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# ハイパー核生成と中性子星内部 のストレンジネス

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J-PARC Branch, KEK Theory Center

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2.  $S = -1$  Nuclei

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- $\Sigma$  hypernuclei

■ Keywords

Hyperon mixing

+  
DCX

3.  $S = -2$  Nuclei

- $\Xi$  hypernuclei
- $\Lambda\Lambda$  hypernuclei

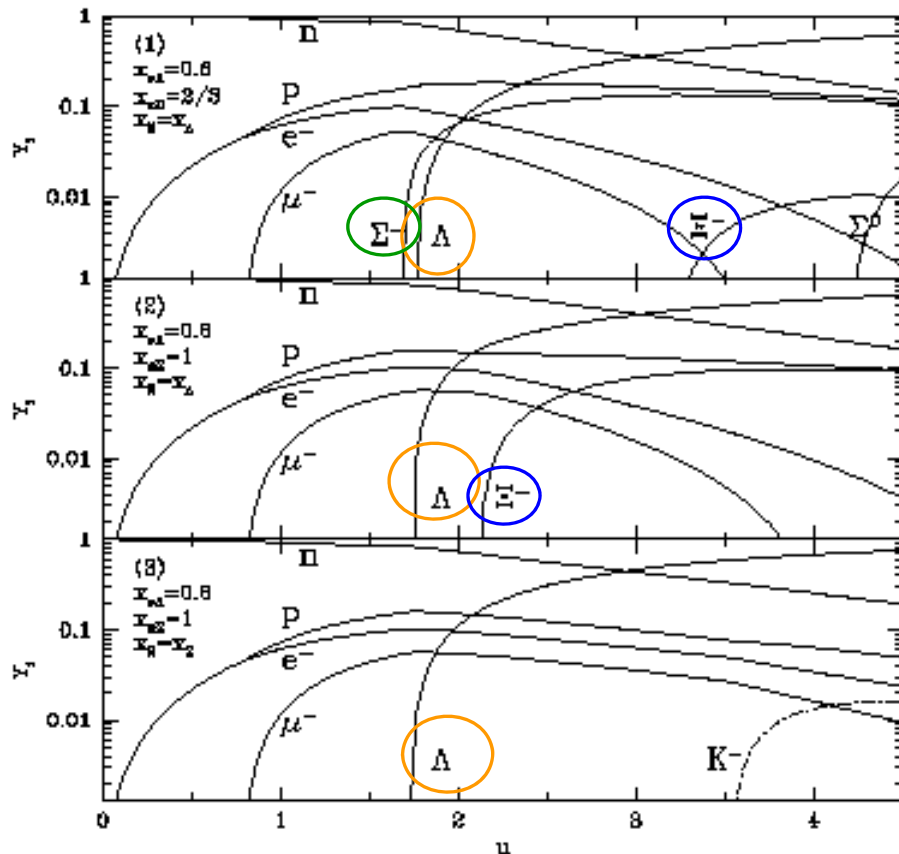
4. Deeply bound  $K^{\text{bar}}$  Nuclei

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高密度中性子星物質グループ 研究計画

# Neutron star core

= “An interesting neutron-rich hypernuclear system”

Coupling constant ratio;  $x_{iY} = g_{iY}/g_{iN}$  ( $i = \sigma, \omega, \rho$ )



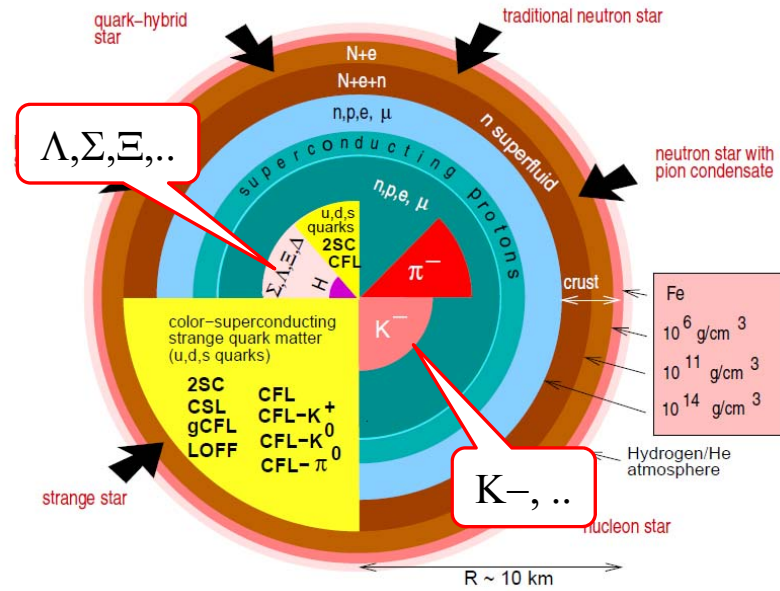
$U_\Sigma < 0$   
 $U_\Xi < 0$

$U_\Sigma > 0$   
 $U_\Xi < 0$

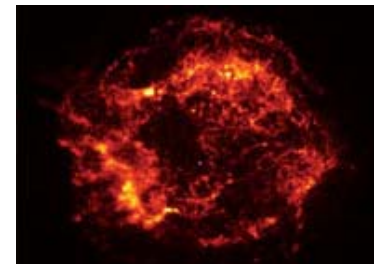
$U_\Sigma > 0$   
 $U_\Xi > 0$

[R. Knorren, M. Prakash, P.J.Ellis, PRC52(1995)3470]

**Hyperon-mixing**

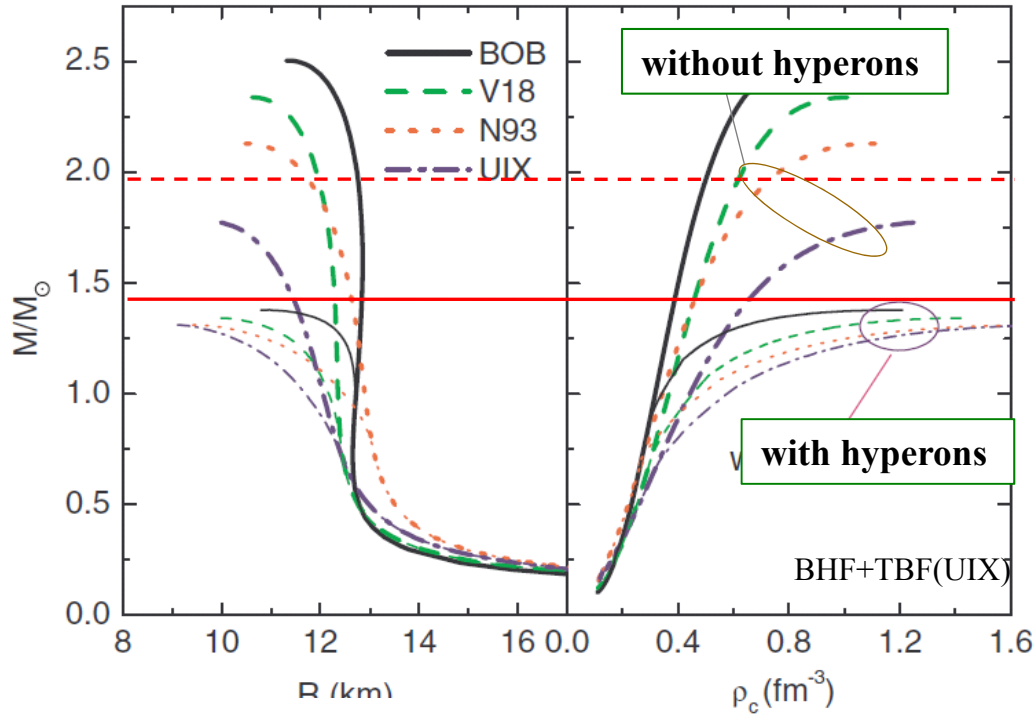


[F. Weber, PPNP 54(2005)193]



Cassiopeia A nebula  
NASA/CXC/SAO.

# Hyperons and massive neutron stars



BHF

Z.H.Li, H.-J.Schulze,  
PRC 78 (2008) 028801

$1.97 M_{\odot}$

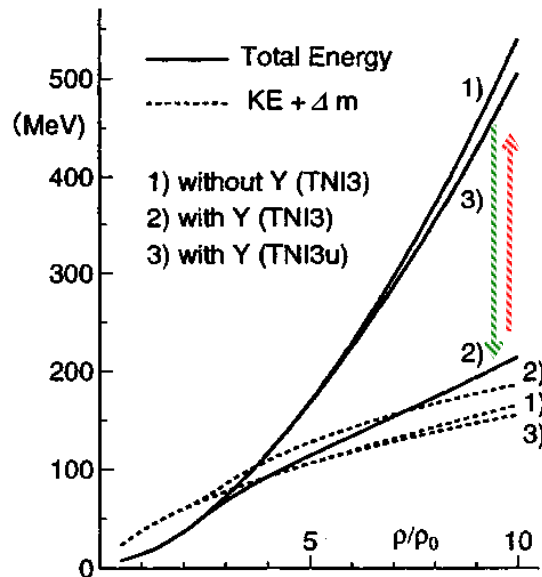
← PSR J1614-2230

$1.44 M_{\odot}$

P. B. Demorest et al.,  
Nature 467 (2010) 1081

**Maximum Mass/Radius**

**Softening on the EOS**



**YN,YY: extra repulsion TNIu**

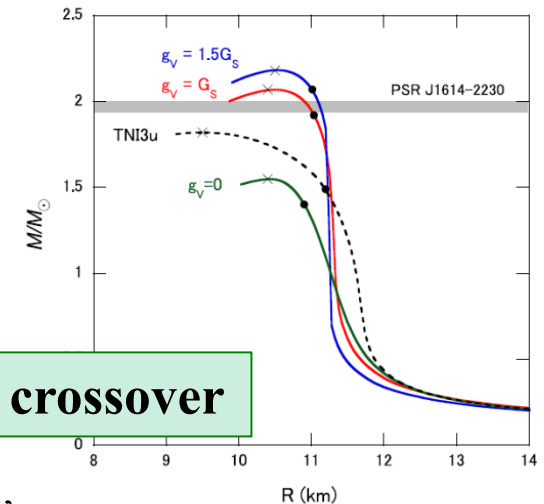
S. Nishizaki, T. Takatsuka, Y. Yamamoto,  
PTP105(2001)607; NPA691(2001)432

短距離斥力をハイペ  
ロン混合により回避

$$n_c(Y) \approx (2-3)n_0$$

**Hadron-Quark crossover**

K. Masuda, et al.,  
arXiv:1205.3621v2 [nucl-th]



# Thermal evolution of neutron stars

Rapid neutrino emission  
via weak processes  
(Direct/Modified Uruga)

$$\Lambda \rightarrow p + e^- + \bar{\nu}_e$$

$$\Sigma^- \rightarrow \Lambda + e^- + \bar{\nu}_e$$

➤ Cooper pair

$^1S_0$  [iner crust]

$^3P_2$ - $^3F_2(n)$ ,  $^1S_0(p)$  [core]

➔ Standard cooling

➤ YY pairing

➔ Hyperon cooling

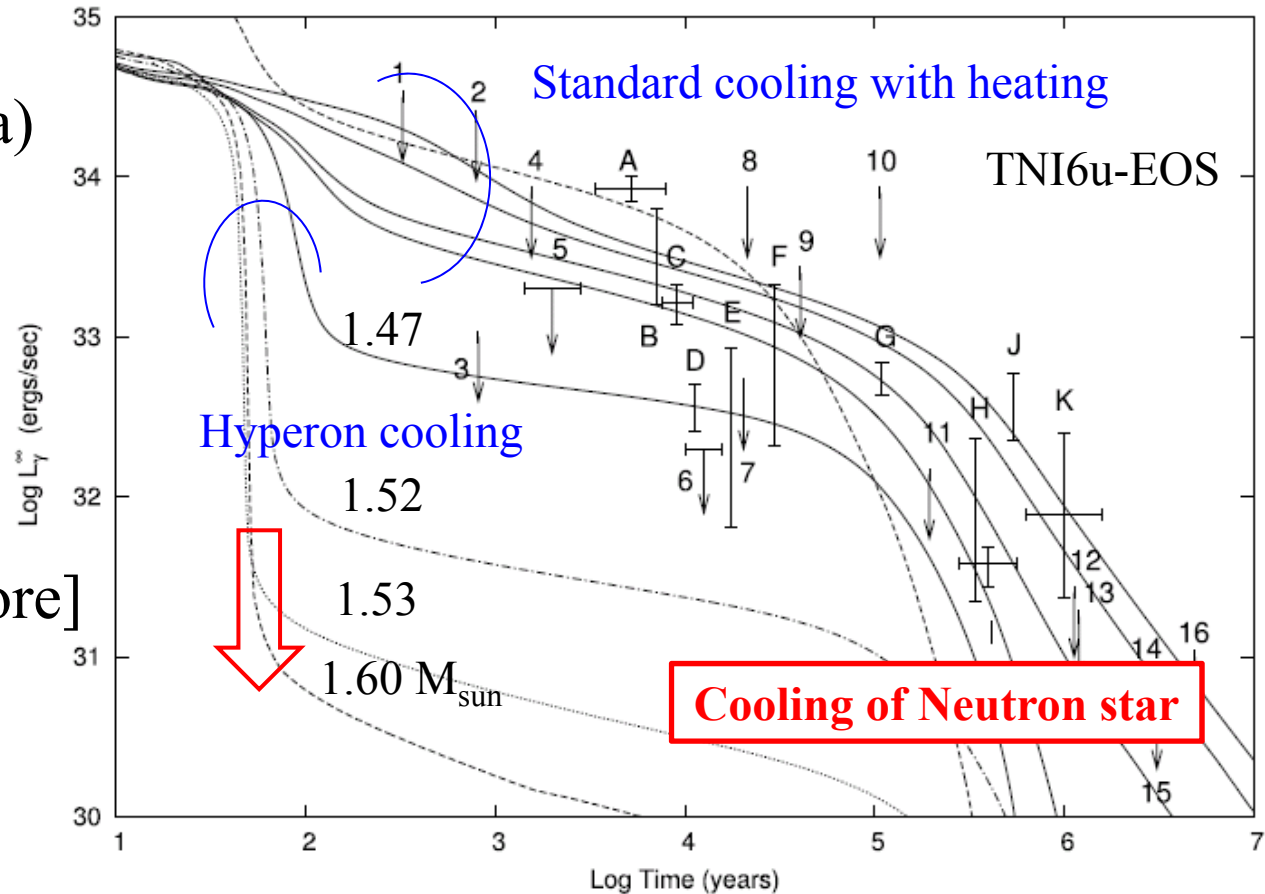
Cooling relaxation?

➤ Hyperon superfluidity v.s. YY interactions

Nagara event  $\Delta B_{\Lambda\Lambda} \sim 0.67$  MeV ➔ no  $\Lambda\Lambda$  superfluidity ?

➡ very sensitive to properties of YN, YY interactions

[S. Tsuruta et al., Astrophys. J 691(2009)621]



# NN, YN, YY Interactions

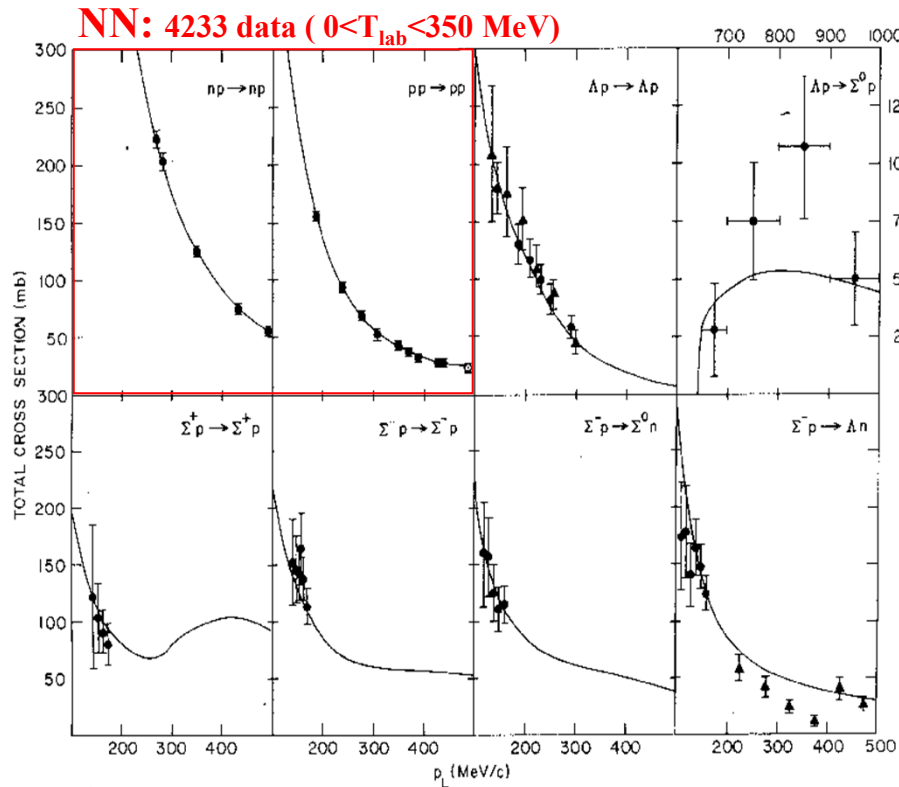
Flavor  $SU(3)_f$  symmetry

symmetric

antisymmetric

C.B. Dover and H. Feshbach,  
Ann. Phys. 198(1990)321

$$[8] \otimes [8] = [27] \oplus [10^*] \oplus [10] \oplus [8_s] \oplus [8_a] \oplus [1]$$



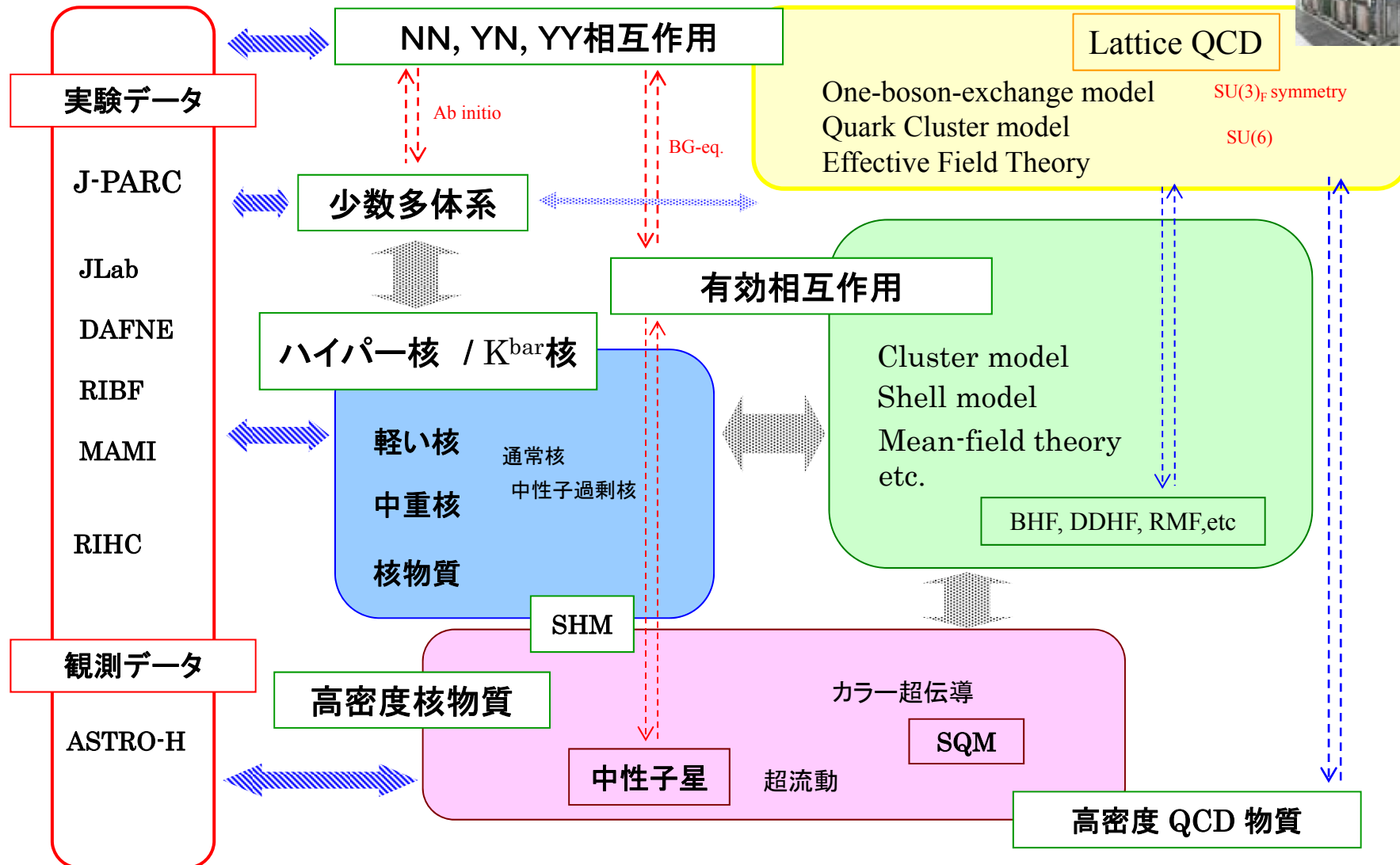
$^1S_0$	$^3S_1$	$\Lambda\Lambda$
NN	NN	S = 0
$\Sigma N, \Sigma N - \Lambda N, \Lambda N$	<b>35 data</b>	S = -1
$\Sigma\Sigma, \Xi N - \Sigma\Lambda - \Sigma\Sigma, \Xi N - \Sigma\Sigma - \Lambda\Lambda$		S = -2
$\Xi\Sigma, \Xi\Sigma - \Xi\Lambda$		S = -3
$\Xi\Xi$	$\Xi\Xi$	S = -4

- One-Boson-Exchange model
- Quark Cluster model
- Chiral LO Effective Field Theory
- Lattice QCD

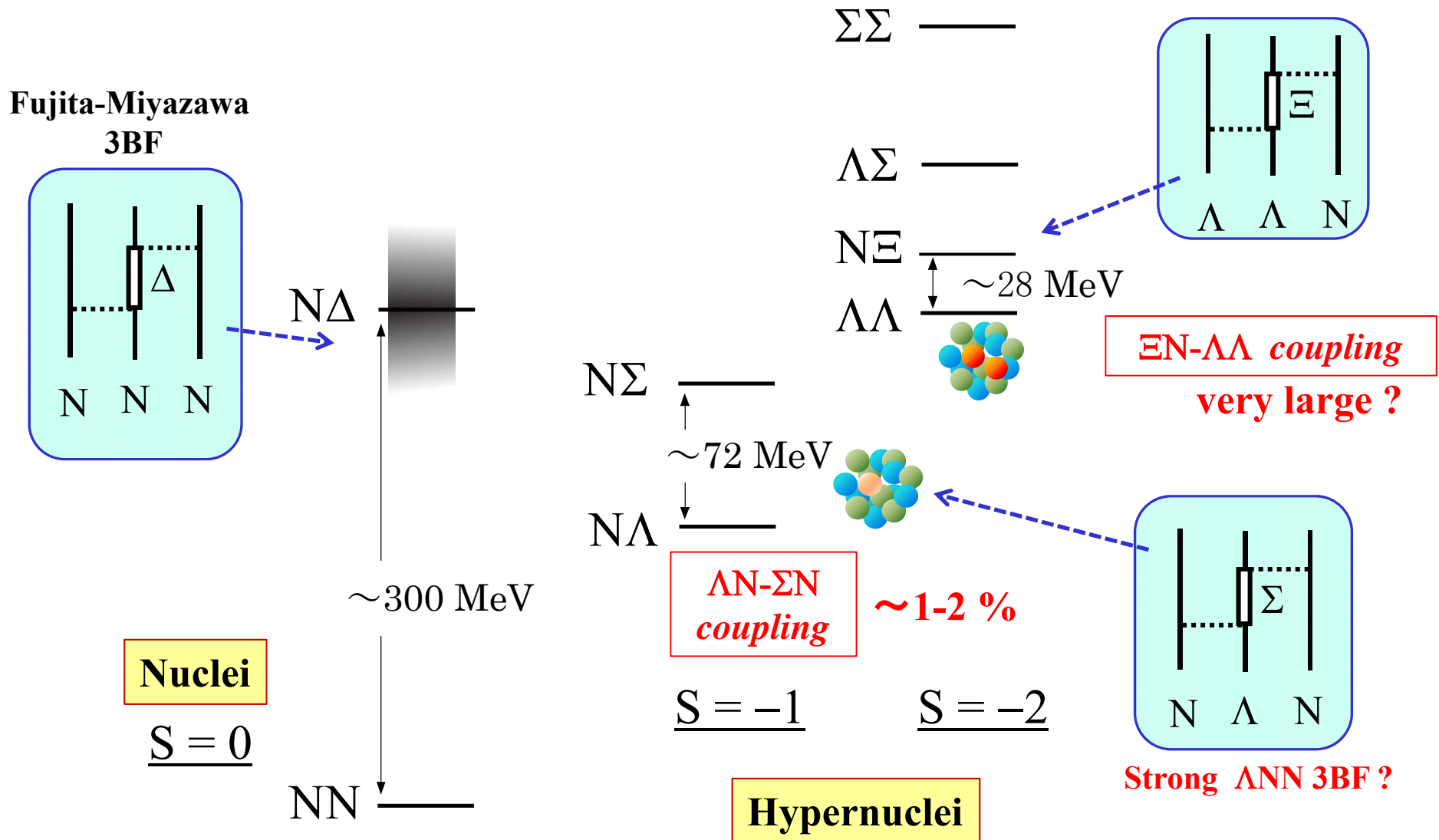
# ストレンジネス核物理の展開

by E.Hiyama

“QCD,核力から核構造へ”と“核構造からQCD,核力へ”



# Dynamics in Strangeness Nuclear Systems



- Various effects on the hyperon mixing
- Related to the 3BF in nuclei



# ストレンジネス核物理

## ➤ ストレンジネスは原子核深部を探るプローブ

– ハイペロンはパウリ排他律を受けない

## ➤ Impurity Physics

– “糊”としての役割

– 原子核構造の変化

■ Keywords

Hyperon mixing

## ➤ Baryon-Baryon Interaction

– YN, YY Interaction based on  $SU_f(3)$

– 核力の統一的理解・斥力芯の起源

## ➤ “Exotic” Nuclear Physics

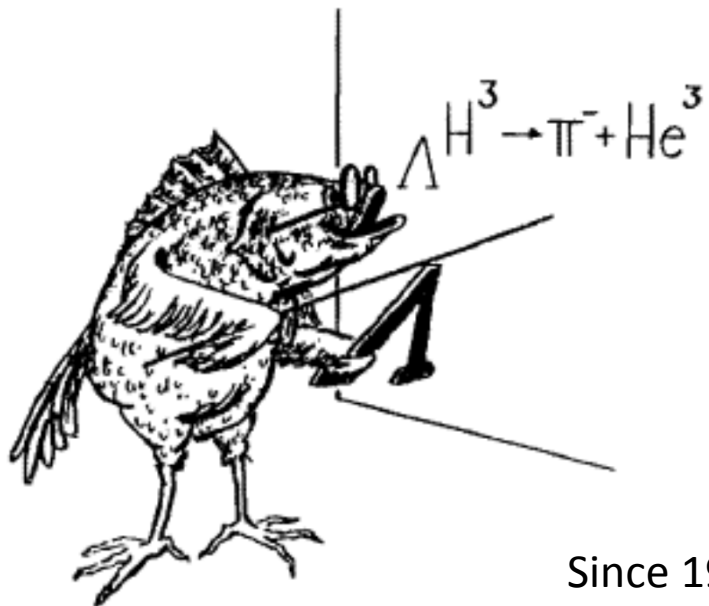
– ストレンジネスが拓く新しい原子核の面白さ

## ➤ Neutron Starの構造と進化

– 高密度核物質, EOS, 最大質量, 冷却, ...

← Serious Problems from hyperon-mixing (Takatsuka)

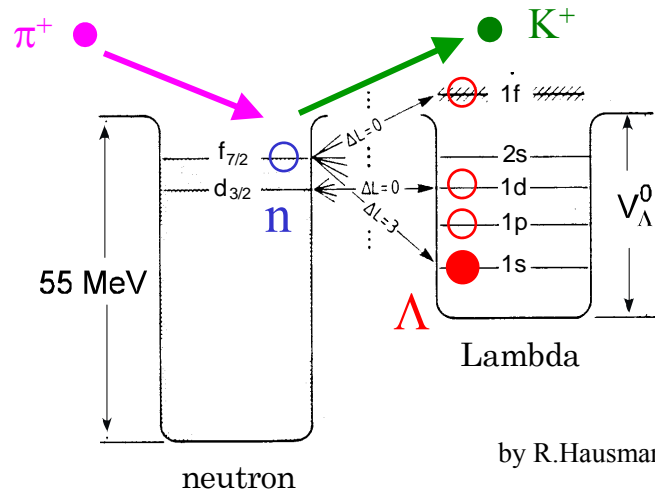
## 2. $S = -1$ Nuclei



Since 1969, ANL

# Hypernuclear Production Reactions

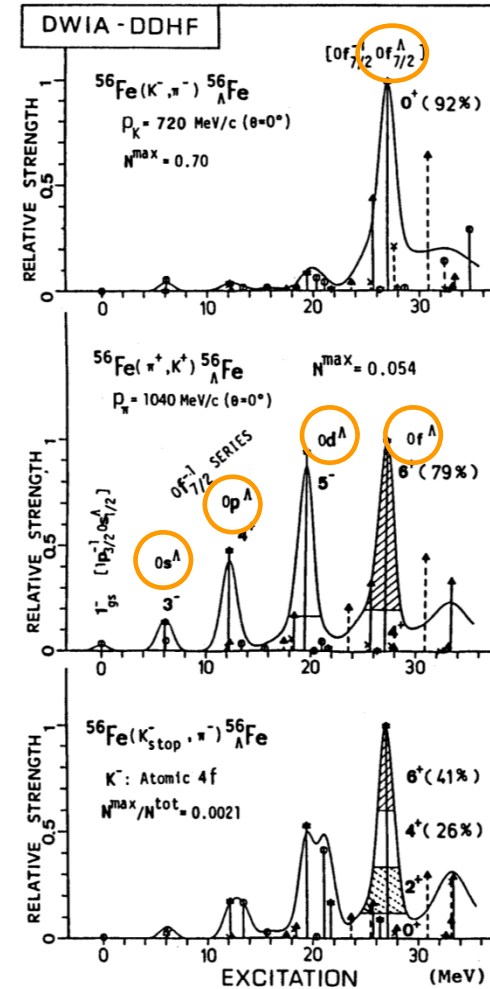
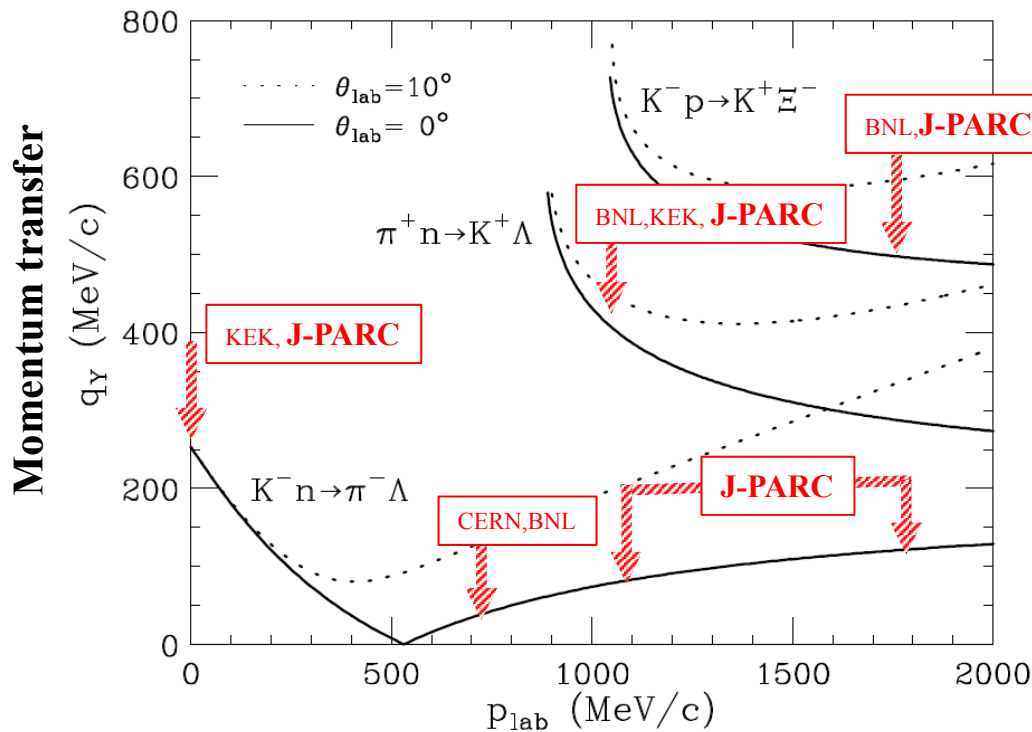
( $\pi^+, K^+$ ) reaction



Theoretical calculations

$^{56}\text{Fe}$  target

H.Bando, T.Motoba, J.Zofka, Int.J.Mod.Phys. A5(1990)4021

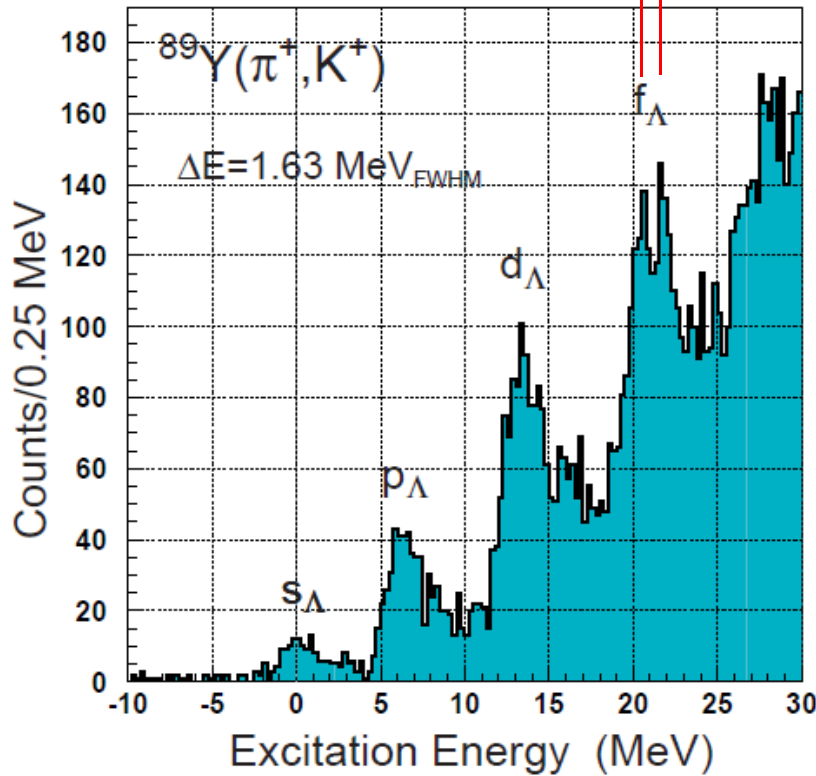


- ( $K^-, \pi^-$ )**  
720 MeV/c  
 $q_\Lambda \sim 60-100 \text{ MeV}/c$   
"Substitutional"  
 $\Delta l \approx 0$
- ( $\pi^+, K^+$ )**  
1040 MeV/c  
 $q_\Lambda \sim 400 \text{ MeV}/c$   
"Spin-Stretched"  
 $[(nlj)_N^{-1} (nlj)_\Lambda]_J$   
 $[J_{N < J_\Lambda}^{-1}]_{J=J_{\max}}$
- ( $K^-, \pi^-$ )**  
Stooped K-  
 $q_\Lambda \sim 280 \text{ MeV}/c$

# $\Lambda$ s.p. potential and $\Lambda$ spin-orbit splitting in $^{89}_{\Lambda}\text{Y}$

H. Hotchi et al.,  
PRC64(2001)044302

KEK E369 (Exp.) 1.7 MeV

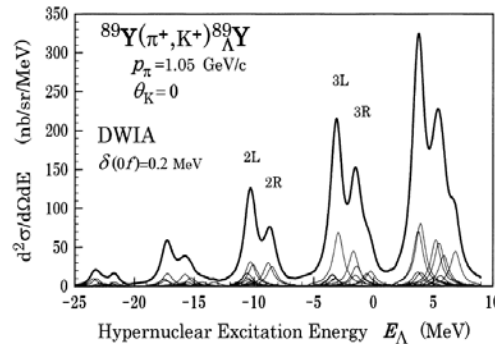


T. Motoba et al.,  
PTPS185(2010)197

SM analysis

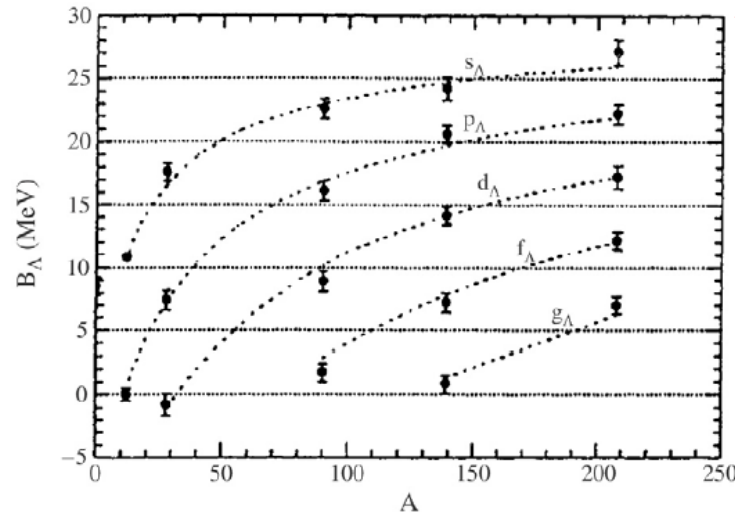
- $\Lambda N^{-1}$  particle-hole ex.
- inter-shell coupling

$$V_{LS}^{\Lambda} \simeq 0.2 \text{ MeV}$$



$$U_{\Lambda} = V_0^{\Lambda} f(r) + V_{LS}^{\Lambda} \left( \frac{\hbar}{m_{\pi} c} \right)^2 \frac{1}{r} \frac{df(r)}{dr} l s$$

$V_{\Lambda} ?$



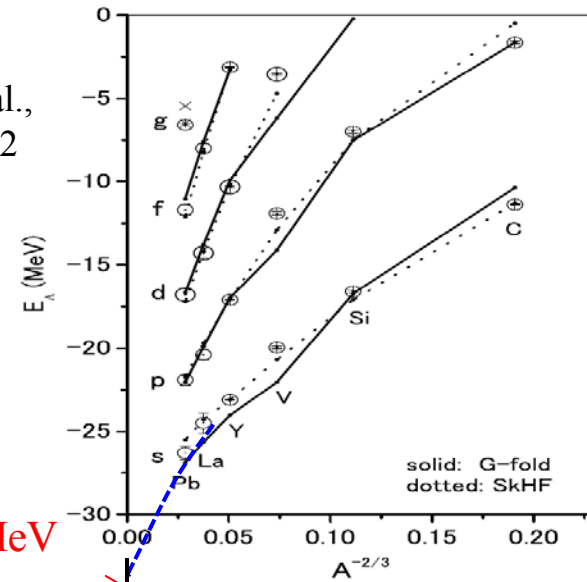
[O. Hashimoto, T. Tamura, PPNP57(2006)564]

Y. Yamamoto et al.,  
PTPS185(2010)72

G-matrix  
folding model

$$V_0^{\Lambda} \simeq -37.2 \text{ MeV}$$

( $A \rightarrow \infty$ )



# Role of the $\Lambda$ -hyperon in nuclei

“gule”

T. Motoba, et al.,PTP70(1983)189  
E. Hiyama, et al.,PRC59(1999)2351

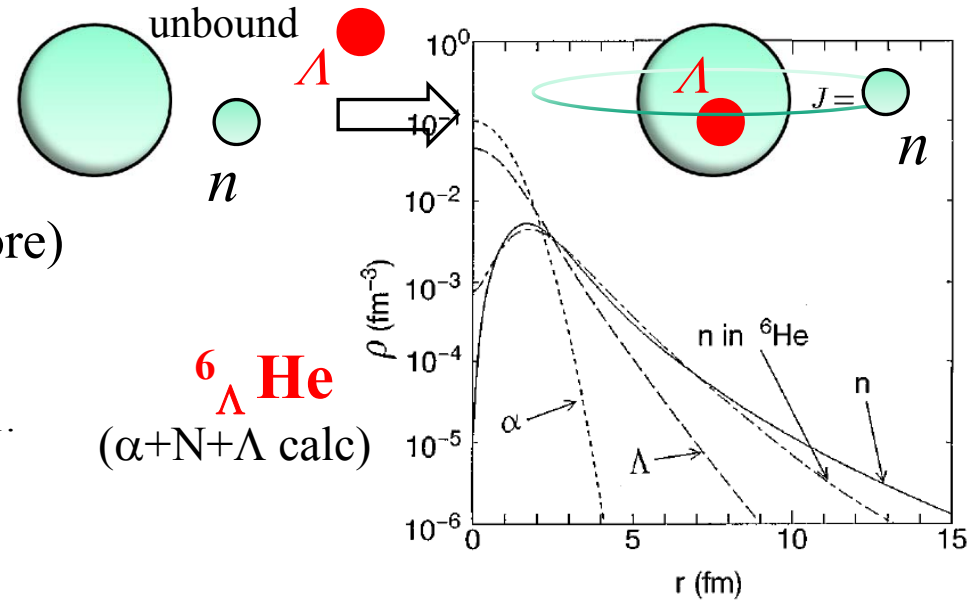
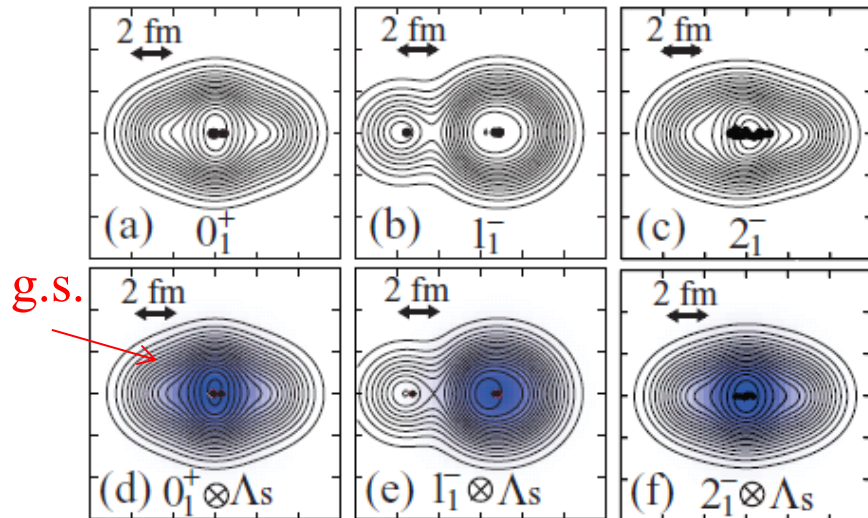
- Shrinkage effects (19% for the  ${}^6\text{Li}$  core)
- neutron-skin or neutron halo

E. Hiyama, et al.,PRC59(1999)2351  
Tretyakova, Lanskoj, EPJ.A5(1999) 391.

“Stabilizing”+“Deformation”

${}^{21}_{\Lambda}\text{Ne}$ ,  ${}^{25}_{\Lambda}\text{Mg}$  (AMD)

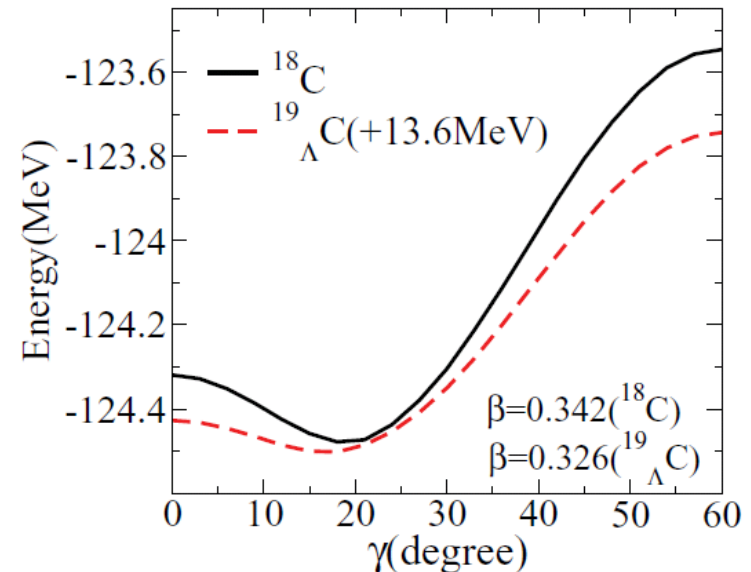
M. Isaka et al, PRC83(2011)054304



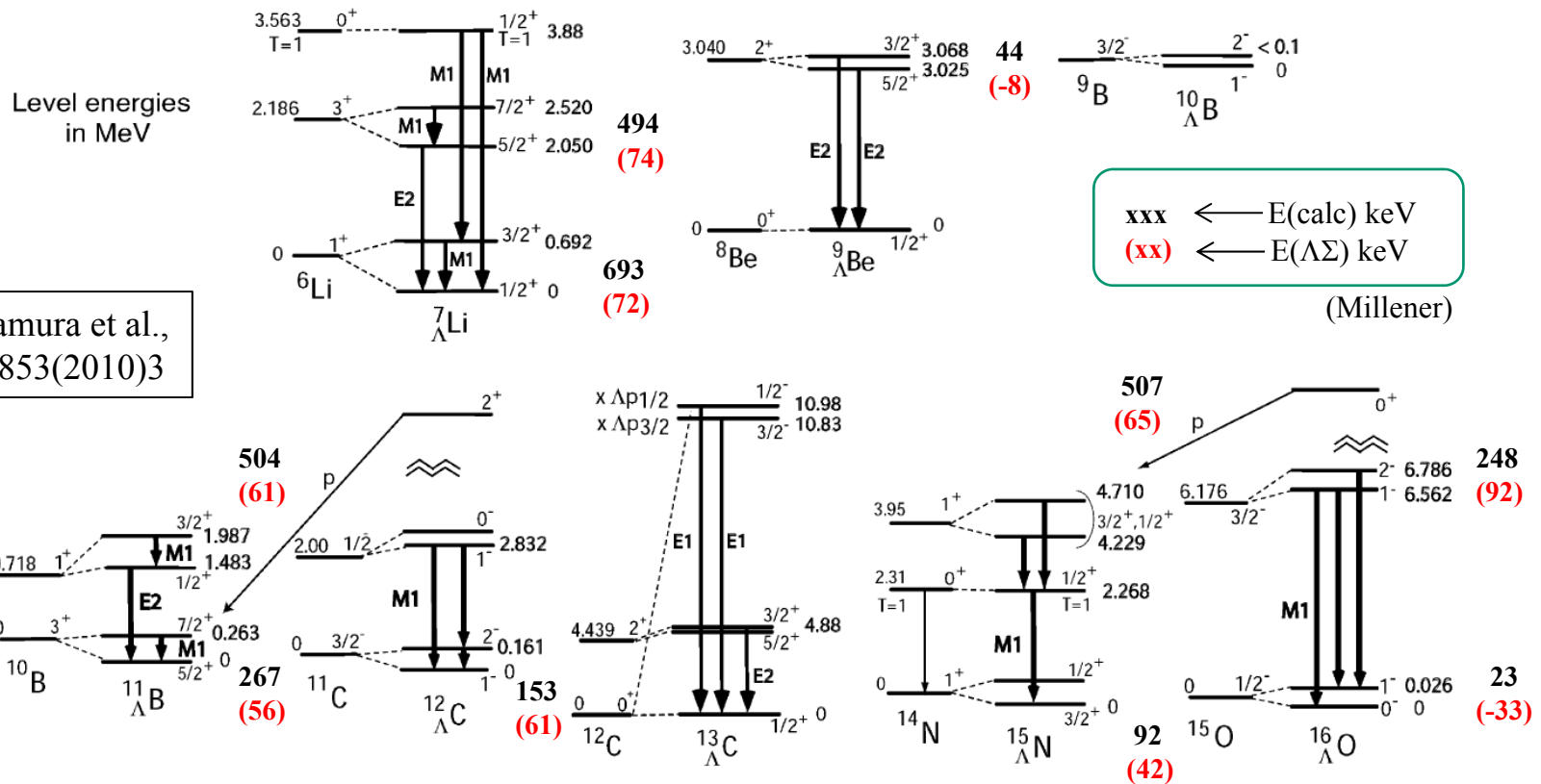
${}^6_{\Lambda}\text{He}$   
( $\alpha+N+\Lambda$  calc)

${}^{19}_{\Lambda}\text{C}$ ,  ${}^{29}_{\Lambda}\text{Si}$ ,  ${}^{25}_{\Lambda}\text{Mg}$ , (CSHF+BCS)

M.T. Win, K.Hagino et al, PRC83 (2011) 014301



# Gamma-ray spectroscopy of light hypernuclei



## Spin-dependence of the effective $\Lambda N$ interaction

[R.H.Dalitz, A.Gal, AnnPhys.116(1978)167]

$$V_{\Lambda N} = \bar{V} + \Delta \vec{s}_N \cdot \vec{s}_\Lambda + S_\Lambda \vec{l}_N \cdot \vec{s}_\Lambda + S_N \vec{l}_N \cdot \vec{s}_N + T S_{12}$$

## Microscopic Shell-Model

$A = 7,9$     $\Delta = 430$ ,  $S_\Lambda = -15$ ,  $S_N = -390$ ,  $T = 30$  (keV)   including  $\Lambda N$ - $\Sigma N$  coupling effects  
 $A > 9$     $\Delta = 330$ ,  $S_\Lambda = -15$ ,  $S_N = -350$ ,  $T = 23.9$  (keV)   [D.J.Millener,NPA835(2010)11]

## E13@J-PARC

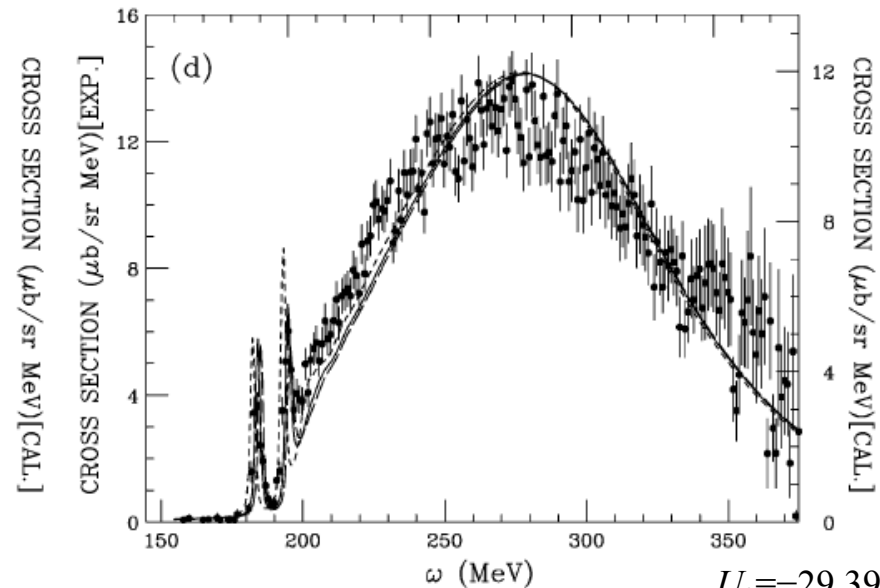
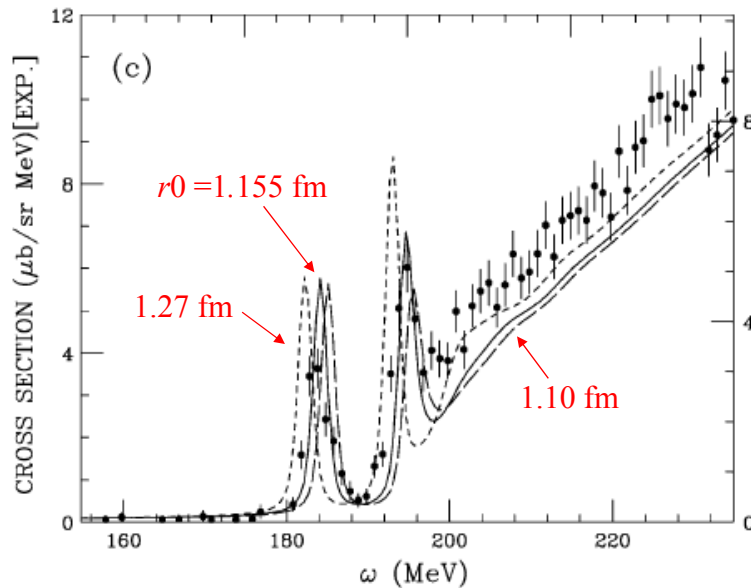
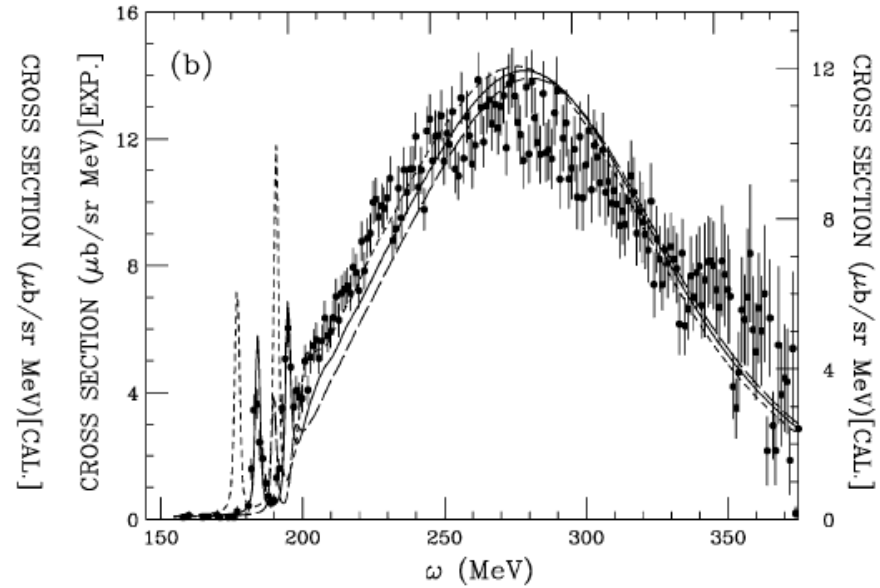
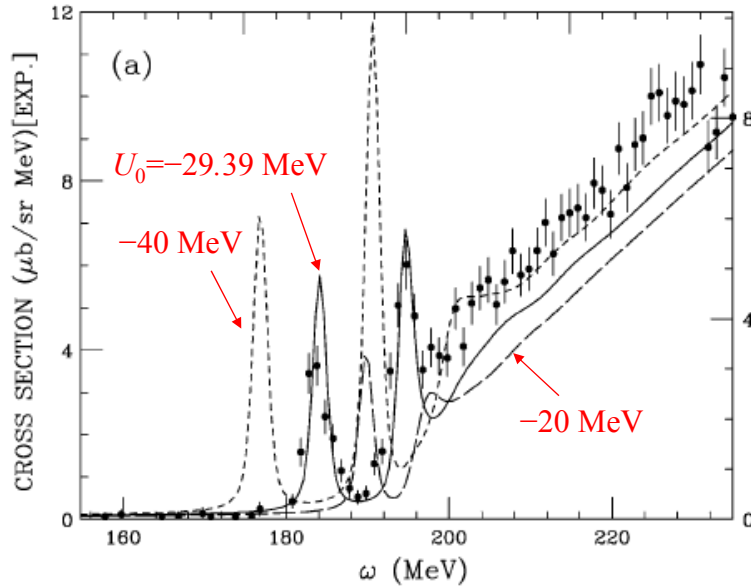
- $\Lambda N$  spin-dependent force/ $\Lambda N$ - $\Sigma N$  coupling force/Charge symmetry breaking ( $\Lambda p \neq \Lambda n$ )
- Magnetic moments  $\mu_\Lambda$  in a nucleus from B(M1)  ${}^4_\Lambda\text{He}$ ,  ${}^{10}_\Lambda\text{B}$ ,  ${}^{11}_\Lambda\text{B}$ ,  ${}^{19}_\Lambda\text{F}$

# $\Lambda$ spectrum by $(\pi^+, \text{K}^+)$ reaction at 1.2 GeV/c ( $6^\circ$ )

Harada, Hirabayashi, NPA744 (2004) 323.

Sensitivity of the spectrum to the  $\Lambda$ -nucleus potential parameters

$r_0 = 1.155$  fm



$U_0 = -29.39$  MeV

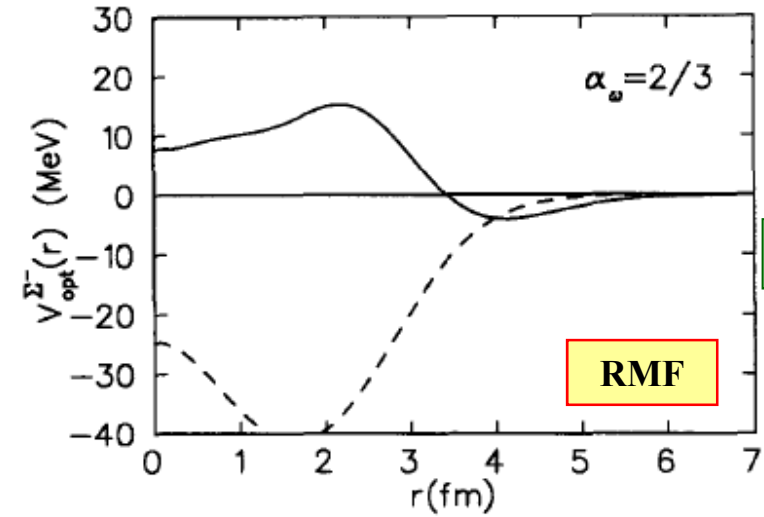
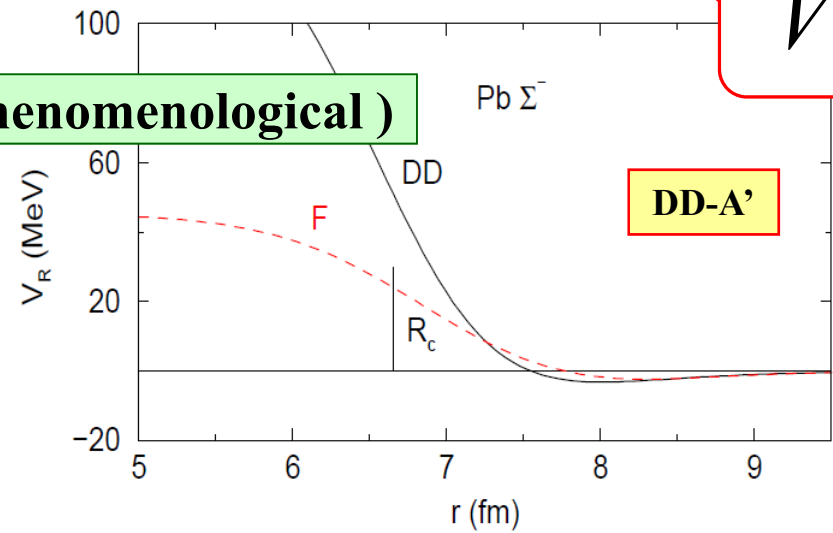


# $\Sigma^-$ s.p. potentials (fitted to the $\Sigma^-$ atomic data)

$V_{\Sigma} ?$

## Density-dependent (DD) potential (Phenomenological)

C.J.Batty et al., Phys.Rep.287(1997)385,  
E. Friedman and A. Gal, Phys. Rep. 452 (2007)89.

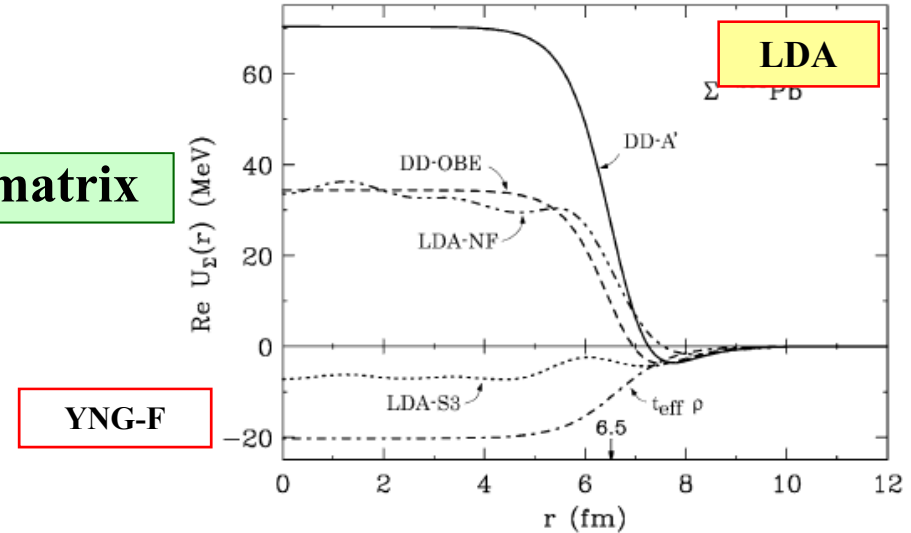


## Relativistic mean-field (RMF) potential

J. Mares et al., NPA594(1995)311.  
K.Tsubakihara et al., EPJA33(2007)295

## Folding-model potential for LDA with G-matrix

D. Halderson, Phys. Rev. C40(1989)2173.  
T.Yamada and Y.Yamamoto, PTP. Suppl. 117(1994)241  
J. Dabrowski, Acta Phys. Pol. B31(2001)2179  
T.Harada, Y.Hirabayashi, NPA759 (2005) 143; 767(2006)206



YNG-F

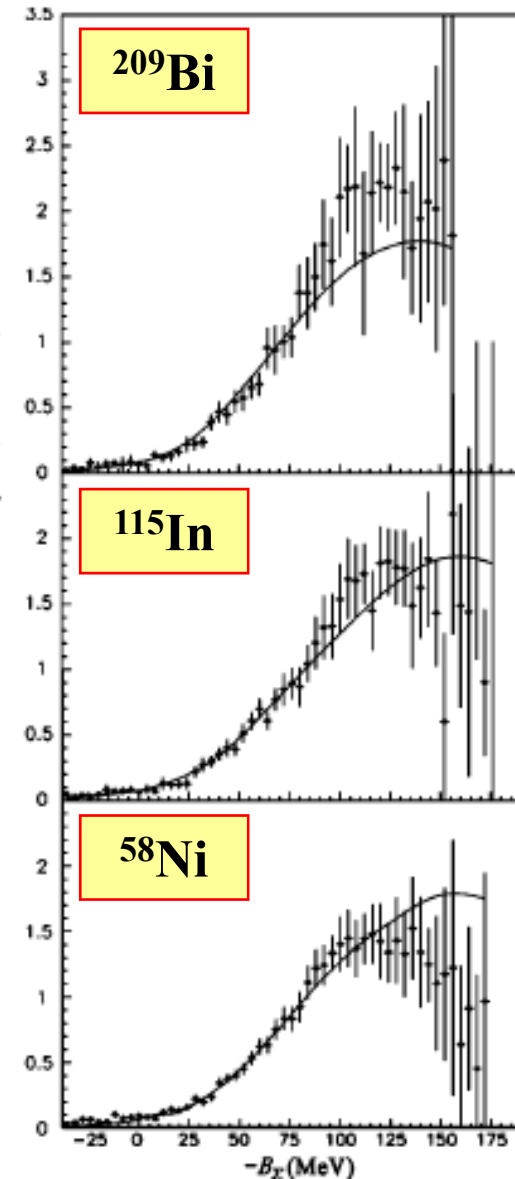
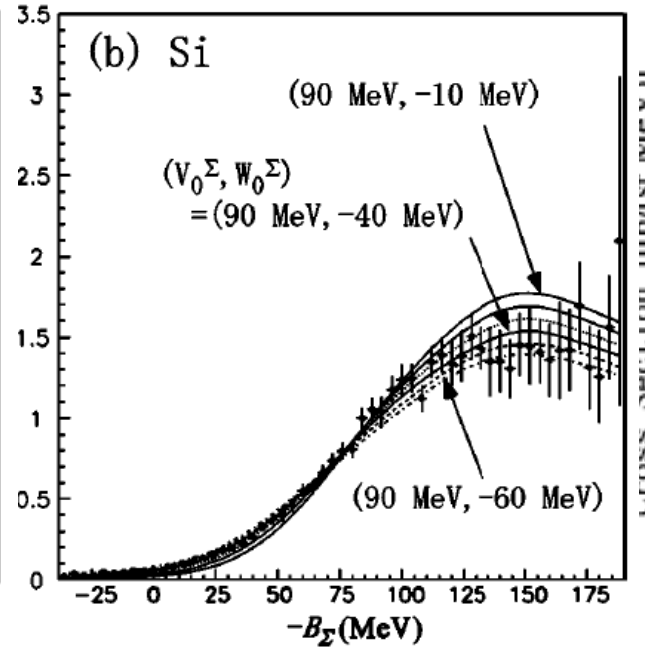
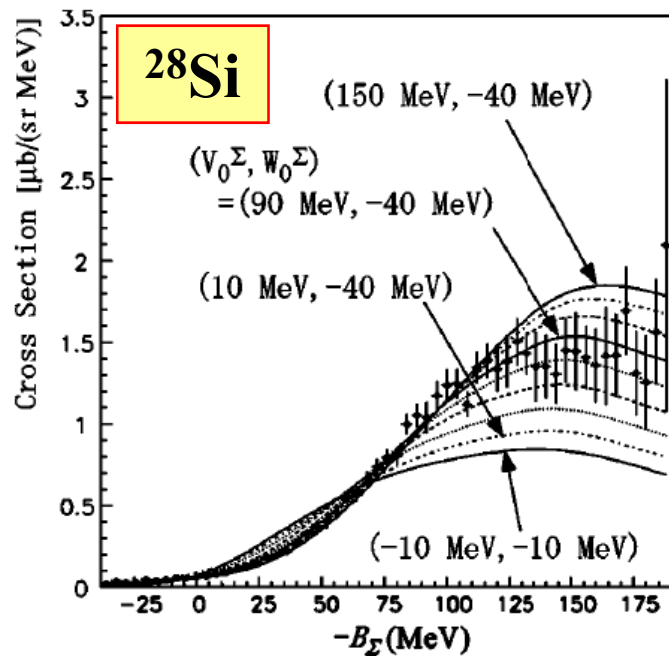
➤ It suggests that  $\Sigma$ -nucleus potentials have a strong repulsion in the real part.



# $\Sigma^-$ spectrum by $(\pi^-, K^+)$ reaction at 1.2 GeV/c

Study of  $\Sigma$  s.p. potentials for heavier targets

[H.Noumi, et al. PRL89(2002)072301]  
 [P.K.Saha, et al., PRC70(2004)044613]



Woods-Saxon form

$$U_{\Sigma} = \frac{V_{\Sigma} + iW_{\Sigma}}{1 + \exp[(r - R)/a]}$$

$$R = r_0(A-1)^{1/3} \text{ fm}$$

$$a = 0.67 \text{ fm} \quad r_0 = 1.1 \text{ fm}$$



$$V_{\Sigma} = +90 \text{ MeV}$$

$$W_{\Sigma} = -40 \text{ MeV}$$

**Strong repulsion with large imaginary**

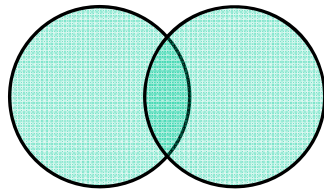
# Short-range repulsive core in baryon-baryon interaction

Spin-flavor SU(6) symmetry

Quark Cluster Model

M.Oka,K.Shimizu,K.Yazaki, PLB130(1983)365; NPA464(1987)700

Quark-exchange  
(anti-symmetrized)



symmetric

antisymmetric

$$[3] \otimes [3] = [6] \oplus [42] \oplus [51] \oplus [33]$$

orbital x flavor-spin x color singlet  $\downarrow L=0$

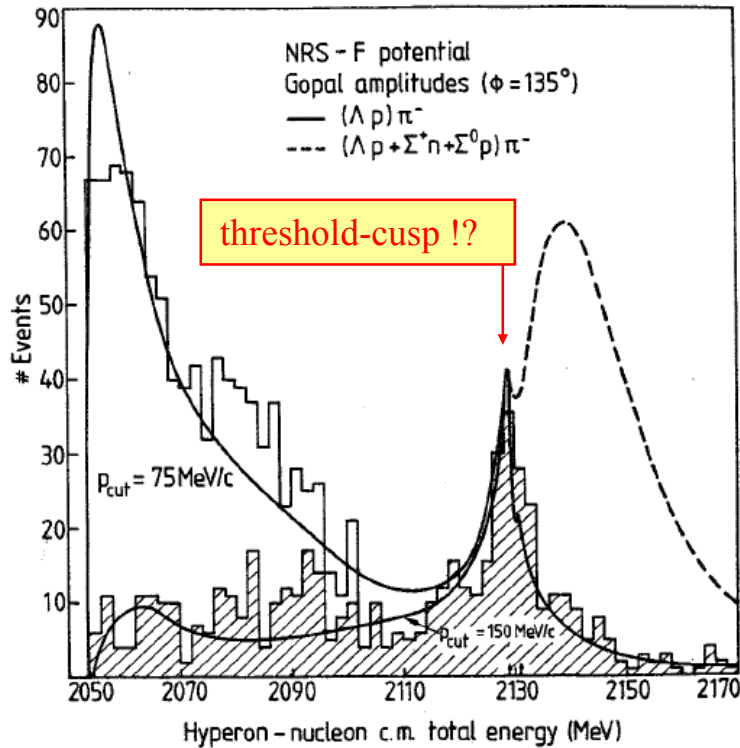
*Pauli forbidden state*

S = 0 state	[51]	[33]	
1			$\Lambda\Lambda$ - $\Xi N$ - $\Sigma\Sigma(I=0)$ , H-dibaryon
$8_s$	<b>1</b>		$\Sigma N(I=1/2, ^1S_0)$ <i>Pauli forbidden</i>
27	4/9	5/9	$NN(^1S_0)$
S = 1 state	[51]	[33]	
$8_A$	5/9	4/9	
10	<b>8/9</b>	1/9	$\Sigma N(I=3/2, ^3S_1)$ <i>almost Pauli forbidden</i>
10*	4/9	5/9	$NN(^3S_1)$ , $\Lambda N$ - $\Sigma N(I=1/2, ^3S_1)$

E40@J-PARC:  $\Sigma^+p$  Scattering

➤ SU(6)<sub>sp</sub> symm. → Strongly spin-isospin dependence

# $K^-d \rightarrow \pi^- \Lambda p$ Reaction in Flight



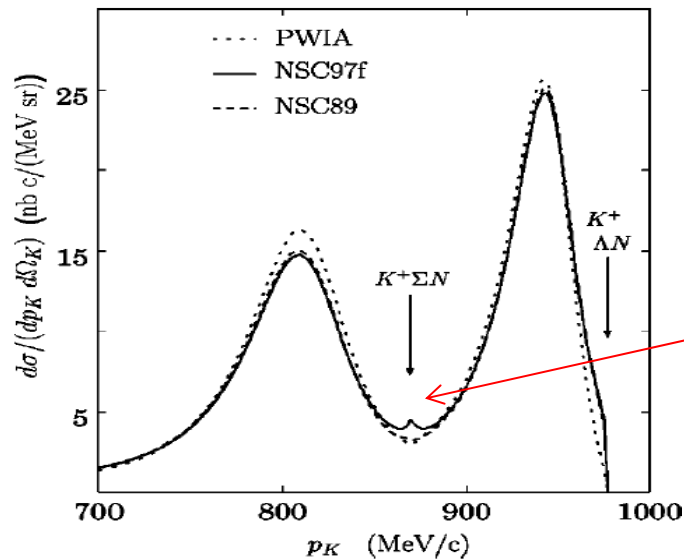
**$\Sigma N \ ^3S_1 [10^*]$ :  
“Strangeness partner of deuteron”**

R.H.Dalitz, A. Deloff,  
Aust. J. Phys., 36 (1983) 617

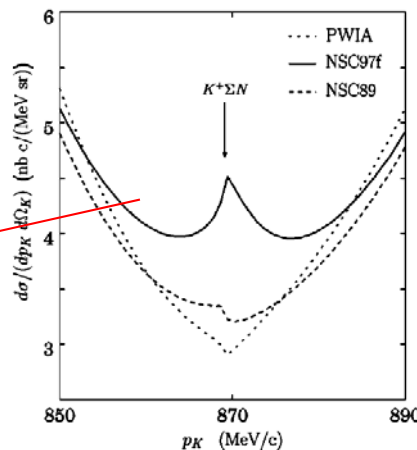


R.H.Dalitz

NHC-F



# $d(\gamma, K^+)$ spectrum near the $\Sigma N$ threshold

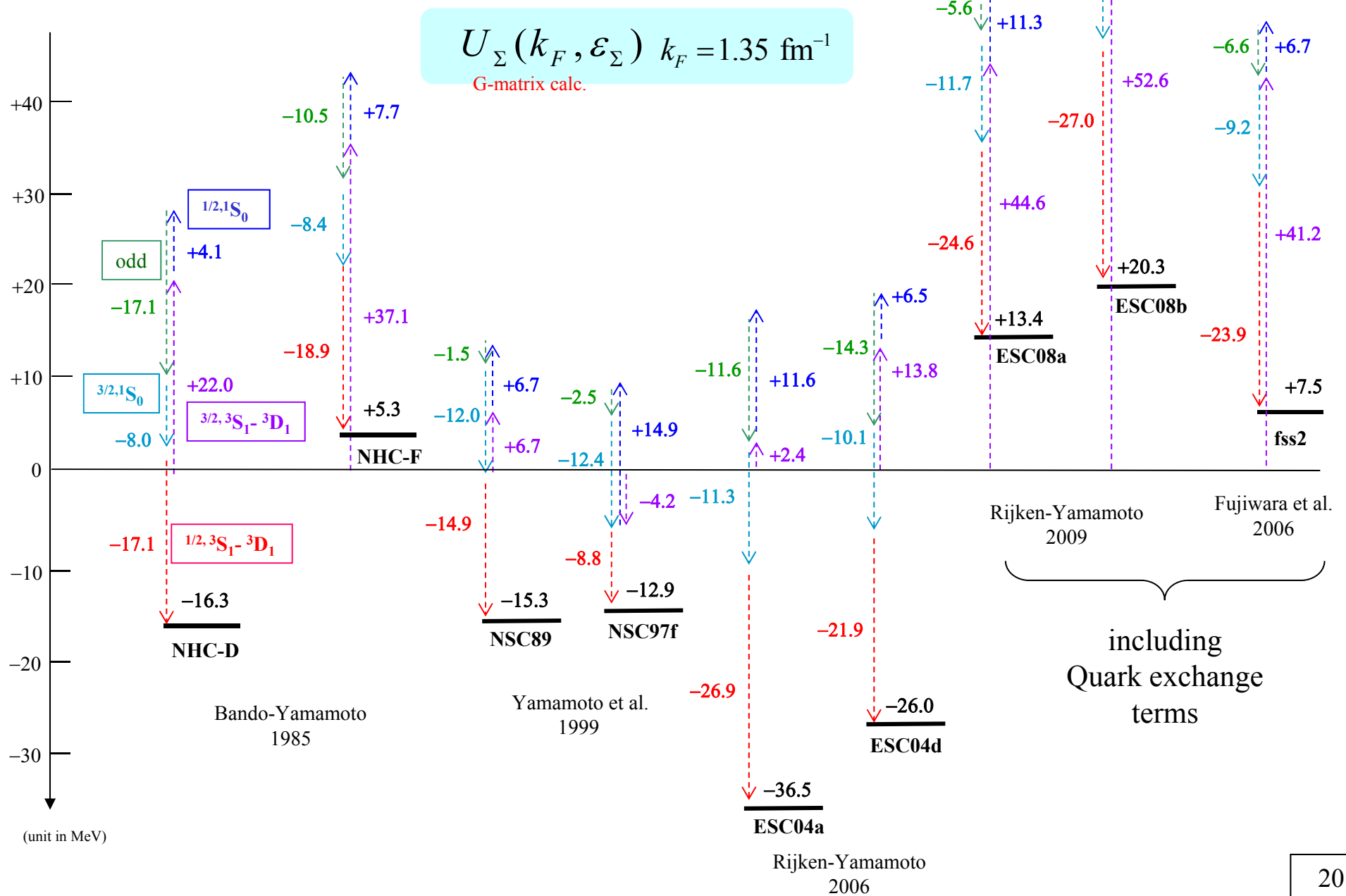


H.Yamamura, K. Miyagawa, et al.,  
PRC61 (1999) 014001

**$d(\gamma, K^+)$  inclusive spectrum**

# $\Sigma$ s.p. energies in symmetric nuclear matter

May, 2010 update

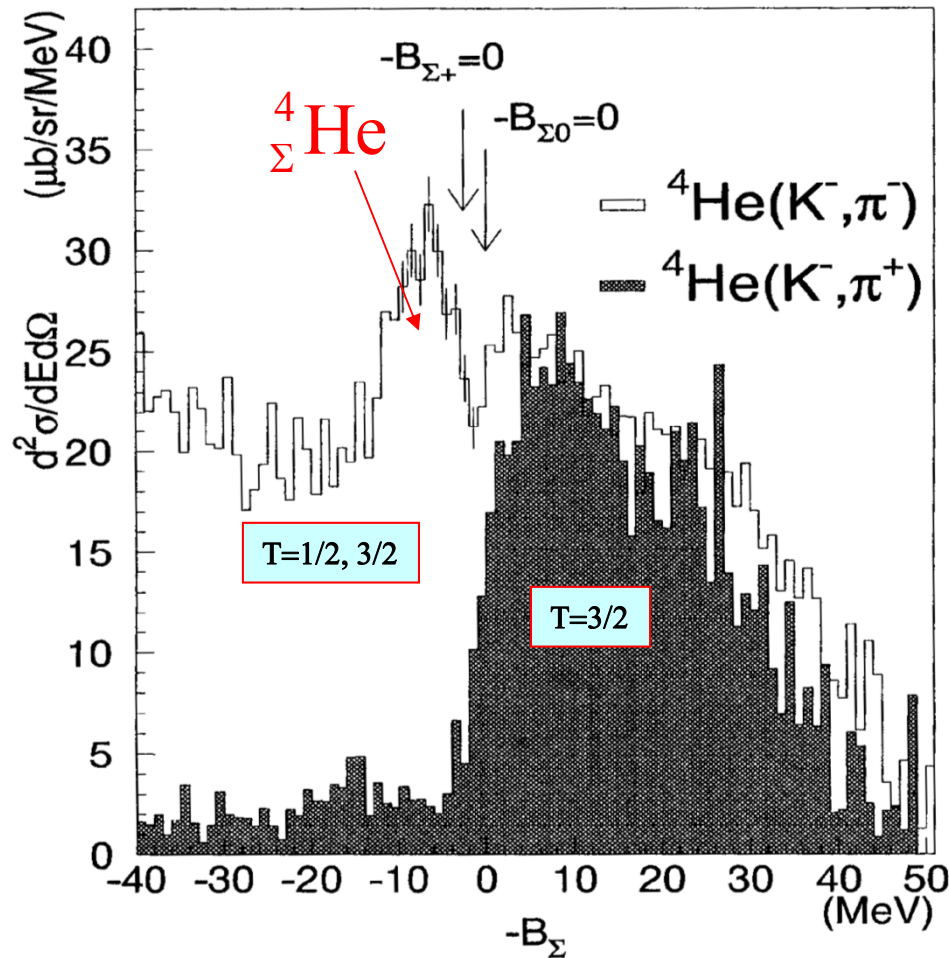


# Observation of a $\Sigma^+{}^4\text{He}$ Bound State

BNL-AGS (1995-)

VOLUME 80, NUMBER 8

PHYSICAL REVIEW LETTERS



T. Nagae, T. Miyachi, T. Fukuda, H. Ota,  
 T. Tamagawa, J. Nakano, R. S. Hayano,  
 H. Tamura, Y. Shimizu, K. Kubota,  
 R. E. Chrien, R. Sutter, A. Rusek,  
 W. J. Briscoe, R. Sawafuta,  
 E. V. Hungerford, A. Empl, W. Naing,  
 C. Neerman, K. Johnston, M. Planinic,  
**Phys. Rev. Lett. 80(1998)1605.**

$B_{\Sigma^+} = 4.4 \pm 0.3 \text{ MeV}$   
 $\Gamma = 7 \pm 0.7 \text{ MeV}$

4.6 MeV  
 7.9 MeV

$T \approx 1/2$   
 $J^\pi = 0^+$

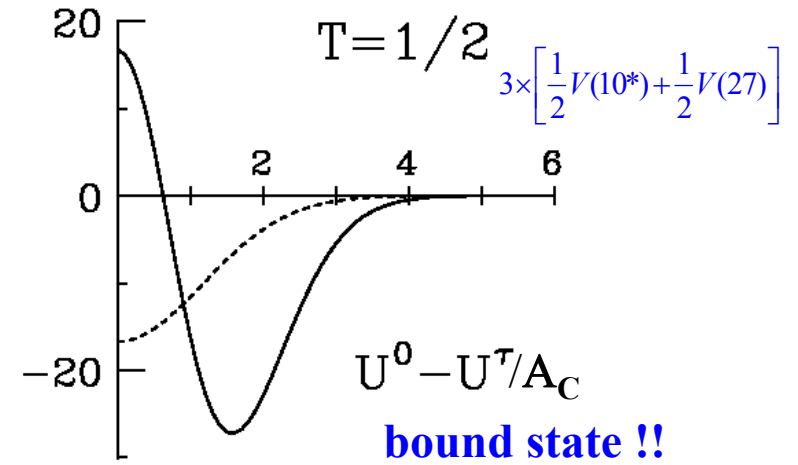
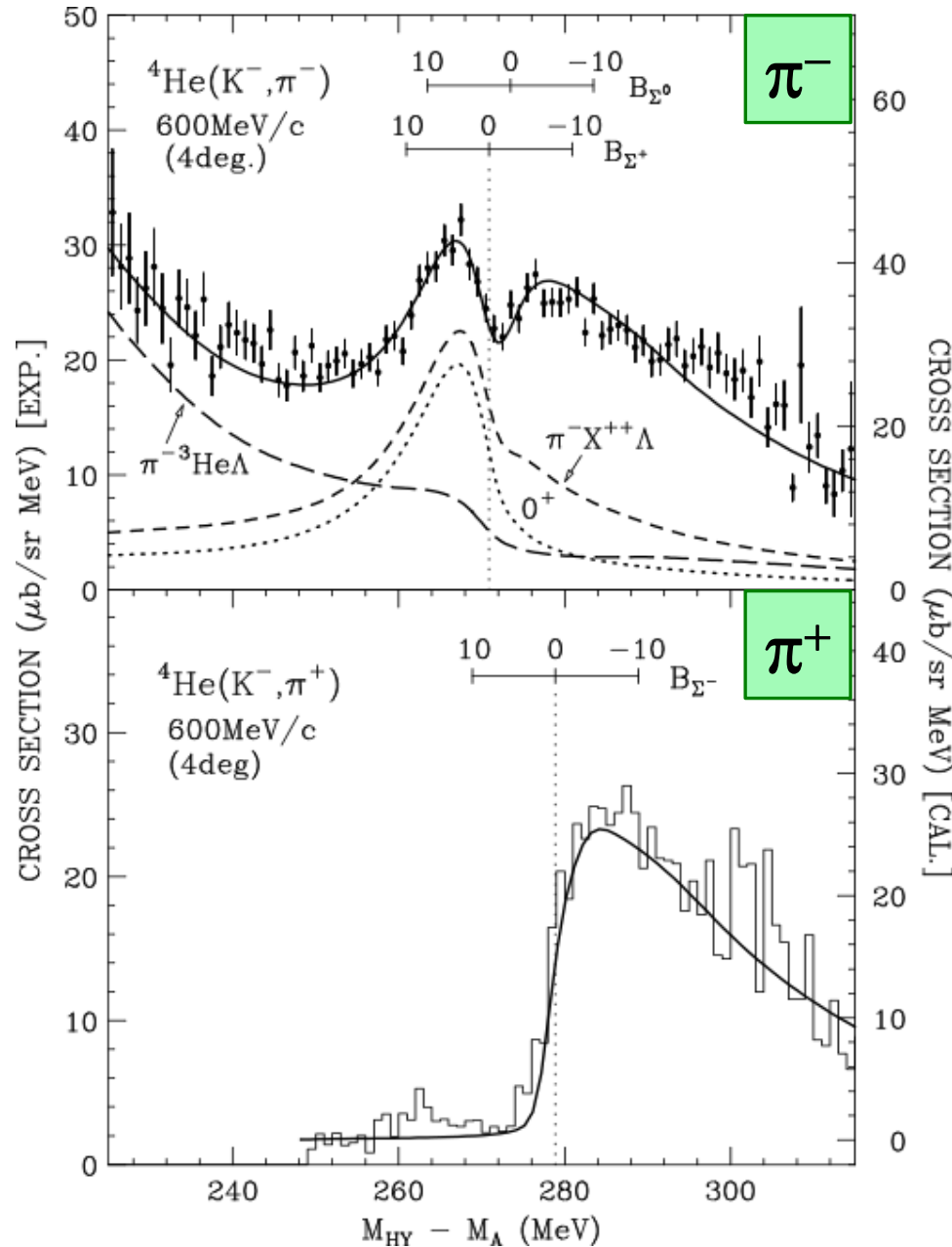
**Theoretical Prediction**

T. Harada, S. Shinmura,  
 Y. Akaishi, H. Tanaka,  
 NPA507(1990)715.

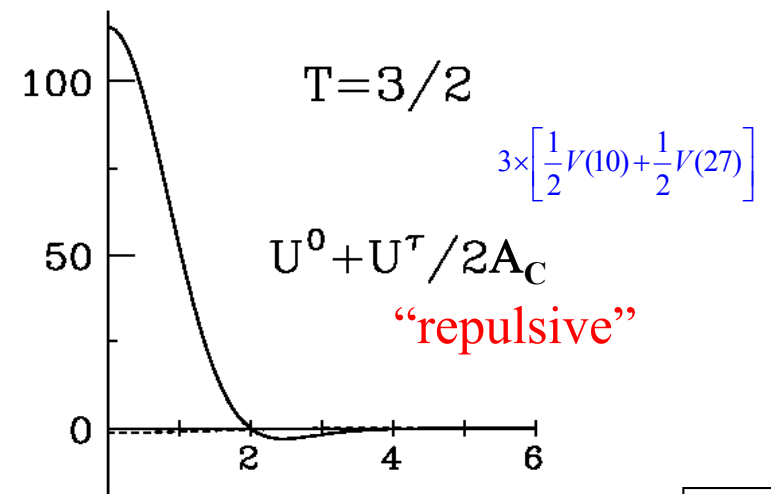
# Isospin dependence of the (3N)- $\Sigma$ potentials

T.Harada, PRL81(1998)5287.

T.Harada, NPA507 (1990) 715.



*“repulsive core  
+ attractive pocket”*



## Remarks

Properties of the  $\Sigma$ -nucleus potentials by comparing theoretical calculations with the available data:

$$U_{\Sigma}(\mathbf{r}) = U_{\Sigma}^0(\mathbf{r}) + \frac{1}{A_{\text{core}}} U_{\Sigma}^{\tau}(\mathbf{r}) (\vec{T}_{\text{core}} \cdot \vec{t}_{\Sigma})$$

“repulsion inside the nuclear surface”

“shallow attraction outside the nucleus”

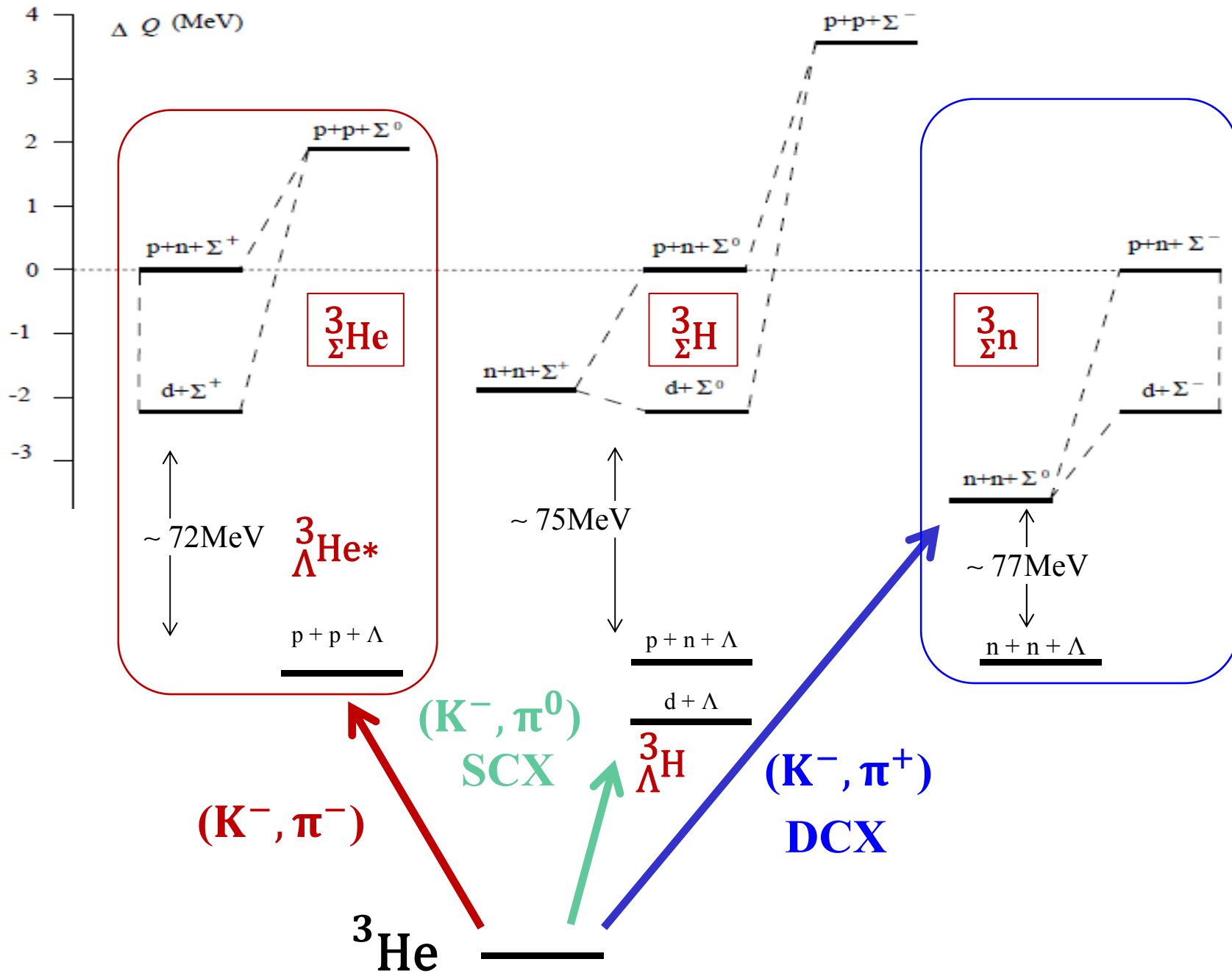
“strong isospin-dependence”

The calculated spectra for  ${}^4\text{He}(\text{K}^-, \pi^{\pm})$  reaction can explain consistently the available data from BNL, KEK, and ANL.

$\Sigma$ -3N potential: the  ${}^4_{\Sigma}\text{He}$  bound state with  $T=1/2$ ,  $J^{\pi}=0^+$

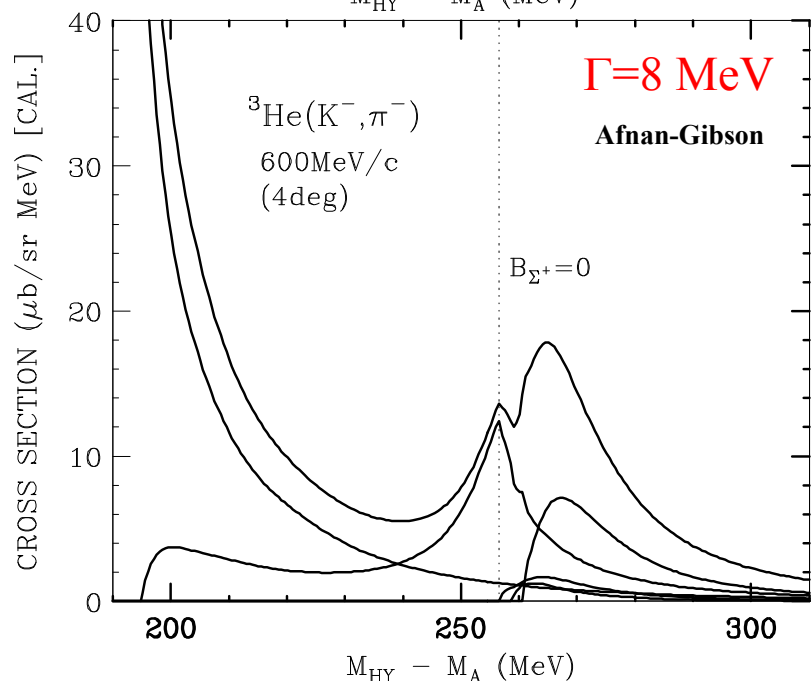
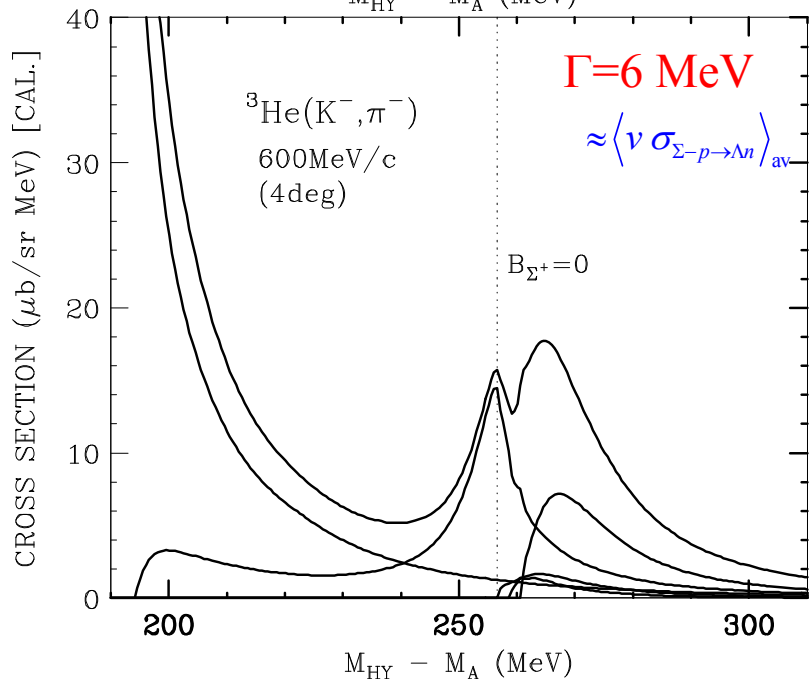
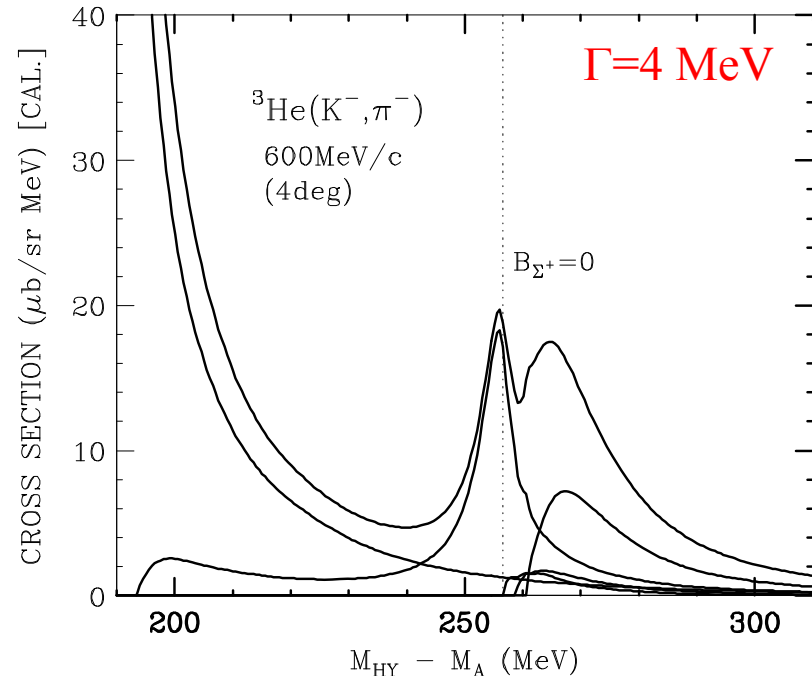
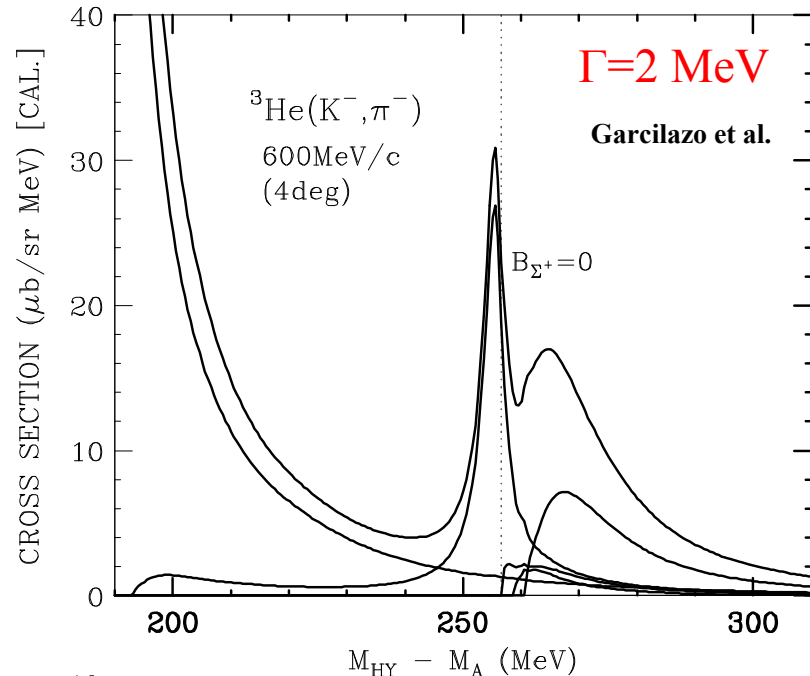
Strong Lane (isospin-dependent) potential and Coherent  $\Lambda$ - $\Sigma$  coupling

# Production by $K^-$ beam from $^3\text{He}$ targets

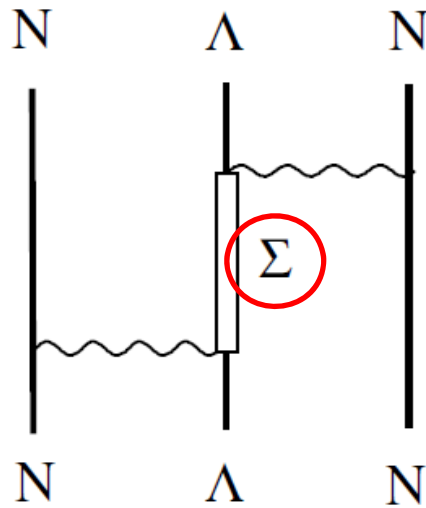




# Inclusive spectrum by ${}^3\text{He}(\text{K}^-, \pi^-)$ reactions at 600MeV/c



# 核物質中の $\Sigma$ ハイペロンの役割



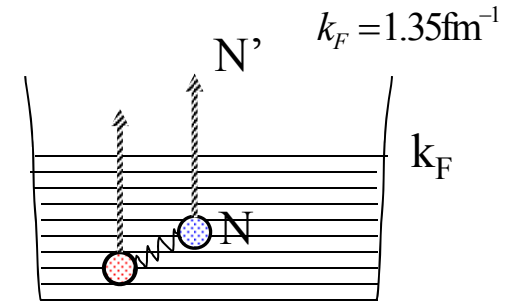
# G-matrix calculation in symmetric nuclear matter

## $\Lambda$ single-particle potential depth

$$U_{\Lambda}(k_F, \varepsilon_{\Lambda}) = \sum_{\mathbf{k}_N} \langle \mathbf{k}_{\Lambda}, \mathbf{k}_N | g_{\Lambda N}(\omega = \varepsilon_{\Lambda} + \varepsilon_N) | \mathbf{k}_{\Lambda}, \mathbf{k}_N \rangle$$

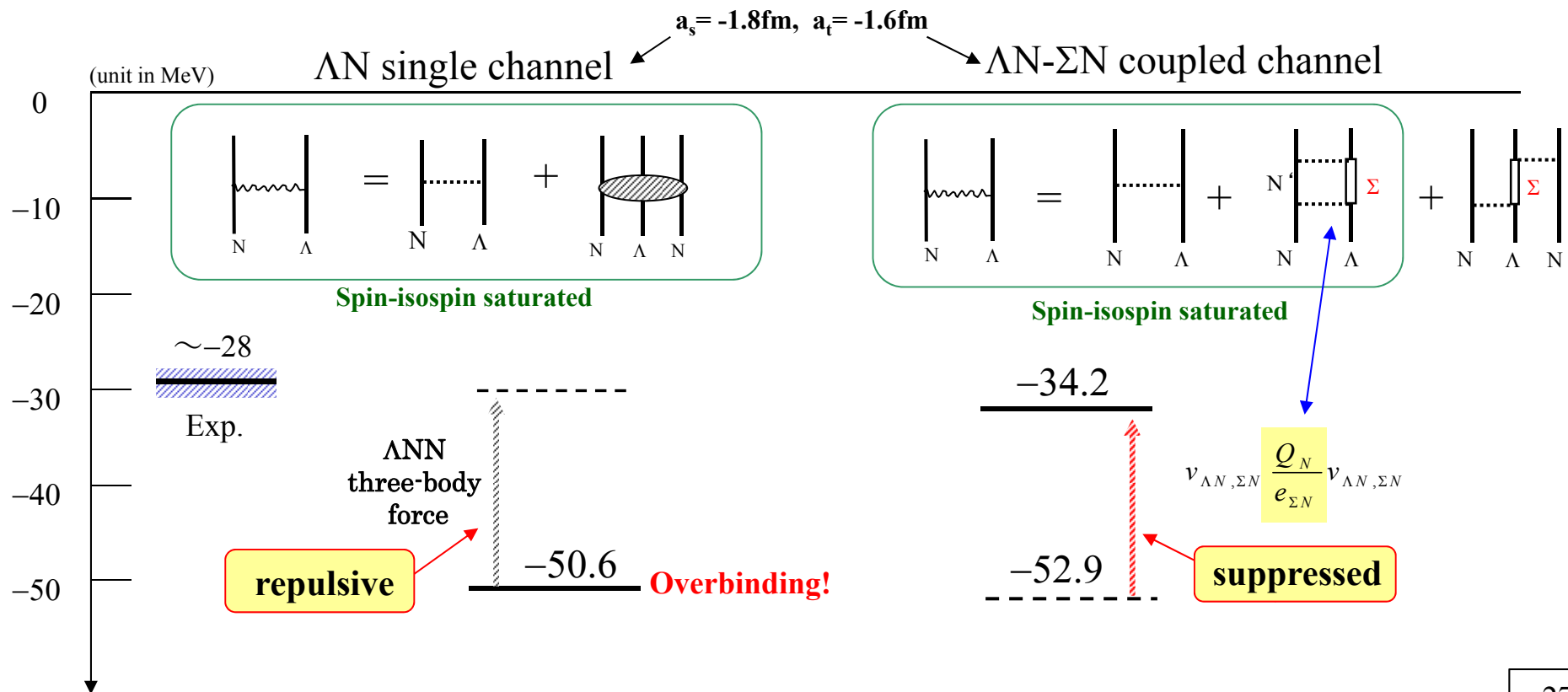
$$g_{YN}(\omega) = v_{YN} + v_{YN} \frac{Q_N}{\omega - QTQ} g_{YN}(\omega)$$

↑ **G-matrix**                      ← **Pauli-operator**



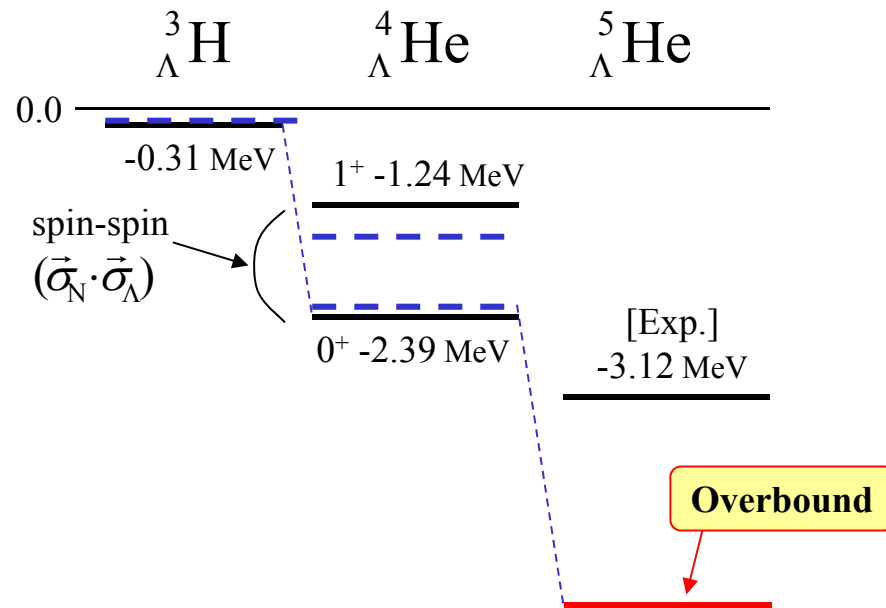
## Effects of the $\Lambda N$ - $\Sigma N$ coupling in nuclear matter

Y.Nogami, E.Sato, NPB19(1970)93



# Overbinding Problem on s-Shell Hypernuclei

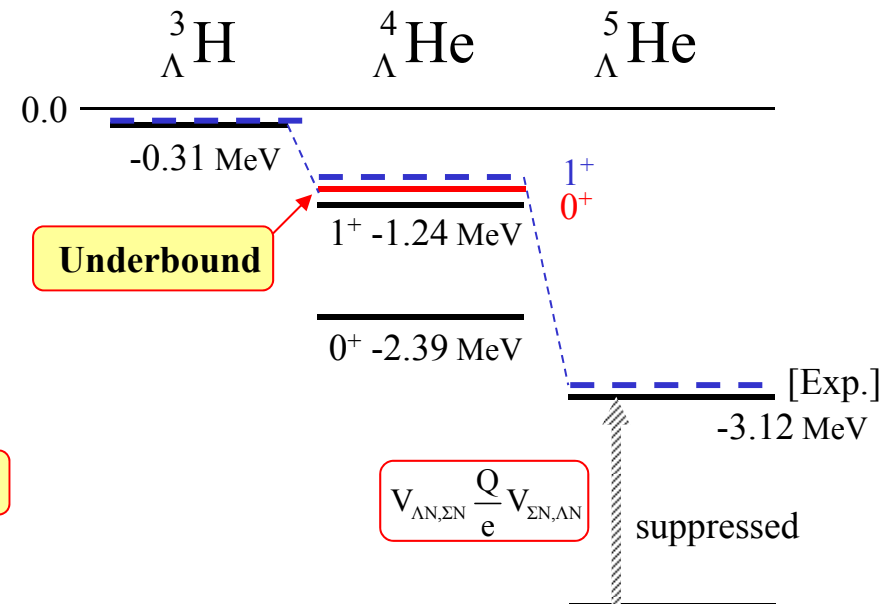
## The Overbinding Problem



$\Lambda\text{N}$  single-channel calc.

Dalitz et al., NP **B47** (1972) 109.

## The Underbinding Problem



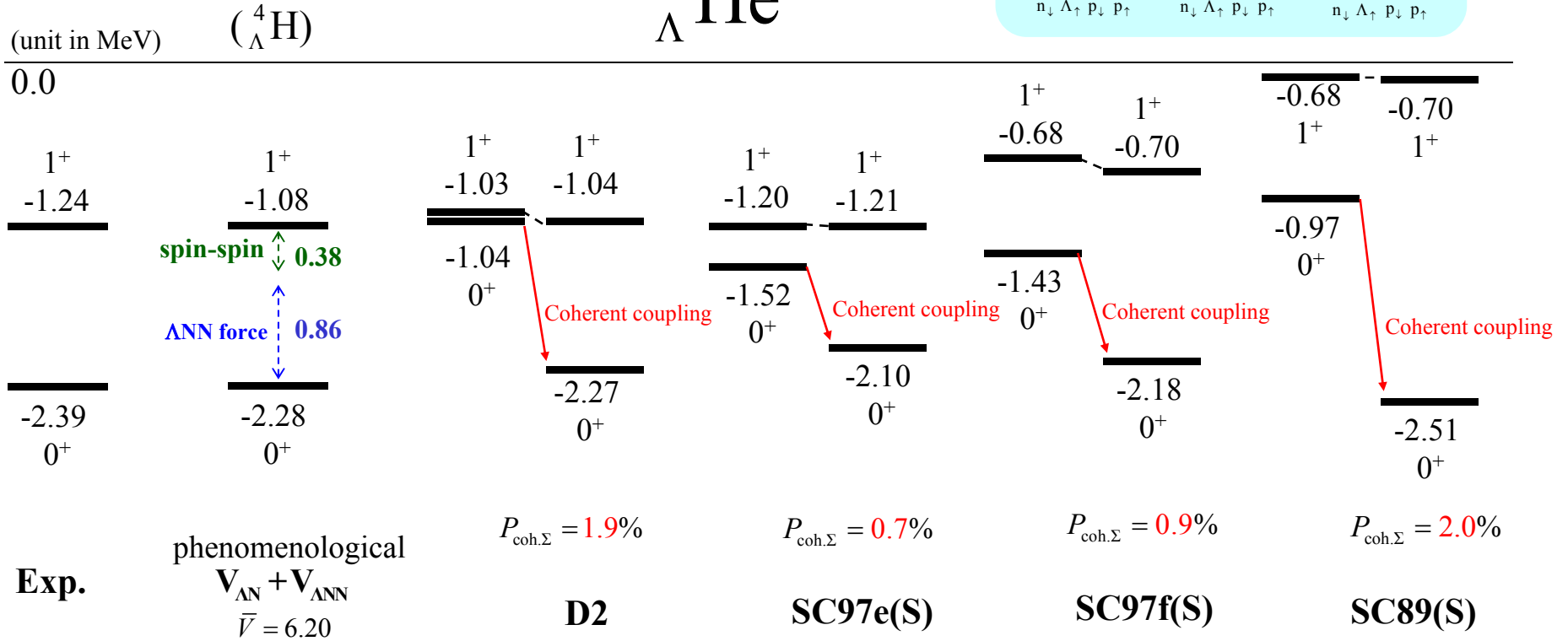
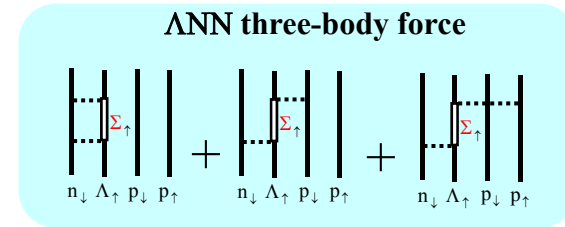
$g$ -matrix calc. with  $\Lambda\text{N}-\Sigma\text{N}(\text{D2})$

Akaishi et al., PRL **84** (2000) 3539.

# “The $0^+ - 1^+$ difference is not a measure of $\Lambda N$ spin-spin interaction.”

by B.F. Gibson

## Hyperon-mixing



VMC

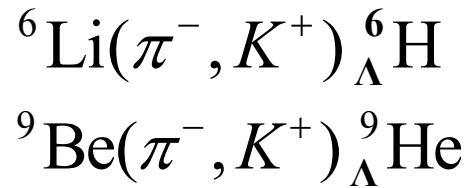
Breuckner-Hartree-Fock

R. Sinha, Q.N. Usmani,  
NPA684(2001)586c

Y. Akaishi, T. Harada, S. Shinmura, Khun Swe Myint,  
PRL84(2000)3539

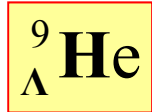
# Production of neutron-rich $\Lambda$ -hypernuclei with the DCX reaction

E10@J-PARC

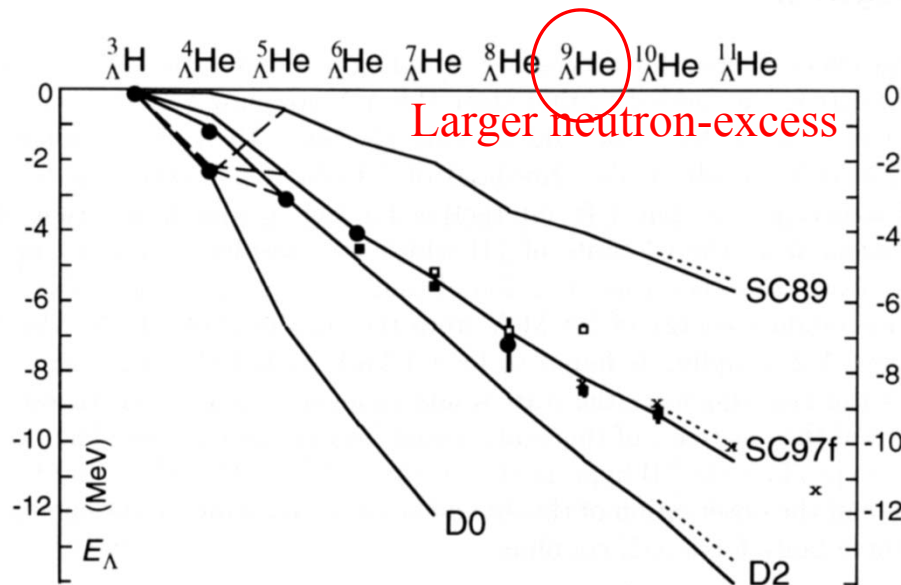


“Hyperheavy hydrogen”

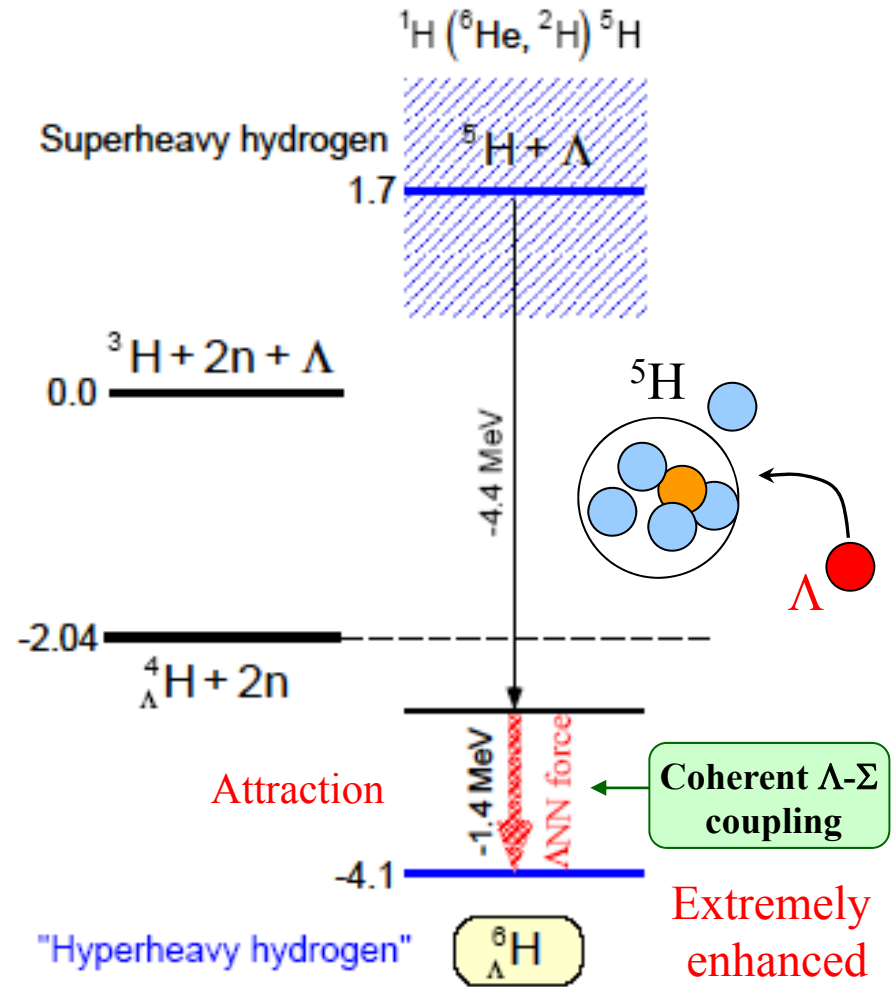
Y.Akaishi, NPA738(2004)80c



Khin Swe Myint et al.,  
FBS. Suppl. 12(2000)383



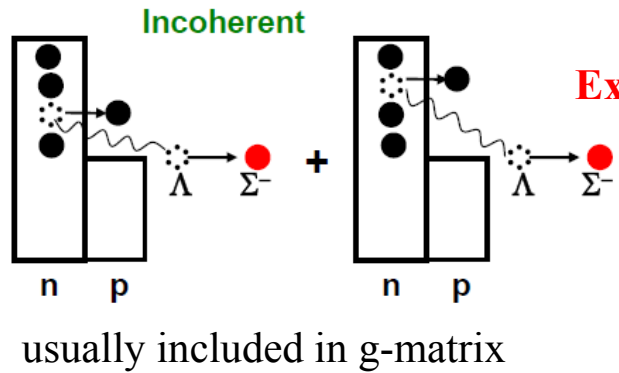
$\Lambda$  binding energies



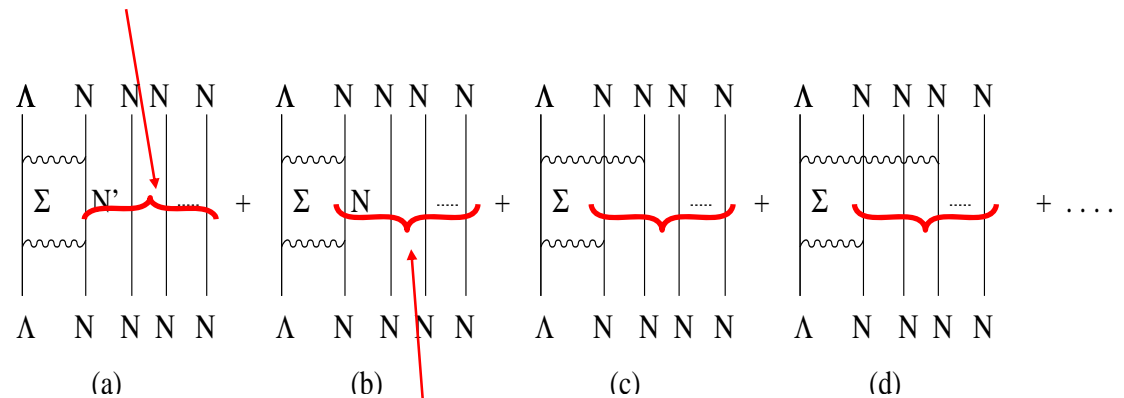
➤ Coherent  $\Lambda$ - $\Sigma$  coupling in neutron-excess environment

# The $\Lambda$ - $\Sigma$ coupling effects in neutron matter

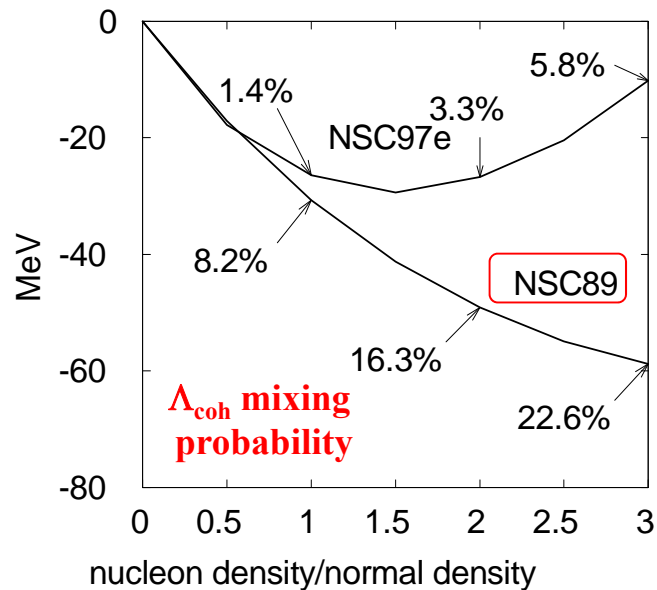
S.Shinmura, Khin Swe Myint, T.H., Y.Akaishi, J.Phys.G28(2002)L1



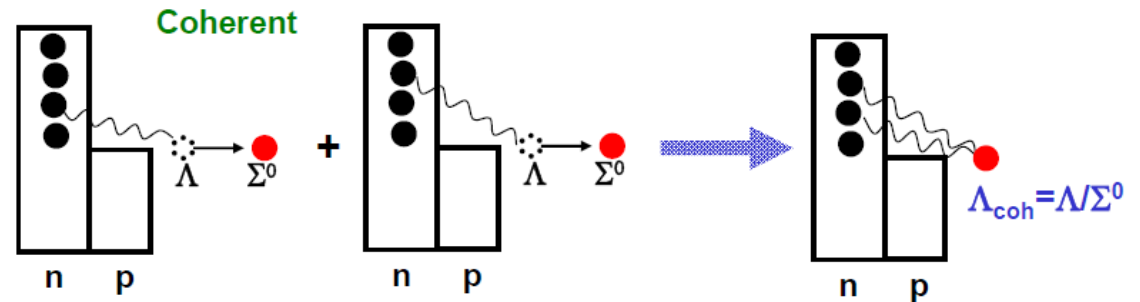
**Excited (1p1h) states**



**Single particle potential for  $\Lambda_{coh}$**



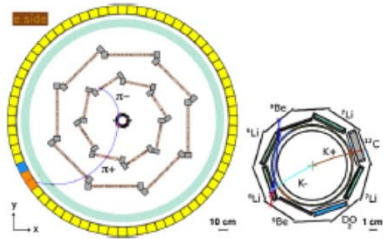
**Ground states**



**coherent  $\Lambda$ - $\Sigma$  coupling**

*The  $\Lambda_{coh}$  mixing is enhanced in the neutron-excess environment.*

# First observation of the superheavy hydrogen ${}_{\Lambda}^6\text{H}$



M. Agnello et al., NPA881(2012)269.

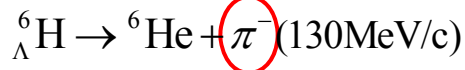
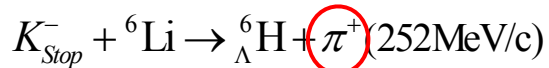
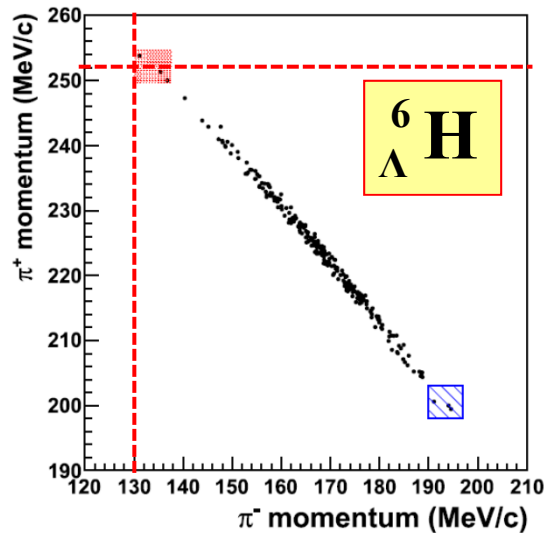
M. Agnello, et al., PRL108 (2012) 042501.

- observation of 3 candidate events of  ${}_{\Lambda}^6\text{H}$  bound state

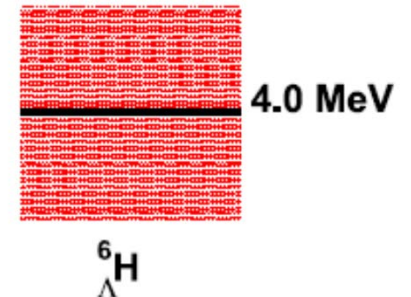
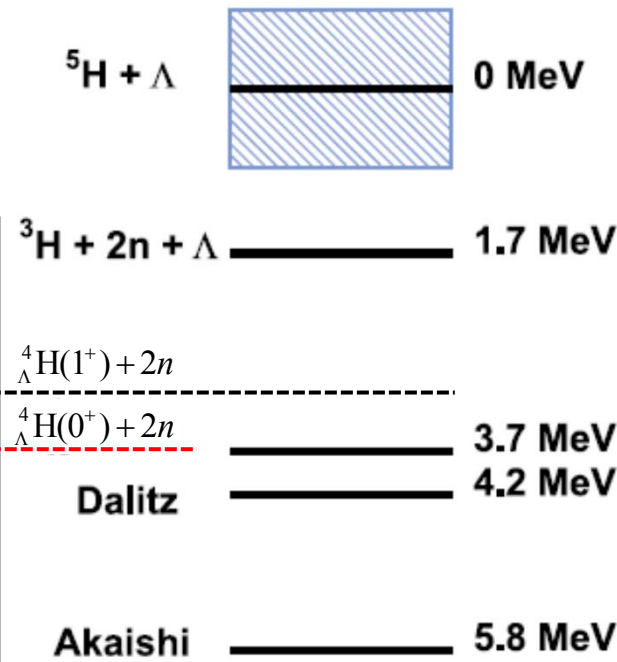
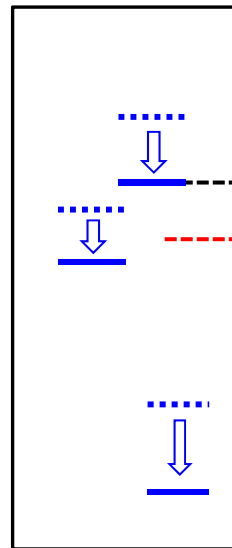
$$B_{\Lambda} = 4.0 \pm 1.1 \text{ MeV}$$

- $\text{BR}(\text{DCX}) / \text{BR}(\text{NCX}, 12\text{LC}) \sim 3 \times 10^{-3}$

$$R = (5.9 \pm 4.0) \cdot 10^{-6} / K_{\text{stop}}^{-}$$



3 events

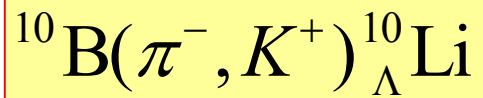


➔ E10@J-PARC

- Produce neutron-rich hypernuclei:  ${}_{\Lambda}^6\text{H}$  and  ${}_{\Lambda}^9\text{He}$
- precise measurement of B.E. of  ${}_{\Lambda}^6\text{H}$  is possible

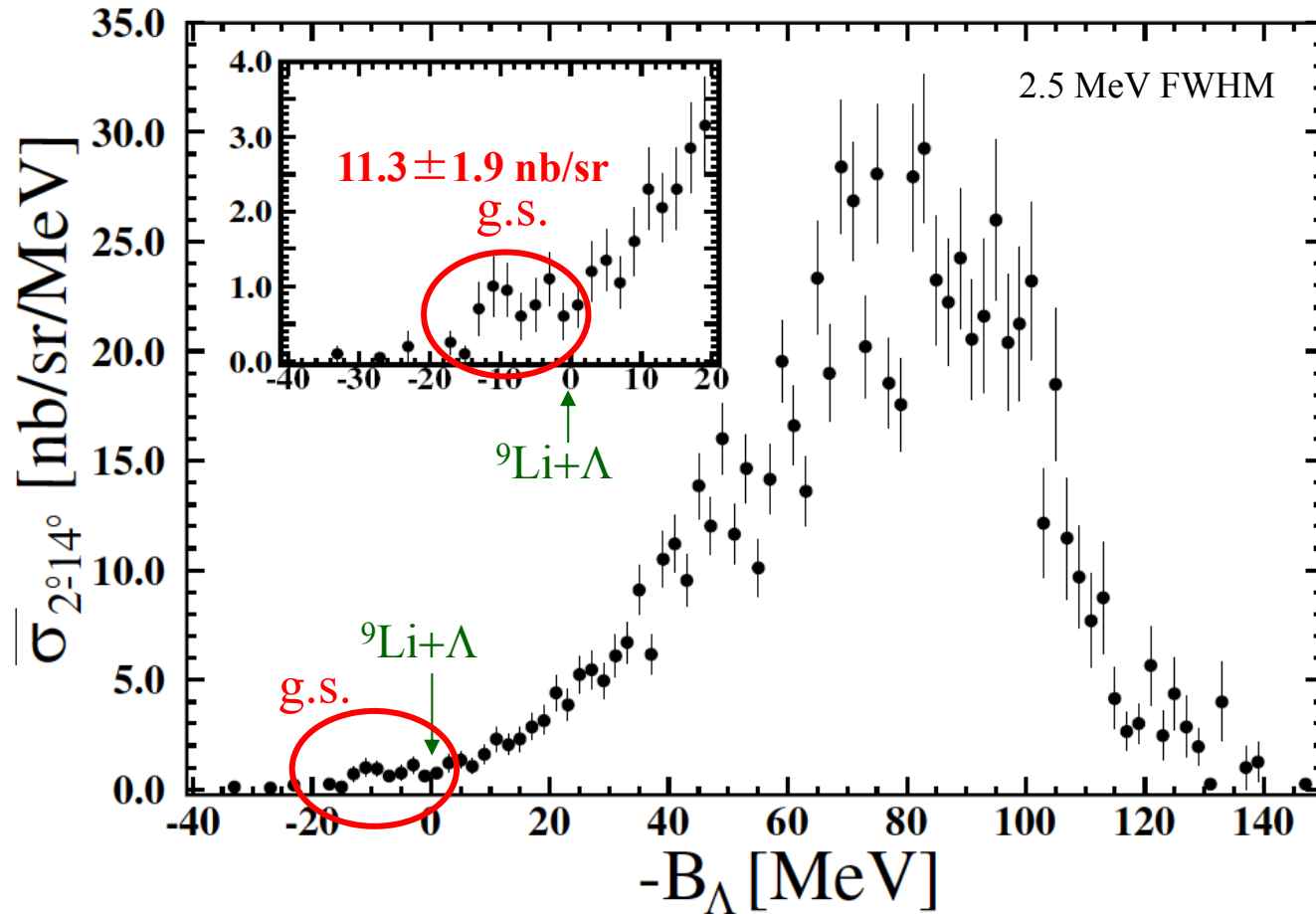


# First production of neutron-rich $\Lambda$ hypernuclei



$\Lambda$  spectrum by DCX ( $\pi^-, K^+$ ) reaction at 1.2 GeV/c

KEK-PS-E521 P. K. Saha, et al., PRL94(2005)052502



## Cross sections

-  $p_{\pi} = 1.20 \text{ GeV/c}$

$$\frac{d\sigma}{d\Omega_L} \approx 11.3 \pm 1.9 \text{ nb/sr}$$

-  $p_{\pi} = 1.05 \text{ GeV/c}$

$$\frac{d\sigma}{d\Omega_L} \approx 5.8 \pm 2.2 \text{ nb/sr}$$

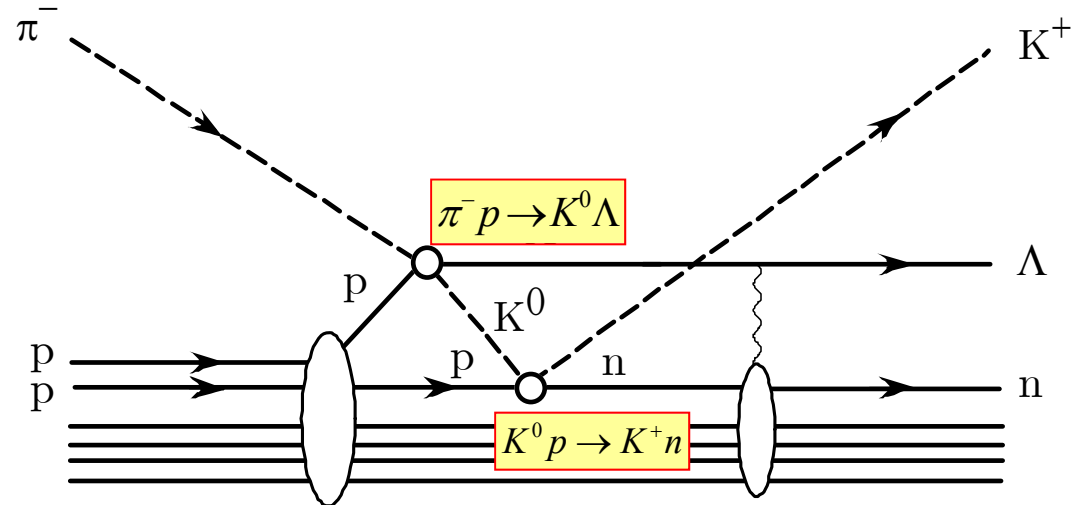
$\sim 1/1000$

$^{12}\text{C}(\pi^+, K^+)_{\Lambda}^{12}\text{C}$  (1.2 GeV/c)

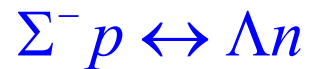
$$17.5 \pm 0.6 \text{ } \mu\text{b/sr}$$

# $(\pi^-, K^+)$ – Double Charge Exchange (DCX) Reaction

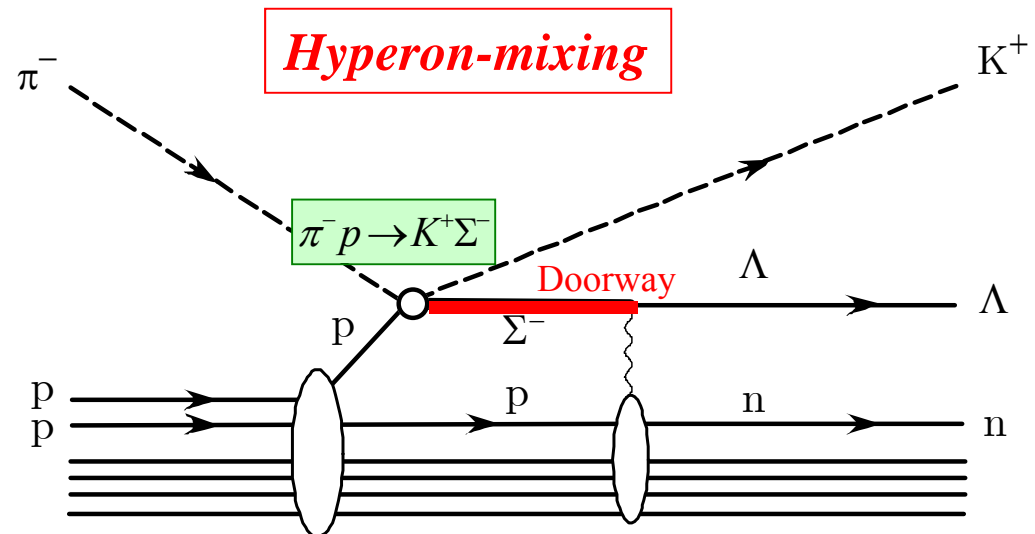
Two-step process:



One-step process:



via  $\Sigma^-$  doorways caused by  $\Lambda N$ - $\Sigma N$  coupling



# $\Lambda$ spectrum by DCX ( $\pi^-$ , $K^+$ ) reactions at 1.2 GeV/c

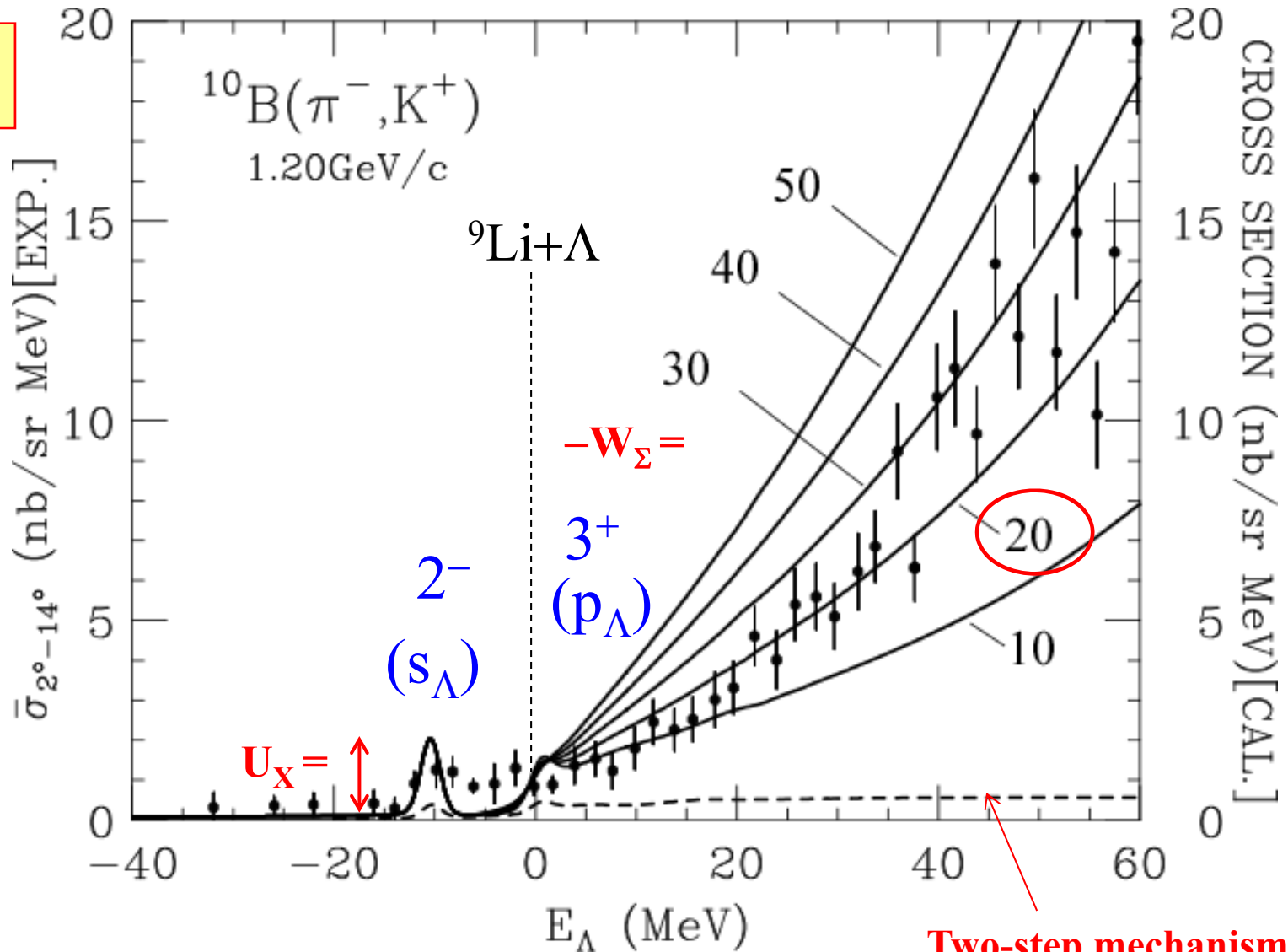
Harada, Umeya, Hirabayashi, PRC79(2009)014603

Spreading potential dep.

$W_\Sigma$

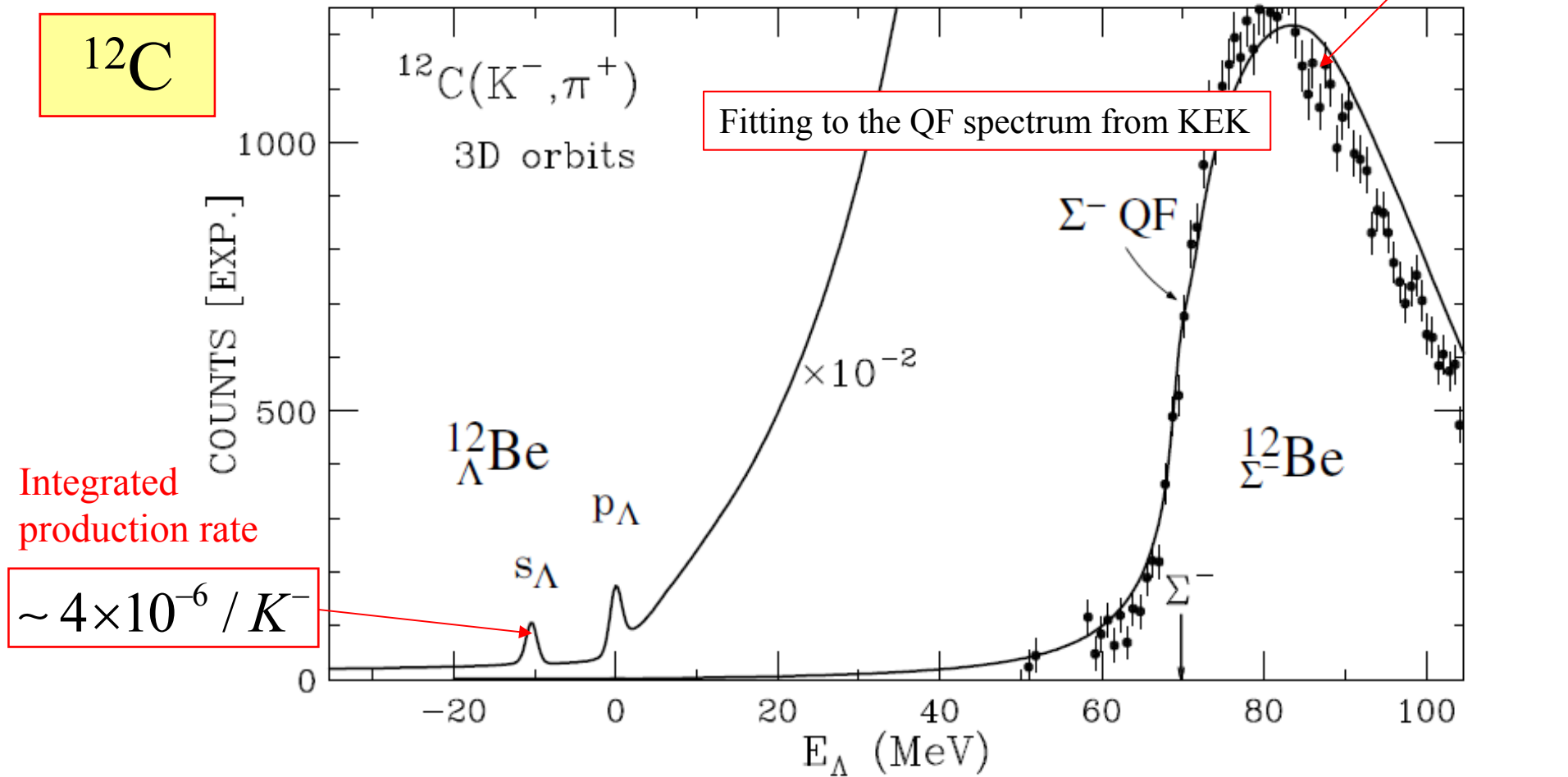
$U_x = 11$  MeV is fixed.  $P_{\Sigma^-} = 0.57\%$

$^{10}\text{B}$



# $\Lambda$ spectrum by DCX (stopped $K^-$ , $\pi^+$ ) reactions

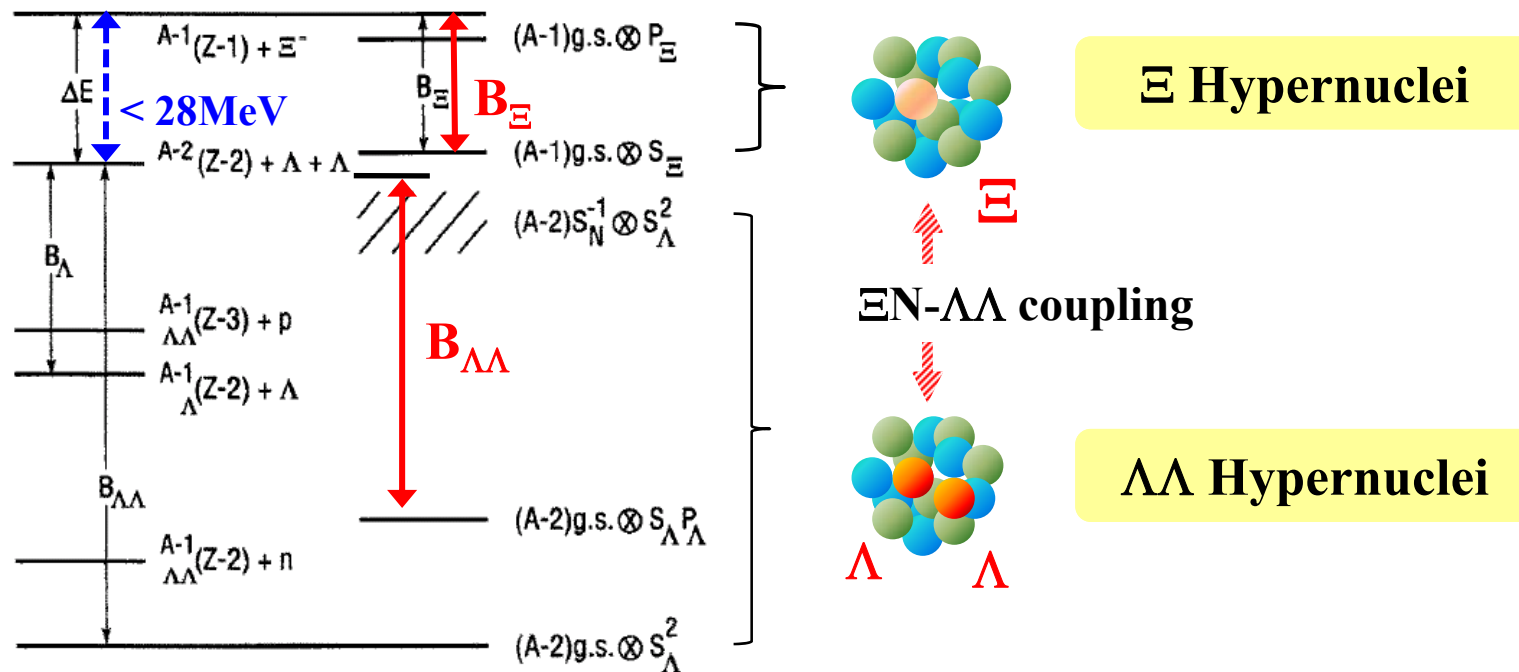
If the  $\Sigma^-$  admixture probability of  $\sim 0.6\%$  is assumed in  $^{12}_\Lambda\text{Be}$ , we demonstrate the (stopped  $K^-$ ,  $\pi^+$ ) spectrum on a  $^{12}\text{C}$  target.



DAΦNE data: U.L.  $\sim (2.0 \pm 0.4) \times 10^{-5} / K^-$

M.Agnello, et al., PLB640(2006)145.

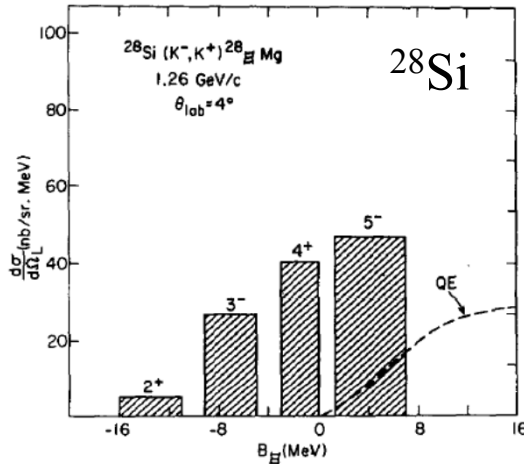
# 3. $S = -2$ Nuclei



# Studies of $\Xi^-$ s.p. potentials

$V_{\Xi} ?$

knowledge is limited



## $\Xi$ -hypernuclei via (K-,K+) reactions

[C.B. Dover, A.Gal, Ann. Phys. 146 (1989) 309.]

$$V_{\Xi}^0 = -24 \pm 4 \text{ MeV for } r_0 = 1.1 \text{ fm } (W_{\Xi}^0 \simeq -1 \text{ MeV})$$

## DWIA analysis of $^{12}\text{C}(K-,K+)$ data at 1.8 GeV/c

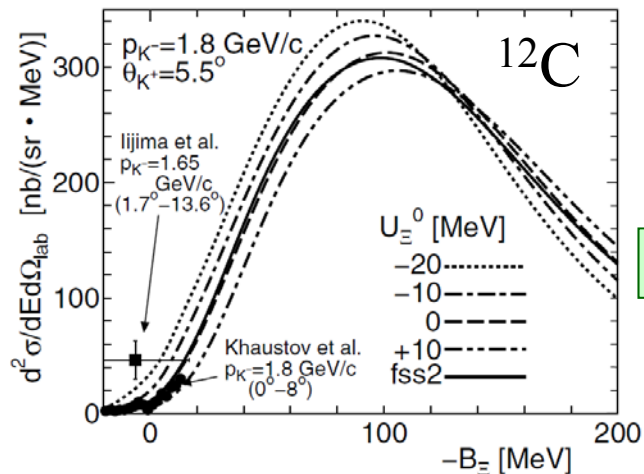
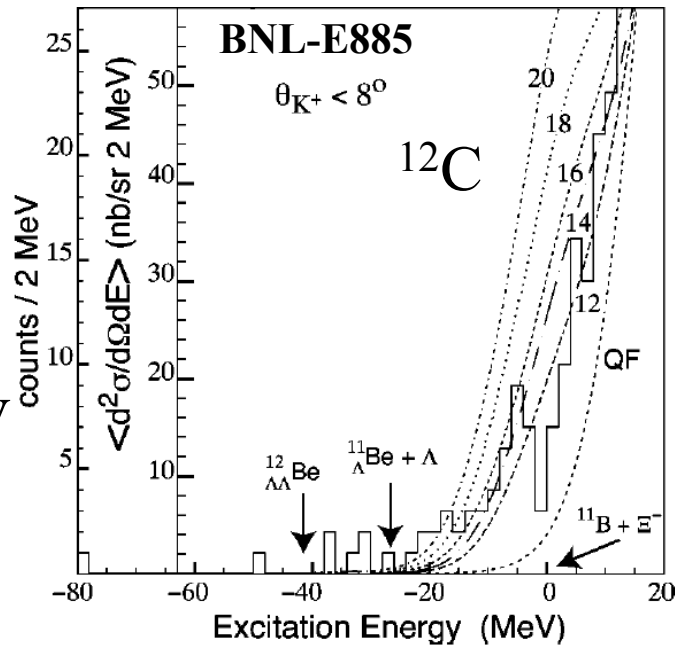
T.Iijima et al., NPA546(1992)588.

Tadokoro et al., PRC51(1995)2656

P.Khaustov et al., PRC61(2000)054603

$$V_{\Xi}^0 \simeq -16 \text{ MeV}$$

$$V_{\Xi}^0 \simeq -14 \text{ MeV}$$



## Semi-Classical Distorted Wave Model Analysis

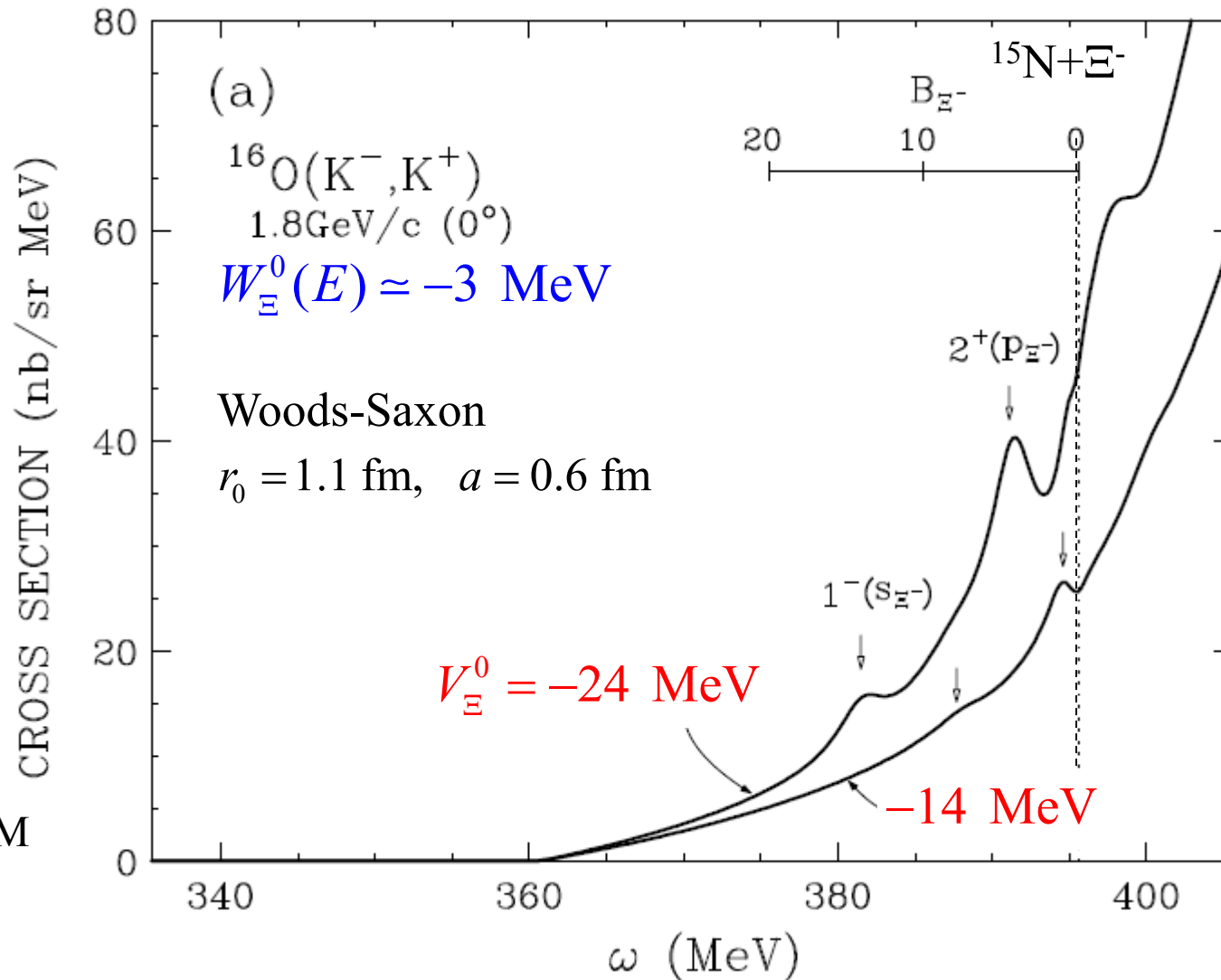
M. Kohno et al., PTP123(2010)157; NPA835(2010)358.

$$V_{\Xi}^0 = -20, -10, 0, +10, +20 \text{ MeV} \longleftrightarrow \text{fss2}$$

# $\Xi^-$ spectrum in DCX ( $K^-, K^+$ ) reactions at 1.8 GeV/c

T. Harada, Y. Hirabayashi, A. Umeya, PLB690(2010)363.

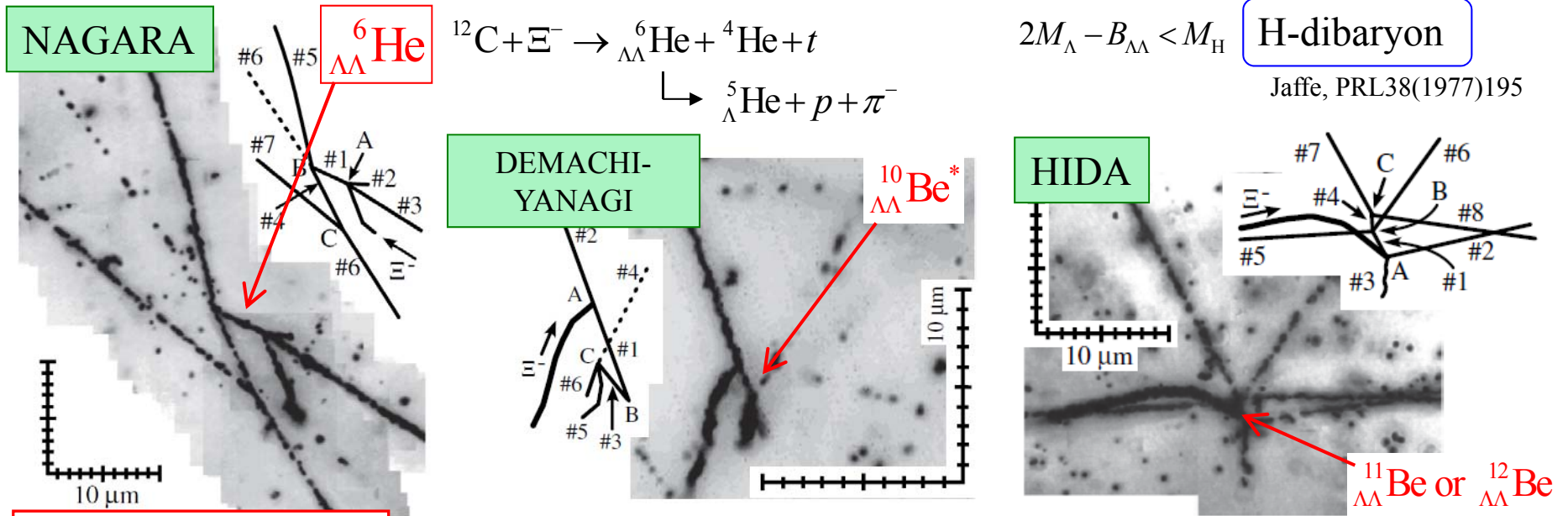
$^{16}\text{O}$



➤ Spin-stretched  $\Xi^-$  states can be populated due to the high momentum transfer.

$$ds/d\Omega [^{15}\text{N}(1/2^-) \otimes s_{\Xi^-}](1^-) = 6 \text{ nb/sr}, \quad ds/d\Omega [^{15}\text{N}(1/2^-) \otimes p_{\Xi^-}](2^+) = 9 \text{ nb/sr} \text{ for } V_{\Xi} = -14 \text{ MeV.}$$

# Observation of $\Lambda\Lambda$ Hypernuclei in E176/E373 Hybrid Emulsion



$\Lambda\Lambda$  bound energy  $\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^AZ) = B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^AZ) - 2B_{\Lambda}({}_{\Lambda}^{A-1}Z)$

Hiyama et al. PRL104(2010)212502 Gal-Millener, PLB701(2011)342

event	${}_{\Lambda\Lambda}^AZ$	Target	$B_{\Lambda\Lambda}$ [MeV]	$\Delta B_{\Lambda\Lambda}$ [MeV]
NAGARA	${}_{\Lambda\Lambda}^6\text{He}$	${}^{12}\text{C}$	$6.91 \pm 0.16$	$0.67 \pm 0.17$
MIKAGE	${}_{\Lambda\Lambda}^6\text{He}$	${}^{12}\text{C}$	$10.06 \pm 1.72$	$3.82 \pm 1.72$
DEMACHIYANAGI	${}_{\Lambda\Lambda}^{10}\text{Be}$	${}^{12}\text{C}$	$11.90 \pm 0.13$	$-1.52 \pm 0.15$
HIDA	${}_{\Lambda\Lambda}^{11}\text{Be}$	${}^{16}\text{O}$	$20.49 \pm 1.15$	$2.27 \pm 1.23$
	${}_{\Lambda\Lambda}^{12}\text{Be}$	${}^{14}\text{N}$	$22.23 \pm 1.15$	-
E176	${}_{\Lambda\Lambda}^{13}\text{B}$	${}^{14}\text{N}$	$23.3 \pm 0.7$	$0.6 \pm 0.8$
Danysz <i>et al</i> [17]	${}_{\Lambda\Lambda}^{10}\text{Be}({}_{\Lambda}^9\text{Be}^*)$	${}^{14}\text{N}$	$14.7 \pm 0.4$	$1.3 \pm 0.4$

$B_{\Lambda\Lambda}^{\text{CM}}$ [MeV]	$B_{\Lambda\Lambda}^{\text{SM}}$ [MeV]
(6.91)	(6.91)
11.88	
18.23	18.40
	20.27
	23.21
14.74 (g.s.)	14.97 (g.s.)

H.Takahashi et al.,PRL87(2001)212502  
 K.Nakazawa , NPA 835 (2010)207  
 K.Nakazawa , H.Takahashi,NPA 835 (2010)207

$\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^6\text{He}) \simeq 4.7 \longrightarrow 1.01 \longrightarrow 0.67$   
 Prowse, 1966      Nagara,2001       $\Xi$  mass update

**“weak attractive”**

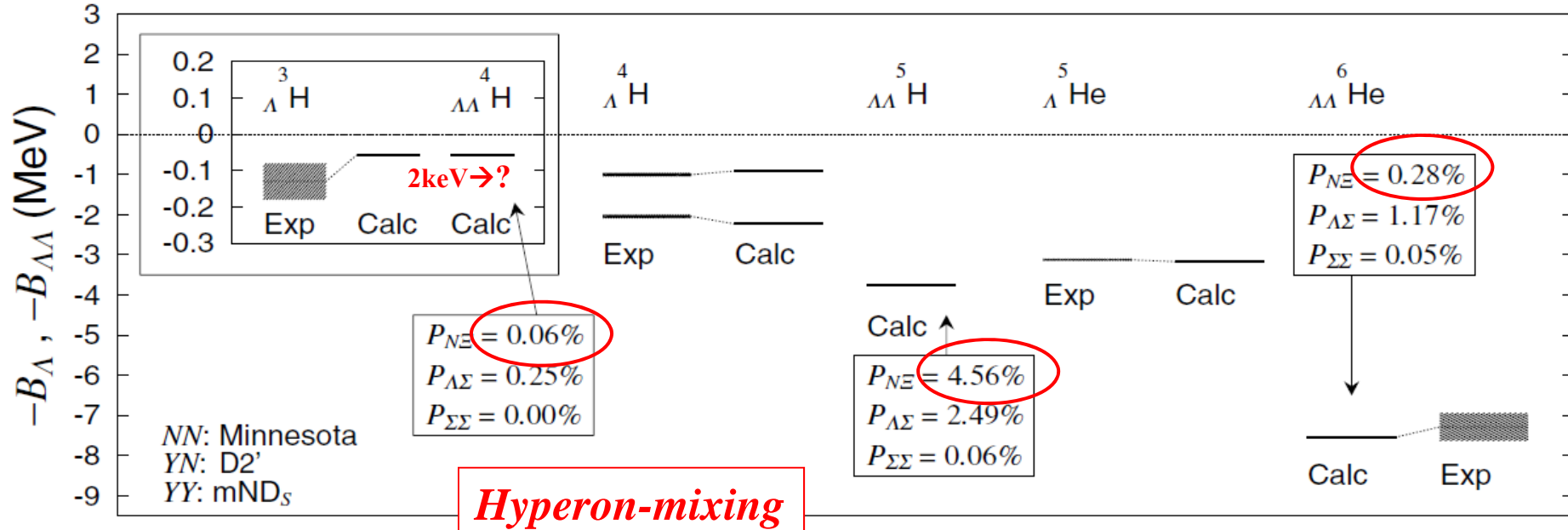


# Coupled Channel Approach to Doubly Strange Hypernuclei

## Ab initio calculations by SVM

H. Nemura et al.,  
PRL94(2005)202502

$\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^6\text{He}) \simeq 1.01 \rightarrow 0.67$   
Nagara,2001  $\Xi$  mass update



## $\alpha\Xi\text{N}-\alpha\Lambda\Lambda$ coupled-channel calculations

T. Yamada, PRC69(2004)044301.

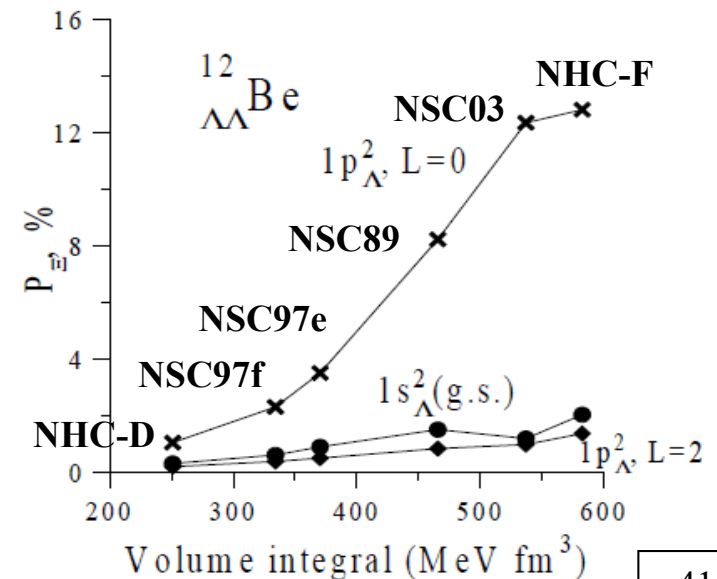
Y. Yamamoto and Th.A. Rijken, PRC69(2004)014303.

$\Lambda\Lambda-\Xi\text{N}$  s-wave:  $P(\Xi) < 1\%$

## $\Xi-\Lambda\Lambda$ coupled-channel calculations

D. E. Lansky and Y. Yamamoto, PRC69(2004)014303.

$1s_{\Lambda}^2$ :  $P(\Xi) < 1\%$ ,  $1s_{\Lambda}1p_{\Lambda}$ :  $P(\Xi) \sim 10\%$

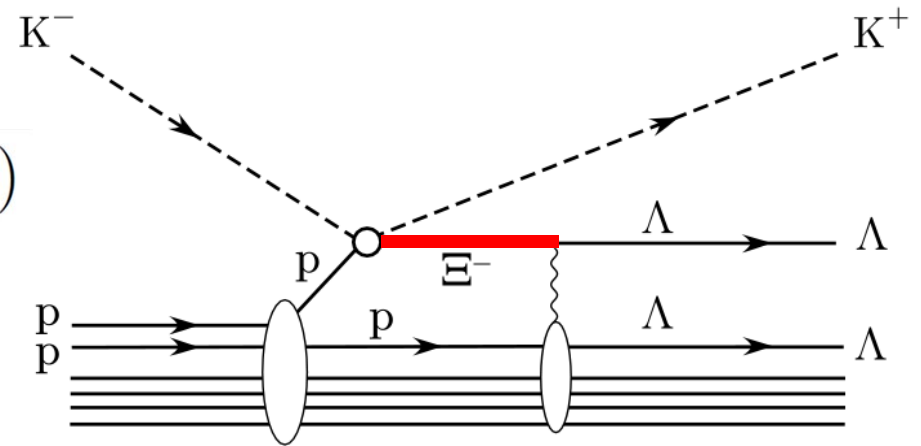


# Coupled-channels DWIA calculation for $\Lambda\Lambda$ - $\Xi$ production

Coupled-channel Green's function

$$\mathbf{G}(\omega) = \mathbf{G}^{(0)}(\omega) + \mathbf{G}^{(0)}(\omega)\mathbf{U}\mathbf{G}(\omega)$$

$$\mathbf{G}(\omega) = \begin{pmatrix} G_\Lambda(\omega) & G_X(\omega) \\ G_X(\omega) & G_\Xi(\omega) \end{pmatrix} \quad \mathbf{U} = \begin{pmatrix} U_\Lambda & U_X \\ U_X & U_\Xi \end{pmatrix}$$



Inclusive cross sections

DWIA+CCGFM

T. Harada, NPA672(2000)181

$$\left( \frac{d^2\sigma}{d\Omega_K dE_K} \right)_{\text{lab}} = \beta \frac{1}{[J_A]} \sum_{M_z} \sum_{\alpha'\alpha} \left( -\frac{1}{\pi} \right) \text{Im} \left[ \int d\mathbf{r}' d\mathbf{r} F_{\Xi}^{\alpha'\dagger}(\mathbf{r}') \rightarrow G_{\Xi}^{\alpha'\alpha}(\omega, \mathbf{r}', \mathbf{r}) F_{\Xi}^{\alpha}(\mathbf{r}) \right]$$

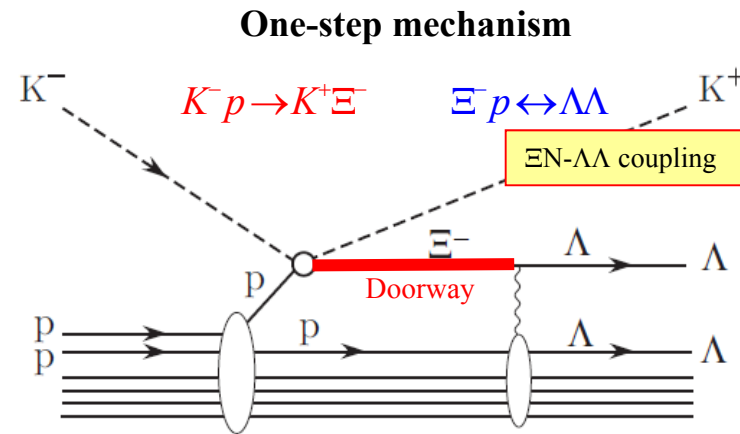
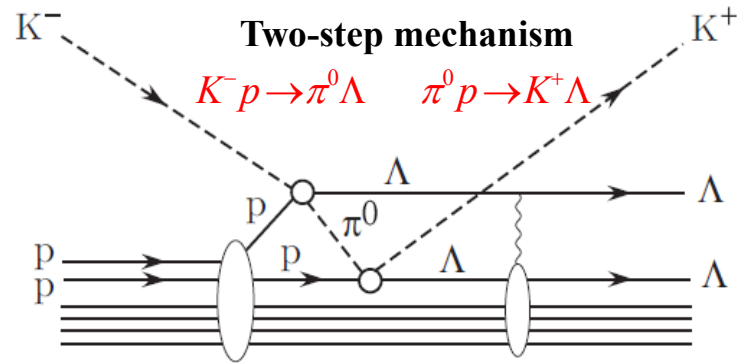
The decomposition of the inclusive spectrum into components

$$\text{Im} \hat{G}_{\Xi} = \underbrace{\hat{\Omega}^{(-)\dagger} \{ \text{Im} \hat{G}_{\Lambda}^{(0)} \} \hat{\Omega}^{(-)}}_{\Lambda\Lambda \text{ escape}} + \underbrace{\hat{\Omega}^{(-)\dagger} \{ \text{Im} \hat{G}_{\Xi}^{(0)} \} \hat{\Omega}^{(-)}}_{\Xi^- \text{ escape}} + \underbrace{\hat{G}^{\dagger} \{ W_{Y,T} \} \hat{G}}_{\text{Spreading (nuclear-core breakup) = Complicated excited states}}$$

Distorted waves for mesons

Eikonal distortion:  $\sigma_{K^-} = 19.4 \text{ mb}$ ,  $\sigma_{K^+} = 28.9 \text{ mb}$ ,  $\alpha_{\pi} = \alpha_K = 0$

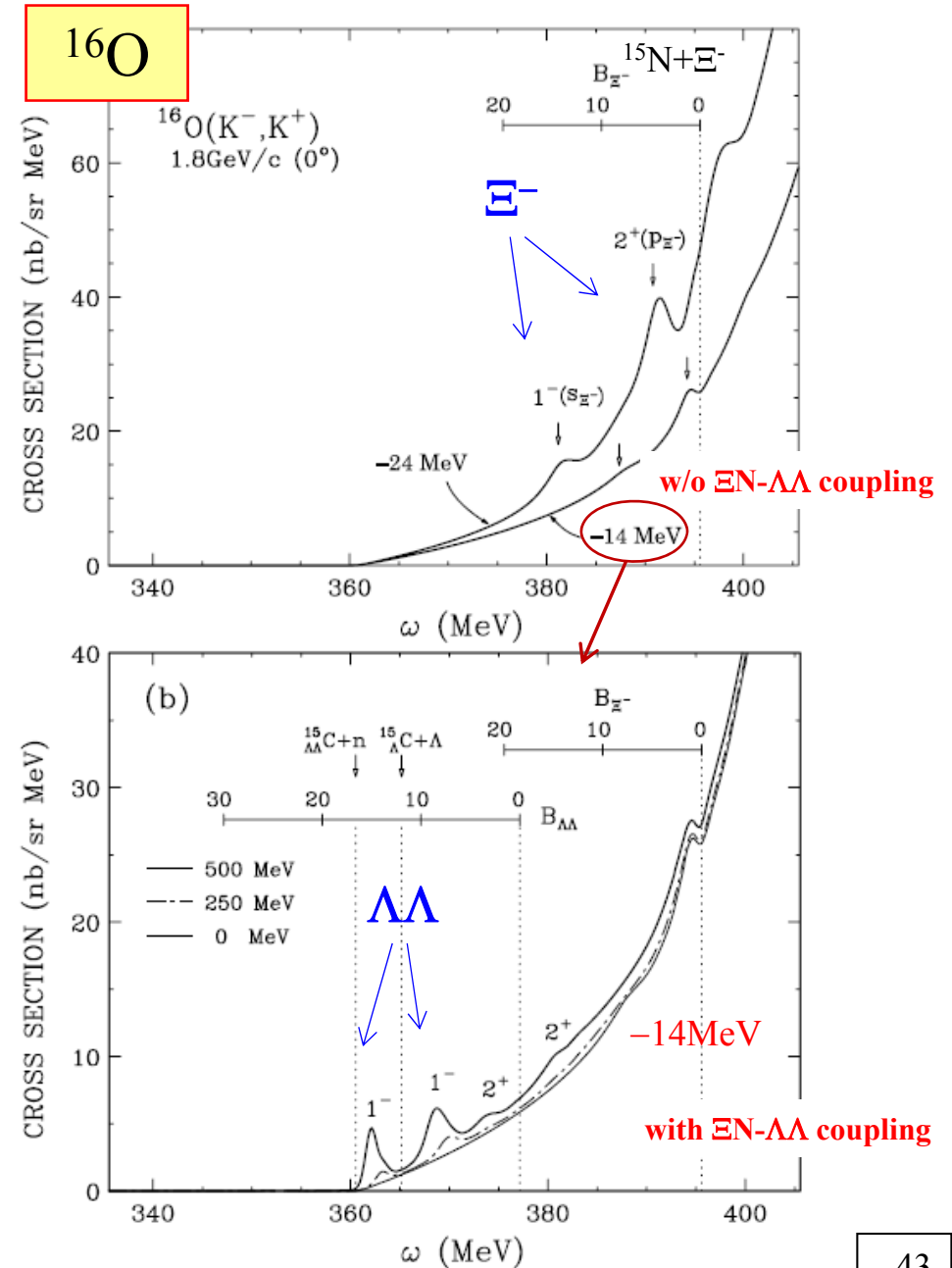
# $\Xi$ - $\Lambda$ spectrum in DCX ( $K^-, K^+$ ) reactions at 1.8 GeV/c



**Hyperon-mixing**

[T. Harada, Y. Hirabayashi, A. Umeya, PLB690(2010)363]

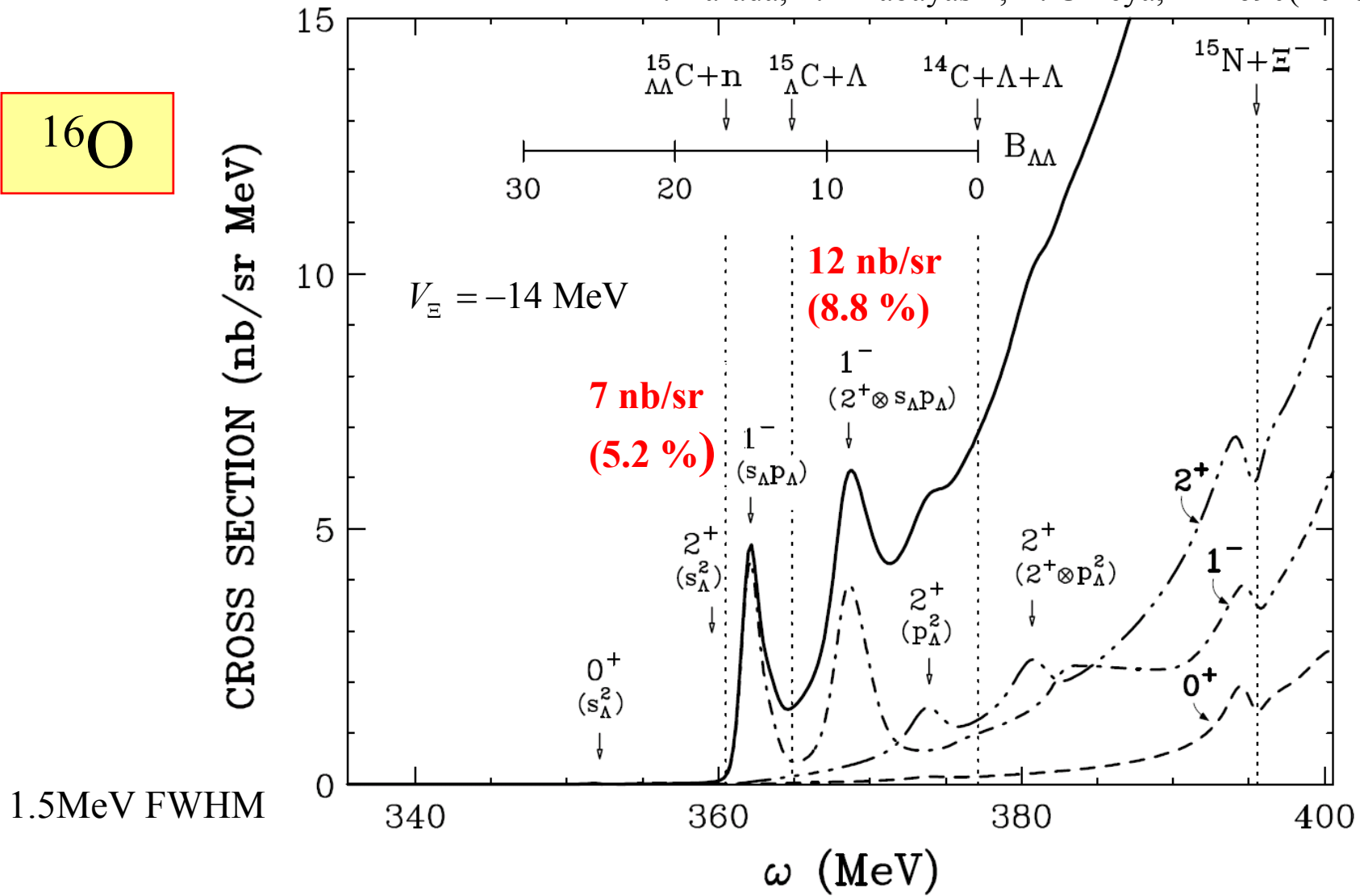
E07@J-PARC



# $\Xi^-$ spectrum in DCX ( $K^-, K^+$ ) reactions at 1.8 GeV/c

T. Harada, Y. Hirabayashi, A. Umeya, PLB690(2010)363.

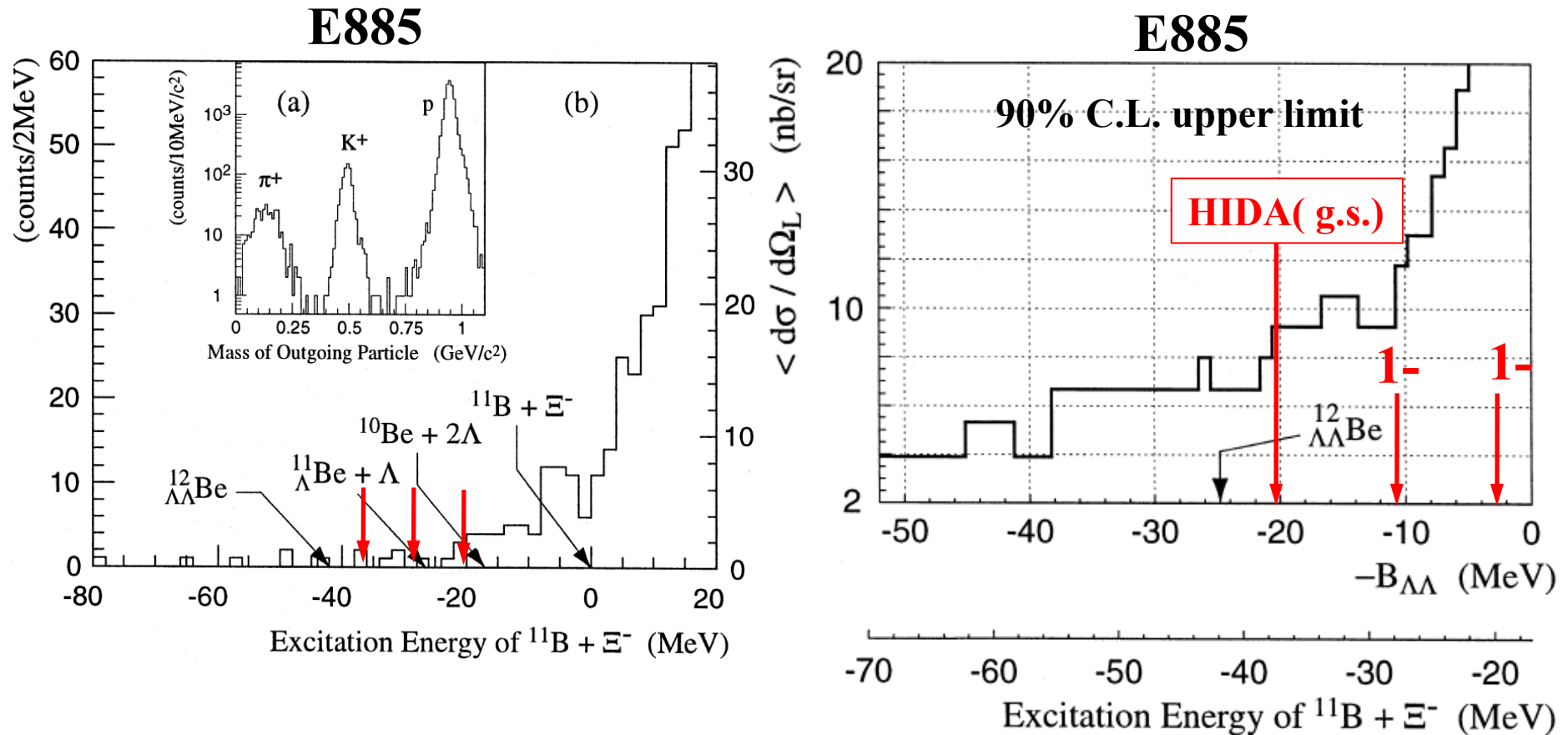
$^{16}\text{O}$



The large momentum transfer  $q_{\Xi^-} \simeq 400$  MeV/c leads to *the spin-stretched  $\Xi^-$  doorway states* followed by  $[^{15}\text{N}(1/2^-, 3/2^-) \otimes s_{\Xi^-}]1^- \rightarrow [^{14}\text{C}(0^+, 2^+) \otimes s_{\Lambda}p_{\Lambda}]1^-$

# Search for $\Lambda\Lambda$ hypernuclei in the $(K^-,K^+)$ reaction on $^{12}\text{C}$

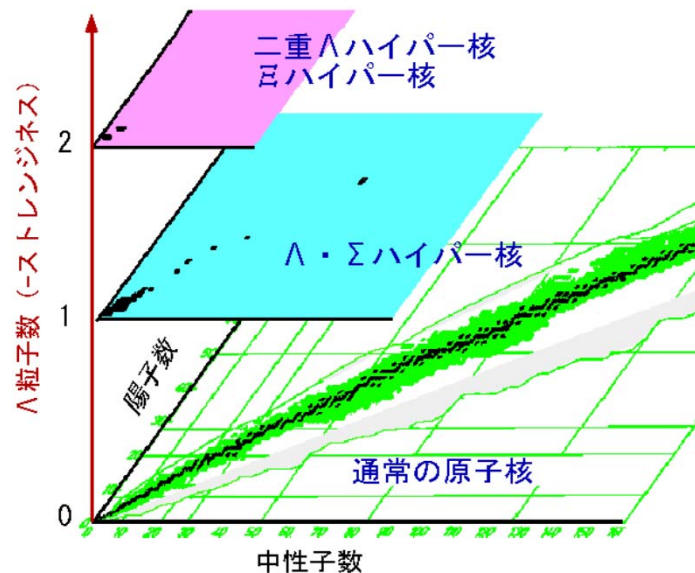
K. Yamamoto et al. (E885 Collaboration), PLB478(2000)401.



- Our results seem to be consistent with the E885 data, which taken from  $^{12}\text{C}$ , not  $^{16}\text{O}$ .

# Remark

Studies of the DCX reactions  $(\pi^-, K^+)$ ,  $(K^-, K^+)$   
for hypernuclear productions  
are  
very important and promising .

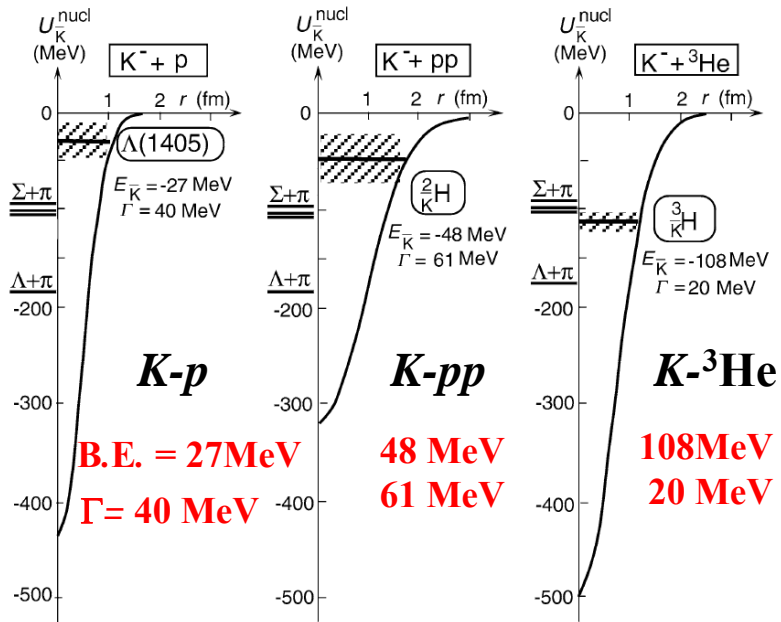


## ■ Keywords

Hyperon mixing  
+  
DCX

# 5. Deeply Bound $K^{\text{bar}}$ Nuclei

# Theoretical prediction for deeply-bound antiKaonic nuclei



## Few-body calculations predicted

T. Yamazaki, Y. Akaishi, PLB535(2002)70; PRC65(2002) 044005

- $K$ - $p$  free scattering data
- (1s) level shifts in kaonic hydrogen atoms
- B.E. and  $\Gamma$  of  $\Lambda(1405)$  = “ $K$ - $p$  quasibound state”

$$V_{\bar{K}N}^{I=0} \quad \Lambda(1405) = "K^- p"$$

**Strongly attractive**

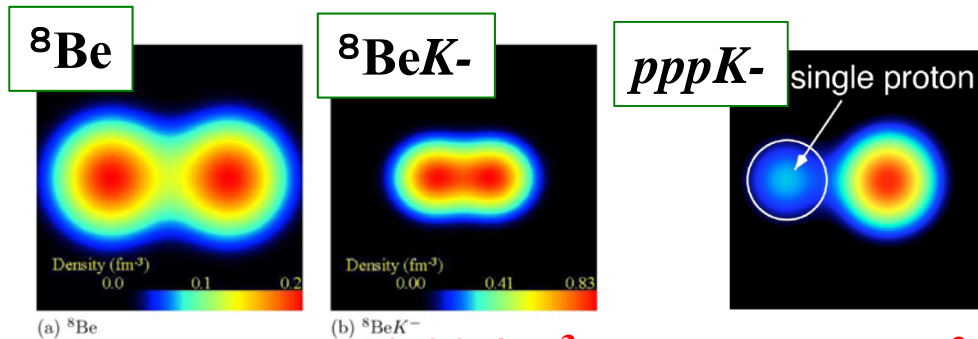
“Super strong nuclear force”

Yamazaki, Akaishi, PJPAS. B82(2007)144

## Exotic states of antiKaonic nuclei by AMD

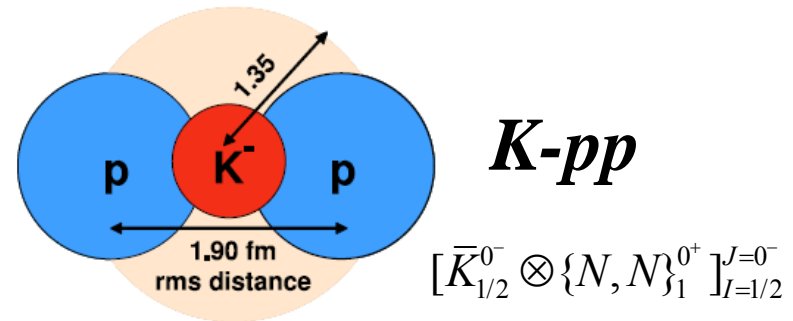
A. Doté et al., PLB590(2004)51; PRC70(2004)044313.

AMD+G-matrix NN,KN(AY)



$$\rho_{AV} = 0.33 \text{ fm}^{-3}$$

$$0.66 \text{ fm}^{-3}$$



$$[\bar{K}_{1/2}^{0-} \otimes \{N, N\}_1^{0+}]_{I=1/2}^{J=0-}$$

Essential antiKaonic nuclei

High dense hadronic matter



# Experimental Candidates for Deeply-Bound State $K^-pp$

2011.6

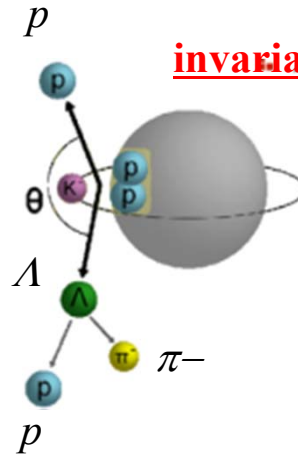
FINUDA Collaboration@DAΦNE

M. Agnello et al., PRL94(2005)212303

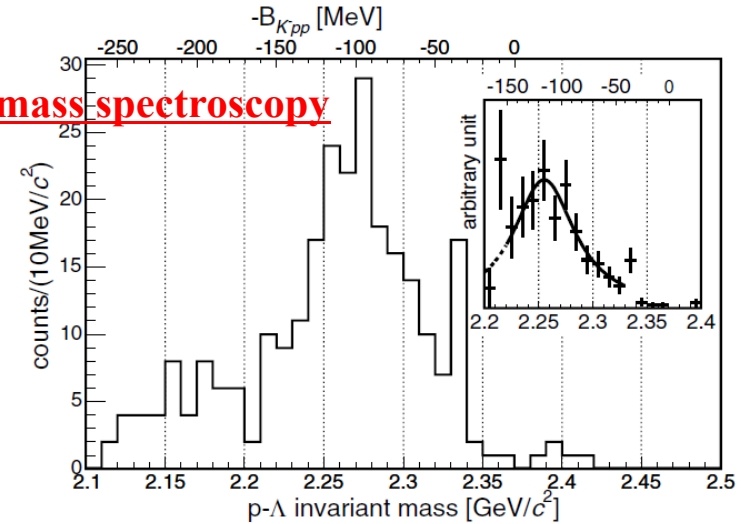
**B.E. =  $115 \pm 9$  MeV**

**$\Gamma = 67^{+16}_{-14}$  MeV**

- $K^-$  absorption on  $6\text{Li}, 7\text{Li}, 12\text{C}, 27\text{Al}$  at Rest
- $\Lambda p$  invariant mass distrib.



**invariant mass spectroscopy**



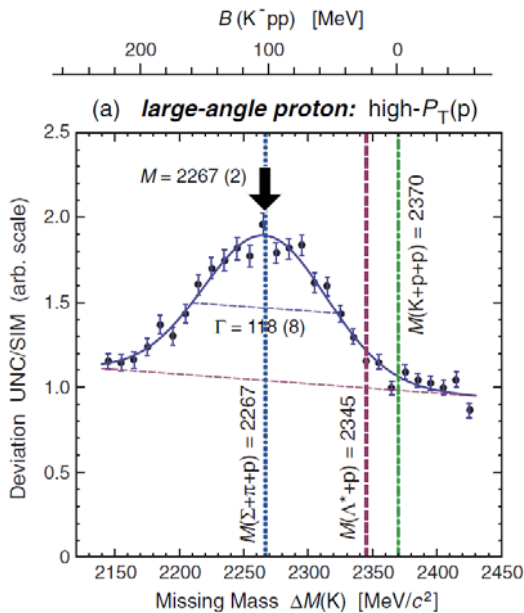
DISTO Collaboration@SATURNE-Saclay

T. Yamazaki et al.,  
PRL104(2010)132502

**B.E. =  $103 \pm 3 \pm 5$  MeV**

**$\Gamma = 118 \pm 8 \pm 10$  MeV**

- $p+p \rightarrow K^+ + \Lambda + p$  at 2.85 GeV
- $\Lambda p$  invariant mass distrib.



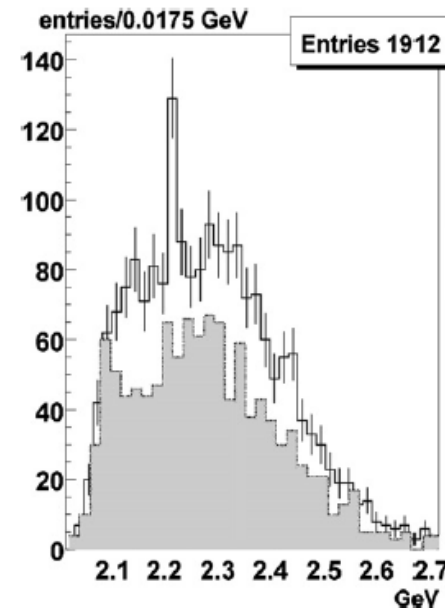
OBELIX Collaboration@LEAR-CERN

G. Bendiscioli et al.,  
NPA789(2007)222.

**B.E. =  $160.9 \pm 4.9$  MeV**

**$\Gamma < 24.4 \pm 8.0$  MeV**

- anti  $p+4\text{He}$  at rest
- $p\pi^-p$  invariant mass distrib.



# $^3\text{He}(\text{K}^-,n)\text{K-pp}$ spectrum at 1.0 GeV/c (0deg)

E15@J-PARC

A search for deeply-bound kaonic nuclear states by in-flight  $^3\text{He}(\text{K}^-,n)$  reaction

missing mass spectroscopy +invariant mass spectroscopy

Integrated cross section  
in the bound region

$\sim 3.5 \text{ mb/sr}$  (for YA)

## Advantage of the use of $^3\text{He}$

### ➤ Distortion effects

$$\frac{D_{\text{dist}}[^3\text{He}(1s_N \rightarrow 1s_K)]}{D_{\text{dist}}[^{12}\text{C}(1p_N \rightarrow 1s_K)]} = 0.47 / 0.095 \rightarrow \text{Factor 5}$$

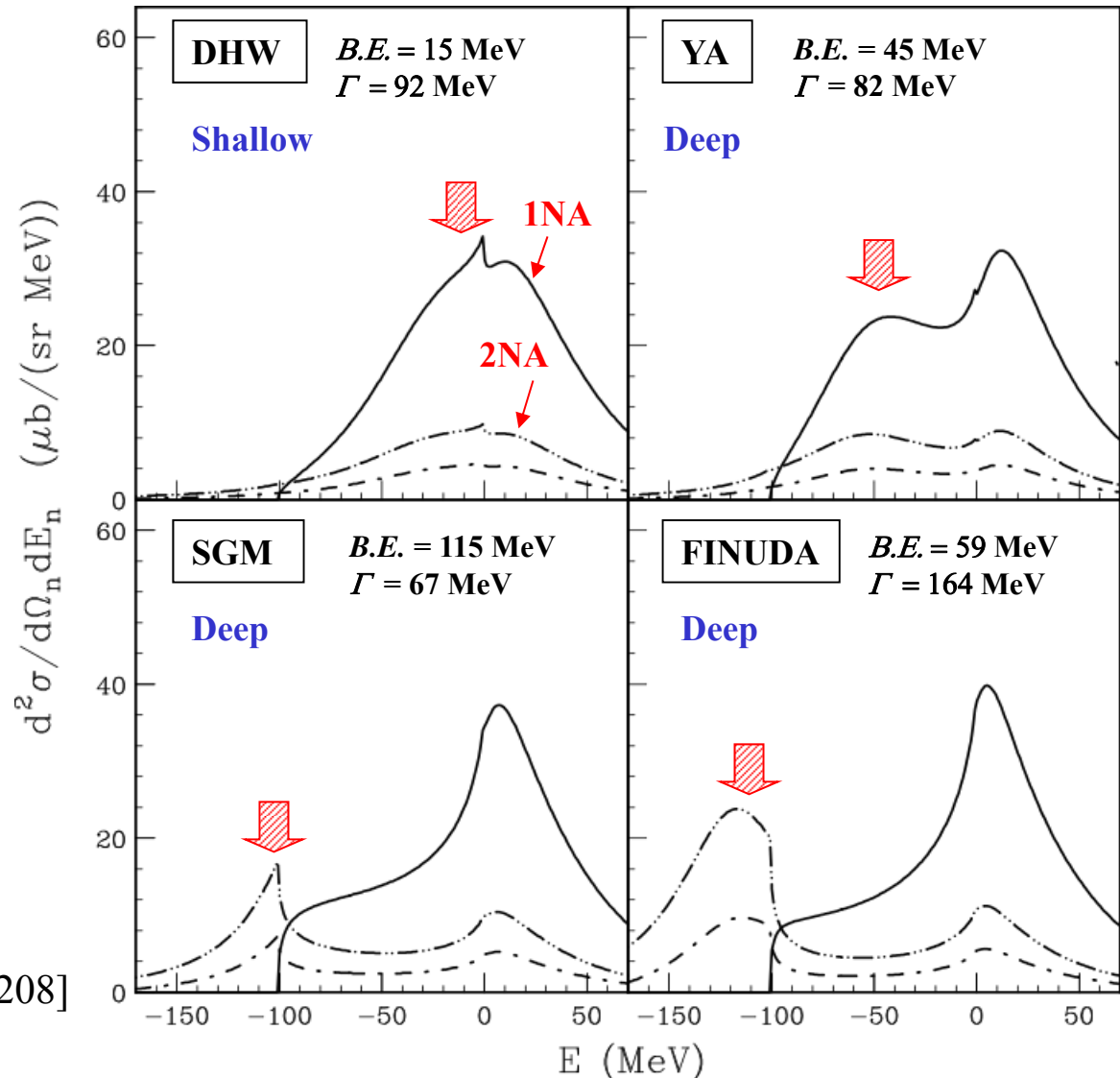
### ➤ Recoil effects

$$M_C/M_A \sim 2/3 \rightarrow \text{Factor 1.8}$$

### ➤ Small-size effects

A bound state in  $L=0$

[T.Koike, T.Harada, PRC80(2009)055208]



# 中性子星の解明を目指して-ハイペロン相互作用

## ■ $\Lambda N$

$U_0(\Lambda) \sim (-30) \text{ MeV}$ ,  $U_{LS}(\Lambda) \sim 2 \text{ MeV} \rightarrow$  精密測定  
-38 MeV? E13@J-PARC

## ■ $\Sigma N$

$U_0(\Sigma) \sim$  斥力的,  $U_{LS}(\Sigma) ? \rightarrow \Sigma^+ p (= \Sigma^- n)$  散乱 E40@J-PARC

## ■ $\Lambda N$ - $\Sigma N$

a few % mixing,  $\Lambda NN3$ 体力  $\rightarrow$  中性子過剰ハイパー核  
E10@J-PARC

## ■ $\Xi N$

$U_0(\Xi) \sim (-14) - (-0) \text{ MeV} ? \rightarrow (K^-, K^+)$  反応,  $\Xi$ -原子X線  
E03,05@J-PARC

## ■ $\Lambda\Lambda$ - $\Xi N$ - $\Sigma\Sigma$

mixing prob. ?, H-particle ?  $\rightarrow$  Hybrid-emulsion,  $\Lambda\Lambda$  相関  
E07, P42@J-PARC

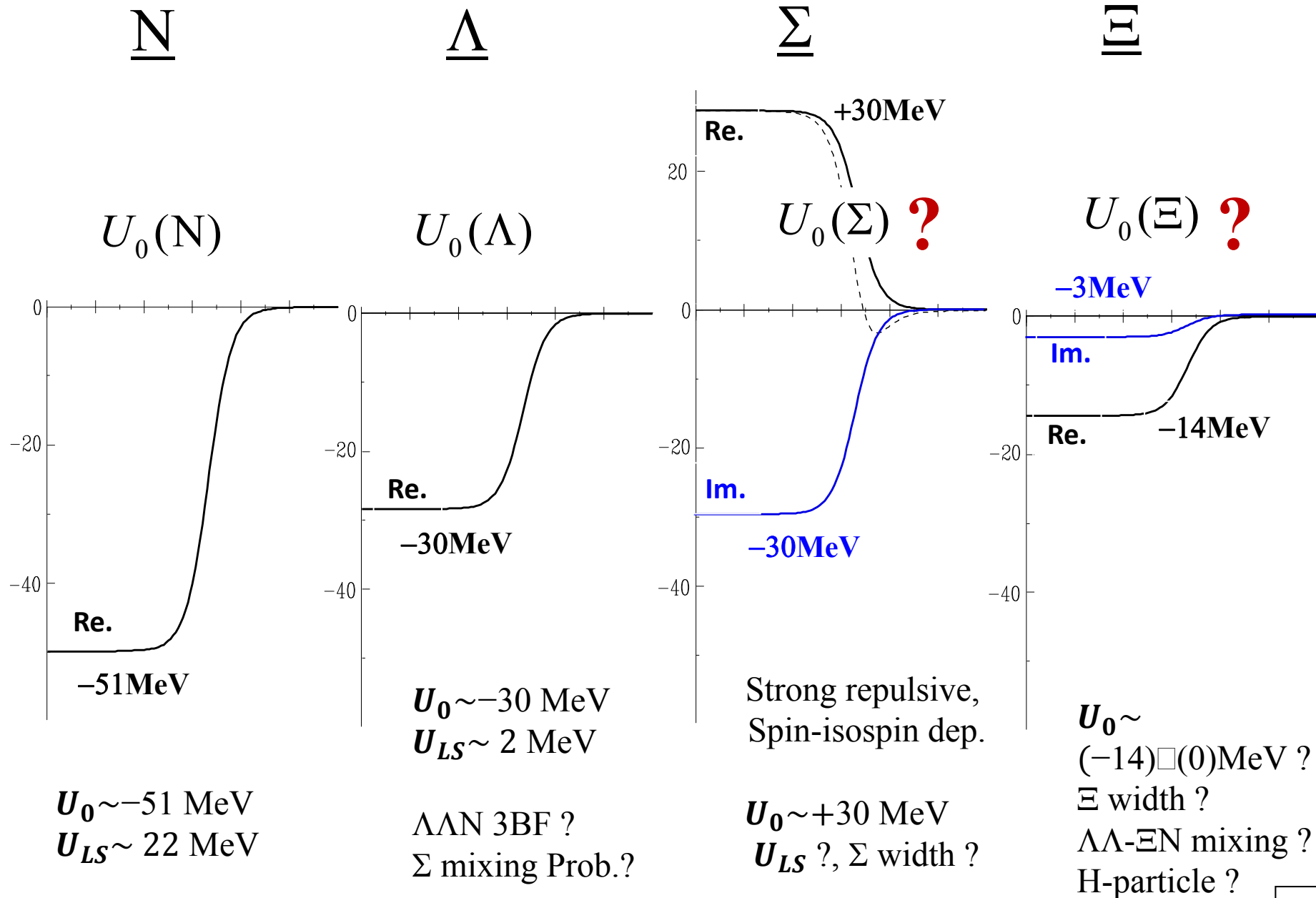
## ■ $K^- N$ - $\Lambda(1405)$ - $\pi\Sigma$

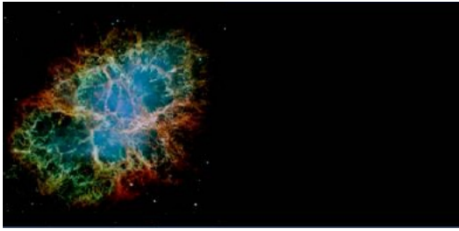
$U_0(K^-) \sim -200 \text{ MeV} / -50 \text{ MeV} ?$ , “K-pp” ?

$\rightarrow (K^-, N), (\pi^+, K^+)$  反応

E15, E23@J-PARC

# Our understanding of hyperon s.p. potentials





新学術領域研究「実験と観測で解き  
明かす中性子星の核物質」



## D01「中性子星と核物質の理論研究」(代表:大西)

### ■ 高密度中性子星物質 – 研究計画 –

- 原田 融      ハイパー核の生成と構造
- 土手昭伸       $K^-$ 中間子を含む原子核と高密度物質
- 木村真明      中性子過剰ハイパー核の構造
- 山縣関原淳子      媒質中における $K^-$ 中間子の性質
- 大西 明      ストレンジネスを含む原子核と核物質

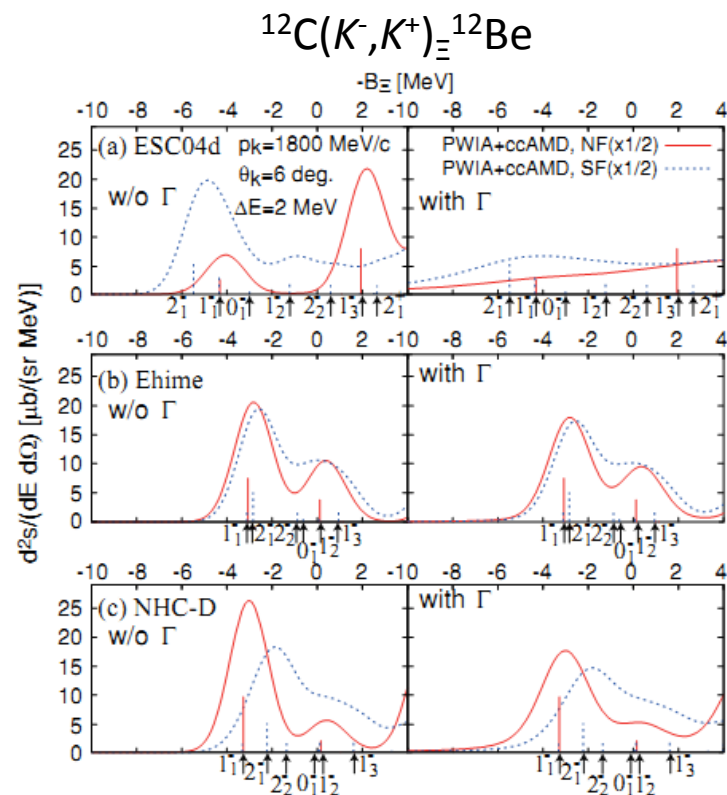
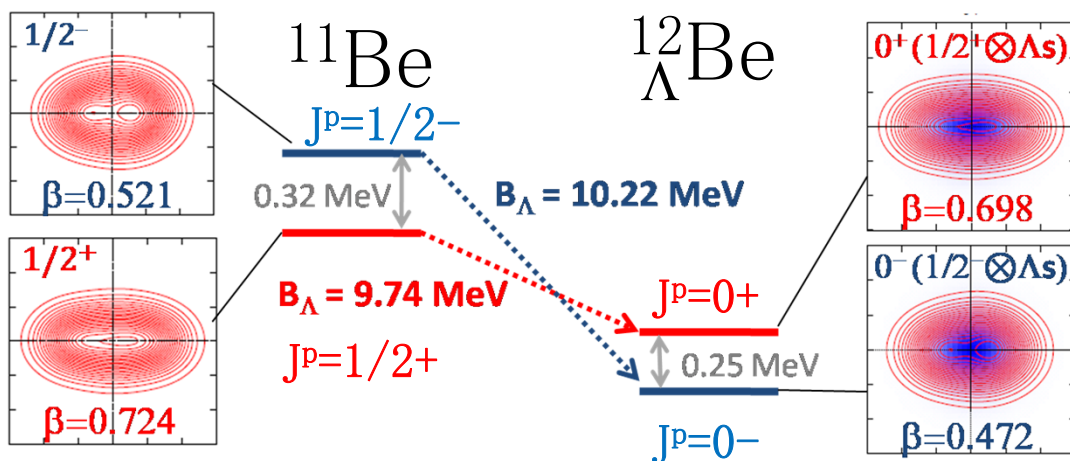
# 微視的核模型による中性子過剰 $\Lambda$ ハイパー核の生成反応と構造

(井坂、木村、土手、大西、原田)

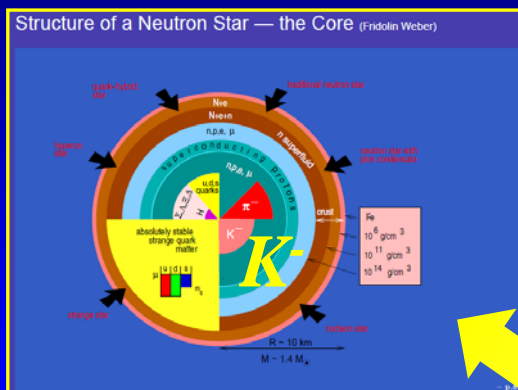
- Impurity effect
- Hyperon as a probe for nuclear structure
- $\Lambda N$  ( $-\Sigma N$ ) interaction in medium
- Evaluation and prediction of production cross section for J-PARC experiments

Research based on a microscopic model  
(AMD: Antisymmetrized Molecular Dynamics)

e.g.: Parity inversion and reversion of  $^{11}\text{Be}$  and  $^{12}_{\Lambda}\text{Be}$



# 中性子星内部でのK-中間子(土手、関原-山縣、..)



## 中性子星内部でのK-中間子の役割？

K- 中間子: スレンジネスを伴うもう一つのハドロンの存在形態  
核子と強い引力的相互作用

高密度下でのK-中間子の振る舞い

高密度状態方程式へのK中間子の影響

### 密度依存性

...「カイラル対称性の部分的回復」

### 中重核領域、多重K原子核の研究

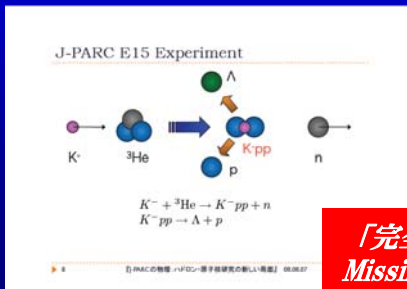
- ・near nuclear matterでのK-中間子
- ・複数Kが存在する場合

### 相互作用の規定

- ・s-wave  $K^{bar}N$  相互作用
- ・p-wave  $K^{bar}N$  相互作用？
- ・ $K^{bar}NN$  三体力??

### Kpp構造計算&反応研究

- ・実験データの解析
- ・観測された状態の正体

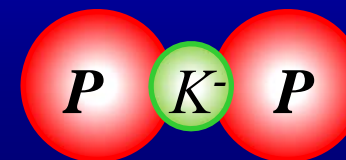


「完全実験」  
Missing mass + Inv. mass

### 今後のK原子核実験

- ・Kpp : J-PARC E15, E27
- ・ $\Lambda(1405)$  : J-PARC E31
- ・K-原子 : SIDDARTA-2,
- (Kp, K-d) J-PARC E17

最も基本的なK原子核





# 媒質中におけるK-中間子の性質

大阪電気通信大学 山縣-関原淳子

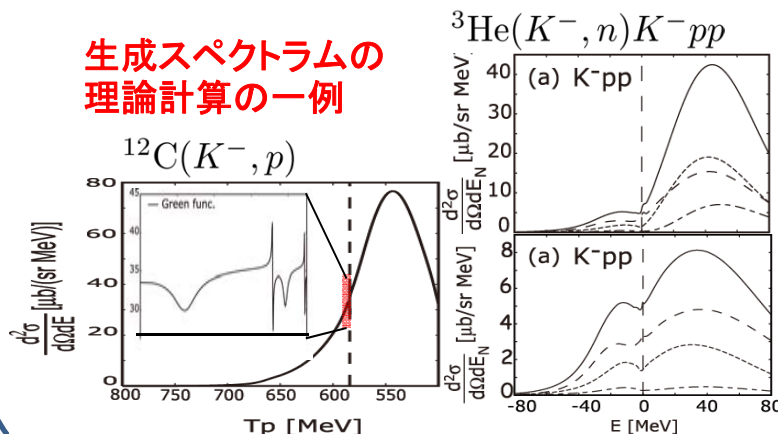
## 現在までの研究

- \* K-中間子と原子核の間の相互作用の強さは？
- \* K-中間子は原子核に束縛するのか？
- \* 実験ではどのように観測されるのか？



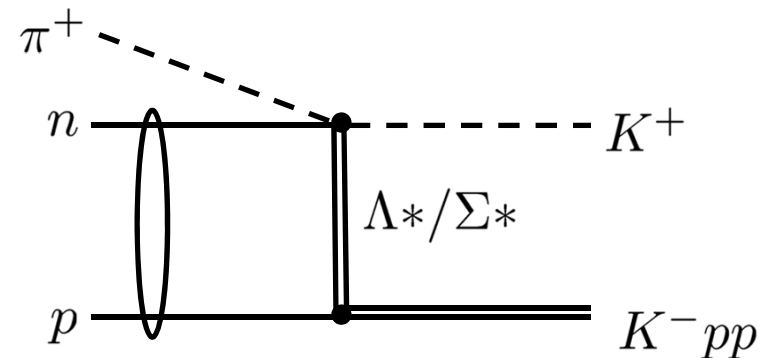
- ・浅くても深くてもK-中間子は束縛する!!
- ・束縛状態の観測のためには、崩壊過程を追うなどの+αが必要

生成スペクトラムの理論計算の一例



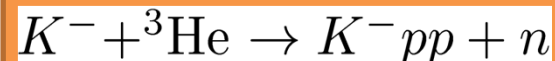
## 今後の研究内容

### J-PARC E27



- \* 中間状態として $\Lambda^*$ や $\Sigma^*$ を考慮
- \* 実験データと直接比較可能な生成スペクトラムの計算

### J-PARC E15



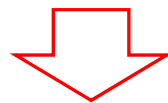
- \* 少数系の取り扱いを行い update



# Conclusion

Studies of the production and spectroscopy of strangeness nuclei are very interesting and exciting at J-PARC.

- スレンジネスが拓く新しい状態の発見、“エキゾチック”な原子核
- バリオン-バリオン間相互作用の理解、短距離斥力の起源
- ハイペロン混合と中性子星の2大問題



中性子星物質の状態方程式の解明

**Thank you very much.**