

# 重イオン衝突で探る核物質

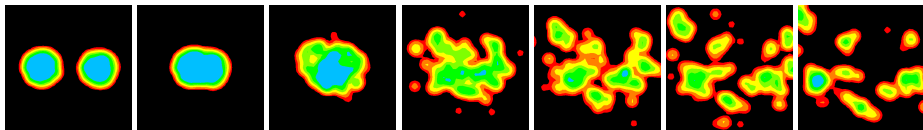
小野章

東北大学

新学術領域「実験と観測で解き明かす中性子星の核物質」キックオフシンポジウム  
2012年10月26日～27日，理化学研究所

- ほぼ一様密度で理解できる現象
- 密度の濃淡が重要になる現象      ⇔ 理論研究の戦略
- クラスタ関連の重要性

# Nuclear Matter during Nuclear Collisions



An event of central collision of Xe + Sn at 50 MeV/nucleon (AMD calculation)

- A large number of nucleons are participating.

≈ Information of bulk.

- Wide range of density:

$$\rho_0 \rightarrow \sim 2\rho_0 \rightarrow 0.5\rho_0 \rightarrow 0$$

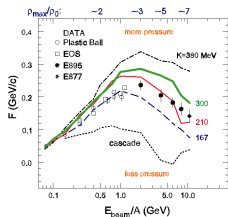
- Excitation energy (finite temperature):

$$12.5 \text{ MeV/nucleon } (\approx \text{B.E.}) \rightarrow 2 \text{ MeV/nucleon} \rightarrow 0$$

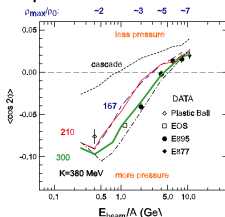
- Density fluctuation and/or cluster correlations

# EOS of Symmetric Nuclear Matter from Flow

## Transverse Flow

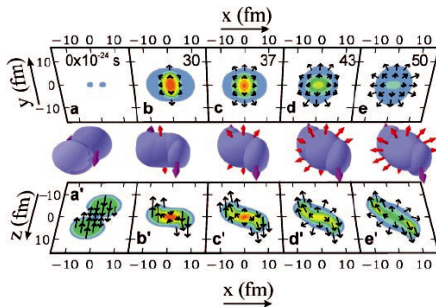
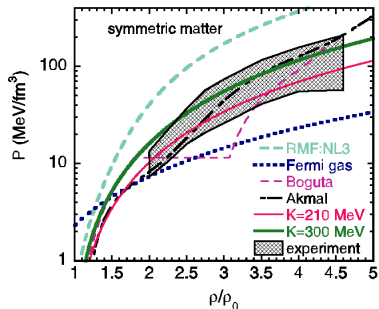


## Elliptic Flow



Danielewicz et al.,  
Science 298(2002)1592.

## Equation of State

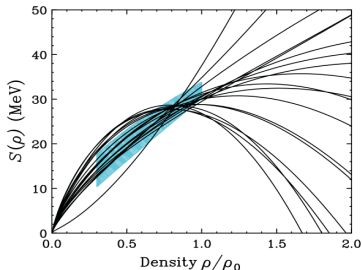


# Symmetry Energy at High and Low Densities

Nuclear EOS (at  $T = 0$ )

$$(E/A)(\rho_p, \rho_n) = (E/A)_0(\rho) + E_{\text{sym}}(\rho)\delta^2$$

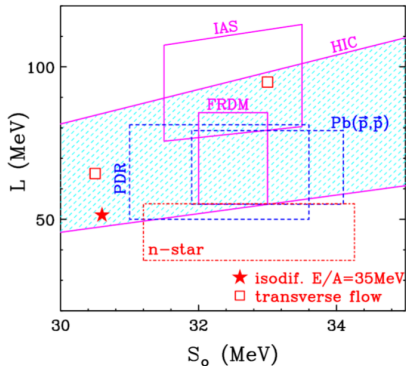
$$\rho = \rho_p + \rho_n, \quad \delta = \frac{\rho_n - \rho_p}{\rho_n + \rho_p}$$



$E_{\text{sym}}(\rho)$  for Skyrme interactions

- $S_0 = E_{\text{sym}}(\rho_0)$  at the saturation density
- $L = 3\rho_0(dE_{\text{sym}}/d\rho)_{\rho=\rho_0}$

Tsang et al., PRC86(2012)015803

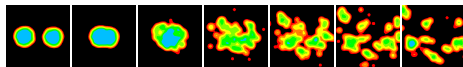
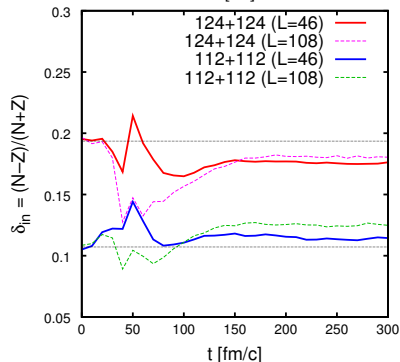
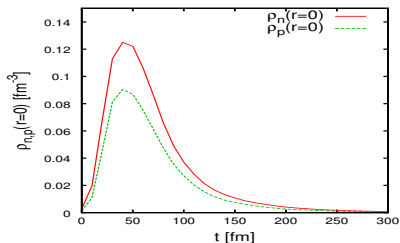


- Nuclear structure
- Heavy-ion collisions
- Neutron stars

Model ambiguities should be reduced.

- 1 ほぼ一様密度で理解できる現象 — 反応初期・中期
- 2 密度の濃淡が重要な現象 — 反応中期・後期
- 3 クラスタ関連の重要性

# Dynamics of Neutrons and Protons at Compression State



Sn + Sn central collisions at  $E/A = 50$  MeV

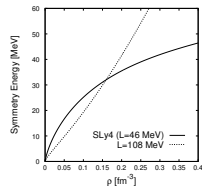
●  $^{124}\text{Sn} + ^{124}\text{Sn}$

●  $^{112}\text{Sn} + ^{112}\text{Sn}$

Skyrme force

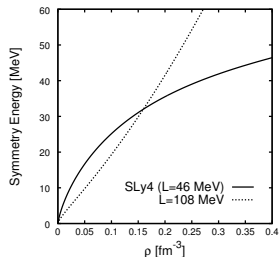
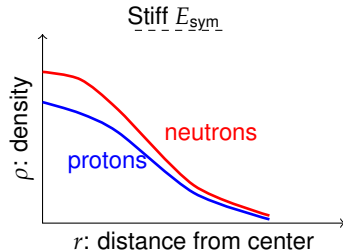
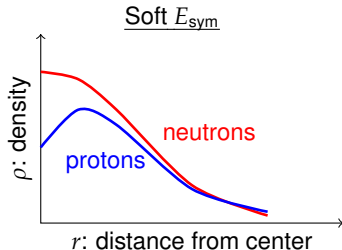
● SLy4 ( $L = 46$  MeV)

●  $L = 108$  MeV



Densities and asymmetry were calculated for an inner part of the system around the center of mass.

# Neutron-Proton Densities at Compression

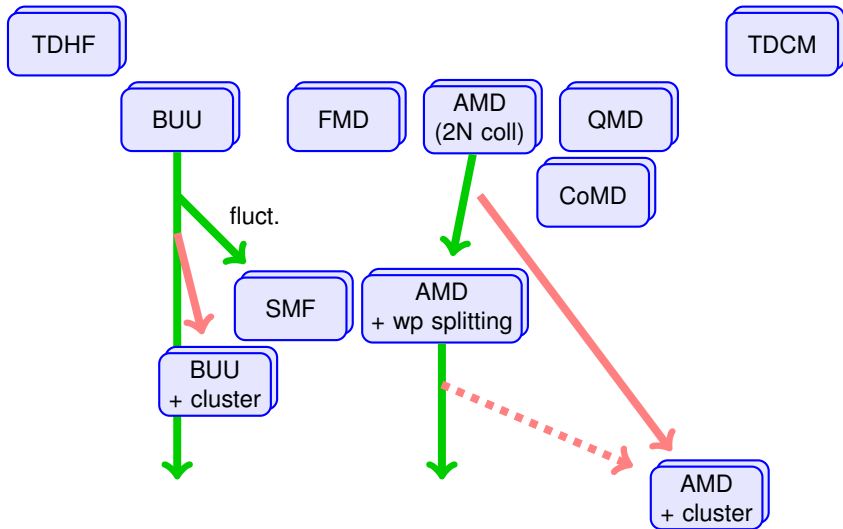


The difference of the motions of neutrons and protons is reflecting the density dependence of the symmetry energy.

## Observables

- $\pi^- / \pi^+$  yield ratio
- Neutrons and protons (or tritons and  $^3\text{He}$ )

# Various Microscopic Approaches





## Single-Particle Dynamics

← Effective interaction ...? ... EOS

- TDHF (quantum)

$$i\hbar \frac{\partial}{\partial t} \varphi_i(\mathbf{r}, t) = \left( -\frac{\hbar^2}{2M} \frac{\partial^2}{\partial \mathbf{r}^2} + U[\Phi] \right) \varphi_i(\mathbf{r}, t)$$

- Vlasov equation (semiclassical)

$$\frac{\partial f(\mathbf{r}, \mathbf{p}, t)}{\partial t} = \frac{\partial h}{\partial \mathbf{r}} \cdot \frac{\partial f}{\partial \mathbf{p}} - \frac{\partial h}{\partial \mathbf{p}} \cdot \frac{\partial f}{\partial \mathbf{r}}$$

- Molecular Dynamics (AMD, QMD)

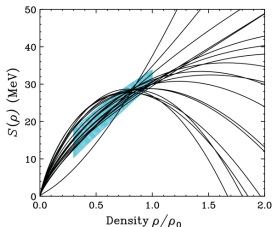
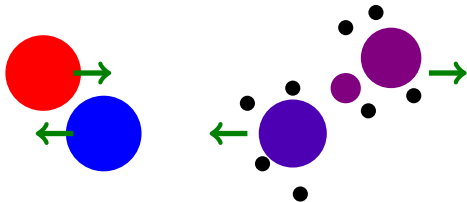
$$\varphi_i(\mathbf{r}) = e^{-\nu(\mathbf{r}-\mathbf{R}_i)^2} e^{(i/\hbar)\mathbf{P}_i \cdot \mathbf{r}}, \quad \frac{d}{dt} \mathbf{P}_i = \{\mathbf{P}_i, \mathcal{H}\}_{\text{PB}}, \quad \frac{d}{dt} \mathbf{R}_i = \{\mathbf{R}_i, \mathcal{H}\}_{\text{PB}}$$

## Nucleon-Nucleon Collisions (residual interaction, two-body correlations)

- Not yet done: TDHF
- Taken into account: VUU, BUU, QMD, AMD

# Isospin Diffusion

Isospin diffusion through the neck between projectile and target



Comparison of different models

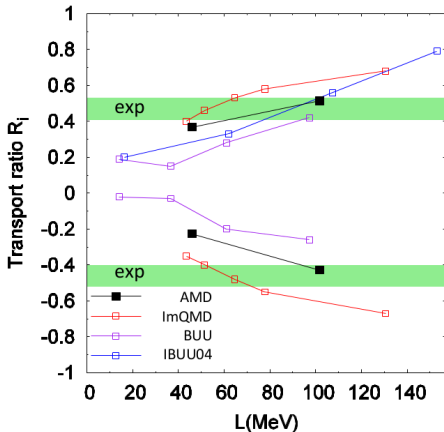


Figure by T. Akaishi

# Mechanism of Isospin Diffusion

Isospin diffusion through the neck between projectile and target



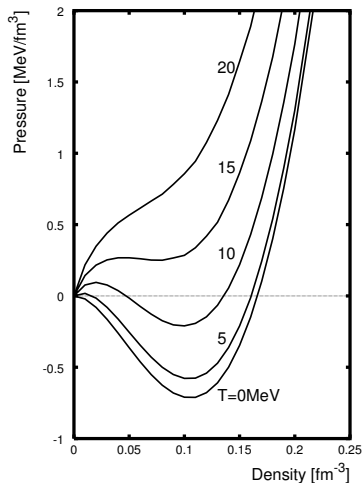
- Diffusion. (depends on single-particle motion and  $\sigma_{NN}$ )
- Symmetry potential. (depends on low-density  $E_{sym}$ )
- .....
- Reaction dynamics. (e.g. reaction time, [Rizzo et al., NPA806\(2008\)79](#) )

Link with low-energy collisions (DIC) should be made clearer.

- Semiclassical approaches (such as BUU and QMD) at medium energies.
- More quantum mechanical approaches (such as TDHF) at lower energies. (charge equilibration, nucleon transfer)

- ① ほぼ一様密度で理解できる現象 — 反応初期・中期
- ② 密度の濃淡が重要な現象 — 反応中期・後期
- ③ クラスタ関連の重要性

# EOS for finite temperature



( $N = Z$  system)

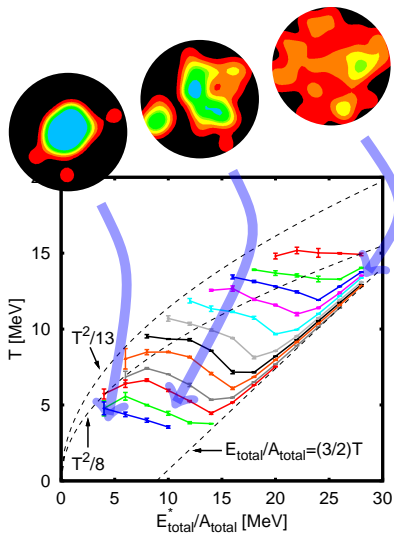
Similarity to Van der Waals EOS

$$\left(P + \frac{a}{v^2}\right)(v - b) = RT, \quad v = V/N$$

Liquid-gas phase transition is expected.

Nuclear Matter EOS for Gogny force  
(mean field approximation)

# Caloric Curves and Liquid-Gas Phase Transition



Constant-pressure caloric curves  
calculated with AMD

## Equilibrium Simulation

Solve long-time evolution for  
given  $(V, E)$ .

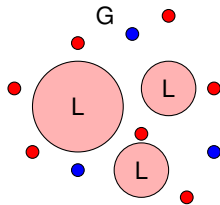
⇒ Microcanonical ensemble

⇒  $(T, P)$

$$\begin{aligned} \frac{1}{T} &= \frac{\partial S(E)}{\partial E} = \left\langle \frac{\partial S_{\text{gas}}(E_{\text{gas}})}{\partial E_{\text{gas}}} \right\rangle_E \\ &= \left\langle \frac{\frac{3}{2}N_{\text{gas}} - 1}{E_{\text{gas}}} \right\rangle_E \approx \frac{3}{2} \left\langle \frac{E_{\text{gas}}}{N_{\text{gas}}} \right\rangle_E^{-1} \end{aligned}$$

Furuta and Ono,  
PRC79 (2009) 014608;  
PRC74 (2006) 014612.

# Liquid-Gas Separation in Neutron-Rich System

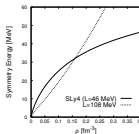
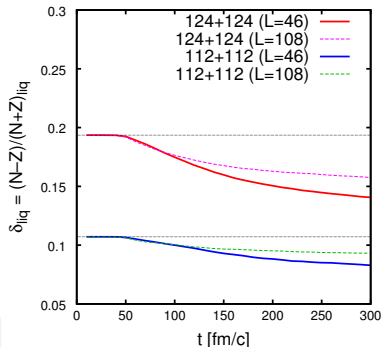


## Fractionation/Distillation

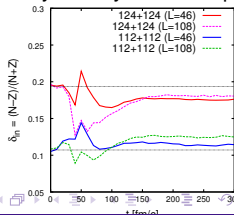
$$\delta(\text{liquid}) < \delta(\text{gas})$$

- Gas =  $\sum(A \leq 4 \text{ particles})$
- Liquid =  $\sum(A > 4 \text{ fragments})$

## Neutron-proton asymmetry of liquid part



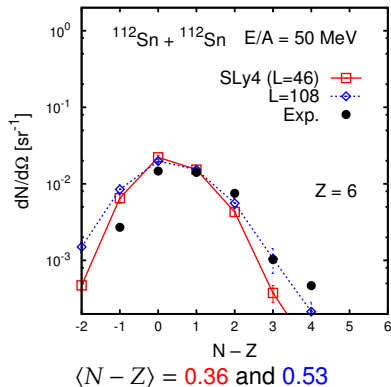
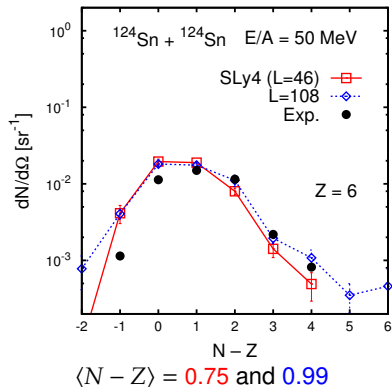
## Neutron-proton asymmetry of central part



# Fragment Isotope Distributions

MSU Data: T.X. Liu et al., PRC 014603 (2004).

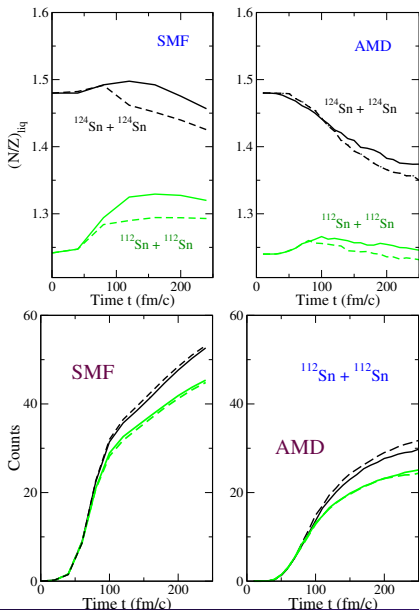
Calculation: AMD



- The average asymmetry and the width are sensitive to the symmetry energy.
- Compared to data,  $Z \geq N$  fragments are overproduced.



# Comparison of AMD and SMF



Colonna, Ono, Rizzo, PRC82 (2010) 054613.

## Neutron-Proton Ratio of Liquid

$$N_{liq} = N_{tot} - N_{gas}, \quad Z_{liq} = Z_{tot} - Z_{gas}$$

- Dependence on the symmetry energy  $E_{sym}(\rho)$  (soft or stiff)
- Dependence on models

$N_{gas}, Z_{gas}$ : Number of Nucleons in Gas

(Emitted nucleons and clusters with  $A \leq 4$ )

- Black line: neutrons
- Green line: protons

Emission of light particles should be described properly!

# General strategy to obtain EOS from HIC

Optimistic:

$$f(\text{model, EOS, other parameters } \dots) = \text{Observable (exp data)}$$

$$\text{Would be happy if } \frac{\partial f}{\partial \text{others}} = 0 \quad \text{and} \quad \frac{\partial f}{\partial \text{model}} = 0.$$

Real life:

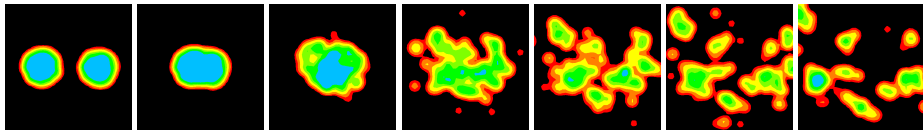
$$\left\{ \begin{array}{ll} f_1(\text{model, EOS, other parameters } \dots) = \text{Obs}_1 & (N/Z)_{\text{liquid}} \\ f_2(\text{model, EOS, other parameters } \dots) = \text{Obs}_2 & \text{Gas/Liquid fraction} \\ f_3(\text{model, EOS, other parameters } \dots) = \text{Obs}_3 & \alpha\text{-particle multiplicity} \\ & \dots \end{array} \right.$$

What to do?

- Choose suitable observables  $\{\text{Obs}_i\}$ .
- Check whether a model can describe  $\{\text{Obs}_i\}$  by assuming an EOS.
- Improve models.

- ① ほぼ一様密度で理解できる現象 — 反応初期・中期
- ② 密度の濃淡が重要な現象 — 反応中期・後期
- ③ クラスタ関連の重要性

# Bulk Properties and Correlations



An event of central collision of Xe + Sn at 50 MeV/nucleon (AMD calculation)

Bulk properties and dynamics  
e.g. EOS  $E(\rho)$

$\rightleftharpoons$   
interplay

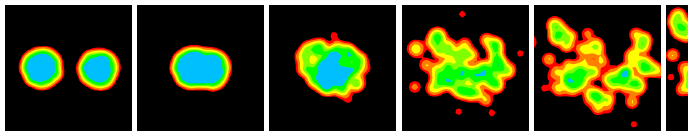
Correlations  
e.g. clusters and fragments



Isospin dynamics, Symmetry energy

$\rho_n - \rho_p$ ,  $n/p$ ,  $t/{}^3\text{He}, \dots$

# Bulk Properties and Correlations



An event of central collision of Xe + Sn at 50 MeV/nucleon (AMC)

## Partitioning of protons

p	≈10%
$\alpha$	≈20%
d, t, $^3\text{He}$	≈10%
$A > 4$	≈60%

Exp. data (INDRA etc.)

Bulk properties and dynamics  
e.g. EOS  $E(\rho)$

↔  
interplay

Correlations  
e.g. clusters and fragments



Isospin dynamics, Symmetry energy

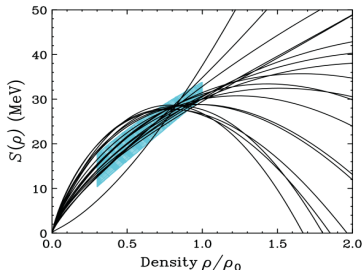
$$\rho_n - \rho_p, \quad n/p, \quad t/^3\text{He}, \dots$$

# Symmetry Energy and Clusters

Nuclear EOS (at  $T = 0$ )

$$(E/A)(\rho_p, \rho_n) = (E/A)_0(\rho) + E_{\text{sym}}(\rho)\delta^2$$

$$\rho = \rho_p + \rho_n, \quad \delta = \frac{\rho_n - \rho_p}{\rho_n + \rho_p}$$

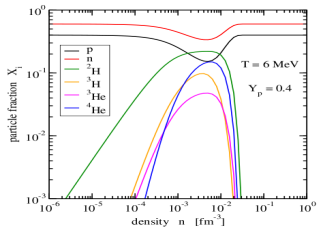
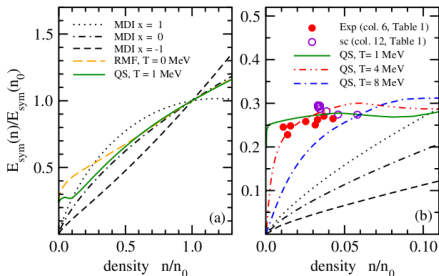


$E_{\text{sym}}(\rho)$  under mean-field approximation

EOS  $\neq$  Skyrme parameters

With clusters

Natowitz et al., PRL104 (2010) 202501.



Generalized RMF by Typel

# Why Clusters? — some theoretical background

Two-nucleon collision:

$$W_{i \rightarrow f} = \frac{2\pi}{\hbar} |\langle \Psi_f | V | \Psi_i \rangle|^2 \delta(E_f - E_i)$$
$$\sum_f |\Psi_f\rangle \langle \Psi_f| = 1$$

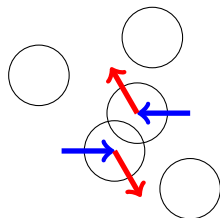
What is a suitable complete basis set for the final states of a two-nucleon scattering?

- A usual choice is to change only the two.

$$\sum_{k_1, k_2} |\varphi_{k_1}(1) \varphi_{k_2}(2) \Psi(3, 4, \dots)\rangle \langle \varphi_{k_1}(1) \varphi_{k_2}(2) \Psi(3, 4, \dots)|$$

- If a deuteron will propagate stably in medium, a more suitable basis will include

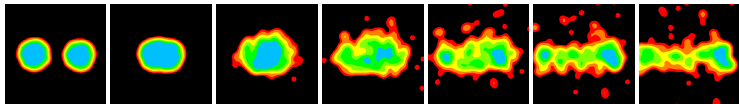
$$|\varphi_{k_1}(1) \psi_d(2, 3) \Psi(4, \dots)\rangle \langle \varphi_{k_1}(1) \psi_d(2, 3) \Psi(4, \dots)| + \dots$$



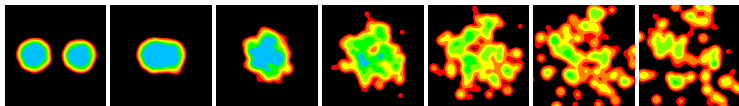
Consider cluster formation up to  $\alpha$ -particles.

# Effect of Clusters on the Density Evolution

Without cluster correlations (AMD with NN collisions)

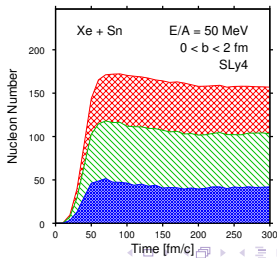


With cluster correlations



During the time evolution, clusters are ...

- formed at NN collisions.
- propagated by AMD equation. (nothing special)
- broken by NN collisions. (nothing special)



Non-clustered

(2N)

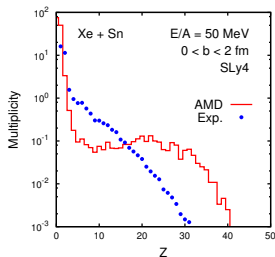
(3N)

(4N)

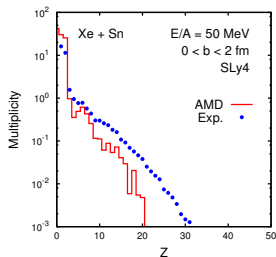


# Effects of Cluster and C-C Correlations on Fragmentation

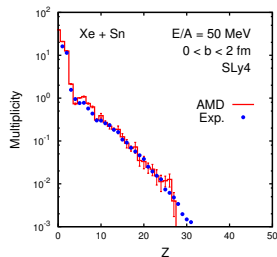
## Usual NN collisions



## With Clusters



## With C & C-C

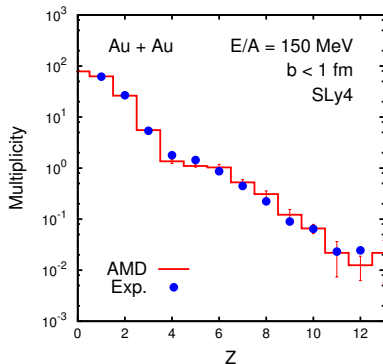


	w/o C	with C	C & C-C	INDRA
$M(p)$	40.2	10.9	10.8	8.4
$M(\alpha)$	2.5	23.2	10.7	10.1
$Z_{\text{gas}}/Z_{\text{tot}}$	55%	78%	43%	(40-50%)

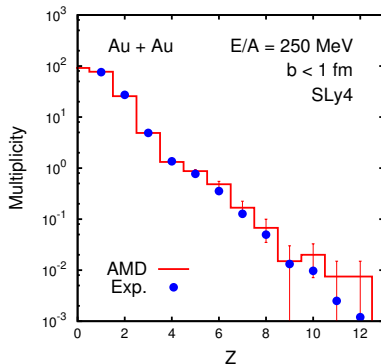
- Gas =  $\sum$  (particles of  $A \leq 4$ )
- Liquid =  $\sum$  (heavier fragments)

# Au + Au Central Collisions at Higher Energies

$E/A = 150$  MeV



$E/A = 250$  MeV



	with C & C-C	FOPI
$M(p)$	32.8	26.1
$M(\alpha)$	20.1	21.0
$Z_{\text{gas}}/Z_{\text{tot}}$	71%	73%

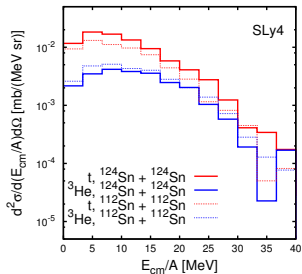
	with C & C-C	FOPI
$M(p)$	42.0	31.9
$M(\alpha)$	19.4	18.2
$Z_{\text{gas}}/Z_{\text{tot}}$	80%	83%

FOPI data: Reisdorf et al., NPA 612 (1997) 493.

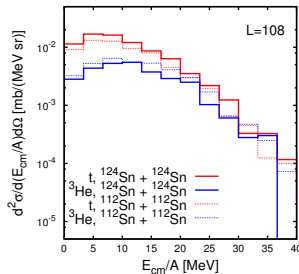


# Energy Spectra of Clusters

$^{124}\text{Sn} + ^{124}\text{Sn}$  and  $^{112}\text{Sn} + ^{112}\text{Sn}$  central collisions at 50 MeV/nucleon  
⇒ Energy spectra of **tritons** and  $^3\text{He}$  emitted to transverse directions



SLy4 ( $L = 46$  MeV)

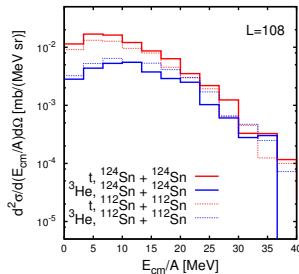
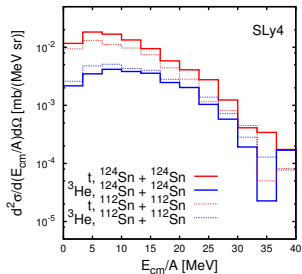
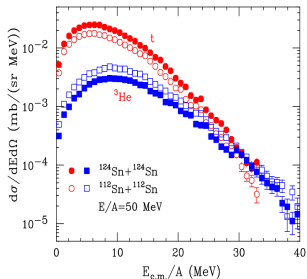


$L = 108$  MeV

- **Triton**/ $^3\text{He}$  difference is consistent with fractionation and is sensitive to the symmetry energy at low density.

# Energy Spectra of Clusters

$^{124}\text{Sn} + ^{124}\text{Sn}$  and  $^{112}\text{Sn} + ^{112}\text{Sn}$  central collisions at 50 MeV/nucleon  
 $\Rightarrow$  Energy spectra of **tritons** and  $^3\text{He}$  emitted to transverse directions



Data @NSCL/MSU

SLy4 ( $L = 46$  MeV)

$L = 108$  MeV

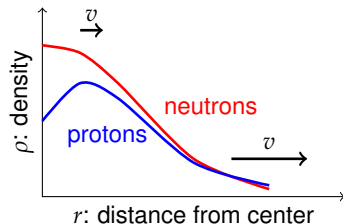
Liu et al., arXiv:1208.3108

- Triton/ $^3\text{He}$  difference is consistent with fractionation and is sensitive to the symmetry energy at low density.
- To reproduce data, there should be more low-energy tritons and less high-energy tritons, and low-energy  $^3\text{He}$  particles (or protons) should be less.

# Compression and Expansion Dynamics of Neutrons and Protons?

Both liquid and gas (low energy part) should be more neutron rich.

( $\Rightarrow$  It is not an issue of fractionation in fragmentation.)



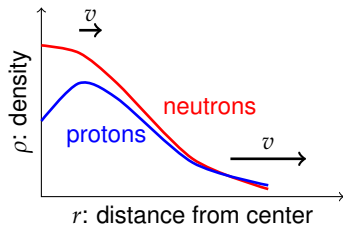
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- the small yield of proton-rich nuclei
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# Compression and Expansion Dynamics of Neutrons and Protons?

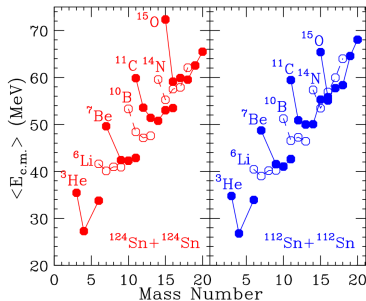
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- the triton spectrum
- the small yield of proton-rich nuclei
- the large energy of proton-rich nuclei



Data @NSCL/MSU

Liu et al., arXiv:1208.3108

Kinetic energies of proton-rich fragments are anomalously large.  
(Yields of low-energy proton-rich fragments are anomalously small.)

- 重イオン衝突での多くの観測量は  $E_{\text{sym}}(\rho)$  を反映している . (  $\rho > \rho_0, \rho < \rho_0$  )
- モデルを仮定すれば結論が得られるが , 結論はモデルに依存する .
- モデルによる不定性を減らす努力が必要 .
  - モデルに依らない物理量を探す .
  - 特定の観測量だけでなく , 反応の大局的様相に注意が必要 .
  - モデルを改良する .
- 重イオン衝突では ( 思ったよりも ) クラスタ相関が強い . ( 数百 MeV/u でも )