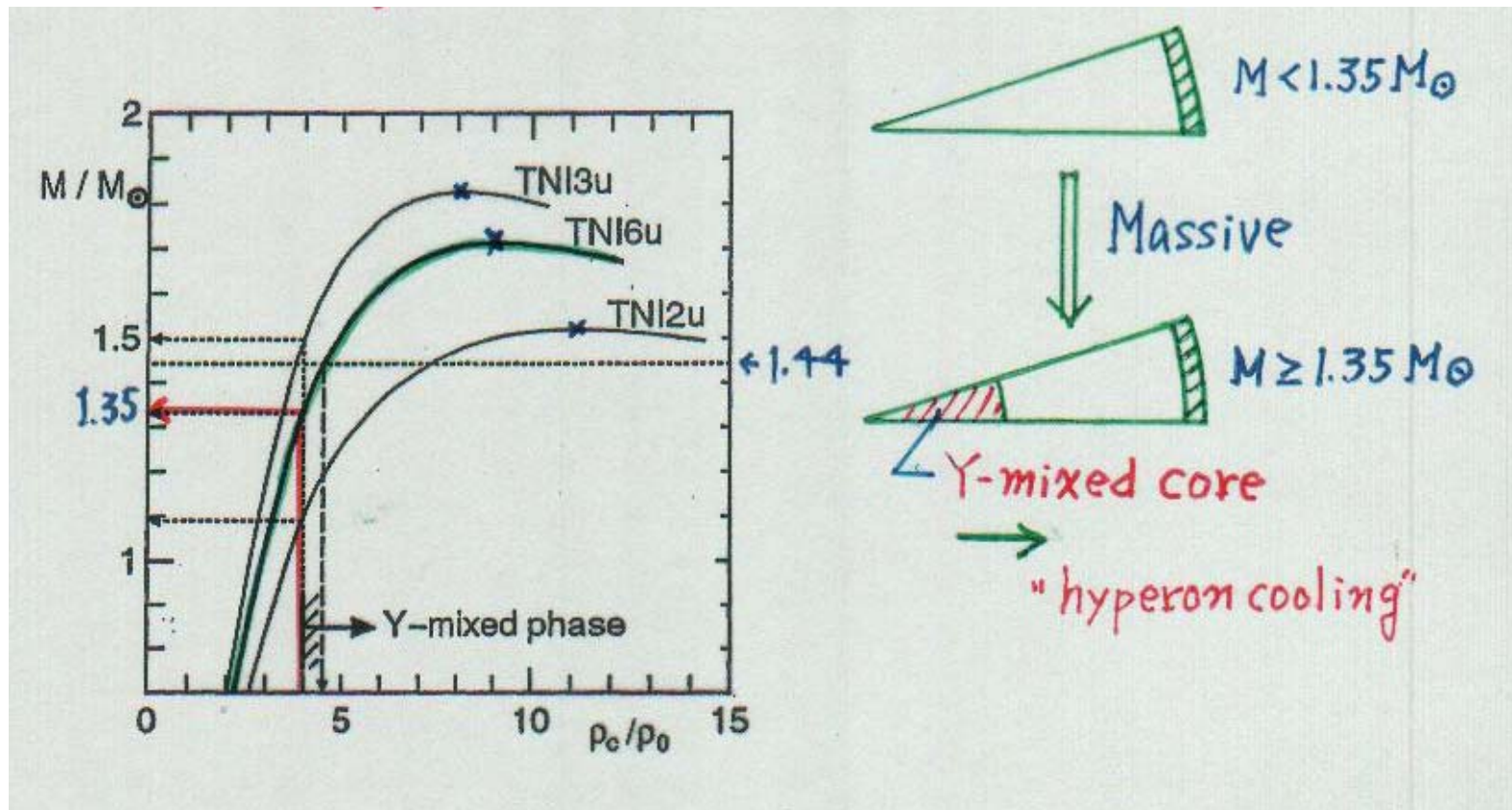
higher ρ_t for $M_{max} \geq 1.44 M_{\odot}$

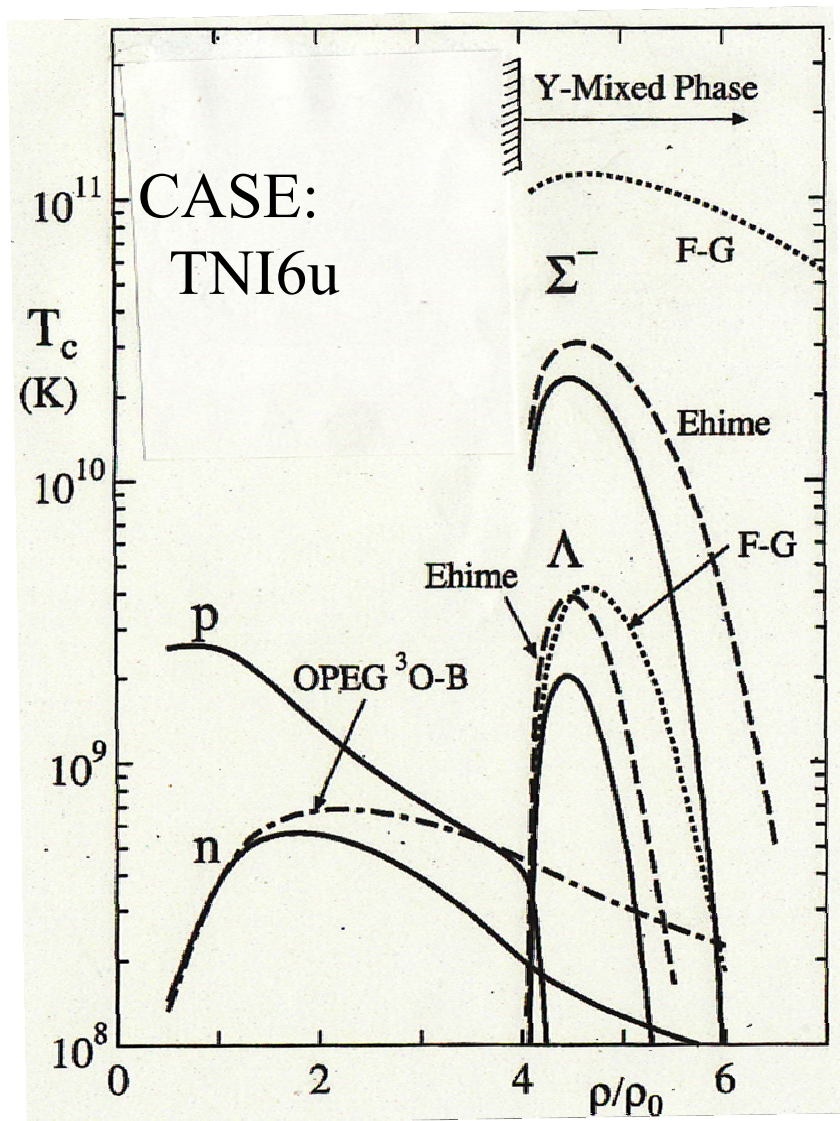


→ Y-mixed star
for $M > M_{\odot}$

→ Y-mixed star
for $M > 1.4 M_{\odot}$

With or without Y-mixed core depends on M





Critical Temperature T_c
versus Density ρ

□ Pairing type:

$n \rightarrow 3P2$

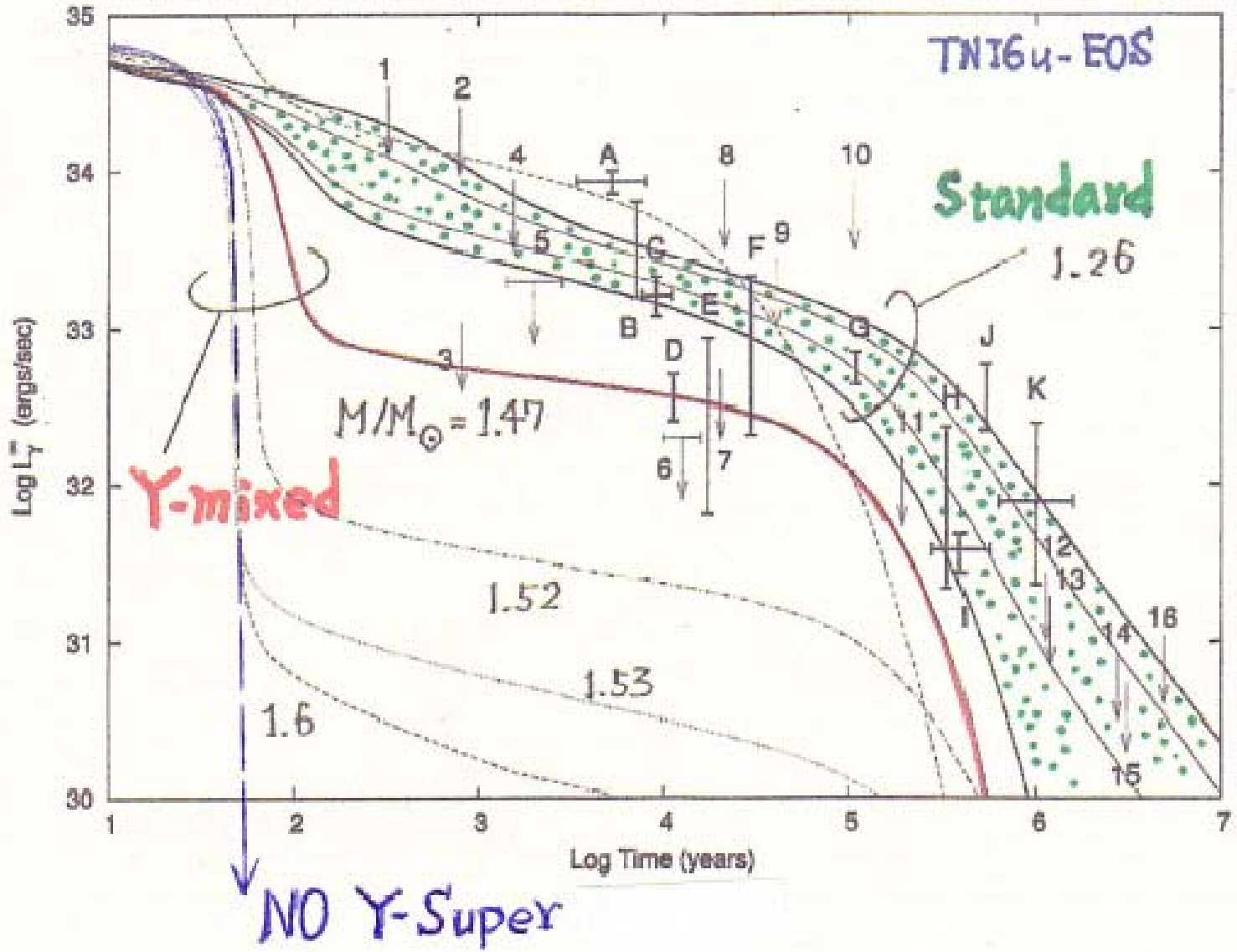
$p, \Lambda, \Sigma^- \rightarrow 1S0$

□ Pairing interactions:

$n, p \rightarrow$ OPEG-A pot.

$\Lambda, \Sigma^- \rightarrow$ ND-Soft

for solid lines

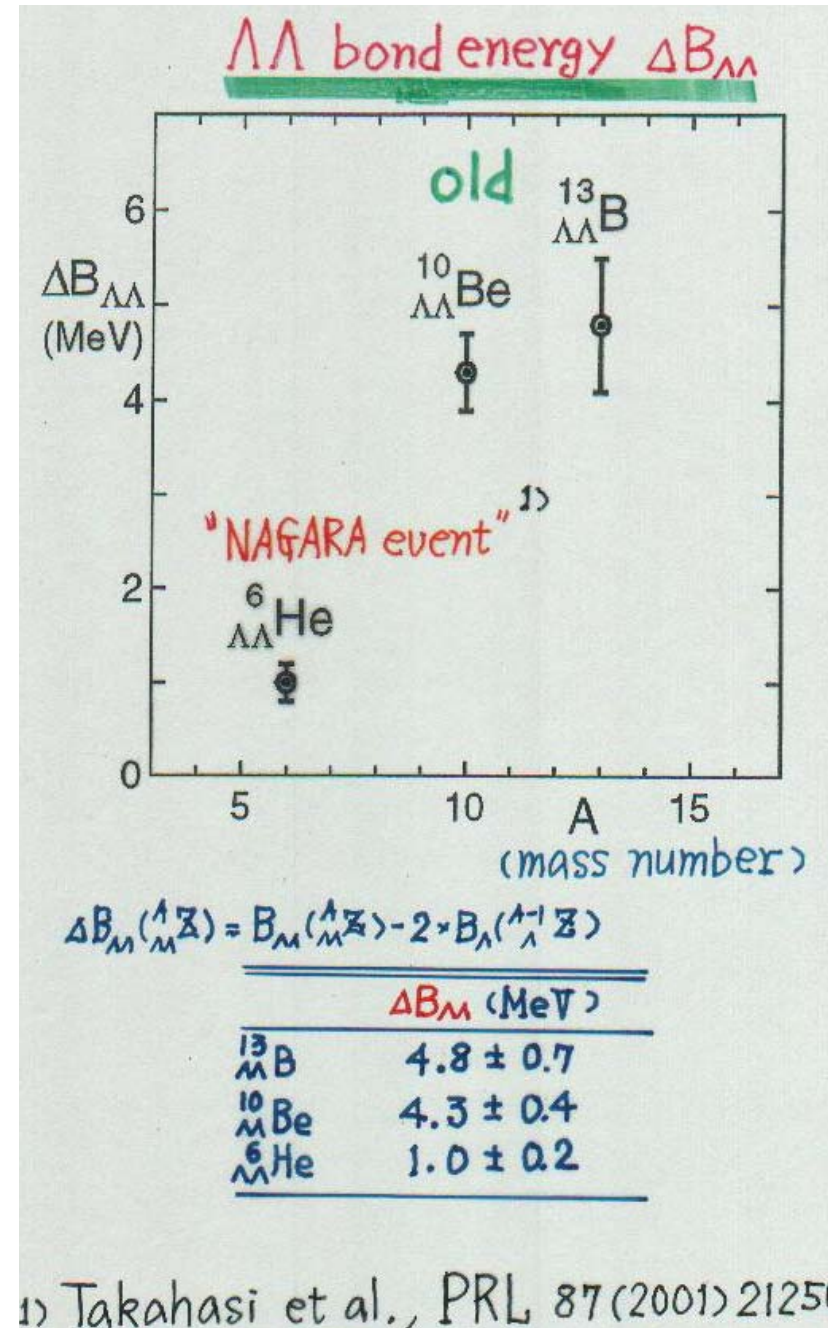


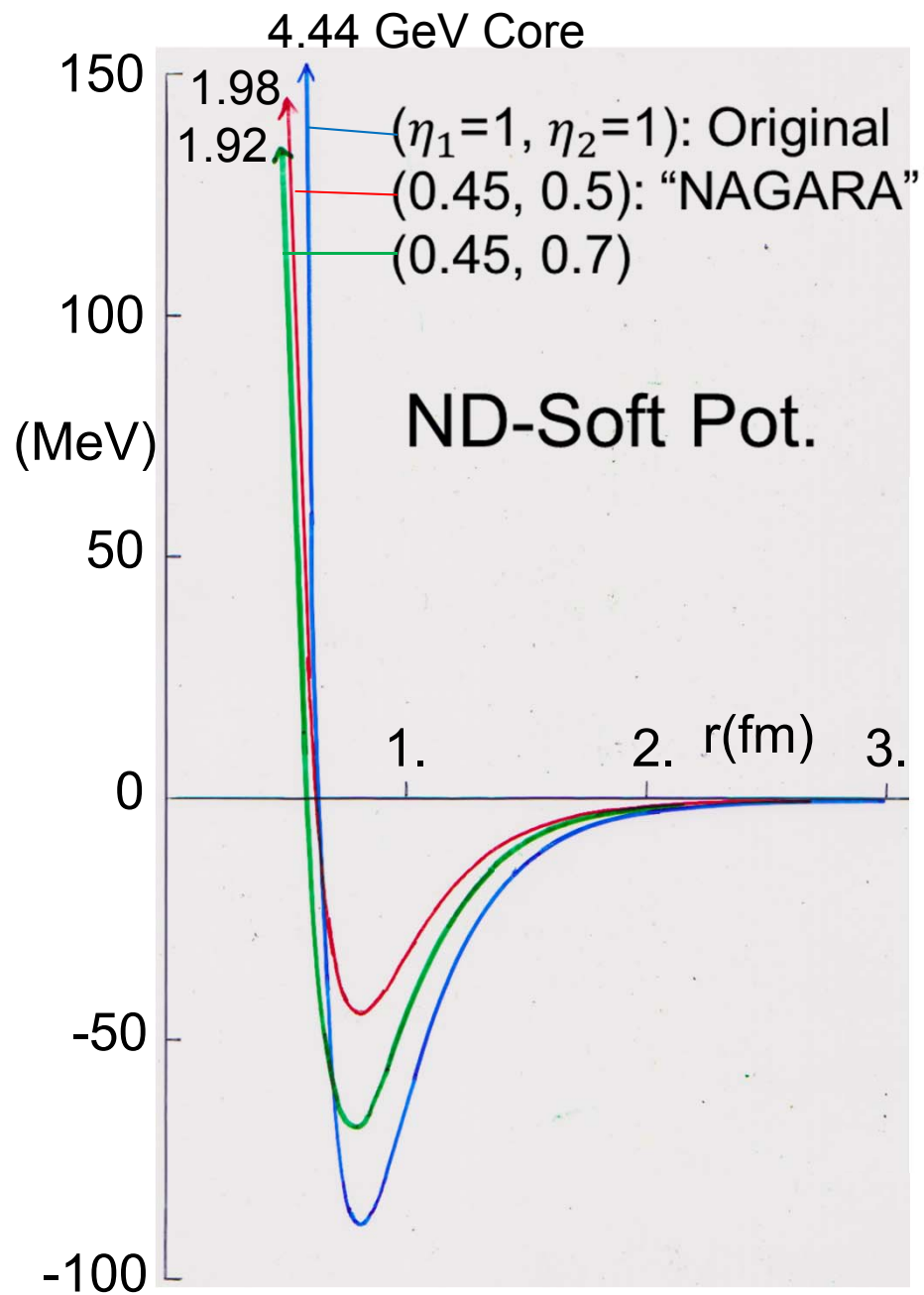
NO Λ -super \Rightarrow Too-rapid cooling \rightarrow
break down of the hyperon cooling scenario

How to overcome the problem ?

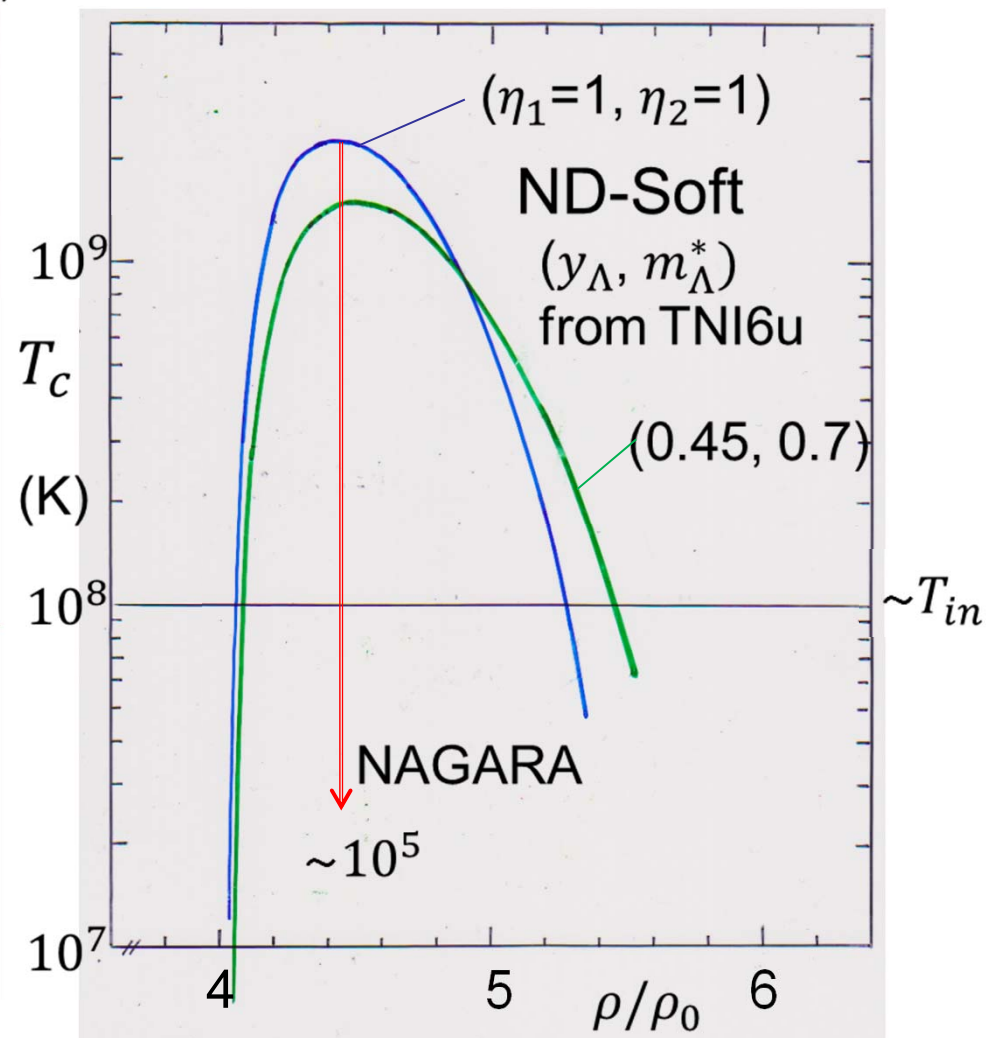
NO Λ -super due to
 “NAGARA”

- 1) “NAGARA event” → directly means “less attractive $\Lambda\Lambda$ interaction?”
- How about the **A-dependence** of $\Lambda\Lambda$ bond energy?
- Repulsive effects of 3-body force?





Critical Temperature T_c v.s. ρ



Brief summary of NS cooling

□ Cooling processes:

- Murca (modified URCA)
- cooper-pair (pair breaking-formation)
- N-Durca (direct URCA)
- Exotic (Υ, π, K, q , etc.) (Durca)

□ Observations:

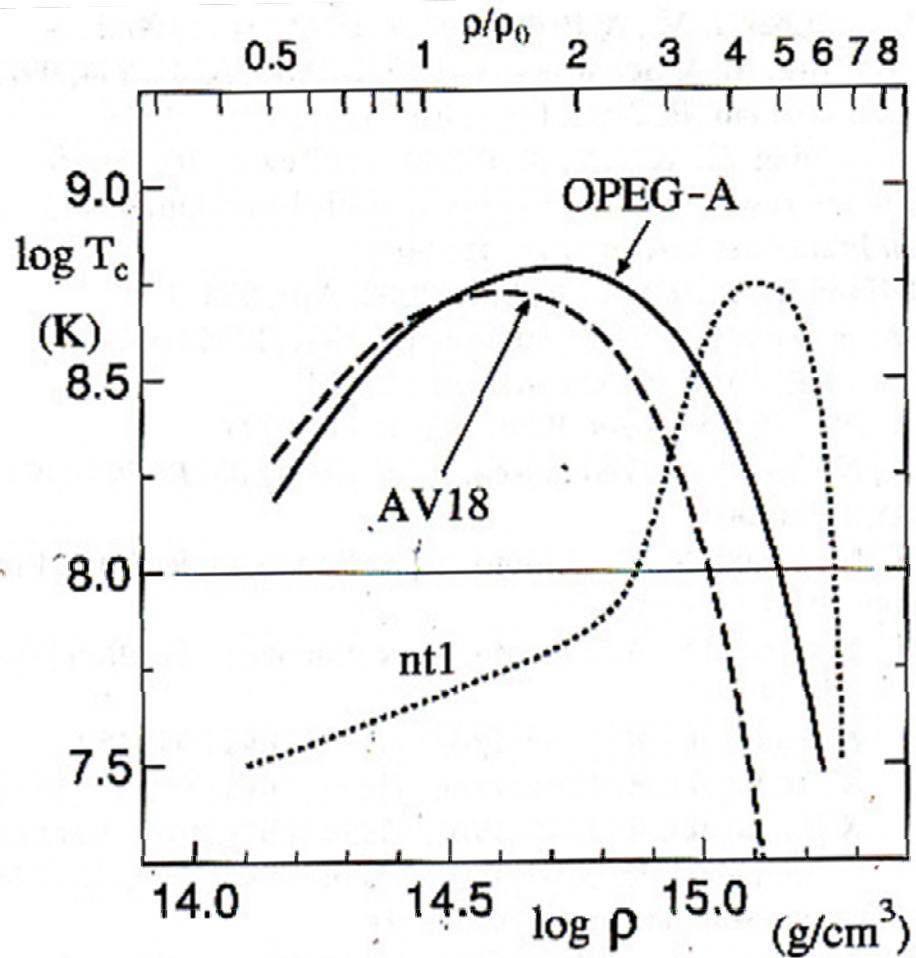
detection---about 10, upper limit---about 16

*hotter NSs(Puppis,CAS-A,RX J002+6246,PSR 0656+14, ---)

*colder NSs(Vela,3C58,CTA-1,Geminga,Vela,Vela-twin ---)

□ Cooling Model

- NO exotics(minimal) versus exotics(non-standard)
- Obs. Cold-class NSs → **necessity of exotics**
- Vela (3C58) → **exotic cooling(Υ) + superfluidity(Υ)**
- CAS-A → **evidence of 3P2-super !**



← Critical temperature of 3P2-Superfluid

○ nt1 from Gusakov, et al., A&A, 423 (2004) 1063.

○ Extraordinary density dependence of 3P2-gap

□ Summary



Theory (with exp.)		Old standard (n, p, e^- , μ^-) \rightarrow New standard (n, p, Y , e^- , μ^-)	
		Dramatically softened EOS	Extremely efficient ν -emission
Obs.		$2M_{\odot}$ -NS !	Cooler NSs !
challenges to solution and open problems	H	<ul style="list-style-type: none"> • Universal 3-body force (\rightarrowOK) • What is the origin (\rightarrow new subject) • Other candidates? 	<ul style="list-style-type: none"> • Y-Durca + Y-super (\rightarrowOK) • “NAGARA” \rightarrow NO Λ-super (\rightarrow breakdown of the scenario?) • Very sensitive to $\Lambda\Lambda$ int. (\rightarrow demands (A-dep., ? effects missing in $\Lambda\Lambda$?))
	H+Q	<ul style="list-style-type: none"> • EOS from H-Q crossover (\rightarrow OK), with conditions (proceeds at $(2-4)\rho_0$, strongly correlated q-matter) • instruction from QGP • Other possibility 	<ul style="list-style-type: none"> • Most NSs ($M \leq 1.9M_{\odot}$) are free from Y-Durca (\rightarrowOK) • How to explain cooler NSs (\rightarrow open; π cond.?) • How about ν-emission from H-Q phase? (\rightarrow new subject)

Remark: We have to solve the two serious problems **at the same time !**